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# Experimental investigation of the early-age mechanical behaviour of oil-well cement paste

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- 8

#### 9 ABSTRACT

10 The knowledge of the behaviour of oil-well cement paste from the early age to the hardened state is 11 important in predicting the performances of the cement sheath in oil/gas wells, specially for prediction 12 of the risk of micro-annulus creation between the cement sheath and the rock formation or the casing. 13 Characterization of the early-age mechanical behaviour is of particular importance, because during the 14 well construction, the cement sheath is submitted to various mechanical loadings when the cement 15 paste is not completely hydrated, as for example during a casing test. In this paper, the early-age 16 mechanical behaviour of a class G cement paste is studied experimentally. A specially designed 17 experimental device is used to investigate the mechanical behaviour of cement paste from the first 18 hour of hydration, under stress states close to in-situ conditions. The macroscopic shrinkage of the 19 cement paste as well as its stress-strain response under oedometric loading are studied for various pressures during hydration, from 0.3 to 45 MPa, and for hydration temperatures from 7 to 30°C. 20 21 These relatively low temperatures are used to slow down the hydration rate. The experimental results 22 show that the macroscopic shrinkage increases significantly with the pressure during hydration. When 23 submitted to a mechanical loading cycles at a given age, the cement paste hydrated under lower 24 pressures, corresponding to shallower depth, exhibits higher deformability, showing a higher risk of 25 creation of a micro-annulus during the mechanical loadings, as for example during a casing test. The 26 experimental results clearly show the influence of the loading history on the mechanical behaviour of 27 the cement paste at a given age. The oedometric experiments are associated with UCA (Ultrasonic 28 Cement Analyser) and isothermal calorimetry experiments for a deeper insight into the behaviour of 29 early age cement paste.

Keywords: early-age, cement hydration, shrinkage, stress-strain response, cement sheath, residual
 strain.

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#### 32 **1. Introduction**

33 In oil and gas industry, when drilling exploration or development wells, a mud is used to support the 34 walls of the geological formation, to maintain the wellbore stability, to cool and clean the drill bit, to 35 carry out the cuttings and to provide hydrostatic pressure which helps in preventing formation fluids to 36 enter into the wellbore. Steel tubular (called "casing") is then run into the well and a cement slurry is 37 pumped to fill the annulus space between two casings or between the casing and the geological 38 formation. The cement slurry hardens progressively and forms a cement sheath, which plays an 39 important role for well integrity. Along the well, it provides zonal isolation of different fluids (i.e. 40 separation of different fluids, water, gas and oil); it protects the tubular against corrosion and provides 41 mechanical support. The loss of cement-sheath integrity can result in the pressurization of the annulus, 42 in gas migration up to a shallower formation or to the surface, and, in catastrophic cases, in a blowout 43 and significant damage of the infrastructure.

44 The cement paste is an evolving porous material, its state changes progressively from fluid to solid 45 during the hydration process. Along a well, different compositions of cement slurries can be used and 46 their hydration takes place in different conditions of temperature and pressure depending on depth. 47 Therefore, at a given time, cement paste behaviour and properties depend on the slurry composition of 48 the cement paste including water-to-cement mass ratio (w/c), presence of additive agents, hydration 49 conditions in terms of temperature and pressure. In addition, during the life of a well, from drilling to 50 completion, production and P&A (plug and abandonment), the cement sheath is submitted to various 51 mechanical and thermal loadings that can potentially damage its principal properties and alter its 52 performance. According to some authors [1, 2] the increase of pressure during drilling can excess 40 53 MPa in the oil wells, and the applied pressure during a casing test can vary from a few tens of MPa in 54 normally pressurized reservoirs to more than 80 MPa in high pressure reservoirs. These loadings may 55 result in non-reversible deformation of cement sheath and consequently the creation of a micro-56 annulus in the cement-casing or cement-rock interface. This is particularly important when these 57 loadings are applied at relatively early age, when the mechanical properties and strength of the cement 58 paste are not yet completely developed. As it was reported in the literature [3, 4, 5], at the early-age, 59 the shrinkage of cement paste and the decrease of its pore pressure are considered to be the main 60 causes of leakage in oil and gas wells. However, very few experimental data exist on the mechanical 61 properties (macroscopic shrinkage, elastic modulus, the stress-strain behavior) of the hydrating oil-62 cement in field conditions and at very early age. Some properties, particularly the macroscopic 63 shrinkage, have been extensively studied for civil engineering applications in which the cement paste 64 is hydrated under ambient pressure and temperature conditions. The situation is quite different for oil-65 well applications in which the cement paste is hydrated under various conditions of pressure and 66 temperature, depending mainly on the depth and reservoir conditions.

