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The performance of the hypergeometric np chart with estimated parameter

Arne Johannssen¹ Nataliya Chukhrova² Philippe Castagliola³

Abstract

Although it is well known that the performance of attribute control charts decreases significantly when the assumption of known process parameters is invalid, this assumption is prevalent in the pertinent literature. However, in most practical applications, the process parameters have to be estimated from a finite in-control Phase I sample, and therefore the performance of attribute control charts should be evaluated from the perspective of estimated process parameters. In this paper, we compare the run length properties of the hypergeometric np chart in both the known and estimated parameter cases. In particular, we investigate the required number of Phase I samples and new specific chart parameters that allow the hypergeometric np chart with estimated parameter p to have approximately the same in-control performance as in the known parameters case. Moreover, we perform a comprehensive in-control and out-of-control comparison of the hypergeometric np chart with its binomial counterpart. In order to achieve these objectives, we also present a new approach to effectively compute the probability distribution of the sum of independent and identically hypergeometric-distributed random variables. The proposed approximation reduces the computational effort to a few seconds while keeping a remarkable high accuracy with only negligible deviations compared to the exact distribution obtained via convolution.

Keywords: Quality control; attribute control charts; convolution; fraction nonconforming; run length properties

1 Introduction

Quality is an increasingly important decisive criterion for consumers to choose between different products or services. It is therefore of vital importance for all industries to produce quality products or offer quality services in order to remain competitive with their competitors. Processes that produce quality products can enable a manufacturing company to achieve good production yield, low production cost and products that exceed customer expectations. The area of Statistical Process Monitoring (SPM) provides a collection of powerful tools that employs statistical techniques to minimize the variability and ensures continuous quality improvement of processes (see e.g. Chong et al. [12]). The most important tools in SPM are control charts, which are well-suited to support measuring, monitoring, and improving of various kinds of processes. They help to distinguish common/chance from special/assignable causes of variation as a guide for decision making, and processes can be enhanced to perform consistently and predictably for higher quality, lower cost, and higher effective capacity. Over the years, and especially in recent times, numerous articles have been published on control charts to optimize process monitoring through various improvements, amendments, and adaptations to current practical needs, see e.g. Teoh et al. [40], Mitra et al. [31], Filho & Valk [18], Song et al. [37, 38], Nguyen et al. [35], just to name a few relevant works.

The majority of the literature on control charts is based on the assumption of known process parameters. In most practical situations, however, the process parameters are rarely known and they need to be estimated from a finite number of Phase I samples. It is therefore important to stress that the performance of control charts deteriorates significantly when the assumption of known parameters is invalid, due to the variability in parameter estimation during the in-control Phase I (see e.g. Chong et al. [12]). The problem of evaluating

¹University of Hamburg, Hamburg, Germany, arne.johannssen@uni-hamburg.de (corresponding author).

²University of Hamburg, Hamburg, Germany, nataliya.chukhrova@uni-hamburg.de.

³Université de Nantes & LS2N UMR CNRS 6004, Nantes, France, philippe.castagliola@univ-nantes.fr.

the performance of control charts when the parameters are estimated has been investigated by many authors, mostly with a focus on continuous, location-type, control charts (see e.g. Jones et al. [24], Nedumaran & Pignatiello [33], Chakraborti [7], Zhang et al. [43], Hu et al. [21], Hu & Castagliola [20], Motsepa et al. [32]) or dispersion-type control charts (see e.g. Maravelakis et al. [30], Maravelakis & Castagliola [29], Castagliola et al. [4], Castagliola & Maravelakis [2], Castagliola et al. [5]). Recently, there are also a lot of works focusing on the effects of parameter estimation on the performance of control charts that are worth to be mentioned, e.g. Zwetsloot & Woodall [44] (conditional performance of control charts), Chong et al. [10, 11] (optimal design of modified group runs charts), Hu et al. [22], Khoo et al. [25], Tang et al. [39] (design of EWMA median charts), and Lee et al. [28] (economic-statistical design of synthetic np charts). For literature reviews on the impact of parameter estimation on control charts performance we refer to Jensen et al. [23] and Psarakis et al. [36].

Since many quality characteristics can be classified as either conforming or nonconforming, attribute control charts such as p charts (for fraction of nonconforming units), np charts (for number of nonconforming units), c charts (for number of nonconformities), and u charts (for number of nonconformities per unit) are commonly used for monitoring attribute process data. Considering the performance of attribute control charts with estimated process parameters, there are relatively few articles to date (to the best of the authors' knowledge), e.g. Braun [1], Chakraborti & Human [8, 9], Castagliola & Wu [3], Tiplica [41], Hashemian et al. [19], Wu et al. [42], Faraz et al. [17], Lee & Khoo [27]. These papers deal with the derivation of run length properties for (Poisson) c charts as well as (binomial) p and np charts when the process parameters are estimated. However, all these papers (with the exception of Tiplica [41]), only focus on the in-control analysis and they do not propose a complete picture by also investigating the out-of-control performance of the corresponding control charts.

Recently, p charts based on the hypergeometric distribution have been proposed to account for the population size effect in periodical processes (see Chukhrova & Johannssen [13, 14]). These charts have a series of benefits including the following:

- They can be used for monitoring continuous and periodical processes.
- They take fluctuations of the underlying process into account.
- They do not require a constant probability being nonconforming for successively sampled units.
- They do not presume independence of successively sampled units.
- They are able to monitor processes with an infinite or a finite horizon.

In particular, Chukhrova & Johannssen [13] introduced the hypergeometric p chart with Shewhart-type control limits in the known parameter case, discussed the operating characteristic function with respect to the type I and II errors linked to the average run length (ARL), studied the impact of the sample and population size on the center line and the control limits, provided guidelines of specifying the appropriate sample size for specific scenarios and gave a practical application including comparative analysis with the binomial p chart. In addition, Chukhrova & Johannssen [14] presented the hypergeometric p chart with probability control limits, in turn in the known parameter case, performed a comprehensive sensitivity analysis in relation to the control limits of both types considering changes in all relevant parameters, gave a brief sensitivity analysis in relation to the ARL, and provided a practical application as well as a comparative study with the binomial p chart.

That is, hypergeometric p charts have been considered only in the case of known parameter and there is the need to extend the analysis to the more realistic (and thus more important) unknown parameter case and to study the effect of the parameter estimation on the control charts performance. To fill this gap, we introduce the hypergeometric np chart and discuss both the known and the unknown parameter case. The np chart

has the benefit that it deals with integer values, while the p chart deals with numbers that are not integer, neither real (even if one treat them as real numbers), i.e., np charts are more convenient to handle in practical applications. Further, we conduct a comprehensive in-control and out-of-control performance analysis of the hypergeometric np chart in both the known and estimated parameter case, that is, we investigate the overall impact of the parameter estimation on the control charts performance. We also compare these results with the results obtained for the binomial np chart, extending in this way the previous literature by performing an out-of-control analysis for the benchmark chart. Moreover, to increase the practical applicability of the proposed hypergeometric np chart, we investigate the required number of Phase I samples and provide alternative chart parameters in the estimated parameter case to have a similar in-control ARL as the one obtained when the parameter p is known.

To achieve these several objectives, we need to compute the probability distribution of the sum of independent and identically hypergeometric-distributed random variables. While convoluting random variables following either a Poisson or a binomial distribution is straightforward, convoluting hypergeometric-distributed random variables is not. To overcome this problem, we also propose a new approximation for the distribution of the sum of independent and identically hypergeometric-distributed random variables. This approximation has remarkable properties and may be helpful – beyond the problem discussed in this paper – in all areas, where the problem of convoluting hypergeometric-distributed random variables occurs.

The paper is organized as follows. In Section 2, we introduce the hypergeometric np chart in both the known and the estimated parameter cases and, moreover, we give a brief scheme of the implementation steps for these control charts in practical applications. In Section 3, we propose exact and approximate approaches for achieving the probability distribution of the sum of independent and identically hypergeometric-distributed random variables. Afterward, in Section 4, we perform both an in- and out-of-control analysis of the hypergeometric np chart in the known and the estimated parameter cases, and carry out comparisons with the binomial np chart. Section 5 presents an illustrative example considering the known and the unknown parameter case. In Section 6, concluding remarks are given.

2 The hypergeometric np chart

2.1 The case of known parameter p_0

Let us assume that Y_i , $i = 1, 2, \dots, k$, are k Phase II independent random variables corresponding to the number of nonconforming units obtained after sampling *without replacement* n units in a population of size $N > n$, $n, N \in \mathbb{N}^*$, containing an *unknown* proportion $p_1 \in [0, 1]$ of nonconforming units. By definition, Y_i , $i = 1, 2, \dots, k$, are hypergeometric random variables of parameters (N, n, p_1) , defined on $\{y_{\min} = \max(0, n - N(1 - p_1)), \dots, y_{\max} = \min(Np_1, n)\}$. Similarly to Chukhrova & Johannssen [13, 14], these random variables can be monitored using a hypergeometric np chart with the following Shewhart-type control limits

$$\text{LCL} = \max \left\{ 0, \left\lceil np_0 - K \sqrt{np_0(1 - p_0) \frac{N - n}{N - 1}} \right\rceil \right\}, \quad (2.1)$$

$$\text{UCL} = \left\lfloor np_0 + K \sqrt{np_0(1 - p_0) \frac{N - n}{N - 1}} \right\rfloor, \quad (2.2)$$

where $\lceil \dots \rceil$ and $\lfloor \dots \rfloor$ denote the rounded up and rounded down integer, p_0 is the *known* in-control proportion of nonconforming units and $K > 0$ is a constant to be fixed. Therefore, the probability θ that the number of nonconforming units Y_i , $i = 1, 2, \dots, k$, is outside the control limits is equal to

$$\theta = 1 - F_{\text{HYP}}(\text{UCL}|N, n, p_1) + F_{\text{HYP}}(\text{LCL} - 1|N, n, p_1),$$

where $F_{\text{HYP}}(y|N, n, p)$ is the c.d.f. of the hypergeometric distribution of parameters (N, n, p) , i.e.,

$$F_{\text{HYP}}(y|N, n, p) = \sum_{x=y_{\min}}^y \frac{\binom{[Np]}{x} \binom{[N(1-p)]}{n-x}}{\binom{N}{n}}.$$

The run length RL of the hypergeometric np chart is a geometric random variable of parameter θ , i.e., the p.m.f. and the c.d.f. of RL are defined for $\ell \in \{1, 2, \dots\}$ and they are equal to $f_{\text{RL}}(\ell) = \theta(1-\theta)^{\ell-1}$ and $F_{\text{RL}}(\ell) = 1-(1-\theta)^\ell$, respectively, and its first two moments are $\text{ARL} = \mathbb{E}[\text{RL}] = \frac{1}{\theta}$ and $\text{SDRL} = \sigma_{\text{RL}} = \frac{\sqrt{1-\theta}}{\theta}$.

2.2 The case of estimated parameter p_0

If the in-control proportion p_0 of nonconforming units is unknown, it has to be estimated from m Phase I independent random variables X_i , $i = 1, \dots, m$, corresponding to the number of nonconforming units obtained after sampling *without replacement* n units in an *in-control* population of size $N > n$ (i.e. containing a proportion $p_0 \in [0, 1]$ of nonconforming units). By definition, X_i , $i = 1, \dots, m$, are hypergeometric random variables of parameters (N, n, p_0) defined on $\{x_{\min} = \max(0, n - N(1 - p_0)), \dots, x_{\max} = \min(Np_0, n)\}$. An estimator \hat{p}_0 of p_0 is given by

$$\hat{p}_0 = \frac{1}{mn} \sum_{i=1}^m X_i = \frac{X}{mn}. \quad (2.3)$$

Since the estimator (2.3) is the sample mean, it is the best linear unbiased estimator (BLUE) of p_0 and satisfies the properties of consistency and efficiency [34].

However, X does in general not follow a hypergeometric distribution, apart from some special cases: $m = 1$ or $n = N$ or $p_0 \in \{0, 1\}$. Thus, we propose an appropriate method to achieve the probability distribution $f_X(x|m, n, N, p_0)$ of X in Section 3.

When p_0 is estimated by \hat{p}_0 , the Shewhart-type control limits of the hypergeometric np chart become

$$\widehat{\text{LCL}} = \max \left\{ 0, \left\lceil n\hat{p}_0 - K \sqrt{n\hat{p}_0(1-\hat{p}_0) \frac{N-n}{N-1}} \right\rceil \right\}, \quad (2.4)$$

$$\widehat{\text{UCL}} = \left\lfloor n\hat{p}_0 + K \sqrt{n\hat{p}_0(1-\hat{p}_0) \frac{N-n}{N-1}} \right\rfloor. \quad (2.5)$$

Let $\hat{\theta}$ be the probability that the number Y_i of nonconforming units in the i -th sample is outside the conditional control limits (that is, control limits $\widehat{\text{LCL}}$ and $\widehat{\text{UCL}}$ defined conditionally to $X = x$), i.e.,

$$\hat{\theta} = 1 - P \left(Y_i \leq \widehat{\text{UCL}} \mid X = x \right) + P \left(Y_i < \widehat{\text{LCL}} \mid X = x \right). \quad (2.6)$$

Replacing $\widehat{\text{LCL}}$ and $\widehat{\text{UCL}}$ in (2.6) by (2.4) and (2.5), respectively, we get

$$\begin{aligned} \hat{\theta} &= 1 - P \left(Y_i \leq \left\lfloor n\hat{p}_0 + K \sqrt{n\hat{p}_0(1-\hat{p}_0) \frac{N-n}{N-1}} \right\rfloor \mid X = x \right) \\ &\quad + P \left(Y_i \leq \left\lceil n\hat{p}_0 - K \sqrt{n\hat{p}_0(1-\hat{p}_0) \frac{N-n}{N-1}} \right\rceil - 1 \mid X = x \right). \end{aligned} \quad (2.7)$$

Replacing \hat{p}_0 in (2.7) by $\frac{X}{mn}$ (given by (2.3)) directly leads to

$$\begin{aligned}\hat{\theta} &= 1 - P\left(Y_i \leq \left\lfloor n \frac{X}{mn} + K \sqrt{n \frac{X}{mn} \left(1 - \frac{X}{mn}\right) \frac{N-n}{N-1}} \right\rfloor \middle| X = x\right) \\ &+ P\left(Y_i \leq \left\lfloor n \frac{X}{mn} - K \sqrt{n \frac{X}{mn} \left(1 - \frac{X}{mn}\right) \frac{N-n}{N-1}} \right\rfloor - 1 \middle| X = x\right)\end{aligned}$$

that can be simplified to

$$\begin{aligned}\hat{\theta} &= 1 - P\left(Y_i \leq \left\lfloor \frac{x}{m} + K \sqrt{\frac{x}{m} \left(1 - \frac{x}{mn}\right) \frac{N-n}{N-1}} \right\rfloor\right) \\ &+ P\left(Y_i \leq \left\lfloor \frac{x}{m} - K \sqrt{\frac{x}{m} \left(1 - \frac{x}{mn}\right) \frac{N-n}{N-1}} \right\rfloor - 1\right).\end{aligned}\quad (2.8)$$

Since $Y_i \sim \text{HYP}(N, n, p_1)$, we have

$$\begin{aligned}\hat{\theta} &= 1 - F_{\text{HYP}}\left(\overbrace{\left\lfloor \frac{x}{m} + K \sqrt{\frac{x}{m} \left(1 - \frac{x}{mn}\right) \frac{N-n}{N-1}} \right\rfloor}^{\text{conditional UCL}} \middle| N, n, p_1\right) \\ &+ F_{\text{HYP}}\left(\underbrace{\left\lfloor \frac{x}{m} - K \sqrt{\frac{x}{m} \left(1 - \frac{x}{mn}\right) \frac{N-n}{N-1}} \right\rfloor - 1}_{\text{conditional LCL}} \middle| N, n, p_1\right)\end{aligned}\quad (2.9)$$

Let RL be the run length of the hypergeometric np chart with estimated parameter p_0 . Since $X \sim \sum_{i=1}^m X_i$ is a random variable of parameters (m, n, N, p_0) defined on $x \in \{mx_{\min}, \dots, mx_{\max}\}$, the (unconditional) p.m.f. and c.d.f. of RL are

$$\begin{aligned}f_{\text{RL}}(\ell) &= \sum_{x=mx_{\min}}^{mx_{\max}} f_X(x|m, n, N, p_0) \hat{\theta} (1 - \hat{\theta})^{\ell-1} \\ F_{\text{RL}}(\ell) &= 1 - \sum_{x=mx_{\min}}^{mx_{\max}} f_X(x|m, n, N, p_0) (1 - \hat{\theta})^{\ell}\end{aligned}$$

where $f_X(x|m, n, N, p_0)$ is the p.m.f. of X (see Section 3 for computational details). The (unconditional) ARL and SDRL of the hypergeometric np chart with estimated parameter p_0 are then defined by

$$\text{ARL} = \sum_{x=mx_{\min}}^{mx_{\max}} f_X(x|m, n, N, p_0) \left(\frac{1}{\hat{\theta}}\right) \quad (2.10)$$

and

$$\text{SDRL} = \sqrt{\mathbb{E}[\text{RL}^2] - \text{ARL}^2}, \quad (2.11)$$

respectively, where

$$\mathbb{E}[\text{RL}^2] = \sum_{x=mx_{\min}}^{mx_{\max}} f_X(x|m, n, N, p_0) \left(\frac{2 - \hat{\theta}}{\hat{\theta}^2}\right). \quad (2.12)$$

Remark 2.1 *To allow adequate comparisons with the performance measures in the known parameter case (given $p_0 = \hat{p}_0$), the calculation of ARL and SDRL in the estimated parameter case should be performed under the condition of reasonable control limits. Due to the nature of Shewhart-type control limits, the (conditional) probability of a violation of the control limits can be equal to zero either for both cases (i.e., $\theta = \hat{\theta} = 0$) or only for the estimated parameter case (i.e., $\hat{\theta} = 0$ for some values of x , see (2.8)) that results in infinitely large values of ARL and SDRL. While in the first scenario both charts are equivalent, in the second scenario the performance measures of the hypergeometric np chart with estimated parameter p_0 would be biased. To overcome this bias, we propose to use $\widehat{\text{UCL}}$ given by (2.5) (which corresponds to UCL in the known parameter case, see (2.2)) instead of conditional UCL (see (2.8)) for affected values of x in the calculation of $\hat{\theta}$. This procedure reduces the bias in an appropriate way by considering $\hat{\theta} > 0$ instead of $\hat{\theta} = 0$, i.e., by implementing a reasonable conditional upper control limit $\text{UCL} < \min(N\hat{p}_0, n)$ and $\text{UCL} < \min(Np_1, n)$, respectively.*

2.3 Implementation of the proposed methods in practical applications

In this section we give a brief scheme of the basic implementation steps for the np chart in practical applications:

- ① Choose the appropriate np chart
 - Ⓐ by specifying whether the population size is finite or infinite and
 - Ⓑ by determining whether the known or estimated parameter case is present
- ② Calculate the center line and the control limits of the selected np chart
- ③ Compute in-control performance measures ARL_0 and SDRL_0 (where $p_1 = p_0$)
- ④ Compute out-of-control performance measures ARL_1 and SDRL_1 (where $p_1 = \tau p_0$ with $\tau > 1$)

To make the above implementation procedure illustrative, we provide a decision tree in Figure 1 with visualization of all implementation steps on the one hand, and on the other hand we give a detailed description of the individual steps in the following.

The first criterion (see step ①Ⓐ) for selecting the appropriate np chart is the type of the underlying process, i.e., whether the process to be monitored is continuous or periodical in nature. If the process is continuous, the population size is considered as infinitely large, while a periodical process implies a finite population size. To correctly account for the effect of a finite population size in periodical processes, the hypergeometric np chart must be chosen, otherwise (if the population size is infinitely large) the common binomial np chart can be used.

The second criterion (see step ①Ⓑ) for choosing the appropriate np chart is given by the knowledge of process parameter p_0 . The parameter p_0 can either be specified by the practitioner/researcher, for instance, by making reference to a nominal value or to a retrospective study on empirical data (known parameter case), or it should be estimated from retrospective process data (estimated parameter case). In the second case, the np chart must be implemented in two consecutive phases (see, e.g., Celano & Chakraborti [6]),

- Phase I: a preliminary retrospective study is carried out to bring the process to the in-control state and to get a reliable estimation of the process parameter p_0 ,
- Phase II: on-line process monitoring with the aim of checking the process stability during production,

while in the first case, the np chart can be implemented directly for on-line process monitoring (Phase II).

Next, the center line and the control limits have to be computed in the first place for on-line process monitoring in both cases (see step ②). In the second place, they also serve as the basis for the computation of

performance measures in the known parameter case, while conditional control limits (see (2.8)) are used for the calculation of single values of $\hat{\theta}$, conditionally to $X = x$, in the estimated parameter case.

Finally, specifying the fraction nonconforming $p_1 = p_0$ or $p_1 = \tau p_0$ with $\tau > 1$, i.e., as in-control or out-of-control fraction nonconforming, ARL_0 and $SDRL_0$ or ARL_1 and $SDRL_1$ can be calculated to make statements regarding process stability (see step ③) and/or shifts in the process quality level (see step ④).

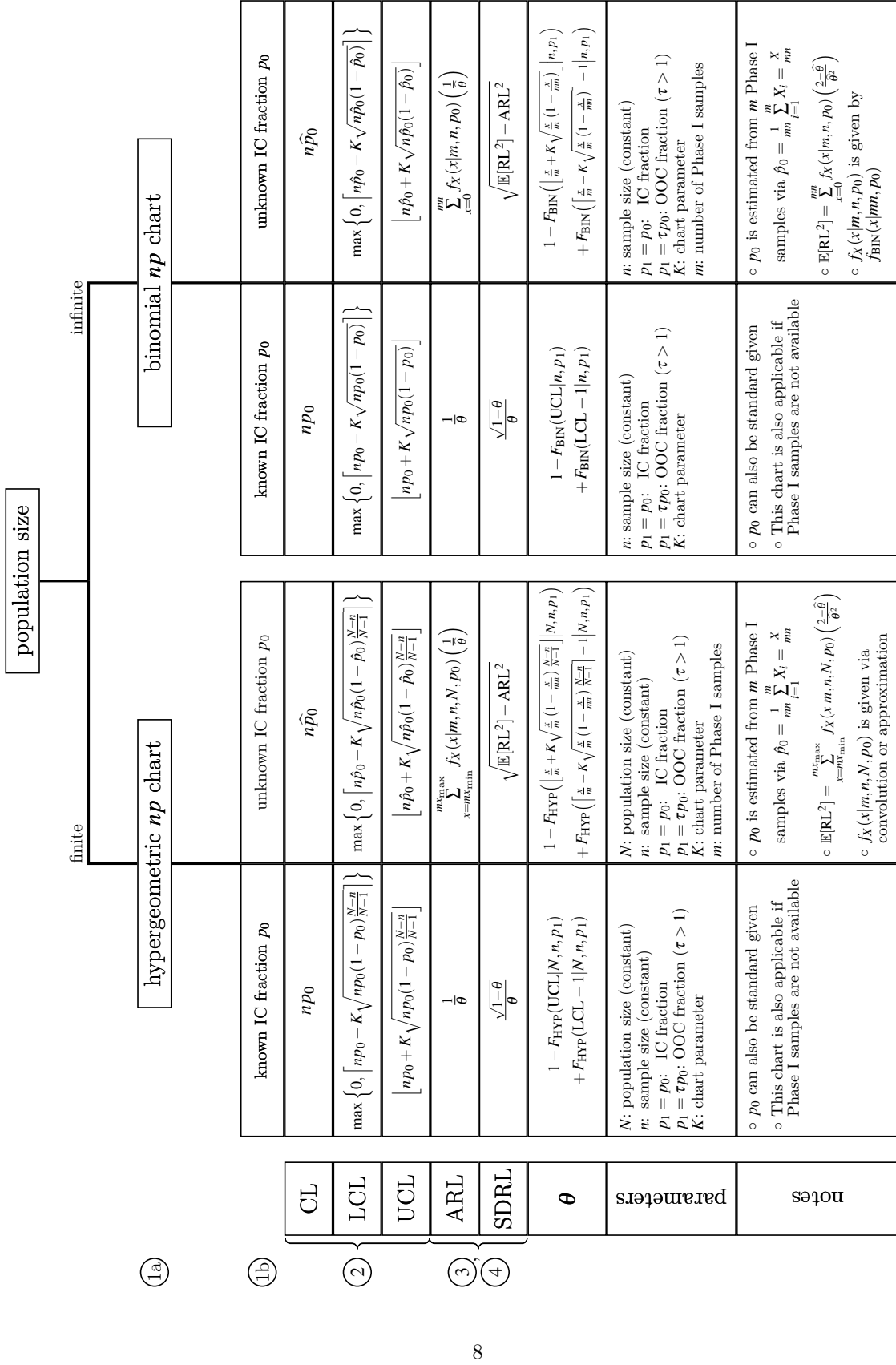


Figure 1: Decision tree for practical implementation of the appropriate np chart (IC = in-control, OOC = out-of-control)

3 Determining the probability distribution of X

3.1 Convolution

As a matter of fact, the random variable $X = \sum_{i=1}^m X_i$ is in general not hypergeometric-distributed. Thus, we need a practicable way to determine its probability distribution. Since X_1, \dots, X_m are i.i.d. random variables, this can be achieved by *convolution*.

Convolution is a direct method to calculate the probability distribution of X . The probability distribution of the sum of i.i.d. hypergeometric distributed random variables X_i , $i = 1, \dots, m$, is the convolution of their individual distributions. Some well known distributions have simple convolutions, e.g. binomial, geometric, Poisson, but unfortunately there is no simple convolution with regard to the hypergeometric distribution.

Regarding the hypergeometric case, the m -fold convolution of F_{X_i} and f_{X_i} can be obtained using the following recursive equations (based on general convolution equations, see e.g. Dickson [16])

$$F_X(s) = F_{X_i}^{(m)}(s) = \underbrace{F_{X_i} \otimes \dots \otimes F_{X_i}}_{\times m}(s) = \sum_{j=mx_{\min}}^s F_{X_i}^{(m-1)}(s-j)f_{X_i}(j) \quad (3.1)$$

$$f_X(s) = f_{X_i}^{(m)}(s) = \underbrace{f_{X_i} \otimes \dots \otimes f_{X_i}}_{\times m}(s) = \sum_{j=mx_{\min}}^s f_{X_i}^{(m-1)}(s-j)f_{X_i}(j) \quad (3.2)$$

where

$$\begin{aligned} F_{X_i}^{(0)}(s) &= 1 & \text{and} & & F_{X_i}^{(1)} &= F_{X_i} \\ f_{X_i}^{(0)}(s) &= \begin{cases} 1 & \text{for } s = 0 \\ 0 & \text{for } s > 0 \end{cases} & \text{and} & & f_{X_i}^{(1)} &= f_{X_i} \end{aligned}$$

and $s \in \{mx_{\min}, \dots, mx_{\max}\}$. Note that the order of convolution does not matter. Since there are no closed form solutions for F_X and f_X , the *analytical* calculation of F_X and f_X using convolution is impossible. In addition, the *numerical* calculation of F_X and f_X with help of (3.1) and (3.2), respectively, requires a very high computational effort for combinations of higher values of n ($n \geq 100$) and m ($m \geq 1000$).

3.2 The algorithm of De Pril [15]

As for the computation of F_X and f_X using smaller values of n and m , i.e., $n \leq 50$ and $m \leq 100$, there are recursive algorithms that can be utilized to calculate F_X and f_X significantly faster (while keeping a very high accuracy). The algorithm of De Pril [15] is such an efficient algorithm:

$$f_{X_i}^{(m)}(s) = P(X = s) = \begin{cases} (f_{X_i}(0))^m & \text{if } s = 0 \\ \frac{1}{f_{X_i}(0)} \sum_{j=1}^s ((m+1)\frac{j}{s} - 1) f_{X_i}(j) P(X = s-j) & \text{if } s \in \mathbb{N}^* \end{cases}$$

where X_i are i.i.d. (hypergeometric) random variables with $f_{X_i}(0) \neq 0$, $i = 1, \dots, m$. Since we are interested in low values of p ($p \ll 1$) in statistical process monitoring, $x_{\min} = 0$ is usually satisfied. Therefore, the algorithm of De Pril [15] can be used in its standard form given above (for $x_{\min} > 0$ see the algorithm in shifted form in De Pril [15]).

However, for mid-sized values of m ($100 < m < 1000$) the results of the algorithm by De Pril [15] converge to zero due to the fact that $(f_{X_i}(0))^m = 0$ using standard settings of statistical software, i.e., double-precision instead of variable-precision floating point numbers. On the other hand, the computation of F_X and f_X with variable-precision floating point numbers is very extensive for $m \geq 1000$ and thus can not be recommended for

the user. A further problem results in turn from above mentioned standard settings and is related to higher values of n or p , which entail substantial errors caused by numerous multiplication operations together with single infinitesimal hidden round-off errors and thus provide unreliable results. Summarized, the algorithm by De Pril [15] is appropriate for calculation of f_X and F_X using combinations of smaller values of m, n, p , i.e., $m \leq 100$, $n \leq 50$, $p \leq 0.1$.

3.3 A new approximation

In order to find a remedy in cases with higher values of m , n or p , we suggest to use a new *approximation* of F_X and f_X which is not based on the algorithm by De Pril [15]. This approximation considerably simplifies the calculation of F_X and f_X , since the sum of i.i.d. hypergeometric distributed random variables X_i , $i = 1, \dots, m$, is approximated by a hypergeometric-distributed random variable Z of parameters (mN, mn, p_0) , i.e.,

$$\begin{aligned} f_X(s) &\approx f_{\text{HYP}}(x|mN, mn, p_0) \\ F_X(s) &\approx F_{\text{HYP}}(x|mN, mn, p_0) \end{aligned}$$

Using this approximation, the time required for the computation of F_X and f_X can be reduced to a few seconds while keeping a remarkable high accuracy. It also allows to approximate the (unconditional) ARL and SDRL in (2.10) and (2.11). Moreover, numerical simulation results show that the higher the values of N , n and m , the better the approximation (see details in Section 4).

4 Numerical analysis

4.1 In-control performance

In Tables 2–8 and Table 9, the in-control ARL and SDRL values (i.e., ARL_0 and SDRL_0) are presented for the hypergeometric np chart and the binomial np chart, respectively, given $K = 3$ as well as

$$\begin{aligned} N &\in \{100, 200, 500, 1000, 2000, 5000, 10000\} && \text{(see Tables 2–8)} \\ n &\in \{25, 50, 75, 100\} && \text{(see blocks in Tables 2–9)} \\ m &\in \{10, 20, 50, 100, 200, 1000, \infty\} && \text{(see columns in Tables 2–9)} \\ p_0 &\in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\} && \text{(see rows in Tables 2–9)} \end{aligned}$$

The above specified values of the parameters N , n , m , p_0 were chosen for the following reasons:

- The values of N show the transition from a finite to an infinite population in Phase I and II.
- The values of n are common attribute-type sample sizes in Phase I and II.
- The finite values of m imply the case of estimated parameter p_0 from a Phase I sample and allow to consider different Phase I lengths (short, middle, long), while $m \rightarrow \infty$ corresponds to the case of known parameter p_0 in Phase II.
- The values of p_0 show the transition from low to larger fractions nonconforming. They can be estimated from a Phase I sample using estimator (2.3).

It should be noted that the in-control values for the hypergeometric np chart are calculated using the approximation of $X = \sum_{i=1}^m X_i$ via $Z \sim \text{HYP}(mN, mn, p_0)$ discussed in Section 3.3 for $m \in \{10, 20, 50, 100, 200, 1000\}$ (estimated parameter case) under the condition of reasonable control limits (see Remark 2.1). As for $m \rightarrow \infty$ (known parameter case), the in-control values for the hypergeometric np chart are obtained by using exact hypergeometric distribution (see Section 2.1).

