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# Experimental Validation of N<sub>2</sub> Emission Ratios in Altitude Profiles of Observed Sprites

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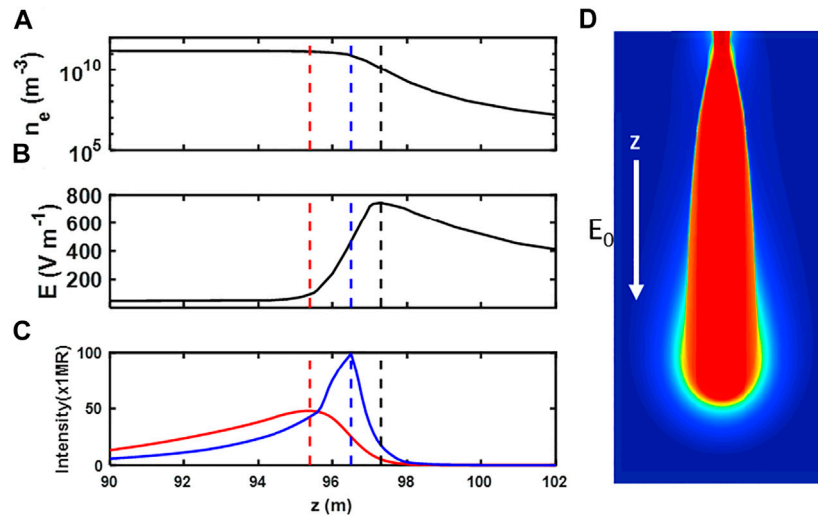
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Recent efforts to compare the sprite ratios with theoretical results have not been successfully resolved due to a lack of theoretical results for sprite streamers in varying altitudes. Advances in the predicted emission ratios of sprite streamers with a simple analytic equation have opened up the possibility for direct comparisons of theoretical results with sprite observations. The study analyzed the blue-to-red ratios measured by the ISUAL array photometer with the analytical expression for the sprite emission ratio derived from the modeling of downward sprite streamers. Our statistical studies compared sprite halos and carrot sprites where the sprite halos showed fair agreement with the predicted ratios from the sprite streamer simulation. But carrot sprites had lower emission ratios. Their estimated electric field has a lower bound of greater than 0.4 times the conventional breakdown electric field ( $E_k$ ). It was consistent with the results of remote electromagnetic field measurements for short delayed or big/bright sprites. An unexpectedly lower ratio in carrot sprites occurred since sprite beads or glow in carrot sprites may exist and contribute additional red emission.

**Keywords:** transient luminous event, sprite, sprite halo, carrot sprites, ISUAL

## INTRODUCTION

A spectrophotometric diagnostic of sprites is of interest because the measured emission ratios indicate their characteristic energy and ionization degree in their discharge phenomena (Armstrong et al., 1998, 2000; Morrill et al., 2002). Previous spectral observations demonstrated two major visual emission bands: N<sub>2</sub> second positive band (2P,  $C^3\Pi_u - B^3\Pi_g$ ) for blue emission, and N<sub>2</sub> first positive band (1P,  $B^3\Pi_g - A^3\Sigma_u^+$ ) for red emission (Mende et al., 1995; Green et al., 1996; Hampton et al., 1996). One of the minor blue emission bands is the N<sub>2</sub><sup>+</sup> first negative band (1N) for ionization associated emission (Armstrong et al., 1998, 2000; Morrill et al., 2002; Kanmae et al., 2010a, 2010b; Stenbaek-Nielsen et al., 2020). Observational techniques for sprite emission ratios have made significant progress using spectrophotometers (Armstrong et al., 1998; 2000), array photometers (Miyasato et al., 2002; 2003), optical spectra at 10,000 fps (Kanmae et al., 2010a, 2010b; Stenbaek-Nielsen et al., 2020) in ground campaigns, airplane campaigns (Morrill et al., 2002), and satellite measurements (Kuo et al., 2005; Mende et al., 2005; Adachi et al., 2006; Liu et al., 2006; Adachi et al.,

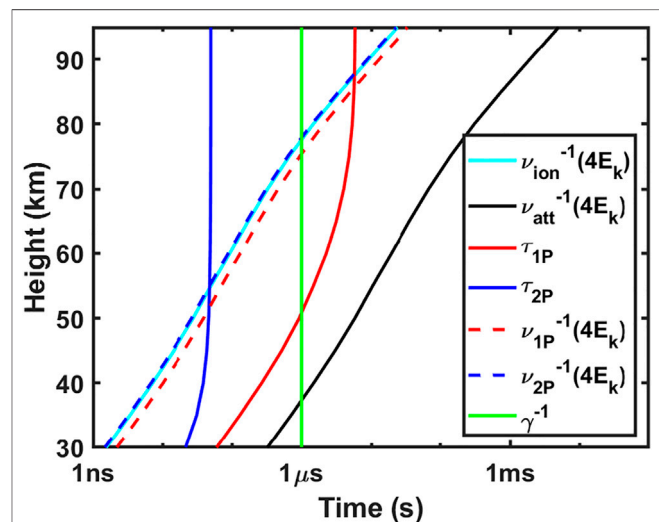


**FIGURE 1** | The inhomogeneous spatial distribution of electron density ( $n_e$ ), electric field ( $E$ ), and their 1P and 2P emission intensity in a sprite streamer. Here we show the computer simulation of a sprite streamer at time of 0.27 ms where the axial profiles of (A) electron density, (B) electric field and (C)  $N_2$  1P and 2P intensity are plotted along the propagating direction ( $z$ ) with the ambient field  $12 \times \frac{N}{N_0} \text{ kV cm}^{-1}$  ( $\sim 0.4 E_k$ ), and at the altitude 70 km. The vertical red, blue and black dashed lines indicate the peaks of  $N_2$  1P, 2P emission and the electric field, respectively. A time lag between their peaks should be considered in sprite emission ratios. Panel (D) show the 2D cross section of the contour plot of positive streamer electron density of a streamer with positive streamer where electric field is downward (Ihaddadene and Celestin, 2017).

2008; Kuo et al., 2008; Kuo et al., 2009). The investigation of the electrical discharge phenomena using remote sensing observation will help us study the impact of plasma chemistry and energy deposition by sprites in the middle atmosphere (Gordillo-Vázquez and Pérez-Invernón, 2021).

The sprite emission ratio of  $N_2$  2P to 1P can indicate the gained energy of accelerated electrons and the applied electric field in the streamer process and stands as a proxy for the electron energy leading to the emissions (Stenbaek-Nielsen et al., 2020). However, an inconsistent interpretation of sprite emission has appeared from past to now. Previous studies show sub-electric breakdown results ( $< 1 E_k$ ) in their observation (Morrill et al., 2002; Miyasato et al., 2003) where  $E_k$  is the electric field required for conventional breakdown. But their interpretation cannot reflect the high electric field ( $3\text{--}5 E_k$ ) at a streamer head with a high emission rate. The estimated peak electric field in a streamer head provides insight into the sprite inception and the later development of sprite streamers from their initiation locations to lower altitude. The sprite emission estimation for a non-uniform streamer (Celestin and Pasko, 2010) complicates the electric field's optical diagnostic method.

The analysis by Celestin and Pasko (2010) may explain why the electric field is estimated in the range of  $1\text{--}2 E_k$  by Adachi et al. (2006). The emission ratios (2P/1N) reported by Kuo et al. (2005, 2009) indicated that the peak electric field of  $\sim 3 E_k$  in sprites and  $\sim 3.4\text{--}5.5 E_k$  in gigantic jets. These derived E-field values were underestimated for a peak electric field greater than  $5 E_k$  in a sprite streamer simulation (Liu et al., 2006). Recently, Ihaddadene and Celestin (2017) developed analytic expressions from a streamer simulation to interpret the observed emission ratios



**FIGURE 2** | The characteristic time coefficient for calculating sprite emissions are compared in units of seconds at different altitudes. The characteristic time scales versus altitude where these time coefficients represent the ionization rate (cyan solid line)  $\nu_{\text{ion}}^{-1}$ , the excitation rate  $\nu_{1P}^{-1}$  for  $N_2 B^3\Pi_g$  state (red dashed line) at  $4 E_k$ , the excitation rate  $\nu_{2P}^{-1}$  for  $C^3\Pi_u$  state (blue dashed line) at  $4 E_k$ , the lifetime  $\tau_{1P}$  of  $N_2$  1P (red solid line), and the lifetime  $\tau_{2P}$  of 2P band (blue solid line) emissions. The lifetimes of the  $N_2$  1P and 2P bands tend to be shorter due to the higher quenching rates (i.e., de-excitation processes) with increased neutral density at lower altitudes. The characteristic time for electron attachment rate  $\nu_{\text{att}}^{-1}$  at  $4 E_k$  (black solid line) indicates the lifetime of streamer body where accumulated electrons at the streamer body are dissipated away after impact ionization by high electric field at the streamer head. The characteristic time ( $\gamma^{-1}$  for the green line) for the growth rate  $\gamma$  in a sprite streamer is almost constant.

at various altitudes. But they still lack spectroscopic data analysis to validate their sprite emission calculation at 50–90 km.

The interpretation of measured sprite emission at a sprite altitude of 50–90 km based on streamer modeling is still challenged (Celestin and Pasko, 2010). The neutral density varies exponentially with altitude. The transmittances for 2P and 1P emissions are sensitive to their observation path, as shown in Eq. 1. For sprite emission calculation in Eq. 2, their associated time coefficients depend on altitude. Besides, a sprite streamer's characteristic spatial and temporal scale decreases exponentially with ambient neutral density at heights from 70 to 30 km. For example, the spatial scale of a sprite streamer varies from tens of meters at an altitude of 70 km to tens of centimeters at an altitude of 30 km (Pasko et al., 1998; Liu and Pasko, 2004). Figure 1 shows a streamer simulation at an altitude of 70 km. The non-uniform spatial distribution of their emission intensity at 1P and 2P makes it impossible to easily estimate their sprite emission ratios, where the red and blue curves in Figure 1C indicate the 1P and 2P intensities along the streamer propagation direction. In Figure 2, the characteristic time coefficients in Eq. 2 vary with altitude. Even for a single streamer, the inhomogeneous emission intensity makes it difficult to estimate their emission ratios. We should consider the observation detection limits on their temporal and spatial scales and the synthesis effects of their spatial and temporal resolution on the emission measurement.

