

Cosmology intertwined: A review of the particle physics, astrophysics, and cosmology associated with the cosmological tensions and anomalies

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Review

Cosmology intertwined: A review of the particle physics, astrophysics, and cosmology associated with the cosmological tensions and anomalies

Elcio Abdalla^a, Guillermo Franco Abellán^b, Amin Aboubrahim^c, Adriano Agnello^d, Özgür Akarsu^e, Yashar Akrami^{f,g,h,i}, George Alestas^j, Daniel Aloni^k, Luca Amendola¹, Luis A. Anchordoqui^{m,n,o}, Richard I. Anderson^p, Nikki Arendse^q, Marika Asgari^{r,s}, Mario Ballardini ^{t, u, v, w}, Vernon Barger ^x, Spyros Basilakos ^{y, z}, Ronaldo C. Batista ^{aa}, Elia S. Battistelli ^{ab, ac}, Richard Battye ^{ad}, Micol Benetti ^{ae, af}, David Benisty ^{ag, ah, ai}, Asher Berlin^{aj}, Paolo de Bernardis^{ab, ac}, Emanuele Berti^{ak}, Bohdan Bidenko^{al, am}, Simon Birrer^{an}, John P. Blakeslee^{ao}, Kimberly K. Boddy^{ap}, Clecio R. Bom^{aq, ar}, Alexander Bonilla^{as}, Nicola Borghi^{at, au}, François R. Bouchet^{av}, Matteo Braglia^{aw, u}, Thomas Buchert^{ax}, Elizabeth Buckley-Geer^{ay,az}, Erminia Calabrese^{ba}, Robert R. Caldwell^{bb}, David Camarena^{bc}, Salvatore Capozziello^{bd,ae}, Stefano Casertano^{be}, Angela Chen^{bg,bh}, Geoff C.-F. Chen^{bf}, Hsin-Yu Chen^{bi}, Jens Chluba^{ad}, Anton Chudaykin^{bj}, Michele Cicoli^{t,v}, Craig J. Copi^f, Fred Courbin^p, Francis-Yan Cyr-Racine^{bk}, Bożena Czerny^{bl}, Maria Dainotti ^{bm,bn,bo}, Guido D'Amico^{bp,bq}, Anne-Christine Davis ^{ag,ah}, Javier de Cruz Pérez ^{br}, Jaume de Haro^{bs}, Jacques Delabrouille^{bt,bu,bv,bw}, Peter B. Denton ^{bx}, Suhail Dhawan ^{by}, Keith R. Dienes ^{bz,ca}, Eleonora Di Valentino ^{cb,*}, Pu Du^{cc}, Dominique Eckert^{cd}, Celia Escamilla-Rivera^{ce}, Agnès Ferté^{cf}, Fabio Finelli^{cg,v}, Pablo Fosalba^{ch,ci}, Wendy L. Freedman^{az}, Noemi Frusciante^{cj}, Enrique Gaztañaga^{ch,ci}, William Giarè^{ck,ac}, Elena Giusarma^{cl}, Adrià Gómez-Valent^{cm}, Will Handley^{cn,co}, Ian Harrison ^{cp}, Luke Hart ^{ad}, Dhiraj Kumar Hazra ^{cq}, Alan Heavens ^g, Asta Heinesen ^{ax}, Hendrik Hildebrandt^{cr}, J. Colin Hill^{cs,ct}, Natalie B. Hogg^{cu}, Daniel E. Holz^{az,cv,cw}, Deanna C. Hooper^{cx}, Nikoo Hosseininejad^{cy}, Dragan Huterer^{cz,da}, Mustapha Ishak^{db}, Mikhail M. Ivanov^{dc}, Andrew H. Jaffe^g, In Sung Jang^{az}, Karsten Jedamzik^{dd}, Raul Jimenez^{de,df}, Melissa Joseph^k, Shahab Joudaki^{dg,dh}, Marc Kamionkowski^{ak}, Tanvi Karwal^{fm}, Lavrentios Kazantzidis^j, Ryan E. Keeley^{di}, Michael Klasen^c, Eiichiro Komatsu^{dj,dk}, Léon V.E. Koopmans^{dl}, Suresh Kumar^{dm}, Luca Lamagna^{ab,ac}, Ruth Lazkoz^{dn}, Chung-Chi Lee^{do}, Julien Lesgourgues^{dp}, Jackson Levi Said^{dq,dr}, Tiffany R. Lewis^{ds}, Benjamin L'Huillier^{dt}, Matteo Lucca^{du}, Roy Maartens^{w,dv,dw}, Lucas M. Macri^{dx}, Danny Marfatia^{dy}, Valerio Marra^{dz,ea,eb}, Carlos J.A.P. Martins^{ec,ed}, Silvia Masi^{ab,ac}, Sabino Matarrese^{ee,ef,eg,eh}, Arindam Mazumdar^{ei}, Alessandro Melchiorri^{ab,ac}, Olga Mena^{ej}, Laura Mersini-Houghton^{ek}, James Mertens^{el}. Dinko Milaković^{eb,ea,em}, Yuto Minami^{en}, Vivian Miranda^{eo}, Cristian Moreno-Pulido^{ep}, Michele Moresco^{at, au}, David F. Mota^{eq}, Emil Mottola^{bk}, Simone Mozzon^{er}, Jessica Muir^{es}, Ankan Mukherjee^{fy}, Suvodip Mukherjee^{es}, Pavel Naselsky^{et}, Pran Nath^{eu}, Savvas Nesseris^{cu}, Florian Niedermann^{ev}, Alessio Notari^{ew}, Rafael C. Nunes^{ex}, Eoin Ó Colgáin^{ey,ez}, Kayla A. Owens^{az}, Emre Özülker^e, Francesco Pace^{fa,fb}, Andronikos Paliathanasis ^{fc, fd}, Antonella Palmese ^{fe}, Supriya Pan ^{ff}, Daniela Paoletti ^{cg, v}, Santiago E. Perez Bergliaffa^{fg}, Leandros Perivolaropoulos^j, Dominic W. Pesce^{fh,fi},





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Valeria Pettorino^{fj}, Oliver H.E. Philcox ^{fk,dc}, Levon Pogosian^{fl}, Vivian Poulin^b, Gaspard Poulot^{cb}, Marco Raveri^{fm}, Mark J. Reid^{fn}, Fabrizio Renzi^{fo}, Adam G. Riess^{ak}, Vivian I. Sabla^{bb}, Paolo Salucci^{fp,fq}, Vincenzo Salzano^{fr}, Emmanuel N. Saridakis^{z,bw,fs}, Bangalore S. Sathyaprakash^{ft,fu,cp}, Martin Schmaltz^k, Nils Schöneberg^{fv}, Dan Scolnic^{fw}, Anjan A. Sen^{fx,fy}, Neelima Sehgal^{fz}, Arman Shafieloo^{ga}, M.M. Sheikh-Jabbari^{gb}, Joseph Silk^{gc}, Alessandra Silvestri^{fo}, Foteini Skara^j, Martin S. Sloth^{gd}, Marcelle Soares-Santos^{bg}, Joan Solà Peracaula^{ep}, Yu-Yang Songsheng^{cc}, Jorge F. Soriano^{m,n}, Denitsa Staicova^{ge}, Glenn D. Starkman^{f,g}, István Szapudi^{gf}, Elsa M. Teixeira^{cb}, Brooks Thomas^{gg}, Tommaso Treu^{bf}, Emery Trott^{bg}, Carsten van de Bruck^{cb}, J. Alberto Vazquez^{gh}, Licia Verde^{gi,gj}, Luca Visinelli^{gk}, Deng Wang^{gl}, Jian-Min Wang^{cc}, Shao-Jiang Wang^{gm}, Richard Watkins^{gn}, Scott Watson^{go}, John K. Webb^{do}, Neal Weiner^{gp}, Amanda Weltman^{gq}, Samuel J. Witte^{gr}, Radosław Wojtak^d, Anil Kumar Yadav^{gs}, Weiqiang Yang^{gt}, Gong-Bo Zhao^{gu,gv}, Miguel Zumalacárregui^{gw}

- ^b Laboratoire Univers & Particules de Montpellier (LUPM), Université de Montpellier (UMR-5299) Place Eugène Bataillon, F-34095 Montpellier Cedex 05, France
- ^c Institut für Theoretische Physik, Westfälische Wilhelms-Universität Münster, Wilhelm-Klemm-Straße 9, 48149 Münster, Germany
- ^d DARK, Niels Bohr Institute, University of Copenhagen, Jagtvej 128, 2200 Copenhagen, Denmark
- ^e Department of Physics, Istanbul Technical University, Maslak 34469 Istanbul, Turkey
- ^f CERCA/ISO, Department of Physics, Case Western Reserve University, 10900 Euclid Avenue, Cleveland, OH 44106, USA
- ^g Astrophysics Group & Imperial Centre for Inference and Cosmology, Department of Physics, Imperial College London, Blackett Laboratory, Prince Consort Road, London SW7 2AZ, United Kingdom
- h Laboratoire de Physique de l'École Normale Supérieure, ENS, Université PSL, CNRS, Sorbonne Université, Université de Paris, F-75005 Paris, France
- ⁱ Observatoire de Paris, Université PSL, Sorbonne Université, LERMA, 75014 Paris, France
- ^j Department of Physics, University of Ioannina, GR-45110, Ioannina, Greece
- ^k Physics Department, Boston University, Boston, MA 02215, USA
- ¹ Institute of Theoretical Physics, Heidelberg University, Philosophenweg 16, 69120 Heidelberg, Germany
- ^m Department of Physics and Astronomy, Lehman College, City University of New York, NY 10468, USA
- ⁿ Department of Physics, Graduate Center, City University of New York, NY 10016, USA
- ^o Department of Astrophysics, American Museum of Natural History, NY 10024, USA
- ^p Institute of Physics, Laboratory of Astrophysics, École Polytechnique Fédérale de Lausanne (EPFL), Observatoire de Sauverny, 1290 Versoix, Switzerland
- ^q Oskar Klein Centre, Department of Physics, Stockholm University, SE-106 91 Stockholm, Sweden
- ^r E.A Milne Centre, University of Hull, Cottingham Road, Hull, HU6 7RX, United Kingdom
- ^s Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh, EH9 3HJ, United Kingdom
- ^t Dipartimento di Fisica e Astronomia, Università di Bologna, viale Berti Pichat 6/2, 40127 Bologna, Italy
- ^u INAF/OAS Bologna, via Piero Gobetti 101, I-40129 Bologna, Italy
- ^v INFN, Sezione di Bologna, viale Berti Pichat 6/2, 40127 Bologna, Italy
- ^w Department of Physics & Astronomy, University of the Western Cape, Cape Town 7535, South Africa
- x Department of Physics, University of Wisconsin, Madison, WI 53706, USA
- ^y Academy of Athens, Research Center for Astronomy and Applied Mathematics, Soranou Efesiou 4, 11527, Athens, Greece
- ^z National Observatory of Athens, Lofos Nymfon, 11852 Athens, Greece
- ^{aa} Escola de Ciências e Tecnologia, Universidade Federal do Rio Grande do Norte, 59078-970, Natal, RN, Brazil
- ^{ab} Dipartimento di Fisica, Sapienza Università di Roma, P.le A. Moro 2, I-00185, Roma, Italy
- ^{ac} INFN Sezione di Roma, P.le A. Moro 2, I-00185, Roma, Italy
- ^{ad} Jodrell Bank Centre for Astrophysics, University of Manchester, Oxford Road, Manchester M13 9PL, United Kingdom
- ^{ae} Scuola Superiore Meridionale, Largo S. Marcellino 10, I-80138, Napoli, Italy
- ^{af} Istituto Nazionale di Fisica Nucleare (INFN) Sezione di Napoli, Complesso Universitario di Monte Sant'Angelo, Edificio G, Via Cinthia, I-80126, Napoli, Italy
- ^{ag} DAMTP, Centre for Mathematical Sciences, University of Cambridge, Wilberforce Road, Cambridge CB3 0WA, United Kingdom
- ^{ah} Kavli Institute of Cosmology (KICC), University of Cambridge, Madingley Road, Cambridge, CB3 OHA, United Kingdom
- ^{ai} Queens' College, Cambridge, CB3 9ET, United Kingdom
- ^{aj} Theoretical Physics Department, Fermilab, P.O. Box 500, Batavia, IL 60510, USA
- ^{ak} Department of Physics and Astronomy, Johns Hopkins University, Baltimore, MD 21218, USA
- ^{al} Kapteyn Astronomical Institute, University of Groningen, P.O. Box 9000, 9700 AA Groningen, the Netherlands
- am Van Swinderen Institute for Particle Physics and Gravity, University of Groningen, Nijenborgh 4, 9747 AG Groningen, the Netherlands
- ^{an} Kavli Institute for Particle Astrophysics and Cosmology and Department of Physics, Stanford University, Stanford, CA 94305, USA
- ^{ao} NSF's National Optical-Infrared Astronomy Research Laboratory (NOIRLab), Tucson, AZ 85719, USA
- ^{ap} Department of Physics, The University of Texas at Austin, Austin, TX 78712, USA
- ^{aq} Centro Brasileiro de Pesquisas Físicas, Rua Dr. Xavier Sigaud 150, 22290-180 Rio de Janeiro, RJ, Brazil
- ar Centro Federal de Educação Tecnológica Celso Suckow da Fonseca, Rodovia Márcio Covas, lote J2, quadra J Itaguaí, Brazil
- ^{as} Departamento de Física, Universidade Federal de Juiz de Fora, 36036-330, Juiz de Fora, MG, Brazil
- ^{at} Dipartimento di Fisica e Astronomia "Augusto Righi", Alma Mater Studiorum Università di Bologna, via Piero Gobetti 93/2, I-40129 Bologna, Italy
- au INAF Osservatorio di Astrofisica e Scienza dello Spazio di Bologna, via Piero Gobetti 93/3, I-40129 Bologna, Italy
- av Institut d'Astrophysique de Paris, CNRS & Sorbonne University, 98 bis Boulevard Arago, 75014, Paris, France
- ^{aw} Instituto de Fisica Teorica, Universidad Autonoma de Madrid, Madrid, 28049, Spain
- ^{ax} Univ Lyon, Ens de Lyon, Univ Lyon 1, CNRS, Centre de Recherche Astrophysique de Lyon UMR5574, F–69007, Lyon, France
- ^{ay} Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510, USA
- ^{az} Department of Astronomy and Astrophysics, University of Chicago, Chicago, IL 60637, USA
- ba School of Physics and Astronomy, Cardiff University, The Parade, Cardiff, CF24 3AA, United Kingdom
- bb Department of Physics & Astronomy, Dartmouth College, 6127 Wilder Laboratory, Hanover, NH 03755, USA
- ^{bc} PPGCosmo, Universidade Federal do Espírito Santo, 29075-910, Vitória, ES, Brazil
- bd Dipartimento di Fisica "E. Pancini", Università degli Studi di Napoli "Federico II", Complesso Universitario di Monte S. Angelo, Ed. G, Via Cinthia, I-80126, Napoli, Italy

^a Instituto de Física, Universidade de São Paulo - C.P. 66318, CEP: 05315-970, São Paulo, Brazil

- ^{be} Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA
- ^{bf} Department of Physics and Astronomy, University of California, Los Angeles CA 90095, USA
- bg Department of Physics, University of Michigan, Ann Arbor, MI 48109, USA
- ^{bh} Kavli Institute for the Physics and Mathematics of the Universe (Kavli IPMU, WPI), Kashiwanoha, Chiba, 277-8583, Japan
- bi Department of Physics and Kavli Institute for Astrophysics and Space Research, Massachusetts Institute of Technology, 77 Massachusetts Ave, Cambridge, MA
- 02139 USA
- ^{bj} Department of Physics & Astronomy, McMaster University, 1280 Main Street West, Hamilton, ON L8S 4M1, Canada
- ^{bk} Department of Physics and Astronomy, University of New Mexico, Albuquerque, NM 87106, USA
- ^{bl} Center for Theoretical Physics. Polish Academy of Sciences. Al. Lotnikow 32/46, 02-668 Warsaw. Poland
- bm National Astronomical Observatory of Japan, 2 Chome-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan
- ^{bn} The Graduate University for Advanced Studies, SOKENDAI, Shonankokusaimura, Hayama, Miura District, Kanagawa 240-0193, Japan
- bo Space Science Institute, Boulder, CO, USA
- ^{bp} Dipartimento di Scienze Matematiche, Fisiche e Informatiche, Università di Parma, Parco Area delle Scienze 7/A, 43124 Parma, Italy
- ^{bq} INFN Gruppo Collegato di Parma, 43124 Parma, Italy
- br Department of Physics, Kansas State University, 116 Cardwell Hall, Manhattan, KS 66502, USA
- ^{bs} Departament de Matemática Aplicada, Universitat Politècnica de Catalunya, Diagonal 647, 08028 Barcelona, Spain
- bt CNRS-UCB International Research Laboratory, Centre Pierre Binétruy, IRL2007, CPB-IN2P3, Berkeley, USA
- ^{bu} Laboratoire Astroparticule et Cosmologie (APC), CNRS/IN2P3, Université Paris Diderot, 75205 Paris Cedex 13, France
- bv IRFU, CEA, Université Paris Saclay, 91191 Gif-sur-Yvette, France
- bw Department of Astronomy, School of Physical Sciences, University of Science and Technology of China, Hefei, Anhui 230026, PR China
- bx High Energy Theory Group, Physics Department, Brookhaven National Laboratory, Upton, NY 11973, USA
- by Institute of Astronomy and Kavli Institute for Cosmology, University of Cambridge, Madingley Road, Cambridge CB3 0HA, United Kingdom
- ^{bz} Department of Physics, University of Arizona, Tucson, AZ 85721, USA
- ca Department of Physics, University of Maryland, College Park, MD 20742, USA
- cb School of Mathematics and Statistics, University of Sheffield, Hounsfield Road, Sheffield S3 7RH, United Kingdom
- ^{cc} Key Laboratory for Particle Astrophysics, Institute of High Energy Physics, Chinese Academy of Sciences, 19B Yuauan Road, Beijing 100049, PR China
- ^{cd} Department of Astronomy, University of Geneva, Ch. d'Ecogia 16, CH-1290 Versoix, Switzerland
- ce Instituto de Ciencias Nucleares, Universidad Nacional Autónoma de México, Circuito Exterior C.U., A.P. 70-543, México D.F. 04510, Mexico
- ^{cf} Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, CA, 91109, USA
- ^{cg} Osservatorio di Astrofisica e Scienza dello Spazio di Bologna & Istituto Nazionale di Astrofisica, via Gobetti 101, I-40129 Bologna, Italy
- ^{ch} Institute of Space Sciences (ICE, CSIC), Campus UAB, Carrer de Can Magrans, s/n, 08193 Barcelona, Spain
- ^{ci} Institut d'Estudis Espacials de Catalunya (IEEC), Carrer Gran Capità 2-4, 08193 Barcelona, Spain
- ^{cj} Instituto de Astrofísica e Ciências do Espaço, Faculdade de Ciências da Universidade de Lisboa, Edificio C8, Campo Grande, P-1749016, Lisboa, Portugal
- ck Galileo Galilei Institute for theoretical physics, National Centre of Advanced Studies of INFN Largo Enrico Fermi 2, I-50125, Firenze, Italy
- ^{cl} Department of Physics, Michigan Technological University, Houghton, MI 49931, USA
- ^{cm} Dipartamento di Fisica and INFN Sezione di Roma Tor Vergata, via della Ricerca Scientifica 1, 00133 Roma, Italy
- ^{cn} Astrophysics Group, Cavendish Laboratory, J. J. Thomson Avenue, Cambridge, CB3 OHE, United Kingdom
- ^{co} Kavli Institute for Cosmology, Madingley Road, Cambridge, CB3 0HA, United Kingdom
- ^{cp} School of Physics and Astronomy, Cardiff University, Cardiff, CF24 3AA, United Kingdom
- ^{cq} The Institute of Mathematical Sciences, HBNI, CIT Campus, Chennai 600113, India
- cr Ruhr University Bochum, Faculty of Physics and Astronomy, Astronomical Institute (AIRUB), German Centre for Cosmological Lensing, 44780 Bochum, Germany
- ^{cs} Department of Physics, Columbia University, New York, NY 10027, USA
- ^{ct} Center for Computational Astrophysics, Flatiron Institute, New York, NY 10010, USA
- ^{cu} Instituto de Física Teórica UAM-CSIC, C/ Nicolás Cabrera 13-15, Universidad Autónoma de Madrid, Cantoblanco, Madrid 28049, Spain
- cv Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA
- cw Department of Physics and Enrico Fermi Institute, University of Chicago, Chicago IL 60637, USA
- ^{cx} Department of Physics and Helsinki Institute of Physics. PL 64. FI-00014 University of Helsinki. Finland
- ^{cy} Department of Physics, Shahid Beheshti University, 1983969411, Tehran, Iran
- ^{cz} Department of Physics, University of Michigan, 450 Church St, Ann Arbor, MI 48109-1040, USA
- da Leinweber Center for Theoretical Physics, University of Michigan, 450 Church St, Ann Arbor, MI 48109-1040, USA
- db Department of Physics, The University of Texas at Dallas, Richardson, TX 75080, USA
- dc School of Natural Sciences, Institute for Advanced Study, 1 Einstein Drive, Princeton, NJ 08540, USA
- ^{dd} Laboratoire de Univers et Particules de Montpellier, UMR5299-CNRS, Universite de Montpellier, 34095 Montpellier, France
- ^{de} ICCUB, University of Barcelona, Marti i Franques 1, Barcelona, 08028, Spain
- ^{df} ICREA, Pg. Lluis Companys 23, Barcelona, 08010, Spain
- dg Waterloo Centre for Astrophysics, University of Waterloo, 200 University Ave W, Waterloo, ON N2L 3G1, Canada
- ^{dh} Department of Physics and Astronomy, University of Waterloo, 200 University Ave W, Waterloo, ON N2L 3G1, Canada
- ^{di} Department of Physics, University of California Merced, 5200 North Lake Road, Merced, CA 95343, USA
- ^{dj} Max Planck Institute for Astrophysics, Karl-Schwarzschild-Str. 1, D-85748 Garching, Germany
- dk Kavli Institute for the Physics Mathematics of the Universe (Kavli IPMU, WPI), Todai Institutes for Advanced Study, The University of Tokyo, Kashiwa 277-8583, Japan
- Kapteyn Astronomical Institute, University of Groningen, P.O. Box 800, 9700AV Groningen, the Netherlands
- ^{dm} Department of Mathematics, Indira Gandhi University, Meerpur, Haryana-122502, India
- ^{dn} Department of Physics, University of the Basque Country UPV/EHU, P.O. Box 644, 48080 Bilbao, Spain
- ^{do} Clare Hall, University of Cambridge, Herschel Rd, Cambridge CB3 9AL, United Kingdom
- ^{dp} Institute for Theoretical Particle Physics and Cosmology (TTK), RWTH Aachen University, D-52056 Aachen, Germany
- ^{dq} Institute of Space Sciences and Astronomy, University of Malta, Msida, MSD 2080, Malta
- ^{dr} Department of Physics, University of Malta, Msida, MSD 2080, Malta
- ds Astroparticle Physics Laboratory, NASA Goddard Space Flight Center, Greenbelt, MD, USA
- ^{dt} Department of Physics and Astronomy, Sejong University, Seoul 05006, Republic of Korea
- ^{du} Service de Physique Théorique, Université Libre de Bruxelles, Boulevard du Triomphe, CP225, 1050 Brussels, Belgium
- dv Institute of Cosmology & Gravitation, University of Portsmouth, Portsmouth PO1 3FX, United Kingdom
- dw National Institute for Theoretical & Computational Sciences (NITheCS), Pretoria 2600, South Africa
- dx George P. and Cynthia W. Mitchell Institute for Fundamental Physics & Astronomy, Department of Physics & Astronomy, Texas A&M University, College Station,
- TX, USA
- ^{dy} Department of Physics and Astronomy, University of Hawaii, Honolulu, HI 96822, USA
- dz Núcleo de Astrofísica e Cosmologia (Cosmo-ufes) & Departamento de Física, Universidade Federal do Espírito Santo, 29075-910, Vitória, ES, Brazil
- ea INAF Osservatorio Astronomico di Trieste, via Tiepolo 11, 34131 Trieste, Italy
- eb IFPU Institute for Fundamental Physics of the Universe, via Beirut 2, 34151, Trieste, Italy
- ec Centro de Astrofísica da Universidade do Porto, Rua das Estrelas, 4150-762 Porto, Portugal

^{ed} Instituto de Astrofísica e Ciências do Espaço, Universidade do Porto, Rua das Estrelas, 4150-762 Porto, Portugal

ee Dipartimento di Fisica e Astronomia "Galileo Galilei", Università degli Studi di Padova, via F. Marzolo 8, I-35131, Padova, Italy

^{ef} INFN, Sezione di Padova, via F. Marzolo 8, I-35131, Padova, Italy

- ^{eg} INAF-Osservatorio Astronomico di Padova, Vicolo dell'Osservatorio 5, I-35122 Padova, Italy
- ^{eh} Gran Sasso Science Institute, Viale F. Crispi 7, I-67100 L'Aquila, Italy
- ei Department of Physics, Indian Institute of Technology Kharagpur, Kharagpur 721302, India
- ^{ej} Instituto de Física Corpuscular (CSIC-Universitat de València), Paterna, Spain
- ek Department of Physics and Astronomy, University of North Carolina at Chapel Hill, NC, 27599, USA
- el Department of Physics and McDonnell Center for the Space Sciences, Washington University, St. Louis, MO 63130, USA
- em INFN, Sezione di Trieste, Via Bonomea 265, 34136 Trieste, Italy
- ^{en} Research Center for Nuclear Physics, Osaka University, Ibaraki, Osaka, 567-0047, Japan
- eo C. N. Yang Institute for Theoretical Physics, Stony Brook University, Stony Brook, NY 11794, USA
- ep Departament de Física Quàntica i Astrofísica and Institute of Cosmos Sciences, Universitat de Barcelona, Av. Diagonal 647, E-08028 Barcelona, Catalonia, Spain
- ^{eq} Institute of Theoretical Astrophysics, University of Oslo, 0315 Oslo, Norway
- er Institute of Cosmology and Gravitation, University of Portsmouth, Portsmouth, PO13FX, United Kingdom
- es Perimeter Institute for Theoretical Physics, 31 Caroline Street N., Waterloo, Ontario, N2L 2Y5, Canada
- ^{et} Niels Bohr Institute, Blegdamsvej 17, Copenhagen, Denmark
- ^{eu} Department of Physics, Northeastern University, Boston, MA 02115, USA
- ev Nordita, KTH Royal Institute of Technology and Stockholm University, Hannes Alfvéns väg 12, SE-106 91 Stockholm, Sweden
- ew Departament de Física Quàntica i Astrofísica & Institut de Ciències del Cosmos (ICCUB), Universitat de Barcelona, Martí i Franquès 1, 08028 Barcelona, Spain
- ex Divisão de Astrofísica, Instituto Nacional de Pesquisas Espaciais, Avenida dos Astronautas 1758, São José dos Campos, 12227-010, SP, Brazil
- ey Center for Quantum Spacetime, Sogang University, Seoul 121-742, Republic of Korea
- ez Department of Physics, Sogang University, Seoul 121-742, Republic of Korea
- ^{fa} Dipartimento di Fisica, Università di Torino, Via P. Giuria 1, I-10125, Torino, Italy
- ^{fb} INFN, Sezione di Torino, Via P. Giuria 1, I-10125, Torino, Italy
- ^{fc} Institute of Systems Science, Durban University of Technology, Durban 4000, South Africa
- ^{fd} Instituto de Ciencias Físicas y Matemáticas, Universidad Austral de Chile, Valdivia, Chile
- ^{fe} Department of Physics, University of California Berkeley, 366 LeConte Hall MC 7300, Berkeley, CA, 94720, USA
- ^{ff} Department of Mathematics, Presidency University, 86/1 College Street, Kolkata 700073, India
- ^{fg} Departamento de Física Teórica, Instituto de Física, Universidade do Estado de Rio de Janeiro, CEP 20550-013, Rio de Janeiro, Brazil
- ^{fh} Center for Astrophysics | Harvard & Smithsonian, 60 Garden Street, Cambridge, MA 02138, USA
- ^{fi} Black Hole Initiative at Harvard University, 20 Garden Street, Cambridge, MA 02138, USA
- ^{fj} AIM, CEA, CNRS, Université Paris-Saclay, Université de Paris, F-91191 Gif-sur-Yvette, France
- ^{fk} Department of Astrophysical Sciences, Princeton University, Princeton, NJ 08540, USA
- fl Department of Physics, Simon Fraser University, Burnaby, BC, V5A 1S6, Canada
- ^{fm} Center for Particle Cosmology, Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, PA 19104, USA
- ^{fn} Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA
- ^{fo} Lorentz Institute for Theoretical Physics, Leiden University, PO Box 9506, Leiden 2300 RA, the Netherlands
- ^{fp} SISSA, Via Bonomea 265, Trieste, 34100, Italy
- ^{fq} INFN, QGSKY Sez. Trieste, Italy
- fr Institute of Physics, University of Szczecin, Wielkopolska 15, 70-451 Szczecin, Poland
- fs CAS Key Laboratory for Research in Galaxies and Cosmology, University of Science and Technology of China, Hefei, Anhui 230026, PR China
- ft Institute for Gravitation and the Cosmos, Department of Physics, Penn State University, University Park, PA 16802, USA
- ^{fu} Department of Astronomy and Astrophysics, Penn State University, University Park, PA 16802, USA
- f^v Dept. Física Quàntica i Astrofísica, Institut de Ciències del Cosmos (ICCUB), Facultat de Física, Universitat de Barcelona (IEEC-UB), Martí i Franqués, 1, E08028

Barcelona, Spain

- fw Department of Physics, Duke University, Durham, NC 27708, USA
- ^{fx} School of Arts and Sciences, Ahmedabad University, Ahmedabad, Gujarat, India
- ^{fy} Centre for Theoretical Physics, Jamia Millia Islamia, New Delhi 110025, India
- ^{fz} Physics and Astronomy Department, Stony Brook University, Stony Brook, NY 11794, USA
- ^{ga} Korea Astronomy and Space Science Institute, Daejeon 34055, Republic of Korea
- ^{gb} School of Physics, Institute for Research in Fundamental Sciences (IPM), P.O.Box 19395-5531, Tehran, Iran
- gc Institut d'Astrophysique, 75014 Paris, France
- gd CP³-Origins, Center for Cosmology and Particle Physics Phenomenology, University of Southern Denmark, Campusvej 55, 5230 Odense M, Denmark
- ge Institute for Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Sofia 1784, Tsarigradsko shosse 72, Bulgaria
- ^{gf} Institute for Astronomy, University of Hawaii, 2680 Woodlawn Drive, Honolulu, HI, 96822, USA
- gg Department of Physics, Lafayette College, Easton, PA 18042, USA
- ^{gh} Instituto de Ciencias Físicas, Universidad Nacional Autónoma de México, Cuernavaca, Morelos, 62210, Mexico
- ^{gi} Institut de Ciències del Cosmos, Universitat de Barcelona, Martí Franquès 1, Barcelona 08028, Spain
- ^{gj} ICREA, Institució Catalana de Recerca i Estudis Avançats, Passeig Lluís Companys 23, Barcelona 08010, Spain
- gk Tsung-Dao Lee Institute (TDLI) & School of Physics and Astronomy, Shanghai Jiao Tong University, Shengrong Road 520, 201210 Shanghai, PR China
- ^{gl} National Astronomical Observatories, Chinese Academy of Sciences, Beijing, 100012, PR China
- gm CAS Key Laboratory of Theoretical Physics, Institute of Theoretical Physics, Chinese Academy of Sciences, Beijing 100190, PR China
- ^{gn} Department of Physics, Willamette University, Salem, OR 97301, USA
- ^{go} Syracuse University, Syracuse, NY, USA
- gp Center for Cosmology and Particle Physics, Department of Physics, New York University, New York, NY 10003, USA
- gq HEPCAT Group, Department of Mathematics and Applied Mathematics, University of Cape Town, 7700, South Africa
- ^{gr} Gravitation Astroparticle Physics Amsterdam (GRAPPA), Anton Pannekoek Institute for Astronomy and Institute for Physics, University of Amsterdam, Science Park 904, 1090 GL Amsterdam, the Netherlands
- gs United College of Engineering and Research, Greater Noida 201310, India
- ^{gt} Department of Physics, Liaoning Normal University, Dalian, 116029, PR China
- ^{gu} National Astronomy Observatories, Chinese Academy of Sciences, Beijing, 100101, PR China
- gv University of Chinese Academy of Sciences, Beijing, 100049, PR China
- gw Max Planck Institute for Gravitational Physics (Albert Einstein Institute), Am Mühlenberg 1, D-14476 Potsdam-Golm, Germany
- * Corresponding author. E-mail address: e.divalentino@sheffield.ac.uk (E. Di Valentino).

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ABSTRACT

The standard Λ Cold Dark Matter (Λ CDM) cosmological model provides a good description of a wide range of astrophysical and cosmological data. However, there are a few big open questions that make the standard model look like an approximation to a more realistic scenario yet to be found. In this paper, we list a few important goals that need to be addressed in the next decade, taking into account the current discordances between the different cosmological probes, such as the disagreement in the value of the Hubble constant H_0 , the σ_8 -S₈ tension, and other less statistically significant anomalies. While these discordances can still be in part the result of systematic errors, their persistence after several years of accurate analysis strongly hints at cracks in the standard cosmological scenario and the necessity for new physics or generalisations beyond the standard model. In this paper, we focus on the 5.0 σ tension between the *Planck* CMB estimate of the Hubble constant H_0 and the SH0ES collaboration measurements. After showing the H_0 evaluations made from different teams using different methods and geometric calibrations, we list a few interesting new physics models that could alleviate this tension and discuss how the next decade's experiments will be crucial. Moreover, we focus on the tension of the Planck CMB data with weak lensing measurements and redshift surveys, about the value of the matter energy density Ω_m , and the amplitude or rate of the growth of structure (σ_8 , $f\sigma_8$). We list a few interesting models proposed for alleviating this tension, and we discuss the importance of trying to fit a full array of data with a single model and not just one parameter at a time. Additionally, we present a wide range of other less discussed anomalies at a statistical significance level lower than the H_0-S_8 tensions which may also constitute hints towards new physics, and we discuss possible generic theoretical approaches that can collectively explain the non-standard nature of these signals. Finally, we give an overview of upgraded experiments and next-generation space missions and facilities on Earth that will be of crucial importance to address all these open questions.

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Refere	nces					

Conventions (Table 1)

Table 1

List of notation conventions used in this paper (unless otherwise stated).

Definition	Meaning
$\hbar = c = k_B = 1$	Natural units
$\kappa^2 \equiv 8\pi G_N = M_{\rm Pl}^{-2}$	Gravitational constant
(-+++)	Metric signature
$g_{\mu u}$	Metric tensor
$G_{\mu\nu} \equiv R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R$	Einstein tensor
Λ	Cosmological constant
$ds^{2} = -dt^{2} + a^{2}(t) \left[\frac{dr^{2}}{1 - kr^{2}} + r^{2} \left(d\theta^{2} + \sin^{2}\theta d\phi^{2} \right) \right]$	Friedmann-Lemaître-Robertson-Walker (FLRW) spacetime metric
<i>a</i> (<i>t</i>)	Scale factor
$a_0 = 1$	Scale factor today (set to unity)
t	Cosmic (proper) time
$\tau(t) = \int_0^t \frac{dt'}{a(t')}$	Conformal time
$=\frac{d}{dt}$	Cosmic time derivative
$l = \frac{d}{d\tau}$	Conformal time derivative
$T^{\mu\nu} = \frac{2}{\sqrt{-g}} \frac{\delta \mathcal{L}_m}{\delta g_{\mu\nu}}$	Energy-momentum tensor of the Lagrangian density ${\cal L}$
$z = -1 + \frac{1}{a}$	Cosmological redshift
$H(z) = \frac{\dot{a}}{a}$	Hubble parameter
H ₀	Hubble constant
$h \equiv H_0 / 100 \mathrm{km s^{-1} Mpc^{-1}}$	Dimensionless reduced Hubble constant
ρ_m, ρ_b, ρ_r	Energy density of total matter, baryonic matter, and radiation
$ ho_{\rm DM}, ho_{\rm DE}$	Energy density of dark matter and dark energy
Ω_m	Present-day matter density parameter
$\Omega_r = 2.469 \times 10^{-5} h^{-2} (1 + 0.2271 N_{\rm eff})$	Present-day radiation density parameter
$\Omega_{\rm DM}, \Omega_{\rm DE}$	Present-day density parameters of dark matter and dark energy
$\Omega_{\rm CDM}$	Present-day density parameters of cold dark matter
$\Omega_m(z) = \frac{\kappa^2 \rho_m}{\frac{3}{3}H^2}$	Matter density parameter
$\Omega_r(z) = \frac{\kappa^2 \rho_r}{3H_2^2}$	Relativistic content density parameter
$\Omega_{\rm DE}(z) = \frac{\kappa^2 \rho_{\rm DE}}{3H^2}$	Dark energy density parameter
$W \equiv \frac{p}{\rho}$	Equation of state (EoS) parameter

(continued on next page)

Table 1 (continued)

Definition	Meaning
C _S	Sound speed
$r_{\rm s} \equiv \int_0^{\tau} c_{\rm s}(\tau') \mathrm{d}\tau'$	Sound horizon
$r_d \equiv \overline{r_s}(\tau_d)$	Sound horizon at drag epoch
σ_8	Amplitude of mass fluctuations on scales of $8 h^{-1}$ Mpc
$S_8 = \sigma_8 \sqrt{\Omega_m / 0.3}$	Weighted amplitude of matter fluctuations

Terminology (Table 2)

Table 2

List of the acronyms/terminology used in the paper.

Acronym	Definition	Acronym	Definition
ΛCDM	Λ (Cosmological Constant)-Cold Dark Matter	KSZ	Kinetic Sunyaev-Zel'dovich
ALTB	Λ-Lemaître-Tolman-Bondi	LHC	Large Hadron Collider
AP	Alcock–Paczynsk	LMC	Large Magellanic Cloud
ATLAS	A Toroidal LHC ApparatuS	LoI	Letter Of Interest
BAO	Baryon Acoustic Oscillations	LSS	Large Scale Structure
BBN	Big Bang Nucleosynthesis	LSST	Legacy Survey of Space and Time
BSM	Beyond Standard Model	MGS	Main Galaxy Sample
bTFR	baryonic Tully-Fisher	MSTOP	main-sequence turn off point
CC	Cosmic Chronometers	NGC	New General Catalog
CDM	Cold Dark Matter	NIR	Near infrared
CL	Confidence Level	PMF	Primordial Magnetic Fields
CMB	Cosmic Microwave Background Radiation	PPS	Primordial Power Spectrum
DDE	Dynamical Dark Energy	QFT	Quantum Field Theory
DDM	Dynamical Dark Matter	QSO	Quasi-stellar object
DE	Dark Energy	RSD	Redshift-Space Distorsion
DM	Dark Matter	RVM	Running Vacuum Models
DR	Data Release	SBF	Surface Brightness Fluctuations
EDE	Early Dark Energy	SIDR	Strongly Interacting Dark Radiation
EDR	Early Data Release	SD	Spectral Distortion
EoS	Equation of State	SM	Standard Model
FLRW	Friedmann-Lemaître-Robertson-Walker	SN	Supernovae
FS	Full shape	sta	Statistical
gDE	Graduated Dark Energy	sys	Systematical
GDR	Gaia Data Release	TG	Teleparallel Gravity
GR	General Relativity	TRGB	Tip of the Red Giant Branch
GRB	Gamma Ray Burst	UVES	Ultraviolet and Visual Echelle Spectrograph
IDE	Interacting Dark Energy	VED	Vacuum Energy Density
GW	Gravitational Wave	WL	Weak Lensing
		ZP	Zero-point

Acronyms and references of experiments/missions

Table 3

List of acronyms of the astronomical missions and projects mentioned in the paper. A division of the facilities for science topic is instead reported in Table 4.

Acronym	Experiment	Website	Status
4MOST	4-metre Multi-Object Spectroscopic Telescope	https://4MOST	expected 2023
ACT	Atacama Cosmology Telescope	https://act.princeton.edu	ongoing
ANDES	ArmazoNes high Dispersion Echelle Spectrograph	https://ANDES	planned
ATLAS Probe	Astrophysics Telescope for Large Area Spectroscopy Probe	https://atlas-probe	proposed
BAHAMAS	BAryons and HAloes of MAssive Systems	https://BAHAMAS	2017-2018
BICEP	Background Imaging of Cosmic Extragalactic Polarization	http://bicepkeck.org	ongoing
BINGO	Baryon Acoustic Oscillations	https://bingotelescope.org	planned
	from Integrated Neutral Gas Observations		
BOSS	Baryon Oscillations Spectroscopy Survey	https://BOSS	ongoing
CANDELS	Cosmic Assembly Near-infrared Deep	https://candels	
	Extragalactic Legacy Survey		
CCHP	Carnegie-Chicago Hubble Project	https://carnegiescience.edu	
CE	Cosmic Explorer	https://cosmicexplorer.org	planned
CFHT	Canada-France-Hawaii Telescope	https://cfht.hawaii.edu	ongoing
CHIME	Canadian Hydrogen Intensity Mapping Experiment	https://chime-experiment.ca	ongoing
CLASS	Cosmology Large Angular Scale Surveyor	https://class	ongoing
CMB-HD	Cosmic Microwave Background-High Definition	https://cmb-hd.org	proposed
CMB-S4	Cosmic Microwave Background-Stage IV	https://cmb-s4.org	planned 2029-2036

Table 3 (continued)

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1. Executive summary

This White Paper has been prepared to fulfill SNOWMASS 2021 requirements and it extends the material previously summarized in the four Letters of Interest Di Valentino et al. (2021a,b,c,d). The Particle Physics Community Planning Exercise (a.k.a. *SNOWMASS*) is organized by the Division of Particles and Fields of the American Physical Society, and this is an effort to bring together the community of theoretical physicists and cosmologists and identify promising opportunities to address the questions described.

This White Paper was initiated with the aim of identifying the opportunities in the cosmological field for the next decade, and strengthening the coordination of the community. It is addressed to identifying the most promising directions of investigation, and rather than attempting a long review of the current status of the whole field of research, it focuses on the upcoming theoretical opportunities and challenges described. The White Paper is a collaborative effort led by Eleonora Di Valentino and Luis Anchordoqui, and it is organized in the topics listed below, each of them coordinated by the scientists indicated (alphabetical order):

- Sec. 3. Models comparison: Alan Heavens and Vincenzo Salzano.
- Sec. 4. H₀ measurements/systematics: Simon Birrer, Adam Riess, Arman Shafieloo, and Licia Verde.
- Sec. 5. S₈ measurements/systematics: Marika Asgari, Hendrik Hildebrandt, and Shahab Joudaki.
- Sec. 6. Early Universe measurements/systematics: Mikhail M. Ivanov and Oliver H.E. Philcox.
- Sec. 7. H₀-S₈ proposed solutions: Celia Escamilla-Rivera, Cristian Moreno-Pulido, Supriya Pan, M.M. Sheikh-Jabbari, and Luca Visinelli.
- Sec. 8. Challenges for Λ CDM beyond H_0 and S_8 : Leandros Perivolaropoulos.
- Sec. 9. Stepping up to the new challenges (Perspectives): Wendy Freedman, Adam Riess, and Arman Shafieloo.

Each section begins with a list of contributors who made particular, and in many cases, substantial contributions to the writing of that section. Furthermore, this White Paper is supported by \sim 203 scientists, who participated in brainstorming sessions from August 2020, and provided feedback via regular Zoom seminars and meetings, and the SLACK platform.

This White Paper has been reviewed by Luca Amendola, Spyros Basilakos, Ruth Lazkoz, Eoin Ó Colgáin, Paolo Salucci, Emmanuel Saridakis and Anjan Sen.

2. Introduction

The discovery of the accelerating expansion of the Universe Riess et al. (1998); Perlmutter et al. (1999) has significantly changed our understanding on the dynamics of the Universe and thrilled the entire scientific community. To explain this accelerating expansion, usually two distinct routes are considered. The simplest and the most traditional one is to introduce some exotic fluid with negative pressure in the framework of Einstein's theory of GR, mostly restricted to the FLRW class of solutions, which drives the late-time accelerating expansion of the Universe Copeland et al. (2006); Bamba et al. (2012). Alternatively, generalizations of the FLRW cosmologies by taking into account the role of regional inhomogeneities on large-scale volume dynamics within the full theory of GR provide a possible route, e.g. Refs. Ellis and Buchert (2005); Buchert (2008). One can also modify GR leading to a modified class of gravitational theories or introduce a completely new gravitational theory Capozziello (2002); Nojiri and Odintsov (2006); Capozziello and Francaviglia (2008); Capozziello and De Felice (2008); Sotiriou and Faraoni (2010); De Felice and Tsujikawa (2010); Harko et al. (2011); Capozziello and De Laurentis (2011); Clifton et al. (2012); Cai et al. (2016a); Nojiri et al. (2017). In the latter approaches, the gravitational sector of the Universe is solely responsible for this accelerating expansion where the extra geometrical terms (arising due to inhomogeneities or the modifications of GR) or the new geometrical terms (coming from a new gravitational theory) play the role of DE. Since the discovery of the accelerating phase of the Universe we are witnessing the appearance and disappearance of a variety of cosmological models motivated from these frameworks, thanks to a large amount of observational data; however, the search for the actual cosmological model having to ability to explain the evolution of the Universe correctly is still in progress. Among a number of cosmological models introduced so far in the literature, the Λ CDM cosmological model, the mathematically simplest model with just two heavy ingredients (equivalently, two assumptions), namely, the positive cosmological constant ($\Lambda > 0$) and the CDM came into the picture of modern cosmology.

There is definitely no doubt in the community that the Λ CDM cosmology has been very successful in the race of cosmological models since according to the existing records in the literature, the standard Λ CDM cosmological model provides a remarkable description of a wide range of astrophysical and cosmological probes, including the recent measurement of the CMB temperature at high redshift from H₂O absorption Riechers et al. (2022). The parameters governing the Λ CDM paradigm have been constrained with unprecedented accuracy by precise measurements of the CMB Aghanim et al. (2020a,b); Adachi et al. (2020); Aiola et al. (2020); Dutcher et al. (2021); Ade et al. (2021a). However, despite its marvellous fit to the available observations, there is no reason to forget that Λ CDM cannot explain the key concepts in the understanding of our Universe, namely, Dark Energy Riess et al. (1998); Perlmutter et al. (1999), Dark Matter Trimble (1987) and Inflation Guth (1981).

In the context of the Λ CDM paradigm, DE assumes its simplest form, that is the cosmological constant, without any strong physical basis. The nature of DM is still a mystery except for its gravitational interaction with other sectors, as suggested by the observational evidences. We know, however, that DM is essential for structure formation in the late Universe, so most of it (though not all) must be pressure-less and stable on cosmological time scales. Although attempts have been made to understand the origin of DE and DM in different contexts, such as the alternative gravitational theories beyond Einstein's GR, no satisfactory answers have been found yet that can significantly challenge Einstein's gravitational theory at all scales. Moreover, despite the significant efforts in the last decades to investigate DM and the physics beyond the SM of particle physics, in laboratory experiments and from devised astrophysical observations, no evidence pointing to the dark matter particle has been found Marrodán Undagoitia and Rauch (2016); Gaskins (2016); Buchmueller et al. (2017).

On the other hand, even though the theory of inflation Pimentel et al. (2022) has solved a number of crucial puzzles related to the early evolution of the Universe, it cannot be considered to be the only theory of the early Universe. For example, we do not have a definitive answer to the initial singularity problem,¹ and some of the well known inflationary models have been put before a question mark Ijjas et al. (2013). Moreover, alternative theories to inflation can also not be ruled out in light of the observational evidences Lehners and Steinhardt (2013); Ijjas and Steinhardt (2016). In addition, the possibilities of unification of the early time inflationary epoch with late time cosmic acceleration captured the geometrical grounds, avoiding the introduction of additional degrees of freedom for inflation or DE (see for instance Benisty and Guendelman (2020a,b)). Finally, the study of the primordial non-Gaussianity contributions to the cosmological fluctuations and other cosmological observables Akrami et al. (2020a); Buchert et al. (2017) will become an important probe

¹ Many of the possible alternatives leading to regular cosmological models have been analyzed in Novello and Bergliaffa (2008).

for both the early and the late Universe. Here, one of the many open problems is how to precisely compute the statistical significance of a tension in the presence of significant non-Gaussianity in the posterior distributions of cosmological parameters. While the issue is conceptually straightforward, the large number of dimensions usually involved when comparing surveys of interest makes the calculation challenging.

Undoubtedly, observational data play a very crucial role in this context and we have witnessed a rapid development in this sector. As a consequence, with the increasing sensitivity in the experimental data from various astronomical and cosmological surveys, the heart of modern cosmology - i.e. the physics of the Universe - is getting updated and we are approaching more precise measurements of the cosmological parameters. The progress in observational cosmology has introduced new directions that will drive us to find a suitable cosmological theory in agreement with the observational evidence. In fact, starting from the early evolution of the Universe to the present DE dominated Universe, there are a large number of open issues that require satisfactory explanations by thorough investigations. Therefore, in the next decade, the primary challenges would be to answer the following questions:

- What is the nature of dark matter? How can multi-messenger Engel et al. (2022) (i.e. photons, neutrinos, cosmic rays, and gravitational waves) cosmology help with determining characteristics (mass spectrum and interactions) of the dark matter sector?
- What is the nature of dark energy? Can dark energy be dynamical? Can the cosmic acceleration slow down in future?
- Did the Universe have an inflationary period? How did it happen? What are the physical observables from the inflationary era?
- Does gravity behave like General Relativity even at present day horizon scale H_0^{-1} ? Is there a more fundamental, Modified Gravity, which includes General Relativity as a particular limit?

Even if the performance of Λ CDM is undoubtedly stunning in fitting the observations with respect to the other cosmological theories and models, due to the assumptions and uncertainties listed before, the Λ CDM standard cosmological model is likely to be an approximation to a first principles scenario yet to be found. And this underlying model, which is approximated by Λ CDM so well, is not expected to be drastically different. For this reason, the first step is to look for small deviations or extensions of the minimal Λ CDM model. Throughout we should be conscious that this may not suffice and any new cosmology could be disconnected from the Λ CDM model.

There are a few theoretical unanswered questions, which could indicate the direction to follow to discover this first principles scenario beyond Λ CDM. For instance it will be important to answer the following questions:

- Why the dark energy and the dark matter densities are of the same order (coincidence problem)? Is this coincidence suggesting an interaction between the DE and the DM?
- Are dark energy and inflation connected (as for example in Quintessential Inflation models)? Can we have dark energy with AdS vacua (presence of a negative Λ)?
- How well have we tested the Cosmological Principle? Is the Universe at cosmic scales homogeneous and isotropic?
- Can local inhomogeneity or anisotropy replace the need for dark energy?
- What is the level of non-Gaussianity?
- Do we need quantum gravity, or a unified theory for quantum field theory and GR to complete the standard cosmological model? How does pre-inflation physics impact our observations today? How can we resolve the big bang singularity?
- Can theoretical frameworks, like effective (quantum) field theory have further implications for the dark sector, especially DE?
- How much can we learn from cosmological dark ages and how does its physics impact our models of cosmology?
- How crucial is physics beyond the SM of particle physics for precision cosmology?
- How can we explain the matter-antimatter asymmetry in the observed Universe? There has been observational evidence for a matterantimatter asymmetry in the early Universe, which leads to the remnant matter density we observe today. The bounds on the presence of antimatter in the present-day Universe include the possibility of a large lepton asymmetry in the cosmic neutrino background.
- What are the mutual implications for cosmology and Quantum Gravity of hypotheses like the swampland conjectures?

Finally, there are a few hints in the data suggesting that Λ CDM should be extended to accommodate the emerging discrepancies with different statistical significance between observations at early and late cosmological time Verde et al. (2019). For this reason, it is timely to focus our attention on the strong and robust disagreement at more than 5σ on the Hubble constant H_0 present between the value inferred by the *Planck* CMB experiment Aghanim et al. (2020b) assuming a Λ CDM model and the latest value measured by the SH0ES collaboration Riess et al. (2021b) (see also the reviews Di Valentino et al. (2021b); Knox and Millea (2020); Jedamzik et al. (2021); Saridakis et al. (2021a); Di Valentino et al. (2021g); Perivolaropoulos and Skara (2021b); Shah et al. (2021)). This is followed by the tension at $\sim 3\sigma$ on $\sigma_8 - S_8$ Di Valentino et al. (2021c); Perivolaropoulos and Skara (2021b), or by the anomalies in the *Planck* CMB experiment results, such as the excess of lensing Addison et al. (2016) at $> 3\sigma$, which have put a question mark on the geometry of the Universe Aghanim et al. (2020b); Handley (2021); Di Valentino et al. (2019b, 2021f) and its age. Meanwhile, several statistically independent measures of the violation of statistical isotropy have been identified with at least 3σ significance in the WMAP and *Planck* CMB temperature maps – suppression of large angular correlations, differences between opposite hemispheres, alignment of the quadrupole and octupole. These are complemented by the statistically less significant studies of the cosmic accelerated expansion rate using supernovae as standard candles, that have indicated that an anisotropic expansion rate fit by means of a dipole provides a better fit to the surveys at hand than an isotropic expansion rate at the 2σ level. This dark energy dipole is aligned with the fine structure constant dipole Mariano and Perivolaropoulos (2012). Moreover, as we discuss later in section 7.8 a number of intriguing dipoles appear to be aligned with th

The accumulation of these tensions may suggest the addition of new physics ingredients in the vanilla Λ CDM model, based on cosmological constant and Dark Matter. Therefore, in the next decade, we aim to address these discrepancies by answering the following key questions:

- Can these tensions, individually or together, be systematic errors in the current measurements? Are these tensions statistical flukes or are they pointing to new physics?
- If not due to systematics, what is the origin of the sharpened tension in the observed and inferred values of H_0 , $f\sigma_8$, and S_8 ?

- Are these tensions uncorrelated, or connected and different manifestations of a single tension?
- Is it possible to explain the tensions within the standard Λ CDM cosmology?
- Is the Universe open, flat or closed?
- Are cosmic tensions pointing beyond the FLRW framework?
- Can the pure geometric generalizations of the ΛCDM model, viz., allowing spatial curvature and/or anisotropic or inhomogeneous expansion on top of the spatially flat FLRW space-time metric assumption, while preserving the physics that underpins it, address the tensions related to the ΛCDM model?

Thus, based on the above untold stories, it is difficult to believe that Λ CDM cosmology can be considered the final description of the Universe that can accommodate all the queries raised over the last couple of years. Since the observational sensitivity is increasing with time, it is important and timely to focus on the above-mentioned limitations of this concordance cosmological paradigm, aiming to find a most suitable cosmological theory that can explain some/all the above points.

3. Quantification of "tensions" and model comparison

Coordinators: Alan Heavens and Vincenzo Salzano.

Contributors: M. Benetti, D. Benisty, R. E. Keeley, N. Schöneberg.

3.1. Tensions and the relation to model comparison

The preponderance of different cosmological probes allows the cosmological model to be tested in various ways, and a situation may arise when the different probes appear to give incompatible results. There is currently a debate about the compatibility of results from probes of the Hubble constant H_0 and to a lesser extent from the degree of clustering of matter, often measured by the quantity $S_8 = \sigma_8 (\Omega_m/0.3)^{1/2}$ (see e.g. Refs. (Riess et al., 2021b; Lemos et al., 2021; Lin and Ishak, 2017a)). "Tension" is the term used to describe results that appear to be discrepant, the interesting question being whether such tensions are indications of the need for a revision to the standard cosmological model, or whether they are due to statistical fluctuations, errors or approximations in analysis, or unmodelled systematic effects in the data. Finding the reasons for the apparent discrepancies is a major driver of cosmological research in the near future.

Ideally, we would like to quantify the significance of the disagreement between the outcomes of two different experiments, and this is often expressed as the difference between estimates (typically maximum marginalised posterior values) of cosmological parameters, expressed in units of the uncertainty, usually taken to be the posterior errors of the two experiments added in quadrature (if independent). The interpretation is often based on the probability to exceed the given shift, assuming a Gaussian distribution. For example a "2 sigma tension" corresponds to a 4.6% probability of a larger discrepancy, assuming the cosmological model is correct. However, the ensuing interpretation that the cosmological model only has a 4.6% probability of being correct is unfortunately wrong, and a more sophisticated analysis is necessary. Here we discuss the linked issues of tensions and model comparison - to decide when the data in tension favour an alternative to the standard cosmological model.

From a Bayesian perspective, the question of "goodness of fit" is a thorny one, and the question of whether the data are somehow compatible with a theory is not usually addressed. Without an alternative model, one often can not exclude a statistical fluke. What can be addressed is the relative posterior probabilities of two or more different data models, through computation of the Bayesian Evidence. The first Bayesian interpretations of cosmological tension were published in Refs. (Verde et al., 2013, 2014). This approach transcends the question of what the model parameters are, and asks for the relative model probabilities, conditioned on the data. The most natural way to apply this in the case of tensions is to compute the Bayes factor (the ratio of model likelihoods) for the standard cosmological model in comparison with an alternative model, and interpret it as the posterior odds for the models. A rather hybrid alternative that does not require a new physics model is to postulate two data models: one is the standard cosmological model where the cosmological parameters are common to all experiments; the other allows the cosmological parameters to be different in each experiment. This is a well-posed comparison (albeit with an arguably unrealistic physics model) and Bayesian methods can be used to address it. Implicitly, this is related to the *R* statistic of (Handley and Lemos, 2019a). In either of these comparisons, the outcome is a relative probability of the models, and this is often interpreted using the Jeffreys scale Jeffreys (1939), or the Kass and Raftery revision Kass and Raftery (1995). The latter arguably provides better descriptive words for the relative probabilities, but in the end the probabilities speak for themselves.

Before discussing the Bayesian approach in more detail, a number of methods of measuring the significance of parameter shifts between experiments have recently been proposed in the cosmology literature. These are frequently referred to as "tension metrics" and seek to answer often subtly different questions about the data, and each has advantages and disadvantages (see for example Lin and Ishak (2017b); Raveri and Hu (2019); Lemos et al. (2021)). As measurements of the tension in cosmological parameters improve it will be crucial for cosmologists to continue furthering understanding of how to interpret these measurements, as well as to understand the interplay of nuisance parameters (such as those from photometric redshift estimation) and model mis-specification (e.g., uncertain baryonic physics) with the conclusions.

In addition, cosmological tensions fundamentally involve disagreement between results of experiments and analyses. Each of these experiments and analyses takes part within a given community and with a given set of tools and models. As new data arrive it will be crucial to avoid unconscious biases towards confirmation of previous measurements, or a desire to confirm or deny a tension as real. As such, significant efforts needs to be made in ensuring analyses are performed "blindly", see e.g. Refs. (Muir et al., 2020; Wong et al., 2020; Sellentin, 2020; Abbott et al., 2021a), in ways in which the result is not known to the experimenters until after the analysis choices have been fixed.

Ensuring that it is possible to re-analyse and jointly analyse data sets is also essential, which means both that efforts towards data sharing and replication studies should be highly valued, and that it is necessary to test the data individually to check if they can be combined. In particular, joint analyses can be carried out between data that independently yield compatible results. Although the combination

of complementary cosmological probes makes it possible to break degeneracies between parameter estimates, and also test systematic effects, data that independently point to different parameter spaces will give misleading and unphysical results when combined Efstathiou and Gratton (2020); Gonzalez et al. (2021); Vagnozzi et al. (2021b); Moresco et al. (2022).

When addressing tensions we are concerned with whether or not a given shift in the preferred parameter space between experiments can most probably be explained by a stochastic fluctuation Jenkins and Peacock (2011); Joachimi et al. (2021b) within a given model, or by a mis-specification of the model used to describe the data in each experiment. The proposed "solutions" in the literature and discussed here are attempts to extend the model to describe better the data, either by including new fundamental physics or better understanding the mediating astrophysics and instruments.

An important aspect in assessing these models is the number of model parameters, since an arbitrarily complex model with a sufficient number of parameters can fit any given data set perfectly, so "goodness-of-fit" (however defined) is not in itself a good measure of model probability - the predictions made from such a model will generally not agree with new data. As such, it is important to penalize models with many free parameters in order to ensure that the considered models generalize robustly to new data. Many criteria include an "Occam factor" which penalizes complex models with many free parameters, either explicitly or by considering the increase in the prior volume of the model parameter space (although for the Bayesian Evidence the penalty is not always obvious – a completely unconstrained additional parameter is not penalized at all). In passing, we notice that it is possible that the Physics underlying Dark Matter and the Dark Energy phenomena may be so disconnected with respect to that presently known that it may violate the Occam Paradigm.

At this point it is important to note that the choice of fixing certain parameters while allowing others to vary is often taken arbitrarily in a given model. As such, an important aspect to consider when comparing models is not only whether they reduce the tension metric of choice, but also whether they overall remain a good fit to the data. A simple example of why this is important is a Λ CDM model with $\Omega_{CDM}h^2$ fixed to 0.11, which does give a reduction of the tension between *Planck* and SH0ES to $\sim 1\sigma$, but is also not a good fit to *Planck* data Schöneberg et al. (2021b). Some models proposed to ease the Hubble tensions in the past have restricted their parameter space to regions in which the tension is reduced, but so is the model's ability to fit the data. Whether or not such models should be considered equally or less valid is an important aspect of a given model comparison study. Bayesian Evidence could certainly be used here to compare data models with $\Omega_{CDM}h^2$ fixed and variable, respectively.

3.2. List of statistical tools

Expansion of parameter dimensions can also have other costs in terms of interpretations of tensions. Very high dimensional probability spaces are often projected down to only two (for plotting posterior contours) or one (for quoting error bars), and such projections can mask higher dimensional tensions. As such, it is usually preferable to derive the tension between data sets using the entire parameter space of the given model. However, this should be done with caution because where additional parameters are included which are poorly constrained by a given experiment, the posteriors on other correlated parameters can become dramatically skewed by the "prior volume effect" in which probability mass is used to fill this extra volume Handley and Lemos (2021).

The "explosion" of the tension problems in the latest years has made even more critical an already almost saturated aspect of cosmological research: the number of proposed models has grown steadily (and will continue to) and it has become quite hard to sort out the *more successful* options from *less successful* ones. At this stage, resorting only to the simplest rule of "let us fit the data and see what happens" is obviously not enough and definitively it is not the ultimate tool, but just the first step. Even if we all played with an established *consensus* set of data, we would still have too much degeneracy and biases to assess a hierarchy of reliable models.

This is not a novelty, of course; indeed, we do have tools to provide such a statistical hierarchy. But recent developments have quite clearly exacerbated this problem. It is thus not pointless to try to apply to the realm of statistical comparison tools the same principles which led to Schöneberg et al. (2021b). Can we make a selection of the best/preferred statistical tools we have and we use nowadays to state if and when a given cosmological model is better than another one?

A provisional and surely non-exhaustive list would include:

- χ^2 and reduced χ^2 . The first "obvious" criterion, but which is not satisfactory for a number of reasons: a lower χ^2 does not necessarily point to a better model, since adding more flexibility with extra parameters will normally lead to a lower χ^2 . At best, it can be considered only as *one* (among many) or the *first* indicator to check, but absolutely not exhaustive and definite. Even the reduced χ^2 cannot take into account the complexity of the problem and the degeneracy among the parameters, and from a Bayesian perspective, the minimum χ^2 contains no information on how finely-tuned the parameters have to be an important consideration when assessing the model probability. Moreover, still in the literature the χ^2_{min} is often misused: in a Bayesian approach, to focus or to center a discussion on the specific set of values which correspond to χ^2_{min} does not reflect the fact that these values are uncertain. Some of the statistics discussed below are prone to this criticism.
- Information Criteria Wu and Sepulveda (1998) AIC Akaike (1974), BIC Schwarz (1978), DIC Spiegelhalter et al. (2002), RIC Leng (2007), WAIC Gelman et al. (2013). These are widely used in literature for their intrinsic simplicity: typically they consist in adding to the χ^2_{min} some algebraic factors which should resume all the complex information about the parameter space. From a theoretical point of view, only the BIC has some Bayesian justification, but makes simplifying assumptions that often do not hold. Thus, in general, they should not be considered as the ultimate tools but as "some among many" and should be used in a complementary way with others methods.
- There also exist some simple goodness of fit measures as for example defined in Ref. Raveri and Hu (2019). These include the trivial Gaussian tension (which quantifies the probability of agreement under the simple assumption of a Gaussian posterior), the difference of maximum likelihood points (a posteriori, DMAP Raveri and Hu (2019)) which computes $\sqrt{\chi^2_{\min,A+B} \chi^2_{\min,A} \chi^2_{\min,B}}$ for two experimental sets *A* and *B* (and naturally generalizes the Gaussian tension to non-Gaussian posteriors), and more complicated parameter difference measures such as the DM (first proposed in (Lin and Ishak, 2017b)) and UDM defined in Ref. Raveri and Hu (2019), which generalize the Gaussian tension to cases of non-Gaussian posteriors in a way that still relies on covariance matrices and means



Fig. 1. Posterior odds ratio for nested Gaussian models vs. \log_{10} (prior width/likelihood width), plotted against the "significance" of the tension (number of σ). We see that as a minimum, 3-4 σ tension is needed before the more complex model is favoured with odds of more than 20:1 (from Trotta, private comm.).

• Bayesian Evidence, Savage-Dickey ratio, Evidence ratio. These are firmly based on a principled Bayesian statistical approach which, for its intrinsic properties and philosophy seems to be the most appropriate for cosmological and astrophysical purposes. The relative posterior probabilities of competing models *M* and *M'*, given data **d** and model parameter sets θ and θ' is (see Ref. (Trotta, 2008) for more details)

$$\frac{p(M'|\mathbf{d})}{p(M|\mathbf{d})} = \frac{\pi(M')}{\pi(M)} \frac{\int d\theta' \, p(\mathbf{d}|\theta', M') \pi(\theta'|M')}{\int d\theta \, p(\mathbf{d}|\theta, M) \pi(\theta|M)}$$

where $\pi(M)$ is a model prior, and $\pi(\theta|M)$ the parameter prior. For equal model priors, this simplifies to the ratio of Bayesian Evidences, called the *Bayes Factor*, being the second ratio on the right hand side. It is this that is often interpreted on the Jeffreys Jeffreys (1939) or Kass-Raftery (Kass and Raftery, 1995) scale. Note. that the multi-dimensional integrals may be challenging to compute, but algorithms like (Skilling, 2006; Mukherjee et al., 2006) and tools such as multiNest (Feroz et al., 2019), PolyCHORD (Handley et al., 2015) and MCEvidence (Heavens et al., 2017b) exist, and for nested models, tricks such as the Savage-Dickey density ratio (Dickey and Lientz, 1970) may be employed.

By choosing a model that relieves the tensions, the maximum of the likelihood term for the joint experiment will increase, which will tend to increase the Evidence. However, if the parameter space is expanded, then the additional prior volume in parameter space counteracts this increase, and the simpler model may still be favoured, even if the maximum of the likelihood of the more complex models goes up. This encompasses to some degree Occam's razor. A drawback of this approach is that the Bayes factor is dependent on the parameter priors (Nesseris and Garcia-Bellido, 2013), even (unlike in parameter inference) in the limit of highly constraining data. Thus, there is some uncertainty unless we have a good physical reason to specify a particular prior. As a result one might want a more stringent condition than implied by the Jeffreys or Kass-Raftery scale before reaching strong conclusions in favour of one model or another, to reflect prior uncertainty. However, when Λ CDM is compared with models that involve introducing one or two extra parameters, it is a very effective approach (Martin et al., 2014; Heavens et al., 2017a), and the Bayes factor may be so large or small as to give conclusions that are robust to reasonable changes in the prior.

What comes out from studies of the Bayes factor is that tensions of *at least* 3 or 4σ are needed before a more complex model is favoured with reasonably high odds (say 20:1) (see Fig. 1), and it can be higher (Trotta, 2008). For example, Ref. (Heavens et al., 2017a) showed that the wCDM model (see Sec. 7.5.10) was favoured only by about 7:1 over Λ CDM with an apparently very significant 3.4 σ Hubble tension at the time (Riess et al., 2016). Using tail probabilities would give a far smaller and erroneous conclusion.

One limitation of the Bayesian Evidence approach is that if many extra parameters are added, the uncertainty in the added prior volume may become extremely large, and the Bayes factor may be highly uncertain, see e.g. Ref. (Lin and Ishak, 2017b). This has prompted the investigation of other techniques, such as the *Index of Inconsistency* (Lin and Ishak, 2017b,a), the *suspiciousness* (Handley and Lemos, 2019b; Lemos et al., 2020) and $\log \mathcal{I}$ statistic (Joudaki et al., 2017a, 2022), which are not dependent on the prior. Other measures have been considered by Refs. (Raveri and Hu, 2019; Seehars et al., 2014; Adhikari and Huterer, 2019; Kunz et al., 2006; Grandis et al., 2016b,a; Nicola et al., 2019).

• Likelihood distribution Koo et al. (2021a,b). This data-driven, frequentist, model validation technique that uses the method of the iterative smoothing of residuals. In other words, this method seeks to test whether the data is generated from a model, independent of how well other models fit the data. The basic procedure to validate a model on a given dataset is to start with the best-fit model to that dataset. Then the iterative smoothing method is applied to that best-fit model; that best-fit model serves as the initial guess for the iterative smoothing method. The iterative smoothing method works by, at each iteration, altering the current function such that the residuals are reduced, as in smoothed, thus improving the χ^2 of the current iterated function. The likelihood distribution then calculates how much over-fitting the iterative smoothing method will perform, i.e. if the data is generated from some fiducial parameters of some model, then how much improvement in the χ^2 is expected when the best-fit of the model is used as an initial guess of the iterated smoothing method. The distribution of the improvement from the iterative smoothing method over different realizations of the data is the likelihood distribution. If the improvement on the real data is outside of the likelihood distribution, then that model is invalidated, ruled out. If the improvement on the real data is within the likelihood distribution, then that model is validated.

In summary, there are many tools that have been proposed to quantify tensions, and these are used to indicate whether that new physics is needed. Quantitatively, the principled Bayesian approach is to use the Bayesian Evidence, which gives posterior odds on models, and this to some degree incorporates an element of Occam's razor. Arguably, this is the best approach when comparing models with one or two extra parameters over Λ CDM, but the prior-dependency of the Bayes factor may become a problem when many extra parameters are added and their prior is not easily constrained, as the Bayes factor may then be determined largely by the prior choice. There are many other instruments that may lack a principled basis, but do not suffer from this limitation. The use and interpretation of such instruments raises interesting questions, some of which are similar to the discussion of p-values elsewhere in science.² Are our instruments fit for purpose, and are they interpreted correctly? The alternative models considered almost always involve additional model complexity, (assuming we accept Occam's view) is not always clear. Another general concern is with the complexity of the data that we collect. Our data models are inevitably simplifications and do not capture all of the astrophysics that is relevant for the real Universe. The influence of such model mis-specification on our inference is one that is rarely explored, and requires further investigation in future, whatever the statistics used.

4. The H₀ tension

Coordinators: Simon Birrer, Adam Riess, Arman Shafieloo, and Licia Verde.

Contributors: Adriano Agnello, Eleonora Di Valentino, Celia Escamilla-Rivera, Valerio Marra, Michele Moresco, Raul Jimenez, Eoin Ó Colgáin, Tommaso Treu, Clécio R. Bom, Mikhail M. Ivanov, Leandros Perivolaropoulos, Oliver H.E. Philcox, Foteini Skara, John Blakeslee.

The 2018 legacy release from the *Planck* satellite Aghanim et al. (2020a) of the Cosmic Microwave Background (CMB) anisotropies, together with the latest Atacama Cosmology Telescope (ACT-DR4) Aiola et al. (2020) and South Pole Telescope (SPT-3G) Balkenhol et al. (2021) measurements, have provided a confirmation of the standard Λ CDM cosmological model. However, the improvement of the methods and the reduction of the uncertainties on the estimated cosmological parameters has seen the emergence of statistically significant tensions in the measurement of various quantities between the CMB data and late time cosmological model independent probes. While some proportion of these discrepancies may eventually be due to the systematic errors in the experiments, their magnitude and persistence across probes strongly hint at a possible failure in the standard cosmological scenario and the necessity for new physics.

The most statistically significant and long-standing tension is in the estimation of the *Hubble constant* H_0 between the CMB data, that are cosmological model dependent and are obtained assuming a vanilla Λ CDM model, and the direct local distance ladder measurements. The Hubble constant H_0 is the present expansion rate, defined as $H_0 = H(z=0)$ where $H(t) \equiv a^{-1} da/dt$ and $a^{-1} = 1 + z$.

In particular, we refer to the *Hubble tension* as the disagreement at 5.0σ between the *Planck* collaboration Aghanim et al. (2020b) value, $H_0 = (67.27 \pm 0.60) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% confidence level (CL), and the latest 2021 SHOES collaboration (R21 Riess et al. (2021b)) constraint, $H_0 = (73.04 \pm 1.04) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL, based on the Supernovae calibrated by Cepheids. However, there are not only these two values, but actually two sets of measurements, and all of the indirect model dependent estimates at early times agree between them, such as CMB and BAO experiments, and the same happens for all of the direct late time Λ CDM-independent measurements, such as distance ladders and strong lensing. We will see a collection of H_0 estimates in the next subsections, and a summary in the whisker plot of Fig. 2.

4.1. Late H₀ measurements

We consider as "Late H_0 measurements" those that are independent of the standard Λ CDM model. In general all of these measurements are in agreement with a higher value for the Hubble constant, and are in tension with the CMB estimate with a different statistical significance depending on the observable.

Here we find for example the best-established and empirical method of the "distance ladder", which allows one to measure H_0 locally, measuring the distance-redshift relation. In this case the geometry, e.g. the parallax, is used to calibrate the luminosities of specific star types which can be seen at great distances. Supernovae calibrated by Cepheids, as it has been done by the SH0ES collaboration, belong to this category. The latest SH0ES measurement gives $H_0 = (73.04 \pm 1.04) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Riess et al. (2021b), a 5 σ disagreement with the CMB one, while previous estimates include $H_0 = (73.2 \pm 1.3) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Riess et al. (2021a), improved with the latest parallax measurements provided by ESA Gaia mission Early Data Release 3 (EDR3) Brown et al. (2021), $H_0 = (73.48 \pm 1.66) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Riess et al. (2018a), and $H_0 = 73.24 \pm 1.74 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Riess et al. (2016). Finally, we have to consider also the final result of the Hubble Space Telescope Key Project, that was (72 ± 8) $\mathrm{km \, s^{-1} \, Mpc^{-1}}$ Freedman et al. (2001), or the result obtained using an improved geometric distance calibration to the Large Magellanic Cloud (LMC), i.e. (74.3 ± 2.1) $\mathrm{km \, s^{-1} \, Mpc^{-1}}$ Freedman et al. (2012).

There has been many independent works trying to re-analyze the SH0ES collaboration result in the last few years, using different formalisms, statistical methods or parts of the dataset, but there is no evidence for a drastic change of the value of the Hubble constant. We have for example the re-analysis of Ref. Cardona et al. (2017) using Bayesian hyper-parameters, i.e. $H_0 = (73.75 \pm 2.11) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL, or of Ref. Camarena and Marra (2021) using the cosmographic expansion of the luminosity distance, i.e. $H_0 = (74.30 \pm 1.45) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL (see Ref. Camarena and Marra (2021) for the H_0 - q_0 covariance) or the previous estimate Camarena and Marra (2020a). We have also the H_0 measurement obtained by Ref. Dhawan et al. (2018) using the measured near-infrared (NIR) Type Ia supernovae (SNIa), i.e. $H_0 = (72.8 \pm 1.6 \text{ (stat)} \pm 2.7 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL, or by Ref. Burns et al. (2018) using a different method for standardizing SNIa light curves, i.e. $H_0 = (73.2 \pm 2.3) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL. We have still the Hubble constant measured by Ref. Follin and Knox (2018) leaving the reddening laws in distant galaxies uninformed by the Milky Way,

² https://www.nature.com/articles/d41586-019-00874-8; https://www.nature.com/articles/d41586-019-00857-9.



Fig. 2. 68% CL constraint on H₀ from different cosmological probes (based on Refs. Di Valentino et al. (2021g); Perivolaropoulos and Skara (2021b)).

i.e. $H_0 = (73.3 \pm 1.7) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL, or by Ref. Feeney et al. (2018) using a Bayesian hierarchical model of the local distance ladder, i.e. $H_0 = (73.15 \pm 1.78) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL. Then we have the measurement based on the Cepheids from the second Gaia data release (GDR2), that is $H_0 = (73.0 \pm 1.9 \text{ (stat + sys)} \pm 1.9 \text{ (ZP)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Breuval et al. (2020), where ZP is the GDR2 parallax zero-point. Finally, there is the re-analysis of the Cepheid calibration used to infer the local value of the H_0 from SNIa, where one does not enforce a universal color-luminosity relation to correct the near-IR Cepheid magnitudes, which gives $H_0 = (71.8 \pm 1.76) \text{ km s}^{-1} \text{ Mpc}^{-1}$, or $H_0 = (66.9 \pm 2.5) \text{ km s}^{-1} \text{ Mpc}^{-1}$, at 68% CL depending on the approach Mortsell et al. (2021a), and $H_0 = (70.8 \pm 2.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL in Ref. Mortsell et al. (2021b).

At the same time, the impact of known and several previously neglected or unrecognized systematic effects on the center values of the SH0ES results has been constrained to be well below the 1% level (Anderson and Riess, 2018; Anderson, 2019; Riess et al., 2020; Javanmardi et al., 2021; Anderson, 2022). Interestingly, correcting reported H_0 values for such systematic effects can result in an increased value of H_0 (e.g., due to time dilation of observed variable star periods, cf. Ref. Anderson (2019)), and thus, to an increased significance of the discord between the distance ladder and the early Universe-based H_0 values.

An independent determination of H_0 is based on calibration of the Type Ia supernovae (SNIa) using the Tip of the Red Giant Branch, where one finds $H_0 = (71.17 \pm 1.66 \text{ (stat)} \pm 1.87 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Jang and Lee (2017), $H_0 = (69.8 \pm 0.8 \text{ (stat)} \pm 1.7 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Freedman et al. (2019), $H_0 = (72.4 \pm 2.0) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Yuan et al. (2019), and the final $H_0 = (69.6 \pm 0.8 \text{ (stat)} \pm 1.7 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Freedman et al. (2019), $H_0 = (72.4 \pm 2.0) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Yuan et al. (2019), and the final $H_0 = (69.6 \pm 0.8 \text{ (stat)} \pm 1.7 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Freedman et al. (2020). Then we have $H_0 = (71.1 \pm 1.9) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Reid et al. (2019), and the H_0 estimate using velocities and TRGB distances to 33 galaxies located between the Local Group and the Virgo cluster, $H_0 = (69.5 \pm 3.5 \text{ (stat)} \pm 2.4 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Kim et al. (2020). Moreover, it is important to mention the Freedman result $H_0 = (69.8 \pm 0.6 \text{ (stat)} \pm 1.6 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Freedman (2021), or the re-analysis of Ref. Anand et al. (2021) that gives $H_0 = (71.5 \pm 1.8) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL. Finally, there are the latest measurements $H_0 = (72.4 \pm 3.3) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL of Ref. Dhawan et al. (2022).

A larger value for H_0 is preferred also by the analysis of the near-infrared HST WFC3 observations of the Mira variable red giant stars in NGC 1559, that gives $H_0 = (73.3 \pm 4.0) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Huang et al. (2019b).

A measurement of the Hubble constant can be obtained with the Surface Brightness Fluctuations (SBF) method calibrated from Cepheids, with $H_0 = (71.9 \pm 7.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Cantiello et al. (2018) from a single galaxy (the host of GW170817) at 40 Mpc and $H_0 = (70.50 \pm 2.37 \text{ (stat)} \pm 3.38 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Khetan et al. (2021) from using SBF as an intermediate rung between Cepheids and SNIa. A re-analysis of the latter performed by Ref. Blakeslee et al. (2021), improving the LMC distance, gives instead $H_0 = (71.1 \pm 2.4(\text{stat}) \pm 3.4(\text{sys})) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL. Moreover, if SBF is used as another long-range indicator calibrated by Cepheids and TRGB, Ref. Blakeslee et al. (2021) finds $H_0 = (73.3 \pm 0.7 \text{ (stat)} \pm 2.4 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL from a new sample of HST NIR data for 63 galaxies out to 100 Mpc.

Another possible observable to constrain H_0 is given by the Standardized Type II supernovae. Using 7 SNe II with host-galaxy distances measured from Cepheid variables or the TRGB, the Hubble constant is equal to $H_0 = 75.8^{+5.2}_{-4.9} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL de Jaeger et al. (2020), while with 13 SNe II Ref. de Jaeger et al. (2022) finds $H_0 = 75.4^{+3.8}_{-3.7} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL. An important independent result was obtained with the Megamaser Cosmology Project, which gives an H_0 estimate by using the

An important independent result was obtained with the Megamaser Cosmology Project, which gives an H_0 estimate by using the geometric distance measurements to megamaser-hosting galaxies, finding $H_0 = (66.6 \pm 6.0) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Gao et al. (2016), and $H_0 = (73.9 \pm 3.0) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Pesce et al. (2020), independent of distance ladders.

In addition, there are the estimates of the Hubble constant based on the Tully-Fisher Relation, i.e. the correlation between the rotation rate of spirals and their absolute luminosity used to measure the galaxy distances. Using optical and infrared calibrated Tully-Fisher Relations, the Hubble constant is equal to $H_0 = (76.0 \pm 1.1 \text{ (stat)} \pm 2.3 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Kourkchi et al. (2020). Considering the baryonic Tully-Fisher relation (bTFR) as a new distance indicator, instead, the Hubble constant is found to be $H_0 = (75.1 \pm 2.3 \text{ (stat)} \pm 1.5 \text{ (sys)}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Kourkchi et al. (2022).

An estimate of H_0 can also be obtained by modelling the extragalactic background light and its role in attenuating γ -rays, but this is challenging and the uncertainties may be underestimated. In this case there is Ref. Domínguez and Prada (2013) that finds $H_0 = 71.8^{+4.6}_{-5.6}(\text{stat})^{+7.2}_{-13.8}(\text{sys}) \,\text{km s}^{-1}\,\text{Mpc}^{-1}$ at 68% CL, the updated value $H_0 = 67.4^{+6.0}_{-6.2} \,\text{km s}^{-1}\,\text{Mpc}^{-1}$ at 68% CL Domínguez et al. (2019), and $H_0 = 64.9^{+4.6}_{-4.3} \,\text{km s}^{-1}\,\text{Mpc}^{-1}$ at 68% CL Zeng and Yan (2019).

The HII galaxy measurement can also act as a good distance indicator independent of SNIa to probe the background evolution of the Universe. Using 156 HII galaxy measurements, we obtain the constraint $H_0 = 76.12^{+3.47}_{-3.44} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Wang and Meng (2017a), which is more consistent with the H_0 value from the SH0ES Team than that from the *Planck* collaboration (see also Fernández Arenas et al. (2018)).

Moreover, we have the strong lensing time delays estimates, that are not Λ CDM model dependent but still astrophysical model dependent, because of the imperfect knowledge of the foreground and lens mass distributions. Here we have the H0LiCOW inferred values $H_0 = 71.9^{+2.4}_{-3.0} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL in 2016 Bonvin et al. (2017), $H_0 = 72.5^{+2.1}_{-2.3} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL in 2018 Birrer et al. (2019), and $H_0 = 73.3^{+1.7}_{-1.8} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL in 2019 Wong et al. (2020),³ based on strong gravitational lensing effects on quasar systems under standard assumptions on the radial mass density profile of the lensing galaxies. A reanalysis of H0LiCOW's four lenses is performed in Ref. Yang et al. (2020b) finding $H_0 = 73.65^{+1.95}_{-2.26} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL. Under the same assumptions, the STRIDES collaboration measures from the strong lens system DES J0408-5354 $H_0 = 74.2^{+2.7}_{-3.0} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Millon et al. (2020). Relaxing the assumptions on the mass density profile for the same sample of lenses, the TDCOSMO collaboration obtains $H_0 = 74.5^{+5.6}_{-6.1} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Birrer et al. (2020), and $H_0 = 67.4^{+3.2}_{-3.2} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Birrer et al. (2020), and $H_0 = 67.4^{+3.2}_{-3.2} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Birrer et al. (2020), and $H_0 = 67.4^{+3.2}_{-3.2} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Birrer et al. (2020), and $H_0 = 67.4^{+3.2}_{-3.2} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Birrer et al. (2020), and $H_0 = 67.4^{+3.2}_{-3.2} \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Birrer et al. (2020), by combining the time-delay lenses with non time-delay lenses from SLACS (Bolton et al., 2008), assuming they are drawn from the same parent sample.

An independent determination of H_0 has been obtained from strongly lensed quasar systems from the HOLiCOW program and Pantheon SNIa compilation using Gaussian process regression. This gives $H_0 = 72.2 \pm 2.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Liao et al. (2019), or the updated result $H_0 = 72.8^{+1.6}_{-1.7} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL using six lenses of the HOLiCOW dataset Liao et al. (2020). Moreover, Ref. Qi et al. (2021) finds $H_0 = 73.6^{+1.8}_{-1.6} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL, taking the derived products of HOLiCOW, and another time-delay strong lensing measurement has been obtained analysing 8 strong lensing systems in Denzel et al. (2021) giving $H_0 = 71.8^{+3.9}_{-3.3} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL.

Finally, a promising probe is the angular diameter distance measurements from galaxy clusters. Using the sample consisting of 25 data

points, Ref. Wang and Meng (2017b) finds $H_0 = (70.1 \pm 0.8) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL, or using another sample containing 38 data points

³ Ref. Wong et al. (2020) and the follow-up paper Millon et al. (2020) find a descending trend of H_0 with lens redshift. This can be interpreted as an expected signature of a late-time resolution to H_0 tension in line with the explanation given in Ref. Krishnan et al. (2021a) (see also Ref. Krishnan et al. (2020); Dainotti et al. (2021a)). Alternatively, switching to orientation on the sky, one can interpret it as a signature of an emergent dipole in H_0 Krishnan et al. (2021b).

 $H_0 = (74.6 \pm 2.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL. This measurement is very sensitive to the temperature calibration and a more conservative analysis gives $H_0 = 67.3^{+21.3}_{-13.3} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL, where errors are dominated by uncertainties of the temperature calibration Wan et al. (2021), and $H_0 = 72.2^{+6.7}_{-6.7} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Mantz et al. (2021).

When the late Universe estimates are averaged in different combinations, these H_0 values disagree between 4.5 σ and 6.3 σ with those from *Planck* Riess (2019); Verde et al. (2019); Di Valentino (2021).

4.2. Cosmological H_0 inferences from modelled galaxy ageing and BAO

In recent years, we have witnessed an increased use of reconstructions of cosmological parameters directly from data. While Gaussian Process (GP) regression Holsclaw et al. (2010a,b); Shafieloo et al. (2012); Seikel et al. (2012) is the most commonly used technique, there are a host of other approaches Crittenden et al. (2009, 2012), including most recently the use of machine learning algorithms Arjona and Nesseris (2020a,b); Mehrabi and Rezaei (2021). The upshot of these reconstruction approaches is evident: one can reconstruct the Hubble parameter H(z) directly from cosmological data without assuming a cosmological model, at least in the traditional sense. Moreover, in the context of the Hubble constant H_0 , one can determine H_0 by simply extrapolating H(z) to z = 0. These approaches are commonly labelled "model independent" or "non-parametric", since they do not make use of a traditional "parametric" cosmological model, such as Λ CDM, wCDM, and so on.⁴

One can construct H(z) directly using Cosmic Chronometers (CC) data Jimenez and Loeb (2002); Moresco et al. (2012); Moresco (2015); Moresco et al. (2016, 2022), before extrapolating to z = 0, as explained above.⁵ The advantage of the cosmic chronometer method is that it infers H(z) directly from the differential age evolution of the most massive and passively evolving galaxies, selected to minimize any possible contamination by star-forming objects. A current comprehensive review on this cosmological probe is provided in Ref. Moresco et al. (2022), and a summary discussed in Sect. 6.4. Current datasets constrain H_0 to $67.8^{+8.7}_{-7.2}$ and 66.5 ± 5.4 km s⁻¹ Mpc⁻¹, respectively for a generic open wCDM and for a flat Λ CDM cosmology Moresco et al. (2022). Moreover, CC observations are also ideal to derive H_0 from GP extrapolations, since not only is GP model agnostic, at least subject to some caveats, but the CC method itself is fully cosmological model independent.

