



HAL
open science

Carbon dioxide methanation kinetic model on a commercial Ni/Al₂O₃ catalyst

Isabelle Champon, Alain Bengaouer, Albin Chaise, Sébastien Thomas,
Anne-Cécile Roger

► **To cite this version:**

Isabelle Champon, Alain Bengaouer, Albin Chaise, Sébastien Thomas, Anne-Cécile Roger. Carbon dioxide methanation kinetic model on a commercial Ni/Al₂O₃ catalyst. *Journal of CO₂ Utilization*, 2019, 34, pp.256 - 265. 10.1016/j.jcou.2019.05.030 . hal-03484503

HAL Id: hal-03484503

<https://hal.science/hal-03484503v1>

Submitted on 20 Dec 2021

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution - NonCommercial 4.0 International License

Carbon dioxide methanation kinetic model on a commercial Ni/Al₂O₃ catalyst

Isabelle Champon^{1,2,3}, Alain Bengaouer¹, Albin Chaise¹, Sébastien Thomas², Anne-Cécile Roger²

¹Université Grenoble Alpes, CEA, LITEN, DTBH, SCTR, LER, 17 Avenue des martyrs, Grenoble F-38054, France

²ICPEES-ECPM, UMR 7515, University of Strasbourg, 25 rue Becquerel, F-67087 Strasbourg, France

³French Environment and Energy Management Agency, 20 avenue du Grésillé, BP 90406, F-49004, Angers Cedex 01, France

Corresponding author: alain.bengaouer@cea.fr (Alain Bengaouer)

Abstract

Intrinsic kinetic characterization of the carbon dioxide methanation was determined over a commercial 14-17 wt.% Ni/Al₂O₃ between 623 K and 723 K at atmospheric pressure in the absence of heat and mass transfer limitations. Following a Hougen-Watson formalism, both direct path (CO₂ methanation rate equation) and indirect path (Reverse Water Gas Shift rate equation + CO methanation rate equation) were described. As a first step, kinetic tests were performed operating in differential mode to evaluate the reaction rate dependence on reactants and products partial pressure at different temperatures in order to select the form of each reaction rate equation. Kinetic models available in the literature were evaluated and compared with the experimental results and model adaptations were proposed to identify the kinetic laws that fit the best the experimental values. Kinetic and adsorption parameters were calculated from these laws. Then, the identified parameters were adjusted simultaneously on experimental tests from 5% to 75% CO₂ conversion using an isothermal plug-flow reactor. The three reaction rates and their reverse reactions were identified in order to minimize the error on CO₂ conversion and CH₄ and CO selectivities at 623 K, 673 K and 723 K. The final identified kinetic model was able to reflect the kinetics from differential conversion to thermodynamic equilibrium with an accuracy of 20% on the CH₄ formation rate for the three temperatures.

Keywords: carbon dioxide, methanation, Power-to-Gas, intrinsic kinetics, Ni/Al₂O₃ catalyst

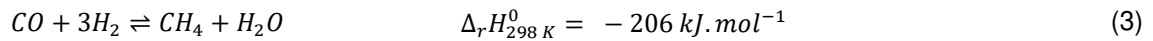
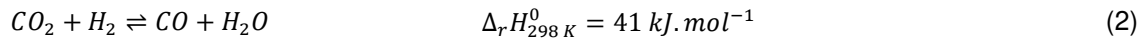
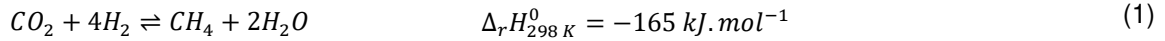
1. Introduction

The CO₂ methanation reaction is of great interest today in the case of Power-to-Gas technologies [1–7]. Actually this reaction, also called the Sabatier reaction [8], produces Substitute Natural Gas (SNG) and enables the CO₂ valorization (from biomass or industrial flux gases for instance) in order to reduce the greenhouse gas emissions. Moreover, Power-to-Gas is known as one of the solutions to store the excess and intermittent electricity production from renewable energy [4]. Hydrogen is first synthesized by water electrolysis, and then combined with carbon dioxide to produce methane and water. Thereafter, methane can be injected in the gas grid and is more easily stored than hydrogen. It can be transported *via* the gas grid, and be used in a great variety of end-use applications (heat, mobility, *etc.*) [4].

The CO₂ hydrogenation into CH₄ (reaction (1)) is balanced, highly exothermic, favored at low temperatures and high pressures.

As reactions in gas phase are extremely slow at moderate temperatures and pressures, a catalyst is needed to obtain an acceptable reaction rate and methane selectivity [5]. Supported catalysts are widely used to perform CO₂ methanation. Usually, they are composed of a metallic active phase (Ni, Ru, Rh, Co), dispersed on an oxide support (Al₂O₃, CeO₂, SiO₂, *etc.*). Nickel based catalysts supported on alumina are the most largely employed because of their high performance/cost ratio [3].

The CO₂ methanation can also be a combination of Reverse Water Gas Shift (RWGS) and CO methanation (balanced reactions (2) and (3)) [9].



Several authors have studied the CO and CO₂ methanation kinetics. Some studies use a simple power rate law [10–12]. However, more rigorous models result from reaction mechanism considerations and follow the Hougen Watson formalism. A recent review introduced exhaustively the CO and CO₂ methanation kinetics [6].

Xu and Froment [13] proposed three reaction rates on a 15.2 wt.% Ni/MgAl₂O₄ catalyst, derived from methane steam reforming, CO₂ methanation and reverse water gas shift experiments. Experimentally, the fixed-bed reactor was operated in integral mode (reaction rates cannot be considered as constant along the catalyst bed) with 400.0 mg of commercial catalyst diluted with α -alumina. The data used for the kinetic study were recorded after 70 h on stream to stabilize its activity. The conditions of the experiments were 573 to 673 K, 300 to 1000 kPa and 6 to 30 ml (STP) min⁻¹. They employed a Marquardt routine to estimate the kinetic parameters by minimization of the sum of weighted residual squares of the conversions, the latter being calculated by the fourth-order Runge-Kutta routine. Finally, they identified 14 parameters: activation energies and pre-exponential factors of the 3 kinetic constants corresponding to the three reactions (Eqs (1), (2), and (3)), following an Arrhenius law and heat of adsorption and pre-exponential factors of 4 adsorption constants, as Van't Hoff-type. However, they obtained a negative heat of adsorption for water, which has no physical meaning.

Ducamp *et al.* [14] proposed a kinetic model based on the Xu and Froment kinetic formalism and adjusted on 15.0-26.0 mg of a commercial 17 wt.% Ni/Al₂O₃ catalyst diluted in SiC and operating in integral mode. The conditions of the experiments were 553 to 673 K, 100 to 1000 kPa and 120 – 125 ml (STP) min⁻¹ in stoichiometric conditions for the CO₂ methanation and in hydrogen excess for the CO methanation – in order to slow down the catalyst deactivation. Only the three kinetic constants and the CO adsorption constant were identified. All other constants were unchanged, even if the two catalysts were different and if the water heat of adsorption was negative.

Weatherbee and Bartholomew [15] measured the rate of CO₂ hydrogenation on 300.0 mg of a 3 wt.% Ni/SiO₂ catalyst, between 500 and 600 K, 140 to 175 kPa, and 500 to 1500 ml (STP) min⁻¹. The CO₂ conversion was limited to 10%, so the reactor was operated in differential mode. H₂ and CO₂ partial pressure rate dependence were established. As CO was produced by the reaction (Eq (2)), some tests were performed with CO at the inlet of the reactor. The CO₂ methanation rate decreased in the presence of CO. A kinetic law for the CO₂ methanation reaction was proposed, assuming the formation of adsorbed CO which could further dissociate or desorb. Nevertheless, they neglected the CO methanation path which could also form CH₄.

Recently, Koschany *et al.* [16] studied the CO₂ methanation kinetic in differential mode considering only the direct path (Eq (1)), neglecting the reverse water gas shift reaction because the CO content in the product gas was below 1000 ppm. They prepared a co-precipitated NiAl(O)_x catalyst. A mass of 25.0 to 75.0 mg of catalyst (30-90 wt.% Ni) diluted in SiC was stabilized for 300 h on stream. Temperature was varied between 453 and 523 K. Pressure was limited to 2000 kPa and flow rates were set from 45 to 75 ml (STP) min⁻¹.

Miguel *et al.* [17] determined the intrinsic kinetics of CO₂ methanation over a commercial calcium aluminate catalyst (20-25 wt.% NiO). Temperature varied between 523 and 623 K at atmospheric pressure. 12.0 to 40.0 mg of catalyst was employed for a total feed flow rates of 30-100 ml (STP) min⁻¹.

At an industrial or pilot scale, different reactor types are used (fluidized bed reactors, adiabatic or cooled fixed-bed reactors, micro-reactors, metallic-foam reactors, structured coated reactors or milli-structured fixed-bed reactors-exchangers) [6,18,19,14,20].

The purpose of this study is to develop a new kinetic model accounting for the direct (Eq (1)) and indirect paths (Eqs (2) + (3)) of the CO₂ methanation reaction with a 14-17 wt.% Ni/Al₂O₃ commercial catalyst from 623 K until 723 K at atmospheric pressure. The temperature range of this study is explained by the fact that the proposed kinetic model is intended to be used to describe the behavior of a milli-

structured fixed-bed reactor-exchanger channel. The temperatures of interest are therefore around 573 K.

