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Near-surface dynamics of a gas bubble collapsing above a crevice

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The impact of a collapsing gas bubble above rigid, notched walls is considered. Such surface crevices and imperfections often function as bubble nucleation sites, and thus have a direct relation to cavitation-induced erosion and damage structures. A generic configuration is investigated numerically using a second-order-accurate compressible multicomponent flow solver in a two-dimensional axisymmetric coordinate system. Results show that the crevice geometry has a significant effect on the collapse dynamics, jet formation, subsequent wave dynamics, and interactions. The wall-pressure distribution associated with erosion potential is a direct consequence of development and intensity of these flow phenomena.

Key words: bubble dynamics, cavitation, compressible flows

1. Introduction

Cavitation damage can result from the collapse of vapour bubbles formed in low pressure regions of a flow, typically at gas nuclei that exist in the free-stream or in crevices on surfaces. When collapse occurs near a surface, the emitted shock waves (Hickling & Plesset 1964; Lord Rayleigh 1917) impinge on nearby surfaces (Benjamin *et al.* 1966; Plesset & Chapman 1971) where, depending on the surface geometry and material properties, they can cause erosion or ablation. The importance of surface geometry, in conjunction with the fact that these low-pressure regions occur more frequently at rough surfaces, motivates the investigation of bubble collapse behaviour near solid walls.

Several studies have analysed bubbles collapsing near smooth walls. Early studies identified an asymmetric behaviour associated with bubble-wall interaction (Benjamin *et al.* 1966; Plesset & Chapman 1971) that leads to an impinging jet. Later, experimental studies have analysed the collapse behaviour (Lindau & Lauterborn 2003), jet formation and velocities (Tomita & Shima 1986), and wall erosion potential (Philipp & Lauterborn 1998) in greater detail. Numerical-simulation-based studies have investigated the collapse dynamics of bubbles attached to (Lauer *et al.* 2012) and near (Johnsen & Colonius 2009) smooth walls. However, such configurations represent the wall pressure and collapse dynamics only if the length scale of the wall roughness is much smaller than the nominal bubble size. When this condition is not satisfied, the bubble collapse, and thus its effect

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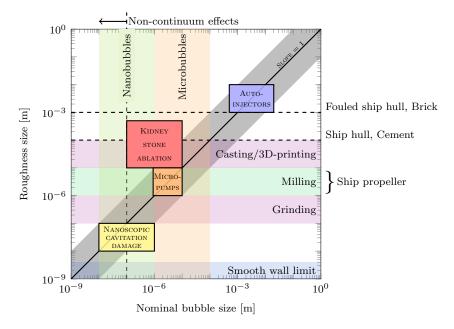


FIGURE 1. Nominal bubble size and surface roughness of common engineering materials, finishing processes, and applications. Roughness sizes are RMS values.

on near-wall erosion, can change qualitatively (Li *et al.* 2018; Tomita *et al.* 2002; Zhang *et al.* 2018). In figure 1 physical limits and regions of relevant manufacturing processes and engineering applications are shown for a range of roughness sizes and bubble length scales. The associated broad list of applications, including urinary stones ablation (Pishchalnikov *et al.* 2003), surface cleaning (Ohl *et al.* 2006; Reuter *et al.* 2017), cavitation in micropumps (Dijkink & Ohl 2008) and pressurized auto-injectors (Veilleux *et al.* 2018) and due to nano-bubbles (Borkent *et al.* 2009) motivates the study of bubble collapse dynamics in this regime.

Our goal is to determine how a surface crevice modifies the collapse of a near-wall bubble, and to assess thus the associated modification of wall pressure, jet and shock formation, and wave interactions, which are of principal importance when considering erosion and damage potential (Brennen 1995; Pöhl *et al.* 2015). For this purpose, the collapse of a spherical gas bubble near or attached to a wall with a cylindrical notch is analysed. Experimental techniques preclude detailed visualization of such small spaceand time-scale dynamics, particularly with respect to the rapid liquid jet formation and the high pressures waves emitted after collapse. Therefore, we use numerical simulations to characterize qualitative and quantitative differences of collapse behaviour associated with the surface geometry.

In section 2.2, we describe the physical model and numerical method. The specific configurations considered are presented in section 3, and include variations in notch size and bubble-wall stand-off distance. The variation in notch size serves as a representation of the varying degrees of surface roughness present in engineering applications (see figure 1), whereas the stand-off distance has a significant impact on the collapse dynamics and wall-pressure for smooth-wall cases (Lauer *et al.* 2012; Philipp & Lauterborn 1998; Tomita & Shima 1986). The collapse behaviour of the bubble is analysed for such configurations in section 4, followed by a consideration of the collapse and jet-impact times, velocities, and wall-pressures. Section 5 concludes the paper.

2. Physical model and numerical methods

2.1. Governing equations

The collapse of a gas bubble in liquid is modelled using a 6-equation multi-component flow model (Saurel *et al.* 2009) that conserves mass, momentum, and total energy. For the driving pressures and gas bubbles we assume that the effects of viscosity and surface tension are insignificant with respect to inertial effects, and so they are not included in our model. The governing equations are

$$\begin{aligned} \frac{\partial \alpha_l}{\partial t} + \mathbf{u} \cdot \nabla \alpha_l &= \mu (p_l - p_g), \\ \frac{\partial \alpha_l \rho_l}{\partial t} + \nabla \cdot (\alpha_l \rho_l \mathbf{u}) &= 0, \\ \frac{\partial \alpha_g \rho_g}{\partial t} + \nabla \cdot (\alpha_g \rho_g \mathbf{u}) &= 0, \\ \frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u} \mathbf{u} + p \mathbf{I}) &= \mathbf{0}, \end{aligned}$$
(2.1)
$$\begin{aligned} \frac{\partial \alpha_l \rho_l e_l}{\partial t} + \nabla \cdot (\alpha_l \rho_l e_l \mathbf{u}) + \alpha_l p_l \nabla \cdot \mathbf{u} &= -\mu p_I (p_l - p_g), \\ \frac{\partial \alpha_g \rho_l e_g}{\partial t} &+ \nabla \cdot (\alpha_g \rho_g e_g \mathbf{u}) + \alpha_g p_g \nabla \cdot \mathbf{u} &= -\mu p_I (p_l - p_g), \end{aligned}$$

where α_k , ρ_k , p_k and e_k are the volume fraction, density, pressure and internal energy of phase k, respectively, ρ , p, and **u**, are the mixture properties, μ is the relaxation coefficient, and p_I is the interfacial pressure (Saurel *et al.* 2009). The mixture total energy is

$$E = e + \frac{1}{2} \|\mathbf{u}\|^2, \tag{2.2}$$

where e is the mixture specific internal energy

$$e = \sum_{k=1}^{2} Y_k e_k \left(\rho_k, p_k \right).$$
 (2.3)

