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Interaction between orthographic and graphomotor constraints in learning to write

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Highlights

- Handwriting of 1st graders is influenced by both orthographic and motor constraints
- Motor and spelling processes interact from the beginning of handwriting acquisition
- This calls into question the relevance of evaluating them separately

Abstract

We investigated the combined effects of orthographic and graphomotor constraints as a function of handwriting proficiency in children. Twenty-four first graders, 20 third graders, and 21 fifth graders wrote single five-letter words in cursive writing on a sheet of paper affixed to a digitizing tablet. The words were chosen according to two orthographic constraints, namely their lexical frequency and the graphemic complexity of the last three letters, and one graphomotor constraint resulting from the motor difficulty of tracing the first letter. In addition to massive improvements of handwriting with grade, the results revealed, in the youngest group only, an interaction between first-letter difficulty and lexical frequency. This finding suggests that, before handwriting movement becomes automated, the cognitive resources needed for retrieving word spelling interferes with motor processing while writing a difficult letter. When students start learning to write, they are particularly sensitive to the combination of orthographic and graphomotor constraints.

Keywords: handwriting; acquisition; spelling; motor control; delayed copy
1. Introduction

Learning to write words constitutes a double challenge: students have to learn both how to spell the words and how to trace the letters. The aim of this study was to find out whether the effect of orthographic constraints associated with word spelling is combined with the effect of graphomotor constraints associated with letter formation during handwriting acquisition, in primary school students. The term “constraints”, which will be used throughout this article, is considered from a generic perspective: it refers to factors, or situations, which have an adverse effect on performance. Orthographic constraints modulate spelling processes, independently of the motor output (e.g., typing, oral spelling, or handwriting). Here, two orthographic constraints were investigated: a) lexical frequency, and b) letter-sound relationships inside the word, as indexed by the graphemic structure.

Graphomotor constraints refer to factors that influence the motor processes involved in controlling handwriting movements, independently of the linguistic content (e.g., at high speed or with eyes closed). Here, we studied the graphomotor constraint arising from motor difficulty in letter formation.

In adults, the relationship between spelling and graphomotor processes has first been considered in van Galen’s model (1991), which proposes parallel processing between spelling (high-level) and graphomotor (low-level) modules in which “higher modules are further ahead to real-time output than lower modules” (p. 182). This vision has been refined in the parallel and cascading model of writing (Olive, 2014), where the dynamics of parallel processing is flexible according to the cognitive resources that have to be allocated to either spelling or graphomotor control. This idea has been tested by Lambert and colleagues (2011), who investigated handwriting in adults who were copying series of words that varied in lexical frequency and orthographic regularity (e.g.: FEMME /fam/, woman is irregular in French because the spelling does not respect the most frequent phoneme-grapheme conversion corresponding to /a/ = A). From the combined analysis of eye and pen movements, the authors identified periods during which participants searched for visual information about the template (the word to be copied) while writing the previous word (meaning that they were processing spelling and graphomotor aspects of the task in a parallel and cascaded fashion). They observed that the extent of parallel processing depended on the orthographic constraints of the word being written: planning the next
word ahead while writing was more probable when the current word being written was frequent and regular, thus confirming the parallel and cascaded account.

The relationship between spelling and graphomotor processes has also been investigated through the study of the effects that orthographic constraints exert on handwriting movements (e.g., Delattre, Bonin & Barry, 2006; Kandel, Álvarez & Vallée, 2006; Kandel & Perret, 2015; Lambert, Alamargot, Larocque, & Caporossi, 2011; Roux, McKeeff, Grosjacques, Afonso, & Kandel, 2013). The basic assumption of these studies is that factors that impact the retrieval of the word’s spelling (e.g., lexical frequency or orthographic regularity) also impact the motor processes involved in the control of handwriting movements. Several indexes calculated from the time-course of the pen trajectory can be used to characterize the efficiency of handwriting behavior (duration, velocity, pauses...). For instance, in a single word copy task, Roux and colleagues (2013) found that letter duration was longer for irregular than for regular words. This convincingly shows that handwriting movement can be impacted by the orthographic constraints imposed by the words being written.

In children, it has been shown that spelling processing changes during the acquisition of handwriting. Humblot, Fayol and Lonchamp (1994) evaluated the performance of Grade 1 and Grade 2 students in a copy task where words varied in frequency and regularity. They concluded that the acquisition of handwriting starts with a letter-by-letter planning, then a syllable-by-syllable planning, and ends with a whole-word planning when the word is frequent. In order to assess whether this evolution affected graphomotor processes, Kandel & Perret (2015) investigated the effects of word frequency and orthographic regularity on word production in students from Grade 3 to Grade 5. They observed that both variables affected handwriting execution in all groups in such a way that the writing of words with high orthographic constraints (irregular or infrequent) took longer than that of words with low orthographic constraints (frequent or regular). To go a step further, Afonso, Coalla, González-Martín and Cuetos (2018) studied the effect of word frequency on handwriting duration in both a spelling-to-dictation task and a copy task in Grade 2, 4, and 6 students. Interestingly, the authors observed that the effect of frequency decreased with the mastery of handwriting: it was significant in grade 2, marginally significant in Grade 4 and
disappeared in Grade 6. This suggests that although students’ handwriting is generally sensitive to orthographic constraints, improvement of handwriting with development and practice allows a more independent management of spelling and motor processes.

Another important orthographic constraint seems also to draw on information about letter-sound relationships as indexed by the graphemic structure (e.g., Kandel & Spinelli, 2010; Spinelli, Kandel, Gueressimovitch, & Ferrand, 2012). In French, at least 34 complex graphemes, composed of more than one letter, have been identified (Catach, 1995). Kandel & Spinelli (2010) compared the handwriting of words containing simple graphemes (e.g., $E$ in SET) to words containing complex graphemes (e.g., $E$ in SEA for a two-letter grapheme). They observed that both the target letter (e.g., $E$) and the preceding letter (e.g., $S$) took more time to be written in the case of complex graphemes. They concluded that the processing of graphemes starts before the actual production of the grapheme and remains activated in parallel with motor processes during the execution of handwriting. This finding was extended to first graders who had not yet mastered handwriting (Kandel, Soler, Valdois & Gros, 2006).

From a motor point of view, writing by hand requires a sophisticated coordination of the muscles and joints recruited in order to form letters consistently as quickly as possible. Graphomotor skills are acquired through one of the longest and most tedious motor learning processes known to humans. In early stages of learning to write, students program their movements stroke-by-stroke until the letters are learned and stored in long-term memory in motor programs (Séraphin Thibon, Gerber & Kandel, 2018). This leads to the question of what motor constraints are, and how they influence performance during the acquisition of handwriting. This question has been explored using tasks in which students had to change their handwriting size, velocity, or script. In 2008, Chartrel & Vinter observed that issuing instructions to write between horizontal lines and to increase speed facilitated the formation of associations between the strokes of a letter and thus benefited students of 5-7 years of age learning to write. Between 5 and 12 years, Bo, Barta, Ferencak, Comstock, Riley and Krueger (2014) showed that printed letters tended to be written with a higher consistency than cursive letters. In both dyslexic and typically developing children, Pagliarini et al. (2015) showed that writing a word with cursive letters turned out to be generally more challenging than writing it with upper-case letters. The authors suggested that the late introduction of
cursive training in the Italian educational system might explain this result. Furthermore, typically developing children, when asked to write big letters or to write quickly, modulated their handwriting movements to maintain the absolute and relative duration of letters (isochrony and homothety principles) whereas children with dyslexia failed to do so (Pagliarini et al., 2015).

Graphomotor constraints also result from the motor difficulty arising from the formation of a letter. Jolly, Huron and Gentaz (2014) analyzed the handwriting of the 26 letters of the Latin alphabet in students followed from preschool, to mid- and end- of the first Grade and second Grade. The results showed a wide variability across letters regarding the students’ motor performance and progress. This variability may be explained by the biomechanical constraints of the effector and coordination dynamics (e.g., Kelso, 1995) that determine a preferential direction of rotation (Meulenbroek, Vinter & Mounoud, 1993), preferential orientations (Dounskaia, Van Gemmert and Stelmach, 2000), and preferential curvatures (Athènes et al. 2004) in the formation of the written trace. Finally, the rotation and pointing movements (pen lifts) involved in letter formation are also of interest. Recently, Seraphin-Thibon et al. (2019) studied the developmental trajectory of students' graphomotor skills as a function of the characteristics of upper-case letters, involving either pointing or rotation movements. They observed that letters with rotations were produced with more velocity peaks (an index of movement dysfluency) and a longer duration than letters with straight strokes and pointing movements.

To sum up, the reported literature indicates that 1) the processing of the orthographic content of words has an impact on the production of writing in adults and children, and 2) strong graphomotor constraints related to writing conditions and letter complexity also influence handwriting movements in children. But to our knowledge, the combined effect of orthographic and graphomotor constraints during handwriting acquisition has not yet been investigated. One study explored this question in adults: Sausset, Lambert, Olive and Larocque (2012) manipulated graphomotor constraints through letter case (upper- / lower-case), visual control (with / without), and letter size, and also an orthographic constraint through the number of syllables in the words, considered as processing units involved in spelling processing (Kandel, Peereman, Grosjacques, & Fayol, 2011). They observed that when graphomotor constraints were high, the writers took longer pauses between syllables,
indicating that each syllable was processed directly before its actual production. When they were low, the syllable processing took place before the onset of writing. This demonstrates that the dynamics of spelling and motor processes vary as a function of both orthographic and graphomotor constraints in adults.

The present study aimed to investigate the combined effect of orthographic and graphomotor constraints on handwriting in students who are learning to write. We asked students at different levels of handwriting proficiency (in Grades 1, 3, and 5) to write single words, without the presence of the template (the word to be copied). We manipulated both the graphomotor constraints associated with the difficulty of tracing the first letter, and two orthographic constraints: the word’s lexical frequency, and the graphemic complexity associated with the last letters. We tested the interaction between these constraints in the different level groups. Knowing that both orthographic (Afonso et al., 2018) and graphomotor (Séraphin Thibon et al., 2018) constraints are larger in students who do not yet master handwriting, we hypothesized that the interaction between the two types of constraints would be larger in younger than in older students. We assume that the younger students will produce a slower and less fluent movement when tracing a difficult letter in a complex or infrequent word than when only one of the two types of constraints is present (tracing an easy letter in a complex or infrequent word or tracing a difficult letter in a simple or frequent word). In order to quantify and compare the graphomotor constraint, we conducted a pre-experiment in which Grade 1 students were asked to copy bigrams in cursive. The aim was to select two letters, respectively representative of high and low graphomotor constraint for students who are at the beginning of cursive acquisition.

2. Pre-experiment: Characterizing graphomotor constraints

2.1. Methods

2.1.1. Participants

Nineteen students in Grade 1 volunteered for the experiment (6;8 years; 8 girls; 3 left-handers for handwriting). Students who were receiving intervention for reading and/or writing difficulties were not included, neither were students who had resumed or skipped a school grade. The students had normal or corrected-to-normal vision. This study was
conducted between March and April and in accordance with local norms and guidelines for the protection of human subjects. This research was approved by the local educational authorities, the school directors, and the teachers. Furthermore, parents signed an informed consent sheet prior to the experiment.

2.1.2. Task

The experiment was conducted individually at school, in a quiet classroom. After a quick familiarization task consisting of writing their first name, students were asked to write isolated bigrams in cursive handwriting on a white sheet of paper affixed to a digitizing tablet (Wacom Intuos 4L, sampling frequency 100 Hz), using an inking pen. Each bigram was presented on a small white paper (5 x 7 cm label) in lowercase cursive letters (Cursive standard font, font-size: 44) and the template remained present until the student had finished writing the bigram. Students were asked to write at their usual speed. No time limit was applied during the task and the presentation order was randomized between students. For data acquisition, we used JAVA software developed in the laboratory.

2.1.3. Stimuli

Eleven consonant-vowel bigrams were selected for the task. Only the consonant varied between the bigrams, the vowel was identical for all conditions (letter ‘i’) to avoid possible motor anticipation on the first letter, a known phenomenon in cursive handwriting (Orliaguet, Kandel & Boë, 1997). The selected consonants were: ‘b’, ‘c’, ‘f’, ‘g’, ‘l’, ‘m’, ‘p’, ‘r’, ‘s’, ‘t’, and ‘v’. Less frequent letters as ‘h’, ‘j’, ‘k’, ‘q’, ‘w’, ‘x’, and ‘z’ were not considered because some first graders did not know how to trace them.

2.1.4. Data analysis

The first letter of each bigram was analyzed. In order to identify a common endpoint, the ascendant stroke of the second letter ‘i’ was included. From the recorded (x, y) coordinates and pen pressure, the first in-air stroke and the strokes produced after the
maxima of the letter $i$ were deleted. The segmentation was conducted with Matlab ®. In order to reduce the statistical risk of Type I errors, four complementary variables were considered: the duration, the mean velocity, the number of stops, and the letter size. These variables respectively describe the temporal (duration), kinematic (mean velocity and number of stops) and spatial (size) content of handwriting performance (see figure 1):

**Figure 1.** Schematic illustration of data processing. (A) Example of the bigram “fi” written by a child. In grey: the whole word recorded. In red: the in-air movements (pen lifts). In black and surrounded: the first letter segmented for further analyses. (B) Absolute velocity profile as a function of time (filtered with a cutoff frequency of 10 Hz) for illustrating the temporal and kinematic variables.