67 This work is dedicated to an experimental study of the mechanical behavior of early-age cement paste, 68 during the first 6 days of hydration under various pressures and temperatures. A specially designed 69 experimental device is used to investigate the macroscopic shrinkage of cement paste and its stress-70 strain response under oedometric conditions, from the first hour of hydration. To investigate the effect 71 of early-age loading history on long-term properties, classical triaxial experiments are performed on 72 hardened samples submitted to various loadings at their early age. The tested material is a class G oil-73 well cement, with water-to-cement ratio equal to 0.44. The same material has been continuously 74 studied by the co-authors providing a rich database of mechanical, hydraulic, thermal and 75 microstructure properties [6, 7, 8, 9, 10, 11, 12, 13, 14] [15]. The hydration conditions correspond to a 76 temperature range from 7 to 30°C and a pressure range from 0.3 to 45 MPa. These relatively low 77 temperatures are used to slow down the cement hydration kinetics. These experiments are associated 78 with UCA (Ultrasonic Cement Analyser) and isothermal calorimetry experiments for a deeper insight 79 into the behaviour of early age cement paste.

#### 80 **2. Experimental devices and tests procedures**

81 To study the mechanical behavior of the cement paste at very early-age, one should be able to apply 82 mechanical loadings on the hydrating paste without modifying its hydration conditions of temperature 83 and pressure. This is a difficult task in a classical testing procedure in which the sample's temperature 84 and pressure are generally brought back to ambient conditions before installing it in the loading cell. 85 The hydration progress during this procedure and the dependence of the cement paste microstructure 86 on temperature during hydration make it difficult to control the conditions at which the experiment is 87 performed. To overcome these difficulties, a special uniaxial strain (oedometric) cell was designed by 88 TOTAL in which the cement paste is poured immediately after mixing, and hydrated under controlled 89 conditions of temperature and pressure. The cement paste can be submitted to mechanical loading 90 cycles, at any time even before setting, without modifying its hydration conditions, what is impossible 91 in a standard triaxial cell.



Figure 1. Uniaxial-strain (oedometric) equipment

92 The oedometric cell, shown in Figure 1, is composed of a hollow cylinder (50.3 mm of internal 93 diameter, 90 mm of external diameter and 125 mm height) made of steel. Within its elastic domain, 94 the hollow cylinder can support a maximum pressure of 123 MPa applied on its inner surface. The 95 hollow cylinder is surrounded by a cooling/heating system, connected to a cryostat, whereby cold/hot 96 fluid is circulated through a small-diameter tubing. The axial displacement of the sample is measured 97 by a Linear Variable Differential Transformer (LVDT). An electromechanical ram, able to apply 650 98 kN, is used to apply the axial stress. The oedometric cell is cooled or heated to the test temperature 99 before the preparation of the slurry.

100 The tested specimen has a diameter of 50.3 mm and a height of 85mm. The axial displacement of the 101 cement paste is measured continuously during hydration. At a given age, a mechanical loading cycle is 102 applied to the hydrating paste to measure its oedometric (P-wave) modulus and to study its stressstrain response. In order to compare this "static" oedometric modulus with the dynamic (P-wave 103 104 modulus), experiments are performed in similar hydration conditions using an Ultrasonic Cement 105 Analyzer (UCA) apparatus which permits to continuously measure the P-wave velocity (at ultrasonic 106 frequency) on the hydrating cement paste. In oedometric cell, as well as in UCA apparatus, the 107 properties of the hydrating cement paste are measured as function of time. In order to analyze the 108 experimental results as a function of the degree of hydration, a high pressure high temperature (HPHT) 109 calorimeter is used to evaluate the hydration kinetics from the measurement of hydration heat. A 110 standard triaxial cell is also used to analyse the effect of loading history at very early-age on the long-111 term properties.

112 To analyze the pore size distribution, the mercury intrusion porosimetry (MIP) is performed on

113 samples with different histories of hydration. The sample dimensions are 25 mm in diameter and 20

114 mm in height. After drying the samples by freeze-drying, the mercury is injected into the sample under

- 115 controlled pressure. At each pressure level the quantity of injected mercury enables calculating the
- 116 porosity and the applied pressure is used to estimate the corresponding pore entry size.

All tests were performed on a slurry made of CEMOIL class G cement (API classification), the chemical composition of which is presented in Table 1. The cement slurry is composed of class G cement powder, distilled and deaerated water with w/c = 0.44, and three additive agents (anti-foaming, dispersing and anti-settling), as presented in Table 2.

