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# Experimental evidence of gas-mediated heat transfer in porous solids measured by the flash method

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## Abstract

Laser/light flash analysis (LFA) is becoming an increasingly popular assessment tool for the thermal properties of porous samples. Elevated temperature measurements are typically conducted under a protective atmosphere; specifically, under inert gas flow. Immersing a sample with interconnected porosity in a gas environment theoretically allows heat transfer via gas conduction or convection. To prove that LFA measurements are affected by the choice of the gas environment, measurements are conducted under inert gas flow (helium and nitrogen), static inert gas (nitrogen) and vacuum with two different instruments and two sets of samples: highly-conductive alloy foams and insulating lightweight concrete. A heat conduction model accounting for light penetration was used to extract the apparent thermal diffusivity of the solid-gas mixture. A correlation between the Biot number and the conductivity of the gas environment was registered. This is unusual for an LFA experiment where radiative heat losses, which are independent of the gas environment, are typically considered to be dominant. At the same time, variations in either the microgeometry of the porous sample or the type of carrier gas produce a systematic change in the shape of the time-temperature profiles and the duration of the temperature transient. In lightweight concrete samples, switching the instrument to helium flow enables a multifold increase in the apparent thermal diffusivity relative to the measurements done under vacuum. An attempt to explain this variation was made with a two-temperature model of coupled solid-gas conduction. It is argued that an additional factor is missing from the analysis.

*Keywords:* thermophysical properties, laser flash analysis, porous materials, heat conduction, convection

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## 1. Introduction

Most standard laser-flash and light-flash analysis (LFA) instruments operate under an inert atmosphere. At high temperatures, an inert gas flow suppresses oxidation and minimises the re-deposition of contaminant gases. At ambient and low temperatures, a purge gas ensures smooth temperature manoeuvring by acting as an efficient coolant. The choice of the purge gas species should be informed by: the target temperature range, gas thermal properties and other factors e.g. the gas ionisation potential when electric discharge is highly probable. While the gas environment should

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7 always be compatible with a safe operation of the instrument, it might also affect the time-temperature transients  
8 intrinsic to the material under study. Ultimately, this is reflected in biased measurement results. Such bias might arise  
9 when measuring open-cell foams [1] or powder compacts [2]. There, the purge gas is able to freely roam the pore  
10 space. Because a potential contribution from the purge gas is expected, the reported values of thermal properties risk  
11 turning into *ad hoc* “effective” quantities with an undefined range of validity. With regards to LFA measurements  
12 of porous materials, some researchers [3] had preferred low-conductivity purge gases such as nitrogen. Others had  
13 used a more conductive helium [4, 5, 6, 7, 8]. Attempts to explain the variation of thermal diffusivity with the gas  
14 environments do exist [9]. At the same time, these explanations relate only to the scaling of the time axis in the LFA  
15 experiments due to the definition of the Fourier number as  $Fo = at/l^2$ , where  $a$  is the thermal diffusivity,  $t$  is the time  
16 and  $l$  is the path of thermal diffusion. It is unknown whether linear scaling is only expected or if nonlinear processes  
17 are at play e.g. resulting in a change of concavity of the heating curves. This issue seems overlooked although the  
18 thermal properties of porous materials are in focus of many ongoing research activities. There has been a growing  
19 interest in applying the LFA technique to measure metal and ceramic foams [10, 11, 12], coal [13], zeolites [14],  
20 concrete [15, 16] and other promising materials.

21 In contrast to other measurement techniques such as the transient plane source (TPS) method [17] or the guarded  
22 hot plate method (GHP) [18], flash measurements produce shorter temperature transients of a small magnitude result-  
23 ing in fairly low temperature gradients. Under these conditions, the dynamic gas flow caused by natural convection is  
24 normally considered negligible, viz. Section 2.3 in [9]. When analysing the “raw” time-temperature profiles measured  
25 experimentally, the contribution of gas conduction inside the porous matrix is typically ignored completely. Indeed,  
26 models of heat conduction in a rod (Cowan [19] – as used in [9]) or a solid cylinder (Cape-Lehman [20]) are employed.  
27 After evaluation, a variation in thermal conductivity  $\lambda$  of porous materials is typically registered under different gas  
28 environments. This variation is explained in terms of effective-medium models also known as mean-field or self-  
29 consistent methods, SCMs. An example is the Bruggeman model referenced in [9]. The theoretical framework giving  
30 rise to SCMs is sometimes referred to as the Maxwell’s approach with a notable result being the Maxwell-Garnett  
31 relation. Limitations of the Maxwell’s approach had previously been discussed in [21] for non-overlapping, non-  
32 interacting inclusions. Limitations of empirical SCMs including the Bruggeman model have recently been assessed  
33 in [22]. In short, an SCM may provide means to reduce a heterogeneous structure formed of many inclusions ( $\lambda_i$ ) in a  
34 matrix ( $\lambda_m$ ) to a single particle with “effective” properties. The homogenisation procedure used to arrive at this result  
35 considers steady-state heat diffusion described by the Laplace’s equation:  $\Delta T = 0$ , where  $\Delta$  is the Laplace operator  
36 and  $T$  is the temperature. Since a transient heat equation includes a time derivative  $\partial T/\partial t$ , the homogenisation pro-  
37 cedure formulated under static conditions is not guaranteed to work in the dynamic mode. As a result, the “effective”  
38 transport properties for the steady-state and transient heat transfer would likely be different. Evidence of the latter has  
39 been recently presented in [1].

40 Unfortunately, papers reporting on LFA measurements in porous materials seldom provide sufficient details of  
41 how raw data (voltage over time) is converted into the reported thermal diffusivity values,  $a$ . As a consequence, it

42 is impossible to estimate the error inherent to this procedure. This was in focus of a recent research [23, 24, 25]  
43 where a typical deviation of the heating curve had been demonstrated in porous rocks. Sophisticated models based  
44 e.g. on the Guyer-Krumhansl equations or the two-temperature ( $2T$ ) approach had been employed to mitigate this  
45 problem. The authors findings [23, 24, 25] have additionally been confirmed in a recent paper on metal foams [1]  
46 providing further insights into the non-Fourier behaviour of porous materials under temperature transients. One of the  
47 key results [1] indicates the porosity distribution alters the curvature of the heating curve registered experimentally.  
48 One of the causes for this deviation is the three-dimensionality of heat fluxes in a porous system. It is unknown though  
49 whether changing the gas medium could also distort the shape of the heating curve.

50 This work aims to close this gap. It explores how a gas environment might affect the heat transfer pathways  
51 activated in a LFA measurement of highly-conductive and insulating porous materials. Secondly, the feasibility of  
52 using the LFA to measure the thermal properties of a porous material in a gas environment is investigated.

