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Nicolò R Sgreva, Anna Massmeyer, Anne Davaille. Inferring the rheology of the crust from the uplift observed above the Altiplano-Puna Magma Body. *Geophysical Journal International*, 2022, 10.1093/gji/ggac258 . hal-03518450

HAL Id: hal-03518450

<https://hal.science/hal-03518450>

Submitted on 9 Jan 2022

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Inferring the rheology of the crust from the uplift observed above the Altiplano-Puna Magma Body

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Abstract

Geophysical imaging techniques together with numerical models have shown that the surface uplift measured above the Altiplano-Puna Magma Body (APMB) can be resolved by the presence and propagation of a diapir from the top of the APMB itself. In this work we interpret deformations that characterize the crustal region above and around APMB through the employment of a viscoplastic type rheology. That is, we assume that at large scale the ductile lower-middle crust that surround the magmatic mush behaves as yield-stress fluid described by a Herschel-Bulkley (HB) model. In this scenario, the main critical conditions needed for the growth and the subsequent rise of the diapir are: (1) the ratio between yield stress and viscous stresses, namely the Bingham number Bi , has to be less than 1, i.e. $Bi \leq 1$; and (2) the ratio between buoyancy stresses and yield stress, namely the inverse of the Yield number $Y_{inv}=Y^{-1}$, has to be larger than a critical value, i.e. $Y_{inv} > Y_{invC}$. By using these critical conditions we infer the bulk

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rheological properties of the heterogeneous lower-middle crust above APMB. We estimate the yield stress of the crust in between 0.5-15 MPa. For a crust that allows the development and the emerge of a 10 to 100 km wide diapir, the coupling of this range of yield stress with the regional uplift velocity measured at the surface allows to estimate a critical strain rate of $\sim 10^{-15}$ - 10^{-16} s^{-1} and a maximum bulk effective viscosity of the lower-middle crust of $\eta_c = 10^{21} \text{ Pa s}$.

Keywords: Rheology: crust and lithosphere, APMB, Diapirism, Yield stress, Viscoplastic

1. Introduction

The Altiplano-Puna Magma Body (APMB) is a mid-crustal magmatic system located at ~ 20 km beneath the Altiplano-Puna Volcanic Complex (APVC) in the central Andes, South America. It represents the largest active, continental magma body in Earth's crust (Zandt et al., 2003) and is considered to be directly related to an uplifting region, centered on the western slope of Uturuncu volcano, and its peripheral subsidence zone (Fig. 1) (Fialko and Pearse, 2012). The entire APMB can be represented as a complex transcrustal magmatic structure, that is a large environment volumetrically dominated by crystal mush (Cashman et al., 2017; Pritchard et al., 2018). Given its impact to the region, a good description of its dynamics becomes crucial to understand both its mobility, lifetime, internal structure (e.g. Massol and Jaupart, 2009; Gonnermann and Manga, 2007; Caricchi et al., 2007; Turner and Costa, 2007) and the role that such an enormous ($\sim 5 \times 10^5 \text{ km}^3$, Ward et al. (2014)) magmatic structure can play on the deformation of the

16 overlying crust.

17 However, to constrain the mush dynamics beneath APVC and the thermo-
18 mechanical response of the surrounding region, a number of geometrical and
19 physical properties of both APMB and lower-middle crust are required. Some
20 of them have been constrained in recent years by using different geophysical
21 investigation methods. For instance, by combining seismic tomography and
22 3D-model inversion to evaluate the crustal 3D shear-wave velocity field, Ward
23 et al. (2014) displayed a very large ($\sim 5 \times 10^5 \text{ km}^3$) low seismic velocity (LSV)
24 zone at a depth of 4-25 km beneath the APVC. This region is interpreted
25 as an hotter zone compared to the surrounding material, and may also be
26 enriched in melt content. A similar broad LSV zone centered below the
27 Uturuncu volcano and at ~ 15 km below sea level has been revealed also by
28 other authors (e.g. Zandt et al., 2003; Chmielowski et al., 1999). However,
29 due to the resolution of seismic tomography that is not better than 1 km
30 (Cashman et al., 2017), the exact geometry and position of this hot body are
31 still debated. This is caused by the difficulty in constraining the spacial melt
32 distribution with the technique, which is not always able to recognize large
33 melt bodies even in regions that are active nowadays or have produced large
34 eruptions in the Quaternary (Cashman et al., 2017).

35 Besides seismic tomography, other geophysical imaging techniques can
36 help to better characterize this anomalous structure. Magnetotelluric data
37 reveals a first large low electrical resistivity ($< 3 \text{ } \Omega\text{m}$) anomaly at ~ 15 km
38 below the sea level and a second ~ 10 -km-wide vertical anomaly on the top
39 of it (Fig. 1c) (Comeau et al., 2015, 2016). Differences in resistivity between
40 the two regions may be related to variations in the composition: while the

