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Rational solutions to the KdV equation depending on multi-parameters

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Abstract

We construct multi-parametric rational solutions to the KdV equation. For this, we use solutions in terms of exponentials depending on several parameters and take a limit when one of these parameters goes to 0. Here we present degenerate rational solutions and give a result without the presence of a limit as a quotient of polynomials depending on 3Nparameters. We give the explicit expressions of some of these rational solutions.

Key Words : KdV equation, rational solutions.

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1 Introduction

We consider the KdV equation

$$4u_t = 6uu_x - u_{xxx},\tag{1}$$

where as usual, the subscripts x and t denote partial derivatives and u is a function of x and t.

Korteweg and de Vries [1] introduced this equation (1) for the first time in 1895.

The KdV equation (1) is the basis of the most common tool for the (1+1)dimensional modelling of shallow water waves. It is now known that this equation describes the propagation of waves with weak dispersion in various nonlinear media. In 1967, Gardner et al. [2] gave a method of resolution of this equation. Zakharov and Faddeev [3] proved that this is a complete integrable equation in 1971.

Using the bilinear method, Hirota [4] constructed solutions in 1971. Among the works which have been realized, we can mention some of them. Solutions in terms of Riemann theta functions [5] were given by Its and Matveev in 1975. Lax gave in 1975 the expressions of periodic and almost periodic solutions [6]; we can also quote, Matveev in 1992 [7], Ma in 2004 [8], Kovalyov in 2005 [9].

We consider solutions to the KdV equation in this paper. From elementary exponential functions depending on several parameters, we construct rational solutions in performing a passage to the limit when one of these parameters goes to 0. We obtain rational solutions as depending on 3N parameters at order N. To get a result which does not depend on a limit, we have to consider another type of functions. With this new functions, we can give explicit solutions and we get a hierarchy of rational solution of order N to the KdV equation depending on 3N parameters.

2 Solutions to the KdV equation

2.1 Solutions to the KdV equation in terms of elementary exponentials

We consider the KdV equation (1)

$$4u_t = 6uu_x - u_{xxx}.$$

We use the following notations. We consider the real numbers α_j , β_j and γ_j defined by :

$$\alpha_j = \sum_{k=1}^N a_k (je)^{2k-1}, \quad \beta_j = \sum_{k=1}^N c_k (je)^{2k-1}, \quad \gamma_j = \sum_{k=1}^N d_k (je)^{2k-1}, \text{ for } 1 \le i \le N$$
(2)

We consider the elementary functions :

$$f_{ij}(x,t) = \alpha_j^{i-1} \exp(\alpha_j x - \alpha_j^3 t + \beta_j) - \alpha_j^{i-1} \exp(\alpha_j x - \alpha_j^3 t + \gamma_j), \text{ for } 1 \le i \le N$$
(3)

Then, we have the following statement :

Theorem 2.1 The function v defined by

$$v(x,t) = -2\partial_x^2 \ln(\det(f_{ij})_{(i,j)\in[1,N]})$$
(4)

is a solution to the KdV equation (1) with e, a_j, c_j and $d_j, 1 \le j \le N$ arbitrarily real parameters.

2.2 Rational solutions to the KdV equation

We are going to perform a limit when the parameter e tends to 0. With this idea, we can obtain rational solutions to the KdV equation,

2.2.1 Rational solutions as a limit case

We get the following result :

Theorem 2.2 The function v defined by

$$v(x,t) = \lim_{e \to 0} -2\partial_x^2 \ln(\det(f_{ij})_{(i,j) \in [1,N]})$$
(5)

is a rational solution to the KdV equation (1) depending on 3N parameters a_j , c_j and d_j , $1 \le j \le N$.

2.2.2 Degenerate rational solutions

We can give give a more precise result avoiding the presence of a limit. For this, we consider another type of functions g_{ij} defined by :

$$g_{ij} = \frac{\partial^{2j-1} f_{ij}}{\partial e^{2j-1}}_{|e=0}, \text{ for } 1 \le i \le N, \ 1 \le j \le N.$$

Then get the following result :

Theorem 2.3 The function v defined by

$$v(x,t) = -2\partial_x^2 \ln(\det(g_{ij})_{(i,j)\in[1,N]})$$
(6)

is a rational solution to the KdV equation (1) depending on 3N parameters a_j , c_j and d_j , $1 \le j \le N$.

So for each positive integer N, we get rational solutions to the KdV equation depending on 3N real parameters.

In the following we give some examples of rational solutions. These results are consequences of the previous result (6).

2.3 First order rational solutions

We have the following result at order N = 1:

Proposition 2.1 The function v defined by

$$v(x,t) = 8 \frac{{a_1}^2}{\left(2 \, a_1 x - d_1 + c_1\right)^2},\tag{7}$$

is a solution to the KdV equation (1) with a_1 , c_1 , d_1 arbitrarily real parameters.

Remark 2.1 This solution independent of t does not present any interest.

2.4 Second order rational solutions

Proposition 2.2 The function v defined by

$$v(x,t) = -2 \frac{n(x,t)}{d(x,t)^2},$$
(8)

with

$$\begin{split} n(x,t) &= -192\,a_1^{\,8}x^4 + 12\,a_1^{\,3}(32\,a_1^{\,4}d_1 - 32\,a_1^{\,4}c_1)x^3 + 12\,a_1^{\,3}(-24\,a_1^{\,3}c_1^{\,2} + 48\,a_1^{\,3}c_1d_1 - 24\,a_1^{\,3}d_1^{\,2})x^2 + 12\,a_1^{\,3}(96\,a_1^{\,5}t - 48\,a_1a_2d_1 - 8\,a_1^{\,2}c_1^{\,3} + 24\,a_1^{\,2}d_1c_1^{\,2} - 48\,a_1^{\,2}c_2 + 8\,a_1^{\,2}d_1^{\,3} - 24\,a_1^{\,2}c_1d_1^{\,2} + 48\,a_1^{\,2}d_2 + 48\,a_1a_2c_1)x + 12\,a_1^{\,3}(4\,c_1a_1d_1^{\,3} - 24\,a_1d_1d_2 + 24\,a_2d_1^{\,2} + 24\,a_2c_1^{\,2} + 48\,a_1^{\,4}c_1 - a_1c_1^{\,4} - a_1d_1^{\,4} + 4\,d_1a_1c_1^{\,3} - 48\,ta_1^{\,4}d_1 - 24\,a_1c_1c_2 - 48\,c_1a_2d_1 + 24\,c_1d_2a_1 + 24\,d_1c_2a_1 - 6\,c_1^{\,2}a_1d_1^{\,2}), \end{split}$$

$$\begin{split} d(x,t) &= 8\,a_1^{\,4}x^3 + (-12\,a_1^{\,3}d_1 + 12\,a_1^{\,3}c_1)x^2 + (6\,a_1^{\,2}c_1^{\,2} - 12\,c_1a_1^{\,2}d_1 + 6\,a_1^{\,2}d_1^{\,2})x - 12\,c_2a_1 + \\ &12\,d_2a_1 - 3\,d_1a_1c_1^{\,2} + a_1c_1^{\,3} + 3\,c_1a_1d_1^{\,2} + 12\,a_2c_1 - a_1d_1^{\,3} + 24\,ta_1^{\,4} - 12\,a_2d_1 \end{split}$$

is a rational solution to the KdV equation (1), quotient of two polynomials with numerator of degree 4 in x, 1 in t, and denominator of degree 6 in x, 2 in t.

2.5 Rational solutions of order three

We get the following rational solutions given by :

