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A plethora of diffuse steep spectrum radio sources in Abell 2034 revealed by LOFAR

T. W. Shimwell,^{1★} J. Luckin,^{1,2} M. Brüggen,³ G. Brunetti,⁴ H. T. Intema,^{1,5}
M. S. Owers,^{6,7} H. J. A. Röttgering,¹ A. Stroe,^{1,8} R. J. van Weeren,⁹
W. L. Williams,^{1,10} R. Cassano,⁴ F. de Gasperin,^{1,3} G. H. Heald,^{10,11†} D. N. Hoang,¹
M. J. Hardcastle,¹² S. S. Sridhar,^{10,11} J. Sabater,¹³ P. N. Best,¹³ A. Bonafede,³
K. T. Chyży,¹⁴ T. A. Enßlin,¹⁵ C. Ferrari,¹⁶ M. Haverkorn,^{17,1} M. Hoeft,¹⁸
C. Horellou,¹⁹ J. P. McKean,^{10,11} L. K. Morabito,¹ E. Orrù,^{10,17} R. Pizzo,¹⁰
E. Retana-Montenegro¹ and G. J. White^{20,21}

Affiliations are listed at the end of the paper

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ABSTRACT

With Low-Frequency Array (LOFAR) observations, we have discovered a diverse assembly of steep spectrum emission that is apparently associated with the intracluster medium (ICM) of the merging galaxy cluster Abell 2034. Such a rich variety of complex emission associated with the ICM has been observed in few other clusters. This not only indicates that Abell 2034 is a more interesting and complex system than previously thought but it also demonstrates the importance of sensitive and high-resolution, low-frequency observations. These observations can reveal emission from relativistic particles which have been accelerated to sufficient energy to produce observable emission or have had their high energy maintained by mechanisms in the ICM. The most prominent feature in our maps is a bright bulb of emission connected to two steep spectrum filamentary structures, the longest of which extends perpendicular to the merger axis for 0.5 Mpc across the south of the cluster. The origin of these objects is unclear, with no shock detected in the X-ray images and no obvious connection with cluster galaxies or AGNs. We also find that the X-ray bright region of the cluster coincides with a giant radio halo with an irregular morphology and a very steep spectrum. In addition, the cluster hosts up to three possible radio relics, which are misaligned with the cluster X-ray emission. Finally, we have identified multiple regions of emission with a very steep spectral index that seem to be associated with either tailed radio galaxies or a shock.

Key words: acceleration of particles – radiation mechanisms: non-thermal – shock waves – galaxies: clusters: individual: Abell 2034 – galaxies: clusters: intracluster medium – radio continuum: general.

1 INTRODUCTION

Diffuse synchrotron emission associated with ultrarelativistic particles and magnetic fields in the intracluster medium (ICM) primarily consists of radio haloes and radio relics (see Ferrari et al. 2008; Brüggen et al. 2012; Feretti et al. 2012; Brunetti & Jones 2014

for recent reviews). It is thought that radio haloes are caused by cluster-wide post-merger turbulence (see e.g. Brunetti et al. 2001; Petrosian 2001), secondary electrons from proton–proton interactions (see e.g. Dennison 1980; Blasi & Colafrancesco 1999) or a combination of the two mechanisms (see Brunetti & Blasi 2005; Brunetti & Lazarian 2011; Pinzke, Oh & Pfrommer 2015), whereas radio relics are apparently associated with localized, post-merger shock-fronts (Ensslin et al. 1998). However, the non-detection of gamma-ray emission by the *Fermi* satellite (see e.g. Brunetti et al. 2012; Zandanel & Ando 2014; Ackermann et al. 2015) disfavours a purely hadronic model for the origin of radio haloes and

* E-mail: shimwell@strw.leidenuniv.nl

† Current address: CSIRO Astronomy, Space Science, 26 Dick Perry Avenue, Kensington, Perth WA 6151, Australia.

challenges standard diffuse shock acceleration to explain radio relics (see e.g. Brunetti & Jones 2014; Vazza & Brüggén 2014). Additionally, the variety of the observed properties of cluster-scale radio emission is becoming increasingly difficult to describe within the current theoretical picture. For example: whilst in the ‘Sausage’ cluster (CIZA J2242.8+5301) van Weeren et al. (2010) observe a textbook example of an arc-like radio relic related to a shock; in ZwCl 2341.1+000 Ogren et al. (2014) observe no X-ray shock at the position of a relic, and in the Bullet cluster (Shimwell et al. 2015), PLCKG287.0+32.9 (Bonafede et al. 2014b) and the Coma cluster (Ensslin et al. 1998) an apparent link is seen between radio galaxies and radio relics. Furthermore, whilst radio haloes are statistically detected in merging clusters (e.g. Cassano et al. 2013), the role of the cluster mass and its dynamical state is difficult to disentangle with current observations (see Cuciti et al. 2015). For example, in CL1821+643 Bonafede et al. (2014a) detect a giant radio halo in a cool core cluster with no obvious merging activity and Russell et al. (2011) observe no diffuse radio emission in Abell 2146, which is a less massive cluster, but a clear merging system. Recently upgraded and new facilities have significantly improved sensitivity to diffuse radio emission from the ICM and are already beginning to reveal increasingly complex phenomena (e.g. Owen et al. 2014) which may shed light on the connection between haloes and relics and further challenge a univocal interpretation of these sources. One such instrument is the Low-Frequency Array (LOFAR; van Haarlem et al. 2013) which can produce deep, high-resolution, high fidelity, low-frequency radio images.

In this publication, we present 118–166 MHz LOFAR observations of Abell 2034, which is a galaxy cluster with known diffuse radio emission and good multiwavelength data sets. Previous studies of this cluster have revealed that Abell 2034 is a massive cluster, with velocity measurements of the member galaxies by Owers et al. (2014) implying a mass of $M_{200} = 1.1 \pm 0.4 \times 10^{15} M_{\odot}$ (where r_{200} is equal to 2.1 Mpc) and Sunyeav Zel’dovich measurements by the Planck Collaboration XXXII (2015) suggesting that $M_{500} = 4.19 \pm 0.4 \times 10^{14} M_{\odot}$ (where r_{500} is equal to 1.16 Mpc). The luminosity of the cluster is also high ($L_{X,0.1-2.4\text{keV}} = 3.51 \times 10^{44} \text{ erg s}^{-1}$; Piffaretti et al. 2011) and the Sunyeav Zel’dovich signal is strong (the Arcminute Microkelvin Imager and Planck measured Y_{500} to be 24 ± 14 and 33 ± 6 , respectively; Planck Collaboration II 2013; Perrott et al. 2015). Abell 2034 is a clear merging system with multiple mass concentrations (Okabe & Umetsu 2008; van Weeren et al. 2011; Owers et al. 2014) and a patchy temperature distribution (Kempner, Sarazin & Markevitch 2003; Owers et al. 2014). The most recent X-ray and optical study by Owers et al. (2014) led to the discovery of a weak shock with Mach number $M = 1.59^{+0.06}_{-0.07}$ at the northern edge of the cluster. Owers et al. (2014) concluded that the merger axis is within $\sim 23^{\circ}$ of the plane of the sky and that the two main components are now moving along the north–south direction ~ 0.3 Gyr after the core passage. Radio observations by Kempner & Sarazin (2001), Rudnick & Lemmerman (2009), Giovannini et al. (2009) and van Weeren et al. (2011) have revealed faint diffuse emission in the X-ray bright region of the cluster which is slightly enhanced in the vicinity of the X-ray-detected shock. The nature of this emission is still disputed and it remains uncertain whether it should be classified as a radio halo, radio relic or both. Additional diffuse radio emission was identified by van Weeren et al. (2011), who classified a radio source far from the X-ray bright region in the western periphery of the cluster as a small radio relic.

The primary aim of this low-frequency study of Abell 2034 is to search for previously unseen radio emission, to offer insights into

the debate regarding the nature of the emission at the low Mach number shock front, and to assess the influence of the shock on that emission. We also aim to take advantage of the existing auxiliary data and the excellent sensitivity of our LOFAR data to steep-spectrum diffuse emission to examine whether there are interactions between the prominent radio sources in this cluster and the diffuse radio emission that appears to be associated with the ICM.

Hereafter, we assume a concordance Λ CDM cosmology, with $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$ and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. At the redshift of the Abell 2034 ($z = 0.1132$; Owers et al. 2014), the luminosity distance is 526 Mpc and 1 arcsec corresponds to 2.06 kpc. We use $S_{\nu} \propto \nu^{\alpha}$, where S_{ν} is the flux density and α is the spectral index. All coordinates are given in J2000.

2 OBSERVATIONS AND DATA REDUCTION

2.1 LOFAR

We used the LOFAR High Band Antenna (HBA) in HBA_DUAL_INNER mode to observe the galaxy cluster Abell 2034 on 2014 April 26 (observation ID L221519). Our observations were performed during the nighttime, centred on 15:10:10.8 +33:30:21.6, and 8 h in duration. We observed the bright and well-characterized calibrator source 3C295 for 25 min prior to the observation of our target. Both the target and the calibrator data were taken with frequency coverage from 118 to 190 MHz. The data were recorded with 1 s sampling and 64 channels per 0.195 MHz sub band. These high spectral and time resolution data were flagged for interference by the observatory with AOFLAGGER (Offringa, van de Gronde & Roerdink 2012) before being averaged to 5 s sampling and 4 channels per sub band. Only these averaged data sets were stored in the LOFAR archive and the raw data were deleted. The observations are summarized in Table 1.

The calibration and imaging procedure mimics the facet calibration scheme that is thoroughly described by van Weeren et al. (2016a) and Williams et al. (2016). In this procedure, the calibration is performed in two stages: we first complete a direction independent calibration of the data before calibrating individual facets to remove time and position varying station beam errors and ionospheric effects. The procedure is briefly summarized below.

In the direction independent calibration step, we initially averaged our 3C295 data to 10 s and 2 channels per sub band, flag bad antenna stations (CS103HBA0 and CS501HBA1 leaving 43 core stations and 14 remote stations) and interference (all frequencies above 166 MHz were removed completely). The XX and YY gains, as well as the rotation angle (to account for differential Faraday Rotation), were determined from calibrating the 3C295 data off a simple two point source model. From these calibration solutions the clock offsets for different antenna stations were then determined. The amplitude and the clock solutions were transferred to the target data before the target data were phase calibrated using a sky model generated from the VLA Low-Frequency Sky Survey (Lane et al. 2014), Westerbork Northern Sky Survey (WENSS; Rengelink et al. 1997) and the NRAO/VLA Sky Survey (NVSS; Condon et al. 1998) – see The LOFAR Imaging Cookbook¹ for details. All VLSS sources within 5 deg of the pointing centre with a flux greater than 1 Jy were included in the phase calibration catalogue and these sources are matched with WENSS and NVSS sources to include the spectral properties of the sources in the phase calibration catalogue.

¹ <https://www.astron.nl/radio-observatory/lofar/lofar-imaging-cookbook>

Table 1. A summary of our LOFAR observations towards Abell 2034.