Using 30 CC data points, the Hubble constant is constrained to $H_0 = (67.38 \pm 4.72) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Wang and Meng (2017c). Analysing 31 H(z) data measured by the cosmic chronometers technique and 5 H(z) data by BAO observations, the Hubble constant is equal to $H_0 = (67 \pm 4) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Yu et al. (2018). Given recent criticism Kjerrgren and Mortsell (2021), some caveat has to be taken when considering the preliminary analysis obtained with CC, while the treatment of both statistical and systematic errors have been fully studied and taken into account in subsequent analyses Moresco et al. (2018, 2020); Borghi et al. (2021) However, at $H_0 \sim (67 \pm 4) \text{ km s}^{-1} \text{ Mpc}^{-1}$, any discrepancy with the SH0ES determination Riess et al. (2021a) is negligible, despite (systematic) errors being possibly underestimated.

An interesting extension of this analysis, including the SNIa data from the Pantheon compilation and the Hubble Space Telescope (HST) CANDELS and CLASH Multy-Cycle Treasury (MCT) programs, gives instead $H_0 = (67.06 \pm 1.68) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Gómez-Valent and Amendola (2018), and $H_0 = (68.90 \pm 1.96) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ when use is made of the Weighted Polynomial Regression technique Gómez-Valent and Amendola (2018). Observe that the inclusion of SNIa has dramatically reduced the errors and the discrepancy with the SH0ES result Riess et al. (2021a) becomes 2.9σ and 1.8σ , respectively. A novel feature of this analysis is that since SNIa require a calibrator to determine H_0 , CC data are being used to calibrate SNIa in an iterative procedure Gómez-Valent and Amendola (2018). That being said, a discrepancy of 2.9σ between two *a priori* "model independent" H_0 determinations, one local ($z \ll 1$) and one making use of GP, is an obvious problem if one neglects i) the tendency of GP to underestimate errors and ii) CC data may not have properly propagated some systematic uncertainties.

Through an extension of the standard GP formalism, and utilising joint low-redshift expansion rate data from SNIa, BAO and CC data, the Hubble constant is found to be $H_0 = 68.52^{+0.94+2.51}_{-0.94}$ km s⁻¹ Mpc⁻¹ at 68% CL Haridasu et al. (2018), in full agreement with Gómez-Valent and Amendola (2018). This marks another interesting result, since an effort has been made to better account for systematic uncertainties, which improves on earlier results. Observe that the inclusion of systematic uncertainties reduces another alarming "model independent" 2.9 σ discrepancy with SH0ES to a much more manageable 1.6 σ . This underscores the importance of systematic uncertainties, especially in the context of CC data as currently addressed in Ref. Moresco et al. (2020). Making use of the same combination of data, i.e. SNIa+BAO+CC, while relying only on few seminal assumptions at the basis of the distance duality relation and using a combination of uncalibrated geometrical data, the authors of Ref. Renzi and Silvestri (2020) find $H_0 = (69.5 \pm 1.7)$ km s⁻¹ Mpc⁻¹, showing the possibility of measuring H_0 at the percentage level without assuming a cosmological model. This determination, being midway between SH0ES and *Planck* is consistent with both. Whereas current data do not allow for a complete resolution of the Hubble tension, this method hints at a twofold reconciliation for the values of H_0 from SH0ES, TRGB Freedman et al. (2019, 2020) and *Planck* Aghanim et al. (2020b). An adjustment in the calibration of the SNIa, i.e. setting $M_B = -19.355 \pm 0.054$, 2.5 σ lower than SH0ES calibration, bring ing local measurements in agreement; and a mild deviation from Λ CDM in the expansion history at intermediate redshift to bring the latter in agreement with the early time measurement of *Planck*.

Interestingly, the H_0 inferences from GP are not restricted below $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. In particular, one can remove SNIa and replace standard BAO with a combination of transversal BAO scale θ_{BAO} , with BBN and CC, to arrive at the value $H_0 = 72.1^{+1.2}_{-1.3} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Nunes and Bernui (2020), which remarkably is completely consistent with the latest SH0ES determination.

⁴ There are some caveats to the "model independent" moniker. One fairly obvious caveat is that reconstructions typically assume correlations, which can lead to interesting results e.g. suggestive wiggles in parameters Zhao et al. (2017); Wang et al. (2018a), but may not be tracking effective field theories Colgáin et al. (2021). See Ref. Pogosian et al. (2021); Raveri et al. (2021) for the pronounced difference a theory prior can make. A secondary concern with GP is that the results depend on the assumed covariance matrix and there may be a tendency to underestimate errors Colgáin and Sheikh-Jabbari (2021a) (see also Ref. Dhawan et al. (2021)).

⁵ The novelty and added value of the CC with respect to other cosmological probes is that it can provide a direct estimate of the Hubble parameter without any cosmological assumption (beyond that of an FLRW metric). From this point of view, the strength of this method is its (cosmological) model independence: no assumption is made about the functional form of the expansion history or about spatial geometry; it only assumes homogeneity and isotropy, and a metric theory of gravity. Constraints obtained with this method, therefore, can be used to constrain a plethora of cosmological models Jimenez et al. (2019b).

Finally, a combined analysis of SNIa, CC, BAO, and HOLiCOW lenses gives $H_0 = (73.78 \pm 0.84) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Bonilla et al. (2021a). Once again, this estimation is in agreement with SH0ES and HOLiCOW collaborations within 68% CL. This may not be so surprising given that HOLiCOW Wong et al. (2020) prefers a value for the Hubble constant $H_0 \sim 73 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$, but observe that all data are still cosmological in nature.

Clearly, GP regression reconstructions of H(z), and by extrapolation H_0 , can lead to different results. In particular, the central values range from $H_0 \sim 67 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ Gómez-Valent and Amendola (2018), consistent with *Planck* Aghanim et al. (2020b), all the way to $H_0 \sim 74 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$, consistent with SH0ES Riess et al. (2021a). Of course, the final outcome depends on the data, but it is worth emphasising that all the observational data are purely cosmological in nature, so the determinations are independent of the local ($z \ll 1$) determinations outlined in Sec. 4.1. For this reason, comparison is meaningful. Throughout CC data is playing a special role in calibrating SNIa and BAO, so it is imperative to unlock the potential in CC by fully accounting for systematic uncertainties and adding new data points. In particular, it will be fundamental to improve and validate galaxy stellar population modelling - which currently represents the main source of systematic uncertainty Moresco et al. (2020) - and to increase the CC statistics with upcoming galaxy spectroscopic surveys. With these improvements, one distinct possibility is that data reconstructions may converge to a *Planck* value Gómez-Valent and Amendola (2018); Haridasu et al. (2018). If they do, given the model independent setup, then either higher $H_0 > 70 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ local determinations are wrong, the cosmological data are wrong, or the Universe is not FLRW, see Sec. 7.8 and Sec. 8.6.

4.3. Gravitational waves standard sirens

It is possible to have Hubble constant measurements from the GW standard sirens: modelling early data on the GRB170817 jet Ref. Guidorzi et al. (2017) gives $H_0 = 74^{+11.5}_{-7.5} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL; late-time GRB170817 jet superluminal motion gives $H_0 = 70.3^{+5.3}_{-5.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Hotokezaka et al. (2019); from the dark siren GW170814 BBH merger Ref. Soares-Santos et al. (2019) finds $H_0 = 75^{+40}_{-32} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL; from GW170817 and 4BBH from O1 and O2 one obtains $H_0 = 68^{+14}_{-7} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Abbott et al. (2019a); finally, from GW190814 and GW170817 one finds $H_0 = 70^{+17}_{-8} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Abbott et al. (2020a). The most recent result on this observable reported by the LIGO-Virgo-KAGRA Collaboration yields $H_0 = 68^{+12}_{-7} \text{ km s}^{-1} \text{ Mpc}^{-1}$ Abbott et al. (2021d). This was obtained using a method that constrains the source population properties of BBHs without galaxy catalogue, but still combines with GW170817 Bright Siren (without GW170817 the result is $H_0 = 50^{+37}_{-3.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$). Other recent dark siren results from Ref. Palmese et al. (2021), using only catalogues from Legacy Survey and no galaxy weighting, presents the value $H_0 = 72.77^{+11.0}_{-7.55} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL from Ref. Mukherjee et al. (2022) cross-correlating dark-sirens and galaxies.

We will discuss the expected improvement in the future using GW in Sec. 9.1.7.

4.4. Early H₀ measurements

We consider as "Early H_0 measurements" those based on the accuracy of a number of assumptions, such as the model used to describe the evolution of the Universe, i.e. the standard Λ CDM scenario, the properties of neutrinos or the Dark Energy (a cosmological constant), the inflationary epoch and its predictions, the number of relativistic particles, the Dark Matter properties, etc. For this reason the Hubble constant tension can be the indication of a failure of the assumed vanilla Λ CDM scenario, particularly the form it takes in the pre-recombination Universe. In general all of these measurements are in agreement with a lower value for the Hubble constant.

As we can see in Fig. 2, there are a variety of CMB probes preferring smaller values of H_0 . For example, we can see the satellite experiments, such as the Wilkinson Microwave Anisotropy Probe (WMAP9) Hinshaw et al. (2013) that assumes the Λ CDM model, gives a value for the Hubble constant $H_0 = (70.0 \pm 2.2) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL in its nine-year data release. Moreover, the *Planck* 2018 release Aghanim et al. (2020b) predicts $H_0 = (67.27 \pm 0.60) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL or in combination with the CMB lensing Aghanim et al. (2020b), i.e. the four-point correlation function or trispectrum analysis, that estimates $H_0 = (67.36 \pm 0.54) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL. However, in perfect agreement there are the ground based telescopes, such as the ACT-DR4 estimate $H_0 = (67.9 \pm 1.5) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Aiola et al. (2020). Alternatively, SPT-3G Dutcher et al. (2021) returns the value of $H_0 = (68.8 \pm 1.5) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL. Aiola et al. (2020).

Yet, also on the low side, we have combinations of complementary probes, such as Baryon Acoustic Oscillation (BAO) data Beutler et al. (2011); Ross et al. (2015); Alam et al. (2017), Big Bang Nucleosynthesis (BBN) measurements of the primordial deuterium Cooke et al. (2018), weak lensing and cosmic shear measurements from the Dark Energy Survey Abbott et al. (2022). For example, the final combination of the BAO measurements from galaxies, quasars, and Lyman- α forest (Ly- α) from BOSS and eBOSS prefers $H_0 = (67.35 \pm 0.97) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL for inverse distance ladder analysis involving a BBN prior on the physical density of the baryons $\Omega_b h^2$ Alam et al. (2021a).

Galaxy power spectra can be used to constrain indirectly the Hubble parameter, via the indirect effect of *h* on the shape of the matter transfer function, in principle without requiring a calibration of the sound-horizon from the CMB as in inverse-distance-ladder approaches (see Sec. 6.2), but using effectively the matter radiation equality horizon calibrated from the CMB, and thus using a different but closely related inverse-distance-ladder approach. A reanalysis of the Baryon Oscillation Spectroscopic Survey (BOSS) data on the full-shape (FS) of the anisotropic galaxy power spectrum gives $H_0 = (67.9 \pm 1.1) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Ivanov et al. (2020c) when the BBN prior on $\Omega_b h^2$ is used, whereas a similar analysis with the baryon-to-dark matter density ratio Ω_b / Ω_{DM} fixed to the *Planck* baseline Λ CDM best-fit value gives $H_0 = (68.5 \pm 2.2) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL D'Amico et al. (2020). Adding the post-reconstructed BAO signal to the FS + BBN data gives $H_0 = (68.6 \pm 1.1) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Philcox et al. (2021) (fixing the spectral slope n_s). This measurement was recently updated by adding the information from the power spectrum of the eBOSS emission line galaxies Ivanov (2021) and the BOSS DR12 bispectrum Ivanov et al. (2021b,a); Philcox and Ivanov (2022), yielding $H_0 = (68.6 \pm 1.1) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ and $H_0 = (68.3 \pm 0.85) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$, respectively. Similar results were obtained by other groups, in particular $H_0 = (69.2 \pm 0.8) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ using the galaxy correlation function, BBN priors and BAO measurements from BOSS and eBOSS (Zhang et al., 2022). By analyzing the BOSS DR12 full-shape data combined

with a prior on Ω_m from the Pantheon Supernovae, $H_0 = (69.5^{+3.0}_{-3.5}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ is found at 68% CL Philcox et al. (2021b); Farren et al. (2021).

These measurements work within the Λ CDM model and Standard Model for the early Universe, to set the power spectrum, with pros and cons as discussed in Brieden et al. (2021a,b) where it is shown that without assuming standard early time physics and a Λ CDM model the H_0 constraint likely gets significantly weakened. If the common fitting formulae of Eisensten & Hu (1998) are used, as done e.g. for the 6dFGS (section 5.2 of Beutler et al., 2011), only a limited range for the sound horizon is allowed. Therefore, the choice of Λ CDM+SM already sets the range of possible H_0 values to $H_0 = (67.5 \pm 2.5) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ even when purely angular measurements of H_0r_d from BAO are used. A reappraisal of the BAO measurement of H_0 with different constraints on $\Omega_m h^2$ yielded $H_0 = (69 \pm 2) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ (BAO +SN +DES +CMBlensing), without constraints on $\Omega_b h^2$ from BBN, with a difference of $\approx 2.5 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ between measurements using CMB lensing power spectra from SPTPol or *Planck* Pogosian et al. (2020). Statistically consistent, albeit more uncertain results can also be obtained from CMB lensing alone, $H_0 = (73.5 \pm 5.3) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ (BAC and BBN and obtained $H_0 = (67.2^{+1.2}_{-1.0}) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL Abbott et al. (2018a). This measurement was carried out within Λ CDM+SM ($N_{\rm eff}$ fixed to ≈ 3.05) and used the 6dFGS BAO inference, and so it indirectly anchored H_0 . It also adopted a compromise BBN estimate so that it would not be in immediate tension with Planck, which however would require a model with free $N_{\rm eff} \approx 3.4$ Cooke et al. (2018).

4.5. Supernovae absolute magnitude

In many of the papers discussing the extended cosmology resolution to the Hubble tension, the distance ladder measurements of H_0 are incorporated into the analysis as a Gaussian likelihood. Recently several works Camarena and Marra (2020a); Benevento et al. (2020); Camarena and Marra (2021); Efstathiou (2021); Greene and Cyr-Racine (2021); Cai et al. (2022a); Benisty et al. (2022) warned against this practice due to possible caveat on extremely late Universe transitional models. The reason is that local late Universe measurements of H_0 depend on observations of astrophysical objects that extend into the Hubble flow, for example the SH0ES Riess et al. (2016) results that have been most frequently quoted uses Pantheon supernovae sample in the redshift range 0.023 < z < 0.15. Hence the distance ladder H_0 actually calibrates the absolute magnitude of the supernovae sample that includes higher redshifts objects. If a model predicts a higher Hubble constant to be achieved by extremely late transitional effect at z < 0.02, like the example of red curve in Fig. 1 of Ref. Benevento et al. (2020) or the hockey-stick dark energy of Ref. Camarena and Marra (2021), it is not actually resolving the Hubble tension. Ref. Raveri et al. (2020); Camarena and Marra (2020a) give the simplest method to correctly combine the distance ladder measurement of H_0 :

$$\mathcal{L} = \mathcal{L}_{\rm SN} \times \mathcal{N}(M, \bar{M}(H_0), \sigma_M^2(\sigma_{H_0})), \tag{1}$$

i.e. to include the distance ladder H_0 measurement as the supernovae absolute magnitude prior. It is possible to marginalize analytically Eq. (1), similarly to the analytical marginalization that is performed when a flat prior on M is assumed, see Section 4.6 of Ref. Camarena and Marra (2021) for details.

This detail should be especially taken care of for extended cosmological models which deviate from Λ CDM phenomenology at late time (i.e. at low redshift). However, note that the consequence is not as severe as implied by Ref. Efstathiou (2021) if the transition is not restrained to z < 0.02. The main point of the discussion above is that the H_0 measured at late time is not exactly the value at z = 0, thus should be related to the supernovae absolute magnitude calibration at the same range of low redshifts. This means models that hide all the new physics at such low redshifts, which are irrelevant to the $0.02 \leq z \leq 0.2$ Hubble flow measurements, are naturally off the mark. For example, consider the red curve in Fig. 1 of Ref. Benevento et al. (2020). If a model has no drastic jump in the Hubble constant at z < 0.02, but a gradual change throughout several redshifts, the low redshift Hubble measurement $z \sim O(0.1)$ could still be a reasonable anchor of current time H_0 , and should be equivalent to Eq. (1).

Besides the previous reasons, Eq. (1) is recommended for any future analysis using distance ladder H_0 combined with supernovae samples because it avoids adopting an unnecessary cosmographic expansion: when performing cosmological inference one should use the luminosity distance of the cosmological model that is being tested. Furthermore, Eq. (1) avoids double counting low-redshift supernovae belonging to the sample that was used to perform cosmography in order to obtain the H_0 constraint.⁶ Recently, the SH0ES and Pantheon+ teams have released the SH0ES Cepheid host-distance likelihood,⁷ which allows for the optimal inclusion of the local calibration of the supernova absolute magnitude in the cosmological analysis of a given theoretical model.

4.6. Distance ladder systematics

For the sake of completeness, this subsection summarizes the outstanding sources of uncertainties in the SNIa distance ladder. The determination of the local Hubble constant is affected by the large-scale structure around us. Considering a spherical inhomogeneity, one expects that an adiabatic perturbation in density causes a perturbation in the expansion rate given by:

$$\frac{\delta H_0}{H_0} = -\frac{1}{3} f(\Omega_m) \frac{\delta \rho(t_0)}{\rho(t_0)},\tag{2}$$

where $f \simeq 0.5$ is the present-day growth function for the concordance Λ CDM model. Fig. 3 shows the expectation for the standard model: the effect of the local structure quickly decreases by considering larger scales. This is the motivation for placing a limiting lower redshift when fitting the supernova data in order to obtain H_0 . The SH0ES collaboration adopts 0.023 < z < 0.15 (Riess et al., 2020), for which estimates based on theoretical computations (see Ref. Camarena and Marra (2018) and references therein) and numerical simulations (see Ref. Odderskov et al. (2017) and references therein) suggest that cosmic variance on H_0 amounts at 0.5–1%. It is worth remarking that the

⁶ The up-to-date prior on *M* is maintained at https://github.com/valerio-marra/CalPriorSNIa and has been implemented in Monte Python 3.5.

⁷ https://pantheonplussh0es.github.io.



Fig. 3. 1, 2 and 3 times the standard deviation $\left\langle \delta_{H}^{2} \right\rangle_{R}^{1/2}$ as a function of redshift *z* and scale *R*(*z*). The dashed line marks the redshift *z* = 0.023. The Hubble constant is estimated by SH0ES in the redshift range 0.023 < *z* < 0.15. Plot from Ref. (Camarena and Marra, 2018).

SH0ES collaboration tries to correct for this systematic effect by correcting the velocity field via local cosmic flow maps. TRGB estimates adopt instead the redshift range 0.004 < z < 0.083 (Freedman, 2021). In this case one expects a larger cosmic variance of about 2%.

Finally, one residual contribution to systematic uncertainties, in determining both r_s and H_0 is the uncertainty in the product H_0r_s from the combination of BAO and Supernovae in the "cosmological" redshift range. Recently, the Pantheon collaboration has re-analyzed the calibration used for the photometry of the SNIa sample, including the calibration used to obtain the SH0ES results Brout et al. (2021); Scolnic et al. (2021). The contribution to the Hubble constant from the systematic SN calibration is smaller than ~ 0.2 km s⁻¹ Mpc⁻¹, so that the tension cannot be attributed to this type of systematics.

5. The S₈ tension

Coordinators: Marika Asgari, Hendrik Hildebrandt, and Shahab Joudaki.

Contributors: Erminia Calabrese, Eleonora Di Valentino, Dominique Eckert, Mustapha Ishak, Mikhail M. Ivanov, Leandros Perivolaropoulos, Oliver H.E. Philcox, Foteini Skara.

Recent observations of probes of the large-scale structure have allowed us to constrain the strength with which matter is clustered in the Universe. These constraints on the strength of matter clustering differ from that inferred by probes of the early Universe. In particular, the primary anisotropies of the cosmic microwave background (CMB) as measured by the *Planck* satellite exhibit a tension in the matter clustering strength at the level of $2 - 3\sigma$ when compared to lower redshift probes such as weak gravitational lensing and galaxy clustering (e.g. Asgari et al. (2020, 2021); Joudaki et al. (2020); Abbott et al. (2022); Amon et al. (2022); Secco et al. (2022); Loureiro et al. (2021); Joudaki et al. (2017b); Heymans et al. (2021); Hildebrandt et al. (2020); Abbott et al. (2020b); Macaulay et al. (2013); Skara and Perivolaropoulos (2020); Kazantzidis and Perivolaropoulos (2019); Joudaki et al. (2017a); Bull et al. (2016); Kazantzidis and Perivolaropoulos (2018); Nesseris et al. (2017); Philcox and Ivanov (2022)).

This tension is often quantified using the $S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3}$ parameter, which modulates the amplitude of the weak lensing measurements. The S_8 parameter is closely related to $f\sigma_8(z=0)$ measured by redshift space distortions (RSD) Li et al. (2016); Gil-Marín et al. (2017), where $f = [\Omega_m(z)]^{0.55}$ approximates the growth rate in GR as a function of the matter density parameter, $\Omega_m(z)$, at redshift *z*. The lower redshift probes, as seen in Fig. 4, generally prefer a lower value of S_8 compared to the high redshift CMB estimates. Measuring S_8 is model dependent and in all cases here the underlying model is the standard flat Λ CDM model. This model provides a good fit to the data from all probes, but predicts a lower level of structure formation compared to what is expected from the CMB observations.

The high redshift data from *Planck* TT,TE,EE+lowE finds $S_8 = 0.834 \pm 0.016$. Combining this data with secondary CMB anisotropies, in the form of CMB lensing, serves to tighten the constraint to $S_8 = 0.832 \pm 0.013$. Constraints from CMB lensing alone are fully consistent with both high and other low redshift measurements as seen in Fig. 4. Combining the high- ℓ data from ACT with the low- ℓ measurements of WMAP yields larger errors on $S_8 = 0.840 \pm 0.030$ Aiola et al. (2020), but is consistent with the *Planck* results. In the following sections, we briefly describe the analyses and data used in Fig. 4 and moreover discuss the possible systematic effects associated with each probe.

In reporting parameter estimates and constraints, we note that there might be differences in the choices that enter each analysis. For instance, a statistical property of the S_8 marginal distribution might be chosen, such as its mean or mode together with the asymmetric 68% region around them or the standard deviation of the sampled points. By contrast, in some analyses, the statistics relevant to the full posterior distribution have been adopted, such as the maximum a posteriori point or the best fitting values and their associated errors. These choices can impact the estimated values of the parameters, in particular when the posterior distributions are significantly non-Gaussian or when the parameter estimates are prior dominated (see e.g. Ref. Joachimi et al. (2021a)). For simplicity, we will use the nominal values reported in each analysis, but caution the reader that the methodology used may differ from case to case (see Sec. 3 for a more detailed discussion).

5.1. Weak gravitational lensing

The images of distant galaxies are gravitationally lensed by the intervening matter. On cosmological scales we use this effect to analyse and understand the large scale structures (LSS) in the Universe. The gravitational lensing effect of the LSS only slightly distorts the shapes of these galaxies (weak lensing). The two main strands of weak lensing that we focus on in this section are cosmic shear, the study of correlations between the shapes of pairs of galaxies, and galaxy-galaxy lensing, the study of the correlation between the position of



Fig. 4. Constraints on S_8 and its corresponding 68% error (updated from Ref. Perivolaropoulos and Skara (2021b)). We show the nominal reported values by each study, which may differ in their definition of the constraints. The definition $S_8 = \sigma_8 (\Omega_m/0.3)^{\alpha}$ with $\alpha = 1/2$ has been uniformly used for all points. In those cases where $\alpha \neq 1/2$ has been used in some references, the value of S_8 with $\alpha = 1/2$ was recalculated (along with the uncertainties) using the constraints on σ_8 and Ω_m shown in those references, assuming their errors are Gaussian. This concerns only 5 CC points where the published value of α was different from 1/2 and the difference from the published S_8 (with different α) is very small. The rest of the points are taken directly from the published values.

foreground galaxies and background galaxy shapes. In addition, galaxy cluster abundance measurements (cluster counts, CC) also utilise gravitational lensing to estimate cluster masses. This will be covered in Sec. 5.5.

Using cosmic shear we can probe the LSS more directly compared to galaxy-galaxy lensing, where we need to make assumptions about the connection between galaxies and the underlying matter distribution. In addition, cosmic shear studies provide tighter constraints on S_8 and can be used as an independent probe. In Sec. 5.4, we discuss analyses that use galaxy-galaxy lensing in combination with other probes of the large scale structure, as they do not currently provide independent competitive constraints on cosmological parameters.

The tension in S_8 between weak gravitational lensing data and *Planck* CMB measurements was first seen when the cosmic shear analysis of CFHTLenS (Canada France Hawaii Lensing Survey, Heymans et al., 2013) was compared to the first *Planck* data release (Ade et al., 2014a). Back then, the tension was still mild at the level of ~ 2σ . Subsequent analysis of the CFHTLenS data with improved methodology Joudaki et al. (2017a) validated these initial observations. This mild tension motivated the weak lensing community to obscure their data by blinding the team to the constraints on cosmological parameters and only unblinding once the analysis has been finalized. The first blinded analysis of this kind was performed by the Kilo Degree Survey on their first 450 square degrees of data (KiDS-450: Kuijken et al., 2015; Fenech Conti et al., 2017; Hildebrandt et al., 2017), which found a 2.3 σ lower value of S_8 compared to the

Planck 2015 constraints Aghanim et al. (2016a). Cosmic shear analysis has seen significant improvements in the recent years and therefore we limit ourselves to results published in the last 5 years (since 2017).

All published results in the last 5 years have found S_8 values that are lower than the early Universe estimates. The first year data from the Dark Energy Survey (DES-Y1, Troxel et al., 2018a) and Hyper Suprime Cam (HSC Hikage et al., 2019; Hamana et al., 2020) found slightly higher but consistent values with the KiDS-450 results. Subsequent analysis of KiDS included photometric data from VIKING which reduced the redshift errors and outlier fractions. The analyses of KiDS-450 + VIKING (KV450, Hildebrandt et al., 2020; Wright et al., 2020b) found consistently low S_8 results. The combination of DES-Y1 and KV450 data were analysed in Refs. Joudaki et al. (2020); Asgari et al. (2020), finding tighter constraints in agreement with previous results. The latest cosmic shear analysis of KiDS (KiDS-1000, Asgari et al., 2021) and DES (DES-Y3, Amon et al., 2022; Secco et al., 2022) show the same trend with better precision. Comparing their S_8 values with the fiducial *Planck* analysis, both surveys find values that are $\sim 2 - 3\sigma$ smaller.⁸

5.2. Weak lensing systematics

Low-redshift measurements of large-scale structure evolution require sophisticated analysis pipelines to correct for a large number of known systematic effects. Here, we discuss the most prominent systematic uncertainties affecting the weak lensing measurements.

5.2.1. Shape measurements

The basic observable in any weak gravitational lensing measurement is the ellipticity of a galaxy. The measured ellipticity is a combination of the intrinsic galaxy ellipticity and the shear effect of gravitational lensing. In the weak lensing regime the small shear is completely dominated by the large intrinsic ellipticity making it necessary to average over many galaxies. The idea behind this is that galaxies are intrinsically randomly oriented on the sky and the intrinsic ellipticities average to zero leaving only the shear (but see intrinsic alignments below). Under the assumption of random intrinsic orientation, a galaxy ellipticity is an unbiased but extremely noisy estimator of the shear.

In cosmic shear, pairs of galaxies are analyzed for coherent shear contributions to their ellipticities as a function of their distance. This typically involves many millions and soon billions of faint galaxy images. In practice, one has to estimate the ellipticities of these very large samples of galaxies from fuzzy, noisy images that make up a few pixels on a detector each. With weak lensing being a statistical measurement, it is not crucially important to estimate a highly accurate ellipticity measurement for every single galaxy. Rather it is important to control the average bias in the shear estimates to very low values. For current Stage-III surveys such as KiDS, DES, and HSC, biases in the shear need to be controlled to a level of $\sim 10^{-2}$, with future Stage-IV experiments requiring almost an order of magnitude better systematics control Laureijs et al. (2011); Mandelbaum et al. (2018b).

Several effects make this a very delicate problem. The atmosphere (in case of ground-based observations) and the telescope and camera optics introduce distortions that are significantly larger than typical shear values. These have to be corrected to high accuracy using PSF (point-spread-function) information from stars before the galaxy-based shear estimates can be used in cosmological measurements Kaiser et al. (1995). In the low signal-to-noise ratio regime, the measurements further suffer from noise bias that needs to be corrected Melchior and Viola (2012). Depending on the actual algorithm, other biases like model bias can play a role Voigt and Bridle (2010); Miller et al. (2013). Furthermore, any sample selection (e.g. through source detection Hoekstra et al. (2021) and tomographic binning via photometric redshifts) can introduce further biases. The electronics of CCDs also play a crucial role and must be understood at a deep level Rhodes et al. (2010); Gruen et al. (2015); Boone et al. (2018); Coulton et al. (2018); Massey et al. (2010).

In order to reach the required accuracy, it is usually necessary to simulate the whole process with a dedicated suite of image simulations, often based on or informed by high-resolution HST (Hubble Space Telescope) observations Rowe et al. (2014); Fenech Conti et al. (2017); Kannawadi et al. (2019); Hoekstra et al. (2017); MacCrann et al. (2021); Mandelbaum et al. (2018a); Bruderer et al. (2016); Li et al. (2021d). Only in this way can the crucial multiplicative bias, which describes the systematic over-/under-estimation of shear values, be calibrated. The community has engaged in several blind challenges over the past two decades to objectively determine the remaining multiplicative biases in weak lensing measurements Heymans et al. (2006); Massey et al. (2007); Bridle et al. (2010); Kitching et al. (2012); Mandelbaum et al. (2015). State-of-the-art algorithms suppress this bias to very small levels at runtime Huff and Mandelbaum (2017); Sheldon and Huff (2017); Sheldon et al. (2020); Kannawadi et al. (2021); Hoekstra (2021). But it is really the robustness to small differences between the image simulations that are ultimately used for calibration and the real Universe that determines the quality of a shape measurement method.

A residual bias in the shear estimates scales almost linearly with S_8 . Hence, the community has put a lot of effort over the past two decades (arguably more effort than into any other weak lensing systematic) into controlling these biases to the percent level in current surveys and is working towards an even better control for stage-IV experiments. As such, the current $\sim 5 - 10\%$ tension in S_8 between cosmic shear measurements and *Planck* is most probably not due to uncontrolled systematics in the shear measurement.

5.2.2. Photometric redshifts

The cosmic shear signal measured from wide-field imaging surveys scales strongly with redshift Van Waerbeke et al. (2006). The higher the redshift of the sources, the stronger the signal due to the increased light path and integrated deflection and distortion of the light-bundles along their way. As the measurement is inherently statistical, averaging the signal from millions of source galaxies, it is the ensemble redshift distribution of all sources that needs to be known to high accuracy in order to obtain unbiased model predictions for the cosmic shear signal. This accuracy is traditionally summarised in the uncertainty of the mean redshift of all sources, as the integrated nature of the cosmic shear effect means that higher-order moments of the redshift distribution are less important for accurate predictions. In order to allow measurements at different cosmic epochs and increase the constraining power for various cosmological parameters, the galaxy source sample is typically split up into tomographic redshift bins via individual photometric redshift estimates.

⁸ Note that the tension level changes depending on the assumed method, see Sec. 3 for details.

Both tasks, determining *precise* individual galaxy redshifts for the tomographic binning as well as estimating *accurate* redshift distribution(s) for the ensemble(s), require photometric techniques because of the large number of faint sources that makes spectroscopic measurements of complete weak lensing source samples infeasible. Typically, a subset of sources is observed spectroscopically and can be used to validate, train, and calibrate the photometrically determined redshifts and redshift distributions.

The individual photometric redshifts used for binning the galaxies along the line-of-sight are unimportant for the accuracy of S_8 measurements from cosmic shear. Rather, their precision influences the signal-to-noise ratio of those measurements and the constraining power of a survey. Thus, these individual photometric redshifts cannot cause a bias in S_8 and will not be discussed in the following. By contrast, the accuracy of the redshift distribution directly impacts the accuracy of cosmological parameter estimates Huterer et al. (2006). Any bias in the mean redshifts of the tomographic bins causes a bias in S_8 .⁹ If the mean redshift estimate is biased high the S_8 estimate will be biased low and vice versa. In practice, one marginalises over the uncertainty in the mean redshifts.

For contemporary Stage-III weak lensing surveys, the requirement on the accuracy of the mean redshifts of the tomographic bins is on the order of 0.01 Hildebrandt et al. (2017); Tanaka et al. (2018); Hoyle et al. (2018). This is necessary for the marginalisation over the redshift uncertainty to not compromise the statistical power of the surveys. Stage-IV surveys such as *Euclid* and LSST will require a calibration that is more accurate by a factor of $\sim 5 - 10$ to reach that goal Laureijs et al. (2011); Mandelbaum et al. (2018b). The importance of this redshift calibration has triggered a lot of work that aims at minimising biases in the determination of the source redshift distributions by different techniques that rely on different types of (typically spectroscopic) calibration samples. Broadly, these can be categorised as either colour-based or position-based techniques.

The colour-based techniques typically employ a deep spectroscopic calibration/reference sample that is as representative of the sources as possible. Any mismatch in redshift between the source and the reference samples needs to be removed before a reliable redshift distribution can be estimated. This is usually done by some re-weighting technique that takes the relative densities of both samples in high-dimensional colour/magnitude space into account Lima et al. (2008); Gruen and Brimioulle (2017); Hartley et al. (2020). Early attempts used *k*-nearest-neighbour counting to estimate these densities whereas most contemporary surveys have employed self-organising maps Masters et al. (2015); Buchs et al. (2019); Wright et al. (2020a); Myles et al. (2021); Wright et al. (2020b); Nishizawa et al. (2020). This latter technique has the advantage of easy visualisation and allows culling of the source sample to remove parts of colour space that are not covered by the spectroscopic reference sample. Covering the colour/magnitude space of future stage-IV weak lensing experiments with deep spectroscopic observations is a huge task. Dedicated spectroscopic surveys on the biggest available optical and near-infrared telescopes are being conducted to secure this essential calibration data Newman et al. (2015); Masters et al. (2017, 2019); Stanford et al. (2021); Guglielmo et al. (2020).

Complementary to the colour-based redshift calibration are techniques that exploit the fact that galaxies are clustered Newman (2008); Hildebrandt et al. (2017, 2021); Morrison et al. (2017); Gatti et al. (2022); van den Busch et al. (2020). Using a wide-area spectroscopic reference sample that covers the whole redshift range of interest, the redshift distributions of the weak lensing source sample can be determined via an angular cross-correlation approach. The amplitude of the angular cross-correlation between thin redshift slices of the reference sample and the unknown target sample (e.g. tomographic bins) is directly related to the target sample's redshift distribution. The great advantage of this technique is that the reference samples does not have to be representative of the target sample, e.g. one can use a bright reference sample to estimate the redshift distribution of a faint target sample since both samples cluster with each other. Correcting for the redshift evolution of galaxy bias in both samples is crucial because it is degenerate with the amplitude of the redshift distribution. This can be done via angular auto-correlation measurements for the reference sample and consistency checks for the target sample.

Both techniques of redshift calibration have been thoroughly tested against each other and on increasingly complex simulations over the past few years. So far, there is no indication that the S_8 tension is caused by a bias in the redshift calibration. A substantial amount of work still needs to be carried out to get those techniques ready for Stage-IV experiments, possibly combining colour and position information Alarcon et al. (2020); Sánchez and Bernstein (2019); Rau et al. (2021), but the current S_8 results from weak lensing seem quite robust in the light of these tests.

5.2.3. Intrinsic galaxy alignments

The intrinsic alignment (IA) of galaxies constitutes one of the most significant sources of systematic uncertainties in weak lensing (e.g. Refs. Hirata and Seljak (2004); Troxel and Ishak (2014); Heymans et al. (2013); Mandelbaum (2018); Bridle and King (2007); Heymans et al. (2004); Joudaki et al. (2017a); Vlah et al. (2020); Leonard and Mandelbaum (2018); Blazek et al. (2011, 2015); Krause et al. (2016); Kirk et al. (2010, 2012); Blazek et al. (2019); Joachimi et al. (2013); Chisari et al. (2015); Johnston et al. (2019); Fortuna et al. (2021); Samuroff et al. (2021)). It was shown in Refs. Bridle and King (2007); Heymans et al. (2004) that if intrinsic alignments are ignored in Stage-IV weak lensing analyses (such as *Euclid* and LSST), the equation of state of dark energy will be biased by up to 50% and the amplitude of matter fluctuations will be biased by up to 30%. Intrinsic alignments of galaxies refer to correlations between galaxies that arise due to the tidal gravitational field where these galaxies formed. These intrinsic alignments produce a spurious signal that contaminates the genuine lensing signal and any cosmological information inferred from it. Interestingly, there are two types of intrinsic alignments that affect lensing on large scales. The first is due to relatively close galaxies being radially aligned by the same dark matter structure, known as the "intrinsic shear – intrinsic shear", or II, correlation. The second type is due to the fact that a dark matter structure aligns radially neighbouring galaxies and at the same time tangentially shears the background galaxy images, thus creating an anticorrelation between the two known as the "gravitational shear – intrinsic shear" correlation, or GI, term. See reviews in Refs. Troxel and Ishak (2014); Kiessling et al. (2015); Kirk et al. (2015) and references therein.

After two decades of developing methods to mitigate the effects of intrinsic alignment contamination to the lensing signal in photometric galaxy surveys, two methods have emerged as being the most efficient at addressing the problem. One is the common marginalization method where an IA model is assumed and its parameters are constrained along with the cosmological parameters (see e.g. Ref. Joudaki

⁹ This is strictly only true in the non-tomographic case or in case of coherent biases of all tomographic bins. Incoherent redshift biases of different tomographic bins can cause e.g. spurious IA signals.

et al. (2018)). The other method is the self-calibration method that is based on calculating additional correlations from the same lensing survey by taking into account the positions of the lens with respect to the sources within the same bin and then using a scaling relation that relates such a correlation to cross-correlations between bins. This method strongly complements the marginalization method as it does not need to assume an IA model and is able to separate the IA signal from the lensing signal (see e.g. Ref. Troxel and Ishak (2012)). It was shown in Ref. Yao et al. (2017) that not correcting for intrinsic alignments can shift cosmological parameters as determined from weak lensing and that correlations between the IA amplitude and other parameters are present. Similarly, it was shown earlier in Ref. Dossett et al. (2015) that the IA amplitude has some correlation with S_8 but that it is not significant enough to explain the S_8 tension. This was confirmed in Ref. Yao et al. (2017). It is fair to assert that while intrinsic alignments need to be corrected for in an era or precision cosmology, these cannot be responsible for a significant tension in S_8 between lensing and the CMB.

5.2.4. Matter power spectrum including baryonic feedback

The matter power spectrum can be accurately obtained on linear scales via Boltzmann codes such as CAMB Lewis et al. (2000) and CLASS Blas et al. (2011). In order to obtain the matter power spectrum on nonlinear scales, numerical simulations need to be carried out at multiple cosmologies spanning the full parameter space of interest (see e.g. Refs. Lawrence et al. (2010); Schaye et al. (2010); Heitmann et al. (2016); McCarthy et al. (2017); Knabenhans et al. (2019, 2021)). An emulator for the simulations or a fitting function calibrated to the simulations can then be created. Examples of emulators include COSMIC EMU Lawrence et al. (2010); Heitmann et al. (2014); Lawrence et al. (2017) and EUCLID EMULATOR Knabenhans et al. (2019, 2021), while the two most popular fitting functions are HALOFIT Smith et al. (2003); Takahashi et al. (2012) and HMCODE Mead et al. (2015, 2016, 2020). On nonlinear scales, the impact of baryonic processes such as radiative cooling, star formation, and feedback from supernovae and active galactic nuclei (AGN) also needs to be taken into account (see e.g. Ref. Chisari et al. (2019) for a review). A particular benefit of HMCODE is that, in addition to calibrating against dark matter simulations, it accounts for these baryonic effects by calibrating against hydrodynamical simulations (originally to the OverWhelmingly Large Simulation, or OWLS, suite Schaye et al. (2010); van Daalen et al. (2011); Le Brun et al. (2014) and most recently to the BAryons and HAloes of MAssive Systems, or BAHAMAS, suite McCarthy et al. (2017)).

The uncertainties in the dark matter simulations and emulators of the matter power spectrum are at the few-percent level down to scales of $k \sim 10 h \,\mathrm{Mpc^{-1}}$ Lawrence et al. (2017); Knabenhans et al. (2021). These uncertainties grow to 5%-10% for the fitting functions for the same highly nonlinear scales Takahashi et al. (2012); Mead et al. (2020). Meanwhile, the uncertainties in the hydrodynamical simulations boil down to the choices that need to be made in regards to the stellar and hot gas content. The uncertainty in the simulations themselves are at the few-percent level (see e.g. Refs. van Daalen et al. (2011); Chisari et al. (2018)), but the impact of baryonic feedback on the matter power spectrum differs substantially between different simulations (suppressing the power between 10–30% for scales in the range of $k \sim$ few and 20 h Mpc⁻¹) due in particular to their different choices for the sub-grid model, resolution, and calibration strategy Chisari et al. (2018); Huang et al. (2019a); Chisari et al. (2019). Further work is therefore needed to capture the impact of baryonic feedback on the nonlinear matter power spectrum to the precision needed for next-generation cosmological surveys. While the KiDS Hildebrandt et al. (2017, 2020); Asgari et al. (2021); Joudaki et al. (2017b); Köhlinger et al. (2017); Joudaki et al. (2018); van Uitert et al. (2018); Heymans et al. (2021) and HSC Hikage et al. (2019); Hamana et al. (2020) analyses have attempted to account for the uncertainty in the matter power spectrum due to baryonic feedback by introducing one or more nuisance parameters, the fiducial approach in the DES analyses Troxel et al. (2018a); Secco et al. (2022); Amon et al. (2022); Abbott et al. (2018b, 2022) has been to avoid the uncertainty altogether by imposing more conservative scale cuts.

5.2.5. Small-angle approximations

The Limber and flat-sky approximations Limber (1954); LoVerde and Afshordi (2008) are commonly employed in cosmic shear analyses and are known to induce an uncertainty in the computation of the angular power spectra and correlation functions on large scales Joudaki and Kaplinghat (2012); Kitching et al. (2017); Kilbinger et al. (2017); Lemos et al. (2017). However, as the impact of these approximations on the observables is smaller than the size of the sample variance, they do not contribute to the S_8 tension and will even remain sufficient approximations for next-generation surveys such as *Euclid* and *Rubin*/LSST Kilbinger et al. (2017); Lemos et al. (2017). We note that in the case of galaxy clustering and galaxy-galaxy lensing, the Limber approximation cannot be reliably used for these surveys (see e.g. Refs. Giannantonio et al. (2012b); Fang et al. (2020)).

5.3. Redshift-space galaxy clustering

The S_8 parameter can also be measured from redshift-space galaxy clustering statistics, such as the galaxy power spectrum and bispectrum. These statistics are commonly used to extract the angular diameter and Hubble distances relative to the sound horizon along with the growth rate parameter, $f\sigma_8(z)$, from redshift-space distortions, all at the effective redshift of the galaxy sample. In combination with CMB surveys, which calibrate the expansion history, such measurements can be used to constrain σ_8 and S_8 . Combined analyses of SDSS and *Planck* data found $\sigma_8 = 0.829 \pm 0.016$ in $\nu \Lambda$ CDM (Alam et al., 2017), or $\sigma_8 = 0.8115^{+0.009}_{-0.007}$ when further including $f\sigma_8(z)$ measurements from eBOSS (Alam et al., 2021a). The former is equivalent to $S_8 = 0.843 \pm 0.016$, and both are consistent with the CMB-only analyses. We caution that these measurements are CMB-dominated, thus this is not a rigorous test of the purported S_8 tension.

Recently, it has been shown that S_8 can be measured from spectroscopic surveys without external calibration, by fitting the full shape of the observed power spectrum and bispectrum with an accurate theoretical model, analogous to that performed in CMB analyses (D'Amico et al., 2020; Ivanov et al., 2020c; D'Amico et al., 2021; Wadekar et al., 2020; Philcox and Ivanov, 2022; Ivanov, 2021; Chen et al., 2022; Kobayashi et al., 2021; Zhang et al., 2022; Colas et al., 2020; Hamann et al., 2010; Schöneberg et al., 2019; Tröster et al., 2020; Chen et al., 2021d). Natively, this measures the σ_8 parameter rather than S_8 ; however, Ω_m can be measured from the power spectrum shape (or alternative datasets such as supernovae), allowing an S_8 constraint to be obtained. Furthermore, Ω_m is generally well constrained and takes values consistent with analyses of supernovae and the CMB, such that any S_8 tension naturally translates into a σ_8 tension. Recent measurements of S_8 from BOSS full-shape power spectra are consistent with the value found from other low-redshift probes: $S_8 = 0.703 \pm 0.045$ lvanov et al. (2020c) or $S_8 = 0.704 \pm 0.051$ (D'Amico et al., 2020).¹⁰ This was recently refined by adding information present in the power spectrum of the eBOSS emission-line galaxies lvanov (2021) as well as the BOSS DR12 bispectrum Philcox and lvanov (2022), yielding $S_8 = 0.720 \pm 0.042$ and $S_8 = 0.751 \pm 0.039$, respectively. These results are similar across various analysis choices and statistics; for example, Ref. (Chen et al., 2022) found $S_8 = 0.736 \pm 0.051$ using the BOSS power spectra alone, Ref. (Kobayashi et al., 2021) found $S_8 = 0.740^{+0.043}_{-0.041}$ in an emulator-based analysis, and Ref. (Tröster et al., 2020) found $S_8 = 0.729 \pm 0.048$ using the BOSS correlation function. In all cases, the results are somewhat lower than *Planck*, though not at particularly large significance (typically less than 3σ). Systematic uncertainties affecting these measurements are described in Sec. 6.3. No major source of systematic that might significantly affect the measurements has been identified.

Finally, the clustering density can be measured from other probes such as the one-dimensional Ly α power spectrum (Palanque-Delabrouille et al., 2020) and peculiar velocity surveys (Boruah et al., 2020). These find similarly low values of S₈ in mild tension with *Planck*.

5.4. Combined weak lensing and galaxy clustering

The self-consistent combined analysis of cosmic shear, galaxy-galaxy lensing, and galaxy clustering at the level of their two-point statistics is commonly referred to as a " $3 \times 2pt$ " analysis. The self-consistency of this analysis allows for an improved self-calibration of the systematic uncertainties that affect the observables, such as galaxy bias and intrinsic galaxy alignments. The first three $3 \times 2pt$ analyses were published approximately simultaneously, using the datasets of KiDS- $450 \times \{2dFLenS+BOSS\}$ Joudaki et al. (2018), KiDS- $450 \times GAMA$ van Uitert et al. (2018), and DES-Y1 Abbott et al. (2018b). We now also have the $3 \times 2pt$ analyses of KiDS- $1000 \times \{2dFLenS+BOSS\}$ Heymans et al. (2021) and DES-Y3 Abbott et al. (2022). Here, the KiDS-1000 analysis Heymans et al. (2021) did not only contain additional imaging data, but further included the full 2dFLenS and BOSS datasets, which had been previously restricted to the areas overlapping with KiDS in Ref. Joudaki et al. (2018). This had the benefit of improving the constraining power from galaxy clustering and the drawback of diminishing the importance of the galaxy-galaxy lensing Joachimi et al. (2021a); Heymans et al. (2021).

Despite the same $3 \times 2pt$ terminology, there are subtle differences between the different analyses. In particular, the KiDS Collaboration has performed combined analyses of overlapping imaging and spectroscopic surveys, while the DES Collaboration has taken the approach of performing "internal" $3 \times 2pt$ analyses where the photometric galaxies are used as both lenses and sources. As a result, the analyses in Refs. Joudaki et al. (2018); Heymans et al. (2021) are the only to consider redshift-space galaxy clustering instead of angular galaxy clustering.

The 3 × 2pt constraints on S_8 and the matter density are driven by the cosmic shear and galaxy clustering, respectively. Here, we focus on the former, where $S_8 = 0.742_{-0.035}^{+0.025}$ in KiDS-450×{2dFLenS+BOSS} Joudaki et al. (2018), $S_8 = 0.800_{-0.027}^{+0.029}$ in KiDS-450×GAMA van Uitert et al. (2018), and $S_8 = 0.794_{-0.027}^{+0.029}$ in DES-Y1 Abbott et al. (2018b), which were followed by the updated constraints on $S_8 = 0.766_{-0.014}^{+0.020}$ in KiDS-1000×{2dFLenS+BOSS} Heymans et al. (2021) and $S_8 = 0.775_{-0.024}^{+0.026}$ in DES-Y3 Abbott et al. (2022). The KiDS-450 and KiDS-1000 analyses using the 2dFLenS and BOSS galaxies are highly consistent with one another (to well within a standard deviation). These analyses are also consistent with Ref. van Uitert et al. (2018), where the clustering of the GAMA galaxies favoured a larger value of S_8 . Likewise, the DES-Y1 and DES-Y3 constraints on S_8 are highly consistent with one another (to well within a standard deviation). Meanwhile, in comparing the constraints on S_8 from KiDS×{2dFLenS+BOSS} and DES, the posteriors seem to have approached one another in the latest analyses and are both in tension with *Planck* at the 2–3 σ level. However, we note that a comparison of the published constraints on S_8 should be carried out with caution as the two collaborations employ a set of different assumptions, which can have a substantial impact on the parameter constraints Joudaki et al. (2020).

We further highlight the 2 × 2pt analysis of galaxy-galaxy lensing and galaxy clustering with the HSC-Y1 and BOSS datasets in Ref. Miyatake et al. (2021), where $S_8 = 0.795^{+0.049}_{-0.042}$ is in agreement with both *Planck* and all of the 3 × 2pt analyses. Additional multi-probe analyses have resulted in low values of the S_8 parameter. In particular, the combined analysis of unWISE galaxy clustering and the cross-correlation with the *Planck* CMB lensing reconstruction resulted in $S_8 = 0.784 \pm 0.015$ Krolewski et al. (2021). The corresponding analysis using the luminous red galaxies of the DESI Legacy Imaging Surveys (DELS) and *Planck* CMB lensing reconstruction resulted in $S_8 = 0.73 \pm 0.03$ (White et al., 2022). Further, the self-consistent combined analysis of KiDS-1000 cosmic shear, Dark Energy Survey Year 1 cosmic shear and galaxy clustering, eBOSS quasars, *Planck* CMB lensing reconstruction, and photometric galaxies in DELS, including the different cross-correlations, gives $S_8 = 0.7781 \pm 0.0094$ García-García et al. (2021). A consistent picture therefore seems to be emerging that combined analyses of weak lensing and galaxy clustering are in tension with the *Planck* CMB temperature measurement of the S_8 parameter.

5.5. Galaxy cluster counts

The number density of the most massive dark matter halos in the Universe is highly sensitive to the growth of structure and hence to S_8 through the cosmological dependence of the halo mass function (see Ref. (Allen et al., 2011) for a review). Comparing the CMB data with Sunyaev-Zel'dovich (SZ) number counts, Ref. Ade et al. (2014b) was the first to note a tension at the level of ~ 3σ between the predictions based on the fiducial *Planck* CMB ACDM model and the observed cluster counts. This tension was confirmed in the full mission data (Ade et al., 2016a) and other cluster count experiments based on SZ (SPT Bocquet et al. (2019); ACT Hasselfield et al. (2013)), X-ray (400d Vikhlinin et al. (2009); RASS-WtG Mantz et al. (2015); XMM-XXL Pacaud et al. (2018)), or optical selection (SDSS Costanzi et al. (2019); DES Abbott et al. (2020b)). The fiducial CMB ACDM model implies there should be about twice as many very massive clusters in the local Universe compared to most studies. The measurements of S_8 from various cluster count experiments are summarized in Fig. 4.

¹⁰ These measurements and a number of other results based on SDSS-III Fourier-space statistics are $\sim 1\sigma$ too low due to a misnormalization of the public BOSS power spectra (Philcox and Ivanov, 2022; Beutler and McDonald, 2021). This occurred due to incorrect treatment of small-scale power in the survey window function, resulting in a 10% suppression of the power spectrum multipoles, and affects any analyses using the BOSS DR12 Fourier-space data prior to (Beutler and McDonald, 2021).

In Ref. Pratt et al. (2019), it is shown that the various cluster count results obtained by different groups and different detection techniques agree well with one another and with the cosmic shear results, providing an unweighted mean $S_8 = 0.789 \pm 0.012$ which is formally different from the CMB expectation (for example *Planck* gives $S_8 = 0.834 \pm 0.016$ assuming Λ CDM) at more than 2σ level.

The leading source of systematic uncertainty in cluster count experiments is the calibration of the relation between mass and observable (see Ref. Pratt et al. (2019) for a review). While the halo mass function and its cosmological dependence are usually based on DM-only simulations (e.g. Ref. Tinker et al. (2008)), current galaxy cluster detection techniques rely on selection through the cluster's baryonic content, either through the hot gas (SZ, X-ray) or the clustering of galaxies (Friends-of-Friends, red sequence, match filter). The relation between the survey observable (e.g. the integrated Compton parameter Y_{SZ} in the case of SZ experiments) and the mass of the host halo needs to be accurately understood to infer cosmological parameters. For instance, the *Planck* SZ cluster counts may be reconciled with the CMB predictions in case the estimated halo masses were biased by a factor $1 - b = M_{obs}/M_{true} = 0.58 \pm 0.04$ Ade et al. (2016a). While early cluster count experiments relied on external observable-mass scaling relations Ade et al. (2014b, 2016a); Vikhlinin et al. (2009), modern experiments use internally-calibrated relations with available WL data for a subset of systems and attempt to marginalize over the uncertainties in the mass bias by performing a joint inference of the cosmological parameters and the scaling relations Pierre et al. (2017); Bocquet et al. (2019); Garrel et al. (2021). Future cluster count experiments such as eROSITA Merloni et al. (2021) and SPT-3G Benson et al. (2014) will take advantage of upcoming wide-field WL data from e.g. *Euclid* to improve both on the statistical precision by including a much larger number of sources and on the accuracy by limiting the systematic uncertainties in the mass calibration Grandis et al. (2019).

For the S_8 constraints in Fig. 4, the errors are propagated according to $\sigma_{S_8}^2 = (\Omega_m/0.3)^{2\alpha}\sigma_{\sigma_8}^2 + \sigma_8^2\alpha^2(\Omega_m/0.3)^{2\alpha-2}\sigma_{\Omega_m}^2$, with the index $\alpha = 1/2$. Here, σ_8 and Ω_m are assumed to be Gaussian distributed and are considered at their published best-fit values.

5.6. CMB S₈ measurements

The amplitude of the CMB power spectrum and even more so the lensing of the CMB set tight bounds on the matter density and on σ_8 , which is usually a derived parameter in CMB analyses. The CMB estimates of these parameters and of their combination, S_8 , strongly depend on the assumptions made in the fits and on the specific data combination Calabrese et al. (2013, 2017); Henning et al. (2018); Aiola et al. (2020). Lately, with uniformity in analyses and with new observations, the CMB estimates have converged on values larger than the galaxy-based estimates of S_8 , as shown in Fig. 4.

As already mentioned above and as shown later in Sec. 7, this measurement is model dependent. In particular, the value of S_8 will fluctuate as other parameters affecting the clustering such as the amplitude and growth of the matter fluctuations are varied. Two examples of these are the sum of the neutrino masses, Σm_{ν} , and the optical depth to reionization, τ , which both affect the overall power spectrum amplitude Ade et al. (2016b). We note that τ is the most uncertain of the Λ CDM parameters while Σm_{ν} is not yet directly measured and is commonly set to the minimum expected value. In every Λ CDM fit then, these two parameters and their uncertainty will carry some weight on the derived S_8 constraints. These correlations are also visualized in the specific case of *Planck* with the excess of lensing anomaly, which Ref. Di Valentino and Bridle (2018) showed can mimick a larger S_8 . However, *Planck* and its lensing excess is not the cause – or not the only cause – of this CMB-LSS tension, the CMB preference for larger amount of matter clustering is also confirmed by the latest ACT+WMAP analysis Aiola et al. (2020) which finds a large value of $S_8 = 0.840 \pm 0.030$ but differently from *Planck* no anomalous value for the lensing amplitude.

Given the significant importance of CMB lensing in these measurements, improvements in small-scale lensing theory, such as nonlinear, foreground and baryonic effects which generate noise biases in lensing will play a major role Beck et al. (2018b).

6. Other measurements and systematics

Coordinators: Mikhail M. Ivanov, Oliver H.E. Philcox.

Contributors: Micol Benetti, Anton Chudaykin, Eleonora Di Valentino, Raul Jimenez, Michele Moresco, Levon Pogosian, Denitsa Staicova, Licia Verde, and Luca Visinelli.

6.1. Planck CMB data and the excess of lensing

It is well known that CMB observations from *Planck* constrain the cosmological parameters with an extraordinary accuracy. However, it is quite natural to understand that, similar to any experimental measurements, *Planck* could be affected by systematic errors. Here, we shall briefly discuss the possible systematic errors in *Planck* that might be propagated in the determination of the cosmological parameters under the assumption of the Λ CDM paradigm as the background cosmological model.

The *Planck* collaboration Aghanim et al. (2020c) presents the constraints on the model parameters using two different likelihood pipelines for the data at multipoles $\ell > 30$, namely, Plik and CamSpec (see the updated version in Ref. Efstathiou and Gratton (2019)). Whilst in principle, both the likelihood pipelines refer to the same measurements, however, they actually consider different sky masks and chunks of data, and additionally, the likelihoods handle foregrounds in a different way, especially for polarization. As a consequence, the observational constraints on the Λ CDM model parameters extracted using Plik likelihood and the CamSpec likelihood thus differ at most by 0.5σ in case of the baryon density, just by 0.2σ in case of the Hubble constant Aghanim et al. (2020c) or by 0.3σ in case of the S₈ parameter. Even though the choice between Plik likelihood and the CamSpec likelihood makes a very mild effect on the Hubble constant or S₈ tensions, however, it should be emphasized that a choice of a different likelihood may shift the constraint on some parameters coming from CMB by 0.5σ , and this should not be completely forgotten as we approach precise measurements of the cosmological parameters.

A possible indication for a systematic error in *Planck* is given by the excess of lensing, i.e. the so called " A_{lens} anomaly", see subsection 8.1 for a detailed explanation. Interestingly, if this parameter is included in the analysis, then both the Hubble constant tension and the S_8 tension are slightly reduced. In fact, due to the inclusion of A_{lens} in the analysis, then the *Planck* and *Planck*+BAO constraints on H_0

are slightly increased leading to $H_0 = (68.3 \pm 0.7) \text{ km s}^{-1} \text{ Mpc}^{-1}$ (at 68% CL for *Planck* data alone) and $H_0 = (68.22 \pm 0.49) \text{ km s}^{-1} \text{ Mpc}^{-1}$ (at 68% CL for *Planck*+BAO), using either Plik likelihood or CamSpec likelihood.

Analogously, when A_{lens} is free to vary, *Planck* gives $S_8 = 0.804 \pm 0.019$ at 68% CL, from $S_8 = 0.834 \pm 0.016$ at 68% CL when $A_{\text{lens}} = 1$. Therefore, for *Planck* constraints, the inclusion of A_{lens} in the analysis reduces the Hubble tension from 5σ to 3.9σ with the R21 value $H_0 = (73.04 \pm 1.04) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Riess et al. (2021b), and reduces the S_8 tension with the weak lensing experiments below 2σ . If A_{lens} is due to systematic errors in the *Planck* data, then we need to understand how the systematics could affect the constraints on the Hubble constant and the S_8 parameter and hence its effect on the cosmological tensions. It is worthwhile to note here that in any case, the increase of the Hubble constant mean value within the Λ CDM paradigm from *Planck* is not enough to cancel out completely the Hubble tension, and that a lower H_0 value is supported by the complementary ground-based CMB experiments, such as ACT and SPT, that are not affected by the excess of lensing. The same conclusion is valid for the S_8 parameter.

Alternatively, the lensing information can be reconstructed from CMB power spectra in a model-independent way by modelling the principal components of the gravitational lensing potential Motloch and Hu (2018). This setup allows for amplitude and shape variations in the lensing power spectrum beyond Λ CDM which can be parametrized by free lensing parameters $\Theta^{(i)}$. This analysis should be contrasted with the common A_{lens} approach which considers only changes in the amplitude of the gravitational lensing potential. Measuring the lensing principal components presents a direct and model-independent consistency test of the lensing information encoded in the CMB data. In this analysis, the amount of lensing determined from the smoothing of the acoustic peaks in the *Planck* power spectra is 2.8 σ higher when compared with Λ CDM expectation based on the "unlensed" temperature and polarization power spectra (after marginalizing over the lensing information $\Theta^{(i)}$) Motloch and Hu (2020). Allowing for an arbitrary gravitational lensing potential still leads to anomalously high lensing power in the *Planck* power spectra, which supports the " A_{lens} anomaly". This result points to possible systematic errors in the *Planck* data or a statistical fluke that can be resolved by more CMB data.

6.2. BAO and the sound horizon problem

It is important to discuss a possible cosmology-dependence of the BAO measurements. This cosmology dependence can come through two channels: (a) underlying cosmology assumptions when converting angles and redshifts into distances, (b) assumptions on fiducial cosmology when creating a post-reconstructed BAO template, which is then used to fit the data. Refs. Heinesen et al. (2019, 2020) have shown that the standard underlying cosmology assumptions are accurate as long as the Universe can be locally described with the isotropic and homogeneous FLRW metric. This is certainly true for most of the cosmological models that are aimed to fit all available cosmological data. However, the caveat on the FLRW metric should be kept in mind when considering more exotic cosmological models with large metric gradients. The second concern is about the choice of the fiducial template. Unlike the standard RSD method, the BAO extraction is not very sensitive to the underlying fiducial template cosmology assumptions. This is because the BAO pattern is, essentially, a quasi-harmonic oscillation function. The BAO method just extracts its frequency, and therefore, any reasonable harmonic-type template is expected to perform well in this situation because the frequency does not depend on the shape of the template. This point was explicitly proven with regards to modifications of the early Universe cosmology in Ref. Bernal et al. (2020). Finally, in terms of non-linear effects, the possible systematic shift in the post-reconstructed BAO is bound to be less than 0.2% Blas et al. (2016a), which proves the common lore that the nonlinear effects are not an issue for the BAO measurements.

With the advent of *Planck* precision, observations on the distributions of galaxies have become increasingly important to studying the late-time evolution of the Universe. Indeed, this type of measurement encodes not only information on the history of cosmic expansion but also on the growth of structure, a fundamental aspect for probing different mechanisms of cosmic acceleration as well as for distinguishing between competing gravitational theories.

A tool for identifying the distribution of galaxies at large scales is the two-point spatial correlation function (2PCF) of large galaxy catalogues, which has shown a tiny excess probability of finding pairs of galaxies separated by a characteristic scale r_s - the comoving acoustic radius at the drag epoch. This signature of Baryon Acoustic Oscillations arises from competing effects of radiation pressure and gravity in the primordial plasma, which is well described by the Einstein-Boltzmann equations in the linear regime, and defines a statistical standard ruler and provides independent estimates of the Hubble parameter H(z) and the angular diameter distance $D_A(z)$. It is worth mentioning that these measures are not model-independent, since they use the radial $(dr_{\parallel} = c\delta z/H(z))$ and transverse $(dr_{\perp} = (1 + z)D_A\theta_{BAO})$, respectively. Analyses of this type assume a fiducial cosmology to transform the measured angular positions and redshifts into comoving distances, such a conversion may distort the constraints on the parameters Eisenstein et al. (2005); Sanchez et al. (2012); Salazar-Albornoz et al. (2017).

Another possibility is to use the 2-point angular correlation function (2PACF), $w(\theta)$, which involves only the angular separation θ between pairs, providing almost model-independent information on $D_A(z)$, as long as the comoving sounding horizon r_s is known (see Refs. Salazar-Albornoz et al. (2017); Carvalho et al. (2016); Alcaniz et al. (2017); Carvalho et al. (2020); de Carvalho et al. (2020) for details and Refs. Benetti et al. (2018a); Santos et al. (2021); Menote and Marra (2021); Bengaly (2021); Mukherjee et al. (2021b); Arjona and Nesseris (2021a); Ferreira et al. (2017); Brinckmann and Lesgourgues (2019); Cid et al. (2019); Dutta Ruchika et al. (2020); Camarena and Marra (2020b); von Marttens et al. (2019); Gonzalez et al. (2018) for cosmological analysis results using this type of measurements). Although the latter would theoretically be more suitable for alternative gravity model analyses, since it does not use a fiducial model, the associated errors of these BAO angular correlation measurement are an order of magnitude larger than those of 2PCF. Furthermore, the technique used for BAO estimation of 2PACF uses a very narrow redshift shell, with $\delta z \sim 0$ making it a sufficiently complex procedure to apply.

We now turn to the problem of the sound horizon. For this we define the sound horizon at redshift z, here $r_s(z)$, as the distance travelled by an acoustic wave in the baryon-photon plasma in terms of the sound speed of the baryon-photon plasma $c_s(z)$, as

$$r_{s}(z) = \int_{z}^{\infty} \frac{c_{s}(z')}{H(z')} \mathrm{d}z' \,. \tag{3}$$

With the energy densities for the baryon $\rho_b(z)$ and the photon $\rho_\gamma(z)$, the speed of sound in the baryon-photon fluid is approximated as $c_s \approx c \left(3 + 9\rho_b/(4\rho_\gamma)\right)^{-0.5}$. Of particular importance is the drag epoch, occurring at redshift z_d , at which the baryons are released from the Compton drag of the photons Zeldovich and Sunyaev (1969); Sunyaev and Zeldovicha (1970); Peebles and Yu (1970). The corresponding distance at drag epoch is $r_d \equiv r_s(z_d)$. Here, one has to take into account the difference between the sound horizon at the CMB last-scattering defined at $z_* \sim 1090.30$ Aghanim et al. (2020b) when photons decouple and the BAO sound horizon at drag epoch $z_d \sim 1059.39$ Aghanim et al. (2020b) when baryons stop feeling the photon drag.

The problem of the sound horizon refers to the different preferred values for the sound horizon by early and late-time measurements. It can be traced to the fact that BAO surveys measure the projected quantities $\Delta z = r_d H/c$ and $\Delta \theta = r_d/(1 + z)D_A(z)$, where Δz and $\Delta \theta$ are the redshift and the angular separation. From here, it follows that without further assumptions, one may derive from BAO only the quantity $r_d \times H$. In order to decouple these quantities, one needs either a model independent measurement of H_0 or an independent evaluation of r_d . The Hubble constant H_0 can be obtained from model independent late-time probes such as cosmic chronometers Moresco et al. (2020), Type Ia supernova Scolnic et al. (2021, 2018), the Cepheids in LMC Riess et al. (2019), or indirect probes such as the matter-radiation equality scale Baxter and Sherwin (2021); Philcox et al. (2021b) (see Section 4). Eq. (3) imposes additional assumptions on the baryon and radiation load of the Universe at decoupling. Furthermore, calculating the angular distance D_A by definition depends on the implied cosmology, and thus on the implied theory of gravity. This problem is known as the H_0-r_d tension, considered in detail in Ref. Knox and Millea (2020), where it is found that the spread in r_d depends mostly on the matter density Ω_m and that it is not possible to reconcile the tension in early and late time Universe measurements by changing Ω_m alone.

As shown in Ref. Pogosian et al. (2020), complementing the BAO data with a prior on $\Omega_m h^2$ makes it possible to determine both r_d and H_0 while treating them as independent parameters, *i.e.* without the need to calculate r_d from theory. One can also decouple r_d and H_0 by combining the BAO data with galaxy and/or CMB weak lensing, which provide a constraint on $\Omega_m h^2$ that is largely independent of the physics before and during recombination. It is interesting that the current BAO data (eBOSS DR16+), combined with the Gaussian prior of $\Omega_m h^2 = 0.143 \pm 0.0011$ corresponding to the value measured by *Planck* within the Λ CDM model, gives $r_d = (143.8 \pm 2.6)$ Mpc and $H_0 = (69.6 \pm 1.9)$ km s⁻¹ Mpc⁻¹, thus preferring a somewhat larger H_0 and a smaller r_d than *Planck* Pogosian et al. (2020). Applying this method to future BAO data will offer a stringent consistency test against the value of r_d derived in a model-dependent way from CMB. In particular, as forecasted in Ref. Pogosian et al. (2020), the upcoming DESI BAO data combined with the *Planck* prior on $\Omega_m h^2 = 0.143 \pm 0.0011$ will measure r_d and H_0 with uncertainties of $\sigma_{r_d} = 0.64$ Mpc and $\sigma_{H_0} = 0.32$ km s⁻¹ Mpc⁻¹, respectively. Possible alternatives that have been considered in the literature are working with $H_0 \times r_d$ as a combined parameter L'Huillier and

Possible alternatives that have been considered in the literature are working with $H_0 \times r_d$ as a combined parameter L'Huillier and Shafieloo (2017); Shafieloo et al. (2018b); Arendse et al. (2020); Benisty and Staicova (2021b), replacing the prior on H_0 with a prior on the peak absolute magnitude M_B Camarena and Marra (2020b, 2021); Efstathiou (2021); Benevento et al. (2020); Perivolaropoulos and Skara (2021a) or using a modified gravity or early dark energy model that changes the value of r_d before recombination (see the discussion in the sections below and Ref. Di Valentino et al. (2021g)). However, as noted in Refs. Jedamzik et al. (2021); Benisty and Staicova (2021a); Staicova (2021), a dark energy model that merely changes the value of r_d would not completely resolve the tension, since it will affect the inferred value of Ω_m and transfer the tension to it. The sound horizon problem should be considered not only in the plane H_0-r_d , but it should be extended to the parameters triplet $H_0-r_d-\Omega_m$.

6.3. Redshift-space galaxy clustering systematics

RSD measurements suffer from a number of systematic effects, which can be loosely categorized as observational, modelling, and analysis systematics. From the observational side one can mention stellar contamination, atmospheric extinction and blurring Ross et al. (2012), fiber collisions Hahn et al. (2017), integral constraints, angular and radial modes' systematics de Mattia and Ruhlmann-Kleider (2019).These effects have been thoroughly studied in the past, and none of them is expected to affect the RSD results in a statistically significant way. Another observational effect that is currently under active investigation is selection bias Hirata (2009), which might directly affect the RSD clustering amplitude measurement. The claims in the literature on the presence of this effect are currently controversial: they vary from significant evidence for selection bias Obuljen et al. (2020) to no detection thereof Singh et al. (2021).

From the theory side, the largest uncertainty has been the accuracy of theoretical models for nonlinear galaxy clustering in redshift space. This uncertainty is now removed after the progress in the effective field theory of large scale structure (see Baumann et al. (2012); Carrasco et al. (2012); Porto et al. (2014); Senatore and Zaldarriaga (2015, 2014); Perko et al. (2016); Lewandowski et al. (2018); Desjacques et al. (2018); Blas et al. (2016b,a); Ivanov and Sibiryakov (2018); Ivanov et al. (2020c); Vlah et al. (2015); D'Amico et al. (2020); Chen et al. (2020b, 2021d); Chudaykin et al. (2020b) and references therein), which provides an accurate and systematic description of the galaxy clustering statistics on large scales. This is especially important in analyses of extended cosmological scenarios, e.g. massive neutrinos Chudaykin and Ivanov (2019); Ivanov et al. (2020d), dynamical dark energy D'Amico et al. (2021); Chudaykin et al. (2021a), non-zero spatial curvature Chudaykin et al. (2021a), axion dark matter Laguë et al. (2021), light relics Xu et al. (2021b), etc., where the use of approximate phenomenological models or fits to ACDM-based simulations (e.g. Halofit) becomes inadequate.

It is also worth mentioning that there has been significant progress in analyzing the redshift space clustering with the fully simulationbased techniques ("emulators"), see e.g. Refs. Heitmann et al. (2009); Kobayashi et al. (2020); Hahn et al. (2020), which nominally allow one to use information from short scales that cannot be described with perturbation theory. The current results from this program show some scatter between different teams Lange et al. (2021); Chapman et al. (2021); Kobayashi et al. (2021); Zhai et al. (2022), which calls for further investigations.

In terms of analysis systematics, another source of uncertainty in the standard RSD measurements are the so-called "shape priors" Ivanov et al. (2020c,b). Most of the RSD analyses fix the shape of the linear matter power spectrum by assuming ACDM cosmological parameters, and only capture the cosmology dependence by means of the so-called scaling parameters. The shape priors make the fixed template analysis intrinsically cosmology-dependent, see e.g. Refs. de Mattia et al. (2021); Smith et al. (2020a). Moreover, while the scaling parameters capture some non-standard late-time cosmological scenarios, they do not account for all possible variations of cosmological parameters.

It is especially important to take into account for the models that modify the physics at high redshifts (with respect to the observed galaxy clustering), e.g. the early dark energy, see Refs. Ivanov et al. (2020c,b) and Sec. 7.4.2 for further discussion. The use of the full-shape

method Ivanov et al. (2020c); D'Amico et al. (2020); Chen et al. (2022) allows one to remove any uncertainty associated with the shape priors. This method currently finds a mild tension with the *Planck* Λ CDM cosmology in the late-time clustering amplitude σ_8 , and this result is consistent across different teams Ivanov et al. (2020c); D'Amico et al. (2020); Chen et al. (2022). Finally, it is worth mentioning that the current RSD results have been shown to be stable under covariance matrix assumptions Wadekar et al. (2020); Philcox et al. (2021a).

6.4. The age of the Universe problem

The age of the Universe is not just a prediction of the Λ CDM model, that for *Planck* 2018 is $t_U = (13.800 \pm 0.024)$ Gyr, but can also be measured using very old objects. In particular, the age of HD 140283 equal to $t_* = (14.46 \pm 0.8)$ Gyr Bond et al. (2013) leads to some mild tension with the *Planck* 2018 predictions corresponding to somewhat lower age. However, the age of HD 140283 becomes $t_* = (13.5 \pm 0.7)$ Gyr Jimenez et al. (2019a) using the new Gaia parallaxes instead of original HST parallaxes and thus becomes fully consistent with the Λ CDM predictions. In addition, using populations of stars in globular clusters Ref. Valcin et al. (2020) finds $t_U = (13.35 \pm 0.16(\text{stat}) \pm 0.5(\text{sys}))$ Gyr which is also marginally consistent with Λ CDM. Thus, at present there is no confirmed tension between the different t_U determinations in the context of the *Planck* 2018 data, in contrast to discrepancies in the past Verde et al. (2013).

This may change in the future if significantly older objects are found in the Universe. In such a case, a possibility to increase the age of the Universe, to be larger than the age of oldest stars, would be to lower the Hubble constant value, because of the anti-correlation between these parameters de Bernardis et al. (2008). However, such an effect would tend to increase rather than decrease the Hubble tension. For example, a positive curvature for the Universe, as suggested by *Planck* 2018, preferring a lower H_0 and worsening significantly the H_0 tension, predicts an older Universe $t_U = (15.31 \pm 0.47)$ Gyr.

Considering the constraints coming from all low and high redshift data together with that of the age of Universe, leaves very little room for late resolutions to the H_0 tension Krishnan et al. (2021b), unless it is an extremely recent (after $z \sim 0.1$) departure from Λ CDM Bernal et al. (2021), requiring a great deal of fine-tuning. Thus, the constraints from the age of the oldest objects in the Universe puts in disfavour a high value of H_0 and late time solutions of the Hubble tension that are based on late time deformation of H(z) that increase H_0 and thus decrease the age of the Universe t_U . For this reason, model-independent measurements of t_U are very important, since they either support or disfavour alternative proposed models that alleviate the Hubble tension Bernal et al. (2021); Vagnozzi et al. (2021d). In particular, the use of new cosmic triangle plots to simultaneously represent independent constraints on key quantities related to the Hubble parameter, i.e. age of the Universe, sound horizon and matter density Bernal et al. (2021) is a welcome development.

Given its direct connection with the Hubble constant and the cosmological parameters driving the expansion history, the age of the Universe is a very important quantity. In particular, the use of extremely old local objects to measure the current age of the Universe (for example, see the reviews in Refs. Catelan (2018); Soderblom (2010); VandenBerg et al. (1996) and the recent determinations in Refs. O'-Malley et al. (2017); Valcin et al. (2020, 2021)), as well as the determination inferred from the oldest objects at higher redshifts Dunlop et al. (1996); Spinrad et al. (1997) have played a significant role supporting the standard cosmological model.

Since the look-back time is directly determined by the expansion rate of the Universe, age measurements can constrain the cosmological parameters determining the background evolution. While, as discussed later, differential ages can be used to measure the Hubble parameter with the cosmic chronometers method, also absolute ages can play an important role, as they have been used for at least 70 years to provide constraints on the cosmological model.

The look-back time of the Universe *t* can be expressed as function of redshift as:

$$t(z) = \frac{977.8}{H_0} \int_0^z \frac{\mathrm{d}z'}{(1+z')E(z')} \,\mathrm{Gyr} \ , \tag{4}$$

with E(z) is the normalized Hubble parameter $H(z)/H_0$, and the constant provides the conversion to km s⁻¹ Mpc⁻¹. The age of the Universe can be expressed from Eq. (4) as $t_U = t(\infty)$.

The age of the oldest star in our Galaxy, as also in many nearby galaxies, can be estimated from the color-magnitude diagram (CMD) of coeval stellar populations. Alternatively, if the metallicity and distance are known, it is also possible to determine the age of individual stars. It is important to underline that the full morphology of the CMD of resolved stellar population can constrain the absolute age without necessarily needing a distance determination. For a more detailed review on the topic, we refer the reader to Refs. Catelan (2018); Soderblom (2010); VandenBerg et al. (1996).

The most accurate method currently available to determine the ages of stars is based on the analysis of the observed CMD of Globular Clusters (GC), but there are also different alternatives. A first possibility is to use the abundances of radioactive elements (e.g., Uranium and Thorium), in an approach named nucleo-cosmochronology Christlieb (2016). A second possibility is to exploit the cooling luminosity function of white dwarfs (see e.g. Ref. Catelan (2018) and references therein).

Interestingly, the measurement of old stellar ages was one of the first indications challenging the Einstein-de Sitter cosmological model Ostriker and Steinhardt (1995); Jimenez et al. (1996); Spinrad et al. (1997), since the stellar ages were larger than the age of the Universe within that model. Clearly, the ages of local objects at z = 0 purely represent a strict lower limit to the age of the Universe, and degeneracies between cosmological parameters, such as H_0 and Ω_m , as can be seen by Eq. (4), make it difficult to precisely disentangle different models. A crucial point that allowed to break this degeneracy was the discovery and measurement of the age of extremely old galaxies at $z \gg 0$ (see e.g. Ref. Dunlop et al. (1996) and Fig. 18 in Ref. Spinrad et al. (1997)).

If we consider the absolute age determined only from the main-sequence turn off point (MSTOP) luminosity, we find that other GC properties are degenerate with it. The most significant source of errors in this approach is the uncertainty on the distance to the GC, which scales almost linearly in percentage with the uncertainty in the measured age. In addition, further contributions to the error budget are given by theoretical systematics involved in stellar evolution models, namely the metallicity content, the dust absorption VandenBerg et al. (1996), and the Helium fraction.

However, as first discussed in Ref. Jimenez and Padoan (1996); Padoan and Jimenez (1997), an important point to stress is that multiple additional information can be exploited in a GC CMD that can complement the MSTOP, since it presents features with which it is possible

to jointly determine its age and distance scale. In particular, if we consider Fig. 2 from Ref. Jimenez and Padoan (1998) it is possible to notice how different parts of the CMD are sensible to different physical quantities, and in Fig. 1 from Ref. Padoan and Jimenez (1997) and in Fig. 3 from Ref. Jimenez and Padoan (1998), it was demonstrated that the luminosity function of the GC can provide information about various physical parameters. With this approach it was possible to determine the absolute ages of GCs M68 Jimenez and Padoan (1996), M5 and M55 Jimenez and Padoan (1998). In addition, it has also been found that the horizontal branch morphology can be analyzed to obtain a measurement of GCs age independent of constraints on their distance (Jimenez et al., 1996).

In this context, the exploitation of Bayesian methods to fit the CMD of GCs has been only recently explored by a few works, either focusing only on some of its features Wagner-Kaiser et al. (2017), or considering it entirely Valcin et al. (2020, 2021). This approach provided a combined measurement of distances, metallicities and ages for 68 GCs observed by the HST/ACS project. One of the most important benefits of this techniques is that it allows to minimize part of the systematic error, providing a larger accuracy. It is important to notice that even considering different methods and observables, the ages determined are all consistent with each other at 13.5 ± 0.27 Gyr.

The determination of the absolute ages of old stellar objects has succeeded in revealing important insights in the Hubble tension debate. In Ref. Bernal et al. (2021) in particular a new approach has been proposed by highlighting the importance of three quantities that can be constrained independently even if they are interconnected: the age of the Universe t_U measurable from the absolute ages (and CMB), the Hubble constant H_0 obtained from the cosmic distance ladder (and CMB), and the combination H_0t_U from standard rules and candles (BAO and SNIa). This triad of measurements, named "new cosmic triangle", can be represented as $\ln t_U + \ln H_0 \equiv \ln(H0t_U)$. In this framework, we have some measurements depending on a cosmological model (namely CMB, SNIa and BAO), while some other being independent (the stellar ages and the distance ladder), but interestingly all the measurements were in agreement with a Λ CDM model.

To further improve the accuracy of absolute age estimates in the future it will be crucial to improve the stellar modelling by decreasing the systematic errors, exploiting better determinations of distances and metallicities for GC, and reducing the degeneracies between parameters. From this point of view, the final release of Gaia will be fundamental since it will provide distances with a percent (and even smaller) accuracy. On the other hand, better constraints on the chemical composition of individual GC stars (in particular below MSTOP) that can be obtained from advanced spectroscopic analyses (e.g. with JWST) will allow to appreciably reduce the priors on the metallicity of the system, leading to better constraints. In this scenario (as also reported by Ref. Valcin et al. (2021)), the main systematic left in the analysis of the full CMD will be the nuclear reaction rates uncertainty, which in turn can be addressed from a combination of theoretical and laboratory works.

With a similar approach, it is also possible to constrain the expansion history of the Universe from the ages of the oldest objects in the Universe at larger redshifts. This method, known as *cosmic chronometers*, provides a cosmological probe able to directly estimate the Hubble parameter H(z) in a direct and cosmology-independent way (see section 4.2). This technique, first proposed by Ref. Jimenez and Loeb (2002), only relies on the direct relation between the scale factor a(t) and the redshift in a universe described by a FLRW metric. Considering this only assumption, the Hubble parameters H(z) can be derived without any other cosmological assumption from the differential age evolution dt of the universe in a specific interval of redshift dz as:

$$H(z) = -\frac{1}{(1+z)} \frac{dz}{dt} \,.$$
(5)

In this equation, since the redshift can be directly measured in astrophysical objects, the only unknown is the differential age dt, and therefore the key points are to obtain an homogeneous population of cosmic chronometers, and to robustly measure their difference in age.

The strength of this approach in comparison to other cosmological probes is that it is based on minimal cosmological assumptions, considering only a FLRW metric and not relying on any explicit functional form of a cosmological model, or implicitly assuming a spatial geometry. For this reason, measurements obtained with the CC method are ideal to test a wide variety of different cosmologies. A comprehensive review on the method is provided in Ref. Moresco et al. (2022), with a detailed discussion on the selection of the optimal CC tracers, current measurements, and systematics involved. In the following, we will just briefly summarize the main points.

Cosmic chronometers are astrophysical objects that can accurately trace the differential age evolution of the Universe as a function of redshift. The ideal tracers, therefore, need to be an extremely homogeneous population of the oldest objects in the Universe at each redshift whose intrinsic evolution takes place on timescales much longer than the evolution due to pure passive ageing. For this reason, the ideal candidates are massive and passively evolving galaxies, carefully selected in order to minimize the possible contamination by star-forming outliers. To maximize the purity of a CC sample, as highlighted in Ref. Moresco et al. (2013, 2018), it is fundamental to exploit and combine different selection criteria, based on photometric, spectroscopic, morphological data, while also including a cut to select the most massive systems.

Once a proper sample of CC is obtained, the fundamental step is to robustly estimate the differential age dt in a redshift bin dz. Since its first application by Ref. Simon et al. (2005), the determination of the differential age dt has been performed with different approaches. The first one relies on exploiting the information contained in the full spectrum of CC through a full-spectrum fitting. This method has the benefit of taking advantage of most of the information that can be extracted from the observation of CC, the drawback being the need for accurate models able to accurately and robustly reproduce all the spectroscopic features observed. This method has been successfully applied in Refs. Simon et al. (2005); Zhang et al. (2014a); Ratsimbazafy et al. (2017), obtaining 13 H(z) measurements at 0 < z < 1.75 from the analysis of different spectroscopic surveys, among which SDSS luminous red galaxies Eisenstein et al. (2001), 2dF–SDSS luminous red galaxies Cannon et al. (2006), GDDS Abraham et al. (2004), and archival data Simon et al. (2005).

A second approach, introduced in Ref. Moresco et al. (2011) and then applied in Refs. Moresco et al. (2012); Moresco (2015); Moresco et al. (2016), instead of relying on the fit of the entire spectrum, relies on the analysis of a specific spectroscopic feature, the *D*4000, which is demonstrated to be linearly dependent on the age of the stellar population (at given metallicity, for the population considered). This approach was found to be particularly valuable since it allows to separate in the analysis the contribution coming from statistical and systematic effects, making it easier to model them. With this revised approach, 15 additional H(z) measurements in the redshift range 0.15 < z < 2 have been obtained by considering more than 140 000 CC from new independent SDSS catalogs (Data Release 6 main galaxy

sample, Data Release 7 luminous red galaxy sample, Data Release 9 BOSS sample), different spectroscopic surveys at higher redshifts (zCOSMOS, K20, UDS), and new archival data. Finally, a last approach only recently exploited in Ref. Borghi et al. (2022, 2021) relies on the estimate of dt based on the analysis of several independent spectroscopic features, the Lick indices, with which it is possible to determine the stellar age and metal content of CC. Within this context, analyzing the LEGA-C survey a new H(z) measurement at $z \sim 0.7$ has been derived.

