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Rheology of protein-stabilised emulsion gels envisioned as composite networks.

1 - Comparison of pure droplet gels and protein gels

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Abstract

Hypothesis

Protein-stabilised emulsion gels can be studied in the theoretical framework of colloidal gels, because both protein assemblies and droplets may be considered as soft colloids. These particles differ in their nature, size and softness, and these differences may have an influence on the rheological properties of the gels they form.

Experiments

Pure gels made of milk proteins (sodium caseinate), or of sub-micron protein-stabilised droplets, were prepared by slow acidification of suspensions at various concentrations. Their microstructure was characterised, their viscoelasticity, both in the linear and non-linear regime, and their frequency dependence were measured, and the behaviour of the two types of gels was compared.

Findings

Protein gels and droplet gels were found to have broadly similar microstructure and rheological properties when compared at fixed volume fraction, a parameter derived from the study of the viscosity of the suspensions

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formed by proteins and by droplets. The viscoelasticity displayed a power law behaviour in concentration, as did the storage modulus in frequency. Additionally, strain hardening was found to occur at low concentration. These behaviours differed slightly between protein gels and droplet gels, showing that some specific properties of the primary colloidal particles play a role in the development of the rheological properties of the gels.

Keywords: Colloidal gel, Rheology, Emulsion, Sodium caseinate, Viscoelasticity, Protein-stabilized droplet, Microstructure



Graphical abstract

1 1. Introduction

Emulsion and protein gels form the basis of many food products, such as 2 voghurt, soft cheese or tofu, where the flocculation of a vegetable or animal 3 milk leads to the formation of a soft solid via aggregation of proteins and 4 fat droplets. This process has been used for millenia in traditional cooking, 5 but a deep understanding of the mechanisms of the physical transformation 6 occurring in these systems only came in recent decades with the study of colloidal gels [1, 2, 3]. While much effort has been spent in correlating the 8 structure formation and the gel properties with the interparticle interactions [4], there is yet to be a full understanding of food-based colloidal gels, both 10 in terms of fundamental science and of specific applications. 11

The gels of interest here typically exhibit a fractal microstructure that can be described by a fractal dimension D_f [5]. This fractal microstructure affects their mechanical properties [6, 7]. The storage modulus G' of the gels also typically shows a power-law variation with the volume fraction ϕ [8, 9]:

$$G' \sim \phi^A$$
 (1)

It has been shown that the exponent A can be related to the fractal dimension 12 of the gels, with the relationship depending on the gelation regime. For gels 13 formed via diffusion limited cluster aggregation, generally at low volume 14 fractions, it was found that $A = (3 + D_b)/(3 - D_f)$, where D_b is defined as 15 the bond (or backbone) dimension of the network [4, 3]. At higher volume 16 fractions, the links between clusters are weaker and $A = 1/(3 - D_f)$ [10]. A 17 general model, as suggested by Wu and Morbidelli, is $A = (1 + (2 + D_b)(1 - D_b))$ 18 (ϵ) $(3 - D_f)$, where $\epsilon \in [0; 1]$ depends on the type of regime [9]. 19

This theoretical framework for colloidal gels can be applied not only to model attractive hard spheres, but also to protein and emulsion gels, and in particular to casein systems [5, 11, 12].

Caseins are the most common proteins in cow's milk. They have attracted considerable attention for the last 40 years, mainly because of their widespread use as food ingredients in numerous commercial products (processed cheese, ice-cream, coffee whiteners, cream liqueur, etc). In this study, sodium caseinate, which is derived from the caseins in milk, was used both as gelling agent and as emulsifier.

Sodium caseinate, when suspended in water, forms naturally-occurring aggregates, that are thought to be elongated with a length around 20 nm [13, 14, 15]. The surface of these aggregates is charged negatively at neutral pH, and electrostatic repulsion is an important condition for their stability [16]. When such suspensions are acidified, the decrease in electrostatic repulsion causes the aggregation of proteins that, if slow and rather homogeneous, leads to the formation of a gel [17, 12, 18, 19, 20].

Previous work using confocal microscopy has highlighted their fractal structure, which was found to be dependent on the pH, ageing time and addition of other components [21, 22, 6, 23, 24, 25]. A power-law dependence of the viscoelasticity on concentration of acid casein gels, using both native casein and sodium caseinate, has been observed in previous studies [7, 18], which was attributed to their fractal nature [12, 5]. In addition, the frequency dependence of the gels has been characterised [12, 7, 26]. Finally, the brittle 43 fracture of casein gels has also been studied from a fundamental perspective
44 [27, 28].

