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# Learning and controlling the source-filter representation of speech with a variational autoencoder<sup>☆</sup>

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## Abstract

Understanding and controlling latent representations in deep generative models is a challenging yet important problem for analyzing, transforming and generating various types of data. In speech processing, inspired from the anatomical mechanisms of phonation, the source-filter model considers that speech signals are produced from a few independent and physically meaningful continuous latent factors, among which the fundamental frequency  $f_0$  and the formants are of primary importance. In this work, we show that the source-filter model of speech production naturally arises in the latent space of a variational autoencoder (VAE) trained in an unsupervised manner on a dataset of natural speech signals. Using only a few seconds of labeled speech signals generated with an artificial speech synthesizer, we experimentally illustrate that  $f_0$  and the formant frequencies are encoded in orthogonal subspaces of the VAE latent space and we develop a weakly-supervised method to accurately and independently control these speech factors of variation within the learned latent subspaces. Without requiring additional information such as text or human-labeled data, this results in a deep generative model of speech spectrograms that is conditioned on  $f_0$  and the formant frequencies, and which is applied to the transformation of speech signals.

*Keywords:* Representation learning, deep generative models, variational autoencoder, source-filter model

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## 1. Introduction and related work

### 1.1. Introduction

High-dimensional data such as natural images or speech signals exhibit some form of regularity which prevents their dimensions from varying independently from each other. This suggests that there exists a latent representation of smaller dimension from which the high-dimensional observed data were generated. Discovering the hidden properties of complex data is the goal of representation learning, and deep latent-variable generative models have emerged as promising unsupervised approaches (Goodfellow et al., 2014; Kingma & Welling, 2014; Rezende et al., 2014; Chen et al., 2016; Higgins et al., 2017; Kim & Mnih, 2018; Chen et al., 2018). The variational autoencoder (VAE) (Kingma & Welling, 2014; Rezende et al., 2014), which is equipped with both a generative and inference model, can be used not only for data generation but also for analysis and transformation. As an explicit model of a probability density function (pdf), the VAE can also be used as a learned prior for solving inverse problems such as compressed sensing (Bora et al., 2017), speech enhancement (Bando et al., 2018; Leglaive et al., 2018), or source separation (Kameoka et al., 2019; Jayaram & Thickstun, 2020). Making sense of the latent representation learned by a VAE and

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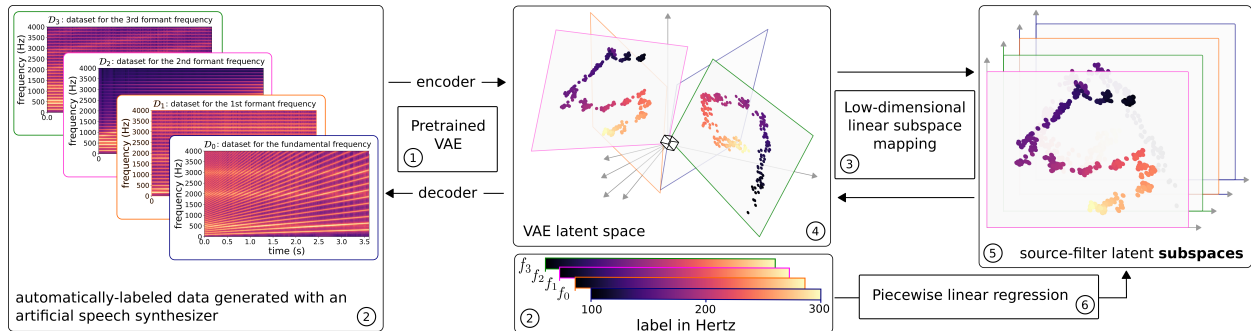


Figure 1: Overview of the proposed method: Given ① a VAE trained on hours of unlabeled speech signals and ② a few seconds of automatically-labeled speech generated with an artificial speech synthesizer, we put in evidence thanks to ③ a linear subspace learning method that ④ the VAE latent space is structured into ⑤ orthogonal subspaces that encode  $f_0$  and the formant frequencies, thus complying with the source-filter model of speech production. We propose ⑥ a weakly-supervised linear regression model to learn how to move into the source-filter latent subspaces, so as to perform speech manipulations in a disentangled manner.

controlling the underlying continuous factors of variation in the data are important challenges to build more expressive and interpretable generative models and probabilistic priors.

A series of previous works on representation learning with deep generative models, in particular VAEs, have focused on images (Higgins et al., 2017; Kim & Mnih, 2018; Chen et al., 2018; Locatello et al., 2019, 2020). Yet, it is not always easy to define the ground-truth latent factors of variation involved in the generation of natural images. For speech data, the latent factors of variation can be directly related to the anatomical mechanisms of speech production. Indeed, the source-filter model proposed by Fant (1970) considers that the production of speech signals results from the interaction of a source signal with a linear filter. In voiced speech, the source originates from the vibration of the vocal folds, which produces a quasi-periodic glottal sound wave whose fundamental frequency  $f_0$ , loosely referred to as the *pitch*, is a key element of speech prosody. In unvoiced speech, a noise source is produced by a turbulent airflow or an acoustic impulse. The source signal is modified by the vocal tract, which is assumed to act as a linear filter. The cavities of the vocal tract give rise to resonances, which are called the *formants* and are characterized by their frequency, amplitude and bandwidth. By moving the speech articulators such as the tongue, lips, and jaw, humans modify the shape of their vocal tract, which results in a change of the acoustic filter, the associated resonances, and the resulting speech sounds. For voiced phonemes, humans are able to control the formants independently of the pitch, i.e., to change the filter independently of the source (Fant, 1970), and of each other (MacDonald et al., 2011). The source-filter model thus considers that a speech signal is mainly characterized by a few continuous latent factors of variation corresponding to the source, among which  $f_0$  plays a central role, and to the filter, mostly characterized by the formants. The independence of the source and filter characteristics makes the speech signals an interesting material for disentangled representation learning methods, especially with deep generative latent-variable models such as the VAE.

In this work, we analyze and control the latent space of a VAE from the perspective of the source-filter model of speech production, which can be beneficial for various applications in speech analysis, transformation, and synthesis. An overview of the proposed approach is shown in Figure 1. We first train a VAE on a dataset of about 25 hours of unlabeled speech signals. Then, using only a few seconds of automatically labeled speech signals generated with an artificial speech synthesizer, we propose a weakly-supervised method to identify and independently control the source-filter continuous latent factors of speech variation within the latent space of the VAE. Our contributions are the following: (i) We identify the source-filter model in the VAE latent space by showing experimentally that  $f_0$  and the frequency of the first three formants are encoded in different subspaces. We put in evidence the orthogonality of the learned subspaces, which not only shows that the representation learned by the VAE complies with the source-filter model of speech production, but it also suggests that we could perform speech transformations in a disentangled manner (i.e., modifying one of the factors would not affect the others) by moving into the learned subspaces. (ii) We

propose to learn a piecewise linear regression model from the labels in the synthetic speech dataset to the coordinates in the corresponding latent subspaces. This weakly-supervised method allows us to precisely and independently control the source-filter factors of speech variation within the learned subspaces, as confirmed experimentally. Without requiring additional information such as text or human-labeled data, the proposed approach leads to a deep generative model of speech spectrograms that is conditioned on  $f_0$  and the formant frequencies. To the best of our knowledge, this is the first study showing the link between the classical source-filter model of speech production and the representation learned in the latent space of a VAE. Thanks to this link, we propose a principled method applied to the generation and transformation of speech signals controlled with interpretable trajectories of  $f_0$  and the formant frequencies.

Regarding this latter application, our objective is not to compete with traditional signal processing methods (these are discussed in the next subsection), which to the best of our knowledge remain the state-of-the-art. The interest of the present paper is rather to advance on the understanding of deep generative modeling of speech signals, while comparing honestly with highly-specialized traditional systems for which signal models are generally specifically designed for the task at hand. Moreover, advancing on the interpretability and control of the VAE latent space could be beneficial for downstream tasks, for instance to develop pitch-informed extensions of VAE-based speech enhancement methods such as those of Bando et al. (2018); Leglaive et al. (2018, 2020); Bie et al. (2021).

### 1.2. Related work

Time-scale, pitch-scale and timbre modification of speech signals is a highly covered research problem originally addressed with signal processing methods. Three main groups of approaches exist (Laroche, 2002): time-domain methods such as the pitch-synchronous overlap and add (PSOLA) algorithm (Moulines & Charpentier, 1990), methods that work in the short-time Fourier transform (STFT) domain such as the phase vocoder (Flanagan & Golden, 1966; Laroche & Dolson, 1999), and parametric approaches based for instance on linear predictive coding (LPC) (Makhoul, 1975; Markel & Gray, 1976), sinusoidal modeling (McAulay & Quatieri, 1986; George & Smith, 1997), or sinusoidal plus noise modeling (Serra & Smith, 1990; Laroche et al., 1993). Other signal-processing-based approaches to real-time speech manipulations include the STRAIGHT (Kawahara, 2006; Banno et al., 2007) and WORLD (Morise et al., 2016) vocoders, which exploit a decomposition of the speech signal into  $f_0$ , spectral envelope, and aperiodicity.

Deep learning has recently emerged as a promising approach to speech signal manipulation. A few methods have investigated combining traditional signal processing models with deep learning (Valin & Skoglund, 2019; Wang et al., 2019; Juvela et al., 2019; Lee et al., 2019; Choi et al., 2021). LPCNet is probably one of the most successful example, which inspired from the source-filter model to develop an efficient neural vocoder (Valin & Skoglund, 2019). It was recently extended to pitch shifting and time stretching of speech signals (Morrison et al., 2021). Yet, this last paper showed that time-domain PSOLA (TD-PSOLA) (Moulines & Charpentier, 1990) remains a very strong baseline that is difficult to outperform with deep learning methods.

Regarding the use of deep generative models (in particular VAEs) for speech modeling and transformation, the studies of Blaauw & Bonada (2016); Hsu et al. (2016, 2017b,a); Akuzawa et al. (2018) are pioneering. Of particular interest to the present paper is the work of Hsu et al. (2017a). The authors proposed to use VAEs for modifying the speaker identity and the phonemic content of speech signals by translations in the latent space of a VAE. Yet, this method requires to know predefined values of the latent representations associated with both the source and target speech attributes to be modified. The performance of the method thus depends on the quality of the estimation of the source attribute (e.g.,  $f_0$ ), which has to be obtained from the input speech signal to be transformed. This differs from the proposed method which relies on projection onto the latent subspace associated with a given attribute, and only requires the target value for this attribute. Moreover, Hsu et al. (2017a) did not address the control of continuous factors of speech variation in the VAE latent space, contrary to the present work.

