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Measurements of pressure gradient and temperature gradient driven flows in a rectangular channel

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Abstract

The objective of this experimental investigation is to characterize the gas-surface interaction under different flow conditions. Therefore, the mass flow rates driven by pressure gradient under isothermal condition and by only temperature gradient under constant pressure condition are measured in the same microchannel for five different gases: helium, neon, nitrogen, argon and krypton. The pressure driven experiments are carried out in hydrodynamic and slip flow regimes, $0.0016 < \text{Kn} < 0.12$, while the temperature driven experiments in slip and transitional flow regimes, $0.05 < \text{Kn} < 0.45$. Using previously developed methodology, the velocity and thermal slip coefficients are derived from the measured mass flow rates. By adopting the classical Maxwell boundary condition, the accommodation coefficients are found very different for both types of flows, with significantly lower value for polyatomic nitrogen in the case of temperature gradient driven flows. An attempt to calculate the tangential momentum and normal energy accommodation coefficients in the frame of the Cercignani-Lampis model was successful only for the tangential momentum accommodation coefficient, which was found very close to that derived with the Maxwell model. However, it was not possible to obtain the values of normal energy accommodation coefficient due to the lack of numerical results which connect thermal slip and normal energy accommodation coefficients for very low values of the latter.

1. Introduction

The knowledge about the characteristics of gas-surface interaction is very important in different fields such as: (i) gas flow at small scale in Micro Electro Mechanical Systems (MEMS), where the ratio of surface area to corresponding volume is very large compared to the conventional devices, (ii) shuttle re-entry and satellite flights, and vacuum technology applications, where the number of molecules in a characteristic volume is relatively low compared to the case of atmospheric working pressure. In all these applications, the number of the molecule-surface collisions are more numerous compared to the molecule-molecule collisions. In addition, in these kinds of flows, the Knudsen number, *i.e.* the ratio of the molecular mean free path to a system characteristic dimension, is usually larger than one. Therefore, to simulate the gas flow in such conditions, the Boltzmann equation (or other kinetic models) has to be implemented. This equation provides the complete description of the gas flow at mesoscopic level, but the boundary conditions have to be formulated at microscopic level. This means that the behavior of the reflected molecules in function of the incident molecules has to be known, *i.e.* a model describing the gas-surface interaction has to be adopted [1, 2].

The influence of gas-surface interaction has to be accounted also for when the Knudsen number is lower than one, and it can be done through the velocity and thermal slip coefficients and temperature jump coefficients in the frame of the continuum modeling based on the Navier-Stokes-Fourier system or on the higher order, as the R13 system [3, 4].

In spite of various models describing the interaction between gas molecules and solid surface, developed during the last fifty years, such as the Epstein model [5], Cercignani-Lampis model [6] and Klinc & Kušcer

26 model [7, 8], the most largely used is the Maxwell model [9]. The simplicity of its application as the
27 boundary condition for the Boltzmann equation and other kinetic type equations explains its popularity.

28 At microscopic scale level, when a gas molecule hits a surface, momentum and energy could be trans-
29 ferred during this interaction. Therefore, two accommodation coefficients – accommodation of momentum
30 and of energy – could be introduced to characterize this exchange. However, in the Maxwell model, only
31 one single accommodation coefficient is introduced, without an identification about the nature of the
32 exchange (momentum or energy).

33 Despite this ambiguous interpretation of the real nature of the exchange (momentum or energy),
34 this Maxwellian model was successfully used to describe various isothermal flows driven by a pressure
35 gradient, both at microscale and low pressures [10, 11, 12, 13, 14, 15]. In this case, since the temperature
36 is kept constant in the system, only the momentum exchange is considered to be important and the
37 accommodation coefficient is identified as tangential momentum accommodation coefficient (TMAC) [16].
38 In the particular case where only energy exchange is taken place between a gas and a surface, without
39 macroscopic gas movement, the thermal or energy accommodation coefficient is introduced in the frame
40 of Maxwellian model to characterize the particularity of this gas-surface interaction [17, 18, 19, 20, 21].
41 However, in the majority of the flows where both exchanges exist, the interpretation of this single coefficient
42 becomes problematic.

43 The main objective of the present work is providing a series of data on the mass flow rate of two types
44 of flows: (i) flow driven by a pressure gradient (Poiseuille flow) and (ii) flow driven by a temperature
45 gradient (thermal creep), both of them in the same microchannel, aiming to test different models of the
46 gas-surface interaction. These two types of flows, pressure gradient [11, 12, 13, 14, 15] and temperature
47 gradient [21, 22, 23, 24, 25] driven flows, were studied in the past, but in different channels, thereby the
48 difference in the value of the accommodation coefficients found from these studies could be attributed to
49 the difference in the surface state (surface preparation, roughness, *etc*). Therefore, in the present work we
50 offer the experimental results on the mass flow rate for pressure and temperature gradient driven flows in
51 the same microchannel, that is using an identical surface state.

52 This paper is organized as following: first, the experimental setup is presented and the particularities
53 of both pressure and temperature gradient experiments are discussed. Then, the accommodation coeffi-
54 cients are extracted using the Maxwellian model and the data on the mass flow rates obtained from both
55 kind of experiments. Finally, a first attempt of extraction of two accommodation coefficients (tangential
56 momentum and normal energy) in the frame of the Cercignani-Lampis model is done.

57 2. Experimental Apparatus

58 The same experimental setup was used to measure the mass flow rate of the pressure and temperature
59 gradient driven flows. The detailed description of this setup will be provided along this section.

60 2.1. Experimental setup

61 The constant volume methodology [12, 13, 14, 25, 26] is applied to measure the pressure and tem-
62 perature gradient driven flows through a microchannel. Each one of these two types of experiments was
63 performed separately, *i.e.* either only pressure gradient or only temperature gradient is applied to generate
64 a flow through the microchannel. A scheme representing the experimental setup is shown in Fig. 1. It
65 basically consists of two tanks, upstream and downstream tanks, which are connected by the microchannel.
66 The upstream tank, represented in Fig. 1 by the blue color (tank 1), is also called high pressure tank,
67 in the pressure gradient experiments, or cold tank, in the temperature gradient experiments. The down-
68 stream tank, represented by the red color (tank 2), is also called low pressure tank in the pressure gradient
69 experiments, or hot tank, in the temperature gradient experiments. Both upstream and downstream tanks
70 are made of stainless steel and their temperatures can be controlled by circulating water (tank 1, cold

71 side) and by an electrical heater (tank 2, hot side), respectively. The positions of the cooling and heating
 72 systems entrances are indicated in Fig. 2 by the numbers 12 and 13, respectively.

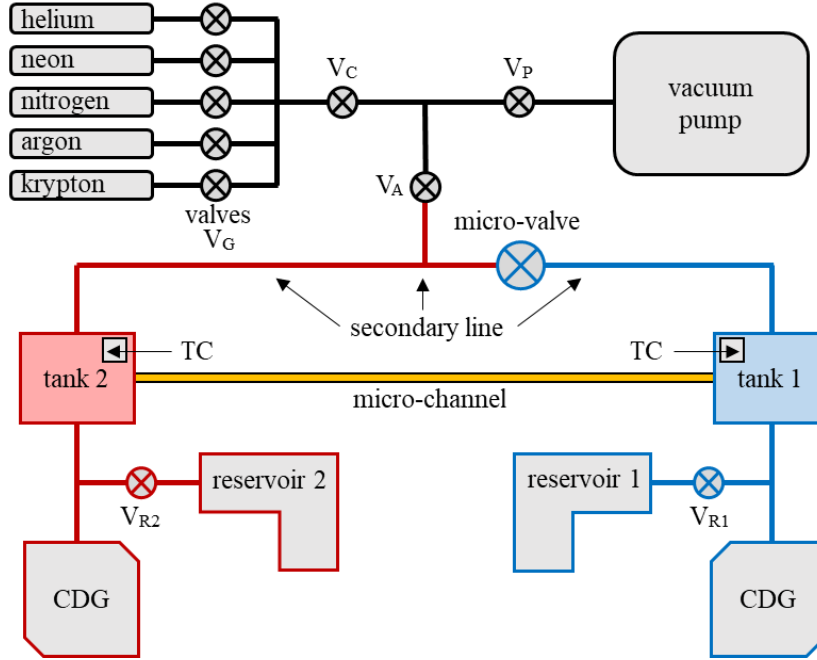


Figure 1: Experimental apparatus used in the pressure and temperature gradient experiments.

73 Figure 2a presents an exploded view of the microchannel plates and tanks. The microchannel is
 74 grooved in the inner plate made in PEEK (PolyEtherEtherKetone) and covered by another flat plate of
 75 same material, but thicker than the first one. **The interface between two plates is provided with a flat seal.**
 76 These two plates are pressed up against each other by fourteen bolts and also pressed against the tanks
 77 by eight of these fourteen bolts. **To improve the seal and reduce leaks, vacuum glue is added around each**
 78 **external interface and white paste at the top of the threaded rod, see Fig. 3(a).**

79 The microchannel has a rectangular cross-section with the following dimensions: height $H = 0.24 \pm$
 80 0.01mm , width $W = 1.00 \pm 0.01\text{mm}$ and length $L = 72.00 \pm 0.05\text{mm}$. The roughness of the microchannel,
 81 Ra parameter, was measured with a 3D digital microscope, following the criteria of ISO4287. This standard
 82 states that to obtain a value of roughness from a topography of a sample, first a flatness correction is
 83 applied to it and then a set of roughness profiles is extracted. The Ra parameter is the arithmetic average
 84 value of the roughness profiles. The roughness was measured in the top and bottom faces of the channel.
 85 The roughness parameter for both faces is found equal to $113 \pm 19\text{nm}$, which is of the order of 0.05% of
 86 the channel height. The roughness of the lateral faces was not measured. **Even if the material of the**
 87 **channel walls is the same, the milling process used to manufacture the channel cannot guarantee the same**
 88 **roughness for the horizontal and vertical walls. Since the areas of the lateral faces are much smaller (five**
 89 **times) in comparison to the top and bottom areas, we assume that the absence of this information cannot**
 90 **essentially impact further conclusions about the flow patterns.**

91 Two additional volumes, referenced in the following as reservoirs 1 and 2, Fig. 1, are connected to
 92 the tanks 1 and 2, respectively, to increase the total volume of the system. The additional reservoirs are
 93 connected to the upstream and downstream tanks by the valves V_{R1} and V_{R2} , respectively. Therefore,
 94 depending on the position of the valves, these reservoirs can be included or not in the measuring system.
 95 For the pressure gradient experiments, the volumes of reservoirs 1 and 2 are equal ($208.9 \pm 4.5\text{cm}^3$). For
 96 the temperature gradient experiments, we do not use any additional reservoirs in the cold side, while a

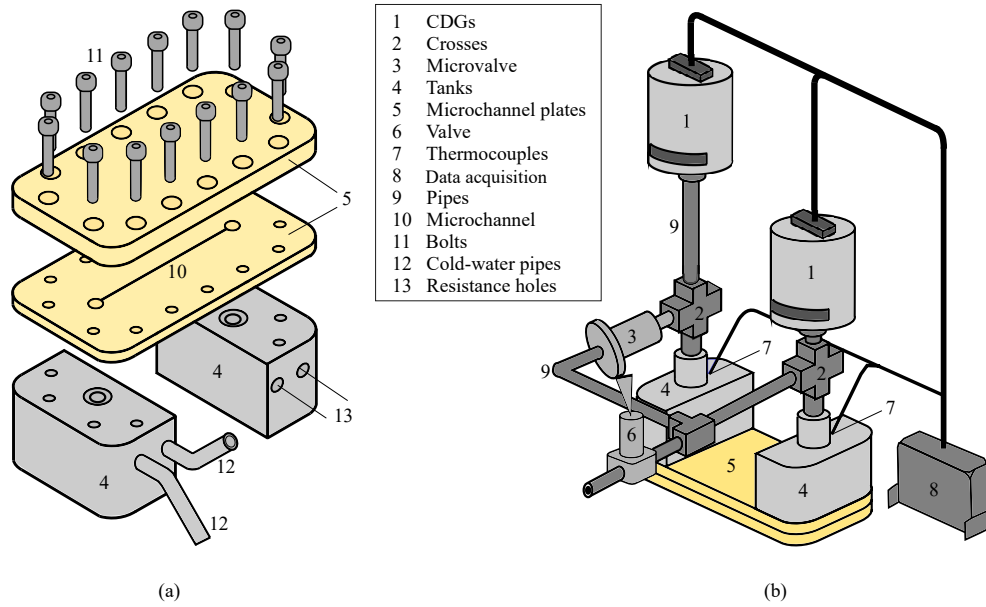


Figure 2: (a) Exploded view of the flat plate, grooved plate and tanks. (b) Tanks and microchannel plates connected to the rest of the system.

97 small reservoir of volume equal to $57.6 \pm 1.2 \text{cm}^3$ is connected to the hot side. The effect of these additional
 98 volumes on the accuracy of mass flow rate measurements and duration of the experiments will be discussed
 99 in Section 4.2.

100 The upstream and downstream tanks are connected not only by the microchannel, but also by a large
 101 diameter pipe system, called secondary connection or secondary line, see Fig. 1. In order to allow or
 102 prevent a gas to flow between these two tanks by the secondary connection, a micro-valve was inserted in
 103 this circuit. During the pressure gradient experiments, this micro-valve is not used, remaining closed all
 104 the time, while in the temperature gradient experiments, this micro-valve is opened in the beginning of
 105 each experiment to insure the development of the stationary thermal transpiration flow.

106 The pressure variation in time in each tank is measured by a high-speed response (30ms) Capacitance
 107 Diaphragm Gauge (CDG), manufactured by Inficon. In the temperature gradient experiments, a single
 108 pair of CDGs is used in all the measurements, both of them with full scale of 1.33kPa, while in the
 109 pressure gradient experiments, three different pairs of CDGs are implemented, with the full scales of
 110 133kPa–133kPa, 133kPa–13.3kPa and 1.33kPa–1.33kPa, depending on the desired pressure measurement
 111 range.

112 During the pressure gradient experiments, the cooling and heating systems are switched off and both
 113 tanks are kept at the room temperature, while in the temperature gradient experiments both systems
 114 work to maintain the tanks at constant but different temperatures. The external temperature of each
 115 tank is measured by a K-type thermocouple (TC). Obviously there should be a discrepancy between the
 116 measured temperatures (external walls of the tanks) and the temperatures at the microchannel entrances.
 117 To associate the measured temperature gradient driven flow to the really applied temperature difference
 118 at the microchannel ends, the temperature at the microchannel surfaces was measured using an Infra-Red
 119 (IR) camera, and the details of these measurements are provided in Section 3. The data measured from the
 120 pressure gauges (CDGs) and the thermocouples (TCs) are captured by a data acquisition system (DAQ)
 121 produced by the National Instruments Corporation.

122 The leakage rate in the system was evaluated using 13.3kPa pressure sensors according to the following
 123 procedure: first, all the valves of the experimental setup, except the valves V_G , see Fig. 1, were opened and

124 the system was pumped down during 72 hours using a vacuum pump, model Adixen Drytel 1025. Then, the
 125 valves V_A , V_{R1} and V_{R2} were closed and both CDGs captured the pressure evolution **from initial measured**
 126 **pressure of 0.133Pa** during two hours. During this period, the pressure inside the system increased in
 127 0.424Pa, which is associated to the leakage rate into the system by the gaps of the microchannel plates,
 128 Fig. 2a, and other connections, see Fig. 1, and also a possible outgassing. This increase in the pressure
 129 corresponds to a mass flow rate of the order of $2.18 \times 10^{-14} \text{kg}\cdot\text{s}^{-1}$, which could be associated to a leakage
 130 rate into the system and an outgassing. However, the lowest value of mass flow rate measured through the
 131 microchannel driven by the temperature gradient was $2.88 \times 10^{-12} \text{kg}\cdot\text{s}^{-1}$, which is more than two orders
 132 of magnitude larger than the leakage rate. Therefore, the leakages and outgassing were considered as a
 133 part of the uncertainties of pressure driven and temperature driven experiments, see Section 4.3.

134 2.2. Volumes setting for pressure and temperature gradient experiments

135 The constant volume technique consists of measuring the pressure variation with time between two
 136 constant volumes connected by a microchannel [23, 24, 27]. The total volume V_i connected to the side
 137 i of the microchannel includes: volume of tank, $V_{\text{tank},i}$, volume of additional reservoir, $V_{\text{res},i}$, volume
 138 of connecting pipes, $V_{\text{pipes},i}$, internal volumes of the valves, $V_{\text{valves},i}$, and internal volume of pressure
 139 transducer, $V_{\text{CDG},i}$:

$$V_i = V_{\text{res},i} + V_{\text{tank},i} + V_{\text{pipes},i} + V_{\text{valves},i} + V_{\text{CDG},i}, \quad (1)$$

140 where the subscript i refers to the upstream ($i = 1$) and downstream ($i = 2$) sides of the microchannel,
 141 see Fig. 1. The total volumes of the upstream and downstream sides for all the settings used in the
 142 pressure and temperature gradient experiments are provided in Table 1. It is clear that the volume of the
 143 microchannel, $V_{\text{ch}} = 0.017 \text{cm}^3$, is much smaller compared to the total upstream and downstream volumes.

