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Saransh Raj Gosain, Edith Bellet-Amalric, Eric Robin, Martien den Hertog, Gilles Nogues, et al.. Quantitative analysis of the blue-green single-photon emission from a quantum dot in a thick tapered nanowire. 2022. hal-03648910v1

HAL Id: hal-03648910

<https://hal.science/hal-03648910v1>

Preprint submitted on 22 Apr 2022 (v1), last revised 15 Feb 2023 (v4)

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Quantitative analysis of the blue-green single-photon emission from a quantum dot in a thick tapered nanowire

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(Dated: April 22, 2022)

Quantum dots acting as single photon emitters in the blue-green range are fabricated and characterized at cryogenic temperature. They consist in CdSe dots inserted in (Zn,Mg)Se nanowires with a thick shell. Photoluminescence spectra, decay curves and autocorrelation functions were measured under nonresonant continuous-wave and pulsed excitation. An analytical approach is applied simultaneously to the decay curves and correlation functions. It allows a quantitative description of how these two quantities are affected by the exciton rise due to biexciton feeding, the bright exciton decay, the effect of the dark exciton, and the re-excitation between two laser pulses. Linewidths at our limit of resolution (200 μeV) are recorded. The reported correlation counts vary from a full control by re-excitation from traps, to a small contribution of re-excitation by mobile carriers or other QDs, as low as 5%.

I. INTRODUCTION

Semiconductor quantum dots (QD) are actively contemplated as single photon emitters for quantum communications [1] [2]. In this context, the main focus is put onto III-V dots grown by the Stranski-Krastanov method and emitting in the IR range, particularly in the so-called telecom window [3]. In spite of impressive achievements, a drawback of this system is the cryogenic temperatures which are needed to make the QDs operate as efficient, pure single-photon emitters. CdSe QDs embedded in ZnSe appear as complementary since (1) they operate as single photon emitters [4] [5] [6] [7] up to room temperature [8] [9], and (2) they emit in the blue-green range, a wavelength range with a specific interest for underwater or water-air quantum communication [10] [11] [12] [13].

An attractive configuration for bright single-photon emission is that of a QD embedded in a waveguide [14], or even in a nanowire (NW) [15] which can be inserted in a photonic circuit [16]. The shell around the QD acts as a waveguide and it constitutes also an efficient environment akin to protect the QD from surrounding defects. This configuration reduces the influence of neighboring QDs which could be excited by the same laser pulse and modify the dynamics of the selected QD [17]. This is a clear advantage with respect to Stranski-Krastanov QDs.

In the case of CdSe QD in NWs, several configurations have been tested, including a QD with no shell [8], or a QD with a shell added post-growth [18]. In addition to the demonstration of room-temperature operation, several studies have explored the CdSe exciton dynamics [19], the spectral diffusion within the electrostatically broadened zero-phonon line [20], and the re-excitation by traps [21]. Here we address the most promising configuration, that of a self-assembled tapered shell grown

together with the QD in a unique run of molecular beam epitaxy (MBE).

The first test of a single-photon emitter is the Hanbury Brown and Twiss experiment, *i. e.*, the measure of the correlation function $g^{(2)}(t)$, either under continuous-wave (CW) or pulsed excitation. Both characterize the single-photon character, and its deviation due to overlap with multi-excitons or uncorrelated background. However, pulsed excitation is needed to characterize the ability to provide on-demand single-photon operation. We show here that the quantitative analysis of a combined measure of decay and correlation under pulsed excitation allows us to fully characterize the different components of the excitonic cascade and the associated signal such as re-excitation from traps, mobile carriers or adjacent QDs [21] [22] [23] [24], as well as spectral overlaps of the constituents of the radiative cascade [25]. To this purpose, we extend the use of the rate equations [25] [26] [27], and their analytical solutions generally used for CW-excitation data, to the case of pulsed-excitation data which usually are analyzed through a probabilistic, numerical approach. We apply this approach to two CdSe QDs in thick tapered ZnSe NWs, a first one which exhibits a strong re-excitation by traps, and a second one which features very good on-demand single-photon emission properties.

The paper is organized as follows. Section II describes the growth conditions and the characteristics of the selected samples, and describes the optical setup. Section III details the experimental results (spectra and correlations) under CW excitation. Section IV is devoted to the results (decay curves and correlations) obtained under pulsed excitation and to their quantitative analysis using the phenomenological analytical model developed in the Appendix. Section V summarizes the information acquired through this approach.

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II. SAMPLES AND EXPERIMENTAL

A. Growth and samples

A schematic of the whole structure is presented in Fig.1a. The growth conditions are detailed in Refs. [28] and [29]. Solid gold nanoparticles, with typical radius 3 to 5 nm, are formed on a ZnSe buffer layer, 8 nm thick, grown on a (111)B GaAs substrate [29]. First, a ZnSe core is grown by molecular beam epitaxy at 350°C. The nanowire radius at its tip is slightly smaller, by 0.5 nm, than the radius of the gold nanoparticle. The radial growth rate is very small so that the core is only weakly tapered [29]. Then, the CdSe QD is inserted close to the top of the ZnSe core and finally a tapered ZnSe or (Zn,Mg)Se shell is grown at 300°C or 320°C.

We present the results of time-resolved spectroscopy obtained on two samples, S10a and S7, with characteristics given in Table I, and electron microscopy images shown in Fig.1b and c, respectively. Scanning electron microscopy (SEM) imaging was performed using the secondary electrons in a Zeiss Ultra 55 (field emission gun) microscope, operated at 5–15 kV with typical beam currents in the 0.1–2.5 nA range. The sample tilt was 65 °C. Transmission electron microscopy (TEM) sample preparation was performed by mechanical/wet dispersion on a holey carbon grid. TEM was performed on a CM300 working at 300 kV. Decreasing the growth temperature of the shell from 320°C (sample S7 in Fig.1c) to 300°C (sample S10a in Fig.1) slightly increases the radial growth rate but induces the formation of structural defects.

Another sample, S10b, was grown with a thin (Zn,Mg)Se shell in order to determine the profile of the CdSe QD using the quantitative analysis of Energy Dispersive X-ray Spectroscopy (EDX) described in Ref. [30]. Scanning TEM and EDX was performed on a probe corrected Themis working at 200 kV. The result is shown in Fig.1d: It confirms the presence of a ZnSe core containing a (Cd,Zn)Se insertion with more than 50% Cd, both with a radius ~ 3 nm which reasonably matches the radius of the nanoparticle determined in Ref. [29]. The QD height is 4 nm. We expect the same size for sample S10a, which contains the same CdSe insertion (10 s of growth), and a 3 nm height for sample S7 with a 7 s insertion.

The overall crystal structure is wurtzite, with a good epitaxial relationship between the core and the shell (Fig. 1d). The possibility of a zinc-blende structure in the QD and around has been demonstrated in CdSe-ZnSe nanowires with a thin diameter [31]. It gives rise to an increased thickness of the shell at the level of the QD. Although we did not observe such a thickening in the present S10a and S7 samples, the structure of a small QD with a thick shell is difficult to assess.

B. Spectroscopy set-up

The as-grown samples were mounted on a cold-finger cryostat cooled down to 5-6 K, and a single nanowire was excited along its axis, and its photoluminescence (PL) detected along the same axis in a confocal setup. CW excitation was provided by a laser diode emitting at 405 nm (a photon energy 3.06 eV, larger than the ZnSe bandgap), focused through a long working distance microscope objective of numerical aperture NA=0.55. This results in a laser spot of about 1 μm in diameter on the sample, small enough to excite a single nanowire in our samples with a low nanowire density. The 0.46 m spectrometer was equipped with a 1800 grooves/mm grating providing a resolution around 0.7 meV with a slit width 0.2 mm, and slightly less than 0.2 meV with the smallest slitwidth (0.05 mm). The detection was ensured by a charge-coupled device (CCD) of 1024 \times 256 pixels, and 26 μm per pixel.