- The duration corresponds to the time elapsed between the beginning and end of letter production, including in-air movement if the writer lifts the pen.
- The mean velocity is the mean of absolute velocity from the time the pen was first in contact with the tablet until the letter was completed. In-air movements were not considered for computing mean velocity.
The number of stops corresponds to the total number of periods that the pen was in contact with the paper but did not move for at least 35 milliseconds.

The letter size corresponds to the distance between the minimal and maximal positions of the letter in the y-axis.

A cluster analysis was applied on the complete data set in order to identify the difficulty level of the letters. All variables were converted to z-scores (i.e. the variables were centered and reduced to a range between 0 and 1) then analyzed by interactive partitioning (K-means), minimizing the within-cluster variability and maximizing the between-cluster variability. This cluster analysis allowed us to separate letters into two categories: easy to write letters (cluster 1) from difficult to write letters (cluster 2).

2.2. Results

The cluster analysis on z-scores confirmed the presence of two clusters with an inter-cluster Euclidian distance of 0.74. Cluster 1 included seven letters: \(c, l, m, r, s, t, \) and \(v\). Cluster 2 included four letters: \(b, f, g, \) and \(p\). The mean performance for each letter is reported in table 1. The Cluster 1 comprised ‘easy’ letters that, on the whole, were small, written with short duration, low velocity, and few stops. The Cluster 2 comprised ‘difficult’ letters which, on the whole, were bigger, written with a longer duration, a high velocity, and more stops.

<table>
<thead>
<tr>
<th></th>
<th>(c)</th>
<th>(l)</th>
<th>(m)</th>
<th>(r)</th>
<th>(s)</th>
<th>(t)</th>
<th>(v)</th>
<th>(b)</th>
<th>(f)</th>
<th>(g)</th>
<th>(p)</th>
<th>Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Duration</strong></td>
<td>1.7 (0.1)</td>
<td>1.9 (0.1)</td>
<td>3.0 (0.1)</td>
<td>2.3 (0.1)</td>
<td>2.3 (0.1)</td>
<td>3.0 (0.1)</td>
<td>2.7 (0.1)</td>
<td>3.5 (0.1)</td>
<td>3.6 (0.1)</td>
<td>3.6 (0.1)</td>
<td>3.0 (0.1)</td>
<td>2.8</td>
</tr>
<tr>
<td><strong>Velocity</strong></td>
<td>(12.8 (0.3))</td>
<td>17.0 (0.4)</td>
<td>(12.1 (0.3))</td>
<td>(10.4 (0.2))</td>
<td>(12.5 (0.3))</td>
<td>16.5 (0.5)</td>
<td>(10.1 (0.2))</td>
<td>(13.2 (0.3))</td>
<td>15.7 (0.4)</td>
<td>14.4 (0.3)</td>
<td>18.1 (0.5)</td>
<td><strong>13.9</strong></td>
</tr>
<tr>
<td><strong>Stops</strong></td>
<td>2.0 (0.1)</td>
<td>0.9 (0.1)</td>
<td>(3.8 (0.1))</td>
<td>(4.2 (0.1))</td>
<td>(3.4 (0.1))</td>
<td>(3.4 (0.1))</td>
<td>3.1 (0.1)</td>
<td>4.5 (0.1)</td>
<td>4.3 (0.2)</td>
<td>2.7 (0.1)</td>
<td>3.9 (0.2)</td>
<td><strong>3.3</strong></td>
</tr>
<tr>
<td><strong>Size</strong></td>
<td>5.7 (0.1)</td>
<td>(12.1 (0.3))</td>
<td>5.0 (0.1)</td>
<td>5.4 (0.1)</td>
<td>6.0 (0.1)</td>
<td>8.5 (0.2)</td>
<td>5.3 (0.1)</td>
<td>(12.7 (0.3))</td>
<td>(17.6 (0.5))</td>
<td>(12.95 (0.3))</td>
<td>(13.6 (0.4))</td>
<td><strong>9.5</strong></td>
</tr>
</tbody>
</table>

Table 1: Mean (standard error) performance for each letter. In bold, value above (below for the velocity) the mean value (on the right). Cluster 1: Black letters on white background. Cluster 2: White letters on black background.
2.3. Interim discussion

This pre-experiment confirmed that \( b, f, g, \) and \( p \) are more difficult to trace than the other tested consonants for 1\(^{st} \) grade students. Letters classified as more difficult have the common characteristic of being composed of several strokes that can be large and that demand significant rotational changes between the strokes. Overall, our results extend this finding to lowercase cursive letters and confirms that the graphomotor constraint of a letter depends on how many strokes it consists of, the difficulty of tracing each stroke, how easy transition between them is (\textit{i.e.}, with turning points – Chang & Yu, 2010). Although some letters took longer to be produced, the writing velocity did not appear a relevant index of automation. This finding is consistent with previous studies in which the authors reported that children with dysgraphia did not write more slowly than proficient children because of their tendency to write larger (\textit{e.g.}, Prunty, Barnett, Wilmot, and Plumb, 2013). In the present study, the more difficult letters contained larger strokes than the easy letters, compensating for any tendency to write them more slowly.

For the next experiment, we finally selected the letters \( f \) and \( t \) as representative of difficult and simple letter, respectively. This choice was based on the conclusion of a work-meeting with two French teachers, taking account our need to build a strictly controlled material with both high and low motor constraints, comprising 5-letter words with an ‘i’ in second position, having a low and high frequency, and a simple vs. complex grapheme in the 3 last letters. Out of curiosity, we checked the developmental values published by Jolly, Huron and Gentaz (2014) in their supplementary content for these two letters. These authors measured several temporal, spatial and kinematic variables of letter production in children between preschool, mid-year and end-year of 1st and 2nd Grade. The letter \( t \) and \( f \) demonstrated different developmental patterns, especially between 1st grade and 2nd Grade mid-year: at 1st grade mid-year, the number of slow movements and static moments was higher for the \( f \) than for the \( t \), although it was comparable at 2nd grade mid-year. The reduction of slow movement and static moment represented respectively 39% and 53% for the \( f \) and 28% and 34% for the \( t \), confirming more progress (\textit{i.e.} a higher difficulty) for the former than for the later one.
3. Main experiment: Interaction between graphomotor and orthographic constraints

3.1. Methods

3.1.1. Participants

Sixty-five French students from two elementary schools volunteered for the experiment, including 24 students in Grade 1 (6;7 years; 13 girls; 3 left-handers for handwriting), 20 in Grade 3 (8;6 years; 11 girls; 2 left-handers for handwriting), and 21 in Grade 5 (10;7 years; 16 girls; 3 left-handers for handwriting). Student who were receiving intervention for reading and/or writing difficulties were not included, neither were students who have repeated or have skipped a school year. The students had normal or corrected-to-normal vision. This study was conducted between March and April and in accordance with local norms and guidelines for the protection of human subjects. This research was approved by the local educational authorities, the school directors, and the teachers. Furthermore, parents signed an informed consent sheet prior to the experiment.

3.1.2. Task

The experiment was individually conducted at school, in a quiet classroom. After a quick familiarization task consisting of writing their first name, the child was asked to write several single words in cursive on a sheet of paper affixed to a digitizing tablet (Wacom Intuos 4L, sampling frequency 100 Hz), using an inking pen. Each word was written twice to avoid any incorrect production (with errors or unusual performance). The template (word to be copied) was first displayed (in lowercase cursive letters, using the Cursive standard font, font-size: 44) on a label (5 x 7 cm) that the experimenter showed and read aloud to the child. Then, the template was hidden before the child started to write. No time limit was applied during the presentation of the template: the experimenter waited for the child to indicate that the template could be removed. Before the second trial, the previous performance was masked but the child could ask to see and hear the template again. The presentation order was randomized between students. They were asked to write at their usual speed. A black line had been traced on each white sheet to help to write horizontally. For data acquisition, we used JAVA software developed in the laboratory.
3.1.3. Stimuli and procedure

A total of eight 5-letter words were selected for the task, including four with the first bigram ‘fi’ and four with the first bigram ‘ti’. These words were selected on the basis of A) the graphomotor constraint arising from the difficulty of tracing the first letter as characterized in the pre-experiment (easy vs. difficult), B) their lexical frequency from the French database Lexique 3 (high-frequency words, i.e., > 50 occurrences per million words, vs. low-frequency words, i.e., < 2 per million; New 2006; New, Pallier, Brysbaert, & Ferrand, 2004) and from the French children database Manulex (CP-CM2 U > 50 for high-frequency words and CP-CM2 U < 1 for low-frequency words; Lété, Sprenger-Charolles & Colé, 2004), and C) the graphemic complexity of the last three letters (simple vs. complex grapheme) also from the Lexique 3 database. As in the pre-experiment, the second letter was identical for all conditions to avoid possible motor anticipation effect on the first letter. The word length was also identical to avoid possible word length effects on working memory (e.g., Baddeley, Thomson & Buchanan 1975). Finally, the orthographic regularity was also checked, and only regular words were chosen. The stimuli are reported in table 2.

<table>
<thead>
<tr>
<th></th>
<th>finir (end)</th>
<th>fille (girl)</th>
<th>firme (firm)</th>
<th>fioul (fuel oil)</th>
<th>titre (title)</th>
<th>tirer (pull)</th>
<th>tibia (tibia)</th>
<th>titan (giant)</th>
</tr>
</thead>
<tbody>
<tr>
<td>First-letter graphomotor constraint</td>
<td>Difficult – “f”</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Easy – “t”</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word frequency</td>
<td>HF</td>
<td>LF</td>
<td>HF</td>
<td>LF</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Graphemic complexity</td>
<td>simple</td>
<td>complex</td>
<td>simple</td>
<td>complex</td>
<td>simple</td>
<td>complex</td>
<td>simple</td>
<td>complex</td>
</tr>
</tbody>
</table>

Table 2: Stimuli according to the first-letter graphomotor constraint, the word frequency (HF: high-frequency or LF: low-frequency), and the graphemic complexity of the three last letters.

3.1.4. Data analysis

The first letter of each bigram was analyzed in the same way as in the pre-experiment. In order to identify a common endpoint, the ascendant stroke of the second letter ‘i’ was also included. Incorrect words were not analyzed. From the 1040 trials collected (65 students * 8 items * 2 trials), 13 trials were not considered for analysis. The percentage of
trials with errors was about 1.0 % in 1st grade, 2.5% in 3d grade, 0.3 % in 5th grade. The same temporal (duration), kinematic (mean velocity and number of stops) and spatial (size) variables were considered in this experiment. A table with correlations between the variables, within grades, is presented in Appendix. For these variables, both frequentist and Bayesian statistics were conducted. For the sake of clarity, we report the results of the frequentist statistics (analyses of variance (ANOVAs) complemented with Bonferroni post-hoc tests when necessary) in the following section. The complete description of the Bayesian analyses and their results are reported in supplementary materials. For the frequentist analysis, we averaged the performance of the two trials when they were correct. To make sure that there was no difference related to the inclusion of one or both trials, we inspected the performance of the students who did only one trial with those from the two averaged trials and found no outliers from performance based on a single trial.

3.2. Results

3.2.1. Duration

The ANOVA revealed a Graphomotor constraint by Grade interaction $F(2, 62) = 7.84, p <.001. \eta^2_p = 0.20$, and a Graphomotor constraint by Frequency interaction, $F(1, 62) = 5.23, p <.05, \eta^2_p = 0.08$. As can be seen in Figure 2A, the Bonferroni post hoc tests showed that students in Grade 1 spent more time writing the difficult letter f when the word was infrequent than when it was frequent ($p < 0.01$). However, this effect of frequency was not observed for the easy letter t, nor for the two other groups ($p = 1$). The ANOVA also revealed a main effect of Grade on mean duration, $F(2, 62) = 63.20, p <.001. \eta^2_p = 0.67$. The post-hoc analysis revealed that 1st graders spent more time writing the first letter than 3rd and 5th graders ($p < .001$ for both comparisons) whereas 3rd and 5th graders did not significantly differ from each other. Finally, the analysis also revealed a main effect of Graphomotor constraint, $F(1, 62) = 74.24, p <.001. \eta^2_p = 0.54$, confirming that the letter f required more time to be written than the letter t. The analysis evidenced neither main effect nor interaction involving graphemic complexity. Interitem correlations between words with simple vs. complex grapheme were between 0.8 and 0.9 ($R^2\text{finir-fille} = 0.87; R^2\text{firme-fioul} = 0.89; R^2\text{titre-tirer} = 0.81; R^2\text{tibia-titan} = 0.80$).
3.2.2. Mean velocity

The analysis revealed a Graphomotor constraint by Frequency interaction, $F(1, 62) = 4.98; p < .05. \eta^2_p = 0.07$, and the post-hoc tests showed that the frequency effect was present in writing the letter $f$ ($p < 0.05$) but not in writing the letter $t$ ($p = .81$, see Figure 3A).
In other words, the first letter of low-frequency words was written more slowly when it imposed stronger graphomotor constraints. The analysis also revealed a main effect of Grade, $F(2, 62) = 26.16$, $p < .001$. $\eta^2_p = 0.46$, and post-hoc tests confirmed that 1\textsuperscript{st} graders wrote more slowly than 3\textsuperscript{rd} and 5\textsuperscript{th} graders ($p < .001$ for both comparisons) whereas 3\textsuperscript{rd} and 5\textsuperscript{th} graders did not significantly differ from each other (see Figure 3B). The ANOVA also showed a main effect of Graphomotor constraint, $F(1, 62) = 31.21$, $p < .001$. $\eta^2_p = 0.33$: The letter $f$ was written faster than the letter $t$. Finally, the analysis evidenced neither main effect of graphemic complexity nor interaction between graphemic complexity and the other factors. Interitem correlations between words with simple vs. complex grapheme were between 0.7 and 0.9 ($R^2 \text{finir-fille} = 0.77; R^2 \text{firme-fioul} = 0.89; R^2 \text{titre-tirer} = 0.81; R^2 \text{tibia-titan} = 0.90$).

