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Frequency Response Optimization of P-I-N Photodiode Based on InGaAsN Lattice Matched to GaAs for High-Speed Photodetection Applications

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Abstract

This paper reports on pin photodiode frequency response optimization based on $In_xGa_{1-x}As_{1-y}N_y$ quaternary lattice matched to GaAs. Two transparent layers are placed on p-side and n-side in order to manage the photodiode frequency response limitations. The lattice matching condition is calculated in order to obtain stable structure. The physical and optical parameters calculations are performed at room temperature showing the impact of nitrogen on the absorption coefficient. A stable structure, having 2 % of nitrogen and 6% of indium, allows to achieve a cutoff frequency of about 116GHz and a capacitance of 5.21fF while the quantum efficiency is 41.59% for a depletion region thickness of about 0.55µm. However, in case of depletion region thickness of about 0.625µm, the cutoff frequency degrades to 98GHz while the capacitance diminishes to 4.58fF and the quantum efficiency increases to 51.56%. In addition, a comparative study with literature results has been carried out in order to show the advantages of the proposed photodiode. This comparison affirms that the proposed photodiode based on InGaAsN lattice matched to GaAs exhibits high-speed photo-detection. This work allowed us to obtain a p-i-n photodiode with stable structure suitable for photo-detection at 1.15µm.

Keywords: In_xGa_{1-x}As_{1-y}N_y quaternary, p-i-n photodiode, stable structure, high-speed photo-detection.

1. Introduction

Nowadays, optoelectronic devices such as p-i-n photodiode become more controversial and sophisticated regarding the enormous progress in optical systems. Heterostructures, those based on III–V quaternaries have taken advantage of this development and become a major candidate in optoelectronic devices thanks to their attractive physical and optical properties. Among them, InGaAsN is considered as a promising compound for optoelectronic devices. Since the last few years, InGaAsN deposed on GaAs substrate has received an intense interest in several researches [1-9]. This is due to, firstly, the beneficial applications such as solar cells [10-12],

photo-detection [13] and laser applications [14, 15]. Secondly, the fact that InGaAsN can be grown lattice matched to GaAs [16, 17]. The lattice matched structure has been adopted in different works [18-22].

On the other side, p-i-n photodiode is considered as a pertinent device in modern optical communication systems because of the remarkable characteristics such as high-speed photo-detection. The latter is well assessed in the photodiode frequency response simulation.

The photodiode frequency response calculation has been extensively tackled in quite number of researches. P-I-N photodiode frequency response has been calculated and optimized [23] using an absorbent region made of $In_{0.5}Ga_{0.5}N$ and a single transparent layer on n-side. An analytical model is presented in [24] in order to accurately study the performances of InGaAs/InP based pin photodiode. In ref [25] a formulation was developed for carrier transport using vertical pin photodiode. Author studied the device high frequency response and cleared up its limiting parameters. Recently, author in ref [26] developed a multiple quantum wells InGaN/GaN based pin photodiode in the aim of fabricating high-speed pin photodiode. A p-i-n photodiode was designed [27] with structure consists of: In_{0.1}Ga_{0.9}N as an absorbent region having a thickness of 0.1µm placed between two layers p-type and n-type made of GaN, their thicknesses are 0.1 µm, and 0.3µm respectively. The achieved cutoff frequency was 400MHz, however for an intrinsic region thickness of 1.5µm, the cutoff frequency attained 4GHz. A new analytical model was developed in order to study the p-i-n photodiode highfrequency performance [28]. In Ref [29] a characterization of high-speed large-area p-i-n photodiodes was tackled. Author has proposed a fully analytic model in order to study the frequency response for a homostructure p-i-n photodiode. P-I-N photodiode having dual-depletion region has been proposed in order to improve the bandwidth [30,31] taking into consideration the transit time and the capacitance effect. Finally, p-i-n photodiode frequency response was calculated analytically in [32].

It is crucial to note that p-i-n photodiode frequency response is mainly limited by two parameters of upmost importance [23-31]: the carriers' transit time and capacitance effect.

The main aim of this research is to obtain a high-speed p-i-n photodiode based on stable structure with low capacitance effect and short transit time. However, in case of conventional photodiode low capacitance effect needs thick absorbent region. This leads to increase the transit time and consequently tends to slow the photodiode response. While, high-speed communications (cutoff frequency >60GHz) need short transit time [33] and low capacitance effect. The influence of both transit time and capacitance effect on the photodiode performances is well shown in the frequency response. In attempt to overcome this issue, a structure based on two transparent layers under field inserted on p-side and n-side of the absorbent region is proposed. In this paper we have assumed that carriers move at their saturation velocities, so the transit time becomes directly proportional to depletion region the thickness.

