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Correlating sulfur solubility with short-to-intermediate-range ordering in the structure of borosilicate glasses

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Abstract

The present study focuses on understanding the structural dependence of sulfur (as $SO_4^{2^\circ}$) solubility in Na₂O–B₂O₃–SiO₂ glasses over a broad composition space exhibiting a rich variety of structural associations. The focus is on probing the impact of the (1) structural role of Na⁺, (2) degree of polymerization, and (3) network former connectivity (formation of Si–O–B and B–O–B linkages) on sulfur solubility in borosilicate glasses. By employing a suite of *state-of-the-art* characterization techniques, including ICP-OES, MAS NMR spectroscopy, and Raman spectroscopy, an inverse correlation has been established between the sulfur solubility and the degree of network polymerization in the glasses across the investigated composition space. While the formation of SO₄²⁻ can successfully compete with the network depolymerization mechanisms (i.e., creation of non-bridging oxygens) and induce re-polymerization in the glass network, the BO₃→BO₄ conversion takes precedence. The results from this study, when extended to more complex borosilicate-based glass chemistries, will not only add to our understanding of the fundamental science controlling the sulfur solubility in borosilicate-based real-world nuclear waste glasses, but will also form a basis for the development of non-empirical Quantitative Structure – Property Relationships based predictive models.

Keywords: Borosilicate glass; nuclear waste; MAS NMR spectroscopy; Raman spectroscopy; ICP– OES.

1. Introduction

Owing to its low solubility (on the order of 1 wt.% SO₃) in borosilicate based radioactive waste glasses, sulfur (as sulfate, SO₄²⁻) has been one of the two critical factors (the second one being the long-term chemical durability) impeding the loading of Hanford low-activity waste (LAW) into vitreous waste forms.¹ Exceeding the solubility limit of sulfate in borosilicate-based nuclear waste glass melt results in the formation of an immiscible sulfate salt layer (known as *"gall"* or yellow phase) that floats on the top of the melt.^{2, 3} The low-viscosity, electrically conductive salt layer, being rich in water-soluble alkali/alkaline-earth sulfates along with specific radionuclides (such as ⁹⁹Tc, ⁹⁰Sr, and ¹³⁷Cs), can cause several problems for the melter—for example, corrosion of container walls, shorting of the heating electrodes, risks of explosion due to low viscosity and low density—thus, severely impacting its performance and lifetime.⁴⁻⁶

In order to avoid the above-mentioned complications, and for the safe operation of the melter, empirical models have been developed to predict the practical limit of salt solubility in the melt as a function of feed composition. For example, Vienna et al.,⁶ based on 253 simulated Hanford LAW glass compositions, established an empirical model to predict the SO₃ solubility in LAW glasses as a function of the concentration of different components in the melter feed (as shown in Eqn. 1).

$$W_{SO_3}^{Pred} = \sum_{i=1}^{q} s_i n_i + selected(\sum_{i=1}^{q} s_{ii} n_i^2 + \sum_{j=1}^{q-1} \sum_{k=j+1}^{q} s_{jk} n_j n_k) \quad (1)$$

where, $W_{SO_3}^{Pred}$ is the predicted SO₃ solubility in weight percent, *q* represents the number of components in the composition with *s* being the coefficient and *n* is the normalized mass fraction of the component. Further, Muller et al.⁷ extended this SO₃ solubility model to a 31-term partial

quadratic mixture model (shown in Equation 2) using the data of 485 LAW glasses with SO_3 solubility (wt.%) ranging from 0.15 to 0.83.

$$SO_3 (wt\%) = \sum_{i=1}^{18} a_i x_i + selected \left\{ \sum_{i<}^{q-1} \sum_j^q a_{ij} x_i x_j \right\}$$
(2)

where *q* represents the number of components in the composition with *a* being the coefficient, and *x* is the normalized mass fraction of the component.⁸

The above-discussed models, though conservative (in terms of SO_3 loading), may work well for the current processing flowsheet where LAW is supposed to be pre-treated before vitrification. However, owing to their empirical nature, it will be impossible for these models to predict LAW glass compositions with higher SO_3 solubility (> 1 wt.%), as anticipated in the case of a direct feed approach.⁴

Further, the implementation of a direct feed approach not only poses a challenge for the established models for predicting the SO₃ solubility in LAW glasses, but it is also expected to aggravate the complexity of high level waste (HLW) vitrification by considerably increasing the sulfate content in the waste stream (since the pre-treatment of HLW for sulfate removal before vitrification shall be by-passed).⁹ Therefore, sulfur tolerant HLW glasses need to be designed to avoid salt segregation in the Joule Heated Ceramic Melter (JHCM). Nevertheless, the existing SO₃ solubility models do not perform well with HLW glass compositions, as these models are based on a statistical rather than Quantitative Structure – Property Relationships (QSPR) based approach and are confined to the compositional database of LAW glasses.¹⁰

The above-mentioned challenges posed by the increasing sulfate content in direct-feed LAW and HLW glasses can be addressed by one of the following two approaches: (1) follow a *trial-and-error* approach to collect enormous amounts of data on LAW and HLW glasses with

enhanced SO₃ loadings leading to the development of empirical composition–SO₃ solubility based predictive models, or (2) combine the strengths of experimental and computational materials science to understand (and elucidate) the underlying compositional and structural descriptors controlling $SO_4^{2^2}$ solubility in borosilicate glasses. Ultimately this should lead to the development of a unified composition–structure– $SO_4^{2^2}$ solubility-based model that can help in the rational design of both LAW and HLW glasses with enhanced SO₃ loadings, irrespective of the differences in their compositional ranges. While the design of advanced glass formulations using the first approach is difficult, if not impossible, the implementation of the second approach requires a new level of conceptual understanding about the impact of structural organization of borosilicate-based glasses on their sulfur solubility.

The challenge with the implementation of the second approach is the limited amount of literature dealing with the composition–structure– SO_4^{2-} solubility relationships in borosilicate glasses. The investigated glass systems are compositionally complex (comprising multiple framework and non-framework moieties). In addition, to date only empirical correlations between composition and properties have been published.^{2, 3, 11-20} Systematic model studies are needed, exploring the dependence of sulfur (as SO_4^{2-}) solubility on short–to–intermediate range ordering in glasses with simplified compositions, before introducing compositional complexity.

In the present contribution we investigate the dependence of SO₃ solubility in Na₂O–B₂O₃– SiO₂ based glasses on composition over a broad composition space, traversing all the four regions (in terms of relative ratios $R = Na_2O/B_2O_3$, and $K = SiO_2/B_2O_3$) in the sodium borosilicate ternary, as described by the Dell–Yun–Bray (DYB) structural description (see Figure 1),²²⁻²⁴ exhibiting a rich variety of structural associations. The DYB model divides the compositional space in the Na₂O–B₂O₃–SiO₂ ternary system into four regions based on the R (=

Na₂O/B₂O₃) and *K* (=SiO₂/B₂O₃ \leq 8) values, as has been shown in Figure 1.^{23, 24} Region 1 comprises the glasses with *R* < 0.5. Region 2 belongs to the glasses with 0.5 \leq *R* \leq *R**, where *R** (= 0.5 + *K*/16) is the value



Figure 1. Compositions of the baseline $Na_2O-B_2O_3$ -SiO₂ glasses investigated in the present study overlaid upon the Dell-Yun-Bray (DYB) ternary diagram. The numbers 1 to 4 represent the four regions as described in the DYB model for sodium borosilicate ternary system. The white circles represent the batched compositions while the red circles represent the experimentally measured glass compositions.

at which anionic functionalization of boron still proceeds exclusively by the conversion of threeto four coordinated boron. The value of R^* assumes that the four-coordinated boron species are

stabilized by four B-O-Si linkages units, which is the structural situation in the mineral reedmergnerite (NaBSi₄O₁₀). In Region 3, defined by $R^* \le R \le (0.5+K/4)$, the additional Na⁺ (left after the formation of B^4 , i.e., BO_4 , units) create NBOs in the silicate network and subsequently, in the borate units, defined by Region 4, where $(0.5+K/4) \le R \le (2+K)$. Accordingly, a total of three sets of glass compositions have been designed with: (1) variation of R at fixed SiO_2 content (NB series), (2) variation of K at fixed Na₂O content (SB series), and (3) variation of the Na₂O/SiO₂ ratio at fixed B₂O₃ content (NS series). Previous structural work on borosilicate glasses suggests that such compositional variations influence the boron speciation (fractions of three-versus four-coordinated species, B(III) and B(IV)), the concentration of non-bridging oxygens (NBOs) bonded to B(III) or silicon, the concentrations of ring-to-non-ring units and the distributions of Si-O-Si, Si-O-B, and B-O-B connectivity.^{22, 24-29} In addition, the extent of network former mixing may be limited by chemical segregation and/or phase separation phenomena. All these variations in the short-to-medium range structure are expected to have an impact on the sulfur solubility in borosilicate glasses.^{11, 30} In turn, incorporation of sulfur may affect network former speciation and network former - network modifier interactions. Thus, the present study aims to employ a suite of state-of-the-art spectroscopic techniques to decipher the underlying structural drivers governing the sulfur solubility in sodium borosilicate glasses.

2. Experimental details

2.1 Synthesis of baseline borosilicate glasses

All glasses were synthesized by the melt quench technique. High purity powders of SiO_2 (Alfa Aesar; >99.5%), H₃BO₃ (Alfa Aesar; >98%), and Na₂CO₃ (Fisher Scientific; >99.5%) were used as precursors. The homogenous batches corresponding to 70 g of oxides were melted in

90%Pt -10%Rh crucibles (loosely covered with a Pt lid) in an electric furnace in the temperature range of 950-1650 °C for 1 h. The melts were quenched on a copper plate maintained at room temperature.

2.2 Synthesis of sulfur-containing borosilicate glasses

Na₂SO₄ has been used as a precursor for adding sulfur (as SO₃) to the baseline glasses. The batch calculations were made to ensure that the total content of Na₂O in the glass remains constant. The example below describes the methodology used to synthesize sulfur-containing glasses in the present study. When adding *x* mol.% SO₃ to a baseline composition, for example, 40 Na₂O–20 B₂O₃–40 SiO₂, the batch was calculated as (40-*x*) Na₂O–20 B₂O₃–40 SiO₂–*x* Na₂SO₄ (mol.%), where *x* mol.% Na₂SO₄ serves as the source of *x* mol.% Na₂O and *x* mol.% SO₃. Accordingly, a batch corresponding to composition (40-*x*) Na₂O–20 B₂O₃–40 SiO₂ was prepared and melted in a Pt-Rh crucible using the methodology described in section 2.1. Once the melt (poured on the copper plate) cooled to room temperature, the resulting glass was kept back in the same Pt–Rh crucible and *x* mol.% Na₂SO₄ was added to it. The Pt–Rh crucible was loaded in the furnace and covered with a Pt lid. The mixture was melted at the same temperature (as the base glass) for another 1 hour followed by quenching of the melt by pouring it on a copper plate.

2.3 Compositional analysis of glass samples

The amorphous/crystalline nature of the resulting samples has been confirmed by powder (particle size < 45 μ m) X-ray diffraction (PANalytical X'Pert Pro X-ray diffractometer with Cu K_a radiation; 45 kV; 40 mA; 20 range of 10-90°; step-size of 0.013°; dwell time of 0.01 s at each step).