## 53 **2. Experimental**

### 54 *2.1. LFA Measurements*

55 The physical phenomenon of interest is demonstrated using two commercial, mainstream instruments. The LFA  
56 457 [26] (near-IR laser source) and LFA 467 (xenon lamp) instruments are used, with differing geometries of the gas  
57 and cooling channels, the direction of the gas flow (top-to-bottom in LFA 467 and bottom-to-top in LFA 457), and  
58 vacuum capabilities. Measurements could be conducted either under a defined inert gas flow with a default value of  
59 100 ml/min, under vacuum or in a static atmosphere. The LFA 457 could be continuously evacuated using an external  
60 rotary pump during the whole measurement duration. The instrument was configured to deliver 0.35 ms laser pulses  
61 at a lamp voltage of 1538 V. The LFA 467 produced 0.6 ms xenon pulses (250 V), which resulted in a somewhat lower  
62 sample heating compared to the laser instrument. In both instruments, pulse shapes were recorded at each flash and  
63 stored for subsequent pulse correction.

64 For each material tested (see Section 2.2), three series of measurements were carried out in a pre-specified tem-  
65 perature range — first, when purging the instrument chamber with helium, then with nitrogen, then under dynamic  
66 vacuum. Additionally, measurements under a static inert atmosphere were conducted in the thermally-insulating ma-  
67 terial. When comparing purge gases, it should be noted that the thermal conductivity of helium ( $\lambda_g = 0.15$  W/m·K)  
68 was significantly higher than in nitrogen ( $\lambda_g = 0.025$  W/m·K).

69 All porous samples were measured without any graphite coating. Uncoated surfaces tend to have lower emissivity,  
70 decreasing the amount of radiative heat losses. This reduces the uncertainty due to the possible radiative heat transfer  
71 contribution. Contrary to the experimental conditions in [9, 27], a lack of surface coating allows the light to penetrate  
72 through the bulk of the samples with open porosity. Light penetration is a source of uncertainty – but it can be  
73 eliminated completely using an appropriate modification of the evaluation procedure while measuring sufficiently  
74 thick samples. This is different from the approach taken in [9, 27] where the samples are rendered opaque by filling

75 the outermost pores with a thin paste layer. Obviously, this eliminates light penetration. However, as explained  
76 previously in [1], the paste layer participates in the heat transfer. Since the paste and the material under study are  
77 dissimilar, heat fluxes across their interfaces must overcome a thermal contact resistance. The presence of a third  
78 phase (the paste) in addition to the other two (the matrix material and the porosity) is highly undesirable if accurate  
79 measurements need to be conducted. It is nearly impossible to account for that additional source of uncertainty. At  
80 the same time, uncoated porous samples are not opaque, making flash-throughs possible. To avoid flash-throughs  
81 during the laser/light shots and reduce stray light, the samples needed to be sufficiently thick. This helps to eliminate  
82 a distortion of the measurement results similar to the one reported in [28].

## 83 2.2. *Materials*

84 Experimental samples included two sets:

- 85 • Aluminium-magnesium foams fabricated by Exxentis AG (Wettingen, Switzerland), with 60% (open) porosity  
86 and a density of 1.09 g/cm<sup>3</sup>. Samples with a nominal pore size of 0.20 – 0.35 mm and 0.40 – 1.00 mm were  
87 tested. The matrix material is very conductive – hence fast transients are expected;
- 88 • Lightweight concrete samples fabricated by Ytong, with densities  $\rho_m = 0.52$  g/cm<sup>3</sup> and 0.54 g/cm<sup>3</sup>. Contrary  
89 to the previous material, Ytong is thermally insulating, producing long transients.

90 Samples from both available materials were prepared in a cylindrical geometry, with a thickness of 5 mm and a  
91 diameter of 12.5 mm. The samples under study had open porosity permeable to the surrounding gas. Al-Mg foams  
92 were measured exclusively with LFA 457, whereas Ytong was measured both with LFA 457 (static atmosphere and  
93 vacuum) and LFA 467 (gas flow).

## 94 2.3. *Data processing*

95 After collecting the time-temperature profiles  $T(t)$ , the latter were exported in a csv format and loaded into  
96 PULsE [29] (version 1.93F [30]), an open-source numerical analysis software, to extract the thermal diffusivity values  
97 from the raw data.

## 98 2.4. *Model accounting for light penetration*

99 The data was processed with a “Penetration model”, which accounted for a spatially distributed absorption of  
100 the laser pulse at the sample front and distributed emission of the thermal radiation measured by the detector at the  
101 rear of the sample. The original problem statement can be found, e.g., in [31] or [32]. In both cases, it is limited to  
102 a infinitesimal pulse generating an initial nonuniform temperature profile. PULsE allows an additional finite-pulse  
103 correction based on the experimental pulse diode data.

104 The boundary problem considered in PULsE is:

$$\frac{\partial \theta}{\partial \text{Fo}} = \frac{\partial^2 \theta}{\partial y^2} + \Phi(\text{Fo})\Psi(y), \quad (1a)$$

$$\left. \frac{\partial \theta}{\partial y} \right|_{y=0} = \text{Bi} \cdot \theta \Big|_{y=0}, \quad (1b)$$

$$\left. \frac{\partial \theta}{\partial (-y)} \right|_{y=1} = \text{Bi} \cdot \theta \Big|_{y=1}, \quad (1c)$$

$$\theta(y, 0) = 0, \quad (1d)$$

105 written for dimensionless heating  $\theta$ , time  $\text{Fo}$  and axial coordinate  $y$  (for the definition of these variables, the reader  
 106 is referred to [33]). In this formulation, both radiative and gas-driven heat losses are linear and sum up to the Biot  
 107 number,  $\text{Bi}$ . The volumetric energy density  $\Psi(y)$  absorbed by the sample may be derived from the Beer-Lambert law  
 108 and the continuity equation, yielding  $\Psi(y) \propto \gamma \exp(-\gamma y)$ , where the parameter  $\gamma$  is the laser absorptivity divided by  
 109 the sample thickness,  $l$ . Because temperature is measured in arbitrary units, the proportionality factor may be omitted.  
 110  $\Phi(\text{Fo})$  refers to a normalised pulse temporal shape. Following [31], the detector registers the sum of contributions  
 111 from a range of  $\theta(y)$  values:  $V \propto \int_0^1 \theta(y) \exp(-\gamma_1 y) dy$ , where  $\gamma_1$  is the absorptivity of thermal radiation.