Besides gel formation, sodium caseinate is widely used to form oil-in-45 water emulsions [29, 30, 31]. Typically, during emulsification, the proteins 46 do not completely adsorb at the interface, leaving a residual fraction of pro-47 tein suspended in the continuous phase after emulsification [32, 33], and the 48 resulting emulsion is thus a mixture of droplets and of un-adsorbed proteins 49 [34]. Consequently, the distinction is made here between protein-stabilised 50 emulsions, and purified droplet suspensions, from which the fraction of un-51 adsorbed proteins was removed. 52

As with caseinate gels, the acidification of sodium caseinate-stabilised emulsions, and of purified droplet suspensions, leads to the formation of fractal gels called *emulsion gels* [16], and of pure droplet gels respectively. For pure caseinate-stabilised droplet gels, the nature of the interactions at play during gelation is the same as for caseinate gels, as the droplets become attractive at the isoelectric point of the protein.

Emulsion gels have been studied in the past and compared to protein gels 59 [12, 11, 16], and they have been shown to present a similar fractal structure 60 [35]. However, the properties of pure droplet gels have not been clearly inves-61 tigated, in that the systems studied have invariably contained both droplets 62 and free protein. This has made it extremely difficult to draw a consis-63 tent comparison of protein assemblies and protein-stabilised droplets as gel-64 forming particles. Investigating the pure components - droplets and proteins 65 - would enable a consistent comparison of their behaviours and understand-66 ing of their mixtures, that would be relevant from both a fundamental and 67 a technological point of view. 68

To this end, the present study investigates the similarities and differences between caseinate gels and pure caseinate-stabilised droplet gels over a wide range of concentrations. It focuses more specifically on the microstructure and on key rheological features of these systems, namely the linear and non-linear viscoelasticity and the frequency dependence, as well as on their variations with the concentration in colloidal species.

This comparison between caseinate gels and droplet gels draws on the results of a previous study of the viscosity of the suspensions that are used to prepare these gels [34]. It was shown that both droplets and protein assemblies can be studied in the framework developed for soft colloidal particles [36]. Consequently, their concentrations can be scaled by the effective volume fraction ϕ_{eff} , which can reach high values due to the possible compression, interpenetration and deformation of soft colloids [37, 38]. It is demonstrated in the present study how the same concentration scaling can be used to understand the behaviour of both sodium caseinate and droplet gels.

⁸⁴ 2. Materials & Methods

2.1. Preparation of protein and droplet suspensions

Suspensions of pure sodium caseinate (hydrodynamic radius 11 nm) and of pure sodium caseinate-stabilised droplets (hydrodynamic radius 110 nm) were prepared at a range of concentrations, as described previously [34]. The procedure is given in detail in Section 1.1 of the supplementary information for completeness. These suspensions were then used as sols for the preparation of acid-induced gels.

In the following, concentrations of both the protein and droplet samples are given in terms of the effective volume fraction ϕ_{eff} . This was determined from intrinsic viscosity measurements on dilute samples as detailed in Ref. [34]. As such the weight concentration is related to ϕ_{eff} by a simple factor, which was found to be $(2.2 \pm 0.1) \text{ mL g}^{-1}$ and $(8.5 \pm 0.2) \text{ mL g}^{-1}$ for the droplet and protein suspensions respectively. The use of this parameter is discussed in detail in Ref. [34].

⁹⁹ 2.2. Preparation of protein and droplet gels

¹⁰⁰ The decrease in pH required for the gelation of the suspensions of sodium ¹⁰¹ caseinate and of pure sodium-caseinate stabilised droplets to occur was achieved ¹⁰² by the slow hydrolysis of glucono δ -lactone (Roquette), as detailed in Section ¹⁰³ 1.2 of the supplementary material.

104 2.3. Laser scanning confocal microscopy

The gels were imaged using laser scanning confocal microscopy, here a setup based on an LSM 780 microscope on inverted Axio observer (Zeiss). It has to be noted that the resolution of confocal microscopy (limited to $\approx 200 \text{ nm}$ by light diffraction) does not allow imaging of the single protein aggregates, or single droplets. Instead, the lengthscale accessible by this imaging technique corresponds to the structure over a few colloidal particles, and is thus suitable for the description of colloidal aggregation and gelation.

112 2.3.1. Protocol for imaging of gels

¹¹³ Rhodamine B (Sigma Aldrich) and Bodipy 493/503 (Molecular Probes) ¹¹⁴ were added to the samples of protein and droplet suspensions, that were then ¹¹⁵ mixed with glucono δ -lactone, as detailed in Section 1.3 of the supplementary ¹¹⁶ material.

117 2.4. Image analysis

The image analysis of 2D micrographs was performed using the image processing software ImageJ [39].

