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► **To cite this version:**

Elodie Cao, Paul Greillier, Raphaël Loyet, Françoise Chavrier, Jade Robert, et al.. Development of a Numerical Model of High-Intensity Focused Ultrasound Treatment in Mobile and Elastic Organs: Application to a Beating Heart. *Ultrasound in Medicine & Biology*, 2022, 48 (7), pp.1215-1228. 10.1016/j.ultrasmedbio.2022.02.017 . hal-03659589

**HAL Id: hal-03659589**

<https://hal.science/hal-03659589v1>

Submitted on 22 Jul 2024

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**Development of a numerical model of HIFU treatment in mobile and elastic organs:  
Application to a beating heart**

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1 **Abstract**

2 High-intensity focused ultrasound (HIFU) is a promising method to treat cardiac arrhythmias, as it can  
3 induce lesions at a distance throughout myocardium thickness. Numerical modeling is commonly used  
4 for ultrasound probe development and optimization of HIFU treatment strategies. This study aims to  
5 describe a numerical method to simulate HIFU thermal ablation in elastic and mobile heart models.  
6 The ultrasound pressure field is computed on a 3-dimensional (3D) orthonormal grid using the  
7 Rayleigh integral method, and the attenuation is calculated step by step between cells. The  
8 temperature distribution is obtained by the resolution of the BioHeat Transfer Equation (BHTE) on a  
9 3D nonorthogonally structured curvilinear grid using the finite volume method. The simulation method  
10 is applied on two regions of the heart (atrioventricular node and ventricular apex) to compare the  
11 thermal effects of HIFU ablation depending on deformation, motion type and amplitude. The  
12 atrioventricular node requires longer sonication than the ventricular apex to reach the same lesion  
13 volume. Motion considerably influences treatment duration, lesion shape, and distribution in cardiac  
14 HIFU treatment. These results emphasize the importance of considering local motion and deformation  
15 in numerical studies to define efficient and accurate treatment strategies.

16 **Keywords:** high-intensity focused ultrasound, cardiac applications, mobile organs, bioheat transfer  
17 equation, curvilinear grid, finite volume method

## 18 Introduction

19 Cardiovascular diseases (CVDs) are the leading cause of mortality worldwide, with more than  
20 twice the number of cancer-related deaths (Roth et al. 2018). Cardiac arrhythmias (CAs) are CVDs  
21 originating from an electrical dysfunction in the heart conduction pathway, which leads to abnormal  
22 heartbeat. While atrial fibrillation is the most common CA (Timmis et al. 2018), ventricular tachycardia  
23 presents the greatest risk of sudden death (Harris and Lysitsas 2016). In clinical routine, these  
24 pathologies are treated by thermal ablation of arrhythmogenic foci or reentrant circuits using a  
25 radiofrequency catheter. This technique remains invasive and has a recurrence rate of 30% to 50%  
26 (Tung et al. 2015).

27 High-intensity focused ultrasound (HIFU) is clinically used in the treatment of several pathologies,  
28 such as prostate cancer (Gelet et al. 2000), uterine fibroids (Ji et al. 2017), and essential tremors  
29 (Park et al. 2019). HIFU enables fast and precise ablation during non or minimally invasive procedures  
30 and has been proposed as an alternative therapy to treat CAs. The transesophageal approach has  
31 been studied because it offers an excellent acoustic window, and the proof of concept has been  
32 presented *in silico* (Constanciel et al. 2013; Pichardo and Hynynen 2009), *in vitro* (Constanciel et al.  
33 2013) and *in vivo* in swine (Bessiere et al. 2016). *Ex vivo* experiments on beating heart models have  
34 demonstrated the ability to produce thermal lesions with a transesophageal probe in mobile organs.  
35 However, further *in vivo* experiments on baboons have emphasized difficulties caused by heart motion  
36 (Greillier et al. 2018). Consequently, it clearly appears that more accurate simulation tools are required  
37 to precisely predict the position and shape of HIFU lesions on the beating heart.

38 Numerical modeling is currently used during the early phases of the design of HIFU probes, and  
39 has contributed to the design of innovative transducer geometry in response to medical needs (Bawiec  
40 et al. 2018; Charrel et al. 2011; Curiel et al. 2002). Additionally, numerical modeling has participated in  
41 the definition and optimization of treatment strategies (Gélat et al. 2014), as well as in the verification  
42 of treatment feasibility (Chavier et al. 2000; N'Djin et al. 2015) and can provide an alternative to  
43 animal testing.

44 The simulation of HIFU treatment requires three models: ultrasound propagation, heat transfer,  
45 and thermal damage models. Several methods have already been described in the literature. For  
46 linear wave propagation computation, the Rayleigh integral method (Kirkup 1994) and the angular

47 spectrum method (Zeng and McGough 2008) are commonly used in homogeneous media and the  
48 hybrid angular spectrum method (Vyas and Christensen 2008) is chosen for computation in  
49 heterogeneous tissues. Heat transfer in biological tissues can be modeled by various models,  
50 including the non-Fourier bioheat transfer equation (Kundu and Dewanjee 2015), the microvascular-  
51 based model (Chen and Holmes 1980; Weinbaum et al. 1984) or the porous media theory  
52 (Mohammadpour and Firoozabadi 2020; Nakayama and Kuwahara 2008; Wessapan and  
53 Rattanadecho 2020; Yuan 2009). However, the most widely used is the Pennes BHTE (Pennes 1948),  
54 which is modeled with partial differential equations. This equation can be discretized with finite  
55 difference, finite element or finite volume methods (Tadmor 2012) on meshes of different types  
56 (Thompson et al. 1998). In some thermal models, changes in tissue acoustic properties during  
57 treatment can be considered (Garnier et al. 2008; Guntur and Choi 2020). Finally, thermal damage  
58 can be estimated with the Cumulative Equivalent Minutes at 43 °C (CEM43) value (Sapareto and  
59 Dewey 1984) or with the Arrhenius damage integral (Orgill et al. 1998). Open access tools already  
60 integrate some of these methods, such as the HITU simulator (Soneson 2015), Field II (Jensen and  
61 Svendsen 1992) or k-wave (Treeby et al. 2012).

62 These models are currently used to simulate HIFU treatment on abdominal organs (N'Djin et al.  
63 2015; Schwenke et al. 2017), on the skull and brain (Padilla et al. 2018) or on other targets. However,  
64 these simulations only consider HIFU treatment effects on static organs. Only a few examples  
65 highlight the respiratory motion impact on HIFU treatment of abdominal organs, such as the liver  
66 (N'Djin et al. 2015; Schwenke et al. 2017; Zhang and Chauhan 2020). N'djin *et al.* (N'Djin et al. 2015)  
67 presented 3D numerical modeling of HIFU treatment in the liver using *in vivo* motion data obtained  
68 with the US-speckle tracking method and provides realistic results, as experimental data are used as  
69 inputs for simulations. However, this motion model only considers a 2D rigid motion because  
70 respiratory motion is mostly described in the cranial caudal direction. Schwenke *et al.* (Schwenke et al.  
71 2017) presented a thermal model to simulate HIFU treatment in the liver using a Lagrangian approach  
72 to describe and resolve the heat transfer equation. Their work focuses on discontinuous motion  
73 considerations to study boundary sliding effects and computation time reduction to approach real-time  
74 simulation during clinical procedures. Nevertheless, precomputation of ultrasonic pressure fields,  
75 enabling real time computation, can also be responsible for long pretreatment work and reduction in  
76 result precision. Zhang *et al.* (Zhang and Chauhan 2020) presented a near real-time model based on

77 the fast explicit dynamics finite element method and considering soft tissue deformation. This model  
78 provides accurate results for short computation times; but their study is only focused on liver cases.  
79 Despite several studies in cardiac biomechanics and the emergence of cardiac modeling as a  
80 diagnostic tool to understand physiopathological heart mechanisms (Humphrey 2002), the influence of  
81 heart motion on HIFU treatment delivery is poorly documented. To our knowledge, there is no  
82 simulation method of HIFU thermal ablation on a beating heart.

