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1	Correcting biases in tropical cyclone		
2	intensities in low-resolution datasets using		
	dynamical systems metrics		
3	dynamical systems metres		
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22	Abstract		
23	Although the life-cycle of tropical cyclones is relatively well under		
24	stood, many of the underlying physical processes occur at scales below		
26	those resolved by global climate models (GCMs). Projecting future		
27	changes in tropical cyclone characteristics thus remains challenging. We		
28	propose a methodology, based on dynamical system metrics, to recon-		

struct the statistics of cyclone intensities in coarse-resolution datasets, where maximum wind speed and minimum sea-level pressure may

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not be accurately represented. We base our analysis on 411 tropical 31 cyclones occurring between 2010 and 2020, using both ERA5 reanal-32 ysis data and observations from the HURDAT2 database, as well as 33 a control simulation of the IPSL-CM6A-ATM-ICO-HR model. With 34 ERA5 data, we compute two dynamical system metrics related to 35 the number of degrees of freedom of the atmospheric flow and to 36 the coupling between different atmospheric variables, namely the local 37 dimension and the co-recurrence ratio. We then use HURDAT2 data 38 to develop a univariate quantile-quantile bias correction conditioned on 39 these two metrics, as well as a multivariate correction method. The 40 conditional approach outperforms a conventional univariate correction 41 of the sea-level pressure data only, pointing to the usefulness of the 42 dynamical systems metrics in this context. We then show that the 43 multivariate approach can be used to recover a realistic distribution 44 of cyclone intensities from comparatively coarse-resolution model data. 45

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Keywords: Tropical cyclones, Extreme Event, Bias Correction

### 47 **1** Introduction

Tropical cyclones are among the most devastating natural disasters, often caus-48 ing fatalities and extensive economic damage (Smith and Katz, 2013; Grinsted 49 et al, 2019). They include several collateral hazards that can have significant 50 impacts on people and property, such as rogue waves, flooding, extreme winds, 51 and tornadoes. The few, most severe episodes account for the bulk of the costs 52 associated with tropical cyclone (Emanuel, 2021). It is thus crucial to model 53 such cyclones correctly. Unfortunately, even state-of-the-art global and regional 54 climate models struggle to reproduce the dynamics of the most severe tropical 55 cyclones (Camargo and Wing, 2016; Roberts et al, 2020b). This is mainly due 56 to their insufficient resolution. Indeed, a grid spacing of the order of 10 kilo-57 meters or below is needed (Rotunno et al, 2009; Moon et al, 2020; Murakami 58 et al, 2012; Manganello et al, 2012). Downscaling techniques can be employed 59 to alleviate this issue, but their use is limited by computational costs; further-60 more, different downscaling approaches can lead to diverging conclusions (e.g., 61 Caron et al, 2011; Lee et al, 2020; Knutson et al, 2020; Emanuel, 2021). The 62 situation is complicated by the reduced length of records in available tropi-63 cal cyclone data sets, which mostly rely on satellite data not available before 64 the '80s (Chang and Guo, 2007). This limitation hinders separating significant 65 changes in tropical cyclone properties from decadal variability (Knutson et al, 66 2019). 67

Mid-latitude synoptic dynamics mostly originate from the chaotic structure of the motions associated with baroclinic instability (Lorenz, 1990; Schubert and Lucarini, 2015). Tropical cyclones are instead characterized by a rapid organization of unstable flows at the convective scale whose dynamics is turbulent and highly sensitive to boundary conditions (Muller and Romps, 2018;

Carstens and Wing, 2020). Here, we investigate whether it may be possi-73 ble to exploit this high level of flow organization to obtain reliable statistics 74 of intense tropical cyclones from relatively coarse-gridded atmospheric data. 75 To achieve this, we compute two metrics that describe cyclones as states 76 of a chaotic high-dimensional dynamical system. The first, the local dimen-77 sion d, reflects the number of active degrees of freedom of an instantaneous 78 state of the cyclone. The second, the co-recurrence ratio  $\alpha$ , is a proxy for the 79 instantaneous coupling between different atmospheric variables which may be 80 interpreted in the sense of covariability. These metrics have recently provided 81 insights on a number of geophysical phenomena, including transitions between 82 transient metastable states (e.g. weather regimes) of the mid-latitude atmo-83 sphere (Faranda et al, 2017; Hochman et al, 2021a; Messori et al, 2021), drivers 84 and predictability of extreme events (Messori et al. 2017; Hochman et al. 2019; 85 De Luca et al, 2020; Faranda et al, 2020; Hochman et al, 2021b), palaeoclimate 86 attractors (Brunetti et al. 2019; Messori and Faranda, 2021), slow earthquake 87 dynamics (Gualandi et al. 2020) and changes in mid-latitude atmospheric pre-88 dictability under global warming (Faranda et al, 2019). A benefit over previous 89 dynamical systems approaches (e.g. Wolf et al. 1985; Cao, 1997) is that these 90 metrics can be easily applied to computationally demanding datasets, such as 91 climate reanalyses or climate models. 92

