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# Inferring the rheology of the crust from the uplift observed above the Altiplano-Puna Magma Body

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## Abstract

Geophysical imaging techniques together with numerical models have shown that the surface uplift measured above the Altiplano-Puna Magma Body (APMB) can be resolved by the presence and propagation of a diapir from the top of the APMB itself. In this work we interpret deformations that characterize the crustal region above and around APMB through the employment of a viscoplastic type rheology. That is, we assume that at large scale the ductile lower-middle crust that surround the magmatic mush behaves as yield-stress fluid described by a Herschel-Bulkley (HB) model. In this scenario, the main critical conditions needed for the growth and the subsequent rise of the diapir are: (1) the ratio between yield stress and viscous stresses, namely the Bingham number  $Bi$ , has to be less than 1, i.e.  $Bi \leq 1$ ; and (2) the ratio between buoyancy stresses and yield stress, namely the inverse of the Yield number  $Y_{inv}=Y^{-1}$ , has to be larger than a critical value, i.e.  $Y_{inv} > Y_{invC}$ . By using these critical conditions we infer the bulk

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rheological properties of the heterogeneous lower-middle crust above APMB. We estimate the yield stress of the crust in between 0.5-15 MPa. For a crust that allows the development and the emerge of a 10 to 100 km wide diapir, the coupling of this range of yield stress with the regional uplift velocity measured at the surface allows to estimate a critical strain rate of  $\sim 10^{-15}$ - $10^{-16}$  s $^{-1}$  and a maximum bulk effective viscosity of the lower-middle crust of  $\eta_c=10^{21}$  Pa s.

*Keywords:* Rheology: crust and lithosphere, APMB, Diapirism, Yield stress, Viscoplastic

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## 1. Introduction

The Altiplano-Puna Magma Body (APMB) is a mid-crustal magmatic system located at  $\sim 20$  km beneath the Altiplano-Puna Volcanic Complex (APVC) in the central Andes, South America. It represents the largest active, continental magma body in Earth's crust (Zandt et al., 2003) and is considered to be directly related to an uplifting region, centered on the western slope of Uturuncu volcano, and its peripheral subsidence zone (Fig. 1) (Fialko and Pearse, 2012). The entire APMB can be represented as a complex transcrustal magmatic structure, that is a large environment volumetrically dominated by crystal mush (Cashman et al., 2017; Pritchard et al., 2018). Given its impact to the region, a good description of its dynamics becomes crucial to understand both its mobility, lifetime, internal structure (e.g. Massol and Jaupart, 2009; Gonnermann and Manga, 2007; Caricchi et al., 2007; Turner and Costa, 2007) and the role that such an enormous ( $\sim 5 \times 10^5$  km $^3$ , Ward et al. (2014)) magmatic structure can play on the deformation of the

16 overlying crust.

17       However, to constrain the mush dynamics beneath APVC and the thermo-  
18 mechanical response of the surrounding region, a number of geometrical and  
19 physical properties of both APMB and lower-middle crust are required. Some  
20 of them have been constrained in recent years by using different geophysical  
21 investigation methods. For instance, by combining seismic tomography and  
22 3D-model inversion to evaluate the crustal 3D shear-wave velocity field, Ward  
23 et al. (2014) displayed a very large ( $\sim 5 \times 10^5 \text{ km}^3$ ) low seismic velocity (LSV)  
24 zone at a depth of 4-25 km beneath the APVC. This region is interpreted  
25 as an hotter zone compared to the surrounding material, and may also be  
26 enriched in melt content. A similar broad LSV zone centered below the  
27 Uturuncu volcano and at  $\sim 15$  km below sea level has been revealed also by  
28 other authors (e.g. Zandt et al., 2003; Chmielowski et al., 1999). However,  
29 due to the resolution of seismic tomography that is not better than 1 km  
30 (Cashman et al., 2017), the exact geometry and position of this hot body are  
31 still debated. This is caused by the difficulty in constraining the spacial melt  
32 distribution with the technique, which is not always able to recognize large  
33 melt bodies even in regions that are active nowadays or have produced large  
34 eruptions in the Quaternary (Cashman et al., 2017).

35       Besides seismic tomography, other geophysical imaging techniques can  
36 help to better characterize this anomalous structure. Magnetotelluric data  
37 reveals a first large low electrical resistivity ( $< 3 \text{ } \Omega\text{m}$ ) anomaly at  $\sim 15$  km  
38 below the sea level and a second  $\sim 10$ -km-wide vertical anomaly on the top  
39 of it (Fig. 1c) (Comeau et al., 2015, 2016). Differences in resistivity between  
40 the two regions may be related to variations in the composition: while the