Coordinates	15:10:10.8 33:30:21.6
Amplitude calibrator	3C295
Frequency range	118–190 MHz (118–166 MHz used)
Spectral resolution	0.048 75 MHz
Time resolution	5 s
On-source integration time	8 h
Image RMS	190 $\mu\text{Jy beam}^{-1}$ at 7 arcsec \times 5 arcsec resolution 210 $\mu\text{Jy beam}^{-1}$ at 12 arcsec \times 10 arcsec resolution 350 $\mu\text{Jy beam}^{-1}$ at 22 arcsec \times 19 arcsec resolution 425 $\mu\text{Jy beam}^{-1}$ at 38 arcsec \times 37 arcsec resolution

In the direction-dependent calibration step our aim is to accurately image Abell 2034, all the emission from which lies within ≈ 15 arcmin of the pointing centre. To achieve this, we must minimize the contamination from bright and nearby sources and correct for the ionospheric and beam errors in the direction of the cluster. The number of directions we must use in the calibration is far fewer than used by e.g. Williams et al. (2016) because their aim was to create a wide-field (19 deg²) thermal noise limited image. We selected 13 directions away from the cluster and for each of these we performed direction-dependent calibration to obtain good sky models and calibration solutions for each direction. The sources in each direction were progressively removed using the good sky models and direction-dependent calibration solutions until just the emission from the region of the cluster was left in the data. As the emission from the cluster is complex, we choose not to do direction dependent calibration directly on this object. Instead, we copied the calibration solutions obtained from a pair of nearby sources (FIRST J150909.6+340508 and FIRST J151007.0+335121) to the facet containing Abell 2034. These sources are separated from the cluster by just ≈ 30 arcmin so the ionospheric effects should be similar to those at the pointing centre.

After our data for Abell 2034 were corrected for ionospheric and beam errors, the data were imaged in *CASA*² using the multiscale multiscale deconvolution algorithm (Rau & Cornwell 2011). When necessary, the resulting images can be corrected for primary beam attenuation in the image plane by dividing out the primary beam using a beam model obtained from *awimager* (Tasse et al. 2013). However, the emission from Abell 2034 is within the 99 per cent power point of the primary beam and such a correction is not required for this study. In the imaging procedure, the images were CLEANED to a depth of 0.5 mJy beam⁻¹ with deconvolution scale sizes equal to zero (point source), 3, 7, 9, 25, 60 and 150 times the pixel size, which is approximately a sixth of the synthesized beam (see Table 1). The robust parameter within the Briggs (1995) weighting scheme was set to -0.75 to apply a more uniform weighting to visibilities across the *uv*-plane and decrease the sidelobes, and a Gaussian taper was applied to reduce the weight of the data from the long baselines to enhance the diffuse emission. This procedure was performed to create full-bandwidth (118–166 MHz) Stokes *I* images. The data were imaged with various Gaussian tapers to examine how its observed structure changes as the synthesized beam FWHM is varied from varied from 5 to 40 arcsec. An example of a medium-resolution 118–166 MHz LOFAR image is shown in Fig. 1 and the properties of the different resolution images are summarized in Table 1.

To determine the uncertainty in our absolute flux calibration we compared fluxes measured from our narrow-band, low-resolution

(≈ 25 arcsec), wide-field, 151 MHz primary beam corrected image of Abell 2034 to those recorded in the 151 MHz LOFAR Multifrequency Snapshot Sky Survey preliminary catalogue (MSSS; Heald et al. 2015). In total, we compared the fluxes of nine sources, which were selected because they are bright (signal to noise greater than 10 in both images), isolated (no other detected sources within 2 arcmin in the Abell 2034 image), compact (≤ 30 arcsec in the Abell 2034 image) and within 2° of Abell 2034. We found that the median ratio of peak fluxes was 0.9 and for integrated fluxes it was 1.0, with the MSSS peak flux being higher than that in the Abell 2034 image. The scatter in the flux ratios was low, with the standard deviation of the ratio of peak fluxes found to be 0.16 and the standard deviation of the total fluxes equal to 0.15. Throughout this publication, we therefore adopt a 15 per cent absolute flux calibration error on our LOFAR images.

2.2 Spectral index maps and integrated spectrum calculations

Abell 2034 was previously observed with the Giant Metrewave Radio Telescope (GMRT) at 610 MHz and the Westerbork Synthesis Radio Telescope (WSRT) at 1.4 GHz (van Weeren et al. 2011b). We use these existing WSRT and GMRT images, together with LOFAR images, to create high resolution 150–610 MHz and low resolution 150 MHz to 1.4 GHz spectral index images. To measure the same spatial scales, for images used to create the 150–610 MHz and the 150 MHz to 1.4 GHz spectral index images we applied the observed GMRT and WSRT inner and outer *uv*-ranges to our LOFAR data during the imaging. These ranges were 102λ to $52.8k\lambda$ and 249λ to $12.4k\lambda$ for the GMRT and WSRT, respectively. When imaging the LOFAR data, we also weighted the visibilities such that the LOFAR images were of comparable resolution to the GMRT and WSRT images. For the LOFAR image used to create the 150–610 MHz spectral index image we used a robust parameter of -0.75 which provided a resolution of 6.4 arcsec \times 4.4 arcsec which is comparable to the GMRT image resolution of 6.8 arcsec \times 4.3 arcsec. Whereas, for the LOFAR image used to create the 150 MHz to 1.4 GHz spectral index image we used a robust parameter of $+0.4$ to obtain a resolution of 26 arcsec \times 23 arcsec, which was chosen because it is comparable to the WSRT image resolution of 30 arcsec \times 16 arcsec. Whilst the weighting we have used in our imaging strategy does partially compensate for the different distribution of visibilities on the *uv*-plane of the GMRT, WSRT and LOFAR observations (see Fig. 2), a more accurate comparison would be to match the *uv*-coverages as closely as possible or to use uniform weighting over the *uv*-plane. However, our approach was used because it provides better sensitivity to the large scale emission from Abell 2034. The pair of images used for each spectral index map were convolved with a Gaussian to produce images with exactly the same resolution which were regridded to have the same pixel size. The resulting

² <http://casa.nrao.edu/>

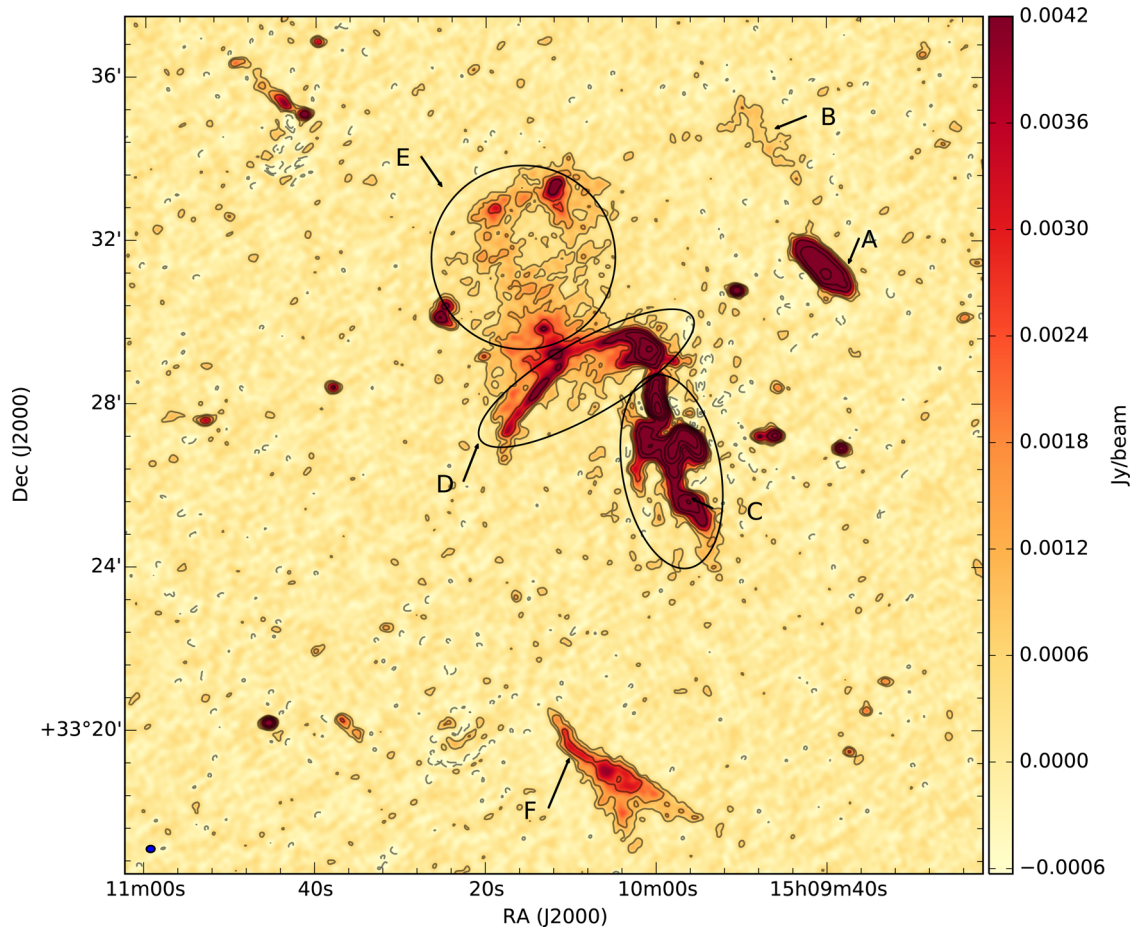


Figure 1. A medium-resolution (12 arcsec \times 10 arcsec) 118–166 MHz Stokes I image towards Abell 2034 with six regions of interest highlighted. The LOFAR contours show the (1, 2, 4, ...) \times $3 \times \sigma_{\text{LOFAR}, 10 \text{ arcsec}}$ levels where $\sigma_{\text{LOFAR}, 10 \text{ arcsec}} = 210 \mu\text{Jy beam}^{-1}$.