The reasons for using the approximate results are as follows. We have conducted comprehensive comparisons of the hypergeometric and approximate hypergeometric np charts and found that the values of exact ARL_0 and $SDRL_0$ are throughout approximately equal to the respective values of approximate ARL_0 and $SDRL_0$, and there is (i) no tendency for a systematic deviation ($ARL_{HYP} - ARL_{HYP\text{appr.}}$, $SDRL_{HYP} - SDRL_{HYP\text{appr.}}$) to one direction regarding n , (ii) a negative tendency regarding p_0 for smaller values of N ($N \leq 100$), and (iii) a positive tendency regarding m and smaller values of N . Moreover, when N, n, m or p_0 increases, the difference between exact and approximate values for $ARL_0, SDRL_0$ decreases in a monotonic way and seems to converge to zero. For instance, the maximum of the relative deviation regarding ARL_0 ($\frac{|ARL_{HYP} - ARL_{HYP\text{appr.}}|}{ARL_{HYP}} \cdot 100\%$) is 2.21% for $N = 100$ and 0.07% for $N = 10000$. We mostly observe relative deviations regarding ARL_0 that are $< 0.1\%$ for $N \leq 1000$ and $< 0.05\%$ for $N > 1000$. Due to the excellent approximation accuracy and with the purpose of reducing the number and size of the tables, we have refrained from explicitly reporting the exact results in this paper.

We have also verified the obtained results in Tables 2–8 by conducting an additional simulation study. In particular, for selected combinations of $(m, N, n, p_0, \tau = 1, K = 3)$, we have computed ARL_0 in the estimated parameter case via $ARL_0^{\text{sim}} = \frac{ARL_0^{(1)} + ARL_0^{(2)} + \dots + ARL_0^{(s)}}{s}$ by repeating the following two steps $s = 10^3$ times:

1. Generate a vector of m hypergeometric random variables X_1, \dots, X_n of parameters (N, n, p_0) and compute $\widehat{p}_0, \widehat{LCL}, \widehat{UCL}$ using (2.3), (2.4), (2.5). Recalculate this step if $\widehat{LCL} = 0 \cup (\widehat{UCL} \geq \min(N\widehat{p}_0, n)) \cup (\widehat{UCL} < \min(Np_0, n))$, i.e., in line with the approach of reasonable control limits.
2. Generate a vector of $r = 10^6$ hypergeometric random variables Y_1, \dots, Y_r of parameters (N, n, p_1) with $p_1 = \tau p_0$, calculate $\widehat{\theta} = \frac{\#\{(Y_i < \widehat{LCL}) \cup (Y_i > \widehat{UCL})\}}{r}$ and compute simulated $ARL_0 = \frac{1}{\widehat{\theta}}$.

Selected results of the simulation study are shown in Table 10. As expected, the smaller the exact values of ARL_0 , the smaller the absolute deviations of the simulated values from the exact ones. The mean percentage deviation between exact and simulated values of ARL_0 is around 1%, thus confirming the accuracy of the results obtained using the exact formulas.

Analyzing Tables 2–9, we obtain the following results:

- ① Estimated parameter case (finite values of m):
 - An increase in N mostly leads to a decrease of ARL_0 and $SDRL_0$.
 - An increase in n provides as a tendency an increase of ARL_0 and $SDRL_0$, but with some exceptions (in particular when $N \leq 200$ or $p_0 \geq 0.15$).
 - An increase in m mostly leads to a decrease of ARL_0 and $SDRL_0$, but with some exceptions (in particular when $p_0 \geq 0.15$ and/or $N \leq 200$).
 - An increase in p_0 up to 0.1 mostly implies an increase of ARL_0 and $SDRL_0$, while a further increase in p_0 leads as a tendency to a decrease of ARL_0 and $SDRL_0$. Moreover, there is as a rule a decreasing behavior of ARL_0 and $SDRL_0$ for lower values of m ($m \leq 20$) in combination with $n \geq 75$ when p_0 increases, but an increasing behavior for larger values of m and any values of n .
- ② Known parameter case ($m \rightarrow \infty$): The conclusions are similar as obtained in ①, except for the results regarding m and p_0 . In particular, when p_0 increases ARL_0 and $SDRL_0$ can increase or decrease.
- ③ Comparison of the estimated and known parameter cases:
 - The values of ARL_0 and $SDRL_0$ differ in general in the known and in the estimated parameter case. In particular, ARL_0 and $SDRL_0$ in the estimated parameter case can be either larger or smaller compared to the known parameter case, i.e., there is no clear tendency for positive or negative differences.

- When N, n, m or p_0 increases, the difference in terms of ARL_0 (between the known and estimated parameter case) tends to decrease but not always in a monotonic way.
- For $N = n = 100$, we have a total inspection of the population and consequently infinitely large values of ARL_0 and $SDRL_0$ in both cases due to the value of the type I error that is equal to zero. In addition, for $N \in \{100, 200\}$ and $p_0 \in \{0.01, 0.02\}$, the values of ARL_0 and $SDRL_0$ can in turn be infinitely large (see Tables 2–3). The reason for these exceptions is given by the fact that these parameter combinations do not ensure reasonable control limits, and thus the (conditional) probability of a violation of the control limits is equal to zero for some values of x in the estimated parameter case as well as throughout in the known parameter case.

④ Comparison of the hypergeometric and binomial np charts (estimated parameter case):

- The values of ARL_0 and $SDRL_0$ are mostly larger with regard to the hypergeometric np chart compared to the binomial np chart, with only a few exceptions (for $N \leq 200$).
- As a consequence of an increase in N , the difference between $ARL_0, SDRL_0$ of both charts decreases and converges to zero.
- There is the tendency of a decreasing difference between $ARL_0, SDRL_0$ of both charts when m or p_0 increases, but with a few exceptions.
- In contrast, there is no clear tendency regarding the difference between $ARL_0, SDRL_0$ of both charts for larger values of N ($N \geq 2000$) when n changes. For smaller values of N ($N \leq 1000$) this difference seems to increase with an increasing n .

⑤ Comparison of the hypergeometric and binomial np charts (known parameter case):

- The values of ARL_0 and $SDRL_0$ are mostly larger in the hypergeometric case compared to the binomial case, with only few exceptions (mostly for $n = 25, 100$).
- For an increasing value of N , the absolute difference between $ARL_0, SDRL_0$ for both charts decreases and converges to zero.
- For increasing values of n and p_0 , the absolute difference between $ARL_0, SDRL_0$ tends to decrease.

4.2 Required number of Phase I samples allowing similar ARL_0 in both cases

As the values of ARL_0 of the hypergeometric np chart differ in the known and in the estimated parameter case, an interesting question arises how large the number m of Phase I samples should be in order to have approximately the same ARL_0 values in both the known and estimated parameter cases, given the same chart parameter $K = 3$. In Table 11 computed values of m for $N \in \{100, 200, 500, 1000, 2000, 5000, 10000\}$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.1, 0.15, 0.2\}$ are presented, satisfying

$$\Delta = \frac{|\text{ARL}_{0,m} - \text{ARL}_{0,\infty}|}{\text{ARL}_{0,\infty}} \leq 0.05.$$

The computation of m was provided using the approximation of $X = \sum_{i=1}^m X_i$ via $Z \sim \text{HYP}(mN, mn, p_0)$ discussed above and in Section 3.3. Depending on the values of N, n and p_0 , the value of m , complying with the constraint on the relative difference between the in-control $ARL_{0,m}$ (estimated parameter case) and the in-control $ARL_{0,\infty}$ (known parameter case), varies between 3 and 8060 and, in some cases, can be larger than 10000. The exceptional cases where we have non-existent values stem from combinations of small values of N and p_0 mentioned above.

In particular, for $n \leq 50$ ($n \geq 75$) and increasing N there is a positive (no) trend regarding m . Further, there is no tendency with respect to m for increasing n or p_0 . As for a comparison with the binomial case (see Castagliola & Wu [3]), the number of cases with m larger than 10000 can be a bit larger (+1) for $n = 75$ or a bit smaller (1 – 3) for other values of n with respect to the binomial value. In addition, the results of the approximate hypergeometric case converge to the respective results of the binomial case for $N = 10000$.

4.3 Alternative chart parameters allowing similar ARL_0 in both cases

Since there are (as in the binomial case) several cases where $m > 10000$, we propose to compute alternative chart parameters K' which take the value of m into account and simultaneously allow the value of ARL_0 of the estimated parameter case to be as close as possible to the value of ARL_0 of the known parameter case using the above mentioned approximation. These values are presented in Tables 12–18 for $N \in \{100, 200, 500, 1000, 2000, 5000, 10000\}$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$ and $m \in \{10, 20, 50, 100, 200\}$. For example, if $N = 1000$, $n = 50$, $p_0 = 0.05$ and $m = 10$ (see Table 15), the alternative chart parameter is given by $K' = 2.87$ and, in this case, $ARL_0 = 420.6$ ($SDRL_0 = 2109.6$). Referring to Table 5, ARL_0 corresponding to $m \rightarrow \infty$ (i.e., the known parameter case) is $ARL_0 = 424.1$. It is worth noting that the use of the new constant $K' = 2.87$ (instead of $K = 3$) allows to reduce ARL_0 from $ARL_0 = 586.6$ to $ARL_0 = 420.6$ (close to 424.1) but it also allows to reduce $SDRL_0$ from $SDRL_0 = 3088.8$ to $SDRL_0 = 2109.6$. In turn, there are some cases of non-existent values due to combinations of small values of N and p_0 .

4.4 Out-of-control performance of the hypergeometric np chart

In Tables 19–25, the out-of-control ARL and SDRL values (i.e., ARL_1 and $SDRL_1$) are presented for the hypergeometric np chart, given $K = 3$ (see triples $(K, ARL_1, SDRL_1)$ in the first line of each cell). These out-of-control values are calculated using the approximation of $X = \sum_{i=1}^m X_i$ via $Z \sim \text{HYP}(mN, mn, p_0)$ discussed in Section 3.3 for $m \in \{10, 20, 50, 100, 200, 1000\}$ (estimated parameter case) under the condition of reasonable control limits (see Remark 2.1). As for $m \rightarrow \infty$ (known parameter case), the out-of-control values are obtained by using exact hypergeometric distribution (see Section 2.1).

In addition, we have verified the obtained results in Tables 19–25 by conducting a simulation study. In particular, for selected combinations of $(m, N, n, p_0, \tau, K = 3)$, we have computed ARL_1^{sim} in the estimated parameter case using the same procedure as for simulation of ARL_0 in Section 4.1, but with an adjustment of τ , i.e., $\tau > 1$ instead of $\tau = 1$. Selected results of the simulation study are shown in Table 27. Comparing the exact and simulated results leads to the same conclusions as discussed in Section 4.1.

The results of the out-of-control performance analysis of the hypergeometric np chart are given in ①–③ below. Moreover, we give the chart parameters K'' , which allow the binomial np chart to obtain an ARL_0 as close as possible to the ARL_0 in the hypergeometric case, and present respective ARL_1 , $SDRL_1$ (see triples $(K'', ARL_1, SDRL_1)$ in the second line of each cell). Comparing the triples $(K, ARL_1, SDRL_1)$ with $(K'', ARL_1, SDRL_1)$ leads to the results presented in ④–⑤ below.

Similar to the in-control performance analysis, we consider the following parameter values:

$N \in \{100, 200, 500, 1000, 2000, 5000, 10000\}$	(see Tables 19–25)
$n \in \{25, 50\}$	(see blocks in Tables 19–25)
$m \in \{10, 20, 50, 100, 200, 1000, \infty\}$	(see columns in Tables 19–25)
$p_0 \in \{0.01, 0.05, 0.10, 0.20\}$	(see areas within blocks in Tables 19–25)
$\tau \in \{1.1, 1.2, 1.5, 2.0\}$	(see rows in Tables 19–25)

excluding $n = 75, 100$ and $p_0 = 0.02, 0.15$, in order to keep the tables manageable and to focus the out-of-control analysis on the most common parameter values. The out-of-control fraction nonconforming p_1 is calculated via multiple τ , $\tau > 1$, of the in-control fraction nonconforming p_0 , i.e., $p_1 = \tau p_0$. Thus, we consider uniform proportional shifts in the process fraction nonconforming by means of $\tau = \frac{p_1}{p_0}$. Since the detection of a significant deterioration of the process quality is crucial, we analyze values of τ that represent realistic upward shifts in the process fraction nonconforming (10%, 20%, 50%, 100%).

It should be noted that there are combinations of very low values of N, p_0 and τ , where the population size is too low for identifying very small shifts in the process quality level. This applies for the following combinations: $N = 100, p_0 = 0.01, \tau \leq 1.5$; $N = 200, p_0 = 0.01, \tau \leq 1.2$; $N = 500, p_0 = 0.01, \tau = 1.1$; $N = 100, p_0 = 0.05, \tau = 1.1$. In these cases, $ARL_0, SDRL_0$ instead of $ARL_1, SDRL_1$ are computed, which is why these values are not given in Tables 19–21. Consequently, these cases, as well as the cases where $ARL_0 \rightarrow \infty$ (see Tables 2–3), are excluded from the out-of-control analysis.

The following results are obtained from the analysis of Tables 19–25:

- ① Estimated parameter case (finite values of m):
 - An increase in N in combination with small values of p_0 ($p_0 = 0.01, 0.05$) generally leads to a decrease of ARL_1 and $SDRL_1$. In contrast, an increase in N in combination with larger values of p_0 ($p_0 = 0.10, 0.20$) mostly results in an increase of ARL_1 and $SDRL_1$ for $n = 25$ and in an increase or a decrease for $n = 50$.
 - An increase in n provides as a tendency a decrease of ARL_1 and $SDRL_1$. This behavior is the more distinct, the larger p_0, τ and the lower m , i.e., the number of exceptions (that is, increasing values of $ARL_1, SDRL_1$) increases for lower values of p_0 in combination with lower values of τ and larger values of m ($p_0 = 0.01, 0.05, \tau = 1.1, 1.2, m \geq 100$).
 - An increase in m generally leads to a decrease of ARL_1 and $SDRL_1$, but with exceptions for $N \leq 200$ in combination with $n = 25$, where an increase of ARL_1 and $SDRL_1$ is also possible.
 - An increase in p_0 mostly implies a decrease of $ARL_1, SDRL_1$ for $p_0 \geq 0.05$ and $\tau \geq 1.2$. Considering $\tau = 1.1$ especially in combination with smaller values of p_0 ($p_0 \leq 0.05$), there is mainly an increase of ARL_1 and a decrease of $SDRL_1$.
 - An increase in τ provides a decrease of both ARL_1 and $SDRL_1$.
- ② Known parameter case ($m \rightarrow \infty$): The conclusions are quite similar as the ones obtained in ①. In general, the following applies:
 - The larger N , the lower $ARL_1, SDRL_1$, except for some cases with $n = 50$ and $N \leq 500$, where ARL_1 and $SDRL_1$ increase with an increasing value of N .
 - The larger n , the larger $ARL_1, SDRL_1$, except for cases with $n = 50$ and $N \leq 500$, where ARL_1 and $SDRL_1$ decrease with an increasing value of n .
 - An increase in p_0 mostly implies a decrease of $ARL_1, SDRL_1$ with some contrary exceptions for $N \leq 500$.
 - The larger τ , the lower $ARL_1, SDRL_1$.
- ③ Comparison of the estimated and known parameter cases:
 - The values of ARL_1 and $SDRL_1$ differ in general in the known and in the estimated parameter case. In particular, for $N \geq 500$ in combination with $n = 25$, $ARL_1, SDRL_1$ are larger in the estimated parameter case compared to the known parameter case, while for $N \leq 200$ they can be either larger or smaller compared to the known parameter case. For $n = 50$, there is no clear tendency for positive or negative differences, except for $p_0 = 0.01$ in combination with $N \geq 500$, where $ARL_1, SDRL_1$ in the known parameter case are smaller than in the estimated parameter case.
 - When N, n, m, p_0 or τ increases, the absolute difference in terms of ARL_1 (between the known and estimated parameter case) tends to decrease but not always in a monotonic way.
- ④ Comparison of the hypergeometric and binomial np charts (estimated parameter case):

- The values of ARL_1 and $SDRL_1$ are mostly lower (or equal) for the hypergeometric np chart compared to the binomial np chart for $N \leq 5000$. Considering $N = 10000$, this behavior changes slightly, i.e., the values of ARL_1 and $SDRL_1$ differ for both charts but with the same tendency.
- As a consequence of an increase in N , the difference between $ARL_1, SDRL_1$ of both charts decreases and converges to zero.
- There is no clear tendency regarding the difference between $ARL_1, SDRL_1$ of both charts for different values of n, m, p_0, τ .
- In general, the value of K'' is the closer to 3, the larger the value of N , regardless of n, m, p_0 (there is no impact of τ on K''). There are only a few exceptions for $N = 100, 200$, where $K'' < 3$ instead of $K'' \geq 3$ (with a maximum positive deviation of +1.25 for $N = 100$). That is, considering smaller values of N , K'' is often biased upwards in the binomial case. While larger values of p_0 ($p_0 = 0.1, 0.2$) rather lead to values of K'' close to $K = 3$ compared to smaller values of p_0 ($p_0 = 0.01, 0.05$), there is no clear pattern regarding the effect of an increasing value of m and n on K'' .

⑤ Comparison of the hypergeometric and binomial np charts (known parameter case):

- Since K'' is mostly equal to 3 in the known parameter case for the binomial np chart, we refer to the respective interpretations regarding Table 26 in Section 4.5. It should be noted that there are some values of K'' that are different from 3, but they do not change the interpretation results.

4.5 Out-of-control performance of the binomial np chart

As for the out-of-control performance of the binomial np chart, the respective ARL_1 and $SDRL_1$ values are provided for $K = 3$ in Table 26, and we get the results summarized in ①-③ below. Afterward we compare the values of Table 26 with the respective values for the hypergeometric np chart (given in the first row of each cell of Tables 19-25), and obtain results summarized in ④-⑤ below. It should be noted that in the cases where we refer to the effect observed for the hypergeometric np chart, interpretations concerning N are by implication not applicable.

① Estimated parameter case (finite values of m):

- The impact of n, p_0, τ on $ARL_1, SDRL_1$ is the same as in the hypergeometric case.
- The general impact of m on $ARL_1, SDRL_1$ is in turn the same as in the hypergeometric case, but with exceptions for $m \geq 200$ in combination with $p_0 = 0.05, 0.10$, which provide an increase of ARL_1 and mostly an increase of $SDRL_1$.

② Known parameter case ($m \rightarrow \infty$):

- Contrary to the hypergeometric case, an increasing n leads to larger values of $ARL_1, SDRL_1$ for $p_0 \leq 0.05$ and to lower values of $ARL_1, SDRL_1$ for $p_0 \geq 0.1$.
- There is no clear effect of a change in p_0 . In particular, when p_0 increases, ARL_1 and $SDRL_1$ can increase or decrease.
- The impact of τ on $ARL_1, SDRL_1$ is the same as in the hypergeometric case.

③ Comparison of the estimated and known parameter cases:

- The values of ARL_1 and $SDRL_1$ differ in general in the known and in the estimated parameter case, i.e., there is no clear tendency for positive or negative differences.
- When n, m, p_0, τ increases, the absolute difference in terms of ARL_1 (between the known and estimated parameter case) tends to decrease but not always in a monotonic way.

④ Comparison of the hypergeometric and binomial np charts (estimated parameter case):

- The values of ARL_1 and $SDRL_1$ differ for both np charts. In particular, for $p_0 = 0.01, 0.05$ in combination with $\tau = 1.1, 1.2$ and for $p_0 = 0.1, 0.2$ in combination with $\tau = 1.5, 2.0$, there are larger and lower values of $ARL_1, SDRL_1$ for the hypergeometric np chart compared to the binomial np chart, respectively.
- As a consequence of an increase in N , the absolute difference between $ARL_1, SDRL_1$ for both charts decreases and converges to zero.
- When m increases, the absolute difference between $ARL_1, SDRL_1$ for both charts decreases. There is on trend the same behavior for an increasing value of n, p_0, τ .

⑤ Comparison of the hypergeometric and binomial np charts (known parameter case):

- The values of ARL_1 and $SDRL_1$ are mostly lower for $N \leq 500$ and larger for $N \geq 1000$ in the hypergeometric case compared to the binomial case.
- For an increasing value of N , the absolute difference between $ARL_1, SDRL_1$ for both charts decreases and converges to zero. The same holds for an increasing value of τ .
- For an increasing value of n and a decreasing value of p_0 , the absolute difference between $ARL_1, SDRL_1$ for both charts decreases.

4.6 Summary of numerical analysis

In the following, we present summarized results for the in-control and out-of-control performance analysis:

Section 4.1:

1. Given unknown parameter p_0 , the hypergeometric np chart with estimated parameter is preferable to the hypergeometric np chart with known parameter, since the values of $ARL_0, SDRL_0$ differ in general in both cases, and the absolute difference in terms of ARL_0 generally decreases when N, n, m or p_0 increases.
2. The exact $ARL_0, SDRL_0$ are throughout approximately equal to the respective approximate $ARL_0, SDRL_0$ with negligible relative deviations. As the absolute difference between exact and approximate $ARL_0, SDRL_0$ converges to zero when N, n, m, p_0 increases, the new approximation is preferable for calculations due to considerable reductions of computational time, in particular for larger parameter values.
3. The lower N, m, p_0 , the more preferable the hypergeometric np chart compared to its binomial counterpart, in the known and estimated parameter case. This result is due to the following two facts:
 - Considering the hypergeometric np chart, larger values of N, m and/or lower values of n mostly lead to a decrease of ARL_0 in the estimated parameter case. The same holds for the known parameter case (except for m by implication).
 - ARL_0 is in general larger for the hypergeometric np chart compared to the binomial np chart in both cases, and there is the tendency of a decreasing difference in terms of ARL_0 when N, m, p_0 increases (estimated parameter case) and when N increases or n, p_0 decreases (known parameter case).

Section 4.2:

The value of m , which is needed to obtain run length properties as in the known parameter case for the hypergeometric np chart with estimated parameter p_0 and 3σ control limits (i.e., $K = 3$), can strongly vary for several combinations of N, n, p_0 . This result is similar to the binomial case.

Section 4.3:

The use of an alternative chart parameter K' (especially dedicated to the number m of Phase I samples) allows ARL_0 corresponding to the estimated parameter case to be as close as possible to ARL_0 corresponding to the known parameter case. These new chart parameters also enable to reduce $SDRL_0$ of the hypergeometric np chart in the estimated parameter case.

Sections 4.4 and 4.5:

1. Given unknown parameter p_0 , the hypergeometric np chart with estimated parameter is preferable to the hypergeometric np chart with known parameter, since the values of $ARL_1, SDRL_1$ differ in general in both cases and the absolute difference in terms of ARL_1 tends to decrease for increasing values of N, n, m or τ .
2. The hypergeometric np chart is preferable compared to its binomial counterpart in situations with lower N in combination with lower n, m, p_0, τ . This result is due to the following two facts:
 - Given $K = 3$, the values of $ARL_1, SDRL_1$ differ for both np charts. That is, the magnitude of $ARL_1, SDRL_1$ can be biased up- or downwards in the binomial case. However, when N, n, m, τ increases, the absolute difference in terms of $ARL_1, SDRL_1$ between both charts decreases, in the estimated and known parameter case.
 - Given similar values of ARL_0 , the corresponding values of $ARL_1, SDRL_1$ of the hypergeometric np chart are mostly lower compared to the binomial np chart for smaller values of N .

5 Illustrative example

A local company uses an automatic welding machine to weld two pieces of stainless steel together. This machine uses a MIG welding technology (“Metal Inert Gas” using electricity to melt and join pieces of metal together). For every pair of stainless steel pieces, the welding process takes about 30s. Therefore, a batch of $N = 1000$ pieces is obtained everyday after a continuous production of about 8 hours. In order to evaluate the quality of the welds, $n = 50$ pieces are taken randomly from the batch, without replacement, and a *destructive* weld testing (a transverse tension test) is operated to evaluate their tensile properties. The results are the number of pieces for which the welds did not pass the destructive test (and are therefore considered as nonconforming ones) during $m = 10$ consecutive days (2 working weeks) considered by the company as an in-control Phase I period of production (see values $x_i, i = 1, \dots, 10$, in Table 1).

Table 1: Number of nonconforming pieces during Phase I and Phase II

i	1	2	3	4	5	6	7	8	9	10
x_i	4	1	2	1	3	3	3	2	2	4
y_i	3	3	2	2	3	7	1	3	4	2

From these results, we can estimate the in-control proportion of nonconforming welds as $\hat{p}_0 = 0.05$. If we assume a hypergeometric np chart with *known* parameter $p_0 = 0.05$ and $K = 3$, the corresponding control limits can be obtained using (2.1) and (2.2), and they are equal to

$$LCL_{HYP} = \max\{0, [-2.0085]\} = 0 \quad UCL_{HYP} = [7.0085] = 7 \quad (5.1)$$

For these values, the corresponding in-control ARL is $ARL_0 = 424.0830$. Now, if we assume a hypergeometric np chart with *estimated* parameter $\hat{p}_0 = 0.05$ based on $m = 10$ Phase I samples, the corrected chart constant to be used is found to be $K' = 2.87$ yielding the following corrected control limits (see (2.4) and (2.5))

$$\widehat{LCL}_{HYP} = \max\{0, [-1.8131]\} = 0 \quad \widehat{UCL}_{HYP} = [6.8131] = 6 \quad (5.2)$$

These corrected control limits allow the hypergeometric np chart with *estimated* parameter to have an exact in-control $ARL_0 = 421.0615$ to be close to the one obtained in the *known* parameter case, i.e., $ARL_0 = 424.0830$.

The values y_i , $i = 1, \dots, 10$, in Table 1 are the number of pieces for which the welds of the pieces did not pass the destructive test during a Phase II period of $k = 10$ days of production.

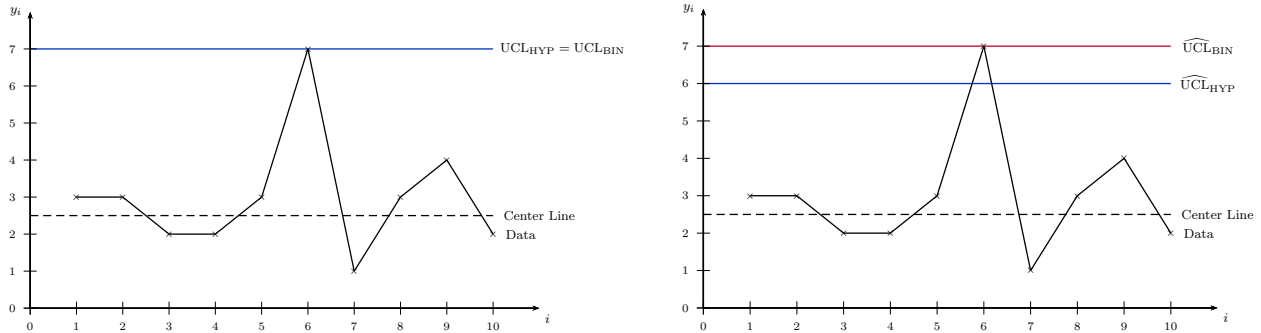


Figure 2: The hypergeometric np chart with known parameter (left) and estimated parameter (right)

The corresponding hypergeometric np chart with *known* and *estimated* parameter is plotted in Figure 2 along with control limits (5.1) and corrected control limits (5.2), respectively. Note that numerical results are displayed by a line plot instead of a scatter plot for better output illustration. As it can be seen, up to the 5th day in Phase II, the welding process seems to be in-control as all the points are within the control limits. During the 6th day, something clearly happened and a higher percentage of pieces did not pass the destructive test. Therefore, the process is declared as out-of-control in the case of estimated parameter ($y_6 > \widehat{UCL}_{HYP}$), while the hypergeometric np chart with known parameter incorrectly triggers no out-of-control signal ($y_6 \not> UCL_{HYP}$). A search for potential assignable causes impacting the welding process has shown that an improper electrical resistance due to the connection between the power source and the gun's power cable plug occurred too frequently leading to a poor and inconsistent weld quality. Once this issue has been fixed, the production went back to an in-control state as it can be seen with points corresponding to days 7–10 within the control limits.

As for a comparison with the common binomial np chart, the control limits in the known and the estimated parameter case are as follows:

$$\begin{aligned} LCL_{BIN} &= \max\{0, [-2.1233]\} = 0 & UCL_{BIN} &= [7.1233] = 7 & (K = 3, ARL_0 = 313.6425) \\ \widehat{LCL}_{BIN} &= \max\{0, [-2.0463]\} = 0 & \widehat{UCL}_{BIN} &= [7.0463] = 7 & (K' = 2.95, ARL_0 = 406.4205) \end{aligned} \quad (5.3)$$

These control limits can also be found in Figure 2. Compared to the hypergeometric np chart with estimated parameter, the process is incorrectly declared as in-control during Phase II in both the known and the estimated parameter case and no signal is triggered on the 6th day. It should be noted that (as in the hypergeometric case) the corrected control limits (5.3) allow the binomial np chart to have an in-control $ARL_0 = 406.4205$ to be close to the one obtained for the hypergeometric np chart in the known (as well as estimated) parameter case.

6 Conclusions

In this paper, we have extended the analysis of hypergeometric attribute control charts with regard to their run length properties in both the known and the estimated parameter cases. We have also compared the

results with the respective results obtained for the binomial np chart. From these comparisons, we have gained some interesting insights that may be useful for practical applications of the hypergeometric np chart.

In the following, we briefly summarize the particular contributions provided in this paper and comment on the respective obtained results.

1. By introducing the hypergeometric np chart, we fill a gap in the framework of hypergeometric attribute control charts. This chart is more convenient for practical applications in comparison with the hypergeometric p chart as it deals with integer values.
2. We extend the analysis of hypergeometric control charts for monitoring attributes data to the more realistic (and thus more important) unknown parameter case and study the effect of parameter estimation on control charts performance.
3. We compare the in-control and the out-of-control run length properties of the hypergeometric np chart in both the known and estimated parameter cases, and therefore we discuss both sides of the coin regarding the overall impact of parameter estimation on control charts performance. Guided by the obtained results, we recommend the use of the hypergeometric np chart with estimated parameter for practical applications, given the in-control proportion p_0 of nonconforming units is unknown, instead of the corresponding chart with known parameter, which provides unpredictable (i.e., up- or downwards) biased in-control and out-of-control measures.
4. We investigate the required number of Phase I samples in the framework of the hypergeometric np chart with estimated parameter p in order to obtain similar values of the in-control average run length ARL_0 compared to the known parameter case. However, the obtained results are not predictable and in turn confirm the recommendation above (see 3.).
5. In order to facilitate the implementation of the hypergeometric np chart with estimated parameter for the practitioner, we consider alternative chart parameters that allow the hypergeometric np chart with estimated parameter p to have approximately the same values of ARL_0 as the ones obtained when the parameter p is known. Tables 12–18 show the respective alternative chart parameters for various combinations of N, n, m, p_0 and therefore enable a direct implementation in practice.
6. We perform a comprehensive in-control and out-of-control comparison of the hypergeometric np chart with the binomial np chart, considering either the same chart parameter $K = 3$ or similar values of ARL_0 . In this way, we also fill a gap in the literature with regard to the non-existing out-of-control analysis of the binomial np chart. Guided by the obtained results, we recommend the use of the hypergeometric np chart instead of the binomial np chart in both the known and estimated parameter cases, given sampling without replacement from a finite population. This is due to the fact that the binomial np chart in general provides downwards-biased in-control measures, and the out-of-control measures either differ for both charts, given $K = 3$, or are mostly lower compared to the binomial np chart for smaller values of N , given similar values of ARL_0 . Since the absolute differences in terms of in-control and out-of-control measures decrease between both charts when N increases, the above recommendation is of particular importance for small population sizes N in combination with smaller values of n, m, p_0, τ . The same applies to the recommendation given in 3.