2. Experimental Study

2.1. Equipment and materials

Experimental kinetic tests were performed at atmospheric pressure, between 623 K and 723 K on a 14-17 wt.% Ni/Al₂O₃ commercial catalyst. Catalyst (mass between 1.5 mg and 10.0 mg) was diluted in SiC ($4 < \Psi < 32$) in the grain size range 125 – 250 μm.

Kinetic measurements setup was divided in three parts: gas alimentation and mixing, reaction zone and analysis section. Mass flow controllers commanded the gas feeding of the six lines (H₂, N₂ – internal standard for the GC analysis, CO₂, CH₄, CO, and Ar). The pure gases were mixed together before the reaction zone and heated up using heating tapes. Liquid water was injected into a vaporization chamber by a micro-pump (GILSON - Model 321322350), and steam mingled with the gas mixture. All the tubes were heated after the vaporization chamber to avoid water condensation. A tubular furnace, constituting the reaction zone, heated the glass reactor until 773 K. The reactor was 30 cm long and 3.0 mm inner diameter. The catalyst bed was fixed with quartz wool and located inside the isothermal zone of the furnace. A thermocouple measured the temperature at the end of the catalyst bed. After the reaction zone, a cold trap condensed the water. The dry gas mixture entered the analysis zone composed by a micro gas chromatography (INFICON 3000 MICRO GC) equipped with two columns. The MS5A module was used to separate H₂, N₂, CH₄ and CO and the PPQ module to separate CH₄, CO₂ and C₂H₆ (if present). Both were equipped with TCD detectors. For one condition (temperature/flow rate), the catalyst was hold until stabilization of the conversion (45 minutes to 60 minutes) and an average of the 15 last minutes (4-5 points) was taken as the mean value of conversion.

2.2. Pretreatment of the catalyst

A step of catalyst activation under hydrogen was needed to reduce NiO into Ni⁰ (Eq (4)):



A temperature-programed reduction (TPR) was realized to establish the reduction conditions. TPR was conducted with 10% H₂ in Ar with a total flow of 50 ml (STP) min⁻¹; heating rate 10 K min⁻¹ - 1273 K, holding for 60 min (see Figure 1). The first reduction zone, below 673 K, was associated with the reduction of bulk NiO and the second one, above 673 K, with NiO in strong interaction with NiAl₂O₄. Following the industrial recommendations and in order to obtain a catalyst as stable as possible, only the bulk NiO reduction was sought by *in situ* reduction. Consequently, the reactor was heated up under a mixture 50% H₂ in N₂, with a total flow of 16 ml (STP) min⁻¹ at 5 K min⁻¹ until 673 K and was kept at 673 K for 1h.

Before starting the kinetic tests, the catalyst was stabilized by thermal cycling under reactive flow (H₂/CO₂/N₂: 74/17/9): 673 K (1h), 723 K (1h) and 748 K during one night (15 h). The repetition of the activity tests at 623 K (1h) – 673 K (1h) – 723 K (1h) showed a stable catalytic activity.

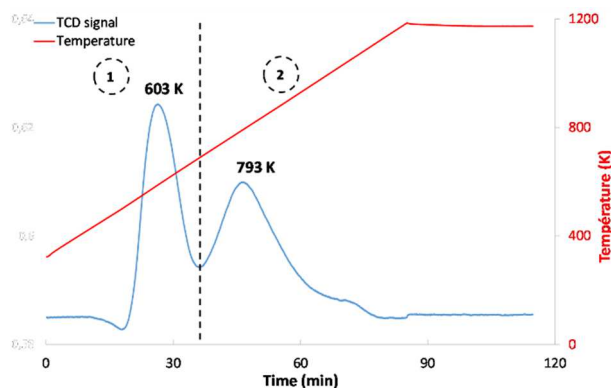


Figure 1 : Reduction profile of the commercial catalyst Ni/Al₂O₃

2.3. Diffusional limitations

Catalyst was diluted in SiC because of its thermal properties but also to increase the height of catalytic bed to obtain a plug flow reactor behavior. The plug flow assumption inside the reactor was validated

theoretically by the absence of axial dispersion ($h_{bed}/d_p > 50$ [21,22]) and radial dispersion ($d_t/d_p > 8$ [23]). The relative pressure drop over the catalyst bed was less than 20% and can be neglected [24].

To ensure the determination of the intrinsic chemical kinetics, both external and internal diffusional limitations were checked at 723 K (maximal temperature of the study). The results are presented in Figure 2.

For the verification of the absence of external transport resistances, the feed flow rate and the catalyst mass were varied, keeping the same ratio flow rate/catalyst mass (same GHSV). The CO₂ conversion obtained with catalyst mass $m = 1.5$ mg and flow rate $Q = 27.5$ ml (STP) min⁻¹ was very close to the one obtained for mass $2m = 3.0$ mg and flow rate $2Q = 55.0$ ml (STP) min⁻¹ at 673 K and 723 K and far from thermodynamic limitations (see Figure 2 (a) for a GHSV = $9.60 \cdot 10^5$ h⁻¹). Similarly, the CO₂ conversion obtained with catalyst mass $m = 1.5$ mg and flow rate $Q = 41.3$ ml (STP) min⁻¹ was very close to the one obtained for mass $2m = 3.0$ mg and flow rate $2Q = 82.5$ ml (STP) min⁻¹ at 723 K and far from thermodynamic limitations (see Figure 2 (a) for a GHSV = $1.44 \cdot 10^6$ h⁻¹).

The external diffusion is promoted by the gas velocity increase, however, as similar conversions were obtained in both cases, the external diffusion can therefore be considered as not limiting for total flow rates over 27.5 ml (STP) min⁻¹.

For the internal diffusional limitations, the size of the catalyst particles was varied between 63 μm and 400 μm in several fragments by crushing and sieving: 63-125 μm, 125-250 μm, 250-315 μm, 315-400 μm. The internal limitations are well seen from CO₂ conversion obtained for 315-400 μm to 63-125 μm fractions (Figure 2 (b)). However, the relative pressure drop over the catalyst bed with 63-125 μm fraction was not negligible. Moreover, the CO₂ conversion relative gap between 125-250 μm fraction and 63-125 μm fraction is less than 7%. Hence, it was assumed that the internal diffusion was not significantly limiting for the grain size 125-250 μm, even if the transport resistance inside the grain is not zero. Thus, the kinetic study is performed with particles size between 125 and 250 μm.

Also, the theoretical heat and mass transfer limitations verifications were calculated according to the Mears-Anderson-Weisz-Prater criteria (see appendix A for details) to verify that the kinetic measurements were not affected by the mass and thermal diffusion limitations.

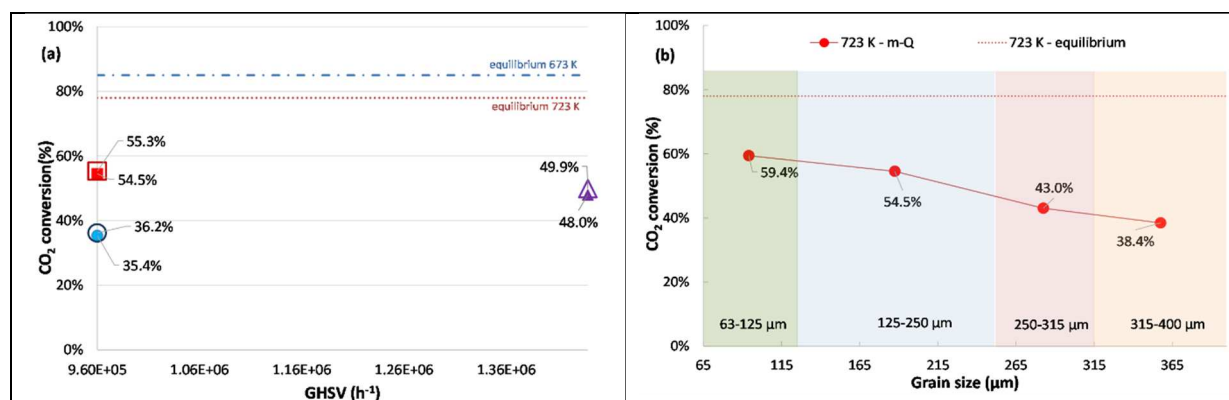


Figure 2: (a) Verification of the absence of external diffusional limitations ; $m = 1.5$ mg ; $Q = 27.5$ ml (STP) min⁻¹ ● at 673 K ■ at 723 K and ▲ $m = 1.5$ mg and $Q = 41.3$ (STP) min⁻¹ at 723 K compared respectively to $2m$ and $2Q$ (○, □, △) (b) verification of the absence of internal diffusional limitations at 723 K ; $m = 1.5$ mg ; $Q = 27.5$ ml (STP) min⁻¹

2.4. Kinetic measurements

Kinetic experiments aim at determining the reaction rate of the three reactions (Eqs (1), (2) and (3)) in a two-step procedure. First, the forms of the reaction rates are identified by low-conversion experiments with a rough estimation of their numerical parameters, which are then adjusted at higher conversion rate.

The aim of the tests at low conversion is to establish the partial pressure rate dependence of each component on each reaction, at different temperatures. To do so, the inlet partial pressure of one compound was varied while keeping the others constant. This was performed with the use of an argon flow. A maximum conversion of 20% was tolerated to assume constant reaction rate along the reactor axis. Indeed, on the basis of low conversion, the reactants partial pressure alongside the catalyst bed was assumed to be constant, and equal to the inlet values. Moreover, the reverse reactions were neglected

(far from thermodynamic limitations), and the effects of the products formed by the reactions (CO, H₂O, CH₄) were expected to be weak enough to be neglected (no chain reaction or products inhibition).