83 The purpose of this paper is to describe a numerical method to simulate the HIFU thermal  
84 procedure in elastic and mobile heart models. This work is based on four simulation methods. Motion  
85 and deformation of the heart muscle are evaluated by registration of 4D (3D+t) CT-scan images of a  
86 heart cycle. Ultrasound propagation is modeled by the classical Rayleigh integral method. The thermal  
87 model is built on the Pennes BHTE on static organs. However, to follow the temperature of each point  
88 of the computation zone along the deformation cycle, the approach described in this paper consists of  
89 solving the BHTE on a 3D nonorthogonally structured curvilinear grid using the finite volume method.  
90 Finally, the thermal damage model is described with the CEM43 value.

91 The remainder of this paper is organized as follows: **first**, mathematical theory used to predict  
92 HIFU thermal effects on moving and deformable tissues is developed; the application of the  
93 implemented simulation method on a clinical case to compare thermal effects of HIFU treatment  
94 depending on motion type and amplitude in two different regions of the heart is then described;  
95 discussions are presented in **the following section**; and finally, conclusions of the study are provided.

## 96 **Simulation methods**

### 97 Simulation overview

98 Simulation of a thermal treatment with organ motions must encompass four aspects: motion  
99 evaluation, acoustic propagation, heat transfers and thermal damage evaluation. Motion evaluation is  
100 not the main subject of this article and is largely treated in the medical image registration literature  
101 (Hoogendoorn et al. 2013). Common elastic registration techniques are used in the present work.  
102 Acoustic propagation simulation is approached with linear equations. Therefore, most of the  
103 challenges arising from tissue deformation are due to the influences of deformation on the heat  
104 transfer equation discretization. The Bio Heat Transfer Equation (BHTE), commonly used in biological  
105 tissue (Chato 1990; Pennes 1948), is derived from the general heat transfer equation as follows:

$$\rho_t c_t \frac{\partial T_p}{\partial t} = \nabla \cdot k_t \nabla T_p + \omega_b c_b (T_A - T_p) + Q \quad (1)$$

106 where  $T_p$  ( $^{\circ}\text{C}$ ) is the temperature at point P and time  $t$ ,  $\rho_t$  ( $\text{kg}\cdot\text{m}^{-3}$ ) is the tissue density,  $c_t$  ( $\text{J}\cdot\text{kg}^{-1}\cdot^{\circ}\text{C}^{-1}$ )  
 107 is the tissue specific heat,  $k_t$  ( $\text{W}\cdot\text{m}^{-1}\cdot^{\circ}\text{C}^{-1}$ ) is the tissue thermal conductivity,  $\omega_b$  ( $\text{kg}\cdot\text{m}^{-3}\cdot\text{s}^{-1}$ ) is the tissue  
 108 blood perfusion rate,  $c_b$  ( $\text{J}\cdot\text{kg}^{-1}\cdot^{\circ}\text{C}^{-1}$ ) is the blood specific heat,  $T_A$  ( $^{\circ}\text{C}$ ) is the arterial blood temperature  
 109 and  $Q$  ( $\text{W}\cdot\text{m}^{-3}$ ) is the source term, which here, is due to the energy added to the medium by ultrasound  
 110 tissue absorption. To numerically solve Equation 1 within the scope of elastic and mobile organs, the  
 111 challenge is to follow the motion of each point of the computation zone to evaluate throughout its  
 112 displacements the heating (needed for temperature evaluation) and the exposure time (needed for  
 113 thermal damage evaluation) at each time step.

114 Consequently, all the numerical solutions based on rigid grids cannot accurately describe  
 115 thermal evolution in highly deformable muscle, as tissue contraction and dilatation continuously modify  
 116 the anatomical geometry. To solve this problem, deformable grid fitting local deformation is used.  
 117 Many teams have developed methods to solve similar partial derivative equations on mesh grids fitting  
 118 complex geometrical models. This work is derived from finite volume methods described in the  
 119 *Handbook of Numerical Heat Transfer* (Minkowycz et al. 2008) and S.E. Norris' thesis (Norris 2000).

#### 120 Deformed model definition

121 The moving heart model is obtained from 4D CT-scans of a heart cycle (3D + t) divided into 20  
 122 time phases by the segmentation and nonrigid registration of the dataset. Tissue segmentation  
 123 describes the anatomic structure of the **numerical heart phantom**, and image registration provides  
 124 motion **and deformation** information between phases (refer to Appendix A).

125 To solve our partial derivative problem, the space is discretized into hexahedral cells. The  
 126 initial phase of the heart cycle defines the reference grid that corresponds to a nondeformed frame.  
 127 The other phases of the cycle define curvilinear grids that are generated from the displacement of the  
 128 reference grid centroids to their new location and that correspond to deformed frames (Fig. 1).

129 Each grid is composed of hexahedral cells, with each cell described by its centroid  $\mathcal{P}$ , six  
 130 faces  $t, b, n, s, w, e$  and eight vertices, which are the barycentric center of each neighboring cell  
 131 centroid (Fig. 2). Because the reference grid spatial discretization can be different from the heart

phantom segmentation, displacement vectors are linearly interpolated in each centroid position. After deformation, the curvilinear grid is considered 3D, nonorthogonal, smooth and structured.

#### 134 Ultrasonic field simulation

135 Ultrasonic fields obtained from any ultrasound propagation models can be used as input data  
 136 for the thermal model. However, in this study, ultrasonic fields are computed using the Rayleigh  
 137 integral equation (Arditi et al. 1981; Maynard and Williams 1982). A unique pressure simulation is  
 138 computed for the first phase of the heartbeat on a 3D orthonormal grid. The medium is considered to  
 139 be attenuating, homogeneous, and isotropic, while refraction and reflection are not considered in the  
 140 field of computation. Ultrasonic propagation is evaluated in a voxel space. To calculate the  
 141 attenuation, the shortest lines between two points of the finite medium are drawn for the whole  
 142 computed zone. Under the hypothesis of constant speed in tissues, the attenuation along each line is  
 143 then calculated by summing the attenuation of each tissue voxel crossed by the line. In the other  
 144 phases of the heartbeat, the same pressure field is applied with the same acoustic parameters, but the  
 145 centroid coordinates of each cell in the reference grid are remapped to the curvilinear coordinates from  
 146 the corresponding displacement maps.

#### 147 BHTE discretization on a curvilinear grid

148 The computation of heat transfer in biological tissues requires the application of the BHTE  
 149 equation. As the equation is defined on a continuous space, we discretize it with the finite volume  
 150 method.

151 First, BHTE is spatially integrated on a cell defined by its volume  $V$  as follows:

$$\underbrace{\iiint_V \rho_t c_t \frac{\partial T_p}{\partial t} dV}_{\text{transient } \Phi_T} = \underbrace{\iiint_V \nabla \cdot k_t \nabla T_p dV}_{\text{diffusion } \Phi_D} + \underbrace{\iiint_V \omega_b c_b (T_A - T_p) dV}_{\text{perfusion } \Phi_{perf}} + \underbrace{\iiint_V Q dV}_{\text{source } \Phi_Q} \quad (2)$$

152 The rate of change of the tissue temperature can be attributed to three physical phenomena, which  
 153 are accounted for by individual terms of the right-hand side of equation 2: diffusion, perfusion, and  
 154 thermal energy deposition. Each term is discretized separately and temporally integrated as detailed in  
 155 Appendix B.