To achieve the above results, we had to compute the probability distribution of $X = \sum_{i=1}^m X_i$ with i.i.d. random variables $X_i \sim \text{HYP}(N, n, p_0)$, $i = 1, \dots, m$. However, the computational effort using convolution with double-precision floating point numbers is very extensive, especially for combinations of larger values of N, n, m, p_0 . In order to get a feasible solution that leads to a considerably faster calculation and simultaneously ensures a high accuracy of the results, we have proposed a new approximation for the probability distribution of X . Although X is in general not hypergeometric-distributed, we have shown by extensive computations and numerical analyzes that X can well be approximated by a random variable

$Z \sim \text{HYP}(mN, mn, p_0)$. By using this approximation the time required for the computation of F_X and f_X can be reduced to a few seconds while keeping a remarkable high accuracy with only negligible deviations compared to the exact distribution obtained via convolution. This result has been considered for the first time in the literature and may be helpful for numerous applications that go beyond the hypergeometric np chart, for instance, it can be used for risk aggregation in quantitative risk management (e.g. credit, insurance, market, and operational risks, see Klugman et al. [26]).

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Appendix: Tables for numerical analysis

Table 2: $(ARL_0, SDRL_0)$ for the hypergeometric np chart with $N = 100$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.02	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.05	(729.8, 1199.7)	(799.3, 1238.7)	(898.8, 1288.7)	(989.0, 1326.5)	(1096.1, 1362.2)	(1332.2, 1409.5)	(1417.0, 1416.5)
0.10	(2937.5, 61362.8)	(949.9, 4647)	(597.8, 1355.8)	(491.2, 650.2)	(484.8, 489.5)	(486.0, 485.5)	(486.0, 485.5)
0.15	(1648.7, 7301.5)	(979.5, 2902.8)	(606.1, 1126.2)	(536.2, 666.4)	(532.6, 538.9)	(535.0, 534.5)	(535.0, 534.5)
0.20	(467.7, 627.7)	(539.4, 685.4)	(604.1, 732.4)	(683.0, 773.8)	(747.9, 797.2)	(812.4, 812.8)	(813.5, 813.0)
$n = 50$							
0.01	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.02	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.05	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.10	(648.4, 792.0)	(742.2, 821.8)	(813.2, 837.4)	(837.2, 841.3)	(842.4, 842.0)	(842.6, 842.1)	(842.6, 842.1)
0.15	(393.9, 443.5)	(405.8, 436.9)	(390.8, 417.9)	(363.2, 392.8)	(331.0, 359.5)	(273.8, 282.0)	(261.8, 261.3)
0.20	(375.8, 504.1)	(375.0, 462.8)	(417.2, 545.7)	(448.6, 607.4)	(492.1, 682.1)	(686.1, 921.5)	(1236.7, 1236.2)
$n = 75$							
0.01	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.02	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.05	(910.0, 1293.8)	(1040.2, 1344.7)	(1220.1, 1392.3)	(1335.5, 1409.9)	(1399.9, 1415.5)	(1417.0, 1416.5)	(1417.0, 1416.5)
0.10	(613.0, 1423.3)	(494.4, 691.3)	(485.4, 486.6)	(486.0, 485.5)	(486.0, 485.5)	(486.0, 485.5)	(486.0, 485.5)
0.15	(533.6, 993.5)	(512.6, 663.3)	(531.6, 543.3)	(534.7, 534.5)	(535.0, 534.5)	(535.0, 534.5)	(535.0, 534.5)
0.20	(423.9, 569.1)	(513.1, 645.2)	(615.3, 720.0)	(709.5, 770.1)	(778.1, 799.1)	(813.4, 813.0)	(813.5, 813.0)
$n = 100$							
0.01	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.02	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.05	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.10	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.15	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.20	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)

Table 3: $(ARL_0, SDRL_0)$ for the hypergeometric np chart with $N = 200$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(49.9, 62.8)	(59.7, 65.1)	(65.7, 65.8)	(66.3, 65.8)	(66.3, 65.8)	(66.3, 65.8)	(66.3, 65.8)
0.02	(1227.7, 3192.9)	(726.8, 2387.4)	(266.8, 1102.4)	(165.5, 364.5)	(155.9, 160.9)	(155.8, 155.3)	(155.8, 155.3)
0.05	(1211.4, 28091.1)	(466.1, 1831.0)	(297.6, 597.8)	(280.0, 321.4)	(290.7, 295.3)	(296.5, 296.0)	(296.5, 296.0)
0.10	(990.1, 7284.9)	(497.0, 1341.7)	(365.7, 639.6)	(299.1, 516.0)	(236.5, 370.8)	(189.5, 189.7)	(189.4, 188.9)
0.15	(1041.2, 5026.2)	(601.2, 1389.3)	(457.4, 727.6)	(387.7, 615.0)	(314.3, 487.6)	(225.6, 233.7)	(223.3, 222.8)
0.20	(731.5, 1748.0)	(603.4, 1129.5)	(500.5, 793.5)	(422.3, 617.8)	(359.9, 441.0)	(331.6, 331.2)	(331.6, 331.1)
$n = 50$							
0.01	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.02	(234.1, 273.1)	(250.0, 276.5)	(276.4, 280.0)	(280.4, 280.3)	(280.9, 280.4)	(280.9, 280.4)	(280.9, 280.4)
0.05	(2954.7, 48065.4)	(990.5, 4840.4)	(590.8, 1349.2)	(425.2, 763.7)	(370.7, 415.7)	(365.3, 364.8)	(365.3, 364.8)
0.10	(700.8, 1292.5)	(698.7, 1252.8)	(565.9, 945.6)	(476.0, 674.1)	(428.9, 472.9)	(418.5, 418.0)	(418.5, 418)
0.15	(412.8, 552.2)	(427.7, 541.1)	(429.6, 530.5)	(468.8, 578.5)	(522.0, 635.5)	(669.5, 749.7)	(807.2, 806.7)
0.20	(376.8, 504.1)	(401.6, 487.5)	(438.9, 486.1)	(466.6, 492.4)	(491.5, 501.0)	(507.2, 506.7)	(507.2, 506.7)
$n = 75$							
0.01	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.02	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.05	(4515.1, 13609.2)	(2994.1, 10364.3)	(1325.7, 3829.8)	(1190.8, 1564.1)	(1269.3, 1345.8)	(1357.6, 1357.7)	(1358.3, 1357.8)
0.10	(474.8, 676.7)	(503.0, 661.8)	(482.3, 594.3)	(441.8, 518.0)	(400.8, 438.1)	(371.7, 371.3)	(371.6, 371.1)
0.15	(352.2, 410.5)	(378.8, 419.7)	(412.4, 437.1)	(428.1, 445.4)	(440.4, 453.2)	(471.0, 473.3)	(478.0, 477.5)
0.20	(325.6, 390.1)	(369.5, 429.1)	(423.7, 481.0)	(471.7, 522.0)	(523.3, 557.4)	(590.7, 592.6)	(594.9, 594.4)
$n = 100$							
0.01	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.02	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)	(∞, ∞)
0.05	(542.4, 622.7)	(588.5, 635.8)	(635.2, 645.8)	(647.2, 647.8)	(648.5, 648.0)	(648.5, 648.0)	(648.5, 648.0)
0.10	(423.9, 568.2)	(482.0, 586.8)	(566.9, 625.5)	(613.3, 639.9)	(639.8, 646.6)	(650.2, 649.7)	(650.2, 649.7)
0.15	(340.8, 414.2)	(384.4, 440.8)	(418.2, 449.2)	(415.7, 430.5)	(404.9, 409.2)	(398.2, 397.7)	(398.2, 397.7)
0.20	(327.4, 385.7)	(364.9, 410.1)	(402.1, 429.8)	(419.2, 433.0)	(423.1, 426.3)	(422.8, 422.3)	(422.8, 422.3)

Table 4: $(ARL_0, SDRL_0)$ for the hypergeometric np chart with $N = 500$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(851.8, 35047.1)	(275.7, 1416.7)	(159.2, 457.5)	(105.7, 337.6)	(59.0, 165.8)	(45.7, 45.2)	(45.7, 45.2)
0.02	(575.9, 8001.7)	(233.7, 869.8)	(162.8, 415.5)	(110.1, 213.1)	(95.9, 105.6)	(95.0, 94.5)	(95.0, 94.5)
0.05	(501.5, 4202.3)	(294.7, 826.1)	(216.1, 394.5)	(183.8, 229.9)	(179.9, 182.1)	(180.2, 179.7)	(180.2, 179.7)
0.10	(673.6, 3450.3)	(405.3, 992.7)	(306.1, 471.3)	(285.6, 426.6)	(259.6, 396.9)	(173.7, 261.2)	(129.7, 129.2)
0.15	(736.1, 3110.3)	(480.7, 1063.2)	(383.9, 564.7)	(374.2, 502.9)	(363.8, 493.0)	(338.5, 470.3)	(154.2, 153.7)
0.20	(665.3, 1534.0)	(554.1, 1122.7)	(452.3, 669.5)	(416.5, 592.8)	(373.6, 538.4)	(257.1, 326.4)	(224.4, 223.9)
$n = 50$							
0.01	(1681.6, 16152.2)	(424.9, 3104.7)	(208.9, 673.0)	(134.9, 281.1)	(122.7, 128.8)	(122.4, 121.9)	(122.4, 121.9)
0.02	(759.8, 16946.2)	(370.8, 1351.5)	(268.4, 496.0)	(215.9, 419.5)	(160.6, 330.5)	(87.6, 108.3)	(84.3, 83.8)
0.05	(684.1, 4621.2)	(406.9, 1037.5)	(324.5, 495.4)	(297.5, 439.0)	(267.3, 406.1)	(177.2, 268.6)	(129.7, 129.2)
0.10	(721.5, 2022.6)	(508.2, 1075.9)	(396.8, 569.4)	(379.4, 475.3)	(388.9, 475.7)	(427.1, 500.0)	(555.8, 555.3)
0.15	(448.6, 747.2)	(441.0, 651.8)	(406.5, 535.9)	(375.4, 469.7)	(337.5, 400.0)	(289.6, 290.8)	(288.6, 288.1)
0.20	(366.1, 476.2)	(377.3, 463.7)	(386.7, 446.8)	(393.0, 448.2)	(409.9, 468.8)	(488.8, 549.3)	(643.4, 642.9)
$n = 75$							
0.01	(1177.0, 5012.7)	(634.1, 3053.1)	(361.9, 830.2)	(369.8, 461.3)	(401.1, 465.1)	(470.4, 477.0)	(478.1, 477.6)
0.02	(1179.6, 49415.1)	(485.7, 1803.1)	(344.9, 622.8)	(309.6, 550.7)	(250.5, 474.8)	(128.8, 208.5)	(109.5, 109.0)
0.05	(917.6, 5521.4)	(515.9, 1266.9)	(389.5, 597.3)	(374.5, 504.8)	(371.4, 499.4)	(341.8, 473.4)	(154.2, 153.7)
0.10	(448.7, 747.2)	(456.7, 703.9)	(417.4, 553.0)	(380.7, 478.4)	(340.1, 405.0)	(289.8, 291.4)	(288.6, 288.1)
0.15	(375.6, 485.7)	(390.3, 480.9)	(405.4, 483.9)	(409.4, 484.2)	(397.7, 469.0)	(324.5, 351.7)	(301.0, 300.5)
0.20	(329.2, 409.2)	(368.4, 438.7)	(389.5, 444.6)	(388.6, 426.5)	(375.3, 394.4)	(355.6, 355.3)	(355.5, 355.0)
$n = 100$							
0.01	(1017.4, 2302.5)	(981.2, 2239.4)	(534.4, 1569.5)	(328.0, 1079.7)	(196.4, 548.9)	(155.3, 154.8)	(155.3, 154.8)
0.02	(1845.7, 58349.4)	(676.2, 3053.8)	(437.1, 852.0)	(354.9, 695.6)	(258.6, 504.0)	(171.9, 177.7)	(171.0, 170.5)
0.05	(981.7, 3229.7)	(655.1, 1559.4)	(474.4, 721.5)	(428.2, 607.5)	(388.2, 557.7)	(265.5, 347.3)	(224.4, 223.9)
0.10	(386.3, 519.9)	(384.1, 480.6)	(388.5, 451.4)	(396.2, 453.4)	(413.7, 474.3)	(490.0, 551.8)	(643.4, 642.9)
0.15	(330.6, 410.1)	(367.7, 439.0)	(390.9, 446.6)	(390.5, 430.4)	(376.9, 397.6)	(355.7, 355.4)	(355.5, 355.0)
0.20	(317.8, 373.3)	(349.0, 392.6)	(375.1, 407.5)	(376.0, 400.9)	(362.2, 381.8)	(319.5, 323.1)	(312.9, 312.4)

Table 5: $(ARL_0, SDRL_0)$ for the hypergeometric np chart with $N = 1000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(425.0, 11105.3)	(216.7, 1080.9)	(122.1, 323.1)	(85.0, 241.2)	(55.6, 141.7)	(41.9, 41.4)	(41.9, 41.4)
0.02	(430.0, 5745.7)	(253.5, 824.1)	(135.4, 315.9)	(100.7, 191.6)	(85.6, 97.9)	(84.1, 83.6)	(84.1, 83.6)
0.05	(555.7, 3054.4)	(301.1, 789.3)	(197.7, 357.0)	(165.5, 216.8)	(158.1, 162.2)	(157.6, 157.1)	(157.6, 157.1)
0.10	(568.9, 3111.0)	(371.5, 847.9)	(295.9, 439.3)	(277.5, 392.0)	(266.5, 381.2)	(219.0, 329.2)	(116.6, 116.1)
0.15	(745.0, 3315.7)	(460.4, 994.3)	(363.7, 525.2)	(360.9, 459.7)	(373.1, 465.4)	(411.7, 488.5)	(539.0, 538.5)
0.20	(756.3, 2071.0)	(531.9, 1085.4)	(444.1, 642.1)	(414.6, 563.3)	(394.5, 542.1)	(315.6, 447.0)	(200.3, 199.8)
$n = 50$							
0.01	(553.0, 12194.3)	(226.8, 1025.1)	(152.3, 377.1)	(104.7, 196.2)	(92.0, 103.7)	(90.8, 90.3)	(90.8, 90.3)
0.02	(576.6, 5139.2)	(293.0, 836.4)	(201.2, 339.2)	(187.3, 311.5)	(167.7, 289.5)	(96.9, 172.8)	(67.5, 67.0)
0.05	(586.0, 3078.5)	(373.7, 864.0)	(277.0, 405.3)	(267.1, 351.9)	(265.8, 349.1)	(275.4, 356.1)	(424.1, 423.6)
0.10	(707.7, 2447.0)	(451.4, 956.3)	(357.7, 511.8)	(342.4, 402.9)	(356.5, 387.5)	(401.0, 404.4)	(406.8, 406.3)
0.15	(449.6, 709.9)	(422.7, 622.6)	(376.0, 479.2)	(359.0, 436.6)	(341.2, 415.9)	(278.9, 333.9)	(224.0, 223.5)
0.20	(364.5, 461.3)	(375.7, 445.2)	(390.2, 437.3)	(408.0, 443.6)	(435.5, 458.5)	(477.3, 478.2)	(479.7, 479.2)
$n = 75$							
0.01	(779.5, 13477.1)	(273.4, 1147.1)	(196.8, 366.9)	(200.5, 230.1)	(217.3, 227.9)	(230.4, 229.9)	(230.4, 229.9)
0.02	(629.2, 4643.4)	(346.0, 905.0)	(255.1, 386.5)	(248.4, 344.3)	(247.1, 342.8)	(245.5, 341.6)	(412.5, 412.0)
0.05	(668.4, 3370.7)	(413.5, 898.5)	(318.5, 464.1)	(303.7, 359.7)	(321.3, 351.2)	(363.0, 366.2)	(368.2, 367.7)
0.10	(475.2, 787.1)	(420.1, 627.6)	(365.4, 459.7)	(351.0, 410.3)	(348.5, 403.0)	(347.3, 401.5)	(562.4, 561.9)
0.15	(370.5, 510.1)	(383.3, 498.1)	(387.2, 464.9)	(379.1, 425.1)	(386.0, 416.2)	(431.2, 440.7)	(450.4, 449.9)
0.20	(338.8, 422.7)	(359.9, 421.4)	(364.9, 398.1)	(361.5, 381.4)	(359.9, 376.4)	(358.8, 374.5)	(608.6, 608.1)
$n = 100$							
0.01	(692.7, 22439.4)	(344.8, 1218.5)	(251.9, 467.8)	(203.2, 389.9)	(161.2, 324.5)	(86.6, 117.1)	(81.1, 80.6)
0.02	(683.0, 5711.7)	(372.6, 1030.5)	(281.9, 438.7)	(277.8, 386.1)	(271.7, 380.3)	(261.1, 371.7)	(95.8, 95.3)
0.05	(719.7, 2856.2)	(451.0, 972.2)	(357.7, 513.2)	(338.9, 404.3)	(354.0, 386.5)	(400.3, 404.1)	(406.8, 406.3)
0.10	(372.6, 508.1)	(392.7, 516.0)	(390.5, 486.0)	(373.2, 436.8)	(352.8, 381.8)	(335.1, 334.7)	(335.1, 334.6)
0.15	(339.1, 419.5)	(356.2, 418.6)	(370.0, 412.4)	(382.5, 417.2)	(403.1, 434.4)	(469.8, 483.8)	(501.0, 500.5)
0.20	(312.6, 363.2)	(339.1, 374.4)	(363.7, 384.4)	(378.7, 393.3)	(394.1, 403.1)	(415.7, 415.5)	(416.4, 415.9)

Table 6: $(ARL_0, SDR L_0)$ for the hypergeometric np chart with $N = 2000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(340.3, 5635.8)	(188.2, 825.8)	(109.9, 280.1)	(77.9, 210.1)	(52.4, 125.0)	(40.3, 39.8)	(40.3, 39.8)
0.02	(369.1, 4118.4)	(227.0, 695.2)	(124.9, 280.6)	(94.5, 172.5)	(81.4, 95.4)	(79.6, 79.1)	(79.6, 79.1)
0.05	(498.9, 2916.7)	(276.2, 701.6)	(186.6, 325.5)	(158.5, 212.0)	(149.1, 154.6)	(148.1, 147.6)	(148.1, 147.6)
0.10	(591.1, 2779.4)	(367.5, 845.1)	(290.9, 425.4)	(277.9, 379.2)	(268.7, 370.9)	(246.2, 350.4)	(110.8, 110.3)
0.15	(688.1, 2951.6)	(459.2, 1017.7)	(354.3, 508.3)	(353.4, 440.0)	(370.4, 446.3)	(425.8, 474.5)	(501.1, 500.6)
0.20	(697.3, 1871.5)	(546.4, 1106.0)	(431.4, 618.5)	(417.6, 550.8)	(410.7, 543.3)	(366.4, 501.0)	(189.7, 189.2)
$n = 50$							
0.01	(381.7, 4543.6)	(232.4, 721.7)	(127.0, 287.9)	(95.8, 176.4)	(82.3, 96.8)	(80.5, 80.0)	(80.5, 80.0)
0.02	(441.9, 3144.9)	(243.4, 668.8)	(187.8, 299.6)	(182.5, 279.9)	(166.6, 265.0)	(118.8, 206.7)	(61.4, 60.9)
0.05	(543.5, 2800.1)	(321.5, 747.2)	(254.1, 373.5)	(252.0, 316.6)	(263.9, 321.0)	(300.3, 340.0)	(362.4, 361.9)
0.10	(636.7, 1990.0)	(426.5, 880.2)	(339.7, 475.8)	(320.7, 375.0)	(329.0, 346.6)	(353.1, 353.0)	(353.8, 353.3)
0.15	(428.8, 707.0)	(407.7, 605.1)	(366.9, 459.0)	(352.6, 414.7)	(350.4, 409.5)	(337.3, 398.3)	(199.6, 199.1)
0.20	(364.9, 482.9)	(368.1, 447.1)	(390.6, 455.4)	(395.5, 434.2)	(405.4, 420.5)	(419.5, 419.0)	(419.6, 419.1)
$n = 75$							
0.01	(452.3, 4319.3)	(250.0, 728.1)	(164.7, 286.6)	(163.6, 182.8)	(172.4, 177.1)	(178.6, 178.1)	(178.6, 178.1)
0.02	(486.7, 2971.0)	(290.3, 727.6)	(214.4, 321.1)	(219.1, 280.3)	(227.9, 283.7)	(265.8, 301.1)	(316.4, 315.9)
0.05	(602.2, 2615.0)	(367.5, 788.7)	(288.2, 414.0)	(270.7, 319.0)	(278.5, 291.6)	(295.3, 294.9)	(295.5, 295.0)
0.10	(455.6, 747.3)	(399.7, 581.3)	(356.8, 440.9)	(352.0, 403.3)	(367.2, 407.0)	(422.1, 438.1)	(450.4, 449.9)
0.15	(374.9, 516.2)	(381.7, 491.2)	(366.9, 436.7)	(354.9, 392.6)	(353.5, 367.8)	(366.9, 366.8)	(367.0, 366.5)
0.20	(331.8, 408.7)	(361.4, 421.7)	(371.2, 411.9)	(384.8, 418.2)	(409.0, 437.6)	(472.8, 481.6)	(492.0, 491.5)
$n = 100$							
0.01	(523.6, 4384.9)	(274.0, 755.6)	(209.0, 339.4)	(189.3, 303.2)	(166.7, 279.7)	(104.1, 187.2)	(65.1, 64.6)
0.02	(523.3, 3210.2)	(299.2, 725.9)	(240.6, 353.9)	(236.7, 296.4)	(251.6, 301.2)	(269.7, 320.6)	(331.0, 330.5)
0.05	(663.9, 2493.2)	(420.4, 876.2)	(323.3, 460.7)	(297.1, 355.4)	(293.6, 307.5)	(302.2, 301.7)	(302.2, 301.7)
0.10	(400.0, 597.2)	(390.3, 544.9)	(363.2, 452.5)	(346.1, 405.6)	(325.9, 374.3)	(270.0, 283.4)	(257.4, 256.9)
0.15	(336.5, 421.8)	(356.1, 427.1)	(369.8, 420.2)	(374.4, 410.7)	(375.4, 393.7)	(378.3, 377.9)	(378.5, 378.0)
0.20	(315.1, 376.4)	(348.0, 396.4)	(367.3, 403.5)	(371.8, 400.2)	(360.8, 381.5)	(323.8, 326.7)	(318.8, 318.3)

Table 7: $(ARL_0, SDR L_0)$ for the hypergeometric np chart with $N = 5000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(303.9, 4190.7)	(174.6, 719.1)	(135.4, 310.6)	(88.6, 228.3)	(54.8, 133.7)	(39.4, 38.9)	(39.4, 38.9)
0.02	(339.6, 3460.6)	(213.4, 633.4)	(138.7, 305.8)	(96.4, 183.8)	(79.4, 96.1)	(77.1, 76.6)	(77.1, 76.6)
0.05	(468.5, 2683.6)	(262.8, 656.1)	(191.0, 338.5)	(156.1, 214.5)	(144.4, 152.1)	(142.9, 142.4)	(142.9, 142.4)
0.10	(606.4, 2830.7)	(353.1, 833.9)	(279.0, 406.1)	(275.8, 369.9)	(270.9, 365.2)	(262.2, 358.1)	(107.6, 107.1)
0.15	(680.1, 2759.3)	(457.2, 968.2)	(354.7, 507.6)	(347.0, 427.2)	(365.6, 433.4)	(427.6, 462.5)	(480.2, 479.7)
0.20	(665.2, 1764.2)	(523.6, 1051.6)	(430.8, 614.3)	(420.5, 544.1)	(415.0, 537.4)	(396.7, 522.0)	(183.8, 183.3)
$n = 50$							
0.01	(319.8, 3080.3)	(204.3, 592.3)	(134.0, 291.5)	(93.9, 176.0)	(77.6, 93.3)	(75.4, 74.9)	(75.4, 74.9)
0.02	(384.5, 2634.4)	(219.2, 574.9)	(187.3, 287.8)	(177.2, 261.3)	(167.1, 252.6)	(133.8, 218.6)	(58.2, 57.7)
0.05	(538.1, 2572.9)	(329.1, 711.6)	(245.7, 357.6)	(244.2, 298.7)	(254.8, 300.6)	(299.0, 320.9)	(331.8, 331.3)
0.10	(659.8, 2252.7)	(427.8, 874.1)	(331.1, 468.2)	(308.7, 362.1)	(311.8, 325.4)	(326.7, 326.3)	(326.8, 326.3)
0.15	(451.0, 725.3)	(407.8, 601.2)	(365.2, 455.3)	(356.0, 416.8)	(364.3, 421.3)	(399.1, 456.2)	(541.7, 541.2)
0.20	(370.3, 494.8)	(383.6, 492.7)	(393.0, 476.6)	(392.9, 446.2)	(387.7, 405.8)	(388.6, 388.1)	(388.6, 388.1)
$n = 75$							
0.01	(353.9, 2705.0)	(213.5, 641.0)	(155.9, 268.2)	(146.9, 166.0)	(152.8, 155.5)	(156.6, 156.1)	(156.6, 156.1)
0.02	(412.0, 2469.1)	(267.0, 636.5)	(199.8, 292.9)	(205.0, 251.3)	(216.8, 254.8)	(255.1, 269.3)	(274.8, 274.3)
0.05	(535.9, 2325.4)	(356.1, 743.5)	(275.5, 392.8)	(255.0, 303.2)	(255.0, 264.6)	(261.9, 261.5)	(262.0, 261.5)
0.10	(418.8, 685.9)	(380.8, 543.8)	(346.6, 421.7)	(341.9, 384.6)	(353.6, 378.5)	(392.6, 395.6)	(398.4, 397.9)
0.15	(361.7, 499.9)	(370.6, 483.0)	(363.0, 427.4)	(351.6, 387.5)	(345.1, 359.4)	(340.4, 341.4)	(327.3, 326.8)
0.20	(334.5, 407.8)	(357.0, 409.2)	(368.4, 401.3)	(382.8, 406.4)	(400.7, 416.4)	(434.4, 435.1)	(436.7, 436.2)
$n = 100$							
0.01	(384.5, 2634.4)	(243.2, 668.7)	(187.3, 287.8)	(177.2, 261.4)	(167.1, 252.6)	(133.8, 218.6)	(58.2, 57.7)
0.02	(452.3, 2272.3)	(284.5, 649.7)	(216.0, 320.2)	(215.6, 259.2)	(231.0, 259.9)	(267.6, 272.8)	(275.4, 274.9)
0.05	(585.3, 2291.5)	(383.8, 774.6)	(304.2, 427.0)	(278.9, 342.6)	(262.3, 280.8)	(258.1, 257.6)	(258.1, 257.6)
0.10	(391.2, 571.8)	(378.6, 526.1)	(348.9, 428.0)	(335.5, 385.1)	(326.2, 370.3)	(288.1, 328.3)	(223.1, 222.6)
0.15	(334.1, 420.4)	(352.7, 422.7)	(367.2, 422.7)	(365.4, 407.8)	(352.1, 377.4)	(325.7, 326.0)	(324.7, 324.2)
0.20	(323.4, 386.7)	(347.3, 396.6)	(363.8, 396.8)	(363.1, 385.1)	(355.8, 373.9)	(320.9, 337.6)	(275.3, 274.8)

Table 8: $(ARL_0, SDRL_0)$ for the hypergeometric np chart with $N = 10000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(293.4, 3841.1)	(170.5, 688.8)	(132.7, 302.8)	(87.1, 222.8)	(54.2, 130.8)	(39.1, 38.7)	(39.1, 38.6)
0.02	(330.8, 3277.2)	(209.2, 614.9)	(136.5, 299.1)	(95.3, 180.2)	(78.6, 94.8)	(76.3, 75.8)	(76.3, 75.8)
0.05	(459.0, 2594.6)	(258.6, 642.0)	(188.4, 332.5)	(154.3, 211.3)	(142.7, 150.2)	(141.2, 140.7)	(141.2, 140.7)
0.10	(595.7, 2760.7)	(347.9, 818.3)	(277.0, 410.7)	(272.1, 364.7)	(273.6, 364.8)	(267.2, 359.8)	(106.5, 106.0)
0.15	(669.7, 2770.1)	(450.6, 951.6)	(350.0, 500.2)	(349.7, 425.6)	(365.6, 430.0)	(427.2, 458.2)	(473.5, 473.0)
0.20	(692.9, 1995.0)	(520.8, 1096.7)	(425.1, 605.5)	(414.9, 536.4)	(416.2, 535.2)	(406.4, 527.3)	(181.9, 181.4)
$n = 50$							
0.01	(303.2, 2752.6)	(196.3, 565.5)	(129.8, 278.7)	(91.6, 169.1)	(76.7, 95.6)	(73.9, 73.4)	(73.9, 73.4)
0.02	(368.0, 2432.0)	(234.9, 636.7)	(181.7, 277.9)	(172.0, 252.7)	(162.3, 244.3)	(138.9, 221.4)	(57.3, 56.8)
0.05	(518.8, 2436.4)	(319.3, 684.9)	(239.1, 346.8)	(237.8, 291.3)	(251.7, 294.2)	(296.5, 314.0)	(322.5, 322.0)
0.10	(638.5, 2157.2)	(415.8, 844.6)	(326.8, 455.6)	(305.0, 358.4)	(306.2, 318.9)	(318.4, 318.0)	(318.5, 318.0)
0.15	(438.9, 704.5)	(397.4, 584.7)	(359.8, 451.3)	(355.7, 416.1)	(367.3, 423.7)	(415.4, 466.4)	(527.0, 526.5)
0.20	(361.1, 481.8)	(388.4, 498.3)	(397.2, 486.4)	(392.6, 449.3)	(381.7, 401.0)	(379.1, 378.6)	(379.1, 378.6)
$n = 75$							
0.01	(329.1, 2355.4)	(202.2, 589.4)	(149.2, 252.5)	(141.0, 158.9)	(147.3, 149.4)	(150.3, 149.8)	(150.3, 149.8)
0.02	(388.2, 2232.2)	(254.4, 596.0)	(194.3, 293.4)	(196.5, 241.0)	(211.5, 245.4)	(248.8, 258.9)	(262.9, 262.4)
0.05	(514.8, 2333.4)	(341.5, 719.4)	(271.6, 391.4)	(251.2, 302.9)	(247.3, 257.2)	(252.1, 251.6)	(252.1, 251.6)
0.10	(402.8, 657.8)	(368.5, 522.9)	(342.9, 414.9)	(337.4, 377.4)	(347.1, 368.1)	(379.9, 381.3)	(383.0, 382.5)
0.15	(376.8, 528.5)	(377.1, 489.8)	(358.4, 420.2)	(348.2, 382.8)	(342.1, 356.6)	(337.7, 338.9)	(315.5, 315.0)
0.20	(322.7, 392.7)	(349.4, 399.2)	(367.0, 396.2)	(378.7, 399.0)	(393.9, 406.2)	(419.2, 419.3)	(420.3, 419.8)
$n = 100$							
0.01	(351.3, 2230.6)	(226.4, 604.4)	(176.0, 268.0)	(166.7, 244.0)	(164.4, 242.0)	(143.7, 223.0)	(56.3, 55.8)
0.02	(420.8, 2292.2)	(271.5, 645.6)	(215.6, 318.5)	(209.0, 248.5)	(223.9, 247.6)	(255.9, 258.5)	(260.1, 259.6)
0.05	(582.1, 2202.4)	(379.4, 777.5)	(298.6, 416.9)	(273.3, 337.6)	(253.7, 275.2)	(245.6, 245.1)	(245.6, 245.1)
0.10	(386.8, 585.3)	(372.7, 512.1)	(346.1, 422.6)	(331.0, 376.8)	(325.6, 365.3)	(306.6, 347.5)	(213.2, 212.7)
0.15	(339.2, 422.9)	(354.2, 421.7)	(363.5, 416.3)	(360.5, 401.7)	(347.3, 375.1)	(311.9, 313.6)	(309.3, 308.8)
0.20	(322.9, 392.5)	(348.5, 398.7)	(360.2, 390.9)	(360.2, 379.1)	(355.6, 370.3)	(336.0, 352.4)	(262.7, 262.2)