In (2.3), e_k is defined via an equation of state and Y_k are the mass fractions

$$Y_k = \frac{\alpha_k \rho_k}{\rho}.$$
(2.4)

The gas g is modelled by the ideal-gas equation of state

$$p_g = (\gamma_g - 1)\rho_g e_g, \tag{2.5}$$

and the liquid l is modelled by the stiffened-gas equation of state

$$p_l = (\gamma_l - 1)\rho_l e_l - \gamma_l \pi_{\infty}, \qquad (2.6)$$

where $\gamma_g = 1.4$, $\gamma_l = 2.35$, and $\pi_{\infty} = 10^9$ Pa are model parameters (Le Métayer *et al.* 2005).

2.2. Numerical method

A second-order-accurate MUSCL scheme is used to solve (2.1). It is implemented in ECOGEN (Schmidmayer *et al.* 2019*a*,*b*), which has been verified for several gas bubble dynamics problems, including free-space (Schmidmayer *et al.* 2020) and wallattached (Pishchalnikov *et al.* 2019) bubble collapses. The approach uses piece-wise linear

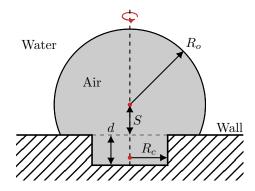


FIGURE 2. Schematic of the problem set-up.

reconstruction (Toro 1997) of the primitive variables to suppress spurious oscillations at material interfaces (Coralic & Colonius 2014). The monotonized central (MC) (Van Leer 1977) slope limiter and THINC interface-sharpening technique (Shyue & Xiao 2014) are used to minimize interface diffusion. The associated Riemann problem is computed using the HLLC approximate solver (Saurel *et al.* 2009; Toro 1997). An explicit two-step time integrator is used (Schmidmayer *et al.* 2019b).

The pressure-non-equilibrium model (2.1) also requires pressure-relaxation to recover a unique equilibrium pressure. This is achieved by an infinite-relaxation procedure (Saurel *et al.* 2009). At each time step it solves the non-relaxed, hyperbolic equations ($\mu \rightarrow 0$), then relaxes the non-equilibrium pressures for $\mu \rightarrow +\infty$. The relaxation procedure is combined with a re-initialization procedure at each time-step stage, which ensures a unique pressure and the conservation of total energy, and thus convergence to the 5-equation mechanical-equilibrium model (Kapila *et al.* 2001).

3. Problem set-up

Figure 2 shows the flow configuration considered. The initial bubble is spherical with radius R_0 and stand-off distance S above a cylindrical crevice of radius R_C and depth $d = 0.25R_0$. We define the stand-off distance S as the distance from the wall to bubble-centre for $R_C/R_0 \leq 0.5$ and as the distance from the crevice-bottom to bubble-centre for $R_C/R_0 > 0.5$. This definition ensures consistency for both limiting cases $R_C/R_0 \to 0$ and $R_C/R_0 \to \infty$.

We consider a $R_0 = 400 \,\mu\text{m}$ bubble filled with non-condensable gas of initial pressure $p_B = 3000 \,\text{Pa}$ and density $\rho_g = 0.035\,65 \,\text{kg}\,\text{m}^{-3}$. Bubbles commonly used in relevant applications predominately consist of non-condensable gas. Furthermore, the collapse dynamics are also only weakly sensitive to the internal bubble pressure when the driving pressure differences are large (Pishchalnikov *et al.* 2019).

The bubble is surrounded by water with a density of $\rho_l = 1002.7 \,\mathrm{kg}\,\mathrm{m}^{-3}$ and varying pressure

$$p(\hat{r}, t=0) = p_{\infty} + \frac{R_0}{\hat{r}} \left(p_B - p_{\infty} \right) \text{ for } \hat{r} > R_0,$$
 (3.1)

where \hat{r} is the radial coordinate with origin at the bubble centre. This initialization matches the pressure distribution predicted by the Rayleigh equation for the Besant problem (Besant 1859; Brennen 1995). For the configurations considered, it provides a suitable approximation of the realistically evolving pressure field and suppresses the formation of spurious pressure waves due to pressure jumps. We use $p_{\infty} = 10^7$ Pa, which

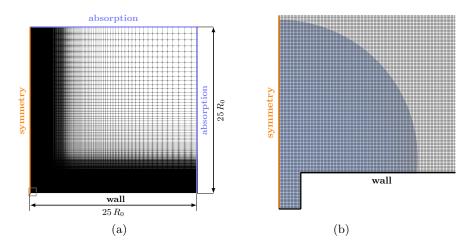


FIGURE 3. (a) 2D axisymmetric grid configuration and boundary conditions for example case small crevice $(R_C/R_0 = 0.15)$ and a stand-off distance of $S/R_0 = 0.35$. (b) Magnification of the near-bubble region with the bubble shaded. Only every fourth grid-line is shown in each coordinate direction.

matches that of previous studies (Beig *et al.* 2018; Lauer *et al.* 2012) and serves as a representation of actual applications involving liquid cavitation, such as high-pressure pumps (Bohner *et al.* 2001).