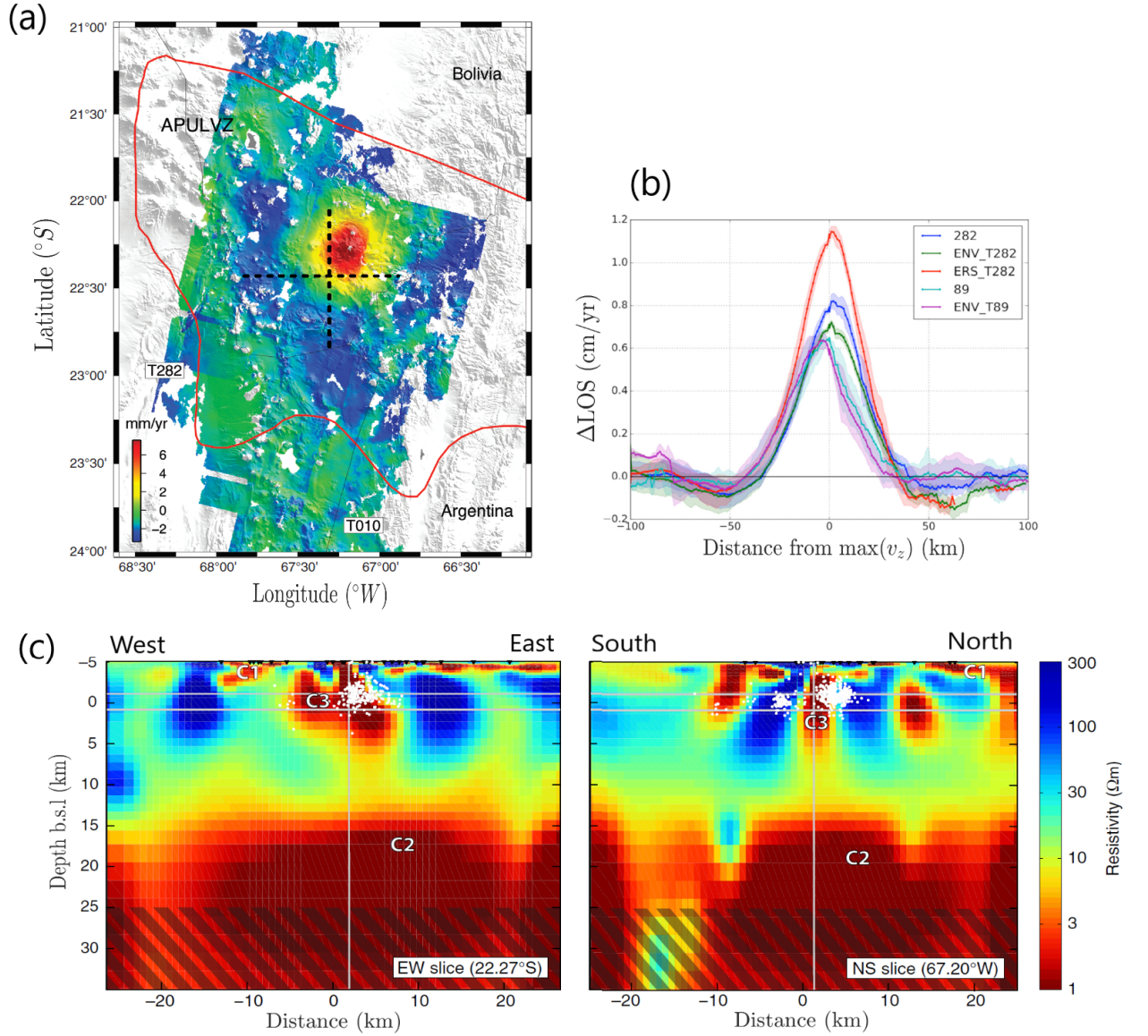


Figure 1: (a) Map view of the Altiplano-Puna region (Southern Bolivia). Colors indicate the elevation rate measured at the surface from InSAR data. Red line indicates the mid-crustal low-velocity zone associated to the APMB. Black dotted lines indicate the locations of cross sections in (c). Modified from Fialko and Pearse (2012). (b) Average velocities of line of sight (LOS) along sections crossing the center of the uplift. Modified from Gottsmann et al. (2017). (c) West-East and South-North vertical cross sections of the 3D resistivity model of (Comeau et al., 2015) across APVC. The main low electrical resistivity anomaly (C2) is associated to the APMB whereas the smaller anomaly on the top of it (C3) is interpreted as an ascent diapir. Modified from Comeau et al. (2016).

41 resistivity of the first deeper body ("C2" in Fig. 1c) can be explained by the
 42 presence of andesite melts in APMB (with a melt fraction $\phi_f > 0.15$), the
 43 resistivity of the region above it ("C3" in Fig. 1c) may reflect the presence of
 44 dacite melts combined with aqueous fluids (Comeau et al., 2016). A similar
 45 vertically elongated structure is revealed also by the inversion of Bouguer
 46 anomaly data that highlights a low density and ~ 15 -km-wide structure on
 47 the top of the APMB (del Potro et al., 2013), interpreted as an active diapiric
 48 ascent of magma (e.g. del Potro et al., 2013; Fialko and Pearce, 2012; Gotts-
 49 mann et al., 2017). The presence of a mid-crustal diapir which slowly moves
 50 upward is in agreement with geodesy data collected above APMB from 1995
 51 to 2010 (Fialko and Pearce, 2012). InSAR data show indeed a ~ 150 -km-wide
 52 region, centered on the western slope of Uturuncu volcano, which is uplifted
 53 at the rate of ~ 1 cm/yr, and surrounded by an approximately 30-km-wide
 54 ring of subsidence (Fig. 1a-b). The morphology and large extent of such a
 55 "sombbrero"-shaped deformation on the surface cannot be caused by a single
 56 large dike as expected for an intrusion in a merely elastic crust (Menand and
 57 Tait, 2001; Jellinek and DePaolo, 2003). But instead it matches well results
 58 of geodynamics models that assume the rise of a large diapir fed by partial
 59 melt from the APMB within a crust that is not-purely elastic (e.g. Fialko and
 60 Pearce, 2012; Gottsmann et al., 2017). Such a large diapir rising from the top
 61 of APMB would cause an extensive deformation of the whole crust, leading
 62 in turn to the displacement measured at the surface by geodesy techniques.

63 The interaction of the rising diapir with the crustal layer above offers
 64 the opportunity to estimate the effective rheology of the crust itself. The
 65 structure of the crust with its rheological properties and mechanical behavior

are indeed heavily influenced by the specific geodynamic context in which the crust is located (Burov, 2011). So the rheology can in fact deviate from the classical case where the whole deformation can be simply described by a purely elastic or a purely viscous model. Moreover, heterogeneities that characterize the crust on all scales, i.e. from small-scale (e.g. grain size, pore fluid pressure, chemical activities of mineral components, etc.) to large-scale (dikes filled with magma, faults, etc.), result in an intricate structure that can easily be locked or "jammed". Thus at the macroscopic scale, the crust bulk behavior could be comparable to that of a yield-stress material whereby flow can only occur when a threshold stress value (i.e. the yield stress, σ_y) is reached (Ancey, 2007; Bonn et al., 2017). Within this perspective, for an heterogeneous lower-middle crust an effective viscoplastic rheology can be claimed, making the yield stress a key aspect to better understand its bulk behavior.

In this paper we infer the rheological properties of the lower-middle crust below APVC from the rate of vertical surface displacement measured in the orogenic region of the Altiplano and by assuming that this uplift is caused by the rise of a diapir from above APMB. To do so we assume that the heterogeneous crust surrounding the diapir behaves as a non-Newtonian yield stress fluid, i.e. as a material whose bulk behavior can be described with a viscoplastic rheological model. In section 2 we introduce the main rheological properties of these materials. In section 3 we discuss the general critical conditions for motion of a buoyant body through an yield stress fluid. The latter are applied to the APMB case in section 4. We end by discussing the implications that our results have for a partially molten lower-middle crust.

91 2. The yield-stress in viscoplastic rheology

92 Viscoplastic fluids (synonym of yield stress fluids) are characterized by
 93 the presence of a yield stress, σ_y (Dinkgreve et al., 2017). A typical example
 94 of them is a suspension of particles in a liquid. When the particle volume
 95 fraction increases, the particles come into close contact, and the material
 96 can face jamming. In this jammed state, the material can support stresses
 97 without flowing. A so-called yield stress fluid does not flow unless the applied
 98 stresses are large enough to unjam the structure, but it does flow when
 99 the stresses become larger than σ_y . This introduces a non-linearity to the
 100 material rheology, with strong impact on its dynamics (Makse et al., 2005;
 101 Coussot, 2005; Barnes, 1995).

102 Simple yield stress fluids are those described by popular rheological mod-
 103 els such as the Bingham model or the Hershel-Bulkley (HB) model. The
 104 latter writes

$$\begin{aligned} \sigma &= \sigma_y + K_v \dot{\gamma}^n & \text{for} & \quad \sigma > \sigma_y \\ \dot{\gamma} &= 0 & \text{for} & \quad \sigma \leq \sigma_y \end{aligned} \tag{1}$$

105 where σ is the stress, $\dot{\gamma}$ the strain rate, K_v the consistency and n the
 106 power-law exponent. Note that the exponent n defined here is the reverse
 107 of the power law index usually used in equations for creep mechanisms in
 108 geophysics (e.g. in Ranalli, 1995). For $n < 1$ the fluid is shear thinning and
 109 the effective viscosity $\eta_{eff} = \sigma / \dot{\gamma}$ decreases as $\dot{\gamma}$ increases. For $n > 1$ the
 110 fluid is shear thickening. For $n=1$ and $\sigma_y > 0$ the HB model reduces to the

111 Bingham model and describes a fluid with a linear flow curve and constant
112 value of viscosity. And, finally, for $n=1$ and $\sigma_y=0$ the fluid is Newtonian.