Chemical composition	Measures	API recommendation Spec 10A	
Magnesium oxide (MgO) %	1.8	Max 6.0	
Sulfurtrioxide (SO3) %	2.5	Max 3.0	
Loss on ignition %	0.6	Max 3.0	
Insoluble residue %	0.10	Max 0.75	
C <sub>3</sub> A %	2.1	Max 3.0	
$C_4AF + 2 C_3A \%$	17.4	Max 24.0	
C <sub>3</sub> S %	58.9	Min 48.0/ Max 65.0	
$(0.658 \times K_2O) + Na_2O \%$	0.55	Max 0.75	

#### Table 1. Chemical Composition of a class G cement (Blaine = 323 m<sup>2</sup>/kg)

122

121

123	Table 2. Composition of 600 ml of cen	nent slurry: w/c = 0.44, d	$ensity = 1900 \pm 10 \text{ kg/m3}$
	1	· · · · · · · · · · · · · · · · · · ·	

Components	Quantity (grams)			
Cement (class G)	783.53			
water (distilled and deaerated)	339.54			
Anti-foaming (D047)*	6.27			
Dispersing agent (D604AM)*	9.47			
Anti-settling (D153)*	1.18			
* commercial identification of the product				

124

125

Distilled and deaerated water is poured into the mixing container, which is then placed on the mixer base. The dry anti-settling agent is added to the water and the motor is turned on and maintained to  $4000 \pm 200$  rotations per minutes for 5 minutes of agitation. Then the liquid anti-foaming and dispersing agents (poured before cement) and the cement powder are put successively into the container in  $20 \pm 5$  seconds, (according to API [16], cement powder shall be added in 15s). The speed is immediately increased to about  $12\ 000 \pm 500$  rotations per minute and mixing ended automatically after  $35 \pm 1$  seconds.

#### **3.** Reliability and repeatability of the oedometric tests

In order to test the reliability of the oedometric test, distilled water is put into the cell. The mechanical loading path of Figure 2a consists of an increase of the axial stress from 5 to 25 MPa, followed by a decrease from 25 to 5 MPa. After maintaining the axial stress at 5 MPa for about 5 minutes, the same loading is again applied. This experiment is equivalent to an isotropic compression on water. The slope of axial stress – axial strain curve gives the bulk modulus of water. The result, presented in Figure 2b, gives the bulk modulus of water equal to 2.09 GPa which is very close to the value found in the literature. Thus, we conclude that the oedometric cell gives reliable results.



141 Figure 2. Reliability test: (a) loading path, (b) stress-strain behaviour and bulk modulus.
142

143 The repeatability of the oedometric tests is examined by performing three different tests with similar 144 cement slurry and under the same conditions of hydration in terms of temperature and axial stress. The 145 cement slurry is put into the oedometric cell previously cooled down at 7°C and the axial stress is then 146 increased immediately to 25 MPa and kept constant. The evolution of the axial strain is measured as a 147 function of time (or hydration). The result is displayed in Figure 3 and shows an excellent 148 repeatability. In conclusion, the oedometric cell gives reliable and repeatable results. The 149 nomenclature of the tests adopted in this study is T followed by the temperature during hydration and 150 *P* followed by the axial stress or pressure during hydration. For example, T7P25 corresponds to the 151 sample hydrated at a temperature of 7°C and under an axial stress of 25 MPa.



Figure 3. Repeatability of the oedometric tests: three cement sample hydrated at 7°C and under 25 MPa of axial stress.

155

#### 156 **4. Experimental results and discussion**

157 During the cement hydration, the sum of the volumes of consumed cement clinker and water is higher 158 than the volume of the produced hydrates. The difference represents the *chemical shrinkage* [17, 18]. 159 The chemical shrinkage results in pore pressure decrease within the cement paste during hydration. As 160 a consequence, the effective stress increases and leads to a decrease of the external macroscopic 161 volume of the hydrating cement paste. When the cement paste is hydrated at constant ambient 162 temperature and under atmospheric pressure, this external volume decrease is called *autogenous* 163 shrinkage [19, 18]. A different term, macroscopic shrinkage, is generally used when the hydration and 164 the resulting volume change take place under pressure higher than the atmospheric pressure and/or 165 temperature different to ambient temperature [18, 20, 17]. The macroscopic shrinkage of cement paste 166 was measured in several studies [18, 20, 21] and more recently by Abuhaikal et al. [22]. In this 167 section, we present a method to measure the macroscopic shrinkage of the cement paste and its stress-168 strain behaviour without modifying the condition of hydration. The effect of temperature and pressure 169 of hydration on macroscopic shrinkage are analysed. The effect of age and macroscopic shrinkage on 170 stress-strain behaviour of cement paste are also analysed.

#### 171 **4.1. Hydration kinetics**

172 The experiments presented in this paper are performed on cement pastes hydrated in a temperature 173 range within 7°C and 22°C, under stresses between 0.3 and 45 MPa. It is known that the hydration 174 kinetics is generally accelerated by increasing the temperature and pressure during hydration [23, 24, 175 25, 26]. The knowledge of the hydration kinetics of the cement paste in the performed oedometric 176 experiments is important for a better understanding and interpretation of the results. A high pressure 177 high temperature calorimeter is used to evaluate the hydration kinetics from the measurement of 178 hydration heat. Calorimeter data provide the cumulative heat of hydration Q(t) released until a given 179 time t. The degree of hydration can be evaluated through the following equation:

180 
$$\xi(t) = \frac{Q(t)}{Q_{T_{CP}}}$$
(1)

181 where  $Q_{T_{CP}}$  is the total cumulative heat released at complete hydration, which can be estimated by 182 knowing the composition of the cement paste, using the following relation.