Table 1: Total volumes of both upstream and downstream sides, V_1 and V_2 , respectively, used in the four different settings. The total volume of the system ($V_T = V_1 + V_2$) and volume ratio ($V_{\text{ratio}} = V_1/V_2$) are also presented.

Setting	CDGs	V_1 [cm^3]	V_2 [cm^3]	V_T [cm^3]	V_{ratio} [-]
pressure gradient 1 (PG1)	133–133kPa	222.2	230.3	452.5	0.964
pressure gradient 2 (PG2)	133–13.3kPa	222.2	230.3	452.5	0.964
pressure gradient 3 (PG3)	1.33–1.33kPa	221.2	227.4	448.6	0.973
temperature gradient (TG)	1.33–1.33kPa	12.6	75.3	87.9	0.168

144 From Table 1, it can be realized that the total volumes of the upstream, V_1 , and downstream, V_2 , sides
 145 are slightly larger for the two first settings, PG1 and PG2, in comparison to the third one, PG3, even if the
 146 same reservoirs are used in all the pressure gradient measurements. This happens because the capacitance
 147 diaphragm gauges (CDGs) with full scale of 1.33kPa have internal volumes slightly smaller than the other
 148 ones. This table also shows that only one volume setting is implemented in the temperature gradient
 149 experiments, since the same pair of CDGs is used in all the measurements.

150 3. Estimation of Temperature Profile along the Microchannel

151 The temperature gradient driven mass flow rate significantly depends on the channel surface temper-
 152 ature, especially on the temperature difference between the channel ends, therefore this temperature has
 153 to be measured or, at least, estimated. The measurements of the temperature field in the tanks and of the
 154 temperature distribution along the microchannel surface were performed using an Infra-Red (IR) camera
 155 which characteristics are given in Table 2.

156 The IR camera is calibrated considering a black-body. Thus, in order to measure the correct value
 157 of temperature, some surfaces of the microchannel plates, tanks, parts of the pipes and connections were

Table 2: Specifications of the Infra-Red camera used in the measurements.

Camera SC6000 FLIR	
Spectral range	3-5 μ m
Detector type	InSb (Indium Antimonide)
Spatial resolution	640 x 512 pixels
Detector pitch	25 μ m
Typical NETD	<20mK (18mK typical)
Temperature ranges	-10°C to 55°C 10°C to 90°C 50°C to 150°C
Accuracy	$\pm 2^\circ\text{C}$
Dynamic range	14bits

158 coated with a black paint, model Nextel Velvet-Coating 811-21, see Fig. 3a. The emissivity of this black
 159 paint was measured with an infra-red spectrophotometer Nexus 670 for a spectral range between 3 μ m and
 160 5 μ m, and its value is found equal to 0.96.

161 All the procedure explained in this section is referred to the highest temperature difference, $\Delta T =$
 162 $T_2 - T_1 = 67.5^\circ\text{C}$, used in the measurements, but the same steps were also performed for the lowest tem-
 163 perature difference as well ($\Delta T = 58.0^\circ\text{C}$). Aiming to have an established temperature profile along the
 164 microchannel, the electrical resistance and the cold water flux were initialized 18 hours before the temper-
 165 ature measurement. During the last two hours of this period, the variation of the temperature measured
 166 by the thermocouples at the external walls of the tanks was lower than 0.5°C. This variation was mostly
 167 caused by the change in the room temperature, which is not controlled. The temperature measurements
 168 of the same external surfaces of both tanks, were carried out with the IR camera during a short period
 169 (around 6 minutes), which correspond to an average experimental time duration for temperature driven
 170 experiments, and the temperature variations in both hot and cold sides did not exceed 0.02°C. This very
 171 small variation confirms the negligible influence of the external convection. The values of temperature
 172 measured by the thermocouples and by the IR camera for two applied temperature differences are provided
 173 in Table 3. The difference between the temperatures obtained by the thermocouples and by the IR camera
 174 is lower than 3°C. This difference is explained because the spots of measurement are not the same, *i.e.* the
 175 thermocouples provide a local measurement of a point on the top part of the tank surface, while the IR
 176 camera gives the average temperature of a substantial part of the front surface of each tank. In addition,
 177 the measurement uncertainty of the IR camera is 2K and of the thermocouple is of 0.5K. The complete
 178 explanation of the exact spots of temperature measurements with both thermocouples and IR camera is
 179 presented in Ref. [28]

180 The temperature field of the whole system measured by the IR camera is shown in Fig. 3b, where
 181 the microchannel is represented by a white dashed line. The temperature at the hot-side cross-section of
 182 the microchannel is considerably lower than the external temperature of the hot tank. Although there is
 183 also a difference between the external temperature of the cold tank and the temperature at the cold-side
 184 cross-section of the microchannel, this difference is much less pronounced compared to that one of the hot
 185 side.

186 The values of the average temperatures of microchannel end cross-sections and tanks for both hot and
 187 cold sides, for the two temperature differences, 58.0°C and 67.5°C, are presented in Table 3. There is a
 188 considerable difference between the surface temperature of the tank measured by the thermocouple at its
 189 upper surface and the wall temperature of the microchannel end cross-section measured by the IR camera,
 190 mainly for the hot side.

191 For instance, for the highest temperature difference, the temperature of the top part of the hot tank,

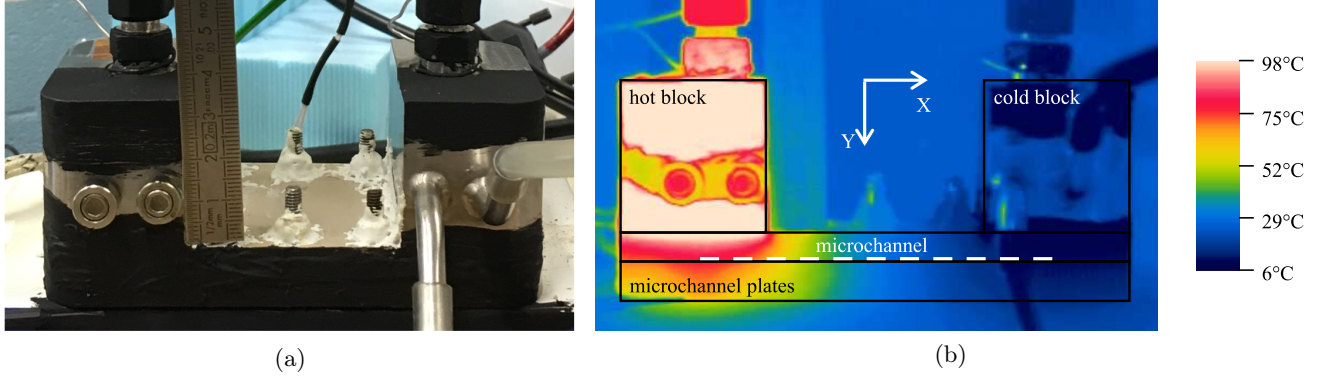


Figure 3: (a) Microchannel plates, blocks and part of the pipes and connections coated with a black paint. (b) Temperature field of the system measured by the Infra-Red camera for the highest temperature difference, $\Delta T = 67.5^\circ\text{C}$.

Table 3: Temperatures measured by the IR camera and thermocouples at the external surfaces of both tanks and at the microchannel end (cold and hot sides) cross-section (ECS) for the two temperature differences.

Instrument	Spot	$\Delta T = 67.5^\circ\text{C}$			$\Delta T = 58.0^\circ\text{C}$		
		$T_{hot} [^\circ\text{C}]$	$T_{cold} [^\circ\text{C}]$	$\Delta T [^\circ\text{C}]$	$T_{hot} [^\circ\text{C}]$	$T_{cold} [^\circ\text{C}]$	$\Delta T [^\circ\text{C}]$
IR camera	channel ECS	79.0	11.5	67.5	69.5	11.5	58.0
IR camera	tank	97.7	10.9	86.8	85.1	10.6	74.5
thermocouple	tank	95.5	8.5	87.0	82.5	8.5	74.0

192 measured by the thermocouple, is 95.5°C , while the temperature of the hot-side end cross-section of the
 193 microchannel, obtained by the IR camera, is 79.0°C . These later data of temperature measurements will
 194 be used in Section 4.2 for the calculations of the mass flow rate for the temperature gradient driven flows.

195 The temperature profile along the microchannel was also measured by the IR camera at the lateral
 196 surface in the interface of the two microchannel plates and it is presented in Fig. 4. As it can be seen
 197 in Fig. 3, the inlet tube of the cooling system of the cold tank disturbs the measurement, since it is
 198 located between the IR camera lens and the lateral surface of the microchannel plates. For this reason,
 199 the temperature along a segment of approximately 10mm nearby the cold-side end cross-section of the
 200 microchannel was reconstructed by the linear interpolation, dotted line on Fig. 4.

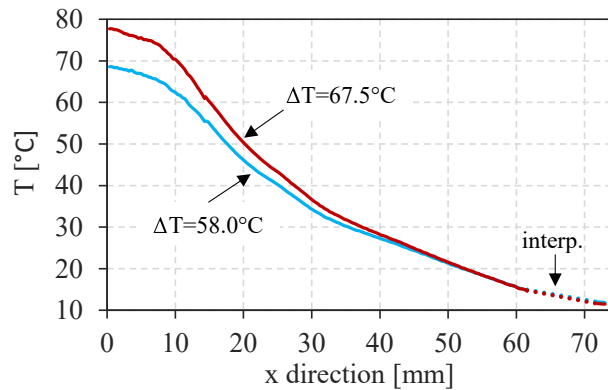


Figure 4: Temperature gradient along the microchannel for the two temperature differences.

201 As previously mentioned, the IR camera measures temperature at a surface. Thus, the temperature

202 profile along the microchannel was obtained by measuring the surface temperature at the lateral face of
 203 the microchannel plates. Hence, to assume that it is correct to extract the temperature profile along
 204 the microchannel from this measurement at the lateral surface, it is necessary to neglect the temperature
 205 gradient in the direction perpendicular to this lateral face. The temperature field shown in Fig. 5 indicates
 206 that actually this assumption is correct, since practically there is no difference between the temperature
 207 in the center line of the bottom plate, $z = 0\text{mm}$, and the temperature in its peripheral region, $z = 30\text{mm}$.

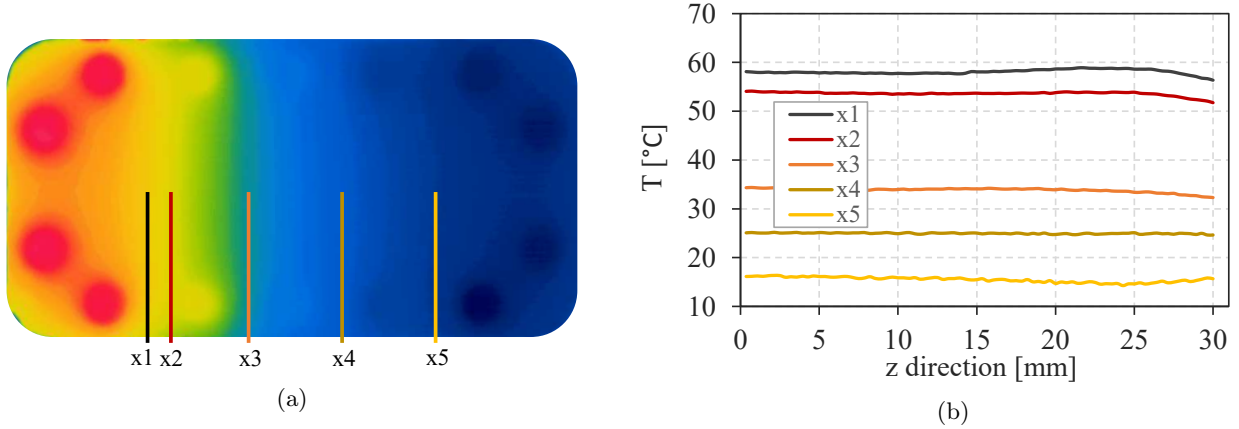


Figure 5: Temperature profiles in the z -direction (channel width) of five different microchannel sections for $\Delta T = 67.5^\circ\text{C}$.

208 4. Mass Flow Rate Measurements

209 The mass flow rate through the microchannel can be generated by setting a pressure difference between
 210 the tanks (pressure gradient experiments) or a temperature difference (temperature gradient experiments).
 211 In both cases, the pressure variation inside the tanks (or the pressure difference between them) is measured,
 212 which is due to the mass of a gas flowing from the upstream to the downstream tank. In order to relate
 213 the pressure variation in time to the mass flow rate, the ideal gas law in each tank is used in the following
 214 form:

$$p_i V_i = M_i \mathcal{R} T_i, \quad i = 1, 2, \quad (2)$$

215 where p_i , M_i and T_i are the pressure, mass and temperature of the gas in the tank i , respectively, V_i
 216 is the volume of tank i , and \mathcal{R} is the specific gas constant. By using the logarithmic derivation of previous
 217 equation and assuming the volume constancy we obtain the following expressions:

$$\frac{dp_i}{p_i} = \frac{dM_i}{M_i} + \frac{dT_i}{T_i}, \quad i = 1, 2. \quad (3)$$

218 Finally, rearranging Eq. (3), we express the mass variation in time in each tank in the form:

$$dM_i = \frac{V_i}{\mathcal{R} T_i} dp_i (1 - \epsilon_i), \quad \epsilon_i = \frac{dT_i/T_i}{dp_i/p_i}, \quad i = 1, 2, \quad (4)$$

219 where ϵ_i is the ratio between the relative temperature and pressure variations in time inside the tank i .
 220 When this ratio is small, *i.e.* the temperature variation is much smaller than the pressure variation during
 221 a specific time interval, dt , we obtain the expressions of the mass flow leaving tank 1 and entering into
 222 tank 2 in following form:

$$\frac{dM_i}{dt} = \dot{M}_i = \frac{V_i}{\mathcal{R} T_i} \frac{dp_i}{dt}, \quad i = 1, 2. \quad (5)$$

223 The derived expressions of Eq. (5) can be used for both pressure and temperature gradient driven flows,
 224 under the conditions of smallness values of ϵ_i in comparison to unity ($\epsilon_i \ll 1$). **The experimental estimation**
 225 **of ϵ_i values in the case of the pressure and temperature driven flows are given in Section 4.3.**

226 To obtain a pressure variation with time in both reservoirs, an initial pressure difference (pressure
 227 gradient experiments) or an initial temperature difference (temperature gradient experiments) must be
 228 imposed between the two tanks. Since the behavior of pressure inside the upstream and downstream
 229 tanks differs from the pressure gradient to the temperature gradient experiments, they will be explained
 230 separately.

231 4.1. Pressure gradient driven flow

232 A brief explanation of the steps followed during the pressure gradient experiments is given below using
 233 the sketch of the experimental setup presented in Fig. 1. Firstly, before performing the measurements
 234 with a gas, the whole system is pumped down during 12 hours with all the valves kept open, except the
 235 valves V_G . After this period, the valve V_P is closed and one of the valves V_G is opened, depending on the
 236 gas to be used, to fill the whole system with the chosen gas. Thereafter, the valves V_A and V_C are closed to
 237 stop the connections between the microchannel with the gas bottles and vacuum pump. Additionally, the
 238 micro-valve is closed too, then tanks 1 and 2 are connected only through the microchannel. After that, the
 239 initial pressure difference $\Delta p(t_0) = p_1(t_0) - p_2(t_0)$ (or with other notation: $\Delta p_0 = p_{1,0} - p_{2,0}$) is imposed
 240 between the two tanks by quickly opening and closing the valve V_A , while the valve V_P is kept open.
 241 Immediately after the opening and closing of the valve V_A , at $t = t_0$, the pressure inside the downstream
 242 tank, p_2 , suffers a drastic reduction, while the pressure inside the upstream tank, p_1 , does not change
 243 due to the high restriction imposed by the microchannel. **Comments about the possible non-isothermal**
 244 **effects at this stage can be found in Appendix A.** After that, for $t > t_0$, the pressure inside the upstream
 245 tank, p_1 , starts to decrease while the pressure inside the downstream tank, p_2 , starts to increase, until
 246 both pressures reach the same final value, p_f . The time when the pressures in both tanks become equal
 247 is denoted t_f and its practical definition is given in the end of this section. The behavior of the pressures
 248 inside the two tanks mentioned above for a generic pressure gradient experiment is shown in Fig. 6. The
 249 experiments for other different initial pressures are performed by opening and closing the valve V_A , keeping
 250 the valve V_P opened, and waiting to the stabilization of pressures in both tanks.