To approach this issue, we revisited similar analyses of the emission ratio by Adachi et al. (2006) based on analytic expressions from a streamer simulation (Ihaddadene and Celestin, 2017). Unlike ground and airplane campaigns, satellite measurement allow for a better transmittance, especially in the shorter wavelength range (e.g., the blue emission). The higher detected intensity in the blue emission may avoid underestimation of total blue emission when considering their transmittance. This study utilized the ISUAL dataset involving sprite blue and red emission onboard the FORMOSAT-2 satellite in *The ISUAL array photometer. Analytical expressions for sprite emission ratios* derived the analytical expressions for sprite emission ratios in an altitude profile of 50–90 km. After analyzing measured emission ratios, we validated an analytic expression for a streamer emission to interpret the observed emission ratios at various altitudes in *Data Analyses*. In the *Summary*, we summarized our results.

## THE ISUAL ARRAY PHOTOMETER

The ISUAL payload on the FORMOSAT-2 satellite consists of an ICCD imager, a six-channel spectrophotometer (SP), and a dual-band array photometer (AP). The ISUAL AP contains blue (370–450 nm) and red (530–650 nm) bands of multiple-anode photometers at a sampling rate of 20 kHz. Each group of the AP has 16 vertically-stacked photomultiplier tubes (PMTs) with a combined field of view (FOV) of 22 deg (H) x 3.6 deg (V) (Chern et al., 2003; Mende et al., 2005; Frey et al., 2016). The ISUAL AP, imager, and SP are co-aligned at the centers of their respective FOVs.

FORMOSAT-2 is a Sun-synchronous satellite with 14 revisiting orbits per day. The ISUAL payload surveys transient luminous events (TLEs) and other luminescent emissions in the upper atmosphere globally with a side-looking view from an orbital altitude of 891 km. Wu et al. (2017) estimated a mean pointing error of 0.05° using star calibration with 1,296 stars from 2004 to 2014. The average pointing accuracy of ISUAL corresponds to a vertical resolution of 3.0 km at the maximum observation distance (3,500 km). Each AP channel has a half-height of 5.7–7.0 km for a distance of 2,900–3,500 km. Using satellite information recorded for TLE events, we can determine the altitude and location of the events based on the assumption that a bright center of a lightning-illuminated cloud has  $10 \pm 5$  km (Kuo et al., 2008). Later, we constrained the uncertainty as a maximum value of the AP half height, considering the ISUAL pointing accuracy and the cloud height error after finally checking the top altitude of sprites at 90 km with an uncertainty of less than the AP half-height. The details of the uncertainty assessment on height are considered in *Uncertainty in sprite emission ratios*.

The AP band emission percentages  $B_k(h)$  for N<sub>2</sub> 1P and 2P band emission were used to convert the AP-measured brightness with blue and red filters into the specified total band emissions (2P and 1P, respectively). This was done while considering the atmospheric transmittance and instrument calibrations, including the filter wavelength range, lens transmittance, and detector response function (Frey et al., 2016). The percentage of the total band emission in an ISUAL AP is defined as the band percentage  $B_k(h)$ , which is also a function of the altitude  $h$  and can be expressed as:

$$B_k(h) = \frac{\int I_k(h, \lambda) T(h, \lambda) R(\lambda) d\lambda}{\int I_k(h, \lambda) d\lambda} \quad (1)$$

where  $I_k(h, \lambda)$  is the intensity of emission lines in the specified band emission (N<sub>2</sub> 1P and 2P band emission) at an altitude  $h$ , which varies with the wavelength  $\lambda$ .  $T(\lambda, h)$  is the atmospheric transmittance, and  $R(\lambda)$  is the AP response function (Frey et al., 2016).

We selected sprite events in the first 7 years (2005–2011) of satellite operation to avoid later-stage degradation in the AP sensitivities. Later, we used the band percentage  $B_k(h)$  to retrieve the AP-measured total emissions of the N<sub>2</sub> 2P and 1P bands. For  $I_k(\lambda)$ , we considered the N<sub>2</sub> 1P and 2P spectrum with a vibrational distribution function obtained by Gordillo-Vázquez et al. (2012), where the vibrational distribution is obtained from halos and sprites at 85 km and from sprites alone at 75 km. The significant changes are the unknown percentage of vibrational number  $v = 0$  for the N<sub>2</sub> 1P spectrum. The uncertainty in the band percentage is typically  $\pm 15\%$ . For the worst case, the error of the ratio is as high as 30%. We neglected the N<sub>2</sub><sup>+</sup> 1N emission in the AP-measured blue emission. For an ambient electric field  $< 2E_k$ , the contribution of N<sub>2</sub><sup>+</sup> 1N emission to N<sub>2</sub> 2P is less than 2% according to similar calculations performed in *Analytical Expressions for Sprite Emission Ratios*.

## ANALYTICAL EXPRESSIONS FOR SPRITE EMISSION RATIOS

A measurement of the  $N_2$  emission band ratio in sprites (e.g., 2P/1P or 1N/2P) is one of the most common remote optical diagnostic methods used to explore the physical conditions of complex sprite phenomena (Armstrong, 1998, 2000; Morrill et al., 2002; Miyasato et al., 2003; Kuo et al., 2005; Adachi et al., 2006; Adachi et al., 2008; Kuo et al., 2008; Kuo et al., 2009; Stenbaek-Nielsen et al., 2020). Sprite streamers associated with the first positive (1P), second positive (2P), and first negative (1N) band emission of  $N_2$  can be analyzed using the analytical expressions for emission ratios in sprite streamer simulations (Celestin and Pasko, 2010; Pérez-Invernón et al., 2018). Here, we present the simplest expression for the sprite emission Ratio 1 ( $r_{CB}$ ) adopted in previous studies (Morrill et al., 2002; Miyasato et al., 2003; Kuo et al., 2005; Mende et al., 2005; Adachi et al., 2006; Adachi et al., 2008; Kuo et al., 2008; Kuo et al., 2009) in *The Spatially Localized Instantaneous Emission Ratio*. In *The spatially and temporally integrated ratio*, we modified the simplest expression by using an integral form for Ratio 2 ( $R_{CB}$ ) by considering the spatially and temporally integrated effects of the observations on the sprite emissions. Finally, we propose a complete presentation of Ratio 3 ( $R_{CB}^*$ ) considering the expansion of sprite streamers in *The Spatially and Temporally Integrated Effect and the Experimental Growth of Streamer Expansion*.

### The Spatially Localized Instantaneous Emission Ratio

Following the calculation of streamer emissions (Pasko et al., 1997; Pasko et al., 1998; Barrington-Leigh and Inan, 1999; Liu et al., 2006; Celestin and Pasko, 2010; Ihaddadene and Celestin, 2017), the number density of the specified  $k$ -th excited state  $n_k$  is calculated using the population and depopulation equation:

$$\frac{\partial n_k}{\partial t} = \nu_k n_e - n_k (A_k + q_{N_2}^k n_{N_2} + q_{O_2}^k n_{O_2}) + \sum_m n_m A_m \quad (2)$$

where  $\nu_k$  is the excitation rate ( $s^{-1}$ ), which depends on the applied electric field (Moss et al., 2006) with consideration of the cascade terms  $\sum_m n_m A_m$ , such as the cascading term  $n_C$  for the  $N_2$  1P ( $B^3\Pi_g - A^3\Sigma_u^+$ ) band emission. The number density of the specified  $k$ -th excited state spontaneously emits photons at a rate of the Einstein coefficient  $A_k$ , and  $\tau_k$  is the lifetime defined by  $\tau_k = (A_k + q_{N_2}^k n_{N_2} + q_{O_2}^k n_{O_2})^{-1}$ . The quenching coefficients  $q_{N_2}^k$  and  $q_{O_2}^k$  are de-excitation rates by the ambient neutral density ( $n_{N_2}$  or  $n_{O_2}$ ). The lifetime  $\tau_k$  of the  $k$ -th excited state is a function of height where larger neutral density at lower altitudes would decrease the lifetimes. If a maximum value of  $n_k$  is reached ( $\frac{\partial n_k}{\partial t} = 0$ ), the spatially localized instantaneous emission ratio  $r_{k'k}$  is represented by (Celestin and Pasko, 2010),

$$r_{k'k} = \frac{n_{k'} A_{k'}}{n_k A_k} = \frac{\nu_{k'} A_{k'} \tau_{k'}}{\nu_k A_k \tau_k}, \quad (3)$$

where  $k'$ -th and  $k$ -th excited states are emission bands of interest. In this study, the Ratio 1 is chosen as the ratio  $r_{CB}$  of the  $N_2$  2P ( $C^3\Pi_u - B^3\Pi_g$ ) to  $N_2$  1P ( $B^3\Pi_g - A^3\Sigma_u^+$ ) band emission, which is given by:

$$r_{CB} = \frac{n_C A_C}{n_B A_B} = \frac{\nu_C n_e \tau_C A_C}{(\nu_B n_e \tau_B + n_C A_C \tau_B) A_B} = \frac{\nu_C A_C \tau_C}{\nu_B A_B \tau_B} \left( 1 + \frac{\nu_C \tau_C A_C}{\nu_B} \right)^{-1} \quad (4)$$

where the cascading term  $(1 + \frac{\nu_C \tau_C A_C}{\nu_B})^{-1}$  is considered as the cascading from the  $C^3\Pi_u$  state into the  $B^3\Pi_g$  state;  $\tau_B$  and  $\tau_C$  indicate the lifetime of their corresponding excited state  $C^3\Pi_u$  and  $B^3\Pi_g$ , respectively. The number densities of the excited state  $n_B = \nu_B n_e \tau_B + n_C A_C \tau_B$  and  $n_C = \nu_C n_e \tau_C$  are obtained from Eq. 2 if a steady-state at its peak value is reached ( $\frac{\partial n_k}{\partial t} = 0$ ). In Eq. 2, the number density  $n_k$  of specified emission band is increased at the excitation rate  $\nu_k$ , which is proportional to the applied electric field. For a maximum electric field, the  $n_k$  takes a time lag to reach its maximum value of specified band emission intensity.

