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Homogenization and μ CT analysis for the trabecular bone remodeling

Claudia Chan Yone, Jean-Louis Milan, Jean-Marie Rossi, Jean-François Witz, Mathias Brieu, Patrick Chabrand

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1 Introduction

 Osteoporosis is a bone disease characterized by low bone mass but also a degradation of can- cellous bone micro-architecture. Bone weakness can generate fracture, that is why tools have been developed to assess probability of fracture. The clinical device DEXA, is a quantitative measure of bone mineral density (result is a T-score), while FRAX ^R (1) is a questionary based on statistical analysis including criteria like age, bone mass index and lifestyle. Although those informations are essential in fracture assessment, one in two person undeclared osteoporotic τ according to WHO definition (T-score $\langle -2.5 \rangle$) will have a fracture (2; 3; 4; 5). That is why bone quantity, or statistical analysis are unsufficient to predict bone weakness, but bone quality i.e bone micro-structure should be considered.

 Many numerical models have been developed in purpose to predict bone alteration and so fracture assessment. Bone alteration is due to an imbalance in the bone remodeling process : quantity of new deposited tissue is smaller than the removal old matrix tissue. Furthermore, bone is well known to adapt its morphology to the mechanical environment. From those obser- vations many researchers developed numerical models based on biological and/or mechanical criteria (6; 7; 8; 9; 10; 11; 12; 13). Among those theoritical approachs, some authors worked on real cancellous bone micro-architecture alteration (14; 15; 16; 17; 18). They have simulated trabecular plate perforation, decrease of bone volume fraction and loss of mechanical properties which can lead to bone fracture. Those approachs are interesting because they used real human bone, and predicted realistic altered cancellous micro-structure due to aging or disease.

20 Those models used micro-finite element analysis $(\mu$ FEA) based on 3-D reconstruction from $_{21}$ micro-computed tomography acquisition (μ CT). Voxels are directly convert in finite elements, as a consequence models are composed of several millions of elements (until 20 millions). The quantity of degree of freedom is not compatible with an iterative process in order to consider biological or mechanical stimuli changes. That is why alteration was randomly distributed over trabeculae and consider not any mechanical criteria. However mechanical environment play a crucial role in activation (19) and localization of bone remodeling : indeed damage and cracks are generally used as precusors of bone remodeling (20; 21; 22; 23).

28 In this study we will present a method to build μ FE model from μ CT acquisition reducing degree of freedom in order to simulate bone degradation with an iterative process, so that to integrate mechanical stimuli variations (bed-ridden case), or biological modifications (medical treatment). We will study what is the influence of reducing model complexity in term of me- chanical global and local behaviour. Furthermore we will investigate if material heterogenities, like hypermineralized bone, influence repartition of areas which are over or under-constrained among the structure. Indeed, hypermineralized bone is a privileged place of cracks accumula-tion (24), and can play an important role in ordre to identify remodeling sites.

37 2 Materials and methods

38 Trabecular bone sample and μ CT imaging

 Studied bone is a human femoral head collected behind a femoral neck fracture. The willing donor, was a woman aged of 87 years old, her bone mass index was 19.8 (limit underweight ≤ 18.5) and was prone to bone weakness because she fractured her shoulder in the past.

 A cubic specimen was harvested (10x10x10mm) from femoral head and prepared removing 43 marrow with a water bath $(37^{\circ}C)$ containing a stirring rod. Remaining marrow was extracted 44 with compressed air. Sample was scanned by a μ CT system (model Skyscan 1172) at 20μ m resolution. Cross-section images were stored in 16-bit format (format tif) with 1000x1000 pixels in size. Phantoms of cortical and trabecular bone were placed under the sample with ⁴⁷ respectively a density of hydroxyapatite of 1750 and $800mg/cm^3$, *i.e* a physical density of 2.17 ⁴⁸ and $1.53g/cm³$. These latters gave us a grayscale reference to identify material component and so mechanical properties. Some morphologic datas were computed directly after acqusition by the sofware SKYSCAN CTANalyser (table 1).