113 The concepts of yield stress and plasticity are not only employed in the
114 rheology of viscoplastic fluids, but they are also largely used in solid mechan-
115 ics through the Coulomb plasticity theory. In Coulomb plasticity, plastic
116 deformation indicates the irreversible deformation of a sample under stress
117 whereas in Bingham viscoplasticity it refers to a solid-liquid transition. In
118 this latter case the yield stress becomes the limit between the elastic (or
119 viscoelastic) solid-like domain and the viscous fluid-like domain where the
120 material flows. Even though the definition of σ_y is not the same among the
121 two theories, the concept behind it relies to some overlapping phenomena:
122 the transition from a reversible to a non-reversible deformation on one side
123 and the not-flowing to flowing on the other side. Besides that, however, the
124 two theories show some differences on their theoretical formulation (Ancy, 2007).
125 The main one regards the description of material's deformation on a
126 macroscopic scale: a viscoplastic fluid behaves as a whole on the bulk scale,
127 i.e. as a one-phase homogeneous material (Coussot et al., 2009). Hence, it
128 only requires a single stress-strain constitutive equation, e.g. eq.(1), where
129 there is no need to separate the role of interstitial fluids from the one of
130 the solid phase. This strongly differs from a two-phases saturated Coulomb
131 material in which the two phases can move at different velocities and have
132 to be considered separately.

133 Throughout the rest of this article, we will always refer for the fluid
134 deformation to the rheological viscoplastic description. That is describing
135 both mush and hot crust as a single-phase incompressible fluid that behaves

136 as a viscous fluid once set in motion.

137 **3. Conditions for the ascent of a buoyant instability in a yield-** 138 **stress fluid**

139 When a yield stress fluid is heated the buoyancy stresses that originate
140 due to thermal expansion may not be large enough to exceed the fluid yield
141 stress. Motion is then prevented and the fluid remains at rest. On the other
142 hand, when local stresses are large enough, a thermal plume can develop
143 and rise within the fluid column. The plume dynamics has been investi-
144 gated experimentally for a simple yield stress fluid heated by a local heat
145 source by Davaille et al. (2013) (see Appendix A for details on experimen-
146 tal conditions). They found that the formation and subsequent growth of a
147 thermal instability can be described in three main stages: (1) a no-motion
148 phase where a hot pocket grows by thermal diffusion around the localized
149 heat source (Fig. 2a and Fig. 3). (2) A stage where slow creep takes place
150 within the growing hot pocket (Fig. 2b). This slow ascent can be observed
151 also in the spatio-temporal evolution shown in Fig. 3 where bright lines that
152 correspond to reflecting particles formed by Thermo-Liquid Crystals (TLCs)
153 are not longer horizontal but begin to move upward. This is because, starting
154 from this stage, the edge of the thermal pocket begins to empty slowly to
155 feed a creep confined around the heating element (Fig. 2c). However, during
156 this phase the fluid outside the hot pocket still remains unyielded. And (3)
157 the stage in which a hot finger rises upward (Fig. 4a). Here upwelling oc-
158 curs only within the thermal anomaly and shear is strongly localized along
159 plume boundaries (Fig. 4b). The fluid within the anomaly moves then as a

160 plug and the overall thermal shape looks more like a finger than the classical
 161 mushroom shape expected for Newtonian fluids.

162 For small Reynolds numbers, the flow resulting from the rising of the
 163 thermal instability can be parameterized by two key dimensionless numbers.
 164 The first is the Yield number, Y , and the second is the Bingham number, Bi
 165 (Davaille et al., 2013; Karimfazli et al., 2016; Massmeyer et al., 2013). For
 166 simplicity here we use the inverse of the Yield number, $Y_{inv} = 1/Y$, which
 167 represents the ratio between the buoyancy stress and the yield stress. It is
 168 usually written as

$$Y_{inv} = \frac{g\Delta\rho D}{3\sigma_y}. \quad (2)$$

169 where g is the acceleration due to gravity and $\Delta\rho$ the density difference
 170 between the hot body, described by a characteristic diameter D , and the
 171 ambient fluid. Y_{inv} has been firstly employed to evaluate motion of a single
 172 rigid sphere in Bingham fluid (Beris et al., 1985). In this case, the critical
 173 value of the (inverse) Yield number, Y_{inv_C} , below which the sphere does not
 174 move is $Y_{inv_C}=6.99$. It has been subsequently confirmed experimentally for
 175 simple HB fluids (Tabuteau et al., 2007) and for more heterogeneous HB
 176 fluids (Sgreva et al., 2020a). In the case of buoyant thermal instabilities
 177 instead of spheres, one can consider the hot pocket forming around the heat-
 178 ing source at stage (1) and (2) as a buoyant "entity" that tries to go up
 179 because it is less dense but is kept anchored at the original position by the
 180 fluid yield stress. Davaille et al. (2013) found that the thermal instability
 181 will rise only if $Y_{inv} > Y_{inv_C} = 8.8 \pm 0.7$, a value close to but different from
 182 the solid sphere case. This is expected given the different geometries and

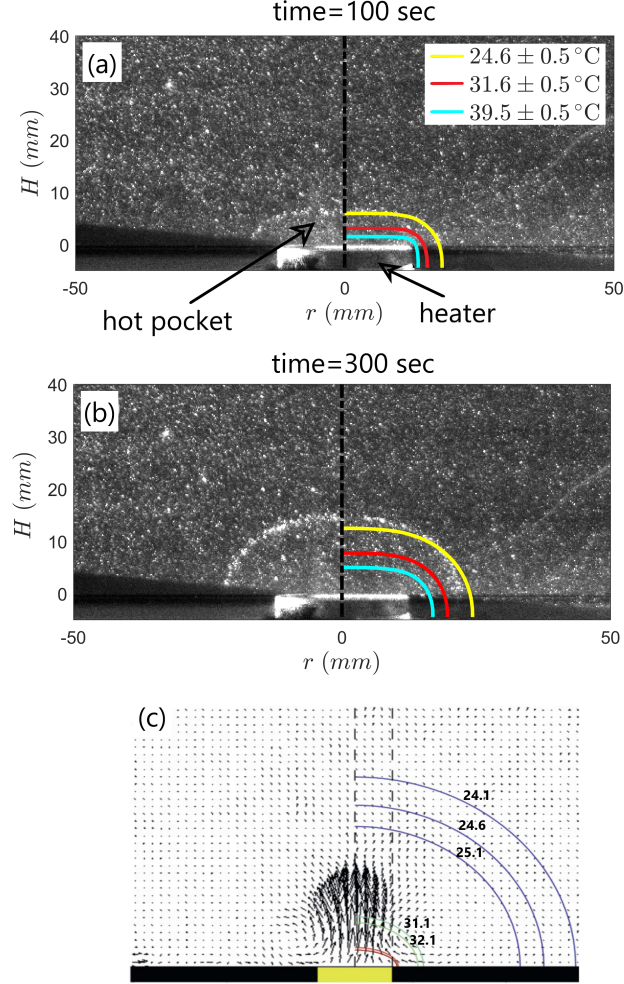


Figure 2: Front view of the growth of a hot pocket in a simple Herschel-Bulkley (HB) fluid (Carbopol) when heated from a localized heating source. Experiment from Davaille et al. (2013), see Appendix A for details on experimental conditions. In (a) and (b) the brighter lines are thermochromic liquid crystals' isotherms. The same isotherms are reproduced numerically in the conductive regime and plotted with different colors: yellow (24.6 ± 0.5 °C), red (31.6 ± 0.5 °C) and blue (39.5 ± 0.5 °C). Time is measured from the start of heating. (a) Growth of a hot pocket. Numerical isotherms fit well the experimental ones (stage (1) in the text). (b) Slow creep stage where the difference between experimental and numerical isotherms indicates the departure from the fully conductive regime (stage (2)). (c) Example of velocity field obtained during the slow creep stage. Solid lines indicate analytical isotherms for a steady-state conductive regime (values are indicated in °C). Significant vertical velocities are recorded at the center of the hot pocket and near the heater while outside the hot pocket the fluid remains motionless.