Table 9: $(ARL_0, SDRL_0)$ for the binomial np chart with $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$, $K = 3$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$							
0.01	(283.6, 3538.1)	(166.6, 660.7)	(130.1, 295.3)	(85.7, 217.5)	(53.6, 128.0)	(38.8, 38.4)	(38.8, 38.3)
0.02	(322.3, 3153.5)	(205.2, 597.3)	(134.4, 292.6)	(94.1, 176.7)	(77.8, 93.5)	(75.5, 75.0)	(75.5, 75.0)
0.05	(471.5, 2957.7)	(254.6, 636.2)	(185.8, 326.7)	(152.4, 208.2)	(141.0, 148.4)	(139.6, 139.1)	(139.6, 139.1)
0.10	(614.0, 2845.8)	(362.8, 808.0)	(285.9, 412.8)	(277.3, 366.1)	(276.2, 364.3)	(274.9, 363.3)	(442.2, 441.7)
0.15	(712.7, 2928.1)	(448.2, 983.7)	(345.4, 493.0)	(345.2, 420.7)	(365.4, 426.5)	(426.3, 453.6)	(467.0, 466.5)
0.20	(711.7, 1958.3)	(534.5, 1084.6)	(432.7, 605.7)	(418.9, 536.6)	(417.3, 532.8)	(415.9, 531.6)	(649.3, 648.8)
$n = 50$							
0.01	(288.0, 2477.0)	(188.8, 533.4)	(125.9, 266.8)	(89.5, 162.7)	(75.2, 93.0)	(72.4, 71.9)	(72.4, 71.9)
0.02	(352.7, 2252.6)	(227.0, 607.1)	(176.4, 268.6)	(167.0, 244.6)	(164.7, 242.5)	(143.9, 223.5)	(56.3, 55.8)
0.05	(500.6, 2310.1)	(309.9, 664.5)	(244.4, 354.1)	(237.3, 287.5)	(252.1, 289.7)	(293.3, 306.9)	(313.6, 313.1)
0.10	(622.1, 2171.5)	(404.8, 817.7)	(325.3, 458.6)	(301.3, 355.0)	(300.6, 312.8)	(310.5, 310.0)	(310.6, 310.1)
0.15	(449.8, 747.5)	(403.4, 587.3)	(361.2, 449.0)	(360.1, 418.7)	(372.2, 426.1)	(426.4, 469.6)	(512.9, 512.4)
0.20	(389.0, 532.5)	(399.9, 521.5)	(400.4, 493.1)	(388.3, 446.4)	(375.8, 396.6)	(369.8, 369.3)	(369.8, 369.3)
$n = 75$							
0.01	(307.1, 2072.2)	(192.0, 544.4)	(143.0, 238.5)	(138.2, 156.7)	(142.2, 143.8)	(144.5, 144.0)	(144.5, 144.0)
0.02	(366.5, 2077.0)	(242.8, 562.8)	(195.0, 283.1)	(194.3, 234.4)	(206.3, 236.4)	(241.9, 248.9)	(251.8, 251.3)
0.05	(520.7, 2211.7)	(345.9, 701.1)	(271.6, 389.3)	(245.6, 297.3)	(239.8, 249.8)	(242.8, 242.3)	(242.8, 242.3)
0.10	(440.5, 715.2)	(380.5, 543.1)	(342.3, 421.7)	(335.1, 380.8)	(340.7, 360.3)	(366.9, 367.3)	(368.5, 368.0)
0.15	(362.8, 507.1)	(366.5, 475.6)	(357.0, 414.4)	(348.3, 381.6)	(340.4, 355.4)	(335.4, 336.4)	(351.2, 350.7)
0.20	(341.1, 423.9)	(354.0, 409.7)	(365.7, 400.4)	(377.5, 401.3)	(388.5, 401.5)	(404.3, 404.0)	(404.7, 404.2)
$n = 100$							
0.01	(322.8, 1942.9)	(211.6, 549.4)	(166.9, 258.3)	(166.6, 236.0)	(161.8, 232.0)	(153.0, 224.8)	(54.4, 53.9)
0.02	(405.8, 2275.0)	(255.5, 600.8)	(204.2, 299.1)	(202.7, 238.6)	(216.7, 236.2)	(243.8, 245.0)	(246.2, 245.7)
0.05	(569.1, 2046.3)	(373.5, 739.4)	(293.2, 407.4)	(267.4, 332.9)	(245.9, 271.1)	(234.0, 233.5)	(234.0, 233.5)
0.10	(395.6, 591.8)	(379.0, 526.7)	(345.1, 419.2)	(330.8, 373.4)	(327.4, 362.1)	(326.5, 360.7)	(498.7, 498.2)
0.15	(326.7, 404.4)	(347.4, 412.4)	(359.6, 408.7)	(356.6, 395.9)	(343.1, 372.4)	(301.3, 306.1)	(294.9, 294.4)
0.20	(322.8, 386.5)	(347.6, 397.4)	(359.3, 389.2)	(357.9, 374.4)	(356.0, 367.1)	(355.2, 365.3)	(547.2, 546.7)

Table 10: Selected results of the simulation study regarding ARL_0

m, N, n, p_0	ARL_0	ARL_0^{sim}	m, N, n, p_0	ARL_0	ARL_0^{sim}	m, N, n, p_0	ARL_0	ARL_0^{sim}
10, 100, 25, 0.01	∞	∞	20, 100, 50, 0.02	∞	∞	50, 100, 75, 0.05	1220.1	1210.9
100, 200, 50, 0.1	476.0	471.0	200, 200, 75, 0.15	440.4	438.3	1000, 200, 100, 0.2	422.8	422.5
10, 500, 25, 0.01	851.8	815.5	20, 500, 50, 0.02	370.8	369.3	50, 500, 75, 0.05	389.5	400.2
100, 1000, 50, 0.1	342.4	340.5	200, 1000, 75, 0.15	386.0	389.5	1000, 1000, 100, 0.2	415.7	415.2
10, 2000, 25, 0.01	340.3	346.2	20, 2000, 50, 0.02	243.4	243.9	50, 2000, 75, 0.05	288.2	282.0
100, 5000, 50, 0.1	308.7	308.9	200, 5000, 75, 0.15	345.1	346.2	1000, 5000, 100, 0.2	320.9	319.2
10, 10000, 25, 0.01	293.4	295.7	20, 10000, 50, 0.02	234.9	234.2	50, 10000, 75, 0.05	271.6	269.2

Table 11: Values of m for $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $N \in \{100, 200, 500, 1000, 2000, 5000, 10000\}$, $K = 3$, satisfying $\Delta = \frac{|\text{ARL}_{0,m} - \text{ARL}_{0,\infty}|}{\text{ARL}_{0,\infty}} \leq 0.05$

$N \setminus p_0$	0.01	0.02	0.05	0.10	0.15	0.20
$n = 25$						
100	–	–	1101	78	70	277
200	18	106	112	407	640	242
500	310	134	83	2751	> 10000	1640
1000	343	150	100	> 10000	14	6763
2000	371	159	117	> 10000	15	> 10000
5000	382	171	125	> 10000	15	> 10000
10000	383	171	125	> 10000	16	> 10000
$n = 50$						
100	–	–	–	41	951	> 10000
200	–	29	144	160	3331	151
500	119	931	2926	16	433	7358
1000	151	2822	15	24	3251	340
2000	164	6904	16	33	> 10000	111
5000	175	> 10000	18	40	> 10000	10
10000	180	> 10000	18	43	8060	10
$n = 75$						
100	–	–	104	15	10	189
200	–	–	46	254	411	409
500	576	1572	> 10000	453	1281	218
1000	210	15	521	> 10000	892	> 10000
2000	147	15	217	10	10	837
5000	38	18	49	11	303	332
10000	38	18	64	13	3, 4, > 10000	250
$n = 100$						
100	–	–	–	–	–	–
200	–	–	30	105	17	49
500	313	597	1923	7884	11	10
1000	1112	> 10000	26	211	1193	216
2000	3834	16	51	984	18	10
5000	> 10000	19	122	6340	10	3531
10000	> 10000	20	160	> 10000	455	4, > 10000

Table 12: $(K', \text{ARL}_0, \text{SDRL}_0)$ for the hypergeometric np chart with $N = 100$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200\}$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$
$n = 25$					
0.01	-	-	-	-	-
0.02	-	-	-	-	-
0.05	(3.83, 1301.2, 1406.1)	(3.84, 1371.3, 1413.4)	(3.90, 1414.9, 1416.4)	(3.93, 1417.0, 1416.5)	(3.95, 1417.0, 1416.5)
0.10	(2.59, 465.8, 3177.5)	(2.78, 506.0, 1689.4)	(2.92, 491.8, 989.2)	(2.99, 488.9, 650.0)	(3.02, 485.9, 495.0)
0.15	(2.77, 495.7, 1359.1)	(2.83, 523.5, 1287.2)	(2.95, 531.4, 897.0)	(3.00, 536.2, 666.4)	(3.03, 535.4, 547.5)
0.20	(3.08, 778.1, 1705.0)	(3.07, 800.4, 1617.8)	(3.08, 802.0, 1269.0)	(3.11, 818.3, 1007.0)	(3.13, 813.4, 831.4)
$n = 50$					
0.01	-	-	-	-	-
0.02	-	-	-	-	-
0.05	-	-	-	-	-
0.10	(3.18, 843.0, 995.8)	(3.16, 837.5, 907.1)	(3.14, 841.2, 850.0)	(3.13, 842.4, 842.2)	(3.13, 842.6, 842.1)
0.15	(2.86, 267.9, 336.9)	(2.81, 259.3, 302.2)	(2.79, 262.3, 279.7)	(2.78, 261.4, 264.9)	(2.78, 261.7, 261.5)
0.20	(3.30, 1292.0, 1640.8)	(3.27, 1267.4, 1503.2)	(3.24, 1238.4, 1345.1)	(3.23, 1235.3, 1267.0)	(3.23, 1236.2, 1239.1)
$n = 75$					
0.01	-	-	-	-	-
0.02	-	-	-	-	-
0.05	(3.20, 1361.4, 1412.5)	(3.20, 1404.2, 1415.8)	(3.20, 1416.8, 1416.5)	(3.20, 1417.0, 1416.5)	(3.20, 1417.0, 1416.5)
0.10	(2.92, 501.0, 1022.6)	(2.98, 485.6, 617.6)	(3.02, 486.0, 488.4)	(3.04, 486.0, 485.5)	(3.05, 486.0, 485.5)
0.15	(3.00, 533.6, 993.5)	(3.01, 548.4, 812.6)	(3.02, 535.4, 558.2)	(3.03, 534.9, 534.8)	(3.04, 535.0, 534.5)
0.20	(3.21, 915.4, 1713.5)	(3.20, 758.3, 787.1)	(3.20, 805.6, 808.7)	(3.20, 812.9, 812.6)	(3.20, 813.5, 813.0)
$n = 100$					
0.01	-	-	-	-	-
0.02	-	-	-	-	-
0.05	-	-	-	-	-
0.10	-	-	-	-	-
0.15	-	-	-	-	-
0.20	-	-	-	-	-

Table 13: $(K', \text{ARL}_0, \text{SDRL}_0)$ for the hypergeometric np chart with $N = 200$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200\}$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$
$n = 25$					
0.01	(3.05, 62.1, 65.5)	(3.05, 64.4, 65.7)	(3.48, 66.3, 65.8)	(3.48, 66.3, 65.8)	(3.61, 66.3, 65.8)
0.02	(2.25, 174.0, 1054.2)	(2.49, 152.3, 669.2)	(2.73, 153.7, 412.8)	(2.88, 156.1, 226.3)	(2.97, 155.8, 157.7)
0.05	(2.61, 306.8, 2699.9)	(2.80, 300.8, 951.4)	(3.00, 297.6, 597.8)	(3.08, 295.2, 379.6)	(3.13, 296.5, 303.2)
0.10	(2.47, 186.1, 653.5)	(2.62, 184.0, 393.9)	(2.74, 192.0, 294.8)	(2.78, 188.4, 218.7)	(2.81, 189.3, 191.8)
0.15	(2.59, 226.3, 470.6)	(2.66, 229.5, 438.2)	(2.74, 221.8, 326.3)	(2.78, 222.3, 257.5)	(2.81, 223.4, 227.4)
0.20	(2.87, 345.8, 632.6)	(2.86, 317.4, 500.3)	(2.87, 334.3, 474.1)	(2.89, 333.8, 394.5)	(2.91, 332.0, 340.3)
$n = 50$					
0.01	-	-	-	-	-
0.02	(3.29, 256.3, 277.6)	(3.38, 275.4, 279.9)	(3.44, 280.7, 280.4)	(3.47, 280.9, 280.4)	(3.49, 280.9, 280.4)
0.05	(2.50, 375.7, 2828.9)	(2.69, 374.4, 1251.5)	(2.85, 367.5, 694.0)	(2.91, 365.1, 476.0)	(2.95, 365.4, 375.6)
0.10	(2.90, 448.5, 881.6)	(2.90, 422.1, 764.3)	(2.90, 417.2, 642.5)	(2.93, 416.2, 509.9)	(2.96, 419.2, 435.9)
0.15	(3.16, 788.3, 1252.6)	(3.15, 822.4, 1288.0)	(3.14, 795.7, 1086.0)	(3.15, 801.3, 942.5)	(3.17, 806.5, 838.4)
0.20	(3.08, 507.9, 703.8)	(3.05, 492.2, 643.4)	(3.03, 501.0, 596.9)	(3.03, 503.4, 550.3)	(3.04, 507.2, 518.6)
$n = 75$					
0.01	-	-	-	-	-
0.02	-	-	-	-	-
0.05	(2.79, 1195.4, 5906.4)	(2.85, 1326.4, 5574.8)	(3.00, 1325.7, 3829.8)	(3.08, 1352.5, 2403.0)	(3.13, 1359.9, 1510.3)
0.10	(2.92, 366.2, 543.9)	(2.90, 383.6, 529.4)	(2.89, 377.0, 453.2)	(2.89, 372.0, 400.9)	(2.90, 371.5, 375.6)
0.15	(3.04, 473.9, 626.5)	(3.05, 472.4, 576.5)	(3.04, 478.5, 532.3)	(3.03, 465.4, 469.2)	(3.03, 472.6, 473.5)
0.20	(3.16, 593.9, 747.9)	(3.13, 603.4, 724.3)	(3.10, 591.7, 660.5)	(3.09, 591.9, 627.8)	(3.09, 594.6, 603.9)
$n = 100$					
0.01	-	-	-	-	-
0.02	-	-	-	-	-
0.05	(3.12, 646.7, 764.8)	(3.09, 643.2, 698.6)	(3.08, 649.7, 659.8)	(3.07, 648.5, 648.6)	(3.06, 648.5, 648.0)
0.10	(3.12, 624.1, 802.3)	(3.09, 646.9, 774.8)	(3.06, 647.7, 708.9)	(3.05, 648.0, 670.6)	(3.05, 649.6, 652.4)
0.15	(3.04, 397.4, 482.8)	(3.01, 402.4, 458.3)	(2.98, 402.3, 433.7)	(2.97, 399.2, 412.4)	(2.96, 397.8, 400.1)
0.20	(3.07, 422.9, 501.3)	(3.05, 432.7, 486.8)	(3.02, 425.5, 454.1)	(3.01, 426.0, 439.5)	(3.00, 423.1, 426.3)

Table 14: $(K', \text{ARL}_0, \text{SDRL}_0)$ for the hypergeometric np chart with $N = 500$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200\}$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$
$n = 25$					
0.01	(1.85, 44.8, 192.8)	(2.16, 45.2, 147.7)	(2.35, 46.4, 92.6)	(2.44, 45.7, 49.5)	(2.50, 45.7, 45.2)
0.02	(2.29, 90.4, 497.8)	(2.54, 92.9, 272.7)	(2.72, 95.8, 165.3)	(2.82, 94.8, 111.8)	(2.86, 95.0, 95.2)
0.05	(2.53, 163.7, 837.5)	(2.76, 170.2, 433.9)	(2.91, 180.1, 290.4)	(2.97, 180.9, 219.5)	(3.01, 180.1, 182.8)
0.10	(2.40, 137.1, 417.4)	(2.53, 132.8, 265.2)	(2.63, 130.0, 184.5)	(2.68, 130.2, 149.2)	(2.70, 129.7, 131.1)
0.15	(2.50, 154.7, 294.8)	(2.56, 154.3, 270.5)	(2.64, 152.0, 211.5)	(2.68, 153.9, 174.5)	(2.70, 154.1, 156.5)
0.20	(2.76, 224.9, 376.8)	(2.75, 210.9, 308.0)	(2.76, 225.1, 305.3)	(2.78, 225.4, 261.4)	(2.79, 224.0, 228.7)
$n = 50$					
0.01	(2.19, 116.9, 1484.3)	(2.49, 133.3, 515.7)	(2.73, 123.0, 284.2)	(2.84, 121.9, 149.5)	(2.92, 122.4, 123.4)
0.02	(2.18, 82.0, 435.8)	(2.35, 84.8, 219.0)	(2.51, 84.9, 131.8)	(2.58, 84.2, 94.8)	(2.62, 84.3, 84.4)
0.05	(2.38, 128.9, 466.4)	(2.51, 132.8, 265.4)	(2.63, 127.6, 184.2)	(2.67, 129.5, 149.0)	(2.70, 129.7, 131.8)
0.10	(2.91, 555.6, 1483.5)	(3.03, 561.8, 1207.4)	(3.13, 549.3, 828.3)	(3.17, 553.1, 685.8)	(3.20, 556.9, 590.6)
0.15	(2.89, 277.9, 385.6)	(2.88, 284.1, 389.7)	(2.88, 290.5, 367.7)	(2.89, 290.9, 335.3)	(2.90, 288.9, 300.3)
0.20	(3.15, 614.0, 848.9)	(3.14, 639.4, 854.8)	(3.14, 657.6, 824.9)	(3.14, 645.3, 742.7)	(3.15, 646.1, 679.7)
$n = 75$					
0.01	(2.42, 362.9, 2363.7)	(2.83, 441.7, 2254.5)	(3.14, 469.4, 1550.2)	(3.29, 480.5, 917.3)	(3.37, 478.4, 529.9)
0.02	(2.20, 109.2, 492.2)	(2.40, 109.9, 280.0)	(2.54, 108.0, 171.8)	(2.61, 110.0, 127.7)	(2.64, 109.5, 110.3)
0.05	(2.49, 159.6, 303.5)	(2.53, 156.0, 290.9)	(2.64, 155.4, 221.5)	(2.67, 153.2, 177.3)	(2.70, 154.3, 158.3)
0.10	(2.89, 293.1, 420.6)	(2.88, 292.6, 408.2)	(2.88, 294.1, 375.9)	(2.88, 286.2, 329.8)	(2.90, 289.1, 302.3)
0.15	(2.95, 289.4, 358.3)	(2.94, 300.4, 347.1)	(2.94, 302.9, 325.1)	(2.93, 298.8, 311.4)	(2.94, 303.4, 308.2)
0.20	(3.01, 348.2, 430.6)	(2.99, 349.1, 415.5)	(2.97, 353.2, 399.6)	(2.96, 351.4, 378.5)	(2.96, 353.7, 364.5)
$n = 100$					
0.01	(2.14, 171.4, 824.5)	(2.47, 168.6, 670.5)	(2.60, 157.2, 379.1)	(2.69, 155.1, 210.1)	(2.75, 155.3, 157.2)
0.02	(2.32, 174.6, 1166.0)	(2.51, 171.1, 454.3)	(2.66, 174.3, 298.2)	(2.71, 170.1, 204.3)	(2.75, 170.9, 173.2)
0.05	(2.74, 224.0, 377.3)	(2.73, 216.0, 338.1)	(2.74, 226.7, 325.5)	(2.77, 225.2, 271.3)	(2.79, 224.4, 233.3)
0.10	(3.14, 617.7, 853.3)	(3.14, 657.1, 893.6)	(3.13, 650.1, 832.4)	(3.13, 637.8, 744.0)	(3.14, 639.7, 677.6)
0.15	(3.01, 354.3, 446.7)	(2.99, 355.0, 424.8)	(2.97, 355.2, 403.1)	(2.96, 353.2, 383.3)	(2.96, 354.5, 366.5)
0.20	(3.00, 317.8, 373.3)	(2.97, 313.8, 354.8)	(2.94, 310.8, 338.2)	(2.93, 310.5, 328.3)	(2.93, 313.9, 322.5)

Table 15: $(K', \text{ARL}_0, \text{SDRL}_0)$ for the hypergeometric np chart with $N = 1000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200\}$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$
$n = 25$					
0.01	(1.85, 39.4, 129.4)	(2.14, 39.8, 110.2)	(2.32, 42.0, 72.7)	(2.41, 41.8, 44.2)	(2.47, 41.9, 41.4)
0.02	(2.26, 76.8, 333.1)	(2.51, 79.8, 210.1)	(2.69, 84.1, 134.2)	(2.79, 84.3, 96.1)	(2.83, 84.1, 84.1)
0.05	(2.51, 166.8, 674.0)	(2.74, 164.5, 398.9)	(2.87, 156.6, 242.8)	(2.94, 158.0, 188.4)	(2.97, 157.5, 159.7)
0.10	(2.37, 121.6, 350.6)	(2.50, 118.3, 228.9)	(2.61, 116.4, 162.3)	(2.65, 116.9, 133.0)	(2.67, 116.6, 118.1)
0.15	(2.90, 579.7, 2157.1)	(3.06, 555.8, 1255.4)	(3.16, 545.3, 847.8)	(3.20, 535.8, 652.2)	(3.23, 539.0, 561.9)
0.20	(2.74, 198.8, 325.1)	(2.72, 197.3, 294.3)	(2.72, 199.0, 263.9)	(2.74, 199.8, 227.9)	(2.76, 200.2, 204.7)
$n = 50$					
0.01	(2.29, 90.6, 634.0)	(2.51, 87.9, 248.9)	(2.71, 91.3, 153.5)	(2.78, 90.6, 105.8)	(2.85, 90.8, 90.9)
0.02	(2.12, 62.2, 234.4)	(2.30, 69.6, 145.9)	(2.45, 67.3, 95.4)	(2.51, 67.3, 73.8)	(2.55, 67.5, 67.4)
0.05	(2.87, 420.6, 2109.6)	(3.06, 428.8, 995.2)	(3.20, 425.0, 671.6)	(3.26, 428.0, 548.4)	(3.29, 424.6, 447.5)
0.10	(2.86, 406.5, 1027.0)	(2.95, 404.9, 812.4)	(3.05, 399.4, 578.2)	(3.09, 403.7, 490.0)	(3.11, 405.4, 427.7)
0.15	(2.82, 225.9, 313.0)	(2.81, 228.9, 304.7)	(2.80, 220.3, 269.3)	(2.81, 223.8, 253.4)	(2.82, 223.0, 231.1)
0.20	(3.07, 457.7, 619.9)	(3.06, 474.2, 618.8)	(3.06, 487.2, 599.1)	(3.06, 485.9, 556.1)	(3.06, 477.3, 499.4)
$n = 75$					
0.01	(2.66, 224.6, 2273.5)	(2.89, 222.9, 704.1)	(3.08, 225.3, 426.1)	(3.18, 228.1, 299.9)	(3.25, 230.4, 237.9)
0.02	(2.84, 431.5, 2345.5)	(3.10, 421.1, 1202.7)	(3.26, 418.2, 777.4)	(3.33, 411.8, 554.6)	(3.37, 412.3, 433.2)
0.05	(2.78, 378.0, 1373.9)	(2.95, 370.4, 791.8)	(3.07, 370.3, 559.9)	(3.11, 371.1, 458.9)	(3.13, 367.6, 387.0)
0.10	(3.06, 568.5, 942.3)	(3.11, 566.1, 831.6)	(3.14, 564.6, 760.5)	(3.16, 568.3, 691.8)	(3.17, 559.3, 599.9)
0.15	(3.06, 462.8, 646.4)	(3.05, 443.2, 575.7)	(3.06, 450.2, 540.9)	(3.07, 447.9, 497.7)	(3.07, 446.3, 464.7)
0.20	(3.17, 601.2, 774.0)	(3.15, 606.7, 749.7)	(3.14, 604.3, 699.8)	(3.14, 612.7, 681.4)	(3.14, 611.0, 642.9)
$n = 100$					
0.01	(2.16, 78.4, 399.2)	(2.34, 81.1, 205.3)	(2.50, 81.6, 125.0)	(2.56, 81.0, 90.9)	(2.60, 81.1, 81.2)
0.02	(2.26, 105.1, 335.7)	(2.41, 93.7, 184.5)	(2.52, 94.7, 134.4)	(2.57, 95.8, 108.9)	(2.60, 95.8, 96.7)
0.05	(2.84, 406.2, 1027.1)	(2.94, 409.3, 863.4)	(3.05, 408.3, 601.0)	(3.09, 407.0, 499.6)	(3.11, 406.2, 432.2)
0.10	(2.96, 323.5, 429.2)	(2.96, 338.1, 435.7)	(2.95, 332.5, 404.0)	(2.96, 339.1, 388.3)	(2.97, 336.8, 356.0)
0.15	(3.11, 496.3, 637.0)	(3.10, 508.3, 626.0)	(3.09, 506.1, 587.3)	(3.08, 496.6, 549.0)	(3.09, 505.4, 533.2)
0.20	(3.08, 413.4, 499.0)	(3.05, 412.3, 476.4)	(3.03, 407.8, 449.1)	(3.03, 420.8, 452.4)	(3.02, 413.0, 427.4)

Table 16: $(K', \text{ARL}_0, \text{SDRL}_0)$ for the hypergeometric np chart with $N = 2000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200\}$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$
$n = 25$					
0.01	(1.84, 37.3, 112.4)	(2.12, 37.8, 98.2)	(2.31, 40.3, 66.2)	(2.39, 40.2, 42.2)	(2.46, 40.3, 39.8)
0.02	(2.25, 71.6, 285.6)	(2.50, 74.7, 188.0)	(2.68, 79.3, 122.7)	(2.77, 79.7, 89.9)	(2.81, 79.6, 79.5)
0.05	(2.50, 154.6, 596.9)	(2.72, 153.1, 361.7)	(2.86, 146.8, 223.8)	(2.92, 148.4, 175.6)	(2.95, 148.0, 150.0)
0.10	(2.35, 109.3, 278.0)	(2.48, 112.1, 213.7)	(2.59, 110.6, 152.7)	(2.63, 111.1, 126.0)	(2.65, 110.8, 111.9)
0.15	(2.88, 486.3, 1882.6)	(3.04, 514.5, 1143.9)	(3.14, 506.0, 778.6)	(3.18, 497.9, 603.6)	(3.21, 501.1, 522.2)
0.20	(2.72, 187.4, 303.1)	(2.71, 199.7, 307.1)	(2.71, 189.5, 251.6)	(2.72, 188.3, 215.0)	(2.74, 189.4, 193.4)
$n = 50$					
0.01	(2.26, 76.4, 414.0)	(2.47, 75.7, 192.6)	(2.67, 77.4, 124.8)	(2.77, 80.2, 91.1)	(2.81, 80.5, 80.5)
0.02	(2.10, 66.1, 207.7)	(2.27, 62.4, 124.2)	(2.42, 60.9, 83.8)	(2.48, 61.1, 66.5)	(2.52, 61.4, 61.3)
0.05	(2.84, 373.0, 1615.0)	(3.03, 361.8, 801.8)	(3.16, 361.1, 554.5)	(3.22, 364.9, 459.7)	(3.25, 362.7, 381.3)
0.10	(2.82, 348.8, 846.3)	(2.93, 354.8, 722.2)	(3.02, 359.1, 512.7)	(3.05, 350.7, 422.0)	(3.07, 352.5, 371.4)
0.15	(2.78, 191.0, 255.0)	(2.78, 203.0, 266.8)	(2.77, 200.3, 246.8)	(2.78, 201.6, 228.3)	(2.79, 200.1, 208.0)
0.20	(3.03, 400.0, 537.1)	(3.02, 413.7, 534.3)	(3.02, 424.9, 518.0)	(3.02, 421.2, 476.3)	(3.02, 416.8, 435.1)
$n = 75$					
0.01	(2.62, 174.8, 1158.0)	(2.84, 191.7, 517.7)	(3.03, 179.6, 327.2)	(3.13, 177.8, 230.3)	(3.19, 178.7, 182.8)
0.02	(2.82, 314.4, 1642.3)	(3.07, 312.0, 793.4)	(3.20, 315.0, 542.1)	(3.27, 314.2, 404.8)	(3.31, 315.9, 329.7)
0.05	(2.73, 296.3, 972.0)	(2.90, 294.1, 597.8)	(3.01, 295.0, 431.1)	(3.05, 296.9, 360.5)	(3.07, 294.8, 309.5)
0.10	(3.00, 455.6, 747.3)	(3.05, 456.5, 668.7)	(3.08, 451.9, 599.1)	(3.09, 445.1, 534.2)	(3.11, 448.5, 479.1)
0.15	(3.00, 374.9, 516.2)	(2.99, 360.2, 461.6)	(3.00, 366.9, 436.7)	(3.01, 365.2, 404.1)	(3.01, 363.6, 378.3)
0.20	(3.11, 484.8, 616.9)	(3.09, 489.1, 597.6)	(3.08, 487.4, 559.3)	(3.08, 497.0, 549.0)	(3.08, 494.5, 519.2)
$n = 100$					
0.01	(2.10, 59.6, 216.6)	(2.29, 66.8, 137.4)	(2.44, 64.8, 90.9)	(2.50, 64.9, 71.0)	(2.53, 65.1, 65.0)
0.02	(2.80, 332.1, 1657.6)	(3.01, 319.7, 787.2)	(3.15, 325.2, 518.7)	(3.22, 331.6, 425.1)	(3.25, 330.5, 345.3)
0.05	(2.77, 309.3, 769.0)	(2.88, 299.9, 595.8)	(2.97, 300.9, 425.6)	(3.01, 303.9, 368.6)	(3.03, 302.1, 319.6)
0.10	(2.88, 248.5, 324.9)	(2.88, 258.2, 326.3)	(2.88, 259.3, 310.2)	(2.88, 256.9, 290.1)	(2.89, 258.2, 272.4)
0.15	(3.03, 373.6, 473.2)	(3.02, 382.2, 463.9)	(3.01, 382.8, 439.8)	(3.00, 374.4, 410.7)	(3.00, 375.4, 393.7)
0.20	(3.00, 315.1, 376.4)	(2.97, 314.8, 359.8)	(2.96, 325.0, 357.2)	(2.95, 321.4, 343.5)	(2.94, 315.9, 326.4)