	BV/TV (%) BS/BV (mm ⁻¹) SMI Tb,Th (mm) Tb,N (mm ⁻¹) Tb,Sp (mm) DA					
29.87	10.18	0.69	0.343	0.869	0.769	0.677

BV/TV : Bone Volume/ Total Volume; BS/BV : Bone Surface/Bone Volume; SMI : Structure Model Index Tb,Th : Trabeculae Thickness; Tb,N : Trabeculae Number; Tb,Sp : Trabeculae Space; DA : Degree of Anisotropy

⁵¹ Homogenization/Coarsening method

 For the numerical study a central cubical sub-volume equivalent to 4x4x4mm (200x200x200 voxels) was extracted. A coarsening method (25; 26) was applied on the whole volume contain- ing both marrow and bone tissue elements : figure 1 describe the principle in two dimensions ⁵⁵: initial voxels of $20x20\mu m^2$ were grouped to new voxels of $40x40\mu m^2$ until $100x100x100\mu m^2$. Initial micro-structure is showed in 3 dimensions without marrow voxels in figure 2(a), and figure $2(c)$ to figure $2(f)$ illustrate different case of coarsened voxel. This method allows to simulate degradation of system acquisition, but also to reduce numbers of voxels contained in studied volume.

					n^8
				n^6	
			n ⁴		
		n^2			
	n				

Figure 1: Principle of coarsening in two dimensions : n^m contain $m \times m$ voxels of $20 \mu m$

Thresholding and mass computation

 Repartition of gray-value of whole volume was plotted (figure 3). Two significant peaks were identified : the highest correspond to the background gray-value (remaining marrow and arte- facts), although the smallest correspond to the bone tissue gray-value. Thresholding between background and bone tissue was determined as the middle point between these two peaks. As the black dash-line is cortical phantom gray-value, this graph puts forward the hypermineral-ized bone : around 70% of bone elements are hypermineralized.

 σ Initial bone mass noted M_0 was computed supposing that element bone mass was linearly correlated to the gray-value element. For coarsened geometry, mass was computed from mass density and also, cortical and trabecular phantom gray-value : each bone mass element was computed and added to get total bone mass. Thresholding was made as sample bone mass was in best agreement with M_0 , so as $\frac{|M-M_0|}{M_0}$ ⁷¹ in best agreement with M_0 , so as $\frac{|M-M_0|}{M_0} \leq 0.1\%$.

Figure 3: Grayscale of whole reference volume (without coarsening), black solid line is tresholding void/bone and black dotted line is tresholding bone/hypermineralized bone

Material heterogeneous method

 Finite element model were generated directly from converting voxels to equally sized eight-node brick elements. All elements are considered elastic linear isotropic. Poisson's ratio was ⁷⁵ set to 0.3 and Young Modulus value was calculated with the formula (25) :

$$
E_{element} = E_{max}(GV_{element})^{\gamma} \tag{1}
$$

where $GV_{element}$ is the normalized gray-value of the element, γ a constant set to 1.5, and E_{max} π is the maximal elastic modulus according to maximal gray-value considered and is determined ⁷⁸ with the equation 2:

$$
E_{max} = exp\left(log(E_{cort}) - \gamma log\left(\frac{GV_{cort}}{GV_{max}}\right)\right)
$$
\n(2)

where E_{cort} is cortical bone elastic modulus defined by nano-indentation and set to 19GPa ⁸⁰ (27; 28), GV_{cort} is cortical phantom gray-value, and GV_{max} is maximum gray-value of coarsened \mathfrak{s}_1 volume. E_{cort} was considered as treshold between mineralized and hypermineralized bone be-⁸² cause at microscopic scale cancellous and cortical bone elastic modulus are similar (27).

⁸³ More than 99.9% of bone elements have a Young modulus between 13 and 40GPa, with a ⁸⁴ maximum at 23GPa (figure 4).

Figure 4: Young modulus distribution taking account of hypermineralized bone for initial voxel size (without coarsening)

⁸⁵ Binarization method

⁸⁶ As previous method, finite element model were generated directly from converting voxels to

 equally sized eight-node brick elements. All elements are considered elastic linear isotropic with a Poisson's ratio was set to 0.3 and Young Modulus set to 19GPa.

89 Computation and post-processing

 Marrow and isolated elements were removed from the finite element analysis. Three static compression tests were simulated with an uniaxial displacement so that global mean strain was equal to -0.3%. Loading was imposed on one face of the sample, on the opposite face displace- ment along the loading was constrained, furthermore one node was encastred (to avoid part sliding). Reaction force was computed to determine apparent Young modulus of the structure and also strain energy density (directly computed with post-processing Abaqus software).