For deep latent representation learning methods, the challenge is to relate the learned representation to interpretable speech attributes. In Qian et al. (2020) and Webber et al. (2020), this interpretability is enforced by the design of the model. Qian et al. (2020) proposed to use three independent encoder networks to decompose a speech signal into  $f_0$ , timbre and rhythm latent representations. Webber et al. (2020) focused



on controlling source-filter parameters in speech signals, where the ability to control a given parameter (e.g.,  $f_0$ ) is enforced explicitly using labeled data and adversarial learning. In this approach, each parameter to be controlled requires a dedicated training of the model. Moreover, these methods are speaker-dependent, as speech generation in Qian et al. (2020) is conditioned on the speaker identity and Webber et al. (2020) used a single-speaker training dataset. This contrasts with the proposed method which is speaker-independent, and in which the source-filter representation of speech naturally emerges in the latent space of a single unsupervised VAE model.

In the machine learning and computer vision communities, variants of the VAE have recently led to considerable progress in disentangled representation learning (Kim & Mnih, 2018; Higgins et al., 2017; Chen et al., 2018). From experimental analyses on image data, these methods suggest that a vanilla VAE cannot learn a disentangled representation. Moreover, Locatello et al. (2019, 2020) recently showed both theoretically and from a large-scale experimental study that the unsupervised learning of disentangled representations is impossible without inductive biases (implicit or explicit assumptions by which a machine learning algorithm is able to generalize) on both the models and the data. In the present study, we experimentally show that learning a disentangled source-filter representation of speech using a simple VAE is possible, complying with the definition of disentanglement proposed in (Higgins et al., 2018). We precisely employ a few examples of artificially-generated labeled speech data in order to disentangle the latent representation of a simple VAE, in terms of source-filter factors of speech variation.

Several methods have been recently proposed to control continuous factors of variation in deep generative models (Jahanian et al., 2019; Plumerault et al., 2020; Goetschalckx et al., 2019; Härkönen et al., 2020), focusing essentially on generative adversarial networks. They consist in identifying and then moving onto semantically meaningful directions in the latent space of the model. The present work is inspired by (Plumerault et al., 2020), which assumes that a factor of variation can be predicted from the projection of the latent vector along a specific axis, learned from artificially generated trajectories. The proposed method is however more generic, thanks to the learning of latent subspaces associated to the latent factors and to the introduction of a general formalism based on the use of “biased aggregated posteriors. Moreover, these previous works on controlling deep generative models only allow for moving “blindly onto semantically meaningful directions in the latent space. In the present study, we are able to generate data conditioned on a specific target value for a given factor of variation (e.g., a given formant frequency value). Finally, these previous works focused on image data. To the best of our knowledge, the present paper proposes the first approach to identify and control source-filter factors of speech variation in a VAE.

The rest of this paper is organized as follows: Section 2 presents the proposed method for analyzing and controlling source-filter factors of speech variation in a VAE. The method is evaluated experimentally and compared with traditional signal processing algorithms and with the approach of Hsu et al. (2017a) in Section 3. We finally conclude in Section 4.

## 2. Analyzing and controlling source-filter factors of speech variation in a VAE

In this section, we first present the VAE model that we build upon. Then, from this VAE trained on natural speech signals and a few artificially-generated labeled speech signals, we propose (i) a method to identify and learn latent subspaces encoding source-filter factors of speech variation, (ii) a simple strategy to measure the disentanglement of the learned representation, and (iii) a weakly-supervised approach to control the continuous factors of variation in the learned subspaces and generate corresponding speech signals.

### 2.1. Variational autoencoder

Generative modeling consists in learning a probabilistic model of an observable random variable  $\mathbf{x} \in \mathcal{X} \subset \mathbb{R}^D$ . Let  $\mathcal{D} = \{\mathbf{x}_1, \dots, \mathbf{x}_N \in \mathcal{X}\}$  be a dataset of  $N = \#\mathcal{D}$  independent and identically distributed (i.i.d.) observations of  $\mathbf{x}$ . The empirical distribution of  $\mathbf{x}$  is defined by  $\hat{p}(\mathbf{x}) = \frac{1}{N} \sum_{\mathbf{x}_n \in \mathcal{D}} \delta(\mathbf{x} - \mathbf{x}_n)$ , where  $\delta$  is the Dirac delta function, which is null everywhere except in 0 where it takes the value 1.

The variational autoencoder (VAE) (Kingma & Welling, 2014; Rezende et al., 2014) attempts to approximate  $\hat{p}(\mathbf{x})$  with a pdf  $p_\theta(\mathbf{x})$  parametrized by  $\theta$ . High-dimensional data such as natural images or speech

signals exhibit some form of regularity which prevents the  $D$  dimensions of  $\mathbf{x}$  from varying independently from each other. We can thus assume that there exists a latent variable  $\mathbf{z} \in \mathbb{R}^L$ , with  $L \ll D$ , from which the observed data were generated. Accordingly, the model distribution in the VAE is defined by marginalizing the joint distribution of the latent and observed data,  $p_\theta(\mathbf{x}) = \int p_\theta(\mathbf{x}|\mathbf{z})p(\mathbf{z})d\mathbf{z}$ .

In this work, the observed data vector  $\mathbf{x} \in \mathcal{X} = \mathbb{R}_+^D$  denotes the power spectrum of a short frame of speech signal (i.e., a column of the short-time Fourier transform (STFT) power spectrogram). Its entries are thus non negative and its dimension  $D$  equals the number of frequency bins. We use the Itakura-Saito VAE (IS-VAE) (Bando et al., 2018; Leglaive et al., 2018; Girin et al., 2019) defined by

$$p(\mathbf{z}) = \mathcal{N}(\mathbf{z}; \mathbf{0}, \mathbf{I}), \quad (1)$$

$$p_\theta(\mathbf{x}|\mathbf{z}) = \prod_{d=1}^D \text{Exp}\left([\mathbf{x}]_d; [\mathbf{v}_\theta(\mathbf{z})]_d^{-1}\right), \quad (2)$$

where  $\mathcal{N}$  and  $\text{Exp}$  denote the densities of the multivariate Gaussian and univariate exponential distributions, respectively, and  $[\mathbf{v}]_d$  denotes the  $d$ -th entry of  $\mathbf{v}$ . The inverse scale parameters of  $p_\theta(\mathbf{x}|\mathbf{z})$  are provided by a neural network called the decoder, parametrized by  $\theta$  and taking  $\mathbf{z}$  as input.

The marginal likelihood  $p_\theta(\mathbf{x})$  and the posterior distribution  $p_\theta(\mathbf{z}|\mathbf{x})$  are intractable due to the nonlinearities of the decoder, so it is necessary to introduce an inference model  $q_\phi(\mathbf{z}|\mathbf{x}) \approx p_\theta(\mathbf{z}|\mathbf{x})$ , which is defined by

$$q_\phi(\mathbf{z}|\mathbf{x}) = \mathcal{N}(\mathbf{z}; \boldsymbol{\mu}_\phi(\mathbf{x}), \text{diag}\{\mathbf{v}_\phi(\mathbf{x})\}), \quad (3)$$

where the mean and variance parameters are provided by a neural network called the encoder network, parametrized by  $\phi$  and taking  $\mathbf{x}$  as input. Then, the VAE training consists in maximizing a lower-bound of  $\ln p_\theta(\mathbf{x})$ , called the evidence lower-bound (ELBO) and defined by

$$\mathcal{L}(\theta, \phi) = \mathbb{E}_{\hat{p}(\mathbf{x})} \left[ \mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\ln p_\theta(\mathbf{x}|\mathbf{z})] - D_{\text{KL}}(q_\phi(\mathbf{z}|\mathbf{x}) \parallel p(\mathbf{z})) \right], \quad (4)$$

where  $D_{\text{KL}}(q \parallel p) = \mathbb{E}_q [\ln q - \ln p]$  is the Kullback-Leibler divergence. During training, the generative and inference model parameters  $\theta$  and  $\phi$  are jointly estimated by maximizing the ELBO, using (variants of) stochastic gradient descent with the so-called reparameterization trick (Kingma & Welling, 2014; Rezende et al., 2014).

## 2.2. Learning source-filter latent subspaces

In addition to the pre-trained IS-VAE speech spectrogram model introduced in the previous subsection, we also assume the availability of an artificial speech synthesizer allowing for an accurate and independent control of  $f_0$  and the formant frequencies. We use Soundgen (Anikin, 2019), a parametric synthesizer based on the source-filter model of speech production. For a given speech sound, the voiced component of the source signal is generated by a sum of sine waves, the noise component by a filtered white noise, and both components are then summed and passed through a linear filter simulating the effect of the human vocal tract. Importantly, this synthesizer allows us to easily generate artificial speech data labeled with  $f_0$  and the formant frequency values.

Formally, let  $f_i$  denote the speech factor of variation (in Hz) corresponding to the fundamental frequency, for  $i = 0$ , and to the formant frequencies, for  $i \in \{1, 2, \dots\}$ . Let  $\mathcal{D}_i$  denote a dataset of artificially-generated speech vectors (more precisely short-term power spectra) synthesized by varying only  $f_i$ , all other factors  $\{f_j, j \neq i\}$  being arbitrarily fixed. All examples in  $\mathcal{D}_i$  are labeled with the factors of variation. It would be relatively difficult to build such a dataset from existing corpora of unlabeled natural speech. In contrast, it is a very easy task using an artificial speech synthesizer such as Soundgen (Anikin, 2019), which precisely takes  $f_0$  and the formant parameters as input, and outputs waveforms from which we extract power spectra.