![Figure 3](image_url)

**Figure 3.** Mean velocity, according to (A) the word frequency (LF: low-frequency vs. HF: high-frequency) and the first-letter graphomotor constraint ($f$ vs. $t$), and (B) the Grade level (Grade 1, 3, and 5). Error bars correspond to standard error of the mean.

### 3.2.3. Number of stops

The ANOVA revealed a Frequency by Grade interaction, $F(2, 62) = 3.25$, $p < .05$. $\eta^2_p = 0.09$, a Graphomotor constraint by Frequency interaction, $F(1, 62) = 4.82$, $p < .05$. $\eta^2_p = .07$, and the Graphomotor constraint by Frequency by Grade double interaction, $F(2, 62) = 4.09$, 


\(p < .05. \eta^2_p = 0.12.\) As can be seen in Figure 2B, the Bonferroni’s post-hoc tests showed that the Frequency effect was only present in 1st graders writing the letter \(f\) \((p < .001)\). The analysis also revealed a main effect of Grade, \(F(2, 62) = 47.70, p < .001. \eta^2_p = 0.61: 1\text{st}\) graders wrote with more stops than 3rd and 5th graders \((p < 0.001\) for both comparisons). Here again, 3rd and 5th graders did not significantly differ from each other and the analysis evidenced neither main effect of graphemic complexity nor interaction between graphemic complexity and the other factors. Interitem correlations between words with simple vs. complex grapheme were between 0.5 and 0.8 \((R^2 \text{ finir-fille} = 0.52; R^2 \text{ firme-fioul} = 0.71; R^2 \text{ titre-tirer} = 0.77; R^2 \text{ tibia-titan} = 0.66)\).

### 3.2.4. Letter size

The analysis revealed a Graphomotor constraint by Grade interaction, \(F(2, 62) = 6.27, p < .01. \eta^2_p = 0.17.\) As can be seen in figure 4A, the size of letter \(f\) tended to decrease between the 1st grade and the 3rd but the post-hoc tests did not confirm these tendencies \((p > 0.10)\). As expected, the analysis revealed a main effect of Graphomotor constraint, \(F(1, 62) = 313.07, p < .001. \eta^2_p = 0.83: \) the written letter \(f\) was larger than the letter \(t\). Finally, the analysis revealed a main effect of Graphemic Complexity \(F(1, 62) = 4.36, p < .05, \eta^2_p = 0.06,\) and the Graphomotor constraint by Graphemic Complexity interaction tended to be significant, \(F(1, 62) = 3.88, p = .053. \eta^2_p = 0.05.\) As can be seen in figure 4B, the Bonferroni post-hoc analysis revealed that the size of \(f\) increased with graphemic complexity \((p < .05)\) whereas the size of \(t\) did not. Interitem correlations between low-frequency and high-frequency words were between 0.7 and 0.9 \((R^2 \text{ finir-firme} = 0.79; R^2 \text{ fille-fioul} = 0.90; R^2 \text{ titre-tibia} = 0.81; R^2 \text{ tirer-titan} = 0.89)\).
4. Discussion

This study aimed to evaluate the combined effects of orthographic and graphomotor constraints on handwriting in beginning, intermediate and advanced writers. From the pre-experiment, we selected two letters with different graphomotor constraint: an easy letter ‘t’ and a difficult letter ‘f’. As expected, in the main experiment, the letter ‘f’ was more difficult to write than the letter ‘t’ in all groups. The longer duration, as well as the higher mean velocity are obviously related to the size of the ‘f’ compared to the ‘t’. At first glance, a longer duration seems to be contradictory with a higher velocity. In fact, the principle of isochrony states a proportional relationship between movement speed and trajectory length, so the total duration of execution remains approximately constant (Viviani & Terzuolo 1982). In the present case, because of a greater difficulty of ‘f’ compared to ‘t’, the increase in velocity is not proportional to the increase in trajectory length. This explains why the students took more time to write the letter ‘f’.

The results showed an effect of grade on all variables. According to the literature (Meulenbroek and Van Galen, 1988; Mojet, 1991; Zesiger, Mounoud & Hauert, 1993), the greatest differences were observed between Grade 1 and Grade 3. The letter size evolved
differently for each letter: it tended to decrease for the ‘f’ whereas it remained relatively stable for the ‘t’. It is well established that the tendency to write larger is one of the criteria that characterize non-mastered handwriting (e.g., Hamstra-Bletze & Blöte, 1993). Taken together, our analyses confirm that the letter ‘f’ was less automated than the letter ‘t’ for Grade 1 students only. Knowing that automation refers to the fact that writing is produced with minimal attentional involvement (Tucha et al., 2008), more attentional resources are allocated to the motor processes when writing the difficult letter than the easy one. If children pay too much attention to handwriting movements, they may have some difficulties in the allocation of cognitive resources to other processes (Berninger & Swanson, 1994; Jones & Christensen, 1999).

In this study, the orthographic constraints were generated by the lexical frequency and the graphemic complexity of the word. Lexical frequency had no direct main effect on any of the variables, but it interacted with letter difficulty and decreased with increasing school grade. This interaction occurred on the number of stops (observed in both frequentist and Bayesian analyses) and, to a lesser extent, on the duration and velocity (observed in the frequentist analysis only). The frequency effect was significant for Grade 1 students but not in the other two groups, and it was observed for letter ‘f’ but not for letter ‘t’. In other words, the effect of orthographic constraints was only observed for beginners in the production of the less automated letter. This finding supports the idea of an interaction between motor and spelling processes from the first stage of handwriting acquisition, which later disappears or changes through automation. Previous studies have revealed a frequency effect on handwriting movements in a word copy task in adults (Delattre et al., 2006; Lambert et al., 2011) and in children (Alfonso et al., 2018; Kandel & Perret 2015). Afonso et al. (2018) studied words written in Grade 2, 4 and 6, and confirmed that the automation of writing skills through learning reduces the effect of word frequency that is significant only in Grade 2. We also observed an effect of frequency for the youngest students, in Grade 1 only. Furthermore, Kandel & Perret (2015) observed, in all groups of children tested (8-10 years), that the effect of frequency was not significant at the beginning but in the middle of the words. In the present study, we did observe a frequency effect when producing the difficult letter. This difference could result, in our study, from the absence of the template, which was removed before the child started to write. We suppose that for frequent words,
students in Grade 1 have already memorized the correct spelling in orthographic long-term memory. Knowing that the acquisition of handwriting starts with a letter-by-letter planning (Humblot et al., 1994), beginners allocate their attention to the motor processes if the letter is non-automated. For low-frequency words, removing the template led the students to retain in orthographic working memory the entire word they had to write (Kandel & Valdois, 2005). According to Olive and Kellogg (2002) who proposed that central and peripheral processes in written production compete for a common cognitive resource (see also and Sausset et al., 2012), our findings suggest that when handwriting movements are not yet automated, the significant cognitive resources required for maintaining the spelling of low-frequency words in working memory, interfere with the motor processing required for writing a non-automated difficult letter.

When focusing on the interaction between graphomotor and orthographic constraints in the younger group of children, the Bayesian analyses (supplementary materials) revealed that the strongest evidence for this interaction effect was in the number of stops. In other words, Grade 1 students discretized their movement. This mode of production was previously reported by Van Mier (2006) in a drawing task. She observed that young children made continuous movements (zigzag) in a discrete manner, producing short strokes separated by stops. She interpreted this finding as a less proficient motor planning in younger children whereas older children program and plan the upcoming segment during the production of the previous segment (see also Badan, Hauert and Mounoud, 2000). This finding is compatible with the results of Sausset et al. (2012) who evidenced similar effects of spelling processes on writing execution in adults when the graphomotor constraints induced by the task were high.

Finally, the effects of graphemic complexity were marginal, with an effect on the letter size in the frequentist analysis only. It has been shown that in a dictation task, the phoneme-grapheme conversion underlying complex graphemes impacts the latency, i.e. the time before starting to write once the word had been heard (Bonin & Delattre 2010). Those authors proposed that the different phoneme-to-grapheme correspondences that are available for a given phoneme are simultaneously activated and compete in spelling to dictation. In the present study, the visual presentation of the words before starting to write
may have limited this competition, and thus the effects of graphemic complexity on writing kinematics.

5. Conclusions: Implications for Primary Education, limitations and perspectives

The combined effects of orthographic and graphomotor constraints in 1st graders indicate that graphomotor and spelling processes build up and interact from the beginning of learning. This finding supports the idea of a parallel activation of spelling (high-level) and graphomotor (low-level) modules that was proposed in the van Galen’s model (1991). It calls into question the relevance of evaluating spelling and graphomotor processes separately. The present study has practical implications for helping teachers to both teach and evaluate handwriting quality and spelling proficiency. In terms of evaluation, if the word to be written is not frequent and contains difficult letters, handwriting performance could be impacted, and the teacher could wrongly interpret this as a graphomotor difficulty. This might explain some of the handwriting difficulties sometimes observed in children with reading disorders (Cheng-Lai, Chan, & Lo, 2013; Kandel, Lassus-Sangosse, Grosjacques, & Perret, 2017).

In terms of instruction, teachers should be careful not to put students who do not yet fully master graphomotor skills in a situation where they have to deal both with unusual graphomotor demands while writing words that are too complex orthographically. Otherwise they risk to slow down one or both learning processes. A very good example is the application of instructional methods that involve modifying visual feedback (Bara & Bonneton-Botté, 2021), while children are used to control both pen movements and word spelling visually. Although this type of method has been tested only with single letters, its extension to whole words should take the combination of orthographic and graphomotor demands of the task into account.

A logical continuation of the present study would be to evaluate how this combined effect of constraints evolves longitudinally between Grade 1 and Grade 2, and differs according to the children’s level of handwriting proficiency, especially at the very beginning of learning. Specific difficulties could emerge in students whose graphomotor coordination is impaired. Indeed, these students would face a double challenge: not only do they have trouble tracing letters in a fast, fluid, and legible manner, but this cost associated with
moving their pen correctly could disrupt the attention that needs to be given to the spelling of words, especially if they are not well known by the child.

In conclusion, our study reveals that when children start to write a word, orthographic constraints underlying the word frequency and, to a much lesser extent, the grapheme structure at the end of the word, influence the production of the first letter when this letter has not yet been automated. Of course, the present study has from some limitations. The main limit is the reduced number of items used, which is due to the very controlled material (5-letter words with the same vowel at the second position and with a complex and simple grapheme within the 3 last letters). Furthermore, this study has not been designed to evaluate the total temporal course of the writing movement, from initialization (with latency) to the end of the word. Further studies are necessary to confirm this combined effect, and to better understand the emergence of the cascading phenomenon between the spelling and motor processes in learning to write (Olive, 2014).

Appendix

<table>
<thead>
<tr>
<th>Grade</th>
<th>DURATION</th>
<th>MEAN VELOCITY</th>
<th>NUMBER OF STOPS</th>
<th>LETTER SIZE</th>
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<td>0,51</td>
<td>0,06</td>
<td>1,00</td>
</tr>
</tbody>
</table>

Table 3: Correlation matrix between the four dependent variables in the main experiment. In bold, significant correlation coefficients.

As can be seen, the dependent variables are partially correlated, which is not surprising knowing that when handwriting is not mastered, students take more time to write the velocity is lower, they make more stops, and they write larger. These correlations evolve
in a non-monotonic way with the school level, and they decrease when the handwriting is mastered (in Grade 5).

References


Supplementary materials to ‘Interaction between orthographic and graphomotor constraints in learning to write’

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1 Visual data exploration

1.1 Univariate raw data exploration

![Graph showing the effect of grade, word frequency, and grapheme complexity on various reading metrics.]

*Figure 1.* Effect of grade, word frequency, and grapheme complexity on the total duration, the number of stops, the mean velocity, and the letter size. The error bars represent the 95% confidence intervals of the mean (assuming a Gaussian distribution).
Figure 1 shows the effect of grade, word frequency, and grapheme complexity on the letter duration, the number of stops, the mean velocity, and the letter size. This figure suggests that the average duration (in seconds) seems to decrease monotonically with grade. The number of stops also seems to decrease with grade, with most trials for children from grade 2 being associated with no stop.

1.2 Bivariate correlations by grade

Figure 2 shows the overall and by-grade Spearman correlation between each pair of variables. This figure reveals medium to strong positive and negative correlations between each pair of variable. These relations are sometimes non-linear (e.g., between duration and mean velocity), hence the use of Spearman (rather than Pearson) correlation coefficients.