The Fast Fourier Transform (FFT) analysis was applied to the image after Hanning windowing. The image in the Fourier space was then radially averaged to obtain the spectrum I(q). The wave vector q represents a spatial frequency, it is a function of the distance from the centre in the Fourier space and of the image size, and is expressed in μm^{-1} .



Figure 1: Protocol for the analysis of a micrograph.

The image is multiplied by a Hanning window of the same size before the Fast Fourier Transform is calculated. The spectrum I(q) is obtained using the plugin Radial Profile to perform a radial average of the Fourier transform.

The decrease of the spectrum I(q) is then fitted by a power law, linear in double logarithmic scale. Its intersection with the plateau defines the critical spatial frequency q_c .

The variations of I(q) can be described by several parameters. The position of the shoulder q_c was chosen in this study as critical wave vector, because it can be estimated in a reproducible way by fitting the power law decrease of the peak, as opposed to the top of the peak that is slightly flattened. The determination of the position of the shoulder q_c is illustrated in Figure 1. This value was then used to estimate the critical lengthscale of the network in the real space $L_C = 2\pi/q_c$.

132 2.5. Rheological measurements

Oscillatory rheology measurements were performed using a stress-controlled 133 MCR 502 rheometer (Anton Paar) and a Couette geometry (17 mm diame-134 ter profiled bob and cup CC17-P6, inner diameter 16.66 mm, outer diameter 135 18.08 mm yielding a 0.71 mm tool gap, gap length 25 mm). To avoid slip at 136 the wall during shearing, profiled bob and cup (serration width 1.5 mm, ser-137 ration depth $0.5 \,\mathrm{mm}$) were selected as measurement tools. The temperature 138 was set by a Peltier cell at 35 °C during the entire measurement sequence. 139 The operating temperature was chosen to ensure that the gelation occurs in 140 the time scale of thousands of seconds for all the samples studied here. To 141 prevent evaporation, a thin layer of silicon oil of low viscosity (10 cSt) was 142 deposited on the surface of the sample. 143

The measurements were started immediately after mixing of the sample with glucono δ - lactone and subsequent loading in the instrument. As represented in Figure 2,the measurements consisted of 4 steps, detailed in Section 1.4 of the supplementary information, for which the strain was chosen to stay in the linear viscoelastic region at steps 1, 2 and 4.

For each sample, 3 measurements of the same batch of sample were performed and the values of each data point were averaged.

151 3. Results & Discussion

The comparison of pure caseinate-stabilised droplet gels and caseinate 152 gels was performed by studying each type of system over a wide range of 153 concentrations, scaled by the effective volume fractions ϕ_{eff} . This extensive 154 characterisation of each type of system ensured that the similarities and 155 differences observed derived from the intrinsic differences in size, structure 156 and softness between caseinate assemblies and caseinate-stabilised droplets. 157 This precaution distinguishes the present study from previous comparisons 158 of emulsion gels and protein gels [40, 12] and is the key to the progress made 159 here. 160

¹⁶¹ 3.1. Microstructure of gels: colloidal species and volume fraction

¹⁶² Confocal microscopy is a commonly used technique to observe the struc-¹⁶³ ture of colloidal gels at the micron scale [41, 42, 43] that makes possible



Figure 2: Illustration of the measuring sequence for the oscillatory rheometry of the emulsion gels, detailed in the Methods section. Frequency (open squares) and strain amplitude (filled triangles) of the oscillatory shear vary with time in the 4 steps of the measurement. The multiwave mode was activated at steps 1 and 2, leading so several signal frequencies were used simultaneously. At the time t = 0s, the glucono δ -lactone was added to the sols.

the comparison of this structure for gels of different composition and volume fraction. Here, gels that were prepared by acidifying suspensions of either sodium caseinate or pure caseinate-stabilised droplets, at different concentrations, are imaged and compared. The micrographs of caseinate and droplet gels, together with their characteristic lengthscale L_C are presented in Figure 3.

As can be seen, the micrographs are similar for protein and droplet gels, especially at lower volume fraction. Indeed, in both cases, the fractal structure typical of colloidal gels is present, with interconnected networks of particle aggregates (in colour) and water-filled pores (in black). At high concentrations, these networks are denser in particles, with the pores of the droplet gels appearing to be smaller than for the protein gels.

In addition, the characteristic lengthscales L_C are of the same order of magnitude for the two components, and their values range between 5 µm and 20 µm for all the gels presented here. The variation of L_C as a function of the volume fraction cannot be interpreted quantitatively because of the significant noise in the data. This is partially related to the fact that the features picked up by the Fast Fourier Transform are probably a combination of the size of the aggregates and the size of the pores.