Applications of d and  $\alpha$  in the literature have used an Eulerian approach 93 over a fixed spatio-temporal domain, rather than tracking the evolution of 94 specific physical phenomena. Here, we follow the recent work of Faranda et al 95 (2023) and apply the two metrics in a semi-Lagrangian perspective to char-96 acterize the structure of tropical cyclones in the  $d - \alpha$  phase-space. That is, 97 we compute the metrics on a spatial domain which follows the track of each 98 cyclone in time. This enables the study of the complex behavior of convectively 99 unstable flows, by focussing on the evolution of the storm's structure instead 100 of the storm's motion across a fixed domain (Crisanti et al, 1991; Vulpiani, 101 2010). The signature of intense cyclones is associated with the presence of 102 inverse energy cascades as suggested by Levich and Tzvetkov (1985) and, more 103 recently, by Faranda et al (2018); Dunkerton et al (2009); Tang et al (2015). 104 Such inverse cascades are associated with potential-kinetic energy conversions 105 and are particularly notable for intense storms (Bhalachandran et al, 2020). 106 These energy conversions are related to the deep convection in the evenall. 107 that redistributes to the upper troposphere the enthalpy gained thanks to sur-108 face heat fluxes in the boundary layer. Such local processes contribute to the 109 generation of the storms' warm core and, ultimately, to wind intensification 110 at the larger, sub-synoptic scale of the storm (Emanuel, 1986). We hypothe-111 sise that these exchanges have a signature in both the large-scale horizontal 112 velocity and potential vorticity fields, which are reasonably well-represented in 113 coarse simulations or reanalyses. If this indeed holds, then the dynamical sys-114 tem metrics should be able to distinguish between different storm intensities 115 due to their different degree of organization and coupling. This would enable 116 a correction conditioned on d and  $\alpha$  of cyclone intensity statistics in datasets 117

where we cannot explicitly access the spatial scales underlying the dynamics of intense tropical cyclones.

Bias correction of climate models is a crucial step in improving the accu-120 racy of climate predictions, and there is a considerable number of different 121 bias correction techniques proposed in the literature. For a review of bias cor-122 rection methodologies, which is beyond the purpose of this paper, we refer 123 the reader to Maraun (2016). One widely used method is empirical Quantile 124 mapping bias correction (QMBC), which has been shown to be effective in 125 reducing biases in precipitation and temperature data (e.g., Li et al (2010); 126 Michelangeli et al (2009); Cannon et al (2015); Cannon (2018)). QMBC has 127 also been applied to assessing the impact of climate change on tropical cyclone 128 (TC) intensity in medium-resolution global climate models (GCMs)(Zhao and 129 Held, 2010; Sugi et al, 2017; Yoshida et al, 2017). These studies have shown 130 that QMBC is very useful in improving the accuracy of GCM simulations by 131 matching the distribution of observed data with the model's output. However, 132 the conventional QMBC has limitations, including not accounting for non-133 stationary characteristics of the data. In this study, we propose a new method 134 for bias correction that implicitly accounts for weak non-stationarity in the 135 data through the dynamical systems metrics, and that may be easily extended 136 to explicitly account for non-stationarity by leveraging well-tested approaches. 137 We demonstrate its effectiveness in improving the accuracy of TC intensity 138 projections. 139

We base our analysis on best track cyclone data from the HURDAT2 140 database, which we take as ground truth, ERA5 reanalysis data and a high-141 resolution global climate model simulation. We compute the two dynamical 142 systems metrics using the square root of the kinetic energy uv [m/s] and the 143 potential vorticity field PV [PVU] at the 850 hPa level. The rationale for using 144 PV follows the works of Peng et al (2012) and Fu et al (2012) who used PV for 145 distinguishing developing versus non-developing disturbances. The square root 146 of the horizontal kinetic energy uv is relevant to the study of tropical cyclones 147 because of its direct connection with the wind speed and with the phases of 148 rapid intensification/decay of the cyclones (Krishnamurti et al, 2005). The 850 149 hPa level is chosen because it lies in-between the planetary boundary layer and 150 the middle troposphere, where most of the potential-kinetic energy conver-151 sions occur in tropical cyclones (Camargo et al, 2007). Although some of the 152 information provided by PV and uv is redundant, they are analytically con-153 nected, and thus we find that their coupling provides nontrivial information 154 which justifies their use. 155

Our study is organized as follows: first, we describe the data, variables for cyclone dynamics and the theoretical bases supporting the computation of the dynamical system metrics. Then, we show the general characteristics of the phase space of tropical cyclones in reanalysis data for the different variables, and use these to define a quantile-quantile correction approach for cyclone intensities conditioned on the two dynamical systems metrics. The correction

is performed on ERA5 reanalysis, using sea-level pressure (SLP) from HURDAT2 as ground truth. We then conduct an out-of-sample test comparing this
approach to an unconditional quantile-quantile correction. Finally, we test this
correction on data from a GCM.

# 166 **2** Data

### <sup>167</sup> 2.1 HURDAT2 tropical cyclone data

We follow 197 North Atlantic and 214 eastern North Pacific tropical cyclones
that occurred between 2010 and 2020, using the HURDAT2 Best Track
Data (Landsea and Franklin, 2013). We use six-hourly information on the location and central pressure of the cyclones, as well as their time of landfall or
special intensity report points.

### <sup>173</sup> 2.2 Representation of tropical cyclones in ERA5 data

We base our analysis on instantaneous<sup>1</sup>  $uv = u^2 + v^2$ , SLP and PV at 850hPa 174 from the ERA5 reanalysis (Hersbach et al, 2020), sampled every 6h and addi-175 tionally whenever the HURDAT2 database displays a cyclone landfall entry 176 or special intensity report points. The horizontal resolution of the data is 177  $0.25^{\circ}$ . We also make use of ERA5 data coarse-gridded to a  $0.5^{\circ}$  horizontal 178 resolution using a nearest neighbour approach. In the vast majority of cases, 179 the SLP difference in the four ERA5 gridpoints around the cyclone core is 1 180 hPa or less. Using a nearest neighbour approach thus provides similar results 181 to other coarse-graining approaches. The coarse-grained dataset will be here-182 inafter referred to as ERA5 cg, and will be used to evaluate the sensitivity 183 of our conclusions to the resolution of the dataset. When comparing ERA5 184 to HURDAT2, we verify that the SLP minimum in ERA5 is located within a 185 region of  $5^{\circ}$  of the HURDAT2 cyclone position. For our analysis we do not use 186 the wind data because this quantity is often used in different ways (e.g. sus-187 tained winds vs. wind-gusts and with different averaging times) to assess TC 188 intensity in reanalyses, models and the HURDAT2 database, while the use of 189 minimum SLP is coherent across all datasets. 190