Let  $\hat{p}^{(i)}(\mathbf{x})$  denote the empirical distribution associated with  $\mathcal{D}_i$ , defined similarly as  $\hat{p}(\mathbf{x})$ . We also introduce the following marginal distribution over the latent vectors:

$$\hat{q}_\phi^{(i)}(\mathbf{z}) = \int q_\phi(\mathbf{z}|\mathbf{x})\hat{p}^{(i)}(\mathbf{x})d\mathbf{x} = \frac{1}{\#\mathcal{D}_i} \sum_{\mathbf{x}_n \in \mathcal{D}_i} q_\phi(\mathbf{z}|\mathbf{x}_n). \quad (5)$$

In the literature, this quantity is referred to as the aggregated posterior (Makhzani et al., 2016). However,  $q_\phi(\mathbf{z}|\mathbf{x})$  is usually aggregated over the empirical distribution  $\hat{p}(\mathbf{x})$  such that the aggregated posterior is expected to match with the prior  $p(\mathbf{z})$  (Chen et al., 2018; Dai & Wipf, 2018). In contrast, in Equation (5) we aggregate over the “biased” data distribution  $\hat{p}^{(i)}(\mathbf{x})$ , where we know only one latent factor varies. This defines the explicit inductive bias (Locatello et al., 2019) that we exploit to learn the latent source-filter representation of speech in the VAE.

In the following of the paper, without loss of generality, we assume that, for each data vector in  $\mathcal{D}_i$ , the associated latent vector  $\mathbf{z}$  has been centered by subtracting the mean vector

$$\boldsymbol{\mu}_\phi(\mathcal{D}_i) = \mathbb{E}_{\hat{q}_\phi^{(i)}(\mathbf{z})}[\mathbf{z}] = \frac{1}{\#\mathcal{D}_i} \sum_{\mathbf{x}_n \in \mathcal{D}_i} \boldsymbol{\mu}_\phi(\mathbf{x}_n). \quad (6)$$

Because only one factor varies in  $\mathcal{D}_i$ , we expect latent vectors drawn from the “biased” aggregated posterior in Equation (5) to live on a lower-dimensional manifold embedded in the original latent space  $\mathbb{R}^L$ . We assume this manifold to be a subspace characterized by its semi-orthogonal basis matrix  $\mathbf{U}_i \in \mathbb{R}^{L \times M_i}$ ,  $1 \leq M_i < L$ . This matrix is computed by solving the following optimization problem:

$$\min_{\mathbf{U} \in \mathbb{R}^{L \times M_i}} \mathbb{E}_{\hat{q}_\phi^{(i)}(\mathbf{z})} \left[ \|\mathbf{z} - \mathbf{U}\mathbf{U}^\top \mathbf{z}\|_2^2 \right], \quad s.t. \quad \mathbf{U}^\top \mathbf{U} = \mathbf{I}. \quad (7)$$

The space spanned by the columns of  $\mathbf{U}_i$  is a subspace of the original latent space  $\mathbb{R}^L$  in which the latent vectors associated with the variation of the factor  $f_i$  in  $\mathcal{D}_i$  are expected to live. In Appendix A, we show that, similarly to the principal component analysis (PCA) (Pearson, 1901), the solution to the optimization problem (7) is given by the  $M_i$  eigenvectors corresponding to the  $M_i$  largest eigenvalues of

$$\mathbf{S}_\phi(\mathcal{D}_i) = \frac{1}{\#\mathcal{D}_i} \sum_{\mathbf{x}_n \in \mathcal{D}_i} \left[ \boldsymbol{\mu}_\phi(\mathbf{x}_n) \boldsymbol{\mu}_\phi(\mathbf{x}_n)^\top + \text{diag}\{\mathbf{v}_\phi(\mathbf{x}_n)\} \right] - \boldsymbol{\mu}_\phi(\mathcal{D}_i) \boldsymbol{\mu}_\phi(\mathcal{D}_i)^\top. \quad (8)$$

The dimension  $M_i$  of the subspace can be chosen such as to retain a certain percentage of the data variance in the latent space. Note that the only source of supervision used here is the knowledge that only the factor  $f_i$  varies in the dataset  $\mathcal{D}_i$ .

### 2.3. Disentanglement analysis of the latent representation

As defined by Higgins et al. (2018), a representation is disentangled if it is possible to learn orthogonal latent subspaces associated with each factor of variation, whether they are single- or multi-dimensional. The approach presented in the previous subsection exactly follows this definition and offers a natural and straightforward way to objectively measure if the unsupervised VAE managed to learn a disentangled representation of the factors of variation under consideration. First, by simply looking at the eigenvalues associated with the columns of  $\mathbf{U}_i \in \mathbb{R}^{L \times M_i}$ , we can measure the amount of variance that is retained by the projection  $\mathbf{U}_i \mathbf{U}_i^\top$ . If a small number of components  $M_i$  represents most of the variance, it indicates that only a few intrinsic dimensions of the latent space are dedicated to the factor of variation  $f_i$  and varying this factor can be done by affine transformations. Second, if for two different factors of variation  $f_i$  and  $f_j$ , with  $i \neq j$ , the columns of  $\mathbf{U}_i$  are orthogonal to those of  $\mathbf{U}_j$ , this indicates that the two factors are encoded in orthogonal subspaces and therefore disentangled. It should however be verified experimentally that applying transformations by moving onto the subspace associated with  $f_i$  generalizes to values of  $\{f_j, j \neq i\}$  different than the ones used in  $\mathcal{D}_i$ .

### 2.4. Controlling the source-filter factors of variation

So far, for each factor  $f_i$ , we have defined a methodology to learn a latent subspace  $\mathbf{U}_i \in \mathbb{R}^{L \times M_i}$  that encodes its variations in the dataset  $\mathcal{D}_i$ , containing a few examples of speech data generated by an artificial synthesizer. Making now use of the labels in  $\mathcal{D}_i$ , we learn a regression model  $\mathbf{g}_{\eta_i} : \mathbb{R}_+ \mapsto \mathbb{R}^{M_i}$  from the

factor  $f_i$ , whose value is denoted by  $y \in \mathbb{R}_+$ , to the data coordinates in the latent subspace defined by  $\mathbf{U}_i$ . The parameters  $\eta_i$  are thus defined as the solution of the following optimization problem:

$$\min_{\eta} \left\{ \mathbb{E}_{\hat{q}_{\phi}^{(i)}(\mathbf{z}, y)} \left[ \|\mathbf{g}_{\eta}(y) - \mathbf{U}_i^{\top} \mathbf{z}\|_2^2 \right] \stackrel{c}{=} \frac{1}{\#\mathcal{D}_i} \sum_{(\mathbf{x}_n, y_n) \in \mathcal{D}_i} \|\mathbf{g}_{\eta}(y_n) - \mathbf{U}_i^{\top} (\boldsymbol{\mu}_{\phi}(\mathbf{x}_n) - \boldsymbol{\mu}_{\phi}(\mathcal{D}_i))\|_2^2 \right\}, \quad (9)$$

where  $\hat{q}_{\phi}^{(i)}(\mathbf{z}, y) = \int q_{\phi}(\mathbf{z}|\mathbf{x}) \hat{p}^{(i)}(\mathbf{x}, y) d\mathbf{x}$ ,  $\hat{p}^{(i)}(\mathbf{x}, y)$  is the empirical distribution associated with  $\mathcal{D}_i$ , considering now both the speech data vector  $\mathbf{x}$  and the label  $y$ , and  $\stackrel{c}{=}$  denotes equality up to an additive constant w.r.t.  $\eta$ . This approach can be seen as a probabilistic extension of principal component regression (Hotelling, 1957; Kendall, 1957). The dataset  $\mathcal{D}_i$  is very small with only a few hundreds examples, and as it is synthetic and labels are not provided by human annotators, the problem can be considered very weakly supervised. For simplicity and because it revealed efficient for this task,  $\mathbf{g}_{\eta_i}$  is chosen as a piece-wise linear regression model learned independently for each output coordinate  $m \in \{1, \dots, M_i\}$ . This choice is supported by the fact that the semi-orthogonal matrix  $\mathbf{U}_i$  decorrelates the data (Bengio et al., 2013). Solving the optimization problem (9) then basically consists in solving a linear system of equations (Jekel & Venter, 2019).

We can now transform a speech spectrogram by analyzing it with the VAE encoder, then linearly moving in the learned subspaces using the above regression model, and finally resynthesizing it with the VAE decoder. Given a source latent vector  $\mathbf{z}$  and a target value  $y$  for the factor  $f_i$ , we apply the following affine transformation:

$$\tilde{\mathbf{z}} = \mathbf{z} - \mathbf{U}_i \mathbf{U}_i^{\top} \mathbf{z} + \mathbf{U}_i \mathbf{g}_{\eta_i}(y). \quad (10)$$

This transformation consists in (i) subtracting the projection of  $\mathbf{z}$  onto the subspace associated with the factor of variation  $f_i$ ; and (ii) adding the target component provided by the regression model  $\mathbf{g}_{\eta_i}$  mapped from the learned subspace to the original latent space by the matrix  $\mathbf{U}_i$ . This operation allows us to move only in the latent subspace associated with the factor  $f_i$ . If this subspace is orthogonal to the latent subspaces associated with the other factors  $\{f_j, j \neq i\}$ , the latter should remain the same between  $\mathbf{z}$  and  $\tilde{\mathbf{z}}$ , only  $f_i$  should be modified. This process can be straightforwardly generalized to multiple factors, by subtracting and adding terms corresponding to each one of them. Contrary to Hsu et al. (2017a), the operation in Equation (10) does not require the knowledge of the factor  $f_i$  associated with the source vector  $\mathbf{z}$ , it only requires the value  $y$  associated with the target vector  $\tilde{\mathbf{z}}$ .