Figure 5: Schematization of method : from micro-tomography acquisition to post-processing of FEA

⁹⁶ 3 Results

⁹⁷ Influence of homogenization

⁹⁸ As far as global mechanical behaviour is concerned, apparent Young modulus was computed ⁹⁹ in 3 principal directions \vec{x} , \vec{y} and \vec{z} which correspond to normal sample faces, for different 100 coarsen voxel size. Apparent Young modulus were sorted as $E_3 > E_2 > E_1$, with $E_3 = E_z$, 101 $E_2 = E_x$ and $E_y = E_1$.

 $_{102}$ Results are plotted in figure 6(a) : for voxel size smaller than 80 μ m relative apparent Young ¹⁰³ modulus error is less than 10% compared to the original micro-structure. Relative mean strain 104 energy density error varies from 2.8% to 29.2% respectively for voxel size of 40μ m and 100μ m 105 (figure 6(b)). Relative error increases significantly from 80μ m voxel size.

Figure 6: Relative apparent Young modulus error (a) and relative mean strain energy error (b) computed for coarsened model

¹⁰⁶ As far as local mechanical behaviour is concerned, we compared distribution of strain energy 107 density between initial and coarsen model. Bone tissue where strain exceeds $3000\mu\varepsilon$, which can ¹⁰⁸ correpond from a biological point of view to remodeling sites, were identified. Indeed, when 109 strain stimulus is over $3000\mu\varepsilon$ new bone tissue is apposed (29), that is why we focused on 110 hyper-stimulated bone, where strain energy density is over w_{max} defined by :

$$
w_{max} = \frac{1}{2} E_{bone} \varepsilon_{max}^2 \quad with \quad E_{bone} = 19GPa, \quad and \quad \varepsilon_{max} = 3000 \mu \varepsilon \tag{3}
$$

 To validate that coarsening method do not degrade localization and volume of remodeling sites, mean distance between remodeling sites was calculated in coarsen model and compared with initial model. Smaller is this value, better is the accuracy of coarsen model. Moreover 114 volume remodeling sites, that is to say bone tissue where strain density exceed $3000\mu\varepsilon$ were compared. As a results, remodeling sites are located in the same place on both coarsen and 116 initial model (figure 7 (a) and (b)). For coarsen voxel of 60 μ m, mean distance between remodeling sites is around two voxels, and relative resorbable volume error is low (table 3).

Figure 7: Comparaison of strain energy distribution on initial (a) and coarsen model (b) - Localization of remodeling sites on initial (c) and coarsen model (d)

CPU time (sec)	35927	634	29	44	23
number of elements	2344910	295180	85336	36924	18927
voxel size (μm)	\approx	₽	3	$80\,$	Ξ

Table 2: Number of bone element in finite element analysis and computation time Table 2: Number of bone element in finite element analysis and computation time

Influence of binarization

 Binarized model, generally used in literature, was computed in order to compare influence of material heterogeneities on mechanical behaviour. Mean relative error on apparent Young modulus due to difference of mineralization is 7.5%, which is in agreement with literature (30). 122 Furthermore relative mean strain energy density error is less than 10% (table 4).

	Heterogeneous model Binarized model	
$E1$ (MPa)	1223	1138
$E2$ (MPa)	1374	1286
$E3$ (MPa)	1852	1682
Mean strain energy density	0.0284	0.0257
(MPa/mm^{-3})		

Table 4: Apparent young modulus and mean strain energy density on heterogeneous and binarized model

 Maximum Von mises stress are not exactly similar : 489MPa and 548MPa respectively for heterogeneous and binarized model. Nevertheless this maximum is reached at the same loca-tion, which means that structure effect is predominant over material heterogeneities.

 From a biological point of view, although number of remodeling sites are same in het- erogeneous and binarized model, difference of volume of remodeling sites reachs 19%. So with heterogeneous model remodeling sites are more expanded, which is correlated to material hetero- geneities distribution (figure 8). Material heterogeneities do not influence the global mechanical behaviour, nevertheless its influence volume of remodeling sites.

Influence of thresholding

133 After μ CT acquisition, thresolding was made to distinguish background to bone tissue. This step is essential for the rest of the numerical study. Indeed a threshold variation result in variation in bone volume fraction and maximal stiffness (31).