In the paper in hand, physical and optical calculations as well as the frequency response optimization for p-i-n photodiode are provided. The photodiode is based on $In_xGa_{1-x}As_{1-y}N_y$ quaternary as an absorbent region lattice matched to GaAs substrate using two transparent layers placed on p-side and n-side. In the first step, the lattice matching condition is calculated in order to obtain stable structure. After that, the bandgap energy as well as the absorption coefficient are calculated at room temperature showing the impact of nitrogen concentration (y) on the absorption coefficient. The next section, on one side, it deals with calculation of the frequency response which corresponds to the transit behavior with highlighting the influence of the absorption coefficient in order to select indium (x) and nitrogen concentrations required in the detection part. On the other side, it deals with the frequency response optimization and the impact of the transit time and the capacitance effect on the frequency response. At a later stage, a comparative study with literature results is provided to evaluate, in term of speed, the benefits of the proposed structure based on InGaAsN lattice matched to GaAs. The next section focuses on the capacitance effect which has a strong impact on the total frequency response. The last section is devoted to the total frequency response and its limitations.

2. Theoretical framework

This study is based on $In_xGa_{1-x}As_{1-y}N_y$ lattice matched to GaAs which allows to obtain a stable structure i.e. $\varepsilon(x,y) = 0$, where $\varepsilon(x,y)$ represents the strain given by [13,34,35]:

$$\varepsilon(x,y) = \frac{a_s - a_e(x,y)}{a_e(x,y)} \tag{1}$$

where:

 a_s : is the lattice parameter of the substrate.

$a_e(x,y)$: is the lattice parameter of In_xGa_{1-x}As_{1-y}N_y.

The variation of the strain $\varepsilon(x,y)$ as a function of indium and nitrogen concentrations is illustrated in figure.1.

After calculation, the condition that allows to obtain a stable structure is:

$$y(x) = \frac{0.40.x}{1.15 - 0.075.x}$$
(2)

Equation.2 presents the variation of nitrogen concentration as a function of indium concentration. For each pair (x, y) we have a stable structure.

Indeed, the introduction of small quantity of nitrogen into InGaAs semiconductor results a drastic reduction in the bandgap energy. This is due to strong interaction between the conduction band and spatially localized state of nitrogen (E_N) [36]. Consequently, the conduction band splits into two subbands E_+ and E_- .

Increasing the amount of nitrogen results a repulsion of E_+ and E_- above and below respectively, which has a significant effect on optical properties. The bandgap reduction due to nitrogen incorporation is well clarified by the Band Anti-Crossing model (BAC) [13, 37-41]:

$$E_{\mp} = \left[(E_N + E_M) \mp \sqrt{(E_N - E_M)^2 + 4V_{MN}^2} \right]$$
(3)

$$E_N = 1.52 - 3.9y \tag{4}$$

$$E_M = E_0 - 1.55 \ eV + \frac{h^2}{2m_e^*} \tag{5}$$

$$V_{MN} = b_{MN} \sqrt{y} \tag{6}$$

where:

b_{MN}=2.3.

E_o: the conduction band minimum of InGaAs.

m*_e : is electron effective mass in the ternary InGaAs.

E_M: is the energy of the InGaAs matrix conduction band edge.

 E_N : is the nitrogen energy level relative to the top of the valence band.

 V_{MN} : is the matrix element describes the interaction between E_M and E_N .

In the equation.3 only E. is taken into account, because E. is responsible for the reduction in bandgap energy [42,43].

Absorbing photons energy to generate electrical signal is the basic role of the photodiode. If an incident optical beam having an energy hv smaller than the semiconductor bandgap, the device appears as transparent to the photons energies, therefore photons are not absorbed. By contrast, if hv is greater than or equal to the bandgap energy, electrons in the valence band absorb the photons energies and move towards the conduction band. The absorption coefficient $\alpha(E)$ in case of absorbed photons is given as follow [34,44-45]:

$$\alpha(E) = \alpha_0 \cdot \frac{\sqrt{E - E_g(x, y)}}{E}$$
(7)

where:

E: is the photon energy.

 α_0 : constant depends on the semiconductor.