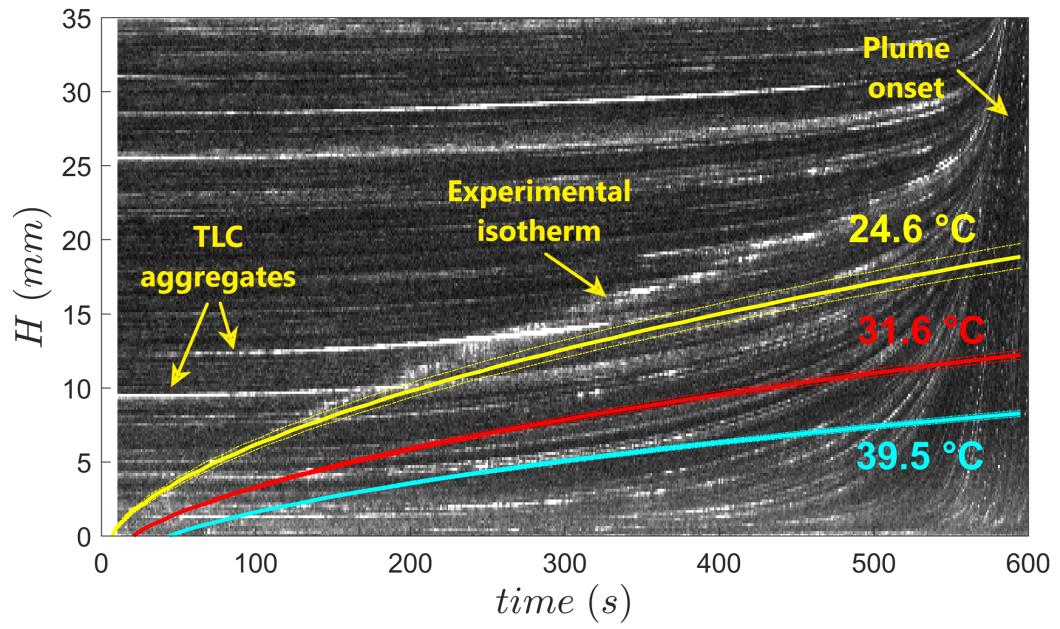


Figure 3: Spatiotemporal evolution of the experiment shown in Fig. 2. The figure shows the light intensity of the pixel line in the center of the setup as a function of time. Colored lines refer to the computed isotherms described in Fig. 2.

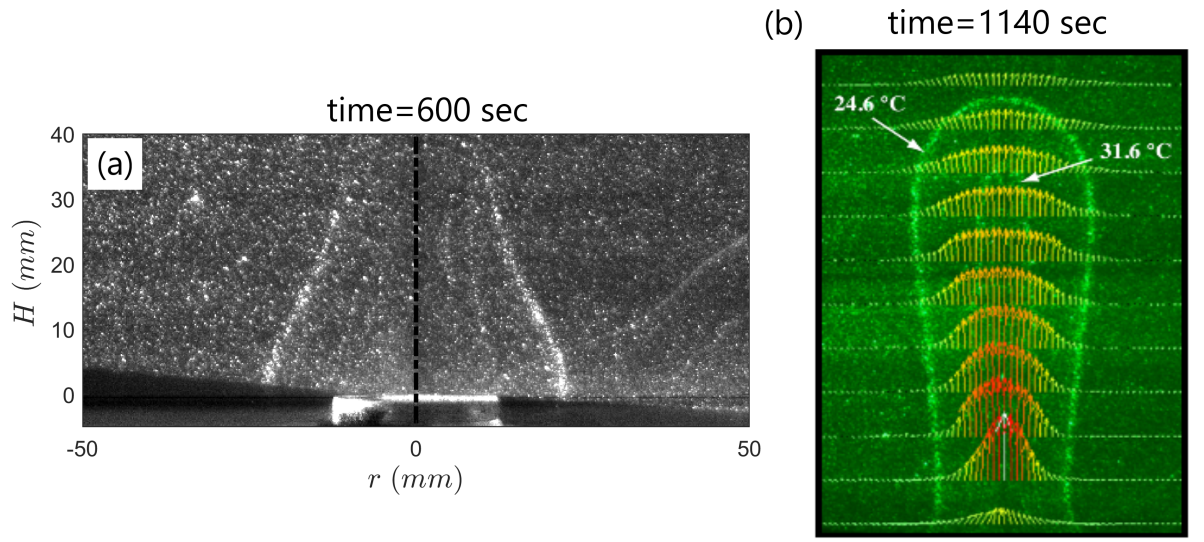


Figure 4: Last stage of the experiment shown in Fig. 2. (a) Rising of the hot plume, corresponding to stage (3) in the text. (b) Developed plume. Bright lines are isotherms. Colored vectors show the velocity field. Adapted from Davaille et al. (2013).

183 boundaries conditions, i.e. a bottom rigid boundary condition and a fluid-
 184 fluid interface between hot pocket and ambient fluid in plume experiments,
 185 and a bottom free surface boundary condition and a solid-fluid interface in
 186 the experiments for the falling sphere. Y_{inv_C} has been afterwards evaluated
 187 also from numerical simulations which investigate the development of ther-
 188 mal plumes in a locally heated simple yield stress fluid (Massmeyer et al.,
 189 2013; Sgreva, 2020b). For conditions similar to the experiments of Davaille
 190 et al. (2013), namely a comparable fluid rheology, geometry of the setup
 191 and imposed heating rate, they led to $Y_{inv_C} = 5.0 \pm 1.2$ in Massmeyer et al.
 192 (2013) and 7.35 ± 0.35 in Sgreva (2020b) (Fig. 5). Differences in this case
 193 can be related to the formulation of the numerical model, i.e. whether elas-
 194 tic deformation in addition to viscoplasticity is used (Sgreva, 2020b) or not
 195 (Massmeyer et al., 2013).

196 For a more geological perspective, the Yield number has already been
 197 used, for instance, to describe the difficulties for magma transport in a dyke
 198 through fracturing lithospheric rocks due to buoyancy forces (Weinberg and
 199 Podladchikov, 1994). Although the formulation of Y_{inv} in this last case re-
 200 mains the same as ours, by the definition of yield stress, Y_{inv} can evaluate a
 201 different physical phenomena. For example, in Weinberg and Podladchikov
 202 (1994) the yield stress used to calculate the Yield number is the rock's brittle
 203 strength defined following Byerlee's law. The result for transporting magma
 204 through dikes is that the condition of $Y_{inv} > Y_{inv_C}$ is very difficult to achieve
 205 and to maintain without invoking other quite specific conditions, i.e. very
 206 large magma bodies, proximity to the surface, tensile tectonics, etc.