There is often a large discrepancy between the minimum SLP reported 191 in HURDAT2 and that in ERA5 (Fig. 1a,c). Especially for the most intense 192 cyclones, ERA5 systematically underestimates minimum SLP. The biases are 193 larger in the eastern North Pacific than in the North Atlantic basin (cf. Fig. 1a 194 and 1c). This affects the capability of ERA5 to accurately assign each tropical 195 cyclone to the appropriate Saffir-Simpson category (Simpson and Saffir, 1974), 196 which we here use relative to SLP (see Table 1). Indeed, recent research argues 197 that SLP is more closely related to cyclone damage than maximum sustained 198 winds (Klotzbach et al, 2020). In particular, ERA5 has a negative bias in the 199 number of tropical cyclones stronger than category 2, namely min(SLP)<980 200 hPa. While this bias is present in both the North Atlantic and eastern North 201

 $<sup>^1\</sup>mathrm{We}$  follow here ECMWF's terminology, see: https://confluence.ecmwf.int



**Fig. 1** Scatterplot of minimum SLP for (a) North Atlantic [NATL] and (c) eastern North Pacific [ENP] tropical cyclones in HURDAT2 versus ERA5 and ERA5 cg. Probability density functions of minimum SLP for (b) North Atlantic and (d) eastern North Pacific tropical cyclones in HURDAT2, ERA5, ERA5 cg and the IPSL-CM6A-ATM-ICO-HR model.

Pacific basins, in the latter the biases for the most intense cyclones appear 202 more severe. This might be due to the more intermittent aircraft reconnais-203 sance activity in that basin with respect to the North Atlantic (Knaff et al, 204 2021). The coarse-graining operation does not notably affect the distribution of 205 cyclone SLP minima (Fig. 1b, d), likely because of the above-mentioned weak 206 SLP variations in the ERA5 dataset in the gridboxes immediately surrounding 207 the cyclone core. We underline that the two ERA5 horizontal resolutions used 208 here are of the same order of magnitude as those of the HighResMIP (High 209 Resolution Model Intercomparison Project, Haarsma et al. 2016) and PRI-210 MAVERA models, which are amongst the current best tools to study climate 211 change impacts on tropical cyclones (Roberts et al, 2020a). 212

# 213 2.3 Representation of tropical cyclones in 214 IPSL-CM6A-ATM-ICO-HR model data

For the purpose of this study, we used a simulation performed with the IPSL-215 CM6A model (Boucher et al, 2020). Model configuration is atmosphere-only 216 (ATM) with forced sea-surface temperatures (SST). The physics component 217 of the model is LMDZ6A, as described in Hourdin et al (2020). The dynam-218 ical core is Dynamico (Dubos et al, 2015, ICO,), which uses an icosahedral 219 grid. A run at high-resolution (HR) is used, corresponding to  $0.5^{\circ}$  horizontal 220 resolution. The CM6A version of the IPSL model has 79 vertical levels. The 221 configuration is named IPSL-CM6A-ATM-ICO-HR. The run was perfored for 222 the HighResMIP, therefore following the protocol described in (Haarsma et al, 223 2016). It is a historical run, over the 1950-2014 period (65 years). Greenhouse 224 gases, aerosols and SSTs are forced to the observed values. 225

We use the TC tracking algorithm from Ullrich et al (2021). We additionally remove tracks starting at latitudes above 30° to minimise incorrect classification of extratropical lows as tropical systems.

The model produces a total of 327 tropical cyclones in the North Atlantic and 989 in the eastern North Pacific (defined following Knutson et al, 2020). Among them, 150 are randomly sampled for each basin, which is deemed a sufficiently large statistical sample for our analysis. The total number of cyclones reproduced by the IPSL-CM6A-ATM-ICO-HR model is in line with that of other HighResMIP models with similar resolution (cf. Roberts et al, 2020b).

A comparison of the distribution of HURDAT2 SLPs with those in the model and in the ERA5 and ERA5 cg data (Fig. 1b, d), suggests that current state-of-the-art GCMs and ERA5 both encounter difficulties when it comes to representing the intensity of tropical cyclones (Kim et al, 2018). Specifically, all three datasets have a sparsely populated left tail of the minimum SLP distribution and, especially for the North Atlantic basin, a different mode when compared to HURDAT2.

## <sup>242</sup> 3 A dynamical systems view of tropical cyclones

In our analysis, for every cyclone we adopt 6-hourly domains of approximately 243 1200 km  $\times$  1200 km at latitudes 10 °N–25 °N (41  $\times$  41 grid points in ERA5 244 corresponding to  $10^{\circ}$  latitude  $\times 10^{\circ}$  longitude), centred at every timestep on 245 the HURDAT2 cyclone location for ERA5 and centered on the minimum of 246 sea-level pressure for the model simulation. We then consider PV and uv at 247 850 hPa in this domain. Each instantaneous state of the cyclone, as represented 248 by these variables and domains, corresponds to a point along a phase-space 249 trajectory representing the cyclone's evolution. We sample this trajectory at 250 discrete intervals determined by the temporal resolution of our data. Our aim 251 is to diagnose the dynamical properties of the instantaneous (in time) and 252 local (in phase-space) states of the cyclone (physical space in Fig. 2). To do 253 so, we leverage two metrics issuing from the combination of extreme value 254 theory with Poincaré recurrences (Freitas et al, 2010; Lucarini et al, 2012, 255