Table 17: $(K', \text{ARL}_0, \text{SDRL}_0)$ for the hypergeometric np chart with $N = 5000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200\}$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$
$n = 25$					
0.01	(1.81, 36.3, 104.0)	(2.12, 36.7, 92.2)	(2.31, 39.3, 63.0)	(2.38, 39.3, 41.1)	(2.45, 39.4, 38.9)
0.02	(2.24, 68.8, 263.0)	(2.49, 71.9, 176.8)	(2.67, 76.7, 116.8)	(2.76, 77.2, 86.6)	(2.80, 77.1, 77.0)
0.05	(2.49, 148.0, 557.4)	(2.71, 147.0, 342.1)	(2.85, 141.4, 213.6)	(2.91, 143.1, 168.7)	(2.94, 142.8, 144.7)
0.10	(2.34, 105.8, 265.9)	(2.47, 108.6, 205.4)	(2.58, 107.3, 147.4)	(2.62, 107.8, 122.1)	(2.64, 107.5, 108.7)
0.15	(2.87, 464.7, 1769.5)	(3.03, 491.9, 1083.7)	(3.13, 484.4, 741.0)	(3.17, 480.8, 590.6)	(3.20, 480.8, 503.0)
0.20	(2.71, 181.1, 291.0)	(2.70, 192.9, 294.9)	(2.70, 183.4, 242.7)	(2.71, 182.4, 208.0)	(2.73, 183.4, 187.3)
$n = 50$					
0.01	(2.24, 70.0, 338.8)	(2.46, 70.1, 169.2)	(2.66, 78.0, 130.5)	(2.75, 75.1, 84.3)	(2.79, 75.4, 75.3)
0.02	(2.09, 61.7, 185.7)	(2.25, 58.7, 113.8)	(2.40, 57.7, 78.1)	(2.46, 58.0, 62.8)	(2.50, 58.2, 58.1)
0.05	(2.82, 337.7, 1390.4)	(3.02, 333.5, 763.5)	(3.14, 329.7, 498.5)	(3.19, 330.3, 405.0)	(3.22, 331.0, 346.2)
0.10	(2.80, 319.9, 759.0)	(2.91, 326.8, 653.6)	(3.00, 331.1, 468.2)	(3.03, 328.4, 395.3)	(3.05, 326.1, 342.9)
0.15	(3.06, 538.9, 860.3)	(3.10, 528.5, 744.2)	(3.13, 549.9, 732.5)	(3.14, 542.1, 652.3)	(3.16, 541.7, 579.5)
0.20	(3.01, 372.4, 494.3)	(3.00, 383.6, 492.7)	(3.00, 393.0, 476.6)	(3.00, 392.9, 446.2)	(3.00, 387.7, 405.8)
$n = 75$					
0.01	(2.59, 147.2, 819.4)	(2.81, 163.1, 410.2)	(3.04, 155.9, 268.2)	(3.10, 157.1, 195.6)	(3.15, 156.5, 159.8)
0.02	(2.79, 265.9, 1232.9)	(3.03, 267.1, 640.6)	(3.17, 271.5, 450.4)	(3.24, 274.9, 344.5)	(3.28, 275.2, 287.9)
0.05	(2.71, 263.1, 878.6)	(2.88, 262.5, 537.4)	(2.97, 260.7, 374.3)	(3.01, 258.9, 309.6)	(3.04, 262.1, 275.5)
0.10	(2.97, 402.5, 655.4)	(3.02, 403.6, 587.2)	(3.04, 395.7, 514.1)	(3.06, 398.6, 476.9)	(3.08, 398.9, 427.4)
0.15	(2.97, 333.3, 454.9)	(2.96, 326.8, 411.0)	(2.97, 331.6, 390.5)	(2.98, 330.1, 364.3)	(2.98, 327.5, 340.7)
0.20	(3.08, 432.4, 546.5)	(3.06, 445.2, 539.7)	(3.05, 442.4, 507.6)	(3.04, 432.9, 474.8)	(3.04, 434.3, 454.1)
$n = 100$					
0.01	(2.08, 61.7, 185.7)	(2.25, 58.7, 113.8)	(2.40, 57.7, 78.1)	(2.46, 58.0, 62.8)	(2.50, 58.2, 58.1)
0.02	(2.79, 268.5, 1228.1)	(2.98, 283.8, 649.9)	(3.12, 277.6, 439.7)	(3.17, 275.0, 344.7)	(3.20, 274.8, 286.3)
0.05	(2.73, 264.5, 634.2)	(2.84, 255.3, 487.4)	(2.93, 259.7, 356.9)	(2.97, 260.6, 311.1)	(2.98, 256.9, 270.7)
0.10	(2.84, 216.7, 281.7)	(2.84, 223.2, 279.2)	(2.83, 219.9, 259.8)	(2.84, 225.0, 253.4)	(2.84, 221.9, 232.8)
0.15	(2.99, 321.4, 401.9)	(2.97, 322.8, 386.8)	(2.96, 323.9, 369.8)	(2.96, 326.9, 359.7)	(2.96, 325.6, 341.9)
0.20	(2.96, 278.1, 329.1)	(2.93, 275.2, 312.9)	(2.91, 275.2, 300.5)	(2.90, 272.5, 289.4)	(2.90, 275.8, 285.4)

Table 18: $(K', \text{ARL}_0, \text{SDRL}_0)$ for the hypergeometric np chart with $N = 10000$, $n \in \{25, 50, 75, 100\}$, $p_0 \in \{0.01, 0.02, 0.05, 0.10, 0.15, 0.20\}$, $m \in \{10, 20, 50, 100, 200\}$

p_0	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$
$n = 25$					
0.01	(1.83, 35.9, 102.1)	(2.11, 36.4, 90.4)	(2.30, 39.0, 62.0)	(2.38, 39.0, 40.7)	(2.44, 39.1, 38.6)
0.02	(2.24, 68.0, 256.2)	(2.48, 71.1, 173.3)	(2.67, 75.8, 115.0)	(2.76, 76.4, 85.6)	(2.80, 76.3, 76.2)
0.05	(2.48, 145.9, 545.1)	(2.71, 145.0, 335.9)	(2.84, 139.7, 210.4)	(2.90, 141.4, 166.4)	(2.94, 141.1, 143.0)
0.10	(2.34, 104.7, 262.1)	(2.47, 107.5, 202.7)	(2.58, 106.2, 145.8)	(2.62, 106.8, 120.9)	(2.64, 106.5, 107.6)
0.15	(2.87, 502.8, 1786.3)	(3.03, 485.7, 1064.4)	(3.13, 477.6, 729.1)	(3.17, 474.1, 581.8)	(3.19, 472.4, 490.8)
0.20	(2.71, 179.1, 287.1)	(2.69, 178.0, 261.3)	(2.69, 180.3, 236.4)	(2.71, 181.4, 206.2)	(2.73, 181.8, 185.9)
$n = 50$					
0.01	(2.21, 65.3, 234.9)	(2.45, 68.4, 162.5)	(2.65, 73.3, 109.2)	(2.74, 73.5, 82.3)	(2.78, 73.8, 73.8)
0.02	(2.08, 60.4, 179.2)	(2.24, 57.6, 110.7)	(2.39, 56.7, 76.4)	(2.45, 57.0, 61.7)	(2.49, 57.3, 57.1)
0.05	(2.81, 327.1, 1317.3)	(3.01, 323.4, 734.2)	(3.13, 320.2, 481.8)	(3.19, 324.2, 403.7)	(3.22, 323.3, 341.0)
0.10	(2.79, 311.0, 732.7)	(2.90, 318.2, 632.9)	(2.99, 322.5, 454.7)	(3.02, 315.5, 377.3)	(3.04, 317.3, 334.0)
0.15	(3.05, 524.3, 835.9)	(3.10, 541.6, 775.9)	(3.12, 532.3, 703.4)	(3.13, 520.2, 622.2)	(3.15, 526.0, 560.7)
0.20	(3.00, 361.1, 481.8)	(2.99, 373.0, 478.0)	(2.99, 383.1, 463.8)	(2.99, 380.2, 428.5)	(3.00, 381.7, 401.0)
$n = 75$					
0.01	(2.58, 139.7, 741.4)	(2.80, 155.3, 382.4)	(3.03, 149.2, 252.6)	(3.09, 150.7, 186.1)	(3.14, 150.2, 153.3)
0.02	(2.79, 270.9, 1276.8)	(3.02, 254.4, 599.7)	(3.17, 266.2, 426.7)	(3.22, 260.3, 327.0)	(3.27, 263.2, 275.1)
0.05	(2.70, 252.4, 828.2)	(2.88, 252.1, 511.1)	(2.96, 250.6, 357.8)	(3.00, 251.2, 302.9)	(3.03, 252.7, 266.5)
0.10	(2.96, 386.7, 628.1)	(3.01, 387.9, 563.1)	(3.03, 381.7, 496.5)	(3.05, 383.2, 457.5)	(3.07, 385.0, 413.0)
0.15	(2.96, 320.8, 436.8)	(2.95, 321.6, 405.4)	(2.96, 319.5, 375.7)	(2.97, 318.2, 350.8)	(2.97, 316.0, 328.7)
0.20	(3.07, 425.4, 540.6)	(3.05, 428.3, 517.9)	(3.03, 413.0, 468.9)	(3.03, 418.7, 458.7)	(3.03, 419.3, 438.6)
$n = 100$					
0.01	(2.07, 59.1, 172.7)	(2.24, 56.5, 107.5)	(2.39, 55.6, 74.7)	(2.45, 56.0, 60.5)	(2.48, 56.3, 56.1)
0.02	(2.77, 251.6, 1105.5)	(2.96, 266.5, 595.0)	(3.10, 261.5, 409.2)	(3.16, 261.8, 323.6)	(3.19, 260.0, 271.9)
0.05	(2.72, 250.3, 591.1)	(2.83, 242.4, 457.8)	(2.92, 246.8, 337.2)	(2.95, 246.3, 294.4)	(2.97, 245.8, 260.1)
0.10	(2.83, 213.0, 279.8)	(2.82, 213.0, 265.5)	(2.82, 212.8, 250.4)	(2.82, 212.2, 237.5)	(2.83, 213.1, 224.1)
0.15	(2.98, 313.1, 393.1)	(2.96, 314.7, 375.4)	(2.95, 311.8, 354.9)	(2.94, 306.1, 334.2)	(2.94, 307.2, 321.4)
0.20	(2.94, 258.8, 306.7)	(2.92, 266.1, 300.6)	(2.90, 267.1, 291.6)	(2.89, 264.4, 281.3)	(2.88, 260.1, 268.2)

Table 19: $(K, ARL_1, SDRL_1)$ for the hypergeometric np chart and $(K'', ARL_1, SDRL_1)$ for the binomial np chart with $N = 100$, $n \in \{25, 50\}$, $p_0 \in \{0.01, 0.05, 0.10, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	-	-	-	-	-	-	-
	1.2	-	-	-	-	-	-	-
	1.5	-	-	-	-	-	-	-
	2.0	-	-	-	-	-	-	-
0.05	1.1	-	-	-	-	-	-	-
	1.2	(3.00, 475.9, 2088.2)	(3.00, 260.0, 1142.6)	(3.00, 190.2, 319.8)	(3.00, 204.8, 265.2)	(3.00, 225.2, 272.7)	(3.00, 270.3, 283.8)	(3.00, 286.5, 285.9)
	1.5	(3.00, 134.1, 1337.0)	(3.00, 76.0, 219.6)	(3.00, 67.5, 93.7)	(3.00, 72.7, 90.8)	(3.00, 79.4, 93.6)	(3.00, 94.1, 97.8)	(3.00, 99.4, 98.8)
	2.0	(3.23, 112.5, 458.7)	(3.48, 127.6, 289.7)	(3.75, 158.2, 264.0)	(3.90, 172.7, 246.4)	(4.05, 184.8, 267.8)	(4.25, 218.2, 347.0)	(3.45, 153.2, 152.6)
0.10	1.1	(3.00, 775.9, 11211.3)	(3.00, 344.4, 1117.3)	(3.00, 245.2, 459.1)	(3.00, 214.0, 254.0)	(3.00, 213.0, 213.9)	(3.00, 213.6, 213.0)	(3.00, 213.6, 213.0)
	1.2	(3.55, 1329.4, 8194.7)	(3.39, 480.7, 1161.3)	(3.34, 311.7, 493.9)	(3.33, 264.4, 347.4)	(3.40, 262.2, 318.0)	(3.55, 266.8, 332.1)	(3.00, 242.7, 242.2)
	1.5	(3.00, 287.5, 1886.4)	(3.00, 153.4, 390.2)	(3.00, 118.5, 192.2)	(3.00, 107.4, 120.0)	(3.00, 107.4, 107.4)	(3.00, 107.7, 107.1)	(3.00, 107.7, 107.1)
	2.0	(3.55, 657.1, 3366.6)	(3.39, 262.0, 577.8)	(3.34, 177.5, 267.0)	(3.33, 153.4, 193.2)	(3.40, 152.6, 178.7)	(3.55, 155.0, 185.7)	(3.00, 142.5, 142.0)
0.20	1.1	(3.00, 257.3, 418.8)	(3.00, 231.4, 327.3)	(3.00, 218.3, 263.1)	(3.00, 233.7, 260.0)	(3.00, 252.2, 266.5)	(3.00, 272.5, 272.2)	(3.00, 272.8, 272.3)
	1.2	(2.90, 202.3, 396.3)	(3.00, 224.5, 411.9)	(3.13, 251.8, 352.5)	(3.22, 284.5, 342.4)	(3.32, 309.4, 378.2)	(3.43, 330.9, 430.1)	(3.00, 276.6, 276.1)
	1.5	(3.00, 132.6, 274.7)	(3.00, 105.0, 171.7)	(3.00, 91.1, 113.3)	(3.00, 95.0, 104.3)	(3.00, 101.6, 106.3)	(3.00, 109.2, 108.8)	(3.00, 109.4, 108.8)
	2.0	(2.90, 100.2, 187.7)	(3.00, 105.5, 177.3)	(3.13, 118.6, 157.2)	(3.22, 133.6, 154.8)	(3.32, 144.3, 169.1)	(3.43, 153.1, 189.5)	(3.00, 130.9, 130.4)
$n = 50$	1.1	(3.00, 16.5, 28.6)	(3.00, 14.0, 18.5)	(3.00, 12.9, 14.1)	(3.00, 13.4, 13.6)	(3.00, 14.1, 14.0)	(3.00, 14.9, 14.3)	(3.00, 14.9, 14.3)
	1.2	(2.90, 18.0, 31.8)	(3.00, 18.4, 24.8)	(3.13, 20.5, 23.7)	(3.22, 22.8, 24.1)	(3.32, 24.2, 25.6)	(3.43, 25.1, 27.7)	(3.00, 22.7, 22.1)
	1.5	(3.00, 2.5, 2.4)	(3.00, 2.4, 2.0)	(3.00, 2.3, 1.8)	(3.00, 2.4, 1.8)	(3.00, 2.4, 1.9)	(3.00, 2.5, 1.9)	(3.00, 2.5, 1.9)
	2.0	(2.90, 3.1, 3.3)	(3.00, 3.3, 3.1)	(3.13, 3.5, 3.2)	(3.22, 3.8, 3.3)	(3.32, 3.9, 3.4)	(3.43, 4.0, 3.5)	(3.00, 3.8, 3.2)
0.01	1.1	-	-	-	-	-	-	-
	1.2	-	-	-	-	-	-	-
	1.5	-	-	-	-	-	-	-
	2.0	-	-	-	-	-	-	-
0.05	1.1	-	-	-	-	-	-	-
	1.2	-	-	-	-	-	-	-
	1.5	-	-	-	-	-	-	-
	2.0	-	-	-	-	-	-	-
0.10	1.1	(3.00, 513.5, 1093.9)	(3.00, 477.9, 999.8)	(3.00, 314.4, 601.4)	(3.00, 257.0, 352.8)	(3.00, 241.8, 248.2)	(3.00, 240.8, 240.2)	(3.00, 240.8, 240.2)
	1.2	(3.01, 267.6, 762.3)	(3.22, 306.9, 615.3)	(3.36, 336.1, 471.2)	(3.40, 352.0, 420.0)	(3.39, 358.6, 393.2)	(3.34, 358.2, 391.5)	(3.30, 417.5, 417.0)
	1.5	(3.00, 151.5, 297.4)	(3.00, 133.7, 263.5)	(3.00, 90.4, 159.9)	(3.00, 75.7, 97.7)	(3.00, 71.8, 72.8)	(3.00, 71.5, 71.0)	(3.00, 71.5, 71.0)
	2.0	(3.01, 123.7, 306.4)	(3.22, 143.1, 259.9)	(3.36, 158.1, 210.6)	(3.40, 166.0, 192.8)	(3.39, 169.3, 183.5)	(3.34, 169.1, 182.9)	(3.30, 195.5, 195.0)
0.20	1.1	(3.00, 10.9, 19.2)	(3.00, 9.6, 12.5)	(3.00, 8.2, 8.9)	(3.00, 7.8, 7.5)	(3.00, 7.7, 7.1)	(3.00, 7.7, 7.1)	(3.00, 7.7, 7.1)
	1.2	(3.01, 21.4, 38.2)	(3.22, 24.8, 35.4)	(3.36, 27.6, 32.4)	(3.40, 29.0, 31.3)	(3.39, 29.6, 30.8)	(3.34, 29.5, 30.7)	(3.30, 33.3, 32.8)
	1.5	(3.00, 1.8, 1.4)	(3.00, 1.8, 1.3)	(3.00, 1.7, 1.1)	(3.00, 1.7, 1.1)	(3.00, 1.7, 1.1)	(3.00, 1.7, 1.1)	(3.00, 1.7, 1.1)
	2.0	(3.01, 3.9, 4.4)	(3.22, 4.4, 4.5)	(3.36, 4.8, 4.5)	(3.40, 4.9, 4.6)	(3.39, 5.0, 4.6)	(3.34, 5.0, 4.6)	(3.30, 5.4, 4.8)
0.01	1.1	(3.00, 211.8, 358.9)	(3.00, 180.1, 275.2)	(3.00, 167.0, 212.6)	(3.00, 168.3, 210.3)	(3.00, 172.5, 214.8)	(3.00, 195.6, 235.4)	(3.00, 278.5, 277.9)
	1.2	(3.00, 190.4, 307.2)	(2.99, 159.2, 231.9)	(3.01, 151.5, 188.7)	(3.06, 160.5, 189.4)	(3.11, 172.0, 202.0)	(3.19, 237.3, 269.1)	(3.19, 318.8, 318.3)
	1.5	(3.00, 58.7, 109.7)	(3.00, 46.3, 72.5)	(3.00, 41.4, 50.7)	(3.00, 41.4, 49.1)	(3.00, 41.9, 49.5)	(3.00, 45.4, 52.0)	(3.00, 59.2, 58.7)
	2.0	(3.00, 80.7, 144.1)	(2.99, 63.7, 93.9)	(3.01, 59.1, 71.0)	(3.06, 62.0, 70.4)	(3.11, 65.9, 74.6)	(3.19, 87.4, 96.8)	(3.19, 113.6, 113.1)
0.05	1.1	(3.00, 3.6, 3.9)	(3.00, 3.4, 3.2)	(3.00, 3.3, 2.9)	(3.00, 3.3, 2.9)	(3.00, 3.3, 2.9)	(3.00, 3.4, 3.0)	(3.00, 3.9, 3.4)
	1.2	(3.00, 9.0, 12.8)	(2.99, 7.8, 9.0)	(3.01, 7.6, 7.7)	(3.06, 7.9, 7.8)	(3.11, 8.2, 8.1)	(3.19, 9.8, 9.8)	(3.19, 11.8, 11.3)
	1.5	(3.00, 1.1, 0.3)	(3.00, 1.1, 0.3)	(3.00, 1.1, 0.3)	(3.00, 1.1, 0.3)	(3.00, 1.1, 0.3)	(3.00, 1.1, 0.3)	(3.00, 1.1, 0.3)
	2.0	(3.00, 1.6, 1.1)	(2.99, 1.6, 1.0)	(3.01, 1.6, 0.9)	(3.06, 1.6, 0.9)	(3.11, 1.6, 1.0)	(3.19, 1.7, 1.1)	(3.19, 1.9, 1.2)

Table 20: $(K, \text{ARL}_1, \text{SDRL}_1)$ for the hypergeometric np chart and $(K'', \text{ARL}_1, \text{SDRL}_1)$ for the binomial np chart with $N = 200$, $n \in \{25, 50\}$, $p_0 \in \{0.01, 0.05, 0.10, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	-	-	-	-	-	-	-
	1.2	-	-	-	-	-	-	-
	1.5	(3.00, 142.1, 357.2)	(3.00, 145.7, 356.5)	(3.00, 61.7, 206.0)	(3.00, 37.3, 124.8)	(3.00, 25.3, 44.2)	(3.00, 24.0, 23.5)	(3.00, 24.0, 23.5)
	2.0	(2.04, 20.4, 52.2) (3.00, 83.5, 651.5) (2.04, 11.5, 23.5)	(2.34, 26.6, 59.3) (3.00, 45.2, 139.5) (2.34, 14.6, 27.4)	(2.75, 25.9, 52.2) (3.00, 22.8, 56.0) (2.75, 14.5, 24.4)	(2.92, 25.8, 51.3) (3.00, 16.5, 35.0) (2.92, 14.5, 24.0)	(3.08, 26.7, 53.8) (3.00, 13.4, 16.0) (3.08, 14.8, 25.1)	(3.31, 27.6, 56.6) (3.00, 13.0, 12.5) (3.31, 15.3, 26.3)	(3.00, 18.7, 18.1) (3.00, 13.0, 12.5) (3.00, 11.3, 10.8)
0.05	1.1	(3.00, 556.5, 5892.6)	(3.00, 250.7, 812.0)	(3.00, 173.5, 309.3)	(3.00, 167.2, 186.1)	(3.00, 173.7, 175.9)	(3.00, 177.0, 176.5)	(3.00, 177.0, 176.5)
	1.2	(3.39, 694.0, 5069.6)	(3.25, 295.4, 756.7)	(3.20, 182.1, 307.9)	(3.26, 183.2, 301.4)	(3.32, 187.6, 307.1)	(3.38, 181.6, 299.0)	(3.00, 94.4, 93.8)
	1.5	(3.00, 292.1, 2088.0)	(3.00, 148.0, 413.3)	(3.00, 109.1, 176.8)	(3.00, 106.8, 116.4)	(3.00, 110.9, 112.1)	(3.00, 113.0, 112.5)	(3.00, 113.0, 112.5)
	2.0	(3.39, 413.7, 2564.6)	(3.25, 190.2, 452.2)	(3.20, 121.8, 198.0)	(3.26, 122.6, 194.5)	(3.32, 125.4, 198.1)	(3.38, 121.6, 192.9)	(3.00, 66.5, 65.9)
0.10	1.1	(3.00, 421.9, 2299.3)	(3.00, 237.1, 552.1)	(3.00, 182.3, 298.3)	(3.00, 152.5, 243.5)	(3.00, 124.2, 178.9)	(3.00, 102.9, 102.6)	(3.00, 102.8, 102.3)
	1.2	(3.18, 455.1, 2112.4)	(3.13, 253.3, 555.2)	(3.12, 197.8, 288.3)	(3.03, 164.8, 207.4)	(2.97, 134.7, 182.4)	(2.96, 106.9, 151.4)	(2.99, 64.1, 63.5)
	1.5	(3.00, 204.7, 878.8)	(3.00, 125.7, 259.4)	(3.00, 100.2, 154.2)	(3.00, 85.3, 127.3)	(3.00, 71.2, 95.7)	(3.00, 60.6, 60.2)	(3.00, 60.6, 60.0)
	2.0	(3.18, 242.1, 957.8)	(3.13, 144.5, 289.4)	(3.12, 116.3, 161.7)	(3.03, 98.3, 121.2)	(2.97, 81.3, 106.9)	(2.96, 65.5, 89.2)	(2.99, 41.3, 40.7)
0.20	1.1	(3.00, 39.9, 103.0)	(3.00, 29.3, 46.4)	(3.00, 25.2, 33.2)	(3.00, 22.4, 28.3)	(3.00, 19.7, 22.7)	(3.00, 17.7, 17.2)	(3.00, 17.7, 17.2)
	1.2	(3.18, 53.9, 145.7)	(3.13, 37.7, 60.7)	(3.12, 32.5, 40.3)	(3.03, 28.5, 33.0)	(2.97, 24.3, 29.3)	(2.96, 20.4, 24.9)	(2.99, 14.4, 13.9)
	1.5	(3.00, 7.6, 11.6)	(3.00, 6.5, 7.6)	(3.00, 6.0, 6.3)	(3.00, 5.6, 5.7)	(3.00, 5.2, 4.9)	(3.00, 4.9, 4.3)	(3.00, 4.9, 4.3)
	2.0	(3.18, 10.4, 17.9)	(3.13, 8.5, 10.6)	(3.12, 7.9, 8.4)	(3.03, 7.2, 7.4)	(2.97, 6.4, 6.7)	(2.96, 5.7, 5.8)	(2.99, 4.6, 4.0)
$n = 50$								
0.01	1.1	-	-	-	-	-	-	-
	1.2	-	-	-	-	-	-	-
	1.5	-	-	-	-	-	-	-
	2.0	-	-	-	-	-	-	-
0.05	1.1	(3.00, 760.3, 14481.2)	(3.00, 350.0, 1106.4)	(3.00, 236.6, 460.3)	(3.00, 184.1, 276.9)	(3.00, 166.8, 177.4)	(3.00, 165.1, 164.6)	(3.00, 165.1, 164.6)
	1.2	(3.64, 1288.9, 8690.3)	(3.50, 493.6, 1194.3)	(3.41, 312.6, 476.8)	(3.33, 232.6, 326.1)	(3.35, 205.8, 263.6)	(3.46, 198.9, 245.7)	(3.00, 176.9, 176.4)
	1.5	(3.00, 277.2, 2171.7)	(3.00, 154.2, 381.8)	(3.00, 113.1, 193.8)	(3.00, 92.9, 124.0)	(3.00, 86.2, 89.1)	(3.00, 85.5, 85.0)	(3.00, 85.5, 85.0)
	2.0	(3.64, 638.4, 3487.8)	(3.50, 269.4, 594.0)	(3.41, 178.7, 260.7)	(3.33, 136.3, 182.9)	(3.35, 122.1, 150.3)	(3.46, 118.4, 141.1)	(3.00, 106.7, 106.1)
0.10	1.1	(3.00, 37.9, 98.9)	(3.00, 27.8, 46.1)	(3.00, 23.5, 30.9)	(3.00, 21.1, 23.2)	(3.00, 20.3, 20.0)	(3.00, 20.2, 19.7)	(3.00, 20.2, 19.7)
	1.2	(3.64, 119.9, 403.5)	(3.50, 63.3, 111.6)	(3.41, 46.8, 61.0)	(3.33, 37.9, 45.7)	(3.35, 35.0, 39.3)	(3.46, 34.2, 37.5)	(3.00, 31.7, 31.1)
	1.5	(3.00, 19.9, 36.3)	(3.00, 16.1, 22.0)	(3.00, 14.4, 16.7)	(3.00, 13.4, 14.5)	(3.00, 12.5, 12.5)	(3.00, 12.1, 11.5)	(3.00, 12.1, 11.5)
	2.0	(3.00, 21.6, 39.5)	(3.04, 20.0, 27.7)	(3.06, 18.5, 21.1)	(3.00, 16.6, 18.3)	(2.97, 15.0, 16.7)	(2.98, 14.4, 16.1)	(2.99, 10.3, 9.7)
0.20	1.1	(3.00, 3.0, 3.2)	(3.00, 2.8, 2.5)	(3.00, 2.7, 2.2)	(3.00, 2.6, 2.1)	(3.00, 2.5, 1.9)	(3.00, 2.5, 1.9)	(3.00, 2.5, 1.9)
	1.2	(3.00, 3.5, 3.8)	(3.04, 3.4, 3.3)	(3.06, 3.3, 2.9)	(3.00, 3.1, 2.7)	(2.97, 3.0, 2.5)	(2.98, 2.9, 2.5)	(2.99, 2.5, 1.8)
	1.5	(3.00, 19.9, 36.3)	(3.00, 16.1, 22.0)	(3.00, 14.4, 16.7)	(3.00, 13.4, 14.5)	(3.00, 12.5, 12.5)	(3.00, 12.1, 11.5)	(3.00, 12.1, 11.5)
	2.0	(3.00, 21.6, 39.5)	(3.04, 20.0, 27.7)	(3.06, 18.5, 21.1)	(3.00, 16.6, 18.3)	(2.97, 15.0, 16.7)	(2.98, 14.4, 16.1)	(2.99, 10.3, 9.7)
0.01	1.1	-	-	-	-	-	-	-
	1.2	-	-	-	-	-	-	-
	1.5	-	-	-	-	-	-	-
	2.0	-	-	-	-	-	-	-
0.05	1.1	(3.00, 250.2, 417.6)	(3.00, 232.4, 381.1)	(3.00, 193.4, 289.3)	(3.00, 169.2, 216.3)	(3.00, 156.4, 165.8)	(3.00, 153.6, 153.0)	(3.00, 153.6, 153.0)
	1.2	(3.04, 279.8, 900.5)	(3.19, 291.5, 565.3)	(3.22, 243.5, 334.2)	(3.19, 210.5, 269.5)	(3.19, 188.5, 236.1)	(3.25, 189.0, 236.8)	(3.00, 144.1, 143.5)
	1.5	(3.00, 114.0, 219.3)	(3.00, 95.6, 154.5)	(3.00, 80.2, 109.8)	(3.00, 72.2, 85.8)	(3.00, 68.0, 70.2)	(3.00, 67.0, 66.5)	(3.00, 67.0, 66.5)
	2.0	(3.04, 128.1, 353.0)	(3.19, 136.7, 241.0)	(3.22, 117.8, 154.1)	(3.19, 103.4, 127.4)	(3.19, 93.7, 112.8)	(3.25, 94.0, 113.1)	(3.00, 74.0, 73.4)
0.10	1.1	(3.00, 15.9, 27.9)	(3.00, 13.8, 18.2)	(3.00, 12.5, 14.0)	(3.00, 11.9, 12.2)	(3.00, 11.5, 11.1)	(3.00, 11.4, 10.9)	(3.00, 11.4, 10.9)
	1.2	(3.04, 21.8, 41.3)	(3.19, 24.0, 33.6)	(3.22, 22.1, 25.6)	(3.19, 20.2, 22.3)	(3.19, 18.8, 20.4)	(3.25, 18.8, 20.4)	(3.00, 16.0, 15.4)
	1.5	(3.00, 2.7, 2.7)	(3.00, 2.6, 2.3)	(3.00, 2.6, 2.1)	(3.00, 2.5, 1.9)	(3.00, 2.5, 1.9)	(3.00, 2.5, 1.9)	(3.00, 2.5, 1.9)
	2.0	(3.04, 3.9, 4.5)	(3.19, 4.3, 4.4)	(3.22, 4.2, 3.9)	(3.19, 4.0, 3.6)	(3.19, 3.8, 3.4)	(3.25, 3.8, 3.4)	(3.00, 3.5, 2.9)
0.20	1.1	(3.00, 192.9, 313.4)	(3.00, 168.7, 241.6)	(3.00, 151.3, 183.6)	(3.00, 146.8, 159.7)	(3.00, 149.7, 152.6)	(3.00, 153.9, 153.3)	(3.00, 153.9, 153.3)
	1.2	(3.00, 190.4, 307.2)	(3.01, 169.0, 246.9)	(3.03, 159.0, 198.8)	(3.07, 166.1, 197.0)	(3.11, 172.0, 202.0)	(3.15, 172.6, 202.7)	(3.00, 131.7, 131.1)
	1.5	(3.00, 72.4, 132.2)	(3.00, 58.7, 88.0)	(3.00, 51.1, 61.8)	(3.00, 49.0, 52.8)	(3.00, 49.6, 50.0)	(3.00, 50.8, 50.2)	(3.00, 50.8, 50.2)
	2.0	(3.00, 80.7, 144.1)	(3.01, 67.2, 99.8)	(3.03, 61.6, 74.4)	(3.07, 63.9, 72.9)	(3.11, 65.9, 74.6)	(3.15, 66.1, 74.8)	(3.00, 52.4, 51.8)
0.01	1.1	(3.00, 6.2, 8.1)	(3.00, 5.6, 6.1)	(3.00, 5.3, 5.2)	(3.00, 5.3, 4.9)	(3.00, 5.3, 4.8)	(3.00, 5.4, 4.9)	(3.00, 5.4, 4.9)
	1.2	(3.00, 9.0, 12.8)	(3.01, 8.1, 9.3)	(3.03, 7.8, 8.0)	(3.07, 8.0, 8.0)	(3.11, 8.2, 8.1)	(3.15, 8.2, 8.1)	(3.00, 7.2, 6.6)
	1.5	(3.00, 1.3, 0.6)	(3.00, 1.3, 0.6)	(3.00, 1.3, 0.6)	(3.00, 1.3, 0.6)	(3.00, 1.3, 0.6)	(3.00, 1.3, 0.6)	(3.00, 1.3, 0.6)
	2.0	(3.00, 1.6, 1.1)	(3.01, 1.6, 1.0)	(3.03, 1.6, 0.9)	(3.07, 1.6, 1.0)	(3.11, 1.6, 1.0)	(3.15, 1.6, 1.0)	(3.00, 1.6, 0.9)