183 
$$Q_{\mathrm{T_{CP}}} = \sum_{\mathrm{X}} m_{\mathrm{X_{CP}}} Q_{\mathrm{T}}^{\mathrm{X}}$$
(2)

- 184 were  $m_{X_{CP}}$  represents the mass fraction of the compound X in the cement paste. The Table 3 gives
- 185 the details of calculation of  $Q_{\rm T CP}$ , assuming the main compounds of cement paste to be: water, alite,
- 186 belite, aluminate and ferrite. Detailed calculation of the volume fractions of the constituents for the
- 187 tested cement can be found in [27, 28].
- 188
- 189

 Table 3. Estimation of hydration heat of a class G cement paste (w/c = 0.44)

<b>Compounds</b>	Chemical composition	$\mathbf{Q}_{\mathrm{T}}^{X}$ (J/g)	<mark>m<sub>X_CP</sub></mark>	Q <sub>T_CP</sub> (J/g)
Water	H <sub>2</sub> O	<mark>0</mark>	<mark>0.3</mark>	
Alite	C <sub>3</sub> S	<mark>500</mark>	0.427	
Belite	$C_2S$	<mark>260</mark>	<mark>0.106</mark>	<mark>297</mark>
Aluminate	<mark>C₃A</mark>	<mark>900</mark>	<mark>0.010</mark>	
Ferrite	<mark>C₄AF</mark>	<mark>420</mark>	<mark>0.111</mark>	

191 The results are presented in Figure 4 as function of time for different conditions of hydration. For a 192 given temperature during hydration (Figure 4a), the degree of hydration increases with the increase of

193 pressure. The same effect is observed for different temperatures when the pressure during hydration is

194 kept constant (Figure 4b).





The presented results are compatible with the well-known pressure and temperature dependency of cement hydration kinetics [24, 29, 30, 25, 31, 27].

#### 200 **4.2.** Typical results of an oedometric test

201 The oedometric cell (presented above) is used to investigate the macroscopic shrinkage of cement 202 paste, its dependence on temperature and pressure, and also the stress strain behaviour of the cement paste. For a typical oedometric test, after mixing, the cement slurry is directly put into the oedometric 203 204 cell which is kept at the test temperature. The axial stress is then increased up to the stress during 205 hydration and keeps constant during the first 144 hours of hydration. At 144 hours, a mechanical 206 loading/unloading cycle is applied with a loading rate of 3 MPa/min. For the samples hydrated under 207 an axial stress higher than 5 MPa (Figure 5a), the loading path consists in a decrease of the axial stress 208 to 5 MPa followed by two cycles with an increase up to 65 MPa and a decrease to 5 MPa and finally 209 of an increase back to the initial axial stress during hydration. For the sample hydrated under axial 210 stress lower than 5 MPa (Figure 5b), the loading path consists in two cycles with an increase up to 211 65 MPa and a decrease to the axial stress during hydration.



Figure 5. Loading path at 144 hours of hydration for different stress during hydration: (a) more than
 5 MPa (b) less than or equal to 5 MPa. Duration of the cycles around 1h30min, loading rate 3 MPa/min.

The results of two typical tests in terms of axial strain as a function of time are shown in Figure 6 for two cement samples hydrated at 7°C, under 0.3 and 25 MPa, respectively. The experimental response is composed of two main parts. The first part up to 144 h for which the axial stress is kept constant (Figure 6a) shows that the macroscopic shrinkage is higher for the sample hydrated under a higher axial stress. The second part (Figure 6b) presents the response of the samples to the mechanical loading/unloading cycles and shows the lower compressibility of the sample hydrated under a higher stress. These results will be analysed in detail in the following.



Figure 6. Typical result for oedometric tests: two samples hydrated at 7°C and under 0.3 and 25 MPa

#### 4.3. Macroscopic shrinkage

225 The macroscopic shrinkage of the cement paste is measured for different conditions of hydration in 226 terms of temperature and stress. At fixed temperature ( $7^{\circ}C$ ) during hydration, the cement samples are 227 hydrated under different axial stresses, from 0.3 MPa to 45 MPa. The evolution of axial strain as a 228 function of time for five samples is presented in Figure 7a, showing a progressive increase of the 229 macroscopic shrinkage during hydration. The deformation of the sample hydrated under 0.3 MPa 230 becomes stable after 40 hours of hydration. This happens a little later, at about 50 and 60 hours 231 hydration, respectively for the sample hydrated under 3 MPa (T7P3) and 10 MPa (T7P10). The 232 deformation of the samples hydrated under 25 MPa (T7P25) and 45 MPa (T7P45) continues to 233 increase at 144 hours. These results show that at a given time, the macroscopic shrinkage is 234 significantly higher for hydration under higher stress. However, one should note that this observation 235 is influenced to some extent by the pressure dependency of cement hydration kinetics, as presented in 236 Figure 4. The results of three experiments under various pressures, for which calorimeter results were 237 available, are plotted in Figure 8 as a function the degree of hydration. Two distinguished responses 238 can be observed for macroscopic shrinkage under high and low pressures: the samples hydrated under 239 high pressure, i.e. 25 and 45 MPa, show almost similar response in terms of a quasi linear macroscopic 240 shrinkage evolution with the degree of hydration, while the sample hydrated under a low pressure of 241 0.3 MPa, shows a more nonlinear response. The initial slope of the axial strain – degree of hydration 242 response at the very beginning is very close to the one of the high-pressure samples. This should 243 correspond to the chemical shrinkage of the cement hydration, as before percolation and formation of 244 a solid skeleton all chemical shrinkage is transformed to the macroscopic shrinkage. A value of 0.044 245 -0.060 can be found for the chemical shrinkage of this cement which is very close to the values 246 presented in the literature [32, 5, 33, 34, 18, 35].