Figure 1 illustrates a simulation result of the sprite streamer (Ihaddadene and Celestin, 2017). The panels (a), (b), and (c) of Figure 1 show the axial profiles of electron density, electric field and  $N_2$  1P/2P intensity along the propagating  $z$ -direction at a time of 0.27 ms and at an altitude of 70 km. For  $N_2$  1P/2P emission peaks (red/blue dashed line in Figure 1B), there exists a time lag between an emission peak and an electric field peak (black dashed line). Hence, Ratio 1 ( $r_{CB}$ ) in Eq. 4 is applied only for the ideal case. However, the optical diagnostic of sprites could not be spatially localized at a streamer head region and at an instantaneous time without considering time delays between their emission peaks. We should consider the temporally and spatially integrated effects compared with observation results. In the next section, we discuss further the temporally and spatially integrated impact on the Ratio 1  $r_{CB}$ .

### The Spatially and Temporally Integrated Ratio

Due to the AP detection limits both on spatial resolution ( $\sim 12$  km at a distance 3,000 km) and temporal scale (50  $\mu s$ ), the spatially localized instantaneous emission ratio  $r_{CB}$  should be considered as the time-integrated and spatial-integrated measurement by the AP. That means that Eq. 3 is spatially and temporally integrated. The spatially and temporally integrated ratio  $R_{k'k}$  (noted by Ratio 2 hereafter) is:

$$R_{k'k} = \iint r_{k'k} dt dV = \frac{A_{k'} \iint (\frac{\partial n_{k'}}{\partial t}) dt dV}{A_k \iint (\frac{\partial n_k}{\partial t}) dt dV} \quad (5a)$$

$$= \frac{A_{k'} \tau_{k'} \iint \nu_{k'} n_e dt dV}{A_k \tau_k \iint \nu_k n_e dt dV} = \frac{A_{k'} \tau_{k'} \nu_{k'} N_{e,k}^*}{A_k \tau_k \nu_k N_{e,k}^*} \quad (5b)$$

where  $N_{e,k}^*$  is the correction term for spatially and temporally integrating the electron density in the streamer region, and is expressed by  $\iint (\frac{\partial n_k}{\partial t}) dt dV \equiv \tau_k \nu_k N_{e,k}^*$  where  $N_{e,k}^*$  is defined by  $\nu_k N_{e,k}^* \equiv \iint \nu_k n_e dt dV$  (Ihaddadene and Celestin, 2017) and in which the maximum contribution to the integration is at peak



time of  $n_k(t)$ . Considering the cascading from the  $C^3\Pi_u$  state into the  $B^3\Pi_g$  state, we reformulated the Ratio 2 ( $R_{CB}$ ), which is expressed by

$$R_{CB} = \frac{A_C \tau_C \nu_C}{A_B \tau_B \nu_B} \left( \frac{N_{e,C}^*}{N_{e,B}^*} \right) \left[ 1 + \left( \frac{N_{e,C}^*}{N_{e,B}^*} \right) \frac{A_C \tau_C \nu_C}{\nu_B} \right]^{-1} \quad (6)$$

where the cascading term is derived in a similar way in the Eq. 4 except for the addition of the term  $\left( \frac{N_{e,C}^*}{N_{e,B}^*} \right)$ .

In Eqs. 5a we can realize that  $\frac{\partial n_k}{\partial t}$  and  $\frac{\partial n_{k'}}{\partial t}$  can be replaced with the right hand side of Eq. 2 where  $n_k$  is the  $B^3\Pi_g$  state and  $n_{k'}$  is the  $C^3\Pi_u$  state for the considered  $N_2$  2P and 1P emission band, respectively. The first term  $\nu_k n_e$  of Eq. 2 indicates the electron impact excitation where the excitation rate  $\nu_k$  means the excitation rate for  $N_2$  1P and 2P and the electron number density  $n_e(t) = n_{e0} \int_0^t \nu_i(E) dt \approx n_{e0} e^{\nu_i(E_h)t}$  under the approximation of constant exponential growth rate  $\nu_i(E_h)$  through the rapidly increasing electron density from the streamer head region to the streamer body region (Babaeva and Naidis, 1997; Liu et al., 2004).

Since the lifetime  $\tau_B$  is greater than the lifetime  $\tau_C$ , the peak time of  $n_B(t)$  is delayed longer than the peak time of  $n_C(t)$ , also shown in Figure 1C. We should consider the time delayed effect of integrating the exponentially increased electron density in the definition form of  $\nu_k N_{e,k}^* = \iint \nu_k n_e dt dV$  where the electron density  $n_e(t)$  in the streamer head exponentially increases over time and can be approximated by  $n_e(t) \approx n_{e0} e^{\nu_i(E_h)t}$  with  $0 \leq t \leq \tau_h$  where  $\tau_h$  denotes the time scale of  $n_e$  from the ambient electron density  $n_{e0}$  to the streamer body electron density  $n_{eb}$ . After its peak time, the number density  $n_B(t)$  relaxes over time with a characteristic time scale of the previously defined lifetime  $\tau_B$ .

In the Eq. 3 for Ratio 1  $r_{k'k}$  we assumed the electron number density can be canceled simultaneously at the same peak  $n_k(t)$  time as  $\frac{\partial n_k}{\partial t} = 0$ . For Ratio 2 ( $R_{k'k}$ ) in Eq. 5, the correction for the higher value of temporal integrating  $n_e$  in  $N_2$  1P as compared with 2P was considered by the spatially and temporally integrated term  $N_{e,k}^*$  (Tables 5, 6 in Ihaddadene and Celestin, 2017). The simulation shows the peak time of  $n_B(t)$  with longer lifetime  $\tau_B$  delay at a time scale of  $<1 \mu s$ . The required propagation time of the streamer head region is defined by  $\tau_h$ . For a typical streamer with a velocity  $5 \times 10^6 \sim 1 \times 10^7$  m/s at an altitude of 70 km (Liu and Pasko, 2004), the  $\tau_h = 1 \sim 2 \mu s$ , corresponding to its streamer radius with  $\sim 10$  m. With the coefficients with  $\tau_h = 1.5 \mu s$  and  $\nu_i(5E_k) = 6 \times 10^6 s^{-1}$ , the electron density drastically increased by  $e^{\nu_i(E_h)\tau_h} \approx 10^4$  in front of the streamer and back to the streamer body. A time delay of peak value  $n_B(t)$  after  $n_C(t)$  will increase the electron density  $n_e(t)$  in the integration term of  $\nu_k N_{e,k}^*$  at the peak time of  $n_B(t)$ . Therefore, we expected that  $\left( \frac{N_{e,C}^*}{N_{e,B}^*} \right) < 1$  for higher integrated values  $N_{e,B}^*$  than  $N_{e,C}^*$ .

Figure 1C clearly shows the unsynchronized issue in the calculation of Ratio 1  $r_{k'k}$  in Eq. 3. The smaller propagation distance ( $z$ ) at the location of the  $N_2$  1P peak value (red) compared to the  $N_2$  2P peak intensity (blue dashed line)

reveals the postponed time of the  $N_2$  1P peak intensity in comparison with  $N_2$  2P peak intensity, i.e., approximated to be the time of peak values for the excited state density  $n_B(t)$  than that for  $n_C(t)$ . When the postponed time of the  $N_2$  1P peak intensity is attained, it corresponds to the higher value of electron density, shown in the red dashed line in Figure 1A.

In addition, Liu et al. (2009) compared their sprite streamer simulations with a high-speed video recording with  $50 \mu s$  resolution. During the initial stage of development, the sprite streamer accelerates its speed while the brightness of the streamer head increases exponentially due to the expansion of the streamer head radius in a concise time of 1 ms. Therefore, we should consider the exponential growth rate of the streamer head brightness at the sprite initial expansion stage, i.e., the left-hand side  $\frac{\partial n_k}{\partial t}$  term cannot be neglected in our ratio calculation.

### The Spatially and Temporally Integrated Effect and the Exponential Growth of Streamer Expansion

For the typical exponential growth of the streamer expansion stage at altitudes of 50–90 km, the time scale is about  $1 \mu s$ ; i.e., the exponential growth rate is  $10^6 s^{-1}$  (Liu et al., 2009; Kosar et al., 2012). Corresponding to streamer head expansion, the time scale of  $1 \mu s$  for the exponential growth rate is much shorter than the AP time resolution of  $50 \mu s$ . Figure 2 shows the  $1 \mu s$  for the exponential growth rate at the green vertical line while the lifetimes of  $N_2$  1P ( $\tau_{1P}$ ) and 2P ( $\tau_{2P}$ ) are compared. The emission band with a lifetime exceeding  $1 \mu s$  should be carefully addressed, especially for 1P at an altitude of  $>50$  km. Therefore, the exponential growth of the streamer expansion stage should be considered, with  $\frac{\partial n_k}{\partial t} = \gamma n_k$ , where the exponential growth rate  $\gamma$  is considered in the streamer simulation of Ihaddadene and Celestin (2017). After substitution with the left-hand-side of Eq. 1, the measured emission ratios  $R_{k'k}^*$  of the  $k'$ -th to  $k$ -th band is modified by the following:

$$R_{k'k}^* = \frac{A_{k'} N_{k'}}{A_k N_k} = \frac{A_{k'} \tau_{k'} \nu_{k'} N_{e,k}^* (1 + \tau_k \gamma)}{A_k \tau_k \nu_k N_{e,k}^* (1 + \tau_{k'} \gamma)} \quad (7)$$

where  $k'$  and  $k$  are  $C^3\Pi_u$  and  $B^3\Pi_g$ , and their corresponding effective spatially and temporally integrated excited state number densities are  $N_{e,C}^*$  and  $N_{e,B}^*$ , respectively.