Table 21: $(K, \text{ARL}_1, \text{SDRL}_1)$ for the hypergeometric np chart and $(K'', \text{ARL}_1, \text{SDRL}_1)$ for the binomial np chart with $N = 500$, $n \in \{25, 50\}$, $p_0 \in \{0.01, 0.05, 0.10, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	-	-	-	-	-	-	-
	1.2	(3.00, 321.4, 8294.7) (3.34, 429.7, 6442.3)	(3.00, 145.3, 529.2) (3.34, 157.1, 593.8)	(3.00, 89.1, 235.2) (3.13, 104.2, 204.9)	(3.00, 62.0, 174.4) (3.10, 65.6, 149.8)	(3.00, 38.2, 87.4) (3.04, 39.4, 87.8)	(3.00, 31.5, 30.9) (3.23, 31.6, 54.8)	(3.00, 31.5, 30.9) (3.00, 27.8, 27.3)
	1.5	(3.00, 162.5, 2178.2) (3.34, 245.9, 2871.9)	(3.00, 88.3, 262.8) (3.34, 101.6, 329.9)	(3.00, 56.7, 138.5) (3.13, 70.0, 132.7)	(3.00, 40.9, 103.1) (3.10, 45.3, 97.3)	(3.00, 27.1, 53.0) (3.04, 28.5, 57.6)	(3.00, 23.2, 22.6) (3.23, 23.5, 36.9)	(3.00, 23.2, 22.6) (3.00, 21.1, 20.5)
	2.0	(3.00, 44.1, 248.4) (3.34, 73.5, 489.5)	(3.00, 31.4, 67.9) (3.34, 38.9, 92.3)	(3.00, 22.1, 44.4) (3.13, 28.9, 49.6)	(3.00, 17.3, 33.6) (3.10, 20.0, 36.7)	(3.00, 13.1, 18.8) (3.04, 14.0, 22.6)	(3.00, 11.9, 11.3) (3.23, 12.2, 15.6)	(3.00, 11.9, 11.3) (3.00, 11.3, 10.8)
0.05	1.1	(3.00, 315.5, 2175.2) (3.08, 318.6, 2008.2)	(3.00, 196.5, 505.5) (3.04, 207.3, 490.8)	(3.00, 149.0, 256.3) (3.06, 153.0, 263.9)	(3.00, 129.2, 155.8) (3.10, 131.7, 207.6)	(3.00, 126.9, 128.0) (3.19, 131.3, 205.4)	(3.00, 127.1, 126.6) (3.32, 125.0, 188.5)	(3.00, 127.1, 126.6) (3.00, 101.7, 101.1)
	1.2	(3.00, 172.2, 928.0) (3.08, 182.2, 928.8)	(3.00, 115.2, 265.3) (3.04, 125.3, 272.3)	(3.00, 91.1, 145.0) (3.06, 95.6, 156.0)	(3.00, 80.8, 93.5) (3.10, 83.6, 124.2)	(3.00, 79.8, 80.0) (3.19, 83.4, 122.9)	(3.00, 80.0, 79.4) (3.32, 79.8, 113.4)	(3.00, 80.0, 79.4) (3.00, 66.5, 65.9)
	1.5	(3.00, 56.9, 198.7) (3.08, 63.9, 220.3)	(3.00, 42.7, 80.5) (3.04, 48.3, 89.1)	(3.00, 36.3, 50.2) (3.06, 39.2, 57.1)	(3.00, 33.5, 36.2) (3.10, 35.4, 46.7)	(3.00, 33.3, 33.0) (3.19, 35.3, 46.3)	(3.00, 33.4, 32.8) (3.32, 34.1, 43.3)	(3.00, 33.4, 32.8) (3.00, 29.6, 29.0)
	2.0	(3.00, 14.5, 30.3) (3.08, 16.7, 35.7)	(3.00, 12.3, 17.8) (3.04, 14.1, 20.7)	(3.00, 11.3, 13.0) (3.06, 12.3, 15.2)	(3.00, 10.8, 10.7) (3.10, 11.5, 13.0)	(3.00, 10.8, 10.3) (3.19, 11.5, 13.0)	(3.00, 10.8, 10.3) (3.32, 11.3, 12.3)	(3.00, 10.8, 10.3) (3.00, 10.3, 9.7)
0.10	1.1	(3.00, 324.0, 1367.3) (3.07, 315.4, 1357.0)	(3.00, 209.2, 462.2) (3.07, 221.5, 455.4)	(3.00, 164.4, 241.7) (3.04, 168.7, 237.6)	(3.00, 154.3, 221.6) (3.02, 160.0, 203.9)	(3.00, 141.2, 206.6) (2.99, 147.9, 193.9)	(3.00, 98.0, 138.5) (2.95, 97.1, 137.7)	(3.00, 75.8, 75.3) (2.99, 64.1, 63.5)
	1.2	(3.00, 171.5, 612.8) (3.07, 172.9, 632.5)	(3.00, 117.4, 236.8) (3.07, 127.6, 241.8)	(3.00, 95.3, 134.4) (3.04, 100.2, 135.7)	(3.00, 89.9, 124.5) (3.02, 95.6, 119.2)	(3.00, 82.8, 116.3) (2.99, 88.8, 113.5)	(3.00, 59.4, 79.5) (2.95, 60.0, 81.4)	(3.00, 47.4, 46.8) (2.99, 41.3, 40.7)
	1.5	(3.00, 38.7, 93.9) (3.07, 41.4, 102.9)	(3.00, 30.1, 48.7) (3.07, 34.1, 53.0)	(3.00, 26.3, 33.2) (3.04, 28.8, 35.2)	(3.00, 25.1, 31.3) (3.02, 27.8, 32.4)	(3.00, 23.5, 29.5) (2.99, 26.1, 31.0)	(3.00, 18.3, 21.4) (2.95, 19.0, 23.0)	(3.00, 15.6, 15.0) (2.99, 14.4, 13.9)
	2.0	(3.00, 8.0, 12.4) (3.07, 8.7, 13.9)	(3.00, 7.0, 8.5) (3.07, 8.0, 9.7)	(3.00, 6.5, 6.9) (3.04, 7.2, 7.6)	(3.00, 6.3, 6.7) (3.02, 7.1, 7.3)	(3.00, 6.1, 6.3) (2.99, 6.8, 7.0)	(3.00, 5.2, 5.0) (2.95, 5.5, 5.5)	(3.00, 4.7, 4.1) (2.99, 4.6, 4.0)
0.20	1.1	(3.00, 265.7, 553.9) (2.99, 264.1, 616.6)	(3.00, 224.0, 412.4) (3.01, 234.6, 439.8)	(3.00, 189.0, 264.7) (3.02, 195.7, 264.3)	(3.00, 175.7, 238.4) (3.02, 183.0, 227.7)	(3.00, 159.2, 217.5) (2.98, 166.3, 212.6)	(3.00, 114.6, 137.8) (2.96, 122.1, 161.2)	(3.00, 102.1, 101.5) (2.99, 85.9, 85.3)
	1.2	(3.00, 123.6, 244.9) (2.99, 123.8, 263.1)	(3.00, 102.5, 173.6) (3.01, 109.6, 188.3)	(3.00, 88.8, 118.2) (3.02, 94.2, 121.5)	(3.00, 83.2, 107.9) (3.00, 88.8, 107.4)	(3.00, 76.1, 98.9) (2.98, 81.3, 100.5)	(3.00, 57.0, 65.5) (2.96, 61.4, 77.3)	(3.00, 51.6, 51.1) (2.99, 45.1, 44.6)
	1.5	(3.00, 20.0, 38.0) (2.99, 20.8, 39.2)	(3.00, 17.1, 23.3) (3.01, 18.8, 25.9)	(3.00, 15.7, 18.2) (3.02, 17.3, 19.7)	(3.00, 15.0, 17.1) (3.00, 16.6, 18.3)	(3.00, 14.1, 15.9) (2.98, 15.5, 17.3)	(3.00, 11.6, 11.9) (2.96, 12.6, 13.9)	(3.00, 10.9, 10.3) (2.99, 10.3, 9.7)
	2.0	(3.00, 3.2, 3.5) (2.99, 3.4, 3.8)	(3.00, 3.0, 2.8) (3.01, 3.3, 3.2)	(3.00, 2.9, 2.5) (3.02, 3.2, 2.8)	(3.00, 2.9, 2.4) (3.00, 3.1, 2.7)	(3.00, 2.8, 2.3) (2.98, 3.0, 2.6)	(3.00, 2.5, 2.0) (2.96, 2.7, 2.2)	(3.00, 2.5, 1.9) (2.99, 2.5, 1.8)
$n = 50$								
0.01	1.1	-	-	-	-	-	-	-
	1.2	(3.00, 443.5, 7915.9) (3.61, 731.5, 8098.9)	(3.00, 163.9, 673.4) (3.44, 197.2, 620.4)	(3.00, 95.3, 243.8) (3.26, 111.0, 205.2)	(3.00, 70.1, 111.2) (3.16, 77.2, 147.9)	(3.00, 66.0, 67.0) (3.25, 70.0, 132.7)	(3.00, 65.9, 65.3) (3.41, 69.1, 130.6)	(3.00, 65.9, 65.3) (3.00, 44.9, 44.4)
	1.5	(3.00, 174.9, 1841.4) (3.61, 362.9, 2907.7)	(3.00, 82.8, 248.2) (3.44, 113.2, 307.1)	(3.00, 53.3, 114.4) (3.26, 67.6, 118.1)	(3.00, 42.3, 57.3) (3.16, 48.6, 86.2)	(3.00, 40.5, 40.5) (3.25, 44.5, 77.6)	(3.00, 40.5, 39.9) (3.41, 44.0, 76.4)	(3.00, 40.5, 39.9) (3.00, 30.3, 29.8)
	2.0	(3.00, 33.7, 117.0) (3.61, 80.1, 337.1)	(3.00, 22.2, 43.0) (3.44, 34.0, 67.7)	(3.00, 17.0, 25.7) (3.26, 23.0, 34.8)	(3.00, 15.0, 16.3) (3.16, 17.8, 26.2)	(3.00, 14.7, 14.2) (3.25, 16.7, 23.9)	(3.00, 14.7, 14.1) (3.41, 16.6, 23.6)	(3.00, 14.7, 14.1) (3.00, 12.8, 12.2)
0.05	1.1	(3.00, 360.9, 1888.0) (3.13, 390.3, 1748.9)	(3.00, 230.3, 528.1) (3.11, 246.2, 520.9)	(3.00, 190.1, 278.3) (3.15, 202.8, 293.7)	(3.00, 175.4, 250.3) (3.14, 186.2, 216.6)	(3.00, 158.7, 231.9) (3.03, 167.7, 185.7)	(3.00, 108.7, 155.8) (2.91, 117.6, 152.5)	(3.00, 82.4, 81.9) (2.91, 57.7, 57.1)
	1.2	(3.00, 159.5, 617.7) (3.13, 186.8, 689.2)	(3.00, 110.6, 221.9) (3.11, 126.7, 242.2)	(3.00, 95.0, 131.7) (3.15, 107.9, 147.6)	(3.00, 88.4, 120.4) (3.14, 100.6, 113.8)	(3.00, 80.7, 111.9) (3.03, 91.4, 100.0)	(3.00, 57.8, 77.0) (2.91, 65.6, 82.3)	(3.00, 45.7, 45.1) (2.91, 34.6, 34.1)
	1.5	(3.00, 37.9, 91.7) (3.13, 48.5, 124.8)	(3.00, 30.0, 47.6) (3.11, 37.2, 58.8)	(3.00, 27.3, 34.1) (3.15, 33.6, 41.2)	(3.00, 25.9, 31.9) (3.14, 32.1, 34.4)	(3.00, 24.1, 29.8) (3.03, 29.6, 31.4)	(3.00, 18.6, 21.8) (2.91, 22.3, 26.0)	(3.00, 15.8, 15.2) (2.91, 13.6, 13.0)
	2.0	(3.00, 7.4, 10.9) (3.13, 9.6, 15.6)	(3.00, 6.6, 7.8) (3.11, 8.4, 10.2)	(3.00, 6.4, 6.7) (3.15, 8.0, 8.4)	(3.00, 6.2, 6.4) (3.14, 7.9, 7.7)	(3.00, 5.9, 6.0) (3.03, 7.4, 7.2)	(3.00, 5.0, 4.8) (2.91, 6.0, 6.1)	(3.00, 4.6, 4.0) (2.91, 4.4, 3.8)
0.10	1.1	(3.00, 270.2, 664.4) (3.05, 298.6, 936.4)	(3.00, 202.0, 379.4) (3.08, 224.1, 420.1)	(3.00, 165.4, 222.8) (3.08, 178.5, 242.9)	(3.00, 159.6, 193.6) (3.11, 172.3, 213.9)	(3.00, 163.4, 194.5) (3.16, 173.0, 209.6)	(3.00, 178.2, 204.4) (3.25, 189.0, 236.8)	(3.00, 228.1, 227.5) (3.00, 144.1, 143.5)
	1.2	(3.00, 118.0, 258.0) (3.05, 135.8, 368.0)	(3.00, 92.2, 156.3) (3.08, 107.6, 184.2)	(3.00, 78.4, 100.1) (3.08, 88.8, 115.0)	(3.00, 76.2, 89.7) (3.11, 86.4, 103.0)	(3.00, 77.9, 90.3) (3.16, 86.8, 101.3)	(3.00, 84.4, 94.8) (3.25, 94.0, 113.1)	(3.00, 106.3, 105.7) (3.00, 74.0, 73.4)
	1.5	(3.00, 18.8, 32.8) (3.05, 22.7, 43.0)	(3.00, 16.2, 21.5) (3.08, 20.1, 27.5)	(3.00, 14.8, 16.5) (3.08, 17.9, 20.4)	(3.00, 14.6, 15.6) (3.11, 17.7, 19.0)	(3.00, 14.8, 15.8) (3.16, 17.8, 18.8)	(3.00, 15.8, 16.5) (3.25, 18.8, 20.4)	(3.00, 18.9, 18.4) (3.00, 16.0, 15.4)
	2.0	(3.00, 3.4, 3.6) (3.05, 4.0, 4.7)	(3.00, 3.2, 3.0) (3.08, 3.9, 3.9)	(3.00, 3.1, 2.7) (3.08, 3.7, 3.3)	(3.00, 3.1, 2.6) (3.11, 3.7, 3.2)	(3.00, 3.1, 2.6) (3.16, 3.7, 3.2)	(3.00, 3.2, 2.7) (3.25, 3.8, 3.4)	(3.00, 3.6, 3.0) (3.00, 3.5, 2.9)
0.20	1.1	(3.00, 181.1, 275.9) (2.99, 181.5, 299.7)	(3.00, 165.2, 238.4) (2.99, 159.2, 231.9)	(3.00, 149.3, 184.8) (2.99, 144.2, 178.5)	(3.00, 145.2, 166.8) (3.01, 142.1, 163.6)	(3.00, 147.3, 166.4) (3.05, 145.4, 161.0)	(3.00, 161.9, 177.9) (3.15, 172.6, 202.7)	(3.00, 198.7, 198.1) (3.00, 131.7, 131.1)
	1.2	(3.00, 74.7, 133.0) (2.99, 78.0, 142.6)	(3.00, 62.5, 91.2) (2.99, 63.7, 93.9)	(3.00, 55.7, 66.7) (2.99, 56.8, 68.1)	(3.00, 54.2, 60.6) (3.01, 55.8, 62.0)	(3.00, 54.8, 60.3) (3.05, 57.0, 61.2)	(3.00, 59.1, 63.5) (3.15, 66.1, 74.8)	(3.00, 70.6, 70.0) (3.00, 52.4, 51.8)
	1.5	(3.00, 7.7, 10.5) (2.99, 8.8, 12.7)	(3.00, 7.0, 7.9) (2.99, 7.8, 9.0)	(3.00, 6.7, 6.7) (2.99, 7.4, 7.5)	(3.00, 6.6, 6.4) (3.01, 7.4, 7.2)	(3.00, 6.6, 6.4) (3.05, 7.5, 7.2)	(3.00, 7.0, 6.7) (3.15, 8.2, 8.1)	(3.00, 7.8, 7.3) (3.00, 7.2, 6.6)
	2.0	(3.00, 1.5, 0.9) (2.99, 1.6, 1.1)	(3.00, 1.5, 0.8) (2.99, 1.6, 1.0)	(3.00, 1.5, 0.8) (2.99, 1.6, 0.9)	(3.00, 1.5, 0.8) (3.01, 1.6, 0.9)	(3.00, 1.5, 0.8) (3.05, 1.6, 0.9)	(3.00, 1.5, 0.8) (3.15, 1.6, 1.0)	(3.00, 1.5, 0.8) (3.00, 1.6, 0.9)

Table 22: $(K, \text{ARL}_1, \text{SDRL}_1)$ for the hypergeometric np chart and $(K'', \text{ARL}_1, \text{SDRL}_1)$ for the binomial np chart with $N = 1000$, $n \in \{25, 50\}$, $p_0 \in \{0.01, 0.05, 0.10, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	(3.00, 292.2, 5510.3)	(3.00, 160.5, 712.8)	(3.00, 93.7, 238.4)	(3.00, 66.4, 178.3)	(3.00, 44.9, 105.5)	(3.00, 34.8, 34.3)	(3.00, 34.8, 34.3)
		(3.13, 311.6, 3615.9)	(3.13, 181.0, 506.7)	(3.00, 101.8, 225.0)	(3.00, 68.1, 166.0)	(3.00, 43.8, 98.2)	(3.19, 34.7, 51.7)	(3.00, 32.6, 32.1)
	1.2	(3.00, 210.6, 3061.0)	(3.00, 123.0, 494.0)	(3.00, 74.0, 181.5)	(3.00, 53.4, 136.0)	(3.00, 37.1, 81.1)	(3.00, 29.5, 28.9)	(3.00, 29.5, 28.9)
		(3.13, 235.0, 2365.4)	(3.13, 142.3, 373.9)	(3.00, 81.5, 175.8)	(3.00, 55.4, 129.9)	(3.00, 36.5, 77.4)	(3.19, 29.5, 41.8)	(3.00, 27.8, 27.3)
1.5		(3.00, 96.2, 809.8)	(3.00, 64.2, 203.4)	(3.00, 41.5, 91.9)	(3.00, 31.3, 69.3)	(3.00, 23.2, 42.4)	(3.00, 19.4, 18.9)	(3.00, 19.4, 18.9)
		(3.13, 117.0, 822.0)	(3.13, 77.7, 176.0)	(3.00, 46.8, 94.0)	(3.00, 33.1, 69.8)	(3.00, 23.2, 42.5)	(3.19, 19.5, 24.7)	(3.00, 18.7, 18.1)
2.0		(3.00, 38.9, 192.8)	(3.00, 29.6, 71.9)	(3.00, 20.7, 39.7)	(3.00, 16.5, 30.4)	(3.00, 13.2, 19.5)	(3.00, 11.6, 11.0)	(3.00, 11.6, 11.0)
		(3.13, 50.3, 225.7)	(3.13, 36.8, 70.5)	(3.00, 23.7, 42.7)	(3.00, 17.7, 32.1)	(3.00, 13.3, 20.3)	(3.19, 11.7, 13.1)	(3.00, 11.3, 10.8)
0.05	1.1	(3.00, 321.5, 1502.6)	(3.00, 186.1, 445.0)	(3.00, 127.3, 215.8)	(3.00, 109.0, 136.3)	(3.00, 104.9, 106.7)	(3.00, 104.6, 104.1)	(3.00, 104.6, 104.1)
		(3.10, 345.1, 1861.0)	(3.04, 189.7, 442.4)	(3.02, 131.2, 220.9)	(3.05, 109.7, 157.5)	(3.13, 104.8, 138.9)	(3.30, 106.5, 144.5)	(3.00, 94.4, 93.8)
	1.2	(3.00, 198.5, 807.9)	(3.00, 121.5, 268.3)	(3.00, 86.2, 138.0)	(3.00, 75.2, 90.5)	(3.00, 72.8, 73.6)	(3.00, 72.6, 72.1)	(3.00, 72.6, 72.1)
		(3.10, 215.0, 999.2)	(3.04, 125.3, 272.3)	(3.02, 89.5, 143.6)	(3.05, 76.1, 104.2)	(3.13, 73.1, 92.8)	(3.30, 74.1, 96.3)	(3.00, 66.5, 65.9)
1.5		(3.00, 62.2, 183.9)	(3.00, 43.4, 79.0)	(3.00, 33.5, 46.6)	(3.00, 30.4, 33.7)	(3.00, 29.8, 29.6)	(3.00, 29.8, 29.2)	(3.00, 29.8, 29.2)
		(3.10, 68.2, 224.1)	(3.04, 45.6, 83.2)	(3.02, 35.2, 49.8)	(3.05, 31.1, 38.1)	(3.13, 30.2, 34.8)	(3.30, 30.6, 35.8)	(3.00, 28.1, 27.6)
2.0		(3.00, 16.7, 34.2)	(3.00, 13.3, 19.2)	(3.00, 11.2, 13.2)	(3.00, 10.6, 10.7)	(3.00, 10.5, 10.0)	(3.00, 10.5, 10.0)	(3.00, 10.5, 10.0)
		(3.10, 18.3, 40.4)	(3.04, 14.1, 20.7)	(3.02, 11.9, 14.3)	(3.05, 11.0, 11.8)	(3.13, 10.8, 11.1)	(3.30, 10.8, 11.3)	(3.00, 10.3, 9.7)
0.10	1.1	(3.00, 283.3, 1260.7)	(3.00, 197.2, 407.6)	(3.00, 162.0, 230.6)	(3.00, 152.8, 209.2)	(3.00, 147.1, 203.6)	(3.00, 122.5, 176.4)	(3.00, 69.5, 69.0)
		(2.99, 295.8, 1164.6)	(3.01, 196.0, 398.4)	(3.03, 167.2, 230.8)	(3.01, 155.2, 200.2)	(2.99, 147.9, 193.9)	(2.98, 128.9, 176.8)	(2.99, 64.1, 63.5)
	1.2	(3.00, 154.1, 573.5)	(3.00, 113.1, 214.4)	(3.00, 95.3, 130.6)	(3.00, 90.3, 120.0)	(3.00, 87.2, 116.9)	(3.00, 73.5, 101.7)	(3.00, 44.1, 43.5)
		(2.99, 162.3, 557.0)	(3.01, 113.9, 213.5)	(3.03, 99.5, 132.4)	(3.01, 92.9, 117.1)	(2.99, 88.8, 113.5)	(2.98, 78.0, 103.6)	(2.99, 41.3, 40.7)
1.5		(3.00, 36.8, 90.1)	(3.00, 30.2, 46.5)	(3.00, 27.0, 33.4)	(3.00, 25.8, 31.5)	(3.00, 25.1, 30.7)	(3.00, 21.9, 27.1)	(3.00, 15.0, 14.4)
		(2.99, 39.1, 95.7)	(3.01, 31.1, 47.9)	(3.03, 28.6, 34.7)	(3.01, 27.1, 31.9)	(2.99, 26.1, 31.0)	(2.98, 23.5, 28.5)	(2.99, 14.4, 13.9)
2.0		(3.00, 7.9, 12.2)	(3.00, 7.2, 8.6)	(3.00, 6.8, 7.1)	(3.00, 6.6, 6.9)	(3.00, 6.5, 6.7)	(3.00, 5.9, 6.1)	(3.00, 4.6, 4.1)
		(2.99, 8.3, 13.4)	(3.01, 7.5, 9.0)	(3.03, 7.2, 7.5)	(3.01, 7.0, 7.2)	(2.99, 6.8, 7.0)	(2.98, 6.3, 6.5)	(2.99, 4.6, 4.0)
0.20	1.1	(3.00, 299.3, 722.6)	(3.00, 219.5, 406.3)	(3.00, 189.2, 259.7)	(3.00, 178.0, 232.9)	(3.00, 170.1, 224.5)	(3.00, 138.9, 186.7)	(3.00, 93.4, 92.8)
		(3.01, 312.7, 734.3)	(3.00, 224.5, 411.9)	(3.02, 195.7, 264.3)	(3.00, 183.0, 227.7)	(2.99, 174.3, 219.7)	(2.97, 134.6, 178.4)	(2.99, 85.9, 85.3)
	1.2	(3.00, 136.5, 297.7)	(3.00, 102.0, 173.4)	(3.00, 90.1, 118.0)	(3.00, 85.4, 107.6)	(3.00, 81.9, 103.9)	(3.00, 68.2, 87.2)	(3.00, 48.2, 47.6)
		(3.01, 142.7, 304.0)	(3.00, 105.5, 177.3)	(3.02, 94.2, 121.5)	(3.00, 88.8, 107.4)	(2.99, 84.9, 103.8)	(2.97, 67.0, 85.0)	(2.99, 45.1, 44.6)
1.5		(3.00, 21.7, 41.6)	(3.00, 17.4, 24.0)	(3.00, 16.3, 18.7)	(3.00, 15.7, 17.7)	(3.00, 15.2, 17.1)	(3.00, 13.3, 14.8)	(3.00, 10.6, 10.0)
		(3.01, 22.8, 42.5)	(3.00, 18.4, 24.8)	(3.02, 17.3, 19.7)	(3.00, 16.6, 18.3)	(2.99, 16.0, 17.7)	(2.97, 13.4, 15.0)	(2.99, 10.3, 9.7)
2.0		(3.00, 3.4, 3.8)	(3.00, 3.1, 2.9)	(3.00, 3.0, 2.6)	(3.00, 3.0, 2.6)	(3.00, 2.9, 2.5)	(3.00, 2.8, 2.3)	(3.00, 2.5, 1.9)
		(3.01, 3.6, 4.0)	(3.00, 3.3, 3.1)	(3.02, 3.2, 2.8)	(3.00, 3.1, 2.7)	(2.99, 3.1, 2.6)	(2.97, 2.8, 2.3)	(2.99, 2.5, 1.8)
$n = 50$								
0.01	1.1	(3.00, 339.5, 5033.5)	(3.00, 154.6, 603.3)	(3.00, 108.4, 249.7)	(3.00, 77.5, 133.0)	(3.00, 69.2, 75.7)	(3.00, 68.5, 67.9)	(3.00, 68.5, 67.9)
		(3.25, 358.4, 3397.2)	(3.11, 143.9, 451.3)	(3.09, 107.9, 217.9)	(3.06, 77.5, 146.6)	(3.15, 69.6, 121.2)	(3.36, 68.9, 118.6)	(3.00, 56.3, 55.8)
	1.2	(3.00, 223.4, 2472.7)	(3.00, 110.5, 381.4)	(3.00, 80.3, 173.4)	(3.00, 59.4, 94.6)	(3.00, 53.7, 57.5)	(3.00, 53.2, 52.7)	(3.00, 53.2, 52.7)
		(3.25, 251.7, 2003.8)	(3.11, 107.1, 310.8)	(3.09, 82.1, 159.5)	(3.06, 60.2, 108.1)	(3.15, 54.5, 90.0)	(3.36, 54.0, 88.1)	(3.00, 44.9, 44.4)
1.5		(3.00, 84.2, 516.5)	(3.00, 49.7, 129.7)	(3.00, 39.0, 71.4)	(3.00, 31.0, 42.0)	(3.00, 28.8, 29.5)	(3.00, 28.6, 28.1)	(3.00, 28.6, 28.1)
		(3.25, 105.6, 553.4)	(3.11, 51.6, 123.8)	(3.09, 41.8, 72.9)	(3.06, 32.2, 50.7)	(3.15, 29.7, 43.0)	(3.36, 29.5, 42.2)	(3.00, 25.5, 25.0)
2.0		(3.00, 28.3, 98.2)	(3.00, 19.8, 38.4)	(3.00, 16.8, 25.1)	(3.00, 14.4, 16.6)	(3.00, 13.7, 13.4)	(3.00, 13.6, 13.1)	(3.00, 13.6, 13.1)
		(3.25, 37.6, 123.1)	(3.11, 21.5, 41.1)	(3.09, 18.5, 27.9)	(3.06, 15.2, 20.3)	(3.15, 14.3, 17.7)	(3.36, 14.2, 17.5)	(3.00, 12.8, 12.2)
0.05	1.1	(3.00, 286.3, 1194.6)	(3.00, 195.0, 406.4)	(3.00, 150.8, 210.3)	(3.00, 146.2, 187.6)	(3.00, 145.6, 186.3)	(3.00, 150.5, 190.0)	(3.00, 227.2, 226.6)
		(3.05, 300.5, 1201.0)	(3.09, 208.1, 426.1)	(3.07, 158.5, 221.8)	(3.06, 150.2, 172.6)	(3.03, 150.6, 166.4)	(2.98, 157.7, 169.5)	(3.00, 176.9, 176.4)
	1.2	(3.00, 154.0, 531.0)	(3.00, 110.7, 211.0)	(3.00, 88.7, 118.6)	(3.00, 86.3, 108.0)	(3.00, 86.0, 107.4)	(3.00, 88.7, 109.5)	(3.00, 131.4, 130.8)
		(3.05, 165.7, 570.8)	(3.09, 120.8, 228.6)	(3.07, 95.2, 127.5)	(3.06, 91.1, 102.9)	(3.03, 91.4, 100.0)	(2.98, 95.5, 101.9)	(3.00, 106.7, 106.1)
1.5		(3.00, 36.5, 82.9)	(3.00, 29.5, 45.4)	(3.00, 25.4, 30.7)	(3.00, 25.0, 29.0)	(3.00, 24.9, 28.9)	(3.00, 25.6, 29.5)	(3.00, 35.8, 35.2)
		(3.05, 40.7, 98.1)	(3.09, 33.2, 51.8)	(3.07, 28.3, 34.0)	(3.06, 27.6, 29.7)	(3.03, 27.7, 29.3)	(2.98, 28.8, 29.8)	(3.00, 31.7, 31.1)
2.0		(3.00, 8.1, 11.9)	(3.00, 7.2, 8.6)	(3.00, 6.7, 6.9)	(3.00, 6.6, 6.7)	(3.00, 6.6, 6.7)	(3.00, 6.7, 6.8)	(3.00, 8.6, 8.1)
		(3.05, 9.0, 14.2)	(3.09, 8.1, 10.0)	(3.07, 7.5, 7.7)	(3.06, 7.4, 7.2)	(3.03, 7.4, 7.2)	(2.98, 7.6, 7.3)	(3.00, 8.2, 7.7)
0.10	1.1	(3.00, 274.3, 812.1)	(3.00, 189.1, 356.2)	(3.00, 156.3, 210.4)	(3.00, 151.5, 173.4)	(3.00, 157.6, 169.3)	(3.00, 176.0, 177.0)	(3.00, 178.5, 177.9)
		(3.04, 279.8, 900.5)	(3.04, 192.9, 358.6)	(3.04, 163.0, 219.1)	(3.06, 154.9, 185.3)	(3.13, 161.6, 187.5)	(3.24, 177.2, 217.1)	(3.00, 144.1, 143.5)
	1.2	(3.00, 122.2, 313.7)	(3.00, 89.7, 152.7)	(3.00, 76.7, 97.9)	(3.00, 75.1, 83.9)	(3.00, 78.0, 82.8)	(3.00, 86.5, 86.6)	(3.00, 87.6, 87.1)
		(3.04, 128.1, 353.0)	(3.04, 94.0, 158.9)	(3.04, 81.8, 104.7)	(3.06, 78.5, 90.6)	(3.13, 81.8, 91.8)	(3.24, 88.7, 104.5)	(3.00, 74.0, 73.4)
1.5		(3.00, 20.0, 36.9)	(3.00, 16.7, 22.3)	(3.00, 15.3, 17.1)	(3.00, 15.3, 15.8)	(3.00, 15.8, 15.9)	(3.00, 17.1, 16.7)	(3.00, 17.3, 16.7)
		(3.04, 21.8, 41.3)	(3.04, 18.2, 24.5)	(3.04, 16.8, 19.0)	(3.06, 16.5, 17.3)	(3.13, 17.1, 17.6)	(3.24, 18.1, 19.3)	(3.00, 16.0, 15.4)
2.0		(3.00, 3.6, 4.0)	(3.00, 3.4, 3.2)	(3.00, 3.3, 2.9)	(3.00, 3.3, 2.8)	(3.00, 3.4, 2.8)	(3.00, 3.5, 2.9)	(3.00, 3.6, 3.0)
		(3.04, 3.9, 4.5)	(3.04, 3.7, 3.6)	(3.04, 3.6, 3.2)	(3.06, 3.6, 3.1)	(3.13, 3.6, 3.1)	(3.24, 3.7, 3.3)	(3.00, 3.5, 2.9)
0.20	1.1	(3.00, 187.6, 303.5)	(3.00, 165.1, 241.2)	(3.00, 147.8, 181.2)	(3.00, 143.0, 158.9)	(3.00, 147.0, 153.9)	(3.00, 159.0, 158.9)	(3.00, 159.8, 159.2)
		(2.99, 181.5, 299.7)	(2.99, 159.2, 231.9)	(2.99, 144.2, 178.5)	(3.02, 146.4, 170.1)	(3.07, 152.7, 173.4)	(3.15, 172.6, 202.7)	(3.00, 131.7, 131.1)
	1.2	(3.00, 78.0, 139.0)	(3.00, 64.3, 94.5)	(3.00, 56.9, 68.3)	(3.00, 54.8, 59.8)	(3.00, 56.0, 57.8)	(3.00, 60.0, 59.6)	(3.00, 60.3, 59.7)
		(2.99, 78.0, 142.6)	(2.99, 63.7, 93.9)	(2.99, 56.8, 68.1)	(3.02, 57.2, 64.0)	(3.07, 59.4, 65.2)	(3.15, 66.1, 74.8)	(3.00, 52.4, 51.8)
1.5		(3.00, 8.4, 11.6)	(3.00, 7.5, 8.5)	(3.00, 7.1, 7.1)	(3.00, 7.0, 6.7)	(3.00, 7.1, 6.7)	(3.00, 7.5, 6.9)	(3.00, 7.5, 6.9)
		(2.99, 8.8, 12.7)	(2.99, 7.8, 9.0)	(2.99, 7.4, 7.5)	(3.02, 7.5, 7.3)	(3.07, 7.7, 7.5)	(3.15, 8.2, 8.1)	(3.00, 7.2, 6.6)
2.0		(3.00, 1.6, 1.0)	(3.00, 1.5, 0.9)	(3.00, 1.5, 0.8)	(3.00, 1.5, 0.8)	(3.00, 1.5, 0.8)	(3.00, 1.5, 0.9)	(3.00, 1.5, 0.9)
		(2.99, 1.6, 1.1)	(2.99, 1.6, 1.0)	(2.99, 1.6, 0.9)	(3.02, 1.6, 0.9)	(3.07, 1.6, 0.9)	(3.15, 1.6, 1.0)	(3.00, 1.6, 0.9)