Pulsed excitation was provided by a near infra-red picosecond Titanium-Sapphire laser, doubled in frequency to 440 nm (2.82 eV) using a frequency doubling β -BaB₂O₄ crystal. The pulse frequency was 76 MHz (repetition time $T_0=13.1$ ns). Spectra shown here were recorded with the same setup as for CW excitation. For time-resolved data, detection was provided by single-photon avalanche photodiodes (APD) id100-50 from id-Quantique, mounted on the side exit of the spectrometer. The same setup was used to measure the decay of luminescence, or the correlation functions in the Hanbury Brown and Twiss (HBT) configuration, using a Becker and Hickl time-correlated single photon counting (TC-SPC) module. The diameter of the active area of the APD's is 50 μm . The spectrometer was equipped with the 1800 grooves/mm grating or a 600 grooves/mm grating, providing a passband from 0.7 to 3 meV FWHM. The time resolution of the setup is limited by the response time of the fast APD's, which is reasonably well described by a Gaussian function of 60 ps FWHM [33], with a few-ns long diffusion tail of intensity less than 1% of the fast pulse [33]. For the two arms of the Hanbury Brown and Twiss setup, the response is thus given by a Gaussian function $\frac{1}{\sigma\sqrt{2\pi}} \exp(-\frac{t^2}{2\sigma^2})$ with standard deviation $\sigma = 40$ ps.

TABLE I. List of samples, with measured base radius (in nm), shell growth temperature (in °C), and measured or expected QD height (in nm).

Sample	Shell content	Base radius nm	Growth Temp. °C	QD height nm
S10a	(Zn,Mg)Se	140	300	4 expected
S10b	(Zn,Mg)Se	30	320	4 measured
S7	ZnSe	90	320	3 expected

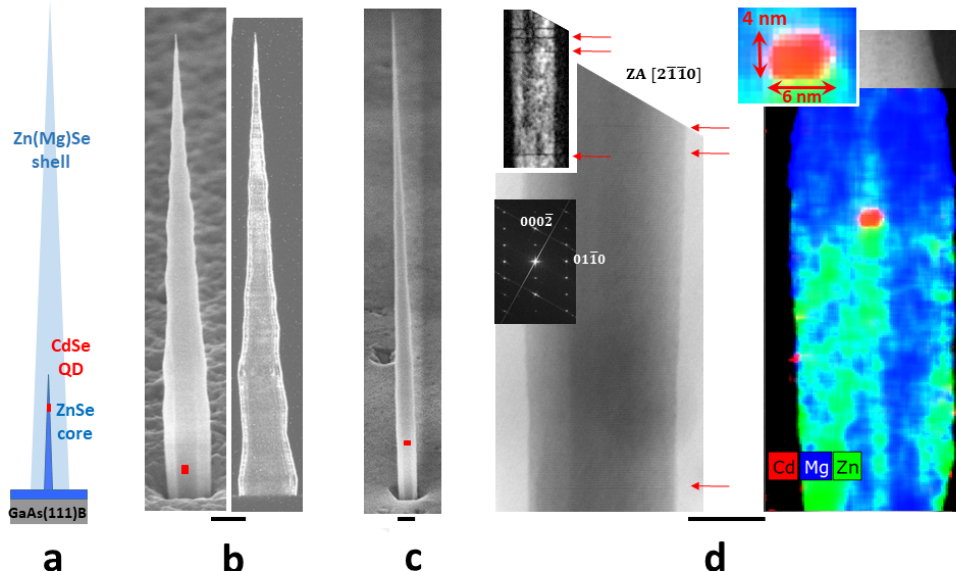


FIG. 1. (a) Schematic of the QD-core-shell structure; (b) Sample S10a with (left) the SEM image of a NW (at 65°) and (right) the scanning-TEM darkfield image of another NW evidencing a large number of stacking faults; (c) Sample S7, SEM image (at 65°); (d) Sample S10b; the left panel is the bright-field TEM image of a NW, showing (see the FFT) the wurtzite structure of the core of radius 8 nm and the 12 nm thick shell; The inset is the amplitude image of the $\{01\bar{1}0\}$ reflection, made with geometrical phase analysis [32] on the same section of the NW, revealing more clearly the few stacking faults (red arrows). The right panel is the EDX map of another NW identifying the ZnSe core and the (Zn,Mg)Se shell, with a CdSe QD of 4 nm height and 3 nm radius (inset). Scale bars: 200 nm for (b) and (c), 20 nm for (d).

III. SPECTROSCOPY AND DYNAMICS UNDER CW EXCITATION

A. Spectra

Figures 2a and d show three PL spectra recorded on a NW from sample S10a (top) and sample S7 (bottom), respectively, for different values of the excitation power. Each of the main lines comprises essentially a rather narrow component on top of a broader one. From the dependence on temperature (not shown), we ascribe the broad component to the Stokes and anti-Stokes acoustic-phonon sidebands, and the narrow component to the zero-phonon line, as already observed for CdTe-ZnTe QDs [34]. Figure 2c shows a spectrum recorded with a better resolution. This high resolution spectrum confirms the presence of an additional, weak narrow line. The intensity of such lines, with respect to the main lines, varies from NW to NW. Their origin is unknown. Note that a line such as that in Fig. 2c will remain out of the spectrometer passband in measures of time dependant quantities, even with the 600 grooves/mm grating (see the blue segment in Fig. 3a).

The attribution of the two main lines (and their side-

bands) to the neutral exciton (X) and biexciton (XX) is deduced from the dependence of their intensity on the excitation power, linear and quadratic, respectively, see Fig. 2b and e. The whole set of data was fitted using Eq. 1,

$$I_X(P) = I_{sat} \frac{P}{P_{sat}} \exp\left(-\frac{P}{P_{sat}}\right),$$

$$I_{XX}(P) = I_{sat} \left(\frac{P}{P_{sat}}\right)^2 \exp\left(-\frac{P}{P_{sat}}\right). \quad (1)$$

This expression results from the simple model described in Ref. 27 and schematized in the left part of Fig. 2g. This model assumes that the probability of decay of the n -exciton is proportional to n , for instance, the lifetime of the biexciton τ_{XX} is half that of bright exciton τ_X ; It neglects the effect of the dark exciton (we will show below that it plays a minor role at low temperature) and the more complex structure of the multi-excitons of higher order than the biexciton (which play a role only at excitation power much larger than P_{sat}). The two fitting parameters, I_{sat} and P_{sat} , essentially depend on the experimental setup, but $P = P_{sat}$ means that the decay rate $\frac{1}{\tau_X}$ and the pumping rate p of the bright exciton are equal.