Figure 3 shows the computational grid. The bubble collapse process is assumed to be axisymmetric with radial coordinate r, and thus a 2D axisymmetric domain of radius and length $25R_0$ is used, matching that of previous studies of smooth-wall collapse (Lauer *et al.* 2012). The grid is equally spaced with 400 finite volumes per R_0 near the bubble (until $\hat{r} = 1.5R_0$) and is progressively stretched farther from the bubble with a stretching factor of 1.01 in each direction. This resolution has been shown to be sufficient for the conditions considered here (Beig *et al.* 2018; Lauer *et al.* 2012; Pöhl *et al.* 2015). Absorbing boundary conditions are used at the outer boundaries to suppress reflecting pressure waves at these locations (Toro 1997). A constant CFL number of 0.4 is used, which corresponds to a time step of $\Delta t \approx 0.15$ ns. The total simulation time is 6 µs, or about $1.5t^*$ where

$$t^* = R_0 \sqrt{\frac{\rho_l}{\Delta p}} \tag{3.2}$$

is an estimate of the collapse time of a bubble collapse near a solid wall (Plesset & Chapman 1971), where $\Delta p \equiv p_{\infty} - p_B$ is the driving pressure difference. The wall has a retarding effect on the collapse and thus t^* is longer than the Rayleigh collapse time for spherical collapses ($t_{\text{Rayleigh}} = 0.915 t^*$). Velocity and pressure are normalized as

$$u^* = \sqrt{\frac{\Delta p}{\rho_l}}, \quad \text{and} \quad p^* = c_l \sqrt{\rho_l \Delta p},$$
(3.3)

where c_l is the liquid speed of sound.

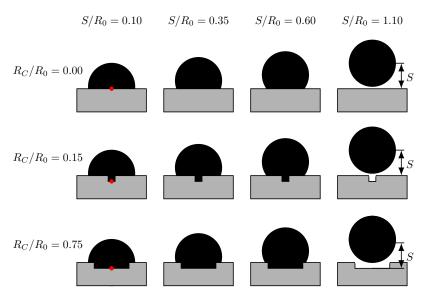


FIGURE 4. Overview of the investigated configurations. The red circle shows the r = 0 wall-centred position used to observe the pressure impact. Rows correspond to constant crevice size R_C/R_0 and columns correspond to constant stand-off distance S/R_0 . The stand-off distance S is also shown; its definition is modified to be measured from the bottom of the crevice for the $R_C/R_0 = 0.75$ cases.

4. Results

4.1. Considered configurations

We use stand-off distances $S/R_0 = 0.1, 0.35, 0.6$, and 1.1 (wall-detached). For each stand-off distance we consider a smooth wall $(R_C = 0)$, a small crevice $(R_C/R_0 = 0.15)$ and a large crevice $(R_C/R_0 = 0.75)$, as shown in figure 4.

We first analyse the collapse behaviour of wall-attached bubbles by increasing crevice size (smooth wall in section 4.2, small crevice in section 4.3 and large crevice in section 4.4), and then consider detached bubbles in section 4.5. In section 4.6, we compare the pressure impact on the wall for all configurations and assess the cavitation erosion potential.

4.2. Smooth-wall-attached bubble collapse $R_C = 0$

Figure 5 visualizes the flow of a collapsing wall-attached bubble using the pressure field p and numerical schlieren Φ (Quirk & Karni 1996) as

$$\Phi = \exp\left(-\frac{k|\nabla\rho|}{\max|\nabla\rho|}\right),\tag{4.1}$$

where k = 400 is used to ensure waves in the liquid are visible (Johnsen 2007; Meng & Colonius 2018). The corresponding pressures at the centre of the wall are shown in figure 6.

For all cases a wall-directed jet is formed during the initial collapse phase. The jet impinges on the wall (row ii) leading to a pressure wave. At subsequent times the remaining toroidal bubble continues to collapse, emitting a pulse that travels radially inward and collides at r = 0.

The collapse of the torus becomes increasingly non-uniform, with a portion near the wall being pinched away from the main torus. Pressure waves emitted near the pinching

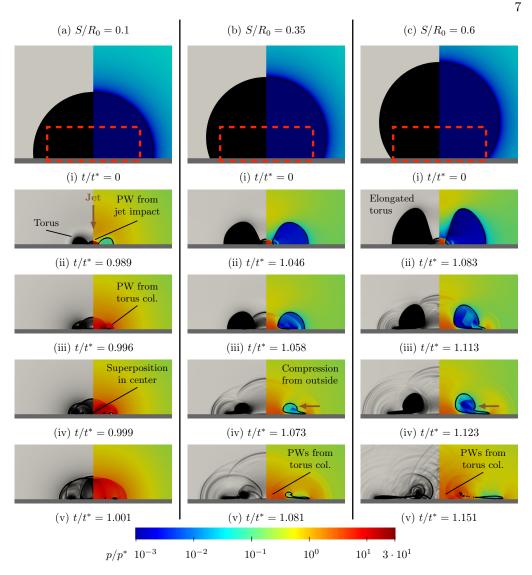


FIGURE 5. Numerical schlieren (left) and log-scale pressure fields (right) of an air bubble collapsing onto a smooth wall of varying stand-off distances S/R_0 (a)–(c) at selected times (i)–(v). Gas volume fraction α_g is shown as a shaded area of decreasing opacity with decreasing α_g (left), while the $\alpha_g = 0.5$ bubble interface is shown as a solid curve (right). (ii)–(v) are magnified to the – – – rectangular region of (i). Selected pressure waves (PW) and collapse dynamics (col.) are also identified.

location are evident, starting in (b,iv) and (c,iii) respectively. In addition, a compression of the torus from the outside pushes its upper part towards the centre (b,iv), (c,iv). During the final collapse phase, two pressure waves propagate inward, focus, and result in two distinct pressure pulses at the wall centre, as visible in figure 6.

