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PIV MEASUREMENTS OF FLOW IN AN AERATED TANK
STIRRED BY A DOWN- AND AN UP-PUMPING AXIAL FLOW IMPELLER

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**Abstract:** Liquid phase hydrodynamics in an aerated tank stirred by a down- and an up-pumping pitched blade turbine have been investigated using Particle Image Velocimetry. The effect of agitator configuration and the gas phase on the mean velocity fields and turbulent quantities in the vessel have been investigated. The global mean gas holdup has also been evaluated for the two pumping conditions. For the gas flow rate used, the presence of gas only slightly alters the liquid flow patterns produced by both the down- and up-pumping configurations and causes a general decrease in the mean liquid velocities. The turbulent kinetic energy in the impeller discharge region was not affected by the presence of gas, but in the bulk of the tank, aeration caused a decrease in this value. Global gas holdup was found to be ~36% greater for the up-pumping impeller and a large amount of gas was found to be entrained by the primary circulation loop.

**Keywords:** mixing, gas-liquid, pitched blade turbine, up-pumping, Particle Image Velocimetry

**INTRODUCTION**

Fermentation, wastewater aeration, oxidation and hydrogenation represent only a small number of the complex mixing processes where gas dispersion is employed in mechanically agitated tanks. Traditionally, gas dispersion in agitated vessels is carried out using radial disc turbines, such as the Rushton turbine. With the aim of reducing the weaknesses of disc turbines in gas-liquid applications, an increased interest in axial flow impellers for such operations has evolved. Customarily, the axial impellers are used in the down-pumping mode and have provided significant advantages over radial flow agitators (McFarlane and Nienow [1, 2]). Recently, the up-pumping concept, which was first conceived in the early 1980s (Kuboi and Nienow [3]; Nienow et al. [4]), has been shown to provide advantages over the down-pumping operation (Nienow [5, 6, 7]) especially for gas-liquid applications. Since the mid-1990s, the investigation of up-pumping impellers aerated and non-aerated tanks has primarily been focused on power characteristics and mixing times (McFarlane [8]; Hari-Prajitno et al. [9]; Hari-Prajitno [10]).

The local investigation of velocity fields of two-phase flows in stirred tanks has been the subject of few reported works (Patterson [11]; Mishra and Joshi [12]; Rousar and Van den Akker [13]; Deen and Hjertager [14]; Ranade et al. [15]). Most of these use Laser Doppler Velocimetry (LDV) to study flows produced by Rushton turbines. Particle Image Velocimetry (PIV) is a recent non-intrusive experimental technique used for the study of instantaneous flow fields, both single phase and multiphase. Due to the inherent difficulties associated with the highly 3-dimensional flow in stirred tanks, PIV has been used very little for the investigation of
hydrodynamics in such configurations. Lamberto et al. [16] used PIV results to validate Computational Fluid Dynamics (CFD) simulations of the laminar flow in a tank stirred by a Rushton turbine. In the turbulent flow regime, Sheng et al. [17] used PIV to determine the mean flow field and turbulence characteristics produced by a down-pumping 4-bladed pitched blade turbine and compared these results with imposed boundary condition CFD simulations. Meyers et al. [18] investigated flow instabilities induced by a down pumping 4-bladed pitched blade turbine and a down-pumping HE-3 (Chemineer), and compared these instantaneous flow fields with time-averaged data. Gas-liquid flows in agitated vessels provide additional complications with respect to data acquisition and processing, and therefore published work in this area is very scarce. A gas-liquid study was carried out by Deen and Hjertager [14] using PIV measurements. They compared single phase flow patterns produced by a Rushton turbine with the liquid velocity fields in a two-phase system. Ranade et al. [15] also used PIV to study the liquid flow field of an aerated stirred tank, concentrating on the effect of the gas flow rate on the trailing vortices behind the blades of a Rushton turbine.

In this work, the hydrodynamics of the liquid phase in an aerated vessel stirred with a 6-blade pitched blade turbine (PBT) have been investigated using PIV. A preliminary study has involved the determination of the single phase flow fields in order to provide a reference point for the two phase study. For the two phase case, the influence of the presence of gas on the mean liquid velocity field has been studied, as well as the effect of the axial agitator configuration, i.e. down-pumping or up-pumping, on the turbulent liquid flow field. With respect to the gas phase, the bubble distribution and global gas holdup have been assessed and discussed. In addition, the effect of aeration on the pumping number has been evaluated for the different pumping configurations.