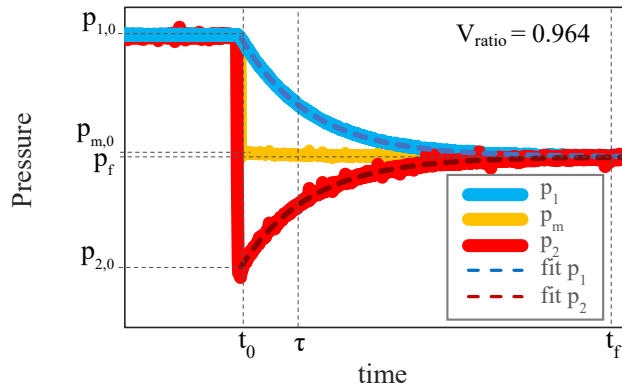


Figure 6: Behavior of upstream, $p_1(t)$, downstream, $p_2(t)$, and mean, $p_m(t) = 0.5(p_1(t) + p_2(t))$, pressures as function of time in a generic pressure gradient experiment. The exponential fittings of p_1 and p_2 are shown by dashed lines.

251 During the experiments, both tanks are kept at room temperature without any external heat sources.
 252 In addition, the amount of gas inside the microchannel is small and cannot considerably change the tank
 253 temperature because of the large thermal inertia of the tanks. During each experimental run, the external
 254 temperature of each tank was monitored, then its mean value over an experimental duration, \bar{T} , and

255 corresponding standard deviation, s , are calculated. Both quantities appear as a pertinent evaluation of
 256 the probable temperature variations in the tanks as $dT_i/T_i \approx s_i/\bar{T}_i$, $i = 1, 2$. These values were found less
 257 than 0.0002 for both low and high pressure sides and they are associated to the corresponding temperature
 258 variations dT_i/T_i , $i = 1, 2$. The pressure variations in the high pressure tank was found in the range of
 259 $0.03 < dp_1/p_1 < 0.24$, while the pressure variations in the lower tank are higher and lay in the range of
 260 $0.03 < dp_2/p_2 < 0.46$. Therefore, the values of ϵ_i parameters, present in Eqs. (4), are estimated to be
 261 in the range of $0.0008 < \epsilon_1 < 0.006$ and $0.0004 < \epsilon_2 < 0.006$ for the higher and lower pressure tanks,
 262 respectively, being very low for all the pressure driven experiments, see Table 4. Based on that, the mass
 263 flow rate for these experiments can be extracted from the measurements of pressure variation in any of
 264 the tanks, using one of Eqs. (5).

265 To obtain the mass flow rate through the microchannel from Eqs. (5), the derivative of the pressure
 266 in time must be calculated. According to Refs. [29, 30], we assume that the pressure variation in the
 267 upstream and downstream tanks can be represented as exponential functions in the following form:

$$p_1(t) = p_f + (p_{1,0} - p_f) \exp(-(t - t_0)/\tau_1), \quad p_2(t) = p_f + (p_{2,0} - p_f) \exp(-(t - t_0)/\tau_2), \quad (6)$$

268 where τ_1 and τ_2 are the pressure relaxation times for the upstream and downstream tanks, respectively.
 269 The exponential form of pressure variation in time, Eqs. (6), was obtained under assumption of constancy
 270 of the pressure relaxation time during an experiment [30]. The pressure difference between the tanks can
 271 be presented analogously as:

$$\Delta p(t) = \Delta p(t_0) \exp(-(t - t_0)/\tau). \quad (7)$$

272 As this relaxation time depends on the mean pressure, the constancy of the mean pressure in time insures
 273 the constancy of τ , and so the validity of Eqs. (6). In the following, we derive the conditions of the mean
 274 pressure constancy in the pressure driven experiments.

275 From the ideal gas law, Eq. (2), and considering the mass conservation along the microchannel at any
 276 time, it is possible to obtain an expression relating the pressure variation in both tanks, dp_1 and dp_2 , with
 277 the volume ratio $V_{ratio} = V_1/V_2$, when the tanks are kept at the same temperature:

$$dp_1 V_1 = -dp_2 V_2. \quad (8)$$

278 By integrating the previous relation from the initial stage of experiment, with pressures $p_{1,0} = p_1(t_0)$ and
 279 $p_{2,0} = p_2(t_0)$, to the final stage, when the pressures are equal in both tanks, $p_1(t_f) = p_2(t_f) = p_f$, we
 280 obtain the following expression:

$$\frac{p_{1,0} - p_f}{p_f - p_{2,0}} = \frac{V_2}{V_1}, \quad (9)$$

281 which allows to control the amplitude of the pressure variation in both tanks between its initial value,
 282 $p_{i,0}$, and its final value, p_f , by changing the volume ratio. From Eq. (9), it is still possible to obtain
 283 another expression to calculate the variation of the mean pressure from the beginning of the experiment,
 284 $p_{m,0} = 0.5(p_{1,0} + p_{2,0})$, to its end, $p_{m,f} = p_f$, as:

$$\frac{p_f}{p_{m,0}} = \frac{2(1 + V_{ratio} p_{ratio})}{(1 + V_{ratio})(1 + p_{ratio})}, \quad (10)$$

285 where $p_{ratio} = p_{1,0}/p_{2,0}$. When the volumes are equal, it follows from Eq. (10) that the mean pressure
 286 does not vary during an experiment and $p_f = p_{m,0}$. Considering that the total volumes of each side
 287 of the microchannel are different, that is V_{ratio} is different from 1, the mean pressure may vary during
 288 an experiment. From a known volume ratio and using Eq. (10), we can calculate the maximum initial
 289 pressure ratio which ensures the mean pressure constancy with some given accuracy. The volume ratio,
 290 V_{ratio} , used in the pressure gradient experiments, is equal to 0.964, see Table 1, thus to ensure the maximal

291 mean pressure variation of the order of 1%, according to Eq. (10), we have to set the initial pressure ratio,
 292 p_{ratio} , less than 3.45. Therefore, in all the experiments this pressure ratio was fixed smaller than 3.

293 In practice, we have to define a time interval to fit the pressure (or pressure difference variation) in
 294 time for each experimental run. In pressure driven experiments, we fit the values of pressure difference
 295 up to time moment t_τ defined as $\Delta p(t_\tau) = \varepsilon_\tau \Delta p(t_0)$, where ε_τ is a low-value parameter. As the pressure
 296 difference between the tanks follows an exponential decay, Eq. (7), we associate this time t_τ to the
 297 relaxation time as $t_\tau = t_0 - \tau \ln \varepsilon_\tau$. In experiments we fix the value of ε_τ equal to 0.02, so the fitting
 298 time becomes $t_\tau = t_0 + 3.9\tau$. The final experimental time is usually longer than the fitting time and it is
 299 defined as $t_f = t_0 + 7\tau$, which corresponds to 0.1% of deviation of the pressure difference from zero. This t_f
 300 parameter means the time where the pressure equilibrium is asymptotically reached. Since the final time
 301 is proportional to the relaxation time, it depends on the gas species, pressure level and reservoirs sizes.

302 **Respecting the condition for the constancy of the pressure relaxation time and using the mass conser-**
 303 **vation property we can write that $\tau_1 = \tau_2 = \tau$.** By calculating the derivative of pressure variation in time,
 304 Eq. (6), and replacing it in Eq. (5), we obtain the expressions for the mass flow rate in each tank:

$$\dot{M}_1(t) = \frac{V_1}{\mathcal{R}T} \frac{p_f - p_{1,0}}{\tau} \exp\left(-\frac{(t-t_0)}{\tau}\right), \quad \dot{M}_2(t) = \frac{V_2}{\mathcal{R}T} \frac{p_f - p_{2,0}}{\tau} \exp\left(-\frac{(t-t_0)}{\tau}\right). \quad (11)$$

305 As it was explained in Ref. [30], in the case of isothermal flow, the mass flow rate can be also calculated
 306 from the pressure difference variation in time, $\Delta p(t) = p_1(t) - p_2(t)$, as following:

$$\dot{M}(t) = \frac{V_0}{\mathcal{R}T} \frac{\Delta p_0}{\tau} \exp\left(-\frac{(t-t_0)}{\tau}\right), \quad V_0 = \frac{V_1 V_2}{V_1 + V_2}, \quad (12)$$

307 where V_0 is the reduced volume. From mass conservation property we have $-\dot{M}_1(t) = \dot{M}_2(t) = \dot{M}(t)$.
 308 **This equality is satisfied in the steady-state flow regime.**

309 4.2. Temperature gradient driven flow

310 It is known that when a temperature gradient is applied along the axis of a microchannel connected
 311 to two reservoirs of infinite volume maintained at the same pressure but at different temperatures, the
 312 gas inside this channel flows continuously from the colder to the hotter side [31]. This phenomenon is
 313 called thermal transpiration. When the volumes connected by a microchannel are finite, the counterflow,
 314 from the hot to the cold tank is generated, which leads to a steady state situation, when the temperature
 315 gradient driven flow is counterbalanced by the pressure gradient driven flow, and the total mass flow rate
 316 through a channel becomes zero.

317 A short description of the specificity of the temperature gradient driven flow experiments is presented
 318 below. Firstly, before performing the measurements with a certain gas, the water cooling of the upstream
 319 tank (tank 1 or cold tank) and the electrical heater inserted in the downstream tank (tank 2 or hot tank)
 320 are turned on. After that, the whole system is connected to the vacuum pump during 12 hours, as it was
 321 done for the pressure gradient experiments. After that, the temperatures of both tanks are stabilized and
 322 the whole system is under vacuum conditions. Then, the system is fulfilled with the gas to be tested, by
 323 following the same steps as it was done for the pressure gradient experiments. After the chosen working gas
 324 fulfills the system, the valve V_A is closed, see Fig. 1. At this moment, even with the imposed temperature
 325 difference between the hot and cold tanks, the gas pressure inside both tanks is exactly the same, since the
 326 micro-valve is still open, and, consequently, the gas can flow from one tank to another not only through
 327 microchannel but also through the secondary line (a large diameter pipe system), see Fig. 1. This fact of
 328 the pressure equality, $p_1(t) = p_2(t) = p_0$, can be clearly seen in Fig. 7, when $t < t_0$.

329 At time t_0 , the micro-valve is closed. From this moment, the two tanks are connected only by the
 330 microchannel, where the gas flows from the cold side to the hot one, so the thermal transpiration flow

331 [23, 31] takes place in the microchannel. This thermal creep flow immediately generates an increase in the
 332 pressure inside the hot tank and a decrease in the pressure inside the cold tank. This pressure difference
 333 between the tanks leads to the appearance of a counterflow, so called Poiseuille flow, from the high pressure
 334 side to the low pressure one, that is in the opposite direction to the thermal transpiration flow. To sum
 335 up, from time t_0 , there is an increase in pressure $p_2(t)$ (hot tank) and a decrease in pressure $p_1(t)$ (cold
 336 tank), as it can be seen in Fig. 7(a).

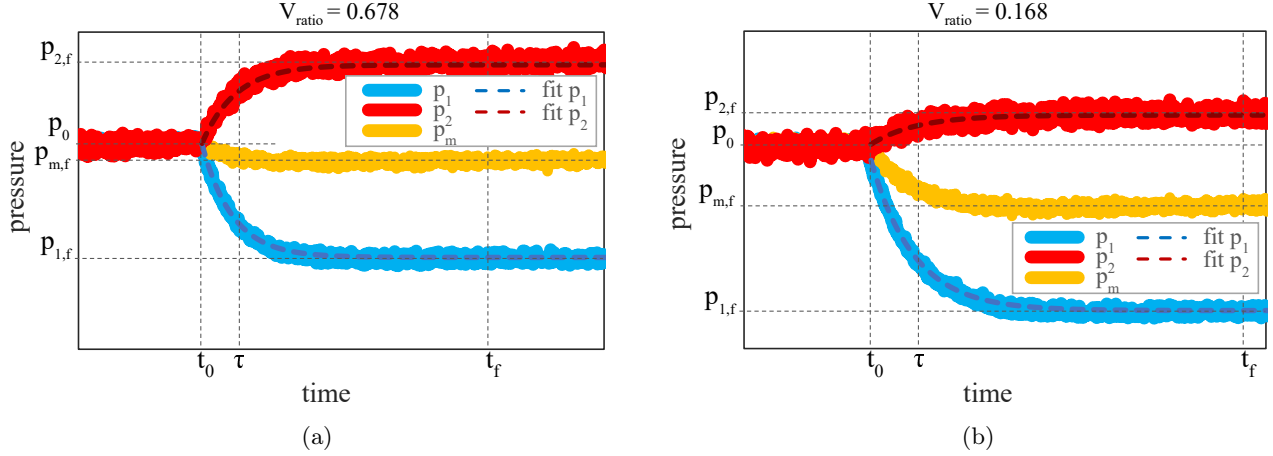


Figure 7: Behavior of cold-side, $p_1(t)$, hot-side, $p_2(t)$, and mean, $p_m(t)$, pressures as function of time in a generic temperature gradient experiment for two different volume ratios: (a) $V_{ratio} = 0.678$ and (b) $V_{ratio} = 0.168$. The exponential fittings of $p_1(t)$ and $p_2(t)$ are also shown by the dashed lines.

337 When the Poiseuille flow reaches the same magnitude as that of the thermal transpiration flow, the
 338 net mass flow rate through the microchannel becomes zero and the pressures inside both tanks achieve
 339 constant but different values, $p_{1,f}$ and $p_{2,f}$, in the cold and hot reservoirs, respectively, as it can be seen
 340 in Fig. 7(a). As for the pressure driven flow, see Section 4.1, we define the final experimental time in
 341 terms of the relaxation time as $t_f = 7\tau + t_0$. Also in the temperature driven experiments, the fitting of
 342 the pressure variation in the cold tank is done during the fitting time t_τ , which is calculated for this tank
 343 as $p_1(t_\tau) - p_f = \varepsilon_\tau(p_{1,0} - p_f)$, with $\varepsilon_\tau = 0.02$.

344 When this zero flow condition is achieved, an important characteristic of the temperature gradient
 345 driven flow can be obtained, the Thermomolecular Pressure Difference (TPD), which is defined by the
 346 difference between the pressures inside the hot and cold tanks, respectively, according to the following
 347 expression:

$$\text{TPD} = p_{2,f} - p_{1,f} = \Delta p_1 + \Delta p_2, \quad (13)$$

348 where $\Delta p_1 = p_0 - p_{1,f}$ and $\Delta p_2 = p_{2,f} - p_0$.

349 Since the temperatures of each tank are constant during an experiment, we can use the same reasoning
 350 as presented in Section 4.1 and make use of expressions (5) to calculate the mass flow rate if the ratios of
 351 the thermal fluctuations to the pressure fluctuations, *i.e.* ϵ_i ($i = 1, 2$), Eq. (4), are small enough compared
 352 to unity. The estimations of ϵ_i are provided in Section 4.2.1.