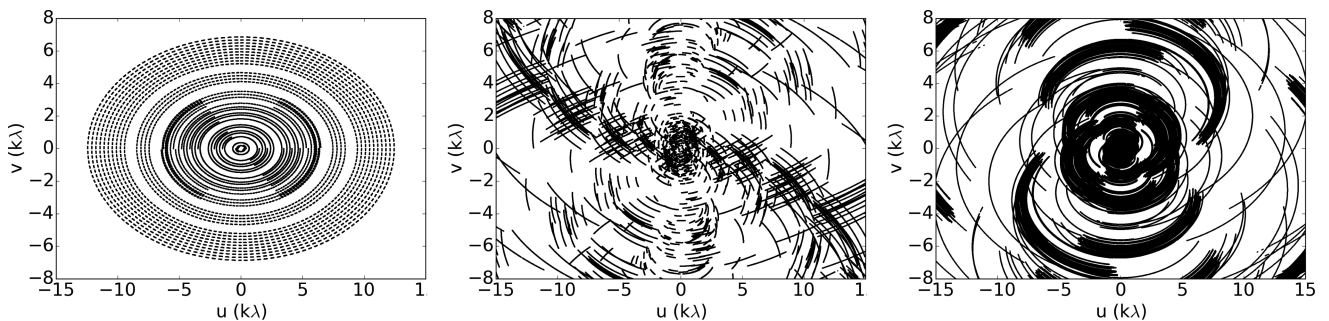


Figure 2. The monochromatic uv -coverage of the 1.4 GHz WSRT (left), 610 MHz GMRT (centre) and 150 MHz LOFAR (right) observations of Abell 2034. This figure shows the entire WSRT uv -coverage but the GMRT and LOFAR coverage extends to $53k\lambda$ and $60k\lambda$, respectively. Here the monochromatic coverage has been presented for display purposes but the full bandwidth used in each observation (160 MHz for WSRT, 32 MHz for GMRT and 48 MHz for LOFAR) provides considerable additional filling of the uv -plane.

31 arcsec 150 MHz and 1.4 GHz and the 7.8 arcsec 150 MHz and 610 MHz images were then used to create spectral index (α) maps where a power-law spectral index was calculated for each pixel (3.3 arcsec). The error on the fit was calculated given the error on the GMRT or WSRT and LOFAR pixel values ($S_{1, \text{err}}$ and $S_{2, \text{err}}$) with

$$\alpha_{\text{err}} = \frac{1}{\ln \frac{v_1}{v_2}} \sqrt{\left(\frac{S_{1, \text{err}}}{S_1}\right)^2 + \left(\frac{S_{2, \text{err}}}{S_2}\right)^2}, \quad (1)$$

where S_1, S_2, v_1 and v_2 are the 150 MHz and the 610 MHz or 1.4 GHz pixel values and frequency values, respectively. The standard deviation of pixels ($S_{2, \text{err}}$) that was measured on the GMRT image in the region of the cluster was $90 \mu\text{Jy beam}^{-1}$ and in the high-resolution LOFAR image we measured a noise ($S_{1, \text{err}}$) of $185 \mu\text{Jy beam}^{-1}$. For the GMRT and the LOFAR images, the noise is approximately constant in the region of interest. The standard deviation of pixels ($S_{2, \text{err}}$) that was measured close to the centre of the input WSRT image was $58 \mu\text{Jy beam}^{-1}$ and the errors put into our spectral index analysis were $58 \mu\text{Jy beam}^{-1}$ divided by the primary beam

attenuation of $\cos^6(c \times \nu \times r)$ where c is a constant equal to 68 (see section 5.1 of the Guide to Observations with the WSRT revision 2 dated 2010-07-20), ν is the observing frequency in GHz and r is the radius in degrees. The low-resolution LOFAR image has a constant noise level ($S_{1, \text{err}}$) of $350 \mu\text{Jy beam}^{-1}$ in the region of interest. In the GMRT, WSRT and LOFAR images, we are sensitive to sufficiently large spatial scales (8 arcmin at for the WSRT and 20 arcmin for the GMRT assuming that the maximum recoverable scale is $0.6 \times \lambda/D$) to not resolve out any of the cluster emission up to 1 Mpc scales, but due to the significant differences in the LOFAR, GMRT and WSRT uv -coverages (see Fig. 2) we urge caution when interpreting the Mpc scale emission in our spectral index images and we stress that further multifrequency observations are required to improve the spectral characterization of this cluster.

We calculated the uncertainty on our integrated flux density measurements for extended sources by adding in quadrature an absolute flux calibration error with the error on the integrated flux density derived from the image noise. We used absolute flux calibration errors of 5 per cent for WSRT (as in e.g. van Weeren et al. 2012), 10 per cent for GMRT (see e.g. Chandra, Ray & Bhatnagar 2004) and 15 per cent for LOFAR (see Section 2.1).

3 RESULTS

In Fig. 3, we present a LOFAR 118–166 MHz image of Abell 2034 which is at a resolution of $38 \text{ arcsec} \times 37 \text{ arcsec}$ and reaches a noise level of $425 \mu\text{Jy beam}^{-1}$. We have overlaid this image on the *Chandra* X-ray image from Owers et al. (2014) to show the correspondence between the X-ray and radio emission. A higher resolution ($7 \text{ arcsec} \times 5 \text{ arcsec}$) LOFAR image of the same region with a noise level of $190 \mu\text{Jy beam}^{-1}$ is presented in Fig. 4 and overlaid on an SDSS *r*-band image with known cluster members that were identified in the redshift-radius phase-space by Owers et al. (2014) highlighted. We present the high-resolution (7.8 arcsec) 150–610 MHz and low-resolution 150 MHz–1.4 GHz spectral index images in Figs 5 and 6, respectively. The low-frequency LOFAR images are significantly more sensitive to the steep spectrum diffuse radio emission from the ICM than the existing 610 MHz GMRT and 1.4 GHz WSRT images which were presented (van Weeren et al. 2011). These deeper images have allowed us to discover new complex steep spectrum emission and characterize known objects in greater detail. In the LOFAR image, there are six main regions of diffuse emission associated with Abell 2034 which we have labelled in Fig. 1.

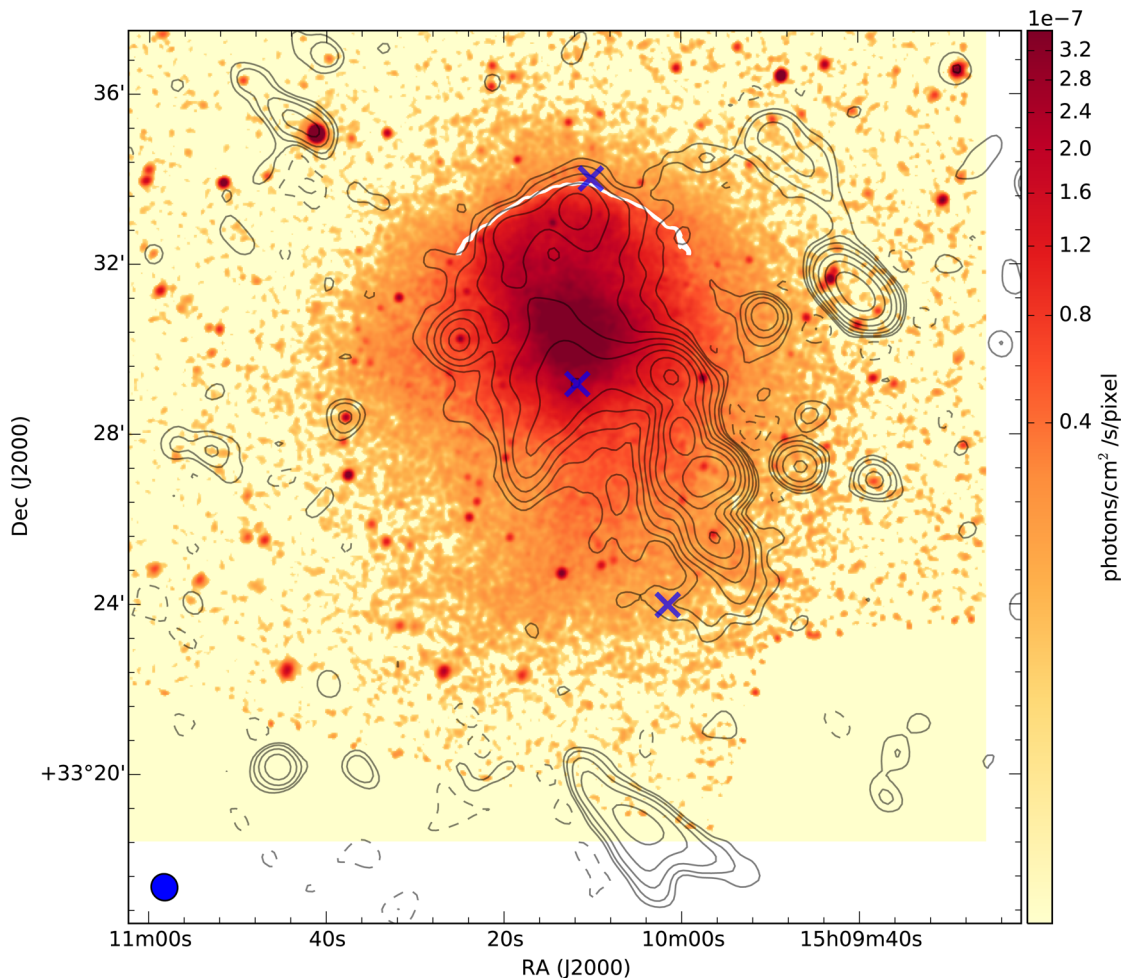


Figure 3. A low-resolution LOFAR image ($38 \text{ arcsec} \times 37 \text{ arcsec}$) overlaid on an exposure-corrected, and background-subtracted *Chandra* image in the 0.5–7.0 keV energy band with a total integration time of 250 ks. The high-resolution *Chandra* image (pixels of 1.968 arcsec) which was originally presented by Owers et al. (2014) has been smoothed with a Gaussian kernel with FWHM = 6 arcsec and the thick white contour shows the X-ray-detected shock front. The LOFAR contours show the $(1, 2, 4, \dots) \times 3 \times \sigma_{\text{LOFAR}, 40 \text{ arcsec}}$ levels where $\sigma_{\text{LOFAR}, 40 \text{ arcsec}} = 425 \mu\text{Jy beam}^{-1}$. The two northern crosses show the prominent BCG of the two main merging clusters and the southern cross shows the position of a local peak in the galaxy surface density which may correspond to a third cluster involved in the merging (Owers et al. 2014).