According to these assumptions, with a H₂/CO₂ flow at the reactor inlet, the CH₄ formation rate is equal to the CO₂ methanation reaction rate, and the CO formation rate equals the RWGS reaction rate:

$$\begin{aligned}r_{meth\ CO_2} &= r_{CH_4} \\r_{RWGS} &= r_{CO}\end{aligned}$$

With a H₂/CO flow at the inlet, the CH₄ formation rate is associated to the CO methanation reaction rate:

$$r_{meth\ CO} = r_{CH_4}$$

In order to study the influence of the products on the reaction rates, some tests were performed with a product of the possible reactions (CH₄ or H₂O) at the inlet of the reactor. To reduce the partial pressure variation alongside the catalytic bed and thus to be able to consider inlet partial pressure in the calculation, relatively high partial pressures of products were used at the reactor inlet in order to obtain $F_{products}^{inlet} \gg F_{products}^{formed}$.

Existing models from the literature were evaluated against the experimental results. They were adapted to better fit the experimental data. Finally, a first estimation of the kinetic and adsorption parameters of the three reactions were determined.

In the second set of experiments, the parameters were adjusted in order to fit experimental data at higher conversion rate. Experimentally, catalyst mass and total reactive flow rate were varied in order to reproduce the conversion rate range of an isothermal plug flow reactor. GHSV between 2.88 10⁶ h⁻¹ and 1.46 10⁵ h⁻¹ were tested at 623 K, 673 K and 723 K according to the following conditions (H₂/CO₂ = 4 and N₂ = 10% of the reactive flow rate):

- A batch of 1.5 mg of catalyst diluted in SiC ($\Psi = 32$) and a flow rate of 82.5 ml (STP) min⁻¹
- A batch of 2.0 mg of catalyst diluted in SiC ($\Psi = 24$) and three flow rates (82.5-55.0-27.5 ml (STP) min⁻¹)
- A batch of 10.0 mg of catalyst diluted in SiC ($\Psi = 4$) and three flow rates (82.5-55.0-27.5 ml (STP) min⁻¹).

Numerically, an isothermal plug flow was modeled by 100 CSTR in series with the same mass of catalyst. The kinetic laws and their roughly estimated numerical parameters were employed to evaluate the partial flow rate alongside the catalytic bed with the three reactions occurring in parallel, according to the composition, flow rate and pressure at the inlet of the reactor and the conditions of temperature and catalyst mass. A linear pressure drop was assumed between the reactor inlet (around 130 kPa) and the atmospheric pressure at the outlet. The equilibrium constants of the three reactions were calculated according to the Gibbs equation. The roughly estimated parameters of the kinetic model were then adjusted simultaneously to minimize the error on CO₂ conversion and CH₄ and CO selectivities at 623 K, 673 K and 723 K.

3. Results

3.1. CO₂ methanation

The CO₂ methanation rate dependence on reactants and products partial pressure has been established at different temperatures with 1.5 mg of Ni/Al₂O₃ catalyst diluted in SiC ($\Psi = 32$). The rate of CH₄ formation is highly dependent on the H₂ concentration (Figure 3 (a) at 22 kPa CO₂ partial pressure) whereas it is weakly dependent on the CO₂ partial pressure (Figure 3 (b) at 55 kPa H₂ partial pressure). No significant influence of CH₄ partial pressure on CH₄ formation rate is detected (Figure 3 (c) at 55 kPa H₂ partial pressure and 22 kPa CO₂ partial pressure) whereas an inhibition by water pressure is observed in Figure 3 (d).

3.2. RWGS

The effect of CO₂, H₂, H₂O and CH₄ partial pressures on the CO formation rate associated with the RWGS reaction was studied on 1.5 mg Ni/Al₂O₃ catalyst diluted in SiC ($\Psi = 32$). No dependence on the H₂ concentration is visible (Figure 4 (a) at 22 kPa CO₂ partial pressure) whereas the rate of CO formation is highly dependent on the CO₂ concentration (Figure 4 (b) at 55 kPa H₂ partial pressure). No influence

of CH₄ partial pressure and an inhibition by water pressure (Figure 4 (c) and (d)) are observed at 55 kPa H₂ partial pressure and 22 kPa CO₂ partial pressure.

The effect of CO partial pressure has been investigated on the CO₂ formation rate associated with the WGS reaction (reverse reaction of Eq (2)), *i.e.* with a flow of CO/H₂O at the entry of the reactor to avoid the competition with methanation reactions. CO₂ formation rate is moderately dependent on CO partial pressure (Figure 5 at 20 kPa H₂O partial pressure).

3.3. CO methanation

The CO methanation rate dependence on reactants partial pressure was determined at 623 K, 673 K and 723 K. A quasi linear dependence on the H₂ partial pressure (Figure 6 (a) at 25 kPa CO partial pressure) was observed whereas the dependence on CO is much weaker (Figure 6 (b) at 40 kPa H₂ partial pressure).

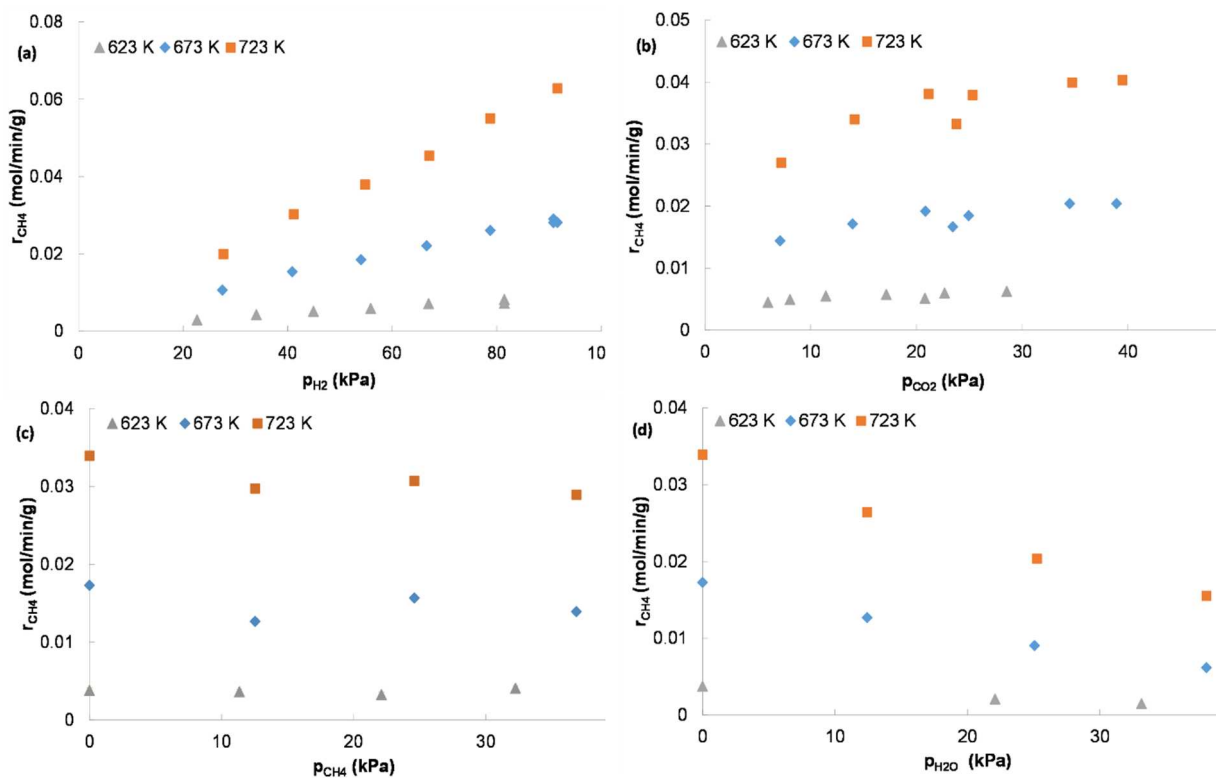
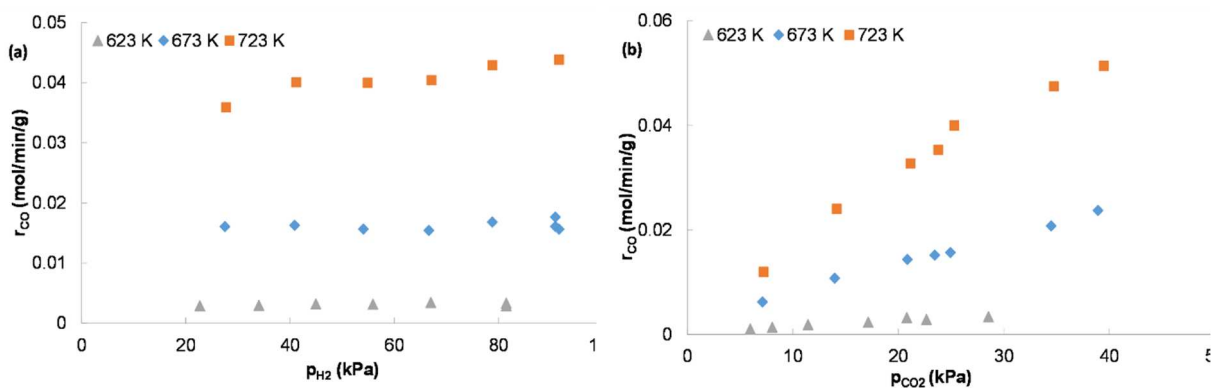