207 Beside Y , diapir development also requires the Bingham number, Bi ,

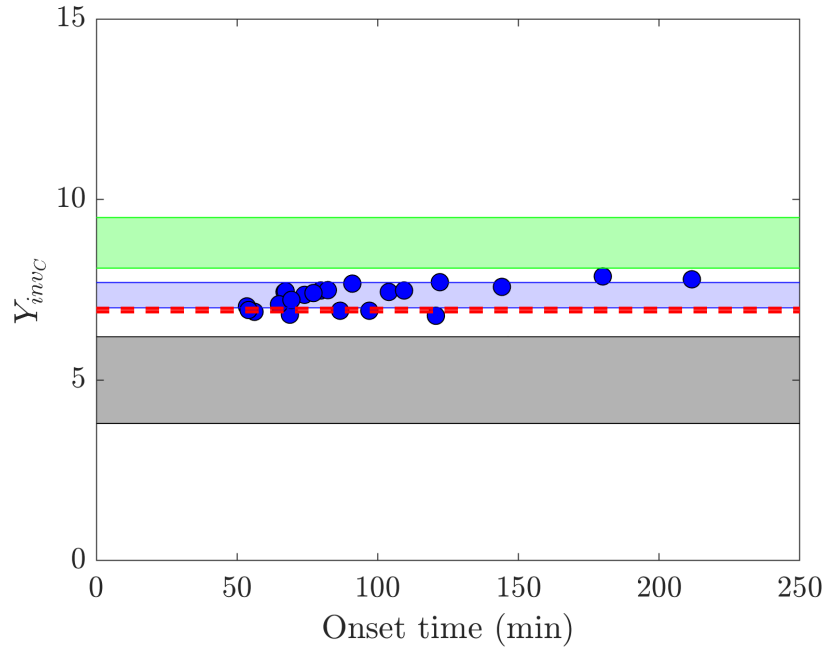


Figure 5: Inverse of the Yield number at the onset (Y_{inv_C}). Blue dots are simulations from Sgreva (2020b) and the blue bar corresponds to $Y_{inv_C}=7.35 \pm 0.35$. Green bar indicates $Y_{inv_C}=8.8 \pm 0.7$ (Davaille et al., 2013), gray bar $Y_{inv_C}=5.0 \pm 1.2$ (Massmeyer et al., 2013) and red dashed line $Y_{inv_C}=6.99$ (Beris et al., 1985; Tabuteau et al., 2007).

208 being supercritical, i.e. $Bi \leq 1$ (Massmeyer et al., 2013). The Bingham
 209 number compares the yield stress to the viscous stress and for a Herschel-
 210 Bulkley fluid writes:

$$Bi = \frac{\sigma_y}{K_v \dot{\gamma}^n}. \quad (3)$$

211 Motion is therefore expected only when local shear rates are larger than
 212 the critical strain rate corresponding to $Bi=1$, that is for $\dot{\gamma} > \dot{\gamma}_c = (\sigma_y/K_v)^{1/n}$
 213 (Fig. 6). It is only when the shear rate reaches this threshold that the hot
 214 pocket that grows from the hypothetical heating point evolves into a diapir.
 215 Note that when $Bi = 1$, the stress defined in eq. (1) is $\sigma_c = \sigma_y + K_v \dot{\gamma}_c^n = 2\sigma_y$
 216 and the effective critical viscosity writes:

$$\eta_c = \frac{\sigma_c}{\dot{\gamma}_c} = \frac{2\sigma_y}{(\sigma_y/K_v)^{1/n}}. \quad (4)$$

217 After the onset, the Bingham number decreases toward a value smaller
 218 than one (i.e. $Bi < 1$). For instance, in Sgreva (2020b) and Massmeyer et al.
 219 (2013) Bi was found to decrease up to 3 times from the value at the onset
 220 when the vertical velocity reaches its maximum (Fig. 6c). This decrease of
 221 Bi and the related increase in strain rate (i.e. $\dot{\gamma}/\dot{\gamma}_c > 1$) translates also into
 222 smaller effective viscosity. Hence the effective viscosity inferred at the onset
 223 ($\eta_{eff} = \eta_c$) represents the largest value of viscosity at which the transition
 224 from jamming to motion takes place and it will then decrease ($\eta_{eff} < \eta_c$)
 225 during the ascent of the diapir.

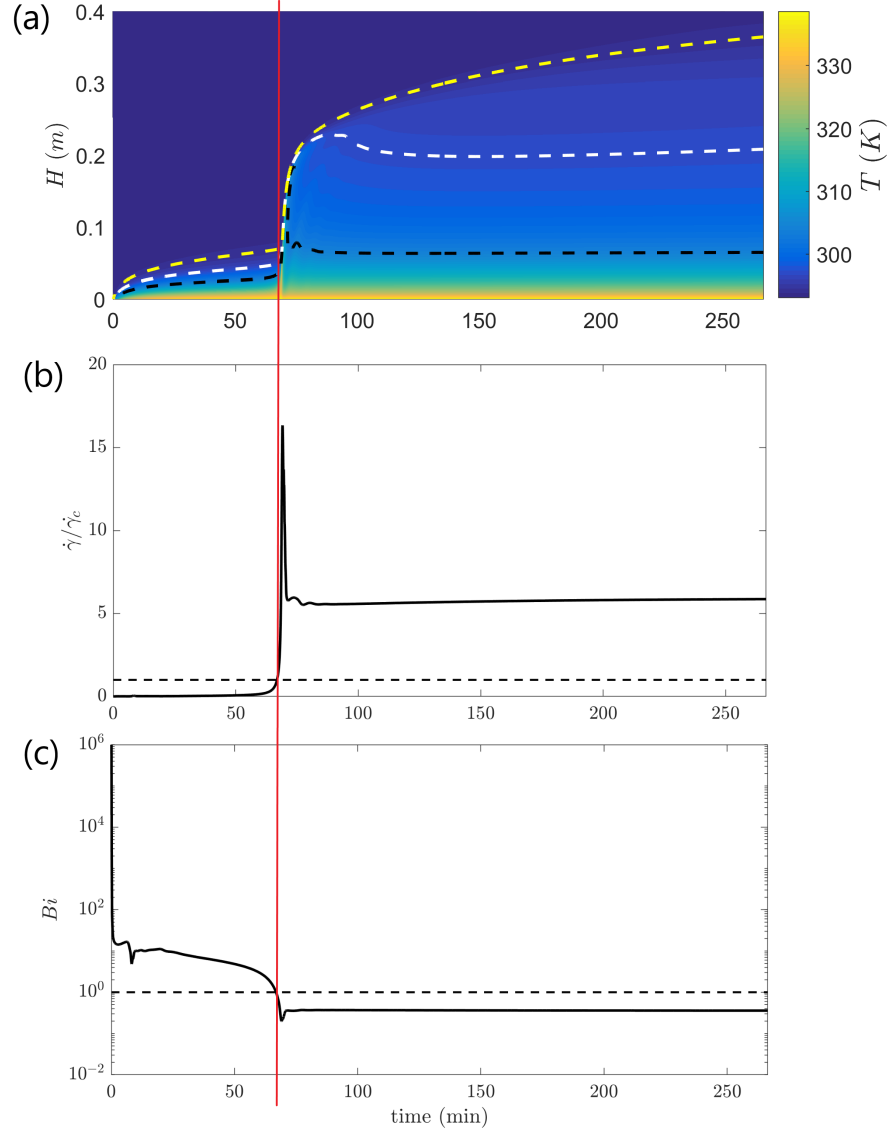


Figure 6: Development of a plume in a HB fluid, from simulation of Sgreva (2020b) ($\Delta T = 44^\circ\text{C}$; $\sigma_y = 0.076$ Pa; $Y_{invC} = 7.44$; $Ra \sim 10^5$). (a) Temporal evolution of temperature T along the central axis. Three isotherms have been highlighted: 21.0°C (in yellow), 23.9°C (in white) and 31.1°C (in black). (b) Evolution of the strain rate $\dot{\gamma}$ normalized by the critical strain rate $\dot{\gamma}_c$ during the development and the rise of the hot instability. The critical strain rate is defined for $Bi = \sigma_y / (K_v \dot{\gamma}_c^n) = 1$. Dashed line indicated $\dot{\gamma}/\dot{\gamma}_c = 1$. (c) Evolution of Bingham number. Dashed line indicated $Bi = 1$. The vertical red line indicates when the Bingham number in (c) becomes one.