**Fig. 2** Schematic of the computation of the dynamical systems metrics for an instantaneous state of a tropical cyclone. We take a snapshot of the cyclone in physical space (black quadrant), PV in this example, which corresponds to state  $\zeta$  in our phase space. The shaded circle is a 2D representation of the surface determined by the high threshold  $s(q, \zeta)$ , which defines recurrences of  $\zeta$ . The distances between measurements defined by  $dist(X_i, \zeta)$  are marked by double-headed arrows. For all points within the hyper-sphere,  $dist(X_i, \zeta) < s(q, \zeta)$  and  $g(X_i, \zeta) > s(q, \zeta)$  hold. Here, i represents the timestep in the dataset. In the schematic, only two measurements qualify as recurrences: timesteps 2 and 987 (adapted from Messori and Faranda (2021)).

 $^{256}$  2016). Recurrences are temporally separated *PV* or *uv* states that resemble each other. As we discuss below, identifying these recurrences is instrumental to compute the two dynamical systems metrics.

We first calculate TC-centered maps of PV and uv to define the TC state 259 i, where i = 0, 1, ..., T - 1, T represents a given timestep in our dataset, T 260 being the total number of timesteps. We then normalize each distance by their 261 respective norms, which yields  $PV_i$  and  $uv_i$ , respectively. Finally, we define 262 the TC state at a given timestep,  $X_i$ , as the pair of  $PV_i$  and  $uv_i$  maps at 263 that timestep. We thus construct a semi-Lagrangian framework tracking each 264 cyclone. We take each pair of maps  $X_i$  in turn as the reference state  $\zeta$  in our 265 calculation (phase space in Fig. 2). We then define logarithmic returns as: 266

$$g(X_i, \zeta) = -\log[\operatorname{dist}(X_i, \zeta)] \tag{1}$$

Here, we define dist as the Euclidean distance between pairs of maps, but 267 it can be chosen as any distance metric between two vectors. In principle,  $\zeta$ 268 can be any state (and does not have to belong in the available  $X_i$ ). In prac-269 tice,  $\zeta$  is one of the  $X_i$ , and the log dist is computed for all other time steps, 270 as  $\log(\operatorname{dist}(X, X))$  is not defined. Note that the distances between maps are 271 computed by respecting the order of the grid points but without specifying 272 their actual position on the maps (longitude and/or latitude). The logarith-273 mic weight comes directly from the Poincaré recurrence theorem, which states 274 that the probability of hitting a ball centered on a state in phase space gets 275 exponentially small when linearly reducing the radius of the ball. Since dist 276

tends to zero as pairs of  $X_i$ s increasingly resemble each other, the series of log-277 arithmic returns  $q_i$  takes large values for  $X_i$  closely resembling  $\zeta$ . The minus 278 sign in Eq. 1 has the function to convert the minima of the distances into 279 the maxima of q, as it is common practice in extreme value theory to define 280 extreme value distributions for maxima rather than for minima. In Fig. 2, 281 an example of the phase space and the geometrical object defined above is 282 provided: the shaded circle is a 2D representation of the surface (in general 283 this is a hyper-sphere for higher dimension) determined by the high thresh-284 old  $s(q,\zeta) = q(X(q),\zeta)$ , which defines recurrences of  $\zeta$ . The distances between 285 measurements are marked by double-headed arrows. For all points within the 286 hyper-sphere,  $dist(X_i, \zeta) < dist(X(q), \zeta)$  and  $g(X_i, \zeta) > s(q, \zeta)$  hold. 287

We next define exceedances as  $u(q,\zeta) = \Pr(q \mid q(X_i,\zeta) > s(q,\zeta))$ , where 288  $s(q,\zeta)$  is a high threshold corresponding to the quantile q of  $q(X_i,\zeta)$ . These are 289 effectively the previously-mentioned Poincaré recurrences, for the chosen state 290  $\zeta$  (phase space in Fig. 2). The Freitas-Freitas-Todd theorem (Freitas et al. 2010; 291 Lucarini et al, 2012) states that the cumulative probability distribution  $u(\zeta) =$ 292  $F(q,\zeta)$  can be approximated by the exponential member of the Generalised 293 Pareto Distribution (i.e. with shape and location parameters equal to zero). 294 We thus have that: 295

$$u(g,\zeta) = F(g,\zeta) \simeq \exp\left[-\frac{g(\zeta)}{\sigma(\zeta)}\right]$$
(2)

The parameters u and  $\sigma$ , the scale parameter of the Generalized Pareto 296 Distribution, depend on the chosen state  $\zeta$ . From the above, we can define 297 the local dimension d as:  $d(\zeta) = 1/\sigma(\zeta)$ , with  $0 < d < +\infty$ . The Freitas-298 Freitas-Todd theorem thus enables us to estimate numerically d from a series 299 of uv or PV data over the semi-Lagrangian domain based on their Poincaré 300 recurrences. The numerical procedure is rather simple: i) we fix  $\zeta = X_i$  for a 301 given time step i, ii) we fix s to be the threshold corresponding to the quantile 302 q = 0.98. iii) we obtain all the  $u(\zeta)$ , namely the 2% (because q = 0.98) of maps 303 having the smallest euclidean distances from  $\zeta$ , iv) we use the fact that Eq.2 304 is an exponential to estimate  $\sigma$ , its standard deviation, as the average value of 305 u once we subtract s. Here we are just using the fact that in the exponential 306 function, average and standard deviation are equal. 307