Figure 3 : Effect of partial pressure on CO₂ methanation on 1.5 mg Ni/Al₂O₃ catalyst diluted in SiC, 115 kPa total pressure and 1.06 10⁶ h⁻¹ at 623 K – 130 kPa total pressure and 3.16 10⁶ h⁻¹ at 673 K and 723 K: (a) H₂ at 22 kPa CO₂ partial pressure; (b) CO₂ at 55 kPa H₂ partial pressure; (c) CH₄ and (d) H₂O at 55 kPa H₂ partial pressure and 22 kPa CO₂ partial pressure



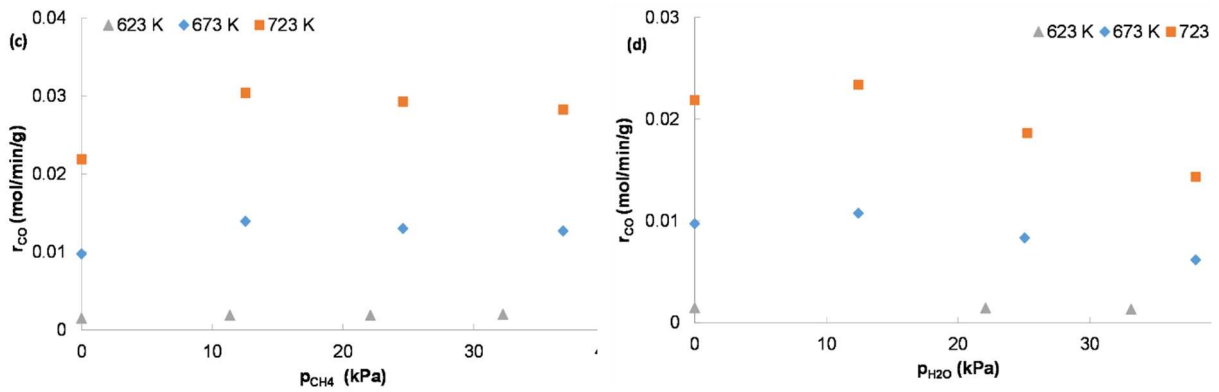


Figure 4 : Effect of partial pressure on RWGS on 1.5 mg Ni/Al₂O₃ catalyst diluted in SiC, 115 kPa total pressure and 1.06 10⁶ h⁻¹ at 623 K – 130 kPa total pressure and 3.16 10⁶ h⁻¹ at 673 K and 723 K: (a) H₂ at 22 kPa CO₂ partial pressure; (b) CO₂ at 55 kPa H₂ partial pressure; (c) CH₄ and (d) H₂O at 55 kPa H₂ partial pressure and 22 kPa CO₂ partial pressure

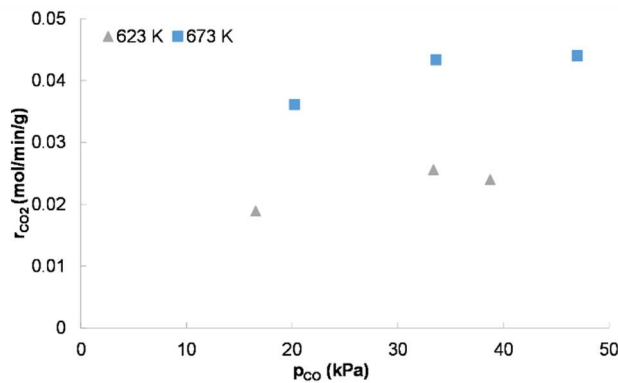


Figure 5 : CO partial pressure dependence on WGS on 1.5 mg Ni/Al₂O₃ catalyst diluted in SiC, 20 kPa H₂O partial pressure, 115 kPa total pressure and 1.06 10⁶ h⁻¹ at 623 K – 140 kPa total pressure and 3.16 10⁶ h⁻¹ at 673 K

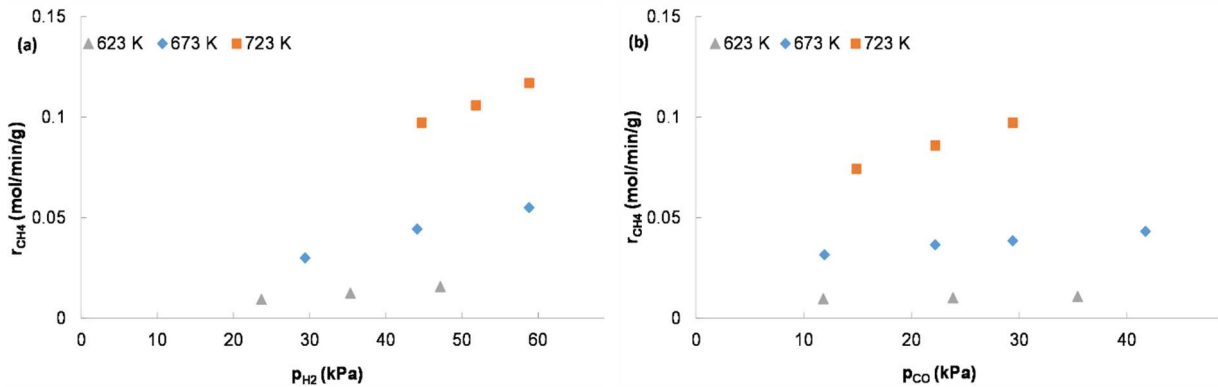


Figure 6 : (a) H₂ partial pressure dependence at 25 kPa CO partial pressure, and (b) CO partial pressure dependence at 40 kPa H₂ partial pressure on CO methanation on 1.5 mg Ni/Al₂O₃ catalyst diluted in SiC, 118 kPa total pressure and 1.66 10⁶ h⁻¹ at 623 K – 148 kPa total pressure and 5.0 10⁶ h⁻¹ at 673 K and 723 K

4. Discussion

The main rate expressions for CO₂ methanation, CO methanation and RWGS commonly used in literature are listed in Table 1. Simplification of these kinetic models in different situations presented below are tested and compared with experimental results obtained at low conversion (below 20%).

Table 1 : Literature rate expressions for CO₂ methanation, CO methanation and RWGS (including reverse reaction)

CO ₂ methanation rate equations		
Xu and Froment [13]	$r_{CO_2\ meth} = \frac{k_{CO_2\ meth} p_{H_2}^{0.5} p_{CO_2} \left(1 - \frac{p_{H_2O}^2 p_{CH_4}}{p_{H_2}^4 p_{CO_2} K_{eq,CO_2\ meth}}\right)}{\left(1 + K_{CO} p_{CO} + K_{H_2} p_{H_2} + K_{CH_4} p_{CH_4} + K_{H_2O} \frac{p_{H_2O}}{p_{H_2}}\right)^2}$	(5)
Bartholomew [15]	$r_{CO_2\ meth} = \frac{k_{CO_2\ meth} p_{CO_2}^{0.5} p_{H_2}^{0.5} \left(1 - \frac{p_{H_2}^4 p_{CO_2}}{p_{H_2O}^2 p_{CH_4} K_{eq,CO_2\ meth}}\right)}{\left(1 + K_1 (p_{CO_2}/p_{H_2})^{0.5} + K_2 (p_{CO_2} p_{H_2})^{0.5} + p_{CO}/K_3\right)^2}$	(6)
RWGS rate equations		
Xu and Froment [13]	$r_{RWGS} = \frac{k_{RWGS} p_{CO_2} \left(1 - \frac{p_{H_2O} p_{CO}}{p_{H_2} p_{CO_2} K_{eq,RWGS}}\right)}{\left(1 + K_{CO} p_{CO} + K_{H_2} p_{H_2} + K_{CH_4} p_{CH_4} + K_{H_2O} \frac{p_{H_2O}}{p_{H_2}}\right)^2}$	(7)
Wheeler [25]	$r_{RWGS} = \frac{k_{RWGS} K_{H_2} K_{CO_2} p_{H_2} p_{CO_2} \left(1 - \frac{p_{H_2O} p_{CO}}{p_{H_2} p_{CO_2} K_{eq,RWGS}}\right)}{\left(1 + K_{CO} p_{CO} + K_{H_2O} p_{H_2O} + K_{CO_2} p_{CO_2} + K_{H_2} p_{H_2}\right)^2}$	(8)
CO methanation rate equations		
Xu and Froment [13]	$r_{CO\ meth} = \frac{k_{CO\ meth} p_{H_2}^{0.5} p_{CO} \left(1 - \frac{p_{H_2O} p_{CH_4}}{p_{H_2}^3 p_{CO} K_{eq,CO\ meth}}\right)}{\left(1 + K_{CO} p_{CO} + K_{H_2} p_{H_2} + K_{CH_4} p_{CH_4} + K_{H_2O} \frac{p_{H_2O}}{p_{H_2}}\right)^2}$	(9)

4.1. CO₂ methanation rate equation

The Xu and Froment kinetic model [13] simplifies as follows at low conversion with a CO₂/H₂ feed (as p_{CO} , p_{CH_4} , and p_{H_2O} are negligible):

$$r_{meth\ CO_2} = \frac{k_{CO_2\ meth} p_{CO_2} p_{H_2}^{0.5}}{(1 + K_{H_2} p_{H_2})^2} \quad (10)$$

However, the proportionality between the CO₂ methanation reaction rate and the CO₂ partial pressure is not obtained experimentally (Figure 7). This model is therefore rejected.