The compositional analysis of the glass samples has been performed by inductively coupled plasma – optical emission spectroscopy (ICP–OES; Perkin Elmer Optima 8300). Prior to analysis for B_2O_3 , the glass samples were digested in a 1:1 (by volume) hydrofluoric acid (37 w/w) to water solution (by volume). Prior to SiO₂ analysis, a mixture of 50 mg glass powder (particle size <45µm), 250 mg Na₂B₄O₇ and 250 mg Na₂CO₃ was prepared and fused at 950 °C. The resulting fused product was subsequently digested by stirring in a 1:1 (by volume) hydrochloric acid to water solution. In the case of sodium analysis, samples were digested in HCl/HF mixtures using multiple heating and drying cycles. The resulting samples were ultimately dissolved in 1:1 (by volume) hydrochloric acid to water solution. For sulfur analysis, a mixture of 250 mg glass powder, 500 mg Na₂B₄O₇ and 500 mg Na₂CO₃ was fused at 950 °C followed by digestion (by stirring) in a 1:1 (by volume) hydrochloric acid to water solution. Each of the above-described solutions has been analyzed via ICP–OES against a matrix-matched blank and standard.

Figure 1 and Table S1 present the batched and analyzed compositions (using ICP-OES) of the sulfur-free (baseline) glasses investigated in the present study. The glasses have been labeled as NB-x, SB-y and NS-z, where x and z represent the molar concentrations of Na₂O, while y represent the molar concentrations of B₂O₃ in the respective series.

2.4 Structural analysis of glasses

The structural analysis of the glass samples has been performed by ¹¹B, ²³Na and ²⁹Si magic angle spinning – nuclear magnetic resonance (MAS NMR) and Raman spectroscopy. ¹¹B MAS NMR spectra have been recorded on a Bruker Avance Neo 600 MHz spectrometer (14.1 T) using a commercially available 2.5 mm MAS NMR probe. Single resonance ¹¹B MAS NMR spectra have been collected using powdered samples packed into zirconia rotors and spun at 15.0-20.0 kHz. All the data has been acquired at 14.1 T (192.63 MHz resonance frequency) using RF pulses of 0.8 μ s (corresponding to a $\pi/6$ tip angle), 1 s recycle delays, and signal averaging over at least 1000 acquisitions. ¹¹B chemical shifts are reported relative to an aqueous solution of BF₃•Et₂O, using solid BPO₄ at -3.5 ppm as a secondary standard. Additional ¹¹B MAS NMR data were measured at 16.4 T using a Bruker Avance III spectrometer and at 5.64 T using a Agilent DD2 spectrometer, using similar acquisition parameters. Fitting of all ¹¹B MAS NMR spectra has been performed using the DMfit software³¹ in order to quantify structural species in the glasses, utilizing "Q MAS ½" and Gauss/Lorentz function program modules for fitting the peaks of 3- and 4-coordinated boron species, respectively. The fraction of four-coordinated boron species, N_4 , has been calculated from the relative peak areas, with a small correction due to the overlapping satellite transition of the 4-fold coordinated boron peak.³²

²³Na MAS NMR spectra have been measured on a Bruker Avance III 600 spectrometer. Spectra were acquired on samples rotating at 15.0 kHz, using short pulses of 1.0µs length, with a relaxation delay of 1s. The data has been fit using the Czjzek distribution model implemented in the DMfit software, considering a wide distribution of quadrupolar coupling constants C_Q , resulting in an average value $\langle C_Q \rangle$ and an average isotropic chemical shift $\langle \delta_{iso}^{23}$ Na \rangle .

 29 Si MAS NMR spectra have been obtained on an Agilent DD2 spectrometer interfaced with a 5.64 T magnet. Samples were rotated within spinners of 7.5 mm outer diameter at a frequency of 5.0 kHz. Spectra were acquired with 90° pulses of 4.5 µs length, 100-150 scans, separated by a relaxation delay of 300 s.

Unpolarized Raman spectra have been collected at room temperature over the range of 300 to 1600 cm^{-1} with a precision of $\pm 1 \text{ cm}^{-1}$, using an inVia Renishaw confocal Raman spectrometer equipped with a CCD detector. The excitation source was the 532 nm line of a green diode laser

operating at 500 mW. The measurements were performed at different positions on the sample surface to ascertain the sample homogeneity. The raw spectra were corrected for temperature and frequency-dependent scattering intensity,³³⁻³⁷ followed by a linear baseline fit. The corrected spectra were then normalized to the integrated signal intensity and deconvoluted into individual components using the OriginPro 2018b software.

2.5 Thermal analysis

Glass transition temperatures, T_g , have been measured on powdered samples (particle size range of 0.85 to 1 mm) by Differential Scanning Calorimetry (DSC; Netzsch simultaneous thermal analyzer, STA-449F Jupiter). The samples were loaded in Pt–Rh (10 wt.% Rh) pans, covered with a Pt lid, and heated in air from room temperature to 1000 °C at a rate of 10 °C/min. An empty Pt–Rh pan was used as a reference. The T_g values reported are averages of at least three measurements.

3. Results

3.1 Sulfur solubility

All the sulfur-free baseline glasses synthesized in the present study are XRD amorphous (Figure S1(a-c)) and optically transparent (Figure S2-S4). To estimate SO₃ solubility, sodium sulfate was added stepwise to the baseline glasses (starting from 0.5 mol.% SO₃) maintaining the total sodium content constant (see section 2.2), until it supersaturates in the melt and appears as a white salt layer on the glass surface. The highest concentration of SO₃ which dissolves in a given quantity (70 g) of glass without altering its amorphous nature (as analyzed by XRD analysis) is

considered to be its (experimental) SO₃ solubility. Once the SO₃ solubility limit has been reached, the excess sulfate tends to partition out of the melt in the form of a salt and floats on the melt surface. Upon quenching the melt, the salt layer forms a white powder that sticks to the surface of the transparent and XRD amorphous glass (Figures S2-S4). All the SO₃-containing glasses (below the solubility limit) are XRD amorphous, (Figure S1-d). The XRD analysis of the salt layer (Figure S1-d) reveals the formation of Na₂SO₄ (PDF# 97-006-3077) as the only crystalline phase in all the three series of glasses.

The compositional analysis of the sulfur-containing glasses has been performed only for the compositions exhibiting the (experimental) solubility limit of SO₃. Therefore, the SO₃ concentrations reported in Table 1 should be considered as the solubility limit of SO₃ in the respective glasses. The chemical analyses of the sulfur-free baseline glasses are in good agreement with the batched compositions (Figure 1 and Table S1) suggesting minimal volatilization of Na₂O or B₂O₃ from the glass melts. Therefore, all the structure–property correlations discussed in this study should be considered as a manifestation of the impact of SO₃ addition to the glasses.

Glass	[Na ₂ O]	$[B_2O_3]$	[SiO ₂]	R	K	[mol.%SO ₃]
NB-15	15	45	40	0.33	0.88	-
NB-25	25	35	40	0.71	1.14	0.90 ± 0.01
NB-30	30	30	40	1	1.33	1.70 ± 0.03
NB-35	35	25	40	1.4	1.6	1.93 ± 0.03
NB-40	40	20	40	2	2	2.82 ± 0.02
SB-75	25	75	0	0.33	0	-
SB-60	25	60	15	0.42	0.25	0.38 ± 0.03
SB-45	25	45	30	0.55	0.67	0.87 ± 0.02
SB-30	25	30	45	0.83	1.5	0.96 ± 0.02
SB-15	25	15	60	1.67	4	-
SB-0	25	0	75	-	-	-

Table 1. Glass compositions and experimentally determined maximum SO_3 solubility in the investigated glasses.

NS-20	20	15	65	1.33	4.33	-
NS-25	25	15	60	1.67	4	-
NS-30	30	15	55	2	3.67	1.93 ± 0.02
NS-35	35	15	50	2.33	3.33	2.88 ± 0.03
NS-40	40	15	45	2.67	3	3.3±0.02
NS-45	45	15	40	3	2.67	3.86 ± 0.02

As shown in Table 1, the SO₃ solubility of the investigated glasses ranges from 0.46 to 4.89 wt%. The glasses with SO₃ solubility less than 0.5 mol.% were not studied further. Although the SO₃ concentration in these glasses was above the detection limit of ICP–OES, the large RSD (relative standard deviation) value (~18%) did not allow us to measure the SO₃ content in these glasses within the range of experimental certainty.

In the NB-*x* series of glasses, SO₃ solubility increases linearly with increasing *R* (Figure S5a). In the glasses with varying SiO₂-to-B₂O₃ ratio (SB-*y*), the SO₃ solubility in glasses near the B₂O₃-rich end, i.e., 25 Na₂O-75 B₂O₃ (SB-75) and 25 Na₂O-15 SiO₂-60 B₂O₃ (SB-60) (mol.%), is ≤ 0.5 mol.% (0.46 wt.%) despite their low melting temperatures (< 1000 °C). On the other hand, SO₃ solubility in the SiO₂-rich end members, i.e., 25 Na₂O-75 SiO₂ (SB-0) and 25 Na₂O-15 B₂O₃-60 SiO₂ (SB-15) (mol.%), is zero owing to their high melting temperatures (1450-1600 °C), leading to sulfur volatilization. Preliminary results,³⁸ indicate that the rate of sulfur volatilization from the melt increases rapidly at temperatures >1300 °C, resulting in complete loss of sulfur near 1350 °C. Similar results pertaining to sulfur volatilization from the glass melts have also been reported in the literature.¹⁸ For the glasses with SiO₂ (or B₂O₃) content varying between 30-45 mol.%, the SO₃ solubility shows an incremental change by a factor of 1.13 with an increase in *K* from 0.67 to 1.5 (Table 1).

In the glasses from NS series, the SO₃ solubility is highly composition dependent. It is zero for glass 25 Na₂O-15 B_2O_3 -60 SiO₂ (NS-25) as all the sulfur volatilizes from the melt due to the

high melting temperature (>1400 °C). An increase in Na₂O/SiO₂ molar ratio from 0.54 to 1.125 results in an increase in the SO₃ solubility by a factor of ~2 (Figure S5-b). Among all the glasses investigated in the present study, the glass with composition (mol.%) 45 Na₂O–15 B₂O₃–40 SiO₂ (NS-45) exhibits the highest SO₃ solubility of 3.86 mol.%.

3.2 Structure of the baseline glasses

3.2.1 Raman spectroscopy

3.2.1.1 Band assignment

Figure 2 presents the Raman spectra of the sulfur-free baseline glasses. For the convenience of readers, the Raman spectra have been divided into three frequency regions, as described below.

(1) Low frequency region (300 to 850 cm^{-1})

In this region, the bands between 300 and 500 cm⁻¹ have been assigned to mixed stretching and bending modes of Si–O–Si and Si–O–B linkages whose frequency increases with increasing alkali content.³⁹⁻⁴² The frequency region of 550-850 cm⁻¹ corresponds to the breathing modes of metaborate units,⁴³ and other borate- and borosilicate-ring unit groups.⁴⁴⁻⁴⁶ In this region, the peak around 630 cm⁻¹ corresponds to the breathing mode of Si–O–BØ₄ linkages (Ø denotes the bridging oxygen) in danburite–like units,^{37, 47} and the band around 700 cm⁻¹ corresponds to the breathing vibrations of metaborate units.⁴³ The band at 770 cm⁻¹ has been assigned to the symmetric breathing vibrations of six-membered borate rings containing one BØ₄ unit, and this band shifts towards the lower frequency side to 750 cm⁻¹ for the borate rings containing two BØ₄ units.^{48, 49} Further, the band around 806 cm⁻¹ corresponds to the vibration of three-coordinated BØ₃ units in the boroxol rings.⁵⁰⁻⁵² For convenience the BØ₄ and BØ₃ units are henceforth labeled B⁴ and B³, where the superscript denotes the number of bridging oxygen atoms.