Finally, as the prior  $p(\mathbf{z})$  and inference model  $q_{\phi}(\mathbf{z}|\mathbf{x})$  are Gaussian (see Equations (2) and (3)), the transformation in Equation (10) has the following probabilistic formulation (using  $\mathbf{U}_i^{\top} \mathbf{U}_i = \mathbf{I}$ ):

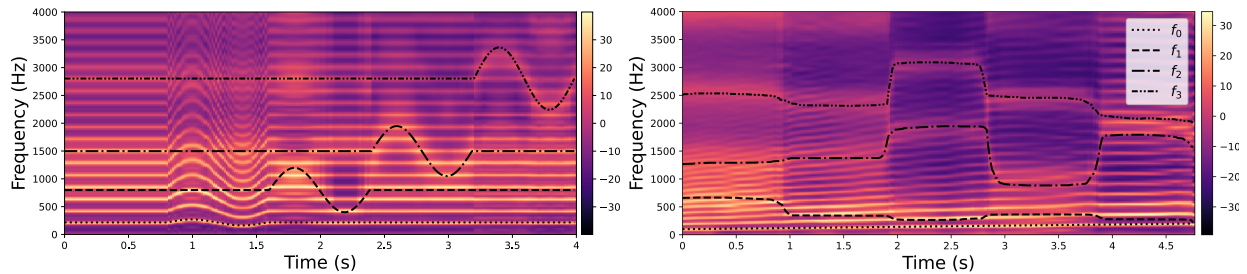
$$p(\tilde{\mathbf{z}}; f_i = y) = \mathcal{N}\left(\tilde{\mathbf{z}}; \mathbf{U}_i \mathbf{g}_{\eta_i}(y), \mathbf{M}_i\right) \quad (11)$$

$$q_{\phi}(\tilde{\mathbf{z}}|\mathbf{x}; f_i = y) = \mathcal{N}\left(\tilde{\mathbf{z}}; \mathbf{U}_i \mathbf{g}_{\eta_i}(y) + \mathbf{M}_i \boldsymbol{\mu}_{\phi}(\mathbf{x}), \mathbf{M}_i \text{diag}\{\mathbf{v}_{\phi}(\mathbf{x})\}\right), \quad (12)$$

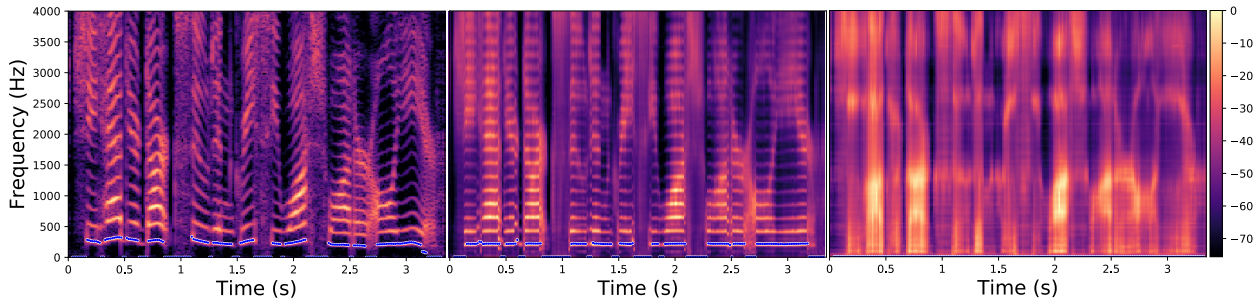
where  $\mathbf{M}_i = \mathbf{I} - \mathbf{U}_i \mathbf{U}_i^{\top}$ . The prior in Equation (11) is now conditioned on the factor  $f_i$  and can be used to generate speech data given input trajectories of  $f_0$  and formant frequencies. As we assumed centered latent data, the mean vector  $\boldsymbol{\mu}_{\phi}(\mathcal{D}_i)$  defined in Equation (6) must be added to  $\tilde{\mathbf{z}}$  before mapping this vector through the generative model  $p_{\theta}(\mathbf{x}|\mathbf{z})$ .

### 3. Experiments

This section presents qualitative and quantitative experimental results of the proposed method for controlling  $f_0$  and the formant frequencies of speech signals with a VAE. The VAE is trained on about 25 hours of multi-speaker speech data from the Wall Street Journal (WSJ0) dataset (Garofolo et al., 1993a). The data space dimension is 513 and the latent space dimension is 16. For a given factor of variation, the corresponding latent subspace is learned (see Section 2.2) using short trajectories of speech power spectra (corresponding to a few seconds of speech) generated with Soundgen (Anikin, 2019), all other factors being arbitrarily fixed. When solving the optimization problem (7), the latent subspace dimension  $M_i$  of each



(a)  $f_0$  and formant transformations of the vowel /a/ uttered by a female speaker. (b) Spectrogram generated from input trajectories of  $f_0$  and formant frequencies.



(c) Left: original spectrogram of a speech signal uttered by a female speaker; Middle: transformed spectrogram where  $f_0$  is set constant over time; Right: transformed spectrogram where the original voiced speech signal (left) is converted into a whispered speech signal (i.e., the pitch is removed).

Figure 2: Qualitative example of modified and generated spectrograms with the proposed method. The color bar indicates the power in dB.

factor of variation is chosen such that 80% of the data variance is retained. This leads  $M_0 = 4$ ,  $M_1 = 1$  and  $M_2 = M_3 = 3$ . The regression models used to control the speech factors of variation in the latent space (see Section 2.4) are learned on the same trajectories, but using the labels that correspond to the input control parameters of Soundgen (i.e.,  $f_0$  and formant frequencies values). More details on the experimental set-up can be found in Appendix B. Given a generated or transformed spectrogram, we use Waveglow (Prenger et al., 2019) to reconstruct the time-domain signal.

### 3.1. Qualitative results

In Figure 2a, we illustrate the ability of the proposed method to modify  $f_0$  and the formant frequencies in an accurate and independent manner. The spectrogram contains five segments of equal length. The first segment corresponds to the original spectrogram of the steady vowel /a/ uttered by a female speaker. In the following segments, we vary successively each individual factor  $f_i$ , for  $i = 0$  to 3, as indicated by the black lines in the figure. Variations of  $f_0$  modify the harmonic structure of the signal while keeping the formant structure unaltered. Variations of  $f_i$ ,  $i \in \{1, 2, 3\}$ , modify the formant frequencies, as indicated by the color map, while keeping  $f_0$  unaltered.

Figure 2b represents a spectrogram generated by using the conditional prior in Equation (11) (generalized to conditioning on multiple factors). We can see that the characteristics of the generated speech spectrogram match well with the input trajectories represented by the lines in the figure. In Figure 2c, from left to right we show the original spectrogram of a speech signal uttered by a female speaker (left), and the transformed spectrograms where  $f_0$  is set constant over time (middle) and where the pitch has been removed (i.e., the original voiced speech signal is converted into a whispered speech signal) (right). This last spectrogram is simply obtained by subtracting to  $\mathbf{z}$  its projection onto the latent subspace corresponding to  $f_0$  (i.e., by considering only the two first terms in the right-hand side of Equation (10)). This results in a spectrogram where the harmonic component is neutralized, while preserving the original formant structure. This is

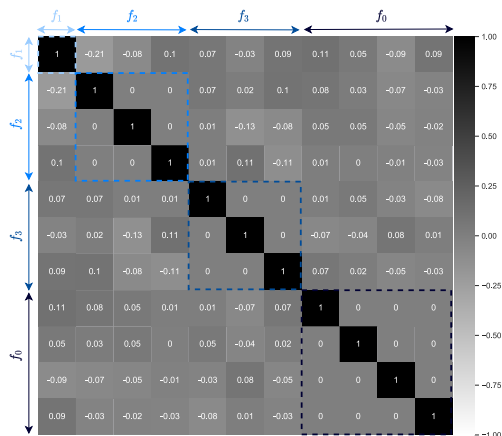


Figure 3: Correlation matrix of the learned latent subspaces basis vectors.

Factor	Min (in Hz)	Max	Step size (in Hz)	
			English vowels dataset	TIMIT dataset
$f_0$	100	300	1	10
$f_1$	300	900	10	50
$f_2$	1100	2700	20	100
$f_3$	2200	3200	20	50

Table 1: Variation range and step size used for the transformation of each test signal in the English vowels and TIMIT datasets, along each factor of variation.

remarkable considering that the VAE was not trained on whispered speech signals, and it further confirms that the proposed method dissociates the source and the filter contributions in the VAE latent space.

Audio examples and additional examples of generated and transformed speech spectrograms can be found online.<sup>1</sup> In Appendix C, through visualizations of trajectories in the learned latent subspaces, we illustrate that, according to each factor, the proximity of two speech spectra is preserved in the corresponding latent subspace.

### 3.2. Quantitative results

#### 3.2.1. Orthogonality of the latent subspaces

In this experiment, we quantitatively evaluate the proposed method in terms of disentanglement of the learned source-filter latent representation. Following the discussion in Section 2.3, we compute the dot product between all pairs of unit vectors in the matrices  $\mathbf{U}_i \in \mathbb{R}^{L \times M_i}$ ,  $i \in \{0, 1, 2, 3\}$ . Figure 3 shows that the resulting correlation matrix is mainly diagonal. Except for a correlation value of  $-0.21$  across  $f_1$  and the first component of  $f_2$ , all other values are below 0.13 (in absolute value), confirming the orthogonality of the learned subspaces and thus the disentanglement of the learned source-filter representation of speech.

#### 3.2.2. Pitch and formant transformations

In this experiment, we quantitatively evaluate the performance of the proposed method regarding the modification of  $f_0$  and the formant frequencies in speech signals (see Section 2.4).

*Experimental set-up.* We use a corpus of 12 English vowels uttered by 50 male and 50 female speakers (Hillenbrand et al., 1995), which is labeled with  $f_0$  and the formant frequencies. We also use the TIMIT dataset (Garofolo et al., 1993b), a corpus of phonemically and lexically transcribed speech of American English speakers of different sexes and dialects. We used the test corpus containing 1680 utterances. Because we are interested in studying the interaction between modifications of  $f_0$  and the formant frequencies, we only evaluate the method on the phonemes that are voiced (40 phonemes over a total of 52), which can be identified using the annotations. We transform each test signal in the English vowels and TIMIT datasets by varying one single factor  $f_i$  at a time, for  $i \in \{0, 1, 2, 3\}$ , according to the ranges and step sizes given in Table 1. For instance, when performing transformations of  $f_0$ , for each test signal in the English vowels dataset, we vary linearly the target  $f_0$  value between 100 and 300 Hz, with a step size of 1 Hz, thus resulting in 200 transformations.

<sup>1</sup><https://samsad35.github.io/site-sfvae/>

*Metrics.* For the modification of each factor  $f_i$ , we measure the performance regarding three aspects: First, in terms of *accuracy* by comparing the target value for the factor (see Equation (10)) and its estimation computed from the modified output speech signal. Second, in terms of *disentanglement*, by comparing the values of  $f_j$  for  $j \neq i$ , before and after modification of the factor  $f_i$ . Third, in terms of speech *naturalness* of the transformed signal.