156 The discretized solution of the equation is defined as follows:



$$T_P^{t+dt} = T_P^t + \frac{\Delta t}{\rho_t c_t} \cdot \left( \frac{1}{V} \sum_{f=\ell, b, n, s, w, e} \Phi_{D_f}^t + \omega_b c_b (T_A - T_P^t) + Q \right) \quad (3)$$

157 where  $\Phi_{D_f}$  is the diffusion through an elementary cell, and it is defined as the sum of the diffusion on  
 158 each face of the cell. For the face ( $\mathcal{E}$ ), the equation is written as follows:

$$\Phi_{D_e} = \underbrace{k_{t_e} G^1 (T_E - T_P)}_{\text{orthogonal}} + \underbrace{k_{t_e} G^2 (T_{ne} - T_{se}) + k_{t_e} G^3 (T_{te} - T_{be})}_{\text{curvilinear}} \quad (4)$$

159 where  $G^1$ ,  $G^2$  and  $G^3$  are local geometry functions of the cell surface, which are defined with  $s^i$  being  
 160 the surface vector and  $d_i$  being the distance vector as follows:

$$G^1 = \frac{s^1 \cdot s^1}{d_1 \cdot s^1}; G^2 = \frac{s^2 \cdot s^1}{d_2 \cdot s^2}; G^3 = \frac{s^3 \cdot s^1}{d_3 \cdot s^3} \quad (5)$$

161 The time step  $dt$  defined in Equation 3 must satisfy the Von Neumann criterion (Crank and Nicolson  
 162 1947).

### 163 Thermal dose

164 The Cumulative Equivalent Minutes at 43 °C (CEM43) described by Sapareto and Dewey  
 165 (Sapareto and Dewey 1984) is an empirical value for estimating thermal damages induced by heating  
 166 in tissues, which is given as follows:

$$t_{43^\circ C}(t) = \int_0^t R^{43-T(t)} dt, \quad R = \begin{cases} 0 & T < 37^\circ C \\ 0.25 & T \in [37^\circ C; 43^\circ C] \\ 0.5 & T > 43^\circ C \end{cases} \quad (6)$$

167 where  $t_{43^\circ C}$  is the equivalent time at 43 °C and  $T$  is the temperature at time  $t$ . According to the  
 168 literature, the thermal dose threshold to create an irreversible lesion in soft tissues corresponds to a  
 169 240-min thermal exposure at 43 °C (Damianou and Hynynen 1993).

### 170 Numerical computation

171 To simulate thermal ablation in the moving heart, the numerical phantom heartbeat is divided  
 172 into 20 phases, which are repeated in time in a cyclic motion. For each phase, motion and  
 173 deformations are accounted for instantaneously in the computation as a snapshot, and no volume  
 174 variation is considered between the phases. Thus, as previously hypothesized, cell volumes are  
 175 assumed constant during the computed phase.

176 The numerical model resolution is computed according to the following pattern. First, to  
177 evaluate the ultrasonic field, the Rayleigh integral equation is computed point-by-point in the selected  
178 area, considering a discretized transducer ( $\lambda/3$ ) as an emitting source. Deformations are then applied  
179 on each centroid of the reference grid, with the vertex of each cell being estimated as a barycenter of  
180 their surrounding centroids. Then, local geometry functions  $G^i$  (Equation B.10) are computed for each  
181 face of every cell and are saved. Thermal conductivity  $k$  is linearly interpolated at the cell faces.  
182 Volumes are evaluated according to Grandy *et al.* (Grandy 1997). According to the Von Neumann  
183 criterion, time step discretization is estimated from the smallest cell after deformation. The source term  
184 is interpolated from the ultrasonic field to the new deformed grid. Finally, Equations 3 and 6 are  
185 applied for each cell at every time step. Cell temperatures calculated to exceed 100 °C are forced to  
186 100 °C for each time step, based on the hypothesis that vaporization occurs and temperature stays  
187 constant (Blauth *et al.* 2020). If a time step goes over a phase time length, the time step is reduced to  
188 the phase time length. Then, the next phase geometry and its corresponding properties are loaded for  
189 the next computation. The results are stored in a 3D cartesian grid where the locations of the  
190 curvilinear grid points are estimated using the stencil walk algorithm (Sadarjoen *et al.* 1998).

191 The numerical model is implemented in C++ on the CIVA platform (CEA-LIST). Computations  
192 are operated on a Dell Tower 7810 computer. The ultrasonic field and BHTE resolution are  
193 parallelized using Microsoft C++ AMP on the GPU (Nvidia GeForce GTX 1080) and the CPU (Intel,  
194 Xeon® E5-2620), respectively.

## 195 **Simulation of a clinical case**

### 196 Targeted zones

197 Two different areas of the numerical heart phantom are targeted: the atrioventricular node  
198 (AVN) and the ventricles apex (VA) (Fig. 3). The AVN is approximately the junction between the four  
199 cardiac cavities where the electrical impulse from the atria propagates in the ventricles. It represents  
200 atria motion and is treated with an esophageal approach. The VA, located at the bottom of the heart, is  
201 treated with a stomach approach. The targets are located at a distance of 55 mm for the AVN and 40  
202 mm for the VA from the ultrasound probe. The motion amplitudes in the AVN and the VA regions are  
203 extracted from displacement maps computed for the deformed model (Appendix A) and are [dX, dY,  
204 dZ] = [9.89±5.12, 13.45±8.83, 6.94±4.89] and [3.92±4.2, 1.70±1.05, 5.38±3.99], with dX, dY and dZ

205 being the displacement amplitude in each dimension in millimeters. The tissue properties are detailed  
206 in Table 1. **The model, as defined in the manuscript, considers the heat-sink effect through a mean**  
207 **perfusion coefficient, valid in any regions of the heart.**

#### 208 Ultrasound probe

209 HIFU is produced with a 3-cm<sup>2</sup> truncated spherical transducer operating at 3 MHz (Vermon,  
210 Tours, France). The transducer is composed of 8 rings, truncated at 14 mm. It has a 40-mm natural  
211 focal length, and it is able to focus electronically in a range of 17 to 55 mm from the transducer surface  
212 (Greillier et al. 2018) (Fig. 4). **As the probe is designed to be used clinically with a transesophageal**  
213 **approach, its movements in the esophagus can be limited. This constraint should be considered**  
214 **numerically to fit in with real applications. Therefore, electronic steering is required to target any**  
215 **regions of the heart without moving the ultrasound source. This source is considered in the ultrasound**  
216 **propagation model with a  $\lambda/3$  discretization.**

#### 217 Simulation parameters

218 On each targeted area, two types of simulations are conducted: one on a static heart to  
219 illustrate the results obtained with a static numerical model (Chavrier et al. 2000) and one on a mobile  
220 and deformable heart using the theory described in this paper (referred to in section *Simulation*  
221 *methods*). **For each simulation, a single continuous sonication** is performed at an acoustic power of 32  
222 W, corresponding to an acoustic intensity of 10.6 W/cm<sup>2</sup> at the transducer surface. **The dimensions of**  
223 **the -3 dB focal zone are 1.5625×12.5×0.625 mm<sup>3</sup> for the AVN and 0.3125×1.25×6.875 mm<sup>3</sup> for the**  
224 **VA.** The heart rate is set to 60 beats per minute (1 Hz). The exposure duration is adapted to reach a  
225 lesion volume of 30 mm<sup>3</sup>.

#### 226 Motion influence on the treatment efficacy and duration

227 The influence of motion on the treatment is evaluated with the following parameters:  
228 temperature distribution,  $t_{43^{\circ}\text{C}}$  distribution (CEM43), volumetric lesion similarity **using the Dice-**  
229 **Sorensen coefficient (DSC) (Dice 1945; Sørensen 1948), undertreated lesion volume corresponding to**  
230 **the lesion volume appearing in the static heart but not in the moving heart ( $V_{\text{under}}$ ), overtreated lesion**  
231 **volume corresponding to the lesion volume appearing in the moving heart and not in the static heart**  
232 **( $V_{\text{over}}$ ) and required duration reaching a 30-mm<sup>3</sup> lesion volume ( $t_v$ ).**

233 Temperature maps are obtained with the new model and are represented in °C for values  
234 exceeding 43 °C. Thermal dose maps are calculated with Equation 6 from temperature maps. All the  
235 results are calculated in seconds and represented in  $\log_{10}(t_{43^{\circ}\text{C}})$  with  $t_{43^{\circ}\text{C}}$  in seconds.

236 The volume of the irreversible lesion is assessed in the thermal dose map, at the end of the  
237 simulation, in the nondeformed grid of the computation space. The number (N) of voxels in the  
238 computed area exceeding the CEM43 thermal dose threshold of 14000 seconds is counted, and the  
239 value is multiplied by the volume of one voxel, also called the elementary volume ( $V_e = 0.3125^3 \text{ mm}^3$ )  
240 as follows:

$$V = N \times V_e \quad (7)$$

241 Volumetric differences in lesion formation are assessed by DSC. DSC considers the  
242 volumetric overlap between the two samples (lesion in the static heart or in the moving heart) to  
243 estimate the volumetric similarity between them as follows:

$$DSC[\%] = \frac{2 \times V_s \cap V_m}{V_s + V_m} \times 100 \quad (8)$$

244 where  $V_s$  and  $V_m$  are the lesions in the static heart and in the moving heart, respectively. However, the  
245 dissimilarity is studied by determining the undertreated (respectively overtreated) volume ratio due to  
246 motion as follows:

$$R_{u/o}[\%] = \frac{V_{u/o}}{V_s} \times 100 \quad (9)$$

247 where  $R_u$  and  $R_o$  are the undertreated and overtreated volume ratios, respectively,  $V_s$  is the reference  
248 volume (in the static heart),  $V_u$  is the undertreated lesion volume and  $V_o$  is the overtreated lesion  
249 volume.