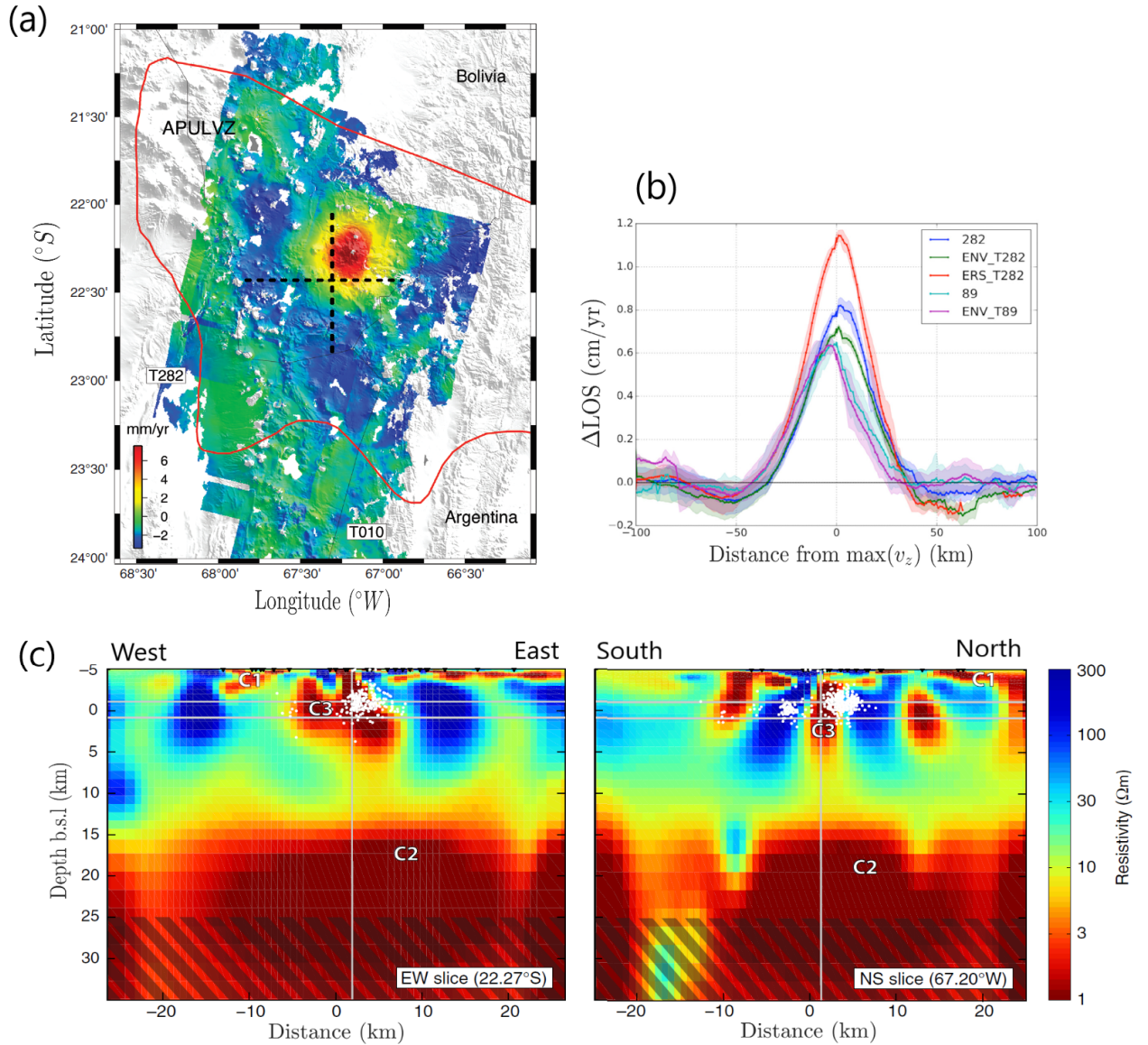


Figure 1: (a) Map view of the Altiplano-Puna region (Southern Bolivia). Colors indicate the elevation rate measured at the surface from InSAR data. Red line indicates the mid-crustal low-velocity zone associated to the APMB. Black dotted lines indicate the locations of cross sections in (c). Modified from Fialko and Pearce (2012). (b) Average velocities of line of sight (LOS) along sections crossing the center of the uplift. Modified from Gottsmann et al. (2017). (c) West-East and South-North vertical cross sections of the 3D resistivity model of (Comeau et al., 2015) across APVC. The main low electrical resistivity anomaly (C2) is associated to the APMB whereas the smaller anomaly on the top of it (C3) is interpreted as an ascent diapir. Modified from Comeau et al. (2016).

41 resistivity of the first deeper body ("C2" in Fig. 1c) can be explained by the  
42 presence of andesite melts in APMB (with a melt fraction  $\phi_f > 0.15$ ), the  
43 resistivity of the region above it ("C3" in Fig. 1c) may reflect the presence of  
44 dacite melts combined with aqueous fluids (Comeau et al., 2016). A similar  
45 vertically elongated structure is revealed also by the inversion of Bouguer  
46 anomaly data that highlights a low density and  $\sim 15$ -km-wide structure on  
47 the top of the APMB (del Potro et al., 2013), interpreted as an active diapiric  
48 ascent of magma (e.g. del Potro et al., 2013; Fialko and Pearse, 2012; Gotts-  
49 mann et al., 2017). The presence of a mid-crustal diapir which slowly moves  
50 upward is in agreement with geodesy data collected above APMB from 1995  
51 to 2010 (Fialko and Pearse, 2012). InSAR data show indeed a  $\sim 150$ -km-wide  
52 region, centered on the western slope of Uturuncu volcano, which is uplifted  
53 at the rate of  $\sim 1$  cm/yr, and surrounded by an approximately 30-km-wide  
54 ring of subsidence (Fig. 1a-b). The morphology and large extent of such a  
55 "sombbrero"-shaped deformation on the surface cannot be caused by a single  
56 large dike as expected for an intrusion in a merely elastic crust (Menand and  
57 Tait, 2001; Jellinek and DePaolo, 2003). But instead it matches well results  
58 of geodynamics models that assume the rise of a large diapir fed by partial  
59 melt from the APMB within a crust that is not-purely elastic (e.g. Fialko and  
60 Pearse, 2012; Gottsmann et al., 2017). Such a large diapir rising from the top  
61 of APMB would cause an extensive deformation of the whole crust, leading  
62 in turn to the displacement measured at the surface by geodesy techniques.

63 The interaction of the rising diapir with the crustal layer above offers  
64 the opportunity to estimate the effective rheology of the crust itself. The  
65 structure of the crust with its rheological properties and mechanical behavior

66 are indeed heavily influenced by the specific geodynamic context in which  
67 the crust is located (Burov, 2011). So the rheology can in fact deviate from  
68 the classical case where the whole deformation can be simply described by  
69 a purely elastic or a purely viscous model. Moreover, heterogeneities that  
70 characterize the crust on all scales, i.e. from small-scale (e.g. grain size, pore  
71 fluid pressure, chemical activities of mineral components, etc.) to large-scale  
72 (dikes filled with magma, faults, etc.), result in an intricate structure that  
73 can easily be locked or "jammed". Thus at the macroscopic scale, the crust  
74 bulk behavior could be comparable to that of a yield-stress material whereby  
75 flow can only occur when a threshold stress value (i.e. the yield stress,  $\sigma_y$ )  
76 is reached (Ancey, 2007; Bonn et al., 2017). Within this perspective, for an  
77 heterogeneous lower-middle crust an effective viscoplastic rheology can be  
78 claimed, making the yield stress a key aspect to better understand its bulk  
79 behavior.

80 In this paper we infer the rheological properties of the lower-middle crust  
81 below APVC from the rate of vertical surface displacement measured in the  
82 orogenic region of the Altiplano and by assuming that this uplift is caused  
83 by the rise of a diapir from above APMB. To do so we assume that the  
84 heterogeneous crust surrounding the diapir behaves as a non-Newtonian yield  
85 stress fluid, i.e. as a material whose bulk behavior can be described with a  
86 viscoplastic rheological model. In section 2 we introduce the main rheological  
87 properties of these materials. In section 3 we discuss the general critical  
88 conditions for motion of a buoyant body through an yield stress fluid. The  
89 latter are applied to the APMB case in section 4. We end by discussing the  
90 implications that our results have for a partially molten lower-middle crust.

## 91 2. The yield-stress in viscoplastic rheology

92 Viscoplastic fluids (synonym of yield stress fluids) are characterized by  
93 the presence of a yield stress,  $\sigma_y$  (Dinkgreve et al., 2017). A typical example  
94 of them is a suspension of particles in a liquid. When the particle volume  
95 fraction increases, the particles come into close contact, and the material  
96 can face jamming. In this jammed state, the material can support stresses  
97 without flowing. A so-called yield stress fluid does not flow unless the applied  
98 stresses are large enough to unjam the structure, but it does flow when  
99 the stresses become larger than  $\sigma_y$ . This introduces a non-linearity to the  
100 material rheology, with strong impact on its dynamics (Makse et al., 2005;  
101 Coussot, 2005; Barnes, 1995).

102 Simple yield stress fluids are those described by popular rheological mod-  
103 els such as the Bingham model or the Hershel-Bulkley (HB) model. The  
104 latter writes

$$\begin{aligned} \sigma &= \sigma_y + K_v \dot{\gamma}^n & \text{for } \sigma > \sigma_y & \quad (1) \\ \dot{\gamma} &= 0 & \text{for } \sigma \leq \sigma_y & \end{aligned}$$

105 where  $\sigma$  is the stress,  $\dot{\gamma}$  the strain rate,  $K_v$  the consistency and  $n$  the  
106 power-law exponent. Note that the exponent  $n$  defined here is the reverse  
107 of the power law index usually used in equations for creep mechanisms in  
108 geophysics (e.g. in Ranalli, 1995). For  $n < 1$  the fluid is shear thinning and  
109 the effective viscosity  $\eta_{eff} = \sigma/\dot{\gamma}$  decreases as  $\dot{\gamma}$  increases. For  $n > 1$  the  
110 fluid is shear thickening. For  $n=1$  and  $\sigma_y > 0$  the HB model reduces to the



111 Bingham model and describes a fluid with a linear flow curve and constant  
112 value of viscosity. And, finally, for  $n=1$  and  $\sigma_y=0$  the fluid is Newtonian.

113 The concepts of yield stress and plasticity are not only employed in the  
114 rheology of viscoplastic fluids, but they are also largely used in solid mechan-  
115 ics through the Coulomb plasticity theory. In Coulomb plasticity, plastic  
116 deformation indicates the irreversible deformation of a sample under stress  
117 whereas in Bingham viscoplasticity it refers to a solid-liquid transition. In  
118 this latter case the yield stress becomes the limit between the elastic (or  
119 viscoelastic) solid-like domain and the viscous fluid-like domain where the  
120 material flows. Even though the definition of  $\sigma_y$  is not the same among the  
121 two theories, the concept behind it relies to some overlapping phenomena:  
122 the transition from a reversible to a non-reversible deformation on one side  
123 and the not-flowing to flowing on the other side. Besides that, however, the  
124 two theories show some differences on their theoretical formulation (Ancy, 2007).  
125 The main one regards the description of material's deformation on a  
126 macroscopic scale: a viscoplastic fluid behaves as a whole on the bulk scale,  
127 i.e. as a one-phase homogeneous material (Coussot et al., 2009). Hence, it  
128 only requires a single stress-strain constitutive equation, e.g. eq.(1), where  
129 there is no need to separate the role of interstitial fluids from the one of  
130 the solid phase. This strongly differs from a two-phases saturated Coulomb  
131 material in which the two phases can move at different velocities and have  
132 to be considered separately.