The total covariance matrix for the CC approach, as presented in Refs. Moresco et al. (2020, 2022), can be expressed as the sum of a statistical and a systematic part, where, in turn, the systematic part is mainly composed by four terms:

$$\operatorname{Cov}_{ij} = \operatorname{Cov}_{ij}^{\text{stat}} + \operatorname{Cov}_{ij}^{\text{sys}} , \quad \operatorname{Cov}_{ij}^{\text{sys}} = \operatorname{Cov}_{ij}^{\text{met}} + \operatorname{Cov}_{ij}^{\text{sys}} + \operatorname{Cov}_{ij}^{\text{model}} + \operatorname{Cov}_{ij}^{\text{model}} .$$

$$(6)$$

The first term in the systematic error is related to the fact that in estimating the age of a stellar population, an uncertainty on the estimate of its metallicity might affect as a consequence the measurement of dt, and therefore the derived H(z). This factor was found to scale linearly with the uncertainty on the metallicity Moresco et al. (2020). The second term takes into account the possible uncertainty in the estimated SFH of CC; even if those tracers are expected to form on extremely short timescales, assuming the SFH as instantaneous is an nonphysical underestimate that might bias the results. Their SFH needs to be, therefore, properly accounted for, introducing an error \sim 2-3% Moresco et al. (2012). The third term includes in the analysis the possible effect that might be caused by a minor, but still non-negligible young stellar component below the otherwise old and passive population of a CC. In Ref. Moresco et al. (2018) it was estimated that a 10% contamination by a star-forming young component affects H(z) with a systematic error of 5%, and with a 0.5% error if it is of the order of 1%. For current measurements (Moresco et al., 2012; Moresco, 2015; Moresco et al., 2016; Borghi et al., 2022), this contribution has been found to be completely negligible due to the very stringent CC selection criteria implemented. Finally, the last term is, with the first one, the currently dominating one. The current uncertainty on galaxy spectral modelling has an impact on the estimate of the differential age dt, or on the calibration of observational proxies to the age, since different models have been proposed in the literature. This term introduces also non-diagonal terms in the covariance matrix, and can be further decomposed in many different ingredients, depending on the assumed initial mass function, on the stellar library adopted, and on the actual recipe of the model considered. It has been fully estimated in Ref. Moresco et al. (2020), obtaining errors depending on the model assumed of the order of \sim 4.5%

As discussed above, an extensive discussion about how to build a full covariance for CC is provided in Ref. Moresco et al. (2022). It is worth underlining that currently provided datasets include in the errors most of the error components but the systematic terms Cov_{ii}^{mod} ,

which need to be included following the indication provided in the reference.¹¹ It is worth recalling that the strict CC selection criterion and the differential approach helps to mitigate several other possible effects that might bias this kind of approach, such as, e.g., a possible dependence of the star formation rate on redshift or of the IMF on stellar mass (see Moresco et al. (2022)). Having selected CC as the most massive and passive galaxies ensures to minimize any SFH-dependent possible effect, since the estimated SF timescales for these objects is always very short by definition, and the differences dt are estimated in redshift intervals very close expressly to further minimize any residual effect. Likewise, the limited extension of the range of CC stellar masses, and the analysis further performed in even smaller bins, is designed to make the analysis extremely robust w.r.t. mass dependent effects (as shown, e.g., in Moresco et al. (2012); Borghi et al. (2021)).

While currently the main limitations of this method are the uncertainty on metallicity and models that at the moment dominate the error budget and the absence of dedicated surveys to properly map CC as a function of redshift (as, for example, for BAO and SNe), a path to improve these points in the future is clear. On one hand, better spectroscopic data (in terms of signal-to-noise ratio and resolution) that could be obtained by present and future instruments (X-Shooter, MOONS, etc.) could be crucial to better constrain the metal content of CC and to discriminate between the various models, significantly reducing the systematic error budget. On the other hand, future spectroscopic surveys will significantly increase the statistics of CCs in the redshift range 0.2 < z < 2, even if not directly being a target of the various mission Laureijs et al. (2011); Wang et al. (2019); Ahumada et al. (2020).

7. Cosmological models proposed to solve the H₀ and the S₈ tensions

Coordinators: Celia Escamilla-Rivera, Cristian Moreno-Pulido, Supriya Pan, M.M. Sheikh-Jabbari, and Luca Visinelli.

Contributors: Guillermo F. Abellán, Amin Aboubrahim, Özgür Akarsu, George Alestas, Daniel Aloni, Luis Anchordoqui, Ronaldo C. Batista, Micol Benetti, David Benisty, Asher Berlin, Thomas Buchert, David Camarena, Anton Chudaykin, Javier de Cruz Perez, Francis-Yan Cyr-Racine, Keith R. Dienes, Eleonora Di Valentino, Noemi Frusciante, Adrià Gómez-Valent, Asta Heinesen, Karsten Jedamzik, Raul Jimenez, Melissa Joseph, Lavrentios Kazantzidis, Michael Klasen, Suresh Kumar, Matteo Lucca, Valerio Marra, Laura Mersini-Houghton, Pran Nath, Florian Niedermann, Eoin Ó Colgáin, Leandros Perivolaropoulos, Levon Pogosian, Vivian Poulin, Joan Solà Peracaula, Emmanuel N. Saridakis, Martin Schmaltz, Nils Schöneberg, Martin S. Sloth, Brooks Thomas, Shao-Jiang Wang, Scott Watson, Neal Weiner.

7.1. Addressing the H_0 tension

Cosmological models addressing the H_0 tension are extremely difficult to concoct. Generally speaking, and maybe counter-intuitively, the reason for this relies in the extremely high precision with which the flat Λ CDM model is able to fit at the same time the multitude of data sets we dispose, ranging from BBN to BAO and LSS data. Indeed, despite the presence of the aforementioned tensions in the cosmological landscape, the minimal 6 parameter flat Λ CDM model is able to deliver a number of accurate predictions for a variety of different effects which impact both the expansion and thermal history of the Universe. Modifying the standard cosmological model without compromising its many successes explaining the current data has proven to be a rather difficult task.

¹¹ Note that a tutorial on how to estimate covariance matrix for CC is provided at https://gitlab.com/mmoresco/CC_covariance.

In the context of the Hubble tension, combined analyses of cosmological data yields strong bounds and restrictions on a wide class of models. Formulating the H_0 tension in a physically more meaningful setting in the H_0-r_s plane, where r_s is the sound horizon at recombination time, which is only affected by the early physics, it has been argued that the late-time solutions intrinsically struggle to solve the problem, favouring early-time solutions as the preferred option Bernal et al. (2016b); Poulin et al. (2018a); Aylor et al. (2019); Knox and Millea (2020); Arendse et al. (2020). A similar conclusion was reached by considering all low redshift data, including constraints from the age of Universe Krishnan et al. (2021b); Bernal et al. (2021); Vagnozzi et al. (2021d); Cai et al. (2022a,b). On the other hand, it has been argued that early resolutions typically exacerbate cosmic shear tension and that they do not provide a complete resolution Vagnozzi (2021); Jedamzik et al. (2021); Gómez-Valent et al. (2021); Lin et al. (2021). Moreover, it was argued that there might be a late-time variation of the Hubble parameter Wong et al. (2020); Krishnan et al. (2020), favouring a late-time solution over the early-time alternatives. At a more fundamental level, one can define a time dependent H_0 ("running Hubble parameter") within a given cosmology model, e.g. Λ CDM, and define a H_0 diagnostic to precisely mark departures from the given model Krishnan et al. (2021a). It has also been suggested that the Hubble tension may be a symptom (of the FLRW framework) and not the main malaise Krishnan et al. (2021b, 2022); Luongo et al. (2021).

The recipe for a successful extension of or modification to the ACDM model appears to be far from straightforward and in the past decade many possibilities have been considered in the literature, as we briefly review below. Given that we do not have fully settled theoretical and experimental understanding, the literature does not yet unambiguously converge on a new concordance model when all data and parameters are taken into account. See the review articles Buchert et al. (2016); Di Valentino et al. (2021g); Schöneberg et al. (2021b); Anchordoqui et al. (2021d); Perivolaropoulos and Skara (2021b); Clark et al. (2021b) and references therein for more detailed discussions.

The goal of this section is to systematically summarize the promising models that try to address the H_0 tension. We discuss their general features without elaborating the detailed analysis. For that, readers may refer to the original papers that we refer to in this section.

To make the comparison between proposed scenarios, we have divided them into two broad early-time and late-time proposals. The former affect the history of the Universe prior to recombination, while the latter after recombination. This allows us to generalize some of the common features, such as the ones mentioned at the beginning of this section, to a whole class of models focusing only on the model-specific features in the dedicated sub-sections. A brief summary of the models (in alphabetical order) we will consider is given below.

7.2. Addressing the S₈ tension

The tension in the S_8 parameter (or in the related σ_8 parameter) has added yet another question mark over the validity of the standard Λ CDM cosmology. Both theoretical and observational attempts have been made by various researchers to solve the S_8 tension. From the theoretical side, the approach consists in modifying the matter sector or the gravity sector of the ACDM model resulting in a plethora of alternative cosmological scenarios (we list them in the next subsections).¹² Even though, these models are successful in relieving the S₈ tension, they, in most situations, fail to provide satisfactory solutions when all the available cosmological probes are considered Di Valentino et al. (2021a,b,c,d). In particular, due to the specific correlation between H_0 and S_8 parameters, models solving S_8 tension usually exacerbate the H_0 tension and vice versa Ade et al. (2016c,a); de Haan et al. (2016). For example, late time transitions in the dark sector preferring a higher H_0 value, if they match the CMB data, prefer a lower value of Ω_m as well, to preserve the well measured value of $\Omega_m h^2$; this is known as the geometric degeneracy. This in turn, produces a modified distances to sources and of the sound horizon, modifies the growth of structures and CMB anisotropies Arendse et al. (2020), and usually results in higher σ_8 than for Λ CDM because of an extended era of matter domination. Similarly, early-time dark energy solutions of the H_0 tension increase σ_8 because they need a higher primordial curvature perturbation amplitude to offset the damping effect of the unclustered component. Therefore, because of the mutual effects and correlations, it is important to perform a conjoined analysis, i.e. fitting with a single model a full array of data Hill et al. (2020); Benevento et al. (2020); Knox and Millea (2020); Evslin et al. (2018), and not just one parameter alone. At the same time, if a model solves the S_8 tension (the z = 0 value), it is important to confirm that it is consistent with growth history (usually studied through parameter $f\sigma_8(z)$ as observed Linder (2017); Di Valentino et al. (2020a). Hence, any solution to the S₈ tension should pass other cosmological tests, i.e. it should simultaneously fit the expansion and growth histories probed by Baryon Acoustic Oscillations (BAO), RSD-lensing cross correlations, galaxy power spectrum shape, and void measurements Hamaus et al. (2020).

Moreover, the use of datasets is an additional key issue in this context since some of the non-CMB observations that are often used to estimate the values of S_8 or σ_8 also assume Λ CDM as the background cosmological model, similar to what *Planck* does and as a consequence the results might be biased. Thus, in order to find a proper solution to the S_8 tension in a specific cosmological model, one needs to match the estimated values of S_8 (or σ_8) from CMB observations and the low redshift probes such as weak gravitational lensing and galaxy clustering. Therefore, solving the S_8 tension is indeed one of the critical challenges for the Λ CDM cosmology given the fact it is related with large span observational probes to both background and perturbed Universe, and hence needs to be studied with great care. Among the variety of cosmological models (in alphabetical order) presented below, some of them have been proposed by many researchers to either alleviate or solve the S_8 tension

7.3. Addressing both the H_0 and S_8 tensions

Thus, looking for a cosmological model accommodating both the tensions is not a cup of tea. Nevertheless, curious minds never stop at any point and as a result it has been argued that in some extended cosmological models beyond Λ CDM, one can simultaneously tackle this problem Berezhiani et al. (2015); Di Valentino et al. (2020c,d); Kumar et al. (2019); Kumar (2021); Solà Peracaula et al. (2021); Akarsu

¹² Additionally to the models listed, there are many other proposals, and the interested reader can find more details in the corresponding papers Troxel et al. (2018b); Anand et al. (2017); Lambiase et al. (2019); Di Valentino and Bouchet (2016); Burenin (2018); Lin and Kilbinger (2018); Wang (2021); Graef et al. (2019).

et al. (2021); Yan et al. (2020b). However, even though we have a series of alternative possibilities beyond the standard Λ CDM model, we are still left with some vital issues that are usually overlooked while discussing the simultaneous solutions to both the tensions. When all the cosmological probes are taken into account, the models do not offer satisfactory solutions to both the tensions. In addition, the choice of the observational data is also a very important issue, since some of the non-CMB cosmological probes that are often used to estimate the value of the S_8 parameter also assume Λ CDM as the background cosmological model in a manner similar to Planck. This, as a consequence, may influence the estimations in S_8 and the conclusion towards the solution or alleviation of the S_8 tension has a high chance to be biased. As a result, finding a viable cosmological platform for the simultaneous solutions to both H_0 and S_8 tensions keeping all the constraints open, becomes very costly and challenging while this is incredibly exciting on the other hand. Below we shall present a number of cosmological scenarios (in alphabetical order) that have been proposed aiming to solve or alleviate the H_0 and S_8 tensions simultaneously.

7.4. Early-time alternative proposed models

7.4.1. Axion monodromy

The axion monodromy model can be an interesting candidate to alleviate the S_8 tension. This model is a realization of inflation Pimentel et al. (2022) in which pseudo-Nambu–Goldstone boson axions arise from symmetry breaking in the shift symmetry, also called the natural inflation Freese et al. (1990). The potential of the axion monodromy is Meerburg (2014)

$$V(\phi) = V_0(\phi) + \Lambda^4 \cos(\phi/f), \tag{7}$$

where ϕ is a canonically normalized scalar field and $V_0(\phi)$ denotes the slow-roll potential in the absence of modulations; Λ and f have the dimensions of mass. In Ref. Meerburg (2014), the model is confronted to a combination of data coming from *Planck* 2013 Ade et al. (2014a), ACT Das et al. (2014), SPT Keisler et al. (2011); Reichardt et al. (2012), BICEP2 Ade et al. (2014c) and low- ℓ WMAP polarization data from *Planck* Likelihood. As discussed in Ref. Meerburg (2014), within this context, the suppression of the matter power spectrum can lead to a lower value of S_8 and thus, this model can alleviate the S_8 tension as a result.

7.4.2. Early dark energy

Early dark energy (EDE) behaves like a cosmological constant for $z \ge 3000$ and decays away as radiation or faster at later times Karwal and Kamionkowski (2016); Poulin et al. (2019); Agrawal et al. (2019); Lin et al. (2019a). Related models include: (*i*) coupling of the EDE scalar to neutrinos Sakstein and Trodden (2020) and to dark matter Karwal et al. (2021); McDonough et al. (2021); (*ii*) a first-order phase transition in a dark sector before recombination, which leads to a short phase of (N)EDE (see later subsection) Niedermann and Sloth (2021a); (*iii*) an EDE model with an Anti-de Sitter phase around recombination Akarsu et al. (2020a); Ye and Piao (2020); Jiang and Piao (2021); Ye et al. (2021b); (*iv*) an evolving scalar field asymptotically oscillating or with a non-canonical kinetic term Agrawal et al. (2019); Lin et al. (2019a), (*v*) an axion-like particle sourcing dark radiation Berghaus and Karwal (2020), (*vi*) a scalar field with a potential inspired by ultra-light axions Smith et al. (2020b); Lucca (2020), (*vii*) an axion field tunnelling through a chain of energy metastable minima Freese and Winkler (2021), (*viii*) α -attractors Braglia et al. (2020b). EDEs with scaling solutions in the matter- and radiation-dominated eras (see Ref. Wetterich (1988); Copeland et al. (1998); Sabla and Caldwell (2021)) are not capable of relieving the H_0 tension in a significant way Pettorino et al. (2013); Gómez-Valent et al. (2021). For a more model-independent reconstruction of the EDE fraction see Ref. Gómez-Valent et al. (2021).

Let us briefly discuss the main results of the original EDE proposal resolving the Hubble tension Karwal and Kamionkowski (2016); Poulin et al. (2019); Smith et al. (2020b), its limitations Hill et al. (2020); Ivanov et al. (2020b); D'Amico et al. (2021); Murgia et al. (2021); Smith et al. (2021), and the recent hint for EDE in ACT data Hill et al. (2021); Poulin et al. (2021); Jiang and Piao (2022) (which is also consistent with SPT data La Posta et al. (2021); Smith et al. (2022); Jiang and Piao (2022)). The model proposes a new scalar field ϕ with a potential of the form

$$V(\theta) = m^2 f^2 \left(1 - \cos\theta\right)^n,\tag{8}$$

where *m* represents the axion mass, *f* the axion decay constant, and $\theta \equiv \phi/f$ is a re-normalized field variable defined such that $-\pi \leq \theta \leq \pi$.

At early times, Hubble friction ensures that the field is held fixed at its initial value until a critical redshift z_c (typically fixed when the approximate condition $9H^2(z_c) \leq |\partial^2 V(\theta)/\partial\theta^2|$ is met Marsh and Ferreira (2010); Smith et al. (2020b)). Subsequently, the field starts rolling down its potential and oscillates about the minimum. As a result, the field dilutes at a rate controlled by the exponent *n*, with an approximate equation of state (EoS) parameter w(n) = (n-1)/(n+1). This oscillatory behaviour can be captured through a cycle-averaged evolution of the background and perturbative field dynamics Poulin et al. (2018b, 2019) or followed exactly provided the oscillation period is not much faster than the Hubble rate Agrawal et al. (2019); Smith et al. (2020b); Hill et al. (2020).

To make the exploration of parameter space easier, most studies traded the "theory parameters" m and f for the "phenomenological parameters", namely the critical redshift z_c at which the field becomes dynamical and the fractional energy density $f_{\text{EDE}} \equiv f_{\text{EDE}}(z_c)$ contributed by the field at this redshift. Therefore, in full generality, the model has four free parameters: z_c , $f_{\text{EDE}}(z_c)$, w(n) (or the exponent n), and the initial field value θ_i which controls the effective sound speed c_s^2 and thus most of the dynamics of perturbations. Note, that most studies assume that the field always starts in a slow-roll regime, as enforced by the very high value of the Hubble rate at early times. It was also shown that data have little constraining power on n provided n > 1 (per construction- the fluid must dilute faster than matter) and $\lesssim 5$ (at 95% CL from *Planck* satellite data Agrawal et al. (2019); Smith et al. (2020b)), such that past works have often simply considered n = 3 to restrict the parameter space.¹³

¹³ Strictly speaking, there is some constraining power on the region 1 < n < 2 which disfavours values too close to n = 1 Agrawal et al. (2021).

The latest fit of this model to *Planck*, BAO, Pantheon, and SHOES data Murgia et al. (2021); Schöneberg et al. (2021b) indicates $f_{\text{EDE}}(z_c) \simeq 0.1 \pm 0.03$ with $z_c \simeq 4070^{+400}_{-840}$. Moreover, it was shown that *Planck* polarization data are very sensitive to the dynamics of perturbations in the EDE fluid, leading to a tight constraint on $\theta_i \simeq 2.6 \pm 0.3$, and therefore on the shape of the potential close to the initial field value. A pure power-law potential is indeed disfavoured by *Planck* satellite data Agrawal et al. (2019); Smith et al. (2020b). In this model, *Planck*+BAO+Pantheon and SH0ES are in agreement at ~ 1.6 σ .

Nevertheless, the combination of *Planck*+BAO+Pantheon data alone does not show signs of non-zero EDE contribution, resulting in an 95% CL upper limit on $f_{\text{EDE}} < 0.08$. This apparent contradiction is partially, but not entirely, driven by the highly non-Gaussian nature of the posteriors, with tails in the f_{EDE^-} and H_0 -posteriors extending to high values, in the EDE model with three free parameters. Indeed, in models where f_{EDE} is too small to be detected, any parameter combination $\{z_c, \theta_i\}$ leads to a cosmology identical to Λ CDM, which greatly enhances the Λ CDM-like volume of parameters. On the other hand, only a narrow region of $\{z_c, \theta_i\}$ values allow for the H_0 -degeneracy within CMB data to clearly appear. In fact, when the degrees of freedom are restricted to f_{EDE} only by fixing $z_c \simeq z_{\text{eq}}$ (where z_{eq} is the redshift at matter-radiation equality) and $\theta_i \simeq 2.8$, *Planck* data alone lead to a non-zero detection of EDE with $f_{\text{EDE}} \simeq 0.08 \pm 0.04$, the Hubble constant $H_0 \simeq (70 \pm 1.5) \,\text{km s}^{-1} \,\text{Mpc}^{-1}$, and $\Delta \chi^2 \simeq 6$ in favour of the EDE model Murgia et al. (2021); Smith et al. (2021). Although this somewhat naïve exercise illustrates that some features within *Planck* data are better fit by the EDE cosmology, the improvement in χ^2 is too mild to drive f_{EDE} away from zero when three EDE parameters are considered. See Ref. Herold et al. (2021) for a frequentist analysis along this line using a profile likelihood with three EDE parameters, which found $f_{\text{EDE}} \simeq 0.072 \pm 0.036$.

Recently, the EDE model has been confronted with ACT data leading to a (perhaps surprising) preference for EDE at ~ 2σ from ACT alone. Once combined with WMAP (or Planck TT at $\ell < 650$), BAO, and Pantheon data, the presence of EDE is favoured at 3σ , with $f_{\text{EDE}}(z_c) \simeq 0.16^{+0.05}_{-0.09}$ (note that posteriors are non-Gaussian) and $H_0 \simeq (73.4 \pm 3) \,\text{km s}^{-1} \,\text{Mpc}^{-1}$, without including any information from SHOES Hill et al. (2021); Poulin et al. (2021); Jiang and Piao (2022). The significance of the preference and the parameter estimation remain consistent with this picture even after the inclusion of SPT-3G La Posta et al. (2021); Smith et al. (2022) and Planck polarization data Poulin et al. (2021); Smith et al. (2022). However, the combination of the full Planck and ACT data leads instead to an upper limit $f_{\text{EDE}}(z_c) < 0.11$, which is weaker than what obtained from using Planck data alone. These somewhat contradicting results were shown to be due to the fact that the ACT best-fit EDE cosmology is disfavoured by high- ℓ Planck TT data because of an amplitude offset in the ACT TE power spectrum compared to that predicted by the best-fit model to Planck TT data, and a (mild) discrepancy between ACT and Planck high- ℓ TT data. For discussions about ACT and Planck statistical consistency, see Refs. Aiola et al. (2020); Handley and Lemos (2021).

The mismatch between ACT and *Planck* TT data on small angular scales gives rise to the different predictions of CMB lensing effect, see Sec. 6.1 for additional detail. For the full *Planck* data it leads to the so-called A_{lens} anomaly introduced in Sec. 6.1. It pulls the late-time amplitude to a higher value Aghanim et al. (2017) being in conflict with the LSS measurements. Since there is no physical justification behind this anomaly, it is warranted to consider alternative CMB measurements specifically on small scales Chudaykin et al. (2020a). Combining the large-scale *Planck* temperature, SPTPol polarization and lensing measurements along with the full-shape BOSS data and information from photometric LSS surveys one finds $H_0 \sim (69.8 \pm 1) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Chudaykin et al. (2021b). The inclusion of SH0ES result leads to $H_0 \sim (71.8 \pm 1.2) \text{ km s}^{-1} \text{ Mpc}^{-1}$ and does not substantially worsen the fit to the galaxy clustering and weak lensing measurements. An alternative strategy to deal with the *Planck* lensing anomaly is to marginalize over the lensing information in the *Planck* CMB power spectra. The lensing-marginalized *Planck* data favour non-zero f_{EDE} at the 2σ level Murgia et al. (2021). Compared to the EDE cosmology reconstructed from the full *Planck* data, the tensions with H_0 and S_8 have decreased by $\sim 1\sigma$ due to a shift in the mean of the reconstructed posterior in the unlensed cosmology.

There are a number of legitimate issues with the EDE model, that certainly indicate that this model cannot be the "end of the story". First, the degeneracy between f_{EDE} and H_0 only appears for somewhat tuned choices of parameters { z_c , θ_i }, with *Planck* and SH0ES data favouring in particular $z_c \simeq z_{\text{eq}}$ (although ACT suggests z_c closer to the recombination epoch Hill et al. (2021)). This is reminiscent of the coincidence problem for "late" dark energy, and could either be the indication of a fine-tuning issue Pettorino et al. (2013), or that a more complicated dynamics between the dark matter and dark energy sectors is at play. Second, the choice of potential itself, that assumes that lower-order terms in the axion-like potential do not play a role, requires some level of fine-tuning. Finally, in this model (as is true for most early Universe solutions), the DM density must be increased in order to compensate for the early integrated Sachs-Wolfe effect introduced by the gravitational potential decay for modes that enter the horizon when the field is dynamically important (i.e. around z_c) Hill et al. (2020); Vagnozzi (2021). This degeneracy between f_{EDE} and Ω_{DM} allows to essentially keep the peak heights as measured by *Planck* Poulin et al. (2019), through the early integrated Sachs-Wolfe effect Vagnozzi (2021). As a consequence, σ_8 increases (Ω_m is kept fixed in this model) worsening slightly the S_8 tension, typically by $\sim 0.5\sigma$ Poulin et al. (2019); Hill et al. (2020); Murgia et al. (2021). Moreover, it was shown that when BOSS data are analyzed using the effective field theory of large-scale structure, they can further constrain EDE because they break the aforementioned $f_{\text{EDE}} - \Omega_{\text{DM}}$ degeneracy Ivanov et al. (2020a); D'Amico et al. (2021b); Ivanov et al. (2020b).

Including both the BOSS full-shape and weak lensing S_8 data, Refs. Ivanov et al. (2020b); D'Amico et al. (2021b) have shown that the parameters of the early dark energy model addressing the Hubble tension are disfavoured at more than 99.95% confidence level in the standard Bayesian analysis. This result is obtained without imposing the SHOES prior on H_0 . However, if the S_8 data from at least DESy1 and HSC are excluded, and the EDE parameters { z_c , θ_i } are fixed instead of marginalizing, the early dark energy model is not disfavoured anymore Smith et al. (2021); Murgia et al. (2021). Besides, it has been shown that the BOSS results depend, in part, on a mismatch in the late-time clustering amplitude σ_8 between BOSS and Planck. Although the two agree at the 95% CL, this non-statistically significant mismatch still contributes to the σ_8 tension. These results suggests that further systematic studies of the EDE model in the context of the large-scale structure data are required.

Nevertheless, it is clear that LSS data have a potentially strong constraining power on the EDE cosmology (including future measurements of the halo mass function at high-redshift by the James Webb Space Telescope (JWST) Klypin et al. (2021)), and that the EDE cosmology cannot resolve the S_8 - and H_0 -tensions simultaneously.
7.4.3. Extra relativistic degrees of freedom

Extra relativistic degrees of freedom at recombination, parametrized by the number of equivalent light neutrino species $N_{\rm eff}$ Steigman et al. (1977), provide one of the simplest extensions of Λ CDM. For three active massless neutrino families, $N_{\text{eff}}^{\text{SM}} \simeq 3.044$ Mangano et al. (2005); de Salas and Pastor (2016); Akita and Yamaguchi (2020); Froustey et al. (2020); Bennett et al. (2021b). For the well-known degeneracy, we can increase H_0 at the price of additional radiation at recombination. Models of dark radiation can generically be classified into two distinct categories: (1) Free streaming radiation and (2) Self interacting Dark Radiation (SIDR). The canonical example of (1) features the addition of 3 superweakly-interacting right-handed (Dirac) neutrinos, which decouple around the QCD phase transition Anchordoqui and Goldberg (2012). This model can be framed within the context of intersecting D-brane models of vibrating strings, and the extra-gauge boson could be within reach of the LHC Run-3 Anchordoqui et al. (2013); Anchordoqui (2020). On the other hand, SIDR models are in local thermal equilibrium and behave as perfect fluids Baumann et al. (2016a); Brust et al. (2017); Blinov and Margues-Tavares (2020); Ghosh et al. (2021). Other generic examples that would enhance the value of N_{eff} include Majorana sterile neutrinos, Goldstone bosons, axions, vector fields, and neutrino asymmetry Jacques et al. (2013); Weinberg (2013); Allahverdi et al. (2014); Di Valentino et al. (2016b); Barenboim et al. (2017); Carneiro et al. (2019); Paul et al. (2019); Green et al. (2019); Ferreira and Notari (2018); D'Eramo et al. (2018); Anchordoqui and Perez Bergliaffa (2019); Gelmini et al. (2021); Di Valentino et al. (2016a); Poulin et al. (2018b); Baumann et al. (2016b); Zeng et al. (2019); Giarè et al. (2021); Seto and Toda (2021); Gu et al. (2021); Fernandez-Martinez et al. (2021); Franchino-Viñas and Mosquera (2021); Feng et al. (2022b); Cuesta et al. (2021). Future surveys will detect deviations from $N_{\text{eff}}^{\text{SM}}$ within $\Delta N_{\text{eff}} \lesssim 0.06$ at 95% CL, allowing us to probe a vast range of light relic models, where $\Delta N_{\text{eff}} = N_{\text{eff}} - N_{\text{eff}}^{\text{SM}}$ Abazajian et al. (2016, 2019a). However, high- ℓ polarization measurements of the CMB disfavour models involving enough additional radiation to substantially increase H_0 . More concretely, the correlation between H_0 and ΔN_{eff} has been estimated numerically using data from *Planck* 2018 TT,TE,EE + lowE + BAO + Pantheon,

$$\Delta H_0 = H_0 - H_0|_{\Lambda \text{CDM}} \simeq 5.9 \,\Delta N_{\text{eff}} \,,$$

(9)

where $H_0|_{\Lambda \text{CDM}} = (67.27 \pm 0.60) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Vagnozzi (2020); Anchordoqui (2021). Using the 95% CL bound $\Delta N_{\text{eff}} < 0.214$ reported by the *Planck* Collaboration Aghanim et al. (2020b), it is straightforward to see that the data disfavour a solution of the H_0 tension in terms of N_{eff} . Even when considering multi-parameter models, the number of extra relativistic degrees of freedom at recombination remains close to $N_{\text{eff}}^{\text{SM}}$ Anchordoqui et al. (2021d).

A special class of SIDR models are *stepped fluids* which were studied in Aloni et al. (2021). In such models the SIDR fluid consists of a mix of massless and at least one massive particles. When the temperature of the dark fluid drops below the mass of a massive particles species the dark radiation undergoes a "step" in which its relative energy density increases as the massive particles deposit their entropy into the lighter species. If this transition occurs while CMB-observable modes are inside the horizon, high- and low- ℓ peaks are impacted differently, corresponding to modes that enter the horizon before or after the step. Such dynamics already occurs in the simplest supersymmetric theory, the Wess-Zumino model with a trilinear interactions and soft supersymmetry breaking. In this model the scalar mass can naturally be near the eV-scale which would lead to CMB-observable effects. Ref. Aloni et al. (2021) investigates the cosmological signatures of such "Wess-Zumino Dark Radiation" (WZDR) and finds that it provides an improved fit to the CMB and BAO data alone, while favouring values of H_0 between 68-72 km s⁻¹ Mpc⁻¹ at 90% confidence. If supernovae measurements from the SHOES collaboration are also included in the analysis, the preferred values of H_0 become larger yet, but the preference for dark radiation and the location of the transition is left nearly unchanged. It was shown in Ref. Aloni et al. (2021) that WZDR is among the most successful models at resolving the H_0 tension and the best of those with a Lagrangian formulation.

Another model where extra relativistic degrees of freedom appear to alleviate the Hubble tension is the one proposed in Ref. Aboubrahim et al. (2022). This model involves a long-lived massive scalar which decays to a pseudo-scalar at late times. These along with a dark fermion and a dark photon make up the dark sector of a Stueckelberg extension of the SM. The dark sector which is feebly coupled to the SM via kinetic mixing is populated by energy injection from the visible sector. The feeble couplings forbid the dark particles from developing an equilibrium number density. This is a key feature which allows evading the constraint on $\Delta N_{\text{eff}}^{\text{BBN}}$. In this model the dark fermion is a DM candidate whose relic density is determined by solving a set of coupled Boltzmann equations for the comoving number density and taking into consideration the evolution of the visible and dark sectors in different heat baths Aboubrahim et al. (2021). After chemical and kinetic decoupling of the dark sector species, the massive scalar decays out of equilibrium into the massless pseudo-scalars increasing their energy density and contributing to $\Delta N_{\text{eff}}^{\text{CMB}}$ as needed to alleviate the tension between high *z* and low *z* measurements of the Hubble parameter. The analysis of Aboubrahim et al. (2022) provides a complete model of particle cosmology from very high temperatures down to the temperatures at CMB consistent with all astrophysical and laboratory constraints on the dark sector.

7.4.4. Modified recombination history

Shifting the sound horizon of baryonic acoustic oscillations has been shown to be a rather successful way of easing the Hubble tension. This can either be accomplished through a variation of the early time expansion history (see above), or through modifying the redshift of recombination. Solutions that modify the recombination history usually attempt to have an earlier recombination in order to infer a smaller sound horizon, which is compatible with a larger Hubble parameter. In particular, a route to explain the Hubble tension can be found by modifying the recombination history through heating processes Chiang and z. Slosar (2018), variation of fundamental constants (Hart and Chluba, 2018, 2020; Sekiguchi and Takahashi, 2021; Hart and Chluba, 2021), the effects of primordial magnetic fields Jedamzik and Pogosian (2020), or a non-standard CMB temperature-redshift relation Bose and Lombriser (2021).

The different proposed models have different mechanisms of accomplishing such a shift in recombination.

• The inclusion of a variation of the effective rest mass of an electron, for example, shifts the atomic energy levels of hydrogen in the early Universe, allowing for a larger energy gap between the various orbitals, which also increases the required photo-ionization temperature. As such, recombination will already be possible at higher temperatures and correspondingly higher redshift (earlier times), while also altering the reionization history. Similarly, adopting a non-standard CMB temperature-redshift relation allows for the

usual photo-ionization temperature to correspond to higher redshifts and thus earlier recombination. The model of baryon clumping (usually assumed to originate from a primordial magnetic field) instead allows recombination to be an inhomogeneous process. Given the non-linear dependence on the baryon abundance of the recombination problem, this allows for earlier recombination when $\langle n_b^2 \rangle \ge \langle n_b \rangle^2$.

Assessing the details of recombination against the *Planck* 2018 + BAO data, while allowing for a varying effective electron rest mass, increases the Hubble constant to $H_0 = (69.1 \pm 1.2) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Hart and Chluba (2020). Including additional curvature (as initially proposed in Ref. Sekiguchi and Takahashi (2021)) allows the model to reach $H_0 = (69.3 \pm 2.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Schöneberg et al. (2021b). Instead, When SNIa data are included, a similar analysis in the Λ CDM framework gives $H_0 = (68.7 \pm 1.2) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Sekiguchi and Takahashi (2021) in a flat Universe, and $H_0 = (72.3 \pm 2.7) \text{ km s}^{-1} \text{ Mpc}^{-1}$ in a curved Universe.

• Primordial magnetic fields (PMFs) have been studied for many decades as a possible ingredient needed for explaining the observed galactic, cluster and extragalactic fields (see Refs. Durrer and Neronov (2013); Subramanian (2016); Vachaspati (2021) for reviews). A PMF present in the plasma before and during recombination would leave a variety of imprints in the CMB Ade et al. (2016d). In particular, as first pointed out in Ref. Jedamzik and Abel (2013) and later confirmed by detailed magnetohydrodynamics (MHD) simulations Jedamzik and Saveliev (2019), the PMF induces baryon inhomogeneities (clumping) on scales below the photon mean free path, enhancing the process of recombination and making it complete at an earlier time. This lowers the sound horizon at last scattering, which helps to alleviate the Hubble tension Jedamzik and Pogosian (2020); Thiele et al. (2021); Rashkovetskyi et al. (2021) and, as a byproduct, also slightly relieves the σ_8 tension. The required PMF comoving strength is ~ 0.05 nG, which happens to be of the right order to naturally explain all the observed galactic, cluster and extragalactic fields.

Like all other solutions that reduce the sound horizon, baryon clumping is limited by how much it can increase the value of H_0 while remaining consistent with both CMB and BAO data Jedamzik et al. (2021). Current constraints on baryon clumping are based on a simple three-zone model first introduced in Ref. Jedamzik and Abel (2013), which contains one free parameter $b \equiv (\langle \rho_b^2 \rangle - \langle \rho_b \rangle^2)/\langle \rho_b \rangle^2$. The most up to date constraints on the $b + \Lambda$ CDM model are provided in Ref. Galli et al. (2022), where the CMB data from *Planck*, ACT DR4 Choi et al. (2020a) and SPT-3G Year 1 data Dutcher et al. (2021) was combined with the latest BAO, SN and distance ladder measurements. Constraints from ACT DR4 and *Planck* data were also presented earlier by Ref. Thiele et al. (2021). Interestingly, ACT and SPT were found to be in mild tension when it comes to *b*, with ACT tightening the *Planck* bound, i.e., tending to disfavour the PMF model, and SPT weakly preferring non-zero clumping. Combining the CMB data together with BAO and SNIa provides an upper limit of b < 0.4 at 95% CL (b < 0.5 without ACT). Adding a SH0ES-based prior on the Hubble constant gives $b = 0.31^{+0.11}_{-0.15}$ and $H_0 = 69.28 \pm 0.56$ km s⁻¹ Mpc⁻¹ ($b = 0.41^{+0.14}_{-0118}$ and $H_0 = 69.70 \pm 0.63$ km s⁻¹ Mpc⁻¹ without ACT). Further work is needed to clarify the potential (in)consistency of constraints on this model from various CMB data sets.

Future high resolution CMB temperature measurements, such as the full-survey Advanced ACT data Henderson et al. (2016), fullsurvey SPT-3G data Benson et al. (2014), Simons Observatory Ade et al. (2019), and CMB-S4 Abazajian et al. (2019a), along with better modelling of magnetically assisted recombination informed by comprehensive MHD simulations, should be able to conclusively confirm or rule out this proposal. Even if baryon clumping did not fully resolve the Hubble tension, a conclusive detection of evidence for a PMF would be a major discovery in its own right, opening a new observational window into the processes that happened in the very early Universe.

7.4.5. New early dark energy

While Early Dark Energy (EDE) Poulin et al. (2018b, 2019); Smith et al. (2020b) shows potential to resolve the Hubble tension, there are challenges at the theoretical level. The EDE potential can be motivated by higher order terms in the axion potential, but such a potential does not follow naturally from the effective field theory expansion and requires some fine-tuning for the lowest order terms in the potential not to dominate. In addition, it is disputed whether EDE leads to a full resolution of the Hubble tension at the phenomenological level Hill et al. (2020); Ivanov et al. (2020b); D'Amico et al. (2021); Gómez-Valent et al. (2021); Benisty et al. (2020a) as a tension remains with LSS, although not at a significantly higher level than in the ACDM model Murgia et al. (2021); Smith et al. (2021).

A promising way forward to resolve these theoretical and phenomenological issues with EDE is the "New Early Dark Energy" (NEDE) Niedermann and Sloth (2021a, 2020). Instead of a slow roll-over phase transition, leading to the aforementioned problems with EDE, it is natural to think that the dark sector instead has undergone an almost instantaneous *first order phase transition*.¹⁴ While this idea is different both at the theoretical and phenomenological level, it maintains the gist of the EDE proposal, and also holds in it the possibility of addressing its weaknesses.

At the background level, it is assumed that a NEDE phase transition took place in the dark sector at zero temperature shortly before recombination, triggered by a sub-dominant scalar field. Such a phase transition lowers an initially high value of the cosmological constant in the early Universe down to its present value as inferred from the measurement of H_0 , potentially resolving the Hubble tension in analogy with the motivation behind the EDE model.

However, similarities between EDE and NEDE end at the perturbation level. The initial condition for the NEDE fluid perturbations after the instantaneous transition are fixed by the covariant junction conditions Israel (1966); Deruelle and Mukhanov (1995) across the space-like transition surface, relating them to adiabatic perturbations of the sub-dominant trigger field. Subsequently, NEDE perturbations evolve in a semi-stiff fluid describing the collision phase of newly nucleated bubbles on large scales. At the perturbative level, the NEDE and the EDE models are therefore very different, which is also exhibited in fits to CMB and LSS data. This will enable future CMB and LSS experiments to further discriminate between the models. The two models also lead to different signatures of gravitational waves (GWs), which will be yet another testing avenue using pulsar timing arrays (compare Ref. Niedermann and Sloth (2020) and Weiner et al. (2021)).

Microscopically, the cold NEDE phase transition can be described by a scalar field whose potential at some critical point develops two non-degenerate minima at zero temperature. This evolution is caused by an additional subdominant trigger field, which at the right moment makes the tunnelling rate very high when the Hubble drag is released. When space becomes filled with bubbles of true vacuum during the phase transition, they will expand and almost instantaneously start to collide. As a part of the collision process the ψ conden-

¹⁴ An effectively instantaneous second order transition is also possible, which has been labeled a "hybrid NEDE model" Niedermann and Sloth (2020).

sate will start to decay. At the microscopic level, the released free energy is converted into small scale anisotropic stress, which sources GWs and is expected to decay as $1/a^6$ similar to a stiff fluid component. After the phase transition, the fluid is therefore effectively, on large scales, a mixture of a stiff fluid as well as scalar and gravitational radiation.

The fast decay of the anisotropic stress is key to the phenomenological success of NEDE. Setting the EoS parameter of the decaying NEDE fluid fixed at 2/3 and fitting the basic cold NEDE model with the fraction of NEDE energy density f_{NEDE} and the trigger mass m as two additional parameters to *Planck* 2018 temperature, lensing and polarization data, large and small-z BAO and LSS data (using the effective field theory of large-scale structure applied to BOSS/SDSS data D'Amico et al. (2020); lvanov et al. (2020c); Colas et al. (2020)), and the Pantheon data set, a preference of NEDE over Λ CDM was reported Niedermann and Sloth (2021b). The phase transition takes place at $z_c = 4900^{+660}_{-800}$ with the Hubble constant $H_0 = (71.2 \pm 1.0) \text{ km s}^{-1} \text{ Mpc}^{-1}$ and a non-vanishing NEDE fraction $f_{\text{NEDE}} = 11.7^{+3.3}_{-3.0}$ %, thus excluding $f_{\text{NEDE}} = 0$ at a $\simeq 4\sigma$ significance.

Notably, in a subsequent analysis, NEDE has been ranked high among other early-time competitors, bringing the DMAP tension¹⁵ below 2σ Schöneberg et al. (2021b). Beyond that, a direct comparison between EDE and NEDE models using ACT and *Planck* data is exemplifying the phenomenological differences between both models at a perturbation level Poulin et al. (2021), although it is not clear how much they are driven by internal tensions between both data sets Hill et al. (2021); Poulin et al. (2021); Moss et al. (2021).

While future CMB, LSS and pulsar timing array experiments can test this model more precisely, more theoretical developments will also be needed to fully resolve the S_8 tension if it turns out to become larger in future measurements Niedermann and Sloth (2021b). This may require to integrate the NEDE sector with other parts of the dark sector and/or the neutrino sector. As outlined in the conclusion of Ref. Niedermann and Sloth (2021b), a minimal resolution might already be present in the model's simplest implementation in terms of NEDE scalar field oscillations around the true vacuum, which constitute a form of interacting dark matter and hold the potential to resolve the S_8 tension Archidiacono et al. (2019); Allali et al. (2021).

As an alternative pathway, it was recently demonstrated that the NEDE phase transition can also be triggered by subsiding temperature corrections (rather than a scalar field) as the Universe expands Niedermann and Sloth (2021c, 2022). This model, dubbed *hot NEDE*, leads to a sizeable fraction of false vacuum energy – doubling as an early dark energy component – in the strongly supercooled region where the dark radiation fluid is subdominant. This phase transition can also give mass to the active neutrinos through the inverse seesaw mechanism Abada and Lucente (2014), when "higgsing" a set of (super)-eV sterile neutrinos. The coupling between the neutrino sector, the NEDE field and the Goldstone boson associated with a spontaneously broken lepton symmetry (the majoron) is expected to change the Boltzmann evolution of neutrinos at late times and provide novel decay channels for the bubble wall condensate. This offers an alternative way of addressing the H_0 and S_8 tension simultaneously. Ultimately, these recent developments of NEDE suggests the possibility that the Hubble tension could be a signature of how neutrinos acquired their mass. For other models building up on NEDE see also Refs. Freese and Winkler (2021); Allali et al. (2021).

We would like to point out, as done in D'Amico et al. (2021a), an interesting consequence of several models aimed at addressing the Hubble tension, in particular early dark energy models and NEDE (but also models with extra relativistic degrees of freedom). Fitting CMB data in terms of these models, a common feature is that the spectral index is bluer with respect to the Λ CDM value (see Di Valentino et al. (2018d); Ye and Piao (2020); Ye et al. (2021a); Tanin and Tenkanen (2021); Takahashi and Yin (2021)): such a shift of n_s will have very important implications for inflationary model constraints.

We illustrate this in Fig. 5, where we plot the contours obtained from the Λ CDM model, and the one we infer from the constraints on n_s in the NEDE model, from the analysis of Niedermann and Sloth (2021a, 2020). This plot clearly shows how many models of inflation such as flattened monodromy models with a long stage of inflation and power-law behaviour of, for example, $\sim \phi^{1/2}$ at large ϕ , which were supposedly excluded by having too large an n_s , may end up being better candidates than, for example, the Starobinsky R^2 . Of course, it is too soon to claim this. But until the H_0 tension is resolved, it may also be too soon to claim the opposite. Therefore, the solution to the (late-Universe) H_0 and S_8 tensions may have important consequences on our understanding of inflation.

7.5. Late-time alternative proposed models

7.5.1. Bulk viscous models

The cosmological scenarios in which a fluid is endowed with a bulk viscosity is an effective description to alleviate the Hubble constant tension Wang et al. (2017b); Yang et al. (2019c); da Silva and Silva (2021a). A bulk viscous fluid is characterized by its energy density ρ and pressure p where this pressure term has two distinct components, namely, $p = p_u + p_{vis}$. The first component of the pressure term p_u is the usual one $p_u = w\rho$, where w is the EoS parameter of the fluid, and the second component p_{vis} characterizes the viscosity of the fluid defined by $p_{vis} = -\xi(t)u^{\mu}_{;\mu}$ in which $\xi(t) > 0$ is the coefficient of the viscosity or the bulk viscous coefficient and u^{μ} is the four-velocity of the fluid Brevik and Gorbunova (2005).

For any bulk viscous fluid, one can write down its evolution in the FLRW Universe as

$$\frac{d\rho}{dt} + 3H(1+w)\rho = 9H^2\xi(t),$$
(10)

where *H* is the Hubble rate of the FLRW Universe. Thus, one can see that for different choices of the bulk viscous coefficient, $\xi(t)$, one can extract the constraints out of various cosmological scenarios. The cosmic fluid endowed by the bulk viscosity can either represent a DE fluid da Silva and Silva (2021a) or a unified fluid which combines both DM and DE behaviours Yang et al. (2019c). The cosmological scenarios in which DE enjoys a viscous nature have been investigated in the literature aiming to address the Hubble tension Wang et al. (2017c); Mostaghel et al. (2017, 2018); Velten and Schwarz (2012). The bulk viscosity coefficient characterized by $\xi(t) \propto H$ Wang et al. (2017c) leads to $H_0 = 69.3 \pm 1.7 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL for the dataset *Planck* 2018 CMB distance priors + Pantheon + BAO + BBN + CC da Silva and Silva (2021a). For the bulk viscosity coefficient $\xi(t) \propto \sqrt{\rho_{\text{DE}}}/H$ Mostaghel et al. (2017, 2018), the Hubble

¹⁵ This tension measure refers to "difference of the maximum a posteriori" as for example discussed in Raveri and Hu (2019). It is applicable in cases with non-Gaussian posterior.



Fig. 5. Tensor-to-scalar ratio *r* versus spectral index n_{s_1} for the Λ CDM model (blue) and for the NEDE model (gold). To get the NEDE model constraint, we approximate the Λ CDM contour as a bivariate Gaussian, and substitute the mean and error on n_s by the ones got in the NEDE model. This approximate procedure reproduces well a full analysis Ye et al. (2021a). The round dots are predictions of potentials $\sim \phi^p$ with $0.1 \le p \le 0.5$. The square dots are the predictions of the Starobinsky R^2 inflation Starobinsky (1980). This figure is from D'Amico et al. (2021a).

constant takes the value $H_0 = 69.3 \pm 1.7 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL for the combined dataset *Planck* 2018 CMB distance priors + Pantheon + BAO + BBN + CC da Silva and Silva (2021a). A different choice of the form $\xi(t) \propto \rho_{DE}^{\nu}$ Velten and Schwarz (2012) can lead to $H_0 = 69.2 \pm 1.7 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ at 68% CL da Silva and Silva (2021a) for *Planck* 2018 CMB distance priors + Pantheon + BAO + BBN + CC. As the choice of the bulk viscous coefficient is not unique, one can therefore introduce a different parametrization to investigate the effectiveness of the models in the light of the Hubble constant tension.

Alternatively, a unified fluid endowed with bulk viscosity can increase the Hubble constant value. In this context, the bulk viscous coefficient $\xi(t) \propto \rho^m$ (*m* is a real number) Velten and Schwarz (2012) leads to $H_0 = 70.2^{+1.6}_{-1.9} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Yang et al. (2019c) (assuming a free w_0 with m = 0) for the dataset *Planck* 2015 + Pantheon Yang et al. (2019c) and $H_0 = 68.0^{+2.7}_{-2.4} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL (assuming both w_0 and *m* are free parameters) for the dataset *Planck* 2015 + Pantheon Yang et al. (2019c).

On the other hand, an inhomogeneous cosmic fluid endowed with the bulk viscosity can also be considered as a possible scenario to alleviate the Hubble constant tension Elizalde et al. (2020). Using the Bayesian machine learning approach, the authors of Ref. Elizalde et al. (2020) investigated two equation of state parameters representing an inhomogeneous cosmic fluid, namely, Model 1: $p = (w_0 + w_1/(1 + z))\rho - AH^n (w_0, w_1, n, A)$ are free parameters) and Model 2: $p = (w_0 + w_1/(1 + z))\rho - AqH^n (w_0, w_1, n, A)$ are free parameters and $q \equiv -1 - \dot{H}/H^2$ is the deceleration parameter of the Universe). For Model 1, the Bayesian approach leads to $H_0 = 73.4 \pm 0.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL (for the redshift interval $z \in [0, 2.5]$) and $H_0 = 73.4 \pm 0.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL (for the redshift interval $z \in [0, 2.5]$) and $H_0 = 73.6 \pm 0.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL (for the redshift interval $z \in [0, 2.5]$) and $H_0 = 73.6 \pm 0.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL (for the redshift interval $z \in [0, 2.5]$).

7.5.2. Chameleon dark energy

The chameleon field Khoury and Weltman (2004a,b); Wang et al. (2012); Upadhye et al. (2012); Khoury (2013); Vagnozzi et al. (2021c); Benisty and Davis (2022) can be considered to be a potential candidate for resolving the Hubble constant tension as recently explored in Ref. Cai et al. (2021b). In addition to the screening effect from changing the effective mass of the chameleon field according to the ambient matter density, the chameleon field also admits a higher potential energy at its effective potential minimum (namely the vacuum energy) in the high-density regions than in the low-density regions. Hence, the over-densities would expand locally faster than the under-densities since there is more chameleon dark energy stored in the overdense regions. Therefore, the chameleon dark energy model Cai et al. (2021b) provides an environmentally dependent determination for the local Hubble constant. For a toy model with a top-hat density profile connecting an inner FLRW region to a outer FLRW region, a 10% matter over-density could raise the local H_0 value up to 70 km s⁻¹ Mpc⁻¹, while a 20% matter over-density could reach a local H_0 value as high as 74 km s⁻¹ Mpc⁻¹, which could be fitted precisely by the following approximation (here $n = 1, 2, 3, \cdots$ is the power of the Peebles-Ratra potential),

$$\frac{\delta\rho_m}{\rho_m} = \left(0.65\,e^{-0.57n} + 2.13\right) \left(\frac{H_0}{67.27\,\mathrm{km\,s^{-1}\,Mpc^{-1}}} - 1\right) + \left(0.65\,e^{-0.27n} + 1.07\right) \left(\frac{H_0}{67.27\,\mathrm{km\,s^{-1}\,Mpc^{-1}}} - 1\right)^2. \tag{11}$$

At large scales beyond $\gtrsim 1$ Gpc, the matter homogeneity is well tested by the CMB data, therefore, the Hubble constant inferred from this scale simply recovers the CMB constraint on H_0 . At the intermediate scales of a few $\sim O(100)$ Mpc, the matter homogeneity is relatively poorly guaranteed due to the presence of some large-scale structures like voids Keenan et al. (2013) and walls de Lapparent et al. (1986); Gott et al. (2005); Lietzen et al. (2016). Therefore, Ref. Cai et al. (2021b) also constructs a realistic model with a LTB metric to describe such intermediate inhomogeneities by explicitly counting the galaxy number excess from BOSS DR12 data Reid et al. (2016); Kitaura et al. (2016) in each concentric spherical shells, however, the outcome is highly dependent on the adopted galaxy bias model Lavaux et al. (2019). At even smaller scales below ~ 100 Mpc, the matter homogeneity is obviously broken by computing the fractal dimension of galaxy number growth within a sphere, see e.g. Ref. Scrimgeour et al. (2012). Using the distance indicators in the small-scale high-density regions (for example, SNIa in galaxies) would generally return back a higher H_0 value than the background. Similarly, calibrating the SNIa with



Fig. 6. Evolution of $\sigma_{8M}(z)$ for clustering and homogeneous DE models. For all models, $w_0 = -1$, $\Omega_m = 0.315$, and $\sigma_{8\Lambda} = 0.811$ have been used to normalize $\sigma_{8M}(z)$ at z_{rec} .

Cepheids Riess et al. (2016, 2018b,a, 2019, 2021a,b) generally renders a larger H_0 value than that with TRGB as the calibrator Freedman et al. (2019); Yuan et al. (2019); Freedman et al. (2020); Soltis et al. (2021); Freedman (2021); Anand et al. (2021). This is because that most of TRGBs are specifically chosen to reside away from high matter density (for example, galaxy disk) to reduce large dust extinctions. Furthermore, the most recent improved measurements of strong lensing time delay from TDCOSMO+SLACS sample Birrer et al. (2020) favours a H_0 value closer to the background CMB value, which could also be explained within the picture of chameleon dark energy model by lensing objects that are specifically chosen in the under-density regions in order to diminish the effect from galaxy clusters. Note in end that since the chameleon dark energy drives the over-density region to expand faster so that the matter fluctuations smear at a larger scale until reaching a new virial equilibrium with lower matter density. This could shed the light on resolving the S_8 tension at the same time, which would require for a full time evolution formulation at perturbation level.

7.5.3. Clustering dark energy

In clustering DE models, the sound speed of DE perturbations is much smaller than unity, allowing for non-negligible dark energy perturbations on scales well inside the horizon, see Ref. Batista (2021) for a review. Consequently, the growth of matter perturbations can be impacted by DE perturbations. Such models have been explored as a possible way to suppress σ_8 Kunz et al. (2015).

In the limit $c_s \rightarrow 0$, on small scales and during the matter-dominated era, DE perturbations follow matter perturbations according to the solution Abramo et al. (2009); Sapone et al. (2009); Creminelli et al. (2009)

$$\delta_{\rm DE} = \frac{1 + w_{DE}}{1 - 3w_{DE}} \delta_m \,. \tag{12}$$

Thus, the impact of clustering DE on σ_8 depends on the $1 + w_{DE}$. For non-phantom (phantom) models, DE perturbations are correlated (anti-correlated) to matter perturbations, enhancing (diminishing) σ_8 . If at intermediate redshifts the w_{DE} is not very close to -1, DE perturbations can be of the same order of magnitude as matter perturbations. In this case, the impact of DE on matter growth is maximal.

Since DE perturbations can also contribute significantly to the gravitational potential, the associated perturbations should include its weighted contribution

$$\delta_{\text{tot}} = \delta_m + \frac{\Omega_{\text{DE}}}{\Omega_m} \delta_{\text{DE}} \,. \tag{13}$$

The redshift evolution of σ_8 for a given model M, $\sigma_{8M}(z) = \sigma_{8M}D_M(z)$, where D_M is the growth function computed with δ_{tot} can be largely affected by clustering DE. Normalizing $\sigma_{8M}(z)$ to the Λ CDM value at z_{rec} , Fig. 6 shows the evolution of $\sigma_{8M}(z)$ for clustering and homogeneous DE models. Phantom clustering DE can potentially alleviate the S_8 tension, whereas the impact of non-clustering DE worsens it. But it is also possible that, for a given evolution of w_{DE} which provides a too low σ_8 , clustering non-phantom DE can be used to increase it.

7.5.4. Diffusion models

A diffusive interaction between dark energy and dark matter was introduced in Refs. Haba et al. (2016); Koutsoumbas et al. (2018). In Ref. Calogero and Velten (2013), the authors formulate diffusion of energy density between dark energy into dark matter by using a non-conserved stress energy tensor $T^{\mu\nu}$ with a source current j^{μ} ,

$$\nabla_{\mu}T^{\mu\nu}_{(\mathbf{M})} = \gamma^2 j^{\nu} \,, \tag{14}$$

where γ^2 is the coupling diffusion coefficient of the fluid. The current j^{μ} is a time-like covariant conserved vector field $j^{\mu}_{;\mu} = 0$ which describes the conservation of the number of particles in the system.

In a homogeneous expansion, the modified Friedman equations read:

$$\dot{\rho}_m + 3H\rho_m = \frac{\gamma}{a^3}, \quad \dot{\rho}_\Lambda = -\frac{\gamma}{a^3} \tag{15}$$

The contribution of the current goes as $\sim a^{-3}$ since the current is covariantly conserved $j^{\mu}_{;\mu} = 0$. In this way, there is a compensation between the dark energy and the dark matter. Ref. Perez et al. (2021) claims that the diffusive interaction models can alleviate the Hubble constant tension with different types of matter fields.

Refs. Benisty and Guendelman (2017a,b, 2018); Benisty et al. (2019) formulate an action principle for these interactions starting from actions. The theory reads:

$$S_{(\chi,A)} = \int d^4 x \sqrt{-g} \chi_{\mu;\nu} T^{\mu\nu}_{(\chi)} + \frac{\sigma}{2} \int d^4 x \sqrt{-g} (\chi_{\mu} + \partial_{\mu} A)^2$$
(16)

where A is a scalar field. From a variation with respect to the vector field χ_{μ} we obtain:

$$\nabla_{\nu}T^{\mu\nu}_{(\chi)} = \sigma(\chi^{\mu} + \partial^{\mu}A) = f^{\mu}, \tag{17}$$

where $f^{\mu} = \sigma(\chi^{\mu} + \partial^{\mu}A)$ is a current source for the stress energy momentum tensor $T^{\mu\nu}_{(\chi)}$. From the variation with respect to the new scalar *A*, a covariant conservation of the current emerges:

$$\nabla_{\mu}f^{\mu} = \nabla_{\mu}(\chi^{\mu} + \partial^{\mu}A) = 0 \tag{18}$$

Different expressions for $T^{\mu\nu}_{(\chi)}$ which depends on different variables give the conditions between the Dynamical Spacetime vector field χ_{μ} and the other variables. Cosmological implications are described in Ref. Benisty and Guendelman (2016, 2018a,b); Anagnostopoulos et al. (2019); Benisty et al. (2020b).

7.5.5. Dynamical dark energy

Dropping the field interpretation of DE, it is possible to explore models in which DE sector deviates from the cosmological constant to a DE fluid with an extended EoS parameter $w_{DE} \neq -1$, which can generally vary with redshift. These dynamical dark energy (DDE) models have been extensively studied in the literature Aghanim et al. (2020b); Zhao et al. (2017); Yang et al. (2019e,d); Di Valentino et al. (2020b); Yang et al. (2019e); Vagnozzi (2020); Keeley et al. (2019); Joudaki et al. (2017b); Di Valentino (2017); Yang et al. (2021b); Benisty and Staicova (2021b); Roy et al. (2022); Sharma et al. (2022), based on considerations over the reconstruction of the effective w_{DE} from data Zhao et al. (2017).¹⁶ DDE models typically solve the H_0 tension within two standard deviations at the price of a phantom-like DE, i.e. $w_{DE} < -1$, because of the geometrical degeneracy present with the DE EoS parameter w_{DE} . However, these models appear to worsen the growth tension of Λ CDM Alestas and Perivolaropoulos (2021), while providing a worse fit to the BAO and SNIa data than Λ CDM. In addition, they favour a value of SNIa absolute magnitude that is marginally consistent with Cepheid measurements Perivolaropoulos and Skara (2021b); Alestas and Perivolaropoulos (2021).

A particular Dynamical DE with a phantom crossing behaviour, as introduced in Ref. Di Valentino et al. (2021e), seems to be able to solve the Hubble constant problem also when BAO and Pantheon data are considered, and at the same time alleviate the S_8 tension, see also Ref. Chudaykin et al. (2022).

7.5.6. Emergent dark energy

A class of dark energy models in which dark energy has no effective presence in the past as it emerges at later times, usually dubbed as the *emergent dark energy* models Li and Shafieloo (2019); Pan et al. (2020c); Rezaei et al. (2020a); Liu and Miao (2020); Li and Shafieloo (2020); Yang et al. (2020c); Benaoum et al. (2020); Yang et al. (2021a), has received considerable attention in the cosmological community. In emergent dark energy models, the parametrization of the dark energy density is inserted into the Hubble equation as

$$H^{2}(z) = H_{0}^{2} \Big[\Omega_{r} (1+z)^{4} + \Omega_{m} (1+z)^{3} + \widetilde{\Omega}_{\text{DE}}(z) \Big],$$
(19)

where $\hat{\Omega}_{\text{DE}}(a) = \rho_{\text{DE}}(z)/\rho_{\text{crit},0}$ is the energy density of the DE fluid with respect to the critical energy density at present, namely $\rho_{\text{crit},0}(z) = 3M_{\text{Pl}}^2H_0^2$. In Ref. Li and Shafieloo (2019), the authors introduced a very simple emergent dark energy scenario, known as phenomenologically emergent dark energy (PEDE) scenario, where the dark energy sector evolves as

$$\widetilde{\Omega}_{\text{DE}}(z) = \Omega_{\text{DE}}\left[1 - \tanh(\log_{10}(1+z))\right],\tag{20}$$

where $\Omega_{\text{DE}} = 1 - \Omega_m - \Omega_r$. It is important to mention that within the PEDE scenario, even if the dark energy sector is dynamical, this scenario has exactly six free parameters as in the Λ CDM model. For *Planck* 2018 alone, this model takes a very high value of the Hubble constant $H_0 = 72.35_{-0.79}^{+0.78} \,\text{km s}^{-1} \,\text{Mpc}^{-1}$ at 68% CL Yang et al. (2020c) which is compatible with Ref. Riess et al. (2021a) within 1σ . Recently, in Ref. Di Valentino et al. (2021i), the PEDE model has been further confronted in the presence of the sterile neutrinos and perfectly agrees with the earlier observations Li and Shafieloo (2019); Pan et al. (2020c); Yang et al. (2020c).

A generalization of the PEDE scenario known as generalized emergent dark energy (GEDE) introduces a dark energy evolution in terms of a free parameter Δ as Li and Shafieloo (2020)

$$\widetilde{\Omega}_{\rm DE}(z) = \Omega_{\rm DE} \frac{1 - \tanh\left(\Delta \times \log_{10}(\frac{1+z}{1+z_t})\right)}{1 + \tanh\left(\Delta \times \log_{10}(1+z_t)\right)}.$$
(21)

While the symbol z_t is a derived parameter representing the epoch where the matter energy density and the DE density are equal, that means equating, $\rho_m(z_t) = \rho_{\text{DE}}(z_t) \implies \Omega_m(1+z_t)^3 = \widetilde{\Omega}_{\text{DE}}(z_t)$, one can derive z_t . Although this scenario does not offer a very large value of the Hubble constant compared with its value estimated in the PEDE scenario, however, as explored in Ref. Yang et al. (2021a), within this GEDE scenario, the Hubble constant tension is reduced to 1.8σ with Riess et al. (2021a) (see also Hernández-Almada et al. (2020)).

¹⁶ However, low redshift data do not necessitate DDE Colgáin et al. (2021).

7.5.7. Graduated dark energy - AdS to dS transition in the late Universe

The positive cosmological constant assumption of the Λ CDM model was investigated via the graduated dark energy (gDE)-borrowed from the proposal of graduated inflation Barrow (1990)-characterised by a minimal dynamical deviation from the null inertial mass density $\rho = 0$ (where $\rho \equiv \rho + p$) of the cosmological constant (or, the usual vacuum energy of QFT) Akarsu et al. (2020a). This deviation is in the form of

$$\varrho \propto \rho^{\lambda},$$
(22)

for which, provided that the conditions $\rho_0 > 0$ (present-day energy density), $\rho_0 < 0$ (present-day inertial mass density), and $\lambda = 1 - \frac{n}{m} < 1$ with *n* and *m* being odd numbers are satisfied, the energy density ρ dynamically takes negative values in the past Akarsu et al. (2020a) (see also Visinelli et al. (2019)). These three conditions lead to the gDE; the first two imply that gDE is in the phantom region in the late/present-day universe, and the last one causes the energy density to take negative values for redshifts larger than a certain redshift (see Ref. Akarsu et al. (2020a) for details). During the transition from negative to positive energy density as the Universe expands, there comes a time t_{\uparrow} (or a redshift z_{\uparrow}) for which the energy density passes through zero and the EoS parameter exhibits a pole. The gDE in fact exhibits a wide variety of behaviours depending on λ , but it is of particular interest that for large negative values of λ , it establishes a phenomenological model characterized by a smooth function that approximately describes a cosmological constant which switches sign in the late Universe to become positive today.¹⁷ The energy density of the gDE model, in terms of redshift, reads

$$\rho_{\text{gDE}} = \rho_{\text{gDE0}} \operatorname{sgn}[1 + \Psi \ln(1+z)] | 1 + \Psi \ln(1+z)|^{\frac{1}{1-\lambda}},$$
⁽²³⁾

where $\Psi < 0$ is a negative constant. Here "sgn" is the signum function that reads sgn[x] = -1, 0, 1 for x < 0, x = 0 and x > 0, respectively. This expression indicates if there exists a sign change in the energy density of the gDE (accompanied by a pole in its EoS parameter Ozulker (2022)), it will happen at the redshift

$$z_{\dagger} = e^{-\Psi^{-1}} - 1, \tag{24}$$

around which, H(z) can exhibit a non-monotonic behaviour. It was shown via the gDE that the joint observational data, including but not limited to the *Planck* CMB and Ly- α BAO (BOSS DR11) data, suggest that the cosmological constant changed its sign at $z \approx 2.32$ and triggered the late-time acceleration, the behaviour of which alleviates the H_0 tension by predicting $H_0 \approx 69.7 \pm 0.9 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ and provides excellent fit to the Ly- α BAO (BOSS DR11) data Blomqvist et al. (2019) at the effective redshift $z \sim 2.34$, which is at $\sim 2.5\sigma$ tension with the *Planck* 2015 best-fit Λ CDM. Note that this tension is reduced to $\sim 1.5\sigma$ when the final eBOSS (SDSS DR16) measurement, which combines all the data from eBOSS and BOSS Blomqvist et al. (2019); Alam et al. (2021a); du Mas des Bourboux et al. (2020), is considered, see Sec. 8.7.1.

Inspired by these observational findings, and the theoretically compelling fact that the gDE submits to the weak energy condition and the bounds on the speed of sound only in the limit $\lambda \to -\infty$ which corresponds to a cosmological constant that rapidly changes sign at redshift z_{\dagger} , this limit was dubbed Λ_s CDM and further investigated in Ref. Akarsu et al. (2021). The Λ_s CDM model can be constructed phenomenologically by simply replacing the usual cosmological constant (Λ) of the standard Λ CDM model with a cosmological constant (Λ_s) that switches its sign from negative to positive, and thus attains its present-day value ($\Lambda_{s0} > 0$), when the Universe reaches a certain energy scale (redshift z_{\dagger}) during its expansion,

$$\Lambda \rightarrow \Lambda_{\rm S} \equiv \Lambda_{\rm S0} \, {\rm sgn}[z_{\dagger} - z]. \tag{25}$$

It was shown in Ref. Akarsu et al. (2021) that, when the consistency of the Λ_s CDM model with the CMB data is guaranteed, (i) H_0 and M_B (SNIa absolute magnitude) values are inversely correlated with z_{\dagger} and reach $H_0 \approx 74.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $M_B \approx -19.2 \text{ mag}$ for $z_{\dagger} = 1.5$, in agreement with the measurements from SH0ES Riess et al. (2016, 2019), and (ii) H(z) presents an excellent fit to the Ly- α data provided that $z_{\dagger} \leq 2.34$. The assessment of the model against *Planck* 2018 yields $H_0 = 70.22 \pm 1.78 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and against *Planck* 2018 + SDSS DR16 yields $H_0 = 68.82 \pm 0.55 \text{ km s}^{-1} \text{ Mpc}^{-1}$ with $z_{\dagger} = 2.44 \pm 0.29$ Akarsu et al. (2021). It was found that the lower and upper limits of z_{\dagger} are controlled by the Galaxy and Ly- α BAO data, correspondingly, and the larger z_{\dagger} values imposed by the Galaxy BAO data prevent the model from achieving the largest estimations of H_0 from the direct local distance ladder measurements. It is intriguing that, as long as $z_{\dagger} \leq 2.34$, the model remains in excellent agreement with the Ly- α data even for $z_{\dagger} \sim 1.1$, which barely satisfies the condition that we live in an ever-expanding Universe; a good agreement with the Ly- α data is an intrinsic feature of the Λ_s CDM model as long as $z_{\dagger} \leq 2.34$.

Similar to the situation with the Ly- α data, alleviating the S_8 discrepancy, prevailing within the ACDM model and its minimal extensions, usually results in exacerbating the H_0 tension, see Sec. 5 and Ref. Di Valentino et al. (2021c). In addition to this, the constraints on S_8 based on the Ly- α data are in agreement with the weak lensing surveys that probe similar late-time redshift scales as the Ly- α measurements Palanque-Delabrouille et al. (2020). Accordingly, it is conceivable that the Λ_s CDM model provides a remedy for the S_8 discrepancy while retaining the better fit to the local measurements of H_0 , like in the case of the Ly- α discrepancy. Indeed, in the CMB-only analysis, it is found that $S_8 = 0.8071 \pm 0.0210$ for the Λ_s CDM model, whereas $S_8 = 0.8332 \pm 0.0163$ for the Λ CDM model. Although σ_8 is smaller for the Λ CDM model, its Ω_m value greater than 0.3 results in an increased S_8 value compared to its σ_8 value. In contrast, the Λ_s CDM model has an Ω_m value lower than 0.3 which results in a decreased S_8 value compared to its σ_8 value. This results in the lower value of S_8 for Λ_s CDM compared to Λ CDM. The Λ_s CDM and Λ CDM models have similar S_8 values when the BAO data are also included in the analysis; this is due to the preference for larger z_{\dagger} values by the Galaxy BAO data, since Λ_s CDM approaches Λ CDM for larger z_{\dagger} values and the Ω_m value of Λ_s CDM becomes greater than 0.3. Thus, the Λ_s CDM model partially reconciles the CMB data with the lower redshift cosmological probes regarding S_8 , and can potentially resolve the discrepancy in the absence of the Galaxy BAO data; however, for a robust conclusion, the constraints on S_8 from low redshift probes should also be explored within the Λ_s CDM model.

 $^{^{17}\,}$ The $\lambda=0$ case is called simple-gDE and investigated in Acquaviva et al. (2021).

Ultimately, it turns out via the Λ_s CDM model that sign switch in the cosmological constant, viz., transition from an Anti-de Sitter background (provided by $\Lambda < 0$) to a de Sitter one (provided by $\Lambda > 0$), at $z \sim 2$ (i) relaxes the SHOES H_0 tension while being fully consistent with the TRGB measurement, (ii) relaxes the M_B tension, (iii) removes the discrepancy with the Ly- α measurements, (iv) relaxes the S_8 tension, and (v) finds a better agreement with the BBN constraints on the physical baryon density Akarsu et al. (2021). These results seem to encourage looking for a phase transition from AdS vacua to dS vacua in the late-Universe.

It is reasonable to look for a potential origin of this phenomenon, viz. a very rapid single transition or its limiting case a single instantaneous (discontinuous) transition in the value of the cosmological constant, in a theory of fundamental physics by considering it as a first-order phase transition. The phase transition approach has been used to address the H_0 tension; see e.g. Refs. Banihashemi et al. (2020, 2019, 2021), which consider that the DE density resembles the magnetization of the Ising model and present a realization of this behaviour within the Ginzburg-Landau framework. Additionally, Ref. Farhang and Khosravi (2021) considers a gravitational phase transition that is justified from the effective field theory point of view (see also Ref. Khosravi and Farhang (2021)). The model studied in Ref. Banihashemi et al. (2020) partially corresponds to a one-parameter phenomenological extension of Λ_s CDM; it considers an arbitrary shift in the value of the cosmological constant, however, at very low redshifts, viz. $z_t = 0.092_{-0.062}^{+0.009}$, signalling that it could suffer from the M_B tension Camarena and Marra (2021); Efstathiou (2021) (see also Refs. Alestas et al. (2021b); Marra and Perivolaropoulos (2021); Alestas et al. (2021c) ans Sec. 7.6.5). Given the promising advantages of having a negative cosmological constant for $z \gtrsim 2$ in light of cosmological tensions, and that negative cosmological constant is a theoretical sweet spot–AdS space/vacuum is welcome due to the AdS/CFT correspondence Maldacena (1998) and is preferred by string theory and string theory motivated supergravities Bousso and Polchinski (2000)—it would be most natural to associate this phenomena with a possible phase transition from AdS to dS that is derived in string theory, string theory motivated supergravities, and theories that find motivation from them.

Besides, there is a rapidly growing literature on the cosmological models that suggest dark energy (as an actual source or an effective source from a modified theory of gravity) transitions in the late Universe from a negative (or vanishing) cosmological constant-like behaviour to a positive cosmological constant-like behaviour, accompanied by a pole in its EoS parameter. These models can relax the H_0 and S_8 tensions and/or the Ly- α discrepancy, and the cosmological data either prefer or are fully consistent with the presence of a negative cosmological constant at high redshifts and the presence of a negative cosmological constant accompanying quintessence/phantom dark energy, see e.g. Refs. Sahni et al. (2014); Poulin et al. (2018a); Wang et al. (2018a); Mörtsell and Dhawan (2018); Dutta Ruchika et al. (2020); Akarsu et al. (2019a); Bonilla et al. (2021a); Calderón et al. (2021); Linares Cedeño et al. (2021); Bag et al. (2021); Escamilla and Vázquez (2021); Sen et al. (2021).

7.5.8. Holographic dark energy

DE motivated from the Holographic principle Li (2004); Huang and Li (2005); Zhang et al. (2014b) is widely known as Holographic DE (HDE). The model has been intensively investigated for its ability to explain the late-time cosmic acceleration (see the review Wang et al. (2017a)). In the simplest (and original) HDE model, the DE density is given by

$$\rho_{\rm DE} = 3c^2 M_{\rm Pl}^2 L^{-2}, \qquad L = a(t) \int_t^\infty \frac{dt'}{a(t')}, \tag{26}$$

where *L* is the radius of the future event horizon of the Universe and *c* is the free parameter of the model. The holographic nature comes in the fact that L^{-2} appears in the dark energy density. In the simplest case therefore, such models have three parameters. There are many models based on variants of this theme which typically have more parameters (see Ref. Wang et al. (2017a) for a review). At late times when the DE is expected to dominate, the above HDE behaves like a cosmic fluid of EoS,

$$w_{\rm HDE} = -\frac{1}{3} - \frac{2}{3c}.$$
 (27)

So, for $c \ge 1$, $w_{\text{HDE}} \ge -1$. It has been argued that HDE can also alleviate the Hubble constant tension, see e.g. Refs. Guo et al. (2019); Dai et al. (2020) (see Ref. van Putten (2017) for an earlier realisation), but as discussed in Ref. Colgáin and Sheikh-Jabbari (2021b) this comes at the expense of violating the null energy condition, or having a turning point in H(z). There are many extensions of the previous holographic model following either the Tsallis non-extensive entropy Tsallis and Cirto (2013); Saridakis et al. (2018), the quantum-gravitational modified Barrow entropy Barrow (2020); Saridakis (2020), or the Kaniadakis relativistic entropy Kaniadakis (2002); Drepanou et al. (2021); Hernández-Almada et al. (2021c). It has been discussed that the Hubble constant tension can be alleviated with Tsallis holographic dark energy da Silva and Silva (2021b) or with Kaniadakis holographic dark energy Hernández-Almada et al. (2021b).

7.5.9. Interacting dark energy

A cosmological scenario in which dark matter (DM) and DE share interactions other than gravitational leads to various interesting features Amendola (2000); Chimento et al. (2003); Cai and Wang (2005); Barrow and Clifton (2006); Chen et al. (2009); Pettorino (2013); Pan et al. (2015); Kumar and Nunes (2016); Nunes et al. (2016a); Pan and Sharov (2017); Sharov et al. (2017); Di Valentino et al. (2017b); Kumar and Nunes (2017); Van De Bruck and Mifsud (2018); Yang et al. (2018b, 2017); Pan et al. (2018); Yang et al. (2019f, 2018c); Barros et al. (2019); Yang et al. (2018d,a, 2019a,b); Martinelli et al. (2019); Pan et al. (2020b); Di Valentino et al. (2020c); Teixeira et al. (2020); Di Valentino et al. (2020d); Teixeira et al. (2019); Pan et al. (2019b); Paliathanasis et al. (2019); Benevento et al. (2020); Gómez-Valent et al. (2020); van de Bruck and Teixeira (2020); Lucca and Hooper (2020); Yang et al. (2020d,h); Pan et al. (2020a); Yang et al. (2019i); Kumar (2021); Lucca (2021a). In Ref. Di Valentino et al. (2020c,d); Pan et al. (2019a); Yang et al. (2020h); Pan et al. (2020d); Kumar (2021); Nunes and Di Valentino (2021); Gariazzo et al. (2021; Guo et al. (2021), the authors have found that the IDE model can solve the tension with SH0ES within one standard deviation, leading to a preference for a non-zero DE-DM coupling at more than 5 standard deviations, while fixing the DE EoS to a cosmological constant. However, this category can be further extended into two classes Di Valentino et al.

(2020d): (*i*) models with $w_{\text{DE}} < -1$ in which energy flows from DE to DM, (*ii*) models with $w_{\text{DE}} > -1$ in which energy flows from DM to DE. Related models can be realized in string theory Agrawal et al. (2021); Anchordoqui et al. (2020, 2021a).

A phenomenological description allows for the interaction between DE and another component, i.e. DM, which leads to an *effective* phantom-like EoS for DE. In more detail, we assume that the densities of DM and DE do not evolve independently but through a "dark coupling" as Gavela et al. (2009)

$$\nabla_{\mu} T_{\text{DE}}^{\mu\nu} = -Q \, u_{\text{DM}}^{\nu}/a \,, \tag{28}$$

$$\nabla_{\mu} T_{\text{DM}}^{\mu\nu} = Q \, u_{\text{DM}}^{\nu}/a \,, \tag{29}$$

where $T_{\text{DE}}^{\mu\nu}$ and $T_{\text{DM}}^{\mu\nu}$ are the energy momentum tensors for DE and DM, respectively, while u_{DM}^{ν} is the DM four-velocity in the DM frame. The quantity Q describes the interaction rate between the two dark sectors, and we specialise it here as $Q = \xi H \rho_{\text{DE}}$, where ξ is a (negative) dimensionless parameter that regulates the flow of DM into DE and $H = \dot{a}/a$. The background evolves as

$$\dot{\rho}_{\rm DE} + 3H(1+w_{\rm DE})\rho_{\rm DE} = -\xi H\rho_{\rm DE}\,,\tag{30}$$

$$\dot{\rho}_{\rm DM} + 3H\rho_{\rm DM} = \xi H\rho_{\rm DE}\,,\tag{31}$$

$$H^2 = \frac{8\pi G_N}{3} \rho \,, \tag{32}$$

where w_{DE} parametrizes the EoS for the DE component and ρ is the total energy content of the Universe at a given time. The solution to Eq. (30) reads $\rho_{DE} \propto a^{-3(1+w_{eff})}$, where the effective EoS $w_{eff} = w_{DE} + \xi/3$ leads to a phantom-like EoS for $\xi < -3(1+w_{DE})$. The DM-DE coupling term Q impacts on the evolution of perturbations Valiviita et al. (2008); Gavela et al. (2009, 2010) and affects the observables in the CMB. In this view, the Λ CDM model augmented with the DM-DE coupling, or $\xi - \Lambda$ CDM model, can be constrained from the observations of the CMB modes. The $\xi - \Lambda$ CDM model is characterized by the usual six cosmological parameters of Λ CDM plus ξ , namely $(\Omega_b h^2, \Omega_{DM} h^2, \theta_s, A_s, n_s, \tau, \xi)$.

The observations used for constraining the model consist of various independent measurements:

- Measurements of the CMB temperature and polarization anisotropies, as well as their cross-correlations, from the *Planck* 2018 legacy data release (*Planck* TT,TE,EE+lowE) Aghanim et al. (2020b,d);
- Measurements of the CMB lensing power spectrum reconstructed from the CMB temperature four-point function Aghanim et al. (2020d);
- Measurements of the Baryon Acoustic Oscillation (BAO) from the 6dFGS Beutler et al. (2011), SDSS-MGS Ross et al. (2015), and BOSS DR12 Alam et al. (2021a, 2017) surveys;
- Measurements of the Type Ia Supernovae (SNIa) distance moduli from the Pantheon sample Scolnic et al. (2018).

A Monte Carlo analysis of the $\xi - \Lambda$ CDM model that accounts for the *Planck* data alone leads to the value of the Hubble constant $H_0 = 72.8^{+3.0}_{-1.5}$ km s⁻¹ Mpc⁻¹ at 68% CL, which is a significant shift in the central value of the Hubble constant with respect to what obtained within the Λ CDM model alone Di Valentino et al. (2020c). The value obtained is within 1 σ from the value $H_0 = (73.04 \pm 1.04)$ km s⁻¹ Mpc⁻¹ obtained from the observation of a sample of long-period Cepheids in the LMC by the Hubble Space Telescope Riess et al. (2021b), and can thus be referred to as a possible solution to the H_0 tension. Incidentally, the method predicts a non-zero DM-DE interaction, with the parameter $\xi = -0.54^{+0.12}_{-0.28}$ differing from zero by more than 4σ . When a joint analysis of the *Planck*+BAO or *Planck*+Pantheon datasets is considered, these results weaken and the tension with the HST results lies within the 3σ level. This mechanism is then not powerful enough to lead to a strong resolution to the H_0 tension.

Stepping away from phenomenological models, explicit examples of a DM-DE coupling can be built within models of supergravity. Of particular interest are models that admit a UV completion to a consistent theory of quantum gravity Addazi et al. (2021), based on satisfying a few key requirements that avoids such theories to lie in the swampland of inconsistent theories instead of in the string theory landscape of vacua Vafa (2005). Cosmological observations can come to hand in constraining swampland conjectures Akrami et al. (2019); Colgáin et al. (2019); Colgáin and Yavartanoo (2019); Kinney et al. (2019); Danielsson (2019); Anchordoqui et al. (2021b). Swampland conjectures generally make it difficult for fundamental theories based on compactification from extra dimensions to accommodate a period of accelerated cosmological expansion Montefalcone et al. (2020). Such a restriction can be avoided in models whose internal space is not conformally Ricci flat, as it is the case for the Salam-Sezgin model Anchordoqui et al. (2021a). Within this supergravity model, dark matter could acquire a mass term which depends on the value of the quintessence field, thus realizing an effective DM-DE coupling which addresses the H_0 tension Anchordoqui et al. (2020), in the so-called fading dark matter model Agrawal et al. (2021).

Apart from providing a valid solution to the H_0 tension, this class of cosmological models can also play an effective role in alleviating the S_8 tension.

For instance, one viable possibility to largely reduce the significance of the tension S_8 is to allow for DE-DM interactions in a scenario where the DE energy density can be transferred to the DM fluid via a coupling function proportional to the DE energy density itself (unlike the model able to address the H_0 tension, where the energy transfer is from the DM to the DE) Di Valentino et al. (2020d); Lucca (2021b) (see also Di Valentino et al. (2020c); Kumar et al. (2019); Kumar (2021). Indeed, in this scenario, because of the additional energy flow from the DE to the DM over the cosmic history, a lower DM energy density with respect to the Λ CDM model is allowed at recombination without a sizable effect on the shape of the CMB anisotropy power spectra. As a consequence, the redshift of matter-radiation equality decreases and since the peak of the matter power spectrum and its amplitude depend on this redshift, it follows that the whole matter power spectrum shits horizontally to larger scales and vertically to lower values (see Ref. Lucca (2021b) and Fig. 1 therein for a more detailed discussion about this mechanism). As a result, after the inclusion of data from *Planck* 2018, BAO and Pantheon the model reduces the significance of the tension below the 2.5σ level even for very discordant estimates. The addition of late-time data from weak-lensing surveys such as DES and KV450 further improves the concordance between early and late-time probes, without exacerbating the H_0 tension nor the overall fit to the data (feature also present when excluding late-time measurements).

Other possible DE-DM interaction scenarios involve for instance elastic interactions between the two fluids that only produce a momentum exchange Pourtsidou and Tram (2016); Amendola and Tsujikawa (2020); Jiménez et al. (2021). In this scenarios, as is common in models where the DM has such interaction channels with other particles, the additional drag effect prevents the DM component from clustering, which results in a suppression of the matter power spectrum at relatively small scales. By comparing this model to data from *Planck* 2018, BAO and Pantheon one obtains that the mean value of the σ_8 parameter does not change with respect to the Λ CDM equivalent but the error bars are enlarged to the point where the tension largely disappears. The inclusion of late-time measurements such as from the *Planck* SZ cluster counts can then pick up the values of the distributions that bring the datasets in agreement, resulting in a clear detection of the interaction parameter, see Fig. 6 of Ref. Jiménez et al. (2021).

Finally, another possibility is an IDE model with a sign-changing interaction, as in Ref. Pan et al. (2019b).

Note that in this Section the DM component enters only in relation to its interaction with DE. Models in which the interaction of DM with either the visible or other dark sectors affects the cosmological evolution are discussed below in Secs. 7.7.2 (cannibal DM), 7.7.15 and 7.7.3 (decaying DM models), 7.7.4 (dynamical DM), and 7.7.7 (interacting DM).

7.5.10. Quintessence models and their various extensions

The present accelerating expansion rate of the Universe can be brought forth by the presence of a light scalar field known as quintessence. The simplest of such models consists of minimally coupled scalar fields with a flat enough potential which, contrary to a cosmological constant, leads to a dynamical EoS parameter, $w_{DE} \neq -1$ Ratra and Peebles (1988); Caldwell et al. (1998), see also Refs. Zlatev et al. (1999); Peebles and Ratra (2003); Copeland et al. (2006); Tsujikawa (2013) for early reviews. The model building of quintessence fields as DE models with a field theory backend has recently featured extensively through string theory swampland conjectures Agrawal et al. (2018); Palti (2019). Various extensions of the simple quintessence models such as coupled quintessence, in which DE sector couples to (dark) matter sector Amendola (2000); Agrawal et al. (2021); Gómez-Valent et al. (2020) or non-minimal derivative Saridakis and Sushkov (2010) couplings, and many other extensions Frieman et al. (1995); Choi (2000); Nomura et al. (2000); Visinelli and Vagnozzi (2019); Choi et al. (2021); Akrami et al. (2018, 2021a,b); Eskilt et al. (2022) have been analysed. As quintessence models generally lead to $w_{DE} > -1$ and exacerbate the Hubble constant tension Vagnozzi (2020); Banerjee et al. (2021b), these are generally not viable DE models. More generally, DE models with $w_{DE} > -1$ can be shown to be at odds with H_0 and S_8 tension Heisenberg et al. (2022a,b); Lee et al. (2022).

7.5.11. Running vacuum models

The persisting tensions between the Λ CDM and some cosmological data (cf. Secs. 4 and 5) suggest that the rigid cosmological constant, Λ , might be performing insufficiently at the observational level. It is tempting to check if we could alleviate some of these problems on assuming that the dark (or just vacuum) energy density might be (slowly) dynamical. A related option is to assume that the gravitational coupling G_N can be mildly time-evolving. These possibilities may occur at a time or individually, but each has different implications on the local conservation laws. Rather than introducing some *ad hoc* phenomenological dependence of Λ and G_N as a function, say, of the cosmic time, we would like to have some more fundamental motivation for such a dependence. The Running Vacuum Model (RVM), see Refs. Solà (2013); Solà and Gómez-Valent (2015) and references therein, may provide such a fundamental dynamics, emanating either from quantum field theory (QFT) or string theory. The RVM can implement any of the mentioned options and is characterized by a vacuum energy density, ρ_{vac} , which at the background level carries a mild dependence on the expansion rate and its time derivative. The relevant structure of the RVM for the current Universe reads as follows:

$$\rho_{\rm vac}(H,\dot{H}) = \frac{3}{8\pi G_N} (c_0 + \nu H^2 + \tilde{\nu}\dot{H}) + \mathcal{O}(H^4),$$
(33)

with $v, \tilde{v} \leq \mathcal{O}(10^{-3})$, G_N the local value of Newton's constant, and the additive constant c_0 is fixed by the boundary condition $\rho_{vac}(H_0) = \rho_{vac}^0$ (current value). The RVM at low energies has been tested repeatedly (and successfully) in the past, see e.g. Refs. Solà et al. (2015, 2017a,b); Solà Peracaula et al. (2018a,b,b, 2019a); Gómez-Valent and Solà (2017); Gómez-Valent and Solà Peracaula (2018); Banerjee et al. (2021a). The state-of-the-art phenomenological performance of the RVM has been presented in a recent study Solà Peracaula et al. (2021). The $\mathcal{O}(H^4)$ terms in Eq. (33) can only be important for the very early Universe as they can trigger inflation, but we shall not address the implications for the early Universe here (see Refs. Solà (2013); Lima et al. (2013); Solà and Gómez-Valent (2015); Solà (2015a); Peracaula and Yu (2020) and references therein).