112 Equation (1) is solved with a fully-implicit finite-difference solver based on the Thomas algorithm [33]. For a  
 113 given time step  $\tau$  and a grid spacing  $h$  this is  $O(h^2 + \tau)$  accurate. The solution has been benchmarked against Proteus  
 114 LFA Analysis where an analytical solution is implemented based on [32]. At  $\gamma_1^{-1} = 0$  and an infinitesimal pulse, both  
 115 models gave identical results when processing data from standard test samples. In the following calculations, it is  
 116 assumed that the absorption of the incoming (laser/light) and induced (thermal) radiation are equal:  $\gamma = \gamma_1$ . Example  
 117  $\theta(\text{Fo})$  solutions of Equation (1) are shown in Figure 1 at  $\gamma = 10$  and  $\gamma = \infty$ . An infinite value of  $\gamma$  corresponds to  
 118 a heat source localised at  $y = 0$ , which reduces to the standard model. The standard and the adiabatic models are  
 119 described in the Supplementary Material, Section S.1.

120 Another important point is the optimisation procedure needed to reverse-engineer the material thermal properties  
 121 from the measured time-temperature profiles. To avoid the influence of data outliers sometimes observed in the time-  
 122 temperature profile, the sum of absolute deviations, rather than sum of squared residuals, was used as an objective  
 123 function metric  $f$ :

$$f = \frac{1}{n_e - n_s} \sum_{i=n_s}^{n_e} \left| V(\tilde{t}_i) - \hat{\theta}(\tilde{t}_i) \right|, \quad (2)$$

124 where  $V(\tilde{t}_i)$  is a detector voltage value proportional to the rear-face heating measured at time  $\tilde{t}_i$ ;  $\hat{\theta}(\tilde{t}_i)$  is the scaled  
 125 solution of Equation (1) interpolated specifically at time  $\tilde{t}_i$  using natural cubic splines;  $n_s$  and  $n_e$  are the end points of  
 126 the search domain. Since the standard Levenberg-Marquardt algorithm only allows a least-squares objective function,  
 127 a BFGS/Wolfe nonlinear optimiser described in [33] was employed to handle  $f$ . A comparison of optimisation using  
 128 ordinary least-squares and absolute deviations is provided in the Supplementary Material, Section S.2.  
 129

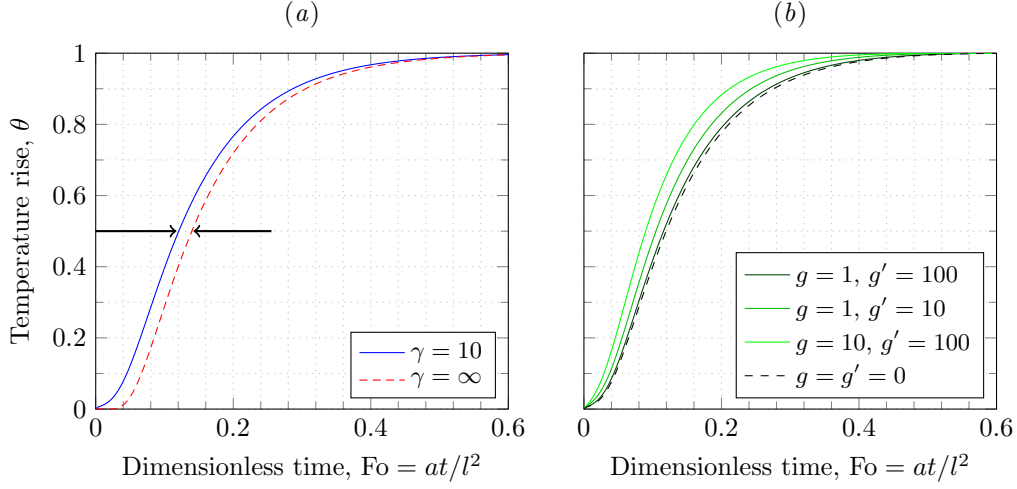


Figure 1: Dimensionless temperature rise curves  $\theta(\text{Fo})$  (a) for the model (1) calculated at  $\gamma = 10$  and  $\gamma = \infty$ , showing the accelerated temperature response at a finite  $\gamma$ ; (b) for the  $2T$  model at  $\gamma = 10$  in helium at various  $g, g'$  combinations.

130 At each test temperature, the thermal diffusivity value was averaged typically over five shots. The statistical error  
 131 was calculated assuming a 95% confidence level. Details on these calculations are provided in the Supplementary  
 132 Material, Section S.4.

### 133 2.5. Two-temperature ( $2T$ ) model

134 The experimental conditions described in Section 2.1 imply that heat is non-uniformly absorbed in the porous  
 135 body. The solid phase absorbs most of the incoming flash energy. Consequently, it responds to the heating faster  
 136 than the gas phase. This produces a temperature difference ( $T^{(s)} - T^{(g)}$ ) between the solid and the gas phase. When  
 137 energy exchange  $g$  between these two systems is negligible, the problem statement (1) holds. When this condition  
 138 is not met, an additional coupling term  $G(T^{(g)} - T^{(s)})$  needs to be introduced into the heat equation, viz. [34]. The  
 139 two-temperature model in porous solids has been used previously e.g. in [23, 35].

140 It is convenient to introduce short-hand notations:  $u_t = \partial u / \partial t$  and  $u_{tt} = \partial^2 u / \partial t^2$ . The heat equation in (1) is  
 141 modified by introducing the coupling term:

$$142 \quad \theta_{\text{Fo}}^{(s)} = \theta_{yy}^{(s)} + \Phi(\text{Fo})\Psi(y) + g(\theta^{(g)} - \theta^{(s)}), \quad (3)$$

143 where  $g = Gl^2 / [(1 - \varepsilon)\lambda^{(s)}]$  and the porosity  $\varepsilon$  is introduced.

144 Assuming no contribution from convection, the gas conduction follows the equation:

$$145 \quad \theta_{\text{Fo}}^{(g)} = \left( \frac{a_g}{a_s} \right) \theta_{yy}^{(s)} + g \left( \frac{1 - \varepsilon}{\varepsilon} \frac{C_p^{(s)} \rho^{(s)}}{C_p^{(g)} \rho^{(g)}} \right) (\theta^{(s)} - \theta^{(g)}), \quad (4)$$

146 where the quantities  $a_i$ ,  $C_p^i$  and  $\rho^i$  indicate the thermal diffusivity, specific heat and density of the phase  $i = (g), (s)$ .  
 147 The Fourier number in both Equation (3) and Equation (4) is defined as  $\text{Fo} = a_s t / l^2$ . The temperature scaling factor  
 148 is the same for both  $\theta^{(s)}$  and  $\theta^{(g)}$ :  $\theta^i = (T^i - T_0^i) / \delta T_{\text{Inf}}$  at  $i = (g), (s)$ .

149 Note the dimensionless equations (3) – (4) are very similar to the ones considered in [35]. Without going into  
 150 details of the pore arrangement, the model is solved numerically, assuming both phases ( $a$ ) are uniformly distributed  
 151 across the  $y$  axis and ( $b$ ) exchange heat with the static surroundings at their  $y = 0$  and  $y = 1$  external boundaries. This  
 152 gives rise to the boundary conditions of cooling viz. Equation (1). The finite-difference scheme for this model is given  
 153 in the Supplementary Material, Section S.6.