Thus, although the individual droplets are one order of magnitude larger 183 than the individual protein assemblies, the gels formed by these two types of 184 colloidal particles present a very similar fractal structure at a given effective 185 volume fraction ϕ_{eff} . It would also be interesting to perform a more thorough 186 investigation of the dependence of the characteristic length scale L_C of the 187 network on the effective volume fraction ϕ_{eff} , by using higher quality confocal 188 micrographs and a more precise image analysis technique, for example texture 189 analysis microscopy [44]. 190

¹⁹¹ 3.2. Rheological study of droplet gels and protein gels

In order to investigate further the comparison between protein gels and droplet gels, it is interesting to characterise their rheological behaviour. As detailed in Figure 2, the viscoelastic moduli, G' and G'', are first compared at fixed frequency, strain and time after gelation for gels of different compositions. Then the dependences of G' and G'' on the frequency are presented. Finally, the non-linear viscoelasticity of the gels is considered.



Figure 3: Micrographs (100 µm × 100 µm) of aged acid-induced gels formed from suspensions of: (top) sodium caseinate, and of (bottom) caseinate-stabilised droplets, at different volume fractions ϕ_{eff} . The scale bars are 30 µm long. The inset in the cartoon representing the droplet gels shows the interactions between the caseinate adsorbed at the oil-water interface. The graph presents the characteristic lengthscale L_C of the gels, as a function of the volume fraction ϕ_{eff} , for caseinate gels (squares, navy blue) and caseinate-stabilised droplet gels (circles, cyan).

For each point, L_C was obtained by performing a FFT of one micrograph and extracting the position of the peak in the spectrum I(q), as described in Figure 1. The inaccuracy of this determination is indicated by the error bar. Where two points are presented for one concentration, they correspond to different micrographs of similar samples.

¹⁹⁸ 3.2.1. Linear viscoelasticity of gels

The gelation of sodium caseinate and sodium caseinate-stabilised droplets 199 is presented in Figure 4(a). As with previous studies on colloidal gels, these 200 systems do not reach an equilibrium state, but go through rearrangements of 201 their network upon ageing [45, 46]. To compare the viscoelasticity of the gels 202 at similar ageing state, it is possible to superimpose the gelation curves by 203 using horizontal and vertical shifts in logarithmic scale [26, 47, 48], as can be 204 seen in Figure 4(b). The horizontal and vertical shift factors α_t and $\alpha_{G'}$, and 205 the protocol used to determine them, can be found in Figure S3 and Section 206 2 of the supplementary material. 207

The viscelastic behaviour of gels was arbitrarily compared at $t/\alpha_t = 1.4$. 208 This value was chosen because it is the highest reached by all the gels studied, 209 even those with a very slow gelation. Because the kinetics that determine 210 α_t remain the same post gelation, the rise in elastic modulus G' with t/α_t 211 is similar for all samples. Thus using G' at constant t/α_t is appropriate for 212 comparison of different concentrations. The elastic modulus G' and the loss 213 modulus G'' of the two types of gels at $t/\alpha_t = 1.4$, measured at 1 Hz, are 214 presented in Figure 4 as functions of their effective volume fraction ϕ_{eff} . 215 In addition, the phase angle $\delta = \arctan(G''/G')$, indicating the viscoelastic 216 character of the gels, is found to be significantly different for each sort of gels, 217 with δ_{prot} varying between 21° and 24°, and δ_{drop} between 13° and 17°. The 218 higher phase angle found for protein gels indicates that their behaviour is 219 slightly shifted towards the viscous materials on the spectrum of viscoelastic 220 behaviour. 221

As can be seen in Figure 4, sodium caseinate and sodium caseinatestabilised droplets form gels of very similar viscoelasticity when scaled by the volume fraction. More precisely, the storage and loss moduli of droplet gels are slightly higher, at a given volume fraction, than those of protein gels. The similarity of the viscoelasticity of the two types of gels can be related to their similar microstructure, as observed in Figure 3.

Our result differs significantly from a previous study on caseinate-stabilised emulsion gels [12]. Although the concentrations chosen for the comparison were arbitrary in Ref. [12], it was shown that emulsion gels had a similar modulus to a protein gel with a threefold increase in protein concentration, and the authors thus concluded that emulsions form gels with a higher viscoelasticity than protein gels. It is thought that this discrepancy arises mostly from the choice of parameter to describe the composition of these systems. Indeed,



Figure 4: Left panel: (a) Storage moduli G' upon formation of droplet gels and protein gels, (b) Master curve for the formation of the colloidal gels, the horizontal (α_t) and vertical $(\alpha_{G'})$ shift factors are presented in Figure S3. Right panel: Storage (G', (c)) and loss (G'', (d)) moduli at 1 Hz of protein-stabilised droplet gels (circles, cyan) and of protein gels (squares, navy blue) at $t/\alpha_t = 1.4$ as functions of the effective volume fraction of the gel ϕ_{eff} . A fit (Equation 2) of each type of system was performed and the model (parameters listed in Table 1) as well as the 95% confidence band are displayed on each graph.