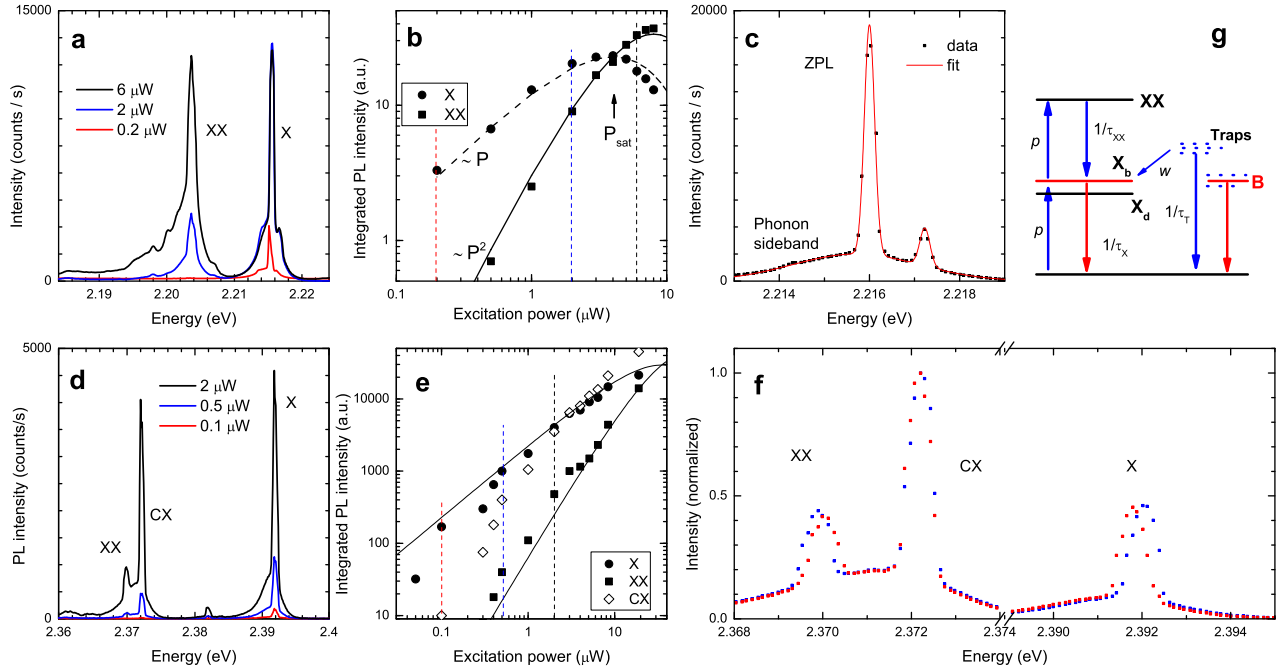


FIG. 2. Photoluminescence of sample S10a (top) and sample S7 (bottom), with CW excitation at 3.06 eV, detection CCD and grating 1800 grooves/mm. (a) to (c) sample S10a: (a) PL spectra for increasing values of the excitation power, as indicated, slits 0.2 mm; (b) PL intensity of the two main lines in (a), as a function of excitation power; the solid lines show the fit with Eq. 1; (c) PL spectrum at 5 μ W excitation power and entrance slit 0.05 mm, with fit shown as a solid line. (d) to (f) Sample S7: (d) PL spectra for increasing values of the excitation power, as indicated, grating 1800 grooves/mm, slits 0.2 mm (e) PL intensity of the three main lines with vertical lines identifying the three spectra in (d), as a function of excitation power; (f) zoomed views of the three main lines for two orthogonal linear polarizations, excitation power 10 μ W, grating 1800 grooves/mm, slits 0.2 mm, with the intensity normalized for the line at 2.372 eV. (g) Scheme of the different levels involved in our analyses. The spectrometer is tuned to the luminescence of the bright exciton X_b ; Eq. 1 involves the biexciton XX and the bright exciton X_b ; the analysis of the pulsed-excitation data considers also the dark exciton X_d and a reservoir of traps T . A part of the background light B is recorded.

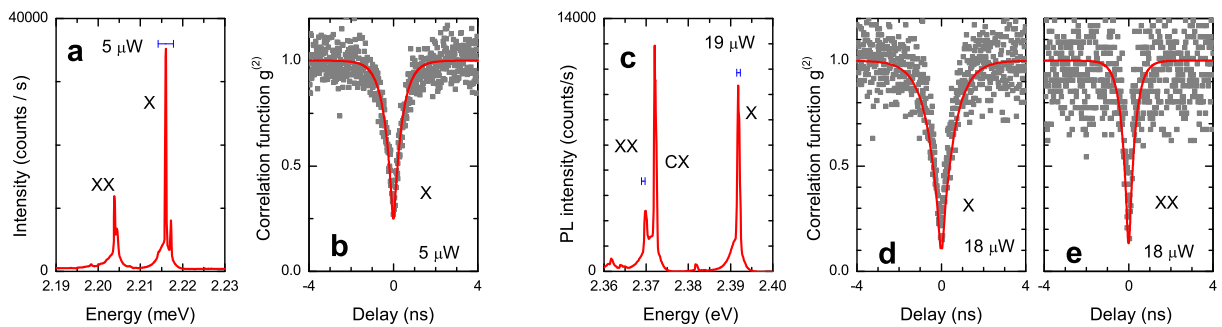


FIG. 3. Normalized photoluminescence autocorrelation $g^{(2)}(t)$. (a and b) Sample S10a with (a) spectrum, grating 1800 grooves/mm, slits 0.2 mm and CCD detection, the blue segment indicates the spectrometer position and passband used in the autocorrelation data in (b); (b) X autocorrelation, grating 600 grooves/mm, slits 0.3 mm and APD detection. (c to e) Sample S7, (c) spectrum, grating 1800 grooves/mm, slits 0.2 mm and CCD detection; the blue segments indicate the spectrometer position and passband used in the autocorrelation data; (d) X autocorrelation and (e) XX autocorrelation with grating 1800 grooves/mm, slits 0.2 mm and APD detection. The red curves are drawn using Eq. 3, with the adjustable parameters $T_{CW} = 0.4$ ns and $\frac{B}{S} = 0.10$ in (b), $T_{CW} = 0.6$ ns and $\frac{B}{S} = 0.02$ in (d) and $T_{CW} = 0.3$ ns and $\frac{B}{S} = 0.02$ in (e).

The power dependence is not totally sufficient to decide which line is the biexciton line in sample S7, since two lines feature a superlinear power dependence. The final attribution is done by comparing the spectra for two orthogonal linear polarizations, Fig. 2f. A fine structure splitting, $\sim 200\mu$ eV, is observed with opposite signs on the two extreme lines (therefore attributed to X and XX), and not on the central line at 2.372 eV (therefore attributed to a charged exciton). A similar distribution in energy of the X, CX and XX lines, with a fine structure present, was observed in self-assembled CdSe QDs [35] and excitons localized at CdSe-ZnSe local fluctuations [36]. An intermediate narrow line is visible on S7 at 2.382 eV in Fig. 2d (see also Fig. 5a below); from polarization studies on another NW with a 10s-insertion (not shown), the corresponding line is very narrow (down 200 μ eV) and not polarized, although a fine structure splitting as high as 400 μ eV is observed on the neutral exciton of the same NW; the non-polarized line is thus attributed to the charged exciton with a charge opposite to that of the previous one.

The splitting between the X and XX lines (the so-called binding energy B_{XX} of the biexciton) is larger in sample S7 (22 meV) than in sample S10a (15 meV).

We also observe additional lines for higher values of the excitation power. They are strongly polarized (not shown) and attributed to multi-excitons of index larger than 2.

A notable characteristics of the exciton lines is the values of their full linewidth at half maximum (FWHM), down to 200 μ eV, and close to the limit of resolution of the setup in all spectra of Fig. 2.

B. Autocorrelations

Figure 3 displays the normalized autocorrelation functions $g^{(2)}(t)$ recorded with CW excitation, from the same NWs as in Fig. 2, measured over the blue windows shown in the spectra recorded with the same excitation power (Figs. 3a and c). The excitation power was slightly below P_{sat} as defined in Eq. 1.

