## Multi-material topology optimization of a rotating electrical machine with a density-based method

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Topology optimization (TO) has been extensively studied in the past decades especially in mechanical engineering. Among different techniques, density-based methods have become very popular. In electrical engineering, TO has been applied essentially to linear actuators [1] or machines rotors [2][3], but few works such as [4] deal with the coil repartition within the stator of rotating machines.

In this study, we investigate a density-based topology optimization method, which aims to maximize the average torque of a rotating electrical machine from random or uniform initial material repartition. Material properties such as magnetic permeability or current density are interpolated on densities between each material to obtain a differentiable optimization problem, using SIMP or RAMP [5] for example. A custom magnetostatic finite element solver was implemented on MATLAB<sup>®</sup>. It takes into account the non-linearity of magnetic materials with Newton-Raphson method. The optimization algorithm relies on sensitivities obtained by the adjoint variable method (AVM) [6]. The methodology was performed for two test cases :

- optimization of iron/air repartition within the rotor of a synchronous reluctant machine (SRM)
- optimization of coils/iron/air repartition within the stator of a one phase permanent magnet synchronous machine (PMSM).

In the air/iron case, a filtering technique inspired by ESO [7] is applied: iron which carries few magnetic flux is removed. No filtering was applied in the multi-material case, but a normalization of the gradient was investigated.

As a result, we obtain flux barriers [8] for the optimized SRM rotor, which correspond to industrial designs. However, some convergence issues happened, especially for multimaterial optimization. The gradient normalization helps preventing this phenomenom but leads to surprising asymptric designs, which need further investigations. It is also necessary to improve the robustness of the method especially for high current density, in order to optimize both the rotor and the stator. Multiphysics considerations will be taken into account in future work.

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