**EXPERIMENTAL APPARATUS**

PIV measurements of instantaneous radial and axial velocity components were performed in a dished-bottom cylindrical vessel made of Perspex. An aspect ratio of 1 was used, i.e. the liquid height ($H$) in the vessel is equal to the tank diameter ($T$), where $T=0.19$ m. The tank is equipped with four transparent baffles made of Perspex ($b=0.17$), which are placed 90° from one another, flush against the vessel wall. The impeller clearance is $C=0.33T$, where $C$ is defined as the distance from the vessel bottom to the lowest horizontal plane swept by the impeller. The cylindrical vessel is placed inside a square tank whose front panel is transparent to allow distortion-free measurements. This tank was filled with plain water in order to minimize refraction at the cylindrical surface of the inner vessel. A 6-blade 45° pitched blade turbine operating in the down- and up-pumping modes was investigated. The impeller diameter was equal to $D=0.5T$ and the agitator shaft ($s=0.008$ m)
extended to the bottom of the vessel where it fitted into a Teflon hub to avoid ‘wobbling’ of the impeller. The rotational speed of the agitator was 300 rpm which is equivalent to a Reynolds number of 45000. Air was sparged into the tank using a ring sparger with diameter $D_s=0.8D$ at a position, $C_s=0.6C$. The gas is introduced into the vessel at 0.5 vvm and an aeration number, $N_A$, equal to 0.01, which corresponds to a complete dispersion regime.

The PIV measurements were taken using a double pulsed Minilite Nd:YAG laser (Continuum) that has a variable frequency between 1 and 15Hz, and a wavelength of 532nm (green). A black and white CCD camera (Kodak) with a resolution of $1008 \times 1018$ pixels$^2$ was used to record simultaneous images of the flow on a plane midway between two baffles. A MasterBox links the lasers, camera and computer, and allows several operating parameters to be optimized. The experimental set-up is shown in Figure 1. The liquid phase was seeded using 30µm hollow glass particles with fluorescent rhodamine (Dantec) implanted on the surface. These particles diffuse light at a wavelength of 575nm which is greater than the wavelength of light diffused by the air bubbles, 550nm. A filter is fitted to the camera which enables only light with a wavelength greater than 550nm to be captured. Images are acquired at 10Hz with an exposure time delay of 500µs and are not synchronized with the passage of the impeller blade. These images are processed using a commercial software VISION+ V2ZIP (Lot Oriel / Coria, France). Each image is divided up into interrogation areas of $64 \times 64$ pixels$^2$ ($8.6 \times 8.6$ mm$^2$) with 50% overlap, and the cross-correlation function in each area is then calculated using fast Fourier transforms in order to determine the corresponding spatially averaged displacement vector. The instantaneous velocity data attained for a number of image pairs are used to determine the time-averaged radial-axial velocity fields. The number of image pairs used to determine the mean fields for each case are summarized in Table 1. As spurious data results when bubbles pass the interrogation area, two correction criteria have been applied whilst averaging the instantaneous data. The first criterion assumes that all vectors with a signal to noise ratio (SNR) less than 2.0 are erroneous due to the gas phase and are therefore not taken into account in the calculation of the mean value. The second criteria is applied for the two-phase studies only. If less than 15% of the vectors at a specific point have a valid SNR (i.e. $SNR > 2.0$), then it is assumed that at that point, the gas phase is often present and a liquid phase vector is not effectuated.

RESULTS AND DISCUSSION

Bubble Distribution and Gas Holdup

Figures 2 (a) and (b) are instantaneous photographic images of the aerated vessel stirred by the PBT in the down- and up-pumping modes, respectively. In the down-pumping mode, the agitator disperses the bubbles throughout
the vessel with oscillations between hydrodynamic flow patterns, and some gas accumulation occurs behind the impeller blades. These observations are comparable with gassed flow patterns described in previous studies (Bujalski et al. [19]; McFarlane et al., [20]). In the up-pumping mode, the bubble distribution can be divided into two parts. In the lower half of the tank, an extremely large number of bubbles are entrained in a lower circulation loop, such that impeller is surrounded by the gas phase. It was noticed that even when the gas flow rate was halted, a significant number of bubbles remained entrained in this loop for at least three minutes. In the upper half of the vessel, the gas holdup appears to be less than in the lower half, however, and the bubbles are well dispersed. Furthermore, the hydrodynamic fluctuations noted in the down-pumping case do not exist with the PBTU, which agrees with the observations made in other reported works concerning up-pumping axial flow impellers (Bujalski et al. [19]; Nienow [7, 21]).