133 Throughout the rest of this article, we will always refer for the fluid  
134 deformation to the rheological viscoplastic description. That is describing  
135 both mush and hot crust as a single-phase incompressible fluid that behaves

136 as a viscous fluid once set in motion.

### 137 **3. Conditions for the ascent of a buoyant instability in a yield-** 138 **stress fluid**

139 When a yield stress fluid is heated the buoyancy stresses that originate  
140 due to thermal expansion may not be large enough to exceed the fluid yield  
141 stress. Motion is then prevented and the fluid remains at rest. On the other  
142 hand, when local stresses are large enough, a thermal plume can develop  
143 and rise within the fluid column. The plume dynamics has been investi-  
144 gated experimentally for a simple yield stress fluid heated by a local heat  
145 source by Davaille et al. (2013) (see Appendix A for details on experimen-  
146 tal conditions). They found that the formation and subsequent growth of a  
147 thermal instability can be described in three main stages: (1) a no-motion  
148 phase where a hot pocket grows by thermal diffusion around the localized  
149 heat source (Fig. 2a and Fig. 3). (2) A stage where slow creep takes place  
150 within the growing hot pocket (Fig. 2b). This slow ascent can be observed  
151 also in the spatio-temporal evolution shown in Fig. 3 where bright lines that  
152 correspond to reflecting particles formed by Thermo-Liquid Crystals (TLCs)  
153 are not longer horizontal but begin to move upward. This is because, starting  
154 from this stage, the edge of the thermal pocket begins to empty slowly to  
155 feed a creep confined around the heating element (Fig. 2c). However, during  
156 this phase the fluid outside the hot pocket still remains unyielded. And (3)  
157 the stage in which a hot finger rises upward (Fig. 4a). Here upwelling oc-  
158 curs only within the thermal anomaly and shear is strongly localized along  
159 plume boundaries (Fig. 4b). The fluid within the anomaly moves then as a

160 plug and the overall thermal shape looks more like a finger than the classical  
161 mushroom shape expected for Newtonian fluids.

162 For small Reynolds numbers, the flow resulting from the rising of the  
163 thermal instability can be parameterized by two key dimensionless numbers.  
164 The first is the Yield number,  $Y$ , and the second is the Bingham number,  $Bi$   
165 (Davaille et al., 2013; Karimfazli et al., 2016; Massmeyer et al., 2013). For  
166 simplicity here we use the inverse of the Yield number,  $Y_{inv} = 1/Y$ , which  
167 represents the ratio between the buoyancy stress and the yield stress. It is  
168 usually written as

$$Y_{inv} = \frac{g\Delta\rho D}{3\sigma_y}. \quad (2)$$

169 where  $g$  is the acceleration due to gravity and  $\Delta\rho$  the density difference  
170 between the hot body, described by a characteristic diameter  $D$ , and the  
171 ambient fluid.  $Y_{inv}$  has been firstly employed to evaluate motion of a single  
172 rigid sphere in Bingham fluid (Beris et al., 1985). In this case, the critical  
173 value of the (inverse) Yield number,  $Y_{invC}$ , below which the sphere does not  
174 move is  $Y_{invC}=6.99$ . It has been subsequently confirmed experimentally for  
175 simple HB fluids (Tabuteau et al., 2007) and for more heterogeneous HB  
176 fluids (Sgreva et al., 2020a). In the case of buoyant thermal instabilities  
177 instead of spheres, one can consider the hot pocket forming around the heat-  
178 ing source at stage (1) and (2) as a buoyant "entity" that tries to go up  
179 because it is less dense but is kept anchored at the original position by the  
180 fluid yield stress. Davaille et al. (2013) found that the thermal instability  
181 will rise only if  $Y_{inv} > Y_{invC} = 8.8 \pm 0.7$ , a value close to but different from  
182 the solid sphere case. This is expected given the different geometries and

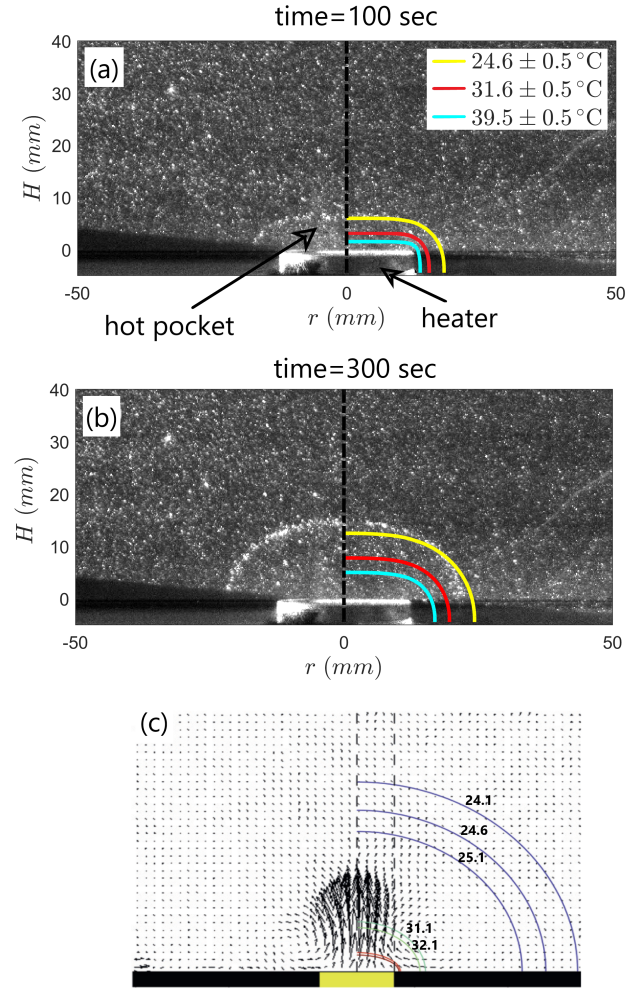


Figure 2: Front view of the growth of a hot pocket in a simple Herschel-Bulkley (HB) fluid (Carbopol) when heated from a localized heating source. Experiment from Davaille et al. (2013), see Appendix A for details on experimental conditions. In (a) and (b) the brighter lines are thermochromic liquid crystals' isotherms. The same isotherms are reproduced numerically in the conductive regime and plotted with different colors: yellow ( $24.6 \pm 0.5$  °C), red ( $31.6 \pm 0.5$  °C) and blue ( $39.5 \pm 0.5$  °C). Time is measured from the start of heating. (a) Growth of a hot pocket. Numerical isotherms fit well the experimental ones (stage (1) in the text). (b) Slow creep stage where the difference between experimental and numerical isotherms indicates the departure from the fully conductive regime (stage (2)). (c) Example of velocity field obtained during the slow creep stage. Solid lines indicate analytical isotherms for a steady-state conductive regime (values are indicated in °C). Significant vertical velocities are recorded at the center of the hot pocket and near the heater while outside the hot pocket the fluid remains motionless.