All feature a simple anti-bunching behaviour, characterized [37] by a bi-exponential distribution (or Laplace distribution [38]):

$$g^{(2)}(t) = 1 - \left[1 - g^{(2)}(0)\right] \exp\left(-\frac{|t|}{T_{CW}}\right), \quad (2)$$

where T_{CW} is the time constant resulting from the dynamics of the exciton or biexciton, described [27] as a two-level system with an excitation rate p and decay rate $\frac{1}{\tau}$, *i.e.*, $\frac{1}{T_{CW}} = p + \frac{1}{\tau}$.

This response must be convoluted with the response function of the Hanbury Brown and Twiss setup. The result of the convolution of the Laplace distribution by a Gaussian function of standard deviation σ is the normal-Laplace distribution [38], for which a straightforward cal-

culational leads to

$$g^{(2)}(t) = 1 - [1 - g^{(2)}(0)] [G(t) + G(-t)]$$

$$G(t) = \frac{1}{2} \exp\left(\frac{\sigma^2}{2T_{CW}^2} + \frac{t}{T_{CW}}\right) \left[1 - \operatorname{erf}\frac{1}{\sqrt{2}}\left(\frac{\sigma}{T_{CW}} + \frac{t}{\sigma}\right)\right], \quad (3)$$

where $\operatorname{erf}(z) = \frac{2}{\sqrt{\pi}} \int_0^z \exp(-t^2) dt$ is the error function.

To first order in $\frac{\sigma}{T_{CW}}$, this reduces to $g^{(2)}(0) \simeq \sqrt{\frac{2}{\pi}} \frac{\sigma}{T_{CW}}$.

A first contribution to non-vanishing of the zero-time correlation is the contribution of the background signal, which leads to replace $[1 - g^{(2)}(0)]$ in Eq. 3 by $[1 - g^{(2)}(0)] \left(\frac{S}{S+B}\right)^2$ [37], where S is the QD signal and B the uncorrelated background. To first order in $\frac{B}{S}$, this adds a contribution $\frac{2B}{S}$ to $g^{(2)}(0)$. The values of the fitting parameters are discussed in Section V B.

IV. DYNAMICS UNDER PULSED EXCITATION

A. Experimental results

Photoluminescence spectra under pulsed excitation are given in Fig. 4a for sample S10a and Fig. 5a for sample S7, for two different values of the excitation power. The exciton and biexciton lines, already identified with CW excitation, exhibit also the characteristic, linear or quadratic, increase with the pulsed excitation power (not shown).

Figure 4b shows the evolution in time of the exciton and biexciton intensity after a low-power excitation pulse. A constant baseline has been subtracted. Both X and XX feature an immediate rise (faster than our time resolution of 60 ps), followed by an exponential decay with characteristic times 0.3 ns (XX) and 0.7 ns (X). A slow component is weak but visible in the decay of the exciton.

At high excitation power the exciton exhibits a slow rise, and the intensity of the slow component dramatically increases (Fig. 4c) so that the signal remains high even at the end of the arrival of the following pulse at $t = T_0$. The whole decay is reasonably well described by a sum of three exponential functions, to be detailed below. We may note that the XX signal follows a similar trend, with a slow component which however is not so intense and not so slow as for the exciton signal.

Finally, the autocorrelation of the exciton is quite singular (Fig. 4d), with a wide Laplace distribution at each non-zero delay nT_0 , and another one around zero-delay with a narrow dip at its center. Similar shapes have been evidenced previously in III-V QDs [22] [23] [24] and in CdSe QDs [21] and attributed to re-excitation effects. The fit will be described in the next subsection.

The same set of data is shown for sample S7 in Fig. 5. At low excitation power (Fig. 5b), the exciton signal exhibits a fast rise and a sub-ns decay as the main component, with characteristic time 0.6 ns, and a slower com-

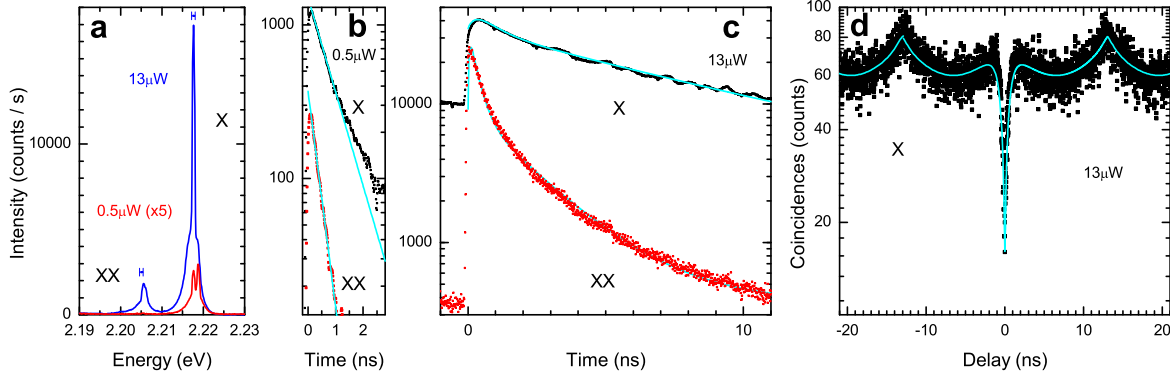


FIG. 4. Sample S10a under pulsed excitation, (a) spectra with 1800 grooves/mm, slits 0.2 mm, CCD detection, and (b to d) time-resolved data with grating 1800 grooves/mm, slits 0.2 mm and APD detection; (a) spectra at two different values of the excitation power, $0.5 \mu\text{W}$ (red curve) and $13 \mu\text{W}$ (black); the blue segments indicate the spectrometer position and passband used in the time-resolved data; (b) decay for the exciton X (black symbols) and biexciton XX (red), with excitation power $0.5 \mu\text{W}$, after subtraction of a constant baseline; the solid lines display exponential decay curves with characteristic times 0.7 and 0.3 ns, respectively (c) decay for X (black symbols) and XX (red), with excitation power $13 \mu\text{W}$; the solid line shows the fit as described in text (d) exciton autocorrelation at $13 \mu\text{W}$; the solid line shows the fit with the same parameters as in (c).

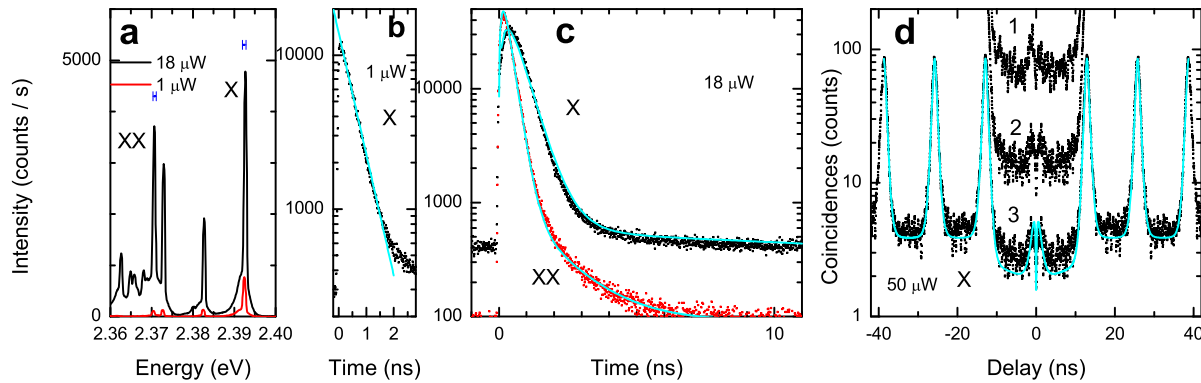


FIG. 5. Sample S7 under pulsed excitation, grating 1800 grooves/mm, slits 0.2 mm (a) spectra at two different values of the excitation power, $1 \mu\text{W}$ (red curve) and $18 \mu\text{W}$ (black) both with CCD; the blue segments indicate the spectrometer position and passband used in the time-resolved data; (b) decay for X (black symbols) with excitation power $1 \mu\text{W}$, after subtraction of a constant baseline; the solid line displays an exponential decay with characteristic time 0.5 ns; (c) decay for X (black symbols) and XX (red), with excitation power $18 \mu\text{W}$; the solid lines show the fit as described in text (d) symmetrized exciton autocorrelation at $50 \mu\text{W}$; the solid line shows the fit with the same parameters as in (c); the data before symmetrization are shown by curve 1 (shifted $\times 25$) and the symmetrized signal without fit by curve 2 (shifted by $\times 5$).