353 The pressure variation inside both cold and hot tanks can be approximated using the relations [24, 32,
 354 33]:

$$p_1(t) = p_{1,f} + (p_0 - p_{1,f}) \exp(-(t - t_0)/\tau_1), \quad p_2(t) = p_{2,f} + (p_0 - p_{2,f}) \exp(-(t - t_0)/\tau_2), \quad (14)$$

355 where τ_1 and τ_2 are the relaxation times for the cold and hot volumes, respectively. The behaviors of
 356 these relaxation parameters will be discussed in Section 6. Taking the time derivative of the pressure

357 variation in each tanks, Eqs. (14), and replacing it in each of Eqs. (5), we obtain the expressions for the
 358 temperature gradient driven mass flow rates:

$$\dot{M}_1 = \frac{V_1}{\mathcal{R}T_1} \frac{p_{1,f} - p_0}{\tau_1} \exp\left(-\frac{(t - t_0)}{\tau_1}\right), \quad \dot{M}_2 = \frac{V_2}{\mathcal{R}T_2} \frac{p_{2,f} - p_0}{\tau_2} \exp\left(-\frac{(t - t_0)}{\tau_2}\right). \quad (15)$$

359 As explained above, the maximum mass flow rate generated by the temperature difference in present
 360 experiments is realized at $t = t_0$, since at that moment, the Poiseuille counter flow is still negligible. If
 361 we evaluate mass flow rate, Eq. (15), at the instant t_0 , we obtain the expressions for the temperature
 362 gradient driven mass flow rates:

$$\dot{M}_1 = \frac{V_1}{\mathcal{R}T_1} \frac{p_{1,f} - p_0}{\tau_1}, \quad \dot{M}_2 = \frac{V_2}{\mathcal{R}T_2} \frac{p_{2,f} - p_0}{\tau_2}. \quad (16)$$

363 4.2.1. Influence of additional volume in the hot side

364 The initial idea for the temperature gradient experiments was to perform the measurements without
 365 considering the additional reservoirs 1 and 2, *i.e.* the valves V_{R1} and V_{R2} would remain closed during all
 366 the experiments. In this configuration, the total volumes of the cold and hot sides are equal to 12.6cm^3
 367 and 18.6cm^3 , respectively. For the lighter gases, such as helium and neon, this volume configuration
 368 could be perfectly used, since the amplitude of pressure variation in the cold tank is sufficiently high for
 369 the whole covered pressure range. However, for heavier gases such as argon and krypton, the amplitude
 370 of pressure variation inside the tanks is considerably lower, mainly for high pressures. In this case, it
 371 becomes very difficult to fit the pressure variation in the cold tank with an exponential function, because
 372 the instantaneous pressure fluctuations start to be very important compared to the pressure variation in
 373 time. Figure 8 shows the pressure variation inside the hot and cold tanks for helium (Fig. 8a) and krypton
 374 (Fig. 8b) considering the same temperature difference and the same level of gas rarefaction. It is clear
 375 that the pressure variation inside the cold tank is much higher for helium ($\sim 3\text{Pa}$) than for krypton (\sim
 376 1Pa). Consequently, in the case of krypton, the fluctuations of the pressure signal are more significant
 377 compared to the total pressure variation in a tank, so it is difficult to fit the pressure behavior with the
 378 exponential function with a good accuracy.

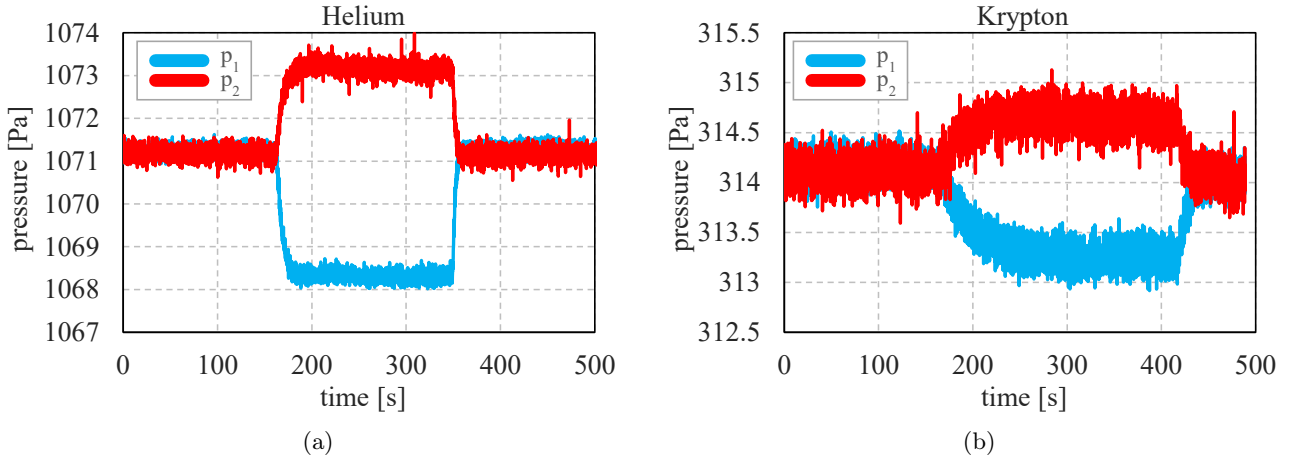


Figure 8: Behavior of the pressure variation inside the hot and cold tanks in temperature gradient experiments using (a) helium and (b) krypton. The volume ratio, rarefaction parameter and temperature difference between the tanks used in both experiments are $V_{ratio} = 0.678$ and $\Delta T = 58^\circ\text{C}$, respectively.

379 To overcome this problem of very small amplitude of the pressure variation in the cold tank, the
 380 total volume of the hot side was increased by including an additional reservoir connected to the system

381 by the valve V_{R2} , see Fig. 1. For this new volumes configuration, the increase in the amplitude of the
 382 pressure variation in the cold side due to the change of the volume ratio between hot and cold sides can be
 383 estimated. As it was shown in Section 4.1, the amplitude of the pressure variation in each tank is related
 384 to the volume of the tanks. However, in the case of the temperature gradient driven flow, Eq. (8) needs
 385 to be modified to take into account the different temperatures of the tanks, so it becomes:

$$dp_1 \frac{V_1}{T_1} = -dp_2 \frac{V_2}{T_2}. \quad (17)$$

386 By integrating this equation between initial, t_0 , and final, t_f , time instants, we have:

$$\Delta p_1 = \Delta p_2 \frac{V_2 T_1}{V_1 T_2}. \quad (18)$$

387 By using Eq. (18), the amplitude of the pressure variation in the cold tank can be estimated for both
 388 volume configurations.

389 By comparing Figs. 7a and 7b it can be observed that the amplitudes of the pressure variation inside
 390 the cold and hot tanks are changed when the volume ratio is modified. For the first scenario, Fig. 7a, when
 391 $V_1 = 12.6\text{cm}^3$ and $V_2 = 18.6\text{cm}^3$, $V_2/V_1 = 1.476$, and $T_1/T_2 = 0.831$ the amplitude of the pressure variation
 392 inside the cold tank is approximately 1.23 times higher than the amplitude of the pressure variation inside
 393 the hot tank, *i.e.* $\Delta p_1 \approx 1.23\Delta p_2$. However, for the second scenario, Fig. 7b, where $V_1 = 12.6\text{cm}^3$ and
 394 $V_2 = 75.3\text{cm}^3$, $V_2/V_1 = 5.976$, the amplitude of the pressure variation inside the cold tank is much higher
 395 than the amplitude of pressure variation inside the hot tank, *i.e.* $\Delta p_1 \approx 4.87\Delta p_2$. Therefore, for the
 396 second setup configuration with the highest difference between the volumes, the amplitude of the pressure
 397 variation in the cold side increases considerably, reducing consequently the importance of its fluctuations,
 398 then increasing the accuracy of exponential fit of the pressure curve. Besides, for the experiments carried
 399 out with additional volume at the hot side, the experiment duration increases, since the relaxation time
 400 is also increase, *i.e.* it takes more time to achieve the stabilization of the pressures in both tanks.

401 During each experiment, which always lasts no longer than 6 minutes, the temperature is monitored by
 402 an IR camera. The mean value of the temperature, \bar{T}_i , and its standard deviation, s_i , are calculated. As
 403 for the pressure driven flows, the ratio s/\bar{T}_i is assumed to be a pertinent representation of the temperature
 404 variation. The temperature fluctuations in the cold tank are found to be $dT_1/T_1 \approx 7 \cdot 10^{-5}$, while in the hot
 405 tank they are $dT_2 \approx 6 \cdot 10^{-5}$. On the other hand, the pressure fluctuations in the cold side are higher than
 406 that at the hot side and they are in the ranges of $0.001 < dp_1/p_1 < 0.03$ and $0.0002 < dp_2/p_2 < 0.004$,
 407 respectively. Summing up, the temperature fluctuations are relatively small compared to the pressure
 408 fluctuations in the cold tank, *i.e.* ϵ_1 is lower than 0.05. However, for the hot tank, the pressure fluctuations
 409 are very small, especially for heavier gases, and for these cases, ϵ_2 is of the order of 0.30. Therefore, it is
 410 not possible to extract the mass flow rate from the pressure measurements in the hot tank (tank 2) using
 411 Eq. (4) (or derived from it under condition of smallness of ϵ_2 , right-hand side of Eq. (16)), because ϵ_2
 412 becomes not small enough compared to unity. In the following, only the measurements made in the cold
 413 side are presented and analyzed.

414 4.3. Uncertainty measurement of the mass flow rate

415 The classical uncertainty calculation technique is used to estimate the measurement uncertainty of
 416 the mass flow rate when it is calculated from the pressure evolution for both pressure and temperature
 417 gradient experiments, Eqs. (11) and (15) respectively. The general expression of uncertainty on the mass
 418 flow rate measurements reads:

$$\frac{\delta \dot{M}_i}{\dot{M}_i} = \frac{\delta V_i}{V_i} + \frac{\delta p_i}{p_i} + \frac{\delta T_i}{T_i} + \frac{\delta \tau}{\tau}, \quad i = 1, 2. \quad (19)$$

419 All the terms presented in the right-hand side of Eq. (19) are described below and their estimations are
 420 given in Table 4. As it was explained in previous section, for the temperature gradient experiments, the
 421 measurements are carried out in the cold side only.

422 To measure the uncertainty of the volume V_i , $\delta V_i/V_i$, a reference reservoir with known volume is used
 423 and the pressure is measured inside this volume [30]. The volume of the reference reservoir implemented
 424 in this procedure has already an uncertainty of approximately 2%. Taking into account the uncertainty on
 425 the internal volumes of the valves, open and closed during the procedure of the volume V_i measurement,
 426 and the uncertainty of the pressure transducers, the total uncertainty of volume is 3%.

427 The uncertainty on the pressure measurements is due to the uncertainty on the pressure sensors. This
 428 value is provided by the manufacturer and it varies from 0.2% to 0.4%, depending on the sensor type. The
 429 uncertainty on the temperature measurements is due to the uncertainty on the thermocouples, which is
 430 of the order of 0.3%, and uncertainty of the IR camera, which is of the order of 0.7%. As for the mass
 431 flow rate extraction, the values of the temperature obtained from the IR camera have been used, being
 432 the uncertainty of 0.7% provided in Table 4.

433 Finally, the uncertainty on the fitting parameter τ is obtained from the difference in magnitude of a
 434 95% confidence interval for τ to represent the experimental data. The value of this uncertainty is higher
 435 for temperature gradient experiments, due to the higher ratio between the fluctuation of the pressure
 436 signal and the pressure variation in time.

437 In Table 4 we provide also two parameters which are not involved in Eqs. (11) and (15) for the mass
 438 flow rate determination, but which impact the uncertainty of its calculation. The first quantity is the
 439 value of ϵ_i , which represents the estimation of the non-isothermal effects, see also Section 4, Eq. (4).
 440 These ϵ_i terms were neglected when deriving Eqs. (11) and (15), therefore they do not appear in Eq. (19).
 441 However, the providing of these terms should give the idea on the accuracy of the model used for the mass
 442 flow rate extraction. This is why we included the values of ϵ_i in the total uncertainty on the mass flow
 443 rate. Finally, the last source of error in the mass flow rate measurement comes from the leakages, \dot{M}_{leak} ,
 444 mainly through the gap between the microchannel plates. The values of \dot{M}_{leak} are also provided in Table
 445 4 and they are included in $\delta \dot{M}_i/\dot{M}_i$ calculations.

446 As it can be seen in Table 4, the uncertainties of the mass flow rate for pressure gradient experiments
 447 are very similar for high pressure and low pressure tanks. In the following, the data coming from the
 448 measurements in low pressure tank are provided. For the temperature gradient experiments only uncer-
 449 tainties for the cold tank are given in Table 4, since the pressure variations in the hot tank were very small
 450 compared to the initial pressure, especially for the high pressure experiments, which has lead to the fact
 451 that ϵ_2 parameter becomes too high (of the order of 0.3) compared to unity and so cannot be neglected
 452 in the expression of mass flow rate (Eq. (4)), see also the comments in Section 4.2.1. In the following, the
 453 data measured in the cold tank are used and analyzed.

454 It should be also mentioned that the maximum values of uncertainties are presented in Table 4. For
 455 example, the uncertainty on the fitting parameter τ is higher for heavier gases than for lighter ones, but
 456 the value obtained for krypton is provided in Table 4. On the other hand, the leakage uncertainties are
 457 higher for light gases, thus, the uncertainty of helium leakage is provided.

Table 4: Measurement of uncertainties of mass flow rate, when the pressure exponential evolution inside the tanks is used for the calculation. The results are presented for pressure (PGDF) and temperature (TGDF) gradient driven flows.

Uncertainty	$\delta V_i/V_i$	$\delta p_i/p_i$	$\delta T_i/T_i$	$\delta \tau/\tau$	ϵ_i	\dot{M}_{leak}	$\delta \dot{M}_i/\dot{M}_i$
Tank 1 - PGDF	3.0%	0.2%	0.7%	<0.8%	<0.6%	<0.8%	<6.1%
Tank 2 - PGDF	3.0%	0.4%	0.7%	<0.8%	<0.6%	<0.8%	<6.3%
Tank 1 - TGDF	3.0%	0.2%	0.7%	<1.2%	<5.0%	<2.0%	<12.1%

458 **5. Background Theory**

459 In this section, firstly, several definitions related to the gas description at molecular level are intro-
 460 duced. Then, the main relations used in the experimental extraction of the velocity slip, thermal slip and
 461 accommodation coefficients in the case of the pressure and temperature gradient flows are presented. A
 462 short description of the two gas-surface interaction models, the Maxwell specular-diffuse model [1] and the
 463 Cercignani-Lampis model [6], may be found in [Appendix C](#).

464 *5.1. General definitions*

465 The mass flow rate through the same rectangular microchannel was obtained from pressure gradient
 466 experiments for the Knudsen number range of $0.0016 < Kn < 0.12$, which means for the hydrodynamic and
 467 slip flow regimes, and from temperature gradient flows for the Knudsen number range of $0.05 < Kn < 0.45$,
 468 which corresponds to the slip and beginning of transitional flow regimes. The Knudsen number is calculated
 469 by using the channel height, H , as the characteristic flow dimension:

$$Kn = \frac{\ell}{H}, \quad (20)$$

470 where ℓ is the equivalent molecular free path, calculated as:

$$\ell = \frac{\mu}{p} \sqrt{2\mathcal{R}T}, \quad (21)$$

471 being μ the viscosity of the gas, calculated according to following expression [34]:

$$\mu = \mu_{ref} \left(\frac{T}{T_{ref}} \right)^\omega, \quad (22)$$

472 where μ_{ref} is the gas viscosity at reference temperature $T_{ref} = 273.15\text{K}$ and ω is the viscosity index. The
 473 rarefaction parameter is also used in the following and it is defined as the inverse of the Knudsen number:

$$\delta = \frac{H}{\ell} = \frac{1}{Kn}. \quad (23)$$

475 *5.2. Pressure gradient driven flow*

476 The pressure gradient driven flows through a channel of a rectangular cross-section were intensively
 477 studied in the last decades. Some numerical and analytical results can be found in Refs. [35, 36, 37]. In
 478 our analysis we used the following expression for the mass flow rate obtained from the Stokes equation
 479 with the first-order velocity slip boundary condition [37]:

$$\dot{M} = \dot{M}_P \left(1 + 6\sigma_p \frac{T_n}{S_n} Kn \right), \quad (24)$$

480 where \dot{M}_P is the Poiseuille mass flow rate, defined as:

$$\dot{M}_P = \frac{H^3 W (1 - \mathcal{K}) \Delta p p_m}{12\mu \mathcal{R} T L}, \quad (25)$$

481 being σ_p the velocity slip coefficient [38, 39] and $p_m = (p_1 + p_2)/2$ the mean pressure. The coefficient \mathcal{K}
 482 allows taking into account the influence of the lateral walls on the Poiseuille mass flow rate, Eq. (25), and
 483 it is obtained from [35, 37]:

$$\mathcal{K} = 192 \frac{H}{W} \sum_{i=0}^{\infty} \frac{1}{n^5} \tanh \left(\frac{nW}{2H} \right), \quad n = \pi(2i + 1). \quad (26)$$

484 The coefficients T_n and S_n in Eq. (24) allow taking into account the influence of the lateral walls on the
 485 mass flow rate in slip flow regime and they are calculated from the following expressions [37]:

$$T_n = \frac{4}{3}S_n - \frac{1}{3} \left(1 - \frac{H}{W}\right) \sum_{n=0}^{\infty} \frac{\tanh^2(0.5\pi(2n+1)W/H)}{(2n+1)^4}, \quad (27)$$

486

$$S_n = \frac{\pi^4}{96} - \frac{2H}{\pi W} \sum_{n=0}^{\infty} \frac{\tanh(0.5\pi(2n+1)W/H)}{(2n+1)^5}. \quad (28)$$

487 It should be mentioned that the equivalent molecular free path, ℓ , Eq. (21), and, consequently, Knudsen
 488 number, Kn , Eq. (20), are calculated here using the mean pressure p_m .