The impact of a liquid jet onto the wall generates a water hammer pressure proportional to the jet velocity $p_{\text{jet}} \propto \rho_l c_l u_{\text{jet}}$. The jet-induced pressure peak p_{jet} is clearly visible from the wall-centred pressure signals of figure 6. For $S/R_0 = 0.1$, the peak is about twice as high as for the others. The high jet velocity at this small stand-off distance is a result of the bubble shape being almost hemispherical. A hemispherical bubble attached

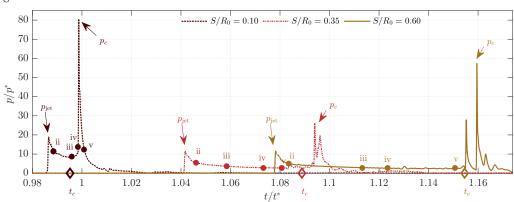


FIGURE 6. Evolution of the wall-centred pressure for the smooth-wall case at varying stand-off distances S/R_0 . The time instances shown in figure 5 are highlighted and labelled with the corresponding row (ii–v). The pressure peaks induced by the jet impact p_{jet} and the collapse p_c are indicated as such. The collapse time t_c is plotted as a diamond on the x-axis.

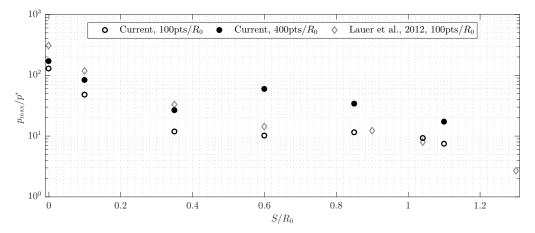


FIGURE 7. Maximum wall pressure for a smooth-wall-attached bubble of varying stand-off distance S/R_0 and grid resolution as labelled. Results from Lauer *et al.* (2012) are also shown for comparison.

to an inviscid wall collapses like a spherical bubble with a uniform and high acceleration of the interface. For $S/R_0 = 0.1$ the initial stages of the collapse resemble those of a collapsing spherical bubble, with the formation of the liquid jet immediately preceding the total collapse and the jet reaching a high velocity. Similar observations were made by Philipp & Lauterborn (1998), who also experimentally recorded the highest jet-induced pressures at small stand-off distances.

In the configurations considered, the total collapse is the collapse of the gas torus. We determine the collapse time t_c by the minimum gas volume. The pressure waves emitted at total collapse result in collapse-induced pressure peaks p_c (see figure 6). Thus, the jet impact on the wall as well as the shock waves emitted during total collapse cause high pressure peaks and potentially material damage. For the rough wall cases, we also observe pressure peaks induced by post-collapse wave dynamics. In section 4.6, we compare these three pressure peaks for all configurations. For the smooth-wall cases, p_c is significantly higher than p_{iet} , which agrees with the findings of Lauer *et al.* (2012).

In figure 7 the maximum wall pressure p_{max} is compared with that of Lauer *et al.* (2012)

for our present resolution $(400 \text{pts}/R_0)$ and $100 \text{pts}/R_0$, which matches their study. The current results follow the same trends, although with lower pressures for the attachedbubble cases $(S < R_0)$. The maximum pressure is known to be sensitive to resolution, although a discrepancy also exists for identical grid resolutions $(100 \text{pts}/R_0)$. Lauer *et al.* (2012) consider condensation, while we model the bubble content as non-condensable gas. The damping of the maximum pressure observed is consistent with previous analysis of bubbles containing non-condensable gas (Pishchalnikov *et al.* 2019; Trummler *et al.* 2018).

4.3. Small crevice $R_C/R_0 = 0.15$

Visualizations of a collapsing $R_C/R_0 = 0.15$ crevice-wall-attached bubble at varying stand-off distances S/R_0 are shown in figure 8 and the corresponding wall pressures are shown in figure 9.

For the smallest stand-off distance case $(S/R_0 = 0.1)$, the initial stages of the collapse match that of the smooth-wall cases, with a jet piercing the bubble and generating a toroidal structure. However, in this case the gas torus is ultimately fully contained in the crevice. As shown in (a,iii), a pressure wave is emitted when the liquid has reached the sharp edge of the crevice and is suddenly stopped there. This wave propagates radially outwards (a,iv) and collides in the centre inducing a small pressure peak at the wallcentre, see $p_{\rm PW1}$ in figure 9. The pressure wave continues to travel towards the other crevice side pushing the gas away from the crevice bottom and pressing it against the opposite side wall (a,v). Between (a,iv) and (a,v) the pressure wave and its reflections induce high pressure fluctuations at the wall centre ($p_{\rm PW2}$). The last time step depicted (a,v) is close to the final collapse, which causes the highest pressure peak.

For the larger stand-off distances $S/R_0 = 0.35$ and 0.6, the jet penetrates the entire bubble and hits the crevice bottom. A gas torus remains on the upper wall and a gas layer covers the side walls. Like in the smooth wall cases, the gas torus outside of the crevice collapses ((b,iv), (c,iv)), emitting intense pressure waves. These waves propagate radially outward, interfere with each other, and are reflected within the crevice. The time steps (b,v) and (c,v) both visualize the complex wave pattern after the total collapse.

Figure 9 shows that the wall-centred pressures associated with the $S/R_0 = 0.35$ and 0.6 cases are qualitatively similar. Both have a pressure peak due to the jet impact, followed by a time-delayed accumulation of pressure peaks during and after the final collapse phase. For $S/R_0 = 0.6$ these pressure peaks are smaller since the intense pressure waves are more concentrated in the area above the crevice (see (c,iv,v)) and thus decay until they reach the crevice bottom.

At all stand-off distances, significant pressure peaks are induced by post-collapse wave dynamics (see p_{post} in figure 9).

4.4. Large crevice $R_C/R_0 = 0.75$

We next consider the large crevice $R_C/R_0 = 0.75$ cases. Recall that S is now measured from the bottom of the crevice wall to the bubble centre, instead of from the top of the crevice wall. Figure 10 visualizes the collapses and the corresponding wall-centred pressures are shown in figure 11.