ponent more than a decade below. The slow component is clearly visible at higher excitation power (Fig. 5c) but again its intensity is much weaker than for sample S10a. The correlation function (Fig. 5d) is dominated by narrow Laplace-like peaks at each non-zero nT_0 . It is necessary to use a log scale plot to obtain a clear evidence of the re-excitation contribution around zero delay. Note also that the plateau between $t = 0$ and $t = T_0$ is significantly lower than between T_0 and $2T_0$. The raw data (curve 1, shifted by $\times 25$) are not totally even with re-

spect to time, which suggests that the two arms of the Hanbury Brown and Twiss setup were not totally equivalent. The re-excitation contribution is clearly visible in the symmetrized signal (curve 2, shifted by $\times 5$) and this symmetrized signal (curve 3) will be fitted below.

B. Analytical model

The process of direct or quasi-direct excitation by the laser pulse is in the sub-ps or ps range and is considered here to be infinitely short. Immediately after the laser pulse ($t = 0$), the QD may contain one or several electron-hole pairs. The cascade which follows is a random process: there is a probability $\mathcal{P}_X(t)$ that the recombination of the last electron-hole pair takes place exactly at time t , and in the absence of non-radiative recombination, the signal $I_X(t)$ recorded at the single exciton wavelength is proportional to the average of $\mathcal{P}_X(t)$ over laser pulses. The ratio I_X/\mathcal{P}_X incorporates all experimental characteristics (escape of photons from the sample, collection on the front lens and throughput of the optical set-up, efficiency of the detector and electronics, accumulation time). Appropriate factors should be introduced to take into account the possibility of non-radiative recombination, we will not consider that in the present simple approach.

In the experimental conditions of non-resonant excitation for on-demand single-photon emission, the QD contains several electron-hole pairs after each laser pulse. As a result, we assume that the initial distribution is restored at each laser pulse at nT_0 , so that the intensity $I_X(t)$ is periodic, with period T_0 .

The intensity signal corresponding to the excitonic cascade in the QD can generally be adequately reproduced by a sum of three exponential functions. In the interval $[0, T_0]$,

$$I_X(t) = \sum_{i=1}^3 A_i \exp\left(-\frac{t}{\tau_i}\right). \quad (4)$$

The parameters entering Eq. 4 can be calculated using a master equation restricted to the exciton+biexciton system, *i.e.*, the QD contains no electron-hole pair, one electron-hole pair or two electron-hole pairs. General results with respect to the parameters of the master equation are detailed in Ref. [19] [22] [27]. It is again based on the left part of Fig. 2g, with no CW excitation ($p = 0$). In the simplest case, the different components of $I_X(t)$ are related to the decay of the bright exciton with $\tau_1 = \tau_X$ (including possible non-radiative channels), and to its rise due to the biexciton-to-exciton transition, with $\tau_2 = \tau_{XX}$ and $A_2 < 0$. At low excitation, A_2 vanishes. The third term, $A_3 \exp(-\frac{t}{\tau_3})$, is the "dark exciton component", actually the final decay of the bright+dark exciton. In CdSe QDs, it has been observed to be weak at 4K and to become visible as the temperature increases [19] [35].

Finally, the description requires at least two additional terms, so that the signal is

$$\begin{aligned} I(t) &= I_X(t) + I_R(t) + I_B(t) & (5) \\ I_R(t) &= A_R \exp\left(-\frac{t}{\tau_R}\right), \\ I_B(t) &= A_B \exp\left(-\frac{t}{\tau_B}\right). \end{aligned}$$

The second term, $I_R(t)$, describes the effect of re-excitation from entities which have been excited by the laser pulse and can re-populate the QD when the last photon of the cascade has been emitted. Such a process has been evidenced in CdSe QDs [21] as well as in III-V QDs [22] [23] [24].

The last term, $A_B \exp(-\frac{t}{\tau_B})$ represents non-correlated luminescence due to any parasitic photon source.

In a Hanbury Brown and Twiss experiment, a first photon is detected at time t_1 and a second photon at time t_2 , and the number of coincidences is recorded as a function of the delay time $t = t_2 - t_1$. The first-photon signal is given by $I(t_1)$, and we can without loss of generality assume that $t_1 \in [0, T_0]$ (this constitutes a definition of the pulse labelling). In order to calculate the coincidence count, we must distinguish the first period $[0, T_0]$, from the following ones $[nT_0, (n+1)T_0]$ with $n > 0$.

If $t \in [T_0, 2T_0]$, then $t_2 \in [T_0, 3T_0]$ and the coincidence count is proportional to

$$\begin{aligned} C(t) &= \int_0^{T_0} dt_1 I(t_1) \int_{T_0}^{2T_0} dt_2 I(t_2 - T_0) \delta(t_2 - t_1 - t) \\ &+ \int_0^{T_0} dt_1 I(t_1) \int_{2T_0}^{3T_0} dt_2 I(t_2 - 2T_0) \delta(t_2 - t_1 - t) \end{aligned} \quad (6)$$

with $I(t)$ given by Eq. 5. As the QD content is reset to the same initial value at each pulse, Eq. 6, shifted adequately, holds if $t \in [nT_0, (n+1)T_0]$.

If $t \in [0, T_0]$, the single-photon character has to be taken into account. In this case, $t_2 \in [0, 2T_0]$ and we must distinguish between the two intervals, $[0, T_0]$ and $[T_0, 2T_0]$.

If $t_2 \in [T_0, 2T_0]$, the QD has been re-excited by the laser pulse at T_0 between t_1 and t_2 and the first member of Eq. 6 applies.

If $t_2 \in [0, T_0]$,

- the QD is empty immediately after t_1 , hence $I_X(t_2) = 0$,
- the non-correlated background is not altered, $I_B(t_2) = A_B \exp(-\frac{t_2}{\tau_B})$
- the QD can be re-excited.

The effect of re-excitation is usually evaluated numerically through a stochastic approach [21] [22] [23] [24]. We propose here an analytical description using the same approach as for CW correlations, *i.e.*, through the solution of the master equation governing the average population of the system comprising the single-exciton state of the QD and the reservoir (bottom of Fig. 2g, with an exciton lifetime τ_1 and a re-excitation rate w by transfer from the reservoir. Immediately after time t_1 , the QD is empty. If the population of the reservoir remains constant, the average QD population at time t after the emission of the first photon is $w\tau[1 - \exp(-\frac{t}{\tau})]$, with $\frac{1}{\tau} = w + \frac{1}{\tau_1}$. This is still reasonably valid if w decreases slowly with

the population of the reservoir, with the characteristic time τ_R , so that the second-photon count at time t_2 is $I_R(t_2)[1 - \exp(-\frac{t}{\tau})]$.