489 The mass flow rate, Eq. (24), can be presented also in the dimensionless form:

$$S^T = \dot{M}/\dot{M}_P = 1 + 6\sigma_p \frac{S_n}{T_n} Kn = C_0^T + C_1^T Kn, \quad (29)$$

490 where

$$C_0^T = 1, \quad C_1^T = 6\sigma_p \frac{S_n}{T_n}. \quad (30)$$

491 We can fit the measured dimensionless mass flow rate analogously to Eq. (29) form as a function of
 492 Knudsen number

$$S^F = C_0^F + C_1^F Kn, \quad (31)$$

493 and then extract the velocity slip from the relation $C_1^T = C_1^F$, as following:

$$\sigma_p = \frac{C_1^F}{6} \frac{T_n}{S_n}. \quad (32)$$

494 When the velocity slip coefficient for each pair gas-surface is extracted from Eq. (32), then the accom-
 495 modation coefficient can be also obtained. The authors of Ref. [40] calculated the velocity slip coefficient
 496 for a given accommodation coefficient using kinetic modeling, namely the BGK model, and the Maxwell
 497 specular-diffuse scattering kernel. Then, a simple expression associating the slip and accommodation
 498 coefficients was proposed:

$$\sigma_p(\alpha) = \frac{2-\alpha}{\alpha} (\sigma_p(1) - 0.1211(1-\alpha)), \quad (33)$$

499 where α is the accommodation coefficient and $\sigma_p(1)$ is the slip coefficient for $\alpha = 1$, being $\sigma_p(1) = 1.016$
 500 [38].

501 The second order (in Knudsen number) polynomial fit was used recently by several authors to extract
 502 the accommodation coefficient from the pressure driven flows [13, 15, 41, 42]. The comparison between the
 503 fit of the experimental data of helium to the polynomial of first and second orders was carried out in the
 504 Knudsen number ranges of [0.0016; 0.12] and [0.0016; 0.67], respectively. It was found that the difference
 505 between the accommodation coefficients derived from the respective fits is of the order of 0.1%, see Table
 506 B.13, so the first order polynomial fit is used for the coefficient extraction. The values of the velocity
 507 slip and accommodation coefficients for each gas-surface pair, obtained for the five analyzed gases, are
 508 provided in Section 6.

509 5.3. Temperature gradient driven flow

510 As it was underlined in Section 4.2, the thermal creep flow is evaluated at instant t_0 , where the pressures
 511 in both tanks are equal between them and the counter flow from the hot side to the cold one did not start
 512 yet. At this stage of established thermal creep between two tanks with different temperatures and equal

513 pressures, a very small pressure gradient is generated inside the microchannel [25, 43, 44, 45, 46]. The
 514 total mass flow rate \dot{M} through the channel can be presented as

$$\dot{M} = -\dot{M}_P + \dot{M}_T, \quad (34)$$

515 where \dot{M}_P is the pressure driven flow rate induced by the thermal creep flow and \dot{M}_T is the thermal creep
 516 mass flow rate. The pressure profile along the channel has a parabolic shape, with maximum value near
 517 to its central point and it was numerically established in Refs. [43, 44]. Using the previously developed
 518 kinetic modeling, the authors of Ref. [25] estimated the ratio \dot{M}_P/\dot{M} in the case of very similar temperature
 519 gradients and in the case of the flow through a rectangular microchannel to be smaller to 0.2%. Therefore,
 520 the total measured mass flow rate could be identified to temperature driven mass flow rate as

$$\dot{M} \approx \dot{M}_T. \quad (35)$$

521 To obtain an explicit expression of the mass flow rate driven by thermal transpiration \dot{M}_T in the slip flow
 522 regime, the Stokes equation subjected to the thermal slip boundary conditions in the following form

$$u_{\text{slip}} = \sigma_T \frac{\mu}{\rho T} \frac{dT}{dx} \quad (36)$$

523 was integrated over the channel cross-section. Then, the mass flow rate reads [3, 25]:

$$\dot{M}_T = \sigma_T HW \frac{\mu}{T} \frac{dT}{dx}. \quad (37)$$

524 In previous expressions, σ_T is the thermal slip coefficient [3], ρ is the gas density and dT/dx is the
 525 temperature gradient along the channel walls in the x -direction. The thermal slip coefficient could be
 526 extracted from Eq. (37) if the temperature gradient along the channel is known [25]. However, this is
 527 only a first order solution according to the Knudsen number and it is not accurate enough [25, 46]. The
 528 higher-order solution for the dimensionless temperature driven mass flow rate between two infinite parallel
 529 plates was obtained from the kinetic theory in Ref. [47]:

$$\dot{M}_T = HW \frac{\mu}{T} \frac{dT}{dx} \left(C_0^T + \frac{C_1^T}{\delta} + \frac{C_2^T}{\delta^2} + O\left(\frac{1}{\delta^3}\right) \right), \quad (38)$$

530 where the values of the two coefficients C_0^T and C_1^T were calculated in Ref. [47], being equal to $C_0^T = 0.9924$
 531 and $C_1^T = -1.3284$. Following the authors of Refs. [25, 46], we integrated this asymptotic solution, but
 532 up to the term of the order of $O(1/\delta^3)$, so the expression for the mass flow rate becomes:

$$\dot{M}_T = \dot{M}_{\text{ref}} \left(C_0^T + \frac{C_1^T C'_1}{\delta_m} + \frac{C_2^T C'_2}{\delta_m^2} + O\left(\frac{1}{\delta_m^3}\right) \right), \quad (39)$$

533 where

$$\dot{M}_{\text{ref}} = \frac{HW \mu_{\text{ref}}}{T_{\text{ref}}^\omega} \frac{T_2^\omega - T_1^\omega}{\omega L}. \quad (40)$$

534 The mean value of the rarefaction parameter, δ_m , is calculated according to:

$$\delta_m = \frac{p_0 H}{\mu(T_m) \sqrt{2 \mathcal{R} T_m}}, \quad (41)$$

535 where $T_m = 0.5(T_1 + T_2)$ is the mean temperature; the viscosity coefficient is calculated also using this
 536 mean temperature. The term C_0^T in Eq. (39) can be identified as the thermal slip coefficient, σ_T . Two
 537 additional coefficients come from the integration of Eq. (38) along the channel and they are equal to

$$C'_1 = \frac{T_2^{2\omega+0.5} - T_1^{2\omega+0.5}}{(2\omega + 0.5) T_m^{\omega+0.5}} \frac{\omega}{T_2^\omega - T_1^\omega}, \quad C'_2 = \frac{T_2^{3\omega+1} - T_1^{3\omega+1}}{(3\omega + 1) T_m^{2\omega+1}} \frac{\omega}{T_2^\omega - T_1^\omega}. \quad (42)$$

538 The values of both coefficients are very close to one with a deviation less than 1%, so they are assumed to
 539 be equal to 1 in the following. Therefore, Eq. (39) can be rewritten in more convenient form by dividing
 540 it by the reference mass flow rate, \dot{M}_{ref} , and by neglecting the terms of the order of $O(1/\delta_m^3)$:

$$\mathcal{G}^T = \frac{\dot{M}_T}{\dot{M}_{\text{ref}}} = \mathcal{C}_0^T + \frac{\mathcal{C}_1^T}{\delta_m} + \frac{\mathcal{C}_2^T}{\delta_m^2} = \mathcal{C}_0^T + \mathcal{C}_1^T Kn_m + \mathcal{C}_2^T Kn_m^2. \quad (43)$$

541 As the fit in the polynomial form is more convenient compared to previous expression, we use the following
 542 expression to fit the experimental data

$$\mathcal{G}^F(Kn_m) = \frac{\dot{M}_T}{\dot{M}_{\text{ref}}} = \mathcal{C}_0^F + \mathcal{C}_1^F Kn_m + \mathcal{C}_2^T Kn_m^2. \quad (44)$$

543 in the slip and beginning of transitional flow regimes, $0.05 < Kn_m < 0.45$. The fitting coefficient \mathcal{C}_0^F is
 544 associated to the coefficient σ_T .

545 Finally, the accommodation coefficient, α , was calculated from the thermal slip coefficient by using
 546 the expression proposed in Refs. [3, 48] and obtained using the S-model kinetic equation with Maxwellian
 547 specular-diffuse boundary condition:

$$\sigma_T = 0.75(1 + 0.5\alpha). \quad (45)$$

548 For the case of a polyatomic gas such as nitrogen, it is necessary to take into account the effects of the
 549 internal degrees of freedom of the molecule, as formulated in the expression proposed in Refs. [49, 50],
 550 where the model of Hanson and Morse was used. Thus the expression of the thermal slip coefficient for a
 551 polyatomic gas reads:

$$\sigma_T = \frac{3}{10} f_{tr}(1 + 0.5\alpha), \quad (46)$$

552 where f_{tr} is the translational Eucken factor, which is equal to 2.25 for nitrogen [22].

553 The thermal slip and accommodation coefficients obtained from temperature gradient driven flow, as
 554 well as the fitting coefficients for all the five gases used in the present work (He, Ne, N₂, Ar and Kr), are
 555 presented in the next section.

556 6. Results

557 Several important parameters of the five gases used in the experiments are presented in Table 5: molar
 558 mass (\mathcal{M}), specific gas constant (\mathcal{R}), reference viscosity (μ_{ref}), viscosity index (ω), and reference most
 559 probable speed (v_{ref}). The reference viscosity and reference most probable speed are given considering the
 560 reference temperature, $T_{\text{ref}}=273.15\text{K}$. It should be noticed, that the viscosity and viscosity index, provided
 561 in Table 5, are taken from the widely used Ref. [34]. However, more recent data on both quantities are
 562 available in Refs. [51], [52].

Table 5: Characteristic parameters of all the five gases used in the experiments.

Parameter	He	Ne	N ₂	Ar	Kr
\mathcal{M} [g/mol]	4.003	20.18	28.00	39.95	83.80
\mathcal{R} [J/(kg.K)]	2078	412.0	296.8	208.1	99.22
$\mu_{\text{ref}} \times 10^5$ [Pa · s]	1.865	2.976	1.656	2.117	2.328
ω [-]	0.66	0.66	0.74	0.81	0.80
v_{ref} [m·s ⁻¹]	1066	474.4	402.8	337.2	234.0

563 Tables with initial and final pressures in the upstream tank and the mass flow rates extracted from
 564 both pressure gradient and temperature gradient driven flows are provided in Appendix D.

565 6.1. Pressure gradient driven flow

566 As explained in Section 5, the analytical expression of mass flow rate, Eq. (24), was obtained from the
 567 solution of the Stokes equation subjected to the first-order velocity slip boundary condition. Therefore,
 568 the measured mass flow rate was evaluated inside the Knudsen number range of $0.0016 < Kn < 0.12$.
 569 Figure 9a shows the measured dimensionless mass flow rate, $S = \dot{M}/\dot{M}_P$, as a function of the Knudsen
 570 number for all the five gases used in the experiments, while Fig. 9b represents this mass flow rate only for
 571 neon and argon, providing also the fitting curves of the affine fitting functions, Eq. (31), for both gases.

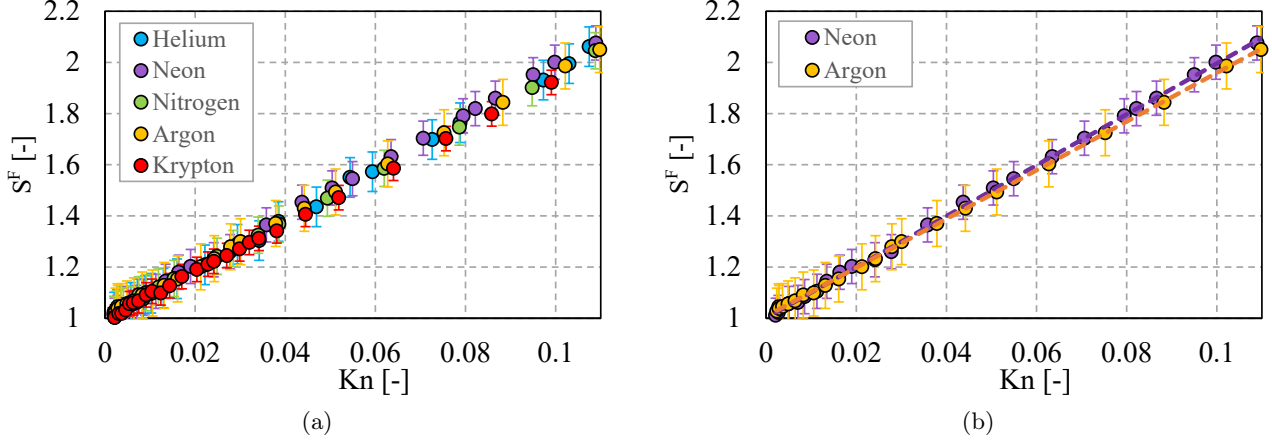


Figure 9: Dimensionless measured mass flow rate, $S^F = \dot{M}/\dot{M}_P$, (filled symbols) as a function of the Knudsen number: (a) for all the five gases used in the experiments; (b) for neon and argon with the affine fitting curves (dashed lines).

572 The fitting parameters, C_0^F and C_1^F , and the determination coefficient, r^2 , for all the five gases are
 573 presented in Table 6. The uncertainty of both fitting coefficients is estimated using the standard error. **The
 574 experimental uncertainty, provided in Table 4, is not added to the adjustment uncertainty. Finally, part of
 575 these uncertainties concerns the random uncertainty linked to the pressure and temperature measurements,
 576 so the influence of these uncertainties is taken into account by the adjustment procedure. The other part
 577 of the systematics uncertainties, such as volume uncertainty, is estimated to be very low. This conclusion
 578 could be obtained by analyzing the values of the coefficients C_0^F in Table 4. Its values are very close to
 579 one, which proves that the measured Poiseuille mass flow rate is obtained with good precision.**

580 As it can be seen in Table 6, the determination coefficient, r^2 , is very close to one, indicating that the
 581 linear regression fits very well to the measured mass flow rate values for all evaluated Knudsen number
 582 range. The values of fitting coefficient C_0^F are very close to one (deviation is lower than 2%) for all
 583 the gases, confirming the good approximation of the Poiseuille mass flow rate [27] **and therefore small
 584 systematic error of the measurements.**

Table 6: Determination coefficient, coefficients of affine fitting, velocity slip and accommodation coefficients obtained from pressure gradient experiments for the five gases.

Parameter	He	Ne	N ₂	Ar	Kr
r^2	0.9985	0.9988	0.9994	0.9998	0.9985
C_0^F	1.018 ± 0.004	1.010 ± 0.004	1.010 ± 0.002	1.019 ± 0.002	0.999 ± 0.003
C_1^F	9.597 ± 0.085	9.836 ± 0.072	9.418 ± 0.055	9.381 ± 0.035	9.922 ± 0.070
σ_p	1.545 ± 0.014	1.584 ± 0.012	1.517 ± 0.009	1.511 ± 0.006	1.485 ± 0.012
α_p^M	0.781 ± 0.004	0.768 ± 0.005	0.790 ± 0.003	0.792 ± 0.002	0.801 ± 0.004

585 The values of the velocity slip coefficient, calculated using Eq. (32), varies from 1.485 for krypton to
 586 1.584 for neon and they are relatively close one to another for all the analyzed gases. These values are far
 587 from 1.016, the value theoretically found in Ref. [38] for the complete accommodation (complete diffuse
 588 scattering).

589 The accommodation coefficients, α_p^M , obtained from Eq. (33), are also presented in Table 6. The
 590 subscript "p" is used to notify that these coefficients are obtained from the pressure driven experiments
 591 and the superscript "M" indicates that the coefficients are extracted using the Maxwell specular-diffuse
 592 kernel. The values of the accommodation coefficient, α_p^M , lie also in the narrow range from 0.768 for neon
 593 to 0.801 for krypton. For all gases, except helium, the dependency from the mass is clearly seen: the
 594 accommodation coefficient is closer to one for the heavier gases. However, it is difficult to explain why the
 595 accommodation coefficient of helium does not follow this trend.