 $E_g(x,y)$: is the bandgap energy of $In_xGa_{1-x}As_{1-y}N_y$.

To perform the frequency response calculation, we have assumed that carriers move with their saturation velocities given by [46-51] at 300K for binary compounds (InAs, GaAs, InN, GaN) and the saturation velocity of InGaAsN can be determined by using Vegard's law.

The total current circulates in the device is given as follow [23].

$$i(t) = B[v_p \cdot P(t) + v_n \cdot N(t)]$$
(8)

where

$$B=\frac{q}{d_t},$$

q is the electron charge, d_t is the depletion region thickness.

 v_p , v_n are holes and electrons saturation velocities respectively.

P(t) and N(t) represent the number of holes and electrons in the depletion region.

Light-generated carriers transit from the absorbent region towards p-type and n-type regions. Holes response is completed after abandoning the depletion region in duration of $d_p/v_p + d_{abs}/v_p$ and electrons in duration of $d_n/v_n + d_{abs}/v_n$. The carriers' contributions are:

for holes:

$$i_p(t) = \frac{qv_p p_0 A}{\alpha \cdot dt} \cdot \left[\frac{e^{\alpha \cdot d} abs - 1}{e^{\alpha \cdot d} abs}\right] \frac{e^{\alpha \cdot d} abs - 1}{e^{\alpha \cdot d} abs} \quad 0 < t < \tau_p$$
(9)

$$i_p(t) = \frac{qv_p p_0 A}{\alpha.d_t} \cdot \left[\frac{e^{\alpha \cdot d_{abs}} - e^{\alpha(v_p \cdot t - d_p)}}{e^{\alpha(v_p t - d_p + d_{abs})}} \right] \qquad \tau_p < t < \tau_p + \tau_{p,abs}$$
(10)

• for electrons:

$$i_n(t) = \frac{qv_n n_0 A}{\alpha \cdot d_t} \cdot \left[\frac{e^{\alpha \cdot d_{abs-1}}}{e^{\alpha \cdot d_{abs}}} \right] \qquad \qquad 0 < t < \tau_n \tag{11}$$

$$i_n(t) = \frac{qv_n n_0 A}{\alpha \cdot d_t} \cdot \left[\frac{e^{\alpha(v_n \cdot t - d_n + d_{abs})} - 1}{e^{\alpha(v_n \cdot t - d_n + d_{abs})}} \right] \quad \tau_n < t < \tau_n + \tau_{n,abs}$$
(12)

where:

 $\tau_{n,abs} = d_{abs}/v_n, \ \tau_n = d_n/v_n \ and \ \tau_{p, \ abs} = d_{abs}/v_p, \ \tau_p = d_p/v_p.$

po and no represent the carriers maximum densities.

 d_{abs} is the absorbent region thickness.

d_p(d_n) is p-side (n-side) transparent layer thickness.

 $\tau_{p,abs}(\tau_{n,abs})$ is the transit time required for holes (electrons) to cross the absorbent region.

 $\tau_p(\tau_n)$ are the transit time that holes(electrons) take to cross the p-side (n-side) transparent layer.

A is the junction area.

The impulse response is the sum of the electrons and holes contributions, it is given as:

$$g(t) = B' \cdot \left[i_p(t) + i_n(t) \right]$$
⁽¹³⁾

where

$$B' = \frac{1}{q \cdot N_{opt}}$$

N_{opt} is the photons number in the optical beam.

The frequency response allows to verify the photodiode performance. From the photodiode impulse response, we are able to obtain the frequency response by using the Fourier transform:

$$G_{p}(w) = \frac{v_{p}}{j \cdot d_{t} \cdot w} \cdot \left(1 + j \cdot \frac{a_{1}}{a_{2}} \cdot \frac{e^{j \cdot (a_{2} - j \cdot a_{4})} + e^{-j \cdot (a_{2} + j \cdot a_{4})}}{e^{a_{1} - e^{-a_{1}}}}\right)$$
(14)

$$G_{n}(w) = \frac{v_{n}}{j \cdot d_{t} \cdot w} \cdot \left(1 + j \cdot \frac{a_{1}}{a_{3}} \cdot \frac{e^{j \cdot (a_{3} - j \cdot a_{5})} + e^{-j \cdot (a_{3} + j \cdot a_{5})}}{e^{a_{1} - e^{-a_{1}}}}\right)$$
(15)

where

w is the angular frequency.