Proposition 2.3 The function v defined by

$$v(x,t) = -2 \frac{n(x,t)}{d(x,t)^2},$$
(9)

with

 $n(x,t) = -24576 a_1^{16} x^{10} - 24 a_1^2 (-5120 a_1^{13} d_1 + 5120 a_1^{13} c_1) x^9 - 24 a_1^2 (11520 a_1^{12} c_1^2 - 24 a_1^2 (-5120 a_1^{13} c_1^2 - 24 a_1^2 c_1^2 - 24 a_1^2 (-5120 a_1^2 - 24 a_1^2 c_1^2 - 2$ $23040\,{a_{1}}^{12}{c_{1}}{d_{1}} + 11520\,{a_{1}}^{12}{d_{1}}^{2})x^{8} - 24\,{a_{1}}^{2}(-15360\,{a_{1}}^{11}{d_{1}}^{3} + 46080\,{a_{1}}^{11}{c_{1}}{d_{1}}^{2} + 15360\,{a_{1}}^{11}{c_{1}}^{3} - 24\,{a_{1}}^{2}(-15360\,{a_{1}}^{11}{d_{1}}^{3} + 46080\,{a_{1}}^{11}{c_{1}}{d_{1}}^{2} + 15360\,{a_{1}}^{11}{c_{1}}{d_{1}}^{3} - 24\,{a_{1}}^{2}{d_{1}}^{3} + 46080\,{a_{1}}^{11}{c_{1}}{d_{1}}^{2} + 15360\,{a_{1}}^{11}{c_{1}}{d_{1}}^{3} - 24\,{a_{1}}^{2}{d_{1}}^{3} + 24\,{a_{1}}^{2}{d_{1}}^{3$ $46080\,{a_{1}}^{11}{c_{1}}^{2}{d_{1}})x^{7} - 24\,{a_{1}}^{2}(-53760\,{a_{1}}^{10}{c_{1}}^{3}{d_{1}} + 80640\,{a_{1}}^{10}{c_{1}}^{2}{d_{1}}^{2} + 13440\,{a_{1}}^{10}{d_{1}}^{4} - 53760\,{a_{1}}^{10}{c_{1}}{d_{1}}^{3} + 1000\,{a_{1}}^{2}{d_{1}}^{2} + 1000\,{a_{1}}^{2} + 1000\,{a_{1}}^{2}{d_{1}}^{2} + 1000\,{a_{1}}^{2} + 1000\,{a_{1}}$ $13440\,{a_{1}}^{10}{c_{1}}^{4})x^{6} - 24\,{a_{1}}^{2}(-207360\,{a_{1}}^{7}{a_{2}}^{2}{c_{1}} + 40320\,{a_{1}}^{9}{c_{1}}{d_{1}}^{4} - 80640\,{a_{1}}^{9}{c_{1}}^{2}{d_{1}}^{3} - 69120\,{a_{1}}^{8}{a_{3}}{d_{1}} + 69120\,{a_{1}}^{6}{a_{1}}^{2}{d_{1}}^{2} - 69120\,{a_{1}}^{6}{a_{1}}^{2} - 69120\,{a_{1}}^{6}{a_{1}}$ $207360 a_1^{-7} a_2^{-2} d_1 - 8064 a_1^{-9} d_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-3} d_1^{-2} + 8064 a_1^{-9} c_1^{-5} - 69120 a_1^{-9} c_3 - 40320 a_1^{-9} c_1^{-4} d_1 + 80640 a_1^{-9} c_1^{-5} d_1^{-5} d_1^{$ $207360\,{a_1}^8{a_2}{d_2} + \,69120\,{a_1}^9{d_3} + \,207360\,{a_1}^8{a_2}{c_2} + \,69120\,{a_1}^8{a_3}{c_1})x^5 - 24\,{a_1}^2(3360\,{a_1}^8{c_1}^6 +$ $3360 a_1^{\,8} d_1^{\,6} + 345600 \, t^2 a_1^{\,14} + 86400 \, a_1^{\,8} c_2^{\,2} + 86400 \, a_1^{\,8} d_2^{\,2} - 345600 \, ta_1^{\,11} c_2 + 345600 \, ta_1^{\,11} d_2 - 366600 \, ta_1^{\,11} d_2 - 366600 \, ta_1^{\,11} d_2 - 366600 \, ta_1^$ $172800\,{a_1}^8{c_1}{c_3} + 172800\,{a_1}^8{c_1}{d_3} - 172800\,{a_1}^8{c_2}{d_2} + 172800\,{a_1}^8{c_3}{d_1} - 172800\,{a_1}^8{d_1}{d_3} + 172800\,{a_1}^7{a_3}{c_1}^2 + 172800\,{a_1}^8{d_1}{d_3} + 172800\,{a_1}^8{d_$ $172800\,{a_{1}}^{7}{a_{3}}{d_{1}}^{2} - 432000\,{a_{1}}^{6}{a_{2}}^{2}{c_{1}}^{2} - 432000\,{a_{1}}^{6}{a_{2}}^{2}{d_{1}}^{2} + 345600\,t{a_{1}}^{10}{a_{2}}{c_{1}} - 345600\,t{a_{1}}^{10}{a_{2}}{d_{1}} + 34660\,t{a_{1}}^{10}{a_{2}}{d_{1}} + 34660\,t{a_{1}}^{10}{a_{2}}{d_{1}} + 34660\,t{a_{1}}^{10}{a_{2}}{d_{1}} + 34660\,t{a_{1}}^{10}{a_{2}}{d_{1}} + 34660\,t{a_{1}}^{10}{a_{2}}{d_{1}} + 34660\,t{a_{1}}^{10}{a_{2}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}}{d_{1}} + 34660\,t{a_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{$ $345600\,a_{1}^{\,7}a_{2}c_{1}c_{2} - 345600\,a_{1}^{\,7}a_{2}c_{1}d_{2} - 345600\,a_{1}^{\,7}a_{2}c_{2}d_{1} + 345600\,a_{1}^{\,7}a_{2}d_{1}d_{2} - 345600\,a_{1}^{\,7}a_{3}c_{1}d_{1} + 345600\,a_{1}^{\,7}a_{2}d_{1}d_{2} - 34660\,a_{1}^{\,7}a_{2}d_{1}d_{2} 864000\,{a_{1}}^{6}{a_{2}}^{2}{c_{1}}{d_{1}})x^{4} - 24\,{a_{1}}^{2}(960\,{a_{1}}^{7}{c_{1}}^{7} - 960\,{a_{1}}^{7}{d_{1}}^{7} + 691200\,{t}^{2}{a_{1}}^{13}{c_{1}} - 691200\,{t}^{2}{a_{1}}^{13}{d_{1}} - 691200\,{t}^$ $6720\,{a_{1}}^{7}{c_{1}}^{6}{d_{1}} + 20160\,{a_{1}}^{7}{c_{1}}^{5}{d_{1}}^{2} - 33600\,{a_{1}}^{7}{c_{1}}^{4}{d_{1}}^{3} + 33600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{4} - 20160\,{a_{1}}^{7}{c_{1}}^{2}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{2}{d_{1}}^{3} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{4} - 20160\,{a_{1}}^{7}{c_{1}}^{2}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{3} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{4} - 20160\,{a_{1}}^{7}{c_{1}}^{2}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{3} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{4} - 20160\,{a_{1}}^{7}{c_{1}}^{2}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{3} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{4} - 20160\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{3} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{4} - 20160\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{3} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{3}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5}{d_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5} + 3600\,{a_{1}}^{5} + 3600\,{a_{1}}^{7}{c_{1}}^{5} +$ $6720\,{a_{1}}^{7}{c_{1}}{d_{1}}^{6} + 172800\,{a_{1}}^{7}{c_{1}}{c_{2}}^{2} + 172800\,{a_{1}}^{7}{c_{1}}{d_{2}}^{2} - 172800\,{a_{1}}^{7}{c_{2}}^{2}{d_{1}} - 172800\,{a_{1}}^{7}{d_{1}}{d_{2}}^{2} - 172800\,{a_{1}}^{7}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{$ $172800\,{a_{1}}^{7}{c_{1}}^{2}{c_{3}} + 172800\,{a_{1}}^{7}{c_{1}}^{2}{d_{3}} - 172800\,{a_{1}}^{7}{c_{3}}{d_{1}}^{2} + 172800\,{a_{1}}^{7}{d_{1}}^{2}{d_{3}} + 172800\,{a_{1}}^{6}{a_{3}}{c_{1}}^{3} - 172800\,{a_{1}}^{6}{a_{3}}{c_{1}}^{3} - 172800\,{a_{1}}^{7}{d_{1}}^{2}{d_{3}} + 172800\,{a_{1}}^{6}{a_{3}}{c_{1}}^{3} - 172800\,{a_{1}}^{6}{a_{1}}{c_{1}}^{3} - 172800\,{a_{1}}^{6}{a_{1}}{c_{1}}{c_{1}}^{3} - 172800\,{a_{1}}^{6}{a_{1}}{c_{1}}{c_{1}}^{3} - 172800\,{a_{1}}^{6}{a_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{$ $172800\,{a_1}^6{a_3}{d_1}^3 - 345600\,{a_1}^5{a_2}^2{c_1}^3 + 345600\,{a_1}^5{a_2}^2{d_1}^3 - 691200\,{ta_1}^{10}{c_1}{c_2} + 691200\,{ta_1}^{10}{c_1}{d_2} + 691200\,{ta_1}{c_1}{d_2} + 691200\,{ta_1}{c_1}{d_2} + 691200\,{ta$ $691200\,{ta_1}^{10}{c_2}{d_1} - 691200\,{ta_1}^{10}{d_1}{d_2} + 691200\,{ta_1}^9{a_2}{c_1}^2 + 691200\,{ta_1}^9{a_2}{d_1}^2 + 345600\,{a_1}^7{c_1}{c_3}{d_1} - 691200\,{ta_1}^9{a_2}{d_1}^2 + 691200\,{ta_1}^9{a_2}{d_1}^2 +$ $345600\,a_{1}^{-7}c_{1}d_{1}d_{3}+172800\,a_{1}^{-6}a_{2}c_{1}^{-2}c_{2}-172800\,a_{1}^{-6}a_{2}c_{1}^{-2}d_{2}+172800\,a_{1}^{-6}a_{2}c_{2}d_{1}^{-2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}^{-2}d_{2}-172800\,a_{1}^{-6}a_{2}d_{1}-172800\,a_{1}^{-6}a_{2}d_{1}-172800\,a_{1}^{-6}a_{2}d_{1}-172800\,a_{1}^{-6}a_{2}d_{1}-172800\,a_{1}^{-6}a_{2}d_{1}-172800\,a_$