(2) Mid-frequency region (850 to 1200 cm^{-1})

This frequency region arises mainly due to the stretching vibrations of Si–O bonds in the Si^{*n*} units of the glass structure. Here *n* is the number of bridging oxygen atoms per Si atom ranging from 1 to 4. The bands centered around 880 cm⁻¹, 950 cm⁻¹, and 1070-1080 cm⁻¹ represent Si–O⁻ stretching vibrations of Si¹, Si² and Si³ units, respectively, while the high frequency band between 1100–1200 cm⁻¹ has been previously identified to be attributable to vibrations involving the fully polymerized Si⁴ units.^{19, 33, 40, 51} The assignment of the band between 1000 and 1050 cm⁻¹ is uncertain. It has been attributed to the stretching mode of Si–Ø in the Si tetrahedra (Si¹, Si², and Si³), or, alternatively, to the vibration in structural units associated with modifier cation.^{33, 37, 53}

(3) High frequency borate stretching region (1200 to 1600 cm^{-1})

This high frequency region represents the stretching vibrations of symmetric B^3 units and asymmetric three-coordinated boron species (such as $BØ_2O^-$ groups linked to two bridging and one non-bridging O-atoms, henceforth denoted by B^2 units, which are possibly linked to form chains.^{47, 54} In this region, the lower-frequency peak around 1400 cm⁻¹ is assigned to B^2 units linked to B^4 units, while the component near 1470 cm⁻¹ is assigned to B^2 units linked to B^3 groups.^{37, 47, 50} Yano et al.⁴⁴⁻⁴⁶ have assigned the component close to 1510 cm⁻¹ to the stretching modes of B^3 units in boroxol rings. A small peak around 1550 cm⁻¹ is observed in all the glasses and has been attributed to the molecular oxygen present in the atmosphere surrounding the glass sample while recording Raman spectra.⁵⁵

The deconvolution of Raman spectra has been performed using the procedure described by Manara et al.³⁷ and Le Losq et al.³³ and is given in the Supporting Materials section. Despite of the deconvolutions provided, these spectra are used only for the qualitative interpretation of the

glass structure and could not be used for the quantitative interpretation of the populations of silicate and borate units.

3.2.1.2 Structural analysis based on band assignment and spectral fitting

Based on the assignment and fitting of bands in the Raman spectra, the following details about the evolution in the short-to-intermediate range ordering in the structure of the investigated glasses, as a function of their composition, have been deduced.

(1) NB-x glasses

For glasses of the NB-x series, Figures 2a, 2b, and S6 suggest the following structural trends with increasing *R*:

- I. The band centered around 500 cm⁻¹, corresponding to the mixed stretching, and bending vibrations of Si–O–Si bonds, shifts towards higher frequencies.
- II. The intensity of the band at $\Box 630 \text{ cm}^{-1}$ increases, passes a maximum at R = 0.71 (NB-25) followed by a subsequent decrease. The increase in the intensity of the peak in glasses with $R \le 0.7$ can be attributed to the increasing molar concentration of B⁴ units (as also observed in ¹¹B MAS NMR, see section 3.2.2) and their tendency to connect with Siⁿ units,²⁶ thus, resulting in an increased concentration of Si–O–B⁴ linkages in the glass structure. The decrease in the Si–O–B⁴ linkages in the glasses with R > 0.71 may be attributed to the increasing fraction of three-coordinated borate units associated with NBOs (i.e., B² units) at the expense of B⁴ units. This is evident from the shifting of the 770 cm⁻¹ band towards lower frequency (up to $\Box 748 \text{ cm}^{-1}$) with reduced intensity, and simultaneous increasing intensities of bands at $\Box 690 \text{ cm}^{-1}$ (B² units) and $\Box 1470 \text{ cm}^{-1}$ (corresponding to B²–B³ linkages). ^{37, 56} These results are in agreement with the ¹¹B MAS NMR results, as the fraction of four-coordinated boron (as deduced from ¹¹B MAS NMR spectra) is the highest in the glass at R = 0.71 (Table 2).

- III. The band at ~806 cm⁻¹, corresponding to the symmetric stretching mode of the boroxol rings, appears in the glass NB-15 (with R = 0.33) and diminishes with an increase in R, indicating a decrease in the concentration of boroxol rings in the glass structure. This structural feature is also supported by the gradual decrease in the intensity of the band at ~1510 cm⁻¹.^{37, 44-46}
- IV. The gradual decrease in the concentration of B^2-B^4 linkages with increasing *R*, as indicated by a decreasing intensity of the band near ~1400 cm⁻¹, further supports the decreasing concentration of B^4 units, and their low tendency to bind with other anionic borate species.



Figure 2. Raman spectra of (a) NB-*x*, (b) SB-*y*, and (c) NS-*z* series of sulfur-free baseline glasses. The corresponding variations of structural linkages are shown as (b), (d) and (f).

- V. The steep increase in the concentration of B^2-B^3 linkages in the glasses with $R \ge 0.71$, as inferred from the increase in intensity of ~1470 cm⁻¹ band,^{37, 43, 47} can be attributed to the cumulative decrease in the concentration of Si–O–B⁴, B²–B⁴, and boroxol units in the glass structure due to increase in the Na₂O content. The increase in concentration of B² units in this composition region is also indicated by the ¹¹B MAS NMR spectra of these glasses (see section 3.2.2).
- VI. With reference to the structural evolution in the silicate network in these glasses, the spectra of NB and NS glasses show a steep rise in the concentration of the Si³ and Si² units (~ 1070 and 950 cm⁻¹, respectively) with increasing R. This change in intensity, together with the observed shift in the 500 cm⁻¹ band towards higher frequency (as discussed in point I), indicates that the degree of polymerization in silicate network decreases with increasing *R*, as evident from Figure 2b.^{37,47}

(2) SB-y glasses

Figure 2c and 2d present the Raman spectra and corresponding structural linkages in the SB– y series of glasses, respectively, while the deconvoluted Raman spectra are shown in Figure S7. The structural information derived from the Raman spectra of these glasses has been summarized below.

I. The Raman spectrum of sodium silicate glass (SB-0) exhibits a characteristic band at $\Box 542$ cm⁻¹ with a shoulder at 596 cm⁻¹ (associated with combinations of bending and stretching modes involving Si–O–Si linkages), a low intensity band $\Box 785$ cm⁻¹ (representing Si–O–Si bending modes), a small hump around 949 cm⁻¹ (Si² units) and a high intensity band at $\Box 1100$ cm⁻¹ (Si³ units).^{33, 39, 41, 57} In agreement with the literature,^{44, 48, 51} the spectrum of sodium borate (SB-75) glass exhibits the characteristic peaks at 498, 773, 950, 1115 cm⁻¹ and a cupola shaped band

centered around 1444 cm⁻¹. The band around 498 cm⁻¹ corresponds to the B–O–B stretching vibration of B⁴ units.^{48, 52} The prominent peak at 773 cm⁻¹ corresponds to the symmetric breathing vibrations of the six–membered borate rings containing one BØ₄ unit as identified in the NB-*x* series. The peak around 950 cm⁻¹ is associated with pentaborate units and the peak at 1115 cm⁻¹ indicates the presence of diborate units in the glass network.⁴⁸ The broad band centered around 1444 cm⁻¹ in the high frequency region represents the stretching vibrations B² units linked to B⁴ units and B² units linked to B³ units.

- II. The substitution of SiO₂-for-B₂O₃ in the glasses reveals a band at ~493 cm⁻¹ corresponding to Si-O-Si bending vibrations, and a broad band in the frequency range of 850-1200 cm⁻¹ associated with Si-O symmetric stretching vibrations of Siⁿ units. An increase in *K* results in an increase in the peak area of Si-O symmetric stretching region along with a concomitant decrease in the peak area corresponding to the high frequency borate stretching region (1250-1600 cm⁻¹).⁴⁷
- III. The intensity of the band ~630 cm⁻¹ increases steeply with increasing *K* up to 1.5, and then changes little up to K = 4. The initial increase is attributed to the increasing SiO₂ content in the glasses and their association with B⁴ units. The increase in the Si–O–B⁴ linkages with an increase in *K* is also illustrated by the ¹¹B MAS NMR spectra (see section 3.2.2).
- IV. The intensity of the Si³ (\Box 1070 cm⁻¹) band increases with increasing *K*, reflecting the increase in silica content.⁴⁷ The intensity of the band at 950 cm⁻¹ attributed to the Si² units appears very low throughout the series. Unlike the situation in the NB-*x* and NS-*z* glasses (see below), the Raman data does not give a clear evidence of dramatic changes in the degree of silicate polymerization with increasing *K*.³⁷

According to Dell–Yun–Bray (DYB) model,²²⁻²⁴ the silicate network in the Na₂O–B₂O₃–SiO₂ glasses should be fully polymerized up to K=0.67, as Na⁺ is supposed to solely act as the charge

compensator for the B^4 units. Nevertheless, this is not the case in the present study, as the presence of Si³ units in the glasses SB-60 (K = 0.25) and SB-45 (K = 0.67) is evident from the presence of band near 1070 cm⁻¹ in their Raman spectra (Figure 2c). This conclusion is further corroborated by the ²⁹Si MAS NMR data reported in the section 3.2.3. Our results are more consistent with Bunker et al.,58 Wang et al.,59 and Martens and Müller-Warmuth,60 who demonstrated the formation of NBOs in silicate and borate network in the glasses from Region I and II of the DYB model. The initial subtle decrease in the relative area ratio $\frac{Si^4}{Si^1+Si^2+Si^3}$ with K $(\leq 0.67 \text{ for SB-60})$ (Figure 2d) is attributed to the fact that although Na⁺ predominantly interacts with the borate network, some Na⁺ interacts with the silicate network and facilitates creation of NBOs.⁵⁸ In the region where K > 0.67, the relative ratio $\frac{Si^4}{Si^1 + Si^2 + Si^3}$ decreases abruptly with increasing K (up to 4), due to the increasing concentration of excess Na^+ (remaining after charge compensation of the B⁴ units) available to create NBOs in the silicate network. This observation is consistent with DYB model,²⁴ according to which Na⁺ acts as a modifier in Regions III and IV of the composition diagram, i.e., in the glasses SB-30 and SB-15, respectively, as shown in Figure 1.

V. The decreasing concentration of boroxol rings, B²–B⁴, and B²–B³ linkages is due to the decreasing B₂O₃ content in the glasses. The ¹¹B MAS NMR analysis (section 3.2.2) suggests that the contribution of B² units to the borate inventory remains relatively low within the SB-y series.
 (3) NS-z glasses

Figure 2e presents the Raman spectra of NS-*z* glasses with characteristic bands for danburitelike ring structures (\Box 630 cm⁻¹), borate rings associated with two B⁴ units (750 cm⁻¹), Si² (\Box 950 cm⁻¹), Si³ (\Box 1070 cm⁻¹), and B² units (1470 cm⁻¹)). The corresponding structural linkages and deconvoluted Raman spectra are shown in Figures 2f and S8, respectively. The following structural information can be derived from the Raman spectra of these glasses.