250 To evaluate the time required to treat a specific volume of tissue,  $t_v$ , the treatment of the AVN  
251 region in the moving heart is used as a reference, as it is harder to obtain a large thermal lesion  
252 considering the motion amplitude in the AVN. From this simulation, the thermal lesion volume to reach  
253 is determined with the method described above. Then, with the other configuration, the thermal lesion  
254 volume is calculated at different steps by only considering the lesion at the focal zone and excluding

255 potential secondary lesions. The time step at which the lesion volume is closest to the reference  
256 volume is chosen.

257 All the results were postprocessed with MATLAB 2019b (The MathWorks Inc., Natick, MA,  
258 USA).

## 259 **Results**

### 260 Treatment duration

261 The required duration to treat the same volume of tissue differs depending on the treatment  
262 region. In a static configuration, reaching a  $(29.75 \pm 0.64)$ -mm<sup>3</sup> volume takes 4 s in the ventricular apex  
263 compared to 13 s in the atrioventricular node. Each region responds differently to motion. In the  
264 ventricular apex, treating the same volume with motion takes 3.6 s, corresponding to a 10% decrease  
265 compared to duration in static simulation. In the atrioventricular node, treatment duration increases  
266 substantially with motion. The duration is increased by a factor of 41 compared to the static  
267 configuration with a value of 9 min. All the results are gathered in Table 2.

### 268 Thermal lesion in the ventricular apex

269 The effects of motion on temperature maps, thermal dose distribution, and lesion spread are  
270 also important. The maximum temperature reached at the focus at the end of sonication is 100 °C in  
271 the static configuration and 73.42 °C in the moving configuration. As expected, the thermal spatial  
272 distribution is more diffused, and the values are lower with motion (Fig. 5). The variability in thermal  
273 dose distribution leads to variability in lesion spread and shape (Fig. 6), with a volumetric similarity of  
274 40.82%. The undertreated and overtreated regions correspond to 55.67% and 57.22% of the  
275 reference lesion (in the static heart).

### 276 Thermal lesion in the atrioventricular node

277 Similar results are observed in the atrioventricular node. During the last phase, the maximum  
278 temperature reached in the focal zone is 82.29 °C in the static configuration and 51.75 °C in the  
279 moving configuration. The highest variability in temperature and lesion spread is observed between  
280 static and moving simulations in the atrioventricular node (Fig. 5), and the lesion shape is substantially  
281 different (Fig. 7). The volumetric similarity between simulations with or without motion is of 19.09%.

282 The dissimilarity is estimated using the undertreated and overtreated volume ratios, which are 81.26%  
283 and 77.67%, respectively.

## 284 **Discussion**

285 This paper introduces the theory of a thermal model to predict HIFU treatment effects on  
286 mobile and elastic organs. The novelty of the method is the consideration of organ motion and  
287 deformations within the heat transfer computation for cardiac applications. Moreover, the Eulerian  
288 method is used to offer a different resolution approach based on well-documented references  
289 (Minkowycz et al. 2008; Norris 2000). The BHTE is numerically resolved with the finite volume method  
290 on a 3D nonorthogonal and structured curvilinear grid. By considering heart deformations, the  
291 ultrasound pressure field, the temperature and the thermal dose are calculated at each time step and  
292 can be displayed in both computational and physical space thanks to the stencil walk algorithm.

293 This simulation method is applied to a specific clinical case: the treatment of focal cardiac  
294 arrhythmias with HIFU. The results provide information to study the influence of motion on treatment  
295 efficacy and accuracy, as well as on potential side effects. According to targeted region and motion  
296 consideration, considerable variability is observed when comparing treatment duration to reach the  
297 same lesion volume. Treatment in AVN takes more time than in VA. This difference could be explained  
298 by the treatment approach. The AVN is an internal structure located 55 mm from the transducer. In  
299 contrast, the VA is an external structure situated at a distance of 40 mm from the transducer. In the  
300 simulations, the anatomical configuration is simplified, and the esophagus (for AVN) and stomach (for  
301 VA) layers are not considered in the pressure field computation. Thus, ultrasound propagates through  
302 more structures and more distance to reach the AVN target than for VA. To treat VA, ultrasound only  
303 propagates through water, and thus, the beam is not attenuated, and lesion formation is faster. In  
304 AVN, ultrasound is highly attenuated by myocardium layers, increasing the treatment duration.  
305 Attenuation compensation could be considered to ensure the same intensity *in situ* in both locations,  
306 but the choice was made to apply the same power as the aim of the study was to understand the  
307 relative variation between simulated cases.

308 Treatment duration variability could also be explained by the influence of motion. In VA,  
309 motion speeds up lesion formation because static simulation only depends on diffusion to enlarge the  
310 lesion, while motion can contribute to lesion extension by focusing ultrasound on nearby points. These

311 variations explain the similar shape but different spread of the lesion. In AVN, motion substantially  
312 increases the treatment duration, and the lesion shape and the spread are considerably altered. As  
313 the motion amplitude is large, a temperature rise is produced in the targeted region, as well as in the  
314 surrounding tissue. In both cases, substantial variability in thermal dose distribution and spread is  
315 observed. This could lead to a decrease in treatment efficacy due to lesion size reduction in the  
316 targeted zone or result in the diminution of treatment accuracy due to secondary lesions in untargeted  
317 regions.

318         Although motion is mainly responsible for the extended treatment duration, perfusion effects  
319 also contribute. **The temperature increase at the targeted point is considerably limited by the**  
320 **convective cooling effect of blood perfusion. In the model, the heat sink effect is only considered**  
321 **through the perfusion rate coefficient, which is the same for both targeted regions. However, from a**  
322 **medical point of view, the heart is composed of four cavities continuously filled by blood and is**  
323 **irrigated by small vessels. As described in the literature, creating HIFU lesions close to vessels is**  
324 **highly challenging because of blood flow (Cilleros et al. 2021; Mohammadpour and Firoozabadi 2020).**  
325 **The heat sink effect is even more critical in cardiac application, as blood circulates both in heart**  
326 **cavities and in vessels irrigating it (Wu et al. 2015). The AVN is located at the center of the four**  
327 **cardiac chambers, creating a lesion in this region could be more difficult than in the VA, which is**  
328 **located between two cavities at the heart tip. Considering perfusion effects due to blood flow in large**  
329 **chambers and in small coronary arteries differently in the model could be interesting to understand**  
330 **their consequences on AVN or VA ablations.**

331         Some limitations may still be acknowledged in the model theory. Under the hypothesis that  
332 acoustic properties are not notably different between healthy tissue and ablated tissue, the ultrasound  
333 propagation map is only computed once on the first frame of the heartbeat cycle. **The other frames are**  
334 **not recomputed, but motion is considered in the thermal model by remapping coordinates of each cell**  
335 **centroid in the reference grid to new curvilinear coordinates, from displacement maps.** While this  
336 reduces computation time, this means that changes in tissue acoustic properties due to lesion  
337 formation are not considered for the computation of pressure field maps and consequently for  
338 temperature maps. Moreover, Guntur *et al.* (Guntur and Choi 2020) recently demonstrated that  
339 underestimating thermal parameter variation can cause a difference of 23% in the temperature

340 distribution. Studying the influence of thermal parameter variation in this manuscript could be  
341 interesting to fit the experimental results of the forthcoming validation study.

342 In the thermal model, arterial blood temperature is assumed to be constant. In some  
343 therapeutic applications, this temperature could increase during sonication and alter the treatment  
344 effects. However, as blood absorption is negligible, the arterial blood temperature increase is low, and  
345 the risk of lesions on vessels is reduced. In fact, our model mainly involves the arterial blood  
346 temperature in perfusion effects during HIFU treatment. As the blood flow is important near the heart,  
347 it can be assumed that the flow can maintain the arterial blood temperature constant enough to  
348 contribute to cooling effects during HIFU sonication.