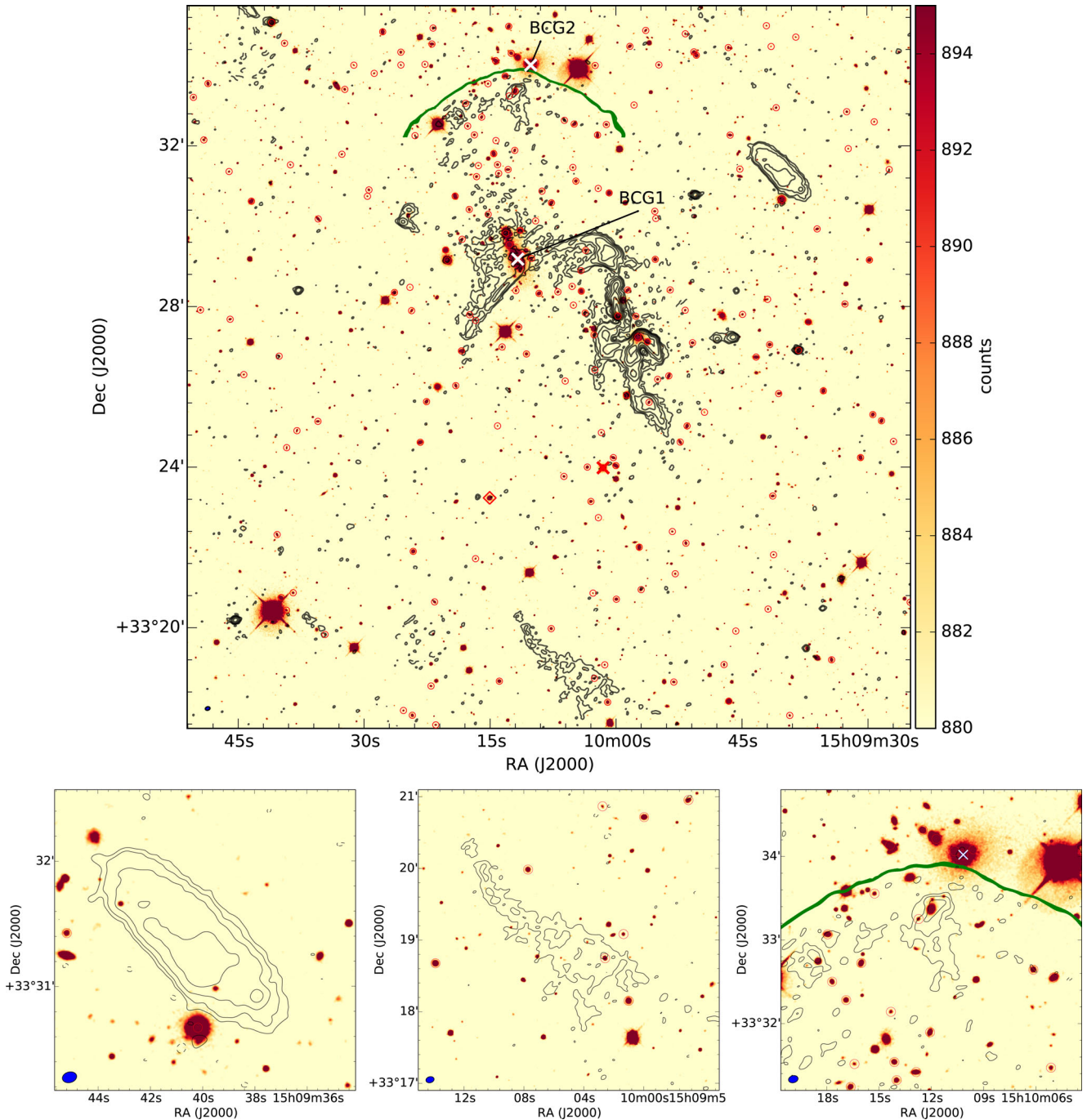


Figure 4. A high-resolution LOFAR image ($7 \text{ arcsec} \times 5 \text{ arcsec}$) overlaid on an SDSS r -band image. The top panel shows the entire region of the cluster and the bottom panels show three regions of interest in more detail. The circles indicate the likely cluster members (based on their location in the redshift-radius phase space) and the two northern crosses show the prominent BCG of the two main merging clusters which we have also labelled BCG1 and BCG2 (see Owers et al. 2014). A third, more southern, cross shows the position of a local peak in the galaxy surface density from Owers et al. (2014) which may correspond to the peak of a third cluster involved in the merging as was suggested by Kempner et al. (2003). The red diamond shows a cluster member which is discussed in Section 4.3 and the thick green contour shows the X-ray-detected shock front. The LOFAR contours show the $(1, 2, 4, \dots) \times 3 \times \sigma_{\text{LOFAR}, 5 \text{ arcsec}}$ levels where $\sigma_{\text{LOFAR}, 5 \text{ arcsec}} = 190 \mu\text{Jy beam}^{-1}$.

3.1 Diffuse source A

Using GMRT and WSRT radio images together with optical data sets, van Weeren et al. (2011) classified source A (centred at $15:09:40 +33:31:20$) as a small radio relic but also noted that the emission could be related to plasma from a nearby radio galaxy and that a more precise classification could be obtained

with polarimetric and resolved spectral index measurements. van Weeren et al. (2011) measured source A to have a size of $220 \text{ kpc} \times 75 \text{ kpc}$, a spectral index ≈ -1.2 and an integrated 1.382 GHz flux of $24 \pm 2 \text{ mJy}$, which, at the redshift of Abell 2034, corresponds to a 1.4 GHz radio power of $8.0_{-0.6}^{+0.7} \times 10^{23} \text{ W Hz}^{-1}$ with our adopted cosmology. From the low-resolution WSRT and LOFAR images

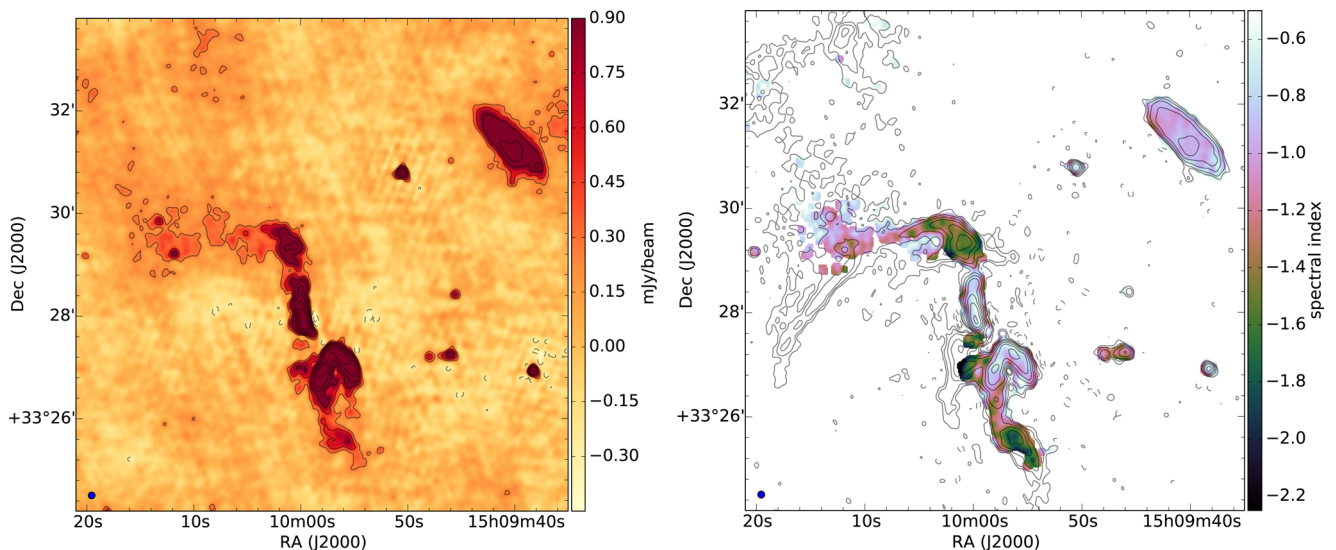


Figure 5. The 150 MHz to 610 MHz high-resolution ($7.8 \text{ arcsec} \times 7.8 \text{ arcsec}$) spectral properties of the emission from Abell 2034. Left: the 610 GHz GMRT image with contours at $(1, 2, 4, \dots) \times 3 \times \sigma_{\text{GMRT}, 8 \text{ arcsec}}$ where $\sigma_{\text{GMRT}, 8 \text{ arcsec}} = 90 \mu\text{Jy beam}^{-1}$. Right: the 150–610 MHz high-resolution spectral index image where pixels with errors greater than 0.3 have been blanked. The contours show a high-resolution ($7.8 \text{ arcsec} \times 7.8 \text{ arcsec}$) 150 MHz LOFAR image with levels at $(1, 2, 4, \dots) \times 3 \times \sigma_{\text{LOFAR}, 8 \text{ arcsec}}$ where $\sigma_{\text{LOFAR}, 8 \text{ arcsec}} = 185 \mu\text{Jy beam}^{-1}$. In both the 610 and 150 MHz images, the uv -range (102λ to $52.8k\lambda$) is the same and the maximum recoverable scale is $\approx 20 \text{ arcmin}$ which is sufficient to not resolve out any of the cluster emission but the resolution is high and the flux per pixel of the very low surface brightness structures is too low to be detected at high significance. The procedure for creating the GMRT and LOFAR images is outlined in Section 2.2.

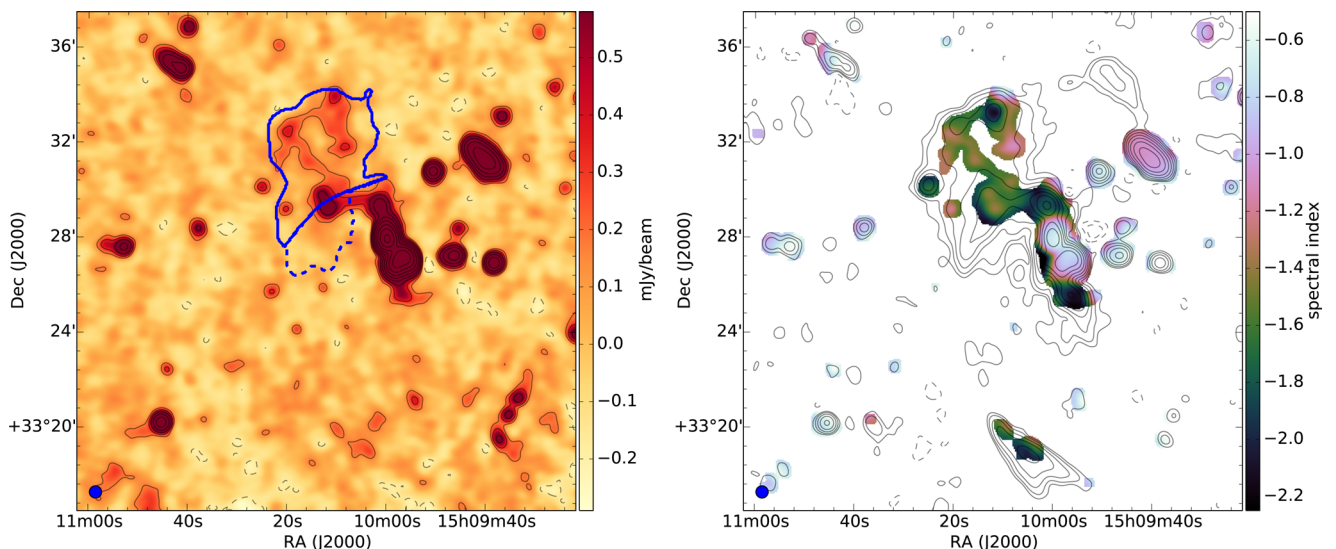


Figure 6. The 150 MHz to 1.4 GHz low-resolution ($31 \text{ arcsec} \times 31 \text{ arcsec}$) spectral properties of the emission from Abell 2034. Left: the 1.4 GHz WSRT image with black contours showing the $(1, 2, 4, \dots) \times 3 \times \sigma_{\text{WSRT}, 30 \text{ arcsec}}$ levels where $\sigma_{\text{WSRT}, 30 \text{ arcsec}} = 58 \mu\text{Jy beam}^{-1}$. The thick contours show the region used for integrated radio halo flux measurements (see Section 3.4). Right: the 150 MHz to 1.4 GHz low-resolution spectral index image where pixels with errors greater than 0.3 have been blanked. The contours show a low-resolution ($31 \text{ arcsec} \times 31 \text{ arcsec}$) 150 MHz LOFAR image with contour levels at $(1, 2, 4, \dots) \times 3 \times \sigma_{\text{LOFAR}, 30 \text{ arcsec}}$ where $\sigma_{\text{LOFAR}, 30 \text{ arcsec}} = 350 \mu\text{Jy beam}^{-1}$. In both the 150 MHz and 1.4 GHz images the uv -range (249λ to $12.4k\lambda$) is the same and the maximum recoverable scale is $\approx 8 \text{ arcmin}$ which is sufficient to not resolve out any of the cluster emission. The procedure for creating the WSRT and LOFAR images is outlined in Section 2.2.