Theoretically, the structure of the RVM can be motivated from different perspectives, to wit: from the renormalization group in curved space-time Shapiro and Sola (2002); Solà (2008); Shapiro and Solà (2009), from scalar-tensor theories such as the Brans-Dicke theory of gravity with a non-vanishing Λ Solà Peracaula (2018); de Cruz Pérez and Solà Peracaula (2018); Solà Peracaula et al. (2019b, 2020); Singh and Solà Peracaula (2021), see Sec. 7.6.3.4, and also from QFT in curved space-time using adiabatic regularization and renormalization techniques Moreno-Pulido and Solà Peracaula (2020, 2022). In addition, beyond the QFT approach, there recently exists an intriguing "stringy" version of the RVM, which is based on the effective action of the bosonic part of the gravitational supermultiplet in string theory, see Ref. Mavromatos and Solà Peracaula (2021) and references therein. At low energies, the stringy version makes the important prediction that DM should be axion-like but otherwise it behaves as the standard RVM. This means that the DE associated to the RVM is in both cases dynamical through a $\sim \nu H^2$ component (with $|\nu| \ll 1$). In contrast, at high energies the stringy version nicely connects inflation with the physics of the primordial GWs, see Ref. Mavromatos and Solà Peracaula (2021) for a comprehensive exposition and Ref. Mavromatos and Sola (2021) for new developments in this direction.

The phenomenological performance of the RVM has last been discussed using the most up-to-date dataset available in Ref. Solà Peracaula et al. (2021), under the assumption $\tilde{\nu} = \nu/2$. Neglecting the higher order terms, which are only relevant during inflation, Eq. (33) takes the form

$$\rho_{\rm vac}(R) = \frac{3}{8\pi G_N} \left(c_0 + \frac{\nu}{12} R \right) \,, \tag{34}$$



Fig. 7. Left panel: Theoretical curves of $f(z)\sigma_8(z)$ for the Λ CDM and type-I RRVM with and without threshold redshift z_* , together with the data points employed in the analysis of Ref. Solà Peracaula et al. (2021); Right plot: 1σ and 2σ CL regions in the (σ_8 – H_0)-plane. H_0 is expressed in units of km s⁻¹ Mpc⁻¹. See also Fig. 10 in Sec. 7.6.3.4, and the numerical tables in Ref. Solà Peracaula et al. (2021).

where R is the Ricci scalar. For this reason, we may call this form of the vacuum energy density (VED) the Ricci RVM, or just "RRVM".

This implementation has the double advantage of using one single parameter and provides a safe path to the early epochs of the cosmological evolution. In fact, when we approach the radiation dominated era we have $R/H^2 \ll 1$ and, hence, the impact of the running is highly suppressed in that epoch. We may consider two types of RRVM scenarios Solà Peracaula et al. (2021): type-I, in which the vacuum interacts with matter; and type-II, where matter is conserved at the expense of an exchange between the vacuum and a mildly evolving gravitational coupling G(H). For type-I models we assume that the vacuum ("vac") exchanges energy with CDM only: $\dot{\rho}_{CDM} + 3H\rho_{CDM} = -\dot{\rho}_{vac}$. Solving for the CDM and vacuum energy densities in terms of the scale factor *a* yields

$$\rho_m(a) = \rho_m^0 a^{-3\xi}, \qquad \rho_{\rm vac}(a) = \rho_{\rm vac}^0 + \left(\frac{1}{\xi} - 1\right) \rho_m^0 \left(a^{-3\xi} - 1\right), \tag{35}$$

where $\xi \equiv \frac{1-\nu}{1-\frac{3}{4}\nu}$ and $\rho_m = \rho_{\text{CDM}} + \rho_b$ (i.e. includes the densities of CDM and baryons). As expected, for $\xi = 1$ ($\nu = 0$) we recover the Λ CDM. For type-I models we admit also the possibility that the dynamics of vacuum is activated only very recently, namely at a threshold redshift $z_* \simeq 1$, so that $\rho_{\text{vac}}(z) = \text{const.}$ for $z > z_*$. This possibility has been deemed plausible in the literature, see e.g. Ref. Martinelli et al. (2019). We compare this option with the situation when there is no such threshold, see Fig. 7. As for type-II models, matter is conserved, but the vacuum can still evolve as long as the effective gravitational coupling also evolves with the expansion $G_{\text{eff}} = G_{\text{eff}}(H)$, starting from an initial value (which enters our fit). The approximate behaviour of the VED for this model in the late-time Universe is:

$$\rho_{\text{vac}}(a) = \frac{3c_0}{8\pi G_N} (1+4\nu) + \nu \rho_m^0 a^{-3} + \mathcal{O}(\nu^2) \,. \tag{36}$$

The effective gravitational coupling evolves very mildly as $G_{\text{eff}}(a) \propto (1 + \epsilon \ln a)$ in the current epoch (with $0 < \epsilon \ll 1$ of order ν). The vacuum dynamics has also an important impact on the large scale structure (LSS) through the $f\sigma_8$ data. For a list of the main equations at the linear perturbation level, see Ref. Solà Peracaula et al. (2021).

To compare the RRVM's with the Λ CDM, we have defined a joint likelihood function \mathcal{L} , where the total χ^2 to be minimized in our case is given by $\chi_{tot}^2 = \chi_{SNIa}^2 + \chi_{BAO}^2 + \chi_H^2 + \chi_{CMB}^2 + \chi_{CMB}^2$. In particular, the χ_H^2 part may contain or not the local H_0 value measured by the SHOES team, but here we only present the results obtained by including it. Fig. 7 shows that the effect of the redshift threshold z_* in type-I RRVM can be very important and suggests that a mild dynamics of the vacuum is welcome, especially if it gets activated at around the epoch when the vacuum dominance appears, namely at $z \simeq 1$. Unfortunately, type-I models without such a threshold do not help to solve the tensions since the values of H_0 and σ_8 remain very close to the CMB values Solà Peracaula et al. (2021). Nevertheless, this might not be a problem if the current expansion is slower than measured by SH0ES, as suggested e.g. in Refs. Freedman (2021); Mortsell et al. (2021a); Gómez-Valent and Amendola (2018); Haridasu et al. (2018). In stark contrast, Fig. 10 shows that type-I models (specifically $H_0 = 70.93_{-0.87}^{+0.93}$ km s⁻¹ Mpc⁻¹ Solà Peracaula et al. (2021)) along with σ_8 and S_8 values in the needed moderate range ($\sigma_8 = 0.794_{-0.012}^{+0.013}$ and $S_8 = 0.761_{-0.017}^{+0.018}$) Solà Peracaula et al. (2021). The values of S_8 in all RRVM's are perfectly compatible with recent weak lensing and galaxy clustering measurements (cf. Ref. Solà Peracaula et al. (2021) and Sec. 5.1). The net outcome of this analysis is that of the two RRVM's considered, only the type-I models are capable of alleviating the two tensions (H_0 and σ_8), whereas the type-I models with the start of the result of the result of alleviating the two tensions (H_0 and σ_8), whereas the type-I models with analysis (which are more model-independent) also favour the RVM option as compared to other models of the dark energy Rezaei et al. (2022).

7.5.12. Time-varying gravitational constant

Seminal work of Weinberg suggests that an effective quantum theory of gravity would be asymptotically safe, with the renormalization group equations possessing a fixed point Weinberg (1978, 2010). A consequence of this framework is an extension of the Λ CDM model in which Newton's gravitational constant G_N could depend on time Xue (2015); Bégué et al. (2019). In more detail, in this model the gravitational coupling is a function that varies with redshift z as $G_N(z) = G_{N,0}(1 + z)^{-\delta_G}$, such that $G_N(z = 0) \equiv G_{N,0}$ is the value today, the suffix "0" refers to the present time values, and δ_G parametrizes the change in the gravitational constant. As a consequence, the cosmological constant would also be redshift-dependent and follows a scaling law, $\Lambda(z) = \Lambda_0(1 + z)^{\delta_{\Lambda}}$. The matter "m" and radiation "r" contents would satisfy the scaling relations

$$(G_N/G_{N,0})\,\rho_m = \rho_{m,0}\,(1+z)^{3(1+w_m)-\delta_G}\,,\tag{37}$$

$$(G_N/G_{N,0})\rho_r = \rho_{r,0} \left(1+z\right)^{3(1+w_r)-\delta_G},$$
(38)

$$(G_N/G_{N,0})\,\rho_{\Delta} = \rho_{\Delta,0}\,(1+z)^{\delta_{\Lambda}}\,.$$
(39)

The requirement for a flat Universe leads to the relation

$$\delta_{\Lambda} = \delta_G \, \frac{\rho_{r,0} + \rho_{m,0}}{\rho_{\Lambda,0}} \,. \tag{40}$$

The assessment of the model against cosmological data is performed in Ref. Gao et al. (2021). In particular, two realizations of this model are considered, namely the $\tilde{\Lambda}$ CDM model in which Eq. (40) is enforced, and the e $\tilde{\Lambda}$ CDM model in which δ_G and δ_{Λ} are kept as independent parameters. Both models cannot ease the tension in the Hubble constant when using an analysis that uses the combination of *Planck* 18 TT,TE,EE+lowE+lensing data Aghanim et al. (2020b) plus BAO plus data from SN1e Pantheon compilation Scolnic et al. (2018). The tension is reduced when the measurement of H_0 by the SH0ES team is used as a Gaussian prior. Recently, it has been speculated that the Hubble tension could be resolved within the stochastic quantization formalism of gravity Lulli et al. (2021), although more work is required along this direction.

Other approaches considering varying gravitational constant are analysed in Sakr and Sapone (2021), that considering G_N as a free parameter, and in Maeda and Panpanich (2022) in the context of a cuscuta-galileon gravity theory. Finally, Ref. Benevento et al. (2022) implements a sharp transition in the value of the effective gravitational constant prior recombination, effectively lowering the sound horizon at CMB last scattering and addressing both the H_0 and the S_8 tensions. Assessing the model against *Planck* 2018 TT,TE,EE + LowE and BAO data, the value inferred for the Hubble constant is $H_0 = 69.22^{+0.67}_{-0.86} \text{ km s}^{-1} \text{ Mpc}^{-1}$ Benevento et al. (2022).

7.5.13. Vacuum metamorphosis

The Vacuum Metamorphosis (VM) model is motivated by the fact that quantum gravitational effects Parker and Vanzella (2004); Parker and Raval (2000); Caldwell et al. (2006) can significantly increase the Hubble constant value leading to a solution for the Hubble tension Di Valentino et al. (2018c, 2020a, 2021h,i). This model is a first principles theory based on a late-time gravitational phase transition that takes place when the Ricci scalar curvature *R* is of the order of the squared mass of the scalar field, m^2 , and is related to the matter density today, Ω_m . For this reason, the VM model has the same number of degrees of freedom as the Λ CDM scenario.

The expansion rate before and after the phase transition result in Di Valentino et al. (2020a):

$$\frac{H^{2}(z)}{H_{0}^{2}} = \begin{cases} \Omega_{m}(1+z)^{3} + \Omega_{r}(1+z)^{4} + \Omega_{k}(1+z)^{2} - M \left\{ 1 - \left[3\left(\frac{4}{3\Omega_{m}}\right)^{4}M(1-M-\Omega_{k}-\Omega_{r})^{3} \right]^{-1} \right\}, & \text{for } z > z_{t}^{\text{ph}}, \\ (1-M-\Omega_{k})(1+z)^{4} + \Omega_{k}(1+z)^{2} + M & \text{for } z \le z_{t}^{\text{ph}}, \end{cases}$$
(41)

with $M = m^2/(12H_0^2)$, $\Omega_k = -k/H_0^2$, and the redshift of the phase transition

$$z_t^{\rm ph} = -1 + \frac{3\Omega_m}{4(1 - M - \Omega_k - \Omega_r)} \,. \tag{42}$$

In other words, after the phase transition the Universe effectively has a radiation component that rapidly redshifts away leaving the Universe in a de Sitter phase, and therefore it is not nested with the Λ CDM scenario.

In the original Vacuum Metamorphosis scenario described above, there is not a cosmological constant at high redshifts and therefore

$$\Omega_m = \frac{4}{3} \left[3M(1 - M - \Omega_k - \Omega_r)^3 \right]^{1/4}.$$
(43)

It is also possible to extend this VM model assuming a possible cosmological constant at high redshifts, as the vacuum expectation value of the massive scalar field. In this case, we have to impose the additional conditions $z_t^{\text{ph}} \ge 0$, i.e. the transition happening in the past, and $\Omega_{\text{DE}}(z > z_t^{\text{ph}}) \ge 0$. With both the VM model and its extension, the Hubble constant $H_0 \sim 73 - 74 \,\text{km s}^{-1} \,\text{Mpc}^{-1}$ is completely in agreement with the SH0ES value, without assuming a Gaussian prior on it. Unfortunately this model fails to fit in a good way the low redshift data, such as BAO and Pantheon: H_0 remains in the SH0ES range but with a much worse χ^2 than Λ CDM.

7.6. Modified gravity models

Modified gravity (MG) models Clifton et al. (2012); Ade et al. (2016e) in which some feature of gravity (such as the gravitational coupling) changes with redshift, can lead to an H_0 estimate from CMB larger than that obtained from late-time probes Umiltà et al. (2015); Ballardini et al. (2016); Raveri (2020); Yan et al. (2020b); Frusciante et al. (2020); Frusciante and Benetti (2021); Solà Peracaula et al. (2019b, 2020); Ballesteros et al. (2020); Braglia et al. (2020a); Ballardini et al. (2020a); Rossi et al. (2019); Joudaki et al. (2022); Braglia et al. (2021); Akarsu et al. (2020b); Benetti et al. (2018b). To solve (or at least relax) the H_0 tension in the context of MG models, instead of modifying the matter content, the gravitational sector is modified in a manner that current cosmic dynamics is derived. In particular, it is easy to argue that Newton's constant needs to decrease as the Universe evolves in order to stand a chance of resolving cosmological tensions Heisenberg et al. (2022a,b); Lee et al. (2022). There has been several proposals in GR that follows this line of thought Clifton et al. (2012); Ishak (2019). One interesting approach in this direction has been the f(R) theories Sotiriou and Faraoni (2010); Faraoni (2008); De Felice and Tsujikawa (2010), in which an arbitrary function of the Ricci scalar replaces the standard Einstein-Hilbert Lagrangian density. In the metric version, the Ricci scalar and the metric tensor evolve in time in an independent fashion. Thus, there is a scalar degree of freedom (absent in GR), which helps to explain the late cosmic acceleration and structure formation without the need of the dark matter

sector.¹⁸ Along with various cosmological models in Einstein gravity, the modified gravity models can also reconcile the S_8 tension Ade et al. (2016e); Di Valentino et al. (2016c); Joudaki et al. (2017b, 2018); Solà Peracaula et al. (2019b, 2020); Wen et al. (2021).

7.6.1. Effective field theory approach to dark energy and modified gravity

Above we have discussed several alternatives to a purely cosmological constant in late-time cosmology, e.g., modified gravity. Much of these alternatives are often very model specific and must confront precise observations. Given the current wealth of data another theoretical approach – motivated by techniques utilized in particle and condensed matter physics – is to utilize methods of effective field theory as applied to cosmology Park et al. (2010); Gubitosi et al. (2013); Bloomfield et al. (2013). This can also lead to an effective method to confront a large, and much general set of models with observations Wen et al. (2021); Frusciante et al. (2014); Raveri et al. (2014).

This approach is to establish how gravity may, or may not, be modified to explain the current acceleration of the expansion of the Universe and at what scales this is relevant (e.g. it is well known that gravity cannot be modified at solar system scales). In the effective field theory approach, one can establish groups of models to collect model dependent approaches and establish these into groups of models independent (universality classes) based on their symmetries (or lack thereof). This allows for a method to connect a large model specific set of predictions to be confronted with observations. For example, Horndeski models (mentioned above) are of broad interest in the community, but in this formalism, they form a universality class that can be viable or ruled out by current and near-term observations.

7.6.2. f(T) gravity

Recently, teleparallel gravity (TG) and its extensions have started to take advantage of their mathematical description to solve the H_0 tension and describe the cosmic late-time dynamics with current data. In these kind of theories, gravity is still described in geometrical terms, but using torsion instead of curvature, namely using the Weitzenböck connection Weitzenböck (1923) instead of the Levi-Civita one. Hence, the actions of GR and TG differ only by a boundary term, and thus they lead to the same equations, that is why the corresponding theory is called Teleparallel equivalent of General Relativity (TEGR). There are several ways to modify the TEGR proposal: (1) through the so-called torsion scalar T Nunes (2018). In this form, we can generalise the Lagrangian to arbitrary functions of the torsion scalar to produce f(T) gravity Ferraro and Fiorini (2007); Linder (2010); Chen et al. (2011); Benisty et al. (2021); Bahamonde et al. (2022), analogous to f(R) theories (for reviews see Cai et al. (2016a); Bahamonde et al. (2021)). (2) Furthermore, the importance of the boundary term, f(T, B) gravity models has also been well-studied Escamilla-Rivera and Levi Said (2020); Bahamonde et al. (2015); Farrugia et al. (2018) as a possible extension to TEGR to infer H_0 Escamilla-Rivera and Levi Said (2020). Performing consistency tests with current astrophysical data allows to identify a gravity theory and deal at the same time with systematic effects in the observational data. In some cases, data samples are sensitive to the geometry and dynamics of the Universe and other samples are sensitive to the growth of LSS. In such cases, these two sets of observations must be consistent with one another in order to solve the cosmological tension inside a specific model. At late-times, any deviations between models can be measured through an effective EoS that mimics a dark energy component near to the Λ CDM EoS value (w = -1). In Ref. Escamilla-Rivera (2020a) it was provided an insightful test via examples in f(R) and f(T, B) gravity theories that can solve the H_0 tension using current late-time surveys (see also Refs. Lambiase et al. (2019); Benetti et al. (2019a); Cai et al. (2020); D'Agostino and Nunes (2020); Wang and Mota (2020); Parashari et al. (2021)). Theories that deviate from GR can be delineated into categories according to what principle or requirement they violate. Theoretical efforts to find a dynamic model describing the data have been placed side by side to kinematic models, as the cosmography, where the current expansion is a function of the cosmic time Sahni et al. (2014); Capozziello et al. (2019); Benetti and Capozziello (2019); El Hanafy and Saridakis (2021).

In its most simple formulation, it is possible to consider f(T) extensions of teleparallel gravity intended as corrections to TEGR where only the torsion scalar T is considered. The action takes the form of

$$S = \frac{M_{\rm Pl}^2}{2} \int d^4 x \, e \left[T + f(T) \right] + S_m \,, \tag{44}$$

where M_{Pl} is the reduced Planck mass, f(T) is a generic function of the torsion scalar *T*, S_m is the action of matter fields, and the tetrad $e = \det(e_{\mu}^i) = \sqrt{-g}$ is the metric determinant.

For a flat FLRW background, it is possible to derive the relation between the torsion *T* and the Hubble parameter, $T = 6H^2$. The sign of such a torsion element depends on the signature of the metric, which is identified by the vierbien fields $e^a_{\mu} = \text{diag}(-1, a, a, a)$. Assuming that matter sector is described by a perfect fluid with energy density ρ and pressure *p*, the field equations give

$$H^{2} = \frac{8\pi G_{N}}{3}\rho_{m} - \frac{f(T)}{6} + \frac{Tf_{T}}{3}$$

$$(45)$$

$$\frac{4\pi G_{N}(\rho_{m} + p_{m})}{2}$$

$$\dot{H} = -\frac{4\pi G_N \left(\rho_m + p_m\right)}{1 + f_T + 2T f_{TT}}.$$
(46)

Moreover, the set of equations is closed with the equation of continuity for the matter sector $\dot{\rho} + 3H(\rho + p) = 0$. Eqs. (45)-(46) can be rewritten in terms of the effective energy density ρ_T and pressure p_T arising from f(T),

$$\rho_{f(T)} = \frac{M_{\rm Pl}^2}{2} \left[2T f_T - f(T) \right] \tag{47}$$

$$p_{f(T)} = \frac{M_{\rm Pl}^2}{2} \left[\frac{f(T) - Tf_T + 2T^2 f_{TT}}{1 + f_T + 2Tf_{TT}} \right],\tag{48}$$

and define the effective torsion equation-of-state

¹⁸ In the Palatini version, the same result is achieved due to the new terms that arise from the affine connection when written in of the Christoffel symbols and of the quantities that describe the matter Sotiriou and Faraoni (2010).

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$$w \equiv \frac{p_{f(T)}}{\rho_{f(T)}} = \frac{f(T) - Tf_T + 2T^2 f_{TT}}{[1 + f_T + 2Tf_{TT}][2Tf_T - f(T)]}.$$
(49)

These effective models are hence responsible for the accelerated phases of the early or/and late Universe Cai et al. (2016a).

In order to study the background evolution, we can rewrite the first FLRW equation, making explicit the form of the torsional energy density Nesseris et al. (2013); Nunes (2018); Nunes et al. (2016b)

$$\frac{H(a)^2}{H_0} \equiv E(a)^2 = \left[\Omega_m a^{-3} + \Omega_r a^{-4} + \frac{1}{T_0} [-f + 2Tf']\right],\tag{50}$$

where we considered the relation $T = 6H^2$ and T_0 is the present value of *T*.

At this point, specific forms of f(T) functions must be chosen and several in the literature have passed basic observational tests Nesseris et al. (2013); Nunes et al. (2016b); Capozziello et al. (2017); Nunes (2018); Briffa et al. (2021). Between them, the simplest form of power-law proved to be the one that predicts an H_0 compatible with Cepheids observations Riess et al. (2019). This model is described by Nesseris et al. (2013)

$$f(T) = \beta \left(-T\right)^b.$$
(51)

Inserting this f(T) form into (45) and for b = 0 and $\beta = -2\Lambda$, the scenario reduces to Λ CDM cosmology, namely $T + f(T) = T - 2\Lambda$.

Analysing this model considering both the background and the linear perturbation evolution, in the light of both large and small scale data, a value of $H_0 = (73.85 \pm 1.05) \text{ km s}^{-1} \text{ Mpc}^{-1}$ has been constrained using CMB+lensing+BAO+R19+Pth+DES data Benetti et al. (2020) (see Ref. Briffa et al. (2021) for analysis with several other combinations of large-scale data). Also, a deviation from the GR was detected at more than 3σ . Noteworthy, this allows to significantly relax the Hubble constant tension, but worsens σ_8 tension MacCrann et al. (2015); Battye et al. (2015); Benetti et al. (2018a) since the correlation of the two parameters does not seem to be removed from this treatment of f(T) models.

Let us now try to suitably extract an f(T) form that could alleviate both tensions simultaneously. In order to avoid the H_0 tension one needs a positive correction to the first Friedmann equation at late times that could yield an increase in H_0 compared to the Λ CDM scenario. As for the σ_8 tension, since at sub-Hubble scales and through the matter epoch, the equation that governs the evolution of matter perturbations in the linear regime is

$$\delta + 2H\delta = 4\pi G_{\rm eff} \rho_{\rm m} \delta \,, \tag{52}$$

where G_{eff} is the effective gravitational coupling. Thus, alleviation of σ_8 tension may be obtained if G_{eff} becomes smaller than G_N during the growth of matter perturbations. In the case of f(T) gravity the effective gravitational coupling is given by Nesseris et al. (2013)

$$G_{\rm eff} = G_N \left(1 + \frac{\partial f}{\partial T} \right)^{-1} \,. \tag{53}$$

According to the Effective Field Theory approach to f(T) gravity Li et al. (2018a); Yan et al. (2020b); Ren et al. (2022) one can choose f(T) in order to obtain a Hubble function evolution of the form

$$H(z) = -\frac{d(z)}{4} + \sqrt{\frac{d^2(z)}{16} + H_{\Lambda \text{CDM}}^2(z)},$$
(54)

where $H_{\Lambda \text{CDM}}(z) \equiv H_0 \sqrt{\Omega_m (1+z)^3 + \Omega_\Lambda}$ is the Hubble rate in ΛCDM after recombination, Ω_m is the present matter density parameter, and primes denote derivatives with respect to *z*. The function d(z) can be selected to be d < 0 in order to have $H(z \rightarrow z_{\text{CMB}}) \approx H_{\Lambda \text{CDM}}(z \rightarrow z_{\text{CMB}})$, therefore the H_0 tension is solved. One should choose |d(z)| < H(z), and thus, since H(z) decreases for smaller *z*, the deviation from ΛCDM will be significant only at low redshift]. Additionally, since G_{eff} becomes smaller than G_N during the growth of matter perturbations, the σ_8 tension is also solved.

We follow Ref. Yan et al. (2020b) and we consider the ansatz $f(T) = -[6H_0^2(1 - \Omega_m) + F(T)]$, where F(T) describes the deviation from GR (mind the difference in the conventions). Under these assumptions, the first Friedmann equation becomes

$$T(z) + 2\frac{F'(z)}{T'(z)}T(z) - F(z) = 6H_{\Lambda \text{CDM}}^2(z).$$
(55)

In order to solve the H_0 tension, we need $T(0) = 6H_0^2$, with $H_0 = 74.03 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ following results with local measurements Riess et al. (2019), while in the early era of $z \gtrsim 1100$ we require the Universe expansion to evolve as in Λ CDM, namely $H(z \gtrsim 1100) \simeq H_{\Lambda \text{CDM}}(z \gtrsim 1100)$. This implies $F(z)|_{z \gtrsim 1100} \simeq cT^{1/2}(z)$ (the value c = 0 corresponds to standard GR, while for $c \neq 0$ we obtain Λ CDM too). Therefore, the perturbation equation at linear order becomes

$$\delta'' + \left[\frac{T'(z)}{2T(z)} - \frac{1}{1+z}\right]\delta' = \frac{9H_0^2\Omega_m(1+z)}{[1+F'(z)/T'(z)]T(z)}\delta.$$
(56)

Since around the last scattering moment $z \gtrsim 1100$ the Universe should be matter-dominated, we impose $\delta'(z)|_{z \gtrsim 1100} \simeq -\frac{1}{1+z}\delta(z)$, while at late times we look for $\delta(z)$ that leads to an $f\sigma_8$ in agreement with redshift survey observations.

By solving Eqs. (55) and (56) with initial and boundary conditions at $z \sim 0$ and $z \sim 1100$, we can find the f(T) form that can alleviate both H_0 and σ_8 tensions. In particular, we find that we can fit the numerical solutions very efficiently through $F(T) \approx 375.47 [T/(6H_0^2)]^{-1.65}$, dubbed Model-1, and $F(T) \approx 375.47 [T/(6H_0^2)]^{-1.65} + 25T^{1/2}$, dubbed Model-2. We examine G_{eff} , and as expected



Fig. 8. Evolution of the Hubble parameter H(z) in the two f(T) models (purple solid line) and in Λ CDM cosmology (black dashed line). The red point (with error bars) represents the latest data from extragalactic Cepheid-based local measurement of H_0 Riess et al. (2019). The figure is from Yan et al. (2020b).



Fig. 9. The evolution of $f\sigma_8$ in Model-1 (brown solid line) and Model-2 (blue solid line) of f(T) gravity and in Λ CDM cosmology (black dashed line). The green data points (with error bars) are from BAO observations in SDSS-III DR12 Wang et al. (2018c), the gray data points (with error bars) at higher redshift are from SDSS-IV DR14 Gil-Marín et al. (2018), while the red point (with error bars) around ~ 1.8 is the forecast from Euclid Taddei et al. (2016). The subgraph in the left bottom displays $f\sigma_8$ at high redshift $z = 3 \sim 5$, which shows that the curve of Model-2 is above the one of Model-1 and Λ CDM scenario and hence approaches Λ CDM slower than Model-1. The figure is from Yan et al. (2020b).

we find that at high redshifts in both models, G_{eff} becomes G_N , recovering the Λ CDM paradigm. We have checked that both models can easily pass the BBN constraints, which demand $|G_{\text{eff}}/G_N - 1| \le 0.2$ Copi et al. (2004a), as well as the ones from the Solar System, which demand $|G'_{\text{eff}}(z=0)/G_N| \le 10^{-3}h^{-1}$ and $|G_{\text{eff}}(z=0)/G_N| \le 10^{5}h^{-2}$ Nesseris and Perivolaropoulos (2007).

In Fig. 8 we present the evolution of H(z), while in Fig. 9 the evolution of $f\sigma_8$, for two f(T) models, and we compare them with Λ CDM. We stress that the H_0 tension can be alleviated as H(z) remains statistically consistent for all CMB and CC measurements at all redshifts. We remind the reader that the two f(T) models differing merely by a term $\propto T^{1/2}$, which does not affect the background as explained before, are degenerate at the background level. However, at the perturbation level, the two models behave differently as their gravitational coupling G_{eff} differs.

We further stress that both models can alleviate the σ_8 tension, and fit efficiently to BAO and LSS measurements. Note that at high redshifts ($z \ge 2$), Model-2 approaches Λ CDM slower than Model-1, but in a way that is statistically indistinguishable for present-day data. Nevertheless, future high-redshift surveys such as eBOSS for quasars and Euclid Laureijs et al. (2011) for galaxies have the potential to discriminate among the predictions of f(T) gravity and the Λ CDM scenario. Moreover, the clusters and CMB measurements on σ_8 are in good agreement in our models, as the CMB preferred values in Λ CDM get further lowered than local ones from rescaling σ_8 by the ratio of the growth factors in f(T) gravity and Λ CDM. In more detail,

$$\sigma_8^{f(T)}(z=0) = \frac{D^{f(T)}(z=0)}{D^{\Lambda}(z=0)} \frac{D^{\Lambda}(z_{\text{eff}})}{D^{f(T)}(z_{\text{eff}})} \sigma_8^{\Lambda}(z=0),$$
(57)

where D(z) is the growth factor, f(T) and Λ denote the models for modified gravity and Λ CDM, respectively, and z_{eff} is the effective redshift of the measurements, with $z_{\text{eff}} \sim 0.1$ for clusters experiments and $z_{\text{eff}} \sim 1100$ for CMB temperature fluctuations observations. At high redshifts $z_{\text{eff}} \sim 1100$, the growth factor is the same in both the f(T) model and in Λ CDM, while at low redshifts $z_{\text{eff}} \sim 0.1$, the growth factor is approximately 1.03 times bigger in the latter one. For this reason, cluster σ_8 -measurements increase by about the same factor, reducing the gap with CMB preferred value in this modified gravity scenario.

In summary, we conclude that the class of f(T) gravity described by

$$f(T) = -2\Lambda/M_{\rm Pl}^2 + \alpha T^\beta , \qquad (58)$$

where only two out of the three parameters Λ , α , and β are independent (the third one is eliminated using Ω_m), can alleviate both H_0 and σ_8 tensions with suitable parameter choices. Moreover, these type of f(T) gravity models could also be examined through galaxygalaxy lensing effects Chen et al. (2020a), strong lensing effects around black holes Yan et al. (2020a), and GW experiments Cai et al. (2018a).

7.6.3. Horndeski theory

7.6.3.1. Shift-symmetric Horndeski theories. After the detection of the gravitational-wave event GW170817 Abbott et al. (2017a) and its electromagnetic counterpart, the speed of GWs c_t is constrained to be very close to that of light c. Without the shift symmetry condition, namely that the theory is invariant under scalar shifts, $\phi \rightarrow \phi + c$ with constant c, Horndeski would reduce to three functions, $G_2(\phi, X)$, $G_3(\phi, X)$ and $G_4(\phi)$ (for example, see Ref. Kase and Tsujikawa (2019)). Further imposing the shift symmetry condition, G_2 and G_3 are reduced to functions of X only, while G_4 becomes a constant. The Lagrangian of the Horndeski theories Horndeski (1974); Kobayashi et al. (2011); De Felice and Tsujikawa (2012); Kobayashi (2019) realizing this condition is strongly constrained Ezquiaga and Zumalacárregui (2017), in particular the cubic-order shift-symmetric Horndeski theories falls back in this class of theories. The cubic-order shift-symmetric Horndeski action is given by Kobayashi (2019)

$$S = \int d^4x \sqrt{-g} \left[\frac{M_{\rm Pl}^2}{2} R + G_2(X) + G_3(X) \Box \phi \right] + S_i(\chi_i, g_{\mu\nu}),$$
(59)

where g is the determinant of the metric tensor $g_{\mu\nu}$, M_{Pl} is the reduced Planck mass, R is the Ricci scalar, and G_2 , G_3 are functions of $X = \nabla^{\mu} \phi \nabla_{\mu} \phi$, with ϕ being the scalar field. Finally, S_i corresponds to the action of standard *i*th fluid fields χ_i . The continuity equations of fluids reads on the FLRW background,

$$\dot{\rho}_i + 3H(1+w_i)\rho_i = 0, \tag{60}$$

where ρ_i is the fluid density, $w_i \equiv p_i/\rho_i$ is the constant barotropic coefficient relating the fluid density and the pressure, $H = \dot{a}/a$ is the Hubble expansion rate, and a dot stands for the derivative with respect to *t*. We recall that the modified Friedmann and scalar-field equations at the background level are given by

$$3M_{\rm Pl}^2 H^2 = \rho_\phi + \rho_m + \rho_r \,, \tag{61}$$

$$2M_{\rm Pl}^2 \dot{H} = -\rho_\phi - P_\phi - \rho_m - \frac{4}{3}\rho_r \,, \tag{62}$$

$$(G_{2,X} - 2\dot{\phi}^2 G_{2,XX} - 6H\dot{\phi}G_{3,X} + 6H\dot{\phi}^3 G_{3,XX})\ddot{\phi} + 3(HG_{2,X} - \dot{H}\dot{\phi}G_{3,X} - 3H^2\dot{\phi}G_{3,X})\dot{\phi} = 0.$$
(63)

The density and pressure of the scalar field are obtained as

. .

$$\rho_{\phi} = -G_2 - 2\dot{\phi}^2 G_{2,X} + 6H\dot{\phi}^3 G_{3,X}, \qquad (64)$$

$$P_{\phi} = G_2 - 2\dot{\phi}\dot{\phi}^2 G_{3,X}, \tag{65}$$

with $G_X \equiv dG/dX$. From this, we can define a scalar field EoS as

$$w_{\phi} \equiv \frac{P_{\phi}}{\rho_{\phi}} = -\frac{G_2 - 2\dot{\phi}\dot{\phi}^2 G_{3,X}}{G_2 + 2\dot{\phi}^2 G_{2,X} - 6H\dot{\phi}^3 G_{3,X}}.$$
(66)

From Eq. (61), there is the constraint $\Omega_{\phi} + \Omega_m + \Omega_r = 1$, where $\Omega_i \equiv \rho_i / (3M_{Pl}^2 H^2)$. Finally, by solving Eqs. (62)-(63) for \dot{H} and $\ddot{\phi}$ one can know the dynamics of the Universe. For linear perturbations we consider the perturbed FLRW line element: $ds^2 = -(1 + 2\Psi) dt^2 + a^2(t) (1 - 2\Phi) \delta_{ij} dx^i dx^j$, where Ψ and Φ are the gravitational potentials and for the perturbations in the matter sector follow the standard perturbation theory Ma and Bertschinger (1995). In the case of modified gravity, in order to derive an explicit relation between the gravitational potentials and the matter perturbation δ_m , one has to use the quasi-static approximation (QSA) Boisseau et al. (2000); Tsujikawa (2007); De Felice et al. (2011); Sawicki and Bellini (2015) which, within the Horndeski class of models, it is a valid assumption for the wavenumber in the range $k > 10^{-3} h \, \text{Mpc}^{-1}$ Peirone et al. (2018); Frusciante et al. (2019). In this approximations one has:

$$-k^2\Psi = 4\pi G_N a^2 \mu(a,k)\rho_m \delta_m \,, \tag{67}$$

$$-k^2(\Psi+\Phi) = 8\pi G_N a^2 \Sigma(a,k) \rho_m \delta_m , \qquad (68)$$

where G_N is Newton's gravitational constant. The dimensionless quantities μ and Σ characterize the effective gravitational couplings felt by matter and light, respectively. For the cubic-order shift-symmetric Horndeski theories one has $\Phi = \Psi$ and De Felice et al. (2011); Kase and Tsujikawa (2019)

$$\mu = \Sigma = 1 + \frac{4\dot{\phi}^4 G_{3,X}^2}{0 \, sc_s^2},\tag{69}$$

where the kinetic term Q_s and the speed of propagation of the scalar field c_s are given by

$$Q_{s} = 4M_{\text{Pl}}^{2} \left(-G_{2,X} + 2\dot{\phi}^{2}G_{2,XX} + 6H\dot{\phi}G_{3,X} - 6H\dot{\phi}^{3}G_{3,XX} \right) + 12\dot{\phi}^{4}G_{3,X}^{2},$$

$$(70)$$

$$c_s^2 = \frac{-4M_{\rm Pl}^2(G_{2,X} - 2\phi G_{3,X} - 4H\phi G_{3,X} + 2\phi \phi^2 G_{3,XX}) - 4\phi^2 G_{3,X}}{Q_s}.$$
(71)

Both the above quantities need to be positive defined to avoid Ghost and Gradient instabilities. Finally the matter perturbation equations can be written as

$$\hat{s}_m + 2H\hat{s}_m - 4\pi G_N \mu \rho_m \delta_m \simeq 0. \tag{72}$$

In the following we specialize to two models which are of interest for alleviating the H_0 tension.

• Galileon Ghost Condensate (GGC): We consider the Galileon Ghost Condensate (GGC) model which is specified by the functions Deffayet et al. (2010); Kase and Tsujikawa (2018)

$$G_2(X) = a_1 X + a_2 X^2, \qquad G_3(X) = 3a_3 X,$$
(73)

where a_1 , a_2 , a_3 are constants. This model departs from the Cubic Galileon model Deffayet et al. (2009) by the inclusion of the term a_2X^2 , which affects the cosmic expansion history and growth of structures at both linear Kase and Tsujikawa (2018); Peirone et al. (2019) and non-linear scales Frusciante and Pace (2020) compared to G_3 . The presence of nonvanishing a_2X^2 allows to prevent the solutions from approaching the tracker at background level. In this case it is possible to realize the phantom behaviour for the scalar field ($w_{\phi} < -1$) without having ghosts Kase and Tsujikawa (2018); Peirone et al. (2019). At linear perturbation μ and Σ in Eq. (69) are larger than 1, so both Ψ and $\Psi + \Phi$ are enhanced compared to those in GR, showing a stronger gravitational interaction. In particular, it has been found that the model suppresses the large-scale CMB temperature anisotropy in comparison to the Λ CDM model. These features lead to the statistical preference of GGC over Λ CDM when data from CMB, BAO, SNIa, and RSDs are used Peirone et al. (2019). Furthermore the CMB temperature and polarization data from *Planck* 2015 release lead to an estimation for today's Hubble parameter H_0 with is higher than the Λ CDM and consistent with its direct measurements at 2σ , $H_0 = \left(69.3^{+3.6}_{-3.0}\right)$ km s⁻¹ Mpc⁻¹ at 95% CL with

best fit $H_0^{bf} = 70 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ Peirone et al. (2019).

• Generalized Cubic Covariant Galileon (GCCG): Let us consider the Generalized Cubic Covariant Galileon (GCCG) model De Felice and Tsujikawa (2012), defined by the functions

$$G_2(X) = -c_2 M_2^{4(1-p)} (-X/2)^p, \qquad G_3(X) = -c_3 M_3^{1-4p_3} (-X/2)^{p_3}, \tag{74}$$

where c_2 , c_3 , p, p_3 are dimensionless constants, and M_2 , M_3 are constants having dimension of mass. For simplicity another parameters are used defined by $q = p_3 - p + \frac{1}{2}$ and s = p/q. The GCCG model is an extension of the Covariant Galileon (s = 2, q = 1/2), and the same as the latter, it also allows for the existence of a tracker solution following the relation $H\dot{\phi}^{2q} = \text{constant}$ with q > 0. For this model it is possible to verify that $\mu \ge 1$ for any viable value of q and s and hence the gravitational interaction is always stronger than in GR.

Observational constraints on H_0 , in the case of *Planck* 2015 alone are: $H_0 = 72^{+8}_{-5} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 95% CL, finding a consistency with its determination from Cepheids at 1σ Frusciante et al. (2020). Such result on H_0 is also compatible with the estimation obtained with the tip of the red giant branch in LMC, $H_0 = (72.4 \pm 2) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Yuan et al. (2019). The main feature behind the eased H_0 tension in the GCCG model is due to a modified low redshift expansion history which is enhanced with respect to Λ CDM. In this model is also interesting to note that if the tension between CMB data and low redshift measurements of H_0 disappears for the GCCG model, another tension between the latter and BAO data appears Frusciante et al. (2020) (see also Renk et al. (2017)).

7.6.3.2. Horndeski theories with non-minimal derivative coupling. Let us now examine one interesting subclass of Horndeski gravity, or equivalently generalized Galileon theory, that contains the G_5 term of the corresponding action, which is called "non-minimal derivative coupling term". Thus, instead of Eq. (59), we consider the action Saridakis and Sushkov (2010); Petronikolou et al. (2021)

$$S = \int d^{4}x \sqrt{-g} \left\{ \frac{M_{\text{Pl}}^{2}}{2} R + K(\phi, X) + G_{5}(\phi, X) G_{\mu\nu} (\nabla^{\mu} \nabla^{\nu} \phi) - \frac{1}{6} G_{5,X} \left[(\Box \phi)^{3} - 3(\Box \phi) (\nabla_{\mu} \nabla_{\nu} \phi) (\nabla^{\mu} \nabla^{\nu} \phi) + 2(\nabla^{\mu} \nabla_{\alpha} \phi) (\nabla^{\alpha} \nabla_{\beta} \phi) (\nabla^{\beta} \nabla_{\mu} \phi) \right] \right\} + S_{i}(\chi_{i}, g_{\mu\nu}),$$
(75)

where $G_{\mu\nu}$ is the Einstein tensor. The Friedmann equations in FLRW geometry become De Felice and Tsujikawa (2012)

$$2XK_{,X} - K - 3H^{2}M_{Pl}^{2} + 2H^{3}X\dot{\phi}(5G_{5,X} + 2XG_{5,XX} - 6H^{2}X(3G_{5,\phi} + 2XG_{5,\phi X}) = -\rho_{m},$$

$$K + M_{Pl}^{2}(3H^{2} + 2\dot{H}) - 4H^{2}X^{2}\ddot{\phi}G_{5,XX} - 2X(2H^{3}\dot{\phi} + 2H\dot{H}\dot{\phi} + 3H^{2}\ddot{\phi})G_{5,X}$$

$$+ 4HX(\dot{X} - HX)G_{5,\phi X} + 4HX\dot{\phi}G_{5,\phi\phi} + 2[2(\dot{H}X + H\dot{X}) + 3H^{2}X]G_{5,\phi} = -p_{m},$$
(76)
(77)

while the scalar-field equation is $\frac{1}{a^3} \frac{d}{dt} (a^3 J) = P_{\phi}$, with $J \equiv \dot{\phi} K_{,X} + 2H^3 X (3G_{5,X} + 2XG_{5,XX}) + 6H^2 \dot{\phi} (G_{5,\phi} + XG_{5,\phi X})$ and $P_{\phi} \equiv K_{,\phi} - 6H^2 X G_{5,\phi\phi} + 2H^3 X \dot{\phi} G_{5,\phi\chi}$. Finally, the conditions in Eqs. (70)-(71) for absence of Laplacian and ghost instabilities become:

$$Q_s \equiv \frac{w_1(4w_1w_3 + 9w_2^2)}{3w_2^2} > 0,$$
(78)

$$c_s^2 = \frac{3(2w_1^2w_2H - w_2^2w_4 + 4w_1w_2\dot{w}_1 - 2w_1^2\dot{w}_2)}{w_1(4w_1w_3 + 9w_2^2)} \ge 0,$$
(79)

with

$$w_1 \equiv M_{\rm Pl}^2 - 2X(G_{5,X}\phi H - G_{5,\phi}), \tag{80}$$

$$w_2 \equiv 2M_{\rm Pl}^2 H + 8X^2 H G_{5,\phi X} + 2HX(6G_{5,\phi} - 5G_{5,X}\dot{\phi}H) - 4G_{5,XX}\dot{\phi}X^2 H^2,$$
(81)

$$w_3 \equiv 3X(K_{,X} + 2XK_{,XX}) - 9M_{\text{Pl}}^2 H^2$$

$$+6H^{2}X\left(2H\phi G_{5,XXX}X^{2}-6X^{2}G_{5,\phi XX}-18G_{5,\phi}+13XH\phi G_{5,XX}-27G_{5,\phi X}X+15H\phi G_{5,X}\right),$$
(82)

$$w_4 \equiv M_{\rm Pl}^2 - 2XG_{5,\phi} - 2XG_{5,X}\ddot{\phi} \,. \tag{83}$$

In order to alleviate the H_0 tension using the above construction we need to obtain a weakening of gravity at low redshifts by the terms depending on the scalar field's kinetic energy. We impose a simple scalar field potential and standard kinetic term, thus $K = -V(\phi) + X$, and we will consider the G_5 term to be shift-symmetric, i.e. $G_5(\phi, X) = G_5(X)$. We consider two models.

• Model I: $G_5(X) = \xi X^2$ In this case, the Friedmann Eqs. (76)-(77) become

$$3M_{\rm Pl}^2 H^2 = \frac{\dot{\phi}^2}{2} + V_0 \phi + 7\xi H^3 \dot{\phi}^5 + \rho_m , \tag{84}$$

$$-2M_{\rm Pl}^2\dot{H} = \dot{\phi}^2 + 7\xi H^3 \dot{\phi}^5 - \xi \dot{\phi}^4 \left(2H^3 \dot{\phi} + 2H\dot{H} \dot{\phi} + 5H^2 \ddot{\phi}\right) + \rho_m + p_m \,. \tag{85}$$

We choose the model parameter V_0 and the initial conditions for the scalar field in order to obtain $H(z_{CMB}) = H_{\Lambda CDM}(z_{CMB})$ and $\Omega_m = 0.31$, in agreement with the results from *Planck* 2018 Aghanim et al. (2020b), and we leave ξ as the parameter that determines the late-time deviation from Λ CDM cosmology necessary to alleviate the H_0 tension. Choosing $1.3 \le \xi \le 1.5$ in Planck units leads to $H_0 \approx 74 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and thus the H_0 tension is indeed alleviated, while c_s^2 remains almost equal to 1 and Q_s remains positive, and therefore the scenario is free from pathologies Petronikolou et al. (2021).

• Model II: $G_5(X) = \lambda X^4$ In this case the Friedmann Eqs. (76)-(77) become

$$3M_{\rm Pl}^2 H^2 = \frac{\phi^2}{2} + V_0 \phi + \frac{11}{2} \lambda H^3 \dot{\phi}^9 + \rho_m \,, \tag{86}$$

$$-2M_{\rm Pl}^{2}\dot{H} = \dot{\phi}^{2} + \frac{11}{2}\lambda H^{3}\dot{\phi}^{9} - \frac{\lambda\dot{\phi}^{8}}{2}\left(2H^{3}\dot{\phi} + 2H\dot{H}\dot{\phi} + 9H^{2}\ddot{\phi}\right) + \rho_{m} + p_{m}.$$
(87)

Choosing $0.9 \le \lambda \le 1.1$ in Planck units leads to $H_0 \approx 74 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$, while c_s^2 remains almost equal to 1 and Q_s remains positive Petronikolou et al. (2021). Hence the Hubble tension is alleviated.

In summary, we showed that the above particular sub-class of Horndeski/generalized Galileon gravity can alleviate the H_0 tension due to the effect of the kinetic-energy-dependent G_5 term. In particular, at early times the field's kinetic term is negligible and hence the $G_5(X)$ terms do not introduce any deviation from Λ CDM scenario, nevertheless as time passes they increase in a controlled and suitable way in order to make the Hubble function, and thus H_0 too, to increase. However, see Refs. Banerjee et al. (2021b); Lee et al. (2022), where it is argued that DE models in a general class of scalar-tensor theories, including quintessence and a good class of Horndeski theories, perform worse than Λ CDM model as far as the H_0 increasing is concerned. Moreover, a similar result is discussed in Refs. Heisenberg et al. (2022b,a) where it is argued that the family of scalar-tensor DE models generically exacerbate H_0 and S_8 anomalies. A further problem of the Horndeski models with non-minimal derivative coupling, i.e. $G_5 \neq 0$, is that to evade constraints from gravitational waves Abbott et al. (2017a), some fine tuning is required.

7.6.3.3. *Minimal scalar-tensor theories of gravity.* The action for the simplest scalar-tensor theories of gravity within the most general Horndeski model Horndeski (1974) with a scalar field σ in units of the reduced Planck mass M_{Pl} and non-minimally coupled (NMC) to the Ricci curvature *R* is Capozziello and de Ritis (1994); Boisseau et al. (2000); Esposito-Farese and Polarski (2001); Nesseris and Perivolaropoulos (2006); Cai et al. (2010)

$$S = \int d^4x \sqrt{-g} \left[\frac{F(\sigma)}{2} R - \frac{g^{\mu\nu}}{2} \partial_{\mu}\sigma \partial_{\nu}\sigma - V(\sigma) + \mathcal{L}_m \right],$$
(88)

where $F(\sigma)$ is a generic function of σ . Examples include induced gravity (IG), i.e. $F(\sigma) = \xi \sigma^2$ where $\xi > 0$ is the coupling to the Ricci scalar, and conformally coupled scalar field (CCSF), i.e. $F(\sigma) = N_{Pl}^2 - \sigma^2/6$ where N_{Pl} is a dimensionless parameter. A scalar-tensor theory allows to easily attain values for H_0 that are larger than in Λ CDM. This effect is mainly due to a degeneracy between the coupling to the Ricci curvature and H_0 and is connected to the rolling of the scalar field, which regulates the gravitational strength, at the onset of the matter dominated era driven by pressureless matter. Therefore, larger values for H_0 can appear already in archetypal models of scalar-tensor theories of gravity, namely Jordan-Brans-Dicke (JBD) models Brans and Dicke (1961a); Dicke (1962), see Sec. 7.6.3.4 for additional detail. This effect is *a*) largely independent on the part of the scalar field potential which acts as an effective cosmological constant, *b*) robust with respect to uncertainties in the neutrino sector, and *c*) possibly enhanced by allowing a difference between the gravitational constant relevant for cosmology and Newton's constant as measured in a Cavendish-like experiment.

The possibility to connect a larger value of H_0 with an early-time modification of GR in the context of scalar-tensor gravity has been highlighted since the first *Planck* 2013 data release, where one of the simplest scalar-tensor gravity model, such as induced gravity (equivalent to JBD) with a quartic potential $V(\sigma) = \lambda \sigma^4/4$ has been studied Umiltà et al. (2015), showing the degeneracy between the coupling to the Ricci scalar and H_0 . Subsequent studies updated and generalized this result for different simple potentials and couplings Ballardini et al. (2016); Rossi et al. (2019); Ballesteros et al. (2020); Ballardini et al. (2020a); Ballardini and Finelli (2021). To sum up, for an effectively massless ($V \propto F^2$) scalar field σ at rest in the radiation era and with adiabatic initial condition for the scalar field perturbations Paoletti et al. (2019), the current constraints on the Hubble parameter from *Planck* 2018 data (temperature, E-mode polarization, and CMB lensing) at 68% CL are $H_0 = (69.6^{+0.8}_{-1.7}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ for IG and $H_0 = (69.0^{+0.7}_{-1.2}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ for CCSF, respectively Ballardini et al. (2020a). When BAO data from BOSS DR12 are added, the constraint at 68% CL becomes $H_0 = (68.78^{+0.53}_{-0.78}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ for IG and $H_0 = (68.62^{+0.47}_{-0.66}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ for CCSF. Once a Gaussian likelihood based on the determination of the Hubble constant from the SH0ES team is also included, i.e. $H_0 = (74.03 \pm 1.42) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Riess et al. (2019), we obtain $H_0 = (70.1 \pm 0.8) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL for IG and $H_0 = (69.64^{+0.65}_{-0.73}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL for CCSF. These constraints have been obtained by fixing the value of the scalar field today $\sigma_0 \equiv \sigma(z=0)$ to

$$\frac{1}{8\pi F_0} \frac{2F_0 + 4F_{0,\sigma}^2}{2F_0 + 3F_{0,\sigma}^2} = G_N,$$
(89)

where $F_0 \equiv F(\sigma_0)$ and $F_{0,\sigma} = \partial F/\partial \sigma |_{\sigma = \sigma_0}$, in order to guarantee that the effective gravitational constant today corresponds to the value of the bare gravitational constant (Boisseau et al., 2000).¹⁹

NMC models with $F(\sigma) = N_{Pl}^2 + \xi \sigma^2$ and a generic negative value of the coupling $\xi < 0$ have been explored in Rossi et al. (2019); Ballesteros et al. (2020); Braglia et al. (2020a); Ballardini et al. (2020a); Abadi and Kovetz (2021), where the scalar field decreases from an initial value σ_I to a final value close to zero, so that the Newton's constant changes after BBN from a value G_N^{BN} to the present value G_N^0 . Such models were shown to lead to $H_0 = (69.08^{+0.60}_{-0.71}) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$, with $1 - G_N^{BBN}/G_N^0 = -0.05403^{+0.047}_{-0.019}$, $\sigma_I = 0.2789^{+0.097}_{-0.054}$ and a marginal improvement of $\Delta \chi^2 = -3.2$ compared to Λ CDM, at the cost of 2 extra parameters (with *Planck* 2018, BAO, SHOES 2019 and Pantheon, plus Solar system constraints) Ballesteros et al. (2020), or $H_0 = (69.65^{+0.8}_{-0.78}) \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ with $1 - G_N^{BBN}/G_N^0 = -0.02239^{+0.0082}_{-0.0087}$, $\sigma_I = 0.6214^{+0.33}_{-0.11}$ and a more significant improvement $\Delta \chi^2 = -5.4$ with 2 extra parameters (with *Planck* 2018, BAO, SHOES 2019 and Pantheon), when ignoring Solar system constraints Ballesteros et al. (2020).

Finally, NMC models have been studied in presence of an effective mass in Ref. Braglia et al. (2021). In this Early Modified Gravity (EMG), the scalar field, which is frozen during radiation era, grows around the time of recombination driven by the coupling to pressureless matter and is subsequently driven into damped oscillations around its minimum at $\sigma = 0$ by the small effective mass induced by a quartic potential. In addition to providing a better fit to cosmological datasets compared to the Λ CDM model and EDE models, in the EMG model the positive branch for $\xi > 0$ also satisfies automatically the tight constraints on the gravitational constant field towards the bottom of the potential. For this model with $F(\sigma) = M_{\text{Pl}}^2 + \xi \sigma^2$ and $V(\sigma) = \Lambda + \lambda \sigma^4/4$, we obtain $H_0 = (71.00^{+0.81}_{-0.79}) \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $\xi < 0.42$ combining *Planck* 2018, BAO and the full shape information from BOSS DR12, SHOES 2019, and Pantheon SNe.

Minimally and non-minimally coupled scalar field models can also potentially decrease the S_8 tension. Minimally coupled models can be classified via their barotropic EoS parameter, $w = P_{\phi}/\rho_{\phi}$. The models with -1 < w < -1/3 are referred to as quintessence models, while the models with w < -1 are referred to as phantom models. When a coupling between the scalar field σ and the Ricci scalar is allowed one has the so-called NMC quintessence models or scalar-tensor theories. In the literature, scalar-tensor theories have been studied as possible solutions to the S_8 tension, since under certain circumstances they can produce a reduced growth rate compared to the standard one in the context of GR that seems to be required by different dynamical data Macaulay et al. (2013); Hildebrandt et al. (2017); Nesseris et al. (2017); Köhlinger et al. (2017); Joudaki et al. (2018); Abbott et al. (2018b); Kazantzidis and Perivolaropoulos (2018); Perivolaropoulos and Kazantzidis (2019); Kazantzidis and Perivolaropoulos (2019); Skara and Perivolaropoulos (2020); Asgari et al. (2020); Joudaki et al. (2022); Heymans et al. (2021). This behaviour can be attributed either to the reduction of the Ω_m parameter or to the existence of an evolving Newton's constant giving $G_{\text{eff}} \leq G_N$ at low *z*.

Ref. Davari et al. (2020) showed that the constraints on the Ω_m - S_8 plane are affected when considering these classes of models. In particular, while minimally coupled models simply feature a different background evolution, NMC models possess a qualitatively different growth of perturbations as the perturbation equation is modified by replacing Newton constant G_N that appears in the Einstein action of GR with the effective gravitational constant that would be measured in Cavendish-like in the context of ST theories expressed as Boisseau et al. (2000); Esposito-Farese and Polarski (2001); Nesseris and Perivolaropoulos (2006),

$$G_{\rm eff} = \frac{G_N}{8\pi F} \left(\frac{2F + 4F_{,\sigma}^2}{2F + 3F_{,\sigma}^2} \right), \tag{90}$$

which is a generalization of Eq. (89). In Ref. Davari et al. (2020) it is found that minimally and NMC models give similar constraints on the Ω_m - S_8 parameter plane and lower values of Ω_m as compared to the standard Λ CDM model. However, this is done considering specific forms of the scalar field potential and non-minimal coupling function, a more general ansatz could relieve the S_8 tension.

In the context of an evolving Newton's constant at low *z*, it has been shown that various mechanisms can produce weaker gravity ($G_{\text{eff}} < G_N$), such as a scalar-tensor theory in a wCDM background with w > -1 Gannouji et al. (2018); Perivolaropoulos and Kazantzidis (2019); Kazantzidis and Perivolaropoulos (2019) as well as more general modified gravity theories involving scalar fields such as Horndeski theories Linder (2018); Kennedy et al. (2018); Gannouji et al. (2021) and beyond Horndeski theories D'Amico et al. (2017). In Refs. Nesseris et al. (2017); Kazantzidis and Perivolaropoulos (2018); Perivolaropoulos and Kazantzidis (2019); Kazantzidis and Perivolaropoulos (2019) the following purely phenomenological parametrization that takes into account the solar system Pitjeva et al. (2021); Will (2006); Uzan (2003) and Big Bang Nucleosynthesis constraints Alvey et al. (2020); Uzan (2003), has been proposed as a possible solution to the growth tension

¹⁹ See Refs. Avilez and Skordis (2014); Akarsu et al. (2020b); Joudaki et al. (2022); Ballardini et al. (2021) for studies of these models without imposing this condition.

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$$G_{\rm eff}(z, g_a, n) = G_N \left[1 + g_a \left(\frac{z}{1+z} \right)^n - g_a \left(\frac{z}{1+z} \right)^{2n} \right],\tag{91}$$

where g_a is an extra parameter and n is an integer constrained at $n \ge 2$ due to solar system tests. It is straightforward to see that for $g_a < 0$ one can reproduce the required behaviour of the evolving Newton's constant. In fact, it has been shown that in the context of the parametrization in Eq. (91), negative values of this parameter are supported by RSD Nesseris et al. (2017); Kazantzidis and Perivolaropoulos (2018); Perivolaropoulos and Kazantzidis (2019); Kazantzidis and Perivolaropoulos (2019) and E_G data Skara and Perivolaropoulos (2020). Another quite interesting alternative parametrization that has the potential to address both the Hubble and growth tensions simultaneously is briefly discussed in Sec. 7.6.5. It includes a late-time abrupt transition of the absolute magnitude M at an ultra low redshift z_t of the following form Alestas et al. (2021b); Marra and Perivolaropoulos (2021); Alestas et al. (2021c)

$$M_B(z) = \begin{cases} M_B^{R20}, & \text{if } z \le z_t, \\ M_B^{R20} + \Delta M_B, & \text{if } z > z_t, \end{cases}$$
(92)

possibly coupled with an equally abrupt transition in the dark energy EoS. The transition Eq. (92), corresponds to a shift in M_B from the Cepheid measurement M_B^{R20} to the M_B^{P18} at $z = z_t$ Alestas et al. (2021b); Marra and Perivolaropoulos (2021); Alestas et al. (2021c) and according to Eqs. (101) and (104) is induced by a reduction of the ratio $\frac{G_{\text{eff}}}{G_N}$. This condition leads immediately to $G_{\text{eff}} < G_N$ in the low redshift regime, alleviating as a result the S_8 tension.

7.6.3.4. Generalized Brans-Dicke theories. Brans-Dicke (BD) theory Brans and Dicke (1961a); Dicke (1962) represents the first historical attempt of incorporating a dynamical gravitational coupling to GR. It is the simplest scalar-tensor theory which can be embedded within the broader class of Horndeski models Horndeski (1974). Apart from the metric tensor, the BD theory involves a new (scalar) degree of freedom φ that controls the strength of the gravitational interaction: $G = G_N/\varphi$, with G_N the (locally measured) Newton constant. The scalar field is non-minimally coupled to gravity via the Ricci scalar and its dynamics is controlled by a new dimensionless parameter ω_{BD} (or equivalently $\epsilon_{BD} \equiv 1/\omega_{BD}$). The action can be written, in the Jordan frame, as

$$S = \int dx^4 \sqrt{-g} \left[\frac{1}{16\pi} \left(\varphi R - \frac{\omega_{BD}}{\varphi} g^{\mu\nu} \partial_\mu \varphi \partial_\nu \varphi \right) - \rho_\Lambda \right] + \int dx^4 \sqrt{-g} \mathcal{L}_m(\chi_i, g_{\mu\nu}), \tag{93}$$

where ρ_{Λ} is the energy density (constant) of the usual vacuum energy.²⁰ The last term stands for the matter action S_m , constructed from the Lagrangian density of the matter fields, denoted by χ_i . The wave equation reads $\Box \varphi = 8\pi G_N T/(3 + 2\omega_{BD})$, with *T* the trace of the total energy-momentum tensor. GR is recovered by considering the simultaneous limits $\varphi \rightarrow 1$ and $\epsilon_{BD} \rightarrow 0$, i.e. by suppressing the dynamics of φ and matching its constant value with G_N . It follows from the action that only the first condition is needed to actually get GR+ Λ . The second condition by itself guarantees that BD goes to GR in the weak field regime, but not for higher orders in the parametrization of post-Newtonian expansion, see for instance Faraoni et al. (2020).

We denote by BD- Λ CDM the Brans-Dicke counterpart of the standard Λ CDM, i.e. the BD model with the usual vacuum energy. The latter was not present in the original BD theory and is needed to trigger the late-time acceleration of the Universe. This theory has been recently tested in the light of a large string of cosmological data Solà Peracaula et al. (2020): SNIa+BAO+H(z)+CMB+LSS, where H(z)may include or not the SH0ES prior on H_0 . Here we discuss only the results obtained including the latter, see Fig. 10. We find that the BD-ACDM model is capable of reducing the H_0 and σ_8 tensions to an inconspicuous level of ~ 1.5 σ (when the high-l polarization and lensing data from *Planck* 2018 are not considered) Solà Peracaula et al. (2020). This is pretty similar to the outcome of type-II RRVM, which the BD- Λ CDM model mimics, see Sec. 7.5.11 and Ref. Solà Peracaula et al. (2021). The BD- Λ CDM fits the cosmological data significantly better than the standard GR-ACDM model (based on GR), and this is confirmed by different statistical criteria (see Ref. Solà Peracaula et al. (2019b, 2020, 2021) for details). Values of the effective cosmological gravitational strength $\sim 7 - 9\%$ larger than G_N are preferred at $\sim 3\sigma$ CL. This is possible thanks to the fact that φ remains below 1 throughout the entire cosmic evolution while keeping the matter and radiation energy densities very close to the typical GR- Λ CDM values. This leads to higher H(z) values during all the stages of the cosmic history without changing dramatically the abundances of the matter species in the pre- and post-recombination epochs. The lowering of the sound horizon at the baryon-drag epoch, r_d , is accompanied by an increase of the Hubble parameter. This helps to alleviate the H_0 tension (cf. Fig. 10, right plot) in perfect accordance with other relevant background data sets, such as e.g. BAO and SNIa. In order not to spoil the correct fit of the CMB temperature data the model needs to accommodate values of the spectral index n_s considerably larger than the GR- Λ CDM. This causes no problem since the dynamics of φ can compensate the changes in the matter power spectrum introduced by this fact (cf. Sec. 3 of Ref. Solà Peracaula et al. (2020)). Remarkably, the model is able at the same time to cut back the σ_8 tension (or S_8 , if preferred), as can also be appraised in the right plot of Fig. 10. The loosening of this tension can be attained through a negative value of ϵ_{BD} , or a positive one if sufficiently massive neutrinos are included Solà Peracaula et al. (2020). In both cases values $|\epsilon_{BD}| \lesssim O(10^{-3})$ are found. This parameter has a direct impact on the LSS through the linear perturbation equations. For instance, for $\epsilon_{BD} < 0$ the friction term in the equation of the matter density contrast grows, and the source term decreases. Both effects contribute to the lowering of σ_8 . The compatibility between the larger cosmological value obtained for the gravitational coupling and the value measured locally, G_N , should be possible provided one can find an appropriate screening mechanism. Note, the model appears to be consistent with the findings

²⁰ It is possible to consider generalizing the original BD theory by introducing a potential $V(\varphi)$ for the scalar (Jordan) field φ Faraoni (2009). Two exceptions are particularly important, as they provide us with the simplest BD extensions of the Λ CDM model. The case with a constant potential, $V(\varphi) = \text{const}$, which, within the original BD theory, corresponds to including the usual vacuum energy (described by $p = -\rho$) as a source, is the one considered here, see the action given in Eq. (93). The other option, the case with a potential proportional to the scalar field, $V(\varphi) \propto \varphi$, corresponds to the inclusion of a bare cosmological constant along with the Ricci scalar, viz., $\varphi R \rightarrow \varphi(R - 2\Lambda)$, in the original BD action Uehara and Kim (1982); Boisseau (2011). This type of BD extension of Λ CDM has been recently investigated in light of observational data Akarsu et al. (2020b). It was found that it exhibits no significant deviations from Λ CDM all the way to the BBN epoch, and does not help with the H_0 tension.



Fig. 10. Left panel: Theoretical curves of $f(z)\sigma_8(z)$ for the GR- Λ CDM, type-II RRVM and BD- Λ CDM, together with the data points used in the fitting analysis of Ref. Solà Peracaula et al. (2021); *Right panel*: 1 and 2 σ CL regions in the (σ_8 - H_0)-plane for the same models. The type-II RRVM and BD- Λ CDM are able to alleviate the H_0 tension without worsening the σ_8 one. See also Sec. 7.5.11 and Refs. Solà Peracaula et al. (2021, 2019b, 2020). H_0 is expressed in units of km s⁻¹ Mpc⁻¹.

of Refs. Heisenberg et al. (2022a,b), once a screening mechanism is invoked. Different studies show that these mechanisms are possible, although other works find that their implementation may not be so straightforward Gómez-Valent and Hassan Puttasiddappa (2021).²¹

As pointed out above, the BD- Λ CDM model mimics the type-II RVM (cf. Sec. 7.5.11), and hence it is perceived from the GR perspective as a running vacuum model with a (very) mild dynamical gravitational coupling Solà Peracaula (2018); de Cruz Pérez and Solà Peracaula (2018); Solà Peracaula et al. (2020). The effective RVM-behaviour of the BD- Λ CDM can be made apparent if one writes the Friedmann and pressure equations in GR-like fashion, from which one can identify the characteristic RVM form of the vacuum energy density: $\rho_{\text{DE}} \sim A + B \Delta \varphi H^2$, with A and B constants and $\Delta \varphi$ tracking the departure of the effective gravitational coupling from the local G_N value Solà Peracaula et al. (2020). In Refs. Solà Peracaula et al. (2019b, 2020) it is shown that the effective EoS of the combined fluid of φ and usual vacuum energy mimics quintessence at more than 3σ CL. This feature could be the smoking gun signalling the departure from GR.

7.6.3.5. A word of caution. Using Horndeski models to address the H_0 and/or S_8 tensions comes with a significant caveat, however. The general form of the Lagrangian may be strongly constrained by requiring that the ensuing equation of motion admits a well-posed initial value formulation. In the strongly coupled regime, this issue was studied in Papallo and Reall (2017), while the weakly coupled regime was considered in Ref. Kovács and Reall (2020). In the latter, some examples of loss of uniqueness through shock formation and evolution with change in character of the equation of motion (from hyperbolic to elliptic through a parabolic stage) were presented in Bernard et al. (2019).

7.6.4. Quantum conformal anomaly effective theory and dynamical vacuum energy

Classical General Relativity receives corrections from the quantum fluctuations of massless conformal fields, through the conformal trace anomaly of the energy-momentum tensor in curved space Duff (1977); Birrell and Davies (1984)

$$\langle \hat{T}^a{}_a \rangle = b C^2 + b' \left(E - \frac{2}{3} \Box R \right) \equiv \mathcal{A}.$$
(94)

This leads to additional gravitational interactions at macroscopic distance scales Mottola and Vaulin (2006); Giannotti and Mottola (2009); Mottola (2010, 2011), as becomes clear from the local form of the effective action of the conformal anomaly,

$$S_{\mathcal{A}}[g;\varphi] = \frac{b'}{2} \int d^4x \sqrt{-g} \left\{ -\left(\Box\varphi\right)^2 + 2\left(R^{ab} - \frac{1}{3}Rg^{ab}\right)\left(\nabla_a\varphi\right)\left(\nabla_b\varphi\right) \right\} + \frac{1}{2} \int d^4x \sqrt{-g} \mathcal{A}\varphi \,, \tag{95}$$

in terms of an additional weakly coupled long range scalar field φ Antoniadis and Mottola (1992); Mazur and Mottola (2001); Mottola (2010, 2017); Coriano et al. (2019). This "conformalon" scalar φ allows vacuum energy to change, leading to a dynamical cosmological dark energy, with potentially observable effects imprinted in the CMB, GWs, and the growth of Large Scale Structure (LSS) Antoniadis et al. (1997, 2007); Mottola (2011); Antoniadis et al. (2012).

Specifically, by recognizing that the linear coupling in the anomaly action involves the topological Euler density *E*, and $\Box R$, both of which are total derivatives, $\left(E - \frac{2}{3} \Box R\right) \propto \varepsilon^{abcd} \nabla_d A_{abc}$ naturally defines a 3-form Abelian potential A_{bcd} . Hence its linear coupling to the scalar φ in (95) can be written

$$\frac{b'}{2}\int d^4x\sqrt{-g}\left(E-\frac{2}{3}\Box R\right)\varphi = -\frac{b'}{2}\frac{1}{3!}\int d^4x\sqrt{-g}\,\varepsilon^{abcd}\,\nabla_d\varphi\,A_{abc} \equiv -\frac{b'}{2\times3!}\int d^4x\sqrt{-g}\,J^{abc}A_{abc}\,,\tag{96}$$

by an integration by parts. The totally anti-symmetric tensor $F_{abcd} = \nabla_{[a} A_{bcd]}$ is the 4-form field strength corresponding to A_{abc} . If the "Maxwell" term

$$S_F = -\frac{1}{2 \times 4! \kappa^4} \int \mathrm{d}^4 x \sqrt{-g} \, F_{abcd} F^{abcd} \,, \tag{97}$$

²¹ The extensions of the BD theory may lead to modifications in the limits on ϵ_{BD} from solar system observations, see Perivolaropoulos (2010).

for this field strength is added to the effective action, where κ is a coupling constant with dimensions of mass, then the "Maxwell" equation $\nabla_d F^{abcd} = 0$ in the absence of any sources implies that $F_{abcd} = \varepsilon_{abcd} \widetilde{F}$ is a constant. Since the stress-tensor for this constant 4-form Maxwell field matched to the number of 4 spacetime dimensions is $-\widetilde{F}^2 g_{ab}/2\kappa^2$, (97) is entirely equivalent to the addition of a positive cosmological constant Λ term to the classical Einstein-Hilbert action Aurilia et al. (1978); Brown and Teitelboim (1988); Aurilia and Spallucci (2004)-in the absence of sources.

With the $I \cdot A$ coupling (96) from the anomaly, the Maxwell eq. acquires a source, and becomes

$$\nabla_d F^{abcd} = -\frac{b'\kappa^4}{2} J^{abc} = -\frac{b'\kappa^4}{2} \varepsilon^{abcd} \nabla_d \varphi, \tag{98}$$

with the derivative of the scalar conformalon φ acting as current source. Hence $\tilde{F} = -b'\kappa^4\varphi/2 + \text{const}$, and the value of the cosmological "constant" vacuum energy, determined by the value of \tilde{F}^2 can change as the scalar field φ does.

This effective field theory of the conformal anomaly (95) coupled to the 3-form potential and 4-form Maxwell field strength term is different from either scalar-tensor theories, or other modified gravity theories of the Hordenski type, but is well-founded on fundamental quantum field theory principles. The fluctuations of φ can lead to the scale invariance of the CMB being promoted to full conformal invariance, with the implication of a well-defined non-Gaussian bispectrum differing from slow roll single field inflation models Antoniadis et al. (1997, 2012).

The scalar φ also couples to the conformal part of the metric and leads to scalar "breather" mode polarization GWs, which should be produced in the early Universe Mottola (2017). Since the vacuum energy can vary in general in both space and time, this effective theory also allows the possibility of spatially inhomogeneous non-FLRW cosmologies. A detailed study of dynamical dark energy based on this theory is now just beginning, in order to derive and test its predictions against the trove of LSS and other observational data expected in this decade.

7.6.5. Ultra-late time gravitational transitions

The extremely tight constraints on the form of $H(z)/H_0$ in the range $z \in [0.01, 1100]$ Lemos et al. (2019); Efstathiou (2020) combined with the local measurement of H_0 , namely $H_0^{R20} = (73.2 \pm 1.3) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Riess et al. (2009), which is inconsistent with the CMB constraint $H_0^{P18} = (67.36 \pm 0.54) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Aghanim et al. (2020b) implies that a possible transition event may have taken place either just before z = 1100, see Sec. 7.4, or just after z = 0.01 (gravitational transition Marra and Perivolaropoulos (2021)). Such a transition event would leave intact the standard model physics in the range $z \in [0.01, 1100]$ while introducing new physics before or after this redshift (time) range. In this subsection we briefly describe the latter possibility.

The absolute luminosity of SNIa may be calibrated using two distinct independent calibrators:

- 1. The sound horizon at recombination ($z \sim 1100$) used as a standard ruler to set the scale H_0^{P18} for the Λ CDM H(z) and thus the SNIa
- absolute magnitude $M_B = M_B^{P18}$ Camarena and Marra (2020b, 2021) and luminosity (inverse distance ladder approach). 2. The locally calibrated standard candles like Cepheid stars which measure the distance to SNIa host galaxies at low redshifts (z < 0.01, D < 40Mpc) and thus calibrate the absolute luminosity L^{R20} and magnitude ($M_B = M_B^{R20}$) of SNIa leading to the best fit value H_0^{R20} Riess et al. (2009) (distance ladder approach).

The two approaches lead to values of the SNIa absolute magnitude M_B that are inconsistent at a level more than 4σ with $\Delta M_B = M_B^{R20} - M_B^{P18} \simeq -0.2$ Camarena and Marra (2021). This inconsistency is the basis of the Hubble tension because the difference in the values of M_B is easily translated to a difference in the values of the Hubble constant, since H_0 and M_B are degenerate Perivolaropoulos and Skara (2021a); Theodoropoulos and Perivolaropoulos (2021) (observable for z > 0.01 using SNIa):

$$\mathcal{M} = M_B + 5\log_{10}\left[\frac{c/H_0}{\text{Mpc}}\right] + 25\,,\tag{99}$$

which implies that a shift of M_B of

$$\Delta M_B \equiv M_B^{P18} - M_B^{R20} \approx 5 \log_{10} \frac{H_0^{P18}}{H_0^{R20}} \approx -0.2, \qquad (100)$$

is needed for a decrease of the locally (SNIa) measured H_0 by about 10% and thus a resolution of the Hubble tension.

The two measurements of M_B however (CMB sound horizon and local calibrators/SNIa) are performed at different redshift ranges: the Cepheid measurement $M_B^{R20} = -19.244 \pm 0.037$ is performed at z < 0.01 where Cepheids and other local distance calibrators are detectable while the measurement $M_B^{P18} = -19.401 \pm 0.027$ using the sound horizon is performed at z > 0.01 where the Hubble flow and the Λ CDM H(z) are applicable. Thus, the two measurements can be made consistent if a fundamental physics transition changes the SNIa absolute luminosity (or equivalently M_B) at a redshift $z_t \lesssim 0.01$ Marra and Perivolaropoulos (2021).

An abrupt step-like shift of Newton's constant G_{eff} in the context of a gravitational spatial or temporal transition could play the role of the required fundamental physics transition Alestas et al. (2021b); Marra and Perivolaropoulos (2021); Alestas et al. (2021c). In this context we have

$$\mu_G(z) \equiv \frac{G_{\text{eff}}}{G_N} = (1 + \Delta \mu_G \,\Theta(z - z_t))\,,\tag{101}$$

where G_N is the locally measured Newton's constant. A very recent false vacuum decay Coleman (1977); Callan and Coleman (1977); Patwardhan and Fuller (2014) in the context of a scalar tensor theory Lee et al. (2006) with vacua energy scale $M_{\Delta} \sim 0.002 \,\text{eV}$ and with the present horizon scale would naturally produce true vacuum bubbles on scales of Perivolaropoulos and Skara (2021a)

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$$R_b \simeq \frac{\ln(M_{\rm Pl}/M_{\Lambda})}{4H_0} \sim (15-20) \,\mathrm{Mpc}\,.$$
(102)

Thus, if we were inside such a true vacuum bubble we would observe a transition of G_{eff} at a distance of about 20 Mpc. Surprisingly, such a transition is consistent with current G_{eff} constraints Uzan (2011); Teller (1948) (which constrain mainly the time derivative of G_{eff} and much less a G_{eff} abrupt transition). In fact, hints for such a transition have recently been pointed out in Cepheid Perivolaropoulos and Skara (2021a); Mortsell et al. (2021a) and Tully-Fisher data Alestas et al. (2021a). It has also been shown that such a transition is consistent with the observed number of galaxies per redshift bin in low redshift galaxy surveys Alestas et al. (2022).

Assuming a SNIa absolute luminosity $L \sim G_{\text{eff}}^{-\alpha}$ Amendola et al. (1999); Garcia-Berro et al. (1999), where α is a parameter determined by the detailed physics of SNIa explosions, it is found that the required transition of M_B is connected with a gravitational transition of G_{eff} as

$$\Delta M_B = -\frac{5}{2} \log_{10} \left(\frac{L^{P18}}{L^{R20}} \right) = \alpha \frac{5}{2} \log_{10} \mu_G^>,$$
(103)

where L^{P18} and L^{R20} are the CMB-calibrated and Cepheid-calibrated SNIa absolute luminosities, respectively. Since the Chandrasekhar mass M_C , which plays a crucial role in the SNIa explosion, is $M_C \sim G_{eff}^{-3/2}$, it is clear that the simplest assumption is that $L \sim M_C \sim G_{eff}^{-3/2}$ which leads to $\alpha = 3/2$. In the context of this simplest generic assumption we have

$$\Delta \mu_G = 10^{\frac{1}{15}\Delta M_B} - 1 \simeq -0.1, \tag{104}$$

which is marginally consistent with current constraints on a possible transition of the Newton constant and implies the presence of weaker gravity by about 10% at times earlier than the transition time corresponding to z_t . Such weaker gravity would lead to weaker growth rate of cosmological matter fluctuations $\delta(z) \equiv \frac{\delta\rho}{\rho}(z)$ according to the dynamical linear growth equation Skara and Perivolaropoulos (2020); Kazantzidis and Perivolaropoulos (2018, 2019):

$$\delta'' + \left[\frac{(H^2)'}{2H^2} - \frac{1}{1+z}\right]\delta' \approx \frac{3H_0^2}{2H^2}(1+z)\,\mu_G(z)\,\Omega_m\,\delta\,,\tag{105}$$

where a prime denotes a derivative with respect to redshift *z*. In fact, a 10% reduction of μ_G would fit the same data with a 10% larger value for Ω_m . In the context of a gravitational transition with a Λ CDM background H(z), RSD and WL data are well fit by Abbott et al. (2019b); Skara and Perivolaropoulos (2020); Alestas et al. (2020)

$$\Omega_m^{\text{growth}} = 0.256^{+0.023}_{-0.031} = (1 + \Delta\mu_G) \,\Omega_m^{\text{P18}} \,, \tag{106}$$

which implies $\Delta \mu_G = -0.19 \pm 0.09$ when setting $\Omega_m^{P18} = 0.3153 \pm 0.0073$ Aghanim et al. (2020b) and leads to a mechanism for the resolution of the growth S_8 tension.

An ultra-late gravitational transition could also have implications on geo-chronology and solar-system chronology addressing corresponding long standing puzzles. For example observational evidence from terrestrial and lunar cratering rates indicates that the impact flux of kilometer sized objects increased by at least a factor of 2 over that last 100 Myrs compared to the long term average Alestas et al. (2021c). It has been demonstrated that such an increase could be explained in the context of the ultra-late gravitational transition required for the resolution of the Hubble and S_8 tensions.

7.7. Specific solutions assuming FLRW

In this subsection, we list some specific solutions of interest to the community that cannot be classified in the previous sections, whether because they are broad enough to enclose very different scenarios, or they simply have an impact along the whole cosmic history. We refer the reader to the more complete review Di Valentino et al. (2021g) or the original papers for a more detailed discussion of proposed solutions of the Hubble tension in: inflationary models Tram et al. (2017); Di Valentino and Mersini-Houghton (2017a); Rodrigues et al. (2020, 2021), self-interacting dark matter Binder et al. (2018), Über-gravity Khosravi et al. (2019), Nonlocal gravity Belgacem et al. (2018), Modified Gravity Lin et al. (2019b); Benetti et al. (2018b), unified fluid Yang et al. (2019g), quintessential models Di Valentino et al. (2019a), screened fifth forces Desmond et al. (2019), Generalized Chaplygin gas models Yang et al. (2019h); Benetti et al. (2021a, 2019b); Salahedin et al. (2020), Viscous Generalized Chaplygin gas Hernández-Almada et al. (2021a), addition of extra SNIa systematic uncertainties with a varying DE Martinelli and Tutusaus (2019), metastable DE Shafieloo et al. (2018a); Li et al. (2019); Yang et al. (2020e), Super-ACDM Adhikari and Huterer (2020); Adhikari (2022), DM-photon coupling Yadav (2019), Local Inhomogeneity Kasai and Futamase (2019), Interaction in the anisotropic Universe Amirhashchi and Yadav (2020), Heisenberg uncertainty Capozziello et al. (2020); Spallicci et al. (2022), Enhanced Early gravity model Zumalacarregui (2020); Joudaki et al. (2022), CMB monopole temperature Ivanov et al. (2020a), Decaying Ultralight Scalar Gonzalez et al. (2020), Decaying coupled fermions Benisty (2019), Early mass varying neutrino DE Gogoi et al. (2021), Neutrino-majoron interactions Escudero and Witte (2020); Escudero Abenza and Witte (2020); Escudero and Witte (2021), Light gravitino scenarios Choi et al. (2020b), Degenerate decaying fermion DM Choi et al. (2020c), Lifshitz cosmology Berechya and Leonhardt (2021), a frame dependent, scale invariant DE Adler (2019), light gravitino dark matter with a small non-thermal fraction Gu et al. (2020), cosmology with a Bianchi type-I metric Akarsu et al. (2019b), Finslerian models Wang and Meng (2018), Dark Energy model from Generalized Proca Theory Geng et al. (2021), Axi-Higgs Universe Fung et al. (2021); Luu (2021), transitional dark energy Zhou et al. (2022), interaction between dark matter and the baryonic component in a modified gravity scenario Adil et al. (2021), Minimal Theory of Massive Gravity de Araujo et al. (2021), Bound Dark Energy de la Macorra et al. (2022), Chameleon Early Dark Energy Karwal et al. (2021), interacting dark energy axions Mawas et al. (2021), the mirror twin Higgs model Bansal et al. (2021), Milgromian gravity Banik and Zhao (2021), a quantum origin for the DE Belgacem and Prokopec (2021), Emergent DE from unparticles Artymowski et al. (2021a,b), General Relativistic Entropic Acceleration theory Arjona et al. (2021b).

7.7.1. Active and sterile neutrinos

The existence of massive neutrinos (either active or sterile) has been confirmed by various observational surveys Araki et al. (2005); Ashie et al. (2005); Abe et al. (2008) and their presence can affect the cosmological parameters (see Refs. Lesgourgues and Pastor (2006); Conrad et al. (2013) for more discussions on the massive neutrinos). According to the observational surveys, the sum of the active neutrino masses, $\sum m_{\nu}$, must be at least 0.06 eV Gonzalez-Garcia et al. (2012). Additionally, some observational experiments indicate that there could be a sterile neutrino which does not interact with the standard model Conrad et al. (2013), but it still contributes a mass $m_{\nu,\text{sterile}}^{\text{eff}}$ and in a model dependent way, an increase in the total number of effective relativistic degrees of freedom, $N_{\text{eff}} = 3.046 + \Delta N_{\text{eff}}$. It has been found that the active and sterile neutrinos in the Universe sector can be effective to alleviate the S_8 tension Battye and Moss (2014); Böhringer and Chon (2016). A Pseudo-Dirac sterile neutrino has been instead proposed as a model to alleviate the Hubble tension in Ref. Chao et al. (2021), as well as an extended parameter space with ground-based CMB data and a total active neutrino mass different from zero Di Valentino and Melchiorri (2021).

7.7.2. Cannibal dark matter

Cannibalistic dark matter models were initially proposed by Refs. Dolgov (1980); Carlson et al. (1992); Dolgov (2017) in the context of general self-interacting dark matter Dolgov et al. (1995); de Laix et al. (1995); Machacek (1994). Such models have received a resurgence of interest within the last decade Hochberg et al. (2015); Kuflik et al. (2016); Pappadopulo et al. (2016); Farina et al. (2016); Erickcek et al. (2021) given their promising ability to impact both the small-scale crisis Spergel and Steinhardt (2000); de Blok (2010); Boylan-Kolchin et al. (2011); Salucci (2019) and the *S*₈ tension Buen-Abad et al. (2018a); Heimersheim et al. (2020).

If the Lagrangian of a massive dark matter candidate permits $2 \leftrightarrow 3$ interactions, such as in Refs. Bernal et al. (2016a); Chu and Garcia-Cely (2017); Bernal et al. (2018); Heeba et al. (2018), it is possible that it exhibits a cannibalistic behaviour. When the species' thermal energy is high compared to its mass, both the $3 \rightarrow 2$ and $2 \rightarrow 3$ interactions will be balanced, and the dark matter will behave as an ordinary relativistic species. However, as the species cools and the thermal energy becomes insufficient to overcome the mass gap inherent in the $2 \rightarrow 3$ interaction, a cannibalistic phase begins, in which the mass energy of particles is converted through an efficient $3 \rightarrow 2$ interaction into thermal energy. As soon as the $3 \rightarrow 2$ interaction freezes out (when the number density is sufficiently diluted due to the expansion of the Universe), the species continues to behave like ordinary cold dark matter. In its cannibalistic regime the species is close to (but not quite) relativistic for an extended time, allowing the species to keep a large Jeans scale (suppressing growth on small scales) while avoiding coupling to other relativistic species through the Einstein equations (and thus impacting CMB observables). As such, the cosmological evolution is very similar to that of warm dark matter, except for the intermediate cannibalistic phase, which allows the model to have a reduced impact on the CMB while still strongly suppressing the power spectrum.

While the initial investigations Buen-Abad et al. (2018a); Heimersheim et al. (2020) in terms of cosmological evolution have shown a promising parameter region, more work is required both at the level of theoretical modelling and complimentary experimental constraints. In particular, joint investigations of constraints from CMB, weak lensing, $Ly-\alpha$ data, and/or small scale probes of clustering would be required to further investigate the validity of this model.