 $518400\,{a_{1}}^{6}a_{3}c_{1}{}^{2}d_{1} + 518400\,{a_{1}}^{6}a_{3}c_{1}d_{1}{}^{2} + 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}{}^{2}d_{1} - 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{7}c_{1}c_{2}d_{2} + 518400\,{a_{1}}^{6}a_{3}c_{1}d_{1}{}^{2} + 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}{}^{2}d_{1} - 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{7}c_{1}c_{2}d_{2} + 518400\,{a_{1}}^{6}a_{3}c_{1}d_{1}{}^{2} + 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2} - 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{7}c_{1}c_{2}d_{2} + 518400\,{a_{1}}^{6}a_{3}c_{1}d_{1}{}^{2} + 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2} - 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{7}c_{1}c_{2}d_{2} + 518400\,{a_{1}}^{6}a_{2}c_{1}d_{1}{}^{2} + 1036800\,{a_{1}}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{7}c_{1}c_{2}d_{2} + 516400\,{a_{1}}^{6}a_{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{6}a_{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{7}c_{1}c_{2}d_{2} + 516400\,{a_{1}}^{6}a_{2}c_{1}d_{1}{}^{2} - 345600\,{a_{1}}^{6}a_{2}c_{1}d_{1}{}^{2} - 34660\,{a_{1}}^{6}a_{2}c_{1}d_{1}{}^{2} - 34660\,{a_{1}}^{6}a_{1}d_{1}{}^{2} - 34660\,{a_{1}}^{6}a_{1}d_{1}d_{1}{}^{2} - 34660\,{a_{1}}^{6$ $345600\,{a_1}^7{c_2}{d_1}{d_2} - 345600\,{a_1}^6{a_2}{c_1}{c_2}{d_1} + 345600\,{a_1}^6{a_2}{c_1}{d_1}{d_2} - 1382400\,{ta_1}^9{a_2}{c_1}{d_1})x^3 - 24\,{a_1}^2(180\,{a_1}^6{c_1}^8 + 13600\,{a_1}^6{c_1}^8 + 13600\,{a_1}^6{c_1}^6{c_1}^8 + 13600\,{a_1}^6{c_1}^6{c_1}^8 + 13600\,{a_1}^6{c_1}^6{c_1}^6{c_1}^6{c_$ $180\,{a_1}^{6}{d_1}^{8} + 518400\,{t^2}{a_1}^{12}{c_1}^{2} + 518400\,{t^2}{a_1}^{12}{d_1}^{2} - 1440\,{a_1}^{6}{c_1}^{7}{d_1} + 5040\,{a_1}^{6}{c_1}^{6}{d_1}^{2} - 10080\,{a_1}^{6}{c_1}^{5}{d_1}^{3} + 5040\,{a_1}^{6}{c_1}^{6}{d_1}^{2} - 10080\,{a_1}^{6}{c_1}^{6}{d_1}^{3} + 5040\,{a_1}^{6}{c_1}^{6}{d_1}^{2} + 5040\,{a_1}^{6}{c_1}^{6}{c_1}^{6}{d_1}^{2} + 5040\,{a_1}^{6}{c_1}^{6}{d_1} + 5040\,{a$ $12600\,a_{1}{}^{6}c_{1}{}^{4}d_{1}{}^{4}-10080\,a_{1}{}^{6}c_{1}{}^{3}d_{1}{}^{5}+5040\,a_{1}{}^{6}c_{1}{}^{2}d_{1}{}^{6}-1440\,a_{1}{}^{6}c_{1}d_{1}{}^{7}-86400\,a_{1}{}^{6}c_{1}{}^{3}c_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+86400\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}{}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+8640\,a_{1}{}^{6}c_{1}^{3}d_{3}+860\,a_{1}^{6}c_{1}^{3}d_{3}+8640\,a_{1}^{6}c_{1}^{3}d_{3}+8640\,a_{1$ $86400\,{a_{1}}^{6}{c_{3}}{d_{1}}^{3} - 86400\,{a_{1}}^{6}{d_{1}}^{3}{d_{3}} + 86400\,{a_{1}}^{5}{a_{3}}{c_{1}}^{4} + 86400\,{a_{1}}^{5}{a_{3}}{d_{1}}^{4} - {129600}\,{a_{1}}^{4}{a_{2}}^{2}{c_{1}}^{4} - {1$ $129600\,a_{1}{}^{4}a_{2}{}^{2}d_{1}{}^{4}+129600\,a_{1}{}^{6}c_{1}{}^{2}c_{2}{}^{2}+129600\,a_{1}{}^{6}c_{1}{}^{2}d_{2}{}^{2}+129600\,a_{1}{}^{6}c_{2}{}^{2}d_{1}{}^{2}+129600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{6}d_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1}{}^{2}d_{2}{}^{2}-12600\,a_{1$ $259200\,{a_1}^6{c_1}{c_2}^2{d_1} - 259200\,{a_1}^6{c_1}{d_1}{d_2}^2 - 259200\,{a_1}^6{c_2}{d_1}^2{d_2} - 1036800\,{t^2}{a_1}^{12}{c_1}{d_1} - 518400\,{ta_1}^9{c_1}^2{c_2} + 1000\,{ta_2}^2{c_2} + 1000\,{t$ $518400\,{ta_1}^9{c_1}^2{d_2} - 518400\,{ta_1}^9{c_2}{d_1}^2 + 518400\,{ta_1}^9{d_1}^2{d_2} + 518400\,{ta_1}^8{a_2}{c_1}^3 - 518400\,{ta_1}^8{a_2}{d_1}^3 + 518400\,{ta_1}^8{a_2}{d_1}^2 + 5184$ $518400\,{a_{1}}^{5}a_{3}c_{1}^{-2}d_{1}^{2} - 345600\,{a_{1}}^{5}a_{3}c_{1}d_{1}^{-3} + 518400\,{a_{1}}^{4}a_{2}^{-2}c_{1}^{-3}d_{1} - 777600\,{a_{1}}^{4}a_{2}^{-2}c_{1}^{-2}d_{1}^{-2} + 518400\,{a_{1}}^{4}a_{2}^{-2}c_{1}d_{1}^{-3} - 518400\,{a_{1}}^{-2}a_{1}^{-2}d_{1}^{-2} + 518400\,{a_{1}}^{-4}a_{2}^{-2}c_{1}^{-3}d_{1}^{-3} - 51640\,{a_{1}}^{-4}a_{2}^{-2}c_{1}^{-3}d_{1}^{-3} - 51640\,{a_{1}}^{-3}d_{1}^{-3} - 51640\,{a_{1}}^{-3} - 51640\,{a_{1}}^{-3}$ $259200\,{a_1}^6{c_1}^2{c_2}{d_2} + 518400\,{a_1}^6{c_1}{c_2}{d_1}{d_2} + 1036800\,{ta_1}^9{c_1}{c_2}{d_1} - 1036800\,{ta_1}^9{c_1}{d_1}{d_2} - 1555200\,{ta_1}^8{a_2}{c_1}^2{d_1} + 1036800\,{ta_1}^9{c_1}{d_2} - 1555200\,{ta_1}^8{c_1}{d_2} - 1555200\,{ta_1}^8{c_1}{d_2} - 1555200\,{ta_1}^8{c_1}{d_2} - 1555200\,{ta_1}^8{c_1}{d_2} - 1556200\,{ta_1}^8{c_1}{d_2} - 1556200\,{ta_1}^8{c_1}{d_2} - 1556200\,{ta_1}^8{c_1}{d_2} - 156660\,{ta_1}^8{c_1}{d_2} - 156660\,{ta_1}^8{c_1$ $1555200\,{ta_1}^8{a_2}{c_1}{d_1}^2)x^2 - 24\,{a_1}^2(-86400\,{a_1}^5{c_2}^3 + 86400\,{a_1}^5{d_2}^3 + 691200\,{t^3}{a_1}^{14} + 20\,{a_1}^5{c_1}^9 - {a_1}^6{a_2}^2)x^2 - 24\,{a_1}^2(-86400\,{a_1}^5{c_2}^3 + 86400\,{a_1}^5{d_2}^3 + 691200\,{t^3}{a_1}^{14} + 20\,{a_1}^5{c_1}^9 - {a_1}^6{a_2}^2)x^2 - 24\,{a_1}^2(-86400\,{a_1}^5{c_2}^3 + 86400\,{a_1}^5{d_2}^3 + 691200\,{t^3}{a_1}^{14} + 20\,{a_1}^5{c_1}^9 - {a_1}^6{a_2}^2)x^2 - 24\,{a_1}^2(-86400\,{a_1}^5{c_2}^3 + 86400\,{a_1}^5{d_2}^3 + 691200\,{t^3}{a_1}^{14} + 20\,{a_1}^5{c_1}^9 - {a_1}^6{a_2}^2)x^2 - 24\,{a_1}^6{a_2}^2 + {a_1}^6{a_2}^2 + {a_1}^6{a$ $20\,{a_{1}}^{5}{d_{1}}^{9} + 518400\,{ta_{1}}^{8}{c_{1}}^{2}{c_{2}}{d_{1}} - 518400\,{ta_{1}}^{8}{c_{1}}^{2}{d_{1}}{d_{2}} - 518400\,{ta_{1}}^{8}{c_{1}}{c_{2}}{d_{1}}^{2} + 