Accuracy and disentanglement are measured in terms of relative absolute error (in percent, the lower the better). For a given factor  $f_i$ , it is defined by  $\delta f_i = 100\% \times |\hat{y} - y|/y$  where  $y$  is the target value of  $f_i$  and  $\hat{y}$  its estimation from the output transformed signal. Let us take the example of a modification of  $f_0$ :  $\delta f_0$  measures the accuracy of the transformation on  $f_0$  while  $\delta f_1$ ,  $\delta f_2$  and  $\delta f_3$  are used to assess if the other factors of variation  $f_1$ ,  $f_2$  and  $f_3$  remained unchanged after modifying  $f_0$ . We use CREPE (Kim et al., 2018) to estimate  $f_0$  and Parselmouth (Jadoul et al., 2018), which is based on PRAAT (Boersma & Weenink, 2021), to estimate the formant frequencies. Regarding speech naturalness, we use the objective measure provided by NISQA (Mittag & Möller, 2020). This metric (the higher the better) was developed in the context of speech transformation algorithms and it was shown to highly correlate with subjective mean opinion scores (MOS) (i.e., human ratings). As a reference, the score provided by NISQA on the original dataset of English vowels (i.e., without any processing) is equal to  $2.60 \pm 0.53$ .

TIMIT is phonemically richer than the English vowels dataset, however it is not labeled with  $f_0$  and the formant frequencies. Therefore, we do not have the ground truth values which makes the evaluation in terms of disentanglement more difficult than with the English vowels labeled dataset. Instead of the ground truth, we use the formant frequencies and  $f_0$  computed on the original speech utterances (i.e., before transformation). This makes the evaluation on TIMIT less reliable than on the English vowels dataset, but it allows us to test the methods on a larger variety of phonemes.

*Methods.* We compare the proposed approach with several methods from the literature: (i) TD-PSOLA (Moulines & Charpentier, 1990) performs  $f_0$  modification through the decomposition of the signal into pitch-synchronized overlapping frames. (ii) WORLD (Morise et al., 2016) is a vocoder also used for  $f_0$  modification. It decomposes the speech signal into three components characterizing  $f_0$ , the aperiodicity, and the spectral envelope. (iii) The method proposed by Hsu et al. (2017a) (here referred to as “VAE baseline”) consists in applying translations directly in the latent space of the VAE. Unlike the proposed approach, this method requires predefined latent attribute representations  $\mu_{\text{src}}$  and  $\mu_{\text{trgt}}$  associated with the source and target values of the factor to be modified, respectively. In particular, computing  $\mu_{\text{src}}$  requires analyzing the input speech signal, for instance to estimate  $f_0$ , which is not the case for the proposed method. The source and target latent attribute representations are then used to perform the translation  $\tilde{\mathbf{z}} = \mathbf{z} - \mu_{\text{src}} + \mu_{\text{trgt}}$ , where  $\mathbf{z}$  and  $\tilde{\mathbf{z}}$  are respectively the original and modified latent vectors. To ensure fair comparison, we build dictionaries of predefined latent attribute representations using the same artificially-generated speech data that were used in the weakly-supervised training stage of the proposed method. All the methods we compare with require a pre-processing of the input speech signal to compute the input trajectory of the factor to be modified, which is not the case of the proposed method.

*Discussion.* Experimental results (mean and standard deviation) are shown in Table 2. Compared to the VAE baseline, the proposed method obtains better performance in terms of accuracy, disentanglement, and naturalness, for both test datasets. These results confirm the effectiveness of performing the transformations in the learned latent subspaces and not directly in the latent space, as well as the advantage of using regression models instead of predefined latent attribute representations. Regarding  $f_0$  transformation, WORLD obtains the best performance in terms of disentanglement, which is because the source and filter contributions are decoupled in the architecture of the vocoder. In terms of naturalness, WORLD and then TD-PSOLA obtain the best performance. This may be explained by the fact that these methods operate directly in the time domain, therefore they do not suffer from phase reconstruction artifacts, unlike the proposed and VAE baseline methods. Naturalness is indeed greatly affected by phase reconstruction artifacts, even from an unaltered speech spectrogram (i.e., without transformation). Phase reconstruction in a multi-speaker setting is still an open problem in speech processing. We want to emphasize that the objective of this study is not to compete with traditional signal processing methods such as TD-PSOLA and WORLD. It is rather to

Factor	Method	English vowels dataset					TIMIT dataset				
		NISQA ( $\uparrow$ )	$\delta f_0$ (% , $\downarrow$ )	$\delta f_1$ (% , $\downarrow$ )	$\delta f_2$ (% , $\downarrow$ )	$\delta f_3$ (% , $\downarrow$ )	NISQA ( $\uparrow$ )	$\delta f_0$ (% , $\downarrow$ )	$\delta f_1$ (% , $\downarrow$ )	$\delta f_2$ (% , $\downarrow$ )	$\delta f_3$ (% , $\downarrow$ )
$f_0$	TD-PSOLA	2.32 $\pm$ 0.55	3.8 $\pm$ 2.5	6.3 $\pm$ 2.8	3.7 $\pm$ 0.9	2.1 $\pm$ 0.5	2.36 $\pm$ 0.50	2.4 $\pm$ 1.9	7.9 $\pm$ 0.6	4.5 $\pm$ 0.3	3.9 $\pm$ 0.2
	WORLD	2.49 $\pm$ 0.60	4.5 $\pm$ 0.6	3.7 $\pm$ 1.8	2.3 $\pm$ 0.7	1.2 $\pm$ 0.2	2.45 $\pm$ 0.47	0.3 $\pm$ 0.1	7.1 $\pm$ 1.2	6.2 $\pm$ 0.4	4.2 $\pm$ 0.2
	VAE baseline	1.94 $\pm$ 0.43	6.21 $\pm$ 2.8	10.4 $\pm$ 2.4	6.2 $\pm$ 0.9	4.5 $\pm$ 0.2	1.59 $\pm$ 0.43	16.1 $\pm$ 6.3	17.0 $\pm$ 3.0	12.1 $\pm$ 0.2	10.9 $\pm$ 1.3
	Proposed	2.08 $\pm$ 0.48	0.8 $\pm$ 0.2	7.2 $\pm$ 1.3	3.6 $\pm$ 1.2	3.8 $\pm$ 0.3	2.28 $\pm$ 0.57	0.8 $\pm$ 0.6	9.1 $\pm$ 1.1	8.3 $\pm$ 0.9	6.0 $\pm$ 1.8
$f_1$	VAE baseline	1.84 $\pm$ 0.5	11.3 $\pm$ 4.2	15.1 $\pm$ 3.5	6.0 $\pm$ 1.2	4.2 $\pm$ 0.4	1.42 $\pm$ 0.34	10.1 $\pm$ 2.8	16.4 $\pm$ 1.4	12.4 $\pm$ 0.9	11.2 $\pm$ 2.6
	Proposed	1.85 $\pm$ 0.4	6.0 $\pm$ 1.6	8.4 $\pm$ 3.2	5.7 $\pm$ 0.4	4.4 $\pm$ 0.3	1.66 $\pm$ 0.31	7.1 $\pm$ 3.6	9.2 $\pm$ 0.8	9.0 $\pm$ 1.3	7.8 $\pm$ 1.1
$f_2$	VAE baseline	2.01 $\pm$ 0.4	19.5 $\pm$ 3.2	10.7 $\pm$ 0.5	10.9 $\pm$ 1.9	5.8 $\pm$ 0.6	1.46 $\pm$ 0.30	19.3 $\pm$ 5.0	16.4 $\pm$ 0.8	20.3 $\pm$ 6.3	11.5 $\pm$ 0.5
	Proposed	2.03 $\pm$ 0.43	8.5 $\pm$ 1.1	8.7 $\pm$ 1.1	6.2 $\pm$ 1.5	5.8 $\pm$ 0.2	1.49 $\pm$ 0.30	9.1 $\pm$ 2.2	8.3 $\pm$ 1.3	4.3 $\pm$ 1.3	8.1 $\pm$ 0.2
$f_3$	VAE baseline	1.82 $\pm$ 0.14	27.0 $\pm$ 1.5	13.0 $\pm$ 1.3	12.0 $\pm$ 1.8	7.3 $\pm$ 1.5	1.40 $\pm$ 0.48	20.4 $\pm$ 1.0	17.4 $\pm$ 0.2	14.4 $\pm$ 0.2	11.7 $\pm$ 2.3
	Proposed	1.94 $\pm$ 0.48	8.3 $\pm$ 1.0	8.6 $\pm$ 0.7	4.9 $\pm$ 0.9	2.0 $\pm$ 0.4	1.48 $\pm$ 0.42	8.5 $\pm$ 1.9	8.7 $\pm$ 0.9	5.7 $\pm$ 2.1	2.5 $\pm$ 1.8

Table 2: Performance (mean and standard deviation) for the transformation of  $f_0$  and the formant frequencies ( $f_1$ ,  $f_2$  and  $f_3$ ) on the English vowel and TIMIT datasets.

Dataset	NISQA ( $\uparrow$ )	$\delta f_0$ (% , $\downarrow$ )	$\delta f_1$ (% , $\downarrow$ )	$\delta f_2$ (% , $\downarrow$ )	$\delta f_3$ (% , $\downarrow$ )
WSJ	2.08 $\pm$ 0.48	0.8 $\pm$ 0.2	7.2 $\pm$ 1.3	3.6 $\pm$ 1.2	3.8 $\pm$ 0.3
SIWIS	1.93 $\pm$ 0.43	1.2 $\pm$ 0.5	10.0 $\pm$ 4.2	8.3 $\pm$ 1.1	14.0 $\pm$ 0.2
TESS	1.98 $\pm$ 0.50	2.7 $\pm$ 2.3	9.3 $\pm$ 3.5	9.0 $\pm$ 0.8	7.0 $\pm$ 0.2
LJspeech	1.96 $\pm$ 0.40	1.2 $\pm$ 0.6	9.3 $\pm$ 1.2	5.6 $\pm$ 0.6	4.6 $\pm$ 0.1

Table 3: Performance (mean and standard deviation) of  $f_0$  transformation with the proposed method, on the English vowels test dataset, using different training datasets for the unsupervised VAE model.

advance on the understanding of deep generative modeling of speech signals and to compare honestly with highly-specialized traditional systems. TD-PSOLA and WORLD exploit signal models specifically designed for the task at hand, which for instance prevents them to be used for modifying formant frequencies. In contrast, the proposed method is fully based on learning and the same methodology applies for modifying  $f_0$  or the formant frequencies.