The horizontal error bars arise from error propagation upon calculation of the volume fraction, as detailed in Section 3 of the supplementary material, while the vertical error bars arise from the uncertainties in determining the shift factors $\alpha_{G'}$ and α_t .

the storage modulus can be presented as a function of either the protein concentration, or of the weight concentration of each colloidal particle, leading
to large differences between protein gels and droplet gels, but in opposite
directions, as illustrated in Figure S4 of the supplementary material.

More generally, the weight concentration is unlikely to be a relevant pa-239 rameter to compare gels made of colloidal particles of a very different nature, 240 such as caseinate assemblies and droplets - the former being water-swollen 241 and soft, while the latter are filled with oil and more rigid. The same is true 242 for the use of the protein concentration, as shown in Ref. [12]. Instead, we 243 argue here that a more appropriate scaling to use for comparing protein gels 244 and droplet gels is the volume fraction, despite its definition being non-trivial 245 for complex colloidal particles [34]. 246

²⁴⁷ Consequently, we find that there is little difference between the two types ²⁴⁸ of gels, provided that the comparison is drawn between samples at the same ²⁴⁹ effective volume fraction ϕ_{eff} . Furthermore, the variation of the viscoelas-²⁵⁰ ticity with the volume fraction for the protein gels and the droplet gels can ²⁵¹ be quantified by using a fit to a power law, as discussed below.

Power-law increase with volume fraction. As can be seen in Figure 4, the variations of both storage G' and loss G'' moduli as functions of effective volume fraction can be described as a power law for the two types of gels:

$$G(\phi_{eff}) = G_{0,\phi} \times \phi^{\alpha}_{eff} \tag{2}$$

²⁵² Where the pre-factor of the power-law $G_{0,\phi}$ and the exponent α are two pa-²⁵³ rameters to be determined. The values found by fitting $G'(\phi_{eff})$ and $G''(\phi_{eff})$ ²⁵⁴ with Equation 2 are summarised in Table 1.

	Storage modulus G'		Loss modulus G''	
Gel type	$G'_{0,\phi}$	α	$G_{0,\phi}''$	α
Droplet gels	(4.78 ± 0.22) kPa	3.1 ± 0.1	$(1.52 \pm 0.21) \mathrm{kPa}$	3.2 ± 0.1
Protein gels	(2.42 ± 0.19) kPa	2.7 ± 0.1	$(1.01 \pm 0.03) \mathrm{kPa}$	2.8 ± 0.1

Table 1: Parameters for Equation 2 to fit viscoelasticity of gels at 1 Hz displayed in Figure 4

This power-law dependence of the viscoelasticity of sodium caseinate gels is in good correspondence with previous studies on casein gels [6, 7, 18, 26, 257 24]. The value of the exponent for sodium caseinate varies significantly with temperature, as it was found that $\alpha = 2.57$ at 30 °C and $\alpha = 3.73$ at 50 °C [26]. The value found here for gels formed at 35 °C is thus in good agreement with these results. In addition, no data is available on the rheological
properties of acid-induced droplet gels.

The power law dependence of the elastic modulus G' is a feature of fractal colloidal gels, as previously observed experimentally and numerically [5, 8, 49, 50, 51, 52], that can be related to the fractal dimension D_f . However, the large range of volume fractions for the gels presented here makes such analysis impractical, in the absence of additional characterisation of these networks..

The study of the gel moduli as a function of their composition, described both by the nature of the elementary particles and by their volume fraction, thus offers some information on the mechanical properties of caseinate gels and caseinate-stabilised droplet gels. The behaviour of the two types of gels is very similar and reminiscent of those of more model colloidal gels. In addition to this static view of protein and emulsion gels, it is important to compare their dynamic properties.

275 3.2.2. Frequency dependence of gels

The moduli of the newly formed gels were then measured over a wide range of frequency. This measurement of the frequency dependence makes it possible to probe the dynamics of the gels. Because these exhibit a solid behaviour in the linear viscoelastic range, this aspect is limited to fluctuations within the gel network, for example rearrangement of the particle bonds, relaxation of the stress bearing strands, or motion of non-stress bearing strands like dangling chains.

Comparison between protein gel and droplet gel. In order to compare similar gels of proteins and of protein-stabilised droplets, gels of equal volume fraction ($\phi_{eff} = 0.53$) are displayed in Figure 5 (a).