154 The model given by Equations (3) and (4) introduces two additional unknown parameters: the dimensionless  
 155 coupling coefficient  $g$  and the gas Biot number  $\text{Bi}_g$ . These parameters are determined from optimisation. Gas thermal  
 156 properties are assumed known. Indeed, the specific heat  $C_p^{(g)}$  may easily be calculated using the equation-of-state.  
 157 At the same time,  $\rho^{(g)}$  is more difficult to define. It depends on the pressure inside the pores, which may roughly  
 158 be deduced from the Laplace equation. It is not practical to try calculating this pressure with just the laser flash  
 159 experimental data. Instead, the coupling factor  $g' = (1 - \varepsilon) / \varepsilon [C_p^{(s)} \rho^{(s)}] / [C_p^{(g)} \rho^{(g)}]$  in (4) may be regarded as an  
 160 unknown parameter. Typically [35],  $g = 0.1 - 20$  and  $g' > g$ . An example calculation of  $\theta^{(s)}(\text{Fo})$  with the  $2T$  model  
 161 is shown in Figure 1 ( $b$ ). Compared to model (1), the  $2T$  model shows a similar shift of the half-time  $t_{1/2}$ . The onset  
 162 of heating seems to be less affected by the coupling term. Largest differences appear at the late heating stages. Here,  
 163 the temperature equilibration seems to lag behind the prediction of the unperturbed  $g = g' = 0$  solution. Interestingly,  
 164 Equations (3) and (4) may be combined, resulting in the so-called dual-phase lag (DPL) model [36]. There are other  
 165 variants of the DPL model including the Jeffreys type equation, criticised in [37, 38].

### 166 3. Results

#### 167 3.1. Al-Mg foams

168 Thermal diffusivity measurements of metal foams are conducted under two purge gas species and under dynamic  
 169 vacuum at temperatures  $T = 25 - 450$  °C. The variation of thermal parameters in metal foams with pore size at  
 170 constant porosity has recently been assessed in LFA experiments in [1]. At the same time, the impact of gas-mediated  
 171 heat transfer was not initially clear. Its influence on the diffusivity values is shown in Figure 2.

172 Thermal diffusivity was calculated with the model (1) based on the experimental time-temperature profiles in  
 173 two cases: ( $a$ ) when  $\gamma$  was allowed to vary and ( $b$ ) using  $\gamma$  values extracted from the computed tomography (CT)  
 174 data in [1]. A ray-casting algorithm was employed in [1] to evaluate the cross-sectional mean of the projected area  
 175 distribution function from CT scans. The axial dependence of the latter was used to fit  $A \exp(-\gamma y)$  as a function of  
 176 the dimensionless coordinate  $y$ . The “real”  $\gamma$  value characterising light attenuation and the  $\gamma$  value calculated as a  
 177 parameter to the heat conduction problem differ. Logically, this manifests in different  $a$  values determined using both  
 178 approaches. Table 1 shows an uncertainty in the  $\gamma$  determination may lead to qualitatively different conclusions on

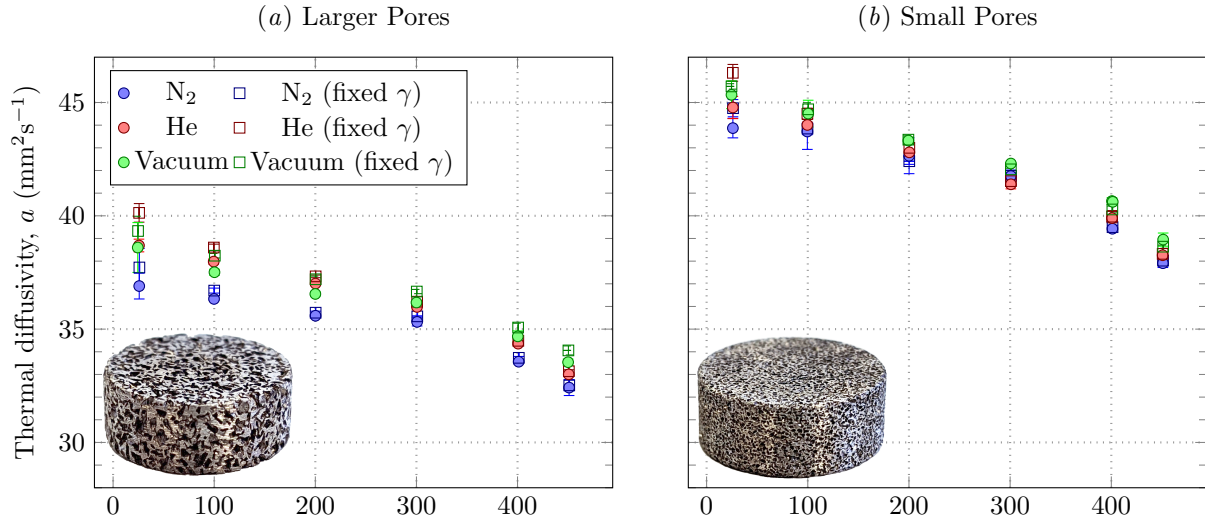


Figure 2: Apparent thermal diffusivity of Al-Mg foams measured in various gas environments. Two cases are considered:  $\gamma$  as an optimisation parameter; and a fixed  $\gamma$  corresponding to the rigorous CT-FEA modelling in [1]. Note that the “thermal diffusivity” measured under vacuum is slightly higher compared to both measurements under a gas environment. This indicates the simple analysis is inapplicable in case of metal foams.

179 the influence of gas. For instance, thermal diffusivity calculated in small-pored samples measured under helium may  
 180 either be lower or higher compared to vacuum measurements, depending on which way the  $\gamma$  value was derived. Still,  
 181 the measurements done under vacuum result in a higher thermal diffusivity value compared to nitrogen. This variation  
 182 cannot be explained consistently using the available effective-medium models, such as those used in [9]. The likely  
 183 reason for this discrepancy are the non-Fourier effects previously reported in [1].

184 For convenience, the thermal parameters extracted from room-temperature measurements of metal foam samples  
 185 under varying gas environment and microgeometry are summarised in Table 1. Additionally, Figure 3 shows example  
 186 room-temperature data and model solutions for samples with small pores. The span of the temperature transient may  
 187 be characterised by the time  $t_{1/2}$  required for the rear surface to reach half of the maximum temperature rise [39].  
 188 This quantity is affected by the heat losses [40]. The difference between using an adiabatic two-parameter pulse-  
 189 corrected model and the model (1) seems small when analysing the datasets displayed in Figure 3 (b) and (c). The  
 190 Biot number is small under nitrogen and near-zero under vacuum, thanks to the high conductivity of the sample and  
 191 short measurement times. The half-time values may also be affected by the solid-gas thermal coupling, as seen from  
 192 Figure 1 (b). This likely adds to the overdiffusive temperature behaviour in metal foams already observed under  
 193 vacuum.