The global gas holdup, $\alpha_g$, for the down- and up-pumping configurations was estimated by simple observation of the liquid level without gassing, $x$, and with gassing, $x_g$. The difference, $x-x_g$, divided by the liquid level without aeration, $x$, is the global gas holdup, $\alpha_g$ (assuming a flat bottomed vessel). The values of $\alpha_g$ for the PBTD and PBTU are given in Table 2. In the up-pumping mode, the PBT entrains approximately 36% more gas in the vessel than in the down-pumping configuration. These results correspond well with the visual observations made, represented by Figure 2.

**Effect of Aeration on Mean Liquid Velocity Fields**

Vector plots of the mean velocity fields in the $r$-$z$ plane at 45° to the baffle plane for the PBTD and PBTU without and with aeration are shown in Figures 3 and 4, respectively. In the ungassed case, Figure 3 (a), the flow pattern is typical for down-pumping pitched blade turbines (Ranade and Joshi [22]; Aubin et al. [23]). A primary circulation loop exists in the lower part of the tank and extends up to almost three-quarters of the vessel. In the upper quarter of the tank, the liquid velocities are low and circulation is poor. Just below the center of the impeller a region of up-flowing liquid exists, which is evidence of a secondary recirculation loop. Due to the dished bottom of the vessel, this entire secondary circulation loop could not be captured with the PIV. For the aerated case, Figure 3 (b), the liquid velocity vectors show that the principal circulation loop is still present, although its form is slightly smaller than that of the single phase case, extending up to only about two-thirds of the vessel height. This ‘shortening’ of the circulation loop is due to the change in pressure around the impeller upon gassing. The flat, inclined blade of the pitched blade turbine leads to the formation of a low pressure trailing vortex at the rear of the blade (Warmoeskerken et al. [24]). Upon aeration, gas is concentrated in these
low pressure regions forming gas cavities. The presence of these low pressure zones may cause the liquid to be
drawn in by the vertical side of the impeller as well as the top, which in turn may decrease the flow path of the
circulation loop. This also results in the displacement of the circulation center towards the vessel base. In the
upper third of the vessel, the velocities are smaller than for the single phase system which suggests that the flow
in this region is controlled not only by the impeller but also by the gas phase. In the outflow of the impeller, the
fluid is discharged strongly at about 30° from the vertical, which is different from the single phase case where
the fluid jet is at about 45° from the vertical. As a result, the conical up-flow region is significantly smaller in the
case of the two phase flow. This phenomenon could be due to the build up of gas behind the impeller blades and
consequent change in the pressure field.

In a more quantitative manner, radial profiles of the axial velocity for the PBTD at several vertical
positions in the vessel are shown in Figure 5 (a). Just above the gas sparger, in the lower part of the tank
($z^* = 0.19$), the axial velocity is greater for the aerated case than for without gassing. This may be due to the
upward rising flow of bubbles from the sparger that consequently entrain nearby liquid. In the impeller discharge
region at $z^* = 0.31$, the magnitude of the axial velocity for both the gassed and ungassed case are very similar.
Above the impeller, however, at positions $z^* = 0.49$, 0.65 and 0.78, the presence of gas causes a significant
decrease in the axial velocity. This suggests that the liquid flow in the upper part of the vessel is controlled not
only by the impeller but also by the gas phase. Similar results of liquid velocity profiles produced by a Rushton
turbine in a two phase system have been reported by Deen and Hjertager [14] and Ranade et al. [15].