For the $S/R_0 = 0.1$ case (column a), the fraction of the bubble surface initially exposed to the high-pressure liquid is comparable to that of a bubble with a small negative stand-off distance $(S/R_0 - d/R_0 = 0.1 - 0.25 = -0.15)$. Consequently, the initial collapse phase resembles that of such a configuration. Lauer *et al.* (2012) and Shima & Nakajima (1977) report a collapse behaviour similar to that of a spherical collapse with

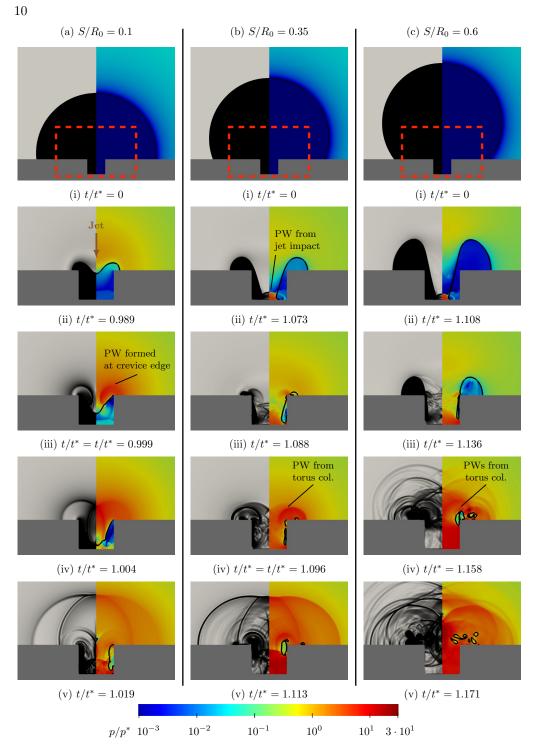


FIGURE 8. Numerical schlieren (left) and pressure fields (right) of an air bubble collapsing onto a wall with a small crevice $R_C/R_0 = 0.15$ at varying stand-off distances S/R_0 (a)–(c) at selected times (i)–(v). (ii)–(v) are magnified to the – – – rectangular region shown in (i). Selected pressure waves (PW) and collapse dynamics (col.) are also identified.

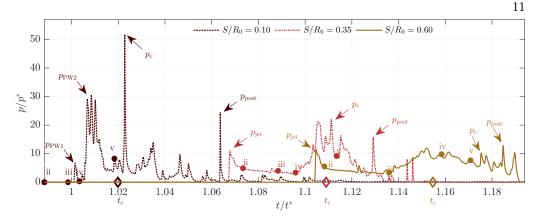


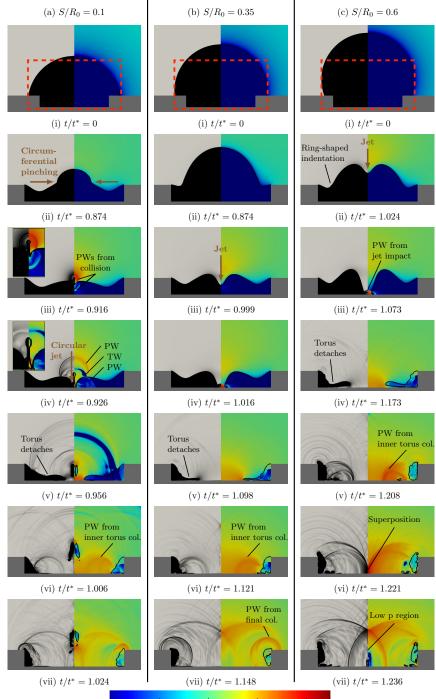
FIGURE 9. Evolution of the wall-pressure at r = 0 for the case $R_C/R_0 = 0.15$ at varying stand-off distances S/R_0 . The time instances shown in figure 8 are highlighted and labelled with the corresponding row (ii–v). The pressure peaks induced by the jet impact p_{jet} , the pressure-wave p_{PW} , the collapse p_c and post-collapse wave dynamics p_{post} are indicated as such. The collapse time t_c is plotted as a diamond on the x-axis.

an additional circumferential pinching at the position of maximum extension, resulting in a mushroom-shape. Here, (a,ii) shows the compressed upper part of the bubble and also a circumferential pinching. Additionally, a ring-shaped indentation of the bubble can be observed.

The circumferential pinching meets at the r = 0 axis of symmetry, generating a pressure wave (a,iii), which propagates radially outward in the liquid and the gas. When the pressure wave in the gas reaches the bottom wall, it induces a pressure peak there (see figure 11, $p_{PW \text{ collision}}$). The pressure wave in the liquid is partially reflected at the gasliquid interface, and generates a tension wave following the initial pressure wave (a,iv,v). Furthermore, the collision of the circumferential pinching results in the formation of a wall-normal circular jet, see (a,iii,iv). The subsequent circular jet impacts on the bottom wall and pushes away the gas in the crevice centre. A secondary bubble pinches off and moves upwards (a,v). From the remaining flattened gas torus, an inner gas torus detaches at the position of the ring-shaped indentation, collapses (a,vi) and emits a pressure wave propagating in the direction of r = 0 (a,vii). At the same time, the remaining gas is pressed towards the crevice side walls and pressure waves are formed at the sharp edges of the crevice (a,vii).

For the $S/R_0 = 0.35$ and 0.6 cases (figure 10 (b) and (c)), a ring-shaped indentation forms close to the crevice edge during the initial collapse phase, similar to that of the $S/R_0 = 0.1$ case. In addition, the jet indents the bubble from the top, as observed for the small crevice and the smooth wall configurations. (b,iv) and (c,iii) show that the larger stand-off distance results in a more curved bubble interface when the jet impacts the wall. Similar to the $S/R_0 = 0.1$ case, an inner torus detaches from the main torus at the position of the ring-shaped indentation ((b,v) and (c,iv)) and collapses, emitting a pressure wave ((b,vi) and (c,v)). The pressure wave propagates to the centre, collides there inducing a pressure peak (c,vi) ($p_{c \text{ inner torus}}$) and then continues, resulting in a low-pressure area (c,vii). This pressure decrease can cause a vapour bubble rebound when phase-change processes are taken into account. The final collapse occurs when the remaining gas torus in the corner of the crevice is compressed to its minimum size (b,vii).