194 The solutions obtained with the model (1) were in close agreement with the experimental datasets displayed in  
 195 Figure 3. Simpler models with fewer parameters including the adiabatic model and the standard model were also  
 196 considered (a detailed description may be found in the Supplementary Material, Section S.1). Unfortunately, these  
 197 models were judged unsuitable for data processing, especially in samples with large pores, based on a statistical

Table 1: Mean values of thermal properties calculated by averaging over a series of five measurements in metal foams with large and small pores at room temperature under different gas environments. The full version of this table may be found in the Supplementary Materials, Table S2.

Parameter	Large pores (0.40 - 1.00 mm)			Small pores (0.20 - 0.35 mm)		
	He	N <sub>2</sub>	Vacuum	He	N <sub>2</sub>	Vacuum
$t_{1/2}$ (s)	$0.077 \pm 0.002$	$0.086 \pm 0.001$	$0.084 \pm 0.004$	$0.072 \pm 0.001$	$0.0765 \pm 0.002$	$0.0749 \pm 0.0008$
$a$ (mm <sup>2</sup> s <sup>-1</sup> )	[1] <b><math>38.69 \pm 0.28</math></b>	$36.90 \pm 0.60$	$38.30 \pm 0.90$	$44.72 \pm 0.33$	$43.90 \pm 0.40$	<b><math>45.30 \pm 0.60</math></b>
	[2] <b><math>40.13 \pm 0.41</math></b>	$37.72 \pm 0.84$	$39.33 \pm 0.65$	<b><math>46.31 \pm 0.37</math></b>	$44.75 \pm 0.38$	$45.71 \pm 0.12$
$\gamma$	[1] $13.18 \pm 0.36$	$13.60 \pm 1.10$	$13.90 \pm 1.30$	$25 \pm 2$	$23 \pm 4$	$30 \pm 20$
	[2] $16.45$			$39.8$		
Bi	[1] $0.074 \pm 0.008$	$0.025 \pm 0.005$	$0.007 \pm 0.008$	$0.084 \pm 0.007$	$0.013 \pm 0.009$	$0.003 \pm 0.004$

[1]  $\gamma$  as an optimisation parameter

[2]  $\gamma$  derived from the absorption profile in [1]

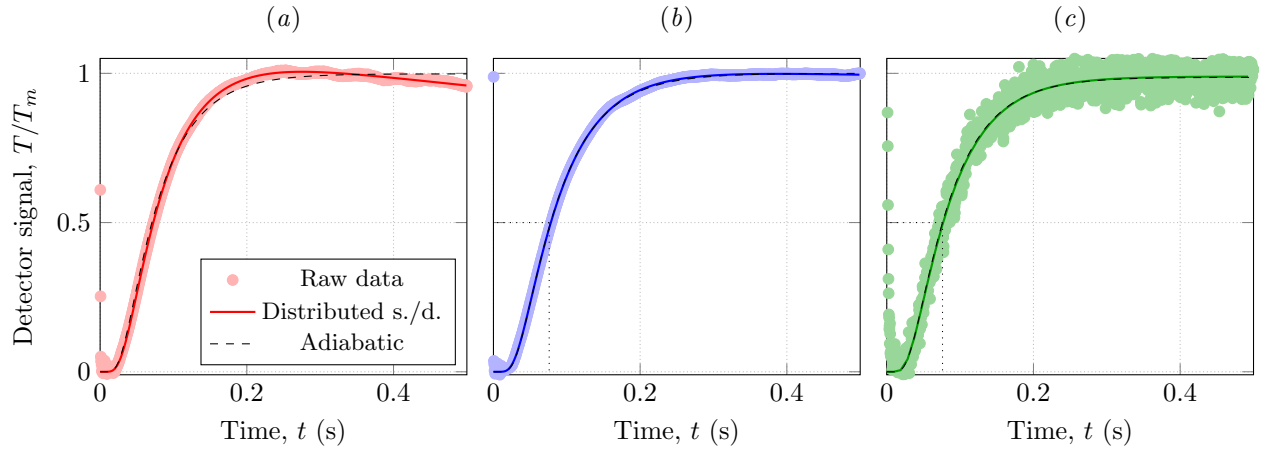


Figure 3: Baseline-subtracted time-temperature profiles showing raw data (markers) and model solutions (solid lines) at room temperature in Al-Mg foams (small pores). Measurements done under (a) helium, (b) nitrogen and (c) vacuum. Curves calculated with the classical adiabatic, pulse-corrected model ( $\gamma^{-1} \equiv 0$ ,  $\text{Bi} \equiv 0$ ) are shown in black dashed lines.

198 comparison. Details on model selection are presented in the Supplementary Material, Table S1 and in Section S.3.  
199 Overall, the model (1) seemed to produce a much better fit. The reason for this was, again, the additional parameter,  
200  $\gamma$ . The latter is usually optimised simultaneously with  $a$ ,  $Bi$  and  $T_{Inf}$ . When this approach was taken, a small variation  
201 in  $\gamma$  could be registered, see Table 1. This variation was difficult to detect in case of metal foams due to its low  
202 magnitude. The variation in the “effective”  $\gamma$  depending on the gas species was also lower compared to the difference  
203 between the “true”  $\gamma$  values determined from the light absorption profile and the average “effective”  $\gamma$ . This difference  
204 likely comes from the influence of the microgeometry [1]. At the same time, the small variations in the “effective”  $\gamma$   
205 are correlated with the gas carrier. In metal foams, a lower  $\gamma$  value seems to be characteristic of a more conductive  
206 carrier gas, in this case, helium.

207 The signal-to-noise data is seen to decrease under vacuum, see Figure 3 (c), when there is no coolant gas necessary  
208 for efficient temperature manoeuvring at or slightly above ambient temperature. Therefore, small random temperature  
209 fluctuations appear. At the same time, the laser heating in a sample without a high-emissivity coating is also small.  
210 Therefore, the raw data displays high noise. This noise does not pose any problems to the optimisation procedure.  
211 The latter was shown to be stable to both Gaussian and Laplacian noise of various magnitudes (see Supplementary  
212 Material, Section S.5). Finally, it should be noted that, under helium, a direct contribution from either convection or  
213 gas conduction results in a pronounced cooling segment, see Figure 3 (a).

214 Summing up the above, in metal foam samples, a change in the gas carrier species in LFA measurements promotes  
215 a lagging temperature response. This affects the thermal diffusivity value,  $a$ . Variations in the thermal diffusivity of  
216 metal foams under different gases cannot be consistently explained with the effective-medium models considered  
217 earlier.