7.7.3. Decaying dark matter

The Λ CDM model postulates the additional form of Dark Matter (DM) which clusters gravitationally but is (almost) immune to other interactions. The nature of DM remains elusive so far. From a theoretical point of view, DM can be easily multi-component itself.²²

One interesting approach that provides a composite content of DM is decaying DM (dDM).²³ The motivation of this scenario arises in purely theoretical considerations Ibarra et al. (2013), it also can explain some interesting experimental results Ibarra et al. (2014); Cirelli et al. (2012); Anchordoqui et al. (2015); Lovell et al. (2015); Iakubovskyi (2014) and address the small-scale problems of the cold DM paradigm Wang et al. (2014); Cheng et al. (2015). The decaying DM model was developed in the 1980s Flores et al. (1986); Doroshkevich et al. (1989) and has recently gained renewed interest because of the appearance of persistent tensions between low-redshift measurements and predictions of the Λ CDM cosmology.

There exist several varieties of the decaying DM proposal. DM can be a single unstable component decaying into invisible radiation with a lifetime exceeding the age of the Universe Audren et al. (2014). This scenario was suggested as a resolution of the S_8 tension, however, the current cosmological data is not constraining enough to unambiguously favour a non-zero DM decay rate Enqvist et al. (2015). Alternatively, the unstable DM may decay to the massive particles and invisible radiation at late times Aoyama et al. (2014); Del Nobile et al. (2016) or even undergo a many-body decay Blackadder and Koushiappas (2014, 2016). However, this decaying DM scenario is unlikely to alleviate the H_0 -tension Haridasu and Viel (2020); Chen et al. (2021a).²⁴ More progress towards reconciling discrepancies between different cosmological measurements can be achieved if one assumes an earlier decay of the DM constituents.

In Ref. Berezhiani et al. (2015) it was argued that the subdominant DM component decaying after recombination may alleviate the cosmological tensions. This decaying DM setup has two extra parameters with respect to the Λ CDM scenario – a fraction of decaying component in the total DM abundance, $f_{dDM} = \omega_{dDM,i}/(\omega_{dDM,i} + \omega_{CDM,i})$ where $\omega_i \equiv \Omega_i h^2$ denotes *initial* densities of decaying and cold DM components, and its inverse lifetime, or width, Γ . The background dynamics for unstable DM (ρ_{dDM}) and dark radiation (ρ_{DR}) abundances is driven by

$\dot{\rho}_{\rm dDM} + 3H\rho_{\rm dDM} = -\Gamma\rho_{\rm dDM},$	(107)
$\dot{\rho}_{\mathrm{DR}} + 4H \rho_{\mathrm{DR}} = \Gamma \rho_{\mathrm{dDM}}$.	(108)

²² Idea of multi-component DM is inspired by the apparent complexity of the "visible" sector. For instance, the current cosmological data resolve at least three different components: photons, neutrinos, and baryons. It seems to be natural that DM which dominates the matter content of the Universe also consists of several different species.
²³ Not to be confused with the "Dynamical Dark Matter" (DDM) model discussed in Sec. 7.7.4.

²⁴ The somewhat related model in which self-interacting dark matter may be converted into a non-interacting form of radiation with rate proportional to the cosmic expansion Bjaelde et al. (2012); Pandey et al. (2020) is also disfavoured by data Liu et al. (2022).



Fig. 11. Posterior distributions (1 σ and 2 σ contours) in the $\Gamma - f_{dDM}$ (*left panel*) and f_{dDM} - H_0 (*right panel*) planes. This analysis includes the full *Planck* likelihood for TT,TE,EE and lensing power spectra, the galaxy cluster counts from *Planck* catalogues, the local measurement of H_0 from SHOES combined with galaxy BAO ("Zhao"), galaxy RSD ("Chuang") or Ly- α BAO ("Ly α ") measurements from the BOSS DR12 samples. The panels are taken from Ref. Chudaykin et al. (2018).

A slightly reduced matter content in the late Universe helps accommodate a low S_8 in full accordance with local probes of Large Scale Structure (LSS). Remarkably, the downward shift in the total matter density must be accompanied by the upward shift of H_0 to keep the angular acoustic scale of the CMB intact. However, the lack of DM at low redshifts reduces the power of the CMB lensing effect which is in odds with the *Planck* observations. Thus, the CMB data alone put the stringent limits on this proposal, $f_{dDM} < 4\% (2\sigma)$ Chudaykin et al. (2016); Poulin et al. (2016) from the Planck 2015 data and $f_{dDM} < 2\%(2\sigma)$ Nygaard et al. (2021) using the newest Planck 2018 likelihood. Including the BAO measurements from BOSS DR12 induces even tighter constraints on the decaying DM fraction by a factor of \sim 1.3 – 1.5 Chudaykin et al. (2018); Nygaard et al. (2021). Corresponding constraints in the $\Gamma - f_{dDM}$ and $f_{dDM} - H_0$ subspaces for a different choice of large-scale structure data are shown in Fig. 11. Since a full resolution of the Hubble tension requires $f_{\rm dDM} \sim 10\%$ Berezhiani et al. (2015) the CMB and BAO analysis makes the decaying DM solution of H₀-tension increasingly unlikely. The main culprit of these strong constraints is a so-called "lensing-like anomaly" in the Planck data that over-predicts the CMB lensing signal Aghanim et al. (2017, 2020b) and thus strongly disfavours the decaying DM solution which, in turn, favours a weaker lensing effect. In this regard, it is curious to see what fraction of decaying DM is available upon marginalizing over the lensing information in the Planck power spectra. By allowing the CMB lensing power amplitude A_{lens} to be a free fitting parameter, the CMB and BAO data along with the Planck cluster counts and SH0ES measurement yield $f_{dDM} = 0.06 \pm 0.02\%$ Chudaykin et al. (2018). Overall, this analysis indicates a mild 1.6 σ preference in favour of the decaying DM scenario over ACDM Chudaykin et al. (2018). Therefore, before making strong conclusions it has to be understood first why the Λ CDM prediction is in tension with the *Planck* CMB lensing effect.

One way to mitigate the tight CMB constraints is to assume a short-lived decaying DM component which decays *before* recombination. Recent investigations Poulin et al. (2016); Nygaard et al. (2021) reveal interesting implementations of the subdominant unstable component of DM decaying between matter-radiation equality and recombination epochs. The tight *Planck* constraints on f_{dDM} in this case can be significantly alleviated Poulin et al. (2016); Nygaard et al. (2021). Moreover, a decay near matter-radiation equality reduces the sound horizon at the drag epoch, r_d , alleviating the tensions with the late-time model-independent probes of r_d , see Ref. Bernal et al. (2016b). However, the Hubble tension in this scenario is only marginally alleviated Poulin et al. (2016); Nygaard et al. (2021). Like an EDE proposal, in the short-lived decaying DM model, the growth of both metric and density perturbations is amplified that exacerbates (although weakly) the S_8 tension.

It was recently proposed that a fraction of DM particles which decay into a much lighter stable relic and photon can solve the long-standing Lithium problem Di Bari et al. (2013). The electromagnetic injection in the specific energy range would destroy enough Lithium without affecting the abundance of other elements. Since the light decay products act as dark radiation in the early Universe, this scenario was also suggested to alleviate the H_0 tension Alcaniz et al. (2021). However, this proposal is tightly constrained by the *Planck* data Anchordoqui (2021). Model-independent constraints from BBN on unstable DM which decay into photons and/or electron-positron pairs are provided in Ref. Depta et al. (2021).

Overall, the totality of the cosmological data put tight constraints on the decaying DM scenario as a resolution of S_8 and H_0 tensions although a few percent decaying DM fraction is still allowable Chudaykin et al. (2018); Nygaard et al. (2021). For models with a subdominant component of DM decaying between recombination and the present epoch, the understanding of the "lensing-like anomaly" in the *Planck* data is highly warranted because this feature is responsible for stringent CMB limits on this proposal. To conclude, the current S_8 and H_0 tensions require either a different (and possibly major) alteration of the Λ CDM model, or derives from some yet unknown systematic effect.

The cosmological scenarios where the heavier particles decay to lighter and invisible radiation are argued to weaken the S_8 tension Aoyama et al. (2014); Enqvist et al. (2015); Abellán et al. (2020). These scenarios also relax the tension of CDM predictions with observation of structures at small scales Wang et al. (2014); Cheng et al. (2015) and can elucidate the origin of high-energy neutrino IceCube events Anchordoqui et al. (2015, 2021c). Ultrahigh-energy cosmic ray experiments could be powerful probes of dDM models in which DM couples to the SM sector Anchordoqui (2019).

7.7.4. Dynamical dark matter

Although many models of decaying DM transcend the canonical WIMP or axion frameworks and involve new regions of the DM parameter space, perhaps none do so as dramatically as those that arise within the Dynamical Dark Matter (DDM) framework. The basic

idea behind DDM is relatively simple Dienes and Thomas (2012a). Rather than focus on one or more stable DM particles, the DDM framework is built on the proposition that the DM in the Universe comprises a vast *ensemble* of interacting fields with a variety of different masses, mixings, and cosmological abundances. Moreover, rather than imposing the stability for each field individually, the DDM framework recognizes that the decay of a DM component in the early Universe is not ruled out if the cosmological abundance of that component is sufficiently small at the time of its decay. The phenomenological viability of the DDM framework therefore requires that those states within the ensemble with larger masses and SM decay widths have correspondingly smaller relic abundances, and vice versa.

In other words, DM stability is not an absolute requirement in the DDM framework, but is replaced by a balancing of lifetimes against cosmological abundances across the entire ensemble. As a result, individual constituents of the DDM ensemble are decaying throughout the evolution of the Universe, from early times until late times and even today. This leads to a highly dynamical scenario in which cosmological quantities such as the total DM abundance Ω_{DM} experience a non-trivial time dependence beyond those normally associated with cosmological expansion.

Many extensions to the SM give rise to large ensembles of dark states in which such a balancing naturally occurs. Moreover, because the DM "candidate" in this framework consists of a carefully balanced DDM ensemble which cannot be characterized in terms of a single well-defined mass, decay width, or interaction cross section, this framework gives rise to many striking experimental and observational signatures which transcend those usually associated with DM and which ultimately reflect the collective behaviour of the entire DDM ensemble.

The DDM framework was originally introduced in Ref. Dienes and Thomas (2012a), while in Refs. Dienes and Thomas (2012b,c) explicit DDM models were constructed which satisfy all known collider, astrophysical, and cosmological constraints. Since then, a considerable body of work has focused on various aspects of the DDM framework. One major direction of research consists of analyzing the various signatures by which this framework might be experimentally tested and constrained. These include unique DDM signatures at direct-detection experiments Dienes et al. (2012a), at indirect-detection experiments Dienes et al. (2012b, 2015b); Curtin et al. (2018); Dienes et al. (2020b, 2021c).

Indeed, such DDM scenarios also give rise to enhanced complementarity relations Dienes et al. (2015a, 2017c) between different types of experimental probes. Moreover, the non-minimal dark sectors which are the cornerstone of the DDM framework can also lead to observable imprints across the cosmological timeline, stretching from structure formation Dienes et al. (2020a, 2021a) all the way to late-time supernova recession data Desai et al. (2020) and unexpected implications for evaluating Ly- α constraints Dienes et al. (2021b). Such dark sectors also give rise to new theoretical possibilities for stable mixed-component cosmological eras and a potential re-examination of the age of the Universe Dienes et al. (2022).

The second direction of DDM research over the past decade has focused on the numerous ways in which suitably-balanced DDM ensembles – i.e., ensembles of dark states in which the widths for decays into SM states are naturally inversely balanced against cosmological abundances – emerge naturally within various models of BSM physics. These include theories involving large extra dimensions, both flat Dienes and Thomas (2012a,b) and warped Buyukdag et al. (2020); theories involving strongly-coupled hidden sectors Dienes et al. (2017a); Buyukdag et al. (2020); theories involving large spontaneously-broken symmetry groups Dienes et al. (2016a); and even string theories Dienes et al. (2017a).

Indeed, the dark states within these different realizations can accrue suitable cosmological abundances in a variety of ways, including not only through non-thermal generation mechanisms such as misalignment production Dienes and Thomas (2012a,b) but also through thermal mechanisms such as freeze-out Dienes et al. (2018). Mass-generating phase transitions in the early Universe can also endow collections of such states with non-trivial cosmological abundances Dienes et al. (2016b, 2017b, 2016c).

In general, the mass spectra and corresponding lifetimes and abundances of the individual states within the DDM ensemble turn out to be tied together through scaling relations involving only a few scaling exponents. This is reviewed, for example, in Sect. III of Ref. Curtin et al. (2018). The particular physical scenario that one has in mind within the DDM framework then determines these scaling exponents. As a result, the DDM ensemble is described by only a few free parameters, rendering the DDM framework every bit as constrained and predictive as more traditional dark-matter scenarios.

DDM scenarios in which the constituents decay entirely within the dark sector - i.e., to final states comprising other, lighter ensemble constituents and/or dark radiation - are particularly challenging to probe and constrain. Nevertheless, there exist observational handles that can be used to probe and constrain DDM ensembles which decay primarily via "dark-to-dark" decay processes of this sort, and thus potentially permit us to distinguish them from traditional DM candidates.

For example, dark-to-dark decays of this sort modify the way in which the expansion rate of the Universe, as described by the Hubble parameter H(z), evolves with redshift. These modifications, in turn, affect the functional relationship between the redshifts z and luminosity distances $D_L(z)$ of Type-Ia supernovae. In Ref. Desai et al. (2020), constraints based on the observed relationship between the redshifts and luminosity distances of Type-Ia supernovae within the combined Pantheon sample Scolnic et al. (2018) were derived for DDM ensembles whose constituents decay via a two-body process of the form $\chi_\ell \rightarrow \bar{\psi}\psi$, where ψ is a massless dark-radiation field. A partial summary of these constraints is provided in Fig. 12.

Since the dark-to-dark decays of a DDM ensemble alter the dependence of H(z) on z, the DDM framework can potentially also provide a way of addressing the H_0 tension. In this regard, the advantage of a DDM ensemble relative to a single decaying dark-matter species is that the timescale across which the decays have a significant impact on the expansion rate can be far broader. Nevertheless, the depletion of the overall DM abundance at late times due to χ_{ℓ} decays leads to a suppression of the CMB lensing effect – and therefore to tension with *Planck* data – just as it does in other late-time decaying DM scenarios Chudaykin et al. (2016). DDM scenarios in which the χ_{ℓ} decay directly into dark radiation are significantly constrained Anchordoqui et al. (2022).

By contrast, scenarios in which the χ_{ℓ} decays primarily via intra-ensemble processes – e.g., of the form $\chi_{\ell} \to \chi_m \bar{\psi} \psi$, where ψ once again denotes a dark-radiation field – are more promising Anchordoqui (2021); Anchordoqui et al. (2022). Such decays endow the final-state χ_m with non-negligible velocities, thereby modifying the equation of state $w_m(z)$ for each ensemble constituent and modifying the DM velocity distribution of the ensemble as a whole. Moreover, complementary scattering processes of the form $\chi_{\ell} \psi \to \chi_m \psi$ through which the different ensemble constituents interact with the dark radiation could potentially also help to ameliorate the σ_8 tension in the same way that they do in partially acoustic DM scenarios Chacko et al. (2016).



Fig. 12. Constraints from Type-Ia supernova data on DDM ensembles whose constituents χ_{ℓ} decay directly to dark radiation. The parameters γ and ξ respectively parametrize the manner in which the abundances and decay widths of the χ_{ℓ} scale across the ensemble as a function of m_{ℓ} . In each panel, the contour plot shows the 3σ lower bound on the lifetime of the lightest ensemble constituent. The results displayed in the left, center, and right panels respectively correspond to ensembles consisting of N = 2, N = 10, and $N = 10^5$ fields. In all cases, the mass splitting $m_{\ell+1} - m_{\ell}$ between successive states in the ensemble is taken to be equal to the mass of the lightest ensemble constituent. All the panels are taken from Ref. Desai et al. (2020).



Fig. 13. *Left panel*: Two examples of DM velocity distributions $g(v) \propto v^3 f(v, 0)$ which have the same present-day average velocity and would naïvely be characterized by the same free-streaming horizon $k_{\text{FSH}} \approx 1.1 h/\text{Mpc}$. The dashed gray curve is the distribution for a warm-dark-matter model, while the solid green curve represents a distribution generated by decay cascades within a non-minimal dark sector Dienes et al. (2020a). *Right panel*: Contours of *R*, plotted within a slice of the parameter space of a model for which g(v) consists of two log-normal peaks, where *R* is a ratio quantifying the difference between the results of two recasting methods König et al. (2016); Murgia et al. (2017) commonly employed in estimating Ly- α constraints on non-cold DM models. The degree to which *R* differs from unity provides a measure of the degree to which the results of the recasts differ. The two thick black curves indicate the Ly- α constraints obtained from these two recasts. The region above and to the right of each of these thick black curves is excluded by the corresponding recast. Both panels are similar to figures which appear in Ref. Dienes et al. (2021b).

In this connection, it is also worth noting that it is not merely the value of σ_8 alone, but rather the detailed dependence of the amplitude of matter-density perturbations across a broad range of wavenumbers, which provides an observational handle on DM scenarios with non-cold DM velocity distributions f(v, z). In such scenarios, free-streaming effects lead to a suppression of cosmic structure on small scales. For DM models such which yield relatively simple, unimodal forms for f(v, z) at all z, assessing the impact of these effects on P(k) is comparatively straightforward.

By contrast, in the context of non-minimal dark-sector scenarios wherein a significant fraction of the dark-matter abundance is produced non-thermally (e.g., from particle decays) and wherein f(v, z) can be highly non-trivial and even multi-modal, the impact of free-streaming on small-scale structure is more complicated König et al. (2016); Heeck and Teresi (2017); Dienes et al. (2020a); Du et al. (2021); Decant et al. (2021). For example, standard "recasting" procedures König et al. (2016); Murgia et al. (2017) employed in deriving constraints on f(v, z) from Ly- α -forest data can become unreliable for velocity distributions of this sort. A study of the performance of these recasts for general dark-matter velocity distributions was performed in Ref. Dienes et al. (2021b). Results from a study of this sort are shown in Fig. 13.

On the other hand, there exist methods Dienes et al. (2020a) which permit one to reconstruct the detailed shape of f(v, z) solely from information contained within the linear matter power spectrum P(k) – methods which are applicable even when that shape is highly non-trivial. In cases in which P(k) differs from the matter power spectrum $P_{CDM}(k)$ for CDM primarily due to free-streaming effects, these methods are quite robust in their applicability and are capable of reconstructing the DM velocity distribution with impressive fidelity. By contrast, the situation becomes more subtle in cases wherein the growth of density perturbations at late times is affected by additional complications – such as decays of the χ_{ℓ} after last scattering and/or dark acoustic oscillations Cyr-Racine et al. (2014) of the sort which would arise from non-negligible interactions between ψ and the χ_{ℓ} . Nevertheless, the relationship between small-scale structure and the dark-matter velocity distribution can provide a valuable cross-check on cosmological models of this sort.

7.7.5. Extended parameter spaces involving A_{lens}

Extended cosmological scenarios beyond the 6-parameter Λ CDM model including the A_{lens} parameter free to vary have been widely investigated in the literature, showing that when $A_{\text{lens}} > 1$ as preferred by the *Planck* data, see the discussion in Sec. 6.1, the S_8 tension disappears Di Valentino et al. (2015, 2016d, 2017a); Di Valentino and Bridle (2018); Di Valentino et al. (2020b); Benisty (2021); Di Valentino et al. (2021f). This could suggest a possible systematic error present in the *Planck* data not accounted for, that is producing the disagreement with the weak lensing and cluster counts measurements. Once the data analysis of the CMB data marginalizes over this A_{lens} phenomenological parameter, the agreement between the S_8 parameter obtained by the *Planck* data and the low redshift measurements is restored.

7.7.6. Cosmological scenario with features in the primordial power spectrum

In Hazra et al. (2019) without considering any extension to the standard model at the background level, authors project the effect of the differences in the values of the key cosmological parameters to the form of the primordial power spectrum (PPS). In order to realize this task, they did uncover the form of the primordial spectrum by implementing the Modified Richardson-Lucy algorithm (MRL) Shafieloo and Souradeep (2004); Shafieloo et al. (2007); Nicholson and Contaldi (2009); Hazra et al. (2013, 2014) that would fit the *Planck* temperature data as good as the case of the concordance Λ CDM model, but with a Hubble constant consistent with local measurements, as well as improving the consistency between the derived S_8 and σ_8 parameters with estimations of the weak lensing surveys. Recently there have been more progress in this line to address various tensions by a featured form of the primordial spectrum Hazra et al. (2022). In this context, Antony et al. (2022) introduces examples of single field inflationary trajectories beyond the slow-roll regime that provides improvements in the *Planck* data compared to the standard model – partially mimics the effect of unphysical excess lensing and closed Universe. This model simultaneously prefers a higher H_0 and lower S_8 – a trend that is enhanced with the addition of H_0 data from the SH0ES measurements.

Furthermore and in Ref. Keeley et al. (2020a) authors did explore a class of primordial spectra that can fit the observed cosmic microwave background data well and that could result in a larger value for the Hubble parameter consistent with the local measurements. This class of spectra consists of a continuous deformation between the power law primordial spectrum and the reconstructions from the MRL deconvolution algorithm. More works are needed to assign significance to such features and seek for possible theoretical implementation from inflation Pimentel et al. (2022). Testing such a form of the primordial spectrum as initial conditions against other cosmological observations would be another important task in this direction.

7.7.7. Interacting dark matter

Several models of interacting dark matter feature a suppression of the matter power spectrum. Some of these models have a cosmologically relevant suppression impacting the S_8 tension even after taking into account constraints from the CMB. In particular, dark matter interactions with photons or neutrinos Ali-Haïmoud et al. (2015); Weiner and Yavin (2012); Wilkinson et al. (2014b); Diacoumis and Wong (2019) have shown to impact structure formation Boehm and Schaeffer (2005); Bringmann et al. (2014); Cherry et al. (2014); Boehm et al. (2014); Wilkinson et al. (2014a); Di Valentino et al. (2018a); Olivares-Del Campo et al. (2018); Escudero et al. (2018); Kumar et al. (2018); Stadler and Bœhm (2018); Stadler et al. (2019); Becker et al. (2021). This is because the small residual interactions introduce a collisional damping on small scales (for which the Fourier modes entered the Hubble horizon early enough to experience significant interactions) that suppresses the power spectrum on these scales. Similarly, interactions with a dark radiation component have also been invoked in the past Cyr-Racine et al. (2014); Chu and Dasgupta (2014); Rossi et al. (2015); Buen-Abad et al. (2015); Schewtschenko et al. (2016); Lesgourgues et al. (2016); Cyr-Racine et al. (2016); Krall et al. (2017); Archidiacono et al. (2017); Buen-Abad et al. (2018b); Archidiacono et al. (2019), though these have been found to be more promising in terms of the Hubble tension Lesgourgues et al. (2016); Becker et al. (2021); Velten et al. (2021). Interacting models and their consequences were considered in several papers reviewed in Wang et al. (2016).

7.7.8. Quantum landscape multiverse

The authors of Refs. Holman and Mersini-Houghton (2006, 2005); Mersini-Houghton (2015, 2008) showed in 2005 that the mystery of the unlikely origin of our Universe can be answered and derived within the framework of a larger phase space of initial conditions, by means of quantum cosmology, when the out of equilibrium dynamics of gravitational and matter degrees of freedom is taken into account. It has been initially proposed Mersini-Houghton (2005); Kobakhidze and Mersini-Houghton (2007); Mersini-Houghton (2006) to allow the wavefunction of the Universe to propagate through the stochastic structure of the string theory landscape vacua, by considering the later to be a physical realization of the phase space of initial conditions from which Universes can spring into existence, and thereby *derive instead of postulate* the probability of the selection of our initial conditions by means of quantum cosmology.

In the second stage, the decoherence among the branches of the wavefunctions was included, thus extending the mini-superspace of three-geometries and landscape moduli fields to include an infinite number of long wavelength fluctuations of space time and of the moduli, which provided the environment and it is sufficiently weakly coupled to the system in order to not interfere with it in process of measurement. Mathematically, this complex system of the wavefunction of the Universe being a functional of an infinite dimensional superspace is similar to known condensed matter systems such as spin glass and quantum dots, and can be solved by means of random matrix theory. Solutions found for the branches of the wavefunction of the Universe Holman and Mersini-Houghton (2006, 2005); Mersini-Houghton (2008, 2015) revealed that: firstly, a whole family of wavepackets of branches of the wavefunction that settled on high energy vacua on the landscape undergo a similar expansion history like our Universe to transition from a quantum to a classical universe, they survive the backreaction of matter fluctuations (which tries to slow their growth), and therefore have the highest chance of existence, while the ones that settled on low energy vacua cannot survive the backreaction matter and remain quantum particles forever; secondly, since there is a whole family of solutions that survive and grow to classical Universes, then the answer to the question of our high energy cosmic inflation comes at the price of extending our standard model of cosmology to a quantum multiverse framework in which our Universe is embedded and is just a humble member in a vastness.

The attraction of this theory is that for the first time it provided an answer to the problem of our unlikely initial state, and it did so by deriving it from first principles, namely to: why our Universes originate from a high energy low and entropy state? Having a formalism

of well trusted quantum equations which allows us to follow consistently a coherent story of evolution of our Universe from before it inflated, when it was just a branch of the wavefunction on some landscape energy vacua, follow it through cosmic inflation, and after it transitions into a large classical Universe, opens a window from which we can glean into the larger structure on which our Universe was embedded, it allows us a way to collect evidence on the multiverse. Until this work, the conventional wisdom was that limited by the speed of light, we cannot test the existence of multiverse and therefore any theory of the multiverse cannot be scientific. Since, the multiverse research has become a mainstream field in cosmology.

In Refs. Holman et al. (2006a,b); Mersini-Houghton (2017) the authors realized that quantum entanglement and decoherence are two sides of the same coin, and that the backreaction of the long wavelength fluctuations, very weakly coupled to the system being 'watched' (our Universe), which triggers decoherence and destroys entanglement among the different branches which becomes decohered Universe, leaves its traces on our CMB sky. The authors proposed to calculate them and thus use quantum entanglement as a way to test this theory and collect evidence for the quantum multiverse in which our Universe is embedded. In two papers named, "Avatars of the Landscape" in 2005 Holman et al. (2006a,b); Mersini-Houghton (2017) they derived a series of predictions leftover in our sky from the early quantum origins, including the Cold Spot, a suppressed σ_8 , a supersymmetry breaking scale which is much higher than the expected tEV scale, a power asymmetry between the two hemispheres, suppressed multipoles at the lowest *l's* and so on. Later observations with WMAP and *Planck* confirmed the existence of these anomalies at exactly the scales and sized that were predicted in Refs. Holman et al. (2006a,b); Mersini-Houghton (2017), in the case of the Cold Spot at a significance higher than 4.

The reason for the giant void that shows as a Cold Spot in temperature CMB maps, and the suppressed value of σ_8 is that the entanglement of our Universe at its infancy with all the other branches of the wavefunction and the backreaction from the collective contribution of long wavelength fluctuations which was calculated in Refs. Holman et al. (2006a,b); Mersini-Houghton (2017) provided a second source of fluctuations that contributed to CMB in addition to the typical inflationary fluctuations. Since the only scales in this problem are the energy of cosmic inflation and that of SUSY breaking scale, then the model does not allow much tweaking room for fitting data to the model. Therefore in Refs. Di Valentino and Mersini-Houghton (2019, 2017b,a) the status of this theory has been checked with the most recent and detailed *Planck* satellite data and found it is reassuring that the fit of anomalies predicted in the theory continues to be robust.

7.7.9. Quantum Fisher cosmology

The aim of Quantum Fisher Cosmology Gomez and Jimenez (2020a); Gómez and Jimenez (2020, 2021b,a); Gomez and Jimenez (2021) is to use the quantum Fisher information about pure de Sitter states to derive model independent observational consequences of the existence of a primordial phase of the Universe of de Sitter accelerated expansion. These quantum features are encoded in a scale dependent quantum cosmological tilt that defines what we can call the de Sitter universality class. The experimental predictions are: i) A phase transition from red into blue tilt at a scale order $k = 1 \text{ Mpc}^{-1}$ that naturally solves the cosmological *trans-Planckian problem*, ii) A spectral index for curvature fluctuations at CMB scales $k = 0.05 \text{ Mpc}^{-1}$ equal to 0.0328, iii) A tilt running at scale $k = 0.002 \text{ Mpc}^{-1}$ equal to -0.0019, iv) An enhancement of the amplitude of CMB peaks for extremely high multipoles ($l > 10^5$) that can provide a natural mechanism for primordial black hole formation as a source of dark matter, v) A lack of power at scales of 8 Mpc with respect to the CMB scale that can explain the σ_8 tension.

The key ingredient is the quantum Fisher information associated with the family of de Sitter invariant vacua describing scalar spectators in a pure de Sitter background. These pure states are sometimes denoted, in the literature, as α -vacua. What the quantum Fisher information naturally defines is a metric on this set of states. In essence, it measures the quantum distinguishability of different α vacua. There exists an extensive literature on both the quantum consistency of α -vacua as well as on the physical viability of using the Bunch Davis vacuum to define the quantum fluctuations describing the CMB spectrum of fluctuations. Some of these problems are related with the trans-Planckian problem and the computation of one loop effects on these vacua. We will surpass some of these well known difficulties focusing on a well defined quantity associated with the family of α vacua, namely the quantum Fisher information associated with this one parameter family of pure states. As stressed before, this quantum information naturally leads to a finite quantum variance for the parameters labelling these vacua. The main message of our work is that this quantum variance can account for the anomalous scale dependence of the cosmological power spectrum normally derived after adding a quasi de Sitter deformation. Moreover, this quantum information encodes the quantum variance of the α parameter. The parameter α can be associated with a natural energy scale defined as $k\eta H$. More precisely $\alpha = \ln \tanh(r(\Lambda)) - 2i\phi(\Lambda)$ with $r(\Lambda) = -\sinh^{-1}(\frac{H}{2\Lambda})$ the standard squeezing parameter and $\phi(\Lambda) = -\frac{\pi}{4} - \frac{1}{2} \tan^{-1}(\frac{H}{2\Lambda})$ with $\Lambda = Hk|\eta|$.

The starting point of the quantum Fisher approach to Cosmology is to identify the scale transformations of this quantum Fisher information. In other words, we are interested in identifying how the information controlling the quantum variance of α depends on the energy scale at which we are working. The main finding of Gomez and Jimenez (2020a); Gómez and Jimenez (2021b); Gomez and Jimenez (2021) is that this scale transformation of the quantum Fisher is anomalous with a scale dependent tilt defined as α_F . This is the tilt depicted in Fig. 14. As discussed in Gomez and Jimenez (2020b) this figure represents the numerical result obtained after evaluating the quantum Fisher information with an IR cutoff on the number of contributing entangled pairs. The sensitivity of the result on this IR cutoff was discussed in Gomez and Jimenez (2020b).

cutoff was discussed in Gomez and Jimenez (2020b). For comoving Lagrangian scales $8 > \frac{1/k}{Mpc} > 1$ we predict that the value of $1 - n_s$ should be larger than at scales of 20 Mpc, which is where Planck18 measured the tilt. Therefore, there should be a lack of power with respect to the CMB inferred one given by the difference in a power-law power spectrum when adopting the CMB value $1 - n_s = 0.0328$ or the value from Fig. 14 corresponding at these scales ($\log_{10}(x) \sim -0.5$). In more detail:

$$\Delta P(k) = \frac{P(k)_{\text{CMB}}}{P(k)_{\sim 8\text{Mpc}}} = \frac{(k/k_0)^{(n_s - 1)_{k\eta = 0.1}}}{(k/k_0)^{(n_s - 1)_{k\eta \sim 0.3}}},$$
(109)

where we have used that the difference in scales between Planck18 CMB and the weak lensing surveys at ~ 8 Mpc is about a factor 3. Now, from Fig. 14 at the corresponding scale of $k\eta \sim 0.3$ we see that $1 - n_s \sim 0.15$, so

$$\Delta P(k) = \Delta(k)^{(0.0328 - 0.15)}, \tag{110}$$



Fig. 14. The quantum cosmological tilt as a function of energy scale as determined by the quantum Fisher. For values of $x = |k\eta| < 0$ the end of inflation is determined by the IR cutoff on the number of particles N. In this plot, for illustrative purposes, we set $N = 10^9$. The different shaded regions correspond to different scales. The blue region is where the dark matter forms and the spectral index is blue. Figure taken from Gómez and Jimenez (2021a).

where $\Delta(k) = 3$ as measured from the CMB scale of $\log_{10}(|k\eta|) \sim -1.0$ (to probe scales of 8 Mpc which is where KiDS and SPT report their measurements). This results in $\Delta P(k) = 0.85$. On the other hand the observed ratio $\Delta P(k)[S_8(\text{KiDS})/S_8(\text{Planck18})] = 0.9 \pm 0.03$. This is in good agreement with our prediction that at small scales the Universe would be less clumpy than the one at CMB scales.

7.7.10. Quartessence

An interesting class of cosmological models, known as quartessence or unified dark matter, in which Λ and dark matter are considered to be the two faces of the same quantity, can explain the current accelerated expansion of the Universe and also can explain the growth of the large scale structure of the Universe Camera et al. (2019). A family of quartessence models can be described by the following Lagrangian Bertacca et al. (2008):

$$\mathcal{L}_{\mathbf{Q}} = f(\varphi)g(X) - V(\varphi), \tag{111}$$

where g(X) ($X = -(1/2)\nabla_{\mu}\varphi\nabla^{\mu}\varphi$) is a Born-Infeld type kinetic term (Born and Infeld, 1934) and

$$f(\varphi) = \frac{\Lambda c_{\infty}}{1 - c_{\infty}^2} \cosh(\xi\varphi) \left[\sinh(\xi\varphi) \left[1 + \left(1 - c_{\infty}^2 \right) \sinh^2(\xi\varphi) \right] \right]^{-1},$$
(112)

$$V(\varphi) = \frac{\Lambda}{1 - c_{\infty}^2} \left[1 + \left(1 - c_{\infty}^2 \right) \sinh^2(\xi \varphi) \right]^{-1} \left[\left(1 - c_{\infty}^2 \right)^2 \sinh^2(\xi \varphi) + 2(1 - c_{\infty}^2) - 1 \right],$$
(113)

in which c_{∞} is a free parameter and $\xi = \sqrt{3/[4(1-c_{\infty}^2)]}$. At the background level, these models are indistinguishable from the Λ CDM model. The only free parameter c_{∞} is dependent on the effective sound speed of quartessence, c_s^2 , and for $t \to \infty$, we have $c_s^2 \to c_{\infty}^2$. In fact, the sound speed evolves with redshift as (Bertacca et al., 2008)

$$c_{\rm s}^2(z) = \frac{\Omega_\Lambda c_\infty^2}{\Omega_\Lambda + (1 - c_\infty^2)\Omega_{\rm DM}(1 + z)^3},\tag{114}$$

where Ω_{Λ} and Ω_{DM} are respectively the present day values of the density parameter for the effective cosmological constant and dark matter. Note, that for $c_{\infty} = 0$, one recovers the Λ CDM model. For the above model labeled as Λ CDM+ c_{∞} Camera et al. (2019), it has been found that *Planck* 2015 alone can estimate a very lower value of $S_8 = 0.719^{+0.15}_{-0.046}$ at 68% CL, which is close to the result $S_8 = 0.745 \pm 0.039$ from KiDS-450 Kuijken et al. (2015); Hildebrandt et al. (2017); Fenech Conti et al. (2017); Joudaki et al. (2017b), thus resolving the S_8 tension completely within 0.2σ .

7.7.11. Scaling symmetry and a mirror sector

Since the Hubble rate (or rather, its inverse H^{-1}) sets the total volume of the observable Universe at any given epoch, changing H means rescaling the universe's overall size. It turns out that if such a transformation is accompanied by a rescaling of all other important cosmological distances by the exact same amount, then important observables seen projected on the celestial sphere such as the CMB and LSS (including baryon acoustic oscillation (BAO)) are left entirely unchanged from our perspective. Fundamentally, this symmetry exists because (i) most cosmological data are analyzed in terms of *n*-point angular correlation functions, which are unaffected by the above scaling since angles are invariant under such transformation; (ii) the equations of motion describing the linear evolution of fractional density fluctuations (for photons, baryons, dark matter, etc.) in the Universe only depend on *ratios* of distances, which are invariant under a rescaling of all length scales in the problem; and (iii) the initial conditions for structure formation in our Universe do not have an

intrinsic scale built-in (i.e. their spectrum is a power law), allowing us to rescale the physical size of density fluctuations without changing their amplitude (up to a small harmless correction Zahn and Zaldarriaga (2003)).

In the pre-recombination Universe ($z \gtrsim 1100$), there are two important length scales in cosmology: the Hubble length H^{-1} and the photon mean free path $\dot{\kappa}^{-1} = (an_e\sigma_T)^{-1}$, where *a* is the scale factor, n_e is the free electron density, and σ_T is the Thomson cross section. Rescaling both quantities by a constant factor *f* (at all times) leaves cosmological observables invariant. Of course, scaling up the Hubble rate *H* implies via the Friedmann equation ($H^2 = (8\pi G/3) \sum_i \rho_i$) that we must increase the energy density of the Universe at all times. To leave the evolution of the gravitational potentials unchanged, the Einstein equations then tell us that this must be done by equally scaling the individual energy densities ρ_i of *all* the constituent of the Universe, $\sqrt{G\rho_i} \rightarrow f\sqrt{G\rho_i}$. In all, Ref. Cyr-Racine et al. (2021) finds that a broad array of cosmological observables are invariant under the following transformation

$$\left\{\sqrt{G\rho_i} \to f\sqrt{G\rho_i}, \ \sigma_{\rm T} n_{\rm e}(a) \to f\sigma_{\rm T} n_{\rm e}(a), \ A_{\rm s} \to A_{\rm s}/f^{(n_{\rm s}-1)}\right\},\tag{115}$$

for some constant f. The third entry in the transformation is necessary to ensure the initial amplitude of fluctuations is unchanged under the transformation. Here, A_s is the amplitude of scalar fluctuations and n_s is the scalar spectral index. The existence of this symmetry opens the doors for the CMB and LSS data to accommodate a larger value of the Hubble constant without necessarily degrading the quality of the fit between model and data, and also leave S_8 unchanged.

We emphasize that the above is *not* another model that could alleviate the Hubble tension, but rather a general paradigm to understand which models can naturally accommodate large Hubble constant values while being automatically consistent with cosmological data. As in much of theoretical physics, the existence of a symmetry broken by different physical effects can lead to key insights about the fundamental origins of the Universe. In our particular case, the scaling symmetry given in Eq. (115) is broken by the COBE/FIRAS measurement of the CMB black body spectrum Fixsen et al. (1996); Fixsen (2009), which fixes the energy density of photons today (and thus prohibits us from performing the transformation $\sqrt{G\rho_{\gamma}} \rightarrow f \sqrt{G\rho_{\gamma}}$). Indirectly, COBE also prohibits us from adding more baryons to the Universe, since the baryon-to-photon ratio is precisely measured by CMB anisotropies. Nevertheless, nothing prevents us from adding *dark photons* that couples to *dark baryons* in a similar way to how regular photons couple to standard baryons Ackerman et al. (2009); Feng et al. (2009); Agrawal et al. (2017); Foot and Mitra (2002); Foot and Volkas (2003); Foot (2004); Foot and Volkas (2004). Such a mirror dark sector has been studied extensively in the literature since it was long recognized that it could help explain why gravity is so much weaker than other forces in the Standard Model (SM). Could the Hubble tension be revealing the existence of such a mirror sector?

While necessary to evade the COBE/FIRAS bound, the mirror sector does not implement by itself to the second important ingredient of the scaling transformation: the necessary increase of the photon scattering rate (the second entry in Eq. (115)). This is certainly the most challenging aspect of the scaling transformation since it involves SM physics at low energies, which is tightly constrained by a multitude of observations. Ref. Cyr-Racine et al. (2021) used a phenomenological approach based on varying the primordial helium abundance, which runs into serious constraints from light-element abundance measurements.²⁵ A more promising approach likely requires variation of fundamental constants, especially the fine-structure constant and the electron mass. Varying these parameters has shown some promises in alleviating the Hubble tension (see e.g. Refs. Sekiguchi and Takahashi (2021); Hart and Chluba (2020, 2021)), and the scaling symmetry given above can help us understand why such ideas work well. Another challenge is how to reconcile BBN predictions in the presence of a rescaled Hubble rate with direct abundance measurements.

In all, the scaling symmetry highlights the important role that the photon scattering rates and BBN light-element abundances play in the H_0 and S_8 tension. It provides a clear target for model builders that, if reached, would guarantee compatibility between CMB, LSS, and local inference of H_0 .

7.7.12. Self-interacting neutrinos

The physics of neutrinos is one of the fascinating topics in modern cosmology even though we have been able to extract only a very minimal information about the neutrinos. Recently, it has been observed that the introduction of new physics in the neutrino sector in terms of the interactions between themselves Kreisch et al. (2020); Lancaster et al. (2017); Blinov et al. (2019); Barenboim et al. (2019), which is theoretically possible, might be able to offer an appealing route to alleviate the cosmological tensions Kreisch et al. (2020); Venzor et al. (2022). After decoupling from other standard model particles, neutrinos are considered to be freely streaming throughout the Universe, but they can interact with each other or with other cosmic species via their gravitational interactions. This gravitationally influenced interaction could affect the cosmic observables and this may result in interesting consequences, including opening up the inflation parameter space Barenboim et al. (2019). In Ref. Kreisch et al. (2020) the authors considered a Lagrangian describing the interaction between different neutrino mass eigenstates of the form

$$\mathcal{L}_{\text{int}} = \theta_{ij} \bar{\nu}_j \nu_i \phi, \tag{116}$$

where v_i is a left-handed neutrino Majorana spinor, θ_{ij} is a (generally complex) coupling matrix in which the indices *i*, *j* labeled the neutrino mass eigenstates. This is a Yukawa-type interaction with a massive scalar ϕ and this may arise in the scenarios where neutrinos interact with a Majoron Gelmini and Roncadelli (1981); Simpson et al. (2018); Berlin and Blinov (2019). The presence of the interaction in the neutrino sector quantified through the above Lagrangian may delay the onset of neutrino free streaming until close to the matter-radiation equality leading to a higher value of the Hubble constant and a lower value of the matter fluctuations Kreisch et al. (2020).

7.7.13. Self-interacting sterile neutrinos

The short baseline (SBL) neutrino oscillation experiments Giunti and Lasserre (2019) suggest the existence of a fourth sterile neutrino with a \sim eV mass. However, the existence of sterile neutrinos is not compatible with cosmology since they suppress the structure formation of the Universe. This problem can be bypassed if by some unknown mechanism they can be either prevented from thermalizing

²⁵ A realistic model of Dark Atoms based on it has been explored in Blinov et al. (2021).



Fig. 15. Left panel: The $f\sigma_8$ as a function of z in the case of soft dark energy. The dashed curve is for ACDM. The solid curve is for soft dark energy with $s_{DE} = 1.1$, i.e. with $w_{DE,Is} = -1$ and $w_{DE,is} = -1.1$, and $c_{eff,DE} = 0.1$, while dark matter is standard (i.e. not soft) with $w_{DM} = 0$. Right panel: The $f\sigma_8$ as a function of z in the case of soft dark matter. The dashed curve is for ACDM. The solid curve is for soft dark matter with softness parameter $s_{DM} = 1.05$, i.e. for dark matter with $w_{DM,Is} = 0$ and $w_{DM,is} = 0.05$ (note that dark energy is not soft). The figures are from Saridakis (2021).

in the early Universe or removed by subsequent annihilation. Considering such limitation, the authors of Ref. Archidiacono et al. (2015) suggested a possible revision in the sterile neutrino sector in which the sterile neutrino interacts with a new light pseudoscalar degree of freedom. This proposal got attention in the cosmological community because with such coupling in the sterile neutrino sector, the effective scenario can increase the Hubble constant value and consequently alleviate the Hubble constant tension Archidiacono et al. (2016a,b, 2020); Corona et al. (2021).

7.7.14. Soft cosmology

In soft cosmology Saridakis (2021); Saridakis et al. (2021b) one allows for small deviations from the usual cosmological framework due to the effective appearance of soft-matter properties in the Universe sectors Jones et al. (2002); Sagis (2011). Hence, as a first approach on the subject, one considers that, intrinsically or effectively, dark energy and/or dark matter may have a different EoS at large scales, i.e. at scales entering the Friedmann equations, and a different one at intermediate scales, i.e. at scales entering the perturbation equations. This possible deviation of the large-scale (ls) and intermediate-scale (is) EoS can be quantified by introducing the softness function *s*. Hence, in the simplest scenario one has

$$w_{\text{DE,is}} = s_{\text{DE}} \cdot w_{\text{DE,ls}} \,, \tag{117}$$

$$w_{\text{DM,is}} + 1 = s_{\text{DM}} \cdot (w_{\text{DM,ls}} + 1), \tag{118}$$

where s_{DE} and s_{DM} are the softness parameters for the dark energy and dark matter sectors, respectively. Standard cosmology is recovered for $s_{\text{DE}} = s_{\text{DM}} = 1$. Thus, although the Friedmann equations are $H^2 = \frac{\kappa^2}{3}(\rho_b + \rho_r + \rho_{\text{DM}} + \rho_{\text{DE}})$ and $2\dot{H} + 3H^2 = -\kappa^2(p_b + p_r + p_{\text{DM}} + p_{\text{DE}})$, where $w_{i,\text{IS}} \equiv p_i/\rho_i$ is the equation-of-state parameter of the *i*th sector at large scales, the (linear, scalar, isentropic) perturbation equations in the Newtonian gauge read

$$\dot{\delta}_{i} + (1 + w_{i,is}) \left(\frac{\theta_{i}}{a} - 3\dot{\Psi}\right) + 3H \left((c_{\text{eff}}^{(i)})^{2} - w_{i,is} \right) \delta_{i} = 0,$$
(119)

$$\dot{\theta}_i + H\left(1 - 3w_{i,is} + \frac{\dot{w}_{i,is}}{H(1 + w_{i,is})}\right)\theta_i - \frac{k^2 (c_{\text{eff}}^{(l)})^2 \delta_i}{(1 + w_{i,is})a} - \frac{k^2 \Psi}{a} = 0,$$
(120)

where $\delta_i \equiv \delta \rho_i / \rho_i$ is the density perturbation, θ_i the divergence of the fluid velocity, *k* the wavenumber of the Fourier modes, and $(c_{\text{eff}}^{(i)})^2 \equiv \frac{\delta p_i}{\delta \rho_i}$ the effective sound speed square for the *i*th sector which determines the clustering properties, being zero for maximal clustering and one for no clustering.

Soft Dark Energy – As the first soft extension of Λ CDM scenario we consider a model where dark matter is the usual, non-soft, dust one at all scales, while dark energy is the soft component with large-scale behaviour that of a cosmological constant. Hence, we impose fixed $s_{\text{DM}} = 1$, namely $w_{\text{DM,Is}} = w_{\text{DM,is}} = 0$ as in the standard dust dark matter case, while we set $w_{\text{DE,Is}} = -1$ and $w_{\text{DE,is}} = s_{\text{DE}} w_{\text{DE,Is}} = -s_{\text{DE}}$, so that s_{DE} is the only extra free parameter comparing to Λ CDM cosmology. Standard cosmology is recovered for the value $s_{\text{DE}} = 1$. In the left graph of Fig. 15 we depict the $f\sigma_8$ as a function of z, where we can see alleviation of the S_8 tension.

Soft Dark Matter – As another soft extension of Λ CDM scenario we consider a model where dark energy is the usual cosmological constant, with $w_{\text{DE},\text{Is}} = w_{\text{DE},\text{is}} = -1$, however dark matter is soft with $w_{\text{DM},\text{Is}} = 0$ and $w_{\text{DM},\text{is}} = s_{\text{DM}} - 1$, and therefore s_{DM} is the only extra free parameter comparing to Λ CDM cosmology (the latter is recovered for the value $s_{\text{DM}} = 1$). In the right graph of Fig. 15 we depict the $f\sigma_8$ as a function of z, where we can see the S_8 tension alleviation.

In summary, soft cosmology can alleviate the S_8 tension due to the slightly deviated perturbation-level properties it introduces. Finally, we mention that the whole consideration is independent of the underlying gravitational theory, and it can be applied both in the framework of general relativity, as well as in modified theories of gravity in which dark energy sector is of gravitational origin (nevertheless, deviating from general relativity would provide additional possibilities to induce effective soft properties to the dark sectors).

7.7.15. Two-body decaying cold dark matter into dark radiation and warm dark matter

One of the solutions proposed to solve the S_8 tension is given by a two-body Decaying Cold Dark Matter (dCDM) model where all of the dark matter is assumed to decay into a massless (dark radiation) and a massive warm DM (WDM) species. See Sec. 7.7.3 for alternative models of decaying DM. The phenomenology of such a model has recently been reviewed in great details in Ref. Abellán et al. (2021). The model is characterized by two parameters, the dCDM lifetime, Γ^{-1} , and the fraction of dCDM rest mass energy transferred to the dark radiation, given by Blackadder and Koushiappas (2014)

$$\varepsilon = \frac{1}{2} \left(1 - \frac{m_{\text{WDM}}^2}{m_{\text{dCDM}}^2} \right), \tag{121}$$

where m_{dCDM} and m_{WDM} denote the mass of the parent particle and massive decay product respectively. Thus, $0 \le \varepsilon \le 1/2$, with the lower limit corresponding to the standard CDM case, so that $\Omega_{CDM} = \Omega_{dCDM} + \Omega_{WDM}$, and $\varepsilon = 1/2$ corresponding to DM decaying solely into dark radiation. In general, small ε values (i.e. heavy massive decay products) and small Γ values (i.e. lifetimes much longer than the age of the Universe) induce little departures from Λ CDM. In the intermediate regime, the velocity-kick received by the warm decay product imprints a characteristic suppression to the matter power spectrum, in a similar fashion as massive neutrinos or warm dark matter. One key difference with respect to these scenarios is the fact that the power suppression is less significant at high redshift, simply because the abundance of the warm decay product is smaller in the past. This allows the model to reduce the σ_8 value as compared to that inferred from the standard Λ CDM model, while preserving a good fit to CMB, BAO, growth factor and uncalibrated SNIa data. The authors of Ref. Vattis et al. (2019) suggested that such a model can provide a resolution of the Hubble tension (see also Clark et al. (2021a)).

However, this conclusion was recently challenged in Refs. Haridasu and Viel (2020), where it was shown that including CMB and SNIa data spoils the success of the model to resolve the Hubble tension. Still, in Ref. Abellán et al. (2020), it was shown thanks to a new fluid approximation to describe the perturbations of the massive decay products, that such a model can in fact resolve the S_8 tension if $\Gamma^{-1} \simeq 55 (\varepsilon/0.007)^{1.4}$ Gyr. As discussed in Ref. Abellán et al. (2020), this model could also have interesting implications for model building, the small-scale crisis of Λ CDM and the recent XENON1T excess.

7.8. Beyond the FLRW framework

The Hubble constant H_0 has a special standing within the class of Friedmann-Lemaître-Robertson-Walker (FLRW) cosmological models, since it arises as an integration constant when one solves the Friedmann equations. As a result, it is generic to *all* FLRW cosmologies. Now, it is no secret that our local Universe is *not* an FLRW Universe and that there are well documented flows towards the Shapley supercluster at a distance of approximately 200 Mpc, e.g. Ref. Hoffman et al. (2017). In the aftermath of the HST Key project Freedman et al. (2001), it was also recognised that H_0 varies across the sky in the local Universe McClure and Dyer (2007). This in itself is unsurprising, since the underlying Hubble flow and the rate of expansion need to be inferred from these averages. Historically, this has been an insanely difficult endeavour and even now disagreements have emerged in the distance ladder between Cepheid Riess et al. (2021a) and TRGB calibration Freedman (2021).

Recall that the cosmological principle paradigm simply states that the Universe is well modelled as being isotropic and homogeneous at *suitably large scales*. If one further assumes the decoupling of scales in the underlying metric theory, such that the dynamical theory defined on such large scales is insensitive to the particularities of the regional matter configurations and dynamics, this implies that cosmic structures and their evolution can be ignored altogether at such scales and that the large-scale Universe can be modelled by an FLRW metric. If one stipulates that the large-scale Universe is well described by a homogeneous-isotropic model, one may ask what the scale of transition towards homogeneity and isotropy is? While this statement is vague, one can try to quantify what is meant by "suitably large scales", and within the flat Λ CDM model, estimates of $260h^{-1}$ Mpc exist Yadav et al. (2010) as a scale beyond which the fractal dimension of the distribution becomes statistically indistinguishable from that of a perfectly homogeneous and isotropic distribution. The homogeneity scale estimates depend on the statistical measure used. Taking into account all correlation properties in the distribution by employing the Minkowski Functionals Mecke et al. (1994) the homogeneity scale seems to be even larger Wiegand et al. (2014). There are claims of large structures in the Universe that appear challenging for the hypothesised transition to homogeneity, for example the Sloan Great Wall Gott et al. (2005), the Huge Large Quasar Group Clowes et al. (2013) or the Hercules–Corona Borealis Great Wall Horvath et al. (2015). These claims of violations of the cosmological principle have quickly been countered Park et al. (2012); Nadathur (2013); Ukwatta and Wozniak (2016); Christian (2020), usually on statistics alone. In short, despite a host of claims, there is little evidence to support any breakdown of the cosmological principle, at least with inhomogeneities.

The strongest observational evidence for an isotropic and homogeneous Universe comes from the CMB. Even to the naked eye, *Planck*'s maps of micro-Kelvin temperature anisotropies provide a convincing snapshot of a statistically isotropic Universe. The statistically isotropic CMB temperature field is conventionally used as a heuristic argument for modelling the large-scale Universe by an FLRW cosmological model. However, the FLRW model assumption is stronger than that of statistical homogeneity and isotropy; cf. the above discussion. Care must therefore be taken in making rigorous any statements about the underlying metric model based on observations such as the CMB. The CMB photon energy field as viewed by the observer is a quantity which is integrated over scales comparable to the age of the Universe. It is possible that large regional departures from FLRW curvature can be present without breaking of the almost-isotropy of the CMB. Extended versions of the Ehlers-Geren-Sachs theorem Stoeger et al. (1995); Rasanen (2009a) that seek to constrain the departures from an FLRW space-time metric based on the level of isotropy of the CMB temperature field within general relativity, must make assumptions on individual components of the covariant *derivatives* of the energy function for classes of observers to arrive at the conclusion that the Universe is "almost-FLRW".²⁶ These components are not directly observable, and are in fact expected to be large in a

²⁶ The original Ehlers-Geren-Sachs theorem Ehlers et al. (1968) states that the space-time is FLRW or static if the Universe energy-momentum content is a *perfectly* isotropic radiation fluid around every point. Almost-versions of the theorem are concerned with the realistic scenario of almost-isotropic CMBs as viewed by observers in space-times with realistic energy-momentum content.

Universe with large density contrasts Rasanen (2009a). Thus, even though appealing as an argument for FLRW modelling of the Universe as a whole, almost-isotropy of the CMB does not constitute a proof of the almost-FLRW Universe.

The most notable anisotropy in the CMB is a dipole ($\ell = 1$ multipole), the magnitude of which is in the milli-Kelvin range. This dipole is assumed to be a Doppler effect due to relative motion. Obviously, this assumption is a loose end, and now that we find ourselves in a time of crisis, potentially confronted by a $\sim 10\%$ discrepancy in H_0 , it is prudent to test the assumption that the dipole is purely kinematic in origin. Interestingly, those tests have been pursued over the last two decades, and caveats aside, a consensus has emerged whereby the magnitude of the cosmic dipole inferred from both radio galaxies Blake and Wall (2002); Singal (2011); Gibelyou and Huterer (2012); Rubart and Schwarz (2013); Tiwari and Nusser (2016); Colin et al. (2017); Bengaly et al. (2018); Siewert et al. (2021) and guasars Secrest et al. (2021) exceeds the CMB dipole. Similar conclusions have been recently reached by studying the Hubble diagram of Type Ia SN Singal (2021) and QSOs Singal (2022). This naïvely implies that distant sources are not in the "CMB frame" and opens up the possibility that the CMB dipole may have been misinterpreted. On the flip side, a recent analysis of the high CMB multipoles is consistent with a kinematic CMB dipole Saha et al. (2021) (see also Ref. Ferreira and Quartin (2021)), but the errors are large. Curiously, various CMB anomalies exist (see Ref. Schwarz et al. (2016) for a review), such as the planar alignment of the quadrupole-octopole de Oliveira-Costa et al. (2004); Schwarz et al. (2004) and the anomalous parity asymmetry Land and Magueijo (2005), which may have some origin in the CMB dipole Kim and Naselsky (2010a); Naselsky et al. (2012). Objectively, if there is no coherence in CMB anomalies, then few conclusions can be drawn. However, if the anomalies have directional dependence, then the plot thickens. Assuming there is a mismatch in the cosmic dipole that can be independently verified by SKAO Bengaly et al. (2019), the simplest and most consequential interpretation is that the Universe is anisotropic. While current data suggests that flat ACDM is a good approximation, one can ask how pronounced is any anisotropy, if real? Tellingly, the CMB dipole direction also appears in a documented preferred axis for QSO polarisations Hutsemekers and Lamy (2001); Hutsemekers et al. (2005) and scaling relations in galaxy clusters Kaiser (1986) also point to an anisotropy consistent with the CMB dipole direction Migkas et al. (2020, 2021). Furthermore, observations of strong lensing time delay Wong et al. (2020); Millon et al. (2020), Pantheon Type Ia SN Scolnic et al. (2018), QSOs standardised through UV-X-ray relation Risaliti and Lusso (2015); Lusso et al. (2020) and GRBs standardised through the Amati relation Amati et al. (2008), consistently return higher values of H_0 in hemispheres aligned with the CMB dipole direction, at least within the flat ACDM model Krishnan et al. (2021b, 2022); Luongo et al. (2021). Obviously, variations of cosmological H_0 across the sky with the flat Λ CDM model make any discrepancy between Planck's determination of H_0 with the same model and local H_0 determinations a moot point. Given the rich variety of the above observations, and the differences in underlying physics, it is hard to imagine that the CMB dipole direction is not a special direction in the Universe. The status quo of simply assuming that it is kinematic in origin, especially since it is based on little or no observational evidence, may be untenable. If this claim is substantiated, not only do the existing cosmological tensions in H_0 and S_8 need revision, but so too does virtually all of cosmology. In short, great progress has been made through the cosmological principle, but it is possible that data has reached a requisite precision that the cosmological principle has already become obsolete.

7.8.1. Cosmological fitting and averaging problems

The cosmological principle stipulates that there is a length scale beyond which the Universe appears as being approximately spatially homogeneous and isotropic. If one further assumes the decoupling of dynamics of volume sections beyond such a scale of homogeneity and isotropy from the local space-time configurations of matter and curvature, this implies the modelling of the large-scale Universe by an FLRW metric model. The Λ CDM framework of cosmology builds on this assumption of decoupling. However, going beyond the Λ CDM framework, one could imagine a Universe which *does* obey the cosmological principle, but where the regional distributional properties of matter and curvature has importance for the large scale cosmological dynamics.

The problem of taking into account such distributional properties in the large scale modelling of our Universe is sometimes referred to as the *cosmological fitting problem* Ellis (1984); Ellis and Stoeger (1987). Various approaches to formalising the fitting problem that build on averaging operations of Einstein's equations have been developed in e.g. Refs. Zalaletdinov (1992, 1993, 1997); Buchert (2000, 2001, 2008); Wiltshire (2007); Rasanen (2009b, 2010a); Korzynski (2010); Gasperini et al. (2009, 2010); Buchert and Räsänen (2012); Wiltshire (2011); Gasperini et al. (2011); Ben-Dayan et al. (2012); Uzun (2020); Buchert et al. (2020). Within such formalisms, the departure of the large-scale dynamics from that of an FLRW Universe without structure is sometimes denoted *cosmological backreaction*; see Refs. Green and Wald (2014); Buchert et al. (2015) for a debate on the level of importance of backreaction effects in our Universe.

The Buchert averaging scheme Buchert (2000, 2001); Buchert et al. (2020) is the most widespread framework for quantifying backreaction effects; see also Buchert et al. (2022) for an extension of the Buchert averaging scheme to the past lightcone of an observer. In this framework, it is made explicit how the large-scale volume evolution is affected by backreaction terms. For instance, in an irrotational dust Universe backreaction in the matter frame is given by variance in expansion rate over volume and regional shearing Buchert (2000). The backreaction effects can in this case be collected in a single term, which enters in the average dynamical equations for the large-scale volume in such a way that it mimics a dark energy-like effect for large-scale isotropic averages (dominance of expansion variance between voids and matter-dominated regions), but also a dark matter-like effect on smaller scales where the backreaction term can change its sign in cases where anisotropic structures dominate the distribution Buchert (2000, 2008). The backreaction term in turn couples to the average spatial Ricci-curvature of the space-time, thus breaking the Friedmann conservation law ⁽³⁾*Ra*²(*t*) =const, where ⁽³⁾*R* is the spatial Ricci-curvature and *a*(*t*) is the scale factor of the FLRW Universe model; see Refs. Buchert (2000); Heinesen and Buchert (2020) for details.

Backreaction as defined by Buchert Buchert (2000) reduces to a boundary term in Newtonian cosmology Buchert and Ehlers (1997); however, see Ref. Vigneron (2021) describing the possibility of volume-integrated backreaction in locally Newtonian theory defined on non-Euclidean topologies, and see also Brunswic and Buchert (2020) for an assessment of topology and GR integral constraints. Non-zero backreaction effects for domains without boundaries defined on non-Euclidean topological structures must thus arise from relativistic effects; see Rasanen (2010b) and references therein. However, such relativistic effects need not be associated with astrophysical structures

with large relative speeds or with structures in the "strong-field" regime,²⁷ in the sense of the Schwarzschild potential 2GM/R, where M is the mass and R is the radius of the structure. We remark that backreaction effects could arise in Newtonian *approximations* of general relativity: The small velocity and weak-gravitational potential limit of general relativity is not strictly Newtonian but subject to additional degrees of freedom and constraints Ellis and Dunsby (1997); Rainsford (2001); see for instance Ref. Senovilla et al. (1998) and references therein for examples of Newtonian theories that cannot be recovered in any limit of general relativity. We might further add to the above mentioned subtleties that, even for space-times with negligible backreaction as measured by the backreaction functionals defined in Buchert (2000, 2001); Buchert et al. (2020), observations might exhibit non-negligible departures from any simple FLRW model prediction, depending on the scale of observation and the type of the cosmological measurement. The reverse is also true: it is in principle possible to have space-times where certain backreaction terms are formally large, but where observations are close to an FLRW prediction.

The dynamical differences of the large-scale universal dynamics from that prescribed by a structure-less FLRW model space-time would be a natural candidate for explaining the differences in Λ CDM parameters as inferred from early and late epoch Universe probes. The potential for explaining the Hubble tension with dynamical backreaction effects has been examined within crude analytical approaches Heinesen and Buchert (2020) and numerical relativity Macpherson et al. (2018), but is far from being an exhausted topic of investigation. The cosmological fitting problem and its significance for Universe observations – including the impact of cosmic structure on the determination of "background" cosmological parameters such as the Hubble constant – is a rich topic of investigation with many subtleties as indicated in the above review. Regional inhomogeneity and anisotropy and any resulting backreaction effects on the large scale Universe description are appealing possible solutions to the dark energy problem, coincidence problem, and parameter tensions in modern cosmology within the theory of general relativity and without the introduction of additional energy-momentum degrees of freedom. Though any physical backreaction effects must likely arise from subtle departures from strict Newtonian Universe modelling, and is therefore an involved topic of research, it might thus at the same time be argued to be one of the simplest possible solutions to the modern challenges faced in cosmology.

7.8.2. Data analysis in an Universe with structure: accounting for regional inhomogeneity and anisotropy

In a Universe that contains structures, a spatial invariance with respect to translation and rotation transformations is necessarily broken at some level. As suggested in the above introduction, such symmetry breaking might be more pronounced and important for cosmological inference than is usually accounted for in Λ CDM analysis of data. One way to take into account regional inhomogeneities and anisotropies is to employ exact solutions or perturbative models, a few examples of which are discussed in Sec. 7.8.3. Another option is to remain agnostic about the particularities of the regional properties of the underlying space-time metric.

For this purpose, we might use cosmographic approaches²⁸ for analysis of data that do not make assumptions about the form of the metric or the determining field equations Kristian and Sachs (1966); Ellis et al. (1985); Ellis and MacCallum (1969); Clarkson and Maartens (2010); Clarkson et al. (2012); Umeh (2013); Heinesen (2021d,a); Bargiacchi et al. (2021a); Benetti and Capozziello (2019). Such approaches rely on geometrical series expansions around the observer, and are thus most appropriate for analysing low-redshift data.²⁹ See also Refs. Korzyński et al. (2021); Korzyński and Kopiński (2018); Heinesen (2021b) for non-perturbative frameworks for model independent determination of Universe properties.

Cosmographic frameworks for model-independent analysis of different observables, such as distance-redshift data, number count statistics, and cosmic drift effects, can be formulated. As an illustration, we shall in the present section focus on luminosity distance cosmography relevant for analysing low-redshift standardisable candles and sirens. Following Ref. Clarkson et al. (2012); Umeh (2013); Heinesen (2021d), we will thus formulate luminosity distance as a Taylor series expansion in redshift in a general continuous and expanding space-time description of emitters and observers between which photons travel on null geodesics. Assuming that Etherington's reciprocity theorem for relating luminosity distance to angular diameter distance Etherington (1933); Ellis and van Elst (1999) holds, the luminosity distance as a function of redshift, z, and position on the sky, e, of the astrophysical source is given by its Taylor series Heinesen (2021d)

$$d_L(z, \boldsymbol{e}) = d_L^{(1)}(\boldsymbol{e})z + d_L^{(2)}(\boldsymbol{e})z^2 + d_L^{(3)}(\boldsymbol{e})z^3 + \mathcal{O}(z^4),$$
(122)

within the radius of convergence of the series, where the anisotropic coefficients up till third order:

$$d_{L}^{(1)}(\boldsymbol{e}) = \frac{1}{\mathfrak{H}_{0}(\boldsymbol{e})}; \qquad d_{L}^{(2)}(\boldsymbol{e}) = \frac{1 - \mathfrak{Q}_{0}(\boldsymbol{e})}{2\mathfrak{H}_{0}(\boldsymbol{e})}; \qquad d_{L}^{(3)}(\boldsymbol{e}) = \frac{-1 + 3\mathfrak{Q}_{0}^{2}(\boldsymbol{e}) + \mathfrak{Q}_{0}(\boldsymbol{e}) - \mathfrak{J}_{0}(\boldsymbol{e}) + \mathfrak{H}_{0}(\boldsymbol{e})}{6\mathfrak{H}_{0}(\boldsymbol{e})}, \tag{123}$$

can be expressed in terms of the effective cosmological parameters

$$\mathfrak{H}(\boldsymbol{e}) \equiv -\frac{1}{E^2} \frac{\mathrm{d}E}{\mathrm{d}\lambda}; \qquad \mathfrak{Q}(\boldsymbol{e}) \equiv -1 - \frac{1}{E} \frac{\mathrm{d}\mathfrak{H}}{\mathrm{d}\lambda}; \qquad \mathfrak{R}(\boldsymbol{e}) \equiv 1 + \mathfrak{Q} - \frac{1}{2E^2} \frac{k^{\mu} k^{\nu} R_{\mu\nu}}{\mathfrak{H}^2}; \qquad \mathfrak{J}(\boldsymbol{e}) \equiv \frac{1}{E^2} \frac{\frac{\mathrm{d}^2 \mathfrak{H}}{\mathrm{d}\lambda^2}}{\mathfrak{H}^3} - 4\mathfrak{Q} - 3, \qquad (124)$$

where the subscript *o* denotes evaluation at the space-time event of observation. Here, λ is the affine parameter defined on the photon path, $d/d\lambda \equiv k^{\mu} \nabla_{\mu}$ is the derivative evaluated along the incoming null ray, where *k* is the 4-momentum of the photon, with energy $E = -u^{\mu}k_{\mu}$ as measured in the congruence frame of emitters and observers as generated by the 4-velocity field *u*, and $z \equiv E/E_o - 1$ is the associated redshift function relative to the observer of interest at *o*. The Ricci curvature of the space-time, $R_{\mu\nu}$, is left unspecified in the general framework and might be given by any theory of gravity.

²⁷ See Korzyński (2015) for an example of an exact GR solution where all of the individual structures are in the "weak-field" regime, but where the global matter distribution nevertheless exhibits manifestly relativistic effects.

²⁸ The cosmographic frameworks listed here do *not* assume the FLRW class of metrics (or any other particular form of the metric), and their applications are thus more general than those in Ref. Visser (2004).

²⁹ Traditionally, cosmography is an expansion in *z*, but one should expect the approximation to break down when *z* becomes a large parameter, $z \gtrsim 1$. See Refs. Cattoen and Visser (2007); Colgáin and Sheikh-Jabbari (2021a) for discussion.



Fig. 16. Sky-maps of the effective Hubble (*Top-left panel*), deceleration (*Top-right panel*), curvature (*Bottom-left panel*), and jerk parameters (*Bottom-right panel*), for an observer placed at the "present epoch" hypersurface of the 200 Mpc/h smoothing scale simulation. The parameters (with the exception of the curvature parameter) are normalised by their Einstein-de Sitter reference values as computed by an average over the simulation domain. This figure corresponds to Fig. 2 in Ref. Macpherson and Heinesen (2021).

We notice that \mathfrak{H} replaces the Hubble parameter of the FLRW cosmography. Thus it is the relation $d_L = z/\mathfrak{H}$ that consistently determines distances in the $\mathcal{O}(z)$ vicinity of the observer for a general space-time. Similarly, the parameters \mathfrak{Q} , \mathfrak{J} , and \mathfrak{R} generalise the FLRW deceleration, jerk and curvature parameters in the FLRW cosmography results Visser (2004). For this reason, we refer to { \mathfrak{H} , \mathfrak{Q} , \mathfrak{J} , \mathfrak{R} } as effective observational Hubble, deceleration, jerk and curvature parameters of the luminosity distance–redshift relation.

The effective cosmological parameters carry information about the space-time kinematics and curvature in the cosmic neighbourhood of the observer. We can get an idea of how such information enters in the effective Hubble parameter, by performing a multipole expansion of \mathfrak{H} in the direction vector, \boldsymbol{e} , of the source Clarkson et al. (2012); Umeh (2013); Heinesen (2021d):

$$\mathfrak{H}(\boldsymbol{e}) = \frac{1}{3}\theta - e^{\mu}a_{\mu} + e^{\mu}e^{\nu}\sigma_{\mu\nu}, \qquad (125)$$

where θ is the expansion rate of space in the observer frame, and where $\sigma_{\mu\nu}$ is the shear tensor describing the anisotropic deformation of space. The 4–acceleration of the observer a^{μ} will usually be set to zero when non-gravitational forces are neglected. The expression in Eq. (125) is exact, and the truncation of the expansion in e at quadrupolar order is true for any congruence description of emitters and observers.

The Hubble law determining cosmological distances in the O(z) vicinity of the observer will vary between observers through spatial variations of θ and $\sigma_{\mu\nu}$ due to breaking of the translation invariance. The Hubble law will also in general vary over the individual observer's sky on account of the anisotropy of expansion incorporated in the shear tensor, $\sigma_{\mu\nu}$. If, for instance, the direction, e, of a particular source as viewed by the observer is pointing towards a direction where $e^{\mu}e^{\nu}\sigma_{\mu\nu} > 0$, there is a positive contribution to the effective Hubble parameter prescribing the O(z) distance to that source.

Similarly, the effective deceleration parameter and the effective curvature and jerk parameters can be written in terms of truncated multipole series in the direction vector, \mathbf{e} , of the source as in Ref. Heinesen (2021d) – See also Ref. Umeh (2013) for the first decomposition of the effective deceleration parameter into multipoles. The dominant anisotropies as predicted by this formalism might be examined with data or within numerical simulations. In Refs. Macpherson and Heinesen (2021), the analytical expression of the luminosity distance in Eqs. (122)–(124) was analysed for an ensemble of observers in fully relativistic large scale numerical simulations. A sky map of a typical observer in this simulation, as smoothed over scales of 200 Mpc/h, is shown in Fig. 16.

The signatures of the anisotropy of the luminosity distance cosmography as seen for the ensemble of observers, and the variations of the cosmography across observers, are discussed in Ref. Macpherson and Heinesen (2021), in context of the Hubble tension. The dominant dipole as seen in \mathfrak{Q} and \mathfrak{R} for the observer in Fig. 16, and as found for the majority of observers in the simulation, is interesting in light of the cosmic dipoles found in data as discussed in Sec. 8.6.³⁰

The general formalism presented in this section provides a consistent way of taking into account anisotropies in standard candle and standard siren data, without the need of imposing exact symmetries at the level of the metric tensor. If inhomogeneous and/or anisotropic features in the luminosity distance–redshift signal are sufficiently large in our Universe, these could significantly impact local measurements and our inference expansion and deceleration of space. The formalism can be extended to include model independent analysis of other observables, such as cosmological drift effects Heinesen (2021a).

³⁰ The dipolar signatures as reported for the Hubble parameter (see Sec. 8.6.6), might be signatures of higher order parameters in the d_L cosmography, which are present in the ratio z/d_L .


Fig. 17. Marginalized constraints on the effective contrast δ_L and size r_L^{out} of the ALTB inhomogeneity at 68% and 95% confidence level. The empty contours show the constraints from the corresponding combination of observables. The green area shows the region of the parameter space that is allowed by the standard model, here represented via the Copernican prior convolved with the CMB likelihood. The figure has been taken from Ref. (Camarena et al., 2022).

7.8.3. Local void scenario

A simple explanation of the H_0 tension could be that we live inside a bubble with a higher expansion rate—the so-called local void scenario.³¹ For such a Hubble bubble model one expects that an adiabatic perturbation in density causes a perturbation in the expansion rate given by:

$$\frac{\delta H_0}{H_0} = -\frac{1}{3} f(\Omega_m) \frac{\delta \rho(t_0)}{\rho(t_0)},\tag{126}$$

where $f \simeq 0.5$ is the present-day growth function for the concordance Λ CDM model. It follows that, to have a $\approx 9\%$ change in H_0 , one needs a Hubble bubble of contrasts ≈ -0.5 . As shown by Fig. 3, within the standard model, such contrasts are reached only at small scales. Therefore, one does not expect that a local structure could explain away the Hubble tension as H_0 is measured at larger scales (see again Fig. 3). As discussed in Sec. 4.6, estimates based on theoretical computations and numerical simulations suggest that cosmic variance on H_0 amounts at 0.5–1%.

However, the previous reasoning assumes the standard model, in particular that the FLRW background can describe observations on cosmological scales. If one drops the FLRW assumption, there could be inhomogeneity around us of arbitrary depth and size.³² Perturbations around us are expected to follow the power spectrum derived from the CMB (the one that was used for Fig. 3) only within the standard FLRW paradigm, which implies that the observer's local Universe is statistically similar to the one at the last scattering surface. One can then study a model that features an arbitrary inhomogeneity around the observer and see how much observations can constrain such inhomogeneous model. Equivalently, one can reconstruct the metric from observations, checking if FLRW is recovered. To this end, the LTB metric with the cosmological constant (the ALTB model) provides a convenient formalism to constrain deviations from FLRW (see Ref. Camarena et al. (2022) and reference therein). Contrary to the Hubble bubble model, the ALTB model features a smooth profile without discontinuities, allowing for a better comparison with observational data.

Ref. Camarena et al. (2022) constrained the ALTB model using the latest available data from CMB, BAO, type Ia supernovae, local H_0 , cosmic chronometers, Compton *y*-distortion and kinetic Sunyaev–Zeldovich effect. Regarding the H_0 tension, it was found that, if one considers CMB, low-redshift supernovae from Pantheon (0.023 < z < 0.15) and the local calibration on the supernova magnitude M_B from SH0ES Camarena and Marra (2021), then a local underdensity of size (700–800) Mpc and contrast -0.15 is indeed preferred by the data, see the red contours in Fig. 17. This structure is clearly non-Copernican and at strong odds with the standard model, which predicts the structures depicted by the green contours. However, if we include all the supernovae, one finds that the void scenario is ruled out and the FLRW limit is basically recovered (black contours in Fig. 17).

Specifically, when including only low-*z* supernovae one finds $H_0 = (72.3 \pm 1.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$. If instead, all supernovae are included, one finds $H_0 = (69.06 \pm 0.56) \text{ km s}^{-1} \text{ Mpc}^{-1}$: as the local structure is very much constrained by data, the H_0 value is close to the one inferred from CMB observations (see Ref. Camarena et al. (2021) for more details). Concluding, assuming that CMB and supernova systematics are under control, an underdensity around the observer as modelled within the ALTB model cannot solve the H_0 tension Wojtak et al. (2014); Odderskov et al. (2014); Wu and Huterer (2017); Kenworthy et al. (2019); Cai et al. (2021a); Martín and Rubio (2021); Castello et al. (2021). See Sec. 7.8.2 for model-independent frameworks for analysing low-redshift cosmological data without imposing a particular form of the metric tensor.

³¹ Here, we are not considering void models as alternative to dark energy, a scenario that has been strongly disfavoured by kSZ constraints (Zhang and Stebbins, 2011). ³² There could also be large-scale anisotropies, but these are much more constrained from observations (see, however, recent studies on large-scale dipole anisotropies (Siew-

8. Challenges for Λ CDM beyond H_0 and S_8

Coordinator: Leandros Perivolaropoulos.

Contributors: Özgür Akarsu, Yashar Akrami, Luis Anchordoqui, David Benisty, Anton Chudaykin, Craig Copi, Eleonora Di Valentino, Celia Escamilla-Rivera, Pablo Fosalba, Enrique Gaztanaga, Dragan Huterer, Andrew Jaffe, Chung-Chi Lee, Benjamin L'Huillier, Matteo Lucca, Roy Maartens, C.J.A.P. Martins, Suvodip Mukherjee, Pavel Naselsky, Eoin Ó Colgáin, Paolo Salucci, Arman Shafieloo, M.M. Sheikh-Jabbari, Foteini Skara, Glenn Starkman, Richard Watkins, John Webb.

In this section we discuss in a unified manner many existing signals in cosmological and astrophysical data that appear to be in some tension (2σ or larger) with the standard Λ CDM model as defined by the *Planck* 2018 parameter values. In addition to the well known tensions discussed in previous sections (H_0 tension and S_8 tension), there is a wide range of other less-discussed less-standard signals, at a statistical significance level lower than the H_0 tension, that may also constitute hints of new physics. The goal of this section is to collectively present the current status of these signals and their levels of significance, refer to recent resources where more details can be found for each signal and discuss possible generic theoretical approaches that can collectively explain the non-standard nature of these signals. It is worth stressing that some of the tensions are painting a coherent picture, whereas others are isolated and potentially even contradict tensions in H_0 and S_8 .

According to these ideas, we adopt the following strategic questions:

- What are the current cosmological and astrophysical datasets that include such non-standard signals?
- What is the statistical significance of each signal?
- Is there a common theoretical framework that may explain these non-standard signals if they are of physical origin?

Along the same lines, a recent extensive broad review of non-standard signals may be found in Ref. Perivolaropoulos and Skara (2021b), which has updated earlier works on the subject Perivolaropoulos (2008, 2011) collecting and discussing signals in data that are at some statistical level in tension with the standard ACDM model. In addition, interesting reviews focusing mainly on the Hubble tension may be found in Refs. Di Valentino et al. (2021b); Knox and Millea (2020); Jedamzik et al. (2021); Saridakis et al. (2021a); Di Valentino et al. (2021g); Shah et al. (2021), while other reviews focusing mainly on CMB anomalies may be found in Refs. Schwarz et al. (2016); Copi et al. (2010), and in Refs. Akrami et al. (2020b); Ade et al. (2016f, 2014d).

In what follows, we provide a short example list of the non-standard cosmological signals in cosmological data. In many cases the signals are controversial and there is currently debate in the literature on the possible systematics origin of some of these signals. However, for completeness we refer to all signals we could identify in the literature referring also to references that dispute the physical origin of these signals.

8.1. The A_{lens} anomaly in the CMB angular power spectrum

The A_{lens} parameter was first introduced in Ref. Calabrese et al. (2008). A_{lens} is an "unphysical" parameter that actually rescales by hand the effects of the gravitational lensing on the CMB angular power spectra, and can be computed by the smoothing of the peaks in the damping tail. For example, $A_{\text{lens}} = 0$ indicates no lensing effect, whilst for $A_{\text{lens}} = 1$ one recovers the value expected in GR. It is quite interesting to note that for *Planck* CMB power spectra one finds a preference for $A_{\text{lens}} > 1$ at more than 95% CL for both Plik and CamSpec likelihoods, with a large improvement of the χ^2 . Moreover, the inclusion of BAO data shows an evidence for $A_{\text{lens}} > 1$ at more than 99% CL for Plik likelihood and about 99% for the CamSpec likelihood.

The evidence for $A_{\text{lens}} > 1$ is not easily describable in the existing theoretical frameworks and this requires some new challenges in theory, for example, we need either a closed Universe model and surely challenge several observational datasets and the simplest inflationary models, see Ref. Di Valentino et al. (2019b); Handley (2021); Di Valentino et al. (2021f) and subsection 8.2, or we need more exotic cosmological theories that would lead to modifications of the GR Ade et al. (2016e); Di Valentino et al. (2016c); Aghanim et al. (2020b), a running of the running of the spectral index Cabass et al. (2016), or compensated baryon isocurvature perturbations Muñoz et al. (2016); Valiviita (2017), or a Ginzburg-Landau Theory of DE Banihashemi and Khosravi (2022). Moreover, this lensing anomaly is not observed in the *Planck* trispectrum data (i.e. CMB lensing) which offer a complementary and independent measurement of the parameters. If the A_{lens} anomaly does not call for a new physics, then this anomaly may connect to a mild but undetected systematic error in all the releases of the *Planck* data Ade et al. (2014e); Di Valentino et al. (2013); Ade et al. (2016g); Aghanim et al. (2020b) that one cannot rule out from the current picture. If A_{lens} is related to systematics, then we need to understand how this systematic could affect the constraints on the Hubble constant or S8 parameter, and hence on the different tensions explored in this work.

A recently developed method to directly constrain the CMB gravitational lensing potential from the CMB data is based on a principal component decomposition of the lensing power spectrum Motloch and Hu (2018). This approach extends the usual A_{lens} analysis by introducing arbitrary shape variations around a fixed fiducial lensing power spectrum. Marginalizing over effective parameters $\Theta^{(i)}$ leads to interesting implications in various extensions of the Λ CDM model. In the Λ CDM+ N_{eff} scenario marginalizing lensing substantially broadens the H_0 constraints, $H_0 = (68.2 \pm 1.6) \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Motloch and Hu (2020). The lensing-like anomaly also strengthens the constraints on neutrino masses. In fact, ignoring *Planck* lensing reconstruction ie allowing for an arbitrary gravitational lensing potential one finds $\sum m_{\nu} < 0.87$ eV at 2σ Motloch and Hu (2020) which is three times weaker than the *Planck* constraint. On the other hand when including BAO, supernova constraints, and *Planck* lensing reconstruction, the neutrino mass constraint degrades only by 20% over the *Planck* constraint after marginalizing over lensing information $\Theta^{(i)}$.

The latest ACT measurements find no deviation from the standard lensing effect predicted in the Λ CDM model, $A_{\text{lens}} = 1.01 \pm 0.11$ Aiola et al. (2020). Recent measurements of TE and EE power spectra collected by SPT-3G are also consistent with the standard model prediction, $A_{\text{lens}} = 0.98 \pm 0.12$ Dutcher et al. (2021). Finally, combining *Planck* TT ($\ell < 1000$) and SPTPol polarization and gravitational lensing measurements arrives at $A_{\text{lens}} = 0.99 \pm 0.03$ Chudaykin et al. (2020a). These results indicate that the lensing anomaly persists only in the *Planck* data at small scales and is absent for other CMB experiments. Forecasts for future CMB data have been performed in Ref. Renzi et al. (2018).



Fig. 18. Left panel: 68% CL and 95% CL contour plots for Ω_k and A_{lens} from Ref. Di Valentino et al. (2019b). Right panel: 1D posterior distributions on Ω_k from Ref. Aiola et al. (2020).

8.2. Hints for a closed universe from Planck data

The enhanced lensing amplitude (A_{lens} anomaly Calabrese et al. (2008); Aghanim et al. (2020b)) in the CMB power spectrum indicated by the different *Planck* data releases is a significant challenge for the standard Λ CDM model. A physical explanation for this enhancement could be provided in the context of a closed Universe which due to this anomaly, is preferred over a flat Universe at a level of 3.4σ Di Valentino et al. (2019b); Aghanim et al. (2020b); Handley (2021).³³ This disagreement with the predictions for a flat Universe of the standard model is due to the strong degeneracy between the A_{lens} parameter Calabrese et al. (2008); Aghanim et al. (2020b), and the spatial curvature parameter Ω_k as indicated in Fig. 18. A closed Universe could also reduce the well-know tension between the low and high *l* multipoles of the angular CMB power spectrum Addison et al. (2016); Aghanim et al. (2017); Di Valentino et al. (2019b). The oscillating features of the CMB power spectrum indicating spatial curvature could be due to unresolved systematics in the *Planck* 2018 data, or can be simply due to statistical fluctuations.

In fact, while *Planck* 2018 Aghanim et al. (2020b) finds $\Omega_k = -0.044^{+0.018}_{-0.015}$,³⁴ i.e. $\Omega_k < 0$ at about 3.4 σ ($\Delta \chi^2 \sim -11$) using the baseline Plik likelihood Aghanim et al. (2020c), the evidence is reduced when considering the alternative CamSpec Efstathiou and Gratton (2019) likelihood (see discussion in Efstathiou and Gratton (2020)), albeit with the marginalized constraint still above the 99% CL ($\Omega_k = -0.035^{+0.018}_{-0.013}$).

If A_{lens} anomaly demands for more lensing, and this is connected to an increase in the cold dark matter density, then it could be explained by a closed Universe. However, in this case, H_0 from *Planck* could be very small, something like $H_0 \sim 55 \,\text{km s}^{-1} \,\text{Mpc}^{-1}$ Aghanim et al. (2020b); Di Valentino et al. (2019b); Handley (2021), exacerbating the Hubble tension as well as the S_8 tension.

Other combinations of data considered in the literature appear to favour (or not favour) a closed Universe at varying levels of statistical significance. In particular:

- The recent results from the ground-based experiment ACT, in combination with data from the WMAP experiment, are fully compatible with a flat Universe with $\Omega_k = -0.001^{+0.014}_{-0.010}$.
- The same ACT data when combined with a portion of the *Planck* dataset lead to slight preference for a closed Universe since in this case $\Omega_k = -0.018^{+0.013}_{-0.010}$ Aiola et al. (2020), see Fig. 18.
- A closed Universe is preferred by a combination of non-CMB data obtained by Baryon Acoustic Oscillation (BAO) measurements Beutler et al. (2011); Ross et al. (2015); Alam et al. (2017); Benisty and Staicova (2021a), SNIa distances from the recent Pantheon catalog Scolnic et al. (2018), and a prior on the baryon density derived from measurements of primordial deuterium Cooke et al. (2018) assuming Big Bang Nucleosynthesis (BBN). In the context of this combination, a much larger H_0 Di Valentino et al. (2019b) is obtained in agreement with the SH0ES value Riess et al. (2021b, 2019) of H_0 .
- A flat Universe is preferred by the combination *Planck* + BAO, or + CMB lensing Aghanim et al. (2020d) or + Pantheon data. However these dataset combinations are in disagreement at more than 3σ when the curvature is allowed to vary Di Valentino et al. (2019b); Handley (2021); Vagnozzi et al. (2021a).
- A phantom closed Universe is preferred by *Planck* combined with the luminosity distance probes, such as Pantheon or SH0ES, when the dark energy equation of state is let free to vary, along the curvature, at more than 99% CL Di Valentino et al. (2021f).
- A flat Universe is also in agreement with the analysis made by Liu et al. (2020) using the H(z) sample from the cosmic chronometers (CC) and the luminosity distance $D_L(z)$ from the 1598 quasars ($\Omega_k = 0.08 \pm 0.31$) or the Pantheon sample ($\Omega_k = -0.02 \pm 0.14$), in agreement with the previous analysis of Cai et al. (2016b) (in these analyses however, the error bars are too large to discriminate among the models).
- In Nunes and Bernui (2020) a combination of BAO+BBN+H0LiCOW provides $\Omega_k = -0.07^{+0.14}_{-0.26}$ with H_0 in agreement with R19, while BAO+BBN+CC gives a positive $\Omega_k = 0.28^{+0.17}_{-0.28}$.
- The curvature can also be measured model-independently via the \mathcal{O}_k parameter Clarkson et al. (2008); L'Huillier and Shafieloo (2017); Marra and Sapone (2018); Shafieloo et al. (2018b)

 $^{^{33}}$ There is a related preference of the *Planck* dataset at more than 2σ for Modified Gravity Aghanim et al. (2020b); Di Valentino et al. (2016c); Ade et al. (2016e); Capozziello (2002).