As a result, for $t \in [0, T_0]$,

$$\begin{aligned}
C(t) &= \int_0^{T_0} dt_1 I(t_1) \int_0^{T_0} dt_2 I_B(t_2) \delta(t_2 - t_1 - t) \\
&+ \int_0^{T_0} dt_1 I(t_1) \int_0^{T_0} dt_2 I_R(t_2) \delta(t_2 - t_1 - t) [1 - \exp(-\frac{t}{\tau})] \\
&+ \int_0^{T_0} dt_1 I(t_1) \int_{T_0}^{2T_0} dt_2 I(t_2 - T_0) \delta(t_2 - t_1 - t)
\end{aligned}
\tag{7}$$

The calculation of Eq. 6 and 7 with Eq. 5 is given in the appendix. In short, if the decay signal is well-reproduced by a sum of exponential functions, the common expectation [39] that the coincidence count around each finite nT_0 is described by a sum of bi-exponential distributions (the so-called Laplace distribution) is correct, but the characteristic time comes as a prefactor for each component. Hence slow components are enhanced. In addition, once again as expected but sometimes overlooked, special terms appear in the $[-T_0, T_0]$ segment, which ensures that the coincidence count vanishes at zero delay unless specific processes take place, such as multi-excitonic stray light or non-correlated emission. If necessary, the Laplace distributions are replaced by normal-Laplace distributions in order to take into account the time resolution of the setup (as in Eq. 3). In the present case, this was found necessary only for the central dip of re-excitation.

For the two samples, a good fit of both the decay and coincidence counts is obtained with a single set of parameters. The relevant parameters, kept constant between decay and coincidence, are the decay time τ_1 , the rise time τ_2 and relative amplitude $\frac{A_2}{A_1}$, the long component in the radiative cascade (dark exciton) with time τ_3 and relative amplitude $\frac{A_3}{A_1}$, the re-excitation with time τ_R and relative amplitude $\frac{A_R}{A_1}$, and the relative amplitude $\frac{A_B}{A_1}$ of background contribution assumed to be constant in time. These values are given in Table II. The vertical scales are left independent between the decay and coincidence plots. This also allows for changes of incident power which should affect the overall scale more than the relative intensities.

V. DISCUSSION AND CONCLUSION

A. Spectroscopy of CdSe quantum dots

Our identification of the biexciton line is based on the characteristic dependence on the excitation power, both in CW and pulsed excitation, but also on the energy shift with respect to the linear polarization, with a symmetric splitting observed on the neutral exciton and biexciton lines of several QDs. This symmetric splitting is the signature of a fine structure splitting. Note that

this observation is possible in the present axial configuration (made easy by the guiding effect of the tapered shell), while it was not in previous studies of CdSe QDs in nanowires with observation along a transverse direction. In the present samples its value varies from NW to NW and ranges from non-measurable (less than 100 μeV) to 400 μeV . The fine structure splitting was reported in self-assembled dots on (001) orientation [35] [40]. Here it is observed in spite of the (111) orientation, which suppresses a mechanism based on the crystal structure, and points to a deviation from a circular or hexagonal shape of the shell or the QD.

We observe a splitting between the neutral exciton and biexciton lines ranging from 15 meV to 22 meV. The lower bound is achieved in the thicker QDs (4 nm), the higher bound in the shorter QDs (3 nm). This agrees with simple ideas on the role of confinement, with a larger binding energy in the smallest nanostructures. It could also point to a role of the piezoelectric field, likely to separate the electron and hole apart in the thicker QD, but the fact that these values are quite similar to previous results not only in QDs inserted in nanowires, but also in self-assembled QDs with the $\langle 001 \rangle$ orientation [40], suggests that the effect of the piezoelectric field remains small.

We have attributed two lines to the two types of charged excitons. These two lines are non polarized even if a fine structure splitting is present, and they exhibit a power dependence intermediate between X and XX. One, giving rise to the central line equidistant from the X and XX lines, appears to be associated with pre-existing carriers. This central line was sometimes attributed to negatively charged exciton [21] [41]. The other line is close to the XX line and exhibits a quadratic dependence on excitation power, which we ascribe to the photocreated nature of the associated charge. Such a charged exciton line close to XX was also occasionally observed [35] [36].

Although not a priority of this study, we observe linewidths much smaller than previously observed in CdSe QDs with a thin shell or a shell deposited post-growth, for instance 0.9 meV in Ref [8], or even 2 meV, with a Gaussian profile, in QDs where spectral diffusion

TABLE II. Values of the main parameters used in Figs. 4 and 5.

Sample	Contribution	A_i/A_1	τ_i (ns)
S10a	X fast decay (i=1)		0.7
	X rise (i=2)	-1	0.3
	X slow decay (i=3)	0	
	X re-excitation (R)	1.4	8
	Background (B)	0.09	∞
S7	X fast decay (i=1)		0.46
	X rise (i=2)	-1	0.23
	X slow decay (i=3)	0.005	30
	X re-excitation (R)	0.05	0.8
	Background (B)	0.001	∞

was studied by cross-correlations [20]. A thick shell is akin to protect the QD from the effect of surface traps. The present linewidths are even smaller than in self-assembled QDs, where the FWHM ranges from 1 meV [21] to 0.3 meV [42]. More precise studies are needed to assess the actual linewidth of the present structures.

B. Three approaches to the dynamics

We have described the results of three complementary approaches: the decay of photoluminescence after pulsed excitation, the correlation function under CW excitation, and the correlation function under pulsed excitation. They bring complementary pieces of information on the dynamics of the QD system.

They are analyzed through a model which assumes a reset of the QD content to an initial value at each pulse: this is reasonable in the present case where, as shown below, non-resonant pumping creates a large number of electron-hole pairs in the QD in order to reach the on-demand regime. This assumption would be questionable at low excitation, resonant or non-resonant.

Also, one has to keep in mind that the proposed phenomenological and analytical approach with three characteristic times for the QD exciton-biexciton system is not an identification of their origin as X lifetime, XX lifetime, dark X lifetime.

The decay curves provide very precise information on the short-time processes. The fast-decay time of the exciton is in the sub-ns range, as expected for a CdSe QD [4] [8][19] [35]. The present QDs are oriented along the polar $\langle 111 \rangle$ axis and experience a mismatch strain from the ZnSe surrounding material, hence a piezoelectric field is built in and the electron and the hole of the excitonic pair are pushed away to opposite interfaces. However, detailed calculations in the parent system CdTe-ZnTe [43] show that for such flat QDs (radius 4 nm and height 4 nm) the shift is small, provided the valence and electron band offsets are not vanishingly small. Then the electron-hole overlap is not dramatically reduced, and the probability of radiative recombination remains high, which offers good perspectives for fast communication close to GHz frequencies. The fast-decay time of the biexciton is significantly smaller than the fast-decay time of the exciton, with a ratio close to 2. This value is assumed in the simplest description of the biexciton, which was used to analyze the power dependence under CW excitation in section III A, assuming no non-radiative decay. The decay of the signal we have attributed to charged excitons (not shown) is similar to the decay of the neutral exciton. An important piece of information in the context of quantum communication is that, in both samples, the risetime of the exciton signal (τ_2) is equal to the short decay time of the biexciton signal. In Figs. 4c and 5c, the exciton rise amplitude is equal to its fast decay amplitude, $\frac{A_2}{A_1} = -1$. In the simple interpretation of the I_1 and I_2 components of the phenomenological de-

scription, that means that each laser pulse creates more than two electron-hole pairs in the QD. Hence, the on-demand condition is fulfilled. At lower P (Figs. 4b and 5b), the absence of rise time, $\frac{A_2}{A_1}$ ratio close to zero, confirms that the pumping is too low to ensure on-demand operation. Note that one expects, and we have observed (not shown) that using a much higher excitation signal results in a complex rise of the exciton and a significant rise of the biexciton. Finally, the origin of the slow signal, which is visible at high excitation power, is difficult to ascertain from the simple decay curve.