Next, we introduce logarithmic returns and high thresholds separately for PV and uv as  $g(PV_i)$ ,  $s_{PV}(q)$  and  $g(uv_i)$ ,  $s_{uv}(q)$  respectively. These allow us to investigate the way in which PV and uv co-vary by defining the co-recurrence ratio  $\alpha$ :

$$\alpha(\zeta) = \frac{\nu[g(PV_i) > s_{PV}(q) \mid g(uv_i) > s_{uv}(q)]}{\nu[g(PV_i) > s_{PV}(q)]}$$
(3)

with  $0 \le \alpha \le 1$ . Here,  $\nu[-]$  is the number of events satisfying condition [-], and all other variables are defined as before. In practice, if all PV recurrences match a uv recurrence, then the number of conditional PV events (numerator) is the same as the number of unconditional PV events (denominator) and hence  $\alpha = 1$ . In contrast, if PV recurrences never match uv recurrences, then the numerator is zero and hence  $\alpha = 0$ . By definition,  $\alpha$  is symmetric with respect to the choice of variable (PV or uv), since  $\nu[g(PV_i) > s_{PV}(q)] \equiv$  $\nu[g(uv_i) > s_{uv}(q)]$ . In other words, the number of events above a given quantile is the same for either variable, given that they are both taken from the same set of TC snapshots. The section "Code availability" provides information on how to download the package used to compute d and  $\alpha$ .

While the derivation of d and  $\alpha$  may seem very abstract, the two metrics 323 can be related intuitively to the physical properties of the tropical cyclones. d 324 is a proxy for the active number of degrees of freedom of the cyclones' instan-325 taneous states, while  $\alpha$  measures the coupling between different variables. The 326 relationship between dynamical systems metrics and the structure of tropical 327 cyclones is elucidated in Figure 3. d and  $\alpha$  are anti-correlated: low dimension-328 ality is generally associated to a high coupling between the PV and uv maps, 329 while the opposite holds for high dimensionality (Fig. 3a). Most of the consid-330 ered time steps fall in a regime of relatively low dimensionality relative to the 331 number of gridpoints in the lagrangian domain  $(41^2)$ , and of low coupling. We 332 first investigate the uv and PV atmospheric patterns corresponding to these 333 timesteps. To do so, we consider all points below the 0.95 quantiles of the 334 d and  $\alpha$  distributions, corresponding to thresholds of  $d_H=30$  and  $\alpha_H=0.35$ . 335 These data show a clear, albeit relatively weak, cyclonic structure in PV, with 336 values peaking at  $\sim 2$  PVU (Fig. 3b). The uv pattern also reflects a cyclonic 337 structure, with values peaking at  $\sim 12 \text{ m s}^{-1}$  (Fig. 3e). The picture is radically 338 different for cyclone timesteps with  $d > d_H$  or  $\alpha > \alpha_H$  (Fig. 3c.d.f.g). High 339 values of d feature a smaller, weaker PV core than the bulk of the data, which 340 is reflected in low values of the square root of the kinetic energy (Fig. 3c.f). 341 High values of  $\alpha$  instead correspond to an intense cyclonic PV core and a 342 correspondingly high uv around it (Figs. 3d,g). The same qualitative features 343 emerge also for the ERA5 cg and HighResMIP data (not shown). To illus-344 trate this for single cyclones, Fig. 4 shows an example of two snapshots: one 345 with very high  $\alpha$  and low d and one with very low  $\alpha$  and high d. These two 346 examples confirm the conclusion drawn from the composite means, altough 347 we cannot directly compare the results presented in Figs. 3-,4 because the 348 first is about composite averages while the second about single cases. 349 350

These results reflect the high degree of symmetry and organization found in 351 intense tropical cyclones with respect to weaker disturbances (e.g., Emanuel, 352 1986, 1997; Montgomery and Smith, 2017). Intense tropical cyclones display a 353 quasi-axisymmetric shape: a state where very few degrees of freedom (i.e., low 354 d values, which typically correspond to high  $\alpha$  values) are needed to describe 355 their dynamics because of the air parcels all aligning with the cyclones' circu-356 lation. On the contrary, the cyclones with higher dimensionality likely display 357 asymmetric or multiple PV patches (as for the example shown in Fig. 4b), 358 with a less organised kinetic energy landscape. This variable geometry of the 359 PV pattern may explain the different degrees of coupling between uv and PV. 360 361



Fig. 3 The scatter plot displays the values of the local dimension d and the co-recurrence  $\alpha$  computed on ERA5 uv and PV maps during tropical cyclone timesteps in the NATL basin. The vertical and horizontal black solid lines mark the 0.95 quantiles of the d and  $\alpha$  distributions, namely  $d_H$  and  $\alpha_H$ , respectively. The maps show composites of PV (b–d) and uv (e–g) for  $d < d_H, \alpha < \alpha_H$  (b,e),  $d > d_H$  (c,f) and  $\alpha > \alpha_H$ (d,g).

The connection between d,  $\alpha$  and cyclone intensity broadly holds when 362 diagnosing the intensity of the cyclones using the minimum SLP, computed 363 from gridded data (Fig. 5). In general, large values of  $\alpha$  (colorscale) correspond 364 to low values of the minimum SLP in both the North Atlantic and eastern 365 North Pacific basins. Moreover, the most intense tropical cyclones phases are 366 marked by a low dimension d. Similar conclusions hold for the HighResMIP 367 data, as further discussed in Sect. 4b. Remarkably, the coarse-graining oper-368 ation on ERA5 data does not alter sensibly the dynamical properties d and 369  $\alpha$ , and the two metrics maintain roughly the same range of values as in the 370 original 0.25° reanalysis (Fig. 5b, d). The explanation for this stability follows 371 that given in Faranda et al (2017) for the SLP data over the North Atlantic: 372



Fig. 4 As Fig. 3b–g, but for an example of a single cyclone snapshot with  $\alpha = 0.61$  and d = 6.02 (a,c) and  $\alpha = 0.08$  and d = 12.36 (b,d).

the dynamical systems metrics are practically insensitive to resolution, provided that the resolution is sufficient to represent the underlying dynamics of
the data. This is the case here since, as previously discussed, ERA5 cg and
ERA5 share near-identical distributions of cyclone SLP minima.