![Figure 2](image-url)
2 Bayesian multilevel modelling

2.1 Modelling positive-only values

A dominant feature of durations (or response times) is that their distribution is generally positively skewed, with the spread and/or the skewness increasing with task difficulty (for review, see for instance Forstmann, Ratcliff, & Wagenmakers, 2016). Therefore, several models have been proposed to account for the peculiarities of the data coming from such tasks as well as to relate it to the underlying cognitive processes. We discuss below why using Gaussian models for this kind of data is generally not a sensible idea and describe our approach in more details. We follow a general “Bayesian workflow” by building our model in an iterative manner and by motivating and validating each modelling choice (for more details, see for instance Gelman et al., 2020).

We first fitted a Bayesian multilevel (also known as “mixed-effects”) Gaussian multivariate (i.e., with multiple outcomes) model. One way of evaluating this model is to evaluate its predictions. If this model is a good description of the process that generated the observed data, then it should be able to generate data that looks like the observed data. The process of generating data from the estimated posterior distribution is called posterior predictive checking and can be used in many different ways using the `pp_check()` method (Gabry, Simpson, Vehtari, Betancourt, & Gelman, 2019). In Figure 3, we depict the distribution of the raw data along with the distribution of 100 simulated datasets.

This figure reveals that the Gaussian model fails to account for the peculiarities of the data at hand. For instance, it systematically fails to predict the right-skew of all four variables, and more dramatically, sometimes predicts negatives values for these variables, although they are strictly positive. Moreover, using a Gaussian distribution to model the number of stops also leads to nonsensical predictions as the number of stops is necessarily a positive integer (whereas the Gaussian distribution can produce any real number), as illustrated in the upper right panel of Figure 3.

2.2 Shifted-lognormal regression model

A useful description of RTs or durations should be able to account for the effects of the difficulty of the task, as well as changes in shift and spread of the distribution. The Log-normal, Ex-Gaussian, or Weibull distributions often provide a good fit to these data, but their parameters are difficult to interpret in terms of difficulty, shift, or spread (i.e., these distributions do not have straightforward interpretable parameters). In contrast, the shifted log-normal distribution has parameters that can easily be interpreted in terms of
The log-normal distribution is called “log-normal” because the parameters are the mean and standard deviation of the log-transformed response, which is assumed to be a normal (Gaussian) distribution. The shifted log-normal distribution is then described by three parameters:

- $\mu$ (mu, difficulty): the mean of the log-normal distribution. The median duration is given by $\text{shift} + \exp(\mu)$.
- $\sigma$ (sigma, scale): the standard deviation of the log-normal distribution. Increases the mean but not the median of $\mu$.
- shift (ndt) indicates the time of the earliest possible response. When $\text{shift} = 0$, the shifted log-normal distribution correspond to the conventional log-normal distribution with two parameters.

Regression models using this family usually aim to predict $\mu$, the mean of the log-
normal distribution. We employ this strategy as well, while noticing that both $\sigma$ and shift could be allowed to vary across conditions as well.

2.3 Poisson regression model

Whereas the previous models are able to take into account the right-skew of the four variables we are interested in, they are still not able to make proper predictions with regards to the number of stops (because the log-normal distribution is continuous). Yet a better model could be fitted by picking up a discrete probability distribution defined on the positive integer real. The Poisson regression model is appropriate for modelling discrete counts of events (e.g., the number of stops) that happen in a fixed interval of space or time with no upper bound. The Poisson model is simpler than the Gaussian or the lognormal one because it has only one parameter $\lambda$ that describes its shape. The parameter $\lambda$ is the expected value of the outcome $y$ (and also its expected variance). However, we need a link function to relate the predictors with the parameter $\lambda$ and to ensure that $\lambda$ is always positive. We use the conventional logarithmic link function, resulting in the following linear model:

$$y_i \sim \text{Poisson}(\lambda_i)$$

$$\log(\lambda_i) = \alpha + \beta_g \cdot \text{grade}_i + \beta_f \cdot \text{frequency}_i + \beta_{graphe} \cdot \text{grapheme}_i + \beta_{grapho} \cdot \text{graphomotor}_i$$

This kind of model is now able to predict valid number of stops (i.e., positive integers). Note that for simplicity, we omit the varying effects and the priors from the above model (for more details on Poisson regression, see Winter & Bürkner, 2021).

2.4 Fitting the final model

To set up the model, we need to invoke the `brms::brmsformula()` function and construct one formula for each of the four dependent variables. We fitted all models using the `brms` package (Bürkner, 2017). We used sum contrasts (i.e., recoding conditions as -0.5 vs. 0.5) for binary predictors (i.e., frequency, grapheme complexity, and graphomotor difficulty) and used the default factor coding scheme (i.e., dummy coding) for grade.

```r
# defining the model formula for the generalised multilevel model
formula_generalised <-
  bf(
    duration ~ 1 + group * frequency * grapheme_complexity *
```

graphomotor_difficulty + (1 | subject),
  family = shifted_lognormal()
) +
  bf(
    mean_velocity ~ 1 + group * frequency * grapheme_complexity *
    graphomotor_difficulty + (1 | subject),
  family = shifted_lognormal()
) +
  bf(
    number_of_stops ~ 1 + group * frequency * grapheme_complexity *
    graphomotor_difficulty + (1 | subject),
  family = poisson()
) +
  bf(
    letter_size ~ 1 + group * frequency * grapheme_complexity *
    graphomotor_difficulty + (1 | subject),
  family = shifted_lognormal()
)

# defining the priors for the multilevel generalised model
priors_generalised <- c(
  prior(normal(1, 0.5), class = Intercept, resp = "duration"),
  prior(normal(0, 0.5), class = b, resp = "duration"),
  prior(exponential(0.1), class = sd, resp = "duration"),
  prior(exponential(0.1), class = sigma, resp = "duration"),
  prior(normal(2, 0.5), class = Intercept, resp = "meanvelocity"),
  prior(normal(0, 0.5), class = b, resp = "meanvelocity"),
  prior(exponential(0.1), class = sd, resp = "meanvelocity"),
  prior(exponential(0.1), class = sigma, resp = "meanvelocity"),
  prior(normal(1, 0.5), class = Intercept, resp = "numberofstops"),
  prior(normal(0, 0.5), class = b, resp = "numberofstops"),
  prior(exponential(0.1), class = sd, resp = "numberofstops"),
  prior(normal(2, 0.5), class = Intercept, resp = "lettersize"),
  prior(normal(0, 0.5), class = b, resp = "lettersize"),
  prior(exponential(0.1), class = sd, resp = "lettersize"),
  prior(exponential(0.1), class = sigma, resp = "lettersize")
)
# centering and reordering predictors
df2 <- df %>%
    mutate(
      group = factor(
        x = group,
        levels = c("CP", "CE", "CM"),
        labels = c("Grade1", "Grade3", "Grade5")
      ),
      frequency = factor(
        x = frequency,
        levels = c("LF", "HF"),
        labels = c("LF", "HF")
      ),
      grapheme_complexity = factor(
        x = grapheme_complexity,
        levels = c("Simple", "Complex"),
        labels = c("Simple", "Complex")
      ),
      graphomotor_difficulty = factor(
        x = graphomotor_difficulty,
        levels = c("EL", "HL"),
        labels = c("t", "f")
      )
    )
  # removes rows where duration is equal to 0
  filter(duration != 0)

  # defining contrasts
  contrasts(df2$frequency) <- c(-0.5, +0.5)
  contrasts(df2$grapheme_complexity) <- c(-0.5, +0.5)
  contrasts(df2$graphomotor_difficulty) <- c(-0.5, +0.5)

  # fitting the model
  mod2 <- brm(
    formula = formula_generalised + set_rescor(rescor = FALSE),
prior = priors_generalised,
chains = 4, cores = 4,
warmup = 2000, iter = 1e4,
control = list(adapt_delta = 0.95),
data = df2,
sample_prior = TRUE,
file = "models/multilevel_generalised_model"
)

We then fit this model below using the \texttt{brms::brm()} function. We run four chains, each for 10000 iterations and using the first 2000 iterations used as warmup (i.e., the first 2000 samples of each chain are discarded from the final analysis). This results in a total of $4 \times (10000 - 2000) = 32000$ samples from the (joint) posterior distribution that will be used for inference.

\subsection*{2.5 Evaluating the model}

One way of evaluating the model is to evaluate its predictions. In Figure 4, we depict the distribution of the raw data along with the distribution of 100 simulated datasets (a posterior predictive check, as introduced previously).

As can be seen from Figure 4, the model seems pretty good at simulating data that looks like the observed data. From this predictive/sampling distribution (i.e., the distribution of simulated data sets), so-called “Bayesian p-values” can be computed to quantify the compatibility between the observed data and the proposed model.
Posterior predictive checks for the multilevel generalised model

The dark blue density depicts the raw data whereas light blue densities represent data simulated from the posterior predictive distribution

Figure 4. Posterior predictive checking. The dark blue line represents the distribution of raw data whereas light blue lines represent data simulated from the posterior distribution.

2.6 Hypothesis testing

We can test any arbitrary hypothesis using the \texttt{brms::hypothesis()} method, which is computing a Bayes factor via the Savage-Dickey method (Wagenmakers, Lodewyckx, Kuriyal, & Grasman, 2010). This method consists in comparing the posterior probability density to the prior probability density for some hypothesised value for the parameter of interest (e.g., $\theta = 0$). For instance, we test below the hypothesis according to which the effect of graphemic complexity in Grade 1 would be null.

\begin{verbatim}
# testing whether the effect of grapheme complexity on duration equal to 0
hyp <- hypothesis(x = mod2, hypothesis = "duration_grapheme_complexity1 = 0")

# prints the output
print(hyp)

## Hypothesis Tests for class b:
##
##      Hypothesis Estimate Est.Error CI.Lower CI.Upper Evid.Ratio
## 1 (duration_graphem... = 0     0    0.05   -0.11     0.1  9.87
\end{verbatim}
## Post.Prob Star

<table>
<thead>
<tr>
<th></th>
<th>0.91</th>
</tr>
</thead>
</table>

---

'CI': 90%-CI for one-sided and 95%-CI for two-sided hypotheses.

'*': For one-sided hypotheses, the posterior probability exceeds 95%; for two-sided hypotheses, the value tested against lies outside the 95%-CI.

Posterior probabilities of point hypotheses assume equal prior probabilities.

---

`data.frame(posterior = hyp$samples$H1, prior = hyp$prior_samples$H1) %>%
gather(type, value) %>%
ggplot(aes(x = value, fill = type)) +
  geom_vline(xintercept = 0, linetype = 2, alpha = 1) +
  geom_area(stat = "density", alpha = 0.8, position = "identity") +
  theme_bw(base_size = 12, base_family = "Open Sans") +
  labs(x = expression(beta[grapheme_complexity]), y = "Probability density") +
  scale_fill_brewer(palette = "Dark2") +
  theme(legend.title = element_blank()) +
  coord_cartesian(xlim = c(-2, 2))

---

**Figure 5.** Hypothesis testing via the Savage-Dickey method. The resulting Bayes factor (BF) is the ratio of the height (i.e., the density probability) of the posterior versus prior distribution at some value of interest for the parameter (here it is 0).

The resulting Bayes factor (BF, called “Evid. Ratio” in the output) may be inter-
interpreted as follows: the observed data are 9.87 more likely under the hypothesis of null effect than under the hypothesis of a non-null effect. From the BF in favour of the null hypothesis (relative to the alternative hypothesis), we can compute the BF in favour of the alternative hypothesis (relative to the null hypothesis), using $BF_{10} = 1/BF_{01}$ (we report the $BF_{10}$ in the following). Alternatively, the BF can be interpreted as an updating factor, indicating by “how much” we should update our prior odds (the ratio of the a priori probability of $\mathcal{H}_0$ versus $\mathcal{H}_1$) to convert them into posterior odds (the ratio of the a posteriori probability of $\mathcal{H}_0$ versus $\mathcal{H}_1$).
3 Interpretation of the results for each variable

Now that we have fitted the model, we are left with the task of interpreting the output from the model. The output of the model is a (joint) posterior distribution over all parameters of the model. We can marginalise this joint distribution to obtain the (marginal) posterior distribution on each parameter. To summarise this distribution, we can retrieve samples from the joint posterior distribution.

```r
# retrieves posterior samples (for all parameters)
posterior_samples <- as_draws_df(mod2)

# displays a summary
posterior_summary <- summarise_draws(posterior_samples)

# displays the first six rows
head(posterior_summary)
```

The above command outputs a matrix with parameters of the model in columns and posterior samples in rows. Let’s examine these results for each parameter in more details. For instance, Figure 6 represents the posterior distribution of the average letter duration in Grade-1 children.

```r
# retrieves the posterior samples for the average letter duration in Grade 1
average_duration_grade1 <- posterior_samples$b_duration_Intercept +
                        posterior_samples$ndt_duration

# plotting it
plotPost(
  paramSampleVec = exp(average_duration_grade1), showMode = TRUE,
```
$\text{xlab = expression(paste(alpha[duration][paste("[", Grade1, "]")])})$

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure6.png}
\caption{Posterior distribution of the intercept (i.e., the average letter duration in Grade 1). The mode (i.e., the most probable value) and the 95\% credible (highest density) interval are also displayed.}
\end{figure}

Recall that we used a logarithmic link function, therefore the median letter duration is given by $\exp(\alpha + \text{shift})$.