349 Volume, and consequently density, is assumed constant in deformation evaluation during  
350 each computed phase, as a snapshot, and only varies instantly between two phases. This assumption  
351 follows historical guiding principles of similar papers hypothesizing that myocardium muscle is  
352 incompressible (Humphrey 2002); thus, variability between phases could be neglected. However,  
353 neglecting it may result in variability in the current results. Furthermore, all the simulations are  
354 computed with a spatial resolution of 0.3125 mm to fit the resolution of the deformation maps. A  
355 convergence study is carried out, as referred to in Appendix C, and demonstrates, in a specific case,  
356 that the thermal model converges for spatial resolutions lower than 0.4 mm. Even if the convergence  
357 study is not performed in the beating heart model, the simulation parameters are similar to the cardiac  
358 model and support the belief that the simulations presented in this manuscript can be considered  
359 accurate. However, a more specific convergence study using the beating heart model should still be  
360 conducted. In addition, heart simulation inputs are not as precise as real heart biomechanics. In this  
361 model, registration parameters do not consider the whole biomechanical complexity of heart motion,  
362 particularly torsion. The image registration quality is highly dependent on the raw data (quality,  
363 resolution, imaging modality, etc.) and the chosen parameters. Even if some methods of measuring  
364 heart torsion are well-established (Lehmonen et al. 2020), torsion evaluation is difficult and time-  
365 consuming. Further studies should be conducted to evaluate the impact of torsion variation on HIFU  
366 treatment efficiency and to determine if more precise deformation fields are required.

367 Finally, all simulations are computed with a fixed sonication power of 32 W. This value is  
368 chosen to adhere to the known limits of the HIFU probe, which will be used for future experimental



369 validation of the model. However, this high power could be the source of nonlinearity. Preliminary  
370 studies, based on Sapozhnikov's method to reconstruct an acoustic plane at the surface of the  
371 transducer from a measured plane (Sapozhnikov et al. 2003) and on Westervelt equations to estimate  
372 nonlinear effects (Lafond et al. 2017), demonstrate that nonlinearity is low at this sonication power. In  
373 any case, the model described in this paper is a thermal model and it can use any results from the  
374 ultrasound propagation model, in linear or nonlinear cases, to simulate temperature variation in  
375 ultrasound therapy.

376 Improvements can also be provided in the model application. Simulations are currently  
377 conducted with raw data from a single healthy heart. Other datasets could be considered to study  
378 motion effects considering specific heart anatomy, biomechanics, or electrophysiological responses. In  
379 this study, the secondary lesions close to the transducer are not considered, as the analysis is related  
380 to the influence of motion on the focal zone. However, to define treatment strategies, secondary  
381 lesions should be considered a potential adverse event. Consequently, cooling effects of the water  
382 balloon around the transducer should also be modeled as a means of reducing secondary lesions  
383 close to the transducer. As surrounding tissues are not included in these simulations, future work  
384 examining the influence of these layers on the heat deposition may be of interest.

385 Despite the stated limitations, the model provides very promising results. Simulations  
386 contribute to the understanding of heart mechanisms and motion consequences on CA treatments  
387 with HIFU. These results also contribute to an explanation of the low rate of successful thermal lesions  
388 during the last *in vivo* experiments (Greillier et al. 2018). This study confirms the necessity of adapting  
389 and optimizing CA treatment strategies according to motion and targeted regions. To ensure treatment  
390 efficacy and accuracy, the lesion should be restrained to the targeted zone. Two options could be  
391 considered: applying a duty cycle on sonication to treat only during diastole or using a tracking system  
392 to follow the targeted point during the whole treatment.

393 Further studies should be conducted on the model to provide numerical and experimental  
394 validation, which could examine the difference between simulated and experimental results, and thus,  
395 could further enhance the accuracy of the model.

396 **Conclusion**

397 In this paper, a novel numerical thermal model for HIFU ablation in mobile and elastic organs  
398 is presented. By discretizing and resolving the BHTE on a curvilinear grid, the model is able to  
399 simulate heat transfers in mobile and elastic organs. Simulations are computed for a clinical case of  
400 cardiac arrhythmia treatment and provide realistic results. The study demonstrates that targeted  
401 regions and motion considerably influence treatment duration, lesion shape, and spread. It also  
402 emphasizes the importance of considering motion in HIFU treatment simulation to define efficient and  
403 accurate treatment strategies. Further studies will validate the model experimentally and investigate  
404 HIFU treatment strategies for cardiac arrhythmia therapy.

405 **Acknowledgements**: This work was supported by the French National Research Agency (ANR)  
406 under the CHORUS Grant project ANR17-CE19-0017 and the SATURN Grant project ANR15-CE19-  
407 0016. The author would like to thank Dr. R. Andrew Drainville for proofreading the manuscript.

408 **Conflict of Interest Statement**: The authors declare that they have no conflicts of interest.

## 409 Appendices

### 410 **Appendix A. Numerical phantom**

411 Our simulation uses a numerical phantom obtained from 4D medical images of a heart cycle (3D + t).  
412 This cycle is divided into 20 time phases acquired by a contrast CT-scan with a spatial resolution of  
413  $0.3125^3 \text{ mm}^3$ . From these images, tissues are segmented, and motions **and deformations** are obtained  
414 by image registration (Fig. A.1).

415 Tissue segmentation, motion **and deformation** of these tissues are estimated using the methods  
416 described by Sandoval *et al.* (Sandoval 2015). Image segmentation consists of dividing medical  
417 images into finite tissue regions. First, the first frame tissues are segmented semiautomatically in  
418 ITKSnap using Active Contours. Then, **an affine and** elastic registration (Bspline deformation model  
419 and Mutual Information as similarity measure) is performed between each consecutive gray level  
420 volume of the sequence using the Elastix Library (Klein et al. 2010). The registration estimates the  
421 tissue deformation as the displacement of each voxel from the first phase to their new position at each  
422 phase. Therefore, for any voxel with a center  $M(x,y,z,t_0)$  at the first phase, its new location  $M'(x',y',z',t_n)$   
423 after deformation at a given phase  $n$  is as follows:

$$\mathbf{OM}'(x', y', z', t_n) = \mathbf{OM}(x, y, z, t_0) + \mathbf{v}_n(x, y, z) \quad (\text{A.1})$$

424 where  $O$  is the reference point and  $\mathbf{v}_n$  is the displacement vector corresponding to the phase  $n$ .

425 These consecutive registrations are used to propagate the tissue segmentation to the other frames  
426 and to estimate the displacement of the tissue voxels among the sequence.

### 427 **Appendix B. BHTE discretization: Mathematical theory**

428 This section details the BHTE discretization over a curvilinear grid. Heat transfer computation in  
429 biological tissues implies the BHTE resolution. As the equation is defined on a continuous space, we  
430 discretize it with the finite volume method.

431 First, BHTE is spatially integrated on a cell defined by its volume  $V$  as follows:

$$\underbrace{\iiint_V \rho_t c_t \frac{\partial T_P}{\partial t} dV}_{\text{transient } \Phi_T} = \underbrace{\iiint_V \nabla \cdot k_t \nabla T_P dV}_{\text{diffusion } \Phi_D} + \underbrace{\iiint_V \omega_b c_b (T_A - T_P) dV}_{\text{perfusion } \Phi_{perf}} + \underbrace{\iiint_V Q dV}_{\text{source } \Phi_Q} \quad (\text{B.1})$$

432 The equation is composed of 4 terms: diffusion, perfusion, source and transient. Each term is  
 433 discretized separately.

434 Diffusion term ( $\Phi_D$ ) – This term describes spatial transfer between one tissue location and neighboring  
 435 ones. The main issue to discretize it is the Laplacian. By defining an arbitrary closed surface, i.e., the  
 436 cell surface,  $\Phi_D$  is simplified by the divergence theorem and then discretized into each face of the cell  
 437 as follows:

$$\Phi_D = \iiint_V \nabla \cdot k_t \nabla T_P dV = \oiint_S k_t \nabla T_P \cdot \mathbf{S} dS = \sum_{f=\mathcal{t},\mathcal{b},\mathcal{n},\mathcal{s},\mathcal{w},\mathcal{e}} k_{t_f} \nabla T_P \cdot \mathbf{S}_f \quad (\text{B.2})$$

438 where  $\mathcal{t}, \mathcal{b}, \mathcal{n}, \mathcal{s}, \mathcal{w}, \mathcal{e}$  are the 6 faces of the cells,  $k_{t_f}$  is the linear interpolation of  $k_t$  with surrounding  
 439 cells and  $\mathbf{S} = S \cdot \mathbf{n}$  is the surface vector, where  $\mathbf{n}$  is the normal vector to the surface S.