If the growth rate satisfies  $\gamma \ll \tau_k^{-1}$  and  $\gamma \ll \tau_{k'}^{-1}$  without considering cascading terms, Eq. 7 is approximated as Eq. 5 at an altitude  $<50$  km ( $\tau_B \sim 1 \mu s$  and  $\tau_C \sim 47$  ns), also shown by red and blue lines in Figure 2. It is noted that the lifetime  $\tau_k$  is decreased by higher neutral density at a lower altitude. Considering the cascading from the  $C^3\Pi_u$  state to the  $B^3\Pi_g$  state and the spatially and temporally integrated excited state  $N_B = \frac{\tau_B \nu_B N_{e,B}^*}{1 + \gamma \tau_B} \left[ 1 + \frac{A_C \tau_C \nu_C}{\nu_B (1 + \gamma \tau_C)} \frac{N_{e,C}^*}{N_{e,B}^*} \right]$ , the spatially and temporally integrated emission ratios with consideration of the exponential growth of streamer expansion (Ratio 3  $R_{CB}^*$ ) become:

$$R_{CB}^* = \frac{A_C \tau_C \nu_C}{A_B \tau_B \nu_B} \left( \frac{N_{e,C}^*}{N_{e,B}^*} \right) \left( \frac{1 + \tau_B \gamma}{1 + \tau_C \gamma} \right) \left[ 1 + \left( \frac{N_{e,C}^*}{N_{e,B}^*} \right) \frac{A_C \tau_C \nu_C}{\nu_B (1 + \tau_C \gamma)} \right]^{-1} \quad (8)$$

where the first factor  $F_1 \equiv \left(\frac{N_{e,C}^*}{N_{e,B}^*}\right)$  is estimated to be about 0.7 (0.57) for streamer head electric fields  $3.7 E_k$  ( $4.6 E_k$ ) under ambient electric fields of  $0.4 E_k$  ( $0.9 E_k$ ) at AP measured altitudes of 50–90 km. The first factor  $F_1$  reflects the correction for the spatially and temporally integrated effect on the streamer head where the electric field in the streamer head is dominant over its peak field magnitude in comparison with the altitude changes (Tables 8, 9 in Ihaddadene and Celestin, 2017). The second factor  $F_2 \equiv \left(\frac{1+\tau_B\gamma}{1+\tau_C\gamma}\right)$  is responsible for the exponential growth of sprite streamers and is sensitive to altitude. The  $\gamma$  value is obtained from the simulation work of Ihaddadene and Celestin (2017). The lifetime ( $\tau_B$  and  $\tau_C$ ) in *The Spatially Localized Instantaneous Emission Ratio* are highly quenched by the increasing neutral density at lower altitude. Therefore, we should carefully estimate the effects using  $F_2$  on the brightness ratios in varying altitude conditions. The third factor  $F_3 \equiv \left[1 + \left(\frac{N_{e,C}^*}{N_{e,B}^*}\right) \frac{A_C \tau_C \nu_C}{\nu_B (1+\tau_C\gamma)}\right]^{-1}$  is the cascading effect term, which is considered by the spatially and temporally integrated effect and the exponential growth of the streamer expansion. Next, in *Data Analyses*, we compare the AP-measured emission ratios of sprite events with Ratio 1  $r_{CB}$  in Eq. 4, Ratio 2  $R_{CB}$  in Eq. 6, and Ratio 3  $R_{CB}^*$  in Eq. 8.

These height-dependent emission values of Ratio 1 ( $r_{CB}$ ), Ratio 2 ( $R_{CB}$ ), and Ratio 3 ( $R_{CB}^*$ ) are shown by the red dotted, dashed, and solid curves for a peak electric field of 0.9–4.6  $E_k$ , and blue ones for 0.4–3.7  $E_k$  in the altitude profiles of Figures 6–10, respectively. The predicted emission ratios are approximately constant above altitudes of the quenching height  $\sim 67$  km for  $N_2$  1P (Kuo et al., 2008) with less quenching effect. Due to the increased quenching rate by ambient molecules below the 1P quenching altitude, the decreasing intensity of 1P emission could cause greater values of predicted emission ratios. In *Data analyses*, we analyzed ISUAL AP data, compared with predicted emission ratios of Ratio 1 ( $r_{CB}$ ), Ratio 2 ( $R_{CB}$ ), and Ratio 3 ( $R_{CB}^*$ ), and validated further the analytic expressions from a streamer simulation (Ihaddadene and Celestin, 2017).

## DATA ANALYSES

Adachi et al. (2008) analyzed the ISUAL AP data and estimated the electric field in sprite events. They confirmed the estimated electric field  $0.8\text{--}3.2 \pm 0.42 E_k$  in sprite streamer regions at altitudes  $< 75$  km. A wide distribution of estimated electric fields from the AP-measured emission ratios needs to be clarified. What kind of process was involved in sprites associated with a lower electric field? In *Uncertainty in Sprite Emission Ratios*, we discuss the strategies to limit the measurement uncertainty of sprite emission ratios for our selected sprite events. After comparing sprite images, we found that most carrot sprite events have lower sprite emission ratios than sprite halo events. In *Comparison with Morphology of Recorded Sprites Observed at 5000 fps*, we associated the streamer processes in ISUAL-observed sprite halo and carrot events with detailed image sequences from a high-speed camera at the Lulin Observatory in Taiwan in 2018. *Two Distinct Types of Observed Sprites Determined by the*

*Inception Altitudes: Sprite Halo Event and the Carrot Sprite Event* presents the altitude profiles of sprite ratios for two typical cases: sprite halo and carrot sprite events, respectively. In *The Statistical Analysis of AP-measured Emission Ratios*, we compared the statistical data on emission ratios with predicted emission ratios, and validated the analytic expressions from a streamer simulation (Ihaddadene and Celestin, 2017). In *The Effects of AP-measured Ratios for a Pre-Existing Sprite on a Later-Occurring Sprite*, we discussed the pre-ionization effects on sprite emissions.

## Uncertainty in Sprite Emission Ratios

We attributed uncertainties in sprite emission measurements to the following: 1) band percentage uncertainties, 2) altitude errors, 3) lightning contamination. In contrast with previous studies using estimated electric field results (Kuo et al., 2005; Adachi et al., 2006; Adachi et al., 2008; Kuo et al., 2008; Kuo et al., 2009), we presented the emission ratio of the total intensity of the 2P to 1P band in the data points of Figures 6–11. The measured emission ratio should be independent of their observed instrument (spectrophotometer, array photometer, or intensified imager) if their relative instrument detection efficiency for 2P/1P emissions is well calibrated. However, that also causes an error of the band percentage  $B_k(h)$  calculation introduced into a total specified band emission.

As mentioned in the discussion of altitude errors in *The ISUAL array photometer*, some of these errors from different calculations could be accumulated. After checks on the ISUAL recorded images, the altitude errors would be controlled within  $\pm 5$  km based on a top altitude of 90 km for triangularly measured sprites (Sentman et al., 1995; Wescott et al., 2001). Besides, we selected sprite events with the distance of 2,900–3,500 km, where few errors in the  $B_k(h)$  would be introduced. The uncertainty in the band percentage can be limited to  $\pm 10\%$ . However, as mentioned in *The ISUAL array photometer*, the unknown percentage of the 1P spectrum with vibrational number  $\nu = 0$  would contribute as much as 30% to the error.

Most sprite events were reported with substantial blue lightning contamination (Adachi et al., 2008) due to the short delay time  $< 0.1$  ms between the parent lightning and sprite events. We chose sprite events for which lightning signals can be separated from sprite emissions. If a time delay between lightning and sprite emission is longer than  $> 0.1$  ms, the AP vertical channel can separate the lower-altitude lightning emission from the higher-altitude sprite emission. For our considered sprite events in Table 1, the AP-measured blue/red emission peak occurred at least 0.1 ms after the time of recorded lightning SP5 at 777.4 nm, and no simultaneous lightning was contaminating other AP channels.

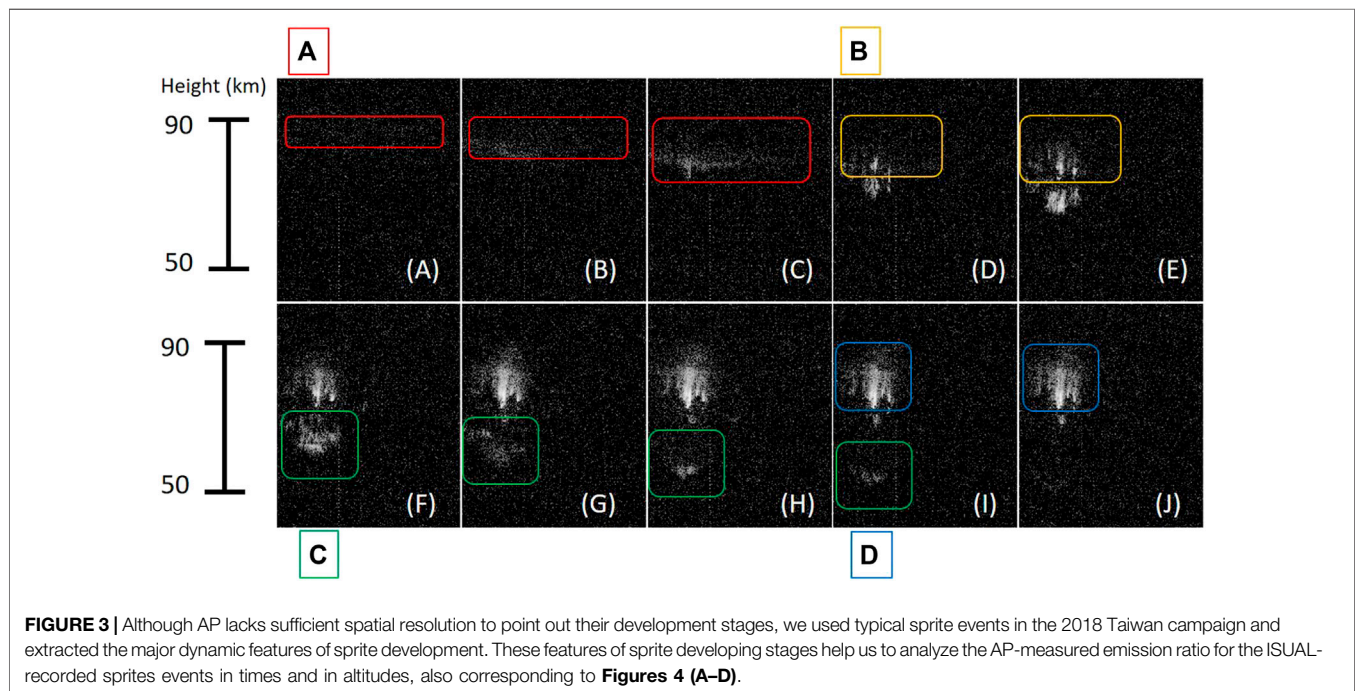
## Comparison With Morphology of Recorded Sprites Observed at 5,000 fps