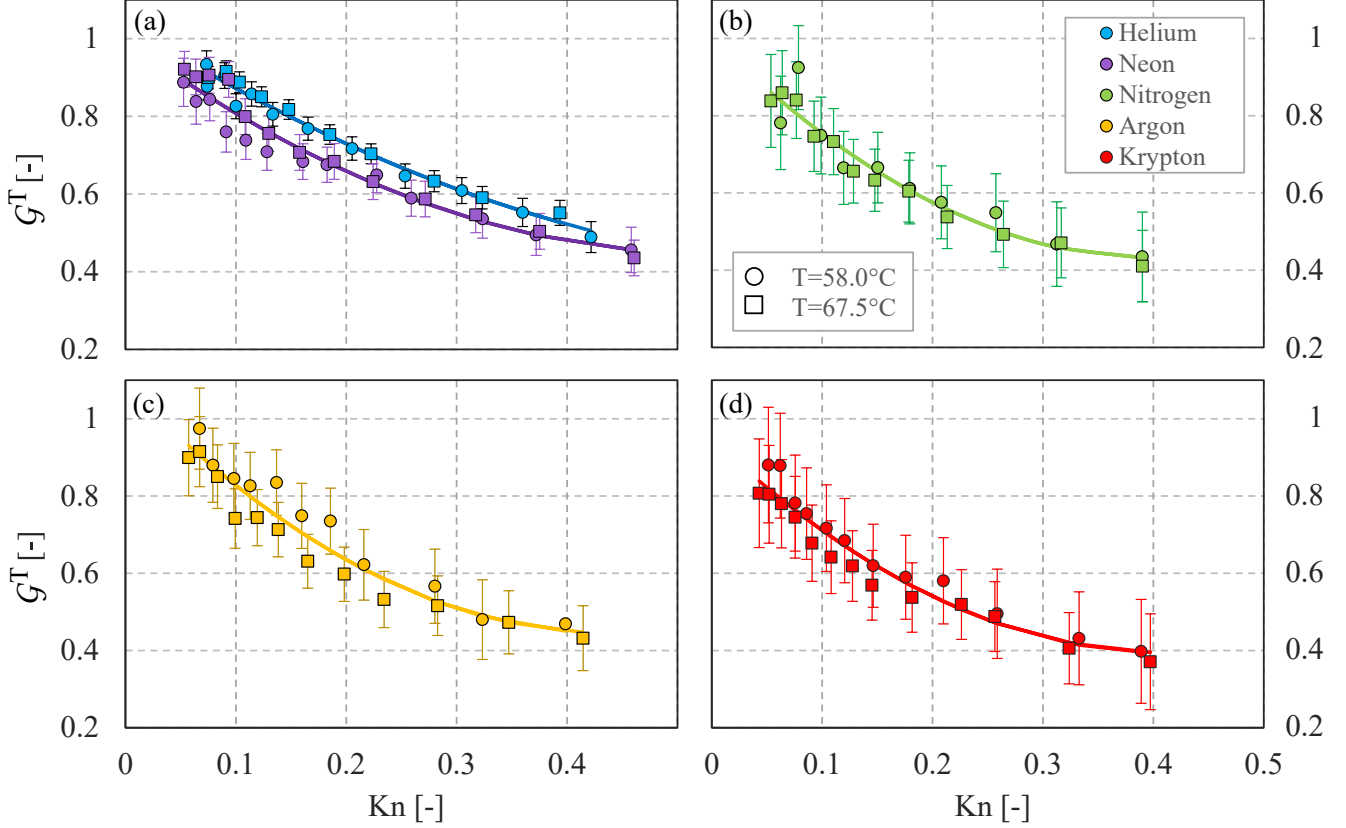
596 The influence of the surface roughness on the gas-surface interaction has been studied from a long
 597 time, nevertheless, up to now it does not exist a common point of view regarding the influence of surface
 598 roughness on flow properties, see review paper Ref. [16]. Generally, the increasing of the surface roughness
 599 leads to an increasing of the accommodation of the molecules on the surface and therefore to an increasing
 600 in the value of the accommodation coefficient. However, the authors of Ref. [53] have made a systematic
 601 study of the roughness influence on PEEK surface (the same as in the present study) and they found out
 602 that an increasing of roughness (from 10 nm to 770 nm) decreases the accommodation coefficient for the
 603 two tested gases: helium (from 0.915 to 0.253) and air (from 0.885 to 0.145). The roughness of the channel
 604 used in present experimental setup was measured to be equal to 113nm, so we consider that our data are
 605 compatible with study carried out in Ref. [53]. Therefore, the fact that the values of the accommodation
 606 coefficients are found relatively far from unit could be explained by the influence of the relatively high
 607 roughness of the microchannel, grooved in a PEEK plate.

608 6.2. Temperature gradient driven flow

609 The reduced mass flow rates, \mathcal{G}^T , Eq. (43), for all the five gases (He, Ne, N₂, Ar and Kr) and for two
 610 temperature differences ($\Delta T = 58.0^\circ\text{C}$ and 67.5°C) are shown in Fig. 10, in function of the mean Knudsen
 611 number. Besides, the fitting curves, Eq. (44), for each gas are also presented in the same figure. It is
 612 important to mention that the fitting curve of each gas was obtained by fitting all the points for each gas,
 613 *i.e.* using both temperatures differences. As we can see in Fig. 10, the values of \mathcal{G}^T obtained for helium
 614 and neon, are almost all of them over their fitting curves, but if we track the \mathcal{G}^T for the heavier gases,
 615 we can see a considerable dispersion, mainly for low values of Knudsen number. Thus, it is extremely
 616 challenging to extract the coefficients from temperature driven experiments working with heavy gases.

617 Table 7 presents the values of the fitting coefficients C_i^F , $i = 0, 1$ and 2 , with corresponding uncertainties,
 618 obtained from the fit of the experimental data, according to Eq. (44). The C_0^F coefficient is associated
 619 to the thermal slip coefficient σ_T . The uncertainties of the fitting coefficients provided in Table 7 do
 620 not consider the uncertainties on the measurements of mass flow rate, but only the standard errors on
 621 the fitting process. In addition, to estimate the quality of the fit, two characteristic parameters are also
 622 provided: the determination coefficient r^2 and the χ^2 value. By analyzing these two parameters, one can
 623 observe that for the two lighter gases, namely helium and neon, both characteristics are good. For helium,
 624 the determination coefficient r^2 is close to 1 (0.9808) and the probability that the two fitted variables are
 625 independent is very small (0.0076). However, for the heavier gases, both characteristic parameters present
 626 worse values, especially for argon.

627 Table 8 provides the σ_T coefficients previously measured by other authors [22, 25, 46] and the values
 628 found in present work. If comparing the later values of σ_T coefficients for monoatomic gases with that
 629 from Ref. [25] obtained using a channel also made by PEEK, one can see that the values obtained here are
 630 slightly higher for helium and argon, very similar (but lower) for neon and essentially lower for krypton,
 631 compared to those obtained in Ref. [25]. It is worth to notice that the roughness of the PEEK surface used



(a)

Figure 10: Reduced mass flow rate (\mathcal{G}^T) as function of the Knudsen number for all the five gases and two temperature differences. Results for (a) helium and neon, (b) nitrogen, (c) argon and (d) krypton. The solid lines represent the fitting curves, Eq. (44), over both temperature differences for each gas.

632 here is relatively high, which could impact the values of σ_T coefficients as it was observed for the pressure
 633 driven flows. The σ_T coefficient of the polyatomic nitrogen is found to be the highest one compared to
 634 those given in previously reported articles [22, 25, 46]. Besides, it was not found any correlation of these
 635 values with the molecular weight of the gas.

Table 7: The fitting parameters C_i^F , $i = 0, 1$ and 2 , obtained from the fit of the temperature gradient driven mass flow rate for all the five gases. The C_0^F coefficient is associated to σ_T . The determination coefficient, r^2 and the χ^2 probability of the fitting variables to be independent are provided. The accommodation coefficients extracted from Eqs. (45) and (46) in the frame of Maxwellian kernel are also given.

Parameter	He	Ne	N ₂	Ar	Kr
r^2	0.9808	0.9565	0.9364	0.9286	0.9447
χ^2	0.0076	0.0242	0.0293	0.0432	0.0287
$C_0 = \sigma_T$	1.041 ± 0.019	0.997 ± 0.022	1.003 ± 0.034	1.088 ± 0.040	0.960 ± 0.026
C_1	-1.821 ± 0.202	-2.090 ± 0.223	-2.847 ± 0.376	-2.942 ± 0.427	-2.809 ± 0.308
C_2	1.306 ± 0.430	1.985 ± 0.450	3.548 ± 0.854	3.364 ± 0.972	3.509 ± 0.716
α_T^M	0.777 ± 0.051	0.659 ± 0.058	0.972 ± 0.100	0.902 ± 0.107	0.559 ± 0.069

Table 8: The σ_T coefficient obtained in present work and by the authors of Refs. [22, 25, 46]. The authors of Ref. [25] used a microchannel made by PEEK (same material as in the present experiments), while in Refs. [22, 46] the microchannels made from glass are considered.

Parameter	He	Ne	N ₂	Ar	Kr
σ_T	1.041 ± 0.019	0.997 ± 0.022	1.003 ± 0.034	1.088 ± 0.040	0.960 ± 0.026
σ_T [25]	1.006 ± 0.020	0.998 ± 0.029	–	1.017 ± 0.057	1.061 ± 0.053
σ_T [46]	–	–	0.998 ± 0.028	1.075 ± 0.031	–
σ_T [22]	1.004 ± 0.002	0.988 ± 0.001	0.923 ± 0.002	1.030 ± 0.003	–

636 By fitting the temperature driven mass flow rate in the second order polynomial form, we associate
637 the thermal slip coefficient to zero order in Knudsen number term. However, this term is very difficult
638 to fix, because we need to have more data for very small Knudsen number, which are difficult to obtain.
639 Let us now analyse the "second thermal slip coefficient", \mathcal{C}_1 coefficient in Eq. (38). Analyzing the values
640 of this coefficient, all gases can be separated to two groups: the two lighter gases (helium and neon) for
641 which the second slip coefficients, \mathcal{C}_1 , has similar values, -1.821 and -2.090, respectively; heavier gases,
642 nitrogen, argon and krypton, for which this second slip coefficient has also similar values, -2.847, -2.942
643 and -2.809, respectively, see also Table 7. The analytical value of this second slip coefficient, $\mathcal{C}_1 = -1.3284$,
644 was provided in Ref. [47] for the case of two parallel plates and Maxwell diffuse scattering. This analytical
645 value has the same sign, but much smaller absolute value as those obtained from the fits of the experimental
646 data.

647 The accommodation coefficients, α_T^M , obtained from the thermal slip coefficients by using Eqs. (45)
648 and (46), are given in Table 7. The subscript "T" is used to notify that these coefficients are obtained
649 from the temperature gradient experiments and the superscript "M" indicates that the coefficients are
650 extracted using the Maxwell specular-diffuse kernel. The values of α_T^M vary in a large range, being the
651 minimum value of 0.559 for krypton and maximum value of 0.972 for nitrogen. As the accommodation
652 coefficient is extracted from the thermal slip coefficient, using Eq. (45) and (46), the uncertainties on α
653 represent 8/3 of the uncertainties on σ_T for all monoatomic gases and 80/27 for nitrogen. Both latter
654 quantities were obtained by classical derivation rule, which allows to calculate the uncertainties. It is clear
655 from Table 7 that for heavier gases the uncertainties on the accommodation coefficients are larger than
656 that for helium and neon, which could be explained by more scattered \mathcal{G}^T values for heavier gases.

657 6.3. Comparison between accommodation coefficients

658 The values of accommodation coefficient obtained from pressure (α_P^M) and temperature (α_T^M) gradient
659 experiments are summarized in Table 9. As previously mentioned, the superscript "M" denotes that
660 the Maxwellian specular-diffuse model was used for the extraction of these coefficients. Analyzing Table
661 9, we can conclude that the values of all accommodation coefficients obtained from pressure gradient
662 experiments are close to each other with the difference between minimal (neon) and maximal (krypton)
663 values of the order of 4%. Moreover, for the accommodation coefficients extracted from temperature
664 gradient experiments, the difference is much higher, being of the order of 42%. Besides, only for helium
665 the two coefficients, obtained from the pressure and temperature gradient experiments, are very close to
666 each other, with 0.5% of difference. For all the other gases, this difference varies between 12% (argon) and
667 30% (krypton). Therefore, the question remains open on which coefficient should be used in numerical
668 simulations when both pressure and temperature gradients are present in a flow and Maxwellian boundary
669 conditions are used. To go forward in answering this question, the numerical studies need to be carried
670 out to conclude on the choice of the coefficients. In the frame of continuum simulations (Navier-Stokes-
671 Fourier equations), different possibilities exist, as, for example, to put the α_P^M in the velocity slip boundary
672 conditions and α_T^M in the thermal slip part. However, if the Maxwell kernel is used in the frame of kinetic
673 equation, a real choice has to be done because only one coefficient is used in the boundary conditions.

Table 9: Accommodation coefficients extracted from both pressure and temperature driven flows, α_p^M and α_T^M , respectively, in the frame of the Maxwellian model.

Parameter	He	Ne	N ₂	Ar	Kr
α_p^M	0.781 ± 0.004	0.768 ± 0.005	0.790 ± 0.003	0.792 ± 0.002	0.801 ± 0.004
α_T^M	0.777 ± 0.051	0.659 ± 0.058	0.972 ± 0.100	0.902 ± 0.107	0.559 ± 0.069

674 A more sophisticated model can also be applied to take into account simultaneously the influence of
675 both, momentum and energy exchanges, through two different accommodation coefficients, *i.e.* considering
676 tangential momentum accommodation coefficient, α_t , and normal energy accommodation coefficient, α_n ,
677 [6]. The extraction of both coefficients in the frame of the Cercignani-Lampis model [6] is presented in the
678 next section.

679 6.4. Accommodation coefficients from Cercignani-Lampis model

680 The Cercignani-Lampis model was implemented by the authors of Refs. [54, 55] in the frame of the
681 S-model kinetic equation, while the author of Ref. [56] solved directly the Boltzmann equation with Hard
682 Sphere model to study the influence of both tangential momentum and normal energy accommodation
683 coefficients on the velocity slip coefficient, σ_p . From these works it was concluded that this coefficient is
684 weakly affected by the normal energy accommodation coefficient, α_n , but it significantly depends on the
685 tangential momentum accommodation coefficient, α_t . The expression relating σ_p and α_t , which interpo-
686 lates the numerical results obtained by the authors, is:

$$\sigma_p = \frac{1.771}{\alpha_t} - 0.754. \quad (47)$$

687 Thus, the first adjustable parameter of the Cercignani-Lampis model, α_t , depends only on the σ_p , and
688 this last coefficient comes from the pressure gradient experiments. Therefore, from the already extracted
689 velocity slip coefficients, see Table 6, the tangential momentum accommodation coefficients, α_t , is obtained
690 and its values are provided in Table 10. It should be mentioned that the values of accommodation
691 coefficient obtained using the specular-diffuse model, α_p^M , are also shown in this table in order to facilitate
692 the comparison with α_t .

Table 10: Velocity slip and accommodation coefficients experimentally obtained from pressure gradient experiments for five gases. Maxwellian specular-diffuse model is used to extract α_p^M , while Cercignani-Lampis one is used to obtain α_t .

Parameter	He	Ne	N ₂	Ar	Kr
σ_p	1.545 ± 0.014	1.584 ± 0.012	1.517 ± 0.009	1.511 ± 0.006	1.485 ± 0.012
α_p^M	0.781 ± 0.004	0.768 ± 0.005	0.790 ± 0.003	0.792 ± 0.002	0.801 ± 0.004
α_t	0.771 ± 0.005	0.758 ± 0.004	0.780 ± 0.003	0.782 ± 0.002	0.791 ± 0.004

693 From Table 10, it is clear that the values of α_t vary inside a narrow range between 0.758 for neon
694 and 0.791 for krypton. Comparing the results from both models, it is noticeable that the values of
695 accommodation coefficient extracted from Cercignani-Lampis model are slightly lower (with maximal
696 difference of 1.3%) than the values obtained from Maxwellian model, for all the five tested gases.

697 According to the results provided in Ref. [3], the thermal slip coefficient, σ_T , is sensitive to both
698 accommodation coefficients, α_t and α_n . Thus, if the values of α_t and σ_T are known, the value of the
699 normal energy accommodation coefficient can be obtained. Unfortunately, we did not find in the open
700 literature any explicit expression, analogous to, for example, Eq. (47), to relate the thermal slip coefficient,
701 σ_T , to both accommodation coefficients, α_t and α_n . Therefore we used a table from Ref. [3], reproduced
702 below as Table 11, to evaluate the behavior of α_n coefficient.

Table 11: Thermal slip coefficient σ_T for Cercignani-Lampis scattering law: (a) Refs. [54, 55], S model, direct solution; (b) Ref. [56], BE with HS, direct solution. Reproduced from Ref. [3].