\subsection{Letter duration}

Table 1 reports the estimates (median of the posterior distribution) and associated 95\% credible intervals and BFs for all parameters regarding the letter duration variable.
### Table 1

*Estimates and BFs for the slopes for letter duration.*

<table>
<thead>
<tr>
<th>Term</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
<th>Rhat</th>
<th>BF10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>1.083</td>
<td>0.030</td>
<td>1.020</td>
<td>1.142</td>
<td>1.000</td>
<td>NA</td>
</tr>
<tr>
<td>groupGrade3</td>
<td>-0.865</td>
<td>0.038</td>
<td>-0.943</td>
<td>-0.793</td>
<td>1.000</td>
<td>7.281 x 10^17</td>
</tr>
<tr>
<td>groupGrade5</td>
<td>-0.966</td>
<td>0.042</td>
<td>-1.050</td>
<td>-0.889</td>
<td>1.000</td>
<td>3.586 x 10^15</td>
</tr>
<tr>
<td>frequency</td>
<td>-0.055</td>
<td>0.050</td>
<td>-0.157</td>
<td>0.049</td>
<td>1.000</td>
<td>0.192</td>
</tr>
<tr>
<td>grapheme_complexity</td>
<td>-0.005</td>
<td>0.050</td>
<td>-0.106</td>
<td>0.097</td>
<td>1.000</td>
<td>0.101</td>
</tr>
<tr>
<td>graphomotor_difficulty</td>
<td>0.423</td>
<td>0.051</td>
<td>0.320</td>
<td>0.526</td>
<td>1.000</td>
<td>9.762 x 10^15</td>
</tr>
<tr>
<td>groupGrade3:frequency</td>
<td>0.074</td>
<td>0.062</td>
<td>-0.049</td>
<td>0.196</td>
<td>1.000</td>
<td>0.258</td>
</tr>
<tr>
<td>groupGrade5:frequency</td>
<td>0.027</td>
<td>0.062</td>
<td>-0.092</td>
<td>0.148</td>
<td>1.000</td>
<td>0.136</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity</td>
<td>0.011</td>
<td>0.062</td>
<td>-0.112</td>
<td>0.132</td>
<td>1.000</td>
<td>0.13</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity</td>
<td>0.004</td>
<td>0.061</td>
<td>-0.115</td>
<td>0.124</td>
<td>1.000</td>
<td>0.124</td>
</tr>
<tr>
<td>frequency:grapheme_complexity</td>
<td>0.046</td>
<td>0.097</td>
<td>-0.151</td>
<td>0.244</td>
<td>1.000</td>
<td>0.225</td>
</tr>
<tr>
<td>groupGrade3:graphomotor_difficulty</td>
<td>0.001</td>
<td>0.063</td>
<td>-0.121</td>
<td>0.127</td>
<td>1.000</td>
<td>0.132</td>
</tr>
<tr>
<td>groupGrade5:graphomotor_difficulty</td>
<td>0.009</td>
<td>0.064</td>
<td>-0.024</td>
<td>0.225</td>
<td>1.000</td>
<td>0.436</td>
</tr>
<tr>
<td>frequency:graphomotor_difficulty</td>
<td>-0.071</td>
<td>0.097</td>
<td>-0.268</td>
<td>0.128</td>
<td>1.000</td>
<td>0.261</td>
</tr>
<tr>
<td>grapheme_complexity:graphomotor_difficulty</td>
<td>-0.008</td>
<td>0.098</td>
<td>-0.203</td>
<td>0.188</td>
<td>1.000</td>
<td>0.197</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity</td>
<td>0.010</td>
<td>0.120</td>
<td>-0.229</td>
<td>0.248</td>
<td>1.000</td>
<td>0.249</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity</td>
<td>-0.101</td>
<td>0.119</td>
<td>-0.337</td>
<td>0.131</td>
<td>1.000</td>
<td>0.352</td>
</tr>
<tr>
<td>groupGrade3:frequency:graphomotor_difficulty</td>
<td>0.007</td>
<td>0.122</td>
<td>-0.233</td>
<td>0.243</td>
<td>1.000</td>
<td>0.246</td>
</tr>
<tr>
<td>groupGrade5:frequency:graphomotor_difficulty</td>
<td>0.068</td>
<td>0.120</td>
<td>-0.167</td>
<td>0.308</td>
<td>1.000</td>
<td>0.285</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity:graphomotor_difficulty</td>
<td>0.072</td>
<td>0.120</td>
<td>-0.162</td>
<td>0.309</td>
<td>1.000</td>
<td>0.291</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity:graphomotor_difficulty</td>
<td>0.035</td>
<td>0.119</td>
<td>-0.201</td>
<td>0.270</td>
<td>1.000</td>
<td>0.252</td>
</tr>
<tr>
<td>frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>-0.040</td>
<td>0.176</td>
<td>-0.401</td>
<td>0.321</td>
<td>1.000</td>
<td>0.368</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>-0.006</td>
<td>0.217</td>
<td>-0.343</td>
<td>0.424</td>
<td>1.000</td>
<td>0.442</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>0.134</td>
<td>0.213</td>
<td>-0.283</td>
<td>0.548</td>
<td>1.000</td>
<td>0.529</td>
</tr>
</tbody>
</table>

*Note.* For each slope (for each line), the first two columns represent the estimated most probable value and its standard error (SE). The 'Lower' and 'Upper' columns contain the lower and upper bounds of the 95% CrI, whereas the 'Rhat' column reports the Gelman-Rubin statistic. The last column reports the Bayes factor in favour of the alternative hypothesis, relative to the null hypothesis (BF10).
These estimations are better understood visually. Thus, we plot the predictions of this model against raw data in Figure 7.

```
# retrieving the model's predictions
duration_predictions <- df2 %>%
  data_grid(graphomotor_difficulty, grapheme_complexity, frequency, group) %>%
  cbind(.,
    fitted(
      object = mod2, newdata = ., resp = "duration",
      scale = "response", probs = c(0.025, 0.975),
      re_formula = NA, robust = TRUE
    )
  ) %>%
  ungroup %>%
dplyr::rename(estimate = Estimate, mad = Est.Error, lower = Q2.5, upper = Q97.5)
```

![Graph showing letter duration by grade and word frequency (x-axis), grapheme complexity (in colour), and graphomotor difficulty (in panels). Transparent points represent individual data per participant. The surimposed dots and intervals represent the model's predictions (median and 95% credible interval of the posterior distribution).](image)

**Figure 7.** Letter duration by grade and word frequency (x-axis), grapheme complexity (in colour), and graphomotor difficulty (in panels). Transparent points represent individual data per participant. The surimposed dots and intervals represent the model’s predictions (median and 95% credible interval of the posterior distribution).

As can be seen in Figure 7, the model predicts larger letter duration for the difficult letter f as compared to the easy letter t for each grade. As can be seen from Table 1, the
only BFs favouring the alternative hypothesis (relative to the null hypothesis) are the BFs for the difference between Grade 1 and Grade 3 in average letter duration ($\beta = -0.865$, 95% CrI [-0.943, -0.793], $BF_{10} = 7.281 \times 10^{-17}$), as well as the difference between Grade 1 and Grade 5 ($\beta = -0.966$, 95% CrI [-1.05, -0.889], $BF_{10} = 3.586 \times 10^{-15}$), and the effect of graphomotor difficulty in Grade 1 ($\beta = 0.423$, 95% CrI [0.32, 0.526], $BF_{10} = 9.762 \times 10^{-15}$).

Predictions from this model for each condition are also summarised in Table 2.

Table 2

<table>
<thead>
<tr>
<th>Group</th>
<th>Frequency</th>
<th>Grapheme complexity</th>
<th>Graphomotor difficulty</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>2.768</td>
<td>0.186</td>
<td>2.416</td>
<td>3.172</td>
</tr>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>4.296</td>
<td>0.287</td>
<td>3.745</td>
<td>4.923</td>
</tr>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>2.680</td>
<td>0.179</td>
<td>2.334</td>
<td>3.077</td>
</tr>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>4.203</td>
<td>0.291</td>
<td>3.651</td>
<td>4.846</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>2.632</td>
<td>0.176</td>
<td>2.303</td>
<td>3.011</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>3.883</td>
<td>0.263</td>
<td>3.387</td>
<td>4.458</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>2.713</td>
<td>0.182</td>
<td>2.367</td>
<td>3.122</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>3.899</td>
<td>0.261</td>
<td>3.401</td>
<td>4.469</td>
</tr>
<tr>
<td>Grade3</td>
<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>1.196</td>
<td>0.084</td>
<td>1.040</td>
<td>1.381</td>
</tr>
<tr>
<td>Grade3</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>1.760</td>
<td>0.127</td>
<td>1.522</td>
<td>2.040</td>
</tr>
<tr>
<td>Grade3</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>1.127</td>
<td>0.080</td>
<td>0.980</td>
<td>1.304</td>
</tr>
<tr>
<td>Grade3</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>1.797</td>
<td>0.127</td>
<td>1.556</td>
<td>2.074</td>
</tr>
<tr>
<td>Grade3</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>1.111</td>
<td>0.085</td>
<td>1.053</td>
<td>1.399</td>
</tr>
<tr>
<td>Grade3</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>1.710</td>
<td>0.121</td>
<td>1.482</td>
<td>1.980</td>
</tr>
<tr>
<td>Grade3</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>1.226</td>
<td>0.087</td>
<td>1.063</td>
<td>1.418</td>
</tr>
<tr>
<td>Grade3</td>
<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>1.802</td>
<td>0.129</td>
<td>1.561</td>
<td>2.090</td>
</tr>
<tr>
<td>Grade5</td>
<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>1.033</td>
<td>0.070</td>
<td>0.902</td>
<td>1.185</td>
</tr>
<tr>
<td>Grade5</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>1.693</td>
<td>0.120</td>
<td>1.470</td>
<td>1.953</td>
</tr>
<tr>
<td>Grade5</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>1.068</td>
<td>0.072</td>
<td>0.931</td>
<td>1.230</td>
</tr>
<tr>
<td>Grade5</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>1.722</td>
<td>0.121</td>
<td>1.493</td>
<td>1.985</td>
</tr>
<tr>
<td>Grade5</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>1.057</td>
<td>0.072</td>
<td>0.923</td>
<td>1.213</td>
</tr>
<tr>
<td>Grade5</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>1.654</td>
<td>0.115</td>
<td>1.435</td>
<td>1.900</td>
</tr>
<tr>
<td>Grade5</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>0.996</td>
<td>0.066</td>
<td>0.869</td>
<td>1.142</td>
</tr>
<tr>
<td>Grade5</td>
<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>1.667</td>
<td>0.117</td>
<td>1.447</td>
<td>1.924</td>
</tr>
</tbody>
</table>

Note. For each condition, the ‘Estimate’ and ‘MAD’ columns contain the median and the median absolute deviation (MAD) of the posterior distribution, respectively. The ‘Lower’ and ‘Upper’ columns contain the lower and upper bounds of the 95% credible interval.

The output of a Bayesian model is a (joint) posterior distribution over all parameters of the model. We can marginalise this joint distribution to obtain the (marginal) posterior distribution on each parameter. To summarise this distribution, we can retrieve samples from the joint posterior distribution. Interestingly, this means we can look at the posterior distribution of any parameter of interest. For instance, and for exploratory purposes, we depict below the posterior distribution of the difference between high-frequency and low-frequency words (i.e., the effect of frequency) separately for each letter (graphomotor difficulty) and each grade. We averaged the predictions across both conditions of graphemic complexity, as this effect appeared to be null.

As can be seen in Figure 8, the posterior distribution for the effect of frequency is
Figure 8. Effect of word frequency on letter duration (in seconds) for each grade (in column) and letter (in row). The histogram contains posterior samples for each effect, where the posterior distribution is summarised by its mean and 95% highest density interval (HDI). The green text indicates the probability that the parameter values is either inferior or superior to 0.

almost perfectly centred on zero in all conditions, except for letter f in Grade 1. Although the 95% credible interval largely encompasses 0 in this condition as well, there is still a 0.82 probability that the effect of frequency on letter duration is negative (given the data and the priors).