### 3.2.3. Robustness with respect to the VAE training dataset

Finally, in this Section we investigate the robustness of the proposed method with respect to different datasets used to train the VAE model. Table 3 presents the results for the modification of  $f_0$  only, applied to the English vowels dataset. We considered three training datasets in addition to the WSJ0 dataset that was used in the previous experiments: (i) the SIWIS French speech synthesis dataset (Honnet et al., 2017), which contains more than ten hours of French speech recordings; (ii) the Toronto emotional speech (TESS) dataset (Dupuis & Pichora-Fuller, 2010), which contains 2800 utterances spoken by two actresses using different emotions (anger, disgust, fear, happiness, pleasant surprise, sadness, and neutral); the LJspeech dataset (Ito & Johnson, 2017), which contains 13,100 short audio clips of a single speaker reading passages from 7 non-fiction books. The artificially-generated speech dataset used for learning the latent subspaces and the regression models along with the test dataset of English vowels remain the same. It can be seen in Table 3 that the performance remains quite stable with different VAE training datasets. WSJ0 is the largest dataset and therefore obtains the best performance. Interestingly, the results obtained with the SIWIS dataset of French speech signals remain satisfactory, even if there is a mismatch between the training (French) and testing (English) datasets.

## 4. Conclusion

The source-filter model of speech production is a fundamental concept in speech processing. In this work, using only a few seconds of artificially generated labeled speech data, we showed that the fundamental frequency and formant frequencies are encoded in orthogonal latent subspaces of an unsupervised VAE and



we proposed a weakly-supervised method to control these attributes within the learned subspaces. The method generalizes well when applied to natural speech signals. To the best of our knowledge, this is the first approach that, with a single methodology, is able to extract, identify and control the source and filter low-level speech attributes within a VAE latent space. This is an important step towards a better understanding of deep generative modeling of speech signals.

The present study focused on generating and transforming speech spectrograms. By learning the inverse of the piecewise linear mapping (see Figure 1 and Section 2.4), the proposed method could probably be extended to the analysis of speech spectrograms, for estimating  $f_0$  and the formant frequencies given the data representation in the corresponding latent source-filter subspace. Future work also includes improving the quality of the generated speech waveforms, by addressing the phase reconstruction issue or by directly modeling the speech waveform (Caillon & Esling, 2021). It also includes extending the proposed method to dynamical VAEs (Girin et al., 2021), to hierarchical latent spaces (Vahdat & Kautz, 2020), and to audio-visual speech processing. The proposed model could also be applied to pitch-informed speech enhancement. Indeed, several recent weakly-supervised speech enhancement methods consist in estimating the VAE latent representation of a clean speech signal given a noisy speech signal (Bando et al., 2018; Leglaive et al., 2018; Sekiguchi et al., 2018; Leglaive et al., 2019b,a; Pariente et al., 2019; Leglaive et al., 2020; Richter et al., 2020; Carbajal et al., 2021; Fang et al., 2021). Using the proposed conditional deep generative speech model, this estimation could be constrained given the  $f_0$  contour computed with a robust  $f_0$  estimation algorithm such as CREPE (Kim et al., 2018).

## Appendix A. Solution to the latent subspace learning problem

In this Appendix, we show that the solution to the optimization problem (7) is given by the principal eigenvectors of  $\mathbf{S}_\phi(\mathcal{D}_i)$  in Equation (8). Without loss of generality, we formulate the problem for a centered version of the latent data:

$$\mathbf{z} \leftarrow \mathbf{z} - \boldsymbol{\mu}_\phi(\mathcal{D}_i), \quad (\text{A.1})$$

where  $\boldsymbol{\mu}_\phi(\mathcal{D}_i)$  is defined in Equation (6). This centering also affects the inference model originally defined in Equation (3), as follows:

$$q_\phi(\mathbf{z}|\mathbf{x}) = \mathcal{N}(\mathbf{z}; \boldsymbol{\mu}_\phi(\mathbf{x}) - \boldsymbol{\mu}_\phi(\mathcal{D}_i), \text{diag}\{\mathbf{v}_\phi(\mathbf{x})\}). \quad (\text{A.2})$$

Using Equation (5), the fact that  $\mathbf{U}^\top \mathbf{U} = \mathbf{I}$ , and Equation (A.2), the cost function in the optimization problem (7) can be rewritten as follows:

$$\begin{aligned} \mathbb{E}_{q_\phi^{(i)}(\mathbf{z})} \left[ \|\mathbf{z} - \mathbf{U}\mathbf{U}^\top \mathbf{z}\|_2^2 \right] &= \frac{1}{\#\mathcal{D}_i} \sum_{\mathbf{x}_n \in \mathcal{D}_i} \mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x}_n)} \left[ \|\mathbf{z} - \mathbf{U}\mathbf{U}^\top \mathbf{z}\|_2^2 \right] \\ &= \text{tr} \left\{ (\mathbf{I} - \mathbf{U}\mathbf{U}^\top) \frac{1}{\#\mathcal{D}_i} \sum_{\mathbf{x}_n \in \mathcal{D}_i} \mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x}_n)} [\mathbf{z}\mathbf{z}^\top] \right\} \\ &= \text{tr} \{ (\mathbf{I} - \mathbf{U}\mathbf{U}^\top) \mathbf{S}_\phi(\mathcal{D}_i) \}, \end{aligned} \quad (\text{A.3})$$

where  $\mathbf{S}_\phi(\mathcal{D}_i)$  is defined in Equation (8). From this last equality, we see that the optimization problem (7) is equivalent to

$$\max_{\mathbf{U} \in \mathbb{R}^{L \times M_i}} \text{tr} \{ \mathbf{U}^\top \mathbf{S}_\phi(\mathcal{D}_i) \mathbf{U} \}, \quad \text{s.t. } \mathbf{U}^\top \mathbf{U} = \mathbf{I}. \quad (\text{A.4})$$

Very similarly to PCA (Pearson, 1901), the solution is given by the  $M_i$  dominant eigenvectors of  $\mathbf{S}_\phi(\mathcal{D}_i)$  (i.e., associated to the  $M_i$  largest eigenvalues) (Bishop, 2006, Section 12.1).

## Appendix B. Experimental setup details

*VAE training.* To train the IS-VAE model (Bando et al., 2018; Leglaive et al., 2018; Girin et al., 2019), we use the Wall Street Journal (WSJ0) dataset (Garofolo et al., 1993a), which contains 25 hours of speech

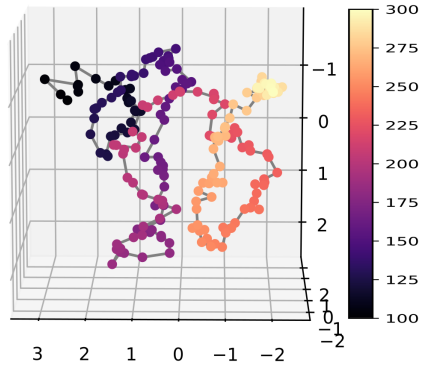
signals sampled at 16 kHz, including 52 female and 49 male speakers. The time-domain speech signals are converted to power spectrograms using the short-time Fourier transform (STFT) with a Hann analysis window of length 64 ms (1,024 samples) and an overlap of 75%. The encoder and decoder networks of the VAE each have three dense layers. Their dimensions are 256, 64 and  $2 \times 16$  for the encoder, and 64, 256 and 513 for the decoder. A hyperbolic tangent (tanh) activation function is used at each layer, except for the output layers of the encoder and decoder where we use the identity function. The VAE input/output dimension is  $D = 513$  (we only keep the non redundant part of the power spectrum at a given time frame) and the latent vector dimension is set to  $L = 16$ . We train the model using the Adam optimizer (Kingma & Ba, 2015) with a learning rate equal to 0.001.

*Artificially generated speech data.* For a given factor of variation, the corresponding latent subspace is learned (see Section 2.2) using trajectories of speech power spectra generated with Soundgen (Anikin, 2019), all other factors being arbitrarily fixed. For  $f_0$ , the trajectory contains 226 points (which corresponds to 3.6 seconds of speech) evenly spaced in the range [85, 310] Hz,  $f_1$ ,  $f_2$  and  $f_3$  being fixed to 600 Hz, 1500 Hz, and 3200 Hz, respectively. For  $f_1$ , the trajectory contains 401 points (which corresponds to 6.4 seconds of speech) evenly spaced in the range [200, 1000] Hz,  $f_0$ ,  $f_2$  and  $f_3$  being fixed to 140 Hz, 1600 Hz, and 3200 Hz, respectively. For  $f_2$ , the trajectory contains 401 points evenly spaced in the range [800, 2800] Hz,  $f_0$ ,  $f_1$  and  $f_3$  being fixed to 140 Hz, 500 Hz, and 3200 Hz, respectively. For  $f_3$ , the trajectory contains 241 points (which corresponds to 3.9 seconds of speech) evenly spaced in the range [2000, 3200] Hz,  $f_0$ ,  $f_1$  and  $f_2$  are fixed to 140 Hz, 500 Hz, and 1200 Hz, respectively. The amplitude and bandwidth of the formants are arbitrarily fixed. The regression models used to control the speech factors of variation in the latent space (see Section 2.4) are learned on the same trajectories, but using the labels that correspond to the input control parameters of Soundgen.