# <sup>378</sup> 4 Bias Corrections of tropical cyclone sea-level <sup>379</sup> pressure minima

# 4.1 Bias Corrections of ERA5 tropical cyclone sea-level pressure minima

We perform two bias corrections for ERA5 minimum sea-level pressure. In both cases we prepare our data as follows. Firstly, we rearrange our set of



**Fig. 5** Scatterplots of minimum SLP vs local dimension d and co-recurrence ratio  $\alpha$  (colorscale) calculated on uv and PV at 850 hPa for (a,c) ERA5 and (b,d) ERA5 cg, in the (a,b) North Atlantic [NATL] and (c,d) eastern North Pacific [ENP] basins.

tropical cyclones randomly. This mixes tropical cyclones from different years 384 and different parts of the cyclone season in the training and in the verification 385 datasets. We thus avoid intraseasonal effects and possible non-stationarities 386 linked to anthropogenic climate change or interannual variability of the 387 atmospheric circulation. We then consider the first 4000 datapoints of our 388 rearranged HURDAT2 SLP minima for each basin as training data and the 380 remaining 2029 datapoints for the North Atlantic basin and 2313 datapoints 390 for the eastern North Pacific basin as verification data. This same split is also 391 applied to ERA5 cg. 392

We next define objective metrics to determine whether our bias corrections improve the cyclone intensities. We use the original Simpson and Saffir (1974) scale of tropical cyclones classification based on the SLP minima and define cyclone categories for the verification datasets (Table 1). We define two error metrics: the total count of tropical cyclones time-steps with the wrong category  $Err_T$ , and the count of major tropical cyclones (intensity $\geq$ 3) with wrong category  $Err_C$ .

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<sup>402</sup> The first bias correction we implement is an unconditional quantile-<sup>403</sup> quantile correction. We begin by subtracting the median of the distributions <sup>404</sup> of SLP minima from the data, which we then add back at the end of the

<sup>405</sup> procedure. We then compute the difference  $\Delta q$  between the empirical cumulative density functions (ECDFs) of SLP minima in HURDAT2 with respect <sup>407</sup> to ERA5 and ERA5 cg evaluated at 100 quantile values q. For each data <sup>408</sup> to correct, the closest quantile q\* in the ECDF(ERA5) or ECDF(ERA5 cg) <sup>409</sup> dataset is found and the value  $\Delta q*$  is added to the original value.

The second bias correction approach is conditioned on the dynamical systems metrics. The results presented in Figures 3 and 5 show that we can discriminate intense tropical cyclones as those having a large value of  $\alpha$  and a small value of d. We test several  $d_H$  and  $\alpha_H$  pairs (using the same convention of Fig.3) to separate the training dataset into intense  $(d < d_H, \alpha > \alpha_H)$  and non-intense cyclones. We next apply the previously described quantile-quantile correction to the two subsets of cyclones separately. We then use a grid-search approach and scan all combinations of  $10 \le d \le 38$  and  $0.1 \le \alpha \le 0.34$ , with resolution  $\Delta d = 1$  and  $\Delta \alpha = 0.1$ , to find the values  $d_c$  and  $\alpha_c$  that minimise the total error

$$Err = Err_T(ATL) + Err_T(ENP) + Err_C(ATL) + Err_C(ENP).$$
(4)

We additionally impose that the chosen values improve upon the unconditional 411 correction for both basins and both  $Err_T$  and  $Err_C$ . By randomizing cyclone 412 timesteps, we obtain two different sets of 100 realizations for ERA5 and ERA5 413 cg training datasets, respectively, which allow to compute two distributions 414 each containing 100 values of  $d_c$  and  $\alpha_c$ . The boxplots of such distributions are 415 presented in Fig.6. We then select the median over each sample. This analysis 416 yields  $d_c = 21$  and  $\alpha_c = 0.16$  for ERA5 and  $d_c = 19$ ,  $\alpha_c = 0.165$  for ERA5 417 cg. The standard deviations of  $d_c$  and  $\alpha_c$  are respectively 4 and 0.04. We can 418 deduce that the minimisation has some sensitivity to the choice of samples. We 419 will refer to these parameters as the best set that realizes the bias correction 420 for the data presented in this study. 421

We illustrate in detail the improvement obtained with the two bias correc-422 tion approaches in Figures 7-8. Panels (a,b) show that the ECDFs of bias-423 corrected SLPs are closer to the verification dataset HURDAT2 than the non-424 corrected ones. However, panels (c,d) show that the correspondence of observed 425 versus modelled SLPs for individual cyclones is not necessarily improved by 426 the bias correction. Specifically, for some of the tropical cyclone timesteps, 427 the bias correction attributes a higher category than the original data. This 428 is shown in panels (e,f) in terms of  $\Delta$  between the categories as estimated for 429 ERA5 (cg) data relative to HURDAT2. Finally panels (g,h) show the evident 430 improvements in terms of intensity histograms: the original non corrected data 431 virtually have no category 4 or 5 tropical cyclones, whereas with the correc-432 tions we are able to retrieve the full cyclone intensity spectrum. The difference 433 between ERA5 and ERA5 cg is limited, although a comparison of panels (d,h) 434 between Figs. 7 and 8 evidences that the coarse-graining does have some effect 435 on the most intense cyclones. As previously noted, a clear difference emerges 436 between the NATL and ENP basins, with the latter generally showing larger 437



Fig. 6 Boxplots for 100 realizations of the grid search procedure used to estimate the values of  $\alpha_c$  and  $d_c$  which minimize the total error in Eq. 4. On each box, the central mark indicates the median, and the bottom and top edges of the box indicate the 25th and 75th percentiles, respectively.