440 The solution is developed only for face ( $\mathcal{E}$ ), and the same method is applied for the other faces. By the  
 441 chain rule, if composed of derivative functions, the gradient  $\nabla T_P$  can be written as follows:

$$\nabla T_P = \text{grad } T_P = \frac{\partial T_P}{\partial x^j} \mathbf{u}_j = \frac{\partial T_P}{\partial \xi^m} \cdot \frac{\partial \xi^m}{\partial x^j} \mathbf{u}_j \quad (\text{B.3})$$

442 where  $\mathbf{u}^j$  is the Cartesian system basis,  $x^j$  are the coordinates in the Cartesian coordinate system,  
 443 and  $\xi^m$  are the coordinates in a new curvilinear covariant coordinate system. The geometrical  
 444 relationship between the Cartesian system, curvilinear system, and its covariant and contravariant  
 445 vectors are presented in Fig. B.1. By definition, contravariant vectors of the system are written as  $\mathbf{e}^m =$   
 446  $\frac{\partial \xi^m}{\partial x^j} \mathbf{u}_j$  in Einstein notation. Therefore, the gradient can be expressed as follows:

$$\nabla T_P = \frac{\partial T_P}{\partial \xi^m} \cdot \mathbf{e}^m \quad (\text{B.4})$$

447 Contravariant vectors can be expressed with covariant vectors as follows:

$$\mathbf{e}^i = \frac{\mathbf{e}_j \times \mathbf{e}_k}{\mathbf{e}_i \cdot (\mathbf{e}_j \times \mathbf{e}_k)} \quad (\text{B.5})$$

448 where  $\cdot$  is the scalar product,  $\times$  is the vector product and  $(i, j, k)$  is the circular permutation of the  
 449 reference frame. The contravariant vectors can be simplified as follows:

$$\mathbf{e}^i = \frac{\mathbf{e}_j \times \mathbf{e}_k}{\mathbf{e}_i \cdot (\mathbf{e}_j \times \mathbf{e}_k)} \frac{\delta \xi^j \delta \xi^k}{\delta \xi^j \delta \xi^k} = \frac{\delta \xi^j \mathbf{e}_j \times \delta \xi^k \mathbf{e}_k}{\mathbf{e}_i \cdot (\delta \xi^j \mathbf{e}_j \times \delta \xi^k \mathbf{e}_k)} = \frac{\mathbf{s}^i}{\mathbf{e}_i \cdot \mathbf{s}^i} \quad (\text{B.6})$$

450 where  $\mathbf{s}^i = \delta\xi^j \mathbf{e}_j \times \delta\xi^k \mathbf{e}_k$  is called the surface vector,  $\mathbf{s}^{ne} = \delta\xi^j \mathbf{e}_j = \mathbf{d}_j$  is the vector going from  $se$  to  
 451  $ne$  points and  $\mathbf{s}^{te} = \delta\xi^k \mathbf{e}_k = \mathbf{d}_k$  is the vector from  $be$  to  $te$  (Fig. 2). Considering the circular  
 452 permutation, the other surface vectors are defined as  $\mathbf{s}^j = \delta\xi^k \mathbf{e}_k \times \delta\xi^i \mathbf{e}_i$  and  $\mathbf{s}^k = \delta\xi^i \mathbf{e}_i \times \delta\xi^j \mathbf{e}_j$  where  
 453  $\mathbf{PE} = \delta\xi^i \mathbf{e}_i = \mathbf{d}_i$ .

454 Thus, the flow over the ( $e$ ) face of Equation B.3 can be approximated as follows:

$$\begin{aligned} \Phi_{P_e} &= \iint_{S_e} \left( k_{t_e} \frac{\partial T_P}{\partial \xi^1} \mathbf{e}^1 + k_{t_e} \frac{\partial T_P}{\partial \xi^2} \mathbf{e}^2 + k_{t_e} \frac{\partial T_P}{\partial \xi^3} \mathbf{e}^3 \right) dS_e \\ &\approx k_{t_e} \frac{\partial T_P}{\partial \xi^1} \cdot S_e \cdot \mathbf{n} \frac{\mathbf{s}^1}{\mathbf{e}_1 \cdot \mathbf{s}^1} + k_{t_e} \frac{\partial T_P}{\partial \xi^2} \cdot S_e \cdot \mathbf{n} \frac{\mathbf{s}^2}{\mathbf{e}_1 \cdot \mathbf{s}^2} + k_{t_e} \frac{\partial T_P}{\partial \xi^3} \cdot S_e \cdot \mathbf{n} \frac{\mathbf{s}^3}{\mathbf{e}_1 \cdot \mathbf{s}^3} \end{aligned} \quad (\text{B.7})$$

455 As  $S_e = S_e \cdot \mathbf{n}$  is the normal vector to a surface and is defined as the normal vector to the ( $e$ ) face. The  
 456 equation can be simplified as follows:

$$\begin{aligned} \Phi_{D_e} &\approx k_{t_e} \frac{T_E - T_P}{\delta\xi^1} \frac{\mathbf{s}^1}{\mathbf{e}_1 \cdot \mathbf{s}^1} \cdot \mathbf{s}^1 + k_{t_e} \frac{T_{ne} - T_{se}}{\delta\xi^2} \frac{\mathbf{s}^2}{\mathbf{e}_1 \cdot \mathbf{s}^2} \cdot \mathbf{s}^1 + k_{t_e} \frac{T_{te} - T_{be}}{\delta\xi^1} \frac{\mathbf{s}^3}{\mathbf{e}_3 \cdot \mathbf{s}^3} \cdot \mathbf{s}^1 \\ &\approx k_{t_e} (T_E - T_P) \frac{\mathbf{s}^1 \cdot \mathbf{s}^1}{\mathbf{d}_1 \cdot \mathbf{s}^1} + k_{t_e} (T_{ne} - T_{se}) \frac{\mathbf{s}^2 \cdot \mathbf{s}^1}{\mathbf{d}_2 \cdot \mathbf{s}^2} + k_{t_e} (T_{te} - T_{be}) \frac{\mathbf{s}^3 \cdot \mathbf{s}^1}{\mathbf{d}_3 \cdot \mathbf{s}^3} \end{aligned} \quad (\text{B.8})$$

457 For readability concerns, the equation is written as follows:

$$\Phi_{D_e} = \underbrace{k_{t_e} G^1 (T_E - T_P)}_{\text{orthogonal}} + \underbrace{k_{t_e} G^2 (T_{ne} - T_{se}) + k_{t_e} G^3 (T_{te} - T_{be})}_{\text{curvilinear}} \quad (\text{B.9})$$

458 where  $G^1$ ,  $G^2$  and  $G^3$  are local geometry functions of the cell surface:

$$G^1 = \frac{\mathbf{s}^1 \cdot \mathbf{s}^1}{\mathbf{d}_1 \cdot \mathbf{s}^1}; \quad G^2 = \frac{\mathbf{s}^2 \cdot \mathbf{s}^1}{\mathbf{d}_2 \cdot \mathbf{s}^2}; \quad G^3 = \frac{\mathbf{s}^3 \cdot \mathbf{s}^1}{\mathbf{d}_3 \cdot \mathbf{s}^3} \quad (\text{B.10})$$

459 Each term illustrates the energy flow through the projection of  $S_e$  along each curvilinear basis  
 460 component. The first term of the equation accounts for orthogonal energy flow, and the second and  
 461 third terms are corrective terms for curvilinear geometry. Further explanation can be found in Norris'  
 462 thesis (Norris 2000).

463 The diffusion  $\Phi_f$  through an elementary cell is the sum of diffusion on each face. Under the hypothesis  
 464 of constant geometry and time linearity during one phase, the diffusion term is temporally integrated as  
 465 follows:

$$E_D \approx \int_t^{t+dt} \sum_{f=t,\&,n,s,w,e} \Phi_{D_f} dt \approx \left[ \sum_{f=t,\&,n,s,w,e} \Phi_{D_f} \right]_t^{t+dt} \quad (\text{B.11})$$

$$E_D \approx \left( \sum_{f=t,\&,n,s,w,e} h\Phi_{D_f}^{t+dt} - (1-h)\Phi_{D_f}^t \right) \Delta t \quad (\text{B.12})$$

466 where  $h \in [0,1]$  is the time level weighting-factor and its value determines the equation form for  
 467 different resolution schemes (Minkowycz et al. 2008).