226 4. Constraints on the diapirism at APMB and crust's rheology

227 An active and rising diapir has been suggested as the cause of the up-
228 lift observed above the Altiplano-Puna Magma Body (Fialko and Pearce,
229 2012; Comeau et al., 2015). Geodesy data and leveling data show in fact a
230 continuous (since 1960s), nearly constant and slow uplifting of an about 100-
231 km-wide region of the Altiplano-Puna volcanic complex (Fialko and Pearce,
232 2012; Henderson and Pritchard, 2013; del Potro et al., 2013). The central
233 area which is being uplifted at about 1 cm/yr is also surrounded by a broad
234 ring of subsidence forming a global sombrero-shape uplift which is consistent
235 with the presence of a diapir deep inside the crust. In this case the diapir
236 would develop from the APMB within a framework of a heterogeneous crust
237 and at greater depth than the brittle-ductile transition. The latter is reported
238 between 4.5 and 10 km below the Altiplano (Jay et al., 2012) whereas the
239 APMB extends from a depth of ~ 20 km below the surface (Comeau et al.,
240 2015).

241 In the previous section we have shown how that two main conditions
242 must be satisfied to allow the ascent of a buoyant instability in a yield stress
243 medium. The first one regards the inverse of the Yield number (here we
244 consider $Y_{inv} > Y_{inv_C} = 7.35 \pm 0.35$ from Sgreva (2020b)), while the second
245 one is accounted by $Bi \leq 1$. Given these two conditions, one can evaluate
246 the emplacement conditions for a buoyant instability (e.g. a diapir) in a
247 jammed crustal mush with HB rheology. We do so for the case of APMB,
248 assuming that the uplift measured at the surface originates from the rising
249 of a hot diapir from the shallowest regions of the magmatic reservoir beneath
250 Ulturncu volcano and rises with a vertical velocity equal to what is measured

251 at the surface, i.e. $v_z=1$ cm/yr (Fialko and Pearse, 2012).

252 In Fig. 7, we show conditions which lead to $Y_{inv} = Y_{inv_C}$ for such a sys-
253 tem. According to geodesy data (Fialko and Pearse, 2012; Gottsmann et al.,
254 2017) and magnetotellurics (Comeau et al., 2016), we assume a characteris-
255 tic diameter $D_{diap}=10-100$ km for the diapir. The density contrast between
256 diapir and surrounding crust is not well constrained and varies between dif-
257 ferent models. Fialko and Pearse (2012) use in their numerical simulations a
258 density difference of $\Delta\rho=400$ kg/m³, whereas smaller values of ~ 100 kg/m³
259 are employed for example by Gottsmann et al. (2017) and Spang et al. (2019).
260 A similar range of possible $\Delta\rho$, based on the inversion of gravity anomalies,
261 is given by del Potro et al. (2013). An upper limit for the density contrast of
262 400 kg/m³ represents an enormous density anomaly produced by the melt-
263 ing of a large enough amount of material below the observed diapiric body.
264 Given a crust density of $\rho_c=2700$ kg/m³, this scenario would require, for in-
265 stance, the presence of a very large melt fraction (ϕ_f), that is $\phi_f \sim 0.9$ for a
266 dacitic melt with $\rho_d=2300$ kg/m³ (del Potro et al., 2013). On the other hand,
267 an overall smaller density contrast reflects a smaller melt fraction which can
268 decrease towards the limit of $\Delta\rho=50$ kg/m³ for a fully crystallized dacite
269 ($\phi_f=0$; $\rho_d=2650$ kg/m³).

270 Within these ranges of diapir’s size and density contrast, we find that
271 a diapir can rise and deform the surrounding crust if the latter has a yield
272 stress within a range of 0.5 and 15 MPa (Fig. 7). Larger values of yield
273 stress clearly need either a broader instability or an unlikely larger density
274 contrast. Here the yield stress has to be interpreted within the rheological
275 definition, i.e. as the stress value needed to unjam a locked medium and to

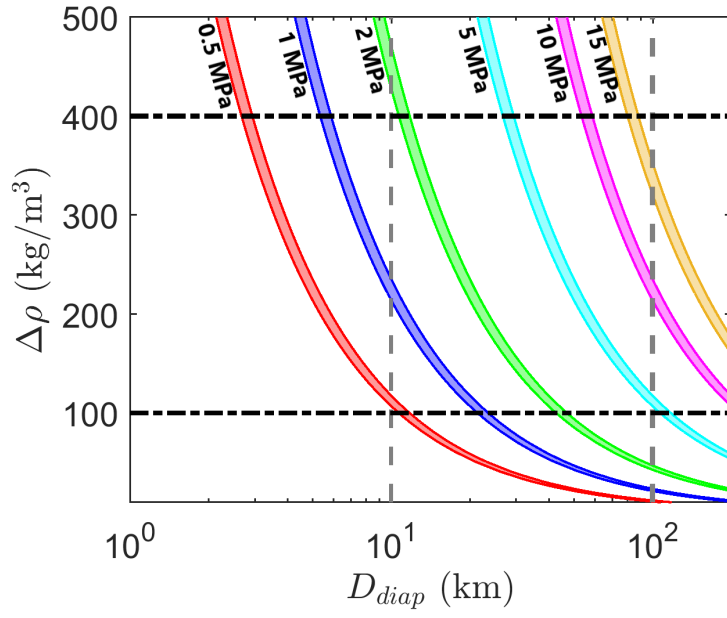


Figure 7: Yield stress (colored lines) allowing the development of a diapir from the top of the APMB according to $Y_{inv_C} = 7.35 \pm 0.35$, as function of diapir diameter and density contrast.

allow it to flow, rather than the threshold at which the medium simply loses the reversibility in deformation.

Beside $Y_{inv} > Y_{invC}$, the other condition for motion is $Bi \leq 1$. As summarized above, this critical condition translates into a critical minimum strain rate required for motion $\dot{\gamma}_c = (\sigma_y/K_v)^{(1/n)}$ and an effective viscosity is then given by $\eta_c = 2\sigma_y/\dot{\gamma}_c$ (eq. (4)). In Fig. 8 we display this viscosity as a function of fluid consistency and the range of yield stress found previously (i.e. σ_y in between 0.5 and 15 MPa). We take two limit values for the shear thinning index, namely $n=0.25$ (Fig. 8a) and $n=0.5$ (Fig. 8b). They correspond to stress exponents $n_E=1/n$ in stress-strain relationships for creep of 4 and 2, respectively, as expected for rocks Ranalli (1995). The viscosity reported in Fig. 8 corresponds to the maximum effective viscosity calculated from the minimum strain rate that guarantees $Bi=1$. As expected from its definition, it depends on the value of fluid consistency that one uses in the HB model. A way to bound the consistency is by taking into account the maximum vertical velocity, v_{max} , at which the thermal instability is moving upward. From the condition $Bi \leq 1$, one can in fact relate v_{max} to the size of the instability and the critical strain rate:

$$v_{max} = C2r_{eq}\dot{\gamma}_c, \quad (5)$$

where C is an experimental constant. Based on numerical simulations (Sgreva, 2020b), the maximum velocity is found to scale as $v_{max} \sim 4.45(2r_{eq}\dot{\gamma}_c)$ for constant $n=0.58$ (Fig. 9). The simulations of Massmeyer et al. (2013) where n was varied between 0.50 and 0.90 present the same trend (Fig. 9). The small differences between the two studies for same n displayed in Fig. 9 can be

299 related to the different formulation of the numerical model used to simulate
 300 plume’s formation, namely a regularized viscoplastic model in Massmeyer
 301 et al. (2013) and an elasto-viscoplastic model in Sgreva (2020b).