$$a_1 = \frac{\alpha \cdot d_{abs}}{2}, a_2 = \frac{d_{abs}}{2} \cdot \left(\frac{w}{v_p} - j \cdot \alpha\right), a_3 = \frac{d_{abs}}{2} \cdot \left(\frac{w}{v_n} + j \cdot \alpha\right), a_4 = -j \cdot \frac{w}{v_p} \cdot \left(\frac{d_{abs}}{2} + d_p\right), a_5 = -j \cdot \frac{w}{v_n} \cdot \left(\frac{d_{abs}}{2} + d_n\right).$$

3. Nitrogen impact on optical behavior

The first step is to calculate the bandgap energy and the absorption coefficient. The pairs (x, y) are extracted from equation.2. Indium concentration is limited at 14% and therefore nitrogen concentration is limited at 4.96%. The evolution of the absorption coefficient versus nitrogen concentration is presented in figure.2 in which some nitrogen concentrations match the stable structure are provided.

The influence of nitrogen on the absorption coefficient is well clarified in figure.2. A slight concentration of nitrogen results a notable reduction in the bandgap energy, consequently a considerable amelioration in the absorption coefficient (α). For example, in case of y=2% the bandgap energy is about 1.08eV and the absorption coefficient is of about α =4.72x10⁴cm⁻¹. However, for y=2.5% the bandgap energy decreases to 1.03eV, while the absorption coefficient rises to α = 4.44x10⁵ cm⁻¹.

The physical and optical properties of $In_xGa_{1-x}As_{1-y}N_y$ lattice matched to GaAs for $6\% \le x \le 7\%$ and $2\% \le y \le 2.5\%$ are as follow: bandgap energy from 1.08eV down to 1.033eV, the photo-detection wavelength from 1.15µm until 1.20µm and the absorption coefficient ranging from $4.72x10^4$ cm⁻¹ to $4.44x10^5$ cm⁻¹.

4. PIN photodiode frequency response optimization

The proposed structure is provided in figure.3. It consists of: n-type GaAs layer followed by the first under field transparent layer made of GaAs having a thickness of $d_n(\mu m)$. The absorbent region is an intrinsic $In_xGa_{1-x}As_{1-y}N_y$ with thickness of $d_{abs}(\mu m)$ and the second under field transparent layer is made of GaAs having a thickness of $d_p(\mu m)$. Finally, the p-type layer is made of GaAs. The cathode and anode contacts are made of Ti/Al/Ni/Au and Ni/Au respectively to guarantee the connection with the electrical circuit.

According to the previous results, two configurations satisfying the stable structure have been adopted taking indium cost and nitrogen influence into consideration. The first configuration is the quaternary $In_{0.07}Ga_{0.93}As_{0.975}N_{0.025}$, while the second is $In_{0.06}Ga_{0.94}As_{0.98}N_{0.02}$. The physical and optical parameters of these two configurations are given in section 3.

Focusing on the link between the cutoff frequency and the absorption coefficient, different absorbent regions thicknesses have been examined using the first configuration $(In_{0.07}Ga_{0.93}As_{0.975}N_{0.025})$: $d_{abs}=0.5$, 0.8 and 1µm, while both d_p and d_n are kept at 0.5µm. The results are as follow: for $d_{abs}=0.5\mu$ m the cutoff frequency at -3 dB is 67.46GHz, this value is unchanged either for $d_{abs}=0.8\mu$ m or 1µm. The cutoff frequency seems stuck at 67.46GHz despite using different absorbent region thicknesses. This is due to the high absorption coefficient caused by the important nitrogen concentration which has a strong impact on the bandgap energy.

The same study is applied on the second configuration: $In_{0.06}Ga_{0.94}As_{0.98}N_{0.02}$ which has a reduced absorption coefficient compared to the first configuration. The results are established in figure.4. According to this figure, for $d_{abs}=0.2\mu$ m the structure reveals a -3dB cutoff frequency of 59.00GHz, then the cutoff frequency degrades to 49.03GHz for $d_{abs}=0.5\mu$ m. Whereas, in case of the absorbent region is sufficiently large, $d_{abs}=0.8$ and 1μ m, the cutoff frequency reduces to 44.33GHz and 42.86GHz respectively. On the other hand, figure.4 affirms that the cutoff frequency depends highly on the absorbent region thickness when using low absorption coefficient (order of 10⁴). For this reason, the second configuration (In_{0.06}Ga_{0.94}As_{0.98}N_{0.02}) is selected.

