

Unlocking the power of unstructured Isogeometric Analysis: a unified framework and some applications to wave propagation and elasticity

Hélène Barucq, Henri Calandra, Julien Diaz, Stefano Frambati

▶ To cite this version:

Hélène Barucq, Henri Calandra, Julien Diaz, Stefano Frambati. Unlocking the power of unstructured Isogeometric Analysis: a unified framework and some applications to wave propagation and elasticity. IX International Conference on Isogeometric Analysis, Sep 2021, Lyon, France. hal-03520492

HAL Id: hal-03520492

https://hal.science/hal-03520492

Submitted on 11 Jan 2022

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Unlocking the power of unstructured Isogeometric Analysis: a unified framework and some applications to wave propagation and elasticity.

H. Barucq*, J. Diaz*, H. Calandra† and S. Frambati*†

* Project-Team Makutu, Inria, E2S UPPA, CNRS Avenue de l'Université, 64012 Pau, France e-mail: [helene.barucq;julien.diaz;stefano.frambati]@inria.fr

† TotalEnergies S.E. R&D, Centre Scientifique Jean Féger, Avenue Larribau, 64018 Pau, France Email: [henri.calandra;stefano.frambati]@totalenergies.com

ABSTRACT

Isogeometric Analysis (IGA) [1] is enjoying a prosperous career in numerical analysis, having been applied with success to many engineering applications and for the solution of many types of partial differential equations. Based on the use of B-splines and NURBS functions as basis for the Finite Elements Method (FEM), its numerical advantages include an almost perfect representation of the problem geometry, less numerical noise and dispersion, longer simulation timesteps and better stability, among others. In two or more dimensions, multivariate bases are usually obtained via a simple tensor product. This approach, convenient in engineering, is impractical for applications where no Computer Aided Design (CAD) model is available and the problem topology is complex and/or unknown, limiting the penetration of the technology in fields outside engineering, such as geophysics.

Recently, some mathematical results on unstructured spline functions [3, 4, 5] have led to an alternative approach where splines are based on general point clouds. Using these functions as basis for isogeometric analysis allows to simulate a domain with arbitrary topology, including general boundary conditions. Moreover, suitable point repetition allows to reproduce the usual FEM and Discontinuous Galerkin (DG) bases, allowing the natural blending of these schemes in the same simulation, as well as a generalized multi-patch IGA-DG hybrid scheme. Some preliminary results of this method and its application to 2D wave propagation have been first presented in [6].

In our work, we explore the foundations of this method, and especially its relationship with traditional FEM/DG mesh-based approaches and the usual (tensor-product) IGA. The naturalness of our unified point of view allows us to draw some direct, simple connections between these schemes, helping shed some light on a few numerical properties that have made the success of the IGA method. We briefly discuss the numerical advantages and disadvantages of our approach in two applications: 2D and 3D wave propagation and 2D hyperelasticity. For wave propagation, we focus on the Courant–Friedrichs–Lewy timestep constraint and the shape of the mass matrix, in view of highly-parallel applications. For elasticity, we explore the advantages coming from the lack of a fixed mesh in systems subject to large amounts of deformation. Finally, we discuss some possible ways forward and avenues of improvement that could turn our approach into a true general-purpose unstructured multi patch DG-IGA scheme.

REFERENCES

- [1] J. A. Cottrell, T. J. Hughes, and Y. Bazilevs. "Isogeometric analysis: toward integration of CAD and FEA". John Wiley & Sons, 2009.
- [2] M. Neamtu. "Delaunay configurations and multivariate splines: A generalization of a result of B.N. Delaunay", Transactions of the AMS., 359(7), pp.2993-3004.
- [3] Y. Liu and J. Snoeyink. "Quadratic and cubic B-splines by generalizing higher-order Voronoi diagrams". 23rd annual symposium on Comp. Geom.. ACM. 2007, pp. 150–157.
- [4] H. Barucq, H. Calandra, J. Diaz, and S. Frambati, "Polynomial-reproducing spline spaces from fine zonotopal tilings", arXiv preprint arXiv:2006.10307 (2020), under review for publication.
- [5] H. Barucq, J. Diaz, H. Calandra, S. Frambati, "Unstructured multi-patch DG-IGA formulation for wave propagation", WCCM-ECCOMAS 2020 congress, Jan 2021.