247 The measured axial strain, i.e. the macroscopic shrinkage, at 144 hours of hydration increases with the 248 axial stress during hydration (Figure 9a). Reddy et al. (2009) also observed this increase of 249 macroscopic shrinkage with the increase of stress applied on the cement paste during its hydration. 250 Figure 7b presents the evolution of the axial strain of the cement paste as a function of time, for 251 hydration under constant axial stress (25 MPa) but at different temperatures (7, 15 and 22°C). As 252 observed in this figure, the effect of temperature is more pronounced during the first 60 hours of 253 hydration and seems to vanish with the advancement of the reaction. The long-term effects of 254 temperature and pressure on macroscopic shrinkage at 144h are presented in Figure 9 for 7°C 255 temperature (variable stress) and 25 MPa axial stress (variable temperature). It can be seen that the 256 effect of temperature is less significant compared to that of stress (Figure 9b). This is of course partly 257 due to the relatively narrow range of the studied temperatures. The results show that higher pressure 258 during hydration leads to higher compaction of the samples. The density of the hydrated material is 259 thus expected to be higher for samples hydrated under higher pressure. The observed macroscopic 260 shrinkage during hydration results from strongly coupled phenomena: at the very early age and before 261 the percolation the slurry is under an isotropic stress state with the pore pressure equal to the total 262 pressure, i.e. zero Terzaghi effective stress. The water consumption during hydration results in a 263 progressive pore pressure decrease in the samples and thus to an increase of the effective stress. 264 Moreover, the progressive hardening of the material results in development of shear stress in the 265 sample which is in oedometric condition. These stress changes result in mechanical deformation of the 266 material which can be a combination of deformations with elastic, elastoplastic and viscous nature. For 267 the samples under lowest pressures, 0.3 MPa and 3 MPa, the water consumption may result in a partial 268 desaturation of the material. A better understanding of the mechanisms of deformation of the samples 269 needs a coupled chemo-poro-mechanical simulation of the presented experiments, taking into account 270 the above-mentioned phenomena.



Figure 7. Experimental measures of macroscopic shrinkage of cement paste during the first 144 hours of
 hydration: (a) constant temperature during hydration (7°C) [T7P10 and T7P3 are from [15]], (b) constant
 axial stress during hydration (25 MPa).



275

 Figure 8. Macroscopic shrinkage of three samples of cement paste hydrated at 7°C and under different stresses





Figure 9. Macroscopic shrinkage of the cement paste at 144 hours of hydration: (a) effect of the axial stress, (b) effect of temperature of hydration.

#### 281 4.4. Oedometric moduli

282 The oedometric moduli are measured in the performed oedometric experiments. The static modulus is 283 measured by performing mechanical unloading and reloading on the hydrating cement paste in 284 undrained condition. The measurements are performed for three samples M-T7P15, M-T7P25 and M-285 T7P45 hydrating at the same temperature (7°C), but under different axial stresses 15, 25 and 45 MPa, 286 respectively. "M-" before the test conditions is related to "modulus". The loading path is similar for 287 the three conditions. It is presented in Figure 10a for the sample M-T7P25, showing an unloading from 288 the axial stress during hydration (i.e. 25 MPa) to 5 MPa and reloading to the stress during hydration. 289 The unloading/reloading cycles were applied at different given times with the rate of 3 MPa/min. The 290 duration of one unloading/reloading cycle is around 7, 13 and 27 minutes for the samples M-T7P15, 291 M-T7P25 and M-T7P45, respectively. Considering the relatively slow hydration rate at 7°C, it can be 292 assumed that these loading cycles are performed at constant degree of hydration. The stress-strain response for one cycle of sample M-T7P25 is presented in Figure 10b. It can be assumed that the cycle is performed in the elastic domain and can be used to evaluate the elastic oedometric modulus. We chose to evaluate the tangent oedometric modulus on the unloading slope for axial stress between 12 and 7 MPa, between 20 and 15 MPa and between 30 and 15 MPa respectively for the samples hydrated under 15, 25 and 45 MPa. The different intervals are chosen to prevent the parasite strains observed at the beginning of the unloading or reloading, which are due to the mechanical system of the frame and to the inertia of the LVDT.