The pressure signals in figure 11 show the jet-induced pressure peak p_{jet} for $S/R_0 = 0.35$ and $S/R_0 = 0.6$. For $S/R_0 = 0.35 p_{jet}$ is higher because the initially liquid-exposed part of the bubble interface is almost a hemisphere and is thus strongly accelerated, see



 $p/p^* \ 10^{-3} \ 10^{-2} \ 10^{-1} \ 10^0 \ 10^1 \ 3 \cdot 10^1$

FIGURE 10. Numerical schlieren (left) and pressure fields (right) of an air bubble collapsing onto a wall with crevice size $R_C/R_0 = 0.75$ at varying stand-off distances S/R_0 (a)–(c) at selected times (i)–(vii). In (a,iii) and (a,iv) the relevant areas are additionally magnified in the upper left corner. (ii)–(vii) are magnified to the – – – rectangular region shown in (i). Selected pressure waves (PW), tension waves (TW), and collapse dynamics (col.) are also identified.

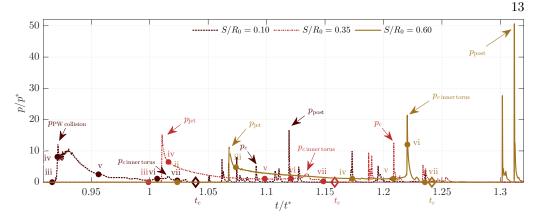


FIGURE 11. Evolution of the wall-pressure at r = 0 for the case $R_C/R_0 = 0.75$ at varying stand-off distances S/R_0 . The time instances shown in figure 10 are highlighted and labelled with the corresponding row (ii–vii). The pressure peaks induced by the jet impact p_{jet} , the collision of the pressure-wave $p_{PW \text{ collision}}$, the collapse of the inner torus $p_{c \text{ inner torus}}$, the total collapse p_c and post-collapse wave dynamics p_{post} are indicated as such. The collapse time t_c is plotted as a diamond on the x-axis.

also section 4.2. For $S/R_0 = 0.1$, there is no jet-induced pressure peak in the centre due to the circular jet. However, a pressure peak of about the same intensity is induced by the pressure wave emitted when the circumferential pinching collides ($p_{PW collision}$).

This first peak is followed by a peak $p_{c \text{ inner torus}}$ caused by the collapse of the inner detached torus. As S/R_0 increases, this pressure peak increases since the volume of the detached inner torus increases, resulting in a stronger pressure wave. Due to the preceding collapse of the inner torus, a smaller gas volume is associated with the final collapse phase. Furthermore, the collapse occurs at the crevice corner, and thus the induced pressure waves are less intense at the wall-centre. As a result, the collapse-induced pressure peak in the centre p_c is comparatively small and is exceeded by p_{jet} (or respectively by $p_{\text{PW collision}}$). Indeed, for $S/R_0 = 0.6$, the total collapse does not generate a pressure peak at the wall centre.

After the final collapse, intense wave dynamics occur, which can lead to high pressure peaks. For $S/R_0 = 0.1$ and 0.6, these post-collapse pressure peaks p_{post} are the maximum pressure observed.

4.5. Collapse of a wall-detached bubble $(S/R_0 = 1.1)$

The collapse of wall-detached bubbles $(S/R_0 = 1.1)$ are visualized in figure 12 for varying crevice sizes. The corresponding wall-centred pressure evolution is shown in figure 13. As observed for previous cases, the aspherical pressure distribution leads to an indentation of the top of the bubble and the formation of a jet penetrating the bubble for all cases. The monitored jet velocities are about $u_{jet}/u^* \approx 10$, which is in good agreement with previous studies for smooth walls (Lauer *et al.* 2012; Supponen *et al.* 2016).

For the smooth-wall case (figure 12 (a)) the jet impacts the far-side bubble interface at $t = 1.1t^*$ and a pressure wave is emitted (a,iii). The impact time of the jet at the bubble wall and the bubble position with respect to the initial configuration are in good agreement with previous observations (Supponen *et al.* 2016). The jet impact results in an upward and a downward moving wave front (see (a,iv)), with the latter being curved. The numerical schlieren shows an additional downward moving density jump corresponding to a contact wave. When the downward moving pressure wave impacts the wall, a pressure peak is induced (see also figure 13, $p_{PW jet}$). The pressure wave is then reflected at the

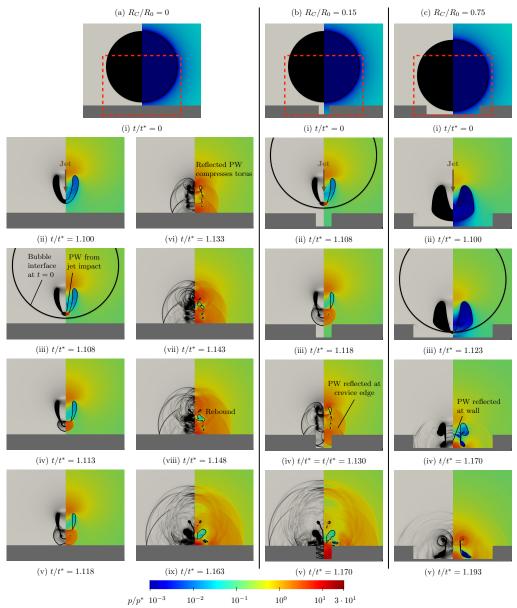


FIGURE 12. Numerical schlieren (left) and pressure fields (right) of a wall-detached air bubble $(S/R_0 = 1.1)$ collapsing onto a wall of varying crevice size R_C/R_0 (a)–(c) at selected times as labelled. (ii)–(ix) are magnified to the – – – rectangular region shown in (i). The solid curve in (a,iii), (b,ii) and (c,iii) indicates the initial position of the bubble interface. Selected pressure waves (PW) are also identified.

wall (a,v), compressing the remaining bubble torus from bottom to top (a,vi) leading to the total collapse. After the collapse (a,vii–ix), a gas torus rebounds and moves towards the wall.