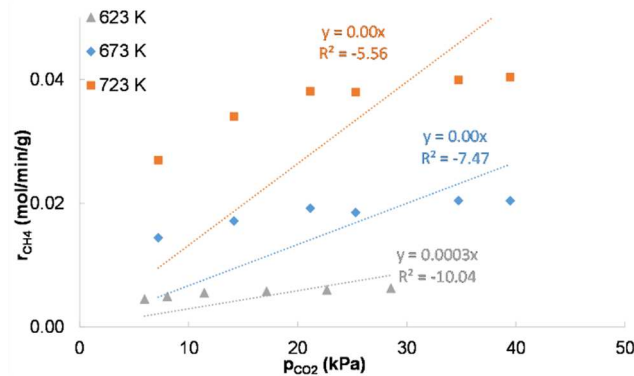


Figure 7 : Xu and Froment linear model of the CO₂ methanation (lines) according to p_{CO_2} vs experimental data (points) at 623 K, 673 K and 723 K (low conversion)

The model proposed by Weatherbee and Bartholomew [15] was also tested. The same method of simplification was applied at low conversion and led to the following expression with a CO₂/H₂ feed:

$$r_{CO_2\ meth} = \frac{k_{CO_2\ meth} p_{CO_2}^{0.5} p_{H_2}^{3/2}}{(p_{H_2}^{0.5} + K_1 p_{CO_2}^{0.5} + K_2 p_{H_2} p_{CO_2}^{0.5})^2} \quad (11)$$

The validity of this model is verified by linearization of (11). In Figure 8 (a) at 55 kPa H₂ partial pressure, straight lines are obtained as a function of $(p_{CO_2})^{0.5}$ while plotting $(p_{CO_2}^{0.25}/r_{CO_2\ meth})^{0.5}$ at 623 K, 673 K and 723 K. However, in Figure 8 (b) at 22 kPa CO₂ partial pressure, plots of $(p_{H_2}^{0.75}/r_{CO_2\ meth})^{0.5}$ with $(p_{H_2})^{0.5}$ admit negative coefficients. This would implies that some adsorption or kinetic constants are negative which is not consistent and leads to the rejection of this model.

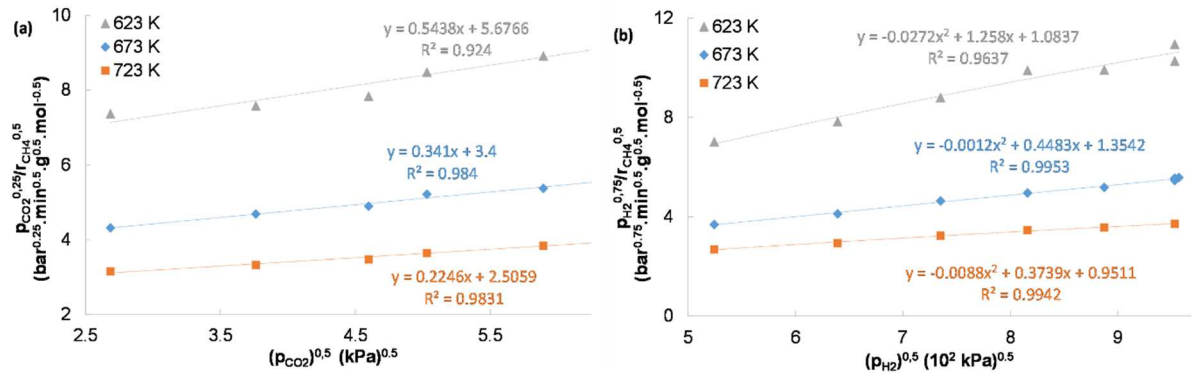


Figure 8 : Bartholomew linear function (a) according to p_{CO_2} and (b) according to p_{H_2} at low CO₂ methanation conversion

The simple kinetic model proposed by Wheeler *et al.* (Eq.(8)) and identified for the WGS reaction [25] is adapted for the CO₂ methanation reaction. In the case of a CO₂/H₂ feed, at low CO₂ conversion, the equation becomes:

$$r_{CO_2\ meth} = \frac{k_{CO_2\ meth} K_{H_2} K_{CO_2} p_{H_2} p_{CO_2}}{(1 + K_{CO_2} p_{CO_2} + K_{H_2} p_{H_2})^2} \quad (12)$$

Linearization of the kinetics leads to plot $(p_{CO_2}/r_{CO_2\ meth})^{0.5}$ as a function of p_{CO_2} at constant p_{H_2} and $(p_{H_2}/r_{CO_2\ meth})^{0.5}$ as a function of p_{H_2} at constant p_{CO_2} . A good fit of the experimental results for linear functions are obtained in both Figure 9 (a) at 55 kPa H₂ partial pressure and (b) at 22 kPa CO₂ partial pressure at 623 K, 673 K and 723 K. The mechanism behind this equation assumes a bimolecular limiting step: $CO_2X + H_2X \rightarrow COX + H_2OX$, where X is a vacant site on the metal surface [25]. The H₂ and CO₂ adsorption constants, and the CO₂ methanation kinetic constant are identified from the slope and intercept of the regression lines of Figure 9 (a) and (b). The identified constants model correctly the CH₄ formation rate at the three temperatures (Figure 10 (a) and (b)).

The inhibition by water (Figure 3 (d)) is accounted for by adding in the adsorption term the H₂O partial pressure modulated by an adsorption constant, meaning an adsorption competition on the available active sites. The reaction rate expression at low conversion for a CO₂/H₂/H₂O feed is thus the following:

$$r_{CO_2\ meth} = \frac{k_{CO_2\ meth} K_{H_2} K_{CO_2} p_{H_2} p_{CO_2}}{(1 + K_{CO_2} p_{CO_2} + K_{H_2} p_{H_2} + K_{H_2O} p_{H_2O})^2} \quad (13)$$

H₂O adsorption constant is identified at 623 K, 673 K and 723 K on the experimental data of Figure 3 (d). The H₂O inhibition model fits well the CH₄ formation rate data (Figure 10 (c)).

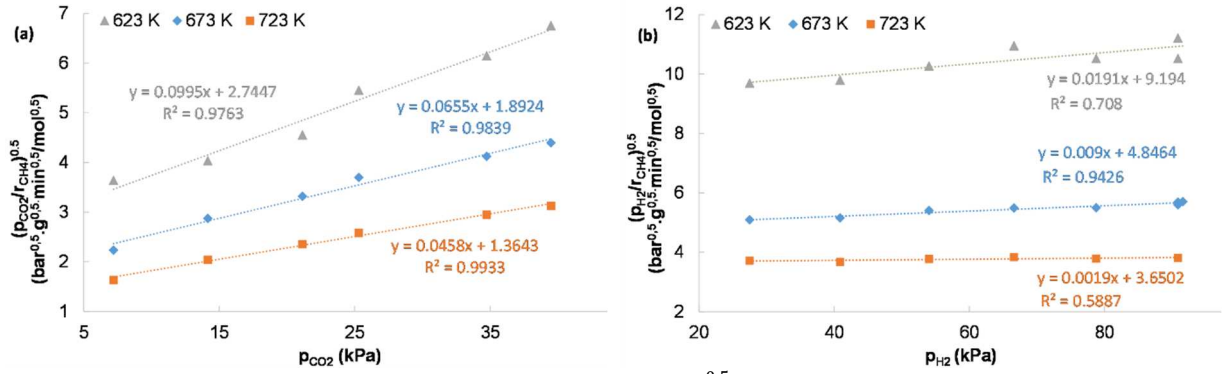


Figure 9 : Plot of the adapted Wheeler linear function $(p_i/r_{meth CO_2})^{0.5}$ versus p_i at low CO_2 methanation conversion (a) $i = CO_2$ at 55 kPa H_2 partial pressure and (b) $i = H_2$ at 22 kPa CO_2 partial pressure