- I. As Na₂O/SiO₂ ratio increases from 0.31 to 1.12, the intensity of the band ~630 cm⁻¹ decreases while that of ~1470 cm⁻¹ band increases, indicating the decrease in Si–O–B⁴ linkages and an increase in B^2 –B³ linkages in the glass structure. The decrease in the Si–O–B⁴ linkages with increasing Na₂O/SiO₂ ratio is due to the increasing concentration of excess Na⁺ available favoring the formation of B² units in lieu of B⁴ groups This trend is evident from the increasing intensity of the band ~1470 cm⁻¹, and also in agreement with the ¹¹B MAS NMR results (section 3.2.2).
- II. Regarding the silicate network in these glasses, the intensity of Si^2 band increases at the expense of the Si^3 bands as the Na₂O/SiO₂ ratio increases, documenting the depolymerization in the silicate network. This is attributed to the increasing Na₂O/SiO₂ ratio, furnishing an increased amount of modifier oxide available for NBO formation.
- III. The decreasing intensity of the band ~1400 cm⁻¹ (B⁴-B² linkages), coupled with the increasing intensity of the band ~1470 cm⁻¹ band (B²-B³ linkages), as shown in Figure 2f, reflects the tendency of anionic borate formation in the form of B² rather than B⁴ units in the glasses with high R values.

Thus, the increasing Na₂O/SiO₂ ratio in the NS-*z* series of glasses induces strong depolymerization in their silicate and borate networks. The observed depolymerization of NS-*z* glasses is consistent with DYB model²⁴ and Bunker et al.⁵⁸ which predicts the formation of NBOs in the silicate as well as borate network in Region 4 of the composition diagram (Figure 1).

3.2.2 ¹¹B MAS NMR

Figure 3 shows the ¹¹B MAS NMR spectra of all the baseline glasses. They reveal two salient features: (i) a broad, structured resonance in the chemical shift region 10-20 ppm, attributed to three-coordinated boron (B(III)) sites, and (ii) a relatively narrow peak around 0 ppm, corresponding to four-coordinated boron (B(IV)) sites.^{8, 25, 26, 61} The lineshapes attributed to the B(III) units are affected by the interaction of the ¹¹B nuclear electric quadrupole moment with the strong local electric field gradients created at the boron nucleus by this trigonal environment. In this case, the effects on the ¹¹B MAS NMR spectra must be calculated by second-order perturbation theory, resulting in only partially narrowed MAS NMR spectra, from which the interaction parameters, isotropic chemical shift, δ_{iso}^{cs} , quadrupolar coupling constant C_0 , and the electric field gradient asymmetry parameter, η_0 , can be determined by simulation. In the present case, the simplest approach towards a successful lineshape deconvolution conducted at three different magnetic field strengths (16.4 T, 14.1 T, and 5.64 T) assumes the presence of two distinct B(III) components and up to two distinct B(IV) components (see Figure S9-14 for some examples). Extensive simulation studies based on different models indicate that there are multiple ways of getting acceptable two-component fits for the signal belonging to the B(III) units. The results of the lineshape analysis summarized in Table 2 represent the two-component deconvolution model yielding the most consistent results at different field strengths. Here we would like to highlight that the asymmetry parameters listed in Table 2 should be viewed as apparent values, which are also influenced by the existence of distributions of isotropic chemical shifts and C_0 -values. Nonetheless, since the scientific outcomes of our study depend only on an accurate determination of N_4 values, and all the deconvolution models considered in this study yield similar N_4 values within experimental error, the conclusions of our work remain unaffected by this issue. In all the glasses with R < 1.5, the isotropic chemical shifts of the B(III)

components are found near 18.2 ± 0.4 ppm, labeled B(III)-1, and 15.8 ± 0.4 ppm, labeled B(III)-2. Following the arguments presented previously, site B(III)-1 may be identified with B(III) units contained within ring structures, and B(III)-2 may be associated with non-ring structures, and/or D(III)

B(III)	species	linked	to	silicon.	For
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Gammela		B(I	II) -1			B(III) -2				V)-1	B(IV)-2		
Sample ID	f(%)	$\frac{\delta_{iso}{}^{cs}}{(ppm)}$	C _Q (MHz)	$\eta_{ m Q}$	f(%)	δ _{iso} ^{cs} (ppm)	C _Q (MHz)	$\eta_{ m Q}$	<i>f</i> (%)	δ _{iso} ^{cs} (ppm)	f(%)	δ _{iso} ^{cs} (ppm)	N_4
NB-15	36	17.8	2.60	0.30	27	15.9	2.61	0.42	37	-0.04			0.37 [0.37]
NB-25	32	18.3	2.60	0.34	7	15.5	2.44	0.31	41	0.43	20	-1.14	0.61[0.61]
NB-30	28	18.4	2.59	0.35	6	15.5	2.45	0.30	43	0.42	23	-1.18	0.66
NB-35	29	18.5	2.57	0.32	13	16.1	2.58	0.24	43	0.37	15	-1.5	0.58
NB-40	28	18.5	2.35	0.38	21	17.4	2.37	0.66	51	0.58			0.51
SB-75	53	18.2	2.60	0.29	10	15.6	2.40	0.44	37	0.72			0.37 [0.37]
SB-60	44	18.3	2.60	0.29	11	16.0	2.45	0.30	44	0.48			0.44[0.47]
SB-45	35	18,3	2.60	0.26	13	16.0	2.45	0.41	53	0.20			0.53[0.57]
SB-30	28	18.3	2.60	0.34	7	15.5	2.44	0.31	40	0.42	26	-1.14	0.66[0.71]
SB-15	14	17.9	2.47	0.38	9	16.2	2.41	0.69	77	-0.66			0.77 [0.77]
NS-20	9	17.8	2.48	0.38	12	15.0	2.40	0.68	78	-1.31			0.78 [0.78]
NS-25	14	17.9	2.47	0.38	9	16.2	2.41	0.69	77	-0.66			0.77 [0.77]
NS-30	21	17.9	2.47	0.38	7	16.2	2.41	0.69	72	-0.26			0.72[0.75]
NS-35	31	18.2	2.45	0.42	7	17.0	2.40	0.69	61	0.28			0.61[0.63]
NS-40	36	18.2	2.37	0.44	10	17.0	2.37	0.67	54	0.40			0.54[0.54]
NS-45	-	-	-	-	53	18.2	2.39	0.57^{a}	47	0.60			0.47[0.46]
NB40-3S	16	18.7	2.57	0.42	24	17.6	2.58^{b}	0.48	46	0.48	12	-1.26	0.58[0.58]
NS35-3S	13	18,6	2.55	0.47	20	17.5	2.63 ^b	0.55	53	0.11	14	-1.73	0.67[0.69]
NS40-3.5S	26	18.7	2.62	0.50	14	17.5	2.59^{b}	0.55	31	0.43	29	-0.86	0.60[0.59]
NS45-4S	38	18.4	2.50	0.55	10	17.3	2.56^{b}	0.56	34	0.65	18	-0.90	0.52[0.53]

Table 2. Fitting parameters of ¹¹B MAS NMR in the studied glasses, including fraction of each species $f (\pm 1 \%)$, isotropic chemical shift $\delta_{iso}^{cs} (\pm 0.5 \text{ ppm})$, quadrupolar coupling constant, $C_Q (\pm 0.10 \text{ MHz})$, $\eta_Q (\pm 0.05)$, and overall N_4 values ($\pm 1 \%$). For the latter, values independently measured at 5.7 T are listed in brackets.

^a B^3 and B^2 units inseparable by simulation; equal parts assumed; ^btentatively assigned to B^2 units, albeit uncertain.

both of these species, the number of bridging oxygen atoms is three, which characterizes them as B^3 units in terms of their connectivity.

In glasses with R > 1.5, the B(III)-1 component is characterized by a distinctly smaller C_0 value (2.45 MHz), and the B(III)-2 unit is characterized by a distinctly larger asymmetry parameter near 0.6 to 0.7. The latter value signifies B(III) species in which only two oxygen atoms are bridging, and one is a non-bridging terminal one as, for example, found in alkali metaborates. These species can thus be denoted as B^2 units. For such B^2 units the local symmetry of the electron distribution around the boron atoms deviates strongly from the trigonal D_{3h} symmetry, which manifests itself in the larger asymmetry parameter (0.6 to 0.7) compared to the situation for the B³ units (where $\eta_Q = 0$ would be expected for the case of perfect D_{3h} symmetry). Quantitative estimates for these "asymmetric" three-fold boron units are listed in Tables 2 and 3. Throughout all the glasses with R > 1.5, their overall contribution to the respective boron inventory appears to be non-negligible, and their contribution increases with increasing R value, consistent with the Raman data (Section 3.2.1). For the glasses with the highest R values, the signal deconvolution in terms of two B(III) components is ambiguous, and in glass NS-45 (R =3), it is possible to simulate the spectrum just by one component, having lineshape parameters intermediate between those of B^2 and B^3 units. We tentatively interpret this spectrum in terms of about equal contributions; however, it is also conceivable that all of the three-coordinate boron species in this glass are of the B^2 type. The trend of increasing B^2 unit contributions to the boron speciation with increasing R is also suggested by the Raman scattering data (see section 3.2.1).

The four-coordinated boron species, B(IV), can be simulated in most of the glasses by a simple Gauss-Lorentz curve. In some glasses, the curves are slightly asymmetric, which can be accounted for by a two-component deconvolution. Because of the poor resolution, this analysis

may appear somewhat arbitrary; we will, therefore, not make specific assignments based on these deconvolution components. Nevertheless, the average chemical shift $<\!\delta_{\!_{\rm ISO}}B^4\!\!>$ is a parameter whose compositional dependence can be discussed. Here it should be noted that we have assumed all four oxygen atoms to be bridging, i.e., B⁴ species. Previous *ab-initio* calculations and experimental results⁶² have shown that $\langle \delta_{so}B^4 \rangle$ is sensitive to the linkages to other network formers. Compared to the connectivity with trigonal B³ units, linking to Si⁴ units produces a shift towards more negative frequencies, whereas linking to anionic B⁴ units produces a shift towards more positive values. Based on empirical chemical shift trends on sodium borosilicate glasses, as well as the whole body of structural information available in this system, $^{22-29, 58, 60, 63-74}$ we further infer that connectivity to other anionic species such as B² and Si³ units will also produce chemical shift changes towards more positive values. In general, although a given B^4 unit may simultaneously participate in different linkages with varying numbers from one site to the next (e.g., B_{4B}^4 , B_{1Si3B}^4 , B_{2Si2B}^4 etc.), whose chemical shifts are distinct, these units do not lead to resolved peaks in the spectra. Bearing these limitations in mind, the compositional trends of the ¹¹B NMR parameters within the three distinct compositional series can be summarized as follows:

(1) Within the NB-*x* series, *R* increases while *K* decreases as the Na₂O/B₂O₃ ratio is systematically increased at fixed SiO₂ content. Due to these counter-acting effects, *N*₄ is found to be only weakly dependent on composition, showing the expected increase with increasing *R* value below 0.7, and only a slight decrease at higher *R* value. This behavior is consistent with the DYB models.²²⁻²⁴ At the highest *R* value (= 2) for this series, the spectra show the evidence of B² units, but their concentration is found to be lower than that predicted in literature.²²⁻²⁴ For similar reasons, the $<\delta_{so}B^4>$ parameter is only weakly dependent on alkali content within this series, for

glasses with $R \le 1.4$. The positive $\langle \delta_{iso}B^4 \rangle$ value observed in the glass with the highest Na₂O content (*K*=*R*=2)

Table 3. Glass compositions (mole %), compositional parameters $K = [SiO_2]/[B_2O_3]$ and $R = [Na_2O]/[B_2O_3]$, experimental N_4 (±0.02) and N_2 (±0.1) values, and corresponding values predicted by the YDB model²²⁻²⁴, average ¹¹B isotropic chemical shifts $<\delta_{iso}>^{11}B(IV)$ of the B(IV) species (±0.05 ppm), for the present sulfur-free baseline glasses and four glasses with SO₃ contents > 3 mol.%. Additional data* from Stone-Weiss et al.⁶²has been included.