3.2 Number of stops

Table 3 reports the estimates (median of the posterior distribution) and associated 95% credible intervals and BF$s for all parameters regarding the number of stops.
Table 3

*Estimates and BFs for the slopes for the number of stops.*

<table>
<thead>
<tr>
<th>Term</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
<th>Rhat</th>
<th>BF10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>1.037</td>
<td>0.035</td>
<td>0.965</td>
<td>1.109</td>
<td>1.000</td>
<td>NA</td>
</tr>
<tr>
<td>groupGrade3</td>
<td>-1.384</td>
<td>0.073</td>
<td>-1.529</td>
<td>-1.243</td>
<td>1.000</td>
<td>4.244 x 10^-16</td>
</tr>
<tr>
<td>groupGrade5</td>
<td>-1.556</td>
<td>0.077</td>
<td>-1.709</td>
<td>-1.409</td>
<td>1.000</td>
<td>6.510 x 10^-15</td>
</tr>
<tr>
<td>frequency</td>
<td>-0.180</td>
<td>0.070</td>
<td>-0.324</td>
<td>-0.034</td>
<td>1.000</td>
<td>2.746</td>
</tr>
<tr>
<td>grapheme_complexity</td>
<td>0.031</td>
<td>0.070</td>
<td>-0.111</td>
<td>0.175</td>
<td>1.000</td>
<td>0.155</td>
</tr>
<tr>
<td>graphomotor_difficulty</td>
<td>-0.051</td>
<td>0.070</td>
<td>-0.192</td>
<td>0.094</td>
<td>1.000</td>
<td>0.184</td>
</tr>
<tr>
<td>groupGrade3:frequency</td>
<td>0.292</td>
<td>0.140</td>
<td>0.019</td>
<td>0.568</td>
<td>1.000</td>
<td>2.537</td>
</tr>
<tr>
<td>groupGrade5:frequency</td>
<td>0.128</td>
<td>0.147</td>
<td>-0.161</td>
<td>0.409</td>
<td>1.000</td>
<td>0.417</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity</td>
<td>0.051</td>
<td>0.142</td>
<td>-0.227</td>
<td>0.329</td>
<td>1.000</td>
<td>0.298</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity</td>
<td>-0.069</td>
<td>0.149</td>
<td>-0.356</td>
<td>0.220</td>
<td>1.000</td>
<td>0.334</td>
</tr>
<tr>
<td>frequency:grapheme_complexity</td>
<td>0.177</td>
<td>0.133</td>
<td>-0.096</td>
<td>0.446</td>
<td>1.000</td>
<td>0.653</td>
</tr>
<tr>
<td>groupGrade3:graphomotor_difficulty</td>
<td>0.112</td>
<td>0.140</td>
<td>-0.164</td>
<td>0.390</td>
<td>1.000</td>
<td>0.378</td>
</tr>
<tr>
<td>groupGrade5:graphomotor_difficulty</td>
<td>0.061</td>
<td>0.144</td>
<td>-0.226</td>
<td>0.346</td>
<td>1.000</td>
<td>0.313</td>
</tr>
<tr>
<td>frequency:graphomotor_difficulty</td>
<td>-0.312</td>
<td>0.134</td>
<td>-0.581</td>
<td>-0.032</td>
<td>1.000</td>
<td>3.307</td>
</tr>
<tr>
<td>grapheme_complexity:graphomotor_difficulty</td>
<td>-0.047</td>
<td>0.135</td>
<td>-0.315</td>
<td>0.224</td>
<td>1.000</td>
<td>0.285</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity</td>
<td>-0.234</td>
<td>0.254</td>
<td>-0.731</td>
<td>0.258</td>
<td>1.000</td>
<td>0.791</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity</td>
<td>-0.147</td>
<td>0.260</td>
<td>-0.653</td>
<td>0.358</td>
<td>1.000</td>
<td>0.602</td>
</tr>
<tr>
<td>groupGrade3:frequency:graphomotor_difficulty</td>
<td>0.102</td>
<td>0.257</td>
<td>-0.396</td>
<td>0.605</td>
<td>1.000</td>
<td>0.55</td>
</tr>
<tr>
<td>groupGrade5:frequency:graphomotor_difficulty</td>
<td>0.326</td>
<td>0.255</td>
<td>-0.176</td>
<td>0.834</td>
<td>1.000</td>
<td>1.153</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity:graphomotor_difficulty</td>
<td>0.068</td>
<td>0.254</td>
<td>-0.427</td>
<td>0.508</td>
<td>1.000</td>
<td>0.529</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity:graphomotor_difficulty</td>
<td>0.004</td>
<td>0.264</td>
<td>-0.511</td>
<td>0.509</td>
<td>1.000</td>
<td>0.52</td>
</tr>
<tr>
<td>frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>0.042</td>
<td>0.231</td>
<td>-0.430</td>
<td>0.518</td>
<td>1.000</td>
<td>0.464</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>-0.057</td>
<td>0.379</td>
<td>-0.801</td>
<td>0.678</td>
<td>1.000</td>
<td>0.766</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>0.073</td>
<td>0.384</td>
<td>-0.679</td>
<td>0.836</td>
<td>1.000</td>
<td>0.782</td>
</tr>
</tbody>
</table>

*Note.* For each slope (for each line), the first two columns represent the estimated most probable value and its standard error (SE). The 'Lower' and 'Upper' columns contain the lower and upper bounds of the 95% CrI, whereas the 'Rhat' column reports the Gelman-Rubin statistic. The last column reports the Bayes factor in favour of the alternative hypothesis, relative to the null hypothesis (BF10).
These estimations are better understood visually. Thus, we plot the predictions of this model against raw data in Figure 9.

```r
# retrieving the model's predictions
stops_predictions <- df2 %>%
  data_grid(graphomotor_difficulty, grapheme_complexity, frequency, group) %>%
  cbind(., fitted(
    object = mod2, newdata = ., resp = "numberofstops",
    scale = "response", probs = c(0.025, 0.975),
    re_formula = NA, robust = TRUE
  )) %>%
  ungroup %>%
  dplyr::rename(estimate = Estimate, mad = Est.Error, lower = Q2.5, upper = Q97.5)
```

![Graph showing number of stops by grade and word frequency, grapheme complexity, and graphomotor difficulty](image)

**Figure 9.** Number of stops by grade and word frequency (x-axis), grapheme complexity (in colour), and graphomotor difficulty (in panels). Transparent points represent individual data per participant. The surimposed dots and intervals represent the model's predictions (median and 95% credible interval of the posterior distribution).

As can be seen in Figure 9, the model most predicts an interaction between the effect of the word frequency and the effect of first-letter graphomotor difficulty in Grade 1, with
infiuent words leading to a greater number of stops than frequent words for f (difficult letter) more than for t (easy letter) ($\beta = -0.312$, 95% CrI [-0.581, -0.032], BF$_{10} = 3.307$). As can be seen from Table 3, others BF$s favouring the alternative hypothesis (relative to the null hypothesis) are BF$s for the difference between Grade 1 and Grade 3 ($\beta = -1.384$, 95% CrI [-1.529, -1.243], BF$_{10} = 4.244 \times 10^{-16}$), as well as between Grade 1 and Grade 5 ($\beta = -1.556$, 95% CrI [-1.709, -1.409], BF$_{10} = 6.510 \times 10^{-15}$), the effect of word frequency in Grade 1 ($\beta = -0.18$, 95% CrI [-0.324, -0.034], BF$_{10} = 2.746$), and Grade 3 ($\beta = 0.292$, 95% CrI [0.019, 0.568], BF$_{10} = 2.537$). Predictions from this model for each condition are also summarised in Table 4.

Table 4
Estimated number of stops in each condition.

<table>
<thead>
<tr>
<th>Group</th>
<th>Frequency</th>
<th>Grapheme complexity</th>
<th>Graphomotor difficulty</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grade 1</td>
<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>2.964</td>
<td>0.275</td>
<td>2.438</td>
<td>3.585</td>
</tr>
<tr>
<td>Grade 1</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>3.411</td>
<td>0.302</td>
<td>2.820</td>
<td>4.070</td>
</tr>
<tr>
<td>Grade 1</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>2.897</td>
<td>0.272</td>
<td>2.382</td>
<td>3.515</td>
</tr>
<tr>
<td>Grade 1</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>3.110</td>
<td>0.289</td>
<td>2.565</td>
<td>3.753</td>
</tr>
<tr>
<td>Grade 1</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>2.676</td>
<td>0.258</td>
<td>2.187</td>
<td>3.246</td>
</tr>
<tr>
<td>Grade 1</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>2.205</td>
<td>0.227</td>
<td>1.791</td>
<td>2.716</td>
</tr>
<tr>
<td>Grade 1</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>3.055</td>
<td>0.283</td>
<td>2.519</td>
<td>3.689</td>
</tr>
<tr>
<td>Grade 1</td>
<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>2.454</td>
<td>0.240</td>
<td>2.004</td>
<td>3.002</td>
</tr>
<tr>
<td>Grade 3</td>
<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>0.589</td>
<td>0.114</td>
<td>0.392</td>
<td>0.855</td>
</tr>
<tr>
<td>Grade 3</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>0.684</td>
<td>0.126</td>
<td>0.469</td>
<td>0.967</td>
</tr>
<tr>
<td>Grade 3</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>0.618</td>
<td>0.115</td>
<td>0.418</td>
<td>0.872</td>
</tr>
<tr>
<td>Grade 3</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>0.775</td>
<td>0.135</td>
<td>0.543</td>
<td>1.075</td>
</tr>
<tr>
<td>Grade 3</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>0.748</td>
<td>0.133</td>
<td>0.518</td>
<td>1.053</td>
</tr>
<tr>
<td>Grade 3</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>0.712</td>
<td>0.127</td>
<td>0.491</td>
<td>1.001</td>
</tr>
<tr>
<td>Grade 3</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>0.783</td>
<td>0.138</td>
<td>0.544</td>
<td>1.093</td>
</tr>
<tr>
<td>Grade 3</td>
<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>0.756</td>
<td>0.134</td>
<td>0.524</td>
<td>1.059</td>
</tr>
<tr>
<td>Grade 5</td>
<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>0.613</td>
<td>0.113</td>
<td>0.419</td>
<td>0.866</td>
</tr>
<tr>
<td>Grade 5</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>0.648</td>
<td>0.116</td>
<td>0.443</td>
<td>0.910</td>
</tr>
<tr>
<td>Grade 5</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>0.611</td>
<td>0.115</td>
<td>0.418</td>
<td>0.872</td>
</tr>
<tr>
<td>Grade 5</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>0.582</td>
<td>0.110</td>
<td>0.394</td>
<td>0.830</td>
</tr>
<tr>
<td>Grade 5</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>0.585</td>
<td>0.112</td>
<td>0.395</td>
<td>0.838</td>
</tr>
<tr>
<td>Grade 5</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>0.590</td>
<td>0.111</td>
<td>0.402</td>
<td>0.844</td>
</tr>
<tr>
<td>Grade 5</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>0.567</td>
<td>0.109</td>
<td>0.380</td>
<td>0.811</td>
</tr>
<tr>
<td>Grade 5</td>
<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>0.582</td>
<td>0.112</td>
<td>0.391</td>
<td>0.838</td>
</tr>
</tbody>
</table>

Note. For each condition, the 'Estimate' and 'MAD' columns contain the median and the median absolute deviation (MAD) of the posterior distribution, respectively. The 'Lower' and 'Upper' columns contain the lower and upper bounds of the 95% credible interval.

For exploratory purposes, we depict below the posterior distribution of the difference between high-frequency and low-frequency words (i.e., the effect of frequency) separately for each letter (graphomotor difficulty) and each grade. We averaged the predictions across both conditions of graphemic complexity, as this effect appeared to be null.

As can be seen in Figure 10, the posterior distribution for the effect of frequency is almost perfectly centred on zero in all conditions, except for letter f in Grade 1. In this condition, the 95% credible interval excludes 0 and there is a 0.98 probability that the effect
Effect of frequency for letter t in Grade 1
-1.0 -0.5 0.0 0.5 1.0
95% HDI
-0.94 0.809
mean=-0.0668
56% < 0 < 44%

Effect of frequency for letter t in Grade 3
-0.2 0.0 0.2 0.4 0.6
95% HDI
-0.193 0.498
mean=0.148
19.5% < 0 < 80.5%

Effect of frequency for letter t in Grade 5
-0.4 -0.2 0.0 0.2
95% HDI
-0.332 0.268
mean=-0.0368
59.3% < 0 < 40.7%

Effect of frequency for letter f in Grade 1
-2.0 -1.5 -1.0 -0.5 0.0
95% HDI
-1.83 -0.0136
mean=-0.928
97.8% < 0 < 2.2%

Effect of frequency for letter f in Grade 3
-0.4 -0.2 0.0 0.2 0.4
95% HDI
-0.351 0.361
mean=0.00501
48.9% < 0 < 51.1%

Effect of frequency for letter f in Grade 5
-0.4 -0.2 0.0 0.2 0.4
95% HDI
-0.331 0.289
mean=-0.0278
57.1% < 0 < 42.9%

Figure 10. Effect of word frequency on the number of stops for each grade (in column) and letter (in row). The histogram contains posterior samples for each effect, where the posterior distribution is summarised by its mean and 95% highest density interval (HDI). The green text indicates the probability that the parameter values is either inferior or superior to 0.

of frequency on the number of stops is negative (given the data and the priors).

3.3 Mean velocity

Table 5 reports the estimates (median of the posterior distribution) and associated 95% credible intervals and BF's for all parameters regarding the mean velocity.
### Table 5
Estimates and BFs for the slopes for the mean velocity.