302 Considering the recorded uplift velocity at the surface v_z as a possible
 303 maximum rising velocity of the diapir, for the case at APMB the scaling of
 304 v_{max} translates to

$$v_z \sim 4.45 D_{diap} \dot{\gamma}_c, \quad (6)$$

305 leading to a critical strain rate of $\dot{\gamma}_c = v_z / (4.45 D_{diap})$. Within the chosen
 306 interval of D_{diap} , the critical strain rate is $\sim 10^{-15} - 10^{-16} \text{ s}^{-1}$. The resulting
 307 consistency is therefore

$$K_v = \sigma_y \dot{\gamma}_c^{-n} = \sigma_y \left(\frac{4.45 D_{diap}}{v_z} \right)^n. \quad (7)$$

308 This value of K_v is reported in Fig. 8 for the interval of diapir’s sizes of
 309 10-100 km.

310 5. Discussion

311 Given the evidence of partial melt and the shallow ductile-brittle tran-
 312 sition, a simple elastic model for the lower-middle crust beneath APVC is
 313 not appropriate to properly describe the whole system but instead a more
 314 complicated rheological model is required. The HB framework developed in
 315 the previous sections provides estimates of the lower-middle crust effective
 316 yield stress and viscosity at APMB.

317 The first crucial aspect regards the proper definition of yield stress needed
 318 to evaluate the conditions of motion. Differently from the already mentioned

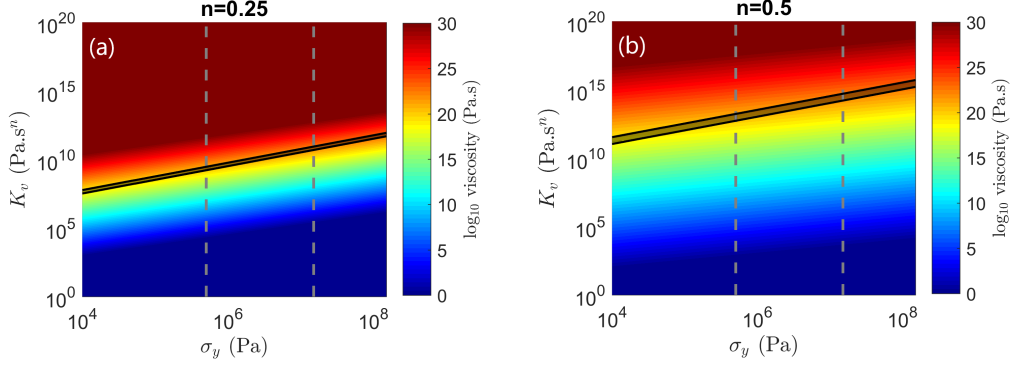


Figure 8: Maximum value of critical effective viscosity η_c (eq.4) corresponding to $Bi=1$, as function of consistency K_v and yield stress σ_y . Grey dashed lines bound the range of yield stress after Fig. 7. Black bands indicate $K_v = \sigma_y(4.45 D_{diap}/v_z)^n$, with D_{diap} between 10 and 100 km and an uplift velocity of $v_z=1$ cm/yr (Fialko and Pearse, 2012). (a) Shear thinning exponent $n=0.25$ and (b) $n=0.5$.

work of Weinberg and Podladchikov (1994), in our equation of the Yield number, σ_y does not indicate the stress threshold needed to the brittle failure of the rocks in the crust but it instead represents the threshold to unjam the locked medium, which could for example involve reactivation of fractures and creep. When Y_{inv} is defined to evaluate the ability of the system to transport magma by opening new fractures it must involve yield strength for ambient rocks in the order of 10^2 - 10^3 MPa, making it dramatically difficult to achieve conditions of $Y_{inv} > Y_{invC}$. However, the rheological (jamming) transition in partially molten rocks that takes place when the solid-particles volume fraction (ϕ_s) decreases approaching the maximum packing fraction ($\phi_m \sim 0.6$) can lead to a strength drop which can span up to four orders of magnitude (Rosenberg and Handy, 2005; Cashman et al., 2017). In addition to this strong dependence on ϕ_s and hence on the melt fraction ϕ_f , the measurement

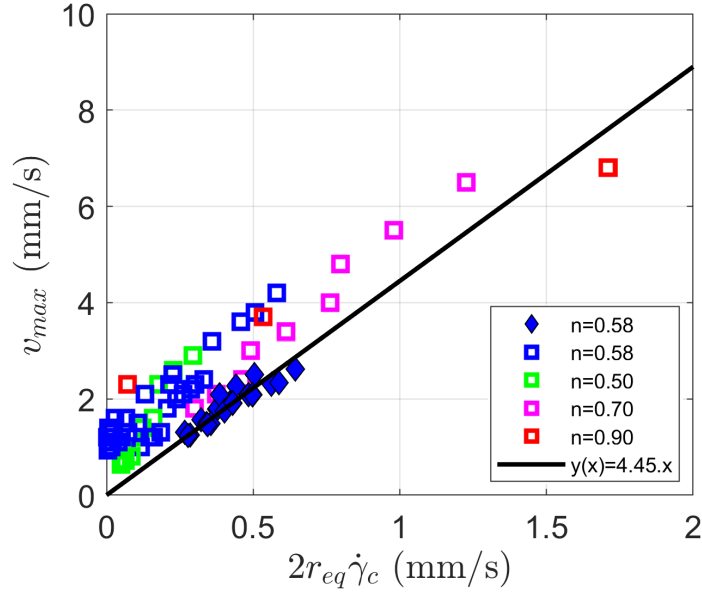


Figure 9: Maximum rising velocity of an hot instability as a function of the product between equivalent diameter $D_{eq} = 2r_{eq}$ and critical strain rate. Diamond symbols refer to numerical simulations of thermal plumes in a yield stress fluid of Sgreva (2020b) computed with a power-law index $n = 0.58$. The later are fitted by the equation $y(x) = 4.45x$. Squared symbols refer to simulations of Massmeyer et al. (2013) and colors are for the different power-index n tested.

332 of the strength of a partially molten rock with relative large melt fraction
 333 (≥ 0.3) falls also very close to the minimum measurable value of σ_y from
 334 experimental apparatus. The latter is estimated around ~ 1 MPa (Pistone
 335 et al., 2012; Rosenberg and Handy, 2005; Caricchi et al., 2007). In this
 336 regard, the range of σ_y of 0.5-15 MPa we found in Fig. 7 for the hot ductile
 337 crust that surrounds the rising diapir corresponds, in order of magnitude,
 338 to the strength of partially molten granite with $\phi_f \sim 0.25$ in Rosenberg and
 339 Handy (2005) (where $\sigma_y \sim 1$ MPa) and those for crustal granitic rocks on the
 340 western Arabian Peninsula, where $\sigma_y \sim 1-3$ MPa (Jónsson, 2012).