The mean vector plots for the up-pumping PBT without and with gassing are presented in Figure 4.
The single phase flow produced by the PBTU, Figure 4 (a), results in two distinct circulation loops, in the lower
and upper parts of the vessel, and a well defined cone-shaped region of down-flowing liquid just above the
impeller. These results agree well with previous studies on up-pumping pitched blade turbines and hydrofoil
impellers using LDV (Aubin et al. [23]; Meyers and Bakker [25]; Mishra et al. [26]). The liquid phase velocity
vectors for the two-phase case, Figure 4 (b), show that the lower circulation loop is conserved in the presence of
gas. The liquid is drawn in by the underside of the PBT at an angle towards the impeller shaft and is then
projected at approximately 45° towards the vessel wall by the upper side of the impeller. The liquid moves down
the vessel wall towards the bottom, where it is taken up by the impeller once again, forming the first circulation
loop. As for the single phase case, down-flowing liquid is present in the center of the upper plane of the impeller.
In the region around the agitator tip, many liquid velocity vectors are not present, which indicates high local gas
holdup according to the criteria used during the post-processing in this work. These results agree well with the observations of gas dispersion shown in the photographic image in Figure 2.

In the upper half of the vessel, the flow patterns for the single and two phase flows are rather different. In the presence of gas, the strong down-flowing velocities coming from the center of the vessel are apparent. This flow joins the impeller jet and is projected towards the tank wall. Most of the liquid then follows the movement of the circulation loop, however, some liquid is deflected and moves up the vessel wall, forming a secondary circulation loop. This second loop is much less well-defined in the two-phase case and it appears that conservation of mass is not satisfied, suggesting that the flow rate and patterns may be dependent on the position of the baffles and/or the tangential velocity component is non-negligible. It would be therefore interesting to compare these results with measurements taken in the baffle plane. Unfortunately, the latter is not currently possible due to the existing experimental setup.

Figure 5 (b) shows the radial profiles of the axial velocity for a range of heights in the tank stirred by the PBTU. Below the impeller, at $z^* = 0.19$ and $0.31$, and in the discharge region at $z^* = 0.49$, the presence of gas causes a decrease in the axial velocity of about 30%. In the upper part of the vessel, however, closer to the liquid surface, the effect of gassing on the liquid flow is negligible. This indicates that the impeller is still controlling the liquid flow even in the presence of gas which suggests that the flow of gas bubbles is dominated by the liquid flow pattern and are entrained in the tank by the second circulation loop.

**Effect of Aeration on Turbulence**

Contour diagrams of rms velocities and turbulent kinetic energy for the PBTD and PBTU are shown in Figures 6 and 7, respectively. Without aeration, the maximum velocity fluctuations for the PBTD are found in the impeller discharge ($0.12V_{tip}$ for the axial component and $0.15V_{tip}$ for the radial component). Above the impeller, rms velocities range from $0.06V_{tip}$ to $0.1V_{tip}$ and the distributions for the two components are different. These results suggest that the flow is generally anisotropic in the impeller discharge and also in the bulk of the tank. Upon gassing, the maximum rms are found in the impeller discharge but vary in magnitude for the two components ($0.12V_{tip}$ for the axial component and $0.17V_{tip}$ for the radial component) which shows anisotropy. In the upper part of the tank, however, the rms velocities are generally not greater than $0.04V_{tip}$ and the flow field tends towards isotropy. Comparing the turbulent kinetic energy distributions, Figures 6 (a-iii) and (b-iii), shows that the maximum value is found in the impeller discharge for both cases. Without aeration, relatively high $k^*$ is found in the region of the primary circulation loop and into the upper part of the vessel. Upon gassing, however,
the energy in this upper region is damped, with values close to zero. It is important to point out that the maximum \( k^* \) found in the impeller discharge is equivalent (with a value of 0.028\( V_{\text{tip}}^2 \)), whether gas is present or not. Bubble break-up occurs through bubble interactions with turbulent eddies that have sufficient turbulent kinetic energy (Hinze [27]). These results therefore suggest that the impeller’s performance for the production of turbulent kinetic energy is not decreased with the addition of gas and will therefore favor bubble break-up.

Radial profiles of \( k^* \) at different heights in the vessel for the PBTD are shown in Figure 8 (a). Below the impeller, the magnitudes of \( k^* \) are similar whether gas is present or not. Above the impeller, however, it can be seen that upon gassing \( k^* \) is decreased by more than 50%.