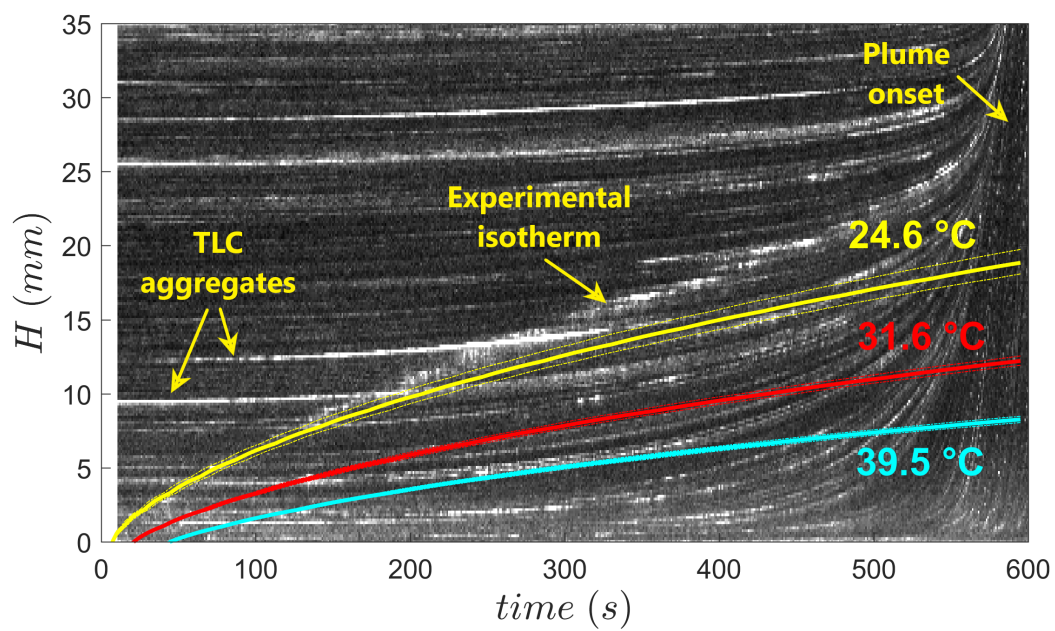


Figure 3: Spatiotemporal evolution of the experiment shown in Fig. 2. The figure shows the light intensity of the pixel line in the center of the setup as a function of time. Colored lines refer to the computed isotherms described in Fig. 2.

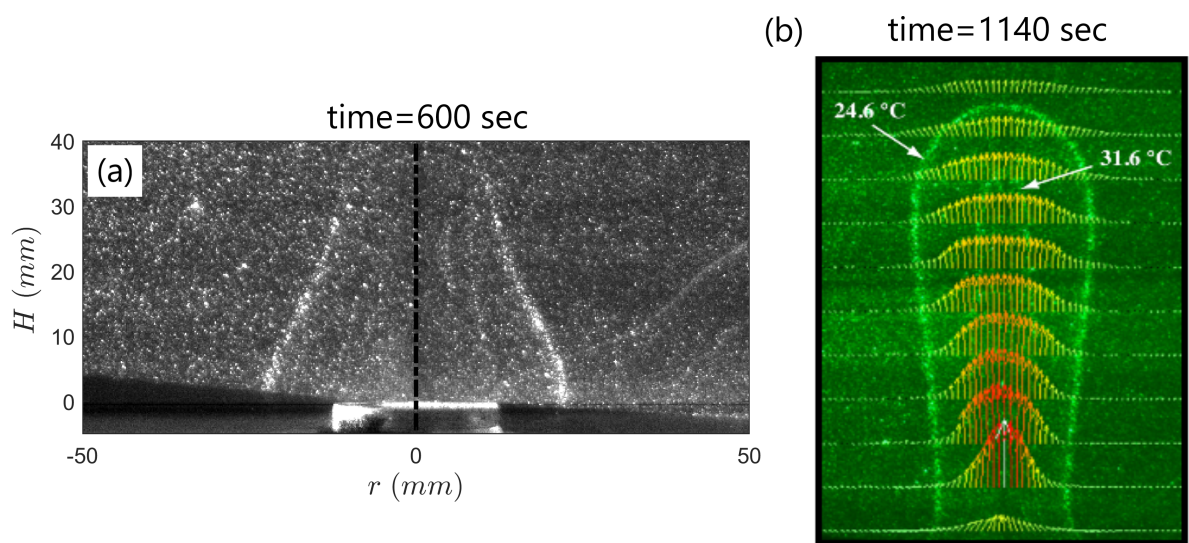


Figure 4: Last stage of the experiment shown in Fig. 2. (a) Rising of the hot plume, corresponding to stage (3) in the text. (b) Developed plume. Bright lines are isotherms. Colored vectors show the velocity field. Adapted from Davaille et al. (2013).

183 boundaries conditions, i.e. a bottom rigid boundary condition and a fluid-  
184 fluid interface between hot pocket and ambient fluid in plume experiments,  
185 and a bottom free surface boundary condition and a solid-fluid interface in  
186 the experiments for the falling sphere.  $Y_{inv_C}$  has been afterwards evaluated  
187 also from numerical simulations which investigate the development of ther-  
188 mal plumes in a locally heated simple yield stress fluid (Massmeyer et al.,  
189 2013; Sgreva, 2020b). For conditions similar to the experiments of Davaille  
190 et al. (2013), namely a comparable fluid rheology, geometry of the setup  
191 and imposed heating rate, they led to  $Y_{inv_C} = 5.0 \pm 1.2$  in Massmeyer et al.  
192 (2013) and  $7.35 \pm 0.35$  in Sgreva (2020b) (Fig. 5). Differences in this case  
193 can be related to the formulation of the numerical model, i.e. whether elas-  
194 tic deformation in addition to viscoplasticity is used (Sgreva, 2020b) or not  
195 (Massmeyer et al., 2013).

196 For a more geological perspective, the Yield number has already been  
197 used, for instance, to describe the difficulties for magma transport in a dyke  
198 through fracturing lithospheric rocks due to buoyancy forces (Weinberg and  
199 Podladchikov, 1994). Although the formulation of  $Y_{inv}$  in this last case re-  
200 mains the same as ours, by the definition of yield stress,  $Y_{inv}$  can evaluate a  
201 different physical phenomena. For example, in Weinberg and Podladchikov  
202 (1994) the yield stress used to calculate the Yield number is the rock's brittle  
203 strength defined following Byerlee's law. The result for transporting magma  
204 through dikes is that the condition of  $Y_{inv} > Y_{inv_C}$  is very difficult to achieve  
205 and to maintain without invoking other quite specific conditions, i.e. very  
206 large magma bodies, proximity to the surface, tensile tectonics, etc.

207 Beside  $Y$ , diapir development also requires the Bingham number,  $Bi$ ,

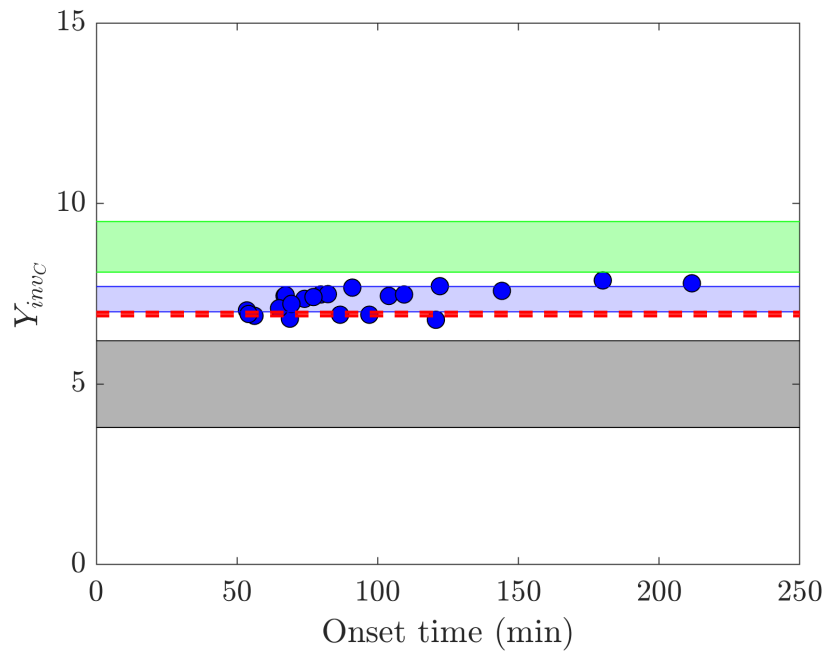


Figure 5: Inverse of the Yield number at the onset ( $Y_{inv_C}$ ). Blue dots are simulations from Sgreva (2020b) and the blue bar corresponds to  $Y_{inv_C} = 7.35 \pm 0.35$ . Green bar indicates  $Y_{inv_C} = 8.8 \pm 0.7$  (Davaille et al., 2013), gray bar  $Y_{inv_C} = 5.0 \pm 1.2$  (Massmeyer et al., 2013) and red dashed line  $Y_{inv_C} = 6.99$  (Beris et al., 1985; Tabuteau et al., 2007).