518400\,{ta_{1}}^{8}{c_{1}}{d_{1}}^{2}{d_{2}} - 518400\,{ta_{1}}^{8}{c_{1}}{d_{2}} - 516400\,{ta_{1}}^{8}{c_{1}}{d_{2}} - 516400\,{ta_{1}}{d_{2}} - 516400\,{ta_{1}}{d_{2}} - 516400\,{ta_{1}$ $691200\,ta_{1}^{7}a_{2}c_{1}^{3}d_{1} + 1036800\,ta_{1}^{7}a_{2}c_{1}^{2}d_{1}^{2} - 691200\,ta_{1}^{7}a_{2}c_{1}d_{1}^{3} - 1036800\,ta_{1}^{7}a_{2}c_{1}c_{2} + 1036800\,ta_{1}^{7}a_{2}c_{1}d_{2} + 1036800\,ta_{1}^{7}a_{2} + 1036800\,ta_{1}^{7}a_{2} + 1036800\,ta_{1}^{7}a_{2} + 1036800\,ta_{1}^{7}a_{2} + 1036800\,ta_{1}^{7}a_{2} + 1036800\,ta_{1}^{7}a_{2} + 10$ $1036800\,ta_{1}{}^{7}a_{2}c_{2}d_{1} - 1036800\,ta_{1}{}^{7}a_{2}d_{1}d_{2} + 172800\,t^{2}a_{1}{}^{11}c_{1}{}^{3} - 172800\,t^{2}a_{1}{}^{11}d_{1}{}^{3} + 259200\,a_{1}{}^{5}c_{2}{}^{2}d_{2} - 103660\,ta_{1}{}^{7}a_{2}d_{1}d_{2} + 172800\,t^{2}a_{1}{}^{11}c_{1}{}^{3} - 172800\,t^{2}a_{1}{}^{11}d_{1}{}^{3} + 259200\,ta_{1}{}^{5}c_{2}{}^{2}d_{2} - 10366\,ta_{1}{}^{7}a_{2}d_{1}d_{2} + 172800\,t^{2}a_{1}d_{2} + 172800\,t^{2$ $259200\,{a_1}^5{c_2}{d_2}^2 + 86400\,{a_1}^2{a_2}^3{c_1}^3 - 86400\,{a_1}^2{a_2}^3{d_1}^3 - {1036800}\,{t^2}{a_1}^{11}{c_2} + {1036800}\,{t^2}{a_1}^{11}{d_2} - {103680}\,{t^2}{a_1}^{11}{d_2} - {103680}\,{t^2}{a_1}{d_2} -$ $180\,{a_1}^5{c_1}^8{d_1} + 720\,{a_1}^5{c_1}^7{d_1}^2 - 1680\,{a_1}^5{c_1}^6{d_1}^3 + 2520\,{a_1}^5{c_1}^5{d_1}^4 - 2520\,{a_1}^5{c_1}^4{d_1}^5 + 1680\,{a_1}^5{c_1}^3{d_1}^6 - 2520\,{a_1}^5{c_1}^2{d_1}^2 + 2520\,{a_1}^5{c_1}^$ $720\,{a_1}^5{c_1}^2{d_1}^7 + 180\,{a_1}^5{c_1}{d_1}^8 + 518400\,{ta_1}^8{c_2}^2 + 518400\,{ta_1}^8{d_2}^2 - 21600\,{a_1}^5{c_1}^4{c_3} + 21600\,{a_1}^5{c_1}^4{d_3} - 21600\,{a_1}^5{c_1}^5{c_1}^4{d_3} - 21600\,{a_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c_1}^5{c$ $21600\,{a_{1}}^{5}{c_{3}}{d_{1}}^{4} + 21600\,{a_{1}}^{5}{d_{1}}^{4}{d_{3}} + 21600\,{a_{1}}^{4}{a_{3}}{c_{1}}^{5} - 21600\,{a_{1}}^{4}{a_{3}}{d_{1}}^{5} - 21600\,{a_{1}}^{3}{a_{2}}^{2}{c_{1}}^{5} + 21600\,{a_{1}}^{3}{a_{2}}^{5} + 21600\,{a_{1}}^{3}{a_{2}}^{2}{c_{1}}^{5} + 21600\,{a_{1}}^{3}{a_{2}}^{5} + 21600\,{a_{1}}^{5}{a_{2}}$ $21600\,{a_{1}}^{3}{a_{2}}^{2}{d_{1}}^{5} + 43200\,{a_{1}}^{5}{c_{1}}^{3}{c_{2}}^{2} + 43200\,{a_{1}}^{5}{c_{1}}^{3}{d_{2}}^{2} - 43200\,{a_{1}}^{5}{c_{2}}^{2}{d_{1}}^{3} - 43200\,{a_{1}}^{5}{d_{1}}^{3}{d_{2}}^{2} - 43200\,{a_{1}}^{5}{d_{1}}^{3}{d_{1}}^{3}{d_{2}}^{2} - 43200\,{a_{1}}^{5}{d_{1}}^{3}{d_{2}}^{2} - 43200\,{a_{1}}^{5}$ $86400\,{a_{1}}^{5}{c_{1}}^{3}{c_{2}}{d_{2}}-129600\,{a_{1}}^{5}{c_{1}}^{2}{c_{2}}^{2}{d_{1}}-129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{1}}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}{c_{2}}^{2}{d_{1}}^{2}+129600\,{a_{1}}^{5}{c_{1}}{d_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{2}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}+129600\,{a_{1}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}+129600\,{a_{1}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}+129600\,{a_{1}}^{5}{c_{1}}^{2}+129600\,{a_{1}}^{2}+129600\,{a_{1}}^{2}+129600\,{a_{1}}^{2}+129600\,{a_{1}}^{2}+129600\,{a_{1}}^{2}+129600\,{a_{1}}+129600\,{a_{1}}^{2}+129600\,{a_{1}}^{$ $86400\,a_{1}{}^{5}c_{2}d_{1}{}^{3}d_{2} - 518400\,t^{2}a_{1}{}^{11}c_{1}{}^{2}d_{1} + 518400\,t^{2}a_{1}{}^{11}c_{1}d_{1}{}^{2} - 172800\,ta_{1}{}^{8}c_{1}{}^{3}c_{2} + 172800\,ta_{1}{}^{8}c_{1}{}^{3}d_{2} + 172800\,ta_{1}{}^{8}c_{1}{}^{6}d_{2} + 172800\,ta_{1}{}^{$ $172800\,{ta_1}^8{c_2}{d_1}^3 - 172800\,{ta_1}^8{d_1}^3{d_2} + 172800\,{ta_1}^7{a_2}{c_1}^4 + 172800\,{ta_1}^7{a_2}{d_1}^4 - 1036800\,{ta_1}^8{c_2}{d_2} + 172800\,{ta_1}^8{c_2}{d_2} + 172800\,{ta_1}^8{c_2}{d_1}^2 - 1036800\,{ta_1}^8{c_2}{d_2} + 172800\,{ta_1}^8{c_2}{d_2} + 172800\,{ta_1}^8{$ $518400\,ta_{1}{}^{6}a_{2}{}^{2}c_{1}{}^{2}+518400\,ta_{1}{}^{6}a_{2}{}^{2}d_{1}{}^{2}+86400\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}-86400\,a_{1}{}^{5}c_{1}{}^{3}d_{1}d_{3}-129600\,a_{1}{}^{5}c_{1}{}^{2}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{3}d_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{3}c_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{2}+1000\,a_{1}{}^{5}c_{1}{}^{2}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+1000\,a_{1}{}^{5}+100$ $129600\,{a_{1}}^{5}{c_{1}}^{2}{d_{1}}^{2}{d_{3}} + 86400\,{a_{1}}^{5}{c_{1}}{c_{3}}{d_{1}}^{3} - 86400\,{a_{1}}^{5}{c_{1}}{d_{1}}^{3}{d_{3}} - 21600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{4}{c_{2}} + 21600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{4}{d_{2}} - 21600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{4}{d_{2}}{d_{2}} - 21600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{4}{d_{2}}{d_{2}} - 21600\,{a_{1}}^{4}{a_{2}}{c_{1}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}$ $21600\,a_{1}^{\ 4}a_{2}c_{2}d_{1}^{\ 4} + 21600\,a_{1}^{\ 4}a_{2}d_{1}^{\ 4}d_{2} - 108000\,a_{1}^{\ 4}a_{3}c_{1}^{\ 4}d_{1} + 216000\,a_{1}^{\ 4}a_{3}c_{1}^{\ 3}d_{1}^{\ 2} - 216000\,a_{1}^{\ 4}a_{3}c_{1}^{\ 2}d_{1}^{\ 3} + 21600\,a_{1}^{\ 4}a_{3}c_{1}^{\ 3}d_{1}^{\ 2} - 216000\,a_{1}^{\ 4}a_{3}c_{1}^{\ 2}d_{1}^{\ 3} + 21600\,a_{1}^{\ 4}a_{3}c_{1}^{\ 3}d_{1}^{\ 2} - 216000\,a_{1}^{\ 4}a_{3}c_{1}^{\ 2}d_{1}^{\ 3} + 21600\,a_{1}^{\ 