In the up-pumping mode without aeration, the highest rms velocities (0.11\( V_{\text{tip}} \) for the axial component and 0.13\( V_{\text{tip}} \) for the radial component) are found in the impeller discharge and the bottom half of the tank, corresponding to the lower circulation loop. In the upper part of the tank, the velocity fluctuations are generally low, not greater than 0.04\( V_{\text{tip}} \). In comparison with the single phase rms velocity fields of the PBTD, the turbulence produced by the PBTU has an overall more isotropic nature. The addition of gas does not decrease the maximum values of the fluctuations but the spatial distribution of these high fluctuations is reduced. Above the impeller, however, the presence of gas slightly increases the rms velocities. Overall, for the aerated case, the flow field tends to be slightly more anisotropic than without aeration. Maximum turbulent kinetic energy is located in the impeller discharge with values of 0.020\( V_{\text{tip}}^2 \) without gas and 0.022\( V_{\text{tip}}^2 \) with gas, and relatively high values are found in the region of the lower circulation loop, although the spatial distribution is decreased upon gassing. Even though the maximum values are approximately 30% smaller than the down-pumping results, the addition of gas increases \( k^* \) which favors bubble break-up. In both cases, the turbulent kinetic energy is close to zero in the upper part of the tank (corresponding to the upper circulation loop) which suggests that minimal bubble break-up will occur in the region.

In a more quantitative manner, the radial profiles of \( k^* \) are presented in Figure 8 (b). As for the PBTD, the magnitudes of \( k^* \) in the impeller discharge are similar. In the lower part of the tank, however, the presence of gas decreases the \( k^* \) by approximately 50%. Like for the axial velocities produced by the PBTU, there appears to be no effect of aeration on the turbulent kinetic energy in the upper part of the tank at \( z^*=0.65 \) and \( z^*=0.78 \).

**Flow Number**

Table 3 presents the flow numbers for the down- and up-pumping PBT in a non-aerated and aerated tank. Comparison of the single phase results shows that the \( Fl \) for the down- and up-pumping modes are quite similar,
having a value of about 0.7. These values are also similar to those found using LDV (Aubin et al. [23]). For the down-pumping case with gassing, $Fl$ is approximately 20% less than the $Fl$ without gas. This decrease in pumping capacity is due to the accumulation of gas in the low pressure regions behind the impeller blades. For the up-pumping PBT, the value of the gassed $Fl$ is again about 20% lower than the single phase case. It should be noted, however, that this value was estimated by interpolation of the radial profile of axial velocity at the impeller discharge because due to high local gas holdup some measurement points were not obtained. Up-pumping pitched blade turbines have been found to handle more gas before flooding occurs and less pumping capacity is lost than in the down-pumping mode (Bujalski et al. [19]). Hence, it would be expected that the gassed $Fl$ value for the PBTU would be greater than for the PBTD. Therefore, the value given here is perhaps underestimated due interpolation.

**CONCLUSIONS**

PIV measurements have been carried out in an aerated vessel stirred by a 6-bladed PBT operating in the down- and up-pumping mode. Mean velocity vector fields and turbulent fields of the liquid phase have shown the effect of gassing on the liquid and have been compared with single phase results. Instantaneous photographs have enabled the bubble distribution of the up- and down-pumping PBT to be assessed.

In the down-pumping mode, the presence of gas causes a shortening of the primary circulation loop and the flow in the upper part of the vessel no longer appears to be controlled by the liquid phase. Furthermore, the liquid jet is projected with a stronger axial component and the cone-shaped up-flow region is consequently reduced. In the up-pumping mode, a strong primary circulation loop is well defined and entrains a large amount of gas in the impeller region. A second circulation loop also exists in the upper part of the tank but is not so well defined as in single phase flow. Relatively strong downward velocities are present in the upper center of the vessel which join the lower circulation loop. Furthermore, the 2D flow appears not to satisfy conservation of mass, which suggests that the flow may be dependent on the position relative to the baffle. Quantitatively, the presence of the gas has been shown to decrease liquid velocities, which agrees well with previous gas-liquid mixing studies.

In general, for both the up- and down-pumping cases, turbulent kinetic energy is similar in the impeller discharge, whether gas is present or not. This suggests that the ability of the impeller to provide turbulent energy does not decrease in the presence of gas and that bubble break-up may be favored. In the bulk of the tank,
however, the turbulent kinetic energy is decreased upon aeration which suggests that minimal break-up will occur.