Figure 3 helps us to study the features for the specific streamer processes using the AP-measured sprite emission ratio. We identify the sprite streamer processes with four major processes: 1) sprite streamer inception, 2) upper branches of

**TABLE 1** | The event list for two sprite categories (sprite halo and carrot sprite events) and their inception altitudes and emission times.

Trigger time (UT)	Type <sup>a</sup>	Inception altitudes (km)	Emission time (ms)
Oct 3, 2005 14:43:37.240	SH	88.5 ± 6.3	0.6
Sep 4, 2006 15:05:30.844	SH	80.5 ± 6.0	1.4
Apr 29, 2007 06:38:30.728	SH	86.5 ± 6.2	0.7
Aug 24, 2007 16:57:01.582	SH	81.5 ± 6.3	0.9
Mar 26, 2005 21:37:06.144	CS	71.9 ± 6.8	3.5
Jul 30, 2005 04:39:42.742	CS	72.4 ± 5.7	3.4
Jul 17, 2007 11:38:13.200	CS	75.3 ± 6.1	3.2
Sep 28, 2009 04:25:56.262	CS	59.2 ± 7.0	2.5
Jul 11, 2010 04:36:16.235	CS	68.8 ± 6.8	3.0
Sep 1, 2011 04:42:58.161	CS	56.7 ± 7.0	2.4

<sup>a</sup>Sprite type is determined by their inception altitudes and by their distinguished halo emission where SH and CS denote sprite halo event and carrot sprite, respectively.

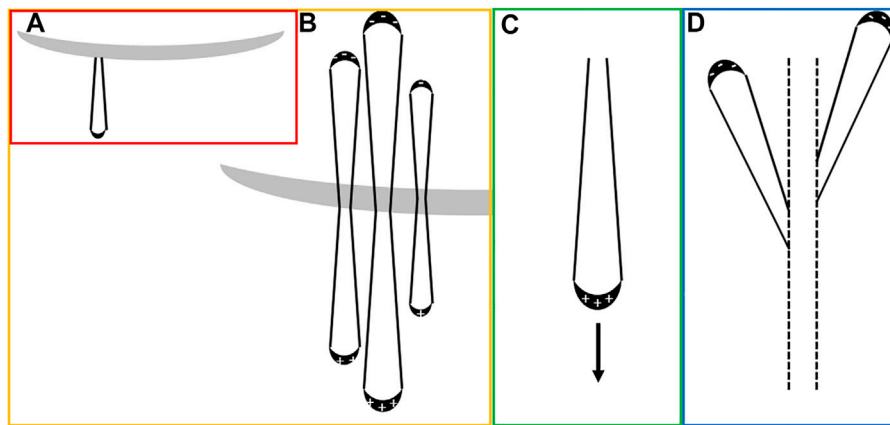


bi-directional streamers with negative polarity, 3) downward propagating streamers with positive polarity, and 4) reigniting of upward streamer in the sprite cluster region. **Figure 4** also illustrates the stages 1–4 of streamer processes for sprites. In the development stage (1), **Figures 3A–C, 4A** pinpoint the occurrence of steamer inception near the downward edge of the sprite halo. The bi-directional streamers fully developed into upper and lower branches in the stage (2) in **Figures 3D,E, 4B**. The streamer heads in their lower branches propagated downward with extra brightness, shown in **Figures 3F–H, 4C**. The sprite body's emission was continuously recorded in several later frames of the images in **Figures 3I,J, 4D**. Next, we will analyze their AP-measured emission ratio based on the time and the height of ISUAL-recorded sprite events. The morphology of a typical sprite event recorded at 5,000 fps helps us imagine the successive image frames and identify the stages 1–4 for recorded sprites since the ISUAL payload lacks the detailed dynamics in their recorded sprites.

## Two Distinct Types of Observed Sprites Determined by Their Inception Altitudes: Sprite Halo Event and the Carrot Sprite Event

Sprites involve streamer heads emerging from the downward leading edge of a halo or plasma inhomogeneity and branching into both downward streamers and upward-propagating streamers simultaneously (Stanley et al., 1999; Stenbaek-Nielsen et al., 2000; Moudry et al., 2003; Marshall and Inan, 2005; Cummer et al., 2006; McHarg et al., 2007; Stenbaek-Nielsen et al., 2013). Numerical studies compared sprite halo and carrot sprites (Qin et al., 2011). The short-delayed halo sprites were possibly produced by a-CG (Cloud-to-Ground lightning with negative polarity) with an impulsive lightning current and without continuing current, while long-delayed carrot sprites were triggered by +CG (Cloud-to-Ground lightning with positive polarity) due to a long-lasting high field region for a





**FIGURE 4** | To analyze the AP emission characteristics of each developed stage in ISUAL recorded sprites, we choose **(A)** sprite streamer inception, **(B)** upper branches of bi-directional streamers with negative polarity, **(C)** downward propagating streamers with positive polarity, and **(D)** reigniting of upward streamer in the sprite body for specific streamer process in **Figure 3** and later used to study the AP measured emission ratio.

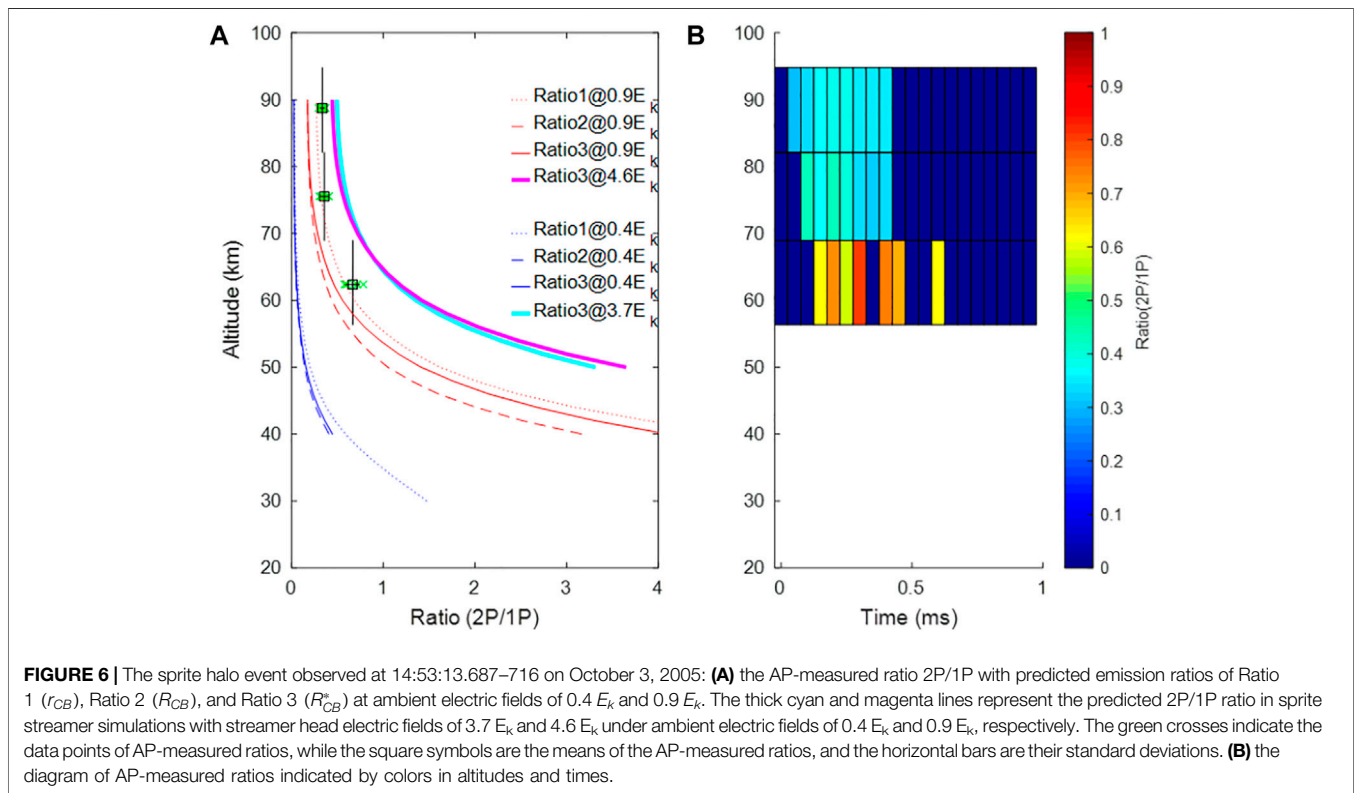
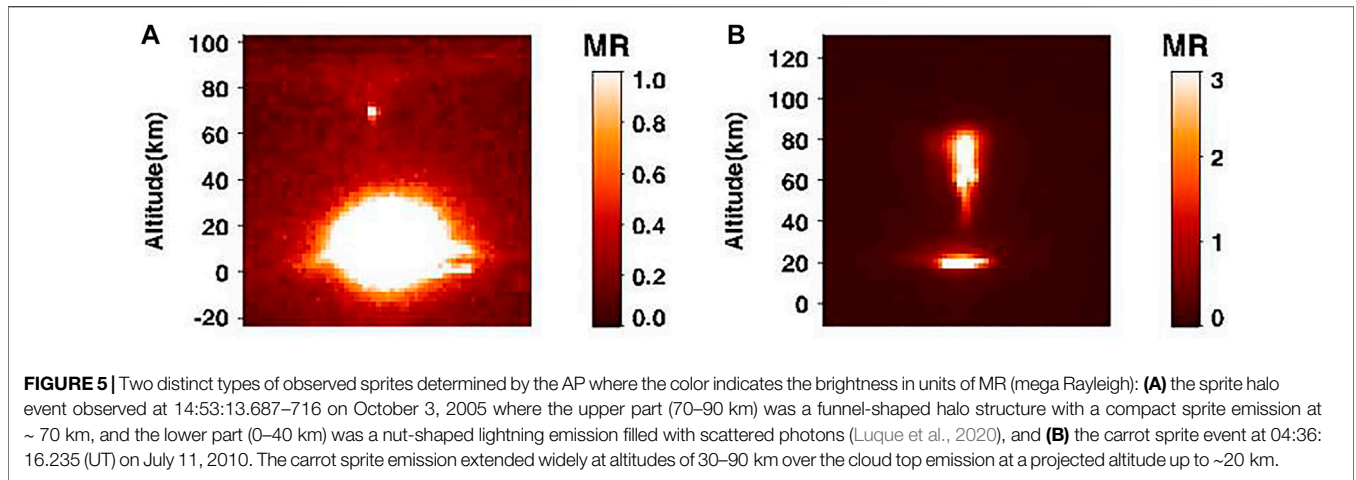
lightning continuing current. Listed in **Table 1**, we selected sprite events from 2005 to 2011 to minimize possible uncertainty in emission ratios. Ten sprite events were excluded from twenty candidates. In six sprite events lightning was more powerful than the AP-measured blue/red emission. Difficulties were faced in another four sprite events in separating the sprite emission from the lightning emission. The final ten selections are included in **Table 1** which shows the characteristics of sprite halo and carrot sprite events in their inception altitudes, AP-measured ratios, and emission times.