Treshold value was chosen as the middle point between the two significant peaks on grayscale

Figure 8: Localization of remodeling sites on heterogeneous and binarized model : sites are located on same place, but more expanded in heterogeneous case which correspond to hypermineralized bone tissue (Young modulus¿19GPa)

 distribution (figure 3), nevertheless a variation of 5% in tresholding was possible and results in a variation of 5% on bone volume fraction. Higher is coarsen voxel size, higher is the difference in bone volume fraction because voxel volume increases while coarsening (table 5). Moreover many tresholding were made on coarsen models, and a linear relationship was established between apparent Young modulus versus gray-value tresholding (figure 9). Decreasing gray-value treshold consiste in considering thicker trabeculaes and so micro-structure becomes stiffer.

Figure 9: Linear relationship between apparent Young modulus (E3) and gray-value treshold

voxel size	Difference in bone	Difference in apparent
(μm)	volume fraction $(\%)$	Young modulus $(\%)$
20	3.5	X
40	3.5	6.3
60	4.1	8.6
80	10.3	8.2
100	13.7	

Table 5: Difference in bone volume fraction and apparent Young modulus for a variation of 5% in tresholding

¹⁴³ 4 Discussion

 Mechanical cancellous bone properties is a decisive parameter in bone fracture. Numerical simulations allow to quantify elastic bone properties during disease or aging (16; 18; 14). Nev- ertheless those methods use millions of elements and models are not suitable for simulation of iterative process like bone remodeling. So mechanical consideration, like stress concentration, or local mechanical stimulus (inside tissue bone) are not available due to computational cost. In this paper we studied the influence of coarsening voxel size in term of global mechanical behaviour, but also in term of local mechanical behaviour. From micro-tomography acquisi tion, we have numerically built new voxels whose gray-value correspond to an average of initial gray-values. This methods allows to increase numerically voxel size, which decrease number of considered elements and degree of freedom for the finite element analysis.

154 Coarsening voxel size from 20μ m (μ CT resolution) to 60μ m, leads to reduce number of elements from 2 millions to 90000 (for a bone sample of 4x4x4 mm). Furthermore, apparent Young mod- ulus varies from 5%, and computation time which initially goes on 10 hours is reduced to 2 minutes. From a biomechanical point a view, if we are interested in bone remodeling we should compare the agreement of remodeling sites between coarsen and initial model. If we focus on 159 sites where strain exceeds $3000\mu\varepsilon$, which correspond to the treshold of activation of new bone tissue deposit, we have seen that over-constrained areas in coarsen and initial model one voxel size away, for a coarsen voxel of 60μ m. This difference of localization is negligible at osteoclast $_{162}$ scale because during remodeling process, several osteoclasts, which measure until $100 \mu m$ of diameter, come on trabeculae surface and dig a channel on hundred micrometers on trabeculae ₁₆₄ bone surface. So a variation of 60μ m on remodeling site localization is insignificant.

 Compared to binarization method which is largely used in the literature, it was put forward that 166 in a hypermineralized bone tissue, volume of bone where strain energy density is over $3000\mu\epsilon$ is under estimated at 19% in a binarized model. Nevertheless binarization give an accurate global $_{168}$ mechanical behaviour until coarsen voxel of 60μ m. Cancellous bone mechanical properties are more dictated by the micro-structure than local material heterogeneities.

 Coarsening method is a relevant method to get mechanical cancellous bone properties, nev- ertheless, as trabeculae are relatively thin, voxel size is limited in order to keep connectivity and realistic bone morphology. Indeed a trabeculae should be composed of 4 or 5 voxels to be relevant in term of mechanical behaviour (32). A numerical study with a voxel size upper than 80 μ m is not conceivable in order to simulate realistic case.

 As a conclusion, it is now possible to compute cancellous bone mechanical properties of re- alistic sample (8x8x8mm) with directly coarsened voxel while reducing the computational cost. However, a remodeling process can be planned in order to simulate a physiological case : bone alertation due to a low-loading case (bed-ridden case, microgravity), or bone adaptation due to an overloading case (sport). Lastly, as hypermineralized bone is a privileged place of cracks concentration, this data can be used as initiator sites of bone remodeling.

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