α_t	σ_T							
	$\alpha_n = 0.25$		$\alpha_n = 0.5$		$\alpha_n = 0.75$		$\alpha_n = 1$	
	(a)	(b)	(a)	(b)	(a)	(b)	(a)	(b)
0.5	1.034	0.915	1.081	0.954	1.127	0.991	1.172	1.028
0.75	1.107	0.964	1.129	0.982	1.152	1.001	1.174	1.019
1	1.175	1.018	1.175	1.018	1.175	1.018	1.175	1.018
1.25	1.240	1.071	1.219	1.053	1.197	1.035	1.175	1.017
1.5	1.305	1.114	1.264	1.080	1.221	1.044	1.177	1.008

703 In fact, the values of α_t and σ_T are known and they can be seen in Tables 10 and 7, respectively.
704 Based on this, normally it would be easy to extract the values of normal energy accommodation coefficient,
705 α_n , from Table 11. As it can be seen in Table 10, the values of tangential momentum accommodation
706 coefficient, α_t , extracted for all the gases, are inside a narrow range from 0.758 to 0.791, which are close
707 to 0.75, value provided in Table 11, see the bold row. However, the implementation of a simple affine
708 interpolation formula obtained from available values of σ_T and corresponding α_n either from Refs. [54, 55],
709 columns (a) or from Ref. [56], columns (b) in Table 11, does not allow to obtain reasonable values of α_n .
710 One of the reasons of that could be the use of an approximate value of $\alpha_t = 0.75$ instead of a real measured
711 value. Another reason is also the fact that the value band of the measured values of σ_T (between 0.960 and
712 1.088, Table 7) is greater than the theoretical band (between 0.964 and 1.019, columns (b) of Table 11),
713 therefore, it is impossible to find a unique match between the two sets of data. A lack of numerical data
714 relating σ_T and α_n , namely values of α_n lower than 0.25, and also a possible non-linear dependency of σ_T
715 from α_n in this range could be other reasons. In principle, by using the numerical approaches proposed in
716 Refs. [54, 55, 56] more data on σ_T and α_n could be obtained. After that, it would be possible to extract
717 α_n from experimental data.

718 Recently, the authors of Ref. [57] applied a variational method to solve the Boltzmann equation based
719 on the true linearized collision operator for hard-sphere molecules and the Cercignani-Lampis boundary
720 conditions. Then, an explicit relation between the first- and second-order thermal slip coefficients (our
721 \mathcal{C}_0 and \mathcal{C}_1 coefficients in Eq. (44)) and the tangential momentum and normal energy accommodation
722 coefficients, defined in the frame of the Cercignani-Lampis scattering kernel, are derived. By comparing
723 the theoretical results with the experimental data from Ref. [25], a pair of accommodation coefficients
724 has been extracted for each noble gas considered in the experiments. The approach developed in Ref. [57]
725 cannot be applied directly to the present experimental data because the two parallel plate configuration
726 is considered and so the influence of the vertical channel walls is not taken into account. It is worth to
727 underline that the authors of Ref. [57] have found the tangential momentum accommodation coefficient
728 in very narrow range of $0.80 < \alpha_t < 0.88$, not far from our finding, but the normal energy accommodation
729 coefficient was found to be very low, between 0.15 and 0.33. This fact coincides with our previous discussion
730 on the necessity of additional data in the low range of α_n .

731 It is worth to add that the authors of Ref. [57] have found, by analyzing the experimental data of Ref.
732 [25], that the second thermal slip coefficient is proportional to the molecular mass of a gas: the smallest
733 in absolute value second-order thermal slip coefficient was found for helium and the largest for krypton.
734 Similar behavior was found from the fit of the present experimental data, see Table 7.

735 7. Conclusion

736 Two types of gas flow through the same microchannel made from PEEK were experimentally studied.
737 In the first case, the flow is generated by applying a pressure difference between the two sides of the
738 microchannel, while in the second one, the flow is generated by a temperature difference imposed between
739 the two extremities of the microchannel. In both experiments the pressure variations inside the tanks
740 connected by the microchannel allow us to obtain the mass flow rate through it. Two important parameters
741 characterizing the gas-surface interaction were calculated from these mass flow rates: the velocity slip and
742 the thermal slip coefficients. They are indispensable to simulate gas flows in the slip flow regime in the
743 frame of the continuum approach. For the first time these data were obtained for the same gas-surface
744 pair.

745 As both, velocity and thermal slip coefficients are related to one (Maxwell model) or two (Cercignani-
746 Lampis model) accommodation coefficients, their values were also extracted. Assuming first the hypothesis
747 of the Maxwellian specular-diffuse interaction, where only one coefficient is used for both types of accom-
748 modation (tangential momentum and normal energy), the accommodation coefficient of each gas-surface
749 pair was extracted separately from the pressure gradient flows and from the temperature gradient flows.
750 These accommodation coefficients were found different when obtained from temperature gradient flows in
751 comparison to the pressure gradient ones, except for helium, for which both coefficients presented very
752 close values, 0.5% of difference.

753 Applying then the Cercignani-Lampis model, the values of tangential momentum accommodation
754 coefficient obtained from pressure gradient experiments were found very close to that previously extracted
755 using the Maxwellian model, being the discrepancy lower than 1.3%. However, it was not possible to
756 extract the normal energy accommodation coefficient from the temperature gradient flows due to a lack of
757 numerical data which relates the thermal slip coefficient to the normal energy accommodation coefficient.
758 The extrapolation of the numerical data was not possible to be done too, since the behavior of thermal
759 slip coefficient as a function of the normal energy accommodation coefficient for the missing range could
760 be different compared to the available one. When these data will be available in the open literature, the
761 normal energy accommodation coefficient could also be extracted from the presented measurements.

762 Finally, the obtained set of experimental data could be useful for numerical modeling of the gas-surface
763 interaction. However, new numerical simulations have to be done to test the capacity of the experimentally
764 extracted coefficients to predict the behavior of the pressure and temperature gradient flows at small scales
765 or at low pressures.

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902 Appendix A. Non-isothermal effects and their estimation

903 The non-isothermal effects could be observed after the quick opening and closing of valve V_A . To
904 avoid the non-isothermal measurements, we have proceeded in the following way. Initially the system is in
905 equilibrium and $p_1 = p_2$, see Fig. A.11 interval "a". Then, at time t_i , the pressure relaxation is actuated
906 by a rapid opening and closing of the valve connected to one of the tanks, where pressure p_2 is measured.
907 Right after the opening and closing of valve V_A (interval "b" in Fig. A.11), the pressure relaxation may
908 be in non-equilibrium and not yet in quasi-equilibrium state. In the non-equilibrium state, we may have a
909 small temperature drop on low-pressure side due to the pressure drop before the system reaches thermal
910 equilibrium again, see Fig. A.11. Therefore, we set a larger pressure ratio than we intend to measure and
911 cut away the first part of the pressure relaxation process, the interval represented by "b" in Fig. A.11.
912 Then, from time instant t_0 , the system reaches the quasi-stationary state, where there is still a pressure
913 change in time. Finally, the final pressure equilibrium is reached, $p_1 = p_2$, interval "d", but with one
914 single relaxation time. This range of the quasi-stationary relaxation process, interval "c" in Fig. A.11, is
915 used for the data fitting. We should mention that Fig. A.11 represents a simplified scheme of the whole
916 process. Furthermore, there is an exaggeration in the duration of the non-equilibrium interval, in order to
917 better illustrate the process.

918 In our experimental setup only the tank temperature is measured. To have an estimation of the time
919 scale of the thermal effects related to the quick opening and closing of the valve V_A , we compare the
920 time needed to a gas reaching equilibrium with the tank, approximattely $4\tau_c$ (τ_c is the gas conduction
921 time)[12] to the waiting time $t_w = t_0 - t_i$ which we spend before starting the measurements.

922 If the tank represents an infinite heat sink at constant temperature to the gas, then the time it takes
923 for the gas to reach equilibrium with the tank can be modeled. In Ref. [12] the transient heat conduction
924 equation was solved analytically and the solution was presented as the infinite series of the Bessel functions.
925 When keeping only the first leading term of the series, the characteristic conduction time can be estimated
926 as:

$$\tau_c = \frac{\rho R_{res}^2 Pr}{2.4\mu}, \quad (\text{A.1})$$

927 where ρ is the gas density, R_{res} is the characteristic reservoir dimension and Pr is the Prandtl number.
928 In our setup the reservoir characteristic dimension (its radius) is equal to $3mm$, the Prandtl number

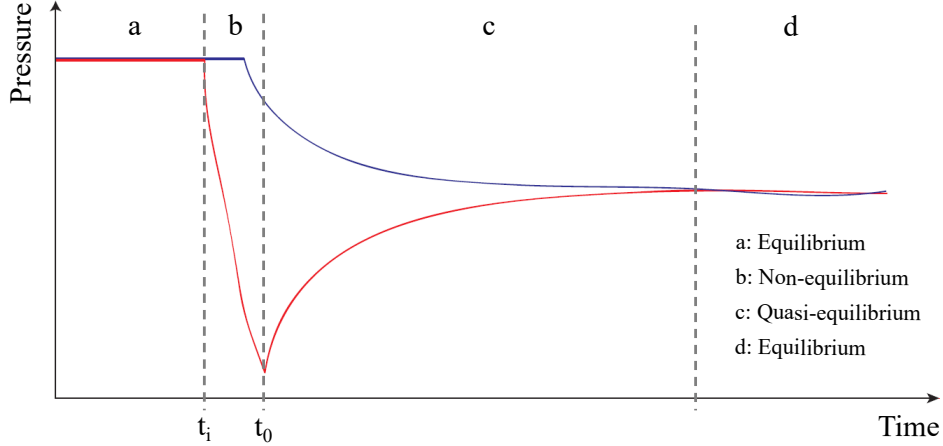


Figure A.11: Illustration of typical stages of pressure evolution in time. The red and blue curves represent the pressure variation in the low and high pressure reservoir, respectively.

929 is equal to $2/3$ and 0.71 , for the monoatomic and polyatomic gases, respectively. The gas conduction
 930 time, Eq. (A.1), is proportional to the gas density and so to the gas pressure under our experimental
 931 conditions. It depends also on the gas nature through the gas viscosity. As the characteristic conduction
 932 time is proportional to the gas density, so it is longer for for the higher pressure (density) experimental
 933 runs. Therefore we provide the values of τ_c in Table A.12 only for the high pressure runs. The minimum
 934 values of the waiting time are also provided in Table A.12. The results given in this table provide the
 935 experimental confirmation that the gas temperature remains close to the constant temperature during the
 936 measurements and that the thermal effects remain negligible under our experimental conditions.

Table A.12: The gas conduction time τ_c and the waiting time t_w for the high pressure runs for all gases used in experiments.

Parameter	He	Ne	N ₂	Ar	Kr
τ_c [s]	0.02	0.08	0.19	0.22	0.36
t_w [s]	1	2	2	2	3

937 Appendix B. First and second order fittings for pressure driven flows

938 The pertinence of using the first or second order fitting was discussed by different authors, see for
 939 example Refs. [13, 27, 41, 42]. It was found that the implementation of the second order fitting formula
 940 provides practically the same results as that given by the first order fitting in corresponding Knudsen
 941 number ranges, see Table B.13.

942 Appendix C. Gas-surface interaction

943 As it was mentioned in Introduction, the gas-surface interaction becomes very important when the
 944 number of molecule-molecule collisions starts to be comparable to the number of molecule-surface collisions.
 945 When the gas behavior is described in terms of the molecular velocity distribution function, the so called
 946 scattering kernel needs to be defined to provide a detailed description of this interaction, *i.e.* for each
 947 known incident distribution function, the reflected distribution function can be calculated. However, in
 948 practice we do not need so detailed description and the average over molecular velocities characteristic,

Table B.13: Determination coefficient, first and second order polynomial fitting coefficients, velocity slip and accommodation coefficients obtained from pressure gradient experiments for helium in the range of [0.0016;0.12] and [0.0016;0.67] for the first and second order, respectively.

Parameter	Helium	
	first order	second order
r^2	0.9985	0.9998
C_0^F	1.018±0.004	1.015±0.005
C_1^F	9.597±0.085	9.566±0.080
C_2^F	–	1.626±0.125
σ_p	1.545±0.014	1.541±0.012
α_p^M	0.781±0.004	0.782±0.004

949 *i.e.* the accommodation coefficient, can be used. The accommodation coefficient can be defined as [58]:

$$\alpha(\psi) = \frac{J_i(\psi) - J_r(\psi)}{J_i(\psi) - J_{\text{dif}}(\psi)}, \quad (\text{C.1})$$

950 where $J_i(\psi)$ and $J_r(\psi)$ are incident and reflected fluxes defined as:

$$J_r(\psi) = \int_{v_n > 0} |v_n| f(\mathbf{v}) \psi(\mathbf{v}) d\mathbf{v}, \quad J_i(\psi) = \int_{v'_n < 0} |v'_n| f(\mathbf{v}') \psi(\mathbf{v}') d\mathbf{v}', \quad (\text{C.2})$$

951 the diffuse flux is calculated using the Maxwellian distribution function f^M [1] as:

$$J_{\text{dif}}(\psi) = \int_{v_n > 0} |v_n| f^M(\mathbf{v}) \psi(\mathbf{v}) d\mathbf{v}. \quad (\text{C.3})$$

952 In previous equations, v'_n and v_n are the normal component of the incident and reflected molecular velocities
 953 and ψ function can present either momentum accommodation, $\psi = m\mathbf{v}$, or energy accommodation, $\psi =$
 954 $\frac{1}{2}mv^2$. From previous definition it is clear that the accommodation coefficient is an integral characteristic
 955 (over molecular velocities) and it does not reflect details of gas surface interaction.

956 If the accommodation coefficient is calculated taking $\psi = mv_t$, where v_t is the tangential velocity com-
 957 ponent of the incident molecule, it is usually called the Tangential Momentum Accommodation Coefficient
 958 (TMAC). When using $\psi = \frac{1}{2}mv^2$ in Eq. (C.1), the accommodation coefficient becomes the energy (or
 959 thermal) accommodation coefficient. In the frame of the Cercignani-Lampis model, the normal energy
 960 accommodation coefficient is defined using $\psi = \frac{1}{2}mv_n^2$.

961 For some particular kernels, as Maxwellian specular-diffuse and Cercignani-Lampis ones, Eq. (C.1) does
 962 not depend on the molecular velocity distribution function. When using the specular-diffuse scattering,
 963 $\alpha(\psi) = \alpha_d$ for any ψ function [58]. This is the main shortcoming of the specular-diffuse kernel, because
 964 it does not allow to distinguish the tangential momentum and energy accommodation coefficients, by
 965 associating both of them to only one coefficient. Contrarily, when using $\psi = mv_t$ with the Cercignani-
 966 Lampis kernel, one obtains $\alpha(\psi) = \alpha_t$, with a meaning of the accommodation of the tangential momentum.
 967 In the same way, by using $\psi = \frac{1}{2}mv_n^2$, the normal energy accommodation coefficient, $\alpha(\psi) = \alpha_n$ is obtained.

968 However, in practice, it is not easy to measure the values of accommodation coefficients for the pairs
 969 of the gas-surface interaction, because only the indirect measurements of the macroscopic quantities are
 970 available [16, 19, 59]. The most accurate data can be obtained from simulations based on the kinetic
 971 theory, by applying the Boltzmann or other model equations, but the analytical expressions exist usually
 972 only in the case of the free molecular flow regime (molecule-molecule collisions are neglected). Contrarily,
 973 in the case of continuum approach, the explicit expressions are available in the case of flow through a

974 channel with different cross-sections. When the continuum modeling is used, the interaction between a
975 gas and a surface is taken into account through the velocity slip and thermal slip coefficients, which are
976 related to the accommodation coefficients [3].

977 **Appendix D. Experimental data**

978 In this section we provide the mass flow through the microchannel for all the five working gases
979 extracted from pressure gradient, Tables [D.14](#) and [D.15](#), and temperature gradient experiments, Tables
980 [D.16-D.19](#). It should be noticed that, associated to each mass flow rate are the initial and final pressures
981 inside the upstream tank (tank 1), used to extract this mass flow rate values.

Table D.14: Mass flow rate (\dot{M}_1) obtained in function of the initial and final pressures inside the upstream tank ($p_{1,0}$ and $p_{1,f}$, respectively) extracted for helium, neon and nitrogen from pressure gradient experiments. Both upstream and downstream tanks were kept at 24°C during the measurements.