### 218 3.2. *Ytong*

219 Lightweight concrete samples were measured under a gas flow (nitrogen and helium), under vacuum and under  
220 a static nitrogen atmosphere at test temperatures  $T = 25 - 120$  °C. Such measurements require very long acquisition  
221 times due to low thermal diffusivity values and a thick sample. To ensure accurate results, temperature should be very  
222 stable over an extended period of time. This is difficult to achieve under a static nitrogen atmosphere or under vacuum  
223 (both measurements done in LFA 457, as opposed to measurements under a gas flow done in LFA 467). In most  
224 cases, a strong linear drift in the baseline detector signal could easily be corrected for. However, when measurements  
225 required particularly long acquisition times, random deviations from this trend were observed. Obviously, the purge  
226 gas also acts as a coolant for the heater and ensures smooth temperature manoeuvring at low temperatures when  
227 radiation cooling is ineffective. When the chamber pressure drops or when no gas flow is maintained, temperature  
228 equilibration is made more difficult. This explains the error margin in measurements under vacuum or under a static  
229 atmosphere shown in Figure 4. As Ytong samples crumble if an excessive load is applied, extra care was taken to  
230 preserve the integrity of the samples.

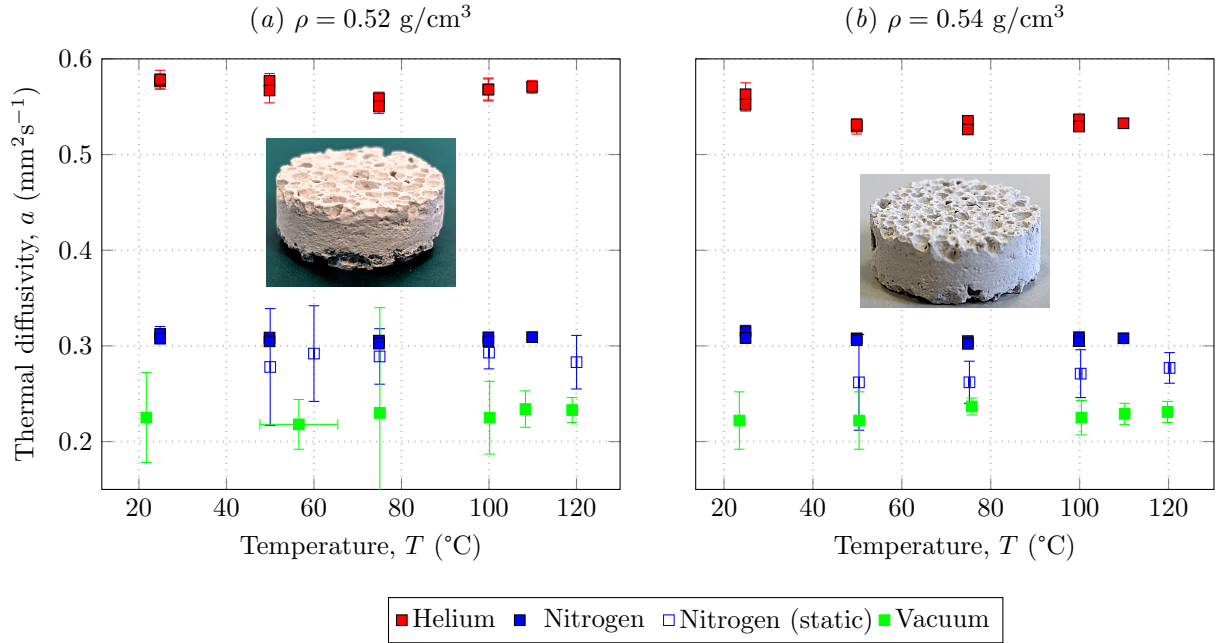


Figure 4: Apparent thermal diffusivity of Ytong lightweight concrete samples measured under various gas environments. At each test temperature for the datasets corresponding to helium and nitrogen flow, two markers are plotted indicative to the measurements done respectively during the heating and cooling stages.

231 The measurement results indicate that any change in atmosphere severely affects the magnitude of thermal diffu-  
 232 sivity in Ytong. In helium, Ytong appears more conductive whereas nitrogen results in temperature transients twice as  
 233 long (Figure 5). At the same time, the apparent thermal diffusivity of Ytong samples under both gases is significantly  
 234 higher than under vacuum.

235 The values of the model parameter  $\gamma$  estimated under various gas environments show a peculiar trend. The cal-  
 236 culated  $\gamma$  values in Ytong are strongly dependent on the gas species (Table 2). Unlike metal foams, Ytong displays a  
 237 larger  $\gamma$  value in helium and the lowest  $\gamma$  value under vacuum. This is reproducible in both samples. Lower  $\gamma$  values  
 238 indicate a sharper initial onset of the curves, which is observed in Figure 5. It is unlikely that any of the gases could  
 239 significantly affect light penetration within the sample volume. An attempt was made to explain this discrepancy us-  
 240 ing the two-temperature model. To allow realistic estimates, these parameter values were fixed:  $\gamma = 9.8$  and  $a = 0.23$   
 241  $\text{mm}^2\text{s}^{-1}$ . Additionally,  $g$  and  $g'$  were optimised. The results of this calculation are shown in Figure 6. A fair agree-  
 242 ment between the raw data and the model solution was observed under nitrogen. This likely indicates the variation in  
 243 the effective thermal diffusivity observed in Figure 4 might be explained by the coupled conduction in the solid and  
 244 the gas phase. In case of helium, the solution appears significantly different from the trends displayed by the raw data.  
 245 This has led us to believe that the  $2T$  model might either be not fully applicable or an unknown contribution appears.