Figure 12 (b) shows that the small crevice does not significantly change the collapse and rebound behaviour compared to the smooth wall. The main difference is the reflection

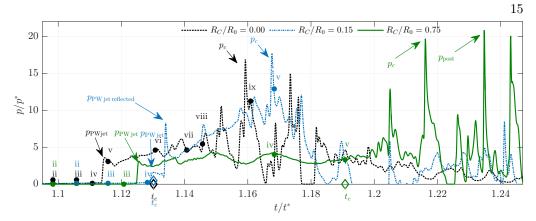


FIGURE 13. Evolution of the wall-pressure at r = 0 for the $S/R_0 = 1.1$ case and varying crevice sizes R_C/R_0 . The time instances shown in figure 10 are highlighted and labelled with the corresponding row (ii–v). The pressure peaks induced the pressure-wave $p_{\rm PW\,jet}$, the collapse p_c and post-collapse wave dynamics $p_{\rm post}$ are indicated as such. The collapse time t_c is plotted as a diamond on the x-axis.

of the pressure wave emitted at jet-bubble-impact at the crevice edge (b,iii–iv) and the resulting different wave patterns.

For $R_C/R_0 = 0.75$ (figure 12 (c)), the crevice initially suppresses the compression of the lower part of the bubble, resulting in a different shape during jet penetration, at jet impact, and also after compression by the reflected wave (c,ii–v). Furthermore, this increases the collapse time by about 5% when compared to the smooth-wall case.

The pressure signals (figure 13) show that the pressure wave due to the jet-bubbleimpact results in a pressure peak $p_{\rm PW jet}$ for all configurations. For the small crevice, the pressure wave has to pass a longer distance and thus the peak is smaller. However, the reflection and superposition of the wave at the edge of the crevice results in a more intense peak following ($p_{\rm PW jet reflected}$).

After the collapse, all three pressure signals exhibit pressure fluctuations with significant peaks that exceed $p_{\rm PW jet}$. For the large crevice, these peaks are modestly higher than those of the other cases, since the collapse, the rebound and the associated wave dynamics take place closer to the wall. In addition, there are pressure peaks induced by post-collapse wave dynamics for the large crevice.

4.6. Assessment of cavitation erosion potential

The previous sections showed that jet impact, collapse and, in certain configurations, post-collapse wave dynamics induce high pressure peaks in the crevice centre. Peak pressures are in the range of $15p^*-80p^*$, which corresponds to about 2 GPa-12 GPa for a bubble exposed to a driving pressure of $p_{\infty} = 10^7$ Pa. These values significantly exceed the strengths of many common engineering materials, such as the 0.55 GPa ultimate tensile strength of stainless steel. Thus, there is potential for significant material erosion. To investigate this, we compare the pressures associated with the various collapse mechanisms, evaluate the induced pressure impulse, and analyse the spatial distribution of maximum wall pressures.

Figure 14 compares the wall-centred pressures associated with the various processes. The jet-induced pressure peaks p_{jet} do not vary significantly for the three wall configurations, with nearly identical values for $R_C = 0$ and $R_C/R_0 = 0.15$. At $S/R_0 = 0.1$, $R_C = 0$ and at $S/R_0 = 0.35$, $R_C/R_0 = 0.75$, high interface accelerations and jet velocities occur,

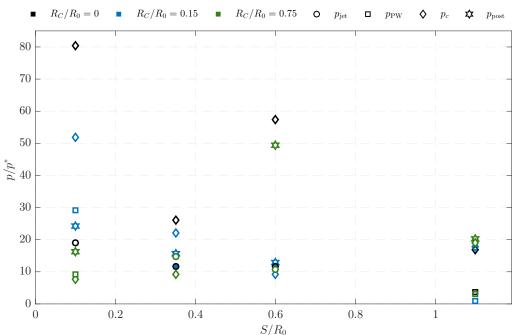


FIGURE 14. Pressure peaks observed at the wall centre (r = 0) over the stand-off distance S/R_0 for varying crevice sizes R_C/R_0 , indicated by different colours. The jet-induced pressure $p_{\rm jet}$, collapse-induced pressure p_c , and pressure from the subsequent wave dynamics $p_{\rm post}$ are shown. For cases with no $p_{\rm jet}$, the pressure peak induced by initial pressure waves $p_{\rm PW}$ is shown instead. Note that no $p_{\rm post}$ is observed for smooth wall configurations.

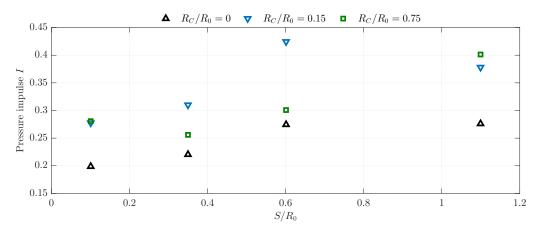
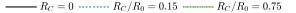


FIGURE 15. Pressure impulse I at the wall centre (r = 0) over the stand-off distance S/R_0 for varying crevice sizes R_C/R_0 , indicated by different colours and symbols.

resulting in an increased p_{jet} as discussed in sections 4.2 and 4.3. For $S/R_0 = 0.1$ with $R_C > 0$ and for $S/R_0 = 1.1$, there are no jet-induced pressure peaks.

The collapse-induced pressure p_c is for the smooth wall higher than for the creviced configurations. At the smooth wall, the final collapse position is closer to the wall-centre (r = 0) and a larger gas volume is associated with the final collapse phase. For the large crevice, p_c is significantly smaller than that of the other configurations. In these cases, a smaller gas volume is associated with the final collapse due to a preceding collapse of



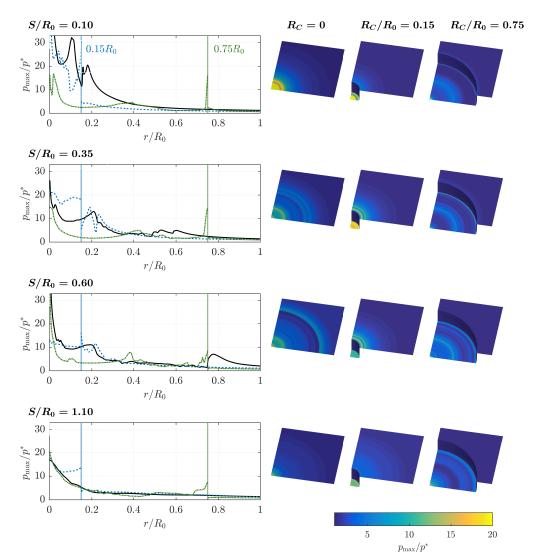


FIGURE 16. Maximum wall pressure p_{max} of the entire bubble-collapse process for varying radial locations r with rows corresponding to the stand-off distances S/R_0 . First column: p_{max} over r, where the pressure axes are truncated to promote visibility; the maximum values over all r are shown in figure 14. Second to fourth column: 3–D visualization of the maximum wall pressure for each crevice size.

an inner detached torus, see section 4.4. Furthermore, the final collapse is in the crevice corner and thus the intensity of the pressure waves decreases until they reach r = 0.