³⁴ All the bounds are reported at 68% confidence level in the text.

$$\mathcal{O}_k(z) = \frac{(h(z)\mathcal{D}'(z))^2 - 1}{\mathcal{D}^2(z)},$$
(127)

which is constant and equal to the curvature parameter Ω_k in an FLRW Universe. Departures from constancy could point towards departure from FLRW or the presence of systematics in the data. Current data (Supernovae from Pantheon and BAO from BOSS) are consistent with a flat FLRW L'Huillier and Shafieloo (2017); Shafieloo et al. (2018b).

• Another approach is to use three distances between a source, lens, and the observer to estimate the curvature independently from cosmological assumptions Räsänen et al. (2015); Denissenya et al. (2018). This does not involve any derivative and is consistent with a flat Universe in the context of large uncertainties.

Overall, the spatial curvature remains insensitive to local H_0 measurements from the Cepheid distance ladder Zuckerman and Anchordoqui (2022). However, in general, letting the curvature free to vary implies an increase of both the H_0 and the S_8 tensions Di Valentino et al. (2019b). Therefore, the constant-curvature degree of freedom of the standard model is not sufficient to explain the tensions and anomalies seen in the data. However, within full GR, in the context of the scalar averaging scheme, the average scalar curvature can provide considerably stronger evolutionary impact Heinesen and Buchert (2020).

Detecting a curvature Ω_k different from zero could be due to a local inhomogeneity biasing our bounds Bull and Kamionkowski (2013), and in this case CMB spectral distortions such as the KSZ effect and Compton-y distortions, present a viable method to constrain the curvature at a level potentially detectable by a next-generation experiment. If a curvature Ω_k different from zero is the evidence for a truly superhorizon departure from flatness, this will have profound implication for a broad class of inflationary scenarios. While open Universes are easier to obtain in inflationary models Gott (1982); Linde (1998); Bucher et al. (1995); Kamionkowski et al. (1994); Kamionkowski and Spergel (1994), with a fine-tuning at the level of about one percent one can obtain also a semi-realistic model of a closed inflationary Universe Linde (2003); Lasenby and Doran (2005). In Ref. Leonard et al. (2016) it has been shown that forthcoming surveys, even combined together, are likely to place constraints on the spatial curvature of $\sim 10^{-3}$ at 95% CL at best, but enough for solving the current anomaly in the *Planck* data. Experiments like *Euclid* and SKAO, instead, may further produce tighter measurements of Ω_k by helping to break parameter degeneracies Di Dio et al. (2016); Vardanyan et al. (2009).

8.3. Large-angular-scale anomalies in the CMB temperature and polarization

Several features unexpected in Λ CDM cosmology have been noted in CMB temperature fluctuations at the largest angular scales. Most of these anomalies share several common features:

- they refer to the largest observable angular scales $\gtrsim 60^{\circ}$ whether directly as large-angle two-point functions (lack of large-angle correlations, quadrupole-octopole anomalies), or as large-angle modulations of smaller-angular-scale fluctuations (hemispherical asymmetries, point parity anomaly);
- they are not captured in a standard experimental Λ CDM likelihood function because they are not deviations of individual C_{ℓ} from the values predicted by Λ CDM with appropriate parameters; they are therefore characterized by statistics that were proposed *post-facto* to capture a pattern noticed in the data;
- WMAP and Planck are in remarkable agreement about them being real features on the sky.

An additional anomaly, that is on somewhat smaller scales ($\simeq 10^{\circ}$), but shares the other features, is the so-called "cold spot." We now describe the most compelling of these anomalies:

- 1. the lack of large-angle CMB temperature correlations;
- 2. hemispherical power asymmetry;
- 3. octopole planarity and alignment with the quadrupole;
- 4. the point-parity anomaly;
- 5. variation in cosmological parameters over the sky;
- 6. the cold spot.

In contrast to the Hubble constant tension ($\sim 5\sigma$), these anomalies are individually statistically less significant (2σ to 4σ). However, within Λ CDM, they appear to be statistically independent, although this has been rigorously demonstrated only for the first and last of the above list. Jointly, they are highly significant. An understanding of their nature can point to new physics in the primary perturbations formation process or shed light on unaccounted systematic effects in both astronomical and CMB data Ade et al. (2016f); Akrami et al. (2020b).

We make clear below why these anomalies are difficult to explain in the context of Λ CDM. We explore the Λ CDM predictions for analogous statistics (if any) for polarization, and contrast those predictions with what might be expected from explanations of the anomalies based on new physics. Finally, we discuss how future experiments could be valuable and why they should make the testing of these predictions a key element of their scientific programs.

8.3.1. The lack of large-angle CMB temperature correlations

Suppressed correlations at the largest observable angular scales had been noticed in the COBE data Bennett et al. (1993). Specifically, the two-point angular correlation function

$$\mathcal{C}(\theta) \equiv \overline{T(\hat{e}_1)T(\hat{e}_2)},$$

(128)

(where the average is over all pairs of pixels with $\hat{e}_1 \cdot \hat{e}_2 = \cos \theta$) was found to be very close to zero on scales above $\sim 60^\circ$ Hinshaw et al. (1996). The near-vanishing of the large-angle correlation function was clear in the early WMAP data Spergel et al. (2003), and was later confirmed in the 3-yr Copi et al. (2007) and the 5-yr WMAP data in Copi et al. (2009), as well as in the *Planck* data Copi et al. (2015a).



Fig. 19. Left panel: Two-point angular correlation function, $C(\theta)$, computed in pixel space, for three different bands masked with the KQ75 mask (from WMAP 5 year data). Also shown is the correlation function for the ILC map with and without the mask, and the value expected for a statistically isotropic sky with best-fit Λ CDM cosmology together with 68% cosmic variance error bars. *Right panel*: Same, but for alternative sky cuts applied to WMAP and *Planck* data. Notice the remarkable mutual agreement between the inferred large-angle correlation functions. Both panels adopted from Ref. Copi et al. (2015a).

Fig. 19, adopted from Ref. Copi et al. (2015a), illustrates the degree to which the correlations are suppressed on the cut sky (part of the sky not contaminated by Galactic emission) for both WMAP and *Planck*. The most striking feature of the cut-sky $C(\theta)$ is that it is very nearly zero above about 60°, except for some anti-correlation near 180°. This is true for all reasonable Galaxy masks, for all WMAP and *Planck* CMB-dominated wavebands, in all data releases. It is also true for $C(\theta)$ calculated from the pseudo- C_{ℓ} using $C(\theta) = \sum_{\ell} C_{\ell} P_{\ell}(\cos \theta)$.

In order to be more quantitative about these observations, the WMAP team Spergel et al. (2003) introduced a statistic that quantifies the deviation of $C(\theta)$ from zero,

$$S_{1/2} \equiv \int_{-1}^{1/2} [\mathcal{C}(\theta)]^2 \, \mathsf{d}(\cos\theta).$$
(129)

Spergel et al. (2003) found that only 0.15% of the realizations in their Markov chain of Λ CDM model CMB skies had lower values of $S_{1/2}$ than the observed one-year WMAP cut sky. Extending this to later releases of WMAP data, as well as *Planck*, the p-value becomes ballpark 0.1%, depending on the map and mask used Copi et al. (2015a); see again Fig. 19. There have been some suggestions that certain three-point and four-point functions are also anomalous Ade et al. (2014d, 2016f); Eriksen et al. (2005); we discuss that below in the context of hemispherical asymmetry, where this anomaly is more evident.

While $C(\theta)$ computed in pixel space over the masked sky agrees with the harmonic space calculation that uses the pseudo- C_{ℓ} estimator, it somewhat disagrees with the $C(\theta)$ obtained from a variety of foreground-corrected reconstructed *full-sky* maps. The latter however agree with the $C(\theta)$ calculated using the maximum-likelihood estimator (MLE) C_{ℓ} that are typically reported. These $C(\theta)$ have $S_{1/2}$ that are low only at the $p \simeq 0.05$ level Copi et al. (2011). However, problematically, the full-sky map $C(\theta > 60^\circ)$ is dominated by pairs of points at least one of which is in the masked region, suggesting that the full-sky $C(\theta)$ is potentially contaminated by artefacts coming from the galactic plane. Nevertheless, it is the angular correlation function observed on unmasked, "clean" portions of the sky that is statistically low at the level of $p \simeq 0.0003$ –0.003 (depending on the choice of the map and the sky cut).

In Ref. Efstathiou et al. (2010) it is argued that $C(\theta)$ cannot be used to exclude the Λ CDM model. The relevant low- ℓC_{ℓ} have large cosmic variance as a fraction of their expected values, so inferred C_{ℓ} can differ markedly from the expected values. This results in very large sampling covariance error predictions for $C(\theta)$ in Λ CDM. Moreover $C(\theta)$ could be small because the Λ CDM predictions have more power on the low C_{ℓ} than the actual CMB measurements. The significance of the discrepancy then depends on the model assumptions Gaztañaga et al. (2003); Camacho-Quevedo and Gaztañaga (2021). Nevertheless, using model-independent errors, based only on direct measured sampling variations, Ref. Camacho-Quevedo and Gaztañaga (2021) finds strong evidence for a homogeneity scale and lack of correlations on scales larger than $\theta_{\text{CMB}} \simeq 66 \pm 9$ degrees on the CMB sky.

It is widely underappreciated, however, that the smallness of $S_{1/2}$ is *not* primarily due to the smallness of any individual C_{ℓ} nor set of C_{ℓ} s, and so is *not* accurately described as a "lack of large-angle power". Rather, it is due to cancellations among the contributions of the low- ℓC_{ℓ} to $S_{1/2}$ up to at least $\ell = 5 - C_2$ is almost optimal Copi et al. (2009) to cancel the contributions of $C_{\ell>2}$. In other words, $\langle C_{\ell}C_{\ell'} \rangle \not\propto \delta_{\ell\ell'}$. The fractionally large variance in the low- ℓC_{ℓ} actually makes such correlations less likely to emerge accidentally. Such correlations between C_{ℓ} do not feature (at least at leading order) in vanilla Λ CDM likelihoods, because Λ CDM says that there are no such correlations. Thus parameter fitting within Λ CDM, comparisons of Λ CDM with other statistically isotropic models, and even goodness-offit tests of Λ CDM will not be sensitive to these correlations—they are either statistical flukes, or evidence of a violation of a fundamental assumption of vanilla Λ CDM.

Thus the $S_{1/2}$ anomaly as realized on the observed sky is evidence for the violation of statistical isotropy, which we might expect to result also in more general correlations between $a_{\ell m}$ as we discuss below. Explanations of this anomaly are relevant only if they accomplish it through such cancellation and not by reducing low- ℓC_{ℓ} . This cannot be accomplished by, for example, changing the primordial power spectrum P(k). Non-trivial topology has been shown to be able to produce low $S_{1/2}$ with appropriate C_{ℓ} Bernui et al. (2018), albeit with a fundamental domain that is ruled out by the absence of pairs of matched circles in CMB *T* maps Vaudrevange et al. (2012).

In Ref. Aurich et al. (2021) it is argued that the lack of power on large scales may be simply due to the fact that our Universe is of a finite topology. Samples of 100,000 CMB maps with cubic 3-torus topology are shown to be consistent with the large-angle CMB temperature correlations, when the Dirichlet domain side length of our Universe is around three times the Hubble length. Meanwhile,

the $\simeq 60^{\circ}$ angular scale corresponds to the causal horizon of a $\Omega_{\Lambda} \simeq 0.7$ Universe Camacho-Quevedo and Gaztañaga (2021), which is in agreement with the super-horizon anomalies found in the fit to the small scale CMB acoustic peaks, see below in Sec. 8.3.5.

8.3.1.1. Predictions. Given the concern that this anomaly (and others) are based on *a posteriori* statistics, with unknown look-elsewhere effects, to be more fully convinced that they are due to new physics, rather than a statistical fluke, requires testable predictions. The first type of predictions come from Λ CDM conditioned on one or more anomaly (or more generally on the measured temperature maps); these can be used to test the "fluke hypothesis" that the anomalies are not signs of new physics. The second type of predictions would best come from a model of new-physics. However, even absent that one can in some cases argue generically that a physical explanation would likely have certain consequences.

Prediction for C_1^T : An important point that is widely overlooked is that $C(\theta)$ as discussed above is actually the monopole-and-dipole subtracted angular correlation function, which we write $C_{\ell \ge 2}(\theta)$. A physical explanation of $S_{1/2}$ seems likely to predict that $C(\theta)$ is small, not just $C_{\ell \ge 2}(\theta)$. This requires that the cosmological (i.e., non-Doppler) contribution to $C_1^T \le 200 \,\mu\text{K}^2 \ll \langle C_1^{\text{ACDM}} \rangle \simeq 3000 \,\mu\text{K}^2$ Copi et al. (2015a). This happens by chance less than 0.5% of the time in ACDM with standard cosmological parameters, and so if a low C_1 were observed it would be compelling evidence of a physical origin for low $S_{1/2}$. This suggests that measuring the CMB Doppler dipole well enough to separate out the intrinsic C_1 is worthwhile. Similar statements could perhaps be made about the cosmological monopole C_0 , the fluctuation in T_{CMB} in our current Hubble patch about the mean calculated over an infinite, or at least much larger volume, but that is presumably not measurable.

Predictions for Polarization: Λ CDM realizations of temperature and *E*-mode and *B*-mode polarization are usually generated together, with $a_{\ell m}^T$, and $a_{\ell m}^E$ correlated Gaussian random variables characterized by C_{ℓ}^{TT} , C_{ℓ}^{TE} , and C_{ℓ}^{TE} , while $a_{\ell m}^B$ is a Gaussian random variable characterized by C_{ℓ}^{BB} . However, given measurements of $a_{\ell m}^T$, one can produce constrained realizations of $a_{\ell m}^E$ yoho et al. (2014); realizations of $a_{\ell m}^B$ are unchanged since *B* is uncorrelated with *E*. One can then calculate $a_{\ell m}^Q$ and $a_{\ell m}^U$, for the Q and U mode polarizations, and assemble predictions for $C^{\text{QQ}}(\theta)$, $C^{\text{UU}}(\theta)$, $C^{\text{TQ}}(\theta)$, and $C^{\text{TU}}(\theta)$, as well as associated $S_{1/2}$ statistics, Because *TE* correlations are weak in Λ CDM ($(C_{\ell}^{\text{TE}})^2 \ll C_{\ell}^{\text{TT}} C_{\ell}^{\text{EE}}$), the suppression of $C^{TT}(\theta > 60^\circ)$ does not lead to the suppression of QQ and UU angular correlation functions Yoho et al. (2015), with, for example, $(S_{1/2}^{QQ}) \simeq 0.012 \,\mu$ K⁴ and $(S_{1/2}^{UQ}) \simeq 0.013 \,\mu$ K⁴ for r = 0.1, essentially unchanged from unconstrained Λ CDM. A low measured value for either would be a statistically independent anomaly for Λ CDM. Meanwhile, it would be expected that a physical model would predict suppression of these correlation functions.

There is some subtlety regarding angular correlation functions for polarization Yoho et al. (2015). Whereas, once certain conventions have been established, $Q(\hat{n})$ and $U(\hat{n})$ are fields measured on the sky, the separation into E and B is performed in harmonic space, and the reassembly into $E(\hat{n})$ and $B(\hat{n})$ is ambiguous. The local-E and local-B fields Yoho et al. (2015), \hat{E} and \hat{B} , are heavily weighted toward high- ℓ contributions, and in particular the usual θ to $1/\ell$ correspondence fails for $C(\theta)$ for $\hat{E}\hat{E}$ or $\hat{B}\hat{B}$. This makes $S_{1/2}^{\hat{E}\hat{E}}$ and $S_{1/2}^{\hat{B}\hat{B}}$ independently interesting Yoho et al. (2015), both as null tests for Λ CDM and as tests of physical explanations for the low $S_{1/2}^{TT}$. It is also possible to put other two-point angular correlation functions to good use, such as between temperature and lensing potential, or temperature and 21-cm fluctuations. In such cases, the optimum range of $\cos \theta$ over which to integrate should be determined *a priori* Yoho et al. (2014). Future full-sky polarization observation programs could readily measure all interesting polarization $S_{1/2}$ statistics and test the Λ CDM predictions Yoho et al. (2015).

8.3.2. Hemispherical power asymmetry

Here, we focus on a number of large-scale anomalies, which in spite of having been detected with different methods and statistics, all show some level of asymmetry in power (or related properties) between hemispheres on the CMB sky; this is why we collectively call them "hemispherical power asymmetry." We do not intend to provide an historical overview of these anomalies or an exhaustive review of the literature on detection, analysis and interpretation of the anomalies. Our aim in this subsection is rather to highlight the most statistically significant hints of the power asymmetry and their common features, with the objective of emphasising their potential importance for both theoretical cosmology and future CMB and large-scale-structure observations.

The bulk of this section discusses tests that involve the so-called dipolar power asymmetry or "dipole modulation," either directly or via measures of directionality, even though there are reasons to believe that such a dipolar description of the asymmetry oversimplifies the actual anomaly. One main reason is that most of the analyses imply that only the hemispheres which include all or most of the northern ecliptic hemisphere are anomalous and the southern ones seem to be consistent with an isotropic Λ CDM CMB sky. Nevertheless, various forms of dipole modulation have been noted since the early WMAP releases Eriksen et al. (2004a) and later confirmed by *Planck* Ade et al. (2014d, 2016f); Akrami et al. (2020b). All the dipole-modulation tests we discuss here can be divided into two categories, amplitude-based and direction-based, and share in common the fitting of a dipole, which is done either by fitting for a dipole explicitly in a map of power on the sky, by employing Bayesian techniques in pixel space for a specific model, or by measuring the coupling of ℓ to $\ell \pm 1$ modes in the CMB covariance matrix. Given the differences in the approaches, it is important to keep in mind that the results cannot usually be directly compared, even though all probe some aspect of dipolar asymmetry.

8.3.2.1. Low northern variance. A low value for the variance of the CMB temperature fluctuations was originally observed in the WMAP data by Refs. Monteserin et al. (2008); Cruz et al. (2011); Gruppuso et al. (2013). This low variance was then confirmed by the *Planck* collaboration Ade et al. (2014d, 2016f); Akrami et al. (2020b), with a *p*-value of 0.5%-1.0% for the low-resolution temperature maps ($N_{side} = 16$), depending on whether the impact of a possible look-elsewhere effect is considered. *Planck* 2013 Ade et al. (2014d) showed, using both full-resolution ($N_{side} = 2048$) and low-resolution ($N_{side} = 16$) maps that the low variance was localised in the northern ecliptic hemisphere, with a *p*-value of ~ 0.1%, while the *p*-value for the southern hemisphere was ~ 45%. Similar levels of significance were also found for the Galactic northern and southern hemispheres when the full-resolution maps were used. No updates on these significance levels have been provided by *Planck* 2015 Ade et al. (2016f) and 2018 Akrami et al. (2020b). It is important to note that the map-based variance is dominated by contributions from large angular scales, whilst the cosmological parameter fits are relatively insensitive to these

low-order ℓ -modes and are instead largely dominated by scales corresponding to $\ell > 50$. Therefore, the variance of the temperature CMB sky appears to be anomalous as there is a dearth of large-angular-scale power compared to the predictions of the Λ CDM model with parameters estimated using the same CMB sky. Finally, it is important to note that although the anomaly discussed here is about the variance of the CMB fluctuations, it can be seen as an indirect indication of power asymmetry, as variance is nothing but a weighted sum of the angular power spectrum of the fluctuations over all multipoles.

8.3.2.2. Hemispherical asymmetry. Refs. Eriksen et al. (2004a); Hansen et al. (2004) discovered that the angular power spectrum of the first year WMAP data calculated for a hemisphere centred at the Galactic coordinates $(l, b) = (273^{\circ}, -20^{\circ})$ was larger than when calculated for the opposite hemisphere over the multipole range $\ell = 2 - 40$. Ref. Park (2004) also presented evidence for the existence of such hemispherical asymmetry by applying a Minkowski functional to the WMAP data. The preferred direction of Ref. Eriksen et al. (2004a) lies close to the ecliptic plane, and they also demonstrated that the large-angular real-space *N*-point correlation functions (for N = 2, 3, 4) were different when computed on ecliptic hemispheres. Many studies then focused on hemispheres in the ecliptic coordinate system, with Ref. Schwarz et al. (2004) particularly emphasizing the connection. Finally, Refs. Eriksen et al. (2004b, 2005); Rath et al. (2007) also detected the hemispherical asymmetry with other measures of non-Gaussianity.

In 2013, the *Planck* collaboration Ade et al. (2014d) studied the asymmetry by computing four *N*-point correlation functions (2-point function, pseudo-collapsed 3-point function, equilateral 3-point function and rhombic 4-point function) on the northern and southern ecliptic hemispheres for the *Planck* 2013 $N_{side} = 64$ temperature maps. The results were in agreement with the findings of Ref. Eriksen et al. (2004a). It was shown, particularly, that the northern ecliptic hemisphere correlation functions were relatively featureless, and in particular, both the 3- and 4-point functions were very close to zero. The northern hemisphere *p*-values for the χ^2 statistic were found to be > 93% for all the four correlation functions and > 99% for the 3- and 4-point functions, with the significance level exceeding 99.9% for the pseudo-collapsed 3-point function. This was all consistent with the anomalous lack of power towards the northern ecliptic pole seen by the simpler one-point statistic, i.e. the low northern variance anomaly discussed earlier. Similar analyses were done in reference frames set by Galactic coordinates and the CMB Doppler boost direction (see e.g. Quartin and Notari (2015)), as well as the angular-clustering and dipole-modulation directions that we will discuss below. Although the largest asymmetry was seen for the ecliptic hemispheres, a substantial asymmetry was present also for Galactic coordinate hemispheres.

The *Planck* 2015 analysis Ade et al. (2016f) confirmed all of these high levels of significance, and additionally found that a substantial asymmetry was present also for the dipole-modulation direction. Surprisingly though, the latest *Planck* 2018 analysis Akrami et al. (2020b) no longer observed the high significance level for the pseudo-collapsed 3-point function of the temperature map in the northern ecliptic hemisphere. The *Planck* collaboration states Akrami et al. (2020b) that this discrepancy between the first two and the final releases of the data may be due to the different masks used in the analyses or a consequence of "the improved treatment of poorly determined modes in the estimated correlation matrix used for the computation of the χ^2 statistic." Even if these are the reasons behind the discrepancy, the fact that the anomaly has been observed persistently and consistently in both the WMAP data and the first two releases of the *Planck* data (with different systematics) strongly suggests that the changes in the mask or the improvement in the analysis might have removed important information in the data that would contribute significantly to this anomaly, and the low significance seen in the *Planck* 2018 data should therefore be considered with caution. *Planck* 2018 found, however, that in the dipole-modulation reference frame the 3-point temperature correlation functions in the negative (northern) hemisphere were somewhat significant, reaching a level of 98% – 99% for the pseudo-collapsed case.

8.3.2.3. Angular clustering of the power distribution. In a search for dipolar power asymmetry, Ref. Hansen et al. (2009) analysed the 5-year WMAP data by computing the CMB power spectrum on a number of discs on the sky and binning them into independent blocks of 100 multipoles from $\ell = 2$ to $\ell = 600$. Each block was then used to look for a dipolar asymmetry in the power distribution. The six ℓ ranges considered showed evidence of a consistent dipole direction, and not a single realization in a set of 10,000 simulations showed a similarly strong asymmetry.

A similar analysis was then performed by the *Planck* collaboration in 2013 Ade et al. (2014d), where a simpler approach developed by Ref. Axelsson et al. (2013) and applied to the 9-year WMAP data was used. *Planck* 2013 estimated the power spectrum amplitude on 12 non-overlapping patches of the sky in ℓ -bins of 16 multipoles each, and fitted a dipole to the spatial distribution of the amplitudes for each ℓ -bin. The alignment of the dipole directions between the different multipole blocks was then used to construct a measure of the power spectrum asymmetry. They compared the clustering of the dipole directions evaluated for the different scales to that observed in simulated maps. None of the 500 available simulations showed degrees of clustering higher than the one observed in the data for two choices of $\ell_{max} = 600$ and $\ell_{max} = 1500$. However, after deboosting the data (i.e. correcting for the Doppler modulation effect), the significance went down for $\ell_{max} \gtrsim 600$, and therefore, a significant power asymmetry was claimed only up to $\ell \sim 600$. The $\ell_{max} = 1500$ deboosted case, however, resulted in the mean dipole direction of $(l, b) = (218^\circ, -21^\circ)$, which was intriguingly close to the direction found for the dipole modulation, as we will discuss below. Even though a power asymmetry was detected using the angular clustering of the preferred directions for different bins, the ratio of the power spectra in the two opposite hemispheres defined by the asymmetry axis for $\ell = 2 - 600$ was not statistically anomalous. The interpretation for this was that the power asymmetry detected through the clustering technique might be different from the one found by other methods with statistics based on the amplitude of the asymmetry, usually quantified by a dipole (as done, e.g., in the cases of dipole modulation and local-variance asymmetry discussed below).

In an updated and extended analysis, *Planck* 2015 Ade et al. (2016f) considered bin sizes between $\Delta \ell = 8$ and $\Delta \ell = 32$ for the multipole range of $\ell = 2 - 1500$. In contrast to the *Planck* 2013 results where the *p*-values started to increase systematically for $\ell_{max} \gtrsim 600$, here they remained low for $\ell_{max} > 750$. Depending on the bin size and component separation method, *p*-values were as low as < 0.04%. These all suggest that, beyond a dipole modulation of power on large angular scales, some form of directional asymmetry continues to small scales. There are also indications that the directions of dipolar asymmetry are correlated between large and small angular scales.

8.3.2.4. Dipole modulation (pixel-based likelihood). Even though no compelling theoretical explanation exists for the nature of the hemispherical power asymmetry, a phenomenological multiplicative dipole modulation model, suggested by Ref. Gordon et al. (2005), has been widely used to study the asymmetry through a model-dependent, Bayesian approach. Here, the asymmetry is modelled in terms of a dipole modulation of the form

$$\frac{\Delta T}{T}|_{\text{mod}}(\hat{\mathbf{n}}) = (1 + \alpha \, \hat{\mathbf{n}} \cdot \hat{\mathbf{p}}) \frac{\Delta T}{T}|_{\text{iso}}(\hat{\mathbf{n}}),$$
(130)

where $\frac{\Delta T}{T}|_{iso}$ and $\frac{\Delta T}{T}|_{mod}$ are the isotropic and modulated CMB temperature fluctuations along a direction $\hat{\mathbf{n}}$ on the sky, respectively, and α is the amplitude of the dipole modulation and $\hat{\mathbf{p}}$ is the preferred direction.

It is important to note that since various other analyses of the CMB sky seemed to imply that the southern hemisphere was relatively consistent with an isotropic ACDM sky and it was the northern hemisphere that showed an anomalous deficit of power, the dipole modulation may not be a well justified way of modelling the asymmetry; it has been used mainly because of its simplicity. Refs. Eriksen et al. (2007); Hoftuft et al. (2009) studied the dipole modulation model using the 3- and 5-year WMAP data, respectively, and the Planck collaboration then performed a similar direct pixel-space likelihood analysis of the model in their 2013 Ade et al. (2014d) and 2015 Ade et al. (2016f) investigations of the hemispherical power asymmetry by only considering large angular scales. Planck used $N_{side} = 32$ temperature maps, smoothed to angular resolutions ranging from 5° to 10° FWHM. Planck 2015 particularly focused on a smoothing scale of 5° FWHM as a representative example and the highest angular resolution accessible for an $N_{side} = 32$ map. The results of the analysis were all consistent with those derived from the 5-year WMAP ILC map in Ref. Eriksen et al. (2007). The significance levels for the amplitude of the dipole compared to the ones from the Λ CDM simulations varied with smoothing scale and the 5° scale showed the highest significance ($\sim 3.5\sigma$). It is important to note that the model of Ref. Gordon et al. (2005) assumes that the modulation amplitude α is equally strong on all scales, but it has been shown Quartin and Notari (2015); Notari et al. (2014) that the data are not consistent with a simple constant-amplitude dipole modulation of the power. The preferred direction derived from the low- ℓ dipole modulation analysis, e.g. $(l, b) = (227^{\circ}, -15^{\circ}) \pm 19^{\circ}$ for the Commander component separation technique, is, however, remarkably consistent with the high- ℓ direction derived from the clustering of directions for $\ell \leq 600$. Both *Planck* 2013 and 2015 found almost exactly the same preferred directions.

8.3.2.5. Dipole modulation (QML analysis). In a harmonic-space analysis, Planck 2015 Ade et al. (2016f) used the quadratic maximum likelihood (QML) estimator introduced by Ref. Moss et al. (2011) to assess the level of dipole modulation for the full-resolution ($N_{side} = 2048$) CMB temperature maps. This technique exploits the fact that dipole modulation is equivalent to coupling of ℓ to $\ell \pm 1$ modes in the CMB covariance matrix to leading order. Planck computed *p*-values of the fitted modulation amplitude as a function of ℓ_{max} , and the *p*-values showed several peaks, at $\ell_{max} \approx 40$, $\ell_{max} \approx 67$ and $\ell_{max} \approx 240$. The latter peak, while not previously emphasized, was also present in the WMAP results Bennett et al. (2011a). The dip at $\ell_{max} \approx 67$, with a *p*-value of 0.9% - 1.0% ($\sim 3\sigma$), corresponds to the low- ℓ dipole modulation, which has been the focus of most attention in the literature.

Planck 2018 Akrami et al. (2020b) repeated the analysis and studied two ranges of $\ell = 2 - 64$ and $\ell = 2 - 220$. The preferred direction for the former range was found to be $(l, b) = (221^\circ, -22^\circ) \pm 31^\circ$, while it was $(l, b) = (213^\circ, -26^\circ) \pm 28^\circ$ for the *Planck* 2015 analysis Ade et al. (2016f), both of which are consistent with the directions found through the pixel-based likelihood analysis of dipole modulation. One should note that this QML analysis was a purely phenomenological one performed in multipole space, with no attempt to connect to any real-space modulation. Even though the preferred directions are close to that of a pixel-space likelihood analysis of the dipolar modulation model, the two methods do not necessarily probe the same thing.

Meanwhile, WMAP also observed a dip in the first Doppler peak ($\ell_{max} \approx 220$), an excess at $\ell_{max} \approx 44$, and a dip at $\ell_{max} \approx 22$ that were present in the ecliptic polar data but not the ecliptic planar data, see Fig. 7 of the first arXiv version of their Year 1 paper on the angular power spectrum Hinshaw et al. (2003). That first peak dip was shown in Ref. Yoho et al. (2011) to be localized to the region of the north ecliptic pole, and to persist beyond WMAP1 into later WMAP data releases. This is consistent with the dip's presence in ARCHEOPS data, taken in the northern hemisphere, but in no other pre-WMAP ground-based data.

8.3.2.6. Dipole modulation (Rayleigh statistic). The results of the analysis of the angular clustering of the power distribution performed by the *Planck* collaboration and discussed above suggest that, beyond a dipole modulation of power on large angular scales, some form of directional asymmetry continues to small scales. There are also indications from the same analysis that the directions of dipolar asymmetry are correlated between large and small angular scales. *Planck* 2015 Ade et al. (2016f) then performed a Rayleigh-statistic-based analysis as a generic test for directionality with minimal assumptions about the nature of the asymmetry. The method, however, takes into account other information pertaining to modulation, including its amplitude, in addition to the direction. An asymmetry was found on scales larger than $\ell \approx 240$, and the minimum *p*-value was 0.1% - 0.2%, to be compared to the *p*-value of 0.9% - 1.0% obtained for the dipole modulation amplitude at $\ell_{max} = 67$. The preferred direction for $\ell_{max} \approx 240$ was found to be $(l, b) = (208^\circ, -29^\circ)$, which is approximately 20° away from the dipole modulation direction determined by the QML analysis for the multipole range of $\ell = 2 - 64$.

8.3.2.7. Generalised dipole modulation (bipolar spherical harmonics). The Planck collaboration studied, in both their 2013 Ade et al. (2014d) and 2015 Ade et al. (2016f) analyses, a generalisation of the dipole modulation using the Bipolar Spherical Harmonics (BipoSH) formalism of Refs. Hajian and Souradeep (2003, 2006). Here, the CMB angular power spectrum corresponds to the L = 0 BipoSH coefficients and a dipole modulation corresponds to the bipolar multipole L = 1. The BipoSH formalism provides a unified way to systematically detect and study properties of different types of statistical anisotropy, which may go beyond the dipole modulation. A BipoSH-based simulation tool is available to model Gaussian realizations of CMB temperature and polarization maps with induced isotropy violation Mukherjee and Souradeep (2014). Planck 2013 applied the BipoSH formalism to $N_{side} = 32$ temperature maps and detected a dipole modulation signal with 2.9 σ to 3.7 σ significance, depending on the component separation method. The amplitude and direction of the dipole modulation matched those obtained via the likelihood analysis of dipole modulation. Both Planck 2013 and 2015 also used higher-resolution maps, but the dipole modulation was recovered at over 3 σ significance only for the lowest multipole bin they considered, i.e. $\ell = 2 - 64$. For the full-resolution $N_{side} = 2048$ maps, *Planck* 2015 found a preferred direction of $(l, b) \approx (230^\circ, -18^\circ) \pm 31^\circ$, in very good agreement with the direction inferred from the likelihood analysis of dipole modulation. No significant power was detected at the higher BipoSH multipoles



Fig. 20. Variance asymmetry directions for the four low-resolution ($N_{side} = 64$) component-separated maps Commander (red), NILC (orange), SEVEM (green) and SMICA (blue), and for 4° discs with the lowest *p*-values for *Planck* 2018 temperature (left) and *E*-mode polarization (right) data in Galactic coordinates. Note that the four directions for the temperature maps match almost perfectly, so that the dots with different colours essentially overlap. For reference, four additional directions are also shown in each panel: the north ecliptic pole (NEP), the south ecliptic pole (SEP), the CMB dipole direction and the preferred dipole modulation direction (labelled as "low- ℓ ") derived from the temperature data through the QML analysis. Both panels adopted from Ref. Akrami et al. (2020b).

of the modulation field, $1 < L \le 32$. Assuming a scale-dependent dipole modulation, Ref. Shaikh et al. (2019) has measured this scale dependence using the BipoSH formalism.

8.3.2.8. Variance asymmetry. In an attempt to study the observed CMB power asymmetry in a model-independent way, Ref. Akrami et al. (2014) invented a pixel-space local-variance estimator of the CMB fluctuations using a set of discs of various sizes uniformly distributed on the sky. The technique was first applied to the WMAP 9-year and *Planck* 2013 temperature data in Ref. Akrami et al. (2014) and later used in the analyses of *Planck* 2015 Ade et al. (2016f) and 2018 Akrami et al. (2020b) for both temperature and polarisation. Since the technique looks for deviations from statistical isotropy in terms of the variance of CMB fluctuations by fitting a dipole to a given local-variance map, it can be considered as an alternative way of detecting the hemispherical power asymmetry which had already been detected through the dipole modulation analysis and the angular clustering of dipole directions. This is because variance is effectively a weighted sum of the power spectrum over all scales (or multipoles).

The original analysis of Ref. Akrami et al. (2014) found that none of the 1000 available CMB temperature simulations had a larger variance asymmetry than that estimated from the data. This suggested presence of a power asymmetry at a statistical significance of at least 3.3σ , with a preferred direction of $(l, b) \approx (212^\circ, -13^\circ)$, in good agreement with other studies of the hemispherical power asymmetry. The local-variance estimator was then applied to the full-resolution $N_{side} = 2048$ Planck 2015 temperature maps Ade et al. (2016f), and significantly low *p*-values were found, although the significance levels and preferred directions showed slight differences for different disc radii. The highest statistical significance was found for 8° discs with *p*-values less than 0.1%. In an analysis with enhanced sky coverage, where a mask smaller than the Planck's common mask was used, a number of anomalies were restudied through an $N_{side} = 256$ Commander temperature map which included about 93% of the sky. While in general the significance levels and preferred directions for the hemispherical power asymmetry inferred from different techniques did not change much with this reduced mask, the local-variance asymmetry method showed higher significance for larger disc radii. The variance asymmetry technique was finally applied to the *Planck* 2018 temperature data Akrami et al. (2020b) and *p*-values smaller than 0.1% were found for disc radii up to 8° when the full-resolution $N_{side} = 2048$ maps were analysed. The preferred direction was found to be $(l, b) = (205^\circ, -20^\circ)$ for this resolution and for 4° discs, and changed slightly for lower-resolution maps; the direction was found to be $(l, b) = (209^\circ, -15^\circ)$ for $N_{side} = 64$; see Fig. 20 (left panel).

Planck 2018 Akrami et al. (2020b) also studied the hemispherical power asymmetry, as well as a few other large-scale anomalies, for the CMB polarization data. By applying the local-variance estimator of Ref. Akrami et al. (2014) to $N_{nside} = 64$ *E*-mode polarization maps, *Planck* 2018 found preferred directions for polarization with the smallest *p*-values of ~ 0.7% and ~ 0.4% for Commander and SEVEM component-separated maps, respectively, and ~ 5.8% and ~ 5.5% for NILC and SMICA, when 4° discs were used. This difference in the significance levels might reflect differences in the component separation approaches, particularly given that the former methods operate in the pixel domain, while the latter in the harmonic domain. Another interesting finding of the *Planck* 2018 variance asymmetry analysis is that the preferred directions for polarization are intriguingly close to those determined for the temperature data, with the smallest polarization-temperature separation angle of arccos (0.99) for Commander and SMICA (with *p*-values of ~ 0.9%). The preferred directions are $(l, b) = (217^\circ, -10^\circ)$ and $(l, b) = (219^\circ, -16^\circ)$, respectively, which are close to the temperature variance asymmetry direction of $(l, b) = (209^\circ, -15^\circ)$ for the same N_{side} and the dipole modulation direction of $(l, b) = (221^\circ, -22^\circ) \pm 31^\circ$ based on the QML analysis of the 2018 data; see Fig. 20 (right panel). While the differences between the *p*-values and preferred directions associated to the different component-separated polarization maps argue against a detection of cosmological power asymmetry in the polarization data and, therefore, the close alignment of the temperature and polarization directions could simply be a coincidence, future higher-quality polarization data may offer additional insight.

8.3.2.9. Peak distribution asymmetry. The Planck collaboration employed, in both their 2015 Ade et al. (2016f) and 2018 Akrami et al. (2020b) analyses, local extrema (or peaks) in the CMB maps to search for localized anomalies by examining how their statistical properties would vary in patches of the sky as a function of their location. This method was particularly used as a further test for large-scale asymmetries by examining the differences in the peak distribution when divided according to orientation with respect to a previously specified asymmetry direction. In the Planck 2015 analysis, a disc of radius 70° centred on $(l, b) = (225^\circ, -18^\circ)$, the dipole modulation direction found in the SMICA temperature map, and its corresponding antipodal disc were used to select the peaks. For maps filtered with a 40' FWHM GAUSS filter, as well as a number of other filtering scales, the distribution of the peaks for the positive-direction disc was in general agreement with the full sky result, while that for the negative direction (close to the northern ecliptic point) was marginally



Fig. 21. Fig. 5 from Ref. Copi et al. (2015b). Quadrupole and octopole multipole vectors for the Doppler-quadrupole (DQ) corrected SMICA map in Galactic coordinates. The background shows the quadrupole+octopole pattern. The multipole vectors are shown as circles, in red and labelled "Qv" for the quadrupole and in black and labelled "Ov" for the octopole. The directions of the area vectors defined in the text, $\hat{w}^{(\ell;i,j)}$, are shown as squares, with $\ell = 2$ in red and labelled "Qa" and $\ell = 3$ in black and labelled "Oa". Since the multipole vectors are only determined up to a sign each vector appears twice in the figure. The area vectors have only been plotted in the maximum angular momentum dispersion direction for $\ell = 3$, $\hat{n}^{(3)}$ is shown as the black star, Since $\hat{n}^{(2)} = \hat{w}^{(2;1,2)}$. The direction of $\hat{n}^{(2)}$ without the DQ correction is the red diamond. For reference also shown are the ecliptic plane (black line), the north (NEP) and south (SEP) Ecliptic poles, and the CMB (dipole).

different—this again showed that the northern hemisphere is anomalous. *Planck* 2018 repeated the analysis using the direction determined by the SMICA QML estimator, $(l, b) = (213^\circ, -26^\circ) \pm 28^\circ$, and confirmed the 2015 results.

8.3.2.10. Predictions. Limited work has been done to study the predictions of Λ CDM for the wide range of hemispherical power anomalies. However, Ref. O'Dwyer et al. (2017) showed that the Λ CDM predictions for the variance in Q and U polarization conditioned on the low northern temperature variance are nearly unchanged from the unconditioned predictions. Any observed suppression of variance in Q and U in the north would therefore be an independent anomaly in Λ CDM, but might be expected in a physical explanation of the temperature anomaly. We expect that similar statements hold for other characterizations of the hemispherical power asymmetry. However, extension of the dipolar power asymmetry signal beyond $\ell > 64$ Aiola et al. (2015); Shaikh et al. (2019) can lead to a power asymmetry in the lensing B-modes of polarization, as shown in Ref. Mukherjee and Souradeep (2016). This could be measured from the upcoming ground-based CMB experiments such as SO Ade et al. (2019) and CMB-S4 Abazajian et al. (2019b). Other probes such as the kinematic and polarized SZ Cayuso and Johnson (2020) can also explore the power asymmetry signal from future surveys. A violation of statistical isotropy can also lead to direction dependence in the inferred cosmological parameters Mukherjee et al. (2016). While Ref. Mukherjee and Wandelt (2018a) concludes that *Planck* temperature maps do not show any significant departure from statistical isotropy in the inferred cosmological parameters, others Fosalba and Gaztanaga (2020); Yeung and Chu (2022) claim strong evidence of such variation (see subsection 8.3.5). In the future, this can be tested using both temperature and polarization data.

8.3.3. Quadrupole and octopole anomalies

ACDM asserts that the $a_{\ell m}$ are statistically independent random variables. Yet, a_{2m} and a_{3m} show anomalous correlations de Oliveira-Costa et al. (2004), suggesting $\langle a_{\ell m}^{\star} a_{\ell' m'} \rangle \propto \delta_{\ell \ell'} \delta_{mm'}$.

There are two principal statistical approaches to describing these anomalous correlations. The first is in terms of the multipole vectors of the quadrupole and octopole (Fig. 21): $\hat{v}^{\ell,i}$, $i = 1, ..., \ell$, $\ell = 2, 3$. These ℓ unit vectors plus a scalar A_{ℓ} , are an alternative to $a_{\ell m}$ for representing real scalar functions on the sphere. In Λ CDM, the $\hat{v}^{\ell,i}$ of different ℓ are uncorrelated; the correlations between $\hat{v}^{\ell,i}$ of fixed ℓ are calculable.

It was observed in Ref. Schwarz et al. (2004) that the oriented areas (normal) of the plane defined by the two quadrupole multipole vectors $\vec{w}^{2;1,2} \equiv \hat{v}^{2,1} \times \hat{v}^{2,2}$, and those of the 3 planes defined by the three octopole multipole vectors ($i \neq j = 1, 2, 3$), $\vec{w}^{3;i,j} \equiv \hat{v}^{3,i} \times \hat{v}^{3,j}$, are unexpectedly close to one another: the magnitude of the dot products of $\hat{w}^{2;1,2}$, with the three $\hat{w}^{3;i,j}$ are approximately 0.95, 0.87, and 0.84. Using instead the $\vec{w}^{\ell;i,j}$ themselves and not unit vectors parallel to them, the three dot products $|\vec{w}^{2;2,1} \cdot \vec{w}^{3;i,j}|$ are 0.85, 0.78, and 0.78; in Λ CDM, the p-value of these being at least this large is 0.02%! In other words, the three octopole multipole vectors nearly share a common plane, this is called octopole planarity, and that plane is nearly that of the quadrupole. This is quadrupole-octopole alignment.

The quality of this alignment improved noticeably on removing (as one ought) the Doppler contribution to the quadrupole Copi et al. (2015b); Notari and Quartin (2015), reducing the p-value from 0.1% to the 0.02% just quoted. This would be a separate "statistical fluke" in Λ CDM.

The original approach to seeing these alignments was through the angular momentum dispersion in each multipole de Oliveira-Costa et al. (2004), $\sum_m m^2 |a_{\ell m}|_{\hat{n}_{\ell}}^2$. The subscript \hat{n}_{ℓ} indicates that this is a function of the choice of *z* axis. For each ℓ , \hat{n}_{ℓ} is the *z*-axis that maximizes the angular momentum dispersion in that ℓ . In the WMAP 1st year ILC map, $\hat{n}_2 \cdot \hat{n}_3 \simeq 0.98$, which has a p-value of $\simeq 1.5\%$; this again is quadrupole-octopole alignment. It was noted that in this frame the magnitudes of $a_{3\pm 3}$ are much larger than those of other a_{3m} .



Fig. 22. Map of $Z(\hat{\mathbf{n}}) \equiv T(\hat{\mathbf{n}})T(-\hat{\mathbf{n}})$ for SMICA with $\Theta = 5^{\circ}$ smoothing Creswell and Naselsky (2021a). Note, the two pairs of very strong high negative peaks of $Z(\hat{\mathbf{n}})$, labelled 1a/1b and 2a/2b, and about twenty negative peaks with smaller amplitudes, mainly localized within the area $|b| \leq 30^{\circ}$ in Galactic coordinates.



Fig. 23. Left panel: The coloured contours show the posterior distribution of the direction of the dipole modulation in combination with the ring of attraction and 1a/1b and 2a/2b peaks responsible for maximum of the parity asymmetry. The right contour corresponds to the maximum of CMB power, the left contour indicates the minimum. Right panel: The 30 GHz *Planck* map with kinematic dipole. The white ring is the zone where the total signal is vanished.

at a level that has a p-value of 7% in Λ CDM; this is octopole planarity. If the three octopole $\hat{w}^{3,i,j}$ had been exactly parallel, then they would have been parallel to \hat{n}_3 . This common axis has been called "the axis of evil" Land and Magueijo (2005). Finally, there are some suggestions of correlations also between $a_{\ell m}$ of pairs of ℓ other than 2 and 3 Copi et al. (2004b); Land and Magueijo (2005).

There are other unexpected correlations of the quadrupole and octopole, in particular with the ecliptic. The great circle defined by the common plane of the quadrupole and octopole is nearly perpendicular to the ecliptic. Near that great circle the quadrupole-plus-octopole combine to produce 6 extrema. The ecliptic great circle seems to trace out surprisingly well the zero separating three strong extrema in the ecliptic south from three weaker extrema in the ecliptic north. This connection to the ecliptic suggests either an experimental systematic or a solar-system foreground. The WMAP and *Planck* satellites orbited in the plane of the ecliptic and their sampling strategies and noise maps are "ecliptic-aware," however their systematics are very different and both see nearly identical quadrupoles and octopoles. As far as solar-system foregrounds, the structure of the quadrupole and octopole as planar and perpendicular to the ecliptic is entirely unlike anything that would be expected from the solar system itself — no reasonable proposal has been made that would generate the observed quadrupole and octopole.

It has been found that if the Universe has non-trivial topology it can induce correlations between the quadrupole and octopole Bielewicz and Riazuelo (2009), though the statistical evidence for that is weak, and the manifolds specifically consider are ruled out by the search for matched circle pairs Vaudrevange et al. (2012). In such an explanation, the correlations with the ecliptic would be a fluke.

8.3.3.1. Predictions. Because $(C_{\ell}^{TE})^2 \ll C_{\ell}^{TT} C_{\ell}^{EE}$ in Λ CDM, the peculiar correlations of the a_{2m}^T and a_{3m}^T has little effect on the multipoles of polarization. This may not be the case in specific model explanations of the temperature anomaly. For example, one would expect that in a topologically non-trivial manifold, the boundary conditions would imprint not just on the $a_{\ell m}^T$, but equally on the $a_{\ell m}^B$. However, the precise prediction is expected to depend strongly on the specific manifold.

8.3.4. Point-parity anomaly

An anomalous power excess of odd ℓ multipoles compared to even ℓ multipoles has been shown to exist in the CMB angular power spectrum on the largest angular scales (2 < ℓ < 30) Land and Magueijo (2005); Kim and Naselsky (2010b,a, 2011); Gruppuso et al. (2011, 2018); Ade et al. (2014d, 2016f); Akrami et al. (2020b). As odd- ℓ (even- ℓ) spherical harmonics possess odd (even) point-parity, this effect is known as the point-parity anomaly.³⁵

³⁵ Note that this is different from the so-called "mirror-parity anomaly", which is about the properties of the CMB maps under reflection with respect to a plane. Both *Planck* 2013 Ade et al. (2014d) and *Planck* 2015 Ade et al. (2016f) reported evidence for an anti-symmetry plane in low-resolution $N_{side} = 16$ temperature maps with the direction $(l, b) = (264^{\circ}, -17^{\circ})$ and a *p*-value ranging from 1.6% to 2.9% depending on the component separation method. The analysis of the higher-resolution $N_{side} = 32$

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Fig. 24. The $Z_{\ell}(\hat{n})$ -maps, defined individually for the quadrupole ($\ell = 2$) (left) and octopole (l = 3) (right) modes, marks the position of the peaks 1a/1b and 2a/2b along the ring of attraction (white line).

In order to compare even and odd multipoles, Ref. Kim and Naselsky (2010a) considered the parity asymmetry statistic $P \equiv P^+/P^-$, where P^+ and P^- are the mean power in even and odd multipoles respectively for the range $2 < \ell < \ell_{max}$.

$$P^{\pm} = \sum_{2}^{\ell_{\max}} \frac{\left[1 \pm (-1)^{\ell}\right] \ell(\ell+1)C_{\ell}}{4\pi}.$$
(131)

The Λ CDM model predicts $P^+ = P^-$, i.e. P = 1. Examining WMAP3 and WMAP5, Ref. Kim and Naselsky (2010a) found that P < 1 for ℓ_{max} up to ~ 25, with a *p*-value in Λ CDM of $\lesssim 1\%$.

The point-parity anomaly was re-examined in Refs. Aluri and Jain (2012); Hansen et al. (2011); Kim et al. (2012); Gruppuso et al. (2011); Kim and Naselsky (2010b) using the 5-year and 7-year releases of WMAP data. Ref. Aluri and Jain (2012) found that the anomaly extended out at least to $\ell \simeq 100$. Focusing on the power spectrum in the 2 < ℓ < 30 domain, an excess of oddness with significance p = 0.004 was found, which was related to the correlation function at large angular scales Kim et al. (2012). The point-parity anomaly persists in the Planck temperature data Ade et al. (2014d, 2016f); Akrami et al. (2020b); Gruppuso et al. (2018); Shaikh et al. (2019) with the lowest *p*-values of $\sim 0.2\%$ found at $\ell \sim 28$.

Recently, properties of the point-parity asymmetry were investigated directly for SMICA CMB map pixels to identify the preferred directions on the sky responsible for this type of anomaly Creswell and Naselsky (2021a,b). The method proposed in Refs. (Creswell and Naselsky, 2021a,b) is based on the signal symmetry properties at each pixel $\hat{\mathbf{n}}$ and its anti-pode $-\hat{\mathbf{n}}$ with respect to the center of the map: $T(\hat{\mathbf{n}}) = S(\hat{\mathbf{n}}) + A(\hat{\mathbf{n}})$, where the symmetric $(S(\hat{\mathbf{n}}))$ and asymmetric $(A(\hat{\mathbf{n}}))$ parts of the temperature anisotropy map are

$$S(\hat{\mathbf{n}}) = 0.5 \left[T(\hat{\mathbf{n}}) + T(-\hat{\mathbf{n}}) \right],$$
(132)

$$A(\hat{\mathbf{n}}) = 0.5 \left[T(\hat{\mathbf{n}}) - T(-\hat{\mathbf{n}}) \right].$$
(133)

Here $\hat{\mathbf{n}}$ is a unit vector pointed to each pixel of the map. Following Refs. Creswell and Naselsky (2021a,b), one can define the estimator of symmetry or asymmetry of the temperature map for each pixel,

$$Z(\hat{\mathbf{n}}) = T(\hat{\mathbf{n}})T(-\hat{\mathbf{n}}) = S^{2}(\hat{\mathbf{n}}) - A^{2}(\hat{\mathbf{n}}).$$
(134)

Thus, if $Z(\hat{\mathbf{n}}) > 0$, then the symmetric component dominates the asymmetric component, and vice versa. In Fig. 22 we plot $Z(\hat{\mathbf{n}})$ maps derived from the Planck 2018 SMICA map with Gaussian smoothing FWHM = $\Theta = 5^{\circ}$ Creswell and Naselsky (2021a,b). An important feature visible in Fig. 22 is the two pairs of very strong high negative peaks of $Z(\hat{\mathbf{n}})$, labelled by 1a/1b and 2a/2b (a and b of each pair are antipodal from one another), and about ten negative peak-pairs with smaller amplitudes, mainly localized within the area $|b| \leq 30^{\circ}$ in Galactic coordinates. These highest peaks (1a/1b and 2a/2b) with $Z(\hat{\mathbf{n}}) < 0$ belong to the asymmetric component of the signal and have the following Galactic coordinates (*l*, *b*):

$$1a:(212^{\circ},-21^{\circ}), 1b:(32^{\circ},21^{\circ}), (135)$$

$$2a:(332^\circ, -8^\circ), \qquad 2b:(152^\circ, 8^\circ).$$
(136)

Peaks 1a/1b lie outside the area of the Union mask smoothed by a Gaussian filter with FWHM = 5° , while peaks 2a/2b are inside this masked area.

The most powerful negative peaks 1a/1b and 2a/2b are located along the kinematic dipole percolation line, where $T_d(\theta, \phi) = 0$ and θ, ϕ are polar and azimuthal coordinates Creswell and Naselsky (2021a,b). The kinematic dipole is a well-known non-cosmological component of the CMB signal induced due to the motion of the solar system with respect to the rest frame of the CMB radiation. Observations from COBE, *Planck* and WMAP give a direction of the kinematic dipole $T_d(\hat{\mathbf{n}})$ of $(l, b) = (264.00^\circ \pm 0.03^\circ, 48.24^\circ \pm 0.02^\circ)$ (*Planck* 2015 nominal) and $(l, b) = (263.99^{\circ} \pm 0.14^{\circ}, 48.26^{\circ} \pm 0.03^{\circ})$ (WMAP) in the Galactic coordinates (l, b) (Adam et al., 2016; Jarosik et al., 2011). Denoting this direction with the unit vector $\hat{\mathbf{q}}$, we introduce the concept of the ring of attraction (RA) including all directions $\hat{\mathbf{g}}$ such that $\hat{\mathbf{q}} \cdot \hat{\mathbf{g}} = 0$, i.e.

maps showed almost the same direction, $(l, b) = (264^\circ, -16^\circ)$, with lower *p*-values (1.6% to 2.9%). This mirror-parity anomaly was first detected in the WMAP 7-year data Finelli et al. (2012), with an anti-symmetry direction almost identical to the one found by Planck, which is within 40° of the dipole modulation direction.

 $\hat{\mathbf{g}}$ are all unit vectors orthogonal to the direction of the kinematic dipole $\hat{\mathbf{q}}$. Fig. 23 shows that RA includes the directions of not only the 1a/1b and 2a/2b parity peaks but also the CMB dipole modulation used in Refs. Ade et al. (2014d, 2016f); Akrami et al. (2020b) to explain the power asymmetry. Analysis of the random simulations for the multidirectional dipoles shows that the coincidence of the point-parity peaks and the power asymmetry direction shown in Fig. 23 is represented in one of the 2000 realizations.

The presence of RA can also be seen in the Z-maps for the quadrupole and CMB octopole shown in Fig. 24. For the quadrupole, the two highest positive peaks coincide with the position of peaks 2a/2b from Fig. 22, while for the octopole Z-map all peaks 1a/1b, 2a/2b coincide with the position of the deepest negative peaks. Overall, the above results might suggest a causal relationship between kinematic dipole, parity anomaly, CMB spectrum power asymmetry and quadrupole and octopole features, motivating more detailed studies of the systematic and calibration effects of CMB data. It is, however, important to note that while the connection to the CMB dipole direction (or the ecliptic pole) would suggest a possible systematic, there is no known common systematic in WMAP and *Planck*. Similarly, there is no known foreground that could be responsible for a connection to the CMB dipole. Additionally, if the signal is dominated by a systematic or foreground, then this suggests that the underlying cosmological signal is even smaller, exacerbating the lack of large-angle correlations.

8.3.5. Variation in cosmological parameters over the sky

Several attempts have been made to assess whether ACDM parameters are homogeneous and isotropic, as FLRW cosmology assumes. (See, for example, Axelsson et al. (2013); Mukherjee et al. (2016); Mukherjee and Wandelt (2018a); Yeung and Chu (2022); Camacho-Quevedo and Gaztañaga (2021).) Given the statistically significant violations of statistical isotropy described above, one might wonder whether the differences in parameters estimated from different parts of the Universe are consistent with the expected variation in perturbed-FLRW.

A recent analysis Fosalba and Gaztanaga (2020) of the *Planck* legacy temperature maps, considering $\ell > 30$, finds evidence for a violation of statistical isotropy. Three patches of the sky $40^{\circ} - 60^{\circ}$ in angular diameter, over each of which the Λ CDM parameters are approximately homogeneous, exhibit sizable differences between one another. For example, H_0 ranges from 61.3 ± 2.6 to 76.6 ± 5.4 ; $\Omega_c h^2$ ranges from 0.102 ± 0.008 to 0.134 ± 0.008 . This level of variation exceeds that in any of the 300 realizations of Λ CDM to which they compare, though the authors calculate that the discrepancy has a 10^{-9} probability of being a statistical fluctuation in Λ CDM. The authors note that these patches subtend the same angular scale (60°) above which $C^{TT}(\theta)$ is unexpectedly close to zero (see Sec. 8.3.1 above). They are also comparable in size to the patterns of the quadrupole and octopole, which are anomalous (see Sec. 8.3.3).

The authors connect the size of these patches to the size of the anti-trapped surface (causal horizon) due to Λ , $r_{\Lambda} = \sqrt{\Lambda/3}$, placed at the last scattering surface. They suggest that the underlying physical mechanism sourcing the observed temperature anisotropies therefore encompasses scales beyond our causal Universe. The authors argue that these well-defined regions may reflect casually disjoint horizons across the observable Universe. They show that, within each patch, the observed relations between its size and the mean value of the dark-energy density or H_0 are in good agreement with expectations from a recently proposed model of the Universe Gaztañaga (2020, 2021a,b, 2022).

The possible existence of similar horizons in the local Universe could provide a simple explanation for the claimed cosmological parameter tensions between the low and high redshift Universe. Future Surveys such as *Rubin*/LSST, Euclid, and *Roman* will map similar scales at z > 1.

More recently, similar conclusions have been arrived at independently in Ref. Yeung and Chu (2022) by using hemispherical masks and fitting the *Planck* temperature angular power spectrum for 48 directions on the sky. It is found that the directional dependences of the cosmological parameters follow a dipole to good approximation and that the Bayes factor strongly disfavours an isotropic Universe. The reported dipole is roughly perpendicular to the fine structure dipole and within 45° of the directions corresponding to the CMB kinematic dipole, the CMB parity asymmetry dipole, and the axis in QSO polarizations. The Hubble constant varies between $64.4 \pm 1.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $70.1 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$ across the sky.

8.3.6. The cold spot

The cold (blue) spot was first found in WMAP 1-year temperature data by Ref. Vielva et al. (2004) and was confirmed in *Planck* data Ade et al. (2014d, 2016f); Akrami et al. (2020b) in the southern hemisphere at the galactic longitude and latitude $(l, b) = (209^{\circ}, -57^{\circ})$. It is a statistical anomaly of the large-angle fluctuations in the CMB indicating non-Gaussian features. The cold spot is an unusually large region of low temperature with the mean temperature decrease $\Delta T \approx -100 \,\mu$ K and is in disagreement with the prediction of Gaussianity of the standard Λ CDM model Cruz et al. (2005, 2006, 2007). Its significance is 2-4 σ depending on the statistical method applied Zhang and Huterer (2010); Nadathur et al. (2014); Kovács (2018). The inconsistency with Gaussian simulations has a *p*-value of ~ 1% Cruz et al. (2009). The anomalous nature of the cold spot corresponds to a rather cold region with an angular radius in the sky of about 5° - 10° from the centre surrounded by a hot ring Zhang and Huterer (2010); Nadathur et al. (2014); Kovács (2018).

The origin of the cold spot anomaly could be due to the following effects: non-Gaussian feature due to a large statistical fluctuation Vielva et al. (2004), an artifact of inflation Cruz et al. (2005), the foreground contamination Cruz et al. (2006); Hansen et al. (2012), the multiple voids Naidoo et al. (2016), the imprint of a supervoid (about 140 - 200 Mpc radius completely empty void at $z \le 1$) through the ISW effect Inoue and Silk (2006, 2007); Rudnick et al. (2007); Granett et al. (2008a); Kovács et al. (2022); Masina and Notari (2009a,b, 2010), the axis of rotation of the Universe Jaffe et al. (2005), the cosmic texture Cruz et al. (2005); Zhao (2013) and the adiabatic perturbation on the last scattering surface Valkenburg (2012) (see Refs. Cruz et al. (2009); Vielva (2010) for reviews).

8.3.7. Explaining the large-angle anomalies

The apparent connection of certain anomalies to the ecliptic plane (quadrupole-octopole, hemispherical asymmetry) – which certainly has no role in a theory of cosmology – suggests a local origin. However, the large angle anomalies are extremely difficult to ascribe to the usual suspects: experimental systematics and foregrounds.

The systematic effects of both WMAP and *Planck* T measurements are thought to be well in hand at low- ℓ , especially outside the Galactic plane. Moreover the experiments have very different observational strategies and it would be very surprising for them to independently generate the same set of anomalies, especially with such remarkable agreement.

A foreground typically adds a signal with its own correlations to the underlying cosmological signal. It would be challenging for a foreground to suppress angular correlations on large angles, or to reduce the variance in the fluctuations over half the sky. If the peculiar quadrupole and octopole are due to a foreground, then that foreground signal is on top of an even more highly suppressed cosmological quadrupole, and the magnitude of the underlying cosmological angular correlation function is even smaller. Any "cancellation" would itself be a fluke. The spatial structure of the quadrupole and octopole – essentially a ring of extrema perpendicular to the ecliptic plane - make them particularly difficult to explain through foreground. It is not easily mapped into any feature of the solar system, nor of the galaxy. Explanations of quadrupole-octopole alignment that produce aligned Y_{20} and Y_{30} - say from an unusual patch of foreground - are irrelevant. Explanations that are perturbative in some small quantity, ϵ must explain why $C_2 < C_3$, rather than $C_3 \sim \epsilon C_2$.

Microphysical explanations are also challenging. Changes in the inflationary potential will change the power spectrum of fluctuations. but will not induce correlations between $a_{\ell m}$. Similarly, changes in the growth of fluctuations. Changes to the propagation of photons will not correlate $a_{\ell m}$ s, unless it is the underlying propagation physics that itself is modulated, and even then will superpose some new signal on top of the "original" cosmological signal, not a tabula rasa.

An attempt to ascribe the absence of large angle correlations (low $S_{1/2}$) to an absence of long distance correlations – by replacing Fourier modes with wavelets Copi et al. (2019), could suppress $|\mathcal{C}(\theta > 60^{\circ})|$, but not $|\mathcal{C}_{\ell>2}(\theta > 60^{\circ})|$, and so not $S_{1/2}$.

The most promising idea appears to be that the anomalies are induced by horizon-scale or super-horizon-scale properties of cosmic geometry, for example by non-trivial spatial topology. Spatial topology changes the boundary conditions of wave operators. Their eigenspectra are altered, as are their eigenmodes. Specifically, radial functions times individual spherical harmonics are no longer eigenmodes, and so even though the background metric may remain homogeneous and isotropic, statistical isotropy is broken and $\langle a_{\ell m}^{\star}a_{\ell'm'}\rangle \approx \delta_{\ell\ell'}\delta_{mm'}$, as required for any explanation for the anomalies. (Non-FLRW metrics would change the differential operators themselves, and would have similar consequences McEwen et al. (2013).)

A number of preliminary attempts Aurich et al. (2008); Bielewicz and Riazuelo (2009); Aurich and Lustig (2012, 2014); Bernui et al. (2018) have been made to explore the potential for topology to explain the anomalies – with some success in reproducing the quadrupoleoctopole structure Bielewicz and Riazuelo (2009) and low $S_{1/2}$ Aurich et al. (2008), without suppressed C_{ℓ} Bernui et al. (2018). However, the specific topologies considered run afoul of existing limits on topology from the absence of pairs of circles on the CMB sky with matched patterns of fluctuations Cornish et al. (1998, 2004); Shapiro Key et al. (2007); Vaudrevange et al. (2012); Ade et al. (2014f, 2016h) (widely accepted despite the claims in Refs. Aurich et al. (2008); Aurich and Lustig (2014)), and from comparisons to the predicted two-point T correlations of specific topologies (with fixed values of certain free parameters) Aslanyan et al. (2013); Ade et al. (2014f, 2016h). More work to search for topology and explore its potential connection to CMB anomalies is ongoing.

8.3.8. Predictions and future testability

The key to establishing whether the observed large-angle anomalies are statistical flukes or exciting evidence for new physics is to identify testable predictions for properties of the CMB polarization, large scale structure, or other cosmological observables. As discussed above, predictions come in three types: predictions of Λ CDM, conditioned on the existing temperature maps (or on summary statistics of those maps); generic predictions expected of physical explanations, but not tied to a specific model; predictions of specific models to explain specific anomalies. To date, there are no specific models for which such predictions have been made.

We summarize what was written above regarding each anomaly.

8.3.8.1. Λ CDM conditional predictions. Largely because the correlation between temperature and polarization is weak in Λ CDM ($(C_{\ell}^{\text{TE}})^2 \ll$ $C_{\ell}^{\text{TT}}C_{\ell}^{\text{EE}}$, $C_{\ell}^{\text{TB}} = 0 = C_{\ell}^{\text{EB}}$), Λ CDM conditional predictions for polarization are nearly indistinguishable from unconditioned predictions. Similar statements likely hold for predictions for other observables such as large-scale structure, lensing, other secondary CMB anisotropies, 21cm and other intensity fluctuations, and so on. This is actually a useful state of affairs because it allows us to test the fluke hypothesis (that anomalies are statistical accidents in ACDM) by searching for analogous anomalies in these other observables. Which anomalies are most amenable to this approach is perhaps best guided by expectations from the generic predictions expected of physical explanations, but not tied to a specific model (see below).

What can change significantly is predictions for correlations between temperature and other observables, e.g. Ref. Yoho et al. (2014) for the temperature-lensing-potential two-point correlation function $C^{T\phi}(\theta)$. Here one finds that the peak of the distribution of $S_{1/2}^{T\phi}$ in constrained realizations is reduced by a factor of approximately 3 compared to unconstrained realizations. Nevertheless, a value of $S_{1/2}^{T\phi}$ far into the low tail of the PDF for unconstrained realizations will still be in the low tail of the PDF for constrained realizations. Similar analyses should be performed for cross correlations of CMB T with other signals that are sensitive to high redshifts (though still with

 $z \ll z_{\text{recombination}}$).

8.3.8.2. Generic predictions expected of physical explanations. Even in the absence of a specific model, one can put forward certain reasonable expectations of a physical explanation for the anomalies:

- The low value of S^{TT}_{1/2} will result in a low S^{QQ}_{1/2} and S^{UU}_{1/2}. There is a weaker expectation for a suppressed value of S^{ÊÊ}_{1/2} of local-E polarization Yoho et al. (2015), because it is dominated by higher-ℓ modes; there is no clear expectation value of properties of non-local versions of the pseudo-field E.
 The low value of S^{TT}_{1/2} implies Copi et al. (2015a) a low Doppler-subtracted (i.e. intrinsic) dipole C^{TT}₁.
 The homispherical examples in T implies a similar to the properties of the pseudo-field E.
- The hemispherical asymmetry in T implies a similar asymmetry for Q, U, E (local), and perhaps B. This should perhaps best be viewed as a low variance in those quantities in the northern (approximately ecliptic) hemisphere.

8.3.8.3. Generic predictions expected of specific models. Specific choices of topology have been argued to potentially explain low $S_{1/2}$ or quadrupole-octopole correlations. However, these specific topologies appear to violate known limits. Some physical models that seek to explain the apparent violation of statistical isotropy observed in T, may also predict independent statistical isotropy violation in polarization of the CMB (i.e. that is not a direct consequence of the observed temperature sky), which could be detected in future polarization data Mukherjee (2015); Mukherjee and Souradeep (2016); Cayuso and Johnson (2020).

8.3.8.4. Future tests. We have identified three specific tests of the fluke hypothesis that are also motivated by expectations for explanations through new physics:

- Measurement of $S_{1/2}^{QQ}$ and $S_{1/2}^{UU}$, as well as $S_{1/2}^{\hat{E}\hat{E}}$ and $S_{1/2}^{\hat{B}\hat{B}}$ Yoho et al. (2015). This would require improvements on *Planck* for large-angle correlations in polarization through an all-sky experiment.
- Measurement of the cosmological contribution to C_1^{TT} , by subtraction of the Doppler contribution to C_1^{TT} . This requires sub-percentaccuracy determination of our velocity relative to the CMB rest frame from mixing between high- ℓ multipoles, enabling the Doppler contribution to C_1 to be subtracted from a similarly accurate direct measurement of C_1 . This would require improvements on *Planck* for high ℓ .
- Measurement of the variance in Q, U, and \hat{E} in the northern hemisphere O'Dwyer et al. (2017); Abazajian et al. (2016). This would require improvements on *Planck* for large-angle correlations in polarization over a large fraction of the north-ecliptic hemisphere, as well as an improved independent determination of the optical depth to reionization τ O'Dwyer et al. (2019).

8.3.9. Summary

There are multiple anomalies on large angular scales in the CMB temperature maps. Each is of $< 5\sigma$ significance, each is characterized with *a* posteriori statistics, but several sets of anomalies are statistically independent (or nearly so) in standard Λ CDM. Collectively they are very troubling. They are common to WMAP and *Planck* (and COBE), so difficult to explain by unaccounted-for observational systematics. They are unexplained by known foregrounds, and a foreground explanation would itself imply an (even more) highly suppressed large-angle cosmological signal.

For several anomalies, one anticipates that a physical explanation would imply an analogous anomaly in the scalar (E-mode) contributions to Q and U polarization, and perhaps in the tensor (B-mode) contribution as well. Similar statements may be applied to other probes of the large-scale Universe – e.g., intensity maps, surveys of large scale structure – but the expectation is weaker. Meanwhile, Λ CDM predictions for polarization (and late-time observables) are nearly unchanged by conditioning on the observed temperature maps, therefore only cross-correlations with temperature are significantly altered.

Large-angle properties of the CMB should be a matter of continued attention for the experimental and theoretical cosmology communities. Conditional predictions in Λ CDM, provide accessible null tests of Λ CDM through improved measurements of polarization on large angular scales, of improved determination of our velocity relative to the CMB, and possibly through large angle/distance auto and cross correlations between observables including those probing moderate redshift. The existence of reasonable expectations for physical models, suggest opportunities to provide compelling evidence for fundamentally important new physics. Non-trivial cosmic topology or anisotropic geometry are the only current promising frameworks for a comprehensive explanation; these should be more thoroughly explored.

8.4. Abnormal oscillations of best fit parameter values

Signature of an oscillation, or unusual behaviour of the data around the best fit Λ CDM model have been reported in Refs. Riess et al. (2018c); Colgáin (2019); Camarena and Marra (2020a); Kazantzidis and Perivolaropoulos (2020); Sapone et al. (2021); Dainotti et al. (2021a). These signatures were mainly found using the binned Pantheon data. However, assigning significance to such oscillations in the data in the residual space around a best fit model requires a large number of simulations. One should note that different realizations of a data based on the same covariance matrix given a specific model would differ from each other and in some particular realizations we might see some specific features. Hence to assign a reliable statistical significance to any specific feature beyond expectations of a given model or hypothesis, we need to generate a large number of Monte Carlo simulations and see how often we might observe such or similar features. We should also consider a "look elsewhere effect" that features due to random fluctuations might occur at different parts of the data and not necessarily at a specific range of the data. Following this approach, Ref. Kazantzidis et al. (2021) generated 1000 realizations of the Pantheon supernovae data and evaluated how likely it is to observe the oscillations we see in the Pantheon real data around the best fit Λ CDM model. Considering the full covariance matrix of the data taking into account both systematic and statistical uncertainties, they did show that at the redshifts below $z \simeq 0.5$ such oscillations can only occur in less than 5% of the simulations. While statistical fluctuations can be responsible for this oscillation, this could also be a hint for some feature beyond the expectations of the standard model. Alternatively this could be a hint for some specific systematics in the data. More observations would make it soon clear if the observed effect is due to statistical fluctuations or there is some real physics or systematics behind such apparent behaviour

8.5. Anomalously strong ISW effect

The decay of cosmological large-scale gravitational potential Ψ causes the integrated Sachs-Wolfe (ISW) effect Sachs and Wolfe (1967) which imprints tiny secondary anisotropies to the primary fluctuations of the CMB and is a complementary probe of dark energy, e.g. Ref. Fosalba and Gaztañaga (2004). Using a stacking technique Marcos-Caballero et al. (2016); Ade et al. (2016f) in the CMB data, an anomalously strong integrated Sachs-Wolfe (ISW) signal has been identified for supervoids and superclusters on scales larger than $100h^{-1}Mpc$ at a $\sim 3\sigma$ level Granett et al. (2008a,b). This stronger than expected within standard Λ CDM signal of the ISW effect first emphasized in Ref. Hunt and Sarkar (2010) has been studied by Refs. Nadathur et al. (2012); Flender et al. (2013); Ilic et al. (2013); Cai et al. (2017a); Kovács (2018); Kovács et al. (2019); Dong et al. (2020).

In particular, the analysis by Ref. Kovács et al. (2019) for DES data alone found an excess ISW imprinted profile with $A_{ISW} \equiv \Delta T^{\text{data}}/\Delta T^{\text{theory}} \approx 4.1 \pm 2.0$ amplitude (where the value $A_{ISW} = 1$ corresponds to the Λ CDM prediction). A combination with independent BOSS data leads to $A_{ISW} = 5.2 \pm 1.6$, in tension at 2.6σ with the predictions from Λ CDM cosmology. The average expansion rate approximation (AvERA) inhomogeneous cosmological simulation Rácz et al. (2017) indicates under the inhomogeneity assumption, about $\sim 2-5$ times higher ISW effect than Λ CDM depending on the *l* index of the spherical power spectrum Beck et al. (2018a). Thus the large

scale spatial inhomogeneities may be the plausible sources of this ISW excess signal. Using angular cross-correlation techniques Ref. Giannantonio et al. (2012a) combines several tracer catalogues to find $A_{\rm ISW} \approx 1.38 \pm 0.32$. In addition the early Integrated Sachs-Wolfe (eISW) effect Bowen et al. (2002); Galli et al. (2010) (30 < z < 1100) has been studied by Refs. Hou et al. (2013); Cabass et al. (2015); Kable et al. (2020); Vagnozzi (2021) and constraints were imposed on the corresponding parameter $A_{\rm eISW}$. In general, the reported $A_{\rm ISW}$ amplitude varies in the literature depending on the dataset and the assumptions of the analysis. Further investigation of this issue is needed.

8.6. Cosmic dipoles

There have been claims of signals indicating the violation of the cosmological principle. Some of these signals coherently point to the CMB dipole direction, which is *assumed* to be of purely kinematic origin. Some of the dipoles have different directional dependence, and for these observations, there is no obvious pattern. A physical mechanism for producing such violation on Hubble scales is studied in Ref. Sanchez and Perivolaropoulos (2011). See also Sec. 7.8.2 for an introduction to the mapping of anisotropies in cosmological observables in general space-times without exact symmetries. The dipolar signals found include the following:

8.6.1. The α dipole

8.6.1.1. Measuring α from quasar spectra. High resolution spectra of distant quasars reveal numerous narrow absorption lines due to gaseous components of galaxies intersecting the Earth–quasar line of sight. The large number of atomic species and transitions detected allow precise measurements of the fine structure constant $\alpha_{SI} = e^2/(4\pi\epsilon_0\hbar c)$ over cosmological distances, where *e* is the electron charge, ϵ_0 the vacuum permittivity, \hbar the reduced *Planck* constant, and *c* the speed of light. The dimensionless α is the ratio of the speed of an electron in the lowest energy orbit of the Bohr-Sommerfeld atom to the speed of light, and hence connects quantum mechanics (through \hbar) with electromagnetism (through the remaining constants in the ratio).

The 1999 invention of the Many Multiplet method (MM) Dzuba et al. (1999) provided an instant order of magnitude precision gain over previous methods in searches for space-time variations of α . This is because the difference between ground-state and/or excited state relativistic corrections can be large; s-p and s-d transitions for example may even be of the opposite sign. The MM method can thus produce sensitive results when applied simultaneously to multiplets of the same atomic species, or to species having widely differing atomic masses. Any real change in α therefore generates a unique pattern of observed wavelength shifts that is not degenerate with a simple redshift.

In parallel with the development of the MM method, its first application to high-resolution quasar spectra from the HIRES spectrograph on the Keck telescope was reported in Ref. Webb et al. (1999) and suggested a possible variation. The acquisition of several further quasar samples, initially from the Keck telescope Webb et al. (2001, 2003); Murphy (2002); Murphy et al. (2003a), also suggested variations and led ultimately to the extensive study carried out using the UVES spectrograph on the VLT, reported in Refs. Webb et al. (2011); King (2010); King et al. (2012). The combined Keck and VLT samples comprised 293 independent measurements of the fractional change $\Delta \alpha / \alpha = (\alpha_z - \alpha_0)/\alpha_0$, where α_z is the value of the fine structure observed in a gas cloud at redshift *z* and α_0 is the terrestrial value. These 293 measurements cover both hemispheres and span a redshift range of $0.2 < z_{abs} < 3.6$, permitting a search for temporal and spatial variations of α .

The main outcome of the detailed 2011 study by King, Webb, and collaborators is the intriguing hint of a spatial variation of the electromagnetic force, consistent with an angular dipole model pointing in the direction $RA = 17.3 \pm 1.0h$, $dec = -61^{\circ} \pm 10^{\circ}$, with amplitude $0.97^{+0.22}_{-0.20} \times 10^{-5}$. A bootstrap analysis showed a dipole model was preferred over a simple monopole model at the 4.1σ level. The apparent dipole was captivating for several reasons: first, measurements made at lower redshift use a different set of atomic transitions to those at higher redshift, yet both measurements independently support a dipole. Second, the independent Keck and VLT samples both suggest a dipole effect, again along the same direction and with consistent dipole amplitudes. Despite these apparent coincidences, it should be noted that measurement uncertainties for subsets of the whole sample are large and not individually significant. A reasonable statistical significance is only seen when the whole sample is modelled simultaneously.

Ref. Berengut et al. (2011b) made use of the 2011 King *et al* data to further examine the properties of the dipole model and to explore the possibility of detecting dipoles in measurements of variation in electron-to-proton mass ratio $\mu = m_e/m_p$, combinations of fundamental constants such as $x = \alpha^2 \mu g_p$ (where g_p is the proton g-factor), and big bang nucleosynthesis probes of the baryonic density parameter Ω_b using measurements of the primordial deuterium abundance, D/H. Since the number of μ , x, and D/H measurements has increased only slightly, little has been done on those dipole studies since the analysis in Ref. Berengut et al. (2011b).

Detailed studies have also been done to check whether α may change in strong gravitational fields Berengut et al. (2013); Bainbridge et al. (2017a,b); Hu et al. (2020). For some white dwarfs, where physical conditions permit, many narrow photospheric absorption lines are detected. The large number of Fev and Niv transitions are particularly useful since they have a broad range of sensitivities to α , so that (as with quasar measurements) any change in α does not emulate redshift. At present, the most detailed analysis to date gives a best result of $\Delta \alpha / \alpha = (6.36 \pm 0.35 \text{ (stat)} \pm 1.84 \text{ (sys)}) \times 10^{-5}$, so there is no clear evidence for a change in α . Although the quality of the astronomical data is high (indicated by σ_{stat}), results are currently severely constrained by the precision of laboratory wavelengths used to compare with the detected lines, the dominant part of σ_{sys} Hu et al. (2020). Significant improvements in the laboratory wavelength measurements are needed to make further progress.

8.6.1.2. Overcoming the systematics. An early list of potential systematic effects associated with $\Delta \alpha / \alpha$ measurements is given in Ref. Murphy et al. (2001, 2003b) although the subject has moved on since that time. We now have a considerably better understanding of systematics and new mathematical/statistical tools have been developed to identify and quantify them. An exhaustive discussion of systematics is not appropriate here so instead a precis of four important effects is given. The first two are essentially solved problems (but exist in previously published surveys) whilst the second two are not yet solved.

Non-uniqueness in absorption system modelling: It has long been recognised that a complex quasar absorption system can be modelled in essentially an infinite number of ways. However, interactive model fitting is a laborious process such that it is impractical to construct more than a single model for an absorption system in most cases. To constrain model options to some extent, a common approach is to

gradually increase the number of model parameters until the model matches the data with a normalised χ^2 of around unity. Although the χ^2 method is reasonable and has been widely used, it is not the best approach, so Ref. King et al. (2012) employed an *information criterion* (IC) to optimise the number of model components. Whilst using an IC strikes a balance between fitting too few and too many parameters, different humans modelling the same data will usually derive slightly different models, each with a slightly different value of $\Delta \alpha / \alpha$. From the point of view of understanding systematics, the important question then becomes, how different? This "non-uniqueness" problem has very recently been solved. A new "Artificial Intelligence" approach was introduced that completely removes human decision making (and time commitment) from the modelling process Lee et al. (2021a). This enables a Monte Carlo approach to modelling, emulating multiple interactive modellers. Computations are intensive but manageable using high performance computers. In conjunction with those advances, a new spectroscopic IC has been developed specific to spectroscopy, that appears to improve on previous statistics Webb et al. (2021b). The three developments just described enable us to quantify, for the first time, the effect of non-uniqueness on $\Delta \alpha / \alpha$ measurement uncertainty Lee et al. (2021b). To summarise, the issue of model non-uniqueness is now a solved problem, *provided that* Al Monte Carlo (or something equivalent) is used to derive a sample of models for each absorption system being measured.

Wavelength calibration problems: Ref. Molaro et al. (2008) first searched for wavelength distortions in high-resolution echelle spectra by correlating the reflected solar spectrum from VLT/UVES asteroid observations with absolute solar calibrations but found no evidence for long-range wavelength distortion. Subsequently, Ref. Rahmani et al. (2013) applied the same technique and indeed found that long-range wavelength distortions do occur in UVES spectra. The form of the distortion appears to be reasonably well approximated by a simple linear function of velocity shift versus observed wavelength. Ref. Whitmore and Murphy (2015) examined the problem in further detail confirming problem. They then attempted to estimate the impact of this distortion effect on possible α dipole but did not take into account the considerably more complex distortion that would apply to a quasar spectrum form the co-addition of multiple exposures at the telescope, some or all having different instrumental settings. That problem was resolved in Refs. Dumont and Webb (2017); Webb et al. (2021a), such that any possible long-range distortion VLT/UVES and Keck/HIRES spectra can be allowed for, as discussed in detail in Ref. Lee et al. (2021b); future α measurements made using archival UVES and HIRES spectra should in principle be unbiased and the total error budget realistic.

Considerable effort has gone into wavelength calibration of the new ESPRESSO spectrograph (*Echelle SPectrograph for Rocky Exoplanets and Stable Spectroscopic Observations*) on the VLT Milaković (2020); Milaković et al. (2020); Probst et al. (2020). In particular, laser frequency combs (LFCs) and Fabry-Pérot devices produce ESPRESSO calibrations down to an accuracy of 24 m/s Schmidt et al. (2021). In principle the accuracy should be somewhat better than this value (and indeed 1 limit of 1-2 m/s has been reached for the High Accuracy Radial Velocity Planet Searcher (HARPS) instrument). Further work is anticipated. A limiting value of 24 m/s corresponds to an uncertainty of $\sim 10^{-6}$ on $\Delta \alpha / \alpha$.

Magnesium isotopes: The Mg II 2796/2803 Å doublet is often strong in quasar absorption systems and is relatively insensitive to α variation. For these reasons, it was introduced as an "anchor" against which to measure relative shifts of more sensitive species such as Fe II Webb et al. (1999). However, the low atomic mass of Mg means isotopic and hyperfine separations are non-negligible in the context of varying α measurements. Therefore, if we fit high redshift absorption lines using models that assume terrestrial isotopic abundances, and if relative isotopic abundances in quasar absorbers are not terrestrial, this may mimic a change in α , as first pointed out in Ref. Webb et al. (1999). Further discussions on this systematic are given in Refs. Murphy et al. (2001, 2003b); Kozlov et al. (2004); Ashenfelter et al. (2004); Fenner et al. (2005); Agafonova et al. (2011); Berengut et al. (2011a); Webb et al. (2014); Vangioni and Olive (2019). This is an unsolved problem in the sense that the Mg relative isotopic abundances at high redshift are not yet well-determined, nor whether they may vary significantly from one quasar absorber to another. Despite that, this systematic is straightforward to quantify simply by treating the Mg isotopic abundances as unknown variables to be solved for in conjunction with modelling for α (the obvious penalty being a slightly weaker constraint on $\Delta \alpha / \alpha$). Of course, Mg is not the only element with this potential problem although it is perhaps the most important in the context of α measurements.

Instrumental profile: It is known that the intrinsic instrumental profile (IP) of the ESPRESSO instrument varies as a function of detector position and wavelength Milaković (2020); Milaković et al. (2020). Since Voigt profile models must be convolved with the IP during the modelling process, it is imperative to have an accurate model of the IP. This problem has not yet been fully solved although numerical and analytic approximations have been made and help. A detailed study for HARPS Zhao et al. (2021) has been carried out but not yet for ESPRESSO.

8.6.1.3. *Current status of the* α *dipole.* IR spectroscopy of very high redshift quasars allow us to extend the cosmological volume of the 2011 α measurements described above. At the time of writing, only one quasar spectrum obtained using the X-SHOOTER spectrograph on the VLT has been analysed, the *z* = 7.085 quasar J1120+0641 Wilczynska et al. (2020). The achievable spectral resolution is at present $\sim 1/4$ that of e.g. UVES/VLT and $\sim 1/10$ that of ESPRESSO/VLT. Whilst the X-SHOOTER $\Delta \alpha / \alpha$ error bars are substantially larger than the higher resolution HIRES/Keck or UVES/VLT data, at the high redshift end, these IR data are the best presently available and contribute 4 new measurements, increasing the sample size very little but significantly augmenting the redshift range to 5.5 < z_{abs} < 7.1.