<sup>438</sup> biases for both the uncorrected and corrected data. The difference between
<sup>439</sup> the conditional and unconditional bias corrections also emerges chiefly in the
<sup>440</sup> ENP. Indeed, the two perform comparably in the NATL, while in ERA5 and
<sup>441</sup> especially in ERA5 cg, the conditional correction shows a vastly improved
<sup>442</sup> performance.

Category	wind [m/s]	minimum sea-level pressure [hPa]
1	33-42	$\geq 980$
2	43-49	965 - 979
3	50 - 58	945-964
4	59-69	920-944
5	>69	$\leq 920$

 Table 1
 Saffir-Simpson tropical cyclone intensity classification.

# 443 4.2 Bias Corrections of HighResMip tropical cyclone 444 sea-level pressure minima

When looking at the cyclone SLP minima for the HighResMIP data, we remark immediately the virtual lack of minima below 960 hPa and the reduced range



Fig. 7 Unconditional bias correction and bias correction conditioned on the dynamical systems metrics for the best d and  $\alpha$  parameters combination (see Fig. 6,  $\alpha_c = 0.16$ ,  $d_c = 21$ ) for a realization of the ERA5 data sample. (a,b) Empirical cumulative density functions (ECDFs), (c,d) scatter plots, (e,f) error  $Err_c$  in category intensities (negative values imply underestimation, positive values overestimation), (g,h) histogram of category intensities and  $ERR_T$  in the inset. (a,c,e,g) North Atlantic [NATL], (b,d,f,h) eastern North Pacific [ENP] basins. See legends for details.



Fig. 8 As in Fig. 7 but for a realization of the ERA5 cg data sample, using  $\alpha_c = 0.165$ ,  $d_c = 19$ .

of d and  $\alpha$  values compared to ERA5 or ERA5 cg data (cf. Fig. 9a,c, and 5). 447 These results point to a different dynamical representation of tropical cyclones 448 in HighResMIP. The consequence is that the statistical dependencies between 449 SLP, d and  $\alpha$  in HighResMIP are not the same as in the reference data (ERA5 450 and HURDAT). Up to now, the unconditional and conditional bias correc-451 tion methods applied to adjust cyclone properties were univariate. Hence, 452 dependencies between the three variables (i.e. SLP minima, d and  $\alpha$ ) were 453 not corrected by the unconditional approach, and only partly with the con-454 ditional one. Thus, the resulting tri-variate dependence structures were likely 455 not appropriately represented by the corrected data. To account for this, we 456 now also make use of a multivariate bias correction (MBC) method to adjust 457 not only the univariate distributions but also the dependence between the 458 three variables of interest. To do so, the "Rank Resampling for Distributions 459 and Dependencies" (R2D2) method is applied to adjust jointly (SLP minima, 460 d,  $\alpha$ ). R2D2 relies on an analogue-based method applied to the ranks of the 461 time series to be corrected rather than to their "raw" values (Vrac, 2018). This 462 MBC method can be easily designed to adjust both inter-variable, inter-site 463 and temporal properties (Vrac and Thao, 2020) but is used only in its inter-464 variable configuration in the present study. Figure 9 shows the scatterplots of 465 minimum SLP vs local dimension d and co-recurrence ratio  $\alpha$  without (a.c) 466 and with (b,d) R2D2 correction. The R2D2 correction retrieves SLP minima 467 of order 920 hPa as well as extends the range of values of d and  $\alpha$ , reproducing 468 a pattern closer to the one observed in ERA5. 469

We next apply the unconditional and conditional bias-correction method-470 ologies, as well as the R2D2 method to the HighResMIP simulations. We do 471 not apply the R2D2 method to ERA5 because this is our reference dataset 472 for the computation of the dynamical systems metrics. The main difference in 473 applying the bias correction to model data rather than to reanalysis is that the 474 correction has to be fitted and applied directly to free-running HighResMIP 475 simulations. In such a context, cross-validation techniques for corrections eval-476 uation have been recently heavily criticized (Maraun and Widmann, 2018) 477 due to the influence of the model internal variability on the correction results. 478 Hence, in the following, no separation into training and test data is performed: 479 we correct the bulk cyclone statistics for all selected cyclones in the IPSL-480 CM6A-ATM-ICO-HR simulation. We first estimate the ECDFs and compute 481 the  $\Delta$  function between HighResMIP and HURDAT2 data. We then cor-482 rect the full dataset using the unconditional, conditional on  $\alpha, d$  – using the 483 ERA5 cg values  $d_c$  and  $\alpha_c$  – and R2D2 corrections. The results are shown in 484 Figure 10. For the ECDFs (panels a,c), corrections obtained with or without 485 the dynamical systems metrics improve, once again, the distribution of SLP 486 minima. The conditional and unconditional corrections appear comparable in 487 the NATL, but show a clear difference in the ENP. The R2D2 correction is 488 virtually indistinguishable from HURDAT in both basins. When looking at 489 the tropical cyclone intensities (panels b,d) we observe that the R2D2 correc-490 tion of SLP minima provides a distribution of intensities which is very close to 491



Fig. 9 Scatterplots of minimum SLP vs local dimension d and corecurrence ratio  $\alpha$  (colorscale) calculated on uv and PV at 850 hPa for (a,c) HighResMIP; (b,d) HighResMIP corrected with R2D2, in the (a,b) North Atlantic [NATL] and (c,d) eastern North Pacific [ENP] basins.

that of the HURDAT2 data in both basins. Over the NATL, the R2D2 shows a clear improvement over the other corrections. In the ENP, it is close to the unconditional correction, which outperforms the conditional correction. Overall, these results suggest that, when applying R2D2, we are able to take into full account the information provided by the two dynamical systems metrics.