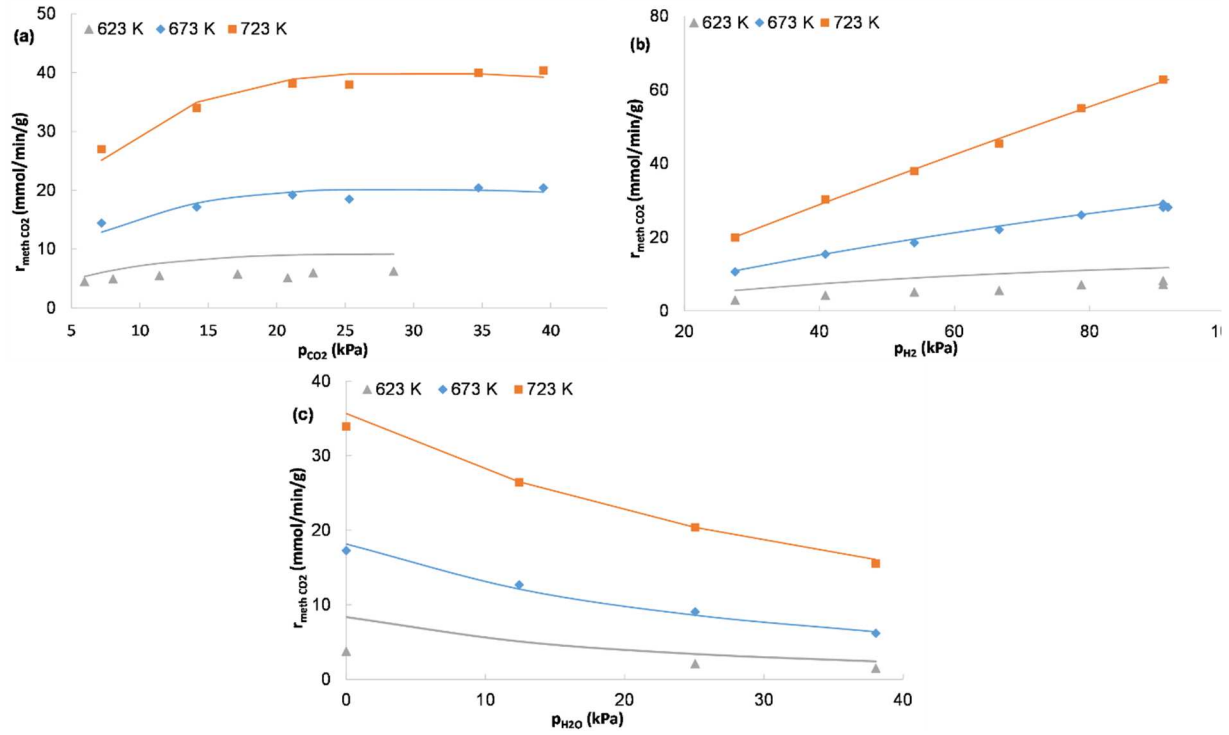


Figure 10 : Comparison between the CH_4 formation rate experimental results (points) and the CO_2 methanation rate equation predicted by the adapted Wheeler model at low conversion (continuous line) at 623 K, 673 K and 723 K: (a) Effect of CO_2 partial pressure at 55 kPa H_2 partial pressure, (b) Effect of H_2 partial pressure at 22 kPa CO_2 partial pressure, (c) Effect of H_2O partial pressure at 55 kPa H_2 partial pressure and 22 kPa CO_2 partial pressure

4.2. RWGS rate equation

According to our results, RWGS is not influenced by hydrogen partial pressure (Figure 4 (a)). The following model is proposed at low CO_2 conversion with a CO_2/H_2 feed assuming CO_2 dissociative adsorption as limiting step: $CO_2 + X \rightarrow CO + OX$ [26,27] and tested on the CO formation rate data:

$$r_{RWGS} = \frac{k_{RWGS} K_{CO_2} p_{CO_2}}{(1 + K_{H_2} p_{H_2} + K_{CO_2} p_{CO_2})} \quad (14)$$

The validity of this model is verified by linearization of (14). In Figure 11, at 55 kPa H₂ partial pressure, straight lines are obtained as a function of p_{CO_2} while plotting (p_{CO_2}/r_{RWGS}) at 623 K, 673 K and 723 K.

Keeping the value of adsorption constants previously determined in the CO₂ methanation study, the resolution gives the RWGS kinetic constant to model the CO formation rate at 623 K, 673 K and 723 K (Figure 12):

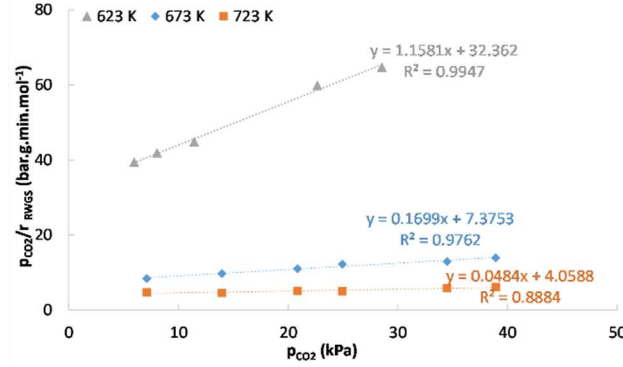


Figure 11 : Plot of the proposed RWGS linear model $p_{CO_2}/r_{meth\ CO_2}$ versus p_{CO_2} at low CO₂ conversion and 55 kPa H₂ partial pressure

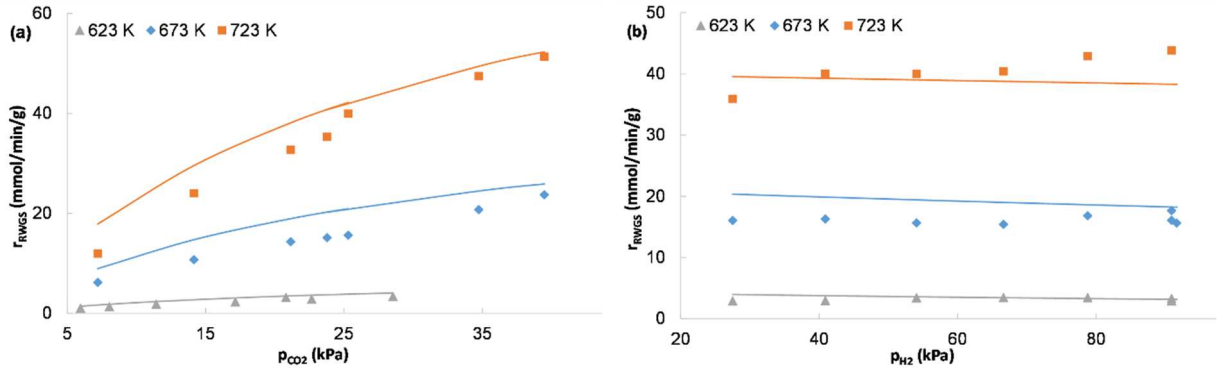


Figure 12 : Comparison between the CO formation rate experimental results (points) and the RWGS rate equation predicted by the adapted model at low conversion (continuous line) at 623 K, 673 K and 723 K: (a) Effect of CO₂ partial pressure at 55 kPa H₂ partial pressure and (b) Effect of H₂ partial pressure at 22 kPa CO₂ partial pressure

4.3. CO methanation rate equation

Linearization of the Xu and Froment kinetics at low conversion with a CO/H₂ feed leads to plot $(p_{CO}^{0.25}/r_{CO\ meth})^{0.5}$ as a function of p_{H_2} at constant p_{CO} . However, results are not presented here because negative coefficients are obtained.

Based on the results of the CO₂ methanation kinetic study (Eq (12)), the following model is proposed in the case of a low conversion CO methanation reaction with a CO/H₂ feed:

$$r_{CO\ meth} = \frac{k_{CO\ meth} K_{H_2} K_{CO} p_{H_2} p_{CO}}{(1 + K_{H_2} p_{H_2} + K_{CO} p_{CO})^2} \quad (15)$$

Linearization of the kinetics leads to plot $(p_{CO}/r_{CO\ meth})^{0.5}$ as a function of p_{CO} at constant p_{H_2} and $(p_{H_2}/r_{CO\ meth})^{0.5}$ as a function of p_{H_2} at constant p_{CO} . A good fit of the experimental results for linear functions are obtained in both Figure 13 (a) at 40 kPa H₂ partial pressure and (b) at 25 kPa CO partial pressure at 623 K, 673 K and 723 K. The CO methanation kinetic constant as well as the CO adsorption constant are identified from the slope and intercept of the regression lines of Figure 13 (a) and (b) knowing the H₂ adsorption constant from the CO₂ methanation rate equation study. The identified model fits adequately the CH₄ formation rate data (Figure 14 (a) and (b)).

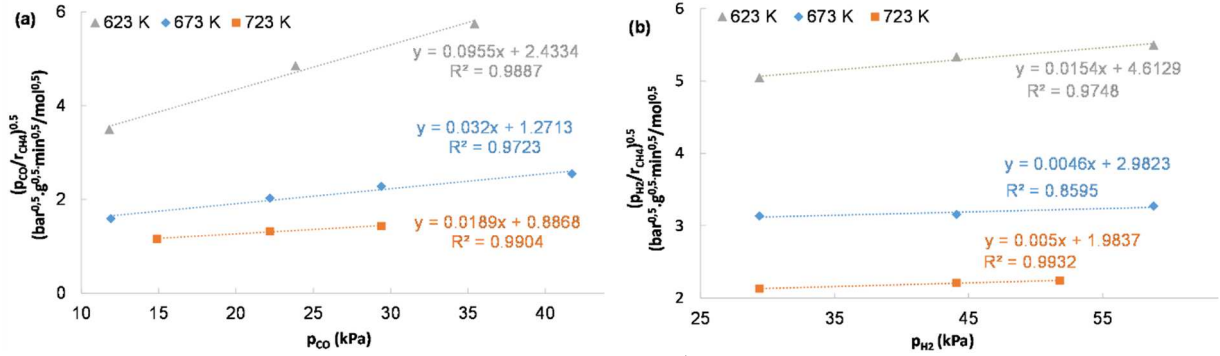


Figure 13 : Plot of the adapted linear function $(p_i/r_{meth,CO})^{0.5}$ versus p_i at low CO methanation conversion (a) $i = CO$ at 40 kPa H_2 partial pressure; (b) $i = H_2$ at 25 kPa CO_2 partial pressure