<table>
<thead>
<tr>
<th>Term</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
<th>Rhat</th>
<th>BF10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>2.338</td>
<td>0.026</td>
<td>2.281</td>
<td>2.387</td>
<td>1.000</td>
<td>NA</td>
</tr>
<tr>
<td>groupGrade3</td>
<td>0.562</td>
<td>0.033</td>
<td>0.496</td>
<td>0.628</td>
<td>1.000</td>
<td>1.213 x 10^-15</td>
</tr>
<tr>
<td>groupGrade5</td>
<td>0.793</td>
<td>0.033</td>
<td>0.729</td>
<td>0.859</td>
<td>1.000</td>
<td>1.859 x 10^-16</td>
</tr>
<tr>
<td>frequency</td>
<td>0.049</td>
<td>0.046</td>
<td>-0.043</td>
<td>0.141</td>
<td>1.000</td>
<td>0.162</td>
</tr>
<tr>
<td>grapheme_complexity</td>
<td>0.036</td>
<td>0.047</td>
<td>-0.057</td>
<td>0.130</td>
<td>1.000</td>
<td>0.123</td>
</tr>
<tr>
<td>graphomotor_difficulty</td>
<td>0.159</td>
<td>0.046</td>
<td>0.066</td>
<td>0.252</td>
<td>1.000</td>
<td>1.6037</td>
</tr>
<tr>
<td>groupGrade3:frequency</td>
<td>-0.063</td>
<td>0.065</td>
<td>-0.188</td>
<td>0.064</td>
<td>1.000</td>
<td>0.199</td>
</tr>
<tr>
<td>groupGrade5:frequency</td>
<td>-0.031</td>
<td>0.064</td>
<td>-0.156</td>
<td>0.095</td>
<td>1.000</td>
<td>0.142</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity</td>
<td>-0.049</td>
<td>0.066</td>
<td>-0.177</td>
<td>0.080</td>
<td>1.000</td>
<td>0.169</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity</td>
<td>-0.025</td>
<td>0.065</td>
<td>-0.151</td>
<td>0.100</td>
<td>1.000</td>
<td>0.137</td>
</tr>
<tr>
<td>frequency:grapheme_complexity</td>
<td>-0.051</td>
<td>0.089</td>
<td>-0.232</td>
<td>0.129</td>
<td>1.000</td>
<td>0.208</td>
</tr>
<tr>
<td>groupGrade3:graphomotor_difficulty</td>
<td>-0.025</td>
<td>0.066</td>
<td>-0.154</td>
<td>0.103</td>
<td>1.000</td>
<td>0.137</td>
</tr>
<tr>
<td>groupGrade5:graphomotor_difficulty</td>
<td>-0.031</td>
<td>0.064</td>
<td>-0.156</td>
<td>0.095</td>
<td>1.000</td>
<td>0.14</td>
</tr>
<tr>
<td>frequency:graphomotor_difficulty</td>
<td>0.158</td>
<td>0.091</td>
<td>-0.024</td>
<td>0.337</td>
<td>1.000</td>
<td>0.78</td>
</tr>
<tr>
<td>grapheme_complexity:graphomotor_difficulty</td>
<td>0.027</td>
<td>0.091</td>
<td>-0.154</td>
<td>0.206</td>
<td>1.000</td>
<td>0.189</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity</td>
<td>0.015</td>
<td>0.125</td>
<td>-0.229</td>
<td>0.261</td>
<td>1.000</td>
<td>0.248</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity</td>
<td>0.097</td>
<td>0.123</td>
<td>-0.144</td>
<td>0.341</td>
<td>1.000</td>
<td>0.342</td>
</tr>
<tr>
<td>groupGrade3:frequency:graphomotor_difficulty</td>
<td>-0.049</td>
<td>0.127</td>
<td>-0.295</td>
<td>0.198</td>
<td>1.000</td>
<td>0.268</td>
</tr>
<tr>
<td>groupGrade5:frequency:graphomotor_difficulty</td>
<td>-0.174</td>
<td>0.124</td>
<td>-0.412</td>
<td>0.069</td>
<td>1.000</td>
<td>0.635</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity:graphomotor_difficulty</td>
<td>-0.036</td>
<td>0.125</td>
<td>-0.284</td>
<td>0.213</td>
<td>1.000</td>
<td>0.255</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity:graphomotor_difficulty</td>
<td>-0.020</td>
<td>0.124</td>
<td>-0.261</td>
<td>0.224</td>
<td>1.000</td>
<td>0.25</td>
</tr>
<tr>
<td>frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>0.070</td>
<td>0.166</td>
<td>-0.249</td>
<td>0.397</td>
<td>1.000</td>
<td>0.357</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>0.044</td>
<td>0.227</td>
<td>-0.395</td>
<td>0.487</td>
<td>1.000</td>
<td>0.457</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>-0.086</td>
<td>0.222</td>
<td>-0.523</td>
<td>0.351</td>
<td>1.000</td>
<td>0.465</td>
</tr>
</tbody>
</table>

**Note.** For each slope (for each line), the first two columns represent the estimated most probable value and its standard error (SE). The 'Lower' and 'Upper' columns contain the lower and upper bounds of the 95% CrI, whereas the 'Rhat' column reports the Gelman-Rubin statistic. The last column reports the Bayes factor in favour of the alternative hypothesis, relative to the null hypothesis (BF10).
These estimations are better understood visually. Thus, we plot the predictions of this model against raw data in Figure 11.

```r
# retrieving the model's predictions
velocity_predictions <- df2 %>%
data_grid(graphomotor_difficulty, grapheme_complexity, frequency, group) %>%
cbind(., fitted(
  object = mod2, newdata = ., resp = "meanvelocity",
  scale = "response", probs = c(0.025, 0.975),
  re_formula = NA, robust = TRUE
)) %>%
ungroup %>%
dplyr::rename(estimate = Estimate, mad = Est.Error, lower = Q2.5, upper = Q97.5)
```

![Graph](image)

**Figure 11.** Mean velocity by grade and word frequency (x-axis), grapheme complexity (in colour), and graphomotor difficulty (in panels). Transparent points represent individual data per participant. The surimposed dots and intervals represent the model’s predictions (median and 95% credible interval of the posterior distribution).

As can be seen in Figure 11, the model most notably predicts higher velocity for the difficult letter f as compared to the easy letter t, excepted for low frequency words in Grade...
1. First graders seem to have lower velocity than third graders, who themselves seem to have lower velocity than fifth graders on average. As can be seen from Table 5, BF s favouring the alternative hypothesis (relative to the null hypothesis) are BF s for the difference between Grade 1 and Grade 3 ($\beta = 0.562$, 95% CrI [0.496, 0.628], $BF_{10} = 1.213 \times 10^{-15}$), as well as between Grade 1 and Grade 5 ($\beta = 0.793$, 95% CrI [0.729, 0.859], $BF_{10} = 1.859 \times 10^{-16}$), and the effect of graphomotor difficulty in Grade 1 ($\beta = 0.159$, 95% CrI [0.066, 0.252], $BF_{10} = 16.037$). Predictions from this model for each condition are also summarised in Table 6.

Table 6

<table>
<thead>
<tr>
<th>Group</th>
<th>Frequency</th>
<th>Grapheme complexity</th>
<th>Graphomotor difficulty</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>10.439</td>
<td>0.649</td>
<td>9.228</td>
<td>11.835</td>
</tr>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>11.350</td>
<td>0.730</td>
<td>9.992</td>
<td>12.881</td>
</tr>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>11.140</td>
<td>0.708</td>
<td>9.836</td>
<td>12.636</td>
</tr>
<tr>
<td>Grade1</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>12.020</td>
<td>0.793</td>
<td>10.538</td>
<td>13.677</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>10.576</td>
<td>0.676</td>
<td>9.321</td>
<td>12.025</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>12.975</td>
<td>0.831</td>
<td>11.427</td>
<td>14.742</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>10.302</td>
<td>0.661</td>
<td>9.131</td>
<td>11.763</td>
</tr>
<tr>
<td>Grade1</td>
<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>13.521</td>
<td>0.855</td>
<td>11.928</td>
<td>15.358</td>
</tr>
<tr>
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<td>LF</td>
<td>Simple</td>
<td>t</td>
<td>19.061</td>
<td>1.367</td>
<td>16.534</td>
<td>21.957</td>
</tr>
<tr>
<td>Grade3</td>
<td>LF</td>
<td>Simple</td>
<td>f</td>
<td>21.336</td>
<td>1.525</td>
<td>18.496</td>
<td>24.615</td>
</tr>
<tr>
<td>Grade3</td>
<td>LF</td>
<td>Complex</td>
<td>t</td>
<td>19.793</td>
<td>1.427</td>
<td>17.149</td>
<td>22.855</td>
</tr>
<tr>
<td>Grade3</td>
<td>LF</td>
<td>Complex</td>
<td>f</td>
<td>20.730</td>
<td>1.487</td>
<td>18.022</td>
<td>23.867</td>
</tr>
<tr>
<td>Grade3</td>
<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>18.659</td>
<td>1.332</td>
<td>16.159</td>
<td>21.537</td>
</tr>
<tr>
<td>Grade3</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>21.965</td>
<td>1.535</td>
<td>19.107</td>
<td>24.769</td>
</tr>
<tr>
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<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>17.680</td>
<td>1.288</td>
<td>15.285</td>
<td>20.402</td>
</tr>
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<td>f</td>
<td>21.822</td>
<td>1.544</td>
<td>18.957</td>
<td>25.160</td>
</tr>
<tr>
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<td>t</td>
<td>23.643</td>
<td>1.627</td>
<td>20.601</td>
<td>27.333</td>
</tr>
<tr>
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<td>Simple</td>
<td>f</td>
<td>26.864</td>
<td>1.876</td>
<td>23.411</td>
<td>30.888</td>
</tr>
<tr>
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<td>t</td>
<td>23.158</td>
<td>1.610</td>
<td>20.167</td>
<td>26.606</td>
</tr>
<tr>
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<td>26.743</td>
<td>1.868</td>
<td>23.308</td>
<td>30.681</td>
</tr>
<tr>
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<td>HF</td>
<td>Simple</td>
<td>t</td>
<td>23.599</td>
<td>1.649</td>
<td>20.547</td>
<td>27.100</td>
</tr>
<tr>
<td>Grade5</td>
<td>HF</td>
<td>Simple</td>
<td>f</td>
<td>26.604</td>
<td>1.844</td>
<td>23.236</td>
<td>30.499</td>
</tr>
<tr>
<td>Grade5</td>
<td>HF</td>
<td>Complex</td>
<td>t</td>
<td>24.416</td>
<td>1.695</td>
<td>21.327</td>
<td>27.982</td>
</tr>
<tr>
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<td>HF</td>
<td>Complex</td>
<td>f</td>
<td>27.526</td>
<td>1.907</td>
<td>24.944</td>
<td>31.594</td>
</tr>
</tbody>
</table>

Note. For each condition, the 'Estimate' and 'MAD' columns contain the median and the median absolute deviation (MAD) of the posterior distribution, respectively. The 'Lower' and 'Upper' columns contain the lower and upper bounds of the 95% credible interval.

For exploratory purposes, we depict below the posterior distribution of the difference between high-frequency and low-frequency words (i.e., the effect of frequency) separately for each letter (graphomotor difficulty) and each grade. We averaged the predictions across both conditions of graphemic complexity, as this effect appeared to be null.

As can be seen in Figure 12, the posterior distribution for the effect of frequency is almost perfectly centred on zero in all conditions, except for letter f in Grade 1. In this condition, there is a 0.92 probability that the effect of frequency on the mean velocity (in mm per second) is positive (given the data and the priors).
Figure 12. Effect of word frequency on the mean velocity (in mm per second) for each grade (in column) and letter (in row). The histogram contains posterior samples for each effect, where the posterior distribution is summarised by its mean and 95% highest density interval (HDI). The green text indicates the probability that the parameter values is either inferior or superior to 0.

3.4 Letter size

Table 7 reports the estimates (median of the posterior distribution) and associated 95% credible intervals and BF for all parameters regarding the letter size.
Table 7

Estimates and BFs for the slopes for the letter size.