### <sup>497</sup> 5 Summary and implications of the results

Starting from the observation that gridded datasets of tropical cyclones have 498 a large bias in the representation of the intensity of extreme cyclones, we have 499 introduced a bias-correction procedure. We have used: i) an unconditional 500 quantile-quantile correction of the sea-level pressure minima of cyclones 501 timesteps towards the HURDAT2 reference dataset; ii) a correction condi-502 tioned on two dynamical systems metrics (local dimension and co-recurrence 503 ratio); and iii) the R2D2 correction. We have applied the first two approaches 504 to ERA5 data, both at the highest available resolution and in a coarse-505 grained version. We have further applied all three approaches to data from 506 the IPSL-CM6A-ATM-ICO-HR HighResMIP model. When using the dynam-507 ical systems metrics, we use the dynamical information from an underlying 508 reduced phase space incorporating the square root of the horizontal kinetic 509



Fig. 10 Unconditional, R2D2, and conditional dynamical systems metrics bias corrections for the IPSL-CM6A-ATM-ICO-HR model. The conditional dynamical systems metrics bias corrections uses the best  $d_c = 19$  and  $\alpha_c = 0.165$  parameters combination from ERA5 cg. Panels (a,c) show Empirical Cumulative Density Functions (ECDFs). and (b,d) histograms of category intensities for the North Atlantic [NATL] (a,b) and eastern North Pacific [ENP] (c,d) basins.

energy uv and potential vorticity PV at 850 hPa. We have observed that the 510 dynamical systems metrics are able to track intense cyclones as organized 511 states of the dynamics, yielding low dimensionality and high coupling. While 512 all bias corrections improve the bulk statistics of tropical cyclone intensity 513 representation in our datasets, the categorisation for individual cyclones is 514 not always improved. The conditional bias correction tends to perform better 515 when the underlying relationship between the predictors and the response 516 variable is strong and well-defined, whereas the unconditional bias correction 517 can be more effective when the relationship is weaker or more variable. For 518 the HighResMIP model, the best bias correction is the multivariate R2D2 cor-519 rection which takes into account the relationships among SLP, d and  $\alpha$ . This 520 suggests that accounting for the multivariate dependence structures associated 521

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with the dynamical systems metrics is crucial to correcting the distribution 522 of tropical cyclone intensities. We also observe non-neglegible differences in 523 the bias correction performances in the two Atlantic and Pacific basins that 524 could be further investigated in the future. For example, the conditional bias 525 correction in the HighResMIP model underperforms in the ENP relative to 526 its unconditional counterpart, yet this is not observed in the reanalysis. We 527 also point out that while the optimal combination of d and  $\alpha$  shows some 528 variability when reshuffling the data, the changes are small. While it is true 529 that the sample used in this study is large, with over 10000 storm timesteps, 530 we would need to repeat the grid-search if significant changes in the storm 531 sample occur, such as a major shift in the frequency or intensity of storms. 532

These considerations have a number of concrete implications for current 534 research on tropical cyclones. Current GCMs — and even reanalysis products 535 - struggle in reproducing minimum sea-level pressures comparable to those 536 observed. Our study offers a way of mapping intense cyclones in  $d, \alpha$  space 537 and a procedure to correct biases in both century-long reanalysis products 538 and high-resolution GCMs. This, in turn, may provide a strategy for studying 539 changes in tropical cyclone intensity driven by anthropogenic forcing. Indeed, 540 while d and  $\alpha$  may not be used to provide a deterministic indication of cyclone 541 intensity, they do provide a robust constraint for statistical correction. The 542 large range of local dimensions associated with the dynamics of different phases 543 of tropical cyclones may explain why it is so difficult to adequately represent 544 them in numerical models. Follow-up studies will include the use of a larger set 545 of HighResMIP data under different forcing scenarios, to test systematically 546 the R2D2 correction on model data. The bias correction procedures will then 547 be adapted to take into account the non-stationarities introduced by anthro-548 pogenic forcing, e.g. by replacing the quantile-quantile mapping with a CDF-t 549 correction (Vrac et al, 2012) allowing to account for climate change in the cor-550 rection procedure. A further avenue for future work will be to move from the 551 pointwise correction of minimum SLP performed here, to correcting the spa-552 tial structure of the field, using multivariate bias correction techniques (e.g. 553 Cannon, 2018; Vrac, 2018; Robin et al, 2019; Vrac and Thao, 2020) or tools 554 from machine learning (e.g. François et al, 2021). 555

## 556 Statements and declarations

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- The Code availability: main results of this work were obtained 582 using Matlab. scripts for computing the dimension The and 583 coefficient available the corecurrence are by downloading the 584 https://fr.mathworks.com/matlabcentral/fileexchange/ package 585 95768-attractor-local-dimension-and-local-persistence-computation 586
- Authors' contributions: DF performed the analysis. DF and GM co-designed the analyses. ST and SB prepared the datasets. All authors participated to the manuscript preparation and contributed to the interpretation of the results.

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