208 being supercritical, i.e.  $Bi \leq 1$  (Massmeyer et al., 2013). The Bingham  
 209 number compares the yield stress to the viscous stress and for a Herschel-  
 210 Bulkley fluid writes:

$$Bi = \frac{\sigma_y}{K_v \dot{\gamma}^n}. \quad (3)$$

211 Motion is therefore expected only when local shear rates are larger than  
 212 the critical strain rate corresponding to  $Bi=1$ , that is for  $\dot{\gamma} > \dot{\gamma}_c = (\sigma_y/K_v)^{1/n}$   
 213 (Fig. 6). It is only when the shear rate reaches this threshold that the hot  
 214 pocket that grows from the hypothetical heating point evolves into a diapir.  
 215 Note that when  $Bi = 1$ , the stress defined in eq. (1) is  $\sigma_c = \sigma_y + K_v \dot{\gamma}_c^n = 2\sigma_y$   
 216 and the effective critical viscosity writes:

$$\eta_c = \frac{\sigma_c}{\dot{\gamma}_c} = \frac{2\sigma_y}{(\sigma_y/K_v)^{1/n}}. \quad (4)$$

217 After the onset, the Bingham number decreases toward a value smaller  
 218 than one (i.e.  $Bi < 1$ ). For instance, in Sgreva (2020b) and Massmeyer et al.  
 219 (2013)  $Bi$  was found to decrease up to 3 times from the value at the onset  
 220 when the vertical velocity reaches its maximum (Fig. 6c). This decrease of  
 221  $Bi$  and the related increase in strain rate (i.e.  $\dot{\gamma}/\dot{\gamma}_c > 1$ ) translates also into  
 222 smaller effective viscosity. Hence the effective viscosity inferred at the onset  
 223 ( $\eta_{eff} = \eta_c$ ) represents the largest value of viscosity at which the transition  
 224 from jamming to motion takes place and it will then decrease ( $\eta_{eff} < \eta_c$ )  
 225 during the ascent of the diapir.

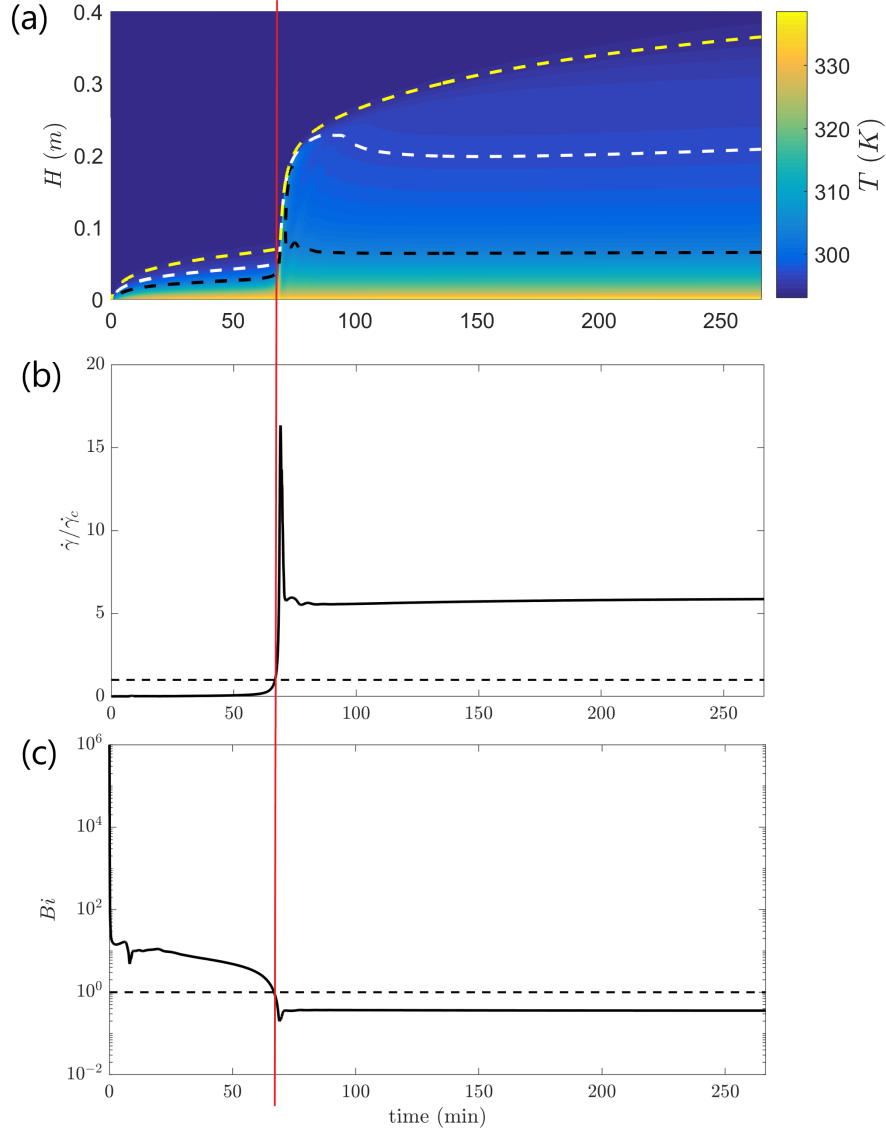


Figure 6: Development of a plume in a HB fluid, from simulation of Sgreva (2020b) ( $\Delta T = 44$  °C;  $\sigma_y = 0.076$  Pa;  $Y_{invC} = 7.44$ ;  $Ra \sim 10^5$ ). (a) Temporal evolution of temperature  $T$  along the central axis. Three isotherms have been highlighted: 21.0 °C (in yellow), 23.9 °C (in white) and 31.1 °C (in black). (b) Evolution of the strain rate  $\dot{\gamma}$  normalized by the critical strain rate  $\dot{\gamma}_c$  during the development and the rise of the hot instability. The critical strain rate is defined for  $Bi = \sigma_y / (K_v \dot{\gamma}_c^n) = 1$ . Dashed line indicated  $\dot{\gamma}/\dot{\gamma}_c=1$ . (c) Evolution of Bingham number. Dashed line indicated  $Bi=1$ . The vertical red line indicates when the Bingham number in (c) becomes one.

#### 226 4. Constraints on the diapirism at APMB and crust's rheology

227 An active and rising diapir has been suggested as the cause of the up-  
228 lift observed above the Altiplano-Puna Magma Body (Fialko and Pearse,  
229 2012; Comeau et al., 2015). Geodesy data and leveling data show in fact a  
230 continuous (since 1960s), nearly constant and slow uplifting of an about 100-  
231 km-wide region of the Altiplano-Puna volcanic complex (Fialko and Pearse,  
232 2012; Henderson and Pritchard, 2013; del Potro et al., 2013). The central  
233 area which is being uplifted at about 1 cm/yr is also surrounded by a broad  
234 ring of subsidence forming a global sombrero-shape uplift which is consistent  
235 with the presence of a diapir deep inside the crust. In this case the diapir  
236 would develop from the APMB within a framework of a heterogeneous crust  
237 and at greater depth than the brittle-ductile transition. The latter is reported  
238 between 4.5 and 10 km below the Altiplano (Jay et al., 2012) whereas the  
239 APMB extends from a depth of  $\sim 20$  km below the surface (Comeau et al.,  
240 2015).