Both the protein gel and the droplet gel exhibit an increase of their vis-286 coelasticity with the angular frequency ω , in agreement with previous studies 287 on colloidal gels [7, 26, 12, 53]. The storage modulus G' increases moder-288 ately for the two types of gels, while the loss modulus G'' also rises with ω , 289 but with a slightly different behaviour for protein gels and droplet gels. The 290 increase of G'' is at odds with the frequency dependence of dilute colloidal 291 gels, for which a decrease of G'' was observed [50], but is in good correspon-292 dence with the computed linear viscoelasticity of a similar system [53]. This 293 behaviour may indicate the presence of a relaxation process that is visible in 294



Figure 5: (a) Comparison of the frequency dependence for protein gels (sodium caseinate: $\phi_{eff} = 53 \%$, in navy blue) and droplet gels (caseinate-stabilised oil droplets: $\phi_{eff} = 53 \%$, in cyan). Storage modulus G' and loss modulus G'' are represented as functions of the angular frequency ω . G' was fitted with a power law for both types of samples, and the fitting parameters can be found in Table 2.

(b) Comparison of frequency dependence for protein gels (squares, navy blue) and proteinstabilised droplets (circles, cyan): power-law exponent β , obtained by fitting $G' = f(\omega)$ with Equation 5, as a function of the effective volume fraction ϕ_{eff} .

the frequency range covered at low concentration, but which moves to much lower frequencies at higher concentrations, and so becomes invisible.

In addition, as can be seen in Figure 5 (a), the viscoelastic response 297 of the two types of gels differ slightly. Indeed, the protein gel displays a 298 higher dependence on frequency than the droplet gel, as both storage and 299 loss moduli increase faster with the angular frequency than for the droplet 300 gel. Another noticeable difference is the non-monotonic behaviour of the loss 301 modulus G'' for droplets gels. This behaviour may be an indication of a 302 relaxation of droplet networks, that would be absent for protein gels in this 303 range of frequency, but an extended spectrum would be required to definitely 304 identify a possible peak. 305

In order to quantify the difference in variation of the storage modulus G' with the angular frequency ω for the two types of gels, its behaviour can be modelled by a power law [54, 55]:

$$G' = G'_{0,\omega} \left(\frac{\omega}{\omega_\beta}\right)^\beta \tag{3}$$

Where $G'_{0,\omega}$ and β are two empirical parameters to be determined, and $\omega_{\beta} = 1.00 \text{ rad s}^{-1}$ is used for dimensional purposes.

The frequency dependence of the protein gel and droplet gel of effective volume fraction $\phi_{eff} = 53\%$ is thus fitted as displayed in Figure 5 (a), and the values of the empirical parameters for can be found in Table 2.

Table 2: Frequency dependence of gels: parameters from using Equation 3 to fit the variation of the storage modulus G' with the angular frequency ω of protein gel and droplet gel of effective volume fraction $\phi_{eff} = 53\%$ displayed in Figure 5.

Gel type	$G'_{0,\omega}$	β
Protein gels	0.5 kPa	0.22
Droplet gels	$1.2\mathrm{kPa}$	0.10

The value of the exponent β for caseinate gels is slightly higher than in previous studies. Indeed, for acid-induced casein gels at 30 °C, β was measured to be 0.15 [7, 26, 12]. This discrepancy may arise from a difference of pH of the gels studied, a parameter which was shown to have a strong influence on the frequency dependence of such systems [12].

No comparable data could be found for the frequency dependence of gels 316 made of pure protein-stabilised droplets, but the comparison between protein 317 gels and gels of mixtures of proteins and droplets was performed and appears 318 to be system-dependent. On one hand, the exponent β was found to be 319 identical for acid-induced gels of caseinate emulsions and for caseinate gels, 320 i.e. 0.15 [12]. On the other hand, for heat-set gels and emulsion gels prepared 321 with β -lactoglobulin, the slope β was found to be three times higher for 322 protein gels than for emulsion gels [11]. This discrepancy is believed to 323 result from the nature of the bonds between particles in these two types of 324 gels: heat-set gels form more transient bonds than acid-induced gels, making 325 for more mobile structures. 326

³²⁷ Influence of the volume fraction on the frequency dependence. This analysis ³²⁸ of the frequency dependence can be extended to gels at all concentrations, as the curves display a similar power-law variation. These can be found
in Figure S6 of the supplementary information. The empirical model in
Equation 3 was thus applied to the gels of droplets and proteins prepared at
different volume fractions, and the resulting value of the power law exponent
for all the gels is displayed in Figure 5 (b).