For the creviced configurations, high pressure peaks can be caused by the wave dynamics present after collapse. These peaks can be close to the maximum pressure induced in the smooth wall configuration (see $S/R_0 = 0.6$), indicating erosion potential. For the detached configuration all pressure impacts are of comparable intensity.

Figure 15 shows the pressure impulse at the crevice centre,

$$I = \frac{1}{1.5 t^* p^*} \int_0^{1.5 t^*} \left(p(t) - p(t=0) \right) \mathrm{d}t.$$
(4.2)

I takes into account whether an increased pressure is present over a longer period of time. In contrast to the maximum wall pressure, the impulse is not biased by single instantaneous peak values. Despite the smaller maximum p for the creviced cases, the impulse for these configurations is larger than that for the smooth-wall cases. For the small crevice, I is about 50% larger than at the smooth wall at all stand-off distances.

Figure 16 shows the maximum wall pressure p_{max} at varying radial locations and a visualization of the p_{max} distribution. First the attached configurations are discussed by crevice size and then the detached ones.

For the smooth wall configurations, there is a collapse-induced peak in p_{max} at the centre with a significant radial decay. In addition, modest pressure peaks are observed at about $r \approx 0.2R_0$, where the torus collapses. This pressure distribution is in agreement with predicted damage patterns by Philipp & Lauterborn (1998), who found ring-shaped damage $(r \approx 0.3R_0)$ and a smooth indentation at the wall centre.

For the small crevice, significant pressure peaks are induced over the entire crevice bottom. They are especially high at $S/R_0 = 0.35$, where they exceed that of the smooth wall. On the upper wall are peaks at about $r \approx 0.2R_0$ which are related to the torus collapsing at this position (see figure 8). For the small stand-off distance $S/R_0 = 0.1$ no increased maximum pressures are observed at the upper wall, because the collapse takes place within the crevice.

For the large crevice, the collapse of the detached gas torus results in a modest pressure peak at $r \approx 0.4R_0$, as described in section 4.4. This gas torus is largest for the $S/R_0 = 0.6$ case, and thus leads to highest pressures at this position. The total collapse is in the crevice corner ($r = R_C$) and induces large pressures at this location. Furthermore, at $S/R_0 = 0.1$ two pressure peaks are observed near r = 0. The impact of the circular jet results in the off-centre peak, while the shock wave after the collapse results in the r = 0maximum pressure.

For all detached-bubble cases, the maximum p_{max} occurs at r = 0, and decays with increasing r apart from a modest increase at $r = R_C$. For the small crevice, there is again a high pressure impact over the entire $r < R_C$ area. Nevertheless, overall the effect of R_C on p_{max} appears to decrease with increasing S.

Three distinct processes can cause high pressures at the crevice walls and thus, potential damage: the jet impact, the primary collapse, and post-collapse wave interactions. For smooth-wall cases, the pressure peaks are most significant at the wall centre and cavitation erosion can be expected at this location. For the small crevice cases, a high pressure occurs across the entire crevice bottom, leading to a broader area of possible cavitation erosion. For the large crevice cases, the pressure peaks seen at the crevice corners are also significant, and cavitation erosion is possible at these locations as well.

5. Conclusion

The collapse of a single gas bubble attached or near a smooth or creviced surface was investigated using high-resolution simulations. Variations of the stand-off distance of the bubble centre from the wall and the crevice size were considered. Changing these parameters significantly alters the behaviour of the bubble collapse and its associated impact on the wall.

For smooth-wall configurations the final collapse of the bubble results in the maximum

wall-pressure, rather than the liquid jet that impinges it. This is in agreement with experimental studies. A similar behaviour is observed for smaller crevice sizes, albeit for larger crevices the jet-induced pressures are more significant than the collapse pressures. The presence of the crevice results in a complex collapse process. Reflection and wave superposition result in wave dynamics, which can induce significant post-collapse pressures.

The part of the bubble interface initially in contact with the high-pressure liquid plays an important role in the collapse behaviour. The bubble collapse behaviour was qualitatively similar for the smooth-wall and small-crevice cases, since the pressure distribution at the interface was comparable. However, large crevices led to a significantly different bubble-liquid interface area, and thus qualitatively different dynamics. The effect of the wall geometry on the collapse behaviour and wall pressure was smaller for walldetached cases.

Lastly, we considered the potential for cavitation erosion. Pressures were recorded over a larger part of the wall. The presence of the small crevice leads to a significant pressure over the entire crevice bottom, as opposed to the smooth-wall cases when largest pressures occurred at the wall centre. For all rough configurations, high pressures also occur at the crevice edges, where they induce stresses that can result in material damage. The pressure impulse also increased by about 50% from the smooth-wall to small-crevice case, indicating an increased potential for material damage.

While assessing the effects of surface topology on hydrodynamics is a necessary step towards understanding this complex process, prediction of actual cavitation erosion also requires investigations of exposed materials. Coupled fluid-material simulations that incorporate suitable material models, and thus also represent elastic and plastic deformation, are one way to accomplish such investigations.

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Declaration of Interests

The authors report no conflict of interest.

Supplementary videos

Supplementary videos of the reported simulations are available online.

Videos of an air bubble collapsing onto a wall. The file names correspond to the different configurations considered. The videos show numerical schlieren (left) and log-scale pressure field (right). Gas volume fraction α_g is shown as a shaded area of decreasing opacity with decreasing α_g (left), while the $\alpha_g = 0.5$ bubble interface is shown as a solid curve (right). Time and pressure correspond to a $R_0 = 400 \,\mu\text{m}$ bubble that is exposed to a driving pressure of $p_{\infty} = 10^7 \,\text{Pa}$.

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