241 In the previous section we have shown how that two main conditions  
242 must be satisfied to allow the ascent of a buoyant instability in a yield stress  
243 medium. The first one regards the inverse of the Yield number (here we  
244 consider  $Y_{inv} > Y_{inv_C} = 7.35 \pm 0.35$  from Sgreva (2020b)), while the second  
245 one is accounted by  $Bi \leq 1$ . Given these two conditions, one can evaluate  
246 the emplacement conditions for a buoyant instability (e.g. a diapir) in a  
247 jammed crustal mush with HB rheology. We do so for the case of APMB,  
248 assuming that the uplift measured at the surface originates from the rising  
249 of a hot diapir from the shallowest regions of the magmatic reservoir beneath  
250 Ulturuncu volcano and rises with a vertical velocity equal to what is measured

251 at the surface, i.e.  $v_z=1$  cm/yr (Fialko and Pearse, 2012).

252 In Fig. 7, we show conditions which lead to  $Y_{inv} = Y_{inv_C}$  for such a sys-  
253 tem. According to geodesy data (Fialko and Pearse, 2012; Gottsmann et al.,  
254 2017) and magnetotellurics (Comeau et al., 2016), we assume a characteris-  
255 tic diameter  $D_{diap}=10-100$  km for the diapir. The density contrast between  
256 diapir and surrounding crust is not well constrained and varies between dif-  
257 ferent models. Fialko and Pearse (2012) use in their numerical simulations a  
258 density difference of  $\Delta\rho=400$  kg/m<sup>3</sup>, whereas smaller values of  $\sim 100$  kg/m<sup>3</sup>  
259 are employed for example by Gottsmann et al. (2017) and Spang et al. (2019).  
260 A similar range of possible  $\Delta\rho$ , based on the inversion of gravity anomalies,  
261 is given by del Potro et al. (2013). An upper limit for the density contrast of  
262 400 kg/m<sup>3</sup> represents an enormous density anomaly produced by the melt-  
263 ing of a large enough amount of material below the observed diapiric body.  
264 Given a crust density of  $\rho_c=2700$  kg/m<sup>3</sup>, this scenario would require, for in-  
265 stance, the presence of a very large melt fraction ( $\phi_f$ ), that is  $\phi_f \sim 0.9$  for a  
266 dacitic melt with  $\rho_d=2300$  kg/m<sup>3</sup> (del Potro et al., 2013). On the other hand,  
267 an overall smaller density contrast reflects a smaller melt fraction which can  
268 decrease towards the limit of  $\Delta\rho=50$  kg/m<sup>3</sup> for a fully crystallized dacite  
269 ( $\phi_f=0$ ;  $\rho_d=2650$  kg/m<sup>3</sup>).

270 Within these ranges of diapir's size and density contrast, we find that  
271 a diapir can rise and deform the surrounding crust if the latter has a yield  
272 stress within a range of 0.5 and 15 MPa (Fig. 7). Larger values of yield  
273 stress clearly need either a broader instability or an unlikely larger density  
274 contrast. Here the yield stress has to be interpreted within the rheological  
275 definition, i.e. as the stress value needed to unjam a locked medium and to

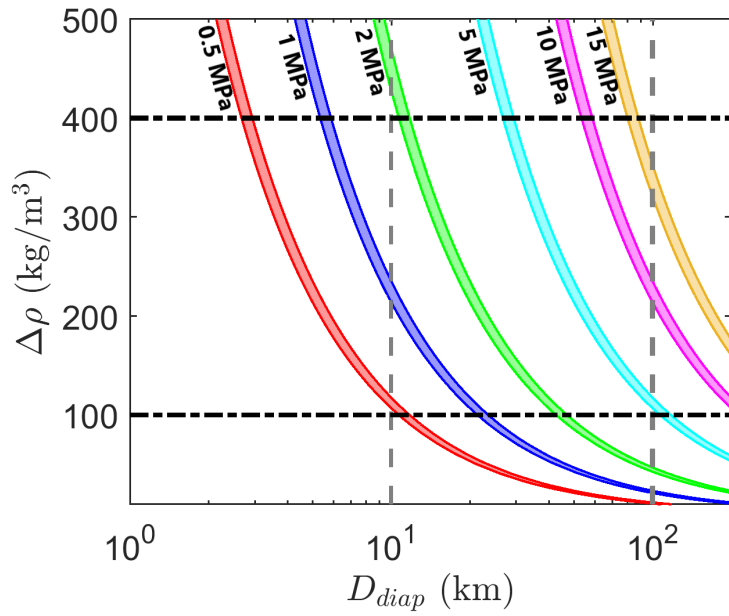


Figure 7: Yield stress (colored lines) allowing the development of a diapir from the top of the APMB according to  $Y_{inv_C} = 7.35 \pm 0.35$ , as function of diapir diameter and density contrast.

276 allow it to flow, rather than the threshold at which the medium simply loses  
 277 the reversibility in deformation.

278 Beside  $Y_{inv} > Y_{invC}$ , the other condition for motion is  $Bi \leq 1$ . As summa-  
 279 rized above, this critical condition translates into a critical minimum strain  
 280 rate required for motion  $\dot{\gamma}_c = (\sigma_y/K_v)^{(1/n)}$  and an effective viscosity is then  
 281 given by  $\eta_c = 2\sigma_y/\dot{\gamma}_c$  (eq. (4)). In Fig. 8 we display this viscosity as a  
 282 function of fluid consistency and the range of yield stress found previously  
 283 (i.e.  $\sigma_y$  in between 0.5 and 15 MPa). We take two limit values for the shear  
 284 thinning index, namely  $n=0.25$  (Fig. 8a) and  $n=0.5$  (Fig. 8b). They cor-  
 285 respond to stress exponents  $n_E=1/n$  in stress-strain relationships for creep  
 286 of 4 and 2, respectively, as expected for rocks Ranalli (1995). The viscosity  
 287 reported in Fig. 8 corresponds to the maximum effective viscosity calculated  
 288 from the minimum strain rate that guarantees  $Bi=1$ . As expected from its  
 289 definition, it depends on the value of fluid consistency that one uses in the  
 290 HB model. A way to bound the consistency is by taking into account the  
 291 maximum vertical velocity,  $v_{max}$ , at which the thermal instability is moving  
 292 upward. From the condition  $Bi \leq 1$ , one can in fact relate  $v_{max}$  to the size of  
 293 the instability and the critical strain rate:

$$v_{max} = C2r_{eq}\dot{\gamma}_c, \quad (5)$$

294 where  $C$  is an experimental constant. Based on numerical simulations (Sgreva,  
 295 2020b), the maximum velocity is found to scale as  $v_{max} \sim 4.45(2r_{eq}\dot{\gamma}_c)$  for  
 296 constant  $n=0.58$  (Fig. 9). The simulations of Massmeyer et al. (2013) where  
 297  $n$  was varied between 0.50 and 0.90 present the same trend (Fig. 9). The  
 298 small differences between the two studies for same  $n$  displayed in Fig. 9 can be

299 related to the different formulation of the numerical model used to simulate  
 300 plume’s formation, namely a regularized viscoplastic model in Massmeyer  
 301 et al. (2013) and an elasto-viscoplastic model in Sgreva (2020b).