As can be observed, there is little influence of the volume fraction on 334 the variation of the elasticity of the gels with the frequency. This indicates 335 that over the range of concentrations studied, the dynamical behaviour of 336 the gels is the same. By contrast, the viscosity of the suspensions increases 337 dramatically over the same range of volume fraction, as discussed in a previ-338 ous study [34]. The negligible variations of the frequency dependence of the 339 gels seem to indicate that there is no change in regime due to the crowding 340 of the colloidal particles in the solid state, and the gels formed by proteins 341 and droplets suspensions are similar in that respect. 342

³⁴³ Consequently, the difference in dynamic behaviour between protein gels ³⁴⁴ and droplet gels observed in Figure 5 (a) is consistent over the range of ³⁴⁵ volume fractions explored here, with the exponent β being larger for protein ³⁴⁶ gels than for droplet gels. This seems to indicate that caseinate gels have ³⁴⁷ more internal fluctuations than droplet gels regardless of their concentration ³⁴⁸ [55].

Furthermore, the non-monotonic behaviour of the loss modulus G'' with 349 the frequency ω observed for the droplet gel in Figure 5 (a) is also consistent 350 over the range of volume fractions, as can be found in Figure S5. This is 351 better visualised by looking at the phase angle of the gels, as presented in 352 Figure S6. In contrast, the phase angle of all the protein gels studied is 353 constant with frequency. The physical mechanism underlying this behaviour 354 is not known but it represents an additional significant difference in the 355 frequency dependence of droplet gels compared to protein gels. 356

Finally, these results of the linear viscoelasticity of colloidal gels can be 357 compared with another sort of arrested state of colloidal particles, such as 358 glasses of soft colloids like microgels [56]. For such systems, it was observed 359 that at moderately high volume fraction, the glasses display a slow increase 360 in elastic modulus G' with the frequency, associated with some mobility of 361 the particles in an entropic glass. By contrast, at higher volume fraction, 362 the particles are completely jammed and G' is constant over the range of 363 frequency explored [57]. The fact that this frequency-independent regime 364 is not reached here seems to indicate that the acid-induced gels studied are 365 quite dynamic, rather than completely arrested, and that this is more the 366

case for protein gels than for droplet gels. Interestingly, this result is true
over the range of volume fraction studied here, even for gels that are very
concentrated.

370 3.2.3. Strain dependence of the gels

The oscillatory strain sweep performed on the protein and droplet gels 371 after formation and frequency sweep, as shown in Figure 2 allows the study 372 of the variations of the storage modulus with the amplitude of the strain 373 oscillation. The typical strain behaviour of the gel is represented in Figure 374 S7, together with the definition and the values of the critical strain γ_c . To 375 highlight the differences in strain response for all gels, this parameter was 376 used to normalise the strain response of the gels and G' was divided by 377 its value in the linear regime. The resulting normalised curves presenting 378 the non-linear viscoelastic behaviour pure gels of proteins and of protein-379 stabilised droplets at different concentrations are displayed in Figure 6. 380

As can be seen, the nature of the non-linear regime varies with the type of gel formed and its volume fraction in proteins or droplets. The behaviour of gels at each concentration range is discussed separately below.

First, for gels prepared with suspensions of moderately low volume frac-384 tion of both proteins and protein-stabilised droplets, an increase of the nor-385 malised storage modulus G'/G'_0 is observed when larger shear amplitudes 386 are applied. This phenomenon is known as strain stiffening, and this result 387 is in correspondence with previous studies of low-concentration gels, both 388 experimental [51] and computational [58, 59]. Using, in one case, ultrasonic 389 imaging and, in the other, simulations of the topology of the gel networks, 390 it was found that this behaviour could be related to irreversible stretching 391 and reorientation of the gel branches. This behaviour was also shown to be 392 very dependent on the structure of the network, and hence on the volume 393 fraction of the gel. The sparser the gel, the more structural heterogeneities 394 make possible the redistribution of the stress before failure of the material. 395 while denser gels are more homogeneous and thus lead to a quicker breaking 396 of bonds in the absence of reorganisation of the network. 397

The strain stiffening is more pronounced, and is present on a wider range of volume fraction, for gels made of protein-stabilised droplets than for protein gels. Because strain stiffening is related to the structural heterogeneities within the network, this result may indicate that the proteins form gels that are overall more homogeneous than the droplet gels at low volume fraction, making these networks less prone to stress redistribution. The decrease in



Figure 6: Storage modulus G' normalised by its value in the linear regime G'_0 as a function of the oscillatory strain amplitude γ normalised by its value at the onset of the non-linear regime γ_c .(a) Sodium caseinate-stabilised droplet gels at several volume fractions ϕ , (b) Sodium caseinate gels at several volume fractions ϕ .