presented in Fig. 6, we measure the integrated flux density of source A in the same region on both maps (defined as being above $4 \times \sigma_{\text{LOFAR}, 30 \text{ arcsec}}$) to be $S_{150 \text{ MHz}} = 310 \pm 47 \text{ mJy}$ and $S_{1.4 \text{ GHz}} = 28.5 \pm 1.5 \text{ mJy}$. This gives a spectral index measurement of $\alpha_{150-1400} = -1.07 \pm 0.07$. Similarly, from the high-resolution GMRT and LOFAR images (Fig. 5), we measure the integrated flux density (in the region with a 150 MHz flux density above $4 \times \sigma_{\text{LOFAR}, 8 \text{ arcsec}}$) to be $S_{150 \text{ MHz}} = 310 \pm 47 \text{ mJy}$ and $S_{610 \text{ MHz}} = 76.8 \pm 7.7 \text{ mJy}$

which corresponds to $\alpha_{150-610} = -0.99 \pm 0.13$. Both the minor and major axis of the source are well resolved in the high-resolution 150–610 MHz spectral index map (Fig. 5), which reveals a fairly uniform spectral index distribution with small variations giving it a slightly patchy appearance. The typical spectral index values range from -0.9 to -1.0 and we observe no obvious trend in the direction towards the cluster centre as may be expected for a radio relic. The spectral index measurements in the southwestern region are

flatter (≈ -0.7) but this area is likely contaminated by a faint point-like source which is visible in our highest resolution images (see Fig. 4). The 150 MHz to 1.4 GHz spectral index map (see Fig. 6) is in broad agreement with the higher resolution 150–610 MHz spectral index map, but due to the low resolution of the image and the contamination from the compact source in the southwestern region, it is difficult to accurately assess the resolved 150 MHz to 1.4 GHz spectral properties of source A.

3.2 Diffuse source B

The diffuse and very faint source B on the periphery of the cluster was previously undetected and is best displayed in our lower resolution LOFAR images (see Figs 3 or 6). The brightest part of the structure is located around 15:09:48 +33:34:43 and has a peak flux density exceeding 15 times the noise in our low-resolution images; it is orientated in a direction similar to source A and runs approximately parallel to the closest X-ray brightness edge. From our low-resolution image in Fig. 6 source B has an integrated 150 MHz flux of 32.0 ± 4.9 mJy (within the $4\sigma_{\text{LOFAR}, 30 \text{ arcsec}}$ contour) and its non-detection within the same region on the WSRT image of the same resolution implies a 3σ upper limit on the 1.4 GHz flux of 0.6 mJy allowing us to constrain its spectral index to be steeper than -1.8 . Although there are several cluster members within the region of diffuse emission (see Fig. 4), there is no obvious optical counterpart and no compact radio structure visible in our high-resolution low-frequency images. At three times the noise level of our low-resolution images we detect faint bridges of emission between this object, the northern edge of the candidate radio relic (source A) and the northwestern edge of the radio halo (source E). Because of the low significance of the detection of a faint bridge, its existence will need to be confirmed by deeper observations. In any case, based on the morphology, the lack of an optical counterpart and its location in the cluster periphery, the properties of this faint emission in region B are similar to those expected for a radio relic. We stress that spectral and polarimetric observations are necessary to robustly classify this source.

3.3 The complex regions C and D

To the south-west of the cluster is region C, which we show enlarged at high resolution in Fig. 7. In this region, there are two prominent tailed radio galaxies with optical counterparts at the cluster redshift, which we refer to as C_A and C_B . Around these galaxies we detect very steep spectrum diffuse emission (see Figs 5 and 6), notably the emission labelled C_C which connects to the eastern tail of C_B and extends southwards with a peak of emission coincident with another cluster member; and the previously unseen emission connected to C_A at the position of its optical counterpart which extends eastwards and then south towards the head of C_B .

In region D, we observe a very unusual feature, with a bright bulb of emission at 15:10:00 +33:29:20 with no obvious optical counterpart in the SDSS *R*-band image (Fig. 7), that we refer to as D_A . To the northeastern edge of D_A we observe a filament of emission that appears to emerge from the bulb of emission. This filament extends eastwards for ~ 0.5 Mpc (245 arcsec) with a slight break in its direction after 195 kpc (95 arcsec) just south of the brightest cluster galaxy (BCG) which is itself a faint radio source. There is additional emission protruding from the southeastern edge of D_A which extends eastwards and has similar morphology to the filament, but its extension is only ≈ 60 kpc (30 arcsec). It is unclear whether D_A and these filamentary structures are related or whether

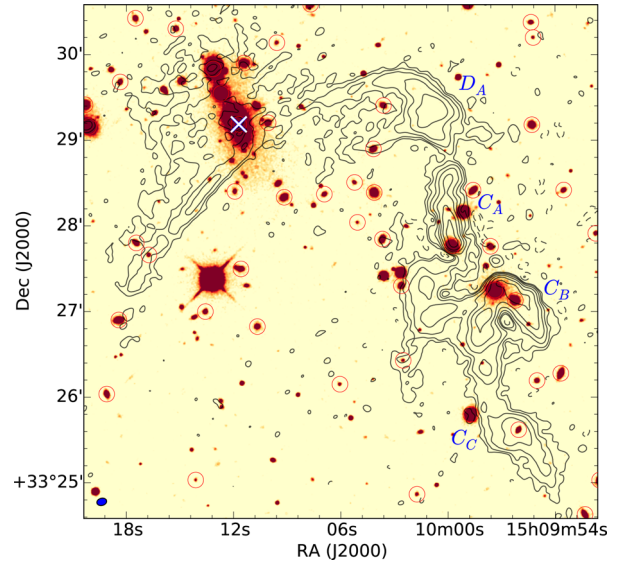


Figure 7. A high-resolution LOFAR image ($7 \text{ arcsec} \times 5 \text{ arcsec}$) overlaid on an SDSS *r*-band image of region C and D of Abell 2034. Similarly to Fig. 4, the BCG is shown with a cross and the circles indicate likely cluster members. The tailed radio galaxies in region C and the bulb of emission in region D are labelled. The LOFAR contours show the $(1, 2, 4, \dots) \times 3 \times \sigma_{\text{LOFAR}, 5 \text{ arcsec}}$ levels where $\sigma_{\text{LOFAR}, 5 \text{ arcsec}} = 190 \mu\text{Jy beam}^{-1}$.

their apparent connection is a chance alignment. However, there is no obvious optical counterpart to either filament.

3.4 The diffuse region E

Both our high- and low-resolution images (Figs 3 and 4) indicate that the X-ray bright region of the cluster (region E) hosts diffuse radio emission, which should most likely be classified as a radio halo. Measuring the integrated flux of the radio halo is challenging due to the contamination from radio sources and the difficulty in properly disentangling it from the bright emission in region D. However, we estimate the total emission from the low resolution WSRT and LOFAR images we presented in Fig. 6 by integrating the flux in the area north of region D which has LOFAR emission exceeding $4\sigma_{\text{LOFAR}, 30 \text{ arcsec}}$, this region is shown by the solid thick contour in the left-hand panel of Fig. 6. We measure the integrated flux in this region to be $S_{150 \text{ MHz}} = 416 \pm 62$ mJy and $S_{1.4 \text{ GHz}} = 8.5 \pm 0.6$ mJy which implies a spectral index of $\alpha \approx -1.7 \pm 0.1$. For comparison, we note that Giovannini et al. (2009) observed Abell 2034 at 1.4 GHz using the VLA *C* and *D* configurations (in these data the shortest baseline was 35 m, whereas the shortest baseline used during the WSRT observation was 52 m) and measured the flux of the radio halo to be of 13.6 ± 1.0 mJy. Whilst we do not have the exact area used for this integrated flux measurement, we approximate it with the total area within the solid and dashed contours displayed in the left-hand panel of Fig. 6 which encompass the emission seen by Giovannini et al. (2009). We estimate the 150 MHz integrated flux density of the radio halo in this region by integrating all the emission and subtracting the contaminating flux from BCG1 (a peak flux of $4.1 \text{ mJy beam}^{-1}$ at 150 MHz) and the filament (which we estimate from our high-resolution images to be approximately 100 mJy). We calculate a spectral index of $\alpha \approx -1.6 \pm 0.1$ between our integrated flux measurement and the Giovannini et al. (2009) measurement.