In ISUAL recorded images (spatial resolution  $\sim 2$  km), sprite halos events have narrow structures (likely column sprites) with a distinguished halo. In contrast, carrot sprites have compact structures with higher brightness and longer emission duration. For AP-measured emission altitudes, sprite halo events were accompanied by downwardly-propagating streamers, and were intercepted at altitudes  $84.3 \pm 3.8$  km with an average emission time  $0.9 \pm 0.3$  ms. Otherwise, the AP measured emission for carrot sprite events began at lower altitudes  $67.4 \pm 7.6$  km and developed into upward and downward-propagating emissions with an average emission time  $3.0 \pm 0.5$  ms. Besides, a mixed type was found that a sprite event at time 21:45:48.239 (UT) on Mach 16, 2006 initialized at  $83.4 \pm 6.8$  km with an emission time 2.9 ms, not listed in **Table 1**. The sprite event has both characteristics of our categorized sprite halos and carrot sprites. We identified this event with the mixed type. The sprite may be accompanied by the halo emission at higher altitudes and finally developed into a whole carrot sprite with a more prolonged emission. The recorded images also show the cloud emission lasted more than 180 ms. We conjecture the sprite event may be affected by the lightning continuing current associated with cloud emissions.

**Figure 5** compares two distinct categories of sprite events (sprite halo and carrot sprite events) distinguished by their inception altitudes and their AP-measured emission, listed in **Table 1**; **Figures 6, 7** show their spatial and temporal diagrams of AP-measured blue-to-red ratios, respectively. For a sprite halo

event (14:43:37.240 UT on October 3, 2005) **Figures 5A, 6A** show AP-measured ratios in green cross symbols as referenced by curves to represent the simulated streamer ratios with  $0.4\text{--}4.6 E_k$ . **Figure 6B** indicates the diagram of AP-measured ratios by colors in altitudes and times. In **Figure 6B**, a sprite halo is initialized at an altitude of  $88.5 \pm 6.3$  km, which corresponds to the altitude range of the transition from a halo to the inception of sprite streamers in **Figure 5A**. The AP signals propagated down to a lower altitude of  $62.6 \pm 6.3$  km. As shown in **Figure 6A**, AP-measured ratios (green cross symbols) are found between  $0.9 E_k$  and  $3.7\text{--}4.6 E_k$  in the streamer head. Although AP-measured ratios have lower values than predicted emission ratios (thick cyan and magenta lines), the statistical analysis in **Figure 8A** with more sprite halo events implies that the AP-measured ratios are consistent with predicted emission ratios.

**Figure 5B** shows a carrot sprite event without a distinguished halo observed at 04:36:16.235 (UT) on July 11, 2010. The AP-measured blue/red emission peaks are delayed about 0.4 ms after the recorded lightning signal by SP5 at 777.4 nm. The carrot sprite event initialized at an estimated altitude of  $68.8 \pm 6.8$  km, and subsequently propagated downwardly and upwardly. **Figure 7A** compares AP-measured ratios with predicted emission ratios while **Figure 7B** shows their timing diagram in altitude. The carrot sprite initialized in an altitude range of 62–76 km at time  $-0.4$  ms, and developed into lower altitude emission in the interval  $-0.4\text{--}0.05$  ms. Unexpectedly, AP-measured ratios approach the red lines ( $0.9 E_k$ ). After the time 0.05 ms, AP-measured ratios gradually decreased and reached to the blue lines ( $0.4 E_k$ ). The gradual decrease of the emission ratios can be understood since the sprite streamer energy is finally dissipated in electron collisions with ambient molecules. In addition, the upper branches of sprite emission occurred after 0 ms where the AP-measured ratios have a maximum value 0.33. Similarly, the AP-measured ratios are slightly higher than red lines ( $0.9 E_k$ ) and are lower than predicted emissions in cyan and magenta lines ( $3.7\text{--}4.6 E_k$ ). Next, we collected

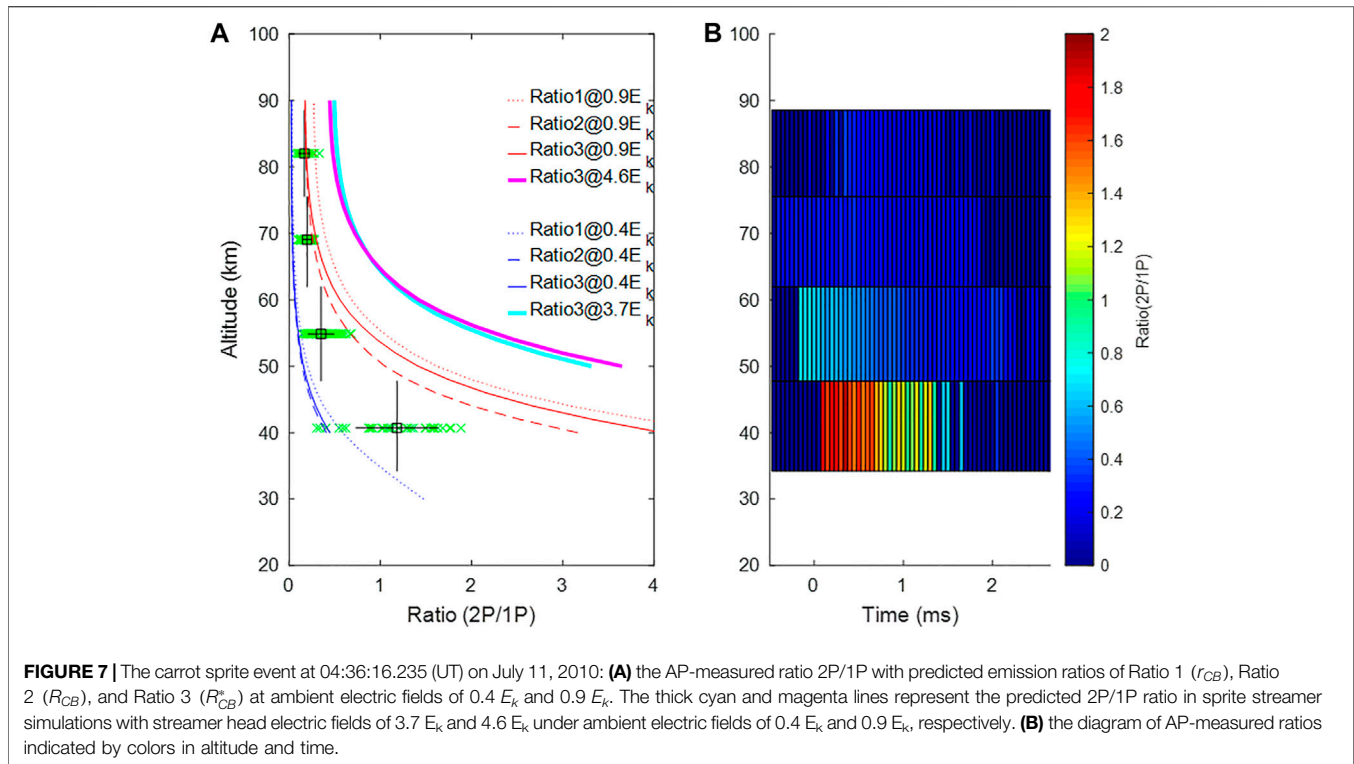


additional sprite events to support more evidence on the higher emission ratios for sprite halos and lower values for carrot sprites.