302 Considering the recorded uplift velocity at the surface  $v_z$  as a possible  
 303 maximum rising velocity of the diapir, for the case at APMB the scaling of  
 304  $v_{max}$  translates to

$$v_z \sim 4.45 D_{diap} \dot{\gamma}_c, \quad (6)$$

305 leading to a critical strain rate of  $\dot{\gamma}_c = v_z / (4.45 D_{diap})$ . Within the chosen  
 306 interval of  $D_{diap}$ , the critical strain rate is  $\sim 10^{-15} - 10^{-16} \text{ s}^{-1}$ . The resulting  
 307 consistency is therefore

$$K_v = \sigma_y \dot{\gamma}_c^{-n} = \sigma_y \left( \frac{4.45 D_{diap}}{v_z} \right)^n. \quad (7)$$

308 This value of  $K_v$  is reported in Fig. 8 for the interval of diapir’s sizes of  
 309 10-100 km.

## 310 5. Discussion

311 Given the evidence of partial melt and the shallow ductile-brittle tran-  
 312 sition, a simple elastic model for the lower-middle crust beneath APVC is  
 313 not appropriate to properly describe the whole system but instead a more  
 314 complicated rheological model is required. The HB framework developed in  
 315 the previous sections provides estimates of the lower-middle crust effective  
 316 yield stress and viscosity at APMB.

317 The first crucial aspect regards the proper definition of yield stress needed  
 318 to evaluate the conditions of motion. Differently from the already mentioned

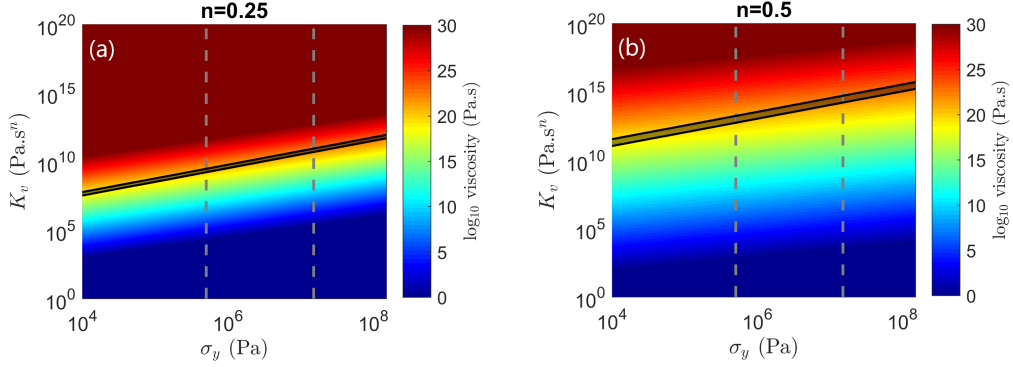


Figure 8: Maximum value of critical effective viscosity  $\eta_c$  (eq.4) corresponding to  $Bi=1$ , as function of consistency  $K_v$  and yield stress  $\sigma_y$ . Grey dashed lines bound the range of yield stress after Fig. 7. Black bands indicate  $K_v = \sigma_y(4.45 D_{diap}/v_z)^n$ , with  $D_{diap}$  between 10 and 100 km and an uplift velocity of  $v_z=1$  cm/yr (Fialko and Pearse, 2012). (a) Shear thinning exponent  $n=0.25$  and (b)  $n=0.5$ .

319 work of Weinberg and Podladchikov (1994), in our equation of the Yield  
 320 number,  $\sigma_y$  does not indicate the stress threshold needed to the brittle failure  
 321 of the rocks in the crust but it instead represents the threshold to unjam the  
 322 locked medium, which could for example involve reactivation of fractures and  
 323 creep. When  $Y_{inv}$  is defined to evaluate the ability of the system to transport  
 324 magma by opening new fractures it must involve yield strength for ambient  
 325 rocks in the order of  $10^2$ - $10^3$  MPa, making it dramatically difficult to achieve  
 326 conditions of  $Y_{inv} > Y_{invC}$ . However, the rheological (jamming) transition  
 327 in partially molten rocks that takes place when the solid-particles volume  
 328 fraction ( $\phi_s$ ) decreases approaching the maximum packing fraction ( $\phi_m \sim 0.6$ )  
 329 can lead to a strength drop which can span up to four orders of magnitude  
 330 (Rosenberg and Handy, 2005; Cashman et al., 2017). In addition to this  
 331 strong dependence on  $\phi_s$  and hence on the melt fraction  $\phi_f$ , the measurement



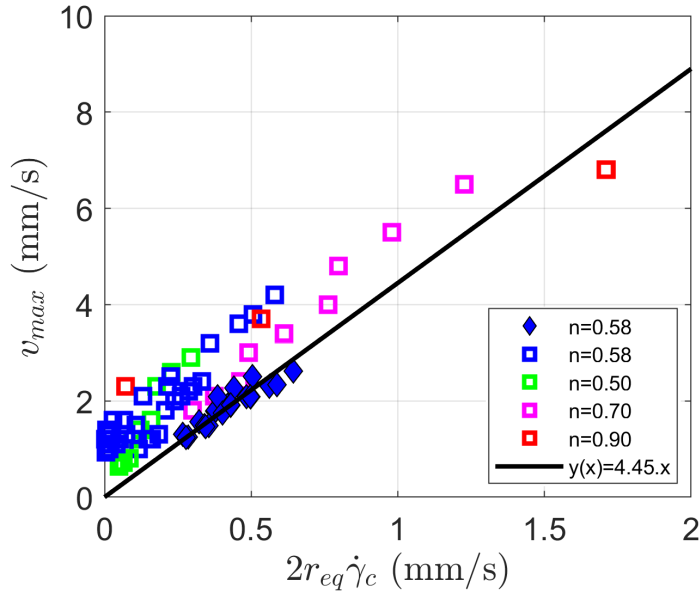


Figure 9: Maximum rising velocity of an hot instability as a function of the product between equivalent diameter  $D_{eq} = 2r_{eq}$  and critical strain rate. Diamond symbols refer to numerical simulations of thermal plumes in a yield stress fluid of Sgreva (2020b) computed with a power-law index  $n = 0.58$ . The later are fitted by the equation  $y(x) = 4.45x$ . Squared symbols refer to simulations of Massmeyer et al. (2013) and colors are for the different power-index  $n$  tested.

332 of the strength of a partially molten rock with relative large melt fraction  
 333 ( $\geq 0.3$ ) falls also very close to the minimum measurable value of  $\sigma_y$  from  
 334 experimental apparatus. The latter is estimated around  $\sim 1$  MPa (Pistone  
 335 et al., 2012; Rosenberg and Handy, 2005; Caricchi et al., 2007). In this  
 336 regard, the range of  $\sigma_y$  of 0.5-15 MPa we found in Fig. 7 for the hot ductile  
 337 crust that surrounds the rising diapir corresponds, in order of magnitude,  
 338 to the strength of partially molten granite with  $\phi_f \sim 0.25$  in Rosenberg and  
 339 Handy (2005) (where  $\sigma_y \sim 1$  MPa) and those for crustal granitic rocks on the  
 340 western Arabian Peninsula, where  $\sigma_y \sim 1-3$  MPa (Jónsson, 2012).