300



301Figure 10. Loading path and stress-strain response for a cement hydrated at 7°C and under 25 MPa302(sample M-T7P25)

303

304 The oedometric moduli for the three samples M-T7P15, M-T7P25 and M-T7P45 are given in Figure 305 11 as a function of time. During the first 15 or 20 hours of hydration, the moduli are relatively 306 constant and vary between 3 and 4 GPa. These values, as also observed by Vu (2012), are slightly 307 higher than the bulk modulus of water (around 2.2 GPa). The difference is probably due to the 308 presence of the clinker grains in the cement slurry. The stable values within this time window shows that the cement paste behaves like fluid with suspensions. There is a fast increase of the modulus 309 310 between 20 and 90 hours for the sample M-T7P15 and between 20 and 140 hours for the samples M-311 T7P25 and M-T7P45. This fast increase is followed by a slighter increase for the later hydration ages.



# Figure 11. Elastic, static oedometric modulus as a function of time for three cement samples hydrating at 7°C and under 15, 25 and 45 MPa.

315

The Ultrasonic Cement Analyser (UCA) is used to measure the ultrasonic P-wave velocity in the cement paste during hydration. The dynamic oedometric modulus  $E_{oed}^{dyn}$  can then be calculated using the following relation as a function of the P-wave velocity  $V_p$ , by knowing the density of the sample  $\rho$ **Error! Reference source not found.** 

$$E_{\rm ord}^{\rm dyn} = \rho V_{\rm P}^{\ 2} \tag{3}$$

321 At ultrasonic frequency, the pore pressure generated within the cement paste during the wave's 322 travelling do not have enough time to diffuse out of the sample. The measured dynamic modulus is 323 thus considered as undrained oedometric modulus. For the samples hydrated under pressure, the 324 average density of the cement paste increases during hydration, due to the compaction effect. For the 325 cement sample hydrated under 25 MPa, the evolution of the average density and of the P-wave 326 velocity during hydration are given in Figure 12. The density (resp. the P-wave velocity) of the cement 327 increases from approximately 1910 kg/m<sup>3</sup> (resp. 1400 m/s) for the slurry state to around 2000 kg/m<sup>3</sup> 328 (resp. 3200 m/s) after 300 hours of hydration. The dynamic modulus, calculated using equation (3) is 329 presented in Figure 13 and compared with the static modulus measured under similar condition of 330 hydration. The results exhibit a dynamic modulus slightly higher than the static modulus. This is in 331 agreement with existing experimental results showing that the dynamic modulus is generally higher 332 than the static modulus for different materials [36, 37, 38].



333

334Figure 12. Average density and ultrasonic P-wave velocity as a function of time for the cement sample335hydrating at 7°C and under 25 MPa [28].



338Figure 13. Comparison between the dynamic and static elastic "undrained" oedometric moduli for339samples hydrated at 7°C and under 25 MPa on the UCA and the oedometric cell, respectively.

337

#### 341 **4.5.** Stress–strain response

#### **4.5.1. Effect of age**

343 Seven samples of cement paste, with the same composition (Table 1 & Table 2), hydrated at 7°C and 344 under 25 MPa, are submitted to mechanical unloading/reloading cycles as shown in Figure 5a. Each 345 sample has been loaded at a different age, 15, 18, 20, 40, 60, 103 and 144 h. The results are presented 346 in Figure 14. The loading cycles applied at earlier age show a quite linear stress-strain response with 347 non-recoverable strains in unloading. The results show a progressively non-linear stress-strain 348 response for later loadings particularly after 40h. During the first loading (5  $\rightarrow$  65 MPa), two main 349 slopes can be distinguished on the samples loaded after 20 hours of hydration. These slopes may 350 characterize the elastic and elastoplastic domain of the response with a transition at the elasticity limit. 351 As presented in Figure 15, this stress limit increases with the degree of hydration (or age) at which the 352 mechanical loadings are applied. Moreover, the slope of the first unloading/reloading cycle  $(25 \rightarrow 5 \rightarrow 25 \text{ MPa})$  increases with the age of the cement paste. This is in agreement with the increase 353 354 of the elastic parameters of the cement paste with hydration as is observed also in the measured 355 oedometric modulus during hydration (Figure 11 & Figure 13).