Instantaneous photographs of the PBTD- and PBTU-stirred tanks have shown that the gas holdup is concentrated in the impeller region for the PBTU with good dispersion in the upper part of the vessel, whereas the PBTD entrains less gas and disperses it throughout the tank. The global gas holdup has been determined for both configurations and the PBTU has shown to entrain approximately 36% more gas than the PBTD. This suggests an improved process performance and/or efficiency with up-pumping axial flow impellers.

This work has concentrated on a local study of the liquid phase hydrodynamics which could be complemented by further studies which aim to characterize the gas phase in a local manner. It would be interesting to undertake mass transfer studies for the determination of the mass transfer coefficient, $k_{L}a$, and also to investigate the effect of bubble size on the hydrodynamics, in order to further assess the performance of up-pumping impellers in agitated tanks. Nevertheless, the detailed results on the liquid phase can be used to start the validation of two phase CFD simulations in stirred tanks.

**NOTATION**

- $b$: baffle width (m)
- $C$: impeller clearance (m)
- $C_{s}$: sparger clearance (m)
- $D$: impeller diameter (m)
- $D_{s}$: sparger diameter (m)
- $\alpha_{g}$: global gas holdup (-)
- $Fl$: flow number ($Q_{fl}/ND^{3}$)
- $k$: turbulent kinetic energy ($m^{2}s^{-1}$)
- $k^*$: turbulent kinetic energy ($m^{2}s^{-1}$)
- $k_{L}a$: volumetric mass transfer coefficient ($s^{-1}$)
- $H$: liquid height (m)
- $N$: impeller rotational speed (rev.$s^{-1}$)
- $N_{a}$: aeration number ($Q_{a}/ND^{3}$)
- $Q_{fl}$: impeller pumping rate ($m^{3}s^{-1}$)
- $Q_{g}$: gas sparging rate ($m^{3}s^{-1}$)
\( s \)  
shaft diameter (m)

\( T \)  
tank diameter (m)

\( v_r, v_z \)  
velocity components (m s\(^{-1}\))

\( v'_r, v'_z \)  
rms velocity components (m s\(^{-1}\))

\( V_{tip} \)  
impeller tip speed (m s\(^{-1}\))

\( x \)  
liquid level without gas (m)

\( x_g \)  
liquid level with gas (m)

REFERENCES


### Table 1: Number of instantaneous image pairs used for averaging the velocity fields.

<table>
<thead>
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<td>PBTD Single Phase</td>
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<tr>
<td>PBTU Single Phase</td>
<td>312</td>
</tr>
<tr>
<td>PBTD Two Phase</td>
<td>624</td>
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<tr>
<td>PBTU Two Phase</td>
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### Table 2: Global gas holdup.

<table>
<thead>
<tr>
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<th>Global Gas Holdup, $\alpha_g$</th>
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<tr>
<td>PBTD</td>
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<tr>
<td>PBTU</td>
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### Table 3: Flow numbers for down- and up-pumping PBT without and with gas.

<table>
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<td>0.68</td>
</tr>
<tr>
<td>Two Phase</td>
<td>0.59*</td>
</tr>
</tbody>
</table>

* value estimated by interpolation.
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Figure 1: Experimental set-up. (1) double pulsed Nd:Yag laser source; (2) optics; (3) lens; (4) laser sheet; (5) Masterbox; (6) computer; (7) CDD camera.

Figure 2: Images of gas-liquid flow in the vessel stirred with a (a) PBTD and (b) PBTU.

Figure 3: Mean radial-axial vector plots for the PBTD without and with aeration.

Figure 4: Mean radial-axial vector plots for the PBTU without and with aeration.

Figure 5: Radial profiles of dimensionless axial velocity at different height in the vessel.

Figure 6: Contour maps of rms velocities and dimensionless turbulent kinetic energy for the PBTD (a) without aeration and (b) with aeration.

Figure 7: Contour maps of rms velocities and dimensionless turbulent kinetic energy for the PBTU (a) without aeration and (b) with aeration.

Figure 8: Radial profiles of dimensionless turbulent kinetic energy at different height in the vessel: (a) PBTD; (b) PBTU.
Figure 1
Figure 2

(a) PBTD with gas

(b) PBTU with gas
Figure 3

(a) PBTD without gas  
(b) PBTD with gas
Figure 4

(a) PBTU without gas

(b) PBTU with gas
Figure 5
Figure 6
Figure 7
Figure 8