Glass	[Na ₂ O]	$[B_2O_3]$	[SiO ₂]	K	R	$N_{4 \exp}$	$N_{ m 4\ pred.}$	$N_{2 \exp}$	$N_{2 \mathrm{\ pred}}$	$<\delta_{iso}>^{11}B(IV)$
NB-15	15	45	40	0.89	0.33	0.37	0.33	0	0	-0.04
NB-25	25	35	40	1.14	0.71	0.61	0.55	0	0.1	-0.03
NB-30	30	30	40	1.33	1	0.66	0.54	0	0.22	-0.16
NB-35	35	25	40	1.6	1.4	0.58	0.52	0	0.38	-0.11
NB-40	40	20	40	2	2	0.51	0.51	0.21	0.47	0.42
SB-75	25	75	0	0	0.33	0.37	0.33	0	0	0.7
SB-60	25	60	15	0.25	0.42	0.44	0.42	0	0	0.5
SB-45	25	45	30	0.67	0.56	0.53	0.54	0	0.01	0.2
SB-30	25	30	45	1.5	0.83	0.66	0.57	0	0.12	-0.19
SB-15	25	15	60	4	1.67	0.77	0.7	0.09	0.23	-0.66
SB-0	25	0	75	-	-	-	-	0	0	-
NS-20	20	15	65	4.33	1.33	0.78	0.75	0.12	0.13	-1.31
NS-25	25	15	60	4	1.67	0.77	0.7	0.09	0.23	-0.66
NS-30	30	15	55	3.67	2	0.72	0.66	0.07	0.34	-0.3
NS-35	35	15	50	3.33	2.33	0.61	0.61	0.07	0.37	0.3
NS-40	40	15	45	3	2.67	0.54	0.56	0.2	0.4	0.4
NS-45	45	15	40	2.67	3	0.47	0.51	0.25^{a}	0.43	0.6
NB40-3S	40	20	$40+2.8SO_3$	2	2	0.58	0.51	$0.24/0^{b}$	0.47	0.12
NS35-3S	35	15	50+2.9SO ₃	3.33	2.33	0.67	0.61	0.20	0.37	-0.27
NS40-3.5S	40	15	45+3.3SO ₃	3	2.67	0.60	0.56	0.14	0.4	-0.19
NS45-4S	45	15	40+3.9SO ₃	2.67	3	0.52	0.51	0.10	0.43	0.11
PB-0*	25	30	45	1.5	0.83	0.63	0.57	0	0.12	-0.21
MB-0*	25	25	50	2	1	0.67	0.59	0	0.16	-0.65
PA-0*	25	20	55	2.75	1.25	0.71	0.63	0	0.19	-0.38

^a B^3 and B^2 units inseparable by simulation; equal amounts assumed, ^b presence of B^2 units uncertain; two scenarios considered.

may be attributed to the connectivity of these B^4 species with other anionic species such as Si^3 and B^2 which are highly concentrated in this glass.

(2) Within the SB-y series, R and K increase simultaneously at fixed Na₂O content with decreasing v. In good quantitative agreement with the DYB predictions, $^{22-24} N_4$ strongly increases with increasing SiO₂/B₂O₃ ratio. At the highest R value (R = 1.67, K = 4), the spectra show evidence of B² units. However, again, their concentration is lower than predicted by DYB.²²⁻²⁴ The isotropic chemical shift of the B^4 units (calculated as a weighted average in all those cases where two B^4 deconvolution components were assumed) decreases monotonically with increasing K. In conjunction with the previous *ab initio* calculations (0.6 ppm for a $B_{3B(IIDB(IV))}^4$ and -2.3 ppm for a B_{4Si}^4 environment),⁶² we interpret this trend to reflect the successive replacement of B–O–B linkages by B–O–Si linkages as K increases, assuming these connectivities are largely driven by statistical probabilities. In the sample with the highest Kvalue (SB-15, K = 4) the most negative $\langle \delta_{iso}B^4 \rangle$ value of -0.66 ppm is measured, in accordance with the highest probability of B^4 -Si⁴ connectivity. The extreme value of -2.3 ppm for a B^4_{4Si} is not reached because other linkages, i.e., B^4-B^3 and B^4-Si^3 , still contribute to the experimental shift measured. Our interpretation is in agreement with the previously reported studies on sodium borosilicate glasses.^{25, 26, 59, 60}

(3) Within the NS-*z* series, the effect of increasing alkali ion content in high-*K* glasses is monitored. Here the main effect is the decrease in *K* and an increase in *R* with increasing alkali ion content, which results in a successive replacement of B⁴ units by B² units. The observed increase in the $\langle \delta_{iso}B^4 \rangle$ parameter with increasing *R* may again be attributed to the increasing B⁴ connectivity with anionic Si³ and B² units, as their concentration increases with increasing *z*.

Figure 4 and Table 3 illustrate that the N_4 values for the entire set of glasses agree quite well with the DYB quantitative predictions.²²⁻²⁴



Figure 4. Comparison of the experimental N_4 values with those predicted using the DYB model.²²⁻²⁴ Black circles: NB series, green squares: SB series, blue triangles, NS series, orange diamonds: results from Stone-Weiss et al.⁶². Red symbols denote results from the SO₃ containing glasses with SO₃ contents \geq 3 mol.%.

This is not the case, however, for the concentrations of the B^2 units. This discrepancy arises because the DYB model may underestimate the fraction of NBOs created at the silicate units. Nevertheless, the general compositional trends are still reproduced by the data.

3.2.3. ²⁹Si MAS NMR

Figure 5 summarizes the ²⁹Si MAS NMR data of the sulfur-free baseline glasses. In some cases, such as the borate-free glass SB-0, two well-resolved components at -90.7 and -103.8 ppm are observed, which are easily assigned to Si³ and Si⁴ units, respectively. For most of the glasses, however, the spectra are poorly resolved, indicating that there is a wide distribution of isotropic chemical shifts that makes it impossible to arrive at an unambiguous deconvolution.

Nevertheless, regardless of the choice of the deconvolution model, the average chemical shift $<\delta_{so}^{29}$ Si> can be determined without ambiguity. The greatest influence on the ²⁹Si chemical shift arises from the NBO species, such as they are found in Si³ units. It is also well-known that the chemical shift of the Si⁴ units in silicate glasses increases when these units are connected with Si³ species.⁷⁵ For example, the Si⁴ species in glass SB-0 is found at -103.8 ppm instead of -110 ppm in glassy silica. Likewise, Si⁴ units connected to B⁴ units in borosilicate are displaced to higher resonance frequencies.⁶² Recent *ab initio* calculations indicate that the connectivity to the anionic B⁴ units produces a high-frequency shift by about 5-10 ppm, even though there is no linear dependence of this shift on the number of such linkages.⁵⁹ In this way the parameter $<\delta_{so}^{29}$ Si> reflects the effect of (1) directly bonded NBOs (the Si³ and Si² units), and (2) the linkage of the Siⁿ species with other anionic units such as Si³, Si², B⁴ and B². In contrast, the connectivity to the (neutral) B³ species has no effect on $<\delta_{so}^{29}$ Si>.⁶⁰

For the glasses in the NB-*x* and NS-*z* series, $\langle \delta_{iso}^{29}Si \rangle$ strongly increases with increasing Na₂O content. This trend mostly reflects the increased contribution of Si³ (and some Si² in glasses containing \geq 35 mol% Na₂O) units to the silicon inventory. In contrast, $\langle \delta_{iso}^{29}Si \rangle$ remains approximately constant in the SB-*y* glasses. This can be understood as the result of the following two counteracting effects upon the concentration of Si³ units: (1) the decreased Na₂O/SiO₂ ratio associated with the increase in *K* tends to decrease the fraction of NBOs available for the modification of silicate network; (2) the increase in *K* also implies that the concentration of the B⁴ units, which scavenge the network modifier for charge compensation, decreases with increasing *K* (because of the decreasing boron content), favoring an increase in the relative concentration of the Si³ units. This effect is also confirmed by the Raman scattering results. As a

result of these two counteracting effects, the ²⁹Si chemical shifts are only weakly dependent on composition within



Figure 5. ²⁹Si MAS NMR data of the sulfur-free baseline glasses. The dashed vertical line indicates the chemical shift of silica (Si⁴ units only, -110 ppm).

the SB-*y* series of glasses. Interestingly, the formation of B–O–Si linkages in the SB-*y* glasses at R = 0.42 (SB-60 glass) contrasts with the DYB model,^{22, 24} which predicts the formation of borosilicate super-structural units (B–O–Si linkages) in sodium borosilicate glasses with R > 0.5. Further, our results are in agreement with Stebbins and coworkers,²⁶ who have demonstrated a considerable degree of Si/B mixing in borosilicate glasses with R < 0.5 through ¹⁷O 3QMAS NMR spectroscopy. Furthermore, the B³ resonance does not show any significant change in line-shape, which indicates that the short–range order around three-coordinated boron remains similar across the compositional range investigated.⁷⁶ A rough estimate of the average number of NBOs per Si unit can be obtained from the "unused balance" of all of the oxide ions introduced by the network modifier Na₂O that is left over after subtracting the sodium equivalent needed for the creation of anionic B⁴ or B² units, as shown in Equation 3 (see Table 4):

$$\langle O/Si \rangle = \{ [2 \times Na_2O] - 2 \times [B_2O_3] \times (N_4 + N_2) \} / [SiO_2].$$
 (3)

Figure 6 illustrates that this parameter shows a linear correlation with the average ²⁹Si chemical shift measured for the current samples under study, confirming conclusions of the present study. The linear regression of this plot indicates that introduction of one unit of NBOs per silicon produces a change in $\langle \delta_{iso}^{29}Si \rangle$ by 10 ± 2 ppm. This value is close to the chemical shift difference of 13.1 ppm between the Si⁴ and the Si³ units in the pure sodium silicate glass SB-0. Finally, the large difference (9.2 ppm) in the $\langle \delta_{iso}^{29}Si \rangle$ values measured for the two glasses with NBO/Si = 0, namely NB-15 and SB-60 arises from their markedly different average numbers of Si⁴–B⁴ linkages: The [B⁴]/[Si] ratios in NB-15 and SB-60 are 0.8 and 3.5, respectively. Thus, the probability of a B⁴ linkage per Si is much lower in NB-15 than in SB-60 glass, offering a rationale for the large chemical shift difference.