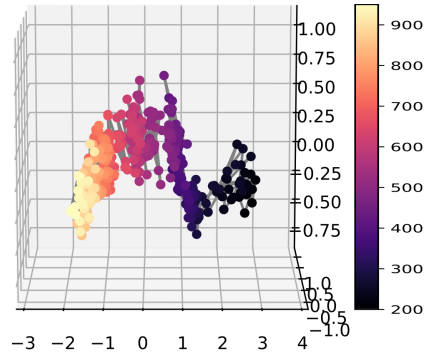
### Appendix C. Visualization of the learned latent subspaces

For  $i = 0, 1, 2$  and 3, Figures C.4a, C.4b, C.4c and C.4d are respectively obtained by projecting the latent mean vectors  $\boldsymbol{\mu}_\phi(\mathbf{x}) \in \mathbb{R}^L$ , for all data vectors  $\mathbf{x} \in \mathcal{D}_i$ , within the latent subspace characterized by  $\mathbf{U}_i \in \mathbb{R}^{L \times M_i}$  (i.e., we perform dimensionality reduction). In the previously reported experiments, the latent subspace dimension  $M_i$  of each factor of variation was chosen such that 80% of the data variance was retained in the latent space. It resulted in  $M_0 = 4$ ,  $M_1 = 1$  and  $M_2 = M_3 = 3$ . In this section, for visualization purposes, we set  $M_i = 3$  for all  $i \in \{0, 1, 2, 3\}$ . However, we can see that the  $f_1$  trajectory (Figure C.4b) is mainly concentrated along a single axis. Regarding  $f_0$  (Figure C.4a), setting  $M_0 = 3$  retained 78% of the variance of  $\mathcal{D}_0$  in the latent space. From these figures, we see that two data vectors  $\mathbf{x}$  and  $\mathbf{x}'$  corresponding to two close values of a given factor have projections of  $\boldsymbol{\mu}_\phi(\mathbf{x})$  and  $\boldsymbol{\mu}_\phi(\mathbf{x}')$  that are also close in the learned latent subspaces. This can be seen from the color bars which indicate the values of the factors of variation. The learned representation thus preserves the notion of proximity in terms of  $f_0$  and formant frequencies.

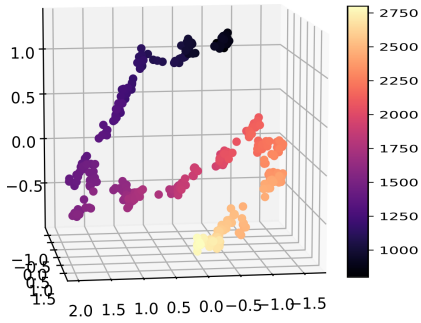
In Figure C.4e, we project three different datasets  $\mathcal{D}_1$ , defined for three different values of  $f_2$ . Similarly, in Figure C.4f we show the trajectories associated with the projection of three datasets  $\mathcal{D}_2$ , defined for three different values of  $f_1$ . We notice that as expected, the trajectories are almost identical and only differ by a translation.



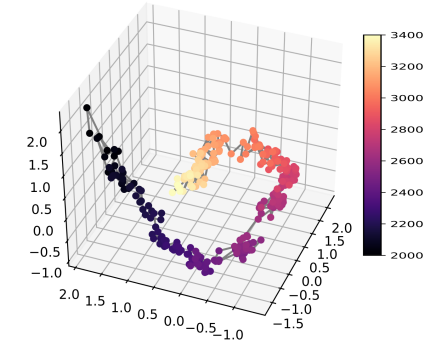
(a)  $f_0$  trajectory corresponding to  $\mathcal{D}_0$ .



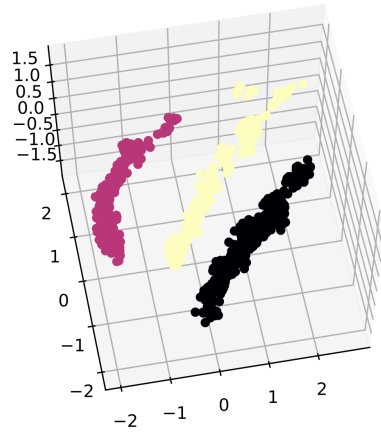
(b)  $f_1$  trajectory corresponding to  $\mathcal{D}_1$ .



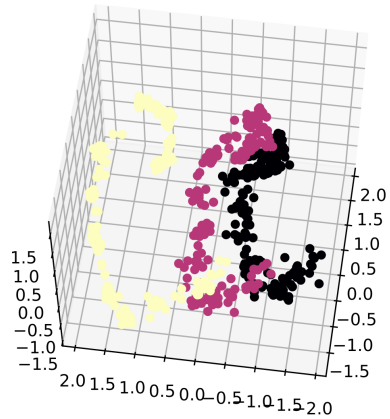
(c)  $f_2$  trajectory corresponding to  $\mathcal{D}_2$ .



(d)  $f_3$  trajectory corresponding to  $\mathcal{D}_3$ .



(e) Three trajectories for  $f_1$ , associated with different values of  $f_2$ .



(f) Three trajectories for  $f_2$ , associated with different values of  $f_1$ .

Figure C.4: Visualization of trajectories in the learned latent subspaces.

- Akuzawa, K., Iwasawa, Y., & Matsuo, Y. (2018). Expressive speech synthesis via modeling expressions with variational autoencoder. In *Interspeech* (pp. 3067–3071).
- Anikin, A. (2019). Soundgen: An open-source tool for synthesizing nonverbal vocalizations. *Behavior Research Methods*, *51*, 778–792.
- Bando, Y., Mimura, M., Itoyama, K., Yoshii, K., & Kawahara, T. (2018). Statistical speech enhancement based on probabilistic integration of variational autoencoder and non-negative matrix factorization. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 716–720).
- Banno, H., Hata, H., Morise, M., Takahashi, T., Irino, T., & Kawahara, H. (2007). Implementation of realtime straight speech manipulation system: Report on its first implementation. *Acoustical Science and Technology*, *28*, 140–146.
- Bengio, Y., Courville, A., & Vincent, P. (2013). Representation learning: A review and new perspectives. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, *35*, 1798–1828.
- Bie, X., Leglaive, S., Alameda-Pineda, X., & Girin, L. (2021). Unsupervised speech enhancement using dynamical variational auto-encoders. *arXiv preprint arXiv:2106.12271*, .
- Bishop, C. M. (2006). *Pattern recognition and machine learning*. Information science and statistics. Springer.
- Blaauw, M., & Bonada, J. (2016). Modeling and transforming speech using variational autoencoders. In *Interspeech* (pp. 1770–1774).
- Boersma, P., & Weenink, D. (2021). Praat: doing phonetics by computer [Computer program]. Version 6.1.38, retrieved 2 January 2021 <http://www.praat.org/>.
- Bora, A., Jalal, A., Price, E., & Dimakis, A. G. (2017). Compressed sensing using generative models. In *International Conference on Machine Learning (ICML)* (pp. 537–546).
- Caillon, A., & Esling, P. (2021). Rave: A variational autoencoder for fast and high-quality neural audio synthesis. *arXiv preprint arXiv:2111.05011*, .
- Carbajal, G., Richter, J., & Gerkmann, T. (2021). Guided variational autoencoder for speech enhancement with a supervised classifier. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 681–685).
- Chen, R. T. Q., Li, X., Grosse, R., & Duvenaud, D. (2018). Isolating sources of disentanglement in variational autoencoders. In *Advances in Neural Information Processing Systems (NeurIPS)* (pp. 2610–2620).
- Chen, X., Duan, Y., Houthoofd, R., Schulman, J., Sutskever, I., & Abbeel, P. (2016). Infogan: Interpretable representation learning by information maximizing generative adversarial nets. In *Advances in Neural Information Processing Systems (NeurIPS)* (pp. 2172–2180).
- Choi, H.-S., Lee, J., Kim, W., Lee, J. H., Heo, H., & Lee, K. (2021). Neural analysis and synthesis: Reconstructing speech from self-supervised representations. In *Advances in Neural Information Processing Systems (NeurIPS)*.
- Dai, B., & Wipf, D. (2018). Diagnosing and enhancing VAE models. In *International Conference on Learning Representations (ICLR)*.
- Dupuis, K., & Pichora-Fuller, M. K. (2010). Toronto emotional speech set (TESS). University of Toronto, Psychology Department.
- Fang, H., Carbajal, G., Wermter, S., & Gerkmann, T. (2021). Variational autoencoder for speech enhancement with a noise-aware encoder. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 676–680).
- Fant, G. (1970). *Acoustic theory of speech production*. 2. Walter de Gruyter.
- Flanagan, J. L., & Golden, R. M. (1966). Phase vocoder. *Bell System Technical Journal*, *45*, 1493–1509.
- Garofolo, J. S., Graff, D., Paul, D., & Pallett, D. (1993a). CSR-I (WSJ0) Sennheiser LDC93S6B. <https://catalog.ldc.upenn.edu/LDC93S6B>. Philadelphia: Linguistic Data Consortium.
- Garofolo, J. S., Lamel, L. F., Fisher, W. M., Fiscus, J. G., Pallett, D. S., Dahlgren, N. L., & Zue, V. (1993b). TIMIT acoustic phonetic continuous speech corpus. In *Linguistic data consortium*.
- George, E. B., & Smith, M. J. (1997). Speech analysis/synthesis and modification using an analysis-by-synthesis/overlap-add sinusoidal model. *IEEE Transactions on Speech and Audio Processing*, *5*, 389–406.
- Girin, L., Leglaive, S., Bie, X., Diard, J., Hueber, T., & Alameda-Pineda, X. (2021). Dynamical variational autoencoders: A comprehensive review. *Foundations and Trends in Machine Learning*, *15*, 1–175.
- Girin, L., Roche, F., Hueber, T., & Leglaive, S. (2019). Notes on the use of variational autoencoders for speech and audio spectrogram modeling. In *International Conference on Digital Audio Effects (DAFx)* (pp. 1–8).
- Goetschalckx, L., Andonian, A., Oliva, A., & Isola, P. (2019). GANalyze: Toward visual definitions of cognitive image properties. In *IEEE/CVF International Conference on Computer Vision* (pp. 5744–5753).
- Goodfellow, I., Pouget-Abadie, J., Mirza, M., Xu, B., Warde-Farley, D., Ozair, S., Courville, A., & Bengio, Y. (2014). Generative adversarial nets. In *Advances in Neural Information Processing Systems (NeurIPS)* (pp. 2672–2680).
- Härkönen, E., Hertzmann, A., Lehtinen, J., & Paris, S. (2020). GANSpace: Discovering interpretable GAN controls. In *Advances in Neural Information Processing Systems (NeurIPS)* (pp. 9841–9850).
- Higgins, I., Amos, D., Pfau, D., Racaniere, S., Matthey, L., Rezende, D. J., & Lerchner, A. (2018). Towards a definition of disentangled representations. *arXiv preprint arXiv:1812.02230*, .
- Higgins, I., Matthey, L., Pal, A., Burgess, C., Glorot, X., Botvinick, M., Mohamed, S., & Lerchner, A. (2017). Beta-VAE: Learning basic visual concepts with a constrained variational framework. In *International Conference on Learning Representations (ICLR)*.
- Hillenbrand, J., Getty, L. A., Clark, M. J., & Wheeler, K. (1995). Acoustic characteristics of American English vowels. *The Journal of the Acoustical Society of America*, *97*, 3099–3111.
- Honnet, P.-E., Lazaridis, A., Garner, P. N., & Yamagishi, J. (2017). *The SIWIS French speech synthesis database - Design and recording of a high quality French database for speech synthesis*. Technical Report Idiap.
- Hotelling, H. (1957). The relations of the newer multivariate statistical methods to factor analysis. *British Journal of Statistical*