356Figure 14. Stress-strain behaviour at different age of cement samples hydrated under similar oedometric357conditions (7°C and 25 MPa)





Figure 15. Elastic limit as a function of the degree of hydration

3624.5.2. Effect of loading history

363 As explained in the introduction, various mechanical loadings can be applied to the cement sheath in 364 an oil-well and it is important to investigate the effect of these early-age loadings on the long-term 365 behaviour of the cement paste. In order to analyse the effect of the previous mechanical loading cycles 366 on the stress-strain behaviour of cement paste at later age of hydration, the samples presented in the 367 Figure 14 have been for a second time submitted to the same mechanical loading at 144 hours. The 368 effect of this first mechanical loading on the cement behaviour is analysed by comparing the result of 369 their second loading with the stress-strain response of the sample submitted for the first time at 370 144 hours (Figure 14g). On the following figures, the samples are identified by the hydration 371 conditions and the time of their first mechanical loading. For example, T7P25-40 (solid line) 372 represents the sample hydrated at 7°C and under 25 MPa on which the first mechanical loading is 373 applied at 40 h. The mechanical loading previously applied at 15, 18 and 20 h (Figure 16a, b and c) 374 seem to have little effect on the stress-strain behaviour at 144 hours. The stress-strain curves are quite 375 similar, even though we can observe that the previously loaded samples are a little less deformable. 376 This is much more visible and significant for the samples loaded previously after 40 hours of 377 hydration. The stress-strain response of these samples shows a lower deformability, higher moduli and 378 lower irrecoverable strains in unloading.





379Figure 16. Effect of previous mechanical loadings applied within 15 h and 103 h on the stress-strain<br/>behaviour of the cement paste submitted to the same mechanical loadings at 144 hours.

382 After the loading at 144 hours, the samples T7P25, T7P25-15, T7P25-18 and T7P25-40 were 383 immediately removed from the oedometric cell and kept into distilled and deaerated water at ambient 384 conditions for at least 3 months. The mercury porosity measurements are then performed and the 385 results are shown in Figure 17. It is worth nothing that the only difference between these samples is 386 the age at which the first mechanical loading was applied. It can be observed that the first loading 387 applied at 15 or 18 h has no significance effect on the mercury porosity, as compared to sample T7P25 388 on which no further loading cycle has been applied (Figure 17). The loading applied at 40 h reduced 389 significantly the mercury porosity. In Table 4, it is shown that the mercury porosity as well as the total 390 porosity are smaller in sample T7P25-40 as compared to the other samples. The mercury and total 391 porosity are in the same order as those found by Ghabezloo et al. Error! Reference source not 392 found.. The decrease of the porosity with the application of the mechanical loading cycles is related to 393 the compaction of the cement sample.



394 395

Figure 17. Mercury porosity on cement paste as a function of the reached pore diameter

396 397

 Table 4. Physical properties of four samples conserved in water at ambient conditions for at least 3 months after the application of the mechanical loading cycles at 144 hours.

	T7P25	T7P25-15	T7P25-18	T7P25-40
Mercury porosity (%)	26.7	27.5	26.2	23.4
Saturated density (g/cm <sup>3</sup> )	2.022	2.022	2.010	2.005
Total porosity (%)	43.5	43.1	43.3	42.8

#### 399

### 4.5.3. Effect of temperature and pressure conditions during hydrafion

400

#### At 144 hours of hydration

401 The stress-strain responses of the samples hydrated under different conditions of temperature and axial 402 stress are presented in Figure 18 (the first phases of these experiments are presented in Figure 7). The 403 experiments performed at 7°C under different initial axial stresses are shown in Figure 18a. 404 Comparing the curves shows that the samples hydrated under higher stress are less deformable during 405 the first loading. For samples hydrated under relatively high stress (10 and 25 MPa), for the first 406 loading until 65 MPa the sample shows a quasi bilinear response corresponding to an elastic response 407 under lower stresses and then an elasto-plastic response for higher stresses with a smooth transition at 408 about 25 to 30 MPa axial stress. The following unloading-reloading cycles result in an almost linear 409 response with a little hysteresis which may be attributed to the viscous behaviour of the cement paste 410 [12]. The samples hydrated under relatively low stress (0.3 and 3 MPa) show a more complex 411 response under the first loading up to 65 MPa. A first change in the slope of the stress-strain curve is 412 observed at 20 to 25 MPa axial stress, similar to the one observed for samples hydrated under higher 413 stress, but a second slope change and a significant hardening of the material is observed under higher 414 axial stress of about 45 to 50 MPa. The physical mechanism behind this hardening of the material can 415 be explored considering an elasto-plastic constitutive law for hydrating cement paste based on these 416 experimental results [28]. Figure 18b presents the results of the experiments performed on cements 417 hydrated under 25 MPa axial stress at different temperatures between 7 and 22°C. The results show 418 quite similar response, which can be related to the narrow range of studied temperatures. One can see 419 however that the samples hydrated under higher temperature are less deformable. This can be related 420 to the increase of the cement hydration rate with temperature. The analysis of the results presented in 421 Figure 7 and Figure 18 shows a strong coupling between the macroscopic shrinkage and stress-strain 422 response of the cement paste. An appropriate constitutive model for the hydrating cement paste should 423 capture this coupling and the physical mechanisms behind the observed response of this material. 424 Another general observation, which can be made based on these experimental results, corresponds to 425 the significantly higher deformability of the cement paste hydrated under relatively low stress. This 426 higher deformability shows the higher risk of creation of a micro-annulus at shallower depths of a 427 well.