Further contributions come from measurements by Molaro and collaborators using UVES on the VLT. The Molaro team concentrated efforts on a small number of high signal to noise spectra, in order to reduce the $\Delta \alpha / \alpha$ statistical uncertainty. That sample of 21 measurements has been published in 10 papers and is summarised, with citations, in Table 1 of Ref. Martins and Pinho (2017). Additionally, another UVES/VLT sample of measurements are reported in Ref. Wilczynska et al. (2015), forming a combined total set of 323 measurements. As reported in Ref. Wilczynska et al. (2020), these additional measurements allow us to update the spatial dipole parameters: the updated dipole amplitude is $A = 0.72 \pm 0.16 \times = 10^{-5}$ and the dipole sky location is right ascension 16.76 ± 1.17 hours and declination $-63.79^{\circ} \pm 10.30^{\circ}$. For that analysis, a dipole is preferred over a simpler monopole model at the 3.9σ level. On the other hand, an independent analysis of essentially the same dataset as in Ref. Martins and Pinho (2017), using a different type of analysis (likelihood with marginalisation over certain parameters), arrives at a lower dipole significance level of 2.3σ . Given the similarity between the samples used by both groups, the origin of the difference between these significance levels is unclear. However, the error budget in a recent dipole estimate Wilczynska et al. (2020) incorporates, in addition to the standard statistical uncertainty, an allowance for an "unknown"



Fig. 25. Putative directions of anisotropy in the Universe in the galactic (1, b) coordinates with the galactic centre in the middle (grey ellipse). Directions from the literature are shown with different markers (if either no uncertainties were reported or the uncertainties are far too small to be seen) or ellipses (with the circle in the middle being the mean coordinates and the size of the ellipses corresponding to their 1σ uncertainties) with text labels. The corresponding anti-directions ($l' = l + 180^\circ$, b' = -b) are shown with the same ellipse/marker without the text label. The following directions are shown: CMB kinematic dipole (cross); CMB octopole (star); CMB quadrupole (square); CMB hemispherical power asymmetry directions based on WMAP (blue triangles) and Planck (black triangles) data and measured with the dipole modulation (left-pointing), power asymmetry (right-pointing), and variance asymmetry (down-pointing) methods; the Great Attractor (black rhombus with no anti-direction shown); dark flow direction (blue ellipse); SNe Ia dipole (green ellipse); fine-structure constant dipole (red ellipse); CMB maximum temperature asymmetry axis (red ellipse); high energy cosmic ray dipole (cyan ellipse); the Cold Spot (purple ellipse with no anti-direction shown). Figure taken, with permission, from Evgeny Zavarygin's PhD thesis, 2020.

systematic σ_{rand} (as described in section 3.5.3 of Ref. King et al. (2012)) and an additional uncertainty associated with possible long range distortion (even though none was found). The error estimate in Ref. Wilczynska et al. (2020) is thus cautious, we are aware of no reason to think it unreliable, and suggest that measurement is the most reasonable. Whether a dipole will persist in new and forthcoming ESPRESSO/VLT spectra remains to be seen. Data is now beginning to accumulate in the ESO archive and new measurements using that higher quality data are underway.

The purpose of explaining at least some of the systematics associated with varying α measurements above was to highlight the importance of fully resolving those issues in order to facilitate rigorous tests of α variation, be they spatial or temporal. The tentative α dipole cannot be meaningfully tested until these issues are dealt with. Concerted efforts have been made, notably the development of AI-VPFIT, the new information criterion SpIC, detailed studies about model non-uniqueness, as well as extensive investigations into wavelength calibration, explicitly to be able to move ahead with stringent tests of α variation. A complete re-analysis of virtually all existing quasar absorption α measurements will soon be completed, together with new measurements from ESPRESSO. Finally, a number of possible anisotropic effects from a broad range of observations have been reported in the literature and are illustrated in the all-sky plot shown in Fig. 25.

8.6.1.4. Theoretical context. Theoretical models incorporating either temporal or spatial variations of fundamental constants require physics beyond General Relativity and hence beyond the standard FLRW cosmological model. Given the broad landscape of possible varying constant theories, the association between variations and the cosmological tensions reported extensively in this article is, as yet, undetermined. A generalised theory of varying α (Barrow and Lip, 2012) has been developed in which electromagnetism varies with the chamelionic scalar field potential ϕ via a variable coupling constant $\omega(\phi)$, the latter being constrained by quasar absorption observations. This theory extends the Bekenstein and Sandvik BSBM theory (Sandvik et al., 2002; Magueijo et al., 2002) in which the observationally constrained coupling parameter does not depend on ϕ . A further BSBM extension shows that if the kinetic energy in the scalar field drives the acceleration of the expansion, α need not asymptote to a constant value at the present epoch (Graham, 2015). If so, this motivates further precision increases in laboratory experiments to measure the time dependence of α (Leefer et al., 2013). Various kinds of spatial variations in physics (i.e. not just fundamental constants) have been explored. For example Audren et al. (2015) examine a quantum gravity scenario in which a preferred time-direction occurs at each point in space-time, parameterised by a vector field coupled to dark matter. The same model could also explain spatial variations in fundamental constants. Interesting coincidences between different types of possible anisotropic phenomena have been pointed out in Mariano and Perivolaropoulos (2012) (also see Fig. 25 for a compilation of various claimed dipole effects). C. Martins and colleagues have explored a range of theoretical ideas showing how constraints on temporal or spatial variation of the fine structure constant provides important new requirements for dark energy models. Recent discussions from that group are given in Leite et al. (2017) and in Martins (2017).

There are also interesting ideas about extreme fine tuning of quantum corrections in theories with variation of α by O'-Donoghue Donoghue (2003) and Marsh Marsh (2017). Self-consistent theories of gravity and electromagnetism, incorporating the fine structure constant as a self-gravitating scalar field, with self-consistent dynamics that couple to the geometry of spacetime, have been formulated in Refs. Bekenstein (1982); Damour and Polyakov (1994); Sandvik et al. (2002); Barrow and Li (2008); Barrow and Lip (2012); Barrow and Graham (2013); Barrow and Magueijo (2014), with extended to the Weinberg-Salam theory in Refs. Kimberly and Magueijo (2004); Shaw and Barrow (2005). They generalise Maxwell's equations and general relativity in analogy to the way that Jordan-Brans-Dicke gravity theory Jordan (1937); Brans and Dicke (1961b) extends general relativity to include space or time variations of the Newtonian gravitational constant, *G*, by upgrading it to become a scalar field. This enables different constraints on a changing α at different redshifts to be coordinated; it supersedes the traditional approach Dyson (1972) to constraining varying α by simply allowing α to become a variable in the physical laws for constant α . Further discussions relating spatial variations of α to inhomogeneous cosmological models can be found in Dabrowski et al. (2016); Balcerzak et al. (2017).

Direct measurements of α are also important for testing dynamical dark energy models, since they help to constrain the dynamics of the underlying scalar field Martins and Pinho (2017) and thus dynamics can be constrained (through α) even at epochs where dark energy is still not dominating the universe. Indeed, the possibility of doing these measurements deep into the matter era is particularly useful, since most other cosmological datasets (coming from type Ia supernovas, galaxy clustering, etc) are limited to lower redshifts. Recent reviews of the range of theoretical models so far explored are given in Solà (2015b) and in the comprehensive article by Uzan (2011). Such a broad theoretical landscape necessarily results in a correspondingly broad range of expectations, all with important implications, but few with tight quantitative predictions. In the absence of a first-principles fundamental theory, high precision experiments and observations are the only way forward if we wish to elucidate the true nature of the world.

8.6.2. Galaxy cluster anisotropies and anomalous bulk flows

8.6.2.1. Scaling relations in galaxy clusters. It has been observed that scaling relations in galaxy clusters (see Ref. Kaiser (1986)) at redshifts $z \leq 0.3$ detect anisotropies at high statistical significance (> 4 σ) in the direction of the CMB dipole Migkas and Reiprich (2018); Migkas et al. (2020, 2021). In particular, Refs. Migkas and Reiprich (2018); Migkas et al. (2020) studied the isotropy of the X-ray luminosity-temperature ($L_X - T$) relation and detected a ~ 4.5 σ anisotropy in a direction consistent with the CMB dipole. The observation was subsequently extended to a suite of scaling relations, and by combining all available information, the authors reported an anisotropy and apparent 10% spatial variation in the local H_0 in the direction (l, b) ~ ($280^{+35}_{-35}, -15^{+20}_{-20}$) deg and the rest of the sky Migkas et al. (2021).³⁶ Given the robustness of the observation across scaling relations, unaccounted X-ray absorption can be discounted as an explanation, leaving i) bulk flows or ii) Hubble expansion anisotropies as potential explanations Migkas et al. (2020).

The first possibility is consistent with previous results in the literature, where anomalously large bulk flows exceeding the expectations of Λ CDM have been observed Lauer and Postman (1994); Hudson et al. (2004); Kashlinsky et al. (2009, 2010); Atrio-Barandela et al. (2015); Howlett et al. (2022), but in contrast to Refs. Migkas et al. (2020, 2021), at smaller scales. Note that such large bulk flows have been questioned in the literature Osborne et al. (2011); Ade et al. (2014g), but such a motion, if confirmed, would require a major revision of large scale structure formation models. In tandem, anomalous bulk flows have been studied in SNIa, but the results are also contested Colin et al. (2011); Dai et al. (2011); Turnbull et al. (2012); Wiltshire et al. (2013); Appleby et al. (2015). The second possibility is an anisotropy in the Hubble expansion and this would necessitate a 10% difference in H_0 between the anisotropy direction and the rest of the sky. Here, one trades the normalization in the scaling relation with the Hubble constant H_0 on the assumption of a fixed matter density Ω_m consistent with *Planck* (see also related Secs. 8.6.3, 8.6.4, 8.6.5, and 8.6.6). Theoretically, attempts have been made to explain such low redshift effects through differences in the deceleration parameter in a "tilted Universe" model Tsagas and Kadiltzoglou (2015); Asvesta et al. (2022).

8.6.2.2. Large scale bulk flows. The bulk flow on the scale of ~ 100Mpc is an important probe of the local Universe that can be compared to predictions from the Λ CDM model. In particular, the scale of ~ 100Mpc is large enough that the expectation for the bulk flow is sufficiently small, while being small enough that it is possible to estimate with some accuracy using peculiar velocity data, whose errors increase rapidly with distance. While some studies (for example Turnbull et al. (2012); Hoffman et al. (2015); Qin et al. (2019b)) have found results consistent with Λ CDM, others have found flows that are larger than expected Watkins et al. (2009); Feldman et al. (2010); Peery et al. (2018), with only ~ 2% chance of obtaining a bulk flow that is as large or larger. However, in comparing these studies it is important to keep in mind that they each probe the local velocity field in ways that emphasize different scales, and hence are not in fact comparable. Some progress has been made in developing an analysis method that estimates the bulk flow defined intuitively as the average velocity in a sphere with a fixed radius Peery et al. (2018). The bulk flow estimated in this way is be comparable between studies and data sets. Bulk flow estimates made using this method are also independent of the value of H_0 , thus decoupling the bulk flow from the uncertainty in its value. With a large quantity of new peculiar velocity data on the horizon, we should soon be able to determine more precisely if there is tension between the bulk flow on these scales and the standard model.

8.6.3. Radio galaxy cosmic dipole

There are two preferred frames in cosmology, based on the CMB and on the large-scale structure, and defined by the vanishing of the dipole in temperature or in number counts. This is a physical definition, independent of coordinates and space-time metric. The Cosmological Principle assumes that space-time is isotropic and homogeneous on large enough scales. It therefore requires that the CMB and matter frames must coincide – otherwise, there will be a violation of large-scale isotropy.

This key test of the Cosmological Principle was proposed by Ellis and Baldwin in 1984 Ellis and Baldwin (1984), who presented an expression for the dipole in radio galaxy number counts projected on the sky. Their proposal was later applied to the data from the NVSS and other radio galaxy surveys (see Refs. Bengaly et al. (2019); Siewert et al. (2021) and references cited therein). The striking point about these results, which cover a significant range of radio frequencies, is that they all find consistency of the radio dipole direction with that of the CMB – but all of them also find that the velocity implied by the radio dipole is significantly higher than the velocity derived from the CMB dipole. A recent analysis of the eBOSS quasar sample in the infrared produced qualitatively similar results Secrest et al. (2021), reporting a 4.9σ disagreement in velocities.

The CMB defines the rest frame of the Universe because we have subtracted the CMB dipole on the assumption that it is purely kinematic, i.e. an effect due to relative motion. Note, given any dipole, one always has the freedom to choose a rest frame. Nevertheless, as a consequence of this choice, the sun is travelling at a precise velocity of $v = (369.8 \pm 0.1)$ km/s in the direction (RA, DEC) = $(167.94 \pm 0.01, -6.944 \pm 0.005)$ deg in equatorial coordinates (J2000) or $(l, b) = (264.02 \pm 0.01, 48.25 \pm 0.005)$ deg in galactic coordinates Aghanim

³⁶ Note that the analysis fixes Ω_m to a *Planck* value and finds that H_0 is *lower* in the CMB dipole direction. This can be contrasted with Refs. Krishnan et al. (2021b, 2022); Luongo et al. (2021) where both H_0 and Ω_m are treated as free parameters and H_0 is *higher* in the CMB dipole direction.

et al. (2020a), with respect to the "CMB frame". This inference can and should be tested, especially since significant ACDM tensions exist. Following the proposal of Ellis and Baldwin Ellis and Baldwin (1984), attempts have been made to check that we recover the same proper motion from counts of radio galaxies Blake and Wall (2002); Singal (2011); Gibelyou and Huterer (2012); Rubart and Schwarz (2013); Tiwari and Nusser (2016); Colin et al. (2017); Bengaly et al. (2018); Siewert et al. (2021). Tellingly, across a number of radio galaxy catalogues, TGSS-ADR1 Interna et al. (2017), WENSS Rengelink et al. (1997), SUMSS Mauch et al. (2003) and NVSS Condon et al. (1998), the analysis returns a dipole that exceeds the CMB expectation in magnitude, but agrees in direction. For example, for the combined NVSS and SUMSS sources, Ref. Colin et al. (2017) infers our proper motion to be $v = (1729 \pm 187)$ km/s in the direction (RA, DEC) = (149 ± 2, -17 ± 12) deg. Interestingly, some frequency dependence with the radio dipole magnitude has been reported Siewert et al. (2021) (see also Ref. Bengaly et al. (2018)), which seems unlikely to be purely kinematic in origin, so it is imperative to tease apart any intrinsic clustering dipole from a kinematic dipole. One possible explanation for the discrepancy is a local (spherical) void with the observer sitting at the edge, e.g. Ref. Paczynski and Piran (1990). This has been investigated Rubart et al. (2014), but a single void model cannot give a sufficient contribution to the dipole to account for any mismatch. An interesting relevant "Ellipsoidal Universe" model was originally proposed to address the low quadrupole amplitude in the CMB Campanelli et al. (2006), but it may also provide an explanation for H_0 and S_8 tensions Cea (2022).

Are we seeing the emergence of another "tension" in the standard model of cosmology? Is there an anomalously large bulk flow in the Universe, possibly generated by a super-Hubble primordial isocurvature mode (see e.g. Ref. Tiwari et al. (2022))? There are intriguing possibilities to explain the apparent anomaly. However, the dipole in the matter is considerably more complex than the one in the CMB. It is sensitive to nonlinearities at low z (e.g. Ref. Bengaly et al. (2019)) and to astrophysical properties of the tracer being used Maartens et al. (2018); Nadolny et al. (2021). It is also noteworthy that a recent determination of the dipole in the Pantheon SNIa sample, while finding agreement in direction with the CMB, also found that the velocity implied by the SNIa is *lower* than that from the CMB Horstmann et al. (2021).

The dipole formula presented by Ellis and Baldwin Ellis and Baldwin (1984) was based on a simplified assumption of no evolution in the source population properties. Since these are averaged over all redshifts, one might think that the assumption is reasonable. The redshift dependence of the kinematic dipole in galaxy (and 21 cm intensity mapping surveys) involves cosmic evolution, magnification bias and source population evolution, as shown in Ref. Maartens et al. (2018). This has recently been applied by Ref. Dalang and Bonvin (2021) to re-derive the radio galaxy dipole without the standard assumption of no-evolution. They find that it is certainly possible in principle for evolution to remove the tension between the matter and CMB velocities. Further work is needed, but this important result shows that it would be premature to conclude that there is a violation of large-scale isotropy.

8.6.4. QSO cosmic dipole and polarisation alignments

Recently, the Ellis and Baldwin test Ellis and Baldwin (1984) was repeated with 1.36 million QSOs from the CatWISE2020 catalogue Eisenhardt et al. (2020). Using mid-infrared data from the Wide-field Infrared Survey Explorer (WISE) Wright et al. (2010) the authors of Ref. Secrest et al. (2021) created reliable AGN/QSO catalogs and a custom QSO sample. It was shown that there is a statistically significant dipole in the counts of distant QSOs with direction (l, b) = (238.2, 28.8) deg (galactic coordinates), which is 27.8 deg away from the direction of the CMB dipole, or within 2σ . However, the dipole amplitude was found to be D = 0.01554, or ~ 2 times larger than the value inferred from CMB, with a statistical significance at the 4.9σ level (or with a p-value of 5×10^{-7}) for a (single-sided) normal distribution. Taken at face value, this is a serious discrepancy, which is on par with H_0 tension, but is to all extent *cosmological model independent*. It should be stressed that this new analysis leads to results consistent with earlier excesses from radio galaxies, but helps to address some systematic concerns. First, since WISE is a satellite, the observational systematics should differ from ground-based radio galaxy surveys. Secondly, the QSOs are expected to be deeper in redshift ($z \sim 1$), so the result is not expected to be significantly contaminated by local sources (z < 0.1), which can introduce an additional dipole Tiwari and Nusser (2016). Separate studies of QSOs have reported much larger velocities, $v = (8100 \pm 1500) \text{ km/s}$ Singal (2022) (see also Ref. Singal (2019)), yet once again in the expected direction.

The most naive interpretation of this result is that the CatWISE QSOs are tracing an anisotropic Universe on an axis aligned with the CMB dipole. Curiously, this same direction appears in the QSO literature in two separate contexts. First, there are documented Large Quasar Groups (LQG) Clowes and Campusano (1991); Clowes et al. (2013), essentially the progenitors of today's superclusters, and also a documented preferred axis for QSO polarizations Hutsemekers and Lamy (2001); Hutsemekers et al. (2005) in the same direction. Moreover, within the LQGs, the QSO polarizations are aligned Pelgrims and Hutsemékers (2016). These coincidences warrant further study.

8.6.5. Dipole in SNIa

More recently, attempts have been made to study our motion with respect to Pantheon SNIa Scolnic et al. (2018), leading to conflicting conclusions. As explained above, cosmology should be conducted in "CMB frame" for consistency, which means that observational redshifts need to be corrected for our motion with respect to the CMB. This is a small correction, but it is imperative to get this right at lower redshifts, especially with SNIa Calcino and Davis (2017); Davis et al. (2019). Indeed, one finds some criticism of Pantheon CMB redshifts in the literature Rameez (2019); Rameez and Sarkar (2021); Steinhardt et al. (2020), and depending on the treatment of redshifts, diverging results have emerged.³⁷ In particular, Ref. Singal (2021) infers our velocity with respect to Pantheon SNe to be $v = (1600 \pm 500)$ km/s, or ~ 4 times larger than the CMB value, in the direction (RA, DEC) = $(173 \pm 12, 10 \pm 9)$ deg. This value is consistent with radio and QSO galaxy dipoles. In contrast, Ref. Horstmann et al. (2021), which employs corrected Pantheon CMB frame redshifts Steinhardt et al. (2020), arrives at the velocity $v = (249 \pm 51)$ km/s towards (RA, DEC) = $(166 \pm 16, 10 \pm 19)$ deg. This value is clearly lower than the CMB expectation, which makes it the first study inferring a smaller velocity. Moreover, the difference with Ref. Singal (2021), highlights the need to better understand SNIa redshifts, especially corrections for CMB frame.

³⁷ Differences in the treatment of SNIa redshifts have even spilled over into a debate on the evidence for dark energy Colin et al. (2019); Rubin and Heitlauf (2020); Rahman et al. (2021).

8.6.6. Emergent dipole in H_0

One can distinguish between bulk flows and Hubble expansion anisotropies through higher redshift data. The H0LiCOW collaboration are credited with one of the first results supporting a higher $H_0 > 70 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ determination Wong et al. (2020), but when one plots the H0LiCOW/TDCOSMO lenses on the sky, one finds that the largest H_0 values are oriented in the direction of the CMB dipole Krishnan et al. (2021b, 2022). Given the small size of the sample, this is no more than a fluke; by running simulations, one assesses the probability of H_0 being higher in the CMB dipole direction at p = 0.12 Krishnan et al. (2022). But is this trend there in other cosmological observables? One finds supporting trends in the Pantheon SNIa sample Scolnic et al. (2018) by performing hemisphere decomposition and inferences within flat Λ CDM across the sky Krishnan et al. (2022). This prompts the pertinent question: when the SNIa sample has been put in "CMB frame" from the outset, why is there still an emergent dipole in the direction of the CMB dipole? It is worth observing that since H_0 is a universal constant in any FLRW cosmology, this trend can be expected to be robust to changes in FLRW cosmologies. Similar configurations can arise by chance within the Λ CDM model with probability p = 0.065 Krishnan et al. (2022). The same observation has been extended to *standardisable* QSOs Lusso et al. (2020) and GRBs Demianski et al. (2017a), which places the observation in the $2 - 3\sigma$ window Luongo et al. (2021). It should be stressed these samples are all at sufficiently high redshift that one would expect the sources to be in "CMB frame". While the strong lensing time delay and Pantheon SNIa result is expected to be solid at 1.7σ , attributing a higher significance to this tendency for cosmological H_0 to be larger in the CMB dipole direction depends on QSOs and GRBs, which are non-standard as distance indicators (see Ref. Moresco et al. (2022) for a recent review).

8.6.7. CMB dipole: intrinsic versus kinematic?

Given that the magnitude of the matter dipoles are currently discrepant with the magnitude of the CMB dipole, systematics aside, this implies that the Universe is not FLRW. Note that this discrepancy between the matter and radiation dipole, if true, is once again an example of an early Universe and late Universe discrepancy, reminiscent of H_0 and S_8 tension. In effect, a breakdown in FLRW could explain both H_0 and S_8 tension, as recently highlighted Krishnan et al. (2021b). This focuses a spotlight on the cosmic dipole and its traditional purely kinematic interpretation, which is a working assumption. In principle, one should be able to determine if the CMB has an intrinsic dipole by studying Doppler-like and aberration-like couplings in the CMB. The first study in this direction constrains the intrinsic dipole to $v \sim (300 \pm 100) \text{ km/s}$ Ferreira and Quartin (2021). Moreover, one can study aberration effects at smaller scales (larger ℓ) Challinor and van Leeuwen (2002); Amendola et al. (2011); Notari and Quartin (2012); Roldan et al. (2016) and this has led to a determination Aghanim et al. (2014) of $v = 384 \text{ km/s} \pm 78 \text{ km/s}$ (stat) $\pm 115 \text{ km/s}$ (sys) in the direction (l, b) = (264°, 48°) and more recently $v = (298.5 \pm 65.6) \text{ km/s}$ Saha et al. (2021) in the direction (l, b) = (268.5 $\pm 49.8, 61.8 \pm 12.3)$ deg using the BipoSH formalism Mukherjee et al. (2014), which are consistent with the expected CMB value. These results are consistent with the kinematic interpretation.

The small magnitude of the dipole-subtracted two-point temperature-temperature angular correlation function $C^{TT}(\theta)$, has been used to predict Copi et al. (2015a) that the intrinsic CMB dipole is extremely small, see Sec. 8.3.8, however given current CMB data, it is difficult to rule out an intrinsic component to the CMB dipole. So the question of whether any matter anisotropy is primordial or not is difficult to address.

8.7. The Ly- α forest BAO and CMB anomalies

8.7.1. The Ly- α forest BAO anomaly

A 2.5 – 3σ discrepancy between the BAO peak in the Ly- α forest at $z \sim 2.34$ and the best fit *Planck* 2018 ACDM cosmology Cuceu et al. (2019); Evslin (2017) has been observed.

Observations of baryon acoustic oscillations in the SDSS DR9 and DR11 have provided for the first time statistically independent measurements of D_H/r_d and D_A/r_d at intermediate redshifts of 0.57 (galaxy BAO) and higher redshifts of 2.34 (Ly- α BAO) using different tracers Delubac et al. (2015); Aubourg et al. (2015). Here $D_H \equiv c/H(z)$ and $D_A \equiv \frac{c}{(1+z)} \int_0^z \frac{dz'}{H(z')}$ are the Hubble and angular diameter distances, respectively. The combined constraints from the two correlation functions of the BAO observations in the Ly- α forest of BOSS DR11 quasars, implied that the estimated D_A/r_d and D_H/r_d are respectively 7% lower and higher than the expectations of the best fit Λ CDM model to the Planck CMB data. This could be translated as a 2.5 σ tension. In Ref. Sahni et al. (2014), it was shown that these measurements can be used to test the concordance Λ CDM model in a model independent manner using a modified version of the Om diagnostic Sahni et al. (2008) called Omh^2 . They confirmed a significant, 2 to 3σ , tension between the BAO Ly- α observations and *Planck* CMB data in the context of the concordance model. In Ref. Sahni et al. (2014); Evslin (2017) it was suggested that this discrepancy arises not from the Λ CDM parameters but from the DE evolution itself at 0.57 < z < 2.34, if there is no systematics in the observations. Further analysis done by Zhao et al. (2017) analyzing various tensions in the standard model of cosmology using Kullback-Leibler (KL) divergence reported this tension as one of the important inconsistencies. In the analysis of the cross-correlation of Ly- α absorption and quasars in eBOSS DR14 Blomqvist et al. (2019); de Sainte Agathe et al. (2019), the significance of the tension has been reduced to lower than 2σ . Higher precision observations are needed to make a clear conclusion about this tension Aghamousa et al. (2016); Cuceu et al. (2019). Currently, it is reduced to $\sim 1.5\sigma$ in the final eBOSS (SDSS DR16) measurement, which combines all the data from eBOSS and BOSS Alam et al. (2021a); du Mas des Bourboux et al. (2020). However, we note that this anomaly is still very important, especially when considered together with the H_0 and S_8 tensions. Similar to the situation with the Ly- α tension, reducing the S_8 tension within the concordance model and its minimal extensions tends to exacerbate the H_0 tension Di Valentino et al. (2021c); moreover, constraints on S_8 based on the Ly- α data are in agreement with the weak lensing surveys which probe similar late-time redshift scales as the Ly- α measurements Palanque-Delabrouille et al. (2020) and the S_8 tension has also weakened with the latest observations Hamana et al. (2020); van Uitert et al. (2018). These seem to imply that a simultaneous solution to the H_0 and $Ly-\alpha$ tensions might also address the S_8 tension, see Sec. 7.5.7. The Planck Collaboration (2018) Aghanim et al. (2020b) does not include the Ly- α in their default BAO data compilation since for the concordance model and its simple/physically well motivated (e.g., spatial curvature, wCDM, quintessence, etc.) extensions, they do not provide significant constraints once the CMB and Galaxy BAO data are used, and they do not conform well with the rest of the data set within the framework of these models. This seems to suggest looking for non-trivial extensions to the ACDM model. The fact that Ly- α BAO prefers $D_H(2.33)$ larger than the Planck- Λ CDM, but $D_A(2.33)$ (is an integral over all z < 2.33) less than the Planck- Λ CDM, implies correspondingly a preference of a smaller H(z) at z = 2.33 and a preference of a long enough larger H(z) period before z = 2.33,

compared to the Planck- Λ CDM predictions. On the other hand, the BAO data from intermediate redshifts $z \sim 0.5$, viz., galaxy BAO data, are consistent with the Planck- Λ CDM Alam et al. (2021a). This picture can be explained with a DE density that decreases significantly with increasing redshift within the redshift range $0.5 \leq z \leq 2.3$, possibly, transitioning to the values below zero (implying a pole in the DE EoS parameter Ozulker (2022)), which can give rise to a non-monotonic behaviour of H(z). This also finds support from model-independent (non-parametric) reconstructions of DE that consider Ly- α together with other data sets. In Ref. Escamilla and Vázquez (2021), it is found that the current Ly- α data prefer a nearly null or negative DE density, or a transition from quintessence to a phantom DE for $z \geq 1.5$; the DE EoS derived from its energy density reconstruction presents a discontinuity at redshift around $z \sim 2$, which is necessary if the DE density transitioned to negative values. Finally, such DE models that fit better the Ly- α data can alox the H_0 tension; they are expected to provide the same comoving angular diameter distance to last scattering, $D_M(z_*) = c \int_0^{z_*} \frac{dz'}{H(z')}$ with $z_* \sim 1090$, with the concordance model, therefore the decreased H(z) at higher redshifts should be compensated by an increased H(z) at lower redshifts (and hence an increased H_0) in order to keep the integral describing $D_M(z_*)$ unaltered (for such models, see Sec. 7.5.7 and references therein).

8.7.2. Ly- α – Planck 2018 tension in $n_s - \Omega_m$

In the last decade, observations of the Ly- α flux power spectrum have emerged as a very powerful tool to extract information on the late-time cosmological evolution. Among the many results, data gathered by MIKE and HIRES, which probe very small scales and high redshifts, have enabled to set stringent bounds on a variety of DM models predicting a suppression of the matter power spectrum at Ly- α scales, including warm DM Viel et al. (2013) and other interacting models (see e.g. Ref. Murgia et al. (2017) and references therein for a review). In addition, several evaluations of the many SDSS data releases have led to very competitive constraints on cosmological parameters such as n_s , Ω_m , and σ_8 Palanque-Delabrouille et al. (2015, 2020), some of which as currently the center of great attention due to the S_8 tension discussed in Sec. 5.

Very recently, Ref. Palanque-Delabrouille et al. (2020) interestingly noticed that, while the values of the cosmological parameters extracted from Ly- α are in overall very good agreement with weak leasing surveys, a (2 – 3 σ) tension in the determination of the tilt of the matter power spectrum exists between Ly- α measurements and the inference from early-time probes such as *Planck* 2018. Specifically, they found that Ly- α prefers a sharper drop off of the spectrum with respect to what *Planck* would predict. This confirms previous findings by Ref. Palanque-Delabrouille et al. (2015). Also, although in a much more qualitative way, a similar conclusion has been drown in Ref. Hooper and Lucca (2021) for the case of MIKE/HIRES data.

These very intriguing results open the door to the possibility that some physics beyond of the standard Λ CDM model might be at play at Ly- α scales. This has been for instance investigated in the context of DM-(massive) neutrino interactions Hooper and Lucca (2021), finding a preference for a non-zero interaction strength at the 3σ level. Although future work will be needed in order to confirm these conclusions (testing the solidity of the numerical setup and extending the cosmological probes employed), the fact that a model is preferred over Λ CDM with such a significance is already *per se* very intriguing and indicative of the potential for discovery that the aforementioned tension might contain.

8.8. Parity violating rotation of CMB linear polarization

A parity-violating pseudoscalar field is a candidate of dark mater and dark energy. The field can couple to the electromagnetic tensor via a Chern-Simons interaction Ni (1977); Turner and Widrow (1988), which rotates the plane of linear polarization of CMB photons by some angle β as they travel from the last scattering surface to the present day Carroll et al. (1990); Carroll and Field (1991); Harari and Sikivie (1992); Carroll (1998), the so-called "cosmic birefringence" (see Ref. Komatsu (2022) for a review). Because polarization patterns of the CMB can be decomposed into parity-even *E* modes and parity-odd *B* modes, β can be measured though the *EB* cross correlation Lue et al. (1999). In 2020, Minami and Komatsu Minami and Komatsu (2020) reported $\beta = 0.35 \pm 0.14$ deg (68% C.L.) with the statistical significance of 2.4 σ , using the *Planck* high-frequency instrument (HFI) data at $\nu = 100$, 143, 217, and 353 GHz released in 2018.

A previous measurement of cosmic birefringence with the *Planck* satellite had been limited by systematic uncertainties on miscalibration angles of polarization-sensitive detectors Aghanim et al. (2016b), which are degenerate with β . Ref. Minami and Komatsu (2020) lifted this degeneracy by determining the miscalibration angles with the polarized Galactic dust emission, assuming that the *EB* cross correlation of the dust emission is null. Recently, Diego-Palazuelos et al. Diego-Palazuelos et al. (2022) relaxed this assumption and accounted for the impact of the foreground *EB* by assuming that it is proportional to the *TB* correlation of polarized dust emission. They found $0.36 \pm 0.11 \text{ deg} (68\% \text{ C.L.})$ from the latest *Planck* public data release 4 (PR4) Akrami et al. (2020c), with the statistical significance exceeding 3σ . Another important test is the frequency dependence of β , as astrophysical effects such as Faraday rotation give $\beta(\nu) \propto \nu^{-2}$. Using all of the *Planck* data including low-frequency instrument (LFI) data at $\nu = 30$, 44, and 70 GHz, Eskilt Eskilt (2022) found $\beta(\nu) \propto \nu^n$ with $n = -0.35^{+0.48}_{-0.47}$ (68% C.L.), which is consistent with no frequency dependence.

In future, analyses of data from the ongoing Adachi et al. (2020); Aiola et al. (2020); Dutcher et al. (2021); Ade et al. (2021a,b); Dahal et al. (2022) and future experiments POLARBEAR-2 et al. (2018); Ade et al. (2019); Moncelsi et al. (2020); Abazajian et al. (2019a); Allys et al. (2022) using the same method as Ref. Minami and Komatsu (2020) are expected to test the reported signal with higher statistical significance. Since the method depends on the assumption of the nature of polarized dust emission, improvements on the knowledge of the *EB* from the dust emission as well as on the calibration method of polarization sensitive detectors, e.g., calibration with Crab Nebula (Tau A) Aumont et al. (2020), are needed.

8.9. The lithium problem

Big Bang nucleosynthesis (henceforth BBN) is one of the cornerstones of the modern cosmological paradigm. In its simplest form, and specifically assuming the standard particle cosmology model and that the relevant nuclear physics is known, it has a single free parameter (the baryon-to-photon ratio), and can therefore provide a consistency test of the overall paradigm, as well as stringent constraints on physics beyond the SM Steigman (2007); locco et al. (2009); Pitrou et al. (2018).

Nevertheless, this is not an unqualified success story due to the well-known lithium problem Fields (2011); Mathews et al. (2020). Indeed, the theoretically expected abundance of lithium-7 (given our present knowledge nuclear and particle physics as well as generic

assumptions of astrophysics) seems to exceed the observed one, obtained from absorption spectroscopy in the photospheres of old, metalpoor Milky Way halo stars, by a factor of about ~ 3.5. When allowing for the statistical uncertainties on both sides, this represents a detection of ignorance (or missing physics) at more than five standard deviations. The canonical observational determination is that of Sbordone et al. Sbordone et al. (2010), ${}^{7}Li/H = (1.6 \pm 0.3) \times 10^{-10}$, while the most up-to-date theoretically expected value is that of Pitrou et al. (2021), ${}^{7}Li/H = (5.464 \pm 0.220) \times 10^{-10}$. The other canonical BBN nuclides (D, ${}^{3}He$, and ${}^{4}He$) have abundances that are in broad agreement with theoretical predictions (cf. the most recent PDG review of the observational status Zyla et al. (2020)), although a possible weak (less than two standard deviations) has been identified for Deuterium, depending on the BBN code and nuclear cross sections that one uses therein Pitrou et al. (2021); Yeh et al. (2021).

Attempts to solve the lithium problem can be broadly classified into four categories. First, a mundane solution would involve systematics in astrophysical observations, although none have been identified so far that would account for the large difference required for a solution. Second, one could analogously envisage systematics on the nuclear physics side, specifically in the measurements of the relevant cross-sections; however, the steady improvements in experimental techniques have all but closed this possible loophole Iliadis and Coc (2020); Hayakawa et al. (2020); Ishikawa et al. (2020); Mossa et al. (2020).

A third possibility involves new physics beyond the standard paradigm, or a different early-time cosmological evolution. Many such attempts exist in the literature, so far without success. Examples of mechanisms considered include scalar-tensor theories, photon cooling, early- or late-time decaying particles (including decaying dark matter, or magnetic fields Larena et al. (2007); Kohri and Takayama (2007); Kawasaki and Kusakabe (2011); Yamazaki et al. (2014); Kusakabe et al. (2014); Poulin and Serpico (2015); Goudelis et al. (2016); Sato et al. (2017); Salvati et al. (2016); Hou et al. (2017); Yamazaki et al. (2017); Luo et al. (2019); Mori and Kusakabe (2019); Anchordoqui (2021). They either fail by being incompatible with other constraints, require strong fine-tuning, or can only alleviate the problem (e.g., by increasing the error bars for the theoretically expected abundances).

As an example, consider the case of BBN in broad class of Grand Unified Theories with varying fundamental constants Coc et al. (2007); Berengut et al. (2010); Cheoun et al. (2011). Superficially this seems a good candidate explanation, because one expects the effects of varying constants to be stronger for heavier nuclei, and therefore one might envisage changing the primordial lithium-7 abundance without significantly changing those of lighter nuclei. A formalism enabling a self-consistent analysis of models where all such parameters (gauge and Yukawa couplings, fundamental particle masses, etc.) are allowed to vary was recently developed Clara and Martins (2020). The analysis of the most recent data Deal and Martins (2021) shows that such models can alleviate the lithium-7 problem, but not completely solve it. Specifically the value of the fine-structure constant at the BBN epoch is constrained to the level of parts per million of relative variation, as compared to the present-day laboratory value—a very stringent constraint, and not to far from the most stringent constraints on α , which come from local laboratory tests with atomic clocks and from high-resolution astrophysical spectroscopy. Interestingly, a variation of α at this level of relative variation could explain the putative Deuterium discrepancy recently suggested in Ref. Pitrou et al. (2021).

Finally, the simplest and currently most plausible solution to the lithium problem is the fourth, an astrophysical one. It is plausible that astrophysical measurements of lithium Sbordone et al. (2010); Melendez et al. (2010) are not representative of the cosmological production mechanism Spite et al. (2012). Specifically, lithium is known the be both created and destroyed in stars Pinsonneault et al. (2002); Richard et al. (2005); Korn et al. (2006); Fu et al. (2015). A recent detailed study Deal and Martins (2021) has quantified the amount of depletion needed to solve the lithium problem, and shown that transport processes of chemical elements in stars are able to account for it. Specifically, the combination of atomic diffusion, rotation and penetrative convection reproduces the lithium surface abundances of Population II stars, starting from the primordial Lithium abundance. More precise astrophysical measurements of abundances of lithium-7 and other nuclides, by a new generation of high-resolution ultra-stable spectrographs, such as ESPRESSO (already operational) and ANDES (forthcoming) will provide decisive tests of this scenario. All in all, it seems likely that the solution of the lithium-7 problem lies inside the stars and not in cosmology.

8.10. Quasars Hubble diagram tension with Planck- Λ CDM

There are various proposals for standardising QSOs in the literature Watson et al. (2011); Wang et al. (2013); La Franca et al. (2014); Dai et al. (2012); Solomon and Stojkovic (2021), but here we focus on a powerful method due to Risaliti and Lusso Risaliti and Lusso (2015). This analysis has indicated that there are large QSO data sets at odds with *Planck*- Λ CDM at ~ 4 σ Risaliti and Lusso (2019); Lusso et al. (2019) and FLRW at ~ 2 σ Luongo et al. (2021).

QSOs satisfy an empirical relation between luminosities in the UV and X-ray Avni and Tananbaum (1986), which serve as the basis for claims that they can be employed as standardizable candles Risaliti and Lusso (2015). In recent years, this program has borne fruit and Risaliti and Lusso have succeeded in producing a compilation of ~ 2000 high redshift QSOs in the redshift range $0.01 \leq z \leq 7.5$ with suitably low internal scatter so that they may be useful for cosmology Risaliti and Lusso (2019); Lusso et al. (2020). Remarkably, the original paper Risaliti and Lusso (2019), and a subsequent follow-up Lusso et al. (2019), which introduces GRB data, make the case for a strong deviation from the *Planck*- Λ CDM cosmological model beyond redshift $z \sim 2.^{38}$

Concretely, Risaliti and Lusso have combined SNIa with QSOs, but given that SNIa become sparse at higher redshifts, great care has been taken to ensure that the luminosity distances of binned QSOs and binned SNIa data agree in the redshift range where SNIa are relevant, namely, $0.01 \leq z \leq 1.4$. For this reason, the data below $z \sim 1.4$ is completely consistent with flat Λ CDM with $\Omega_m \sim 0.3$. Nevertheless, at higher redshift, one finds that the calibrated QSOs exhibit a strong deviation from the standard model. This is essentially driven by a preference for lower values of the luminosity distance $D_L(z)$ at higher redshifts, but it routinely gets interpreted in terms of matter density Ω_m , curvature $\Omega_k < 0$, and dynamical dark energy Yang et al. (2020a); Velten and Gomes (2020); Khadka and Ratra (2020, 2021, 2022); Bargiacchi et al. (2021b,a).

Interestingly, it has been shown that the QSO data set is consistent with the standard model, i.e. no tension, provided one does not cross-correlate with Type Ia supernovae Melia (2019). In other words, the $\sim 4\sigma$ deviation from *Planck*- Λ CDM may rest upon the

³⁸ In the original papers Risaliti and Lusso (2019); Lusso et al. (2019), the actual claim is that the data is inconsistent with ACDM for any value of Ω_m . This strong result has been impacted by the cosmographic expansion Yang et al. (2020a); Banerjee et al. (2021c), however, the ~4 σ discrepancy from *Planck*-ACDM is real Yang et al. (2020a).

calibration. Indeed, in Ref. Li et al. (2021b), GP reconstruction is employed to perform the calibration and the discrepancy reduces to $\sim 2\sigma$. However, calibration may not be the problem. It has been suggested that because the Risaliti-Lusso QSOs return different values of the constants entering the underlying UV-X-ray relation seems to vary across cosmological parameters Khadka and Ratra (2020, 2021, 2022). But, this may be a bit quick, since it is clear that cosmological parameters jump in the presence of (large) negative curvature, $\Omega_k < 0$, which is somewhat consistent with observations in Sec. 8.2, but this probably has a simple analytic explanation: one can lower $D_L(z)$ by invoking negative curvature Luongo et al. (2021). So, in some sense, it may be misleading to interpret the Risaliti-Lusso QSO data in any of the simple cosmological models, e.g. Λ CDM, wCDM, $w_0 w_a$ CDM. Now, the question is, since the Risaliti-Lusso QSOs are inconsistent with *Planck*- Λ CDM, are they a complete outlier? Surprisingly, the answer may be no. One should observe that Ly- α BAO Delubac et al. (2015); du Mas des Bourboux et al. (2020) returns distances consistently lower than *Planck*, see Sec. 8.7.1. Moreover, there appears to be some evolution in (H_0 , Ω_m) within the HST SNIa Dainotti et al. (2021a) ($1 \leq z$), which prefers lower values of H_0 and higher values of Ω_m , a behaviour that is once again consistent with the QSOs. Finally, Ref. Solomon and Stojkovic (2021) has recently also constructed a Hubble diagram from SDSS QSOs MacLeod et al. (2012), which appears to show a similar drop off in $D_L(z)$ relative to *Planck* at $z \sim 2$. These comments may be speculative, but there appears to be a need to target a greater number of high redshift SNIa.

Recently, Ref. Hodgson et al. (2020) introduced a new method to measure the luminosity distances to QSO jets by equating the size of the flare as measured by Very Long Baseline Interferometry to the variability timescale via a light travel-time argument, effectively making AGN jets a standard ruler constrained by the speed of light. They applied the method to 3C 84, a local AGN at $z \simeq 0.078$, and obtained a luminosity distance of 72^{+5}_{-6} Mpc, corresponding to $H_0 = 73^{+5}_{-6}$ km s⁻¹ Mpc⁻¹. The error-bars could be reduced when more sources are observed. An advantage of the method is that it is single rung and can be applied from the local Universe to $z \simeq 6$. However, the systematics still need to be understood further.

8.11. Oscillating force signals in short range gravity experiments

The scale of dark energy, required so that it starts dominating the Universe at recent cosmological times is $\lambda_{DE} \equiv \sqrt[4]{hc/\rho_{DE}} \approx 0.085$ mm, assuming $\Omega_m = 0.3$ and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. Therefore, if the origin of the accelerating expansion is geometrical ie due to modifications of GR, it is natural to expect the presence of signatures of modified gravity on scales of about 0.1 mm.

A wide range of experiments has focused on this range of scales (Murata and Tanaka, 2015; Kapner et al., 2007; Hoyle et al., 2004, 2001; Qvarfort et al., 2021) and constraints have been imposed on particular parametrizations of extensions of Newton's gravitational potential. Such parametrizations are motivated by viable extensions of GR and include Yukawa interactions leading to an effective gravitational potential

$$V_{\rm eff} = -G_N \frac{M}{r} (1 + \alpha e^{-mr}) \,. \tag{137}$$

For $m^2 < 0$ the Yukawa correction becomes generically oscillatory. Even though this type of behaviour is associated with tachyonic instabilities in most theories, this is not the case for non-local gravity theories where such an oscillating correction to the Newtonian potential is consistent with stability. In particular, non-local (infinite derivative) gravity theories Edholm et al. (2016); Kehagias and Maggiore (2014); Frolov and Zelnikov (2016) predict such spatial oscillations of the Newtonian potential without the presence of ghosts (instabilities), while keeping a well-defined Newtonian limit.

The analysis by Refs. Perivolaropoulos (2017); Antoniou and Perivolaropoulos (2017); Perivolaropoulos and Kazantzidis (2019) of short range gravity experiments has indicated the presence of an oscillating force signal with sub-millimeter wavelength. In particular Ref. Perivolaropoulos (2017) has indicated the presence of a signal at 2σ level of spatially oscillating new force residuals in the torsion balance data of the Washington experiment Kapner et al. (2007). As an extension of the previous analysis the study by Ref. Antoniou and Perivolaropoulos (2017) using Monte Carlo simulation and analyzing the data of the Stanford Optically Levitated Microsphere Experiment (SOLME) which involves force measurements an optically levitated microsphere as a function of its distance *z* from a gold coated silicon cantilever Rider et al. (2016) reports a oscillating signal at about 2σ level.

8.12. ACDM and the dark matter phenomenon at galactic scales

There is no doubt that the nature of dark matter plays a fundamental role in Cosmology. There is observational evidence that this elusive unseen component mostly resides in and around galaxies of very different luminosities and morphologies that therefore become unique and fundamental cosmological laboratories. In most galaxies there is overwhelming evidence for a dark spherical component, extended out to a radius fifteen times bigger than that of the stellar component Rubin et al. (1980); Persic et al. (1996), see also Ref. Salucci (2019). From the theoretical point of view, it is well known that the Λ CDM scenario has established itself as the predominant one, in virtue of its simplicity, usefulness in accounting for open issues of the Standard Model and a very good agreement with many large-scale cosmological observations, see e.g. Ref. Freese (2017). This galaxy formation scenario, starring cold and collisionless Beyond Standard Model particles with a particular bottom up perturbation spectrum (e.g. Ref. Profumo (2017)), has been carefully investigated by large-N cosmological numerical simulations that have revealed an ubiquitous presence in the Universe of dark halos with a very large range in masses Navarro et al. (1997). The crucial feature of these structures, formed in a bottom-up merging process, is their *universal* density profile, *cuspy* at the center: $\rho_{\text{NFW}} \propto r^{-1}$, a marking feature of the Λ CDM collisionless dark particle scenario. In detail, the above simulations show that, over 20 orders of magnitude in halo mass, the density profiles $\rho_{\text{NFW}}(r)$ of the DM halos take the form Navarro et al. (1997)

$$o_{\rm NFW}(r) = \frac{\rho_s}{(r/r_s)(1+r/r_s)^2} = \frac{M_{\rm vir}}{4\pi R_{\rm vir}} \frac{c^2 g(c)}{\tilde{x}(1+c\tilde{x})^2},$$
(138)

with $g(c) = [\ln(1 + c) - c/(1 + c)]^{-1}$. In Eq. (138) the density parameter ρ_s and the scale radius r_s vary from halo to halo in a strongly correlated way Klypin et al. (2011), $\tilde{x} \equiv r/R_{vir}$ and $c \equiv r_s/R_{vir}$, with M_{vir} and R_{vir} the virial mass and the virial radius, respectively, with



Fig. 26. Observed Data (points with errorbars) vs the collisionless NFW halo + stellar disk model (dashed line). Also shown the cored Burkert halo + stellar disk model (solid line) (see Ref. Gentile et al. (2007)).

the latter defined as the radius inside which the DM halo mass is 200 times the critical density of the Universe times the volume inside this radius; finally, *c* is weak function of the halo mass (Klypin et al., 2011): $c = 9 [M_{vir}/(10^{12} M_{\odot})]^{-0.13}$.

It is well known that the internal kinematics of galaxies endows us with a striking observational evidence that the dark matter halo density profiles do not comply with Eq. (138), see e.g. Refs. de Blok and Bosma (2002); Bullock and Boylan-Kolchin (2017); Salucci (2001); Gentile et al. (2004); Oh et al. (2011); Donato et al. (2009), and show a central core, i.e. a central region at about constant density of size r_c . Observational data, in fact, are very successfully represented by a cored Burkert profile (Burkert, 1995; Salucci and Burkert, 2000) according to which

$$\rho_B(r) = \frac{\rho_0 r_c^3}{(r + r_c)(r^2 + r_c^2)},\tag{139}$$

where ρ_0 is the central density and r_c the core radius. Such profile only at large galactocentric distances ($r > 1/3 R_{vir}$) converges to the (collisionless) NFW profile. Remarkably, this finding, which rules out the cuspy NFW profile in disk systems, is obtained from an accurate mass modelling of both the *individual*, see Fig. 26, and the *coadded* disk kinematics Dehghani et al. (2020). Furthermore, we stress that the presence of a cored halo distribution occurs in galaxies of: 1) different halo masses, (in the range $10^9 M_{\odot} - 10^{13} M_{\odot}$) and 2) different Hubble Types (see Ref. Salucci (2019)). It is crucial to point out that, as result of the inferred dark matter halo density profiles, we detect core radii ranging from 100 pc, in the dwarf galaxies, to 100 kpc, in the giant ones Salucci (2019), as shown in Fig. 27. Thus, the sizes of the inner halo regions of constant DM density of different galaxies possess an impressive large range of values, ruling out the case in which all objects have a similar value for the size due to a dark particle-related physical process, as in the case of the (simplest) self-interacting DM scenario.

Within the classic Λ CDM scenario, in which the density cores are obviously absent, the only reasonable core-forming process relies on the feedback mechanism involving supernovae explosions (e.g. Ref. Pontzen and Governato (2014); Di Cintio et al. (2014)) whose energy, injected in the interstellar gas, although by means of a very indirect and fine tuned process, is able to warm up the inner DM halo and create a constant DM density region. However, the recent evidence of the existence in dwarfs, giant and LSBs galaxies, see Refs. Karukes and Salucci (2017); Di Paolo et al. (2019), all systems for which this mechanism is inefficient due to the insufficient number of SN explosions occurring the unit of time, rules out the Λ CDM + baryonic feedback scenario as a viable explanation for the presence of the DM halo cores in the Λ CDM scenario.

Therefore, in all disk systems, and in many spheroidal systems Salucci et al. (2012), the total mass distribution consists in 1) a spherical dark matter halo with two structural parameters: a core radius and a central halo density, both varying among galaxies and 2) a stellar component (disk or spheroid) with two structural parameters: the stellar mass and its photometric radius R_D , also both varying among galaxies.

A further and perhaps more serious issue for the collisionless nature of the dark matter content of the Universe arises from the realization that all the above galaxy structural parameters are found related among themselves, in detail, those of the DM component: ρ_0 , r_c strongly correlate with those of the luminous component, M_D and R_D (see Ref. Salucci et al. (2020) and references therein). In order to realize the importance of such evidence let us first remind that: $\rho_B(r)$ and $\mu(R) \propto \exp(-r/R_D)$ are the spherical DM density and the luminous surface density. Then, for galaxies and their DM halos, $r_c = -(3/2)\rho(r)/(d\rho(r)/dr)|_{r_c}$ is a quantity deeply inserted in the *Dark* world, while $R_D = \frac{\dim \mu(R)}{d\ln R}$ is a main quantity of the *Luminous* world. Surprisingly, these two quantities, that, incidentally, are obtained from observations in totally different ways, strongly correlate over three orders of magnitudes, see Fig. 27, giving rise to a tight relationship. The latter is the strongest evidence for a dark matter-luminous matter connection leading us to invoke a direct interaction between the dark particles and the Standard Model particles of the stellar disk/spheroid beyond the collisionless status of the pure gravitational interaction. However, one can claim a full entanglement between the dark and the luminous components of galaxies, evidenced by the existence of Universal Rotation Curve Salucci et al. (2007); Karukes and Salucci (2017); Di Paolo et al. (2019).

Let us stress that such evidence in the dark and luminous mass distribution in galaxies, allied with a complete non-detection of the WIMP particle from accurate astrophysical observations and from properly devised experiments in underground laboratory or at LHC collider (e.g. Ref. Arcadi et al. (2018)), has recently opened the way for old and new scenarios in which the DM particles are other than cold and collisionless WIMPS, such as keV fermions, ultra light axions, self-interacting particles, boson condensates and interacting particles (e.g. Refs. Spergel and Steinhardt (2000); Hui et al. (2017); Drewes et al. (2017); Visinelli (2017)).

Thus, the dark matter phenomenon at galactic scales seems to provide us with a portal towards the true nature of dark particle that clearly appears to be much more complex than cold, collisionless and particle mass independent as that of the Λ CDM Universe. Regarding



Fig. 27. $\log_{10} r_c$ vs $\log_{10} R_D$ for galaxies of different stellar mass ($10^7 M_{\odot} \le M_{\star} \le 10^{12} M_{\odot}$) and morphology (High and Low Surface Brightness disks, the Giant Elliptical M87 and Dwarf Disks). Data come from the URC for HSBs, LSBs and DDs and from the individual kinematics for DDs and M87 (see Refs. Karukes and Salucci (2017); Di Paolo et al. (2019), Salucci et al. (2020)).

this latter, the lack of coldness in the dark particles in galaxies and their emergent capability to sustain interactions with themselves or/and Standard Model particles, are likely to be fatal for its ambition to represent the actual cosmos Salucci et al. (2020).

9. Stepping up to the new challenges

Coordinators: Wendy Freedman, Adam Riess, and Arman Shafieloo.

Contributors: Elcio Abdalla, Luis Anchordoqui, Nikki Arendse, Micol Benetti, Emanuele Berti, Kimberly K. Boddy, Alexander Bonilla, Erminia Calabrese, Bozena Czerny, Maria Dainotti, Eleonora Di Valentino, Celia Escamilla-Rivera, Ian Harrison, Dhiraj Kumar Hazra, J. Colin Hill, Daniel Holz, Ryan E. Keeley, Ruth Lazkoz, Benjamin L'Huillier, Matteo Lucca, Roy Maartens, Dinko Milaković, Suvodip Mukherjee, Savvas Nesseris, Rafael Nunes, Antonella Palmese, Leandros Perivolaropoulos, Levon Pogosian, Dan Scolnic, Neelima Sehgal, Joseph Silk, Tommaso Treu, Jian-Min Wang, Amanda Weltman, Radosław Wojtak, Gong-Bo Zhao.

In order to address all the open questions, and to change the Λ CDM from an effective model to a physical model, testing the different predictions, the goals for the next decade will be to:

- improve our understanding of systematic uncertainties;
- maximize the amount of information that can be extracted from the data by considering new analysis frameworks and exploring alternative connections between the different phenomena;
- improve our understanding of the physics on non-linear scales;
- de-standardize some of the ΛCDM assumptions, or carefully label them in the survey analysis pipelines, to pave the road to the beyond-ΛCDM models tests carried out by different groups.

This agenda is largely achievable in the next decade, thanks to a coordinated effort from the side of theory, data analysis, and observation. In 4 separate Lols Di Valentino et al. (2021a,b,c,d), we provide a thorough discussion of these challenging questions, showing also the impossibility we have at the moment of solving all the tensions at the same time.

The next decade will provide a compelling and complementary view of the cosmos through a combination of enhanced statistics, refined analyses afforded by upgraded experiments and next-generation space missions and facilities on Earth:

- Local distance ladder observations will achieve a precision in the H_0 measurement of 1% Riess et al. (2020).
- Gravitational time delays will reach a \sim 1.5% precision on H_0 without relying on assumption on the radial mass density profiles Birrer and Treu (2021) with resolved stellar kinematics measurement from JWST or the next generation large ground based extremely large telescopes (ELTs).
- CMB-S4 will constrain departures from the thermal history of the Universe predicted by the SM Abazajian et al. (2019a,b). The departures are usually conveniently quantified by the contribution of light relics to the effective number of relativistic species in the early Universe, N_{eff} Steigman et al. (1977). CMB-S4 will constrain $\Delta N_{\text{eff}} \leq 0.06$ at the 95% confidence level allowing detection of, or constraints on, a wide range of light relic particles even if they are too weakly interacting to be detected by lab-based experiments Abazajian et al. (2019a). CMB spectral distortions will be another possible avenue to test a variety of different cosmological models in the next decade Chluba et al. (2019); Kogut et al. (2019); Lucca et al. (2020)
- The *Euclid* space-based survey mission Laureijs et al. (2011) and Dark Energy Spectroscopic Survey (DESI) Aghamousa et al. (2016) will use cosmological probes (gravitational lensing, baryon acoustic oscillations (BAO) and galaxy clustering) to investigate the nature of DE, DM, and gravity Capozziello and De Laurentis (2011).
- The *Rubin* Observatory Legacy Survey of Space and Time (LSST Ivezić et al. (2019)) is planned to undertake a 10-year survey beginning in 2022. *Rubin*/LSST will chart 20 billion galaxies, providing multiple simultaneous probes of DE, DM, and ΛCDM Science et al. (2009); Zhan and Tyson (2018); Sahni and Starobinsky (2006).
- The *Roman* Space Telescope (formerly known as WFIRST Akeson et al. (2019)) will be hundreds of times more efficient than the Hubble Space Telescope, investigating DE, cosmic acceleration, exoplanets, cosmic voids.

- The combination of *Rubin*/LSST, *Euclid*, and *Roman*/WFIRST will improve another factor of ten the cosmological parameter bounds, allowing us to distinguish between models candidates to alleviate the tensions.
- The Square Kilometre Array Observatory (SKAO) will be a multi-purpose radio-interferometer, with up to 10 times more sensitivity, and 100 times faster survey capabilities than current radio-interferometers, providing leading edge science involving multiple science disciplines. SKAO will be able to probe DM properties (interactions, velocities and nature) through the detection of the redshifted 21 cm line in neutral hydrogen (HI), during the so-called Dark Ages, before the period of reionization. SKAO will also be able to test the DE properties and the difference between some MG and DE scenarios by detecting the 21 cm HI emission line from around a billion galaxies over 3/4 of the sky, out to a redshift of $z \sim 2$.
- GW coalescence events will provide a precise measurement of H_0 Schutz (1986); Abbott et al. (2017b, 2021d). With the LIGO-Virgo-KAGRA network of GW detectors, it is expected to constrain H_0 to a precision of ~ 2% with about 50 binary neutron star events Chen et al. (2018); Feeney et al. (2019). Among the sources without electromagnetic counterpart (called dark standard sirens), either by using the statistical host identification technique Gray et al. (2020); Palmese et al. (2019), or using the spatial crosscorrelation Oguri (2016); Mukherjee et al. (2021a); Bera et al. (2020) of the GW sources with spectroscopic galaxies detectable from DESI and SPHEREx Diaz and Mukherjee (2022), one can achieve a similar precision with a few thousands of dark sirens from the future detector network. The dark siren measurement of the expansion history may also be possible from the mass spectrum of binary black holes by using a few hundreds of sources, if the mass spectrum can be standardized Farr et al. (2019); Mastrogiovanni et al. (2021b); Mukherjee (2021); Ezquiaga and Holz (2022).
- CERN'S LHC experiments ATLAS and CMS will provide complementary information by searching for the elusive DM particle and hyperweak gauge interactions of light relics Buchmueller et al. (2017); Penning (2018); Cid Vidal et al. (2019); Anchordoqui (2020). In addition, the ForwArd Search ExpeRiment (FASER) will search for light hyperweakly-interacting particles produced in the LHC's high-energy collisions in the far-forward region Ariga et al. (2018, 2019); Feng (2019).

In what follows, we review the cosmological observations and challenges we will face in next coming years.

9.1. Future investigations in cosmology

9.1.1. Supernova cosmology

SNe Ia remain the premier tool to link the very local Universe (z < 0.01) to the Hubble flow and beyond. Over the next decade, there will be a wealth of data from recently finished and upcoming surveys that will be released. At low-z (z < 0.1), the statistics will increase from current samples by a factor of $10 \times$ from surveys like ZTF and YSE; at mid-z 0.1 < z < 1.0, statistics will increase by a factor of $> 300 \times$ from *Rubin*/LSST; and at high-z (z > 1.0), statistics will increase by a factor of $10 \times$ from surveys like ZTF and YSE; at mid-z 0.1 < z < 1.0, statistics will increase by a factor of $> 300 \times$ from *Rubin*/LSST; and at high-z (z > 1.0), statistics will increase by a factor of $100 \times$ from the *Roman* Space Telescope. While the predominant cosmological measurements with SNe Ia have been with the Hubble diagram to measure w_{DE} or Ω_M or from its role in the distance ladder to measure H_0 , the large increase in statistics will enable its usage for a variety of different cosmological measurements. These are described in Ref. Scolnic et al. (2019) and include measurements of σ_8 from peculiar velocities at low-z (Stahl et al., 2021) and from the impact of lensing at high-z (Zhai et al., 2020) and further measurements of H_0 from lensed SNe Ia Huber et al. (2019).

There are limitations to how well analyses will be able to leverage this boon in statistics. First, for the direct distance ladder measurement of H_0 , current measurements are limited by the number of SNe Ia that have exploded very nearby (z < 0.01), which only occurs roughly once per year. As current measurements utilize now ~ 40 SNe Ia to calibrate the second rung of the distance ladder Riess et al. (2021b), it will be difficult to significantly improve this measurement unless measurements of the Cepheids or TRGB can be made accurately at higher distances. Second, as the statistics grow by orders of magnitude, pushing down the systematic floor will become an even higher priority. For measurements of H_0 , this means that the sample of SNe used to calibrate Cepheids/TRGB is consistent with the sample of SNe used in the Hubble flow. For measurements of w_{DE} , this means improving calibration, constraints on evolution, etc.

9.1.2. Local distance ladder

The local distance ladder remains the most precise and direct method to produce a high precision determination of the local value of the Hubble constant. There is much reason for optimism for continued progress due to the availability of new facilities like JWST, the *Roman* and *Rubin* Observatories, ELTs, and LIGO-Virgo-KAGRA as well as future data releases from Gaia. These facilities are likely to improve upon current measurements while improving the connections between the nearest links. While the distance ladder is approaching the ambitious goal of a 1% determination of the Hubble constant, we may anticipate this goal being approached by a broader range of methods than those available now. Standard Sirens have the potential to provide a fully independent check on the local distance ladder though calibration uncertainties may produce an error floor short of the 1% goal.

9.1.3. Spectroscopic galaxy clustering

The BAO and RSD measurements available in the next decade will provide key information of the expansion and growth history of the Universe, respectively. Compared to the precision offered by existing galaxy surveys such as SDSS BOSS Dawson et al. (2013) and eBOSS Dawson et al. (2016), surveys in the next decade, including DESI Aghamousa et al. (2016), PFS Ellis et al. (2014), Euclid Laureijs et al. (2011), *Roman* Spergel et al. (2015), *Rubin*/LSST Science et al. (2009) and so forth, are able to tighten the constraint on both BAO and RSD parameters significantly in a wide range of redshifts, thanks to the order-of-magnitude increase in the optical spectra to be collected.

Challenges exist to reach that precision though, as efforts are needed to mitigate both the theoretical and observational systematics when analyzing the clustering of galaxies. In this regard, the goal for the BAO measurement is relatively more straightforward to achieve, as the BAO signal is more robust against systematics Ross et al. (2017); Ding et al. (2018). The measurement of RSD, however, requires more care to control the impact from both the observational and theoretical systematics. The observational systematics, for example, can root from issues of target selection from the imaging data, the effect of fibre collision, etc (see de Mattia et al. (2021) for a recent study on the eBOSS ELG sample). Theoretical systematics may include biases for inferring RSD parameters using a fixed template, as commonly used for RSD measurements from existing surveys. Recent development of the EFT-based approach can effectively remove the dependence

on the template Baumann et al. (2012); Carrasco et al. (2012); Perko et al. (2016); Blas et al. (2016a); Ivanov and Sibiryakov (2018), although more nuisance parameters are needed.

It is commonly known that the BAO data, on its own, can only measure the product $r_d h$, where r_d is the sound horizon at the baryon decoupling. However, one can measure both r_d and h separately in a way that is independent of the early Universe physics (e.g., physics prior and during recombination) if the BAO data is combined with a prior information on $\Omega_m h^2$ Pogosian et al. (2020). One possibility is to combine BAO with the CMB lensing and galaxy lensing data, which provide a handle on $\Omega_m h^2$ with practically no dependence on recombination physics. Alternatively, one could simply do a consistency test by taking the value of $\Omega_m h^2$ determined from CMB anisotropies and using it as a prior in the BAO analysis to see if the deduced values of r_d and h agree with those obtained from CMB. Any disagreement would signal a missing ingredient in the model used to determine r_d when analyzing the CMB data. As forecasted in Ref. Pogosian et al. (2020), the DESI BAO data, combined with the *Planck* prior on $\Omega_m h^2$, will be able to determine H_0 to 0.5% accuracy, or $\sigma_{H_0} \sim 0.3 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$.

Over the past five years, full-shape analyses of galaxy clustering datasets have proven their worth as a tool to constrain both the Λ CDM cosmological model and a wealth of extensions (e.g., Ivanov et al., 2020d; D'Amico et al., 2021; Chudaykin et al., 2021a; Ivanov et al., 2020b; Xu et al., 2021b; D'Amico et al., 2022; Cabass et al., 2022; Vagnozzi et al., 2021a). In the next decade, the power of such tools will only increase as the survey volume grows, and will eventually lead to large scale structure dominating the constraining power on a wide variety of parameters.

Whilst significant improvements will undoubtedly be possible by applying the current analysis methods and pipelines (which have already been tested on simulations larger than the observable Universe (Ivanov et al., 2021a; Nishimichi et al., 2020; Chen et al., 2020b)) to upcoming data (e.g., Chudaykin and Ivanov, 2019), improved theoretical modelling will sharpen the constraints further still. The error on the Hubble parameter measurement from this method will reach $\sigma_{H_0} \sim 0.05 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ with the currently available power spectrum and bispectrum models Chudaykin et al. (2020b, 2021c); Ivanov et al. (2021a). However, even better results can be obtained from extending the EFT calculations up to higher-loop order, such as implementation of the two-loop and three-loop power spectra (Carrasco et al., 2014; Baldauf et al., 2015; Konstandin et al., 2019), one-loop bispectrum (Eggemeier et al., 2019), or two-loop bispectrum (Baldauf et al., 2021). This will extend the validity of the models, allowing smaller-scale information to be captured in a robust fashion, marginalizing over all relevant galaxy formation and hydrodynamic effects via symmetry arguments. Similar improvements can be obtained from simulation-based inferences (Kobayashi et al., 2021, 2020), although care will be needed to avoid bias arising from hydrodynamic effects not captured in the modelling. Generalization to additional redshift components, such as the bispectrum multipoles, can also add a tranche of new data, and thereby constraining power (Gualdi and Verde, 2020; Philcox and Slepian, 2021).

Another promising avenue is via the inclusion of higher-order statistics, such as the galaxy trispectrum or four-point correlation function and beyond. Initial forecasts suggest that the statistics can yield impressive constraining power on σ_8 (Gualdi et al., 2021), arising due to degeneracy breaking, and recently, the first detections of such quantities have been made (Philcox et al., 2021c; Gualdi and Verde, 2022). Of course, their use will require the development of rigorous theoretical models (Steele and Baldauf, 2021) that must be tested on simulations (including systematic effects) before their application to data. *N*-point functions are not the only way to proceed, however: field-level inference provides a promising manner in which to analyze the galaxy survey without compression to summary statistics (Schmidt, 2021; Cabass and Schmidt, 2020; Schmidt et al., 2020; Seljak et al., 2017), and could lead to strong constraints on parameters such as σ_8 from a perturbative- or simulation-based framework, once the relevant galactic effects are marginalized over.

Finally, it is important to discuss concerns on the applicability of the standard BAO template fitting method in the future. The fixed template method is currently proven to be biased and to result in loss of information for the galaxy RSD/AP measurements. The galaxy redshift clustering data, however, can be efficiently analyzed by means of the EFT-based full-shape method Ivanov et al. (2020c); D'Amico et al. (2020). As far as the BAO measurement is concerned, the dependence on the fiducial template is not so strong, and probably it will not cause a large systematic error even in the era of future galaxy surveys Bernal et al. (2020). However, strictly speaking, it is not clear by default what fiducial cosmology should be used in the BAO template. One option is to fix it by first running the full-shape analysis without the post-reconstructed BAO data. This analysis will already constrain the cosmological parameters very tightly Chudaykin and Ivanov (2019). Then the BAO template can be calculated for the best-fit full-shape cosmology. All in all, all these arguments suggest that the BAO method does not require a major modification in order to match the precision of the future datasets.

9.1.4. Cosmic microwave background

Over three decades, with observational campaigns from space, balloons, and ground-based telescopes, the CMB has been the driving force in establishing the standard cosmological model. The most stringent limits on the Λ CDM parameters are obtained from *Planck* data or a combination of *Planck*/WMAP and ACT/SPT ground-based experiments. These experiments have accumulated observations in temperature and polarization over many frequencies and extended ranges of angular scales. In particular, with the latest *Planck* data we have hit the limit of cosmic variance over large and intermediate scales in temperature (*Planck* CMB temperature power spectrum measurements are cosmic-variance-limited for $\ell \leq 1600$). However, much more information can be extracted from improved small-scale temperature measurements and high-accuracy polarization data at all scales, which are the key target of the next decade's CMB experiments.

From the ground there are several ongoing, planned, and future experiments that will continue to improve CMB temperature and polarization observations. For the topics covered here, the most relevant experiments are those pushing observations over extended and high-resolution scales. These include future releases from the ongoing ACT and SPT experiments, as well as new experiments including the Simons Observatory Ade et al. (2019), the South Pole Observatory, CMB-S4 Abazajian et al. (2016, 2019a), and the proposed CMB-HD Sehgal et al. (2019a,b, 2020). The new power spectra from these observatories will constrain H_0 with sub-percent precision in the context of Λ CDM (e.g. Ref. Ade et al. (2019)). Even within more extended models, such as those proposed to resolve the tensions discussed earlier, the statistical power of these upcoming measurements will be sufficient to yield precise H_0 constraints and potentially discriminate amongst proposed resolutions, an extremely exciting prospect. In addition, the extracted lensing signal will be revolutionary for constraining the growth of structure with percent level constraints on σ_8 when correlating CMB lensing with other tracers of the matter distribution.

Anomalies in the present CMB data and tensions between CMB temperature and other cosmological datasets in determining cosmological parameters can be tested with much better precision with upcoming CMB space- and ground-based surveys. *Planck* temperature data reveals an anomaly in the lensing amplitude. While this lensing anomaly can be resolved with a closed Universe Aghanim et al. (2020b); Di Valentino et al. (2019b); Handley (2021), it aggravates the already existing tensions between the observations in determination of H_0 and S_8 . Atacama Cosmology Telescope Aiola et al. (2020) temperature and polarization data, however, do not find this lensing anomaly and the standard model stays consistent with the data. Several new physics candidates and different possibilities of systematic uncertainties have been proposed to solve these discordances. These anomalies and disagreement between CMB datasets and the necessity of new physics will be tested with upcoming observations. Three major improvements in upcoming observations will be able to help in this regard. Firstly temperature anisotropy measurements from ground-based experiments such as Simons Observatory, CMB-S4, and CMB-HD will be able to explore the small differences between *Planck* and ACT at much better precision. Cosmic-variance-limited polarization measurements from LiteBIRD out to $\ell \sim 800$ and small-scale polarization data from the ground-based surveys will help in identifying the potential source of anomalies and tensions. Finally, precise measurements of the lensing potential will also independently estimate the lensing amplitude and thereby can provide a statistically significant angle in the study of the lensing anomaly.

The most advanced proposal for a next-generation CMB satellite is the JAXA-led LiteBIRD satellite Allys et al. (2022). With a predicted launch towards the end of the decade, LiteBIRD aims to measure the CMB temperature and polarization anisotropies with unprecedented precision and with the ultimate goal to deeply characterize the signal from inflation Pimentel et al. (2022), ruling in or out well-motivated inflation models. The new maps will help shed light on existing parameter tensions in two ways: 1) LiteBIRD will provide a new, independent of *Planck* H_0 satellite measurement, which will be highly robust to systematic effects due to the use of data from a single, well calibrated CV limited polarization data up to 0.2 degree scales; 2) the new E-mode measurements will provide a new, cosmic-variance-limited measurement of τ reducing degeneracies with other parameters and S_8 in particular.

As already clear from the previous sections, the experimental effort invested in the cosmological landscape has been extremely prolific in the past decades and will continue to grow in the coming years. However, there are some intrinsic limitations in many observables that do not depend on the sensitivity or the duration of the given experiment, and can only be overcome with complementary probes. For instance, in the case of the CMB anisotropies, the presence of the cosmic variance or the well-known degeneracy between A_s and τ_{reio} , as well as the limited observable scales, limit the amount of information that can be extracted from these measurements of the last-scattering surface.

In this regard, CMB spectral distortions (SDs) Zeldovich and Sunyaev (1969); Sunyaev and Zeldovichb (1970); Burigana et al. (1991); Hu and Silk (1993a,b); Hu (1995); Chluba and Sunyaev (2012) have been shown to have a remarkably deep synergy with the observation of the CMB power spectra André et al. (2014); Chluba and Jeong (2014); Chluba et al. (2021, 2019); Lucca et al. (2020); Fu et al. (2021); Schöneberg et al. (2021a). In fact, they are mainly produced in the pre-recombination era by any process that affects the energy spectrum of the CMB photons, and are therefore predicted to exist even within the standard Λ CDM model Chluba and Sunyaev (2012). In this way, they enable to probe a large section of the history of the Universe which overlaps and complements the one already tested by means of the CMB power spectra. The applications in this direction range from Λ CDM Chluba (2016) to models invoking BSM physics Chluba (2013), from inflation Schöneberg et al. (2021a) to recombination Hart et al. (2020).

In particular, one of the main production mechanisms within ACDM is the dissipation of acoustic waves Chluba et al. (2012). This effect takes place when the length scale of the density anisotropies is comparable to the mean free path of the CMB photons, so that the latter stream from the overdense to the underdense regions effectively creating a flow of energy injection which ultimately affects the global energy spectrum. Because of Thompson and Coulomb interactions, the photons end up dragging electrons and protons, which results in an isotropization of the plasma and a damping of the anisotropies at small scales, effect known as Silk damping. Since the amount of density anisotropies at a given scale directly depends on the value of primordial power spectrum (PPS) at that scale, SDs are very sensitive to the cosmological parameters ruling the PPS. This dependence and the fact that SDs are produced prior to recombination are of significant importance as they allow to probe the shape of the PPS (and the inflationary potential more in general) over more than four decades in Fourier space otherwise unexplored by other (complementary) measurements. In combination with, for instance, the CMB observation by *Planck* this would in principle allow to test the inflationary epoch to an unprecedented degree of precision (see e.g. Ref. Schöneberg et al. (2021a)). It is also worth nothing that, as shown in Ref. Hart et al. (2020), also the eventual observation of the cosmic recombination radiation Chluba and Ali-Haimoud (2016) would further increase the sensitivity of SDs to inflation, on top of the large amount of information it would provide on the recombination epoch.

Additionally, as recently pointed out in Ref. Lucca (2020), the fact that SDs can put strong constraints on the scalar spectral index n_s can also play a significant role in the Hubble tension, see Sec. 4. Indeed, many extensions of the Λ CDM model recently proposed to address this tension, such as the EDE and the SI ν models discussed in Secs. 7.4.2 and 7.7.12, respectively, introduce significant shifts in the standard cosmological parameters in the attempt to compensate for the new physics while still accurately fitting the CMB power spectra. This inevitably introduces strong degeneracies between the affected standard parameters and the model-specific quantities. Since one of the most common parameters that vary in these scenarios is n_s , SDs constitute an ideal independent probe to break the aforementioned degeneracies and potentially constrain the efficacy of these models as solutions to the Hubble tension. Moreover, in the context of the Hubble tension, SDs have also been advanced as a possible avenue to obtain an (almost) model-independent measurement of the H_0 value Abitbol et al. (2019). This can be achieved by precisely observing the evolution of the CMB monopole temperature over an extended timescale, thereby obtaining a measure for the cooling of the Universe and thus its expansion rate.

Interestingly, together with the dissipation of acoustic waves, SDs are also sensitive to the dissipation of tensor modes, making them a window to another large class of inflationary scenarios Chluba et al. (2015). In this context, as recently discussed in Ref. Kite et al. (2021), through this mechanism SDs are also able to probe primordial GWs over six orders of magnitude in frequency space. This can tightly bound a variety of scenarios involving phase transitions or cosmic strings Kite et al. (2021), among many more.

Along with the spectral distortions on the CMB monopole, spatially fluctuating polarised CMB spectral distortion can also arise due to conversion of photons to axions (or axion like particles (ALPs)) in the presence of external magnetic field as proposed in Refs. Mukherjee et al. (2018a, 2020a). The measurement of the polarised axion distortion will provide a new way to detect the coupling of photons with ALPs in the mass range 10^{-11} – 10^{-14} eV. This is possible from the upcoming ground based CMB experiment such as Simons Observatory, CMB-S4, CMB-HD and from space-based CMB telescope LiteBIRD.

The complementary between CMB anisotropies and SDs mentioned at the beginning of this section can also be applied to models requiring, for example, primordial magnetic fields (PMFs) Jedamzik et al. (2000); Kunze and Komatsu (2014); Jedamzik and Saveliev (2019), DM with non-standard characteristics, such as decays Hu and Silk (1993b); Lucca et al. (2020) or interactions Ali-Haïmoud et al.

(2015); Slatyer and Wu (2018), Axion-Like Particles Mukherjee et al. (2018a, 2020a) and dark photons, or primordial black holes Tashiro and Sugiyama (2008); Lucca et al. (2020); Acharya and Khatri (2020); Eroshenko (2021); Papanikolaou et al. (2021). Many of this scenarios have also been shown to solve either the Hubble tension, such as for PMFs Jedamzik and Pogosian (2020), the EDGES anomaly, such as for DM-b interactions Kovetz et al. (2018), or the σ_8 tension, such as for DM-photon interactions Stadler and Bœhm (2018); Becker et al. (2021). Therefore, also in this context SDs could play a competitive and complementary role in the search for a solution to these modern problems.

However, profiting from the constraining power of SDs will only be possible with the advent of advanced dedicated missions such as SuperPIXIE Kogut et al. (2019) and Voyage 2050 initiative Chluba et al. (2021), which, most likely, will have to be preceded by pathfinders from the ground or space. Therefore, the goal of the next decade in the context on CMB SDs will not only have to be in the theoretical and numerical development of the field, but will also have to be particularly devoted to the experimental realization of a concrete observational strategy to measure both temperature anisotropy and spectral distortions in a same setup Mukherjee et al. (2018b, 2019).

9.1.5. Weak lensing

A number of ongoing and planned weak lensing surveys promise to provide significantly tighter constraints on the amplitude of matter fluctuations σ_8 and the equation of state of dark energy (see Tables 3 and 4).

These include ongoing surveys such as Kilo-Degree Survey (KiDS) Kilo-Degree Survey (2022), Dark Energy Survey (DES) Dark Energy Survey (2022), Hyper Suprime-Cam (HSC) Hyper Suprime-Cam (2022), and planned to start surveys such as the *Rubin* Legacy Survey of Space and Time Large Synoptic Survey Telescope (2022), Euclid Euclid (2022), Nancy Grace *Roman* Space Telescope Nancy Grace Roman Space Telescope (2022), and the Ultraviolet Near-Infrared Optical Northern Survey (UNIONS) which is a collaboration between two the Hawai'ian observatories CFHT (Canada-France-Hawaii Telescope on Mauna Kea) and Pan-STARRS (Panoramic Survey Telescope and Rapid Response System on Maui) Ultraviolet Near-Infrared Optical Northern Survey (2022); Canada-France Imaging Survey (2022); Panoramic Survey Telescope and Rapid Response System on Maui (2022).

These lensing surveys promise not only to map the photo-z sky and dark matter but also constrain the growth of large structures to unprecedented accuracy and precision.

9.1.6. Time lag cosmography and time delay cosmography

In this Section we describe two methods based on "standard clock", i.e. the measurement of time intervals that can be converted into a cosmic distance and thus a cosmological tool. First, we describe the use of the time lag between variability of the accretion disk surrounding black holes, which we refer to as "time lag cosmography". Then we describe the use of the time delay between multiple images of strongly gravitationally lensed sources, which we refer to as "time delay cosmography" (Treu and Marshall, 2016).

9.1.6.1. H_0 measurements from quasars with Rubin/LSST monitoring The oldest method to use active galactic nuclei for cosmology is the method based on continuum time lag measurements Collier et al. (1999) in the accretion disk. The method is conceptually simple, it is based on the concept of accretion disk model of Ref. Shakura and Sunyaev (1973), which well describes the accretion disk at radii of order of 100 - 1000 gravitational radii, where the optical continuum forms. The method is not very sensitive to the innermost part of the accretion flow, close to the black hole, see e.g. Ref. (Kammoun et al., 2020), where the local approximation of the disk emission by a black body might not apply (Czerny et al., 2003; Kubota and Done, 2018). However, the method was not successful so far since the so called disk size problem appeared: although the time measured delay τ scaled with the wavelength λ as expected ($\tau \propto \lambda^{4/3}$). Ref. Collier et al. (1999)), the normalization of this relation did not follow the theoretical expectations, and the measured time delays were frequently longer implying larger disk size, see e.g. Refs. Collier et al. (1999); Cackett et al. (2007); Shappee et al. (2014); Fausnaugh et al. (2016); Jiang et al. (2017); Mudd et al. (2018); Yu et al. (2020); Fian et al. (2021), although part of the effect may be due to pre-selecting at the basis of S/N requirements and large intrinsic dispersion due to orientation, spin or accretion efficiency (Homayouni et al., 2019). Disk sizes larger than expected were also found from microlensing measurements, see e.g. Ref. (Rauch and Blandford, 1991). The problems might have come from the considerable departure from the local black body emission, see e.g. Ref. (Hall et al., 2018), but recent dense reverberation mapping proved that the problems with disk size come from the contribution to the continuum from the Broad Line Region, most notably Balmer continuum, but also Fe II continuum (Cackett et al., 2018; Edelson et al., 2019; Netzer, 2022). Identification of the problem opens a way to use the multicolour monitoring data from Rubin/LSST from the Dip Drilling Fields to cosmology (Yu et al., 2020), if the corrections due to Balmer continuum and Fe II are implemented. It will nicely complement the quasar method based on emission line time delays which allow to constrain other cosmological parameters, see e.g. Refs. (Zajaček et al., 2021; Khadka et al., 2021) but is not yet applicable to measuring H_0 since it still requires external scaling.

9.1.6.2. Constraining cosmology with multiply imaged supernovae and quasars. Time delay cosmography relies on the gravitational time delay between multiple images of a lensed variable source to constrain cosmology. The time delays between the images are primarily sensitive to the Hubble constant, but also weakly to several other cosmological parameters such as the matter density, curvature of the Universe and the EoS parameter for dark energy and its evolution over time. Other aspects that influence the time delays are the lens potential, microlensing due to substructure in the lens galaxy, and line-of sight-structures. If accounted for these effects properly, gravitationally lensed quasars and supernovae (glSNe) can be powerful probes to yield constraints on cosmological parameters, independently from the distance ladder or CMB.

Multiply imaged quasars have been used for cosmology since their discovery in the late 70s. Since the year 2000 advances in sample size, data quality and analysis methods have shown that they can be used to determine the Hubble constant with high precision and accuracy. An account of the history of quasar based time delay cosmography and future prospects can be found in the review by Treu and Marshall (2016). Briefly, hundreds of multiply imaged quasars have already been discovered and future surveys by the Euclid, *Roman, Rubin,* and SKAO Telescopes are going to increase the samples by orders of magnitudes (e.g. Oguri and Marshall, 2010). The precision and accuracy of the inferred cosmology will not be limited by sample size, but rather by the quality of the follow-up data and understanding of systematic errors, which are in many case common to the study of glSNe, and therefore are discussed below.

When Refsdal predicted in 1964 how the phenomena of strong gravitational lensing could be used to calculate the cosmic expansion rate Refsdal (1964), he initially suggested glSNe for this purpose. Only recently has this avenue become a reality. The first discovery of a glSN was made by the Panoramic Survey Telescope and Rapid Response System 1 (Pan-STARRS1), when it detected an unusually red and bright SN. After spectroscopic confirmation of a foreground lensing galaxy, the transient was classified as a gravitationally lensed SNIa, although the imaging data had insufficient resolution to separate the images Quimby et al. (2014). The Hubble Space Telescope (HST) provided data of the first resolved and multiply-lensed SN, a core-collapse SN appropriately named "Refsdal" Kelly et al. (2015). Four images were detected around an elliptical galaxy, and the prediction that another one would appear in a second host-galaxy image was verified one year later Kelly et al. (2016). SN Refsdal alone will provide a measurement of H_0 with a statistical error of 7% Grillo et al. (2018).

The intermediate Palomar Transient Factory (iPTF) identified glSN iPTF16geu, which was followed up by ESO VLT, Keck Observatory, and HST and spectroscopically identified as a type Ia SN Goobar et al. (2017); Cano et al. (2018). The third resolved strongly lensed supernova AT2016jka ("SN Requiem") was discovered in Hubble Space Telescope data, and is predicted to host a fourth image in two decades time, which should allow for a sub-per cent precision measurement of the time delay Rodney et al. (2021).

Current transient surveys capable of detecting glSNe, such as the Zwicky Transient Facility (ZTF) and Pan-STARRS, are only estimated to discover a few objects a year (6-9 Goldstein and Nugent (2017); Goldstein et al. (2019); Wojtak et al. (2019) and two Wojtak et al. (2019) for ZTF and Pan-STARRS, respectively). The true potential of discovering and observing glSNe will be unveiled by future telescopes, which are predicted to discover orders of magnitude more. The *Rubin* Observatory Legacy Survey of Space and Time (LSST) Science et al. (2009) is estimated to detect around 89 type Ia and 250 core collapse glSNe a year Goldstein and Nugent (2017); Goldstein et al. (2019); Wojtak et al. (2019), although the actual discovery rates may be lower when employing more restrictive criteria for selecting plausible candidates. The discovery rates of the *Roman* Space Telescope Green et al. (2012), estimated with the image multiplicity method, are 9-56 Ias and 17-126 core collapse SNe a year, depending on the observing strategy Pierel et al. (2021). The majority of the lensed core collapse SNe will be type IIn; however, this prediction is based on a relatively poor set of observed spectral templates of type IIn SNe and thus will likely be a subject to further improvement in the future. Gravitationally lensed SNe appear as peculiarly bright (relative to type Ia brightness at redshift of the apparent host galaxy) and multiply imaged sources. These are the two main observational properties which can be used to select plausible glSN candidates. Novel techniques can be employed to help identify glSNe with partially blended images, such as neural networks trained on time series of images (Ramanah et al., 2021; Morgan et al., 2021). Another strategy for finding glSNe is to monitor known lensed galaxies (Craig et al., 2021). Precise measurements of gravitational time delays will strongly rely on follow-up observations compensating insufficient cadence of large transient surveys Huber et al. (2019).

Gravitationally lensed quasars and supernovae are highly complementary. In the remainder of this section we compare the pros and cons of each variable source and conclude by highlighting the common challenges. Firstly, lensed quasars are around 60 times more numerous than lensed supernovae Oguri and Marshall (2010). In terms of the variability, supernovae (especially type Ia) have welldescribed light curves that can be fit with established templates, while quasars are characterized by a stochastic variability. Another important difference between gISNe and lensed quasars is that supernovae fade away over time. This poses a challenge, since follow-up observations are highly time-sensitive, but it also offers an advantage, as it allows for better kinematic follow-up observations of the lens and host galaxy once the supernova has faded away (Ding et al., 2021). Such velocity dispersion measurements can help constrain the mass sheet degeneracy, which is a transformation of the potential that leaves all imaging observables the same, while changing the time delays Falco et al. (1985); Gorenstein et al. (1988); Saha et al. (2000). Type la supernovae offer another way of breaking the mass sheet degeneracy: their standard candle nature can provide an estimate of the absolute magnification Foxley-Marrable et al. (2018); Birrer et al. (2022). However, it is worth noting that these constraints depend on the precision of type Ia SN standardisation, as current samples still yield intrinsic scatter in the Hubble diagram of around 0.12 mag (or 6 % in distance) Scolnic et al. (2018). The utility of the standard candle nature of lensed type Ia SNe can also be limited by the effect of microlensing, which gives rise to extra stochastic magnifications in every lens image Yahalomi et al. (2017). Another difference is that gISNe typically have a smaller angular size and smaller image separations than lensed quasars, due to the lower mean redshifts of gISNe. Therefore, lensed SNe are prone to have very short time delays, of the order of several days or weeks. This means that time-delay measurements only require weeks of follow-up observations instead of year-long monitoring campaigns as is usual for lensed quasars. However, obtaining precise measurements of such short time delays can be highly challenging. The small angular size of gISNe also leads to a higher sensitivity to microlensing from stars and other substructures in the lens galaxy. Microlensing can perturb light curves independently in each supernova image, which can lead to additional systematic errors in time delays of order 4% Goldstein et al. (2018). Fortunately, effects of microlensing can be minimised if multi-colour follow-up observations are obtained of the initial phase of the explosion. In this phase, the SN can be approximated as a point source and thus look identical in every filter, which leads to the same microlensing distortion across all wavelengths. This "achromatic" phase is expected to last until 3 rest-frame weeks after the explosion Goldstein et al. (2018); Huber et al. (2019), in which 70% of Rubin/LSST gISN Ia images will be discovered. The useful implications are that the microlensing effects are expected to cancel out in early time colour curves, reducing the systematic uncertainties to 1% for typical Rubin/LSST systems Goldstein et al. (2018). Since microlensing is capable of altering the brightness of the multiple images, thereby changing whether they fall above or below our detection limits, it could impact the number of glSNe and lensed quasar we will be able to observe.