Table 23: $(K, \text{ARL}_1, \text{SDRL}_1)$ for the hypergeometric np chart and $(K'', \text{ARL}_1, \text{SDRL}_1)$ for the binomial np chart with $N = 2000$, $n \in \{25, 50\}$, $p_0 \in \{0.01, 0.05, 0.10, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	(3.00, 243.0, 3237.6)	(3.00, 142.4, 568.0)	(3.00, 85.6, 210.4)	(3.00, 61.8, 158.2)	(3.00, 42.7, 94.8)	(3.00, 33.7, 33.1)	(3.00, 33.7, 33.1)
		(3.10, 234.5, 3611.3)	(3.10, 128.2, 477.9)	(2.98, 79.0, 188.0)	(2.98, 57.9, 142.0)	(3.00, 43.8, 98.2)	(3.16, 33.7, 42.8)	(3.00, 32.6, 32.1)
	1.2	(3.00, 180.3, 1996.8)	(3.00, 111.0, 406.9)	(3.00, 68.5, 162.5)	(3.00, 50.2, 122.4)	(3.00, 35.6, 73.9)	(3.00, 28.6, 28.1)	(3.00, 28.6, 28.1)
		(3.10, 175.1, 2361.6)	(3.10, 101.3, 349.9)	(2.98, 63.8, 147.0)	(2.98, 47.5, 111.3)	(3.00, 36.5, 77.4)	(3.16, 28.6, 35.1)	(3.00, 27.8, 27.3)
	1.5	(3.00, 87.1, 633.4)	(3.00, 59.9, 179.0)	(3.00, 39.4, 84.8)	(3.00, 30.0, 64.3)	(3.00, 22.6, 39.9)	(3.00, 19.0, 18.5)	(3.00, 19.0, 18.5)
		(3.10, 85.6, 818.8)	(3.10, 56.2, 161.2)	(2.98, 37.5, 78.8)	(2.98, 29.0, 60.1)	(3.00, 23.2, 42.5)	(3.16, 19.1, 21.6)	(3.00, 18.7, 18.1)
	2.0	(3.00, 36.8, 170.5)	(3.00, 28.4, 66.9)	(3.00, 20.2, 37.8)	(3.00, 16.2, 29.0)	(3.00, 13.0, 18.9)	(3.00, 11.5, 10.9)	(3.00, 11.5, 10.9)
		(3.10, 36.5, 223.1)	(3.10, 27.4, 62.8)	(2.98, 19.6, 36.0)	(2.98, 15.9, 27.8)	(3.00, 13.3, 20.3)	(3.16, 11.5, 12.0)	(3.00, 11.3, 10.8)
0.05	1.1	(3.00, 293.9, 1439.7)	(3.00, 173.1, 403.4)	(3.00, 121.6, 199.7)	(3.00, 105.3, 134.3)	(3.00, 99.8, 102.5)	(3.00, 99.3, 98.7)	(3.00, 99.3, 98.7)
		(3.08, 288.6, 1752.0)	(3.03, 166.9, 420.1)	(3.01, 121.7, 202.7)	(3.02, 106.7, 148.4)	(3.09, 100.0, 120.5)	(3.27, 98.6, 114.2)	(3.00, 94.4, 93.8)
	1.2	(3.00, 184.0, 775.3)	(3.00, 114.3, 247.0)	(3.00, 83.1, 129.3)	(3.00, 73.1, 89.7)	(3.00, 69.8, 71.0)	(3.00, 69.4, 68.9)	(3.00, 69.4, 68.9)
		(3.08, 182.2, 928.8)	(3.03, 111.0, 257.4)	(3.01, 83.5, 132.2)	(3.02, 74.2, 98.6)	(3.09, 70.1, 81.7)	(3.27, 69.2, 78.0)	(3.00, 66.5, 65.9)
	1.5	(3.00, 59.4, 177.4)	(3.00, 41.8, 75.0)	(3.00, 32.8, 44.8)	(3.00, 30.0, 33.7)	(3.00, 29.0, 28.9)	(3.00, 28.9, 28.4)	(3.00, 28.9, 28.4)
		(3.08, 59.9, 201.9)	(3.03, 41.1, 77.9)	(3.01, 33.2, 46.3)	(3.02, 30.5, 36.5)	(3.09, 29.3, 31.8)	(3.27, 29.0, 30.7)	(3.00, 28.1, 27.6)
	2.0	(3.00, 16.3, 33.4)	(3.00, 13.1, 18.8)	(3.00, 11.2, 13.0)	(3.00, 10.6, 10.8)	(3.00, 10.4, 9.9)	(3.00, 10.4, 9.8)	(3.00, 10.4, 9.8)
		(3.08, 16.7, 35.7)	(3.03, 13.0, 19.3)	(3.01, 11.4, 13.5)	(3.02, 10.8, 11.4)	(3.09, 10.5, 10.5)	(3.27, 10.5, 10.3)	(3.00, 10.3, 9.7)
0.10	1.1	(3.00, 297.2, 1165.8)	(3.00, 196.3, 412.4)	(3.00, 160.8, 225.5)	(3.00, 154.3, 204.9)	(3.00, 149.5, 200.5)	(3.00, 137.7, 189.6)	(3.00, 66.7, 66.1)
		(2.99, 295.8, 1164.6)	(3.01, 196.0, 398.4)	(3.02, 160.5, 226.7)	(3.01, 155.2, 200.2)	(2.99, 147.9, 193.9)	(2.99, 140.5, 187.7)	(2.99, 64.1, 63.5)
	1.2	(3.00, 162.5, 545.7)	(3.00, 113.1, 219.1)	(3.00, 95.3, 128.8)	(3.00, 91.8, 118.7)	(3.00, 89.1, 116.3)	(3.00, 82.5, 110.0)	(3.00, 42.6, 42.1)
		(2.99, 162.3, 557.0)	(3.01, 113.9, 213.5)	(3.02, 95.7, 129.9)	(3.01, 92.9, 117.1)	(2.99, 88.8, 113.5)	(2.99, 84.6, 109.9)	(2.99, 41.3, 40.7)
	1.5	(3.00, 38.9, 91.0)	(3.00, 30.4, 48.2)	(3.00, 27.3, 33.5)	(3.00, 26.5, 31.7)	(3.00, 25.9, 31.1)	(3.00, 24.3, 29.6)	(3.00, 14.7, 14.1)
		(2.99, 39.1, 95.7)	(3.01, 31.1, 47.9)	(3.02, 27.7, 34.0)	(3.01, 27.1, 31.9)	(2.99, 26.1, 31.0)	(2.99, 25.1, 30.1)	(2.99, 14.4, 13.9)
	2.0	(3.00, 8.3, 12.8)	(3.00, 7.3, 8.9)	(3.00, 6.9, 7.3)	(3.00, 6.8, 7.0)	(3.00, 6.7, 6.9)	(3.00, 6.4, 6.6)	(3.00, 4.6, 4.0)
		(2.99, 8.3, 13.4)	(3.01, 7.5, 9.0)	(3.02, 7.0, 7.4)	(3.01, 7.0, 7.2)	(2.99, 6.8, 7.0)	(2.99, 6.6, 6.8)	(2.99, 4.6, 4.0)
0.20	1.1	(3.00, 280.8, 666.6)	(3.00, 226.9, 417.7)	(3.00, 185.8, 253.1)	(3.00, 180.8, 230.8)	(3.00, 178.1, 227.8)	(3.00, 160.3, 210.6)	(3.00, 89.5, 88.9)
		(3.00, 287.7, 699.2)	(3.00, 224.5, 411.9)	(3.00, 188.0, 250.8)	(3.00, 183.0, 227.7)	(3.00, 182.3, 226.4)	(2.99, 165.0, 211.5)	(2.99, 85.9, 85.3)
	1.2	(3.00, 129.9, 279.6)	(3.00, 105.7, 179.0)	(3.00, 89.2, 116.1)	(3.00, 87.2, 107.7)	(3.00, 86.0, 106.5)	(3.00, 78.1, 98.7)	(3.00, 46.6, 46.0)
		(3.00, 132.4, 288.9)	(3.00, 105.5, 177.3)	(3.00, 90.8, 116.1)	(3.00, 88.8, 107.4)	(3.00, 88.5, 106.8)	(2.99, 80.7, 100.0)	(2.99, 45.1, 44.6)
	1.5	(3.00, 21.3, 40.3)	(3.00, 18.1, 24.8)	(3.00, 16.4, 18.7)	(3.00, 16.1, 18.0)	(3.00, 16.0, 17.8)	(3.00, 14.9, 16.7)	(3.00, 10.4, 9.9)
		(3.00, 21.6, 39.5)	(3.00, 18.4, 24.8)	(3.00, 16.8, 19.1)	(3.00, 16.6, 18.3)	(3.00, 16.5, 18.2)	(2.99, 15.4, 17.2)	(2.99, 10.3, 9.7)
	2.0	(3.00, 3.4, 3.8)	(3.00, 3.2, 3.0)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.6)	(3.00, 3.0, 2.6)	(3.00, 2.9, 2.5)	(3.00, 2.5, 1.9)
		(3.00, 3.5, 3.8)	(3.00, 3.3, 3.1)	(3.00, 3.2, 2.8)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(2.99, 3.0, 2.6)	(2.99, 2.5, 1.8)
$n = 50$								
0.01	1.1	(3.00, 251.8, 2402.5)	(3.00, 163.3, 463.8)	(3.00, 93.2, 198.5)	(3.00, 72.1, 123.6)	(3.00, 63.0, 71.7)	(3.00, 61.8, 61.2)	(3.00, 61.8, 61.2)
		(3.04, 270.6, 1960.9)	(3.12, 183.7, 477.3)	(3.04, 93.7, 189.6)	(3.04, 72.3, 130.9)	(3.09, 63.2, 95.4)	(3.33, 62.4, 91.9)	(3.00, 56.3, 55.8)
	1.2	(3.00, 174.6, 1381.5)	(3.00, 119.3, 314.0)	(3.00, 70.7, 142.3)	(3.00, 56.0, 90.1)	(3.00, 49.6, 54.9)	(3.00, 48.7, 48.1)	(3.00, 48.7, 48.1)
		(3.04, 190.7, 1209.1)	(3.12, 136.0, 330.9)	(3.04, 71.9, 139.0)	(3.04, 56.5, 96.9)	(3.09, 49.9, 71.7)	(3.33, 49.3, 69.2)	(3.00, 44.9, 44.4)
	1.5	(3.00, 72.5, 372.3)	(3.00, 55.3, 121.9)	(3.00, 36.0, 62.7)	(3.00, 30.0, 41.7)	(3.00, 27.3, 28.7)	(3.00, 27.0, 26.4)	(3.00, 27.0, 26.4)
		(3.04, 80.6, 374.5)	(3.12, 64.6, 134.0)	(3.04, 37.3, 64.0)	(3.04, 30.6, 46.0)	(3.09, 27.7, 35.5)	(3.33, 27.5, 34.5)	(3.00, 25.5, 25.0)
	2.0	(3.00, 26.2, 84.2)	(3.00, 22.3, 40.1)	(3.00, 16.1, 23.4)	(3.00, 14.2, 16.9)	(3.00, 13.3, 13.2)	(3.00, 13.2, 12.6)	(3.00, 13.2, 12.6)
		(3.04, 29.1, 95.1)	(3.12, 26.2, 45.3)	(3.04, 16.9, 24.8)	(3.04, 14.6, 18.7)	(3.09, 13.6, 15.3)	(3.33, 13.5, 15.0)	(3.00, 12.8, 12.2)
0.05	1.1	(3.00, 270.8, 1153.9)	(3.00, 172.8, 361.6)	(3.00, 141.5, 197.9)	(3.00, 141.0, 173.3)	(3.00, 147.3, 176.0)	(3.00, 166.6, 186.5)	(3.00, 199.5, 199.0)
		(3.04, 258.7, 1008.8)	(3.02, 171.8, 351.4)	(3.02, 142.8, 193.3)	(3.04, 144.5, 167.9)	(3.03, 150.6, 166.4)	(3.01, 168.8, 173.8)	(3.00, 176.9, 176.4)
	1.2	(3.00, 147.8, 534.0)	(3.00, 100.4, 191.8)	(3.00, 84.6, 113.4)	(3.00, 84.6, 101.9)	(3.00, 88.3, 103.7)	(3.00, 99.2, 109.9)	(3.00, 117.9, 117.4)
		(3.04, 144.6, 480.0)	(3.02, 101.1, 190.3)	(3.02, 86.5, 112.6)	(3.04, 87.8, 100.3)	(3.03, 91.4, 100.0)	(3.01, 102.0, 104.5)	(3.00, 106.7, 106.1)
	1.5	(3.00, 36.0, 87.9)	(3.00, 28.0, 43.1)	(3.00, 25.1, 30.3)	(3.00, 25.2, 28.6)	(3.00, 26.2, 29.1)	(3.00, 28.9, 30.8)	(3.00, 33.6, 33.1)
		(3.04, 36.7, 84.2)	(3.02, 28.8, 44.3)	(3.02, 26.2, 30.9)	(3.04, 26.7, 29.0)	(3.03, 27.7, 29.3)	(3.01, 30.5, 30.6)	(3.00, 31.7, 31.1)
	2.0	(3.00, 8.1, 12.6)	(3.00, 7.1, 8.4)	(3.00, 6.7, 7.0)	(3.00, 6.8, 6.8)	(3.00, 7.0, 6.9)	(3.00, 7.5, 7.3)	(3.00, 8.4, 7.9)
		(3.04, 8.4, 12.8)	(3.02, 7.4, 8.8)	(3.02, 7.1, 7.3)	(3.04, 7.2, 7.1)	(3.03, 7.4, 7.2)	(3.01, 8.0, 7.5)	(3.00, 8.2, 7.7)
0.10	1.1	(3.00, 256.0, 694.6)	(3.00, 183.0, 338.5)	(3.00, 151.8, 200.8)	(3.00, 145.2, 165.0)	(3.00, 149.2, 155.8)	(3.00, 159.5, 159.1)	(3.00, 159.8, 159.2)
		(3.00, 254.4, 757.1)	(3.01, 185.7, 336.8)	(3.02, 152.9, 204.5)	(3.03, 147.4, 172.1)	(3.09, 151.6, 165.6)	(3.22, 160.0, 183.4)	(3.00, 144.1, 143.5)
	1.2	(3.00, 117.1, 279.3)	(3.00, 88.4, 148.5)	(3.00, 75.8, 95.4)	(3.00, 73.2, 81.1)	(3.00, 75.3, 77.9)	(3.00, 80.2, 79.7)	(3.00, 80.3, 79.8)
		(3.00, 117.8, 303.5)	(3.01, 90.8, 150.6)	(3.02, 77.2, 98.3)	(3.03, 75.1, 84.9)	(3.09, 77.3, 82.5)	(3.22, 81.1, 90.0)	(3.00, 74.0, 73.4)
	1.5	(3.00, 20.1, 35.5)	(3.00, 17.0, 22.6)	(3.00, 15.6, 17.3)	(3.00, 15.4, 15.8)	(3.00, 15.8, 15.6)	(3.00, 16.6, 16.0)	(3.00, 16.6, 16.0)
		(3.00, 20.6, 37.6)	(3.01, 17.7, 23.7)	(3.02, 16.1, 18.1)	(3.03, 16.0, 16.6)	(3.09, 16.4, 16.5)	(3.22, 17.0, 17.4)	(3.00, 16.0, 15.4)
	2.0	(3.00, 3.7, 4.1)	(3.00, 3.5, 3.3)	(3.00, 3.4, 2.9)	(3.00, 3.4, 2.8)	(3.00, 3.4, 2.9)	(3.00, 3.5, 2.9)	(3.00, 3.5, 2.9)
		(3.00, 3.8, 4.3)	(3.01, 3.6, 3.5)	(3.02, 3.5, 3.1)	(3.03, 3.5, 3.0)	(3.09, 3.6, 3.0)	(3.22, 3.6, 3.1)	(3.00, 3.5, 2.9)
0.20	1.1	(3.00, 187.1, 304.5)	(3.00, 162.5, 234.9)	(3.00, 147.3, 181.2)	(3.00, 140.6, 157.2)	(3.00, 140.5, 145.4)	(3.00, 144.6, 144.1)	(3.00, 144.6, 144.1)
		(2.99, 181.5, 299.7)	(2.98, 156.6, 224.2)	(2.99, 144.2, 178.5)	(3.01, 142.1, 163.6)	(3.05, 145.4, 161.0)	(3.13, 151.3, 170.6)	(3.00, 131.7, 131.1)
	1.2	(3.00, 78.6, 140.5)	(3.00, 64.3, 93.9)	(3.00, 57.4, 68.8)	(3.00, 54.7, 59.9)	(3.00, 54.6, 55.8)	(3.00, 56.1, 55.5)	(3.00, 56.1, 55.5)
		(2.99, 78.0, 142.6)	(2.98, 62.9, 90.5)	(2.99, 56.8, 68.1)	(3.01, 55.8, 62.0)	(3.05, 57.0, 61.2)	(3.13, 59.0, 64.3)	(3.00, 52.4, 51.8)
	1.5	(3.00, 8.6, 12.2)	(3.00, 7.7, 8.8)	(3.00, 7.3, 7.4)	(3.00, 7.1, 6.9)	(3.00, 7.2, 6.7)	(3.00, 7.3, 6.7)	(3.00, 7.3, 6.7)
		(2.99, 8.8, 12.7)	(2.98, 7.8, 8.8)	(2.99, 7.4, 7.5)	(3.01, 7.4, 7.2)	(3.05, 7.5, 7.2)	(3.13, 7.7, 7.4)	(3.00, 7.2, 6.6)
	2.0	(3.00, 1.6, 1.0)	(3.00, 1.6, 0.9)	(3.00, 1.5, 0.9)	(3.00, 1.5, 0.9)	(3.00, 1.5, 0.9)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)
		(2.99, 1.6, 1.1)	(2.98, 1.6, 1.0)	(2.99, 1.6, 0.9)	(3.01, 1.6, 0.9)	(3.05, 1.6, 0.9)	(3.13, 1.6, 0.9)	(3.00, 1.6, 0.9)

Table 24: $(K, ARL_1, SDRL_1)$ for the hypergeometric np chart and $(K'', ARL_1, SDRL_1)$ for the binomial np chart with $N = 5000, n \in \{25, 50\}, p_0 \in \{0.01, 0.05, 0.10, 0.20\}, m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	(3.00, 220.8, 2538.9)	(3.00, 133.5, 504.5)	(3.00, 105.4, 235.3)	(3.00, 70.1, 173.3)	(3.00, 44.6, 102.1)	(3.00, 33.0, 32.5)	(3.00, 33.0, 32.5)
		(3.00, 208.2, 2204.1)	(3.10, 128.2, 477.9)	(3.12, 101.8, 225.7)	(3.04, 68.1, 166.0)	(3.00, 43.8, 98.2)	(3.13, 33.1, 37.5)	(3.00, 32.6, 32.1)
	1.2	(3.00, 166.1, 1630.9)	(3.00, 104.9, 367.2)	(3.00, 84.1, 183.0)	(3.00, 56.8, 135.0)	(3.00, 37.1, 80.0)	(3.00, 28.1, 27.6)	(3.00, 28.1, 27.6)
		(3.00, 157.9, 1447.2)	(3.10, 101.3, 349.9)	(3.12, 81.5, 176.3)	(3.04, 55.4, 129.9)	(3.00, 36.5, 77.4)	(3.13, 28.2, 31.2)	(3.00, 27.8, 27.3)
	1.5	(3.00, 82.5, 558.8)	(3.00, 57.6, 167.0)	(3.00, 47.8, 96.8)	(3.00, 33.7, 71.8)	(3.00, 23.5, 43.5)	(3.00, 18.8, 18.3)	(3.00, 18.8, 18.2)
		(3.00, 79.7, 517.7)	(3.10, 56.2, 161.2)	(3.12, 46.8, 94.2)	(3.04, 33.1, 69.8)	(3.00, 23.2, 42.5)	(3.13, 18.9, 19.8)	(3.00, 18.7, 18.1)
	2.0	(3.00, 35.7, 159.5)	(3.00, 27.8, 64.2)	(3.00, 24.0, 43.6)	(3.00, 17.8, 32.7)	(3.00, 13.4, 20.6)	(3.00, 11.4, 10.8)	(3.00, 11.4, 10.8)
		(3.00, 35.0, 153.0)	(3.10, 27.4, 62.8)	(3.12, 23.7, 42.8)	(3.04, 17.7, 32.1)	(3.00, 13.3, 20.3)	(3.13, 11.4, 11.4)	(3.00, 11.3, 10.8)
0.05	1.1	(3.00, 278.8, 1340.8)	(3.00, 166.0, 381.4)	(3.00, 124.6, 208.6)	(3.00, 104.1, 136.2)	(3.00, 97.2, 101.0)	(3.00, 96.3, 95.7)	(3.00, 96.3, 95.7)
		(3.00, 280.3, 1494.1)	(3.03, 166.9, 420.1)	(3.01, 121.7, 202.7)	(3.01, 104.0, 140.2)	(3.05, 97.3, 108.4)	(3.25, 96.3, 103.6)	(3.00, 94.4, 93.8)
	1.2	(3.00, 176.0, 729.5)	(3.00, 110.4, 235.6)	(3.00, 85.1, 135.5)	(3.00, 72.5, 91.0)	(3.00, 68.2, 70.1)	(3.00, 67.6, 67.1)	(3.00, 67.6, 67.1)
		(3.00, 176.8, 816.0)	(3.03, 111.0, 257.4)	(3.01, 83.5, 132.2)	(3.01, 72.5, 93.6)	(3.05, 68.3, 74.5)	(3.25, 67.7, 71.7)	(3.00, 66.5, 65.9)
	1.5	(3.00, 57.8, 170.6)	(3.00, 40.9, 72.8)	(3.00, 33.6, 47.0)	(3.00, 29.9, 34.2)	(3.00, 28.6, 28.7)	(3.00, 28.6, 29.9)	(3.00, 28.5, 27.9)
		(3.00, 57.9, 188.6)	(3.03, 41.1, 77.9)	(3.01, 33.2, 46.3)	(3.01, 30.0, 35.0)	(3.05, 28.7, 29.8)	(3.25, 28.5, 29.1)	(3.00, 28.1, 27.6)
	2.0	(3.00, 16.1, 32.8)	(3.00, 13.0, 18.5)	(3.00, 11.4, 13.6)	(3.00, 10.6, 10.9)	(3.00, 10.3, 9.9)	(3.00, 10.3, 9.7)	(3.00, 10.3, 9.7)
		(3.00, 16.1, 34.9)	(3.03, 13.0, 19.3)	(3.01, 11.4, 13.5)	(3.01, 10.7, 11.1)	(3.05, 10.4, 10.1)	(3.25, 10.3, 10.0)	(3.00, 10.3, 9.7)
0.10	1.1	(3.00, 304.5, 1212.9)	(3.00, 190.0, 407.7)	(3.00, 155.3, 217.0)	(3.00, 153.9, 201.3)	(3.00, 151.3, 198.9)	(3.00, 146.7, 195.0)	(3.00, 146.7, 195.0)
		(3.00, 310.9, 1211.7)	(3.00, 196.0, 398.4)	(3.00, 159.4, 221.0)	(3.00, 155.2, 200.1)	(3.00, 154.6, 199.2)	(2.99, 140.5, 187.7)	(2.99, 140.5, 187.7)
	1.2	(3.00, 166.3, 575.9)	(3.00, 110.1, 216.9)	(3.00, 92.6, 124.7)	(3.00, 91.9, 117.3)	(3.00, 90.5, 115.9)	(3.00, 87.9, 113.7)	(3.00, 87.9, 113.7)
		(3.00, 170.9, 573.2)	(3.00, 113.9, 213.5)	(3.00, 95.1, 127.2)	(3.00, 92.9, 117.1)	(3.00, 92.6, 116.6)	(2.99, 84.6, 109.9)	(2.99, 84.6, 109.9)
	1.5	(3.00, 39.6, 97.5)	(3.00, 30.0, 47.9)	(3.00, 26.8, 32.8)	(3.00, 26.8, 31.7)	(3.00, 26.4, 31.4)	(3.00, 25.8, 30.8)	(3.00, 25.8, 30.8)
		(3.00, 41.2, 96.9)	(3.00, 31.1, 47.9)	(3.00, 27.6, 33.6)	(3.00, 27.1, 31.9)	(3.00, 27.0, 31.8)	(2.99, 25.1, 30.1)	(2.99, 25.1, 30.1)
	2.0	(3.00, 8.4, 13.5)	(3.00, 7.2, 8.8)	(3.00, 6.9, 7.2)	(3.00, 6.9, 7.1)	(3.00, 6.8, 7.0)	(3.00, 6.7, 6.9)	(3.00, 6.7, 6.9)
		(3.00, 8.7, 13.6)	(3.00, 7.5, 9.0)	(3.00, 7.0, 7.4)	(3.00, 7.0, 7.2)	(3.00, 6.9, 7.2)	(2.99, 6.6, 6.8)	(2.99, 6.6, 6.8)
0.20	1.1	(3.00, 270.7, 635.9)	(3.00, 219.4, 401.3)	(3.00, 186.5, 252.8)	(3.00, 183.0, 229.7)	(3.00, 180.7, 227.1)	(3.00, 173.3, 220.8)	(3.00, 173.3, 220.8)
		(2.99, 264.1, 616.6)	(3.00, 224.5, 411.9)	(3.00, 188.0, 250.8)	(3.00, 183.0, 227.7)	(3.00, 182.3, 226.4)	(3.00, 181.7, 225.9)	(2.99, 181.7, 225.9)
	1.2	(3.00, 126.2, 269.5)	(3.00, 103.0, 173.4)	(3.00, 89.9, 116.4)	(3.00, 88.5, 107.9)	(3.00, 87.5, 106.8)	(3.00, 84.2, 103.9)	(3.00, 84.2, 103.9)
		(2.99, 123.8, 263.1)	(3.00, 105.5, 177.3)	(3.00, 90.8, 116.1)	(3.00, 88.8, 107.4)	(3.00, 88.5, 106.8)	(3.00, 88.2, 106.6)	(2.99, 85.4, 114.6)
	1.5	(3.00, 21.0, 39.6)	(3.00, 17.9, 24.4)	(3.00, 16.6, 18.9)	(3.00, 16.5, 18.2)	(3.00, 16.3, 18.1)	(3.00, 15.8, 17.6)	(3.00, 15.8, 17.6)
		(2.99, 20.8, 39.2)	(3.00, 18.4, 24.8)	(3.00, 16.8, 19.1)	(3.00, 16.6, 18.3)	(3.00, 16.5, 18.2)	(3.00, 16.5, 18.2)	(2.99, 10.3, 9.7)
	2.0	(3.00, 3.4, 3.8)	(3.00, 3.2, 3.0)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(3.00, 3.0, 2.6)	(3.00, 2.5, 1.8)
		(2.99, 3.4, 3.8)	(3.00, 3.3, 3.1)	(3.00, 3.2, 2.8)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(2.99, 2.5, 1.8)
$n = 50$								
0.01	1.1	(3.00, 217.3, 1748.7)	(3.00, 146.2, 392.8)	(3.00, 98.8, 204.4)	(3.00, 71.2, 125.0)	(3.00, 59.9, 69.6)	(3.00, 58.4, 57.8)	(3.00, 58.4, 57.8)
		(3.00, 198.9, 1457.9)	(3.11, 143.9, 451.3)	(3.04, 93.7, 189.6)	(3.01, 72.3, 130.9)	(3.03, 59.6, 77.6)	(3.29, 58.5, 70.6)	(3.00, 56.3, 55.8)
	1.2	(3.00, 154.2, 1060.9)	(3.00, 108.5, 272.6)	(3.00, 75.2, 148.5)	(3.00, 55.5, 92.1)	(3.00, 47.5, 53.6)	(3.00, 46.3, 45.8)	(3.00, 46.3, 45.8)
		(3.00, 143.0, 909.8)	(3.11, 107.1, 310.8)	(3.04, 71.9, 139.0)	(3.01, 56.5, 96.9)	(3.03, 47.3, 59.2)	(3.29, 46.5, 54.4)	(3.00, 44.9, 44.4)
	1.5	(3.00, 66.9, 316.6)	(3.00, 51.9, 111.1)	(3.00, 38.4, 67.0)	(3.00, 30.0, 43.3)	(3.00, 26.6, 28.3)	(3.00, 26.1, 25.5)	(3.00, 26.1, 25.5)
		(3.00, 63.7, 287.3)	(3.11, 51.6, 123.8)	(3.04, 37.3, 64.0)	(3.01, 30.6, 46.0)	(3.03, 26.6, 30.5)	(3.29, 26.2, 28.7)	(3.00, 25.5, 25.0)
	2.0	(3.00, 25.2, 77.6)	(3.00, 21.5, 38.0)	(3.00, 17.2, 25.4)	(3.00, 14.3, 17.6)	(3.00, 13.1, 13.1)	(3.00, 13.0, 12.4)	(3.00, 13.0, 12.4)
		(3.00, 24.5, 73.8)	(3.11, 21.5, 41.1)	(3.04, 16.9, 24.8)	(3.01, 14.6, 18.7)	(3.03, 13.2, 13.8)	(3.29, 13.0, 13.3)	(3.00, 12.8, 12.2)
0.05	1.1	(3.00, 272.8, 1082.1)	(3.00, 178.5, 353.0)	(3.00, 138.4, 191.9)	(3.00, 138.3, 165.8)	(3.00, 144.0, 167.4)	(3.00, 167.8, 178.8)	(3.00, 185.4, 184.9)
		(3.04, 258.7, 1008.8)	(3.04, 184.1, 373.5)	(3.01, 138.5, 191.3)	(3.01, 138.5, 163.2)	(3.01, 145.4, 163.8)	(3.01, 168.8, 173.8)	(3.00, 176.9, 176.4)
	1.2	(3.00, 150.7, 509.3)	(3.00, 104.4, 190.8)	(3.00, 83.5, 111.1)	(3.00, 83.8, 98.6)	(3.00, 87.1, 99.8)	(3.00, 100.8, 106.6)	(3.00, 110.9, 110.4)
		(3.04, 144.6, 480.0)	(3.04, 107.8, 202.4)	(3.01, 84.0, 111.3)	(3.01, 84.3, 97.7)	(3.01, 88.4, 98.4)	(3.01, 102.0, 104.5)	(3.00, 106.7, 106.1)
	1.5	(3.00, 37.4, 87.2)	(3.00, 29.3, 44.3)	(3.00, 25.2, 30.2)	(3.00, 25.4, 28.3)	(3.00, 26.3, 28.7)	(3.00, 29.8, 30.7)	(3.00, 32.4, 31.9)
		(3.04, 36.7, 84.2)	(3.04, 30.3, 47.0)	(3.01, 25.5, 30.5)	(3.01, 25.8, 28.4)	(3.01, 26.9, 28.8)	(3.01, 30.5, 30.6)	(3.00, 31.7, 31.1)
	2.0	(3.00, 8.4, 13.0)	(3.00, 7.4, 8.8)	(3.00, 6.8, 7.0)	(3.00, 6.9, 6.9)	(3.00, 7.1, 7.0)	(3.00, 7.8, 7.5)	(3.00, 8.3, 7.7)
		(3.04, 8.4, 12.8)	(3.04, 7.6, 9.2)	(3.01, 6.9, 7.2)	(3.01, 7.0, 7.0)	(3.01, 7.3, 7.1)	(3.01, 8.0, 7.5)	(3.00, 8.2, 7.7)
0.10	1.1	(3.00, 266.5, 779.9)	(3.00, 185.5, 341.0)	(3.00, 149.6, 199.9)	(3.00, 141.6, 161.1)	(3.00, 143.5, 148.5)	(3.00, 150.0, 149.5)	(3.00, 150.1, 149.5)
		(3.02, 268.4, 778.9)	(3.01, 185.7, 336.8)	(3.00, 148.2, 197.6)	(3.01, 141.9, 163.7)	(3.04, 144.2, 150.3)	(3.20, 150.8, 161.7)	(3.00, 144.1, 143.5)
	1.2	(3.00, 122.2, 311.0)	(3.00, 90.2, 151.1)	(3.00, 75.3, 95.7)	(3.00, 72.1, 79.9)	(3.00, 73.2, 75.1)	(3.00, 76.4, 75.8)	(3.00, 76.4, 75.9)
		(3.02, 123.9, 311.5)	(3.01, 90.8, 150.6)	(3.00, 75.0, 95.2)	(3.01, 72.6, 81.3)	(3.04, 73.9, 76.1)	(3.20, 77.0, 80.9)	(3.00, 74.0, 73.4)
	1.5	(3.00, 20.9, 38.4)	(3.00, 17.5, 23.4)	(3.00, 15.7, 17.6)	(3.00, 15.4, 15.8)	(3.00, 15.7, 15.4)	(3.00, 16.2, 15.7)	(3.00, 16.2, 15.7)
		(3.02, 21.4, 38.2)	(3.01, 17.7, 23.7)	(3.00, 15.8, 17.7)	(3.01, 15.6, 16.1)	(3.04, 15.9, 15.7)	(3.20, 16.4, 16.3)	(3.00, 16.0, 15.4)
	2.0	(3.00, 3.8, 4.3)	(3.00, 3.6, 3.4)	(3.00, 3.4, 3.0)	(3.00, 3.4, 2.9)	(3.00, 3.4, 2.9)	(3.00, 3.5, 2.9)	(3.00, 3.5, 2.9)
		(3.02, 3.9, 4.4)	(3.01, 3.6, 3.5)	(3.00, 3.4, 3.0)	(3.01, 3.4, 2.9)	(3.04, 3.5, 2.9)	(3.20, 3.6, 3.0)	(3.00, 3.5, 2.9)
0.20	1.1	(3.00, 189.4, 314.8)	(3.00, 165.1, 241.4)	(3.00, 146.4, 181.7)	(3.00, 140.0, 159.1)	(3.00, 136.5, 142.3)	(3.00, 136.6, 136.1)	(3.00, 136.6, 136.1)
		(2.99, 181.5, 299.7)	(2.99, 159.2, 231.9)	(3.00, 147.9, 183.9)	(3.00, 139.2, 159.3)	(3.02, 137.7, 147.3)	(3.11, 139.5, 148.4)	(3.00, 131.7, 131.1)
	1.2	(3.00, 80.6, 148.4)	(3.00, 65.6, 97.1)	(3.00, 57.3, 68.9)	(3.00, 54.8, 60.4)	(3.00, 53.7, 55.0)	(3.00, 53.8, 53.3)	(3.00, 53.8, 53.3)
		(2.99, 78.0, 142.6)	(2.99, 63.7, 93.9)	(3.00, 57.9, 69.6)	(3.00, 54.8, 60.6)	(3.02, 54.4, 56.8)	(3.11, 55.0, 57.2)	(3.00, 52.4, 51.8)
	1.5	(3.00, 8.9, 12.8)	(3.00, 7.9, 9.1)	(3.00, 7.4, 7.5)	(3.00, 7.2, 7.0)	(3.00, 7.2, 6.7)	(3.00, 7.2, 6.7)	(3.00, 7.2, 6.7)
		(2.99, 8.8, 12.7)	(2.99, 7.8, 9.0)	(3.00, 7.5, 7.6)	(3.00, 7.3, 7.1)	(3.02, 7.3, 6.9)	(3.11, 7.4, 6.9)	(3.00, 7.2, 6.6)
	2.0	(3.00, 1.6, 1.1)	(3.00, 1.6, 1.0)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)	(3.00, 1.5, 0.9)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)
		(2.99, 1.6, 1.1)	(2.99, 1.6, 1.0)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)	(3.02, 1.6, 0.9)	(3.11, 1.6, 0.9)	(3.00, 1.6, 0.9)