The next step is dedicated to search the optimal depletion region thickness that improves the photodiode frequency response taking into account carriers' transit time and capacitance effect. Figure.5 depicts the cutoff frequency values variation as function of d_p where d_{abs} ranging from 0.1 to 0.4µm, and d_n =0.2, 0.5µm. Figure.6 provides the cutoff frequency values variation as function as function of d_n where d_{abs} ranging from 0.1 to 0.4µm, and d_n =0.2, 0.5µm. Figure.6 provides the cutoff frequency values variation as function of d_n where d_{abs} ranging from 0.1 to 0.4µm, while d_p =0.5, 0.375 µm in figure.6.a and d_p =0.2µm in figure.6.b.

According to figure.5, in case $d_n=0.2\mu m$ (dashed curves) the maximum cutoff frequency is 143GHz, this is given when $d_p=0.15\mu m$ and $d_{abs}=0.1\mu m$. After that, the cutoff frequency decreases to 116.20GHz for

 $d_p=0.15\mu m$ and $d_{abs}=0.2\mu m$, then it degrades to 98.4GHz for $d_p=0.125\mu m$ and $d_{abs}=0.3\mu m$. The last depletion regions have approximately the same transparent layers thicknesses but different absorbent regions which enhance the quantum efficiency as 25.62% for $d_{abs}=0.1\mu m$ to 41.59% in case $d_{abs}=0.2\mu m$ until 51.56% for $d_{abs}=0.3\mu m$.

Still in figure.5, in case $d_n=0.5\mu m$ (solid curves) the structure exhibits low cutoff frequencies. The maximum cutoff frequency is about 66.23GHz which is obtained for $d_p=0.375\mu m$ and $d_{abs}=0.1\mu m$. This degradation in the cutoff frequency values is due to increasing the depletion region thickness. This fact leads to reducing the capacitance, but at the same time a long transit time which slows the photodiode response.

Referring to figure.6.a, when $d_p=0.375\mu m$ (dashed curves) the highest cut off frequency is 97.9GHz, this is given for $d_n=0.2\mu m$ and $d_{abs}=0.1\mu m$. Enlarging the depletion region produces low cutoff frequencies as illustrated in case of $d_p=0.5\mu m$ (solid curves). The revealed cutoff frequency is 75.97GHz which is obtained when $d_n=0.275\mu m$ and $d_{abs}=0.1\mu m$. However, figure.6.b affirms that high cutoff frequencies needs low thicknesses [52]. In this figure a very thin depletion region shows high cutoff frequencies (>160GHz).

To summarize this part, three situations are distinguished. For very thin depletion region, the capacitance effect attains its maximum since it is inversely proportional to the depletion region thickness while the transit time is very short. Enlarging the depletion region reduces gradually the capacitance effect and rises progressively the transit time. At this stage, the situation arrives to an equilibrium point between the capacitance effect and the transit time which enhances the cutoff frequency. Then, when the depletion region becomes sufficiently large, the capacitance effect diminishes while the transit time increases rapidly since it is directly proportional to the depletion region thickness. Consequently, the cutoff frequency leaves its maximum and decreases rapidly. These results show the dominance of the capacitance for thin depletion regions and the transit time for thick depletion regions, so there is a tradeoff between the transit time and the capacitance effect.

5. Comparative study

In order to reinforce the present work, this section focuses on the benefit of using p-i-n photodiode based InGaAsN lattice matched to GaAs having double transparent layers instead of single transparent layer or totally absorbent region.

The cutoff frequency (Fc) of p-i-n photodiode has been tackled in several works such as Ref [53] where author adopted three structures based on different depletion regions thicknesses. The results of comparison with this study are shown in figure.7.

The first structure is a conventional photodiode in which the depletion region is totally absorbent with a thickness of 0.8μ m. The frequency response can be obtained by setting d_p and d_n to zero in equations 14 and 15. In our work F_c is equal to 74GHz, whereas in Ref [53] F_c=37GHz.

The second structure consists of single transparent layer placed on n-side of the absorbent region. Their thicknesses are 0.2 and 0.6 μ m respectively. Using the proposed structure, we have found F_c=69.60GHz, whereas in Ref [53] F_c=45GHz.