### Statistical Analysis of AP-Measured Emission Ratios

Figure 8 shows the selected sprite events where each event has 3–4 points measured in the corresponding altitude range by the AP vertically-stacked channels. The square symbol indicates the mean sprite ratio at a specified altitude, where the vertical

error bars show the altitude range of the AP measurements. The horizontal error bars indicate the standard deviation of the AP-measured ratios in the same AP channels. In Figure 8A, the AP-measured ratios (2P/1P) in sprite halo events have data points scattered around the curves for predicted emission ratios from streamer head electric fields ( $3.7\text{--}4.6 E_k$  for cyan and magenta lines). The scatter in the distribution of AP measured ratios in sprite halos events of Figure 8A may be attributable to the variances of large-scale quasi-steady electric field magnitudes caused by charge transfer inside the clouds beneath or to uncertainty in the AP measurement with unknown reasons.



In **Figure 8B**, the carrot sprite events initialized at a lower altitude of 60–75 km, and have lower emission ratios than sprite halos events in **Figure 8A**. AP-measured ratios are slightly lower than the predicted ratios (streamer head electric fields of  $3.7 E_k$  and  $4.6 E_k$  in cyan and magenta lines) in higher altitudes of 65–90 km (sprite upper branches and central regions). The lower tendrils in carrot sprites at lower altitudes (50–65 km) have increased emission rates. The emission ratios reflect the quenching effect in *Analytical expressions for sprite emission ratios*. But these values are unexpected, ranging between blue lines ( $0.4 E_k$ ) and red lines ( $0.9 E_k$ ) in **Figure 8B**.

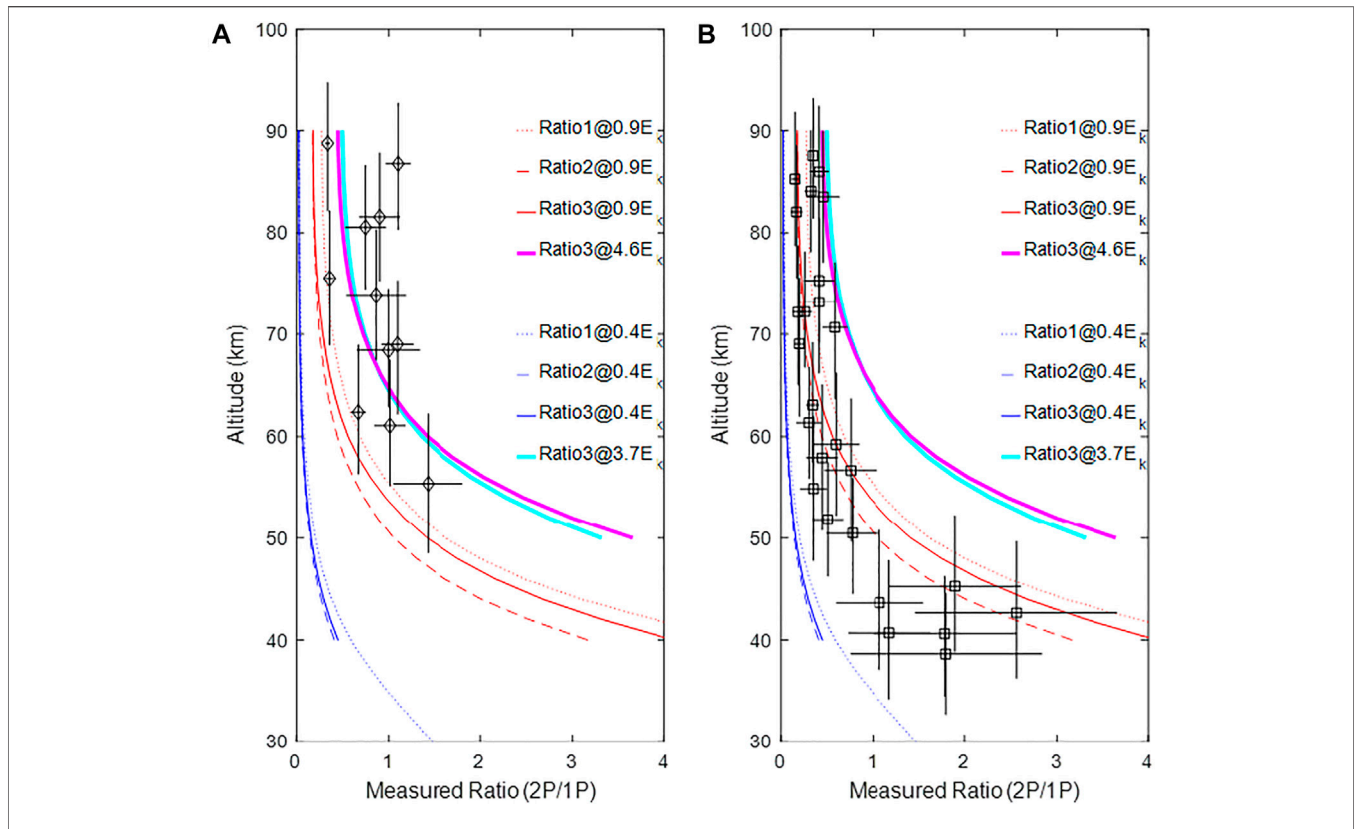
**Figure 8B** have a lower bound of data points near blue lines ( $0.4 E_k$ ). Most of the estimated ambient electric fields were greater than  $0.4 E_k$ . The ambient electric field threshold ( $0.4 E_k$ ) is consistent with the results of remote electromagnetic field measurements for short-delayed or big/bright sprites (Hu et al., 2002; Li et al., 2008). The non-streamer head regions (such as sprite streamers' bodies and tails or the surroundings of sprite streamers) may contribute additional red (1P) emission, which may cause lower emission ratios (2P/1P). Stenbaek-Nielsen et al. (2020) compared the blue-to-red emission ratio and found that upper propagating streamer, sprite beads, and glow have lower emission ratios. For those non-streamer processes, a large percentage of 1P (red) emission makes lower AP-measured ratios, especially for the case of long emission time in the carrot sprites. Hence, for carrot sprites, our study shows that sprite inception at lower altitudes may favor development into the whole complex structures of sprites, which may be accompanied by non-streamer emission or sprite beads caused by attachment instability in streamer channels (Luque

et al., 2016). The Possibly a pre-existing free ionized plasma patch in the early stage of sprites may provide more free energized electrons. More non-streamer processes with lower emission ratios could occur and co-exist with reigniting of upward streamers. Next, we provide an example case to show the effect of a favorable plasma environment.

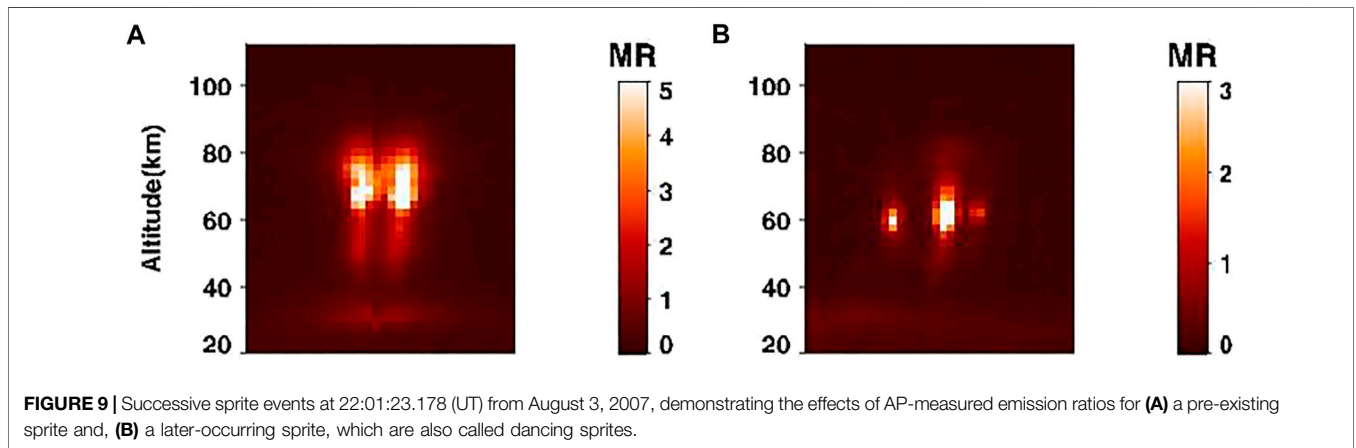
### The Effects of AP-Measured Ratios for a Pre-existing Sprite on a Later-Occurring Sprite

**Figure 9** shows successive sprite events at 22:01:23.178 (UT) on August 3, 2007, which are also called dancing sprites (Lyons, 1994; Bór et al., 2018 and reference therein). The preceding sprite event in **Figure 9A** began ~85 ms before the second sprite event with lower brightness in **Figure 9B**. We also demonstrate the decrease in emission ratios for a pre-existing sprite on a later-occurring sprite in **Figures 10, 11**. The measured emission ratios for the pre-existing sprite and the later-occurring sprite are compared with predicted emission ratios Ratio 1 ( $r_{CB}$ ), Ratio 2 ( $R_{CB}$ ), and Ratio 3 ( $R_{CB}^*$ ).

The comparison of **Figure 10A** with **Figure 11A** shows a slightly lower value of AP-measured emission ratio 2P/1P, which may imply that the plasma environment and the generation mechanism of the second sprite event may be different from that of the first sprite event. Successive sprite events have been reported in previous studies using a high-speed image-intensified camera (Stenbaek-Nielsen et al., 2000). A second sprite occurred in the fading region of the first sprite, gradually brightened, and developed branched tendrils towards lower altitudes. The



**FIGURE 8** | AP-measured emission ratios of 2P to 1P for 10 selected sprite events without potential lightning contamination. Two categories of ISUAL sprite events are shown in AP-measured ratios: **(A)** sprite halo events with impulse AP emission time ( $0.9 \pm 0.3$  ms) and higher estimated electric fields, and **(B)** carrot sprite events with long AP emission time ( $3.0 \pm 0.5$  ms) and lower estimated electric fields.