Helium			Neon			Nitrogen		
$p_{1,0}$ [kPa]	$p_{1,f}$ [kPa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [kPa]	$p_{1,f}$ [kPa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [kPa]	$p_{1,f}$ [kPa]	\dot{M}_1 [kg/s]
98.6	76.7	3.41×10^{-6}	131	124	6.21×10^{-6}	129	106	3.44×10^{-5}
74.1	57.8	2.00×10^{-6}	123	117	4.70×10^{-6}	102	82.6	2.44×10^{-5}
56.4	43.6	1.21×10^{-6}	112	88.3	1.35×10^{-5}	79.9	62.0	1.72×10^{-5}
42.4	32.7	7.01×10^{-7}	85.1	68.0	7.76×10^{-6}	60.4	48.0	9.59×10^{-6}
31.5	25.0	3.65×10^{-7}	66.0	51.8	5.00×10^{-6}	46.4	35.2	6.41×10^{-6}
23.8	15.6	2.99×10^{-7}	50.5	39.6	2.97×10^{-6}	34.2	27.1	3.24×10^{-6}
15.5	12.3	9.46×10^{-8}	38.5	30.3	1.73×10^{-6}	26.2	21.9	1.54×10^{-6}
12.3	9.97	5.67×10^{-8}	29.6	23.4	1.01×10^{-6}	21.2	18.1	9.27×10^{-7}
12.9	10.5	6.20×10^{-8}	23.3	18.2	6.63×10^{-7}	18.0	15.0	7.81×10^{-7}
10.5	8.67	3.87×10^{-8}	18.1	14.2	4.08×10^{-7}	14.9	12.7	5.08×10^{-7}
7.97	6.87	1.89×10^{-8}	14.1	11.9	1.94×10^{-7}	13.5	11.9	3.49×10^{-7}
6.84	5.56	1.85×10^{-8}	13.7	12.6	1.08×10^{-7}	11.8	10.2	3.01×10^{-7}
5.51	4.00	1.65×10^{-8}	12.6	8.99	2.42×10^{-7}	10.1	8.55	2.41×10^{-7}
3.99	3.03	8.47×10^{-9}	8.96	7.45	8.74×10^{-8}	8.53	7.38	1.53×10^{-7}
3.02	2.60	3.31×10^{-9}	7.46	5.62	7.96×10^{-8}	7.37	5.07	2.12×10^{-7}
2.63	2.32	2.06×10^{-9}	5.62	4.73	3.38×10^{-8}	5.05	4.01	8.02×10^{-8}
2.32	1.90	2.55×10^{-9}	4.71	3.89	2.61×10^{-8}	3.99	3.29	4.43×10^{-8}
1.32	1.23	4.26×10^{-10}	3.90	3.35	1.57×10^{-8}	3.29	2.54	3.68×10^{-8}
1.26	0.92	1.35×10^{-9}	3.34	2.63	1.61×10^{-8}	2.53	1.96	2.27×10^{-8}
1.23	1.14	4.31×10^{-10}	2.63	2.29	6.91×10^{-9}	1.95	1.77	6.97×10^{-9}
1.00	0.54	1.47×10^{-9}	2.30	1.78	8.71×10^{-9}	1.79	1.54	7.22×10^{-9}
0.91	0.87	1.78×10^{-10}	1.76	1.46	4.59×10^{-9}	1.30	1.22	2.22×10^{-9}
0.87	0.83	1.37×10^{-10}	1.34	1.26	9.92×10^{-10}	1.22	1.06	3.66×10^{-9}
0.83	0.77	2.39×10^{-10}	1.26	1.16	1.32×10^{-9}	1.06	0.89	3.54×10^{-9}
			1.18	1.00	2.08×10^{-9}	0.89	0.78	1.96×10^{-9}
			1.05	0.90	1.61×10^{-9}	0.78	0.61	2.69×10^{-9}
			0.99	0.80	1.87×10^{-9}	0.61	0.49	1.67×10^{-9}
			0.95	0.77	1.70×10^{-9}	0.49	0.39	1.20×10^{-9}
			0.84	0.74	1.05×10^{-9}	0.38	0.32	6.91×10^{-10}
			0.83	0.67	1.49×10^{-9}	0.32	0.28	4.08×10^{-10}
			0.77	0.64	1.20×10^{-9}			
			0.63	0.59	3.42×10^{-10}			
			0.59	0.55	2.95×10^{-10}			

Table D.15: Mass flow rate (\dot{M}_1) obtained in function of the initial and final pressures inside the upstream tank ($p_{1,0}$ and $p_{1,f}$, respectively) extracted for argon and krypton from pressure gradient experiments. Both upstream and downstream tanks were kept at 24°C during the measurements.

Argon			Krypton		
$p_{1,0}$ [kPa]	$p_{1,f}$ [kPa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [kPa]	$p_{1,f}$ [kPa]	\dot{M}_1 [kg/s]
129	116	2.39×10^{-5}	99.8	84.6	4.75×10^{-5}
112	88.3	3.44×10^{-5}	80.8	66.8	3.21×10^{-5}
84.8	66.4	2.13×10^{-5}	64.6	53.3	2.25×10^{-5}
64.2	49.2	1.36×10^{-5}	51.8	42.2	1.58×10^{-5}
47.6	36.2	7.72×10^{-6}	41.2	32.7	1.00×10^{-5}
35.0	25.4	4.61×10^{-6}	31.0	24.6	5.51×10^{-6}
24.5	18.3	2.14×10^{-6}	23.7	19.0	3.16×10^{-6}
18.1	13.6	1.21×10^{-6}	18.6	14.6	2.11×10^{-6}
13.5	11.6	4.21×10^{-7}	14.5	11.3	1.32×10^{-6}
13.6	11.2	5.52×10^{-7}	13.5	11.4	9.18×10^{-7}
11.2	8.85	4.31×10^{-7}	11.3	9.51	6.19×10^{-7}
8.81	6.61	3.03×10^{-7}	9.47	7.97	4.41×10^{-7}
6.58	5.01	1.68×10^{-7}	7.98	6.56	3.45×10^{-7}
4.97	3.91	8.95×10^{-8}	6.53	5.34	2.44×10^{-7}
3.94	3.05	5.69×10^{-8}	5.35	4.53	1.45×10^{-7}
3.05	2.46	3.24×10^{-8}	4.53	3.91	9.42×10^{-8}
2.45	2.01	1.92×10^{-8}	3.89	3.31	7.87×10^{-8}
2.00	1.52	1.73×10^{-8}	3.29	2.70	6.51×10^{-8}
1.32	1.16	4.65×10^{-9}	2.73	2.37	3.51×10^{-8}
1.16	1.08	2.27×10^{-9}	2.39	1.98	3.03×10^{-8}
1.08	0.86	5.10×10^{-9}	1.97	1.72	1.74×10^{-8}
0.85	0.73	2.47×10^{-9}	1.27	1.21	3.05×10^{-9}
0.73	0.63	1.84×10^{-9}	1.21	1.08	6.11×10^{-9}
0.63	0.52	1.89×10^{-9}	1.16	1.02	6.40×10^{-9}
0.52	0.43	1.24×10^{-9}	1.02	0.92	4.53×10^{-9}
0.43	0.37	8.43×10^{-10}	0.92	0.83	3.38×10^{-9}
0.37	0.32	6.12×10^{-10}	0.83	0.77	2.06×10^{-9}
0.32	0.30	2.65×10^{-10}	0.77	0.72	1.70×10^{-9}
			1.06	0.65	1.34×10^{-8}
			0.72	0.56	4.86×10^{-9}
			0.56	0.48	2.27×10^{-9}
			0.48	0.39	2.05×10^{-9}
			0.34	0.33	2.73×10^{-10}
			0.39	0.29	1.87×10^{-9}
			0.29	0.25	6.82×10^{-10}
			0.25	0.22	5.07×10^{-10}

Table D.16: Mass flow rate (\dot{M}_1) obtained in function of the initial and final pressures inside the upstream tank ($p_{1,0}$ and $p_{1,f}$, respectively) extracted for helium, neon and nitrogen from temperature gradient experiments using $\Delta T = 58.0^\circ C$. During all these measurements, the cold tank was kept at $11.5^\circ C$ while the hot tank at $69.5^\circ C$.

Helium			Neon			Nitrogen		
$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]
1321.8	1318.1	1.18×10^{-11}	1312.2	1310.1	1.78×10^{-11}	1302.5	1302.0	8.68×10^{-12}
1310.3	1306.7	1.11×10^{-11}	1079.1	1076.7	1.68×10^{-11}	1061.1	1060.5	8.66×10^{-12}
1080.4	1076.1	1.14×10^{-11}	903.62	901.09	1.70×10^{-11}	891.14	890.43	9.20×10^{-12}
970.05	965.98	1.04×10^{-11}	756.15	753.47	1.53×10^{-11}	760.78	760.00	9.26×10^{-12}
850.18	845.38	1.08×10^{-11}	632.51	629.82	1.48×10^{-11}	527.91	527.12	8.84×10^{-12}
727.77	722.92	1.02×10^{-11}	538.29	535.53	1.42×10^{-11}	419.81	418.89	1.05×10^{-11}
587.47	582.64	9.68×10^{-12}	429.52	426.62	1.37×10^{-11}	333.49	332.19	8.47×10^{-12}
473.39	468.50	9.04×10^{-12}	378.28	375.21	1.36×10^{-11}	276.04	274.69	7.52×10^{-12}
383.42	378.82	8.14×10^{-12}	303.33	300.05	1.30×10^{-11}	219.27	217.97	7.53×10^{-12}
319.07	314.41	7.67×10^{-12}	266.70	263.80	1.19×10^{-11}	183.90	182.59	6.92×10^{-12}
270.03	266.04	6.97×10^{-12}	213.49	210.71	1.08×10^{-11}	158.47	157.18	6.51×10^{-12}
230.36	226.70	6.17×10^{-12}	185.58	183.19	9.95×10^{-12}	128.17	126.86	6.21×10^{-12}
183.56	180.28	5.33×10^{-12}	150.70	148.48	9.17×10^{-12}	105.54	104.52	5.29×10^{-12}
156.58	153.47	4.64×10^{-12}	125.77	123.63	8.14×10^{-12}	84.57	83.55	4.92×10^{-12}
126.25	123.51	4.23×10^{-12}	104.47	102.63	6.93×10^{-12}	70.08	69.24	4.34×10^{-12}
110.50	107.97	3.84×10^{-12}	85.49	83.92	5.98×10^{-12}			

Table D.17: Mass flow rate (\dot{M}_1) obtained in function of the initial and final pressures inside the upstream tank ($p_{1,0}$ and $p_{1,f}$, respectively) extracted for argon and krypton from temperature gradient experiments using $\Delta T = 58.0^\circ C$. During all these measurements, the cold tank was kept at $11.5^\circ C$ while the hot tank at $69.5^\circ C$.

Argon			Krypton		
$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]
1306.0	1305.4	1.85×10^{-11}	1291.6	1291.0	2.19×10^{-11}
1091.3	1090.7	1.49×10^{-11}	1087.9	1087.3	1.53×10^{-11}
934.32	933.62	1.14×10^{-11}	898.65	898.07	1.82×10^{-11}
772.34	771.59	1.56×10^{-11}	727.04	726.42	1.59×10^{-11}
642.41	641.57	1.51×10^{-11}	647.45	646.74	1.54×10^{-11}
531.23	530.39	1.42×10^{-11}	526.92	526.19	1.41×10^{-11}
449.52	448.19	1.28×10^{-11}	435.53	434.65	1.41×10^{-11}
362.95	361.59	1.23×10^{-11}	357.72	356.80	1.21×10^{-11}
315.63	314.01	1.21×10^{-11}	314.57	313.52	1.15×10^{-11}
260.60	259.13	1.22×10^{-11}	260.23	259.22	1.10×10^{-11}
223.22	221.83	1.09×10^{-11}	224.43	223.41	9.93×10^{-12}
192.03	190.58	1.07×10^{-11}	184.81	183.85	9.31×10^{-12}
165.22	163.67	9.08×10^{-12}	153.94	152.92	7.94×10^{-12}
127.19	125.83	8.27×10^{-12}	128.81	127.85	6.92×10^{-12}
110.29	109.31	7.01×10^{-12}	104.52	103.66	6.38×10^{-12}
89.45	88.19	6.85×10^{-12}	81.25	80.45	1.25×10^{-12}
65.13	64.08	5.76×10^{-12}	69.50	68.79	9.45×10^{-12}

Table D.18: Mass flow rate (\dot{M}_1) obtained in function of the initial and final pressures inside the upstream tank ($p_{1,0}$ and $p_{1,f}$, respectively) extracted for helium, neon and nitrogen from temperature gradient experiments using $\Delta T = 67.5^\circ C$. During all these measurements, the cold tank was kept at $11.5^\circ C$ while the hot tank at $79.0^\circ C$.

Helium			Neon			Nitrogen		
$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]
1315.4	1310.6	1.31×10^{-11}	1314.2	1311.6	2.14×10^{-11}	1322.0	1321.2	8.29×10^{-12}
1083.4	1078.2	1.34×10^{-11}	1101.3	1098.6	2.10×10^{-11}	1070.9	1070.1	1.36×10^{-11}
957.31	952.10	1.30×10^{-11}	926.85	923.94	2.11×10^{-11}	909.25	908.46	1.05×10^{-11}
802.01	796.61	1.24×10^{-11}	751.47	748.27	2.08×10^{-11}	751.62	750.66	1.25×10^{-11}
668.06	662.48	1.19×10^{-11}	647.78	644.41	1.86×10^{-11}	626.74	625.70	1.10×10^{-11}
533.95	528.33	1.10×10^{-11}	540.70	537.22	1.76×10^{-11}	526.88	525.56	1.13×10^{-11}
444.32	438.84	1.03×10^{-11}	445.17	441.76	1.65×10^{-11}	438.29	436.99	1.10×10^{-11}
353.40	348.00	9.24×10^{-12}	371.41	367.97	1.59×10^{-11}	362.68	361.46	9.79×10^{-12}
305.93	300.69	8.62×10^{-12}	313.24	309.77	1.47×10^{-11}	304.55	303.20	9.61×10^{-12}
251.16	246.41	8.05×10^{-12}	258.76	255.50	1.37×10^{-11}	261.79	260.41	8.61×10^{-12}
205.01	200.70	7.08×10^{-12}	221.42	218.33	1.27×10^{-11}	227.44	226.02	8.30×10^{-12}
165.16	161.51	5.89×10^{-12}	187.21	184.34	1.17×10^{-11}	188.31	186.90	7.93×10^{-12}
140.72	137.44	5.07×10^{-12}	152.48	149.96	1.01×10^{-11}	157.62	156.30	7.05×10^{-12}
113.76	110.80	4.39×10^{-12}	130.70	128.36	9.04×10^{-12}	127.20	125.86	6.46×10^{-12}
93.92	91.60	3.71×10^{-12}	109.14	107.02	8.04×10^{-12}	106.16	105.02	6.17×10^{-12}
71.72	70.05	3.14×10^{-12}	85.48	83.85	6.49×10^{-12}	86.13	84.92	5.38×10^{-12}
55.35	54.05	2.16×10^{-12}	65.57	64.29	5.15×10^{-12}	68.33	67.50	4.74×10^{-12}

Table D.19: Mass flow rate (\dot{M}_1) obtained in function of the initial and final pressures inside the upstream tank ($p_{1,0}$ and $p_{1,f}$, respectively) extracted for argon and krypton from temperature gradient experiments using $\Delta T = 67.5^\circ C$. During all these measurements, the cold tank was kept at $11.5^\circ C$ while the hot tank at $79.0^\circ C$.

Argon			Krypton		
$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]	$p_{1,0}$ [Pa]	$p_{1,f}$ [Pa]	\dot{M}_1 [kg/s]
1287.4	1286.4	2.06×10^{-11}	1074.4	1073.6	2.20×10^{-11}
1072.7	1071.6	1.60×10^{-11}	910.64	910.05	1.16×10^{-11}
877.95	876.92	1.93×10^{-11}	771.56	770.83	1.38×10^{-11}
764.48	763.35	1.64×10^{-11}	640.78	639.96	1.50×10^{-11}
634.49	633.19	1.52×10^{-11}	530.76	529.93	1.50×10^{-11}
540.49	539.08	1.55×10^{-11}	436.46	435.40	1.45×10^{-11}
435.74	434.17	1.44×10^{-11}	364.63	363.56	1.39×10^{-11}
365.85	364.41	1.26×10^{-11}	303.54	302.54	1.26×10^{-11}
304.36	302.66	1.26×10^{-11}	255.04	254.07	1.19×10^{-11}
262.69	261.20	1.21×10^{-11}	216.24	215.10	1.15×10^{-11}
220.21	218.50	1.07×10^{-11}	189.89	188.93	1.06×10^{-11}
183.47	182.00	1.01×10^{-11}	151.93	150.78	9.99×10^{-12}
155.24	153.75	9.02×10^{-12}	121.86	120.90	9.66×10^{-12}
128.58	127.11	8.74×10^{-12}	107.49	106.47	9.08×10^{-12}
104.73	103.46	8.01×10^{-12}	85.15	84.29	7.55×10^{-12}
87.74	86.55	7.32×10^{-12}	69.38	68.64	6.90×10^{-12}
68.99	68.11	5.75×10^{-12}			