Each curve is the average of 3 measurements, but for clarity the error bars are not represented here.

404 strain stiffening with the volume fraction for the two types of gels studied 405 here is also in agreement with this phenomenological explanation. As no 406 difference in the homogeneity of the gels is visible in the micrographs in Fig-407 ure 3, it can only be hypothesised that the difference is at smaller length 408 scales.

In addition, for gels at higher concentrations, the protein gels show a 409 slight softening in the non-linear regime, over one order of magnitude of 410 strain amplitude, before fracture of the material. This effect is absent in the 411 gels made of protein-stabilised droplets, where concentrated gels break at the 412 end of the linear regime. This difference in the stress-bearing behaviour of 413 concentrated gels may arise from structural differences between the networks; 414 which is similar to more dilute gels. Indeed, it seems that the breakage of 415 some bonds in the dense protein gels is not critical to the elasticity of the 416 overall network, and leads only to a moderate decrease of G' as the shear 417 amplitude increases. On the other hand, for the dense droplet gels, the 418 immediate drop in elasticity seems to indicate that the integrity of the whole 419 structure is degraded upon application of a critical shear stress σ_c . 420

This suspected difference in the structure of the two networks would thus possibly explain the different non-linear behaviours for protein gels and droplet gels. To test this hypothesis however would require imaging each of the gel samples over a wide range of lengthscales to quantify the structural heterogeneity not only over the scale of the fractal clusters, but also over the scale of the stress-bearing backbone.

Finally, a common feature of all the protein and droplet gels is the fracture of the material at very high shear, indicated by the decrease in their elasticity. The subsequent application of low-amplitude oscilllatory shear on the gels led to no time-dependent recovery of the viscoelasticity, as presented in Figure S8, which indicates that the gel structure was irreversibly damaged. This result is in agreement with an extensive study on the fracture of caseinate gels [28].

434 4. Conclusion

The full sequence of rheological measurement presented in Figure 2 and confocal imaging allowed a thorough characterisation of protein gels and droplet gels by their microstructure, linear and non-linear viscoelasticity, and frequency dependence. As the two types of gels are made with colloidal particles of different nature, their behaviour was characterised over a wide range of volume fraction, in order to discriminate the intrinsic differences
between the gels. Thus, in addition to the relevance of droplet gels to food
products like yogurt, this comparison also yields fundamental insights into
the nature of the gels.

The first notable result is the similar properties of the two types of gels 444 as a function of volume fraction ϕ_{eff} , derived from the viscosity of semi-445 dilute suspensions [34]. This result is significant, as the differences seen 446 in the gel properties of proteins and protein stabilised emulsions that have 447 been observed previously [40, 12] are accounted for by a careful choice of the 448 composition parameter. The approximation of the effective volume fraction 449 ϕ_{eff} held for the gels studied here, despite the complex structure of the 450 primary colloidal particles, caseinate assemblies in one case and caseinate-451 coated oil droplets in the other case. 452

When comparing the behaviour of protein gels and droplet gels in more 453 detail, some differences appear between the two types of system. First, at 454 fixed volume fraction, the droplet gels present a slightly higher elasticity 455 than protein gels, as can be seen by the slightly higher value for the storage 456 modulus G' and the lower phase angle. Then, the viscoelasticity of protein 457 gels is more frequency-dependent than for droplet gels, as both the storage G'458 and the loss G'' moduli vary more with frequency. The phase angle of droplet 459 gels also displays a non-monotonic behaviour with frequency that is not seen 460 for the protein gels. Finally, if the two types of gels at low concentrations 461 display strain stiffening at moderate shear amplitude, this behaviour is more 462 marked for the droplet gels, while for concentrated gels, the non-linear regime 463 is more extended for protein gels than for droplet gels. 464

These minor differences seem to indicate that the theoretical framework 465 of colloidal gels may not be sufficient for an entirely accurate description of 466 case in gels and case in-stabilised droplet gels. It may thus be necessary to take 467 into account some system-specific characteristics. It is possible that droplets 468 and protein assemblies have a different inter-particle interaction, as it is be-469 lieved that the single proteins adsorb at the surface of the droplets upon 470 emulsification, and these proteins change conformation as the hydrophobic 471 parts of their chains are anchored in the oil. Another possible explanation 472 is that the size difference between protein assemblies and droplets leads to a 473 different mobility of these two colloidal elements during gelation, which could 474 be the reason for a discrepancy of microstructure and consequently of rheo-475 logical behaviour. Finally, it is possible that a role is played by the softness 476 of the particles, as the protein assemblies are soft and water-swollen, while 477

the droplets have an incompressible oil core below the soft layer of adsorbedproteins.

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