**FIGURE 9** | Successive sprite events at 22:01:23.178 (UT) from August 3, 2007, demonstrating the effects of AP-measured emission ratios for **(A)** a pre-existing sprite and, **(B)** a later-occurring sprite, which are also called dancing sprites.

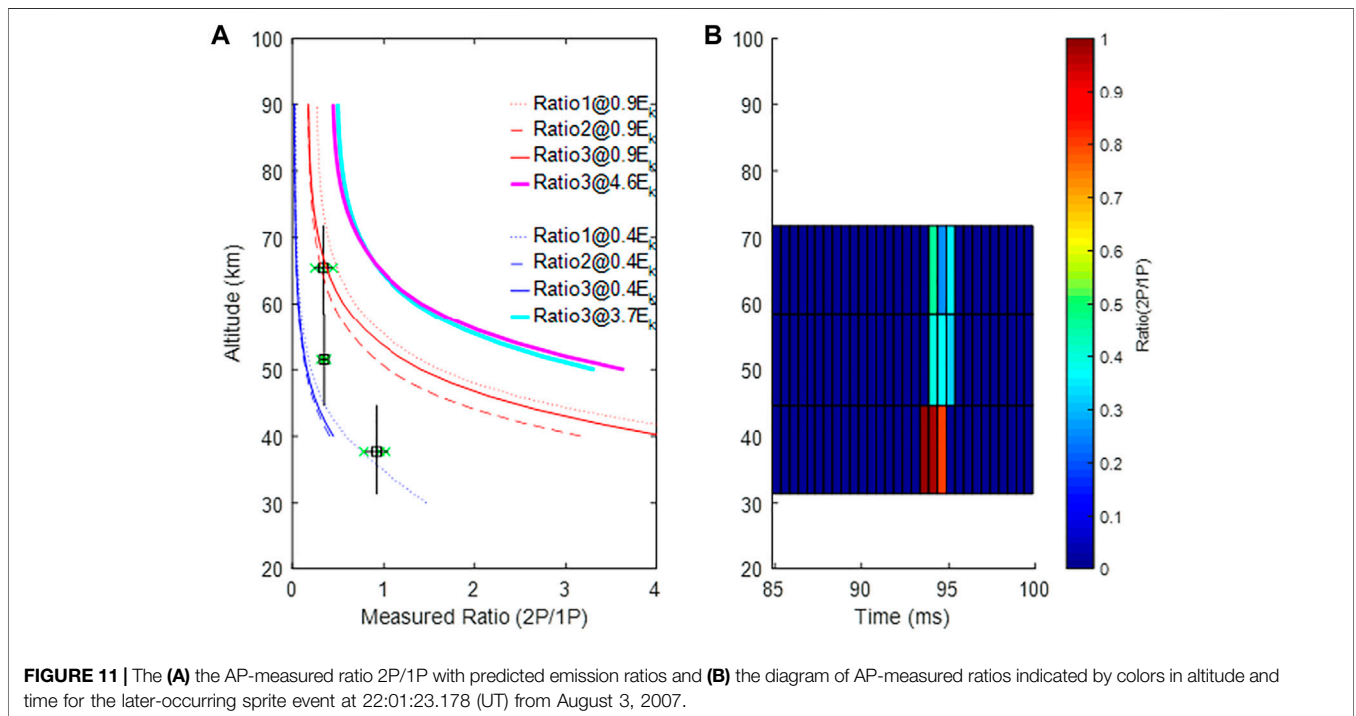
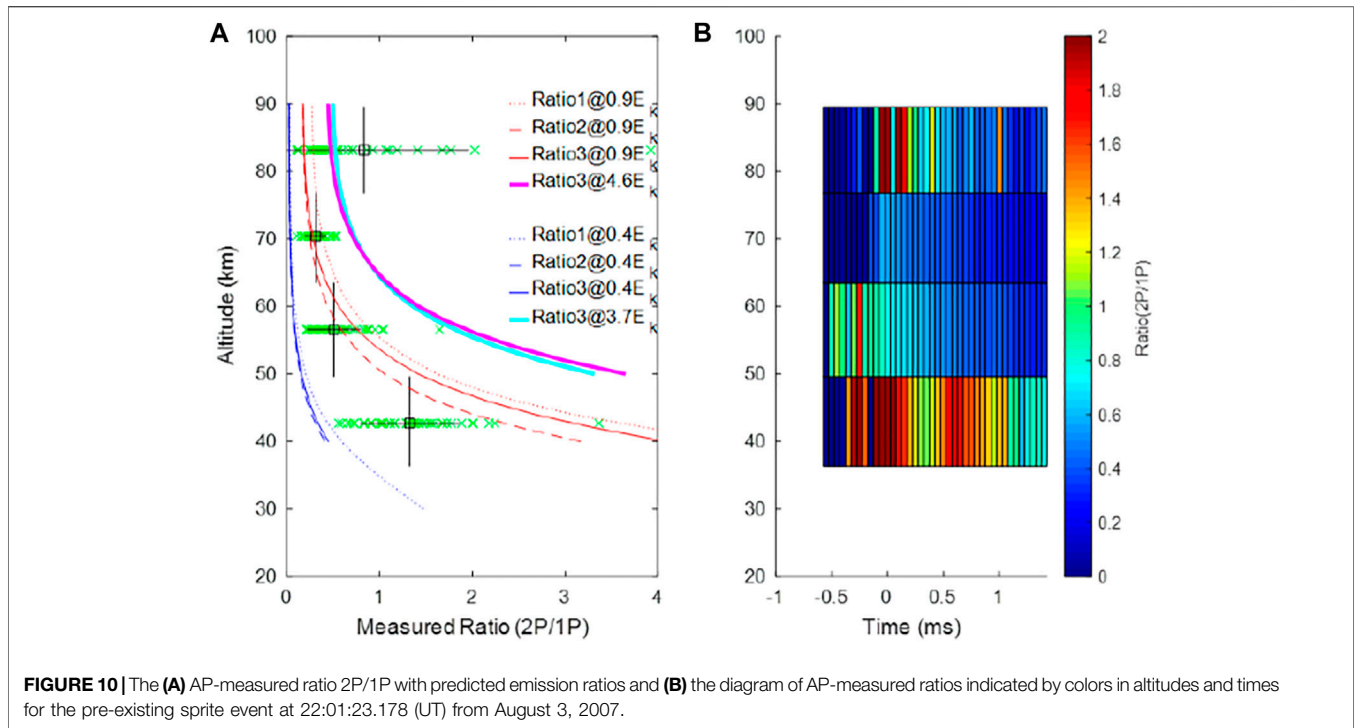
upwardly branched streamers may arise from previous older streamer channels (Stenbaek-Nielsen et al., 2000; Luque et al., 2016). The AP-measured emission ratio in **Figure 11B** provides direct evidence of the upper branches developing in pre-existing sprite structures where lower-altitude AP-measured ratios developed into the region at higher altitude. The AP-measured ratios in the later-occurring sprite are lower than that in the previous sprite event. That may support the idea that the change

of the plasma environment may cause lower emission ratios in carrot sprite events.

### SUMMARY

We verified experimentally the AP-measured emission ratio 2P/1P and compared it with the theoretically predicted sprite





emission ratio 2P/1P using numerical results on sprite streamers (Celestin and Pasko, 2010; Pérez-Invernón et al., 2018). AP-measured ratios in sprite halo events are consistent with predicted ratios for streamer head electric fields of 3.7  $E_k$  and 4.6  $E_k$  in **Figure 8A**. Most carrot sprite events initialized at altitudes  $67.4 \pm 7.6$  km with lower estimated electric field 1~3 or 4  $E_k$ . Below

60 km, surprisingly, AP-measured ratios fell below the predicted ratio 1  $E_k$ . We conjectured that the lower emission ratios are contributed from those non-streamer regions (upper propagating streamer, sprite beads, and glow) by Stenbaek-Nielsen et al. (2020). In addition, the AP-measured ratios have a lower bound of predicted emission ratios associated with 0.4  $E_k$ .

For space-based optical diagnostics in limb observation, as with the ISUAL mission, the main conclusions from our studies on the sprite emission ratio  $2P/1P$  are the following:

- 1) For accurate analyses of ISUAL AP data, we selected sprite events from the first 7 years (2004–2011) of operation to avoid the degradation in instrument performance. After analyzing the ten selected sprite events, the AP-measured ratios scatter widely as previous results in sprites (Adachi et al., 2008), and estimated electric fields range between  $0.4 E_k$  and greater than  $4 E_k$ . The downward propagating streamers verified the streamer head electric fields in the range  $\sim 3.7\text{--}4.6 E_k$ . At lower altitudes, AP-measured ratios have a lower bound, corresponding to the predicted ratio for  $0.4 E_k$ . The threshold of the estimated electric field ( $0.4 E_k$ ) is consistent with the earlier results of remote electromagnetic field measurements for short-delayed or big/bright sprites (Hu et al., 2002; Li et al., 2008).
- 2) The AP-measured ratios of downward propagating streamers in sprite halo events scattered around the ratios predicted by numerical streamer head electric fields with  $3.7\text{--}4.6 E_k$  (Ihaddadene and Celestin, 2017) where the estimated electric field was in the range  $0.4\text{--}0.9 E_k$ . However, for carrot sprite events, the AP-measured emission ratio  $2P/1P$  showed lower values than predicted ratios. The extra  $1P$  red emission may be contributed from non-streamer dominant emissions: sprite beads and glow or possibly by plasma environment changes in upper streamers in carrot sprites with lower inception altitude and longer emission time Qin et al., 2014.

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## DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material, and further inquiries can be directed to the corresponding author.

## AUTHOR CONTRIBUTIONS

EW conceived the study to check AP data for sprite halos. C-LK analyzed AP data. KI and SC formulated the analytical equations for sprite emission ratios and conducted the simulation of sprite streamers. TA, YT, HF, and SM provided the AP calibration data. YT, HF, SM, R-RH, and L-CL were all part of the ISUAL science team. All authors contributed to the final interpretation and writing of the manuscript with major contribution by C-LK.

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