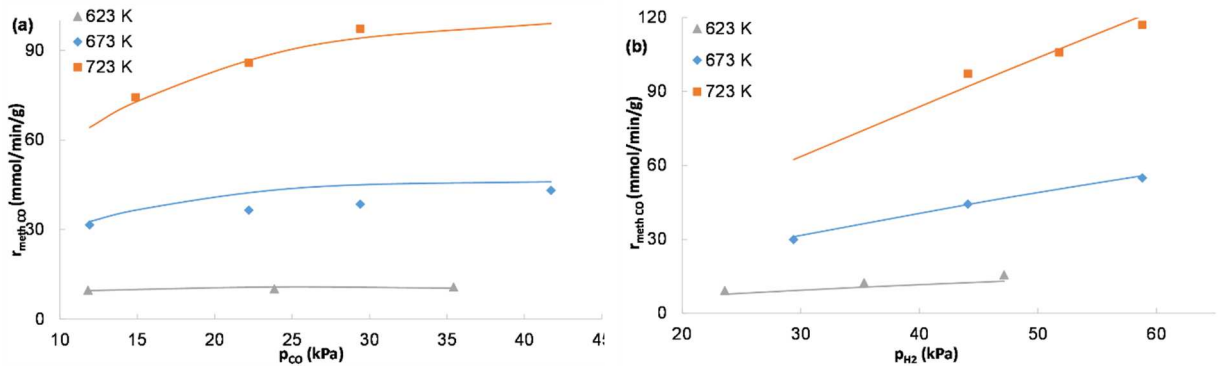


Figure 14 : Comparison between the CH_4 formation rate experimental results (points) and the CO methanation rate equation predicted by the adapted model at low conversion (continuous line) at 623 K, 673 K and 723 K: (a) Effect of CO partial pressure at 40 kPa H_2 partial pressure and (b) Effect of H_2 partial pressure at 25 kPa CO_2 partial pressure

4.4. Parameters adjustment

The kinetic experiments performed at low conversion (below 20% for all reactive components) allowed to determine the form of the three reaction rates (Eqs (1), (2) and (3)) as well as a first identification of the kinetic and adsorption parameters. The thermodynamic limitations were added to the kinetics established at low conversion in order to consider the global reaction rate of the balanced reaction:

$$r_{global} = r^+ - r^- = r^+ \left(1 - \frac{Q_r}{K_{eq}} \right)$$

Moreover, the adsorption of all species likely to compete significantly on the catalyst active sites (*i.e.* H_2 , CO_2 , H_2O , and CO) was taken into account. The obtained equations are given in Table 2.

Table 2 : Kinetic model of this study

CO₂ methanation rate equations

$$r_{CO_2\ meth} = \frac{k_{CO_2\ meth} K_{H_2} K_{CO_2} p_{H_2} p_{CO_2} \left(1 - \frac{p_{CH_4} p_{H_2O}^2}{p_{H_2}^4 p_{CO_2} K_{eq,CO_2\ meth}} \right)}{\left(1 + K_{CO_2} p_{CO_2} + K_{H_2} p_{H_2} + K_{H_2O} p_{H_2O} + K_{CO} p_{CO} \right)^2} \quad (16)$$

RWGS rate equations

$$r_{RWGS} = \frac{k_{RWGS} K_{CO_2} p_{CO_2} \left(1 - \frac{p_{CO} p_{H_2O}}{p_{H_2} p_{CO_2} K_{eq,RWGS}} \right)}{\left(1 + K_{CO_2} p_{CO_2} + K_{H_2} p_{H_2} + K_{H_2O} p_{H_2O} + K_{CO} p_{CO} \right)} \quad (17)$$

CO methanation rate equations

$$r_{CO\ meth} = \frac{k_{CO\ meth} K_{H_2} K_{CO} p_{H_2} p_{CO} \left(1 - \frac{p_{CH_4} p_{H_2O}}{p_{H_2}^3 p_{CO} K_{eq,CO\ meth}} \right)}{\left(1 + K_{CO_2} p_{CO_2} + K_{H_2} p_{H_2} + K_{H_2O} p_{H_2O} + K_{CO} p_{CO} \right)^2} \quad (18)$$

For a separated set of experiments (described in 2.4), an isothermal plug flow model was used to integrate the three reactions occurring in parallel. As the three reaction rates include three kinetic constants and four adsorption constants, a total of 14 parameters are involved in the rate equations. The adjustments were first performed on the kinetic constants and the adsorption constants at 673 K. This allowed to first reduce the number of parameters from 14 to 7 while keeping a physical meaning when adjusting parameters.

Experimental and theoretical CO₂ conversion and CH₄ and CO selectivities are plotted as a function of an equivalent mass of catalyst defined by:

$$equivalent\ mass = real\ mass \frac{reference\ flow\ rate}{real\ flow\ rate}$$

A reference flow rate, being arbitrary fixed at 100 ml (STP) min⁻¹, is used to link the experimental results (with different mass and flow rates) to the modeled values.

First, reaction rates expressions were simplified by introducing apparent kinetic constants as follows:

$$k_{app,CO_2\ meth} = k_{CO_2\ meth} K_{CO_2} K_{H_2} \quad (19)$$

$$k_{app,RWGS} = k_{RWGS} K_{CO_2} \quad (20)$$

$$k_{app,CO\ meth} = k_{CO\ meth} K_{CO} K_{H_2} \quad (21)$$

The aim of this mathematical operation is to avoid the influence of adsorption parameters on both numerator and denominator.

With a H₂/CO₂ feed, the CO₂ methanation and the RWGS are both primary reactions whereas the CO methanation is a secondary reaction. Hence, for each temperature, the ratio between CH₄ and CO selectivities extrapolated at equivalent mass of zero corresponds to the ratio of CO₂ methanation over RWGS initial rates. The obtained ratio allowed to link kinetic constants of CO₂ methanation to RWGS reaction. The number of parameters is thus declined to 6.

As conversion at relatively low equivalent mass is not sensitive to secondary reaction, conversion was then adjusted by tuning RWGS kinetic constant (and so CO₂ methanation automatically with). Furthermore, the kinetic constant of the CO methanation was adjusted by adjusting CO selectivities in the whole range of equivalent mass.

The adsorption constants were then modified in the denominator of the rate equations to fit the form of the curve of CO₂ conversion and CH₄ and CO selectivities (*i.e.* inhibit more or less the reaction rates). Based on the roughly estimated parameters, the influence of the CO adsorption constant on the reaction rates is much weaker than the ones of the three other compounds involved (CO₂, H₂ and H₂O), this parameter was thus not changed.

Once the adsorption parameters modified, the sequence was repeated iteratively until good fits were obtained at a given temperature. The procedure was then repeated for the 2 other temperatures with the constraint of acceptable Arrhenius plots for each of the 7 kinetic and adsorption constants.

Comparison of the experimental and theoretical CO₂ conversions and CH₄ and CO selectivities at 623, 673 and 723 K are presented in Figure 15 for the adjusted parameters. As the obtained error is small at the three temperatures, the adjusted apparent kinetic constants allowed to calculate real kinetic constants present in Eqs (16), (17) and (18).

The final parameters given in Table 3 predict with an accuracy of 20% the CH₄ formation rate (Figure 16) for the three temperatures and conversion rates ranging from 5% to 75%.

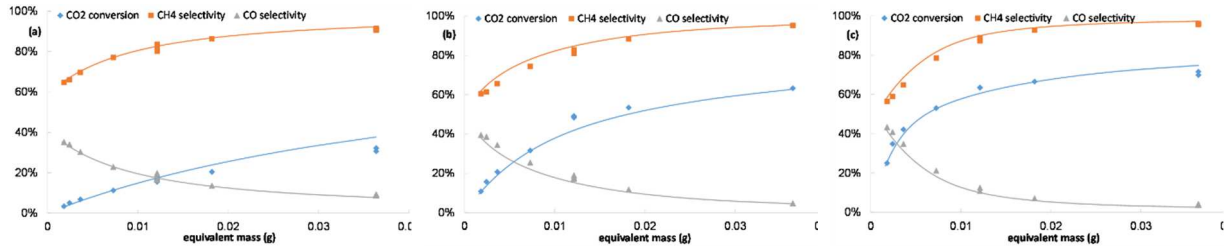


Figure 15: CO₂ conversion and CH₄ and CO selectivities of an isothermal plug flow reactor for a molar ratio H₂/CO₂/N₂ = 74/17/9 – continuous line: model – point: experimental value: (a) at 623 K; (b) at 673 K and (c) at 723 K

Table 3 : Final parameters of the kinetic model following an Arrhenius law for the kinetic constants and as Van't Hoff type for the adsorption constants

Adsorption constants		K _{CO}	K _{H₂O}	K _{CO₂}	K _{H₂}
	Q (kJ mol ⁻¹)		40.6	14.5	9.72
K ₀ (bar ⁻¹)		2.39 10 ⁻³	6.09 10 ⁻¹	1.07	5.20 10 ⁻⁵

Kinetic constants		k _{CO₂ meth}	k _{RWGS}	k _{CO meth}	
	Ea (kJ mol ⁻¹)		110	97.1	97.3
	k ₀ (mol min ⁻¹ g ⁻¹)		1.14 10 ⁸	1.78 10 ⁶	2.23 10 ⁸

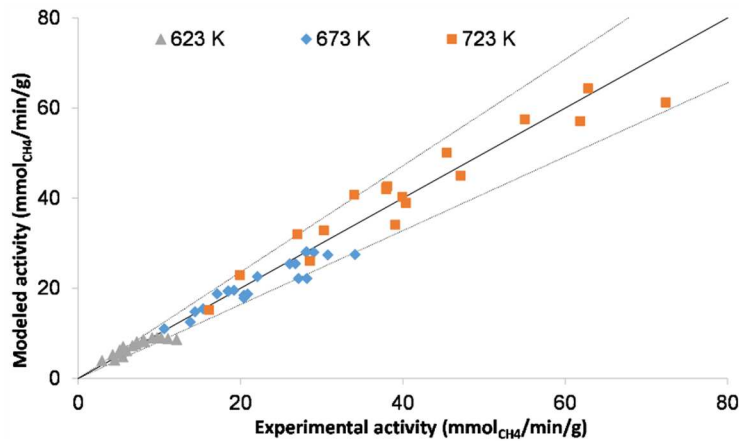


Figure 16: Parity plot of the experimental and modeled CH₄ activity within 20% error at 623 K, 673 K and 723 K - H₂/CO₂/N₂ at the reactor inlet (data taken from experiments at low conversion and parameters adjustment experiments)

5. Conclusion

An intrinsic kinetic model was proposed to represent both the direct and indirect paths of the CO₂ methanation reaction (*i.e.* CO₂ methanation and Reverse Water Gas Shift + CO methanation) between 623 K and 723 K, at atmospheric pressure.