468 Transient term ( $\Phi_T$ ) – The transient term describes the time effect in the equation as follows:

$$E_T = \int_t^{t+dt} \iiint_V \rho_t c_t \frac{\partial T_p}{\partial t} dV dt \quad (\text{B.13})$$

469 Under the hypothesis of constant volume during time, the transient term is integrated as follows:

$$E_T = \rho_t c_t (T_p^{t+dt} - T_p^t) V \quad (\text{B.14})$$

470 Perfusion term ( $\Phi_{\text{perf}}$ ) – The perfusion term, also named the heat sink, accounts for blood perfusion  
 471 effects in tissues. Under the hypothesis of constant volume and time linearity, the perfusion term is  
 472 integrated as follows:

$$E_{\text{perf}} = \int_t^{t+dt} \iiint_V \omega_b c_b (T_A - T_p) dV dt \quad (\text{B.15})$$

$$E_{\text{perf}} = \omega_b c_b [T_A - (hT_p^{t+dt} - (1-h)T_p^t)] V \Delta t \quad (\text{B.16})$$

473 Heat source ( $\Phi_Q$ ) – The heat source is the ultrasonic energy absorbed by the tissue. It was defined by  
 474 Damianou *et al.* (Damianou and Hynynen 1993) as follows:

$$Q = F_{\text{mu}} \cdot \alpha \cdot f \cdot \frac{p^2}{\rho \cdot c} \quad (\text{B.17})$$

475 where  $F_{\text{mu}}$  is the absorption ratio,  $\alpha$  ( $\text{Np.m}^{-1}$ ) is the acoustic attenuation,  $p$  (Pa) is the acoustic  
 476 pressure,  $\rho$  ( $\text{kg.m}^{-3}$ ) is the density,  $f$  (Hz) is the frequency and  $c$  ( $\text{m.s}^{-1}$ ) is the speed of sound. Under  
 477 the hypothesis of constant volume and time linearity, the source term is integrated as follows:

$$E_Q = \int_t^{t+dt} \iiint_V Q dV dt = QV \Delta t \quad (\text{B.18})$$

478 where  $Q$  is calculated from pressure fields obtained previously. The pressure is computed in a different  
 479 simulation grid, and its value is estimated by trilinear interpolation at the cell centroid.

480 Equation solution – Gathering all the equation terms, the equation is as follows:

$$\rho_t c_t (T_P^{t+dt} - T_P^t) V = \sum_{f=t,b,n,s,w,e} \left( h \Phi_{D_f}^{t+dt} - (1-h) \Phi_{D_f}^t \right) \Delta t + \omega_b c_b V [T_A - (h T_P^{t+dt} - (1-h) T_P^t)] \Delta t + Q V \Delta t \quad (\text{B.19})$$

481

482 By factorizing, the equation is as follows:

$$T_P^{t+dt} = T_P^t + \frac{\Delta t}{\rho_t c_t} \left( \sum_{f=t,b,n,s,w,e} \frac{h \Phi_{D_f}^{t+dt} - (1-h) \Phi_{D_f}^t}{V} + \omega_b c_b [T_A - (h T_P^{t+dt} - (1-h) T_P^t)] + Q \right) \quad (\text{B.20})$$

483 In computational fluid dynamics (CFD),  $h \in [0,1]$  gives information on the resolution type. Here, the  
 484 explicit solution scheme ( $h = 0$ ) is chosen for implementation concerns. The partial derivative equation  
 485 must be solved with an adapted time step defined with the Von Neumann criterion (Crank and  
 486 Nicolson 1947).

$$T_P^{t+dt} = T_P^t + \frac{\Delta t}{\rho_t c_t} \cdot \left( \frac{1}{V} \sum_{f=t,b,n,s,w,e} \Phi_{D_f}^t + \omega_b c_b (T_A - T_P^t) + Q \right) \quad (\text{B.21})$$

### 487 **Appendix C. Model accuracy: the convergence study**

488 In this section, the accuracy of the model is evaluated. Convergence of the results is assessed by  
 489 studying quantitative result variation depending on the simulation spatial resolution.

490 As the beating heart model is complex, the study is carried out on a simplest model presenting the  
 491 same properties as the heart. The model is a heterogeneous matrix ( $40 \times 40 \times 70 \text{mm}^3$ ) composed of two  
 492 tissues (myocardium and blood) with the properties described in Table 1, and undergoing helical  
 493 displacements, with an absolute amplitude of  $[dX, dY] = [3.11, 17.16]$  mm. Periodic motion repetition is  
 494 set to 1 Hz.

495 The simulated ultrasound probe is the same as that described in section 3.2. Sonication is performed  
 496 continuously at an acoustic power of 32 W (acoustic intensity of  $10.6 \text{ W/cm}^2$ ) at the transducer surface  
 497 for 5 s, with a 36-mm focus. Simulations are computed with different spatial resolutions, ranging from

498 0.2 to 2 mm. For each simulation, the maximum temperature in the focal zone is selected and  
499 compared to the reference. The reference temperature is the value obtained with the smallest spatial  
500 resolution. To consider the convergence of the model, the temperature values should be consecutively  
501 included in the 5%-interval around the reference temperature.

502 The convergence interval is [64.99, 68.33] °C in position 1 and [57.95, 60.93] °C in position 2. The  
503 model starts to converge for a number of elements higher than  $7.1 \times 10^5$ , corresponding to a spatial  
504 resolution of 0.4 mm (Fig. C.1 and Table C.1).

505 The results may still be subject to small variation, since the Von Neumann criterion is used to ensure  
506 model stability, which links the time step with the spatial step. As the spatial step varies in our  
507 convergence study, the time step also changes and the final temperature results can fluctuate.



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809

810 **Figure captions list**

811 Fig. 1. Visualization of the two grids used to describe the simulation model. (a) The reference grid  
812 corresponds to the discretization of the first frame on a heart cycle, which defines the nondeformed  
813 grid of the computation space. (b) The curvilinear grid corresponds to the displacement of reference  
814 grid centroids to their new location according to heart deformation extracted from another frame. Each  
815 frame has its specific curvilinear grid that defines the physical space, as the grid describes the real  
816 heart deformations.

817 Fig. 2. Description of 3D hexahedral cell geometry. In (a), the cell is described by its centroid  $\mathcal{P}$ , eight  
818 vertices and six faces:  $t, b, n, s, w$  and  $e$ . Each neighboring cell is described by its own centroid: top  
819 ( $\mathcal{T}$ ), bottom ( $\mathcal{B}$ ), north ( $\mathcal{N}$ ), south ( $\mathcal{S}$ ), west ( $\mathcal{W}$ ) and east ( $\mathcal{E}$ ). In (b), the surface vector of face  $e$  is  
820 expressed in the system coordinates base ( $e_1, e_2, e_3$ ).

821 Fig. 3. Targeted zones in the heart: atrioventricular node (AVN) and ventricular apex (VA).

822 Fig. 4. Ultrasound probe: (a) Probe head photography, (b) Geometry of the HIFU transducer where all  
823 the rings are of equal-area.  $\varnothing_{\text{HIFU}}$ : diameter of the HIFU transducer;  $T_{\text{HIFU}}$ : truncation;  $\varnothing_{\text{hole}}$ : diameter of  
824 the hole for the imaging probe.

825 Fig. 5. Temperature (left) and thermal dose (right) distributions in the focal zone for static and mobile  
826 heart simulations in the ventricular apex (top) and the atrioventricular node (bottom) for the last  
827 computed phase of the treatment sequence.

828 Fig. 6. Simulation results in the VA. (a) Position of the transducer and the computation zone to target  
829 the VA in the numerical model. Temperature maps, after the last sonication, in the static heart (b) and  
830 in the moving heart (c) for temperatures  $> 43$  °C. The three representations are the 3 planes  
831 intersecting the location of maximum temperature. The colormap is temperature (°C) between 43 and  
832 100 °C. Thermal dose maps of the static heart (d) and the moving heart (e) simulations, with  
833 visualization of the targeted region. The first figure is a 3D representation of the lesion. The three  
834 others are the 3 planes cutting around the maximum dose. The colormap is at a power of 10 seconds,  
835 between 4.15 (14400 seconds) and 15 ( $10^{15}$  seconds).