For both types of variable sources, the precision and accuracy of the inferred cosmology will likely not be limited by sample size but by the quality of follow-up data and systematic uncertainties associated with the analysis. Most of these are common between lensed quasars and supernovae. In addition to the time delays themselves, that will likely required dedicating monitoring capabilities to supplement the cadence of the survey themselves, e.g. through a dedicated 3-4m class telescope, the cosmological inference requires: i) angular resolution images at resolution of 10mas or better; ii) spatially resolved kinematics of the deflector galaxy or cluster galaxies to break the mass sheet degeneracy and the mass anisotropy degeneracy Birrer et al. (2020); Xu et al. (2012); iii) information about the structure along the line of sight. Whereas the information about the mass along the line of sight will likely be provided by the same surveys used for the discovery of the targets, in combination with high precision next generation cosmological simulations, the high angular resolution imaging and spatially resolved kinematics can only be obtained with the James Webb Space Telescope or the next generation of extremely large telescopes.

With proper follow-up, time delay cosmography will be able to deliver measurements of the Hubble constant with a precision and accuracy of $\sim 1\%$, independent of all other methods, contributing to the resolution of the Hubble tension (e.g., Birrer and Treu, 2021).

9.1.7. Gravitational wave cosmology

It took almost 100 years for the prediction of gravitational waves to finally be directly confirmed Abbott et al. (2016). Since the first detection of gravitational waves in 2015 by LIGO-Virgo Scientific Collaboration Abbott et al. (2016), 90 events from compact object binary mergers have now been observed by the network of LIGO-Virgo detectors Abbott et al. (2021c), and the field of GW astronomy is exploding.

The third generation ground-based interferometers (such as Cosmic Explorer Reitze et al. (2019); Evans et al. (2021), Einstein Telescope Maggiore et al. (2020)) as well as space based gravitational wave detectors (e.g. LISA Amaro-Seoane et al. (2017), TianQin Luo et al. (2016), Taiji Hu and Wu (2017), and DECIGO Kawamura et al. (2021)), scheduled for the next decade, will open an even broader spectrum of gravitational-wave sources, providing novel cosmological probes with great precision. Also, possibly operating in conjunction, these experiments can improve our ability to investigate fundamental physics with GWs. In what follows, some perspectives on GWs for cosmology are presented.

In the next decade, gravitational wave standard sirens (GWSS) Schutz (1986); Holz and Hughes (2005); Dalal et al. (2006); Chen et al. (2018); Di Valentino et al. (2018b); Vitale and Chen (2018); Palmese et al. (2019), the GW analog of astronomical standard candles, are expected to play an important role in the context of cosmology. The amplitude of GWs is inversely related to the luminosity distance from the source, hence they can be used in conjunction with redshift information to the source to probe the distance-redshift relation. Observations of the merger of the binary neutron-star system GW170817, along with the redshift from its host galaxy, identified thanks to the observation of an electromagnetic counterpart, yield $H_0 = 70^{+12}_{-8} \text{ km s}^{-1} \text{ Mpc}^{-1}$ at 68% CL Abbott et al. (2017b). Though this constraint is broad, it does not require any cosmic "distance ladder" and is model-independent: the absolute luminosity distance is directly calibrated by the theory of general relativity Schutz (1986). In other words, GWSS of this kind are an ideal independent probe to weigh in on the Hubble tension problem. Around 50 additional observations of GWSS with electromagnetic counterparts are needed to discriminate between *Planck* and R19 measurements of H_0 with a precision of 1–2% Nissanke et al. (2013); Chen et al. (2018); Mortlock et al. (2019). Measurements of this kind can also play an important role in an extended parameter space Di Valentino and Melchiorri (2018); Di Valentino et al. (2018b) in which CMB data are unable to strongly constrain H_0 , in a way that breaks degeneracies amongst parameters. Standard sirens with EM counterparts are therefore expected to be extremely powerful cosmological probes, while the upgrades to the LIGO-Virgo second generation design sensitivities are critical to provide the above desired number of BNS merger detections.³⁹ On the other hand, kilonovae associated with BNS mergers are expected to be close to isotropic, and are thus the most promising of all BNS EM counterparts. However, the kilonova associated with GW170817 was intrinsically faint, and nonetheless was thought to be on the bright end of the kilonova luminosity function. In order to provide new associations, and hence a standard siren measurement that is informative for the Hubble tension, deep optical-to-near-infrared observations will be required to identify the fainter kilonovae, with more precise GW localizations playing a significant role in the success of these follow-up campaigns. Multi-object spectroscopic observations could play a central role in these campaigns through rapid classification of all the viable variable objects in the GW localization regions, which is currently a bottleneck for the identification of counterparts from imaging observations. Experiments such as DESI-II Dawson et al. (2020) could design a specific program aimed at standard siren cosmology through the identification of counterparts and observation of transients host galaxies' redshifts, along with other key science projects.

Complementary dark GWSS (GW sources without EM counterparts) such as those used in Ref. Fishbach et al. (2019); Palmese et al. (2020); Abbott et al. (2021d); Palmese et al. (2019) are expected to provide percent-level uncertainty on H_0 after combining a few hundreds to thousands of events from the statistical host identification technique Gray et al. (2020) or by identifying the host galaxy for the nearby sources Borhanian et al. (2020) using upgraded detector network in the future. In this case, a galaxy catalog overlapping with the GW events is necessary to provide the redshift information of the potential host galaxies. The implementation of this method depends on the completeness of the galaxy catalog up to high redshift, understanding the GW sources population, and better sky localization error of the GW sources. In order to avoid any biased measurement of the Hubble constant H_0 Trott and Huterer (2021), a promising approach can be to use the statistical host identification technique as demonstrated by Fishbach et al. (2019); Gray et al. (2020); Palmese et al. (2019, 2020); Abbott et al. (2021d). Another promising method to infer cosmological parameters from dark GWSS consists in crosscorrelating GW sources with photometric or spectroscopic galaxy surveys to infer the clustering redshift of the GW sources Oguri (2016); Mukherjee and Wandelt (2018b); Scelfo et al. (2018); Mukherjee et al. (2020b, 2021a); Bera et al. (2020); Scelfo et al. (2020); Diaz and Mukherjee (2022); Mukherjee et al. (2022). The cross-correlation technique is a promising avenue to achieve a 2% measurement of the Hubble constant from the LIGO-Virgo-KAGRA network operational in its design sensitivity in synergy with galaxy surveys such as SPHEREx and DESI Diaz and Mukherjee (2022) after combining a few hundreds of well-localised GW sources. Moreover, this technique will also make it possible to measure the DE EoS and the connection between GW sources and dark matter from dark standard sirens. Though the implementation of the cross-correlation does not require the host galaxy of the GW source to be present in the catalog, its success will depend on the availability of GW sources with better sky localization error. This may be feasible by using multiple detectors, overlapping galaxy surveys with accurate redshift estimation, and marginalization over the redshift-dependent GW bias parameters Mukherjee et al. (2021a); Diaz and Mukherjee (2022); Mukherjee et al. (2022). It follows that for the success of dark GWSS appropriate full sky galaxy catalogs that cover the redshift range of GW sources are required. Alternatively, it is possible to use features in the mass spectrum of binary black holes to infer redshift, providing a powerful and independent standard siren probe of cosmology Chernoff and Finn (1993); Farr et al. (2019); Ezquiaga and Holz (2021); Mukherjee (2021); Abbott et al. (2021d); Ezquiaga and Holz (2022). These "spectral sirens" may provide percent-level constraints on the expansion history at $z \sim 1$ and beyond. However, for this technique to work, the mass distribution of the GW sources need to be standardised. Any redshift evolution Mukherjee (2021) of the GW mass distribution needs to be mitigated in order to avoid any systematic error in the inference of the cosmological parameters. Another dark siren approach is to use knowledge of the EoS of neutron stars to infer redshift. For third-generation detectors, this would allow us to use these systems as

³⁹ Cosmic Explorer and Einstein Telescope are expected to observe far more binary neutron star mergers.

standard sirens to constrain cosmology even in the absence of an electromagnetic counterpart Messenger and Read (2012); Chatterjee et al. (2021). Space-based, low-frequency GW detectors such as LISA may observe well-localized GW signals from SMBH binary mergers with EM counterparts. Depending on uncertainties in SMBH formation models and EM emission mechanisms, these SMBH standard sirens could provide useful constraints on the Hubble constant, Ω_M and Ω_{Δ} up to $z \sim 8$ Tamanini et al. (2016).

Since standard sirens can be detected at cosmological redshifts, they can be sensitive to other cosmological parameters besides H_0 such as Ω_m and w(z). As would be the case for any other probe, should one assume a specific model that were not true (e.g. Λ CDM), then the inferred parameters from that assumed model would be biased relative to the true ones. In the case of cosmological standard sirens that extend to $z \sim 1.0$ the bias on the inferred cosmological parameters exceeds 3σ when the true model was a Chevallier – Polarski – Linder parameterization (CPL) Chevallier and Polarski (2001); Linder (2003) model that is consistent with current SN constraints Shafieloo et al. (2020). The biases that arise from assuming the wrong model can be mitigated, however, with the use of model-independent statistics such as Gaussian process regression Keeley et al. (2020b). Because of their high redshifts, some GW sources are expected to be strongly lensed Wang et al. (1996); Oguri (2018); Li et al. (2018b); a catalog of multiply-imaged sources, and associated lensing rates, time-delays, and magnification distributions, may provide additional cosmological constraints Oguri (2018); Xu et al. (2021a).

In the next decade, GWSS are expected to provide strong constraints on dark energy, modified gravity, dark matter and neutrinos, and shed light on several other important aspects in cosmology Cai and Yang (2017); Pardo et al. (2018); Du et al. (2019); Yang et al. (2020f); Wei (2018); Zhang et al. (2019a); Wang et al. (2018b); Zhang et al. (2020); Qi et al. (2019); Yang et al. (2019); Fu et al. (2019); Yang et al. (2019); Y

The physical degrees of freedom of GWs are imprints of the nature of gravity, and by modifying general relativity (GR), we have two major possibilities that can modify and leave fingerprint in the GW signal.

- Propagation Effects: A common feature in almost all gravity theories beyond GR, considering the Universe on large scales, is that the new degrees of freedom in each theory modify the gravitational force/interaction on cosmological scales, mainly to explain the late-time acceleration of the Universe (dark-energy-dominated era). This roughly corresponds to an effective time-varying gravitational constant that will affect the propagation of GWs along the cosmic expansion, which in turn can induce amplitude and phase corrections on the GW signal over cosmological volumes Cai and Yang (2017); Pardo et al. (2018); Du et al. (2019); Yang et al. (2020f); Wei (2018); Zhang et al. (2019a); Wang et al. (2018b); Zhang et al. (2020); Qi et al. (2019); Yang et al. (2019j); Fu et al. (2019); Yang et al. (2019 al. (2020g); Bonilla et al. (2020); Cutler and Holz (2009); Nishizawa et al. (2010, 2011); Yagi (2013); Nunes et al. (2019a); Cai et al. (2018b); Saltas et al. (2014); Nishizawa (2018); Belgacem et al. (2018a,b); Arai and Nishizawa (2018); Belgacem et al. (2019a); Lagos et al. (2019); Nunes et al. (2019b, 2018); Belgacem et al. (2019b); D'Agostino and Nunes (2019); Gao and Hong (2020); Belgacem et al. (2019c); Calcagni et al. (2019); Dalang et al. (2020); Wolf and Lagos (2020); Nunes (2020); Baker and Harrison (2021); Mitra et al. (2021); Mastrogiovanni et al. (2021a); Mukherjee et al. (2021b); Heisenberg et al. (2022a,b); Lee et al. (2022). The effective time variation of the gravitational constant could be measured with a few percent precision using a multi-messenger Engel et al. (2022) approach exploiting the unique relation between the GW luminosity distance, BAO angular scale and the sound horizon at decoupling Mukherjee et al. (2021b). We may also be able to test the propagation effect from gravitational lensing of GW sources Holz and Wald (1998); Mukherjee et al. (2020bc); Ezquiaga and Zumalacárregui (2020); Ezquiaga et al. (2021); Finke et al. (2021), which will provide new tests of general relativity Bettoni et al. (2017); Brax et al. (2017); Belgacem et al. (2018a); Bonilla et al. (2020).
- Generation Mechanism: By changing the gravity interaction in the inspiral-merger-ringdown phases, we also change the generation mechanism of the gravitational radiation emitted by the binary systems. Such methodology can be quantified through the parameterized post-Einsteinian framework Yunes and Pretorius (2009); Cornish et al. (2011); Carson et al. (2020); Carson and Yagi (2020). Future ground-based and LISA observations can lead to improvements of 2-4 orders of magnitude with respect to present constraints, while multiband observations can yield improvements of 1-6 orders of magnitude Perkins et al. (2021).

An interesting and realistic approach might be to combine both effects on the waveform signal modelling. Some specific theoretical cases of these effects were recently investigated using the LIGO-Virgo-KAGRA GW Transient Catalog Abbott et al. (2019c, 2021b). On the other hand, searching for polarization modes beyond the GR prediction provides a strong test of GR. This aspect can also be combined with the above mentioned effects. At a local level, the GW information from isolated or binary systems in the strong space-time curvature regime also provides several tests of GR Berti et al. (2015). The improvement in amplitude of the spectral noise density in future detectors will be fundamental to investigate the limits of these theoretical aspects.

Another interesting possibility is the detection of *stochastic gravitational waves*. Direct evidence of GWs has thus far been in the form of coherent measurements of resolved waveforms in processing the detected signals, which can be traced back to their origin as single points. Consequently, only a tiny fraction of these GW can be seen from a presumably much larger population spread throughout space at different scales. The extensive set of unresolved signals corresponding to multiple point sources or extended sources increases incoherently, leading to gravitational-wave backgrounds (GWBs). A variety of different backgrounds is expected, given the range of diverse GW sources in the Universe. Most of these backgrounds are treated as stochastic, as they may be described by a non-deterministic strain signal and are hence referred to as stochastic gravitational-wave backgrounds (SGWBs). Indeed, the existence of a SGWB is a robust prediction of several well-motivated cosmological and astrophysical scenarios operating at both the early and late Universe Maggiore (2000); Caprini and Figueroa (2018); Giovannini (2020). Below we present some of the most prominent observational projects to detect the SGWB across a broad range of frequencies of the GW spectrum.

• *Very low frequencies*. Cosmic inflation is currently the leading paradigm to explain the initial conditions of our Universe. Single-field slow roll inflation, as well as alternative treatments Benetti et al. (2021b); Myrzakulov et al. (2015); Odintsov et al. (2022); Cannone et al. (2015); Graef and Brandenberger (2015); Ricciardone and Tasinato (2017); Graef et al. (2017); Baldi et al. (2005); Dimastrogiovanni et al. (2017); Obata (2017); Cook and Sorbo (2012); Mukohyama et al. (2014); Cai et al. (2016c, 2021c); Stewart and Brandenberger (2008); Brandenberger et al. (2014); Hipolito-Ricaldi et al. (2016); Kinney et al. (2019); Odintsov et al. (2020); Odintsov and Oikonomou (2020); Trivedi (2020); Oikonomou (2021), predict the existence of a SGWB. Such GWs induce a B-mode pattern in the polarization of the CMB. From the lack of a detection of primordial B-modes, CMB observations place upper limits on the amplitude

of the primordial GW power spectrum Ade et al. (2018); Aghanim et al. (2020b). For an angular resolution scale of $k \leq 0.1 \text{ Mpc}^{-1}$, these limits can be translated into limits on the amplitude of the SGWB for frequencies $f \leq 10^{-16}$ Hz. Current ground-based CMB experiments—ACT Aiola et al. (2020), BICEP/Keck Ade et al. (2018), CLASS Harrington et al. (2016), POLARBEAR/Simons Array Suzuki et al. (2016), SPT Sayre et al. (2020) —measure the CMB polarization to high precision and will continue to better constrain primordial B-modes. Upcoming experiments, like Simons Observatory Ade et al. (2019) and CMB-S4 Abazajian et al. (2019a, 2022), will achieve even greater sensitivity. In addition, satellite missions such as LiteBIRD Allys et al. (2022) and balloon missions such as SPIDER Gualtieri et al. (2018) will complement ground-based efforts.⁴⁰

• *Low frequencies.* The high-precision timing of Galactic millisecond pulsars enables a search for nHz GWs, which are expected to be generated primarily by SMBH binaries. A GW transiting through the line of sight between Earth and the pulsar distorts the intervening spacetime, altering the expected time of arrival of pulses. A SGWB affects the timing of all pulsars in the Galaxy, causing spatially correlated time-delay signals between pulsar pairs, known as Hellings-Downs correlations Hellings and Downs (1983). These correlations are primarily quadrupolar, with subdominant contributions from higher multipoles, and are distinct from two main sources of spatially-correlated noise, errors in the terrestrial time standard (monopolar) and errors in the planetary ephemeris (dipolar) Sazhin (1978); Detweiler (1979); Foster and Backer (1990); Brazier et al. (2019); Alam et al. (2021b). World-wide efforts to search for a SGWB are underway: the North American Nanohertz Observatory for Gravitational Waves (NANOGrav) Arzoumanian et al. (2020), the Parkes Pulsar Timing Array (PPTA) Hobbs (2013); Kerr et al. (2018), all operate both individually and as a collective under the International Pulsar Timing Array (IPTA) Perera et al. (2019). Recent evidence of a common-spectrum process has provided intriguing hints that a detection may be soon to come, but observing the Hellings-Downs spatial correlation will be key to interpreting any signal as a possible SGWB detection Arzoumanian et al. (2020); Goncharov et al. (2021); Chen et al. (2021b).

Distortions of spacetime affect not only the timing of pulsars, but also induce a shift in the apparent position of stars. These shifts may be observed in astrometric surveys Braginsky et al. (1990); Kaiser and Jaffe (1997) for GWs in the frequency range 10^{-18} Hz $\lesssim f \lesssim 10^{-8}$ Hz. Similar to PTAs, the shifts also exhibit particular angular correlations from a SGWB Book and Flanagan (2011). Indeed, there are expected cross correlations between PTAs and astrometric shifts that could permit complementary studies Mihaylov et al. (2018); Qin et al. (2019a); Mihaylov et al. (2020); Qin et al. (2021). Astrometric data from GAIA and extragalactic radio sources have set constraints on the energy density of the SGWB Darling et al. (2018). Future missions such as Theia could provide improved sensitivity Boehm et al. (2017).

- Intermediate frequencies. The GWs are emitted mainly by individual binary systems, like, for instance, from binary black holes (BBH), binary neutron stars (BNS), and binary black hole-neutron stars (BBH-NS). The superposition of the signal from these sources over cosmological volumes is expected to form an SGWB of astrophysical origin. This signal strongly depends on the sources that produce them, and we expect that signal to exist in the most diverse frequencies (in this case, for example $10^{-3} \ge f \ge 10^2$) Zhu et al. (2013); Mingarelli et al. (2019); Jenkins et al. (2018). Nevertheless, this specific type of signal has not been detected until the present moment, and only some upper limits on the SGWB signal have been obtained, for instance, the LIGO-VIRGO-KAGRA collaboration reported an astrophysical background with amplitude $< 4.8 \times 10^{-8}$ Abbott et al. (2019d). With the improvements in instrumental sensitivity in the coming years and the prospects of future detectors like the Einstein Telescope (ET) Maggiore et al. (2020), Cosmic Explorer (CE) Reitze et al. (2019), and LISA Amaro-Seoane et al. (2017); Caprini et al. (2019), it is expected to achieve enough sensitivity to detect SGWBs of astrophysical origin.
- *Ultra-high frequencies*. Recently, IPTA gave hints of GWs from cosmic strings Antoniadis et al. (2022), which has further encouraged the community to build a strong case for experiments that can tackle ultra-high-frequency gravitational waves (UHGW). This is because, on the one hand, cosmic strings are a great scenario that can be analyzed in the multiband frequency range and hence with experiments already covering the low, medium, and high-frequency range (e.g., PTA experiments, LISA and LIGO-Virgo-KAGRA, respectively). Further experiments that can cover the MHz to GHz region are missing. Their construction could then complement the study of cosmic string signals in the broadband frequency range. On the other hand, SGWB due to cosmic origin, for example, from inflation models, from the evaporation of primordial black holes or phase transitions generated when Grand Unified Theories break into the SM or other subgroup can have signals in the MHz to GHz range. Hence, the current GW experiments will not be able to detect them. Different initiatives are being carried out to promote the creation of a network of researchers to develop the science of GW's in the frequency range above 10 kHz.⁴¹

Finally, several authors have pointed to the implementation of GW standard sirens and GW stochastic backgrounds to explore the late and early Universe, in a broad spectrum of possibilities ranging from the Hubble tension Li and Shapiro (2021) through the search for modified gravity Nunes (2020); Allahyari et al. (2021), variation of the speed of propagation of GWs Bonilla et al. (2020), inflation models Li and Shapiro (2021) and even explore the exotic fundamental physical possibility as the variation of fundamental constants Nunes et al. (2017); Colaço et al. (2022).

9.1.8. 21 cm cosmology

Up to now, the key probes of large-scale structure in the Universe have been based on galaxy surveys, and the upcoming generation of these surveys promises to deliver a revolutionary advance in precision cosmology. Next-generation galaxy surveys will be complemented by a new type of survey, which will map the 21 cm emission line of neutral hydrogen (HI) in the post-reionization era ($z \leq 6$). The 21 cm emission of galaxies that contain HI provides a tracer of the dark matter distribution, with extremely precise redshift measurement as a direct by-product of detection. However, the faintness of the emission means that next-generation HI galaxy surveys with SKAO-MID will not be competitive with contemporaneous spectroscopic surveys in the optical/ infra-red bands, although they will provide valuable complementary information and help to deal with systematics at low redshift Bacon et al. (2020).

⁴⁰ See Ref. Caldwell et al. (2022) for a study of the potential of using an early Universe GW signal to probe fundamental physics.

⁴¹ Go to this home page, for example: http://www.ctc.cam.ac.uk/activities/UHF-GW.php.

An alternative approach foregoes the detection of individual galaxies and measures instead the integrated emission from all galaxies in each 3-dimensional pixel. 21 cm intensity mapping in principle allows for spectroscopic surveys with high effective number densities, that can measure large-scale fluctuations in huge cosmological volumes, over reasonable observing times Bull et al. (2015b); Villaescusa-Navarro et al. (2018); Bacon et al. (2020). So far the signal has only been detected in cross-correlation with existing galaxy samples Chang et al. (2010); Masui et al. (2013); Wolz et al. (2022); Amiri et al. (2022), and upper limits on the power spectrum have been set by data from GBT Switzer et al. (2013) and uGMRT Chakraborty et al. (2021). Next-generation 21 cm intensity mapping surveys are capable of producing very high precision measurements of redshift-space distortions and BAO (e.g. Santos et al. (2017); Bacon et al. (2020); Castorina and White (2019); Cunnington et al. (2020); Kennedy and Bull (2021); Abdalla et al. (2021); Sailer et al. (2021); Costa et al. (2021), provided that effective foreground-cleaning techniques are developed for the data pipeline.

These foregrounds are orders of magnitude larger than the signal, but their different properties can be exploited to separate them with various cleaning techniques. In addition to foregrounds, other sources of contamination, such as polarization leakage, 1/f noise, and radio frequency interference (RFI), need to be precisely understood for the pipeline construction. Currently major efforts are underway, in particular those based on recent measurements with CHIME Amiri et al. (2022) and MeerKAT Wang et al. (2021); Li et al. (2021c); Matshawule et al. (2021); Cunnington et al. (2021a), the 64-dish precursor of the SKAO-MID telescope array that will have 197 dishes upon completion. Other current work includes an SKAO blind foreground subtraction challenge Spinelli et al. (2021), and methods preparing for science operations of OWFA Chatterjee et al. (2020), HIRAX Crichton et al. (2022) and BINGO Fornazier et al. (2021).

The interferometer arrays CHIME and HIRAX, and the large single-dish telescope BINGO are designed for cosmological constraints, especially via BAO measurements. By contrast, SKAO-MID (and its precursor MeerKAT) were not designed for cosmology, but in fact forecasts show that SKAO-MID could deliver competitive constraints from a 21 cm intensity mapping survey $(0.3 < z < 3 \text{ and } 20,000 \text{ deg}^2)$ in single-dish mode Bacon et al. (2020). In particular, the combination of the huge volume of an SKAO 21cm intensity mapping survey with next-generation galaxy and CMB surveys can potentially provide the tightest constraints on local primordial non-Gaussianity, using the multi-tracer technique Alonso and Ferreira (2015); Fonseca et al. (2015); Bacon et al. (2020); Ballardini et al. (2019); Viljoen et al. (2021) (the multi-tracer also provides tight constraints on neutrino mass using only linear scales Ballardini and Maartens (2022)). Interferometer arrays such as HIRAX (and the futuristic PUMA) are better suited to constrain other forms of primordial non-Gaussianity, using the power spectrum and bispectrum Karagiannis et al. (2020). The 21 cm intensity bispectrum is an important tool for cosmology with next-generation surveys, in interferometer or single-dish mode Sarkar et al. (2019); Durrer et al. (2020); Jolicoeur et al. (2021); Cunnington et al. (2021b).

Cross-correlation of upcoming 21 cm intensity maps with photometric galaxy samples can deliver measurements of weak lensing magnification Jalilvand et al. (2020); Witzemann et al. (2020). In addition, this combination can be used to calibrate photometric redshifts through the clustering signal (Alonso et al., 2017; Cunnington et al., 2019; Guandalin et al., 2021), potentially reducing one of the most significant systematic uncertainties in weak lensing experiments. Cross-correlation with a spectroscopic galaxy survey offers the exciting prospect of reconstructing the large-scale modes lost to foreground cleaning from their coupling to measured small-scale modes Modi et al. (2021).

9.2. Potential probes of the Universe

9.2.1. Quasars as geometric rulers

It has been a long pursuit to use quasars and active galactic nuclei (AGNs) for cosmology since the discovery of the first quasar 3C 273 in 1963. Most of the proposed approaches were found to be invalid or ineffective in the end. In recent years the situation changed thanks to the GRAVITY instrument onboard the Very Large Telescope Interferometer (VLTI), which provides an unprecedented spatial resolution down to 10μ as in near-infrared bands with the spectroastrometry (SA) technique. Such a high spatial resolution immediately led to successful measurements of the characterized angular sizes ($\Delta \theta_{BLR}$) of the broad-line regions (BLRs) in two quasars 3C 273 ($z \approx 0.158$, $\Delta \theta_{BLR} \approx 46 \pm 10 \mu$ as (Sturm et al., 2018)) and IRAS 09149-6206 ($z \approx 0.0573$, $\Delta \theta_{BLR} \approx 65^{+30}_{-39} \mu$ as (Amorim et al., 2020)), as well as inferences on angular distributions of the ionized gas in the BLRs. Complementary to SA that measures angular sizes, the well-established reverberation mapping (RM) technique measures linear sizes (ΔR_{BLR}) of BLRs of quasars and AGNs through detecting time delays ($\Delta \tau_{BLR}$) of variations between broad emission lines (BELs) and ionizing continuum, which transfer to BLR sizes simply as $\Delta R_{BLR} = c \Delta \tau_{BLR}$ (Blandford and McKee, 1982; Peterson, 1993), where *c* is the speed of light. The delays can be routinely measured by cross-correlation analysis of the observed light curves of BELs and continuum.

With SA and RM (SARM) observations, the angular-size distances of quasars and AGNs are then, in principle, directly determined by the geometric relation of

$$D_{\rm A} = \frac{\Delta R_{\rm BLR}}{\Delta \theta_{\rm BLR}} = 677.5 \,\Delta R_{20} \Delta \theta_{50}^{-1} \,\mathrm{Mpc},\tag{140}$$

where $\Delta R_{20} = \Delta R_{BLR}/20$ ltd and $\Delta \theta_{50} = \Delta \theta_{BLR}/50 \,\mu$ as (here ltd is the unit of light-day and μ as is 10^{-6} arcsecond). In practice, the spatial distributions of BLRs need to be taken into account to mimic real situations. The competitive advantages of the SARM approach for cosmic distances lies at: 1) it is fully free of extinction and reddening corrections, and 2) it also does not invoke standardized processes and calibrations of distance ladders.

The first SARM application had been made successfully on the quasar 3C 273 (Wang et al., 2020), which simultaneously yielded the angular-size distance $D_A = 551.50^{+97.31}_{-78.71}$ Mpc and the mass of the central supermassive black hole (SMBH) $M_{\bullet} = 5.78^{+1.11}_{-0.88} \times 10^8 M_{\odot}$, as well as the Hubble constant $H_0 = 71.5^{+11.9}_{-10.6}$ km s⁻¹ Mpc⁻¹ with a statistic error of ~ 15%. The second SARM application has been recently made by GRAVITY Collaboration (Amorim et al., 2021) on NGC 3783. Those analysis only employed the light curves of the continuum and BEL in the RM data and therefore is usually denoted as 1D SARM. As a comparison, 2D SARM analysis additionally employs profile variations of the BEL in the RM data and can make better use of the RM data. In particular, the 2D SARM analysis on 3C 273 carried out by Ref. (Li et al., 2022a) made use of the fact that H β (from RM data) and Pa α (from SA data) regions are gravitationally bound by the same potential of the SMBH and also share the inclination. As such, 2D SARM approach can naturally remove the systematical arising from the possible differences between the H β and Pa α line emission regions.

In general, the systematic errors in SARM analysis are composed of three major sources (see details in Wang et al., 2020). First, RM measures variable parts of the BLR over a monitoring period while SA measures snapshots of the whole BLR in a specific epoch. This raises a potential discrepancy between SA and RM measurements, leading to a systematic error. Fortunately, this issue can be tested by comparing the mean spectrum with the root mean square (RMS) spectrum of BELs. To be specific, if the two spectra have similar profiles and full widths half maximum (V_{FWHM}), the variable parts are consistent with the whole BLR and therefore the resulting systematics can be neglected. A similarity of the mean and RMS spectra was indeed found in 3C 273 (Zhang et al., 2019b). Second, complicated structure and dynamics of BLRs constitutes another important source of systematics, considering the simple BLR modelling in present SARM analysis. Most of AGNs with RM observations showed disk-like structures from wavelength-resolved delays (Grier et al., 2017). Multiple campaigns for one individual AGNs at different epochs can directly testify the underlying dynamics of the BLR through the $\tau_{BLR} - V_{FWHM}$ relation. It has been demonstrated that several AGNs follow $\tau_{BLR} \propto V_{FWHM}^{-1/2}$, implying a simple Keplerian rotation (Peterson, 2014). Third, currently RM campaigns are conducted in optical band whereas GRAVITY operates in near-infrared band so that their corresponding BELs are different. This issue can be resolved by directly mapping near-infrared BELs in RM or by implementing 2D SARM analysis as in Ref. (Li et al., 2022b). In a nutshell, all of the above systematics can be understood observationally.

In a few years, the next generation of GRAVITY, called GRAVITY+, will come available. It incorporates several key improvements with new technology and can detect much fainter quasars up to redshifts z = 2 - 3 (see detailed information about GRAVITY+). Moreover, the forthcoming Extremely Large Telescope has the inherent capability of doing spectroastrometry and therefore can also be employed for geometric measurements of cosmic distances. Recent Monte-Carlo simulations showed that the SARM approach is able to achieve a precision of 1 - 2% for the Hubble constant with about 100 AGNs (Songsheng et al., 2021). SARM campaigns to measure cosmic distances at the noon of the Universe for the history of cosmic expansion therefore have a high merit.

9.2.2. Redshift drift

In the standard cosmological model, a fixed observer will observe the redshift of objects of the Hubble flow to slowly change (or drift) systematically with time as the Universe expands ($\dot{z} \equiv \frac{dz}{dt_{obs}} \neq 0$) Sandage (1962); McVittie (1962). The drift at redshift *z* is related to the values of the Hubble parameter at that redshift, H(z), and today, H_0 , as McVittie (1962):

$$\dot{z}(z) = (1+z)H_0 - H(z).$$
 (141)

This can equivalently be expressed as acceleration, $\dot{v} = c\dot{z}(1+z)^{-1}$, where *c* is the speed of light and $\dot{v} \equiv \frac{dv}{dt_{obs}}$. The measurement principle is simple: one compares the redshifts of an object in the Hubble flow derived from multi-epoch observations, where the epochs are sufficiently separated in time so that the measurement uncertainty is smaller than the expected cosmological signal. A significant advantage of this experiment is that the signal grows linearly with time and the measurements are straightforward to interpret, requiring no assumptions about astrophysical processes (unlike standard candle measurements for example). Reconstructing $\dot{z}(z)$ is therefore a direct and model-independent way to measure the expansion history of the Universe Heinesen (2021c,a); Korzyński and Kopiński (2018) and can be used to constrain cosmological and dark energy models and extensions to GR Teppa Pannia and Perez Bergliaffa (2013); Martins et al. (2016); Heinesen (2021b). It is also independent of other cosmological probes, such as supernovae, the CMB, and large scale structure measurements so its contribution to cosmology is unique.

Within Λ CDM, \dot{z} depends on the densities of radiation, matter, and dark energy components in the Universe. Assuming $\Omega_m = 0.3$ and $\Omega_{\Lambda} = 0.7$, the value of \dot{z} reaches $+0.2 \,\mathrm{cm}\,\mathrm{s}^{-1}$ per year at $z \sim 1$ before becoming negative at z > 2. If, however, $\Omega_{\Lambda} = 0$, then \dot{z} is always negative and quickly grows more negative with increasing redshift, c.f. Fig. 2 of Ref. Liske et al. (2008). Redshift drift measurements can therefore provide an independent check on dark energy effects or other types of effects from alternative cosmologies. For example, the prediction of the scale invariant model of Ref. Maeder (2017) is similar to that of Λ CDM if $\Omega_m \approx 0.3$ but otherwise diverges significantly (Maeder, private communication). The most interesting prediction of Ref. Maeder (2017) (in the context of redshift drift) is that, if $\Omega_m < \infty$ 0.2, \dot{z} is positive at least until z = 5 – in stark contrast with the predictions of Λ CDM. In fact, this model does not require the presence of dark matter so Ω_m is expected to be $\ll 0.2$, in which case \dot{z} reaches at least $+1 \text{ cms}^{-1}$ per year at z = 3 and grows more positive with redshift.

New, advanced astronomical instrumentation is being built to perform the redshift drift measurement in the near future. The SKAO aims to measure the drift by monitoring up to 1 billion neutral hydrogen 21cm emission lines for galaxies at redshifts $z \le 2$ in the radio-frequency domain Klöckner et al. (2015), as first done for C3 273 Davis and May (1978). Similarly, the high-resolution optical/NIR spectrograph ANDES on the future Extremely Large Telescope aims to obtain \dot{z} measurements by monitoring up to one million absorption systems towards approximately a dozen bright quasar targets Maiolino et al. (2013). These optical measurements will probe redshifts z > 2 so are complementary to the SKAO ones. Exploratory studies have demonstrated that, for the required measurement precision to be reached, monitoring should last for more than 10 years Klöckner et al. (2015); Liske et al. (2008).

Observations of the 21cm line of neutral hydrogen for ten objects at $\langle z \rangle = 0.5$ over a period of 13.5 years found $\dot{z} = (-0.23 \pm 0.8) \times 10^{-8}$ or $\Delta v / \Delta t_{obs} = (-5.5 \pm 0.2) \text{ cm s}^{-1}$ per year, where the quoted numbers are averages over the ten objects Darling (2012). The uncertainty of this measurement is \sim 100 times larger than the expected signal, making it obvious that there is a long way until the required precision is reached in practice. Regarding the optical measurements, an important issue that must be solved relates to the wavelength calibration of the instrument. Instrumental calibration must be stable to a level comparable to the expected cosmological signal, that is several $cm s^{-1}$ per decade over the lifetime of the experiment. This level of precision is approximately equal to measuring the centres of absorption features with a relative precision of $\frac{\Delta\lambda}{\lambda} \sim 10^{-11}$ or only 3×10^{-10} m on the detector image plane – less than the separation between individual Si atoms of the detector. Novel calibration methods using Laser Frequency Comb technology have been demonstrated to provide this stability, but only over periods of several hours Milaković et al. (2020); Probst et al. (2020).

Additional systematic effects arise from variations of the point spread function of the instrument across the detector, variations in pixel sizes and sensitivities, and data reduction process. Significant further effort is therefore required to ensure the technical feasibility of the experiment. Another topic of ongoing research concerns identifying optimal methods for measuring the redshift drift from quasar spectra. It is currently unclear whether existing methods (e.g. cross-correlation) are sufficient or more advanced methods, based on absorption system modelling using artificial intelligence Lee et al. (2021a), are required. Data collected using existing ultra-stable, high-resolution spectrographs such as HARPS and ESPRESSO is expected to provide useful input.
9.2.3. Lunar astronomy

Lunar astronomy did not get a mention in the main text of the 2020 decadal review. Yet many of the goals of lunar astronomy overlap with traditional astronomy and high energy astrophysics. If our current decadal planning program does not get the ball rolling now for input into lunar telescopes, we expect that in the next decade the process will be more or less set in stone. There are many fields already vying for a slice of the lunar science pie. We need to penetrate new frontiers and open up new funding horizons that can best be achieved with unified planning. For large telescope projects, the planning should start now.

This is happening of course to some extent in the various lunar programs (NASA, China, ESA). But it is unfortunate that mainstream US astronomy planning (as exemplified in the recent Decadal Review) seems to be ignoring this potentially novel direction. Lunar telescopes are very much complementary to current and planned terrestrial and space projects.

The funding might come in part from lunar exploration resources. This joint approach would open up the prospect of building otherwise unaffordably large telescopes and open up new science frontiers that are otherwise unattainable. A low frequency radio interferometer on the lunar far side is certainly the first major project one might develop incrementally, in part because we have mastered most of the relevant technology and are already building terrestrial counterparts such as SKAO-LOW. This would explore one of the last remaining great frontiers, the Dark Ages, the epoch before the first galaxies, stars and massive black holes.

Farside Burns et al. (2021a,b) is a NASA probe-class proposal with 128 dipole antennae deployed over 10 km envisaged for the 2030s. The base station correlator would relay the signal to an orbiting lunar satellite, to be transmitted back to Earth. This could be a pilot project for a much larger lunar low frequency radio interferometer with millions of antennae.

Clearly advance planning of a road map is essential for such projects. But there is equally more to do in the realms of infrared and GW astronomy Harms et al. (2021).⁴² Planning for alternative lunar projects is required now while the lunar astronomy program is being developed. And the beauty of developing such studies is that the science case is very compelling and therefore very competitive. However there will be strong competition within the space agencies for lunar science projects. Support from the astronomical community could play a key role in advancing such telescopes.

The fact that this perspective is long term is not necessarily a disadvantage for astronomy. The perspective is no more long term than the key project in the decadal review Review (2022), a UV/optical/IR telescope for launch in 2045+. Or to give an example from a different field, high energy physics, the proposed 100 TeV proton accelerator for 2050+.

We emphasize that lunar telescopes can highlight frontier science that is unique and that no other proposed telescope can do. This includes unprecedented scope for exploration of the dark ages, probing the birth of the Universe and imaging of the nearest exoplanets. These represent the most adventurous and exciting cosmology and astronomy prospects of all. Lunar telescopes have potential for opening new science frontiers, and represent the new frontier of human space exploration.

There are many issues to be discussed Silk et al. (2021); Burns (2021); Chen et al. (2021e); Silk (2021); Morabito and Silk (2021); Adami and Farhat (2021); Maillard (2021); Labeyrie (2021); Schneider et al. (2021); Woolf and Angel (2021); Eads and Angel (2021); Crawford et al. (2021); Wedler et al. (2021); Heinicke and Foing (2021); Klindzic et al. (2021); Elvis and Milligan (2021), including how to discriminate the elusive science signals from pervasive low radio frequency and terahertz foregrounds, and handling the abrasive role of lunar dust. One can add imaging via mega-telescopes in dark and cold polar craters and making use of the seismic stability of the Moon for deployment of GW telescopes, using technology that dates back to, and goes far beyond, the Apollo-era era seismometers. We urge that a detailed planning effort be immediately initiated to examine the feasibility and competitiveness of such potentially break-through projects.

9.2.4. Cosmology with Gamma-ray bursts and fast-radio bursts

Gamma-Ray Bursts (GRBs) are spectacular events in high-energy γ -rays. Their peculiarity is that in a few seconds they can emit the same amount of energy that our Sun emits in its entire lifetime. Because they are the most powerful events in the Universe after the Big Bang they can be observed at very large distances up to redshift 9.4 (Cucchiara et al., 2011) and in principle up to z = 20 (Lamb, 2003), since they are practically free from dust extinction in their γ -rays.

Because they span over a large redshift range from z = 0.0085 with the closest GRB (GRB 980425) ever observed at a local distance and the largest redshift observed (z = 9.4) are very appealing candidates to map the evolution history of the Universe and to investigate cosmological parameters beyond the epoch of re-ionization. GRBs are in principle excellent candidates for being standard candles, however their luminosities and energies span over 8 - 9 order of magnitude from 10^{46} erg to 10^{55} erg, which can be contrasted with Supernova la (SNe Ia). However, similarly to SNe Ia, the Hubble diagram of GRBs is built using observed correlations between properties of the GRB light curve and the GRB luminosity, thus enabling the indirect measurement of a luminosity distance Demianski et al. (2017a,b); Dirirsa et al. (2019).

In this realm, there have been attempts to use GRBs as standard candles by several groups by using the above mentioned correlations among properties of the prompt (Amati et al., 2002; Yonetoku et al., 2004; Amati et al., 2008, 2019; Dirirsa et al., 2019) and the afterglow emission (Dainotti et al., 2008, 2010, 2011a,b, 2013, 2015a; Del Vecchio et al., 2016; Dainotti et al., 2016, 2017a,b; Dainotti and Del Vecchio, 2017; Dai et al., 2020; Srinivasaragavan et al., 2020; Dainotti et al., 2020a,b, 2021d,a).

More specifically, if we consider the prompt emission properties, one crucial variable is the observed photon energy of the peak spectral flux $E_{p,i}$. This quantity is observed to be correlated with the isotropic equivalent radiated energy E_{iso} through the so-called Amati relation (Amati et al., 2002). E_{iso} is written as follows:

$$n\left(\frac{E_{\rm iso}}{1\,\rm erg}\right) = b + a\ln\left(\frac{E_{p,i}}{1\,\rm keV}\right).$$
(142)

Here, E_{iso} is related to the cosmological the luminosity distance $(d_L(z))$ via

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⁴² An attractive idea for lunar astronomy consists in detecting gravitational waves from the Moon Harms et al. (2021); Jani and Loeb (2020) propose lunar GW detectors that would fill the gap in GW frequency between the LISA and the ground based detectors bands. Such experiments would be able to detect massive and intermediate mass BBH and stellar BBH and BNS inspirals, and they would therefore contribute to the GW cosmology probes explored in Section 9.1.7.

 $E_{\rm iso} = 4\pi d_I^2(z) S_{\rm bolo} (1+z)^{-1}$,

where S_{bolo} is the bolometric fluence, which is analogous to the observed brightness but in gamma rays. Thus measuring both $E_{p,i}$ and S_{bolo} from GRBs allows one to construct a Hubble diagram, with a given set of calibration parameters a and b. This process is completely analogous to constructing a Hubble diagram from SNe.

Regarding the use of GRB afterglow the crucial quantity, object of study, is the rest frame end time of the plateau emission, T_a^* which anti-correlates with the luminosity at the end of the plateau emission, L_a (Dainotti et al., 2008), which in turn correlates with the peak prompt luminosity, L_{peak} (Dainotti et al., 2011b, 2015b). Also here, the luminosity depends on the distance luminosity similarly as in Eq. (143).

However, the problem of using GRB relations as standardizable candles is that their errors are large compared to the relations used for SNIa, thus make GRBs less appealing. Indeed, GRBs as all sources observed at cosmological distances are hampered by the so-called Malmquist bias effects which allow us to detect only the brightest GRBs at high-z, and thus, we have a missing population of sources at low-z which are not detectable. In addition, we have to consider that the correlations which can be good candidates to be standardizable are also subjected to redshift evolution and selection biases. To overcome these problems we need to use reliable statistical methods such as the non-parametric methods Efron and Petrosian (1992) that can allow to define the slope of a given function which mimics the evolution. We can assume any function of the evolution such as a simple power law $(g(z) = (1 + z)^k)$ or a more complex one. Once the variables are corrected for the evolution and for selection biases we can then safely use these variables to determine if the correlations used for constraining cosmological parameters are due to the intrinsic physics or are due to the mere result of selection biases. If such evolutionary effects are not taken into account these can lead to a degeneracy in the cosmological parameter space which are induced by the biases rather than the underlying cosmology or to the physics of the correlations used. Another relevant point is that the correlation parameters even if they change for different cosmological setting, they sure must not change in a way which would change the physics of the underlying physics. For example if the so-called Dainotti relation in two dimensions can be interpreted within the magnetar model, than the slope of the correlation is expected to be 1 within 1 σ . For details on the topic of GRB correlations, on the selection biases they undergo and their application as cosmological tools see a series of review papers (Dainotti et al., 2015b, 2018; Dainotti and Del Vecchio, 2017; Dainotti et al., 2021b,c)

Recent works Rezaei et al. (2020b); Muccino et al. (2021); Demianski et al. (2020) have used the Hubble diagram of GRBs to constrain the expansion history of the Universe and to measure the properties of dark energy. These works rely on methodology developed earlier in Refs. (Cardone et al., 2009, 2010; Postnikov et al., 2014; Dainotti et al., 2013).

Besides the use of GRBs as cosmological tools, GRBs are similarly useful for tests of cosmic isotropy Ripa and Shafieloo (2017); Řípa and Shafieloo (2019) (see also Luongo et al. (2021)). Since these bright tracers are observed out to high redshift (0.0085 < z < 9.4), their distribution on the sky should be isotropic, should the Universe be. Using the Kolmogorov-Smirnov statistic *D*, Kuiper *V*, Anderson-Darling *AD*, and χ^2 statistic, three of the standard GRB catalogs *Fermi*/GBM *CGRO*/BATSE *Swift*BAT all show consistency with an isotropic distribution, both in terms of position on the sky and the properties of the GRBs.

Fast Radio Bursts (FRBs) are very bright (\sim Jy), brief ($\sim \mu$ s to \sim ms scale) transients, observed in the radio part of the spectrum. The first FRB was discovered in 2007 Lorimer et al. (2007) with many more discovered largely in archival data over the next decade. More recently, purpose built radio telescopes and arrays are on target to find thousands if not tens of thousands of bursts every year. Our understanding of the properties of FRBs is still evolving; it appears that many but not all repeat, with unknown possible periodicity, and it is likely that FRBs will eventually be categorised in classes based on some subset of their properties. Their other properties such as polarisation, rotation measures etc, are all still unknown as the observations do not all point to a single pattern and it is not always possible to disentangle host galaxy effects from propagation effects and intrinsic properties of the bursts. It does appear certain that they are found in host galaxies, and that they lie at cosmological distances Tendulkar et al. (2017), thus making FRBs potential candidates for cosmological measures as their propagation will probe the intergalactic medium, offering yet another tool to constrain cosmological parameters, for example Walters et al. (2018, 2019); Weltman and Walters (2019) and references therein.

The progenitor mechanism driving FRBs is not yet known though there are strong hints that at least some are driven by magnetars through one of many physical possible mechanisms. A full database of theories Platts et al. (2019), once outnumbered the observations, but as further observations occur, the possibilities for theoretical explanations shrinks and so it is likely that soon we will have only a handful of possible contenders remaining, perhaps matching future classes of FRBs.

There are a number of ways Fast Radio Bursts can be used as cosmological probes. Here we focus on a single application. After emission from the source, the photons from the burst travel to the observer through the intergalactic medium, and are slowed down as a function of their wavelength. The dispersion measure thus contains information about the distribution of electrons from the source to the observer,

$$DM \simeq \int \mathrm{d}l \, n_e \,, \tag{144}$$

where n_e is the number of electrons along the line of sight and the integral dl runs from the source to the observer. The quantity n_e contains cosmological information and indeed this simple equation combined with precision cosmology constraints from the early Universe allows us to make a prediction for the fraction of baryons in the intergalactic medium Walters et al. (2019), which can then be experimentally verified. Indeed, the so-called missing baryon problem is no longer an outstanding problem as the results of Ref. Macquart et al. (2020) used a handful of well located FRBs with the observed dispersion measures to show that the missing baryons are in the intergalactic medium and are playing the expected role of dispersing the FRB signal. This longstanding open problem is thus resolved not due to any great technological or theoretical breakthrough, but simply through the use of a few transient observations and an understanding of the contributions to the dispersion measure from our own galaxy. This brief example shows the power and potential use of FRBs as cosmological probes. There is immense and untapped potential for great discoveries with FRBs.

9.2.5. The forward physics facility at the high-luminosity LHC

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Signals from the Universe could play significant role in the development of particle physics Arkani-Hamed and Maldacena (2015). Likewise, collider experiments offer a unique environment in which to search for the direct production of DM and DE particles, since they

are sensitive to a variety of signatures and therefore to a wider array of possible DM and DE interactions with matter. Like other signals of new physics, DM and DE (if accessible at small scales) could manifest itself in high-energy particle collisions either through direct production or via modifications of electroweak observables induced by virtual DM/DE particles.

Future data to be collected at the CERN's LHC can make accurate microscopic determinations of the cross sections that are important for DM detection. On the one hand, these determinations could give evidence that the observed particle does in fact make up the DM. On the other hand, they could be useful for astrophysics in estimating the local density of DM and in mapping its distribution in the Galaxy.

The newly proposed LHC Forward Physics Facility (FPF), planned to operate near the ATLAS interaction point, offers a complementary new terrain to test some of the many proposed models to address the H_0 and S_8 tensions Anchordoqui et al. (2021e); Feng et al. (2022a). The FPF experiments to be operating during the LHC high-luminosity era will attain very large statistics to search for light and very weakly-interacting particles. The existence of such a light dark sector is predicted by many BSM models attempting to solve some of the biggest puzzles in fundamental physics, such as the nature of DM, the origin of neutrino masses, and the imbalance between matter and antimatter in the present-day Universe. New physics searches at the FPF would thus advance our understanding of the Universe on both the smallest and the largest distance scales.

9.3. Data analysis challenges

In recent decades, cosmology has established itself in the era of precision thanks to an interplay between theory, observation and statistics, where the latter has functioned as a glue for the first two, including highly refined numerical simulations. A large number of statistical methods have been developed to find a suitable way that can lead to answers to the most fundamental problems in this field. In this way, Bayesian methods have been widely used and they have been very successful, for example, in determining the main cosmological parameters that define the standard model of cosmology. However, the large amount of data that are extracted from current observational projects and its continuous increase in quantity and complexity, make the expected scientific return will be limited by the efficiency and sophistication of our statistical inference tools, which, if used improperly, can lead to biased or completely wrong conclusions Trotta (2017).

The present section will review some of the most recent and prominent developments in statistical techniques, focusing on the determination of cosmological parameters and specifically on the most relevant tensions, such as H_0 and S_8 , not pretending to give a concrete solution to this "hot topic", but trying to point to an alternative or independent analysis, given certain sets of astrophysical and cosmological data set that are at hand. The topics we have chosen cover only a small part of the current amount of statistical methods that we have at our disposal and are part of our opinion about what we believe is most relevant for the community of astrophysicists and cosmologists, at least for the next decade.

9.3.1. The inverse problem and inference in cosmology

The inverse problem in science is the process of estimating the causal factors that produced them from a set of experimental observations. In cosmology, given a set of observational data (SNe, CMB, BAO, LSS, among others), it is possible to calculate the value of the different parameters that characterize a specific model (i.e. the six parameters of Λ CDM),⁴³ and in this way extrapolate, for example to the past, to find the initial conditions that gave rise to the Universe that we can perceive in the present and that in some measure reproduces what we can observe today.⁴⁴ So the situation is "given a data set **x**, what is the range of physical parameters θ most probable?", and the answer to this question has traditionally been Bayesian statistics, determining the posterior probability distribution function (pdf) $p(\theta | x)$, that encapsulates the final state of information about the parameters θ starting from the prior $p(\theta)$ and including the full knowledge of the data **x** through likelihood and so on, the posterior is obtained via Bayes' theorem, methodology generally known as Bayesian inference. However, the combination of CMB and LSS through this methodology demands the calculation of the theoretical power spectrum, obtained from Einstein-Boltzmann Solvers such as CLASS Blas et al. (2011),⁴⁵ and CAMB,⁴⁶ and the use of Markov Chain Monte Carlo (MCMC) and/or Nested sampling algorithms to sample the posterior distribution and, in this way, the observables are obtained computationally. Afterward, a comparison between the predictions at different parameter space points with the available data is made and based on the likelihood, a best-fit of the parameters is determined. In general, this process is computationally expensive for theoretical models that include many parameters or contain "slow parameters",⁴⁷ since the Einstein-Boltzmann Solver is executed at each step in the parameter space.

9.3.2. Current developments

A promising approach for investigation of the cosmological parameters is to consider independent analysis of the physical model. In principle, this can be done via cosmographic approach Kristian and Sachs (1966); Ellis et al. (1985); Heinesen (2021d,a), which consists of performing a series expansion of a cosmological observable around z = 0, and then using the data to constrain the kinematic parameters. Such a procedure works well for lower values of z, but can be problematic at higher values of redshift; though see Cattoen and Visser (2007); Hu and Wang (2022) for strategies of analysing high redshift data with cosmographic approaches. Another possibility is to use the technique called *machine learning* (ML), which in addition, can help us with the automated analysis of the great flood of data that can be produced in some observational project. In general, machine learning can be understood as a set of methods that automatically detect patterns in the data and thus use the discovered patterns to predict specific characteristics of interest for our analysis. ML can be supervised or unsupervised: in the latter case we can find problems of clustering, dimensionality reduction, model selection and

⁴³ This base model can be treated in two groups: the *late-time* group formed by Ω_c , Ω_b , τ and Θ_{MC} , which trace the dynamic evolution of the background and the *primordial* given by A_s and n_s , that describe the initial conditions of the perturbations produced by quantum fluctuation during inflation.

⁴⁴ In general, this methodology is used in numerical N-body simulations, i.e., given the value of a set of parameters, it is possible to run a simulation from the past (high redshifts) and estimate how similar it is to what we can observe at present, at least statistically, for example, through the power spectrum of matter.

⁴⁵ http://class-code.net.

⁴⁶ https://camb.readthedocs.io/en/latest/.

⁴⁷ Most of them are late-time and delay the calculation of the power spectrum.

processing, among others. Regarding the first class (supervised), we can find classification or regression problems, of which only the last ones are of interest to us for the present work. Data sets such as CMB, BAO, SNe, CC, HOLiCOW, among many others, are perfect candidates to be used in supervised regression problems and thus of great importance to the community of astrophysicists and cosmologists. ML has been widely used in cosmology, both for regression and classification problems, in order to estimate the main cosmological parameters of the standard model and beyond Arjona and Nesseris (2020a); Munõz and Escamilla-Rivera (2020); Arjona and Nesseris (2020b), detect gravitational lens systems and detect low-mass binaries on X-rays Pearson et al. (2018); Pattnaik et al. (2021). In this subsection, we will deal with regression problems with ML (mainly focused on Gaussian Processes - GP, and Genetic Algorithms - GA) and deep learning (DL), being a subset of ML in which multilayered neural networks learn from the vast amount of data and what we will deal with in the BNNs paragraph. We will focus on the estimation of cosmological parameters, with special emphasis on H_0 and S_8 . The most prevalent techniques are then:

- Gaussian Processes (GPs): An interesting and robust alternative can be to consider a Gaussian process (GP) to reconstruct cosmological parameters in a physically model-independent way. The GP approach is a generic method of supervised learning (tasks to be learned and/or data training in GP terminology), which is implemented in regression problems and probabilistic classification. A GP is essentially a generalisation of the simple Gaussian distribution to the probability distributions of a function into the range of independent variables. In principle, this can be any stochastic process, however, it is much simpler in a Gaussian scenario and it is also more common, specifically for regression processes. The GP also provides a model independent smoothing method that can further reconstruct derivatives from data. In this sense, the GP is a non-parametric strategy because it does not depend on a set of free parameters of the particular model to be constrained, although it depends on the choice of the covariance function. The GP method has been used to reconstruct the dynamics of the DE, modified gravity, cosmic curvature, estimates of Hubble constant, and other perspectives in cosmology by several authors Seikel et al. (2012); Shafieloo et al. (2012); Seikel and Clarkson (2013); Zhang and Xia (2016); Busti et al. (2014); Sahni et al. (2014); L'Huillier and Shafieloo (2017); L'Huillier et al. (2018b); Belgacem et al. (2020); Pinho et al. (2018); Cai et al. (2017b); Haridasu et al. (2018); Zhang and Li (2018); Wang and Meng (2017d); Shafieloo et al. (2018b); Bengaly et al. (2020); Bengaly (2020); L'Huillier et al. (2020); Sharma et al. (2020); Nunes et al. (2020); Briffa et al. (2020); Bahamonde et al. (2021); Li et al. (2021a); Simon et al. (2005). Estimates of H_0 can be found in Refs. Liao et al. (2019); Gómez-Valent and Amendola (2018); Colgáin and Sheikh-Jabbari (2021a); Krishnan et al. (2021a) and a recent estimate yields a value of $H_0 = (73.78 \pm 0.84)$ km s⁻¹ Mpc⁻¹ constrained at 1.1% precision at 1 σ CL Bonilla et al. (2021a), using data from SNe, BAO, CC and HOLiCOW, developing a joint analysis, which was also used in Ref. Bonilla et al. (2021b) to estimate the interaction strength in a model of interaction between dark matter and dark energy (IDE), an analysis that also includes simulated data from GWs like standard sirens. Regarding σ_8 and/or S_8 measurements, authors report $S_8 = 0.707 \pm 0.085$, using selected Red Shift Space Distortion (RSD) data set in the form of $f\sigma_8(z)$ Benisty (2021). Recently, Ref. Avila et al. (2022) found the following estimates: $\sigma_8(z=0) = 0.766 \pm 0.116$, $S_8(z=0) = 0.732 \pm 0.115$ and $\gamma(z=0) = 0.465 \pm 0.140$ (growth index), using select independent data measurements of the growth rate f(z) and of $[f\sigma_8](z)$ according to criteria of non-correlated data.
- An alternative to Gaussian process is the iterative smoothing method introduced by Shafieloo et al. (2006); Shafieloo (2007); Shafieloo et al. (2018b). The idea is to start with an initial guess for the function to reconstruct, and convolve the residuals with a smoothing kernel. The resulting smooth function is then subtracted from the data at the next iteration to form new residuals, and reiterate for a given number of iteration. One can then vary the initial guess, and the reconstructions all converge to the same solution, which is thus independent from the initial guess and purely driven by the data. This method has been used to reconstruct the expansion history Shafieloo et al. (2006); Shafieloo (2007); L'Huillier and Shafieloo (2017); Shafieloo et al. (2018b); Koo et al. (2021a,b), test the curvature, to perform model-selection and parameter estimation L'Huillier and Shafieloo (2017); Shafieloo et al. (2018b); Koo et al. (2021b). Varying the initial guess makes the method less sensitive to the choice of the mean function in GP regression. However, the interpretation of the uncertainties is less straightforward than in GP regression.
- Genetic Algorithms (GA): The GA is an ML approach that can be used for unsupervised regression of data. Specifically, it allows for non-parametric reconstructions of data, using analytic functions of one or more variables. The GA is very loosely based on the idea of natural evolution, which is implemented via the genetic operations of crossover and mutation. In a nutshell, an initial set of randomly chosen functions evolves over time under the evolutionary pressure of the two aforementioned operators, namely mutation, i.e. a random change of the function, and crossover, i.e. the partial merging and swapping of parts of two or more functions of the population. This procedure is then iterated hundreds of times and with different random seeds, so as to explore the functional space and to ensure convergence. As the GA is a stochastic ML approach aiming to emulate evolution, the probability that a population of functions will obtain offspring, i.e. the next generation of functions, is taken to be proportional to its fitness to the data. The latter is usually measured by a χ^2 statistic, which determines how well every function agrees with the data. Then, the probability to have offspring and the fitness of each individual is proportional to the likelihood causing an "evolutionary" pressure that favours the bestfitting functions in every population, hence directing the fit towards the minimum in a few generations. The GA have been extensively used in cosmology for several reconstructions of a plethora of different data, see for example Refs. Bogdanos and Nesseris (2009); Nesseris and Shafieloo (2010); Nesseris and Garcia-Bellido (2012); Nesseris and García-Bellido (2013); Sapone et al. (2014); Arjona (2020); Arjona and Nesseris (2020b,a, 2021a,b); Arjona et al. (2021a); Arjona and Nesseris (2021c); Arjona et al. (2021c) and also to perform forecasts for the Euclid survey, see Refs. Martinelli et al. (2020, 2021); Nesseris et al. (2021). Similar applications of the GA have also been performed in related areas such as particle physics Abel et al. (2018); Allanach et al. (2004); Akrami et al. (2010), astronomy and astrophysics Wahde and Donner (2001); Rajpaul (2012); Ho et al. (2019).
- Bayesian Neural Networks (BNNs): Bayesian evidence method remains the preferred method compared with information criteria and GP in the literature. A full Bayesian inference for model selection –in the case we have a landscape in where we can discriminate a pivot model from a hypothesis– is computationally expensive and often suffers from multi-modal posteriors and parameter degeneracies. This latter issue leads to a large time consumption to obtain the final best fit for such parameters. As the study of LSS of the universe indicates, all our knowledge relies on state-of-the-art cosmological simulations to address several questions by constraining the cosmological parameters at hand using Bayesian techniques. Moreover, due to the computational complexity of these simulations, some studies look to remain computationally infeasible for the foreseeable future. It is at this point where computational techniques

as machine learning (ML) can have some important uses, even for trying to understand our universe. The idea behind the ML is based in consider a Bayesian Neural Network (BNN) with a complex combination of neurons organised in nested layers. And every layer of a neural network thus transforms one input vector –or tensor depending the dimension– to another through a differentiable function, e.g. the BNN can learn the distribution of the distance moduli in the dark energy models, then feed the astrophysical surveys to the network to reconstruct the dark energy model and then discriminate between models. With BNNs we can design numerical architecture cases in order to train data instead of simulate them. These kind of cases have been used in cosmology to train significant amount of information on several cosmological parameters without assuming a weight function as in comparison with GP regressions. Some interesting architectures have been treated in Escamilla-Rivera et al. (2020, 2021) in order to discuss dark energy models through parametrised equation of state. Also, it has been discussed the possibility to combine BNNs with MCMC methods to study anisotropies in the CMB data Hortúa et al. (2020b). As an extension, in Hortúa et al. (2020c) BNNs architectures were used to estimate parameters from the 21 cm signal and in Hortúa et al. (2020a) the method was extended to reconstruct the history of reionization.

We leave the reader free to expand their knowledge of the previous topics, specifically in applications such as deep learning (DL) Escamilla-Rivera (2020b), or iterative smoothing Shafieloo et al. (2006); Shafieloo (2007); Shafieloo and Clarkson (2010); L'Huillier and Shafieloo (2017); Shafieloo et al. (2018b); L'Huillier et al. (2018b); Koo et al. (2021b), which are totally related to the present discussion. However, Bayesian inference will not stop being used in the coming decades since it is the most suitable for treating data in astrophysics and cosmology, whether it is used in combination with maximum likelihood or minimum chi-square (which is more traditional) or with the most recent techniques of a machine learning like the ones presented here. We can only finish by giving suggestions and recommendations for its correct use in future projects, pointing to some persistent difficulties.

9.3.3. Checking the conventional Λ CDM assumptions for extended cosmology analysis

In response to the Hubble tension between late and early Universe measurements, a growing number of extended cosmological models beyond Λ CDM model have been proposed and examined (see Section 7). To obtain strong constraints on the model parameters and to explore their possible remedy to the tensions, many of these tests are done by combining published measurements from different surveys. However, the data analysis of current high-precision cosmological and astrophysical probes is complicated and uses many assumptions based on Λ CDM in the analysis pipeline to compress the large amount of data into limited degrees of freedom. Some of these assumptions are as obvious as the Λ CDM background geometry, while others are hidden in the details. The misuse of measured data based on Λ CDM assumptions on the beyond- Λ CDM models where these assumptions break down could result in misleading conclusions Barreira et al. (2016); Hill et al. (2020); Taruya et al. (2014); Macpherson and Heinesen (2021); Koksbang (2021). To combat this, theorists should be cautious when analyzing their models, and observers should be clear about the specific assumptions in published key paper results, if possible.

Strictly speaking, there is no clear-cut boundary between the statement of "doing your theoretical model predictions right" and the point of "alleviating the Λ CDM assumptions in the surveys". Here, the focus on the latter aims to elucidate the relatively-easy-to-check but profound technical details that are risky to be overlooked by the working groups using the publicly published and deeply post-processed cosmological/astrophysical survey results on their extended models.

9.3.3.1. Baryonic acoustic oscillation. Recently the impact of fiducial cosmology assumptions on BAO measurements are discussed in several papers Heinesen et al. (2019, 2020); Carter et al. (2020); Sherwin and White (2019). A standard methodology for the recent BAO analysis is to reconstruct the galaxy power spectrum in a fiducial cosmology, then extract the sharpened BAO features from the reconstructed galaxy over-densities Gil-Marín et al. (2016). In this way, the BAO feature that has been smeared by the bulk flow of the astrophysical objects is recovered. The paper by Carter et al. Carter et al. (2020) discussed the effect of fiducial cosmology assumption in the reconstruction process, and summarized three approximations that extended models should obey to avoid bias when using the fiducial BAO measurements. Among them, the first thing that we should pay attention to is the re-scaling of the redshift-distance relationship, at least on the scales relevant to the BAO survey. If the redshift-distance relationship rescaling is more complicated than a linear factor multiplication in the redshift range of the galaxy samples, the configuration space distortion introduced by placing the galaxy at wrong distance is likely be unable to be captured by the Alcock–Paczynski (AP) parameters. The other approximations are mainly related to whether the power spectrum template used in the BAO information compression is inclusive enough to mitigate the cosmology dependence. They need further detailed analytic or simulation validation per model. The reassuring news is that in most of the cases studied so far, BAO measurement bias is below current precision for models. Both Ref. Sherwin and White (2019); Carter et al. (2020) warned that this might be no longer true in higher precision next generation measurements due to fiducial cosmology assumption, even just in Λ CDM with varying cosmological parameters.

The inverse distance ladder approach of the BAO measurements is also worth mentioning. In this method, the sound horizon at drag scale r_d is taken as a standard ruler, thus the BAO measured angle corresponding to r_d at given redshift calibrates the distance to the observation. In this way we can get the constraint on H_0 . Some literature cites this method as a "late Universe" or "cosmology independent" measurement of H_0 , which is not exactly true. There is no way to constrain H_0 without any early Universe physics assumption on r_d , when the only information we know is $H_0 \times r_d$ (maybe plus $\Omega_b h^2$, which still does not specify the sound speed completely). This is an indicator that Λ CDM or fixed early Universe is an essential presumption in inverse distance ladder H_0 constraints. Actually, in several strictly classical distance ladder BAO analysis Aylor et al. (2019); Wojtak and Agnello (2019) without any cosmological assumptions (not inverse, anchored to the late Universe supernovae or strong lensing), r_d is found to be systematically smaller than the *Planck* CMB result. Given these, it is not surprising that the inverse distance ladder BAO constraint on H_0 is on the early Universe side of the current H_0 tension.

9.3.3.2. Redshift space distortion. It has been discussed extensively for some relatively more established beyond- Λ CDM model, like f(R) modified gravity, that the compressed RSD survey results typically reported in the form of $f\sigma_8(z)$ values might not be applicable to extended model constraints Taruya et al. (2014); Barreira et al. (2016); Bose et al. (2017). By definition, the growth factor and the fluctuation of matter field are scale insensitive in standard Λ CDM,

.. . .

$$f(z) \equiv \frac{\mathrm{d}\ln D(z)}{\mathrm{d}\ln a},$$
(145)
$$\sigma_8^2(z) \equiv \int_0^\infty \Delta^2(k, z) \left(\frac{3j_1(kR)}{kR}\right)^2 \mathrm{d}\ln k,$$
(146)

where $R = 8h^{-1}$ Mpc. The estimate of $f\sigma_8(z)$ is usually based on a fixed fiducial cosmology template of the redshift-space power spectrum Taruya et al. (2010); Sanchez et al. (2012), because we expect this quantity to be only dependent on the amplitude of the measured RSD. When the fiducial template cannot mitigate the scale-dependent features in the clustering, $f\sigma_8$ measurement could be biased. The robustness of RSD estimates of $f\sigma_8$ against certain modified gravity simulations has been tested by Refs. Taruya et al. (2014); Barreira et al. (2016); Bose et al. (2017). Specifically, these studies found that the bias tends to be non-negligible for the models with scale dependent growth rate deviating from standard Λ CDM. This might be due to the fact that the multiplicative template parameters cannot absorb such scale dependent deviations from the fiducial cosmology. This finding is likely to generalize to other beyond- Λ CDM models that introduce a scale-dependent growth rate in the scale range sensible to the RSD measurements (0.01h Mpc⁻¹ $\leq k \leq 0.2h$ Mpc⁻¹), and the RSD compression into $f\sigma_8$ constraints should be handled carefully.

9.3.3.3. Weak lensing. In weak lensing, the main limitation of a fiducial cosmology assumption usually comes from the modelling of nonlinear matter power spectrum. Most halo model calculations used in fiducial pipelines for weak lensing analyses assume the same non-linear regime clustering physics as GR and Λ CDM. When testing a beyond- Λ CDM (and GR) model, the nonlinear regime should either be removed from the analysis or the non-linear modelling should be modified and validated – e.g. by using N-body simulations or perturbation theory calculations Cataneo et al. (2019); Giblin et al. (2019).

Another place where beyond- Λ CDM modelling is needed is in the default analysis pipeline of the weak lensing surveys, for example the one used in DES Krause et al. (2017), where the lensing kernel takes the form:

$$q_{\kappa}(\chi) = \frac{3H_0^2 \Omega_m}{2c^2} \frac{\chi}{a(\chi)} \int_{\chi}^{\chi_h} d\chi' \frac{n_{\kappa}(z(\chi')dz/d\chi'}{\bar{n}_{\kappa}} \frac{\chi'-\chi}{\chi'}.$$
(147)

This is based on the late Universe where: 1. the matter is predominant contributor to the gravitational potential, and 2. gravity is described by standard General Relativity. The lensing kernel above thus relates the matter overdensity to the potential using the Poisson equation:

$$\Phi = \frac{4\pi G_N \rho_m a^2 \delta_m}{k^2}.$$
(148)

However, when the two conditions above break down in extended cosmologies, for example in certain modified gravity theories, or when extra relativistic species in the late Universe are added, one should use the Weyl potential power spectrum and the corresponding lensing kernel to calculate the projected 2D correlations. This approach does not presume the Poisson equation, namely the matter power

spectrum and the Weyl potential power spectrum are not necessarily linearly related by the factor $\left(\frac{4\pi G_N \rho_m a^2}{k^2}\right)^2$. There are multiple ways to realize this adjustment to the analysis pipeline, the simplest being correcting the matter power spectrum used in Λ CDM pipeline by the ratio:

$$R_{\text{Weyl}}(k,z) = \left(\frac{k^2(1+z)^2}{4\pi G_N \rho_m}\right)^2 \frac{P_{\text{Weyl}}(k,z)}{P_m(k,z)},$$
(149)

where $P_{Wevl}(k, z)$ is the 3D k-space spectrum for Weyl potential perturbation for general gravitational potentials.

9.3.3.4. CMB. The CMB is known for its "cleanness" in terms of cosmological theory predictions, as it happens in the fairly early era of the Universe. Most of the problems can be avoided as long as the Einstein and Boltzmann equations are carefully modified in the Boltzmann solving code. When using a CMB lensing likelihood and/or high- ℓ lensed TT, EE, TE likelihoods, one should note that the non-linear matter power spectrum inducing the lensing effect is expected to be different from the Λ CDM modelling. The non-linear matter power spectrum or the Weyl potential power spectrum used for CMB lensing calculations should be treated as is described above in the 'Weak lensing' paragraph. Alternatively, we can limit our analysis to linear scales, for example the conservative multipole range ($L \leq 400$) of the *Planck* 2018 CMB lensing likelihood Aghanim et al. (2020d).

9.3.4. N-body simulations beyond Λ CDM

N-body simulations have been a pillar of cosmology, allowing to predict structure formation in the non-linear regime. While the current trend is to simulate ever larger volumes at ever larger resolutions, to accompany the next generation cosmological surveys, in the last few years new codes have also appeared aiming to go beyond Λ CDM.

- Dark energy: Several groups have run suites of simulations of non-Λ dark energy models, such as *w*CDM with the Quijote simulations Villaescusa-Navarro et al. (2020), and CPL with the Mira-Titan simulations Heitmann et al. (2016).
- Modified gravity: Modified gravity N-body codes can be divided into two main categories: Newtonian codes with modified Poisson equation Puchwein et al. (2013); Li et al. (2012); Llinares et al. (2014), and relativistic codes Adamek et al. (2016); Hassani et al. (2019, 2020). See Ref. Winther et al. (2015) for a comparison of Modified Gravity N-body codes, and Llinares (2018) for a recent review. Such simulations have been used for studying voids, clustering and alignment L'Huillier et al. (2017).

• Initial conditions: While simulations of primordial non-gaussianities have been carried out since the 1990s Messina et al. (1990), a more recent development is the simulation of primordial features, i.e., deviation from power law, in the power spectrum L'Huillier et al. (2018a); Beutler et al. (2019); Ballardini et al. (2020b).

9.3.5. Optimal practices and recommendations

A consistent statistical methodology requires following a principle-based inference approach, using an incorrect or oversimplified sampling distribution, ignoring significant observational effects that affect data (for example, selection effects) or unrepresentative training data or simulations in machine learning. In all these circumstances and many others, best practices help achieve robust results, which are more likely to survive scrutiny and be corroborated by more extensive and more accurate future data. Astrophysics data often suffer from selection effects or bias. In statistical terms, the observed sample is non-representative of the total population of observed data whose global characteristics one might wish to infer (e.g., cosmological parameters). The latter translates into poor generalization onto the test from a non-representative training set in supervised learning as in GPs and BNNs. In machine learning, "Covariate shift" is a type of model drift that occurs when independent variables' distribution changes between the training environment and the live environment. Ignoring covariate shift leads to incorrect inferences on physical properties and affects the robustness of the results (e.g., for population studies for gravitational lensing classification, photon sources/x-ray, or GWs). Possible solutions include correcting selection effects using simulations, data increment, and unsupervised learning. Extensive use of data compression and summary statistics is common and persistent in cosmology and particle physics. Cosmology, in particular, typically analyses low-order correlation functions because often these carry most of the information, and model predictions are inestimable on small scales, where both non-linear gravity and baryonic effects become essential. Computational advances and a simulation-based approach construct sophisticated nonperturbative summary statistics both by hand and via neural compression methodology. Similar methods, along with more accurate physical modelling, will be essential in the coming years to extract complete scientific information from observational data sets whose volumes and complexity will increase dramatically.

Simultaneous modelling of cosmological data sets across multiple probes will be of crucial importance in both extracting the most precision possible from the data, and in ensuring accuracy is not lost to un-modelled systematics. Where different types of data are combined or compared, it is crucial that simulations used in their calibration and in calculating their likelihoods share the same underlying physical models. For example, combined modelling of radio and optical observations could assist both shear measurement (Harrison et al., 2016) and galaxy redshift measurements (Alonso et al., 2017; Cunnington et al., 2019) and lead to improved and more robust measurements of the S_8 tension. New astrophysical discoveries such as GWs and Fast Radio Bursts (FRBs) will also provide new information for cosmology, with gains that will be maximised by modelling their sources alongside the large scale structures measured by other experiments. Meeting this challenge will require co-ordination and openness between different experiments and communities, the construction of modelling and inference pipelines that work simultaneously for multiple data types (see S. Collaboration, 2020, for an early attempt at this), and infrastructure for sharing and accessing extremely large data sets.

9.4. The road ahead: beyond ΛCDM

In view of the accumulation the Λ CDM tensions discussed in the previous sections it is becoming apparent that the need for a new standard cosmological model has been increasing during the last few years. The present time has similarities with the late nineties when it was becoming apparent that the standard model of that time (flat sCDM based on the Einstein-de Sitter model) had been accumulating a range of inconsistencies with data including indications for excess clustering on large scales, hints for $\Omega_m < 1$, age of the Universe tension, velocity flows etc. It is interesting to recall the conditions that lead to the birth of the current standard cosmological model (Λ CDM) in order to identify similarities and use them as a possible guide for the construction the new standard model that may be approaching. These conditions can be summarized as follows

- 1. The emergence of the tensions of sCDM. These tensions include the observations for excess of clustering on large scales > 10 Mpc Davis et al. (1992), observations for low velocities on small scales (1 Mpc) Davis et al. (1985), the ages of globular clusters which appeared to be larger than the predicted age of the Universe in the context of sCDM Janes and Demarque (1983) and indications for missing matter density ($\Omega_m < 0.3$) Bartlett and Silk (1993); Davis et al. (1992).
- 2. The use of simple new parameters to address these tensions. This lead to simple extensions of sCDM including the mixed dark matter (mixture of hot and cold dark matter), ACDM, titled primordial power spectrum, open Universe, loitering Universe etc.
- 3. Theoretical motivation and predictive power played an important role in the selection of specific parametrizations including Λ CDM. Mixed dark matter and Λ CDM were the two models based on simple and generic theoretically motivated mechanisms and as such they had an advantage over the other approaches which were purely phenomenological and required tuned potentials and/or initial conditions (e.g. the open or the loitering Universe models). Λ CDM had an additional advantage that it could make a smoking gun unique and testable prediction: accelerating expansion at low redshifts. This was the crucial feature of the Λ CDM model that when combined with the SNIa observations in and after 1998 established it as the new standard cosmological model.⁴⁸

In the context of an analogy with the above developments for the emergence of Λ CDM as a new standard cosmological model, it could be stated that we are currently at stage 2 in the process of the emergence of the new standard model beyond Λ CDM. Well defined tensions of Λ CDM with data have developed well beyond the level of the tensions that gave rise to it. These tensions include the H_0 tension (5 σ Riess et al. (2021b)), statistical anisotropy of the CMB temperature on large angles (multiple > 3 σ anomalies), cosmic dipoles-anisotropies (4 – 5 σ Secrest et al. (2021); King et al. (2012)), growth S_8 (2 – 3 σ Asgari et al. (2020); Abbott et al. (2020b); Macaulay et al. (2013); Skara and Perivolaropoulos (2020); Kazantzidis and Perivolaropoulos (2019); Bull et al. (2016); Kazantzidis and Perivolaropoulos

⁴⁸ The inertia of the sCDM was however not easy to overcome and it is well known that the first study of the Hubble diagram using SNIa did not favour ACDM Perlmutter et al. (1997) but sCDM albeit with large uncertainties.

(2018); Nesseris et al. (2017); Joudaki et al. (2018)) and others. Simple mechanisms and parametrizations have been proposed to address specific of the existing tensions.

In view of existing current status of events, the following question emerges: *What could be the features of the next standard cosmological model?*. Based also on the experience of the previous change of standard cosmological model that occurred in the late nineties, the following features of the next standard cosmological model could be anticipated:

- Consistency with main Λ CDM tensions (H_0 , S_8 , cosmic dipoles)
- Existence of simple parametrization (one or two more parameters) in the context of a specific physically, motivated mechanism.
- Simple and generic theoretical framework that justifies the parametrization.

Specific generic phenomenological parameters that may be considered in the above context include

- The dark energy equation of state parameter w_{DE} .
- The effective parameters μ and Σ connected with the strength of gravity with respect to matter and light; see Eq. (67).
- The dipolar anisotropy parameter defined in Eq. (130) and the anisotropy parameter $S_{1/2}$ defined in Eq. (129).
- The dimensionless fine structure constant connected with the strength of the electromagnetic force.

These (and other similar) effective parameters however have the following problems which make it difficult for them to replace Λ CDM soon:

- They are purely phenomenological, usually motivated by fine tuned effective scalar field potentials, and a number of these scalar models can be shown to exacerbate tensions Banerjee et al. (2021b); Heisenberg et al. (2022a,b); Lee et al. (2022).
- In most cases they lack generic detectable smoking gun signatures in upcoming cosmological data as was the case for the accelerating expansion prediction of ΛCDM.
- These parameters appear to be disconnected and it seems unlikely that a single one of them will be able to simultaneously resolve more than one of the ΛCDM tensions.

The high accuracy and precision of the current cosmological data makes it probable that some type of an abrupt transition in space and/or in time either before recombination (z > 1100) Niedermann and Sloth (2021a, 2020, 2021b) or after the end of the Hubble flow (z < 0.01) Marra and Perivolaropoulos (2021); Alestas et al. (2021a); Perivolaropoulos and Skara (2021a). Such an event would have the following advantages:

- 1. It would leave intact the expansion history of the Universe from the time of recombination until the end of the Hubble flow, which is extremely well constrained by current data.
- 2. If the transition is spatial (involving e.g. a first order phase transition) it has the potential to simultaneously address a wide range of tensions including the detection of cosmic dipoles, Hubble tension and growth tension.
- 3. It has the potential for specific unique and generic signatures in cosmological and astrophysical data
- 4. It may be based on a simple and generic physical mechanism: *The decay of the false vacuum* which has been well studied during the past few decades.

In view of the above discussion, the strategic steps for the road ahead towards a possible discovery of a new standard model for cosmology could be the following:

- The tuning of current missions towards verification or rejection of the existing non-standard signals and tensions of ΛCDM.
- The use of model-independent, data driven reconstructions of cosmological observables such as $(H(z), \mu(z), \Sigma(z), ...)$ to identify simple forms for their possible evolution.
- Use these forms to identify favoured parametrizations of H(z, w(z), r), $\mu(z, r)$, $\Sigma(z, r)$, $\alpha(z, r)$ and dipole anisotropy parameters assuming that at least some of the non-standard signals are physical.
- Identify theoretical models (field Lagrangians) that are consistent with these parametrizations. Interestingly, for example only a small subset of modified gravity models is consistent with the weak gravity + Λ CDM background Wittner et al. (2020); Pizzuti et al. (2019); Gannouji et al. (2021, 2018) suggested in the context of the S₈ tension.

An exciting new era is probably approaching for cosmology which may soon lead to new discoveries in fundamental physics.

10. Conclusions

The present tensions and discrepancies among different measurements, in particular the H_0 tension as the most significant one, offer crucial insights in our understanding of the Universe. For example, the standard distance ladder result has many steps in common with the accelerating Universe discovery (which gave cosmology the evidence for DE). So, whatever the definite finding may be, whether about stars and their evolution, or DE, this is going to have far reaching consequences.

Solving the H_0 tension is very much an ongoing enterprise. The resolution of this conundrum will likely require a coordinated effort from the side of theory and interpretation (providing crucial tests of the exotic cosmologies), and data analysis and observation (expected to improve methods and disentangle systematics). This agenda will flourish in the next decade with future CMB and distance ladder experiments, that are expected to reach an uncertainty of, respectively, ~ 0.15% and ~ 1% in the H_0 estimates, see Table 4 and Section 9. In other words, the next decade will test the Λ CDM model through next-generation experiments that will usher in a new era of cosmology.

Table 4

List of Experiments	per science topic.	The timeline is i	instead reported in	Table 3.
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Science	Facilities	
21 cm	BINGO, CHIME, GBT, HIRAX, MeerKAT, OWFA, PUMA , SKAO, uGMRT	
BAO and RSD	4MOST, BINGO, CHIME, COMAP, DESI, Euclid, HIRAX, PFS, Roman, Rubin, SKAO, SPHEREx	
CC	ATLAS, Euclid, SPHEREx	
CMB	ACT, BICEP/Keck, CMB-HD, CMB-S4, LiteBIRD, SO, SPT	
Distance ladder	ELTs, Gaia, GBT, JWST, LIGO, Roman, Rubin, VLA, VLBA	
FRB	CHIME	
GW	Cosmic Explorer, DECIGO , ET, LGWA, LIGO/Virgo/KAGRA/LIGO-India, LISA, Taiji, TianQin	
Quasars	GRAVITY+	
Redshift drift	ANDES, ELTS, SKAO	
SDs	SuperPIXIE	
SNe	Rubin, Roman, YSE, ZTF	
Time Delay cosmography	Euclid, Pan-STARRS, Roman, Rubin, SKAO, ZTF	
Time Lag cosmography	Rubin	
Varying fundamental constant	ANDES, ELTS, ESPRESSO	
WL	4MOST, CFHT, DES, Euclid, HSC, KiDS, Pan-STARRS , Roman, Rubin, SKAO, UNIONS	

In the near future, moreover, we expect precise measurements of the expansion and growth history over a large range of experiments (see Table 4 and Section 9), i.e. using maps of the Universe obtained by the *Euclid* satellite, measuring the peculiar motions of galaxies using Type Ia supernovae from *Rubin*/LSST Howlett et al. (2017); Scolnic et al. (2019), considering RSD with DESI and 4MOST, or using voids Hamaus et al. (2020). An important role will be played by the SKAO telescopes performing BAO surveys and measuring weak gravitational lensing using 21 cm intensity mapping Pourtsidou and Metcalf (2015); Santos et al. (2015); Bull et al. (2015a). Additional upcoming 21 cm neutral hydrogen experiments measuring the expansion history will be CHIME and HIRAX. Finally, line-intensity mapping of emission from star-forming galaxies can be used to measure BAO, reaching percent-level constraints Karkare and Bird (2018); Bernal et al. (2019) with the SPHEREx satellite or the ground-based COMAP instrument. All of these efforts will either reveal a systematic cause or harden the tension to strong statistical significance, thus informing the theories mentioned above and guiding any extension/overhaul of the standard model.

Meanwhile, the CMB temperature map has a number of independent pieces of evidence, each with *p*-values less than 0.3% (i.e. less likely than a 3σ fluctuation), that the Λ CDM prediction of statistical isotropy is violated (see Sec. 8.3). These cannot be addressed by mere changes in the background scale factor dynamics. They demand early universe or large scale departures from homogeneity and/or isotropy. A theoretical priority is exploring potential physical models, such as cosmic topology. Existing data, ongoing and future observational programs can increase our confidence that these are not mere statistical flukes by exploring conditional predictions of Λ CDM, especially those for which we would expect physical models to disagree.

In the four LoIs Di Valentino et al. (2021a,b,c,d) before, and now in this White Paper, we presented a snapshot, at the beginning of the SNOWMASS process, of the concordance ACDM model and its connections with the experiments, and monitored the new advances in the field to come out with a clear roadmap for the coming decades. This is a cutting-edge field in the area of cosmology, with unrestrained growth over the last decade. On the experimental side, we have learned that it is really important to have multiple precise and robust measurements of the same observable, with experiments conducted blindly in regard to the expected outcome. This provides a unique opportunity to study similar physics from various points of view. While on the theory side, it is really important to have robust and testable predictions for the proposed physical models that can be probed with the data. With the synergy between these two sides, significant progress can be made to answer fundamental physics questions.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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