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Comparison of two linear modeling of the learning effect in a two-resources flowshop

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1 Introduction

Despite the technological advances in productive systems, the inclusion of workers is essential as well as the development of models that approach human behavior. In recent years, scheduling problems have started to integrate human factors. However, research opportunities exist to propose realistic models taking these factors into account when calculating job processing times in hand-intensive manufacturing system. The aim of this work is to compare two approaches to modeling the learning effect proposed in the literature in order to evaluate their complexity and to assess the effect over the makespan in a flowshop scheduling problem (FSSP).

2 Problem description and proposed solution approach

We consider a flowshop configuration where the M resources are workers, and a set of N independent jobs are to be processed in order to minimize the makespan. Each worker can process one job at a given time and preemption of a job is not allowed (that is, the execution of a job cannot be interrupted once its processing has started). All workers are available at the beginning of the scheduling horizon and have a 100% production rate.

In the basic problem (named “case 1”), \bar{p}_{ij} is the baseline processing time without learning of the i -th operation of job j . We then consider two different ways to model the learning effect, a position-based learning [1] (hereafter named “case 2”), and a truncated position-based learning [2] (hereafter named “case 3”), where the processing time of each operation j can then be calculated respectively as follow:

- Case 2: FSSP with position-based learning $P_{ijr} = \bar{p}_{ij}r^\alpha$
- Case 3: FSSP with truncated position-based learning $P_{ijr} = \bar{p}_{ij} * \max\{r^\alpha, \beta\}$

Where r is the position of job j in the sequence, P_{ijr} is the actual processing time of the i -th operation of job j located in position r , α is a parameter of learning effect ($\alpha < 0$), and β is a control parameter with $0 < \beta < 1$.

MILP-type models have been developed for all the three cases and numerical experiments were undertaken in order to evaluate the impact of the two kinds of learning effect modeling.

3 Results

MILP models were coded on Python and were solved using Pyomo library [3]. Processing times were generated using a uniform distribution between 1 and 100. In this preliminary experiments, 2 workers and 8 jobs were considered. The rationale for these values is based on the computational complexity of the flowshop problem, which increases the CPU time when increasing the number of jobs and workers. When required, the values of α were fixed to be -0.152 , -0.322 , and -0.515 , and the values of β were fixed as 0.25 , 0.50 , and 0.75 . A total of 30 replications for each combination were performed. Table 1 shows the average results obtained. We can conclude that the variation of makespan depends on the learning rate, so a lower value of α means a greater variation of makespan relative to the baseline scenario. However, lower α values and higher β values (case 3) reduce the variation.

Case	Workers	Jobs	Replications	α	β	Makespan		Average deviation from baseline makespan	CPU time (sec)		
						Average	Standard deviation		Average	Standard deviation	Min-Max
Case 1	2	8	30	-	-	459.50	65.27	-	53.83	14.50	34.49 -113.23
Case 2	2	8	30	-0.152	-	369.14	53.95	-19.70%	75.34	12.30	62.98 -131.08
Case 2	2	8	30	-0.322	-	292.75	44.39	-36.34%	61.89	7.38	44.30 -83.41
Case 2	2	8	30	-0.515	-	227.16	36.65	-50.63%	45.27	8.71	20.97 -69.14
Case 3	2	8	30	-0.152	0.25	369.14	53.95	-19.70%	75.70	11.32	63.27 -119.55
Case 3	2	8	30	-0.152	0.50	369.14	53.95	-19.70%	75.29	11.51	63.61 -126.32
Case 3	2	8	30	-0.152	0.75	370.93	54.08	-19.30%	74.90	10.43	58.67 -106.95
Case 3	2	8	30	-0.322	0.25	292.75	44.39	-36.34%	62.71	7.57	43.68 -85.30
Case 3	2	8	30	-0.322	0.50	295.75	44.39	-36.34%	62.64	7.94	43.96 -87.03
Case 3	2	8	30	-0.322	0.75	355.91	51.79	-22.56%	74.37	8.78	59.53 -90.50
Case 3	2	8	30	-0.515	0.25	227.16	36.65	-50.63%	44.76	8.38	21.29 -65.16
Case 3	2	8	30	-0.515	0.50	260.20	40.10	-43.41%	51.86	10.62	30.28 -76.38
Case 3	2	8	30	-0.515	0.75	353.76	51.44	-23.03%	74.42	7.34	61.67 -89.74

TAB 1 – Experimental results

4 Conclusions and perspectives

The originality of the study lies in the fact that it reviews different approaches proposed in the literature to model the learning effect in the FSSP, experimentally evaluate the impact of such learning effect modeling approaches. We will continue to work to overcome the current limitations (e.g., only linear learning effect models, computing time). Other modelling approaches could also be included, and given the complexity of these type of problems, alternative solution methods will be required. In addition, the deteriorating effect is expected to be incorporated.

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