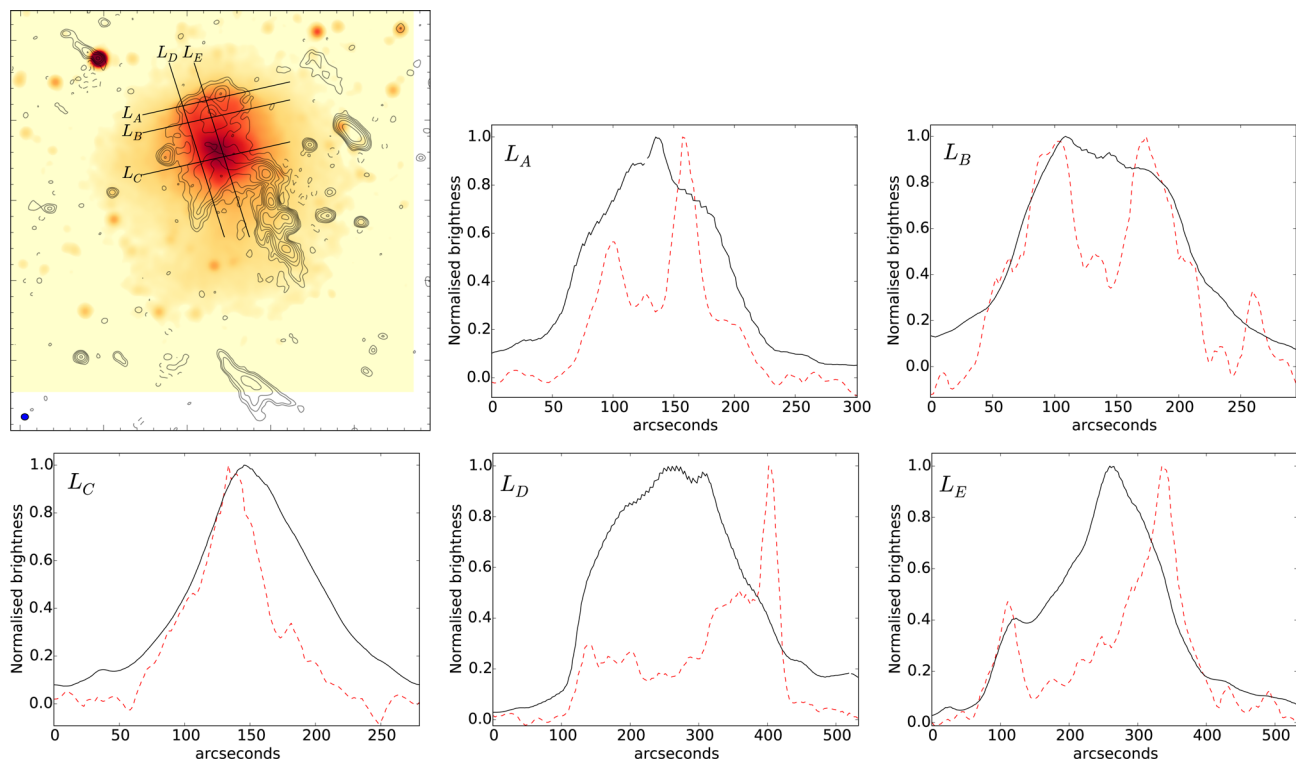


Figure 8. One-dimensional brightness profiles of the X-ray (black lines) and radio emission (red dashed lines). The top-left figure shows the lines L_A (15:10:30.7 33:32:17.1 to 15:09:55.3 33:33:55.8), L_B (15:10:30.7 33:31:23.5 to 15:09:55.3 33:33:01.8), L_C (15:10:30.7 33:29:17.1 to 15:09:55.3 33:30:55.8), L_D (15:10:18.3 33:34:53.6 to 15:10:05.0 33:26:10.1) and L_E (15:10:24.3 33:34:53.6 to 15:10:11.0 33:26:10.1) together with the medium-resolution (22 arcsec \times 19 arcsec) LOFAR contour image and the high-resolution X-ray intensity image (pixels of size 1.968 arcsec) convolved with a Gaussian kernel of FWHM = 20 arcsec for comparison with the LOFAR image. The LOFAR contours show the (1, 2, 4, ...) \times $3 \times \sigma_{\text{LOFAR}, 20 \text{ arcsec}}$ levels where $\sigma_{\text{LOFAR}, 20 \text{ arcsec}} = 350 \mu\text{Jy beam}^{-1}$ and the region shown is identical to that presented in Fig. 3. The brightness profiles of these images through the 3.3 arcsec radio pixels or 2.0 arcsec X-ray pixels that are crossed by the five profile lines are shown in the other panels as indicated in the top left-hand corner of each panel.

Brightness profiles through comparable resolution (~ 20 arcsec) radio and X-ray images along the likely cluster merging axis ($\sim 16^\circ$ from north–south), and approximately perpendicular to this, are shown in Fig. 8. Where the precise locations of the profiles were selected to avoid contaminating sources in the X-ray and radio images. In the direction of the cluster merger the brightness profiles (L_D and L_E) show emission that covers the region from the shock front down to region D. The excess of emission in the north of the cluster at the shock front and the bright filaments of emission (region D) dominate the profiles along the direction of the cluster merging axis. In the perpendicular direction the three profiles we have taken show very different behaviour. In the southernmost profile (profile L_C), the radio emission has a similar structure to the X-ray emission but it is narrower and there is a lack of radio emission on the western side. In our middle profile (profile L_B), the radio and X-ray emission have similar extents but there is a large dip in brightness (~ 50 per cent) in the centre of the radio halo (see Fig. 1). The northernmost profile (profile L_A) is across the excess of radio emission that is coincident with the X-ray-detected shock front where a peak of steep spectrum radio emission coincident with a cluster member (see Fig. 4) is the brightest region of emission.

3.5 Diffuse source F

Source F is a previously undetected, faint diffuse structure at 15:10:05 33:18:59 which lies 620 arcsec (1.86 Mpc) south of the southern BCG. It has an integrated flux density of 145 ± 22 mJy at 150 MHz (within the $4\sigma_{\text{LOFAR}, 30 \text{ arcsec}}$) and an extension along its

major axis of 600 kpc (290 arcsec) and 165 kpc (80 arcsec) along its minor axis. Within the same region of the WSRT image of the same resolution, we measure a flux of 1.2 ± 0.3 mJy which is a marginal detection given the high noise due to the large primary beam attenuation at this distance from the pointing centre (12 arcmin) and would need confirmation. These measurements imply that this object has a spectral index $\alpha \leq -2.15$. Assuming a spectral index of -2.15 , we calculate a 1.4 GHz radio power of $\approx 4.0 \times 10^{22}$ W Hz $^{-1}$ with our adopted cosmology. This steep spectrum object has no obvious optical counterpart (see Fig. 4) and at this distance from the cluster centre there is no significant X-ray signal, although it is partially outside of the X-ray field of view. With a peripheral location, lack of optical counterparts and a steep spectrum, this object has the properties expected for a radio relic, but resolved spectral index images and polarization measurements of this source would help to classify it.

4 DISCUSSION

The complexity of the emission seen in Abell 2034 is similar to what is now being uncovered in high-resolution observations of massive merging galaxy clusters that are sufficiently sensitive to radio emission from the ICM (e.g. Owen et al. 2014). Whilst good optical, radio and X-ray auxiliary data sets have been helpful to interpret the large variety of complex diffuse radio emission we have observed in Abell 2034, unfortunately many features still cannot be classified with certainty, and much of our interpretation remains speculative. A more thorough and robust interpretation and

classification of all the diffuse objects we have detected would be achieved with high-quality resolved spectral index and polarimetric measurements.

In Owers et al. (2014), the dynamics of this cluster were described and we outline the key points here to aid the interpretation of the radio emission associated with the ICM. Abell 2034 is primarily a two body head-on collision between a secondary cluster (associated with BCG2) and a primary cluster (associated with BCG1), with the merging axis aligned in the north–south direction and within 23° of the plane of the sky. A secondary subcluster fell into the primary cluster from the south leaving behind an excess of X-ray emission as it was stripped of gas during the infall. During this event the force exerted by the infalling cluster temporarily displaced the X-ray emitting ICM from BCG1 (which is coincident with a peak in the optical galaxy surface density) by 172 kpc in the north–south direction. The core of the secondary infalling cluster passed the core of the primary cluster ~ 0.3 Gyr ago – a similar time period to the merging events in dissociative mergers such as the Bullet cluster (Markevitch et al. 2002) and Abell 2146 (Russell et al. 2012). After core passage the secondary subcluster has continued to move north (away from the primary cluster) and has become increasingly disrupted. Any cool core that it may have had is now difficult to discern and the shock of low Mach number ($M = 1.59_{-0.07}^{+0.06}$), coincident with the galaxies from the subcluster and preceding its gas, is thought to be weakening and slowing down. It is possible that there is also a third substructure involved in the merger and that this is responsible for the X-ray excess in the southern region (Kempner et al. 2003). Indeed, in addition to the large mass concentrations at the positions of two prominent BCGs, Owers et al. (2014) did observe a local peak in the galaxy surface density ≈ 685 kpc south-west of BCG2 coincident with a bright galaxy (see Fig. 4 or see fig. 7 of Owers et al. 2014). Furthermore, a weak-lensing study with Subaru suggested that Abell 2034 may belong to a large-scale filamentary structure which would further complicate the dynamical properties (Okabe & Umetsu 2008).

4.1 Diffuse emission in the central region

Region E hosts the X-ray intensity peak (Fig. 3), the detected SZ signal (Planck Collaboration II 2013) and the highest projected surface mass density (e.g. Okabe & Umetsu 2008). An excess of radio emission close to the shock front was previously observed in this region but its classification was uncertain as it was not detected at high significance. Giovannini et al. (2009) suggested it was an irregular elongated radio halo, whilst van Weeren et al. (2011) noted a poor correspondence with the X-ray emission and suggested it may be a radio relic. Our images confirm the existence of a radio halo in region E of Abell 2034 which, according to e.g. Brunetti et al. (2001) and Petrosian (2001), suggests that the ongoing merger has introduced turbulence throughout a large area of the ICM where particles have been accelerated sufficiently to produce observable synchrotron radiation. The halo is well characterized in our lower resolution images (see Fig. 3) and we find it is most extended in the merging direction (375 arcsec or 775 kpc in this direction and 280 arcsec or 570 kpc in the perpendicular direction) similar to what is seen in radio haloes in other well-characterized merging clusters (e.g. Macario et al. 2011; Lindner et al. 2014; Shimwell et al. 2014) and independently suggesting that the merging is occurring primarily in the north–south direction. However, the structure of the observed radio halo and the diffuse emission embedded within it is very unusual. There is a ridge of enhanced brightness in the north of the halo; a dip in brightness in the centre; a lack of emission on the

western side; and an indication of a steep integrated spectral index. We discuss these features in this order in the following paragraphs.

In the northern region of the halo close to the shock front some of the excess brightness at 150 MHz is due to two bright spots, the brightest being at 15:10:11 +33:33:24, with another fainter structure at 15:10:19 33:32:48. The brightest spot is 45 arcsec south-east of BCG2 (this BCG is faint at 150 MHz but visible at 1.4 GHz) and is elongated in the direction towards that BCG, it has a very steep spectrum (≈ -2) and has a cluster member located within its region of high brightness. The fainter bright spot is slightly extended in the north-west direction and has no clear optical counterpart. There is an optical source close to the brightest region, but it is not certain if it is a cluster member as the redshift was not measured by Owers et al. (2014). In addition to these two bright spots that could be associated with cluster members, there is an excess of 150 MHz radio emission close to the shock – in the brightness slices we present in Fig. 8, we avoided the two bright spots and still see a clear brightness ridge in the north. The brightness edge is quite different from what is seen in the Bullet cluster, where a much stronger shock ($M = 3.0 \pm 0.4$) does not produce a relic or enhanced brightness but does cause a very distinctive shape to the edge of the radio halo that traces the shock (Shimwell et al. 2014). However, enhanced brightness is also seen at the position of the southern shock in the ‘Toothbrush’ cluster (1RXS J0603.3+4214): van Weeren et al. (2012) suggested this may be a radio relic, but later measured it to have a rather uniform spectral index across its structure, which argues against that interpretation (van Weeren et al. 2016b). Unfortunately, it is difficult to accurately assess the resolved spectral properties in the region of the Abell 2034 shock as the complete structure is not detected due to the low signal to noise in the 610 MHz and 1.4 GHz images and there is contamination due to the two bright spots that were previously discussed. In agreement with Owers et al. (2014), we suggest that for this very weak shock ($M = 1.59_{-0.07}^{+0.06}$) in Abell 2034 to produce enhanced emission, there must be a pre-existing population of electrons in this region as a significant amount of direct acceleration from a thermal pool of electrons would require a stronger shock (e.g. Hoeft & Brüggén 2007). If we consider the scenario where the seed relativistic electrons have been very recently reaccelerated by the shock, and they have not had time to cool, then the Mach number can be related to the energy spectrum of the emitting electrons (Blandford & Eichler 1987) as

$$\delta_{\text{inj}} = 2 \frac{M^2 + 1}{M^2 - 1}, \quad (2)$$

where δ_{inj} is the injection power-law index of the energy spectrum of emitting electrons, and is related to the injection spectral index by $-\alpha_{\text{inj}} = (\delta_{\text{inj}} - 1)/2$. Hence from the X-ray measured Mach number, we may expect a radio spectral index of ~ -1.8 which is consistent with our measurements in this region. The pre-existing electrons may be associated with the two bright spots that we observe close to the shock. The connection between these bright spots and the shock would also explain their apparent elongations in the approximate direction of the shock front. It would be interesting to know the polarimetric properties of this region and see if it is unpolarized (as expected for a halo) or strongly polarized with polarization vectors aligned with the shock direction (as expected for a relic).