341 The second aspect that arises from the ascent of a diapir at APMB regards
 342 the values of effective viscosity and strain rate we have found. According to
 343 Fig. 7, a diapir of $D_{diap}=50$ km and $\Delta\rho=100$ kg/m³ would set on motion and
 344 would travel through a crust with yield stress of around $\sigma_y=2.2$ MPa. By tak-
 345 ing the typical stress exponent expected for creep mechanisms of lower-middle
 346 crustal rocks, that is $n_E=n^{-1}=3.0$ (Ranalli, 1997), the previous conditions
 347 lead to a consistency of $\sim 10^{13}$ Pa s^{0.3} and to an effective maximum value
 348 of viscosity for the lower-middle crust above APMB of $\eta_c \sim 10^{21}$ Pa s. This
 349 value corresponds to what is needed to trigger the rise of the diapir since it
 350 is calculated from the critical condition of $Bi=1$. However, after the plume
 351 onset, Bi continues to decrease (Fig. 6c) while the strain rate increases (Fig.
 352 6b), leading in turn to values of effective viscosity that are lower than those
 353 found for $Bi=1$. From eq. (6), considering a vertical velocity of 1 cm/yr, the
 354 critical strain rate results in $\dot{\gamma}_c \sim 10^{-15}$ s⁻¹ for a 50-km-wide diapir. Hence,
 355 at conditions of $Bi < 1$ where the strain rate can increase up to one order of
 356 magnitude compared with $\dot{\gamma}_c$ (Fig. 6b), we can expect a crustal region that

deforms at a strain rate of 10^{-14} s^{-1} . This corresponds to values of strain rate previously employed for APVC, e.g. $\sim 10^{-14} \text{ s}^{-1}$ in Jay et al. (2012), and other compression areas, such as Southern-Tibet where $\dot{\gamma} \sim 10^{-14}$ - 10^{-15} s^{-1} (Wang et al., 2019; Molnar, 2020) and Southern-Aegean where $\dot{\gamma} \sim 10^{-15} \text{ s}^{-1}$ (Kreemer and Chamot-Rooke, 2004; Kumar and Gordon, 2009).

Regarding the critical effective viscosity value, we found $\eta_c \sim 10^{21} \text{ Pa s}$. Such a high viscosity corresponds in order of magnitudes to the one of hot sub-solidus host rocks inside which magma bodies are usually emplaced (Sparks et al., 2019). To our knowledge, for the specific case at APMB there are not many independent constraints on the viscosity of the lower-middle crust. A list of them is reported in Table 1. The viscosity of the partially molten zone has been inferred from resistivity maps by Comeau et al. (2016) who estimated a viscosity of $\eta \sim 10^{12} - 10^{16} \text{ Pa s}$ with 20% melt fraction for the shallow magma reservoir. Viscosity of around $\eta \sim 10^{16} - 10^{18} \text{ Pa s}$ has been estimated by Fialko and Pearse (2012) by assuming a linear Maxwell viscoelastic rheology for the lower-middle crust. Similar values ($< 10^{16} \text{ Pa s}$) are obtained by using the same viscoelastic rheology for the structure beneath APVC also by Gottsmann et al. (2017). However, although those values mainly represent either the viscosity of the APMB itself or that of the hot diapir rising from it, they do not give much information about the effective bulk viscosity of the whole inelastic crust. The latter should have in fact a reasonable larger value of η due to the contribution of the regions of the crust where both temperature and melt fraction are lower than the APMB's. Rheological measurements on larger timescales (i.e. millions of years) resulting from the analysis of lithosphere response to unloading of the

Table 1: Effective viscosities beneath APVC. "VE model" indicate simulations carried out with a viscoelastic (VE) rheology.

Technique	Viscosity (Pa s)	Reference
VE model	$\sim 10^{16} - 10^{18}$ for APMB	Fialko and Pearce (2012)
VE model	$< 10^{16}$ for APMB; $\sim 10^{16} - 10^{19}$ for diapir	Gottsmann et al. (2017)
VE model	$< 10^{21} - 10^{22}$ at ~ 20 km beneath APVC	Gerbault et al. (2005)
from resistivity model	$< 10^{16}$ for APMB with 20% melt	Comeau et al. (2016)
from paleo-lake load	$< 5 \times 10^{20}$ for crustal plate	Bills et al. (1994)

large paleo-lake in the Central Andes of Bills et al. (1994) give in fact a viscosity for the crustal plate that is larger than what predicted for APMB alone. The maximum effective bulk viscosity obtained in this way is $\eta < 5 \times 10^{20}$ Pa s, definitely closer to the estimation for the maximum critical viscosity η_c we obtain by using a HB rheology (Fig. 8).

6. Conclusion

In this work we propose a mechanical interpretation for the well documented uplift above APMB, based on the assumption that the effective rheology at large scale of the crust is the one of a yield stress material. In material with such rheology, the diapir take-off and growth require two local conditions: (1) the ratio between yield stress and viscous stress to be supercritical ($Bi < 1$), and (2) the ratio between the buoyancy stress of the hot diapir and the yield stress to be larger than a critical value ($Y_{inv} > Y_{inv_c}$).

We find that in order to allow the formation and the rise of a 10-100 km-wide diapir from above APMB with a density contrast with respect to

397 surrounding rocks of 100-400 kg/m³, the lower ductile crust needs a yield
 398 stress of $\sim 0.5\text{-}15$ MPa to respect condition (1). Moreover, from condition (2)
 399 with an uplift velocity of 1 cm/yr, we can bound the maximum bulk effective
 400 viscosity η_c for the APMB lower-middle crust at $\eta_c \sim 10^{21}$ Pa s.

401 **Appendix A. Details on experiments of thermal plumes**

402 Figures 2 - 4 show the experiments on the development of thermal plumes
 403 in Carbopol of Davaille et al. (2013). These experiments are carried out
 404 by using a 166-mm-high rectangular tank into which the fluid is poured.
 405 The fluid is heated by a circular heater located at the center of the bottom
 406 surface. The maximal imposed temperature difference between the heater
 407 and the ambient fluid is $\Delta T \sim 44^\circ\text{C}$. The fluid rheology is described with
 408 a HB model with the following parameters: $\sigma_y=0.10$ Pa, $n=0.54$, $K_v=0.76$
 409 Pa s^{*n*}. For the case in Figs. 2 - 4, the Rayleigh number at the onset of motion
 410 is

$$Ra = \frac{\alpha \rho g \Delta T h^3}{k \eta_c} \sim 10^6, \quad (\text{A.1})$$

411 with α being the fluid thermal expansion (4.62×10^{-4} K⁻¹), ρ the density
 412 (1142 kg/m³), k the thermal diffusivity (1×10^{-7} m²/s), η_c the viscosity ob-
 413 tained from eq. (4) and h the height of the tank. The critical Yield number
 414 found in Davaille et al. (2013) ($Y_{inv_C} = 8.8 \pm 0.7$) can be determined from eq.
 415 (2) during stages (1) and (2) of plume development by assuming $D=2r_{eq}$,
 416 with r_{eq} being the equivalent radius of a sphere having the same volume as
 417 the hot pocket. Experimentally, the hot pocket can be quantitatively de-
 418 fined within the temperature field by the isotherm $T_{lim} = 0.1 \Delta T$, where

419 $\Delta T = T_{max} - T_{amb}$ and T_{max} is the heater temperature and T_{amb} the ambient
 420 temperature. The hot pocket is therefore represented by the volume of fluid
 421 with $T \geq T_{lim}$. For the density difference term in eq. (2) one can refer to the
 422 mean $\Delta\rho$ within the fluid pocket, that is $\Delta\rho \simeq \overline{\Delta\rho} = \alpha\rho(\overline{T}_{hot\ pocket} - T_{amb})$
 423 where $\overline{T}_{hot\ pocket}$ is the average temperature of the pocket.

424 **Acknowledgments**

425 N.R. Sgreva was supported by the Initial Training Network No. 642029-
426 ITN CREEP, an Horizon 2020 - Marie Skłodowska-Curie Action. This re-
427 search was also supported by LabEx PALM (ANR-10-LABX-0039- PALM).

428 **Data Availability**

429 The data underlying this article will be shared on reasonable request to
430 the corresponding author.

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