<table>
<thead>
<tr>
<th>Term</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
<th>Rhat</th>
<th>BF10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>2.289</td>
<td>0.023</td>
<td>2.241</td>
<td>2.333</td>
<td>1.000NA</td>
<td></td>
</tr>
<tr>
<td>groupGrade3</td>
<td>-0.125</td>
<td>0.029</td>
<td>-0.181</td>
<td>-0.070</td>
<td>1.000</td>
<td>7.090 x 10^-3</td>
</tr>
<tr>
<td>groupGrade5</td>
<td>0.006</td>
<td>0.028</td>
<td>-0.049</td>
<td>0.061</td>
<td>1.000</td>
<td>0.059</td>
</tr>
<tr>
<td>frequency</td>
<td>0.023</td>
<td>0.042</td>
<td>-0.059</td>
<td>0.107</td>
<td>1.000</td>
<td>0.097</td>
</tr>
<tr>
<td>grapheme_complexity</td>
<td>0.032</td>
<td>0.042</td>
<td>-0.051</td>
<td>0.116</td>
<td>1.000</td>
<td>0.115</td>
</tr>
<tr>
<td>graphomotor_difficulty</td>
<td>0.703</td>
<td>0.042</td>
<td>0.618</td>
<td>0.788</td>
<td>1.000</td>
<td>-9.629 x 10^-16</td>
</tr>
<tr>
<td>groupGrade3:frequency</td>
<td>-0.021</td>
<td>0.057</td>
<td>-0.133</td>
<td>0.090</td>
<td>1.000</td>
<td>0.124</td>
</tr>
<tr>
<td>groupGrade5:frequency</td>
<td>-0.004</td>
<td>0.055</td>
<td>-0.112</td>
<td>0.105</td>
<td>1.000</td>
<td>0.112</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity</td>
<td>-0.027</td>
<td>0.056</td>
<td>-0.138</td>
<td>0.085</td>
<td>1.000</td>
<td>0.126</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity</td>
<td>-0.012</td>
<td>0.055</td>
<td>-0.121</td>
<td>0.097</td>
<td>1.000</td>
<td>0.111</td>
</tr>
<tr>
<td>frequency:grapheme_complexity</td>
<td>0.023</td>
<td>0.081</td>
<td>-0.139</td>
<td>0.186</td>
<td>1.000</td>
<td>0.17</td>
</tr>
<tr>
<td>groupGrade3:graphomotor_difficulty</td>
<td>-0.115</td>
<td>0.057</td>
<td>-0.225</td>
<td>-0.003</td>
<td>1.000</td>
<td>0.843</td>
</tr>
<tr>
<td>groupGrade5:graphomotor_difficulty</td>
<td>-0.193</td>
<td>0.055</td>
<td>-0.303</td>
<td>-0.084</td>
<td>1.000</td>
<td>42.547</td>
</tr>
<tr>
<td>frequency:graphomotor_difficulty</td>
<td>0.074</td>
<td>0.081</td>
<td>-0.090</td>
<td>0.235</td>
<td>1.000</td>
<td>0.251</td>
</tr>
<tr>
<td>grapheme_complexity:graphomotor_difficulty</td>
<td>0.022</td>
<td>0.081</td>
<td>-0.142</td>
<td>0.186</td>
<td>1.000</td>
<td>0.169</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity</td>
<td>0.004</td>
<td>0.109</td>
<td>-0.208</td>
<td>0.220</td>
<td>1.000</td>
<td>0.222</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity</td>
<td>-0.048</td>
<td>0.108</td>
<td>-0.260</td>
<td>0.164</td>
<td>1.000</td>
<td>0.237</td>
</tr>
<tr>
<td>groupGrade3:frequency:graphomotor_difficulty</td>
<td>-0.041</td>
<td>0.110</td>
<td>-0.257</td>
<td>0.177</td>
<td>1.000</td>
<td>0.237</td>
</tr>
<tr>
<td>groupGrade5:frequency:graphomotor_difficulty</td>
<td>-0.102</td>
<td>0.108</td>
<td>-0.316</td>
<td>0.108</td>
<td>1.000</td>
<td>0.334</td>
</tr>
<tr>
<td>groupGrade3:grapheme_complexity:graphomotor_difficulty</td>
<td>0.012</td>
<td>0.111</td>
<td>-0.207</td>
<td>0.228</td>
<td>1.000</td>
<td>0.228</td>
</tr>
<tr>
<td>groupGrade5:grapheme_complexity:graphomotor_difficulty</td>
<td>0.030</td>
<td>0.109</td>
<td>-0.185</td>
<td>0.244</td>
<td>1.000</td>
<td>0.229</td>
</tr>
<tr>
<td>frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>0.053</td>
<td>0.150</td>
<td>-0.248</td>
<td>0.352</td>
<td>1.000</td>
<td>0.324</td>
</tr>
<tr>
<td>groupGrade3:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>-0.025</td>
<td>0.204</td>
<td>-0.423</td>
<td>0.370</td>
<td>1.000</td>
<td>0.408</td>
</tr>
<tr>
<td>groupGrade5:frequency:grapheme_complexity:graphomotor_difficulty</td>
<td>0.023</td>
<td>0.201</td>
<td>-0.369</td>
<td>0.414</td>
<td>1.000</td>
<td>0.409</td>
</tr>
</tbody>
</table>

Note. For each slope (for each line), the first two columns represent the estimated most probable value and its standard error (SE). The 'Lower' and 'Upper' columns contain the lower and upper bounds of the 95% CrI, whereas the 'Rhat' column reports the Gelman-Rubin statistic. The last column reports the Bayes factor in favour of the alternative hypothesis, relative to the null hypothesis (BF10).
These estimations are better understood visually. Thus, we plot the predictions of this model against raw data in Figure 13.

```r
# retrieving the model's predictions
size_predictions <- df2 %>%
  data_grid(graphomotor_difficulty, grapheme_complexity, frequency, group) %>%
  cbind(., fitted(
    object = mod2, newdata = ., resp = "lettersize",
    scale = "response", probs = c(0.025, 0.975),
    re_formula = NA, robust = TRUE
  )) %>%
  ungroup %>%
  dplyr::rename(estimate = Estimate, mad = Est.Error, lower = Q2.5, upper = Q97.5)
```

![Graph showing letter size by grade and word frequency (x-axis), grapheme complexity (in colour), and graphomotor difficulty (in panels). Transparent points represent individual data per participant. The surimposed dots and intervals represent the model's predictions (median and 95% credible interval of the posterior distribution).](image)

*Figure 13.* Letter size by grade and word frequency (x-axis), grapheme complexity (in colour), and graphomotor difficulty (in panels). Transparent points represent individual data per participant. The surimposed dots and intervals represent the model’s predictions (median and 95% credible interval of the posterior distribution).

As can be seen in Figure 13, the production of difficult letters was associated with greater letter size than the production of easy letters for all grades. As can be seen from
Table 7, BFs favouring the alternative hypothesis (relative to the null hypothesis) are BFs for the difference between Grade 1 and Grade 3 ($\beta = -0.125$, 95% CrI [-0.181, -0.07], BF$_{10} = 7.090 \times 10^{-3}$), the effect of graphomotor difficulty in Grade 1 ($\beta = 0.703$, 95% CrI [0.618, 0.788], BF$_{10} = -9.629 \times 10^{-16}$), and the effect of graphomotor difficulty in Grade 5 ($\beta = -0.193$, 95% CrI [-0.303, -0.084], BF$_{10} = 42.547$). Predictions from this model for each condition are also summarised in Table 8.

Table 8

*Estimated letter size in each condition.*

<table>
<thead>
<tr>
<th>Group</th>
<th>Frequency</th>
<th>Grapheme complexity</th>
<th>Graphomotor difficulty</th>
<th>Estimate</th>
<th>MAD</th>
<th>Lower</th>
<th>Upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grade1 LF</td>
<td>Simple</td>
<td>t</td>
<td>7.489</td>
<td>0.427</td>
<td>6.691</td>
<td>8.391</td>
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</tr>
<tr>
<td>Grade1 LF</td>
<td>Simple</td>
<td>f</td>
<td>14.538</td>
<td>0.837</td>
<td>12.946</td>
<td>16.292</td>
<td></td>
</tr>
<tr>
<td>Grade1 LF</td>
<td>Complex</td>
<td>t</td>
<td>7.665</td>
<td>0.436</td>
<td>6.838</td>
<td>8.586</td>
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</tr>
<tr>
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<td>Complex</td>
<td>f</td>
<td>14.815</td>
<td>0.872</td>
<td>13.109</td>
<td>16.659</td>
<td></td>
</tr>
<tr>
<td>Grade1 HF</td>
<td>Simple</td>
<td>t</td>
<td>7.405</td>
<td>0.429</td>
<td>6.614</td>
<td>8.310</td>
<td></td>
</tr>
<tr>
<td>Grade1 HF</td>
<td>Simple</td>
<td>f</td>
<td>15.058</td>
<td>0.852</td>
<td>13.431</td>
<td>16.889</td>
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</tr>
<tr>
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<td>Complex</td>
<td>t</td>
<td>7.550</td>
<td>0.430</td>
<td>6.725</td>
<td>8.483</td>
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<tr>
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<td>f</td>
<td>16.120</td>
<td>0.922</td>
<td>14.372</td>
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<td>Simple</td>
<td>f</td>
<td>12.482</td>
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<td>10.983</td>
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</tr>
<tr>
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<td>Complex</td>
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<td>0.449</td>
<td>6.197</td>
<td>7.969</td>
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<td>12.503</td>
<td>0.787</td>
<td>11.021</td>
<td>14.182</td>
<td></td>
</tr>
<tr>
<td>Grade3 HF</td>
<td>Simple</td>
<td>t</td>
<td>6.998</td>
<td>0.434</td>
<td>6.180</td>
<td>7.962</td>
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<tr>
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<td>Simple</td>
<td>f</td>
<td>12.454</td>
<td>0.786</td>
<td>11.002</td>
<td>14.111</td>
<td></td>
</tr>
<tr>
<td>Grade3 HF</td>
<td>Complex</td>
<td>t</td>
<td>6.972</td>
<td>0.446</td>
<td>6.139</td>
<td>7.925</td>
<td></td>
</tr>
<tr>
<td>Grade3 HF</td>
<td>Complex</td>
<td>f</td>
<td>13.006</td>
<td>0.832</td>
<td>11.461</td>
<td>14.752</td>
<td></td>
</tr>
<tr>
<td>Grade5 LF</td>
<td>Simple</td>
<td>t</td>
<td>8.081</td>
<td>0.498</td>
<td>7.157</td>
<td>9.157</td>
<td></td>
</tr>
<tr>
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<td>Simple</td>
<td>f</td>
<td>13.509</td>
<td>0.824</td>
<td>11.949</td>
<td>15.281</td>
<td></td>
</tr>
<tr>
<td>Grade5 LF</td>
<td>Complex</td>
<td>t</td>
<td>8.288</td>
<td>0.506</td>
<td>7.343</td>
<td>9.378</td>
<td></td>
</tr>
<tr>
<td>Grade5 LF</td>
<td>Complex</td>
<td>f</td>
<td>14.054</td>
<td>0.873</td>
<td>12.399</td>
<td>15.896</td>
<td></td>
</tr>
<tr>
<td>Grade5 HF</td>
<td>Simple</td>
<td>t</td>
<td>8.625</td>
<td>0.525</td>
<td>7.638</td>
<td>9.761</td>
<td></td>
</tr>
<tr>
<td>Grade5 HF</td>
<td>Simple</td>
<td>f</td>
<td>13.495</td>
<td>0.827</td>
<td>11.942</td>
<td>15.235</td>
<td></td>
</tr>
<tr>
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<td>t</td>
<td>8.310</td>
<td>0.515</td>
<td>7.359</td>
<td>9.412</td>
<td></td>
</tr>
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<td>f</td>
<td>14.209</td>
<td>0.884</td>
<td>12.551</td>
<td>16.088</td>
<td></td>
</tr>
</tbody>
</table>

*Note.* For each condition, the 'Estimate' and 'MAD' columns contain the median and the median absolute deviation (MAD) of the posterior distribution, respectively. The 'Lower' and 'Upper' columns contain the lower and upper bounds of the 95% credible interval.

For exploratory purposes, we depict below the posterior distribution of the difference between high-frequency and low-frequency words (i.e., the effect of frequency) separately for each letter (graphomotor difficulty) and each grade. We averaged the predictions across both conditions of graphemic complexity, as this effect appeared to be null.

As can be seen in Figure 14, the posterior distribution for the effect of frequency is almost perfectly centred on zero in all conditions, except for letter f in Grade 1. In this condition, there is a 0.76 probability that the effect of frequency on the letter size (in mm) is positive (given the data and the priors).
Figure 14. Effect of word frequency on the letter size (in mm) for each grade (in column) and letter (in row). The histogram contains posterior samples for each effect, where the posterior distribution is summarised by its mean and 95% highest density interval (HDI). The green text indicates the probability that the parameter values is either inferior or superior to 0.

4 Acknowledgements

Acknowledgements will be included in the final version of the supplementary materials.
5 Session information

```r
sessionInfo()
```

```r
## R version 4.1.1 (2021-08-10)
## Platform: x86_64-apple-darwin17.0 (64-bit)
## Running under: macOS Big Sur 10.16
##
## Matrix products: default
## BLAS: /Library/Frameworks/R.framework/Versions/4.1/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/4.1/Resources/lib/libRlapack.dylib
##
## locale:
##
## attached base packages:
## [1] stats  graphics  grDevices  utils  datasets  methods  base
##
## other attached packages:
## [1] brms_2.16.2  Rcpp_1.0.7  BEST_0.5.3  HDInterval_0.2.2
## [5] glue_1.4.2  knitr_1.36  papaja_0.1.0.9997  readxl_1.3.1
## [9] GGally_2.1.2  modelr_0.1.8  tidybayes_3.0.1  posterior_1.1.0
## [13] patchwork_1.1.1  forcats_0.5.1  stringr_1.4.0  dplyr_1.0.7
## [17] purrr_0.3.4  readr_2.0.2  tidyr_1.1.4  tibble_3.1.5
## [21] tidyverse_1.3.1  ggbeeswarm_0.6.0  ggplot2_3.3.5  extraDistr_1.9.1
##
## loaded via a namespace (and not attached):
## [1] backports_1.3.0  plyr_1.8.6  igraph_1.2.6
## [4] splines_4.1.1  svUnit_1.0.6  crosstalk_1.1.1
## [7] rstantools_2.1.1  inline_0.3.19  digest_0.6.28
## [10] htmltools_0.5.2  rsconnect_0.8.24  fansi_0.5.0
## [13] magrittr_2.0.1  checkmate_2.0.0  tzdb_0.1.2
## [16] RcppParallel_5.1.4  matrixStats_0.61.0  xts_0.12.1
## [19] prettyunits_1.1.1  colorspace_2.0-2  rvest_1.0.1
## [22] ggdist_3.0.0  haven_2.4.3  xfun_0.26
## [25] callr_3.7.0  crayon_1.4.2  jsonlite_1.7.2
## [28] lme4_1.1-27.1  zoo_1.8-9  gtable_0.3.0
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## [34] pkgbuild_1.2.0 rstan_2.26.3
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## [37] scales_1.1.1 mvtorm_1.1-3
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## [52] reshape_0.8.8 loo_2.4.1
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## [55] dbplyr_2.1.1 utf8_1.2.2
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## [64] cli_3.1.0 generics_0.1.0
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## [67] ggridges_0.5.3 evaluate_0.14
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## [70] yam_2.2.1 processx_3.5.2
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## [73] nlme_3.1-152 projpred_2.0.2
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## [94] vctrs_0.3.8 pillar_1.6.4
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## [109] colourpicker_1.1.1 gtools_3.9.2
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## [118] minqa_1.2.4 coda_0.19-4
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## [121] shiny_1.7.1 lubridate_1.8.0
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## [124] dygraphs_1.1.1.6
References