South of this region of enhanced emission and towards the centre of the radio halo there is a decline (~ 50 per cent in our 20 arcsec resolution images) in the 150 MHz surface brightness of the radio halo, which is also visible in the 1.4 GHz images. We have not found any similar decrements in other radio haloes in the literature. It could be that the radio halo is concentrated just around the southern region

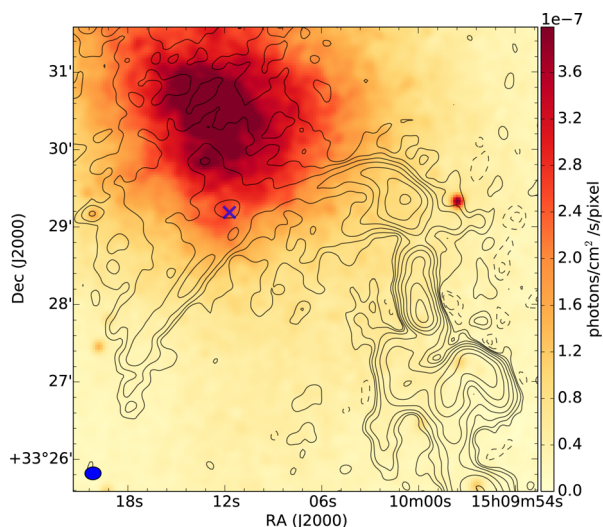


Figure 9. Contours from a medium-resolution ($12\text{ arcsec} \times 10\text{ arcsec}$) LOFAR image of Abell 2034 overlaid on a high-resolution *Chandra* image (pixels of 1.968 arcsec) which has been smoothed with a Gaussian kernel of $\text{FWHM} = 6\text{ arcsec}$. The *Chandra* image is the same as that in Fig. 3 and the radio image is the same as that in Fig. 1. The cross shows the position of BCG1.

near BCG1 (which is the larger cluster) and we are only seeing emission associated with the shock in the north. In this scenario the passage of the shock could also be responsible for the turbulence which causes the radio halo. A similar explanation was provided for the region of very steep spectral index radio emission between the radio relic and the radio halo in the ‘Toothbrush cluster’ (van Weeren et al. 2016b), where the size of the region with little radio emission (or the very steep spectrum region) is dictated by the time it takes for the large-scale turbulence induced by the passage of the shock to decay into smaller scales for particle acceleration (see Brunetti & Lazarian 2007 for details on turbulent decay and acceleration). Assuming this scenario is correct, and that the shock has a constant downstream velocity of 1125 km s^{-1} (where the downstream velocity is the shock velocity of 2057 km s^{-1} divided by the shock compression ratio of 1.83; Owers et al. 2014), then from the $\approx 2\text{ arcmin}$ (250 kpc) diameter of the region of decreased brightness in the centre of the halo we can approximate that it takes $\sim 0.22\text{ Gyr}$ for the large-scale turbulence induced by the shock to both decay to smaller scales for particle acceleration and to accelerate electrons to produce observable synchrotron emission.

The brightest region of the radio halo is around the southern BCG and is offset from the peak of the X-ray emission. This offset is best illustrated in Fig. 9 or slice L_C in Fig. 8, which shows the lack of radio emission in the west of the cluster. The offset between BCG1 (where the peak in the mass distribution is) and the X-ray peak was explained by Owers et al. (2014) as being due to collisional effects and the force exerted by the infalling cluster temporarily displacing the X-ray emitting gas. Since the radio emission is similarly displaced, we suggest that the merging is causing a stretching of the ICM and the magnetic field, and that this produces a large amount of turbulence in the region between the BCG and the X-ray peak.

Our spectral index maps do not constrain the spectral index of the radio halo well but our integrated flux measurements at 1.4 GHz and 150 MHz suggest that it has a steep spectral index with $\alpha \approx -1.6$. Whilst more sensitive, higher frequency radio observations are needed to confirm this value and to further characterize the

spatial variations, such steep spectra radio haloes are expected to be naturally produced in the context of the turbulent reacceleration scenario (e.g. Cassano, Brunetti & Setti 2006; Brunetti et al. 2008) as a consequence of less energetic merger events (mergers between clusters of small mass). With a mass of $M_{500} = 4.19 \pm 0.4 \times 10^{14}\text{ M}_{\odot}$ (Planck Collaboration XXXII 2015), Abell 2034 is one of the least massive cluster systems known to host a radio halo (see e.g. Cassano et al. 2013), so it may be that the energetics involved in the merger are relatively low and this can explain the steep spectrum nature of its emission. Alternatively, it is also thought that a steep spectral index should be observed during the switch-on or switch-off phase of the radio halo (see e.g. Donnert et al. 2013), and although these periods are short, Abell 2034 is a young merger.

4.2 Filamentary emission in the central region

Just south of the brightest region of the halo there are narrow filaments of emission which the halo seems to merge into (see Fig. 4). This newly discovered filamentary structure has a very steep spectrum and is one of the most intriguing features we have detected in Abell 2034. Coincident with these narrow filaments, there is a rapid decline in the emission of the halo. The lack of radio halo emission south of these narrow filaments gives the halo an asymmetry about its peak in the north–south direction along which the cluster is also merging (see slices L_D and L_E of Fig. 8). A reverse shock with respect to the northern shock seems unlikely to be the cause of this due to the lack of any obvious shock signature in the bright X-ray signal at this position. The shape of the narrow filaments of emission does not trace a path of constant X-ray brightness and the narrow filaments do not have the classic arc-shape seen in e.g. van Weeren et al. (2010). Instead, the morphology of the narrow filaments is nearly the reverse of a classic arc and is similar to that seen in the northern relic of PLCKG287.0 +32.9 (Bonafede et al. 2014b). That relic emission was explained as being shock acceleration of a plasma linked to a nearby radio source with typical radio morphology but without an optical counterpart. In Abell 2034, the narrow filaments of emission could again be plasma associated with a nearby galaxy that is now supplying plasma to the radio halo. Whilst there is no obvious connection between cluster galaxies or AGNs and the filaments, BCG1 is just north of the centre of the filamentary structure where there is a break in its direction (see Figs 4 and 7), and the filaments could be associated with fossil plasma from old radio lobes that propagated in the east–west direction away from this BCG. If this fossil plasma were recently compressed by the ongoing merger then its brightness would be enhanced and it may be able to form the well-defined structure we observe. Furthermore, if the narrow filaments of emission are fossil plasma, and were present when the cluster associated with BCG2 fell into BCG1 from the south, it would have disturbed this plasma and spread it northwards explaining the halo emission we see north of the narrow filaments and the lack of emission south of them. There is a hint of a connection between the central region of the filaments, a region of slightly enhanced X-ray emission close to BCG1 (see Fig. 9) and a region where the X-ray measured temperature is hot and patchy (see fig. 3 of Owers et al. 2014). This may deserve further analysis in the future but it is likely that in this region there is a significant contribution from the hot atmosphere of BCG1. Alternatively, the morphology of the filaments may indicate that they are not associated with the main subcluster, but are seen in projection. It is apparent from X-ray (e.g. Owers et al. 2014) and optical studies (e.g. Okabe & Umetsu 2008) that Abell 2034 has very complex dynamics and could possibly be part of a filamentary structure. Whilst there is little evidence

that this filamentary structure is along the line of sight, under such complex conditions projection effects can be important and we cannot exclude the possibility that the filamentary structure we see in the radio is a foreground or background relic associated with a sub-cluster in the Abell 2034 complex and is projected on the X-ray emission from the main cluster. A similar scenario was suggested by Pizzo et al. (2011) to explain the filamentary radio emission seen close to the centre of Abell 2255.

We have speculated in the previous paragraph that the filamentary structures could be associated with plasma from other radio galaxies (such as BCG1) or a shock, however, their nature remains very uncertain. The only similar emission that we have found in the literature is the ‘Line’ in Abell 2256 (see fig. 4 of Owen et al. 2014). In that cluster, the ‘Line’, which has no optical counterpart and a very steep spectrum, is detected close to the position of a cold front and a Narrow Angled Tail source (Owen & Rudnick 1976) but its origin is similarly unclear and its spectral properties have yet to be determined.

4.3 Diffuse emission in the peripheral regions

There are several regions of diffuse radio emission in the peripheral regions of Abell 2034 that we have either discovered or further characterized using our 150 MHz images. In the following paragraphs we discuss the previously classified radio relic (source A) and two newly detected faint and steep spectrum diffuse structures (sources B and F).

The previously classified radio relic in region A is bright and compact: with its largest linear size being just 220 kpc it is one of the smallest radio relics known (e.g. Feretti et al. 2012) and with a $\log(\nu P(\nu)/LLS^2) = 41.41 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ (where LLS is the largest linear size) it has one of the highest surface brightnesses of the known radio relics (see Brunetti & Jones 2014). Like most relics, this object is orientated approximately parallel to the closest X-ray brightness edge (see Fig. 3) but its location is slightly unusual as it is not in the direction of merging, which is approximately north to south. Unfortunately, in this region (0.85 Mpc or 6.8 arcmin from the nearest BCG) there were too few X-ray counts for Owers et al. (2014) to search for a shock associated with the relic. In our 150–610 MHz spectral index map (see Fig. 5), we resolve the minor axis of source A and our measurements indicate that this object does not have the spectral index gradient that may be expected for a radio relic, with a flatter spectrum on the side furthest from the cluster centre where the electrons have most recently been accelerated. Instead, the resolved spectral index maps suggest a fairly uniform spectral index distribution with no obvious spectral gradients but small variations giving it a patchy appearance. We measure a region of flatter spectral index at the southwestern tip of the object where there is a faint point-like radio source (see Fig. 4). However, this point-like radio emission is likely associated with a massive elliptical galaxy and therefore the correspondence with a faint optical source (shown in fig. 20 of van Weeren et al. 2011) indicates it is probably at higher redshift than the cluster. Assuming that the diffuse emission in region A is at the redshift of cluster it is possible that it could be associated with an existing population of electrons that has been compressed or reaccelerated. This scenario is similar to what is speculated for the relics shown in e.g. Bonafede et al. (2014b) and Shimwell et al. (2015). A promising candidate for the source of the existing population of electrons is the bright elliptical galaxy at 15:09:40 33:30:40, which van Weeren et al. (2011) originally suggested could be responsible for the bright emission from region A.