4}a_{3}c_{1}^{\ 3}d_{1}^{\ 2} - 216000\,a_{1}^{\ 4}a_{3}c_{1}^{\ 3}d_{1}^{\ 4} + 21600\,a_{1}^{\ 4}a_{3}c_{1}^{\ 4}d_{1}^{\ 4} + 21600\,a_{1}^{\ 4}a_{1}^{\ 4}a_{2}c_{1}^{\ 4}d_{1}^{\ 4} + 21600\,a_{1}^{\ 4}a_{1}^{\ 4}d_{1}^{\ 4} + 21600\,a_{1}^{\ 4}d_{1}^{\ 4} + 21600\,a_{1}^{\ 4}a_{1}^{\ 4}d_{1}^{\ 4} + 21600\,a_{1}^{\ 4}d_{1}^{\ 4} + 21600\,a$ $108000\,{a_1}^4{a_3}{c_1}{d_1}^4 + 108000\,{a_1}^3{a_2}^2{c_1}^4{d_1} - 216000\,{a_1}^3{a_2}^2{c_1}^3{d_1}^2 + 216000\,{a_1}^3{a_2}^2{c_1}^2{d_1}^3 - 108000\,{a_1}^3{a_2}^2{c_1}{d_1}^4 + 108000\,{a_1}^3{a_2}^2{c_1}^4{d_1} - 216000\,{a_1}^3{a_2}^2{c_1}^3{d_1}^2 + 216000\,{a_1}^3{a_2}^2{c_1}^2{d_1}^3 - 108000\,{a_1}^3{a_2}^2{c_1}{d_1}^4 + 108000\,{a_1}^3{a_2}^2{c_1}^2{d_1}^2 - 216000\,{a_1}^3{a_2}^2{c_1}^2{d_1}^2 - 216000\,{a_1}^3{a_2}^2{a_1}^2{d_1}^2 - 216000\,{a_1}^3{a_2}^2{a_1}^2 - 216000\,{a_1$ $259200\,a_{1}^{\ 4}a_{2}c_{1}c_{2}^{\ 2}+259200\,a_{1}^{\ 4}a_{2}c_{1}d_{2}^{\ 2}-259200\,a_{1}^{\ 4}a_{2}c_{2}^{\ 2}d_{1}-259200\,a_{1}^{\ 4}a_{2}d_{1}d_{2}^{\ 2}-259200\,a_{1}^{\ 3}a_{2}^{\ 2}c_{1}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}c_{1}^{\ 2}c_{2}^{\ 2}d_{1}-259200\,a_{1}^{\ 4}a_{2}d_{1}d_{2}^{\ 2}-259200\,a_{1}^{\ 3}a_{2}^{\ 2}c_{1}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{1}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+259200\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+2560\,a_{1}^{\ 4}a_{2}^{\ 2}c_{2}+2560\,a_{1}^{\ 4}a_{2}^{\ 4}c_{2}+2560\,a_{1}^{\ 4}c_$ $259200\,a_1^{\,3}a_2^{\,2}c_1^{\,2}d_2 - 259200\,a_1^{\,3}a_2^{\,2}c_2d_1^{\,2} + 259200\,a_1^{\,3}a_2^{\,2}d_1^{\,2}d_2 - 259200\,a_1^{\,2}a_2^{\,3}c_1^{\,2}d_1 + 259200\,a_1^{\,2}a_2^{\,3}c_1d_1^{\,2} + 259200\,a_1^{\,2}a_2^{\,3}c_1d_1^{\,2} + 259200\,a_1^{\,3}a_2^{\,2}d_1^{\,2}d_2 - 259200\,a_1^{\,3}a_2^{\,2}d_1^{\,2}d_2 - 259200\,a_1^{\,3}a_2^{\,3}d_1^{\,2}d_2 - 259200\,a_1^{\,3}a_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}d_2^{\,3}d_1^{\,3}$ $1036800\,t^2a_1{}^{10}a_2c_1\,-\,1036800\,t^2a_1{}^{10}a_2d_1\,+\,259200\,a_1{}^5c_1{}^2c_2d_1d_2\,-\,259200\,a_1{}^5c_1c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1d_2\,-\,259200\,a_1{}^5c_1c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1d_2\,-\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_1{}^2d_2\,+\,259200\,a_1{}^5c_1{}^2c_2d_2\,+\,25600\,a_1{}^5c_1{}^2c_2d_2\,+\,25600\,a_1{}^5c_1{}^2c_2d_2\,+\,25600\,a_1{}^5c_1{}^2c_2d_2\,+\,25600\,a_2{}^2c_2d_2\,+\,25600\,a_2{}^2c_2d_2\,+\,25600$ $86400\,{a_{1}}^{4}{a_{2}}{c_{1}}^{3}{c_{2}}{d_{1}} - 86400\,{a_{1}}^{4}{a_{2}}{c_{1}}^{3}{d_{1}}{d_{2}} - 129600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{2}{c_{2}}{d_{1}}^{2} + 129600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{2}{d_{1}}^{2}{d_{2}} + 129600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{2}} + 129600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{2}} + 129600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{2}{d_{1}}^{2}{d_{2}} + 129600\,{a_{1}}^{4}{a_{2}}{c_{1}}^{2}{d_{1}}^{2}{d_{2}}^{2}{d_{1}}^{2}{d_{2}}^{2}{d_{1}}^{2}{d_{2}}^{2}{d_{1}}^{2}{d_{2}}^{2}{d_{1}}^{2}{d_{2}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{2}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1}}^{2}{d_{1$ $86400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}{}^{3}-86400\,a_{1}{}^{4}a_{2}c_{1}d_{1}{}^{3}d_{2}-518400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{2}+518400\,a_{1}{}^{4}a_{2}c_{2}d_{1}d_{2}+518400\,a_{1}{}^{3}a_{2}{}^{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}{}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-6400\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}^{4}a_{2}c_{1}c_{2}d_{1}-640\,a_{1}-660\,a_{1}^{4}a_{$ $518400\,a_{1}{}^{3}a_{2}{}^{2}c_{1}d_{1}d_{2} - 1036800\,ta_{1}{}^{6}a_{2}{}^{2}c_{1}d_{1})x - 24\,a_{1}{}^{2}(518400\,a_{1}{}^{3}a_{2}c_{1}c_{2}d_{1}d_{2} + 1036800\,ta_{1}{}^{6}a_{2}c_{1}c_{2}d_{1} - 1036800\,ta_{1}{}^{6}a_{2}c_{1}c_{2}d_{1}d_{2} + 103680\,ta_{1}{}^{6}a_{2}c_{1}c_{2}d_{1}d_{2} + 103680\,ta_{1}{}^{6}a_{2}c_{1}c_{2}d_{1}d_{2} + 103680\,ta_{1}{}^{6}a_{2}c_{1}c_{2}d_{1}d_{2} + 103680\,ta_{1}c_{2}d_{2}d_{2} + 103680\,ta_{1}c_{2}d_{2} + 103680\,ta_{1}c_{2}d_{2} + 103680\,ta_{1}c_{2}d_{2} + 103680\,ta_{1}c_{2}d_{2} + 103680\,ta_{1}c_{2} + 103680\,ta_{1}c_{2$ $1036800 \, ta_{1}{}^{6}a_{2}c_{1}d_{1}d_{2} + 518400 \, a_{1}{}^{2}a_{2}a_{3}c_{1}c_{2} - 518400 \, a_{1}{}^{2}a_{2}a_{3}c_{1}d_{2} - 518400 \, a_{1}{}^{2}a_{2}a_{3}c_{2}d_{1} + 6160 \, a_{1}{}^{2}a_{2}a_{3}c_{2}d_{1} + 6160 \, a_{1}{}^{2}a_{2}a_{3}c_{1}d_{2} - 518400 \, a_{1}{}^{2}a_{2}a_{3}c_{2}d_{1} + 6160 \, a_{1}{}^{2}a_{2}a_{3}c_{1}d_{2} - 518400 \, a_{1}{}^{2}a_{2}a_{3}c_{2}d_{1} + 6160 \, a_{1}{}^{2}a_{2}a_{2}a_{2}d_{2}d_{2} + 6160 \, a_{1}{}^{2}a_{2}a_{2}d_{2}d_{2} + 6160 \, a_{1}{}^{2}a_{2}a_{2}d_{2} + 6160 \, a_{1}{}^{2}a_{2}a_{2}d_{2} + 6160 \, a_{1}{}^{2}a_{2}a_{2}d_{2} + 6160 \, a_{1}{}^{2}a_{2}a_{2}d_{2} + 6160 \, a_{1}{}^{2}a_{2}d_{2} + 6160$ $518400\,{a_{1}}^{2}a_{2}a_{3}d_{1}d_{2} + \\1036800\,{a_{1}}a_{2}^{2}a_{3}c_{1}d_{1} + \\43200\,{a_{1}}^{4}c_{1}^{-3}c_{2}d_{1}d_{2} - \\64800\,{a_{1}}^{4}c_{1}^{-2}c_{2}d_{1}^{-2}d_{2} + \\1036800\,{a_{1}}a_{2}^{-2}a_{3}c_{1}d_{1} + \\1036800\,{a_{1}}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}d_{1}d_{2} + \\1036800\,{a_{1}}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}d_{1}d_{2} + \\1036800\,{a_{1}}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}d_{1}d_{2} + \\1036800\,{a_{1}}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}d_{2} + \\1036800\,{a_{1}}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}d_{2} + \\1036800\,{a_{1}}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2} + \\1036800\,{a_{1}}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{-2}a_{2}^{ 43200\,{a_{1}}^{4}{c_{1}}{c_{2}}{d_{1}}^{3}{d_{2}}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}^{2}{c_{2}}{d_{2}}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{c_{2}}^{2}{d_{1}}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}{d_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}^{2}-259200\,{a_{1}}^{3}{a_{2}}{c_{1}}{d_{1}}{d_{2}}{d_{1}}{d_{1}}{d_{2}}{d_{1}}{d_{1}}{d_{1}}{d_{2}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_{1}}{d_$ $259200\,{a_1}^3{a_2}{c_2}{d_1}^2{d_2} - 86400\,{ta_1}^7{c_1}^3{d_1}{d_2} - {129600}\,{ta_1}^7{c_1}^2{c_2}{d_1}^2 + {129600}\,{ta_1}^7{c_1}^2{d_2} + 86400\,{ta_1}^7{c_1}{c_2}{d_1}^3 - {129600}\,{ta_1}^7{c_1}^2{d_1}^2 + {129600}\,{ta_1}^7{c_1}^2{d_2} + {129600}\,{ta_1}^7{c_1}{c_1}^2{d_2} + {129600}\,{ta_1}^7{c_1}^2{d_2} + {12$ $86400\,{ta_1}^7{c_1}{d_1}^3{d_2} - 108000\,{ta_1}^6{a_2}{c_1}^4{d_1} + 216000\,{ta_1}^6{a_2}{c_1}^3{d_1}^2 - 216000\,{ta_1}^6{a_2}{c_1}^2{d_1}^3 + 108000\,{ta_1}^6{a_2}{c_1}{d_1}^4 - 216000\,{ta_1}^6{a_2}{c_1}^2{d_1}^2 + 216000\,{ta_1}^6{$ $777600\,ta_{1}{}^{5}a_{2}{}^{2}c_{1}{}^{2}d_{1}+777600\,ta_{1}{}^{5}a_{2}{}^{2}c_{1}d_{1}{}^{2}+86400\,ta_{1}{}^{7}c_{1}{}^{3}c_{2}d_{1}-518400\,ta_{1}{}^{7}c_{1}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{1}d_{2}-518400\,ta_{1}{}^{7}c_{2}d_{1}d_{2}-518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{1}d_{2}-518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{1}d_{2}-518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}d_{2}+518400\,ta_{1}{}^{7}c_{2}+518400\,ta_{1}{}^{7}c_{2}+518400\,ta_{1}{}^{7}c_{2}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+51640\,ta_{1}+$ $518400\,ta_{1}{}^{6}a_{2}c_{1}{}^{2}c_{2}+518400\,ta_{1}{}^{6}a_{2}c_{1}{}^{2}d_{2}-518400\,ta_{1}{}^{6}a_{2}c_{2}d_{1}{}^{2}+518400\,ta_{1}{}^{6}a_{2}d_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}c_{1}{}^{4}c_{2}d_{1}-600\,a_{1}{}^{2}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}{}^{3}a_{2}a_{1}{}^{2}d_{2}+21600\,a_{1}a_{1}a_{2}a_{2}+21600\,a_{1}a_{1}a_{2}a_{2}+21600\,a_{1}a_{1}a_{2}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+21600\,a_{1}a_{2}+21600\,a_{1}a_{1}a_{2}+216$ $21600\,{a_{1}}^{3}a_{2}c_{1}{}^{4}d_{1}d_{2}-43200\,{a_{1}}^{3}a_{2}c_{1}{}^{3}c_{2}d_{1}{}^{2}+43200\,{a_{1}}^{3}a_{2}c_{1}{}^{3}d_{1}{}^{2}d_{2}+43200\,{a_{1}}^{3}a_{2}c_{1}{}^{2}c_{2}d_{1}{}^{3} 43200\,{a_{1}}^{3}a_{2}c_{1}{}^{2}d_{1}{}^{3}d_{2}-21600\,{a_{1}}^{3}a_{2}c_{1}c_{2}d_{1}{}^{4}+21600\,{a_{1}}^{3}a_{2}c_{1}d_{1}{}^{4}d_{2}+388800\,{a_{1}}^{2}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}c_{1}d_{1}{}^{4}d_{2}+388800\,{a_{1}}^{2}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}c_{1}d_{1}{}^{4}d_{2}+388800\,{a_{1}}^{2}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}c_{1}d_{1}{}^{4}d_{2}+388800\,{a_{1}}^{2}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}c_{1}d_{1}{}^{4}d_{2}+388800\,{a_{1}}^{2}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}{}^{2}c_{2}d_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}{}^{2}c_{1}-2600\,{a_{1}}^{3}a_{2}-2600\,{a_{1}}^{3}a_{2}-2600\,{a_{1}}^{3}a_{2}-2600\,{a_{1}}^{3}a_{2}-2600\,{a_{1}}^$ $518400\,a_{1}{}^{3}a_{2}c_{3}d_{2} - 518400\,a_{1}{}^{3}a_{2}d_{2}d_{3} - 172800\,a_{1}{}^{3}a_{3}c_{1}c_{3} + 172800\,a_{1}{}^{3}a_{3}c_{1}d_{3} + 172800\,a_{1}{}^{3}a_{3}c_{3}d_{1} - 172800\,a_{1}{}^{3}a_{3}c_{3}$ $172800\,{a_1}^3{a_3}{d_1}{d_3} + 518400\,{a_1}^2{a_2}^2{c_1}{c_3} - 518400\,{a_1}^2{a_2}^2{c_1}{d_3} - 1555200\,{a_1}^2{a_2}^2{c_2}{d_2} - 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_2}{d_2} - 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_2} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_2} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_2} + 518400\,{a_1}^2{a_2}^2{c_3}{d_2} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_2} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_1} + 518400\,{a_1}^2{a_2}^2{c_3}{d_2} + 518400\,{a_1}^2{a_2}^2{c_3}{d_2} + 51840$ $518400\,a_{1}^{2}a_{2}^{2}d_{1}d_{3} - 172800\,a_{1}^{2}a_{3}^{2}c_{1}d_{1} - 1555200\,a_{1}a_{2}^{3}c_{1}c_{2} + 1555200\,a_{1}a_{2}^{3}c_{1}d_{2} + 1555200\,a_{1}a_{2}^{3}c_{2}d_{1} - 1555200\,a_{1}a_{2}^{3}c_{2}^{3}c_{2}d_{1} - 1555200\,a_{1}a_{2}^{3}c_{2}^{3}c_{2} - 156560\,a_{1}a_{2}^{3}c_{2}^{3}c_{2} - 15666\,a_{1}^{3}c_{2}^{3}c_{2} - 1566\,a_{1}^{3}c_{2}^{3}c_{2} - 1566\,a_{1}^{3}c_{2}^{3}c_{2} - 1566\,a_{1}^{3}c_{2}^{3}c_{2} - 1566\,a_{1}^{3}c_{2}^{3}c_{2} - 1566\,a_{1}^{3}c_{2}^{3}c_{2} - 1566\,a_{1}^{3}c$