- Psychology*, 10, 69–79.
- Hsu, C.-C., Hwang, H.-T., Wu, Y.-C., Tsao, Y., & Wang, H.-M. (2016). Voice conversion from non-parallel corpora using variational auto-encoder. In *Asia-Pacific Signal and Information Processing Association Annual Summit and Conference (APSIPA)* (pp. 1–6).
- Hsu, W.-N., Zhang, Y., & Glass, J. (2017a). Learning latent representations for speech generation and transformation. In *Interspeech* (pp. 1273–1277).
- Hsu, W.-N., Zhang, Y., & Glass, J. (2017b). Unsupervised learning of disentangled and interpretable representations from sequential data. In *Advances in Neural Information Processing Systems (NeurIPS)* (pp. 1878–1889).
- Ito, K., & Johnson, L. (2017). The LJ speech dataset. <https://keithito.com/LJ-Speech-Dataset/>.
- Jadoul, Y., Thompson, B., & de Boer, B. (2018). Introducing Parselmouth: A Python interface to Praat. *Journal of Phonetics*, 71, 1–15.
- Jahani, A., Chai, L., & Isola, P. (2019). On the “steerability” of generative adversarial networks. In *International Conference on Learning Representations (ICLR)*.
- Jayaram, V., & Thickstun, J. (2020). Source separation with deep generative priors. In *International Conference on Machine Learning (ICML)* (pp. 4724–4735).
- Jekel, C. F., & Venter, G. (2019). PWLF: a Python library for fitting 1D continuous piecewise linear functions. URL: [https://github.com/cjekel/piecewise\\_linear\\_fit\\_py/raw/master/paper/pwlf\\_Jekel\\_Venter\\_v2.pdf](https://github.com/cjekel/piecewise_linear_fit_py/raw/master/paper/pwlf_Jekel_Venter_v2.pdf).
- Juvela, L., Bollepalli, B., Tsiaras, V., & Alku, P. (2019). GlotNeta raw waveform model for the glottal excitation in statistical parametric speech synthesis. *IEEE/ACM Transactions on Audio, Speech, and Language Processing*, 27, 1019–1030.
- Kameoka, H., Li, L., Inoue, S., & Makino, S. (2019). Supervised determined source separation with multichannel variational autoencoder. *Neural computation*, 31, 1891–1914.
- Kawahara, H. (2006). STRAIGHT, exploitation of the other aspect of VOCODER: Perceptually isomorphic decomposition of speech sounds. *Acoustical Science and Technology*, 27, 349–353.
- Kendall, M. (1957). *A course in multivariate analysis*. London: Charles Griffin.
- Kim, H., & Mnih, A. (2018). Disentangling by factorising. In *International Conference on Machine Learning (ICML)* (pp. 2649–2658).
- Kim, J. W., Salamon, J., Li, P., & Bello, J. P. (2018). Crepe: A convolutional representation for pitch estimation. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 161–165).
- Kingma, D. P., & Ba, J. (2015). Adam: A method for stochastic optimization. In *International Conference on Learning Representations (ICLR)*.
- Kingma, D. P., & Welling, M. (2014). Auto-encoding variational Bayes. In *International Conference on Learning Representations (ICLR)*.
- Laroche, J. (2002). Time and pitch scale modification of audio signals. In *Applications of digital signal processing to audio and acoustics* (pp. 279–309). Springer.
- Laroche, J., & Dolson, M. (1999). Improved phase vocoder time-scale modification of audio. *IEEE Transactions on Speech and Audio processing*, 7, 323–332.
- Laroche, J., Stylianou, Y., & Moulines, E. (1993). Hns: Speech modification based on a harmonic+ noise model. In *IEEE International Conference on Acoustics, Speech, and Signal Processing* (pp. 550–553). Minneapolis, MN volume 2.
- Lee, J., Choi, H.-S., Jeon, C.-B., Koo, J., & Lee, K. (2019). Adversarially trained end-to-end Korean singing voice synthesis system. In *Interspeech* (pp. 2588–2592).
- Leglaive, S., Alameda-Pineda, X., Girin, L., & Horaud, R. (2020). A recurrent variational autoencoder for speech enhancement. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 371–375).
- Leglaive, S., Şimşekli, U., Liutkus, A., Girin, L., & Horaud, R. (2019a). Speech enhancement with variational autoencoders and alpha-stable distributions. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 541–545).
- Leglaive, S., Girin, L., & Horaud, R. (2018). A variance modeling framework based on variational autoencoders for speech enhancement. In *IEEE International Workshop on Machine Learning for Signal Processing (MLSP)* (pp. 1–6).
- Leglaive, S., Girin, L., & Horaud, R. (2019b). Semi-supervised multichannel speech enhancement with variational autoencoders and non-negative matrix factorization. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 101–105).
- Locatello, F., Bauer, S., Lucic, M., Raetsch, G., Gelly, S., Schölkopf, B., & Bachem, O. (2019). Challenging common assumptions in the unsupervised learning of disentangled representations. In *International Conference on Machine Learning (ICML)* (pp. 4114–4124).
- Locatello, F., Bauer, S., Lucic, M., Rättsch, G., Gelly, S., Schölkopf, B., & Bachem, O. (2020). A sober look at the unsupervised learning of disentangled representations and their evaluation. *Journal of Machine Learning Research*, 21, 1–62.
- MacDonald, E. N., Purcell, D. W., & Munhall, K. G. (2011). Probing the independence of formant control using altered auditory feedback. *The Journal of the Acoustical Society of America*, 129, 955–965.
- Makhoul, J. (1975). Linear prediction: A tutorial review. *Proceedings of the IEEE*, 63, 561–580.
- Makhzani, A., Shlens, J., Jaitly, N., Goodfellow, I., & Frey, B. (2016). Adversarial autoencoders. In *International Conference on Learning Representations (ICLR) Workshop*.
- Markel, J. D., & Gray, A. J. (1976). *Linear prediction of speech*. New York: Springer-Verlag.
- McAulay, R., & Quatieri, T. (1986). Speech analysis/synthesis based on a sinusoidal representation. *IEEE Transactions on Acoustics, Speech, and Signal Processing*, 34, 744–754.
- Mittag, G., & Möller, S. (2020). Deep learning based assessment of synthetic speech naturalness. In *Interspeech* (pp. 1748–1752).
- Morise, M., Yokomori, F., & Ozawa, K. (2016). World: a vocoder-based high-quality speech synthesis system for real-time

- applications. *IEICE Transactions on Information and Systems*, 99, 1877–1884.
- Morrison, M., Jin, Z., Bryan, N. J., Caceres, J.-P., & Pardo, B. (2021). Neural pitch-shifting and time-stretching with controllable lpcnet. *arXiv preprint arXiv:2110.02360*, .
- Moulines, E., & Charpentier, F. (1990). Pitch-synchronous waveform processing techniques for text-to-speech synthesis using diphones. *Speech Communication*, 9, 453–467.
- Pariante, M., Deleforge, A., & Vincent, E. (2019). A statistically principled and computationally efficient approach to speech enhancement using variational autoencoders. In *Interspeech* (pp. 3158–3162).
- Pearson, K. (1901). On lines and planes of closest fit to systems of points in space. *The London, Edinburgh, and Dublin Philosophical Magazine and Journal of Science*, 2, 559–572.
- Plummerault, A., Borgne, H. L., & Hudelot, C. (2020). Controlling generative models with continuous factors of variations. In *International Conference on Learning Representations (ICLR)*.
- Prenger, R., Valle, R., & Catanzaro, B. (2019). Waveglow: A flow-based generative network for speech synthesis. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 3617–3621).
- Qian, K., Zhang, Y., Chang, S., Hasegawa-Johnson, M., & Cox, D. (2020). Unsupervised speech decomposition via triple information bottleneck. In *International Conference on Machine Learning (ICML)* (pp. 7836–7846).
- Rezende, D. J., Mohamed, S., & Wierstra, D. (2014). Stochastic backpropagation and approximate inference in deep generative models. *International Conference on Machine Learning (ICML)*, (pp. 1278–1286).
- Richter, J., Carbajal, G., & Gerkmann, T. (2020). Speech enhancement with stochastic temporal convolutional networks. In *Interspeech* (pp. 4516–4520).
- Sekiguchi, K., Bando, Y., Yoshii, K., & Kawahara, T. (2018). Bayesian multichannel speech enhancement with a deep speech prior. In *Asia-Pacific Signal and Information Processing Association Annual Summit and Conference (APSIPA)* (pp. 1233–1239).
- Serra, X., & Smith, J. (1990). Spectral modeling synthesis: A sound analysis/synthesis system based on a deterministic plus stochastic decomposition. *Computer Music Journal*, 14, 12–24.
- Vahdat, A., & Kautz, J. (2020). NVAE: A deep hierarchical variational autoencoder. In *Advances in Neural Information Processing Systems (NeurIPS)* (pp. 19667–19679).
- Valin, J.-M., & Skoglund, J. (2019). LPCNet: Improving neural speech synthesis through linear prediction. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)* (pp. 5891–5895).
- Wang, X., Takaki, S., & Yamagishi, J. (2019). Neural source-filter waveform models for statistical parametric speech synthesis. *IEEE/ACM Transactions on Audio, Speech, and Language Processing*, 28, 402–415.
- Webber, J. J., Perrotin, O., & King, S. (2020). Hider-finder-combiner: An adversarial architecture for general speech signal modification. In *Interspeech* (pp. 3206–3210).