Overall, the combined interpretation of the Raman scattering, ¹¹B and ²⁹Si MAS NMR data suggest the following structural trends:

- (1) Increasing *R* in NB-*x* glasses at fixed SiO_2 content produces a significant depolymerization of the silicate network, and at high *R* values significant amounts of B^2 units are formed.
- (2) Increasing *R* in NS-*z* glasses at fixed B_2O_3 content leads to a similar result. In addition, anionic B^2 units are increasingly formed at the expense of B^4 units.
- (3) Increasing *K* in SB-*y* glasses at fixed Na₂O content promotes the formation of Si–O–B⁴ linkages, while having relatively little impact on the average state of network polymerization.

Based on the average coordination numbers of the boron and silicon network forming units

(NFUs), we can deduce an average network connectivity by quantifying the average fraction of

bridging oxygen species per NFU using the Equation 4:

$$= \{2 \times [B_2O_3] \times (4 \times [N_4] + 3 \times N_3 + 2 \times N_2) + [SiO_2] \times (4 - \langle O/Si \rangle)\} / \{[2 \times [B_2O_3] + [SiO_2]\} (4) \}$$

Table 4. Glass compositions (mole %), isotropic ²⁹Si chemical shifts $\langle \delta_{iso}^{29}Si \rangle$ (±0.5 ppm), average number of NBOs per Silicon $\langle O/Si \rangle$ values (±0.05) deduced from eqn. (4), average NFU coordination number $\langle n \rangle$ (±0.02), calculated from eqn. (5), glass transition temperatures T_g (±1 °C) and average ²³Na chemical shift. $\langle \delta_{iso}^{23}Na \rangle$ (±0.5 ppm) for the present sulfur-free glasses and four glasses with SO₃ contents > 3 mol.%. Additional data* from Stone-Weiss et al.⁶² has been included.

Glass	[Na ₂ O]	$[B_2O_3]$	[SiO ₂]	<δ _{iso} ²⁹ Si>	<o si=""></o>	<n></n>	T _g /K	<δ _{iso} ²³ Na>
NB-15	15	45	40	-102,3	0	3,56	499	-11.8
NB-25	25	35	40	-92,6	0,18	3.69	534	-8.2
NB-30	30	30	40	-87,6	0.51	3.59	504	-5.0
NB-35	35	25	40	-82,2	1.02	3.32	473	-0.5
NB-40	40	20	40	-82,9	1.26	3.03	434	1.8
SB-75	25	75	0	N.D.	0	3.37	480	N.D.
SB-60	25	60	15	-93,1	0	3.50	499	-8.3
SB-45	25	45	30	-94,7	0.11	3.61	524	-8.0
SB-30	25	30	45	-92,5	0.26	3.68	543	-8.0
SB-15	25	15	60	-93,1	0.40	3.62	537	-4.1
SB-0	25	0	75	-95,8	0.67	3.33	496	-2.2
NS-20	20	15	65	-96.8	0.20	3.79	573	-8.1
NS-25	25	15	60	-93,1	0.40	3.62	538	-4.1
NS-30	30	15	55	-89	0.66	3.45	496	-4.2
NS-35	35	15	50	-84,9	0.99	3.21	467	-1.5
NS-40	40	15	45	-82,6	1.28	2.97	437	-0.7
NS-45	45	15	40	-79.2	1.70	2.69	404	2.0
NB40-3S	40	20	$40+2.8SO_3$	-82.2	$1.03/1.27^{a}$	3.09	438	-3.5
NS35-3S	35	15	$50+2.9SO_{3}$	-92.0	0.76	3.25	492	-4.2
NS40-3.5S	40	15	45+3.3SO ₃	-85.0	1.14	3.02	448	-3.0
NS45-4S	45	15	$40+3.9SO_3$	-83.1	1.59	2.87	421	-0.9
PB-0*	25	30	45	-91.9	0.27	3.67	558	-4.8
MB-0*	25	25	50	-92.1	0.33	3.67	560	-3.0
PA-0*	25	20	55	-91.3	0.39	3.65	542	-5.2

^atwo scenarios considered; the second value assuming the absence of B^2 units in this glass. ND: not determined.

The values of $\langle n \rangle$ are listed in Table 4. As shown in Figure 7, they are universally correlated with the values of the glass transition temperature (T_g) for all the glasses, including a set previously studied in our laboratory.⁶³ This correlation also includes the SO₃ containing glasses discussed below (red data points in Figure 7), for which the NMR analysis reveals that the NFU average coordination number increases relative to the one found in SO₃-free reference glasses (see below).



Figure 7. Correlation between T_g and average connectivity $\langle n \rangle$ in the sodium borosilicate glasses, as obtained from MAS NMR analysis. Red symbols denote results from the SO₃ containing glasses with SO₃ contents \geq 3 mol.%.

*3.2.4.*²³*Na MAS NMR*

Figure 8 summarizes the results from ²³Na MAS-NMR for the three glass systems under investigation. The spectra display the typical lineshape observed for quadrupolar nuclei requiring analysis in terms of second-order perturbation theory, in the presence of a wide distribution of electric field gradients and magnetic shielding effects. The Czjzek model, as implemented in the DMfit software, was employed to analyze these lineshapes in terms of average isotropic chemical shifts, $\langle \delta_{\rm iso}^{\rm cs 23} Na \rangle$ (listed in Table 4) and nuclear electric quadrupolar coupling constants $\langle C_Q \rangle$ near 2.0 to 2.4 MHz. The following trends can be identified: Within the NB-*x* and NS-*z* series, a systematic shift towards higher frequencies is observed, reflecting the increase in *R* with increasing



Figure 8. ²³Na MAS NMR spectra of the sulfur-free baseline glasses.

sodium content. This chemical shift change signifies two effects, which are impossible to separate: (1) a systematic change in the distribution of anionic species interacting with the cations, and (2) an overall increase in the number of Na^{+...}O^{...}Na⁺ contacts. While in glasses with low *R* values, the anionic charge compensation proceeds mostly via B⁴ units, interactions with NBOs associated with Si³, Si², and B² units dominate at higher sodium content. At the same time, the number of shared interactions with NBOs (i.e., Na^{+...}O^{...}Na⁺ contacts) keeps increasing.

Within the SB-*y* series, which is characterized by a systematic change in B_2O_3/SiO_2 ratio at fixed Na⁺ content, the change in chemical shift is much less pronounced. For glasses in this compositional series, the charge compensation of the Na⁺ is dominated by the B⁴ units, at least in glasses with *R* < 1. A chemical shift change is only noted in the high-SiO₂ glasses (SB-0 and SB-15), in which the charge of Na⁺ must be at least partly compensated by NBO species bound to either Si³ or B² units. As noted before, the interaction with NBOs shifts the resonance line to higher frequency, indicating a stronger bond covalency, and/or stronger Na^{+…}O[…]Na⁺ contacts.

3.3 Structure of the sulfur-containing glasses

3.3.1 Sulfur speciation in glasses

Sulfur is known to exist in the glasses with valence states ranging from S^{2-} (sulfide) to S^{6+} (sulfate), depending upon the oxidizing/reducing conditions of the glass melt.¹⁸⁻²⁰ Polysulfide chains or rings would give rise to S–S stretching modes in the region 300-460 cm⁻¹, and for SO₃²⁻ (sulfite) groups two closely spaced bands at 950-970 and 970-990 cm⁻¹ would be expected.⁷⁷⁻⁷⁹ For the glasses investigated in the present study, we did not find any evidence of sulfur speciation with oxidation state other than +6, i.e., sulfur is exclusively found in the form of sulfate species. A comparison of Raman spectra of the baseline and sulfur-containing NB-*x*

glasses as a representative example to depict the speciation of sulfur in the investigated glasses has



representative example; (b) Comparison of the relative area ratio $Si^4/(Si^3+Si^2+Si^1)$ for baseline and sulfur-containing NB-*x* glasses; and (c) Peak area plots of Si¹, Si² and Si³ units in sulfur-free baseline and sulfur-containing NB-*x* glasses.

been shown in Figure 9(a). Two new bands can be seen to evolve in the Raman spectra of sulfurcontaining glasses: the band at 469 cm⁻¹ corresponding to asymmetric S–O bending modes, and a band at 988 cm⁻¹ attributed to symmetric O–S–O stretching modes. While the group theoretical analysis predicts four vibrational modes assigned as: v₁ (symmetric S–O stretching modes) \Box 990 cm⁻¹; v₂ (symmetric O–S–O bending modes) \Box 460 cm⁻¹; v₃ (asymmetric S–O stretching modes) \Box 1100 cm⁻¹; and v₄ (asymmetric O–S–O bending modes) \Box 620 cm⁻¹,^{3,15} only the bands corresponding to the modes characterized by the frequencies v_1 and v_2 are visible. The other two modes are difficult to identify because they overlap with bands attributed to vibrational modes associated with the borosilicate network.

In the present work, the sharp band at 988 cm⁻¹ in the glass samples has been taken as the fingerprint of the presence of sulfur as SO_4^{2-} in the investigated glasses, and its intensity increases with increase in SO_3 concentration.

3.3.2 Structural analysis of sulfur-containing glasses by Raman and MAS NMR spectroscopy

A comparison of the Raman spectra of baseline glasses and sulfur-containing glasses reveals a change in the band positions and intensity of silicate (900-1200 cm⁻¹) and borate stretching regions (1200-1600 cm⁻¹), thus reflecting the changes in the concentration and structural configurations of the NFU, as a function of SO_4^{2-} content. In particular, the disappearance of the Raman band near 950 cm⁻¹ attributed to Si^2 units and the shift in the position of Si^3 band towards higher frequencies is significant; simultaneously a shift in the 500 cm⁻¹ band towards lower frequencies can be noted. Furthermore, Figures 10 (a-c) also indicate significant changes in the ¹¹B,²⁹Si, and ²³Na MAS NMR spectra, documenting an increase in N_4 and a decrease of $<\delta_{150}^{29}$ Si> and $<\delta_{150}^{23}$ Na> in the sulfur-containing glasses relative to the respective baseline glasses. Thus, both the Raman as well as the ¹¹B and ²⁹Si MAS NMR data clearly indicate a significant increase in network connectivity of the sulfur-containing glasses, involving both the borate and the silicate components. Here, it is noteworthy that the fitting models for the ¹¹B MAS NMR spectra of the four glasses with the highest SO₃ contents, namely NB-40-3S, NS-35-3S, NS-40-3.5S, and NS-45-4S differ significantly from those of the corresponding baseline glasses. For these SO₃-containing glasses, a distinct contribution of a high- η_Q component is not evident; rather two contributions with different chemical shifts but relatively similar quadrupolar

coupling parameters are seen. Our assignment of the lower-frequency and higher- η_Q (0.55) component to B² units must be considered tentative: in the case of the NB-40-3S we consider the two possible scenarios of this component reflecting B² or B³ units.



We also tried to quantify the impact of sulfate incorporation on the structure of the investigated glasses from the Raman spectra. To this end, the silicate stretching region (850-1200 cm⁻¹) was deconvoluted into seven bands, out of which six bands are the same as those of the baseline glass, as shown in Figures S6-S8, and the seventh band at 988 cm⁻¹ belongs to S–O

stretching mode in SO₄²⁻ anion. A comparison of $\frac{Si^4}{Si^1+Si^2+Si^3}$ and individual Siⁿ species for sulfur-free and sulfur-containing NB-*x* glasses is shown in Figures 9(b) and 9(c). The increase in the $\frac{Si^4}{Si^1+Si^2+Si^3}$ ratio and individual Siⁿ species for sulfur-containing glasses as compared to the baseline glasses manifests the increased polymerization of the silicate network upon sulfur incorporation.