The last structure is organized as follow: double transparent layers inserted on n-side and p-side of a very thin absorbent region. Their thicknesses are respectively: $d_n=0.45\mu m$, $d_p=0.35\mu m$ and $d_{abs}=4nm$. The exhibited cutoff frequency in our study is $F_c=80.63$ GHz, whereas in Ref [53] $F_c=62$ GHz.

Another comparison with literature results has been performed. Ref [27] adopted a conventional photodiode structure in which the absorbent region thickness is $d_{abs}=1.5\mu$ m and the cutoff frequency was found 4GHz.

To accomplish this comparison, we have kept the absorbent region thickness at $1.5\mu m$ (d_{abs}= $1.5\mu m$), the results of this comparison are illustrated in figure.8 for d_p and d_n ranging from 0 to 0.4µm. From the obtained results we have selected some transparent layers thicknesses (found in section.4) that improve the photodiode response to show the influence of the transparent layers on the photodiode response.

In case $d_p=0.375\mu m$ and $d_n=0.2\mu m$, the obtained cutoff frequency is about 51.5GHz, whereas, when $d_p=0.125\mu m$ and $d_n=0.2\mu m$ F_c reaches 56.2GHz. However, for $d_p=0.15\mu m$ and $d_n=0.2\mu m$ F_c is about 56.23GHz.

This section asserts that the p-i-n photodiode based InGaAsN lattice matched to GaAs using double transparent layers exhibits high-speed compared to both the conventional one and that whose depletion region consists of single transparent layer.

6. Capacitance effect

The capacitance is directly proportional to the area, but inversely to the depletion region thickness. It is given as [23, 26, 54-56]:

$$C = \varepsilon_0 \cdot \varepsilon_r \cdot \frac{A}{d_t}$$
(16)

where

 ϵ_{o} is the permittivity of free space,

 ε_r is the relative permittivity of In_xGa_{1-x}As_{1-y}N_y. In case of x=0.06 and y=0.02 the relative permittivity is 12.95.

A is the junction area and d_t is the depletion region thickness.

Figure.9 illustrates the variation of the capacitance as a function of the depletion region thickness and the area. As shown in this figure, important capacitance is obtained for thin depletion regions and big areas. The variation of the capacitance with the depletion region thickness and the area is resumed in table.1.

According to table.1, structures whose depletion regions have thicknesses of d_{ti} ; i=1...6 exhibit high capacitance by incrementing 'i'. Besides, this table shows the impact of the area on the capacitance. Areas of $100\mu m^2$ show important capacitance compared to those given for areas of $25\mu m^2$.

7. The total frequency response

This section is devoted to the total frequency response calculation and simulation with highlighting its limitations. The total cutoff frequency is given as [23,54,55]:

$$f_{3dB} = \frac{1}{\sqrt{f_{RC}^2 + f_t^2}}$$
(17)

where

 f_t : is the transit cutoff frequency which is related much more to the transit phenomenon.

 f_{RC} : is the capacitive cutoff frequency, it is directly proportional to the depletion region thickness and inversely to the area. It is given as [23,26,54-56]:

$$f_{\rm RC} = \frac{d_t}{2 \cdot \pi \cdot \mathbf{R} \cdot \varepsilon_0 \cdot \varepsilon_r \cdot \mathbf{A}} \tag{18}$$

Where, R is the photodiode total resistance and the load resistance.

The variation of the total cutoff frequency as function of d_n is presented in figure.10 (a,b,c) for different areas: 25, 50 and 100µm² using different depletion regions thicknesses: in (a) $d_p=0.50µm$ and $d_{abs}=0.1µm$, in (b) $d_p=0.375µm$ and $d_{abs}=0.1µm$ and in (c) $d_p=0.20µm$ and $d_{abs}=0.1µm$. The same is in figure.11 (a,b,c), it illustrates the variation of the total cutoff frequency depending on d_p for different areas: 25, 50 and 100µm² using different depletion regions thicknesses, for (a) $d_n=0.20µm$ and $d_{abs}=0.30µm$, for (b) $d_n=0.20µm$ and $d_{abs}=0.20µm$, and for (c) $d_n=0.20µm$ and $d_{abs}=0.10µm$. The total cutoff frequency shows degradation when increasing the area from 25 to 50µm², this is due to the capacitance effect increases, which is directly proportional to the area. For areas ranging from 50 to 100µm² the capacitance effect increase considerably, thereby a severe degradation is observed in the total cutoff frequency.