246 As opposed to the considerably higher conductive metal foams, Ytong displays significant heat losses, see Figure 5  
 247 and Table 2. The Biot number, which should be representative of either radiative or gas-mediated cooling, is very high

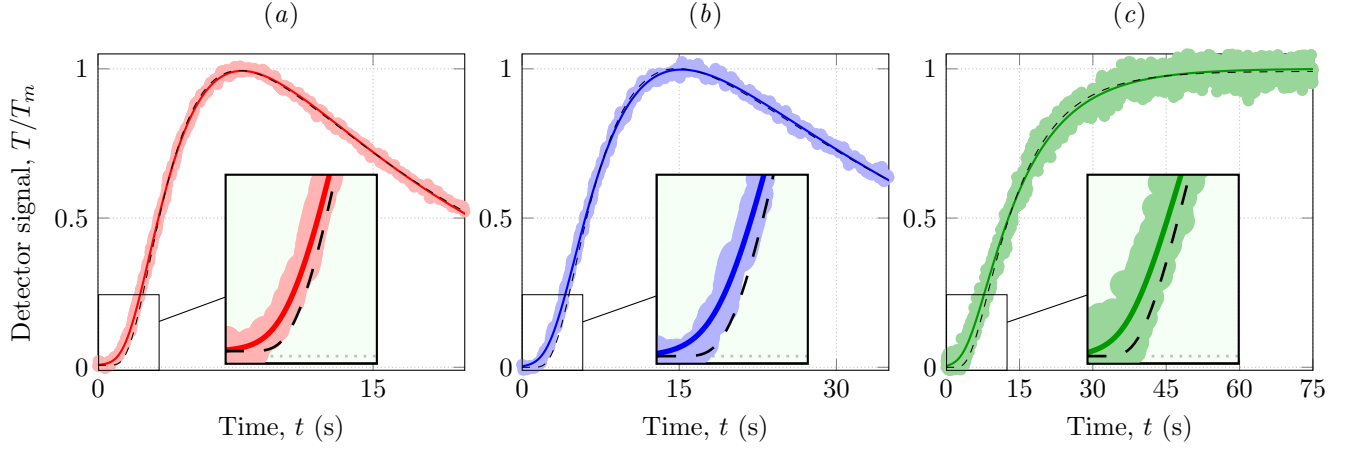


Figure 5: Baseline-subtracted time-temperature profiles showing raw data (markers) and model solutions (solid lines) at room temperature in Ytong ( $\rho = 0.54 \text{ g/cm}^3$ ). Data is shown from measurements done under (a) helium, (b) nitrogen and (c) vacuum. The model solutions correspond to the following Biot values in Equation (1): (a) 2.12, (b) 1.68 and (c)  $\simeq 0$ . To illustrate the difference between Equation (1) and a model where the heat source is localised at front surface, results of a constrained calculation with a zero distributed heat source ( $\gamma^{-1} \equiv 0$ ) are shown in black dashed lines.

Table 2: Mean values of thermal properties calculated by averaging over a series of five measurements in Ytong ( $\rho = 0.52 \text{ g/cm}^3$ ) at  $T_0 = 21\text{-}50 \text{ }^\circ\text{C}$  under various gas environments. The full version of this table may be found in the Supplementary Materials, Table S3.

Parameter	Gas environment			
	He	N <sub>2</sub> (dynamic)	N <sub>2</sub> (static)	Vacuum
$T_0$ ( $^\circ\text{C}$ )	24.85	24.85	$50.0 \pm 0.1$	$21.2 \pm 0.7$
$a$ ( $\text{mm}^2 \text{ s}^{-1}$ )	$0.576 \pm 0.008$	$0.312 \pm 0.008$	$0.28 \pm 0.06$	$0.23 \pm 0.05$
$\gamma$	$11.27 \pm 0.22$	$10.4 \pm 0.3$	$9.8 \pm 1.2$	$9.7 \pm 4.8$
Bi	$2.17 \pm 0.07$	$1.63 \pm 0.11$	$1.23 \pm 0.8$	0

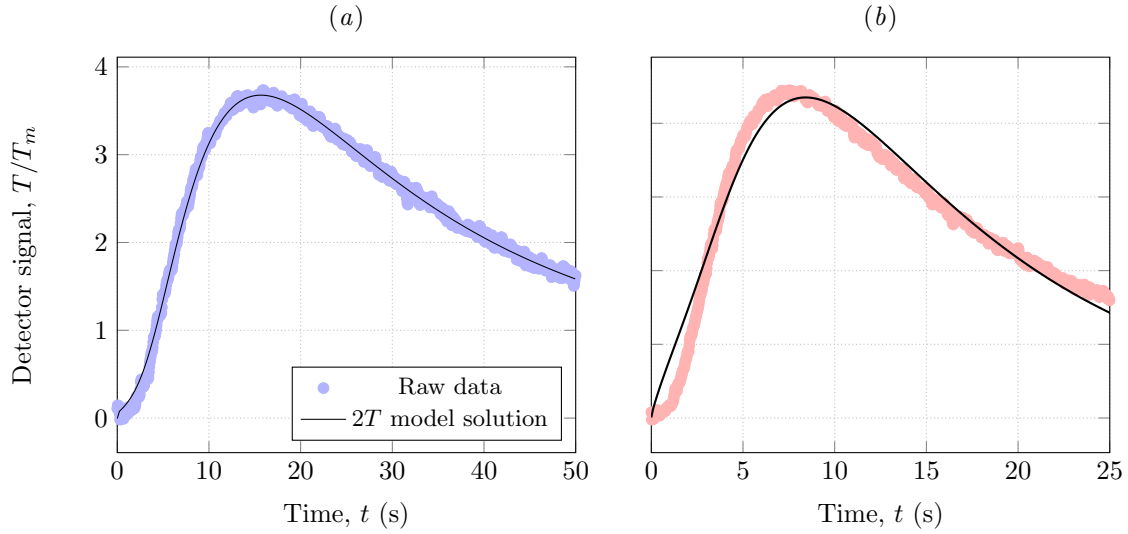


Figure 6: Raw data and optimised solutions with the two-temperature model (3) – (4) corresponding to measurements under (a) nitrogen ( $g = 1.22$  and  $g' = 0.9657$ ) and (b) helium ( $g = 19.74$  and  $g' = 1 \times 10^4$ ).

248 at room temperatures under a gas flow, reaching values of up to 2.12. At the same time, it is much lower – almost zero  
 249 – under vacuum. This means that the cooling segment in Figure 5 (a) and (b) is exclusively associated with the gas  
 250 environment. Since the temperature maximum is reached after about 90 s as compared to about 15 s in helium, heat  
 251 transfer in the gas phase within this sample volume may actually be more efficient than conduction.

252 Another important point is that the time-temperature profiles in all cases could still be described by Equation (1)  
 253 quite well, showing no significant abnormality in the residual distribution. However, despite the fit being good, this  
 254 does not mean that the model is correct. One of the key factors producing shorter temperature transients in a Ytong  
 255 sample placed in a gas environment seems to be the coupling between solid-state thermal conduction, convection and  
 256 gas-phase conduction.

#### 257 4. Discussion

258 The observations made in this work fall in two categories:

- 259 (a) Relating to the apparent thermal diffusivity of porous solids depending on the gas species. The increase is more  
 260 pronounced in lighter, more conductive gases;
- 261 (b) Relating to a deviation from the expected behaviour of the heating curve modelled using eq. (1), when  $\gamma$  is  
 262 representative of light absorption.

263 The term “apparent” thermal diffusivity is used to highlight that the parameter,  $a$ , responds to the way measure-  
 264 ments are conducted. Not always  $a$  is representative of the material under study (even in the sense of an effective  
 265 medium).