Alternatively, we can estimate the $\langle O/Si \rangle$ ratio from the boron speciation in Table 2 (as extracted from the ¹¹B MAS NMR spectra), if the molar SO₃ contents are known. Considering that for each mole of SO₃ one equivalent of Na₂O will not be available for the creation of NBO species in the silicate network, an expression to this effect can be written as presented in Equation (5), and the resulting values are presented in Table 4.

$$\langle O/Si \rangle = \{2 \times [Na_2O] - 2 \times [SO_3] - 2 \times [B_2O_3] \times (N_4 + N_2)\} / [SiO_2],$$
 (5)

Indeed, in glasses NS-35-3S, NS-40-3.5S, and NS-45-4S the average number of NBOs per Si, $\langle O/Si \rangle$, is seen to decrease in comparison to the situation in the baseline glasses, which is confirmed by corresponding changes in $\langle \delta_{iso}^{29}Si \rangle$ towards lower values (Table 4). An apparent exception is observed for glass pair NB-40 and NB-40-3S, where there is no apparent change in $\langle \delta_{iso}^{29}Si \rangle$ (see Table 4 and Figure 10b-III). For this glass, the ¹¹B MAS NMR spectra show a clear indication of B² units in the S-free glass, whereas the presence of B² units in the spectrum of NB-40-3S is less evident, and the two distinct scenarios mentioned above are considered. If in this glass the main effect of SO₃ upon the structure is the elimination of B² units, Table 4 indicates that the degree of polymerization of the silicate network would indeed remain unaffected, thereby providing a rationale for the absence of change in the ²⁹Si MAS NMR spectra upon SO₃ incorporation (Figure 10b-III).

A notable influence of sulfur incorporation upon the borate network is indeed also evident from the Raman spectra. The intensity maximum found near 1470 cm⁻¹ shifts towards lower frequencies suggesting a decrease in the concentration of asymmetric $BO_2 \emptyset^-$ (B²) units and an increasing fraction of $B\emptyset_4$ (B⁴) units in the glass structure, which corroborates the ¹¹B MAS NMR analysis of the sulfur-containing glasses (Figure 10a and Tables 2, and 3), revealing an increase in the fraction of B⁴ units after sulfur incorporation in the glasses.



Figure 10b. $-S_1$ MAS NMR spectra of sulfur-free baseline glasses (black color) and SO₃containing glasses (blue color). The dashed vertical line indicates the chemical shift of silica (Si⁴ units only, -110ppm).

In addition, the ²³Na chemical shifts of the SO₃-containing glasses are systematically decreased in relation to those of the baseline glasses, reflecting an increased quantitative contribution of the B^4 units and the decreased quantitative contribution of NBOs (associated with B^2 , Si³ and Si² units) in the first coordination sphere of the sodium ions. In addition, there is of course the effect of a direct interaction of those (relatively few) sodium ions that find themselves in the first coordination sphere of the sulfate anions, which cannot be separately assessed.



Figure 10c. ²³Na MAS NMR spectra of sulfur-free baseline glasses (black color) and SO₃-containing glasses (blue color). The dashed line denotes the chemical shift of a 1M NaCl solution used as a reference standard.

Basically, the incorporated SO_4^{2-} anions can successfully scavenge the NBO-creating Na⁺ (from the network formers) for their charge compensation. Thus, the Na⁺ attracted by SO_4^{2-} (for charge compensation) is no longer available to break the B–O–B, Si–O–Si or B–O–Si bonds. Consequentially, the formation of NBOs bound to either silicate or trigonal boron species is diminished. In contrast, sulfur incorporation does not affect the modification mechanism leading to the formation of B⁴ species; the fraction of these units is consistently higher in the SO₃ containing glasses than in the baseline glasses. Consequently, the glasses in which the primary modification mechanism is the creation of B⁴ units have zero or very low SO₃ solubility (see Section 4). Finally, consistent with the literature, ^{13, 15, 18, 19, 66} we did not find any evidence for bridging oxygen species linking sulfate units with the glass network.

4. Discussion

4.1 Sulfur solubility in borosilicate glasses in the context of Dell-Yun-Bray model

The glass compositions in the present study have been designed in a manner that they can be formally described in terms of the introduction of SO₃ into the baseline glass melt, where sulfur (in the form of SO₄²) will compete with silicate and borate units for the fixed amount of Na⁺. The solubility of SO₃ in the melt will thus be controlled by the effectiveness of this competition. As indicated by the results of the present study, the solubility of SO₃ in the three glasses in the Region 1 (R< 0.5) of the DYB model, i.e., SB-60, SB-75 and NB-15 (Figure 1), is \leq 0.5 mol.%. According to the NMR and Raman scattering results, these three glasses are close to fully polymerized, i.e., have few NBOs attached to either B(III) or silicate network. Evidently SO₃ competes unsuccessfully with the network forming borate units for the network modifier Na⁺, thus, allowing the B³ \rightarrow B⁴ conversion to proceed in an unperturbed manner. As a matter of fact,

 N_4 systematically increases in the SO₃-containing glasses. Because of the higher extent of network connectivity, one also observes that the SO₃ containing glasses have significantly increased glass transition temperatures, reflecting the higher average coordination number of the network forming units. The SO₃-containing glasses also follow the universal correlation of T_g versus $\langle n \rangle$, supporting the idea that the glasses follow the DYB model if one assumes that an equivalent amount of Na₂O is removed from the network modification process because it is needed to provide charge compensation for the SO₄²⁻ ions. Finally, although SO₃ solubility of glasses in the region R < 0.5 is very low, Manara et al.³ have reported non-zero (< 0.25 wt.% SO₃) values in such glasses. This may be attributed to a small extent of silicate depolymerization^{26, 80} signifying a slight departure from the DYB model.²²⁻²⁴ This idea is also supported by the Raman data presented in Figure 2.

In glass SB-45 representing Region 2 of the DYB model (Figure 1), the SO₃ solubility of 0.87 mol % (1.07 wt.%) is significant (compared to the SO₃ solubility in glasses in the Region 1). In addition, the shift of the 490 cm⁻¹ Raman band to 500 cm⁻¹ (Figure 2c), the spectroscopic changes in the 850-1200 cm⁻¹ region and the value of $< \delta_{150}^{29}$ Si> (deduced from ²⁹Si MAS NMR spectrum) suggests the formation of NBOs in the silicate network. Furthermore, the appearance of metaborate Raman band near \Box 700 cm⁻¹ suggests the formation of NBOs in the borate network. This interpretation contrasts with the DYB model,²² but is consistent with Bunker et al⁵⁸ and Wang et al.⁵⁹ The increased SO₃ solubility in the glass SB-45 can thus be correlated with some extent of depolymerization of silicate and borate network in the baseline glass, making some Na₂O available for charge compensating SO₄²⁻, resulting in an increase in the average coordination number as compared to the baseline glass. The SO₃ solubility in glasses in Region 3

(Figure 1) is higher (0.90 mol.% (1.12 wt.%) for NB-25, and 0.96 mol.% (1.21 wt.%) for SB-30) than those from Regions

1 and 2. According to DYB model,²²⁻²⁴ and confirmed by the present NMR results, in this region the excess Na⁺ (left after the formation of BØ₄ units) creates NBOs in the silicate network, whereas no NBOs are formed in the borate network to a significant extent. The SO₃ solubility in glasses in Region 4 (Figure 1) is highest, varying between 1.69 mol. % (2.1 wt.%) to 3.86 mol. % (4.89 wt.%), owing to the highest degree of depolymerization in the glass network, and availability of excess Na⁺ to charge compensate SO₄²⁻. Region 4 in the present study comprises eight glass compositions, i.e., five from the NS-*z* series (NS-25, NS-30, NS-35, NS-40, and NS-45) and three from the NB-*x* series (NB-30, NB-35, and NB-40). In both NB-*x* and the NS-*z* series, the increased SO₃ solubility with increasing sodium content can be correlated to the increased number of NBOs in the silicate and borate networks, as evident from both the NMR and the Raman spectroscopic data. Figure 11 illustrates a good anti-correlation between the SO₃ solubility and the average network connectivity *<n>* obtained from the analysis of the NMR data of the baseline glasses.

4.2 Implications of the present studies in designing advanced borosilicate glass compositions with enhanced SO₃ solubility

As discussed, the sulfur solubility in the investigated glasses is highest in Region 4 of the DYB model (Figure 1), specifically for the glasses in the NS-*z* series and NB-*x* series with high Na₂O concentrations. The glasses in these two series with SO₃ solubility \geq 1.9 mol % (2.4 wt.%) are (from highest to lowest): NS-45>NS-40>NS-35>NB-40>NS-30>NB-35. Of these, the SO₃ solubility scales with the *R* value, i.e., higher the Na₂O/B₂O₃ higher is the SO₃ solubility in glasses.







Figure 12. Normalized molar ternary composition diagrams. (a) $SiO_2-B_2O_3-Na_2O$ and (b) $SiO_2-B_2O_3-(A_2O+AeO)$, where $A_2O = Li_2O+Na_2O+K_2O+Cs_2O$ and AeO = MgO+CaO+SrO+BaO; here LAW glasses are black crosses, HLW glasses are green carats, and glasses from this study are red squares.

Figure 12a, a $Na_2O-B_2O_3-SiO_2$ molar ternary phase diagram, compares the compositions from the present study to ~950 LAW^{3, 5, 7,19, 81-92} and ~50 HLW^{2, 86, 93-96} formulations of simulated nuclear waste glasses, wherein the complex oxide LAW and HLW glass compositions are normalized to these three components. It is evident that most LAW glasses are to the low B_2O_3 side of the ternary spanning across all the regions of the DYB ternary diagram (Figure 1) with majority of them located in the Region 4. Figure 12b shows the same compositions but now normalized the alkali $(Li_2O+Na_2O+K_2O+Cs_2O)$ alkaline to total and earth (MgO+CaO+SrO+BaO) content rather than only Na₂O. The comparisons with total alkali only appear similar for LAW glasses, but HLW glasses have considerably more alkaline-earths, so normalized compositions move closer to this corner. Whether considering only Na₂O or total alkali plus alkaline earth oxides, the normalized LAW compositions are similar to the NS-z series of glasses investigated here, those that showed the highest sulfur solubility and whose structure has been described here.

The significance of this comparison is that it demonstrates that higher *R* should drive higher sulfur solubility due to the (1) depolymerization of the glass network, (2) availability of Na₂O for charge compensation of $SO_4^{2^-}$, and (3) reduction of the content of B_2O_3 which competes with $SO_4^{2^-}$ for Na⁺ in converting B³ to B⁴ units. The insights from the current study support the empirical prediction of positive coefficients for alkali and alkaline earth oxides in the sulfur solubility model (Eq. 1), as depolymerizing agents,⁴ as well as the negative coefficient for Al₂O₃ as a polymerizing agent competing for Na₂O (please refer to Table S2). The large negative values for Cl and Cr₂O₃ probably relate to their propensity for creating the molten salt phase and thus, removing Na₂O (or other alkali) from the glass to the salt phase, thus reducing the ability to incorporate SO₃ in the glass. The reason for positive coefficients for B₂O₃ and SiO₂ is still unclear. Note, however, that the SO₃ solubility model (Eq. 1) does not correctly predict the order

of glass compositions in terms of their SO_3 solubility (from highest to lowest): NB-45>NB-40>NS-45>NS-35>NS-30, as has been shown in Table S3.