Table 25: $(K, \text{ARL}_1, \text{SDRL}_1)$ for the hypergeometric np chart and $(K'', \text{ARL}_1, \text{SDRL}_1)$ for the binomial np chart with $N = 10000$, $n \in \{25, 50\}$, $p_0 \in \{0.01, 0.05, 0.10, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	(3.00, 214.3, 2361.3)	(3.00, 130.8, 486.2)	(3.00, 103.5, 230.1)	(3.00, 69.1, 169.6)	(3.00, 44.2, 100.1)	(3.00, 32.8, 32.3)	(3.00, 32.8, 32.3)
		(3.00, 208.2, 2204.1)	(3.10, 128.2, 477.9)	(3.12, 101.8, 225.7)	(3.04, 68.1, 166.0)	(3.00, 43.8, 98.2)	(3.10, 32.8, 34.1)	(3.00, 32.6, 32.1)
	1.2	(3.00, 161.9, 1534.2)	(3.00, 103.1, 355.6)	(3.00, 82.8, 179.3)	(3.00, 56.1, 132.4)	(3.00, 36.8, 78.7)	(3.00, 28.0, 27.5)	(3.00, 28.0, 27.4)
		(3.00, 157.9, 1447.2)	(3.10, 101.3, 349.9)	(3.12, 81.5, 176.3)	(3.04, 55.4, 129.9)	(3.00, 36.5, 77.4)	(3.10, 28.0, 28.8)	(3.00, 27.8, 27.3)
	1.5	(3.00, 81.1, 537.5)	(3.00, 56.9, 163.3)	(3.00, 47.3, 95.4)	(3.00, 33.4, 70.8)	(3.00, 23.3, 43.0)	(3.00, 18.7, 18.2)	(3.00, 18.7, 18.2)
		(3.00, 79.7, 517.7)	(3.10, 56.2, 161.2)	(3.12, 46.8, 94.2)	(3.04, 33.1, 69.8)	(3.00, 23.2, 42.5)	(3.10, 18.7, 18.7)	(3.00, 18.7, 18.1)
	2.0	(3.00, 35.3, 156.2)	(3.00, 27.6, 63.4)	(3.00, 23.8, 43.1)	(3.00, 17.8, 32.4)	(3.00, 13.4, 20.4)	(3.00, 11.4, 10.8)	(3.00, 11.4, 10.8)
		(3.00, 35.0, 153.0)	(3.10, 27.4, 62.8)	(3.12, 23.7, 42.8)	(3.04, 17.7, 32.1)	(3.00, 13.3, 20.3)	(3.10, 11.4, 11.0)	(3.00, 11.3, 10.8)
0.05	1.1	(3.00, 274.1, 1304.4)	(3.00, 163.8, 374.5)	(3.00, 123.1, 205.5)	(3.00, 103.0, 134.5)	(3.00, 96.2, 100.0)	(3.00, 95.3, 94.8)	(3.00, 95.3, 94.8)
		(2.99, 269.5, 1269.6)	(3.00, 161.6, 371.2)	(3.01, 121.7, 202.7)	(3.01, 104.0, 140.2)	(3.03, 96.4, 104.3)	(3.03, 95.3, 98.4)	(3.00, 94.4, 93.8)
	1.2	(3.00, 173.5, 713.2)	(3.00, 109.1, 231.9)	(3.00, 84.3, 133.7)	(3.00, 71.9, 90.1)	(3.00, 67.6, 69.5)	(3.00, 67.1, 66.5)	(3.00, 67.1, 66.5)
		(2.99, 171.1, 697.4)	(3.00, 107.9, 230.0)	(3.01, 83.5, 132.2)	(3.01, 72.5, 93.6)	(3.03, 67.8, 72.1)	(3.23, 67.1, 68.6)	(3.00, 66.5, 65.9)
	1.5	(3.00, 164.3, 168.3)	(3.00, 40.6, 72.1)	(3.00, 33.4, 46.7)	(3.00, 29.7, 34.0)	(3.00, 28.5, 28.5)	(3.00, 28.5, 27.7)	(3.00, 28.5, 27.7)
		(2.99, 56.8, 166.1)	(3.00, 40.3, 71.7)	(3.01, 33.2, 46.3)	(3.01, 30.0, 35.0)	(3.03, 28.5, 29.2)	(3.23, 28.3, 28.3)	(3.00, 28.1, 27.6)
	2.0	(3.00, 16.1, 32.6)	(3.00, 12.9, 18.4)	(3.00, 11.4, 13.5)	(3.00, 10.6, 10.9)	(3.00, 10.3, 9.9)	(3.00, 10.3, 9.7)	(3.00, 10.3, 9.7)
		(2.99, 16.0, 32.4)	(3.00, 12.9, 18.3)	(3.01, 11.4, 13.5)	(3.01, 10.7, 11.1)	(3.03, 10.3, 10.0)	(3.23, 10.3, 9.8)	(3.00, 10.3, 9.7)
0.10	1.1	(3.00, 300.1, 1188.4)	(3.00, 187.7, 401.4)	(3.00, 154.4, 219.1)	(3.00, 152.2, 198.9)	(3.00, 153.0, 199.1)	(3.00, 149.6, 196.4)	(3.00, 149.6, 196.4)
		(2.99, 295.8, 1164.6)	(2.99, 185.4, 395.3)	(2.99, 151.8, 211.6)	(2.99, 150.4, 196.3)	(3.00, 154.6, 199.2)	(3.00, 154.0, 198.7)	(2.99, 144.1, 143.5)
	1.2	(3.00, 164.3, 566.4)	(3.00, 109.0, 214.2)	(3.00, 92.1, 125.7)	(3.00, 91.1, 116.1)	(3.00, 91.5, 116.3)	(3.00, 89.6, 114.7)	(3.00, 89.6, 114.7)
		(2.99, 162.3, 557.0)	(2.99, 107.9, 211.5)	(2.99, 90.8, 122.1)	(2.99, 90.2, 114.9)	(3.00, 92.6, 116.6)	(3.00, 92.2, 116.3)	(2.99, 41.3, 40.7)
	1.5	(3.00, 39.3, 96.6)	(3.00, 29.8, 47.6)	(3.00, 26.8, 33.0)	(3.00, 26.6, 31.5)	(3.00, 26.7, 31.6)	(3.00, 26.3, 31.2)	(3.00, 26.3, 31.2)
		(2.99, 39.1, 95.7)	(2.99, 29.6, 47.2)	(2.99, 26.5, 32.4)	(2.99, 26.5, 31.3)	(3.00, 27.0, 31.8)	(3.00, 27.0, 31.7)	(2.99, 14.4, 13.9)
	2.0	(3.00, 8.4, 13.5)	(3.00, 7.2, 8.8)	(3.00, 6.9, 7.2)	(3.00, 6.8, 7.1)	(3.00, 6.9, 7.1)	(3.00, 6.8, 7.0)	(3.00, 6.8, 7.0)
		(2.99, 8.3, 13.4)	(2.99, 7.2, 8.8)	(2.99, 6.8, 7.2)	(2.99, 6.8, 7.1)	(3.00, 6.9, 7.2)	(3.00, 6.9, 7.1)	(2.99, 4.6, 4.0)
0.20	1.1	(3.00, 279.1, 708.9)	(3.00, 218.4, 414.4)	(3.00, 184.5, 249.9)	(3.00, 181.0, 227.1)	(3.00, 181.6, 226.8)	(3.00, 177.6, 223.5)	(3.00, 177.6, 223.5)
		(3.00, 287.9, 699.2)	(2.99, 214.6, 390.9)	(3.00, 188.0, 250.8)	(3.00, 183.0, 227.7)	(3.00, 182.3, 226.4)	(3.00, 181.7, 225.9)	(2.99, 85.9, 85.3)
	1.2	(3.00, 128.2, 291.6)	(3.00, 102.6, 177.5)	(3.00, 89.1, 115.3)	(3.00, 87.8, 106.9)	(3.00, 88.0, 106.8)	(3.00, 86.2, 105.3)	(3.00, 86.2, 105.3)
		(3.00, 132.4, 288.9)	(2.99, 101.2, 169.9)	(3.00, 90.8, 116.1)	(3.00, 88.8, 107.4)	(3.00, 88.5, 106.8)	(3.00, 88.2, 106.6)	(2.99, 45.1, 44.6)
	1.5	(3.00, 20.9, 39.5)	(3.00, 17.9, 24.6)	(3.00, 16.5, 18.8)	(3.00, 16.4, 18.1)	(3.00, 16.4, 18.1)	(3.00, 16.2, 17.9)	(3.00, 16.1, 15.5)
		(3.00, 21.6, 39.5)	(2.99, 17.8, 24.2)	(3.00, 16.8, 19.1)	(3.00, 16.6, 18.3)	(3.00, 16.5, 18.2)	(3.00, 16.5, 18.2)	(2.99, 10.3, 9.7)
	2.0	(3.00, 3.4, 3.8)	(3.00, 3.2, 3.0)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(3.00, 2.5, 1.8)
		(3.00, 3.5, 3.8)	(2.99, 3.2, 3.0)	(3.00, 3.2, 2.8)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(3.00, 3.1, 2.7)	(2.99, 2.5, 1.8)
$n = 50$								
0.01	1.1	(3.00, 207.7, 1592.5)	(3.00, 141.3, 377.2)	(3.00, 96.2, 196.6)	(3.00, 69.7, 120.8)	(3.00, 59.3, 71.2)	(3.00, 57.3, 56.8)	(3.00, 57.3, 56.8)
		(3.00, 198.9, 1457.9)	(3.04, 143.8, 443.0)	(3.04, 93.7, 189.6)	(3.00, 68.3, 116.9)	(3.03, 59.6, 77.6)	(3.27, 57.5, 64.0)	(3.00, 56.3, 55.8)
	1.2	(3.00, 148.4, 980.5)	(3.00, 105.3, 262.9)	(3.00, 73.5, 143.5)	(3.00, 54.5, 89.4)	(3.00, 47.1, 54.7)	(3.00, 45.6, 45.1)	(3.00, 45.6, 45.1)
		(3.00, 143.0, 909.8)	(3.04, 107.1, 306.2)	(3.04, 71.9, 139.0)	(3.00, 53.6, 86.9)	(3.03, 47.3, 59.2)	(3.27, 45.7, 49.9)	(3.00, 44.9, 44.4)
	1.5	(3.00, 65.3, 301.3)	(3.00, 50.9, 108.3)	(3.00, 37.8, 65.4)	(3.00, 29.7, 42.5)	(3.00, 26.4, 28.8)	(3.00, 25.8, 25.2)	(3.00, 25.8, 25.2)
		(3.00, 63.7, 287.3)	(3.04, 51.6, 122.8)	(3.04, 37.3, 64.0)	(3.00, 29.3, 41.8)	(3.03, 26.6, 30.5)	(3.27, 25.9, 27.0)	(3.00, 25.5, 25.0)
	2.0	(3.00, 24.8, 75.7)	(3.00, 21.3, 37.5)	(3.00, 17.1, 25.1)	(3.00, 14.2, 17.5)	(3.00, 13.1, 13.3)	(3.00, 12.9, 12.3)	(3.00, 12.9, 12.3)
		(3.00, 24.5, 73.8)	(3.04, 21.5, 40.9)	(3.04, 16.9, 24.8)	(3.00, 14.1, 17.3)	(3.03, 13.2, 13.8)	(3.27, 12.9, 12.8)	(3.00, 12.8, 12.2)
0.05	1.1	(3.00, 264.9, 1035.9)	(3.00, 174.2, 342.1)	(3.00, 135.3, 187.2)	(3.00, 135.3, 162.4)	(3.00, 142.8, 164.6)	(3.00, 167.0, 175.8)	(3.00, 181.1, 180.6)
		(3.04, 258.7, 1008.8)	(3.02, 171.8, 351.4)	(3.00, 138.5, 191.3)	(3.00, 135.4, 160.9)	(3.00, 143.5, 162.8)	(3.01, 168.8, 173.8)	(3.00, 176.9, 176.4)
	1.2	(3.00, 147.1, 491.7)	(3.00, 102.3, 186.0)	(3.00, 82.0, 108.8)	(3.00, 82.3, 96.9)	(3.00, 86.7, 98.5)	(3.00, 100.7, 105.3)	(3.00, 108.8, 108.2)
		(3.04, 144.6, 480.0)	(3.02, 101.1, 190.3)	(3.00, 84.0, 111.3)	(3.00, 82.6, 96.3)	(3.00, 87.3, 97.8)	(3.01, 102.0, 104.5)	(3.00, 106.7, 106.1)
	1.5	(3.00, 36.9, 85.6)	(3.00, 29.0, 43.7)	(3.00, 24.9, 29.8)	(3.00, 25.2, 28.0)	(3.00, 26.3, 28.6)	(3.00, 29.9, 30.6)	(3.00, 32.1, 31.5)
		(3.04, 36.7, 84.2)	(3.02, 28.8, 44.3)	(3.00, 25.5, 30.5)	(3.00, 25.4, 28.0)	(3.00, 26.6, 28.6)	(3.01, 30.5, 30.6)	(3.00, 31.7, 31.1)
	2.0	(3.00, 8.4, 12.9)	(3.00, 7.4, 8.8)	(3.00, 6.8, 7.0)	(3.00, 6.9, 6.9)	(3.00, 7.1, 7.0)	(3.00, 7.8, 7.5)	(3.00, 8.3, 7.7)
		(3.04, 8.4, 12.8)	(3.02, 7.4, 8.8)	(3.00, 6.9, 7.2)	(3.00, 6.9, 6.9)	(3.00, 7.2, 7.1)	(3.01, 8.0, 7.5)	(3.00, 8.2, 7.7)
0.10	1.1	(3.00, 259.7, 753.8)	(3.00, 181.3, 331.9)	(3.00, 148.4, 195.8)	(3.00, 140.5, 160.0)	(3.00, 141.6, 146.2)	(3.00, 147.0, 146.5)	(3.00, 147.0, 146.5)
		(3.00, 254.4, 757.1)	(3.01, 185.7, 336.8)	(3.00, 148.2, 197.6)	(3.01, 141.9, 163.7)	(3.02, 141.9, 146.6)	(3.18, 146.5, 150.4)	(3.00, 144.1, 143.5)
	1.2	(3.00, 119.8, 302.8)	(3.00, 88.6, 148.0)	(3.00, 75.0, 94.3)	(3.00, 71.8, 79.5)	(3.00, 72.5, 74.2)	(3.00, 75.2, 74.6)	(3.00, 75.2, 74.6)
		(3.00, 117.8, 303.5)	(3.01, 90.8, 150.6)	(3.00, 75.0, 95.2)	(3.01, 72.6, 81.3)	(3.02, 72.9, 74.5)	(3.18, 75.1, 76.3)	(3.00, 74.0, 73.4)
	1.5	(3.00, 20.7, 37.9)	(3.00, 17.3, 23.1)	(3.00, 15.7, 17.5)	(3.00, 15.4, 15.8)	(3.00, 15.6, 15.4)	(3.00, 16.1, 15.5)	(3.00, 16.1, 15.5)
		(3.00, 20.6, 37.6)	(3.01, 17.7, 23.7)	(3.00, 15.8, 17.7)	(3.01, 15.6, 16.1)	(3.02, 15.8, 15.5)	(3.18, 16.1, 15.7)	(3.00, 16.0, 15.4)
	2.0	(3.00, 3.8, 4.3)	(3.00, 3.6, 3.4)	(3.00, 3.4, 3.0)	(3.00, 3.4, 2.9)	(3.00, 3.4, 2.9)	(3.00, 3.5, 2.9)	(3.00, 3.5, 2.9)
		(3.00, 3.8, 4.3)	(3.01, 3.6, 3.5)	(3.00, 3.4, 3.0)	(3.01, 3.4, 2.9)	(3.02, 3.5, 2.9)	(3.18, 3.5, 2.9)	(3.00, 3.5, 2.9)
0.20	1.1	(3.00, 185.4, 307.1)	(3.00, 164.6, 238.3)	(3.00, 147.2, 182.8)	(3.00, 140.3, 160.2)	(3.00, 135.2, 141.3)	(3.00, 134.1, 133.5)	(3.00, 134.1, 133.5)
		(2.99, 181.5, 299.7)	(3.00, 166.7, 239.5)	(3.00, 147.9, 183.9)	(3.00, 139.2, 159.3)	(3.01, 135.5, 143.3)	(3.09, 134.2, 137.1)	(3.00, 131.7, 131.1)
	1.2	(3.00, 79.3, 145.5)	(3.00, 65.5, 95.9)	(3.00, 57.6, 69.1)	(3.00, 55.0, 60.8)	(3.00, 53.4, 54.8)	(3.00, 53.1, 52.5)	(3.00, 53.1, 52.5)
		(2.99, 78.0, 142.6)	(3.00, 66.2, 96.0)	(3.00, 57.9, 69.6)	(3.00, 54.8, 60.6)	(3.01, 53.6, 55.6)	(3.09, 53.3, 53.7)	(3.00, 52.4, 51.8)
	1.5	(3.00, 8.8, 12.7)	(3.00, 7.9, 9.0)	(3.00, 7.4, 7.5)	(3.00, 7.3, 7.1)	(3.00, 7.2, 6.7)	(3.00, 7.2, 6.6)	(3.00, 7.2, 6.6)
		(2.99, 8.8, 12.7)	(3.00, 8.0, 9.1)	(3.00, 7.5, 7.6)	(3.00, 7.3, 7.1)	(3.01, 7.2, 6.8)	(3.09, 7.2, 6.7)	(3.00, 7.2, 6.6)
	2.0	(3.00, 1.6, 1.1)	(3.00, 1.6, 1.0)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)
		(2.99, 1.6, 1.1)	(3.00, 1.6, 1.0)	(3.00, 1.6, 0.9)	(3.00, 1.6, 0.9)	(3.01, 1.6, 0.9)	(3.09, 1.6, 0.9)	(3.00, 1.6, 0.9)

Table 26: $(ARL_1, SDRL_1)$ for the binomial np chart with $n \in \{25, 50\}$, $p_0 \in \{0.01, 0.05, 0.10, 0.20\}$, $m \in \{10, 20, 50, 100, 200, 1000, \infty\}$

p_0	τ	$m = 10$	$m = 20$	$m = 50$	$m = 100$	$m = 200$	$m = 1000$	$m \rightarrow \infty$
$n = 25$								
0.01	1.1	(208.2, 2204.1)	(128.2, 469.0)	(101.8, 225.0)	(68.1, 166.0)	(43.8, 98.2)	(32.6, 32.1)	(32.6, 32.1)
	1.2	(157.9, 1447.2)	(101.3, 344.6)	(81.5, 175.8)	(55.4, 129.9)	(36.5, 77.4)	(27.8, 27.3)	(27.8, 27.3)
	1.5	(79.7, 517.7)	(56.2, 159.9)	(46.8, 94.0)	(33.1, 69.8)	(23.2, 42.5)	(18.7, 18.1)	(18.7, 18.1)
	2.0	(35.0, 153.0)	(27.4, 62.6)	(23.7, 42.7)	(17.7, 32.1)	(13.3, 20.3)	(11.3, 10.8)	(11.3, 10.8)
0.05	1.1	(280.3, 1494.1)	(161.6, 371.2)	(121.7, 202.5)	(102.0, 132.8)	(95.2, 99.0)	(94.4, 93.8)	(94.4, 93.8)
	1.2	(176.8, 816.0)	(107.9, 230.0)	(83.5, 132.0)	(71.2, 89.1)	(67.0, 68.9)	(66.5, 65.9)	(66.5, 65.9)
	1.5	(57.9, 188.6)	(40.3, 71.7)	(33.2, 46.3)	(29.6, 33.8)	(28.3, 28.3)	(28.1, 27.6)	(28.1, 27.6)
	2.0	(16.1, 34.9)	(12.9, 18.3)	(11.4, 13.5)	(10.6, 10.9)	(10.3, 9.8)	(10.3, 9.7)	(10.3, 9.7)
0.10	1.1	(310.9, 1211.7)	(196.0, 398.4)	(159.4, 221.0)	(155.2, 200.1)	(154.6, 199.2)	(154.0, 198.7)	(242.7, 242.2)
	1.2	(170.9, 573.2)	(113.9, 213.5)	(95.1, 127.2)	(92.9, 117.1)	(92.6, 116.6)	(92.2, 116.3)	(142.5, 142.0)
	1.5	(41.2, 96.9)	(31.1, 47.9)	(27.6, 33.6)	(27.1, 31.9)	(27.0, 31.8)	(27.0, 31.7)	(39.3, 38.8)
	2.0	(8.7, 13.6)	(7.5, 9.0)	(7.0, 7.4)	(7.0, 7.2)	(6.9, 7.2)	(6.9, 7.1)	(9.2, 8.6)
0.20	1.1	(287.7, 699.2)	(224.5, 411.9)	(188.0, 250.8)	(183.0, 227.7)	(182.3, 226.4)	(181.7, 225.9)	(276.6, 276.1)
	1.2	(132.4, 288.9)	(105.5, 177.3)	(90.8, 116.1)	(88.8, 107.4)	(88.5, 106.8)	(88.2, 106.6)	(130.9, 130.4)
	1.5	(21.6, 39.5)	(18.4, 24.8)	(16.8, 19.1)	(16.6, 18.3)	(16.5, 18.2)	(16.5, 18.2)	(22.7, 22.1)
	2.0	(3.5, 3.8)	(3.3, 3.1)	(3.2, 2.8)	(3.1, 2.7)	(3.1, 2.7)	(3.1, 2.7)	(3.8, 3.2)
$n = 50$								
0.01	1.1	(198.9, 1457.9)	(136.7, 358.9)	(93.7, 189.2)	(68.3, 116.9)	(58.3, 69.5)	(56.3, 55.8)	(56.3, 55.8)
	1.2	(143.0, 909.8)	(102.3, 252.0)	(71.9, 138.8)	(53.6, 86.9)	(46.3, 53.7)	(44.9, 44.4)	(44.9, 44.4)
	1.5	(63.7, 287.3)	(49.9, 105.3)	(37.3, 64.0)	(29.3, 41.8)	(26.1, 28.4)	(25.5, 25.0)	(25.5, 25.0)
	2.0	(24.5, 73.8)	(21.1, 36.9)	(16.9, 24.8)	(14.1, 17.3)	(13.0, 13.2)	(12.8, 12.2)	(12.8, 12.2)
0.05	1.1	(257.3, 992.6)	(170.0, 333.5)	(138.5, 191.3)	(135.4, 160.9)	(143.5, 162.8)	(165.9, 172.7)	(176.9, 176.4)
	1.2	(143.7, 475.0)	(100.3, 182.0)	(84.0, 111.3)	(82.6, 96.3)	(87.3, 97.8)	(100.3, 103.8)	(106.7, 106.1)
	1.5	(36.4, 84.0)	(28.7, 43.1)	(25.5, 30.5)	(25.4, 28.0)	(26.6, 28.6)	(30.0, 30.4)	(31.7, 31.1)
	2.0	(8.3, 12.8)	(7.4, 8.7)	(6.9, 7.2)	(6.9, 6.9)	(7.2, 7.1)	(7.9, 7.5)	(8.2, 7.7)
0.10	1.1	(254.4, 757.1)	(177.6, 323.4)	(148.2, 197.6)	(139.3, 159.0)	(139.6, 144.0)	(144.1, 143.5)	(144.1, 143.5)
	1.2	(117.8, 303.5)	(87.2, 144.9)	(75.0, 95.2)	(71.4, 79.3)	(71.8, 73.4)	(74.0, 73.4)	(74.0, 73.4)
	1.5	(20.6, 37.6)	(17.2, 22.9)	(15.8, 17.7)	(15.4, 15.8)	(15.6, 15.3)	(16.0, 15.4)	(16.0, 15.4)
	2.0	(3.8, 4.3)	(3.6, 3.4)	(3.4, 3.0)	(3.4, 2.9)	(3.4, 2.9)	(3.5, 2.9)	(3.5, 2.9)
0.20	1.1	(190.4, 307.2)	(166.7, 239.5)	(147.9, 183.9)	(139.2, 159.3)	(133.9, 140.6)	(131.7, 131.1)	(131.7, 131.1)
	1.2	(80.7, 144.1)	(66.2, 96.0)	(57.9, 69.6)	(54.8, 60.6)	(53.1, 54.7)	(52.4, 51.8)	(52.4, 51.8)
	1.5	(9.0, 12.8)	(8.0, 9.1)	(7.5, 7.6)	(7.3, 7.1)	(7.2, 6.7)	(7.2, 6.6)	(7.2, 6.6)
	2.0	(1.6, 1.1)	(1.6, 1.0)	(1.6, 0.9)	(1.6, 0.9)	(1.6, 0.9)	(1.6, 0.9)	(1.6, 0.9)

Table 27: Selected results of the simulation study regarding ARL_1

m, N, n, p_0, τ	ARL_1	ARL_1^{sim}	m, N, n, p_0, τ	ARL_1	ARL_1^{sim}	m, N, n, p_0, τ	ARL_1	ARL_1^{sim}
10, 100, 25, 0.01, 1.1	–	–	20, 100, 25, 0.05, 1.2	260.0	265.1	50, 100, 50, 0.1, 1.5	8.2	8.1
100, 200, 25, 0.05, 1.2	106.8	105.2	200, 200, 50, 0.1, 1.5	11.5	11.5	1000, 200, 50, 0.2, 2	1.3	1.3
10, 500, 25, 0.01, 1.1	–	–	20, 500, 25, 0.05, 1.2	115.2	111.2	50, 500, 50, 0.1, 1.5	14.8	14.8
100, 1000, 25, 0.05, 1.2	75.2	75.1	200, 1000, 50, 0.1, 1.5	15.8	15.8	1000, 1000, 50, 0.2, 2	1.5	1.5
10, 2000, 25, 0.01, 1.1	243	241.9	20, 2000, 25, 0.05, 1.2	114.3	110.7	50, 2000, 50, 0.1, 1.5	15.6	15.5
100, 5000, 25, 0.05, 1.2	72.5	72.9	200, 5000, 50, 0.1, 1.5	15.7	15.7	1000, 5000, 50, 0.2, 2	1.6	1.5
10, 10000, 25, 0.01, 1.1	214.3	215.9	20, 10000, 25, 0.05, 1.2	109.1	105.4	50, 10000, 50, 0.1, 1.5	15.7	15.5