First, the partial pressure rate dependence of each component was established on each reaction, at different temperatures to select the form of the three kinetic laws and to identify the kinetic and adsorption parameters. For these tests, the CO₂ conversion (CO conversion) was limited to 20% in order to consider only the direct direction of the CO₂ methanation and RWGS (CO methanation).

Then, these parameters were adjusted by minimizing the error between the CO₂ conversion and CH₄ and CO selectivities predicted by an isothermal plug-flow model and several tests at higher conversion rate at 623 K, 673 K and 723 K. An excellent fit was obtained allowing the prediction of the CH₄ formation rate within 20% error.

Future works will include a kinetic model validation at the CO₂ methanation milli-structured fixed-bed reactor-exchanger scale. The final purpose will be the prediction of the catalyst activity over time on stream inside the CO₂ methanation reactor using the kinetic model of this study coupled with a deactivation model.

Acknowledgments

This work was supported by the French Environment and Energy Management Agency (ADEME), French Alternative Energies and Atomic Energy Commission (CEA) and ATMOSTAT. It is the result of experiments conducted at the ICPEES Laboratory in Strasbourg.

Nomenclature

E_a	Activation energy (J mol ⁻¹)
F	Molar flow (mol min ⁻¹)
$GHSV$	Gas Hourly Space Velocity (h ⁻¹)
k_j	Reaction rate constant of reaction j (mol min ⁻¹ g ⁻¹)
k_0	Pre-exponential factor of rate constant (mol min ⁻¹ g ⁻¹)
K_i	Adsorption equilibrium constant of constituent i (bar ⁻¹)
K_0	Pre-exponential factor for adsorption equilibrium constant (bar ⁻¹)
$K_{eq,j}$	Equilibrium constant of reaction j
p_i	Partial pressure of constituent i
Q	Heat of adsorption (J mol ⁻¹)
Q_r	Reaction quotient (-)
r_j	Reaction rate of reaction j
r_{CH_4}	Reaction rate of methane formation (mol min ⁻¹ g ⁻¹)
r_{CO}	Reaction rate of CO formation (mol min ⁻¹ g ⁻¹)
r_{global}	Global reaction rate (mol min ⁻¹ g ⁻¹)
r^+	Direct reaction rate (mol min ⁻¹ g ⁻¹)
r^-	Reverse reaction rate (mol min ⁻¹ g ⁻¹)
R	Ideal gas constant (R = 8.314 J mol ⁻¹ K ⁻¹)
T	Temperature (K)
<i>Greek letters</i>	
$\Delta_r H$	Heat of reaction (J mol ⁻¹)
Ψ	Inert dilution factor ($\Psi = m_{SiC}/m_{catalyst}$)

Appendices

Supplementary material related to the theoretical heat and mass transfer limitations verifications is available.

References

- [1] M.A.A. Aziz, A.A. Jalil, S. Triwahyono, A. Ahmad, CO₂ methanation over heterogeneous catalysts: recent progress and future prospects, *Green Chem.* 17 (2015) 2647–2663. doi:10.1039/C5GC00119F.

- [2] P. Frontera, A. Macario, M. Ferraro, P. Antonucci, Supported Catalysts for CO₂ Methanation: A Review, *Catalysts*. 7 (2017) 59. doi:10.3390/catal7020059.
- [3] J. Gao, Q. Liu, F. Gu, B. Liu, Z. Zhong, F. Su, Recent advances in methanation catalysts for the production of synthetic natural gas, *RSC Adv.* 5 (2015) 22759–22776. doi:10.1039/C4RA16114A.
- [4] M. Götz, J. Lefebvre, F. Mörs, A. McDaniel Koch, F. Graf, S. Bajohr, R. Reimert, T. Kolb, Renewable Power-to-Gas: A technological and economic review, *Renew. Energy*. 85 (2016) 1371–1390. doi:10.1016/j.renene.2015.07.066.
- [5] Y. Li, S.H. Chan, Q. Sun, Heterogeneous catalytic conversion of CO₂: a comprehensive theoretical review, *Nanoscale*. 7 (2015) 8663–8683. doi:10.1039/C5NR00092K.
- [6] S. Rönsch, J. Schneider, S. Matthischke, M. Schlüter, M. Götz, J. Lefebvre, P. Prabhakaran, S. Bajohr, Review on methanation – From fundamentals to current projects, *Fuel*. 166 (2016) 276–296. doi:10.1016/j.fuel.2015.10.111.
- [7] W. Wang, S. Wang, X. Ma, J. Gong, Recent advances in catalytic hydrogenation of carbon dioxide, *Chem. Soc. Rev.* 40 (2011) 3703. doi:10.1039/c1cs15008a.
- [8] J. Sabatier, P. Senderens, Nouvelles synthèses de méthane, *Compt Rend.* (1902) 514–516.
- [9] J. Gao, Y. Wang, Y. Ping, D. Hu, G. Xu, F. Gu, F. Su, A thermodynamic analysis of methanation reactions of carbon oxides for the production of synthetic natural gas, *RSC Adv.* 2 (2012) 2358. doi:10.1039/c2ra00632d.
- [10] P.J. Lunde, F.L. Kester, Carbon dioxide methanation on a ruthenium catalyst, *Ind. Eng. Chem. Process Des. Dev.* 13 (1974) 27–33.
- [11] J.H. Chiang, J.R. Hopper, Kinetics of the hydrogenation of carbon dioxide over supported nickel, *Ind. Eng. Chem. Prod. Res. Dev.* 22 (1983) 225–228.
- [12] R.E. Hayes, W.J. Thomas, K.E. Hayes, A study of the nickel-catalyzed methanation reaction, *J. Catal.* 92 (1985) 312–326.
- [13] J. Xu, G.F. Froment, Methane steam reforming, methanation and water-gas shift: I. Intrinsic kinetics, *AIChE J.* 35 (1989) 88–96.
- [14] J. Ducamp, A. Bengaouer, P. Baurens, Modelling and experimental validation of a CO₂ methanation annular cooled fixed-bed reactor exchanger, *Can. J. Chem. Eng.* 95 (2017) 241–252. doi:10.1002/cjce.22706.
- [15] G.D. Weatherbee, C.H. Bartholomew, Hydrogenation of CO₂ on group VIII metals: II. Kinetics and mechanism of CO₂ hydrogenation on nickel, *J. Catal.* 77 (1982) 460–472.
- [16] F. Koschany, D. Schlereth, O. Hinrichsen, On the kinetics of the methanation of carbon dioxide on coprecipitated NiAl(O)_x, *Appl. Catal. B Environ.* 181 (2016) 504–516. doi:10.1016/j.apcatb.2015.07.026.
- [17] C.V. Miguel, A. Mendes, L.M. Madeira, Intrinsic kinetics of CO₂ methanation over an industrial nickel-based catalyst, *J. CO₂ Util.* 25 (2018) 128–136. doi:10.1016/j.jcou.2018.03.011.
- [18] A. Bengaouer, J. Ducamp, I. Champon, R. Try, Performance evaluation of fixed-bed, millistructured, and metallic foam reactor channels for CO₂ methanation, *Can. J. Chem. Eng.* 96 (2018) 1937–1945. doi:10.1002/cjce.23140.
- [19] S. Danaci, L. Protasova, J. Lefebvre, L. Bedel, R. Guilet, P. Marty, Efficient CO₂ methanation over Ni/Al₂O₃ coated structured catalysts, *Catal. Today*. 273 (2016) 234–243. doi:10.1016/j.cattod.2016.04.019.
- [20] D. Schlereth, O. Hinrichsen, A fixed-bed reactor modeling study on the methanation of CO₂, *Chem. Eng. Res. Des.* 92 (2014) 702–712. doi:10.1016/j.cherd.2013.11.014.
- [21] H. Gierman, Design of laboratory hydrotreating reactors: scaling down of trickle-flow reactors, *Appl. Catal.* 43 (1988) 277–286.
- [22] D.E. Mears, The role of axial dispersion in trickle-flow laboratory reactors, *Chem. Eng. Sci.* 26 (1971) 1361–1366.
- [23] C.F. Chu, K.M. Ng, Flow in packed tubes with a small tube to particle diameter ratio, *AIChE J.* 35 (1989) 148–158.
- [24] S. Ergun, Fluid Flow through packed columns, *Chem. Eng. Prog.* 48 (1952) 89–92.
- [25] C. Wheeler, The water–gas-shift reaction at short contact times, *J. Catal.* 223 (2004) 191–199. doi:10.1016/j.jcat.2004.01.002.
- [26] M.S. Spencer, On the activation energies of the forward and reverse water-gas shift reaction, *Catal. Lett.* 32 (1995) 9–13.
- [27] E.L. Fornero, D.L. Chiavassa, A.L. Bonivardi, M.A. Baltanás, Transient analysis of the reverse water gas shift reaction on Cu/ZrO₂ and Ga₂O₃/Cu/ZrO₂ catalysts, *J. CO₂ Util.* 22 (2017) 289–298. doi:10.1016/j.jcou.2017.06.002.