The correlation functions $g^{(2)}(t)$ under CW excitation bring additional pieces of information. The characteristic times are of the same order as τ_1 from decay curves, or slightly smaller. This agrees with the fact that the correlation functions were recorded under such conditions that the XX signal is quite visible but smaller than the X signal, so that the pumping rate p is smaller than $\frac{1}{\tau_1}$. Fitting with the normal-Laplace distribution shows that a large part of the $g^{(2)}(0)$ value is due to the finite time resolution of our setup. From the spectra in Fig. 3, a biexciton contribution to $g^{(2)}(0)$ is likely to be negligible. What remains is probably due to a background contribution, which is quite small ($\frac{B}{S} \approx 0.02$ in Figs. 3d and e) for Sample S7. It is larger (≈ 0.1) in Fig. 3b for sample S10a, due at least in part to the broader detection window.

The correlation function under pulsed excitation carries more information. Actually, on-demand single-photon source needs to be characterized through pulsed spectroscopy. The presence of the characteristic time τ_i as a prefactor of the Laplace distributions which constitute the coincidence peaks, makes them less sensitive to the existence of a risetime. Although the exciton rise is extremely visible in the initial part of the decay signal, the coincidence peak is merely broadened. For the same reason, the slow component of the excitonic cascade significantly contributes to the plateaus, with a different value for the plateau around zero delay and for the plateau between coincidence peaks. Such a long component within the excitonic cascade signal is needed for the fit of S7. In sample S10a, it is hidden by the re-excitation process even if its value can be of the same order. A tentative attribution to dark excitons should be checked at slightly higher temperature, where this channel is expected to acquire significant values [19]. In the present data at low temperature, the contribution is small and we cannot exclude an artefact from a long tail of the APD response [33]. Again, as in CW, we did not need to introduce a biexciton contribution to a zero-delay correlation peak, which should be of the order of $\frac{I_{XX}}{I_X}$ where I_{XX} is the leak of biexciton signal at the exciton energy [44], too low to be detected due to the large binding energy from the spectra in Figs. 2a and c.

The main difference between the two samples is the presence of a large density ($\frac{A_R}{A_1} \simeq 1$) of deep ($\tau_R = 8$ ns) traps in S10a: The X-signal is mostly fed by traps, so that the integrated spectrum displays a X-line stronger

than XX. The direct excitation dominates for S7, and there is only a trace of re-excitation, with a low value of $\frac{A_R}{A_1} = 0.05$ and a contribution of a few % to the coincidence count. In addition, the value of the time constant, $\tau_R = 1$ ns, suggests free carriers or at most shallow traps, or neighbouring QDs. In both cases the characteristic time of the re-excitation cycle, τ , was kept equal to the exciton lifetime τ_1 . Re-excitation can be minimized by resonant excitation [1] [39] or even better by two-photon excitation of the biexciton [45]. Note that the deep traps of S10a are not related to the structural defects due to the low-temperature growth since traps are also observed (not shown) in an intermediate sample with 10s QD and shell as in S7, grown at 320°C with no Mg.

When applied to examples from the literature, the present calculation reproduces satisfactorily the presence of a significant re-excitation with a characteristic time τ in the sub-ns range, much shorter than the exciton lifetime $\tau = 1.5$ ns in Ref. [17]. In Refs. [16] and [39], no re-excitation is visible but a slow signal (slow component, dark-exciton type) is clearly evidenced at the center of the coincidence plot. The model is easily extended in order to include the possibility of stray photons from the excitonic cascade, for instance biexciton photons detected within the window around the single exciton [44].

To sum up, by making explicit the link between a description of the time-dependence of the photoluminescence signal by exponential functions, and the description of the coincidence count by Laplace-distributions which follows, we reveal different aspects of the dynamics of the excitons in a QD. The time-dependence of the photoluminescence signal brings a more direct information on the fast processes, and helps in determining the conditions for achieving the on-demand regime of single-photon emission. The coincidence count is highly sensitive to slow processes such as the influence of the dark exciton, to re-excitation processes, and of course to the single-photon character of the emission. This approach was applied here to CdSe QDs inserted in tapered ZnSe nanowires, so that their photoluminescence can be excited and recorded in a confocal configuration along the nanowire axis. These QDs emit in the blue-green range adapted for undersea quantum communication. Flat QDs exhibit a large splitting, 22 meV, between the exciton line and the biexciton line, thus increasing the purity of the single-photon emitter. The observed linewidths are smaller than previously achieved in CdSe QDs in nanowires and in self-assembled CdSe QDs. The role of re-excitation is clearly evidenced in the $g^{(2)}(t)$ curve around $t = 0$ and is quantified thanks to the phenomenological analytical approach. More generally, this phenomenological approach is extremely helpful in identifying the mechanisms limiting the purity of single-photon emitters.

ACKNOWLEDGMENTS

SRG acknowledges the European Union Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 754303 (GRENoble QUantum Engineering). The authors thank the CEA "Programme Exploratoire Bottom-Up" for financial support. We benefitted from the access to the nano characterization platform (PFNC) in CEA Minatec Grenoble.

Appendix A: Details of the calculation

The starting point is the probability of the difference between two variables t_1 and t_2 , each having an exponential distribution $f_i(t_i) = \frac{1}{\tau_i} \exp(-t_i/\tau_i)$ for $t_i > 0$ and 0 for $t_i < 0$. This joint density is described by the asymmetric Laplace distribution,

$$\begin{aligned} f_L(t) &= \int_0^\infty f_1(t_1) dt_1 \int_0^\infty f_2(t_2) dt_2 \delta(t_2 - t_1 - t) \\ &= \frac{1}{\tau_1 + \tau_2} \exp(t/\tau_1), t < 0 \\ &= \frac{1}{\tau_1 + \tau_2} \exp(-t/\tau_2), t > 0. \end{aligned} \quad (\text{A1})$$

The Laplace distribution is peaked at $t = 0$, with a characteristic constant τ_1 on the negative side and τ_2 on the positive side.

The calculation of Eq. 6 and 7 involves essentially two modifications with respect to this simple case: (1) The exponential distributions are repeated at each multiple of T_0 (which induces Laplace-type peaks at each nT_0

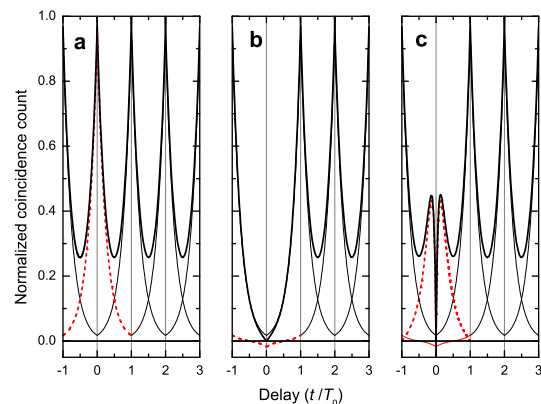


FIG. 6. (a) $C_{1B}(t) + C_{B1}(t)$ contribution, normalized, with $\tau_1 = \frac{T_0}{4}$ and $\tau_B = \infty$ (thick solid curve); the red dashed curve is the Laplace distribution peaked at $t = 0$, the thin solid curves are the other Laplace distributions; (b) $C_{11}(t)$ with $\tau_1 = \frac{T_0}{4}$; the Laplace distribution centered at $t = 0$ is replaced by the contribution shown by the red dashed curve; (c) $C_{RR}(t)$ with $\tau_R = \frac{T_0}{4}$ and $\tau = \frac{T_0}{10}$; the additional contribution is shown by the red dashed curve.

and renormalization factors), and (2) a special treatment must be applied to the first interval $t_2 \in [0, T_0]$, which implies a special treatment for $t \in [-T_0, T_0]$.

values of t . A straightforward calculation leads to:

$$C(t) = \sum_{i,j} C_{ij}(t) \quad (\text{A2})$$

As $C(t)$ is an even function of t we consider positive

with the $C_{ij}(t)$ as follows.