Thus, at first look, it may be suspected that enhancement in the SO₃ solubility in nuclear waste glasses, particularly LAW glasses, can be made by simply increasing Na₂O concentration (which would be akin to increasing waste loading since most of the waste is caustic including high concentrations of Na⁺). However, it is known that an increase in Na₂O can also have negative effects, particularly on the chemical durability. In the present study, this is evident from the predictions from the vapor hydration test (VHT) and product consistency test (PCT) models for LAW glasses (Tables S4-S7).⁴ According to the VHT model, the glass NS-45 (with the highest measured SO₃ solubility) is expected to be exhibit highest rate of corrosion (largest alteration thickness) followed by NB-40 and NS-40, the result being primarily driven by their Na₂O content. For the LAW PCT model, the worst performance (highest normalized release of Na, B) of the six glasses with highest SO₃ solubility has been predicted from NB-35, driven by its low SiO₂ content, followed by NS-45, again driven by its high Na₂O concentration.

Thus, while it is tempting to simply add more Na_2O to improve sulfur solubility, it can have severe impact on the chemical durability of the final waste form. Therefore, the approach for increasing sulfur in the nuclear waste glasses must then be to increase network depolymerization with other components such as Li₂O or K₂O (which show less deleterious effects on PCT compared to Na_2O), or even alkaline-earths (which show positive coefficients, presumably protective for Na and B release). Any composition changes to improve the waste form performance must also be balanced by constraints for processing, such as viscosity, melting temperature, and electrical conductivity. Thus, the real value of the present study is to provide structural insight into the mechanisms of sulfur incorporation that could not be obtained for realistic compositions due to their complexity. These structural insights allow the rationalization of the empirical models used for predicting properties of the complex nuclear waste glasses, thus, leading us towards the development of non-empirical models based on Quantitative Structure – Property Relationships.

5. Conclusions

The structural dependence of SO_3 solubility in sodium borosilicate glasses has been investigated over a broad composition space. The SO₃ solubility in the investigated glasses scales positively with R and can be viewed to be the result of a competition of SO₃ with the network formers B₂O₃ and SiO₂ for the Na₂O network modifier in the melt. This competition is unsuccessful against the network modification mechanism $B^3 \rightarrow B^4$, but effective against the conversion $B^3 \rightarrow B^2$ and $Si^4 \rightarrow Si^3 \rightarrow Si^2$ effected by the modifier. There is no clear evidence that B^2 units are present in glasses containing sulfate ions at the level of their maximum solubility. Likely re-polymerization sites include B(Si) –O–Si², B(Si) –O–Si³ and B²–B³ linkages. The SO₃ solubility shows a negative linear correlation with the average extent of network connectivity < n > derived from NMR studies of the baseline glasses. The low SO₃ solubility, 0.38-0.96 mol % (0.46-1.21 wt.%), in SB-y series of glasses can be understood in terms of their generally high degree of polymerization. The higher SO₃ solubility of NB-x and NS-y series in region 4 arises from the strong tendency towards network depolymerization with increasing alkali content. In particular, the Si² sites appear to be repolymerized preferentially suggesting that the sulfate ions tend to be localized in regions of a lower degree of polymerization.

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Supporting Information Description

Figure S1: X-ray diffractograms of the glass powders for (a) NB–x series, (b) SB–y series, (c) NS–z series, (d) sulfur-containing glasses, and (e) Na_2SO_4 crystalline phase observed as white salt layer over the surface of phase separated NB–40 glass containing 4 mol% SO₃.

Figure S2: Images of the baseline and sulfur-containing NB–x glass samples depicting the solubility limit and white salt layer formation.

Figure S3: Images of the baseline and sulfur-containing SB–y glass samples depicting the solubility limit and white salt layer formation.

Figure S4: Images of the baseline and sulfur-containing NS–z glass samples depicting the solubility limit and white salt layer formation.

Figure S5: Linear increase in SO₃ solubility for (a) NB–x series of glasses with Na₂O/B₂O₃ and (b) NS-z series of glasses with Na₂O/SiO₂ ratio.

Figure S6: Spectral deconvolution of Raman spectra of baseline NB-x series of glasses.

Figure S7: Spectral deconvolution of Raman spectra of baseline SB-y series of glasses.

Figure S8: Spectral deconvolution of Raman spectra of baseline NS-z series of glasses.

Figure S9: Representative ¹¹B MAS-NMR spectra of NB-35 glass at three different magnetic fields and their deconvolutions into one B(III) and one B(IV) spectral components. The parameters for the simulation of the B(III) component are: $\delta_{iso} = 18.9$ ppm, $C_Q = 2.68$ MHz, $\eta_Q = 0.51$. Note that the fit leading to perfect agreement with the experimental lineshape at 16.4 T leads to deviations from the experimental lineshapes at lower fields (compare dashed red and black curves). Experimental conditions at 16.4 T: Agilent DD2 spectrometer, resonance frequency of 224.516 MHz, 3.2mm MAS NMR probe, spinning frequency 20.0 kHz sample spinning, $\pi/12$ pulses of 0.6 ms, recycle delay 10s. Experimental conditions at 5.64 T: Agilent DD2 spectrometer, resonance frequency 18.0 kHz sample spinning, $\pi/8$ pulses of 1.0 µs, recycle delay 3 s.

Figure S10: Representative ¹¹B MAS-NMR spectra of NB-35 glass at three different magnetic fields and their deconvolutions into two B(III) and one or two B(IV) spectral components. The parameters for the simulation of the two B(III) component are: $\delta_{iso} = 18.5$ and 16.1 ppm, C_Q = 2.57 and 2.58 MHz, $\eta_Q = 0.32$ and 0.24; 29 and 13%. Note that the fit leading to perfect agreement with the experimental lineshape at 16.4 T also leads to good agreement with the experimental lineshape at 16.4 T also leads to good agreement with the experimental lineshape at 16.4 T also leads to good agreement with the experimental lineshape at 16.4 T also leads to good agreement with the experimental lineshapes at lower fields (compare dashed red and black curves). Experimental conditions at 16.4 T: Agilent DD2 spectrometer, resonance frequency of 224.516 MHz, 3.2mm MAS NMR probe, spinning frequency 20.0 kHz sample spinning, $\pi/12$ pulses of 0.6 ms, recycle delay 10 s. Experimental conditions at 5.64 T: Agilent DD2 spectrometer, resonance frequency 18.0 kHz sample spinning, $\pi/8$ pulses of 1.0 µs, recycle delay 3s.

Figure S11. ¹¹B MAS-NMR spectra of baseline NB-*x* series of glasses and their deconvolutions into two B(III) and one or two B(IV) spectral components (red curves). Red dashed curves are the superimposed simulated lineshapes in best agreement with the experimental data (black curves).

Figure S12. ¹¹B MAS-NMR spectra of baseline SB-*y* series of glasses and their deconvolutions into two B(III) and one or two B(IV) spectral components (red curves). Red dashed curves are the superimposed simulated lineshapes in best agreement with the experimental data (black curves).

Figure S13. ¹¹B MAS-NMR spectra of baseline NS-*z* series of glasses and their deconvolutions into two B(III) and one or two B(IV) spectral components (red curves). Red dashed curves are the superimposed simulated lineshapes in best agreement with the experimental data (black curves).

Figure S14. ¹¹B MAS-NMR spectra and their deconvolutions into two B(III) and one or two B(IV) spectral components (red curves) for sulfur-containing glasses with SO₃ content \geq 3 mol.%. Red dashed curves are the superimposed simulated lineshapes in best agreement with the experimental data (black curves).

Figure S15. Variations of the onset of glass transition temperature (T_g) as a function of the relative ratio Na₂O/B₂O₃, SiO₂/(SiO₂+B₂O₃) and Na₂O/SiO₂ for (a) NB–x, (b) SB–y, and (c) NS– z series of baseline glasses.

Table S1. Batched and ICP-OES analyzed glass composition (shown in brackets within ± 0.2 wt%) of NB-x, SB-y, and NS-z series of baseline glasses.

Table S2. Band assignment, peak position (v), area (A) and FWHM (W) of deconvoluted Raman bands for the baseline glasses.

Table S3. Fitting parameters and N4 values obtained from the ¹¹B MAS NMR spectra of NB-35 glass sample at three different magnetic fields and their deconvolutions into one B(III) and one B(IV) spectral components.

Table S4. Fitting parameters and N4 values obtained from the ¹¹B MAS NMR spectra of NB-35 glass sample at three different magnetic fields and their deconvolutions into two B(III) and one or two B(IV) spectral components.

Table S5. Coefficients of the recommended W_{SO_3} model for LAW glasses¹ (in wt.%) used in the present study.

Table S6. Predicted SO₃ solubility values of glasses belonging to region-4 of ternary diagram (Figure 1) using the empirical model for LAW glasses proposed by Vienna et al.¹ using equation: $W_{SO_3}^{Pred} = \sum_{i=1}^{q} s_i n_i + selected(\sum_{i=1}^{q} s_{ii} n_i^2 + \sum_{j=1}^{q-1} \sum_{k=j+1}^{q} s_{jk} n_j n_k)$. Here, $W_{SO_3}^{Pred}$ is the predicted SO₃ solubility in weight percent, *q* represents the number of components in the composition with *s* being the coefficient and *n* is the normalized mass fraction (wt.%) of the component as given below in the table.

Table S7. Coefficients of the recommended $\ln(\text{VHT }D)$ model for LAW glasses², in $\ln(\mu m)$, used in the present study.

Table S8. Calculated VHT alteration thickness in ln (D, μ m) of the glasses belonging to region-4 of ternary diagram (Figure 1) using the VHT model² using the equation: $\ln(D, \mu m) = \sum_{i=1}^{q} b_i g_i + Selected \{ \sum_{i=1}^{q} b_{ii} g_i^2 + \sum_{i=1}^{q-1} \sum_{j=i+1}^{q} b_{ij} g_i g_j \}$. Here, q is number of LAW glass

components in the model, b_i is the coefficient of i^{th} component in LAW glass, g_i is the mass fraction of i^{th} component in LAW glass, b_{ii} is the coefficient of the squared term of the i^{th} component in LAW glass, and b_{ij} is the coefficient of the cross-product term involving the i^{th} and j^{th} components in LAW glass.

Table S9. Coefficients of the recommended $\ln(PCT NL)$ model for LAW glasses², in $\ln(g/L)$, used in the present study.

Table S10. Calculated normalized PCT response (*NL*) of the glasses belonging to region-4 of ternary diagram (Figure 1) using the average natural logarithmic of normalized PCT response $[\ln(NL, g/L)]$ model² using the equation:

 $\ln(NL, g/L) = \sum_{i=1}^{q} b_i g_i + Selected \{ \sum_{i=1}^{q} b_{ii} g_i^2 + \sum_{i=1}^{q-1} \sum_{j=i+1}^{q} b_{ij} g_i g_j \}$

where q is number of LAW glass components in the model, b_i is the coefficient of i^{th} component in LAW glass, g_i is the mass fraction of i^{th} component in LAW glass, b_{ii} is the coefficient of the squared term of the i^{th} component in LAW glass, and b_{ij} is the coefficient of the cross-product term involving the i^{th} and j^{th} components in LAW glass.

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