836 Fig. 7. Simulation results in the AVN. (a) Position of the transducer and the computation zone to target  
837 the AVN in the numerical model. Temperature maps, after the last sonication, in the static heart (b)



838 and the moving heart (c) for temperatures  $> 43$  °C. The three representations are the 3 planes  
839 intersecting the location of maximum temperature. The colormap is in temperature (°C) between 43  
840 and 100 °C. Thermal dose maps of the static heart (d) and the moving heart (e) simulations, with  
841 visualization of the targeted region. The first figure is a 3D representation of the lesion. The three  
842 others are the 3 planes cutting around the maximum dose. The colormap is at a power of 10 seconds,  
843 between 4.15 (14400 seconds) and 15 ( $10^{15}$  seconds).

844 Fig. A.1. Schematic of the process to obtain the 4D numerical heart phantom. Raw data is composed  
845 of 4D CT scans of a heart cycle, divided into 20 phases, with a spatial resolution of  $0.3125^3$  mm<sup>3</sup>.  
846 From the raw data, semiautomatic segmentation with ITK-snap provides a label map of different heart  
847 parts (atria, ventricles, myocardium), and elastic registration with Elastix provides deformation maps at  
848 each phase. A 4D heart model is constructed by combining these two results.

849 Fig. B.1. 2D representation of the relationship between the Cartesian system in the  $(\mathbf{u}_1, \mathbf{u}_2)$  basis and  
850 the curvilinear system described with its covariant  $(\mathbf{e}_1, \mathbf{e}_2)$  and contravariant vectors  $(\mathbf{e}^1, \mathbf{e}^2)$ .  $x^i$  are the  
851 coordinates in the Cartesian system, and  $\xi^m$  are the coordinates in the covariant curvilinear system.

852 Figure C.1. Results of the convergence study. (a) Position of the voxels of interest. (b) Temperature  
853 variation in two points of the mesh grid depending on the number of elements in the mesh (and  
854 consequently on the spatial resolution of the computation). Each point corresponds to the temperature  
855 in position 1 (left) and in position 2 (right) in degrees Celsius (°C) for different spatial resolutions in  
856 mm. The two horizontal lines delimit the convergence interval, and the vertical line delimits the number  
857 of elements from where the results converge.

858 **Tables**

	<b>Heart muscle</b>	<b>Blood</b>
<b>Tissue density, <math>\rho_t</math> (kg.m<sup>-3</sup>)</b>	1081	1050
<b>Acoustic velocity, <math>c</math> (m.s<sup>-1</sup>)</b>	1561	1578
<b>Acoustic attenuation, <math>\alpha</math> (dB.cm<sup>-1</sup>.MHz<sup>-1</sup>)</b>	0.34 (b = 1.26)	0.206 (b = 1.05)
<b>Thermal conductivity, <math>k_t</math> (W.m<sup>-1</sup>.°C<sup>-1</sup>)</b>	0.558	0.517
<b>Specific heat capacity, <math>c_t</math> (J.kg<sup>-1</sup>.°C<sup>-1</sup>)</b>	3686	3617
<b>Perfusion, <math>\omega_b</math> (kg.m<sup>-3</sup>.s<sup>-1</sup>)</b>	19	1160

859 Table 1. Heart and blood properties used in the HIFU treatment numerical model. (Hasgall et al. 2018)

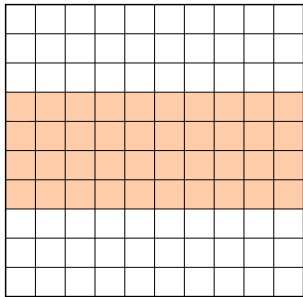
	<b>Ventricular apex</b>	<b>Atrioventricular node</b>
<b>Static heart</b>	duration: 4 s volume: 29.81 mm <sup>3</sup>	duration: 13 s volume: 30.16 mm <sup>3</sup>
<b>Moving heart</b>	duration: 3.6 s volume: 29.08 mm <sup>3</sup>	duration: 9 min volume: 29.51 mm <sup>3</sup>

860 Table 2. Comparison of treatment duration according to the targeted region (ventricular apex or  
861 atrioventricular node) and the presence or absence of motion.

Spatial resolution (mm)	0.2	0.3	0.4	0.5	0.6	0.8	1.0	1.2	1.4	1.6	1.8	2.0
Number of elements in mesh	5.7e6	1.7e6	7.1e5	3.6e5	2.1e5	8.8e4	4.6e4	2.4e4	1.6e4	1.2e4	7.6e3	5.7e3
Temperature at voxel in position 1 (°C)	66.66	65.03	67.18	47.85	55.24	41.55	49.85	40.97	45.53	37	37	37
Temperature at voxel in position 2 (°C)	59.44	59.24	59.23	64.47	52.92	41.2	64.47	41.3	44.89	51.17	45.8	53.78

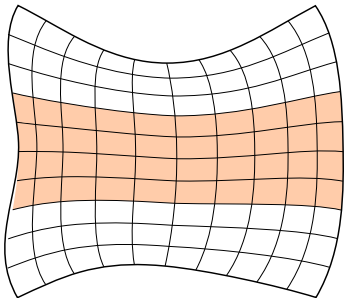
862 Table C.1. Numerical results of the temperature at positions 1 and 2 depending on the spatial  
863 resolution of the simulation.

(a)

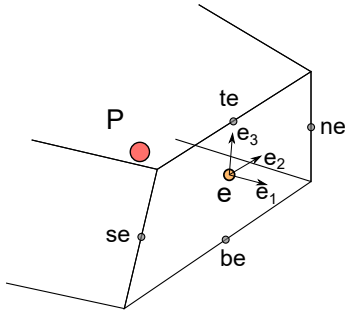
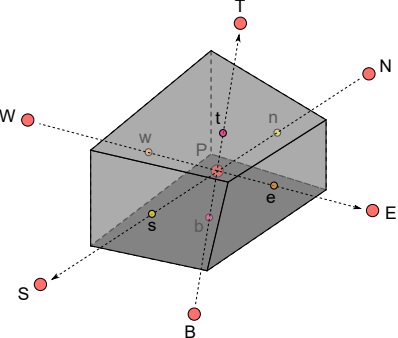


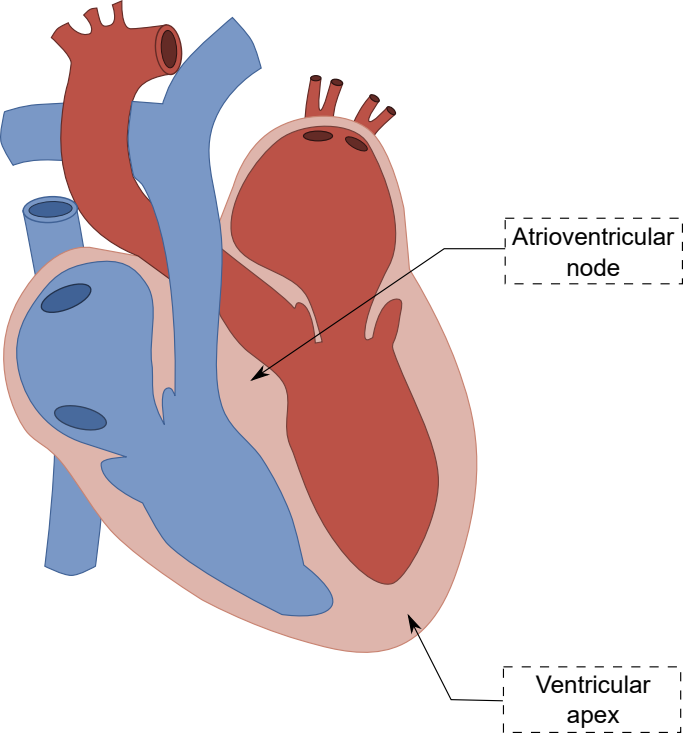
reference grid  
(computation space)

(b)



curvilinear grid  
(physical space)





(a)



(b)