Just north of source A, there is a very faint, previously unknown diffuse structure (region B) that we cannot robustly classify, but it has similar properties to those expected for a relic or fossil plasma associated with an old AGN. In our low-resolution images, there is a hint of a possible bridge (see Fig. 3) that connects region B to both the northwestern region of the radio halo and the north of region A. Whilst this bridge is detected at very low significance and would need to be confirmed with deeper observations, it may indicate that there is a physical link between the halo, region A and region B. In this scenario these regions of emission could be one structure that was formed or enhanced by the same shock, albeit one with unusual morphology but complex patterns of shocks are predicted by numerical simulations (e.g. Vazza et al. 2009; Skillman et al. 2011).

Object F is 1.86 Mpc from the nearest BCG and has a very steep spectral index of at least ≈ -2.15 . Similarly to regions A and B we are unable to robustly classify this source but it again has the properties expected for fossil plasma or a radio relic. Extrapolating its flux to 1.4 GHz with this spectral index limit indicates that the 1.4 GHz power of the source is at most $\approx 4.0 \times 10^{22} \text{ W Hz}^{-1}$ ($\log P(1.4 \text{ GHz}) = 22.59 \text{ W Hz}^{-1}$). Therefore, if this object is a radio relic then it is the lowest power radio relic that we are aware of (e.g. Feretti et al. 2012). Furthermore, with a $\log(\nu P(\nu)/LLS^2) = 39.18 \text{ erg s}^{-1} \text{ Mpc}^{-2}$ it would have the lowest surface brightness of a confirmed radio relic (see fig. 18 of Brunetti & Jones 2014). At a separation of 1.86 Mpc in projection ($0.9 \times r_{200}$ or $1.6 \times r_{500}$), it is unusually far from the cluster centre although other relics have been detected at comparable distances and several are even further from the X-ray bright region of the cluster (e.g. Pizzo et al. 2008; Bonafede et al. 2014b). The interpretation of such distant objects varies, with Pizzo et al. (2008) favouring a structure formation shock, whilst Bonafede et al. (2014b) suggested the relic could have been created from an earlier core passage between the main merging clusters or an infall of a smaller group into the main cluster. It is plausible that object F is a relic caused by a structure formation shock that now has a very steep spectrum as it is fading. Alternatively it could be caused by a third substructure infalling from the south. A third substructure is compatible with X-ray observations as, although Owers et al. (2014) preferred the two-body interpretation for Abell 2034, there is a suggestion from their work and the work of Kempner et al. (2003) that there is a third smaller subcluster to the south-west of BCG1 (see Figs 3 or 4). However, assuming this third substructure is associated with Abell 2034, its expected motion is towards or away from the two main components of Abell 2034. This implies that a peripheral shock in the third substructure, on the edge opposite the bulk of the Abell 2034 mass, would likely propagate south-west, whereas the putative relic is observed ≈ 600 kpc directly south of the third substructure.

Finally, we note that the symmetry between the southern relic candidate (region F) and the narrow filaments at the southern part of the radio halo (region D) is difficult to ignore, with object F and the narrow filaments of emission in region D having similar length and curvature. Although, at high resolution, the structure of the emission in region D and region F is different, with the southern relic candidate appearing diffuse whilst the filaments of emission remain narrow and well defined. As indicated by the diamond symbol in Fig. 4, almost halfway between the eastern edge of these two objects, at 400 kpc (195 arcsec) from each edge, there is an elliptical galaxy (SDSS J151015.05+332314.4), which is a cluster member and has Mg, Na D and H α absorption features which are expected for a ‘red and dead’ radio galaxy that used to host radio emission but is no longer active (there is no radio emission exactly coincident with

this elliptical galaxy – the closest significant radio point source we detect is displaced by 15 arcsec to the east). Whilst this alignment is most likely a coincidence, as many of the large elliptical galaxies in clusters are ‘red and dead’ with these absorption features, it leads us to suggest that the emission in region F and region D could possibly be the old lobes of a very large radio galaxy where the narrow filaments in region D have been compressed and enhanced by the ongoing merger or revived by a shock. The extent of such a galaxy would be large with the distance from the core to the end of each lobe being ≈ 1 Mpc.

4.4 Other unclassified steep spectrum emission

Besides the candidate relics, the halo and the filamentary structure in Abell 2034, we have discovered further steep spectrum emission. In region C, which is shown in Fig. 7, there is a region of previously unobserved diffuse emission that appears to connect the tailed radio galaxies. Also, north of the C_A region there is a bright region (D_A) without an optical counterpart, whose emission merges with the radio filaments we have briefly discussed in previous sections. These two bright and steep spectrum regions are close to the lobes of tailed radio galaxies and it may be that there are large amounts of aged plasma in these regions which originated from the tailed galaxy lobes and is visible at low frequencies. Or it may be that the emission has been enhanced by reacceleration during the ongoing merging. Similar features are also seen close to the tailed radio galaxies in e.g. the Sausage cluster (Stroe et al. 2013) and Abell 2443 (Cohen & Clarke 2011). Much of this newly discovered emission could simply be long and complex tails from radio galaxies, where the old plasma is bright at low frequencies and is seen in projection. Although, in this scenario, it is difficult to explain the morphology of source D_A and its apparent connection to the fainter filaments extending from its northern and southern peripheries which give the impression that D_A is travelling westwards through the ICM, whereas the nearby tailed galaxy is travelling south.

5 CONCLUSIONS

With this LOFAR observation, we demonstrate the importance of low-frequency observations of merging galaxy clusters and highlight the wealth of additional diffuse steep spectrum sources that can be discovered even in already well-studied clusters. Many of the features we have discovered now require resolved spectral index and polarimetric measurements to make robust claims on their origin and to further develop our understanding of the dynamical history of this interesting cluster and the interaction between the ICM and radio galaxies. From our study of Abell 2034 our main conclusions are the following.

(i) In region D a bright bulb of emission is connected to two previously undetected filaments of steep spectrum emission which extend across the south of the cluster in the direction perpendicular to the cluster merger axis. We speculate that these may be related to either a shock or the lobes of a radio galaxy which are disturbed or reaccelerated by the ongoing merger. The complication is that neither the bulb or the filaments have an obvious connection with AGNs or cluster galaxies, nor do they correspond to the position of a known X-ray shock. This may be a natural consequence of observing at low frequency, where the sensitivity to steep spectrum emission from old plasma is high.

(ii) An irregular radio halo (region E) is detected in the region of the highest X-ray intensity. The halo was previously known but

LOFAR observations suggest it has a very steep spectrum, with $\alpha < -1.6$. The northern region of the radio halo has an excess of emission close to an X-ray-detected shock, as was suggested by previous studies, but it remains uncertain whether this should be classified as a part of the halo, a relic or a combination of the two. The brightness distribution of the halo is complex, we find that there is a decline in the centre and that the region of highest brightness is offset from the BCG. It may be that this complex radio halo structure probes the distribution of turbulence and magnetic fields in the cluster and their interplay with the dynamics of the ICM. Future studies including polarimetry and resolved spectral index analysis are required to investigate this further.

(iii) Three candidate radio relics are detected in the cluster (regions A, B and F). The brightest of the prominent relic candidates is a previously classified relic that lies 0.85 Mpc west of the cluster and is connected via a very low significance bridge of emission to the northern region of the radio halo. The other prominent relic candidate lies ≈ 2 Mpc from the cluster centre and has the lowest surface brightness of any previously known relic. It is possible that our observations are beginning to reveal radio emission that is produced by the complex network of shocks which numerical simulations predict will embed dynamically active systems.

(iv) There are other regions of very steep spectrum emission close to either tailed radio galaxies or the northern shock. Due to its low observing frequency LOFAR is exceptionally sensitive to steep spectrum emission from old plasma and it may be that this emission is related to long and complex tails of radio galaxies seen in projection or the reacceleration of fossil particles.

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- ¹*Leiden Observatory, Leiden University, PO Box 9513, NL-2300 RA Leiden, the Netherlands*
- ²*Department of Physics, University of Maryland, Baltimore County, 1000 Hilltop Circle, Baltimore, MD 21250, USA*
- ³*Hamburger Sternwarte, Gojenbergsweg 112, D-21029 Hamburg, Germany*
- ⁴*INAF/Istituto di Radioastronomia, via Gobetti 101, I-40129 Bologna, Italy*
- ⁵*National Radio Astronomy Observatory, 1003 Lopezville Road, Socorro, NM 87801-0387, USA*
- ⁶*Department of Physics and Astronomy, Macquarie University, NSW 2109, Australia*
- ⁷*Australia and Australian Astronomical Observatory PO Box 915, North Ryde, NSW 1670, Australia*
- ⁸*European Southern Observatory, Karl-Schwarzschild-Str. 2, D-85748, Garching, Germany*
- ⁹*Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA*
- ¹⁰*ASTRON, the Netherlands Institute for Radio Astronomy, Postbus 2, NL-7990 AA Dwingeloo, the Netherlands*
- ¹¹*Kapteyn Astronomical Institute, PO Box 800, NL-9700 AV Groningen, the Netherlands*
- ¹²*School of Physics, Astronomy and Mathematics, University of Hertfordshire, College Lane, Hatfield, Hertfordshire AL10 9AB, UK*
- ¹³*SUPA, Institute for Astronomy, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK*
- ¹⁴*Astronomical Observatory, Jagiellonian University, ul. Orla 171, PL-30-244 Kraków, Poland*
- ¹⁵*MPI f. Astrophysik, Karl-Schwarzschild-Str. 1, D-85741 Garching, Germany*
- ¹⁶*Laboratoire Lagrange, UMR 7293, Université de Nice Sophia-Antipolis, CNRS, Observatoire de la Côte d'Azur, F-06300 Nice, France*
- ¹⁷*Department of Astrophysics/IMAPP, Radboud University, PO Box 9010, NL-6500 GL Nijmegen, the Netherlands*
- ¹⁸*Thüringer Landessternwarte, Sternwarte 5, D-07778 Tautenburg, Germany*
- ¹⁹*Department of Earth and Space Sciences, Chalmers University of Technology, Onsala Space Observatory, SE-439 92 Onsala, Sweden*
- ²⁰*Department of Physical Sciences, The Open University, Milton Keynes MK7 6AA, England*
- ²¹*RAL Space, The Rutherford Appleton Laboratory, Chilton, Didcot, Oxfordshire OX11 0NL, UK*

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