Figure 18. Experimental measures of stress-strain behavior of cement paste at 144 hours of hydration: (a)
 constant temperature during hydration (7°C), (b) constant axial pressure during hydration (25 MPa).

#### 431 • After 3 months of hydration

432 Three samples hydrated at the same temperature (7°C) but under different axial stresses 3, 10 and 433 15 MPa (T7P3, T7P10, T7P15) have been submitted to triaxial testing after 3 months of hydration. 434 The samples were submitted to the same mechanical loading path at 144 hours as presented in Figure 435 5. The samples were then kept at the ambient temperature in saturated condition for 3 months before 436 performing triaxial experiments. These experiments have been performed under a confining pressure 437 of 25 MPa. The differential stress as a function of axial and radial strain is presented in Figure 19. The 438 results clearly show that the stress-strain behaviour of the cement paste is affected by the condition of 439 hydration during the first 144 hours. Samples hydrated under lower stress show higher deformability 440 and lower shear strength. This confirms once again the higher potential of micro-annulus formation at 441 shallower depths.





Figure 19. Results of the triaxial tests on the cement paste hydrated under oedometric conditions during
 the first 144 hours and kept at ambient conditions for 3 months. The confining pressure was 25 MPa [15]
 446

447 The mechanical static and dynamic properties of the samples are presented in Table 5. The static 448 moduli have been evaluated in the unloading-reloading cycles. The static drained bulk and Young 449 moduli increase with the increase of the axial stress during hydration applied on the samples during 450 the first 144 hours of hydration. As commonly observed, the dynamic bulk modulus and Poisson's 451 ratio are higher compared to the static values. The explanation of this difference can be traced to the 452 fact that the dynamic parameters are measured under quasi-undrained conditions whereas the statics 453 ones are obtained under drained conditions. It can also be due to the amplitude of deformation which is much smaller for dynamic measurements (around  $10^{-7} - 10^{-6}$  in dynamic measurements, and  $10^{-3}$  in 454 455 static measurements [39]) as also mentioned by Oku and Eto (1993). The effect of hydration 456 conditions in these samples shows that the cement paste stiffness in long-term increases with the 457 increase of the stress applied during the early-age of hydration.

459Table 5. Static and dynamic parameters of three samples of cement paste hydrated under oedometric<br/>conditions during the first 144 hours and kept at ambient conditions for 3 months.

	Static parameters			Dyna	mics parar	neters
Samples	T7P15	T7P10	T7P3	T7P15	T7P10	T7P3
K <sub>d</sub> (GPa)	7.56	7.16	6.95	16.32	16.15	16.25
G (GPa)	7.08	6.56	5.56	8.21	8.36	8.34
ν	0.14	0.15	0.18	0.31	0.30	0.30
<i>E</i> (GPa)	16.18	15.08	13.17			
Eoed (GPa)	16.99	15.91	14.36			
$\Delta(\sigma_{ax} - \sigma_{rad})_{max}$ (MPa)	81	76	64			

#### 461 **5.** Conclusion

462 The early-age mechanical behaviour of a class G oil-well cement paste is experimentally investigated 463 using a specially designed cell, which permits mechanical loading application from the first hour of 464 hydration, even before the setting of the cement. The macroscopic shrinkage of the cement paste as 465 well as its stress-strain response under oedometric loading are studied for various pressures during 466 hydration, from 0.3 to 45 MPa, and for temperatures during hydration from 7 to 30°C. The results 467 showed a significant increase of the macroscopic shrinkage with the pressure during hydration. At a 468 given age, the cement paste hydrated under lower pressures exhibits a significantly higher 469 deformability when submitted to a mechanical loading cycle. This result shows a higher risk of 470 creation of micro-annulus at shallower depth during the mechanical loadings, for example during a 471 casing test. The stress-strain response of the cement paste strongly depends on the cement age. When 472 submitted to a loading cycle at different times, a mostly linear and reversible response observed at the 473 very early age is progressively transformed to a highly nonlinear response and increasing irreversible 474 deformations. At a given time, the mechanical response of the cement paste submitted to a loading 475 cycle depends on the loading history. This is an important point showing that the simulation of the 476 cement sheath response in an oil well needs a complete modelling of its behaviour from the placement 477 to the current state, including various applied loads. This is confirmed also for the long-term behaviour 478 by performing classical triaxial experiments after 3 months hydration on cement samples with 479 different loading history at early age. The samples submitted to lower stress at early age show higher 480 deformability. In the studied ranges of pressure and temperature, the pressure has a much more 481 significant effect on the mechanical response of the cement, compared to the temperature effect. 482 However, one should note that a relatively narrow range of mostly low temperature are investigated 483 here, mainly to slow down the hydration rate for performing loading cycles application in a relatively 484 constant hydration degree. This study will be extended in the future by exploring a broader range of 485 higher temperatures.

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