341 The second aspect that arises from the ascent of a diapir at APMB regards  
 342 the values of effective viscosity and strain rate we have found. According to  
 343 Fig. 7, a diapir of  $D_{diap}=50$  km and  $\Delta\rho=100$  kg/m<sup>3</sup> would set on motion and  
 344 would travel through a crust with yield stress of around  $\sigma_y=2.2$  MPa. By tak-  
 345 ing the typical stress exponent expected for creep mechanisms of lower-middle  
 346 crustal rocks, that is  $n_E=n^{-1}=3.0$  (Ranalli, 1997), the previous conditions  
 347 lead to a consistency of  $\sim 10^{13}$  Pa s<sup>0.3</sup> and to an effective maximum value  
 348 of viscosity for the lower-middle crust above APMB of  $\eta_c \sim 10^{21}$  Pa s. This  
 349 value corresponds to what is needed to trigger the rise of the diapir since it  
 350 is calculated from the critical condition of  $Bi=1$ . However, after the plume  
 351 onset,  $Bi$  continues to decrease (Fig. 6c) while the strain rate increases (Fig.  
 352 6b), leading in turn to values of effective viscosity that are lower than those  
 353 found for  $Bi=1$ . From eq. (6), considering a vertical velocity of 1 cm/yr, the  
 354 critical strain rate results in  $\dot{\gamma}_c \sim 10^{-15}$  s<sup>-1</sup> for a 50-km-wide diapir. Hence,  
 355 at conditions of  $Bi < 1$  where the strain rate can increase up to one order of  
 356 magnitude compared with  $\dot{\gamma}_c$  (Fig. 6b), we can expect a crustal region that

357 deforms at a strain rate of  $10^{-14} \text{ s}^{-1}$ . This corresponds to values of strain  
358 rate previously employed for APVC, e.g.  $\sim 10^{-14} \text{ s}^{-1}$  in Jay et al. (2012),  
359 and other compression areas, such as Southern-Tibet where  $\dot{\gamma} \sim 10^{-14}$ - $10^{-15}$   
360  $\text{s}^{-1}$  (Wang et al., 2019; Molnar, 2020) and Southern-Aegean where  $\dot{\gamma} \sim 10^{-15}$   
361  $\text{s}^{-1}$  (Kreemer and Chamot-Rooke, 2004; Kumar and Gordon, 2009).

362 Regarding the critical effective viscosity value, we found  $\eta_c \sim 10^{21} \text{ Pa s}$ .  
363 Such a high viscosity corresponds in order of magnitudes to the one of  
364 hot sub-solidus host rocks inside which magma bodies are usually emplaced  
365 (Sparks et al., 2019). To our knowledge, for the specific case at APMB there  
366 are not many independent constraints on the viscosity of the lower-middle  
367 crust. A list of them is reported in Table 1. The viscosity of the partially  
368 molten zone has been inferred from resistivity maps by Comeau et al. (2016)  
369 who estimated a viscosity of  $\eta \sim 10^{12} - 10^{16} \text{ Pa s}$  with 20% melt fraction for  
370 the shallow magma reservoir. Viscosity of around  $\eta \sim 10^{16} - 10^{18} \text{ Pa s}$  has  
371 been estimated by Fialko and Pearse (2012) by assuming a linear Maxwell  
372 viscoelastic rheology for the lower-middle crust. Similar values ( $< 10^{16} \text{ Pa s}$ )  
373 are obtained by using the same viscoelastic rheology for the structure be-  
374 neath APVC also by Gottsmann et al. (2017). However, although those  
375 values mainly represent either the viscosity of the APMB itself or that of  
376 the hot diapir rising from it, they do not give much information about the  
377 effective bulk viscosity of the whole inelastic crust. The latter should have  
378 in fact a reasonable larger value of  $\eta$  due to the contribution of the regions  
379 of the crust where both temperature and melt fraction are lower than the  
380 APMB's. Rheological measurements on larger timescales (i.e. millions of  
381 years) resulting from the analysis of lithosphere response to unloading of the

Table 1: Effective viscosities beneath APVC. "VE model" indicate simulations carried out with a viscoelastic (VE) rheology.

Technique	Viscosity (Pa s)	Reference
VE model	$\sim 10^{16} - 10^{18}$ for APMB	Fialko and Pearce (2012)
VE model	$< 10^{16}$ for APMB; $\sim 10^{16} - 10^{19}$ for diapir	Gottsmann et al. (2017)
VE model	$< 10^{21} - 10^{22}$ at $\sim 20$ km beneath APVC	Gerbault et al. (2005)
from resistivity model	$< 10^{16}$ for APMB with 20% melt	Comeau et al. (2016)
from paleo-lake load	$< 5 \times 10^{20}$ for crustal plate	Bills et al. (1994)

382 large paleo-lake in the Central Andes of Bills et al. (1994) give in fact a viscos-  
383 ity for the crustal plate that is larger than what predicted for APMB alone.  
384 The maximum effective bulk viscosity obtained in this way is  $\eta < 5 \times 10^{20}$   
385 Pa s, definitely closer to the estimation for the maximum critical viscosity  $\eta_c$   
386 we obtain by using a HB rheology (Fig. 8).

## 387 6. Conclusion

388 In this work we propose a mechanical interpretation for the well doc-  
389 umented uplift above APMB, based on the assumption that the effective  
390 rheology at large scale of the crust is the one of a yield stress material. In  
391 material with such rheology, the diapir take-off and growth require two local  
392 conditions: (1) the ratio between yield stress and viscous stress to be super-  
393 critical ( $Bi < 1$ ), and (2) the ratio between the buoyancy stress of the hot  
394 diapir and the yield stress to be larger than a critical value ( $Y_{inv} > Y_{invC}$ ).

395 We find that in order to allow the formation and the rise of a 10-100  
396 km-wide diapir from above APMB with a density contrast with respect to

397 surrounding rocks of 100-400 kg/m<sup>3</sup>, the lower ductile crust needs a yield  
 398 stress of ~0.5-15 MPa to respect condition (1). Moreover, from condition (2)  
 399 with an uplift velocity of 1 cm/yr, we can bound the maximum bulk effective  
 400 viscosity  $\eta_c$  for the APMB lower-middle crust at  $\eta_c \sim 10^{21}$  Pa s.

## 401 **Appendix A. Details on experiments of thermal plumes**

402 Figures 2 - 4 show the experiments on the development of thermal plumes  
 403 in Carbopol of Davaille et al. (2013). These experiments are carried out  
 404 by using a 166-mm-high rectangular tank into which the fluid is poured.  
 405 The fluid is heated by a circular heater located at the center of the bottom  
 406 surface. The maximal imposed temperature difference between the heater  
 407 and the ambient fluid is  $\Delta T \sim 44$  °C. The fluid rheology is described with  
 408 a HB model with the following parameters:  $\sigma_y=0.10$  Pa,  $n=0.54$ ,  $K_v=0.76$   
 409 Pa s<sup>*n*</sup>. For the case in Figs. 2 - 4, the Rayleigh number at the onset of motion  
 410 is

$$Ra = \frac{\alpha \rho g \Delta T h^3}{k \eta_c} \sim 10^6, \quad (\text{A.1})$$

411 with  $\alpha$  being the fluid thermal expansion ( $4.62 \times 10^{-4}$  K<sup>-1</sup>),  $\rho$  the density  
 412 (1142 kg/m<sup>3</sup>),  $k$  the thermal diffusivity ( $1 \times 10^{-7}$  m<sup>2</sup>/s),  $\eta_c$  the viscosity ob-  
 413 tained from eq. (4) and  $h$  the height of the tank. The critical Yield number  
 414 found in Davaille et al. (2013) ( $Y_{invC} = 8.8 \pm 0.7$ ) can be determined from eq.  
 415 (2) during stages (1) and (2) of plume development by assuming  $D=2r_{eq}$ ,  
 416 with  $r_{eq}$  being the equivalent radius of a sphere having the same volume as  
 417 the hot pocket. Experimentally, the hot pocket can be quantitatively de-  
 418 fined within the temperature field by the isotherm  $T_{lim} = 0.1 \Delta T$ , where

419  $\Delta T = T_{max} - T_{amb}$  and  $T_{max}$  is the heater temperature and  $T_{amb}$  the ambient  
420 temperature. The hot pocket is therefore represented by the volume of fluid  
421 with  $T \geq T_{lim}$ . For the density difference term in eq. (2) one can refer to the  
422 mean  $\Delta\rho$  within the fluid pocket, that is  $\Delta\rho \simeq \overline{\Delta\rho} = \alpha\rho(\overline{T}_{hot\ pocket} - T_{amb})$   
423 where  $\overline{T}_{hot\ pocket}$  is the average temperature of the pocket.

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428 **Data Availability**

429 The data underlying this article will be shared on reasonable request to  
430 the corresponding author.

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