In an interval $t \in [nT_0, (n+1)T_0]$ with $n > 0$ an integer,

$$\begin{aligned} C_{ij}(t) + C_{ji}(t) &= A_i A_j \frac{\tau_i \tau_j}{\tau_i + \tau_j} \left[\exp\left(-\frac{t - nT_0}{\tau_i}\right) + \exp\left(\frac{t - (n+1)T_0}{\tau_i}\right) \right] \left[1 - \exp\left(-\frac{T_0}{\tau_j}\right) \right] \\ &+ A_i A_j \frac{\tau_i \tau_j}{\tau_i + \tau_j} \left[\exp\left(-\frac{t - nT_0}{\tau_j}\right) + \exp\left(\frac{t - (n+1)T_0}{\tau_j}\right) \right] \left[1 - \exp\left(-\frac{T_0}{\tau_i}\right) \right] \end{aligned} \quad (\text{A3})$$

for $i, j = 1$ to 3, R and B , including the diagonal terms C_{ii} . We recognize in the first line the right-hand side of Laplace distribution with characteristic time τ_i peaked at nT_0 , followed by the left-hand side of the same distribution peaked at $(n+1)T_0$. Note also that the time constants enter the contribution to $C(t)$ as prefactors, so that the long-lived contributions will be enhanced in the coincidence count.

The same expression holds in the first interval, $t \in [0, T_0]$, for coincidences involving the (non-correlated) background contribution:

$$\begin{aligned} C_{iB}(t) + C_{Bi}(t) &= A_i A_B \frac{\tau_i \tau_B}{\tau_i + \tau_B} \left[\exp\left(-\frac{t}{\tau_i}\right) + \exp\left(\frac{t - T_0}{\tau_i}\right) \right] \left[1 - \exp\left(-\frac{T_0}{\tau_B}\right) \right] \\ &+ A_i A_B \frac{\tau_i \tau_B}{\tau_i + \tau_B} \left[\exp\left(-\frac{t}{\tau_B}\right) + \exp\left(\frac{t - T_0}{\tau_B}\right) \right] \left[1 - \exp\left(-\frac{T_0}{\tau_i}\right) \right] \end{aligned} \quad (\text{A4})$$

for $i = 1$ to 3, including the diagonal term C_{BB} .

The coincidence count $C(t)$ thus contains Laplace distributions peaked at each nT_0 . As an example, Fig. 6a shows, for $(C_{1B} + C_{B1})$, the Laplace distribution centered at $t = 0$ (red dashed line), specific to the background contributions, and the other ones at non-zero nT_0 (thin black line), relevant for all contributions. The coincidence count is the sum of all these contributions (thick black line). It keeps finite values between two peaks if the time constants are not infinitely small with respect to T_0 .

The expression in $[0, T_0]$ is different for the coincidences involving the QD exciton cascade and the re-excitation. The Laplace distribution centered at $t = 0$ disappears, and additional terms ensure that the contributions to $C(t)$ identically vanish at $t = 0$.

For the excitonic cascade in $[0, T_0]$:

$$C_{ij}(t) + C_{ji}(t) = A_i A_j \frac{\tau_i \tau_j}{\tau_i + \tau_j} \left[\exp\left(\frac{t - T_0}{\tau_i}\right) - \exp\left(-\frac{t}{\tau_i} - \frac{T_0}{\tau_j}\right) + \exp\left(\frac{t - T_0}{\tau_j}\right) - \exp\left(-\frac{t}{\tau_j} - \frac{T_0}{\tau_i}\right) \right] \quad (\text{A5})$$

for $i, j = 1$ to 3, including the diagonal terms C_{ii} . This can be rewritten as:

$$\begin{aligned} C_{ij}(t) + C_{ji}(t) &= A_i A_j \frac{\tau_i \tau_j}{\tau_i + \tau_j} \left\{ \exp\left(\frac{t - T_0}{\tau_i}\right) \left[1 - \exp\left(-\frac{T_0}{\tau_j}\right) \right] + \exp\left(\frac{t - T_0}{\tau_j}\right) \left[1 - \exp\left(-\frac{T_0}{\tau_i}\right) \right] \right\} \\ &+ A_i A_j \frac{\tau_i \tau_j}{\tau_i + \tau_j} 2 \left\{ \sinh\left(\frac{t - T_0/2}{\tau_i}\right) \exp\left(-\frac{T_0}{2\tau_j}\right) + \sinh\left(\frac{t - T_0/2}{\tau_j}\right) \exp\left(-\frac{T_0}{2\tau_i}\right) \right\} \exp\left(-\frac{T_0}{2\tau_i}\right) \exp\left(-\frac{T_0}{2\tau_j}\right) \end{aligned} \quad (\text{A6})$$

which evidences in the first line the left-hand side of the Laplace distributions centered at $t = T_0$, and in the second line an additional contribution which ensures vanishing at $t = 0$ (shown as a red dashed line in Fig. 6b for $C_{11}(t)$). This differs from the mere suppression of the central peak [39].

Finally, the re-excitation contributions comprise another additional term:

$$\begin{aligned} C_{iR}(t) + C_{Ri}(t) &= A_i A_R \frac{\tau_i \tau_R}{\tau_i + \tau_R} \left\{ \exp\left(\frac{t - T_0}{\tau_i}\right) \left[1 - \exp\left(-\frac{T_0}{\tau_R}\right) \right] + \exp\left(\frac{t - T_0}{\tau_R}\right) \left[1 - \exp\left(-\frac{T_0}{\tau_i}\right) \right] \right\} \\ &+ A_i A_R \frac{\tau_i \tau_R}{\tau_i + \tau_R} 2 \left\{ \sinh\left(\frac{t - T_0/2}{\tau_i}\right) \exp\left(-\frac{T_0}{2\tau_R}\right) + \sinh\left(\frac{t - T_0/2}{\tau_R}\right) \exp\left(-\frac{T_0}{2\tau_i}\right) \right\} \exp\left(-\frac{T_0}{2\tau_i}\right) \exp\left(-\frac{T_0}{2\tau_R}\right) \\ &+ A_i A_R \frac{\tau_i \tau_R}{\tau_i + \tau_R} \left[1 - \exp\left(-\frac{t}{\tau}\right) \right] \left[\exp\left(-\frac{t}{\tau_R}\right) - \exp\left(\frac{t - T_0}{\tau_i} - \frac{T_0}{\tau_R}\right) \right] \exp\left(\frac{T_0}{2\tau_i}\right) \end{aligned}$$

for $i = 1$ to 3, and including the diagonal terms C_{RR} . The additional term (third line) is shown in red in Fig. 6c for $C_{RR}(t)$. It appears essentially as a Laplace distribution centered at $t = 0$, with the contribution close to $t = 0$ cut by the re-excitation factor with characteristic time τ .

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