The degradation is less important in figures 10.a and 10.b, however in figure 10.c the degradation is severe. In figure 10.a, area of $100\mu m^2$ allows a degradation of 4% in the total cutoff frequency relative to area of $25\mu m^2$. In figure 10.b, area of $100\mu m^2$ allows a degradation of 10% in the total cutoff frequency relative to area

of $25\mu m^2$, while in figure 10.c it is 35% relative to area of $25\mu m^2$. The same is in figure 11; the degradation in the total cutoff frequency in both figures 11.a and 11.b is slight compared to figure 11.c. In figure 11.a, area of $100\mu m^2$ allows a degradation of 11% in the total cutoff frequency relative to area of $25 \mu m^2$. In figure 11.b, for A=100 μm^2 the degradation is 18% in the total cutoff frequency relative to area of $25\mu m^2$, while in figure 10.c it is 28% relative to area of $25\mu m^2$. These results confirm the impact of increasing the area on the total frequency response.

Indeed, the total cutoff frequency depends not only on the area but also on the depletion region thickness, the latter influences more on the carriers' transit time than the capacitance. In figures 10.c, the degradation in total cutoff frequency is very important owing to the use of thin depletion region $d_{t,c}$. The latter produces short transit time compared to those thicknesses in figure 10.a and figure 10.b given as: $d_{t,a}$ and $d_{t,b}$ respectively. These two factors can be expressed as function of $d_{t,c}$ as follow: $d_{t,a} = 2.187d_{t,c}$ and $d_{t,b} = 1.687d_{t,c}$. The same observation is in figures 11. In figure 11.c the degradation in total cutoff frequency is very important due to the use of relatively thin depletion region $d'_{t,c}$ which engenders short transit time compared to $d'_{t,a}$ and $d'_{t,b}$ for figure 11.a figure 11.b respectively. These two thicknesses can be written as function of $d'_{t,c}$ as follow: $d'_{t,a} = 1.388d'_{t,c}$ and $d'_{t,b} = 1.166d'_{t,c}$.

Thus, using thin depletion regions and at the same time high areas increases the severity of degradation in the total cutoff frequency. Whereas, a relatively thick depletion regions ($d_{t,a}$, $d_{t,b}$ in figure 10 and $d'_{t,a}$, $d'_{t,b}$ in figure 11) make it possible to compensate the increase of the capacitance effect caused by increasing the area, thereby, reducing the severity of degradation in the total cutoff frequency.

On the other hand, very high speed responses need low thicknesses [33]. This can be observed if we compare for example blue curve (A=25 μ m²) of figure 10.a (or figure 11.a) with blue curve (A=25 μ m²) of figure 10.c (or figure 11.c). In figure 10.c (figure 11.c) the depletion region has low thickness and it exhibits high cutoff frequencies compared to figure 10.a (or figure 11.a) in which we have relatively thick depletion region.

In summary of these results, in figures 10 and 11, areas less than or equal $25\mu m^2$ (blue curves) exhibit low capacitance effect. This fact increases significantly the capacitive cutoff frequency versus the transit one, thereby the total cut of frequency becomes strongly dominated by the transit cutoff frequency which related to the transit phenomenon, this dominance is as follow $f_{RC}/\sqrt{1 + (f_{RC}/f_t)^2}$. By contrast, areas greater than $25\mu m^2$ increase the capacitance effect, thereby, decrease the capacitive cutoff frequency. With increasing the area till $100\mu m^2$, the capacitance effect becomes important which decreases significantly the capacitive cutoff frequency versus the transit component. Thus, the total cutoff frequency becomes dominated by the capacitive cutoff frequency as in $f_t/\sqrt{1 + (f_t/f_{RC})^2}$.

8. Conclusion

In this work, the lattice matched $In_xGa_{1-x}As_{1-y}N_y/GaAs$ based pin photodiode whose depletion region consists of double transparent layers is proposed in order to improve the device performances. Besides, the link between the absorption coefficient and the device response has been tackled in order to select the suitable nitrogen and indium concentrations. For a concentration of nitrogen at 2.5% allows to get an absorption coefficient of $4.44x10^5$ cm⁻¹and an unchangeable cutoff frequency of about 67.46GHz regardless the absorbent region thickness. However, 2% of nitrogen leads to an absorption coefficient of about 4.72.10⁴cm⁻¹ and an improvement in the cutoff frequency by varying the absorbent region thickness as follow: 42.86GHz for 1µm to 49.03GHz for 0.5µm and 59.00GHz for 0.2µm with keeping the transparent layers thicknesses d_p and d_n at 0.5µm. In addition, this study affirms that thin depletion regions make it possible to achieve cutoff frequencies (>100GHz). It has been also found that the total cutoff frequency completely depends on the transit cutoff frequency for areas less than 25µm². Besides, the proposed structure is able to be adopted for ultra-high-speed applications.