266 First, consider the thermal diffusivity of metal foams. Note that diffusivity will change if the sample surface  
267 is made opaque. The range of diffusivity values reported in [1] for the small-pored samples under nitrogen is 36-  
268  $42 \text{ mm}^2\text{s}^{-1}$ . Lower values are obtained when the heat propagation path,  $l$ , is taken equal to the sample thickness.  
269 A longer thermal diffusion path in porous solids is characterised by their tortuosity. On the other hand, there is an  
270 advantage of measuring samples with open porosity located at the external surface. Namely, model calculations using  
271 Equation (1) do not need to explicitly account for the difference between the geodesic and the Euclidean paths. This is  
272 explained in more detail in [1]. However, when the samples are made opaque, accounting for tortuosity requires using  
273  $l$  equal to the geodesic distance. If  $l$  is taken as the Euclidean distance, lower thermal diffusivity values are obtained.  
274 When conducting measurements in samples with open porosity, the value of the thermal diffusivity is influenced by  $\gamma$ ,  
275 the mean absorption depth in the Beer-Lambert law. It may be argued that  $\gamma$  may only be accurately determined when  
276 the real absorption profile is known. Therefore, measurements with sealed surface pores (e.g. in [9] and in the second  
277 part of [1]) and open surface porosity reported in this work require additional information. This information may be  
278 extracted from computed tomography (CT).

279 At the same time, even knowing the precise light absorption depth or the tortuosity of the material, determining  
280 the thermal diffusivity,  $a$ , remains challenging. There are fundamental reasons behind this difficulty. Porous samples  
281 require adjustments to the macroscopic Fourier law, as explained in [1]. Another reason is the coupling between solid  
282 conduction with either gas conduction, gas convection, or both. The two-temperature model [Equations (3) and (4)]  
283 offers a way to explain the difference in the apparent thermal diffusivity caused by the gas species by coupling the heat  
284 equation of the solid phase with the respective equation for the gas phase. Note that the same model is expected to  
285 hold in phase-change materials during the formation of the mushy regions, where a solid and a liquid phase co-exist.  
286 At the same time, the deviation of the model solution shown in Figure 6 from the raw data suggests there is a missing  
287 factor in the explanation. This points to the possible role of convection. Alternatively, this might be due to purely  
288 geometric reasons [35].

289 Given the above, it is possible that accounting for convection may be necessary to correctly describe the tem-  
290 perature transients in the laser flash experiments. Convection normally gives rise to an additional term in Equa-  
291 tion (4), called the advective term [35]. Additionally, convection is usually characterised by the Rayleigh-Darcy  
292 number  $\text{Ra} = gk\Delta TL/(va_gT_0)$ , where  $g$  is the gravitational acceleration and  $k$  is the permeability of the matrix. Unfor-  
293 tunately, the latter cannot be quantified from the experimental time-temperature profiles directly. Another parameter,  
294 the Biot number  $\text{Bi} = h\lambda/L$ , is directly inferred from the measurements. It can be thought of as the ratio between the  
295 resistance to conduction  $\lambda/L$  and resistance to convection  $h^{-1}$ . In the previous section, Bi was calculated assuming  
296 the gas simply drives away heat from the sample surface to the external volume.

297 Convection is expected to influence measurement results due to the geometric arrangement of the laser source  
298 relative to the sample. In a conventional LFA setup, the sample is arranged vertically, and its bottom part is heated up  
299 by the flash. A porous sample in a gas environment is effectively a composite material made of the solid matrix and  
300 the gas inside the pores. Following the flash, an energy exchange between the solid and the gas leads to a temperature

301 increase in the lower parts of the gas sub-system. Colder, and therefore denser, gas portions experience a stronger  
 302 gravitational pull than the rarefied hot gas as the bottom. This creates conditions for a convective flow. The convective  
 303 contribution to heat transfer may be estimated based on the formalism provided by Soboleva [41]. In case of one-  
 304 dimensional heat transfer, the following governing equation of heat transfer applies (here the time derivative of mean  
 305 pressure  $dP/dt$  is assumed zero):

$$306 \quad [(1 - \phi)\rho_m C_m + \phi\rho_g C_g] \frac{\partial T}{\partial t} = \frac{K_0}{\text{RePr}} \lambda' \frac{\partial^2 T}{\partial x^2} - \phi\rho_g C_m \left( u \frac{\partial T}{\partial x} \right), \quad (5)$$

307 where  $\rho_g$  and  $C_g$  are the density and heat capacity of the gas at constant pressure,  $\rho_m$  and  $C_m$  are the corresponding  
 308 quantities in the solid matrix,  $\phi$  is the porosity value and  $u$  is the gas axial filtration velocity. Additionally,  $K_0 \simeq 1$  is a  
 309 constant defined in [41], Re and Pr are the Reynolds and Prandtl numbers,  $\lambda' = (1 - \phi)\lambda_m + \phi\lambda_g$ .

310 Therefore, the convective contributions could present a significant problem in the quantification of thermal diffu-  
 311 sivity in porous materials. Another possibility is forced convection. Since, at low temperature, the heat losses under  
 312 vacuum are near-zero, the Biot numbers calculated by solving the inverse problem in Equation (1) could be repre-  
 313 sentative of convective heat transfer either by forced or natural convection. The impact of forced convection on the  
 314 thermal diffusivity measurements results in generally lower values, see Figure 4. At the same time, the error margin  
 315 is too high to draw a definitive conclusion on this part. Regardless, since the gas flow rate is adjustable, it can be  
 316 decreased to minimise forced convection.

## 317 5. Conclusions

318 Measuring thermal properties in highly-porous solids with the flash method remains problematic. Even under vac-  
 319 uum, the complex microgeometry of porous materials manifests in the experimental temperature transients deviating  
 320 from the expected model behaviour. This odd behaviour appears irrespective of whether external pores are open or  
 321 blocked. When measurements are conducted under a gas environment, the gas infiltrates the open pores (if any are  
 322 accessible) and participates in the transient heat transfer caused by the thermal flash. When a model accounting only  
 323 for solid conduction is used to describe the transients, its intrinsic parameter and the “measurement” result, the ther-  
 324 mal diffusivity  $a$ , stops being representative of just the solid material. Despite previous claims, the thermal diffusivity  
 325 extracted from this model may not even be representative of the solid-gas mixture. This is caused by the non-linear  
 326 terms in the coupled heat equation. An attempt was made to account for this nonlinearity using a simplified two-  
 327 temperature model of coupled solid and gas conduction. Unfortunately, this model also produced solutions deviating  
 328 from the experimental time-temperature profiles. This suggests two possibilities. Either convection should be ac-  
 329 counted for during measurements of highly-porous solids — or the microgeometry of the pores needs to be explicitly  
 330 accounted for in the heat equation. It is hoped that future work might address these possibilities.

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