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Figure captions

Figure 1. Variation of the strain versus the indium and nitrogen concentrations, we are interested in $\varepsilon(x,y)=0$.

Figure.2. Variation of the absorption coefficient versus nitrogen concentration using different indium concentrations providing some nitrogen concentrations for the stable structure and E=1.08eV.

Figure.3. Structure of the proposed InGaAsN/GaAs p-i-n photodiode.

Figure.4. Frequency response simulation for $In_{0.06}Ga_{0.94}As_{0.98}N_{0.02}/GaAs p-i-n$ photodiode depending on different absorbent region thicknesses, d_p and d_n are kept at 0.50 µm.

Figure 5. Variation of the cutoff frequency as a function of the p-side transparent layer thickness using different absorbent region thicknesses ; $d_n=0.20\mu m$ for dashed curves and 0.50 μm for solid curves.

Figure.6. (a, b). Variation of the cutoff frequency as a function of the n-side transparent layer thickness using different absorbent region thicknesses, $a)d_p=0.375\mu m$ for dashed curves and 0.5 μ mfor solid curves.

b) $d_p = 0.20 \mu m_1$

Figure.7. Frequency response of the $In_{0.06}Ga_{0.94}As_{0.98}N_{0.02}/GaAs$ p-i-n photodiode for different depletion region thicknesses compared to that in Ref [53].

Figure.8. Frequency response variation of the In_{0.06}Ga_{0.94}As_{0.98}N_{0.02}/GaAs p-i-n photodiode for d_{abs}=1.50µm.

Figure.9. Variation of the capacitance as a function of the n-side and p-side transparent layers thicknesses. The area A is $25\mu m^2$ and $100\mu m^2$ and the absorbent region thickness d_{abs} is $0.1\mu m$ and $0.3\mu m$.

Figure.10. (a,b, c)Variation of the total cutoff frequency as a function of n-side transparent layer thickness using different areas, a) $d_p=0.50\mu m$ and $d_{abs}=0.10\mu m$, b) $d_p=0.375\mu m$ and $d_{abs}=0.10\mu m$, c) $d_p=0.20\mu m$ and $d_{abs}=0.10\mu m$.

Figure.11. (a,b,c).Variation of the total cutoff frequency as a function of p-side transparent layer thickness using different areas, $d_n=0.20\mu m$ and $d_{abs}=0.30\mu m$, b) $d_n=0.20\mu m$ and $d_{abs}=0.20\mu m$, c) $d_n=0.20\mu m$ and $d_{abs}=0.10\mu m$.

Table.1. Impact of the area and the depletion region thickness on the capacitance.



Figure 1



Figure 2



Figure 3



Figure 4



Figure 5



Figure 6.a



Figure 6.b



Figure 7



Figure 8







Figure 10.a



Figure 10.b



Figure 10. c



Figure 11.a



Figure 11.b



Figure 11.c

| Ta | ble. | 1 |
|----|------|---|
| | | - |

| | | A= $25\mu m^2$ | A=100µm ² |
|--------------------------------------|----------------------------------------------------------------------|----------------|----------------------|
| dti, depletion region thickness (µm) | | Capacity (fF) | Capacity (fF) |
| d _{t1} =0.875 | d _p =0.5, d _n =0.275 and d _{abs} =0.1 | 3.27 | 13.1 |
| d _{t2} =0.675 | d_p =0.375, d_n =0.2 and d_{abs} =0.1 | 4.24 | 16.98 |
| d _{t3} =0.625 | d_p =0.125, d_n =0.2 and d_{abs} =0.3 | 4.58 | 18.34 |
| d _{t4} =0.55 | d _p =0.15, d _n =0.2 and d _{abs} =0.2 | 5.21 | 20.85 |
| d _{t5} =0.45 | d _p =0.15, d _n =0.2 and d _{abs} =0.1 | 6.37 | 25.48 |
| d _{t6} =0.4 | $d_p=0.2$, $d_n=0.1$ and $d_{abs}=0.1$ | 7.16 | 28.66 |