 $1555200\,a_{1}a_{2}{}^{3}d_{1}d_{2}-518400\,a_{1}a_{2}{}^{2}a_{3}c_{1}{}^{2}-518400\,a_{1}a_{2}{}^{2}a_{3}d_{1}{}^{2}+259200\,ta_{1}{}^{5}a_{2}{}^{2}c_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-259200\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-25620\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-25620\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-25620\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-25620\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-25620\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-25620\,ta_{1}{}^{5}a_{2}{}^{2}d_{1}{}^{3}-25620\,ta_{1}{}^{2}d_{1}{}^{2}d_{1}{}^{2}-2562$ $10800\,{a_1}^4{c_1}^4{c_2}{d_2} - 21600\,{a_1}^4{c_1}^3{c_2}^2{d_1} - 21600\,{a_1}^4{c_1}^3{d_1}{d_2}^2 + 32400\,{a_1}^4{c_1}^2{c_2}^2{d_1}^2 + 32400\,{a_1}^4{c_1}^2{d_1}^2{d_2}^2 - 21600\,{a_1}^4{c_1}^2{d_1}^2{d_2}^2 - 21600\,{a_1}^4{c_1}^2{d_2}^2 -$ $21600\,{a_1}^4{c_1}{c_2}^2{d_1}^3 - 21600\,{a_1}^4{c_1}{d_1}^3{d_2}^2 - 10800\,{a_1}^4{c_2}{d_1}^4{d_2} + 129600\,{a_1}^3{a_2}{c_1}^2{c_2}^2 + 129600\,{a_1}^3{a_2}{c_1}^2{d_2}^2 + 129600\,{a_1}^3{a_2}{c_1}^2{d_2}^2$ $129600 a_1^{\ 3} a_2 c_2^{\ 2} d_1^{\ 2} + 129600 a_1^{\ 3} a_2 d_1^{\ 2} d_2^{\ 2} - 518400 a_1^{\ 3} a_2 c_2 a_3 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 3} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 7} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 4} c_2 + 518400 a_1^{\ 7} a_2 c_2 d_3 - 21600 t a_1^{\ 7} c_1^{\ 7} c_1^{\ 7} c_2 + 518400 a_1^{\ 7} c_1^{\ 7}$ $21600\,ta_{1}{}^{7}c_{1}{}^{4}d_{2}-21600\,ta_{1}{}^{7}c_{2}d_{1}{}^{4}+21600\,ta_{1}{}^{7}d_{1}{}^{4}d_{2}+21600\,ta_{1}{}^{6}a_{2}c_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}{}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}a_{1}^{6}a_{2}d_{1}{}^{5}-21600\,ta_{1}a_{1}^{6}a_{2}d_{1}{}^{5}-21600\,ta$ $172800\,a_{1}a_{2}{}^{3}c_{1}{}^{3}d_{1}+259200\,a_{1}a_{2}{}^{3}c_{1}{}^{2}d_{1}{}^{2}-172800\,a_{1}a_{2}{}^{3}c_{1}d_{1}{}^{3}-86400\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{2}d_{1}{}^{2}-172800\,a_{1}a_{2}{}^{3}c_{1}d_{1}{}^{3}-86400\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{2}d_{1}{}^{2}-172800\,a_{1}a_{2}{}^{3}c_{1}d_{1}{}^{3}-86400\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{2}d_{1}{}^{2}-172800\,a_{1}a_{2}{}^{3}c_{1}d_{1}{}^{3}-86400\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{2}d_{1}{}^{2}-172800\,a_{1}a_{2}{}^{3}c_{1}d_{1}{}^{3}-86400\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}{}^{3}d_{1}+129600\,t^{2}a_{1}{}^{10}c_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}+1260\,t^{2}a_{1}$ $86400\,t^2a_1{}^{10}c_1d_1{}^3 + 21600\,a_1{}^2a_2{}^2c_1{}^3d_1{}^3 - 16200\,a_1{}^2a_2{}^2c_1{}^2d_1{}^4 + 6480\,a_1{}^2a_2{}^2c_1d_1{}^5 + 129600\,a_1{}^4c_1c_2{}^2d_2 - 16600\,a_1{}^2a_2{}^2c_1{}^2d_1{}^4 + 6480\,a_1{}^2a_2{}^2c_1d_1{}^5 + 129600\,a_1{}^4c_1c_2{}^2d_2 - 16600\,a_1{}^4c_1{}^2c_2{}^2d_2 - 16600\,a_1{}^2a_2{}^2c_1{}^2d_1{}^4 + 6480\,a_1{}^2a_2{}^2c_1{}^2d_1{}^5 + 129600\,a_1{}^4c_1{}^2c_2{}^2d_2 - 16600\,a_1{}^4c_1{}^2c_2{}^2d_2 - 16600\,a_1{}^4c_2{}^2c_2{}^2d_2 - 16600\,a_1{}^2c_2{}^2c_2{}^2d_2 - 16600\,a_1{}^2c_2{}^2$ $129600\,{a_1}^4{c_1}{c_2}{d_2}^2 - 129600\,{a_1}^4{c_2}^2{d_1}{d_2} + 129600\,{a_1}^4{c_2}{d_1}{d_2}^2 - 518400\,{t^2}{a_1}^{10}{c_1}{c_2} + 518400\,{t^2}{a_1}^{10}{c_1}{d_2} + 518400\,{t^2}{a_1}{d_2} + 516400\,{t^2}{a_1}{d_2} + 516400\,{t^2}{a_1}{d_2}$ $518400\,t^2a_1{}^{10}c_2d_1 - 518400\,t^2a_1{}^{10}d_1d_2 + 518400\,t^2a_1{}^9a_2c_1{}^2 + 518400\,t^2a_1{}^9a_2d_1{}^2 - 129600\,a_1{}^2a_2{}^2c_1{}^3c_2 + 518400\,t^2a_1{}^9a_2d_1{}^2 - 129600\,a_1{}^2a_2{}^2c_1{}^3c_2 + 518400\,t^2a_1{}^9a_2{}^2d_1{}^2 - 129600\,a_1{}^2a_2{}^2c_1{}^3c_2 + 518400\,t^2a_1{}^9a_2{}^2d_1{}^2 - 129600\,a_1{}^2a_2{}^2c_1{}^3c_2 + 518400\,t^2a_1{}^9a_2{}^2d_1{}^2 - 129600\,a_1{}^2a_2{}^2c_1{}^3c_2 + 518400\,t^2a_1{}^9a_2{}^2d_1{}^2 - 518400\,t^2a_1{}^9a_2{}^2d_1{}^2 - 518400\,t^2a_1{}^9a_2{}^2d_1{}^2 - 518400\,t^2a_1{}^3a_2{}^2d_1{}^2 - 518400\,t^2a_1{}^2a_2{}^2d_1{}^2 - 518400\,t^2a_1{}^2a_2{}^2d_$ $129600\,{a_1}^2{a_2}^2{c_1}^3{d_2} + 129600\,{a_1}^2{a_2}^2{c_2}{d_1}^3 - 129600\,{a_1}^2{a_2}^2{d_1}^3{d_2} + 259200\,{ta_1}^7{c_1}{c_2}^2 + 259200\,{ta_1}^7{c_1}{d_2}^2 - 259200\,{ta_1}^2{c_2}^2{d_1}^3 - 129600\,{a_1}^2{a_2}^2{d_1}^3{d_2} + 259200\,{ta_1}^2{c_1}{d_2}^2 - 259200\,{ta_1}^2{c_2}^2{d_1}^3 - 259200\,{ta_1}^2{c_2}^2{d_1}^2 - 259200\,{ta_1}^2{c_$ $259200\,ta_{1}{}^{7}c_{2}{}^{2}d_{1}-259200\,ta_{1}{}^{7}d_{1}d_{2}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{3}d_{1}-10800\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{3}-21600\,a_{1}{}^{4}c_{1}{}^{3}c_{3}d_{1}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{3}d_{1}-10800\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{3}-21600\,a_{1}{}^{4}c_{1}{}^{3}c_{3}d_{1}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{3}d_{1}-10800\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{3}-21600\,a_{1}{}^{4}c_{1}{}^{3}c_{3}d_{1}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{3}d_{1}-10800\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{3}-21600\,a_{1}{}^{4}c_{1}{}^{3}c_{3}d_{1}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{3}d_{1}-10800\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{3}-21600\,a_{1}{}^{4}c_{1}{}^{3}c_{3}d_{1}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{3}d_{1}-10800\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{3}-21600\,a_{1}{}^{4}c_{1}{}^{3}c_{3}d_{1}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{1}{}^{4}d_{1}d_{3}-21600\,a_{1}{}^{4}c_{1}{}^{3}c_{3}d_{1}{}^{2}+10800\,a_{1}{}^{4}c_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}{}^{4}d_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}d_{2}-21600\,a_{1}{}^{4}c_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_{1}d_{2}-21600\,a_$ $21600\,a_{1}{}^{4}c_{1}{}^{3}d_{1}{}^{2}d_{3}+21600\,a_{1}{}^{4}c_{1}{}^{2}c_{3}d_{1}{}^{3}-21600\,a_{1}{}^{4}c_{1}{}^{2}d_{1}{}^{3}d_{3}-10800\,a_{1}{}^{4}c_{1}c_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}d_{1}{}^{4}d_{3}-21600\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{2}d_{1}a_{3}-21600\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{3}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+10800\,a_{1}{}^{4}c_{1}a_{2}d_{1}{}^{4}+1080\,a_{1}{}^{4}+1080\,a_{1}a_{2}d_{1}{}^{4}+1080\,a_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_{2}d_{1}a_$ $32400\,{a_{1}}^{3}a_{3}{c_{1}}^{4}{d_{1}}^{2} - 43200\,{a_{1}}^{3}a_{3}{c_{1}}^{3}{d_{1}}^{3} + 32400\,{a_{1}}^{3}a_{3}{c_{1}}^{2}{d_{1}}^{4} - {12960\,{a_{1}}^{3}}a_{3}{c_{1}}{d_{1}}^{5} + {6480\,{a_{1}}^{2}}a_{2}{}^{2}{c_{1}}^{5}d_{1} - {12960\,{a_{1}}^{3}}a_{3}{c_{1}}d_{1}^{5} + {6480\,{a_{1}}^{2}}a_{2}{}^{2}{c_{1}}^{5}d_{1} - {12960\,{a_{1}}^{3}}a_{3}{c_{1}}d_{1}^{5} + {6480\,{a_{1}}^{2}}a_{2}{}^{2}{c_{1}}^{5}d_{1} - {12960\,{a_{1}}^{3}}a_{3}{c_{1}}d_{1}^{5} + {6480\,{a_{1}}^{2}}a_{2}{}^{2}{c_{1}}^{5}d_{1} - {12960\,{a_{1}}^{3}}a_{3}{}^{2}{c_{1}}d_{1}^{5} + {6480\,{a_{1}}^{2}}a_{2}{}^{2}{c_{1}}^{5}d_{1} - {12960\,{a_{1}}^{3}}a_{3}{}^{2}{c_{1}}d_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{3}d_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{3}}a_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{3}d_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{3}d_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{3}d_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{3}d_{1}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{5} + {12960\,{a_{1}}^{3}}a_{1}{}^{$ $16200\,{a_{1}}^{2}{a_{2}}^{2}{c_{1}}^{4}{d_{1}}^{2} + 5400\,{a_{1}}^{4}{c_{1}}^{4}{c_{2}}^{2} + 5400\,{a_{1}}^{4}{d_{2}}^{2} + 5400\,{a_{1}}^{4}{c_{2}}^{2}{d_{1}}^{4} + 5400\,{a_{1}}^{4}{d_{1}}^{4}{d_{2}}^{2} - 5400\,{a_{1}}^{4}{d_{2}}^{2} + 5400\,{a_$ $172800 a_1^4 c_3 d_3 + 777600 a_1^2 a_2^2 c_2^2 + 777600 a_1^2 a_2^2 d_2^2 + 86400 a_1^2 a_3^2 c_1^2 + 86400 a_1^2 a_3^2 d_1^2 - 26400 a_1^2 a_2^2 a_2^2 + 86400 a_1^2 a_2^2 + 86400 a_1^2$ $1555200\,{a_{2}}^{4}{c_{1}}{d_{1}} + 45\,{a_{1}}^{4}{c_{1}}^{8}{d_{1}}^{2} - 120\,{a_{1}}^{4}{c_{1}}^{7}{d_{1}}^{3} + 210\,{a_{1}}^{4}{c_{1}}^{6}{d_{1}}^{4} - 252\,{a_{1}}^{4}{c_{1}}^{5}{d_{1}}^{5} + 210\,{a_{1}}^{4}{c_{1}}^{4}{d_{1}}^{6} - 252\,{a_{1}}^{4}{c_{1}}^{5}{d_{1}}^{5} + 210\,{a_{1}}^{4}{c_{1}}^{6}{d_{1}}^{6} - 252\,{a_{1}}^{6}{c_{1}}{d_{1}}^{5} + 210\,{a_{1}}^{6}{c_{1}}^{6}{d_{1}}^{6} + 210\,{a_{1}}^{6}{c_{1}}^{6}{d_{1}}^{6} - 210\,{a_{1}}^{6}{d_{1}}^{6}{d_{1}}^{6} - 210\,{a_{1}}^{6}{d_{1}}^{6}{d_{1}}^{6} - 210\,{a_{1}}^{6}{d_{1}}^{6}{d_{1}}^{6} - 210\,{a_{1}}^{6}{d_{1}}^{6}{d_{1}}^{6} + 210\,{a_{1}}^{$ $120\,a_{1}^{\ 4}c_{1}^{\ 3}d_{1}^{\ 7} + 45\,a_{1}^{\ 4}c_{1}^{\ 2}d_{1}^{\ 8} - 10\,a_{1}^{\ 4}c_{1}d_{1}^{\ 9} - 2160\,a_{1}^{\ 4}c_{1}^{\ 5}c_{3} + 2160\,a_{1}^{\ 4}c_{1}^{\ 5}d_{3} + 2160\,a_{1}^{\ 4}c_{3}d_{1}^{\ 5} - 2160\,a_{1}^{\ 4}c_{1}^{\ 5}d_{3} + 2160\,a_{1}^{\ 4}c_{3}d_{1}^{\ 5} - 2160\,a_{1}^{\ 6}c_{1}^{\ 6}c_{1}^{\ 6} - 2160\,a_{1}^{\ 6}c_{1}^{\ 6} - 2160\,a_{1}^{\ 6}c_{1}^{\ 6} - 2160\,a_{1}^{\ 6}c_{1}^{\ 6} - 2160\,a_{1}^{\ 6} - 2160\,a_{1}^{\ 6}c_{1}^{\ 6} - 2160\,a_{1}^{\ 6}c_{1}^{\ 6} - 2160\,a_{1}^{\ 6} - 2160\,a_{1}^{\$ $2160\,{a_{1}}^{4}{d_{1}}^{5}{d_{3}} + 2160\,{a_{1}}^{3}{a_{3}}{c_{1}}^{6} + 2160\,{a_{1}}^{3}{a_{3}}{d_{1}}^{6} - 1080\,{a_{1}}^{2}{a_{2}}^{2}{c_{1}}^{6} - 1080\,{a_{1}}^{2}{a_{2}}^{2}{d_{1}}^{6} - 43200\,{a_{1}}^{4}{c_{1}}{c_{2}}^{3} + 2160\,{a_{1}}^{3}{a_{3}}{d_{1}}^{6} - 1080\,{a_{1}}^{2}{a_{2}}^{2}{c_{1}}^{6} - 1080\,{a_{1}}^{2}{a_{2}}^{2}{d_{1}}^{6} - 43200\,{a_{1}}^{4}{c_{1}}{c_{2}}^{3} + 2160\,{a_{1}}^{3}{a_{3}}{d_{1}}^{6} - 1080\,{a_{1}}^{2}{a_{2}}^{2}{c_{1}}^{6} - 1080\,{a_{1}}^{2}{a_{2}}^{2}{d_{1}}^{6} - 1080\,{a_{1}}^{2}{a_{$ $43200 a_1^{\ 4} c_1 d_2^{\ 3} + 43200 a_1^{\ 4} c_2^{\ 3} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} c_1 - 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 3} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 5} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 5} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 5} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 5} + 345600 t^3 a_1^{\ 13} d_1 - 43200 a_1^{\ 4} d_1 d_2^{\ 5} + 345600 t^3 a_1^{\ 13} d_1 - 4345600 t^3 a_1^{\ 13} d_1 - 434560$ $10\,a_{1}{}^{4}c_{1}{}^{9}d_{1} + 43200\,a_{1}a_{2}{}^{3}c_{1}{}^{4} + 43200\,a_{1}a_{2}{}^{3}d_{1}{}^{4} + 21600\,t^{2}a_{1}{}^{10}c_{1}{}^{4} + 21600\,t^{2}a_{1}{}^{10}d_{1}{}^{4} + a_{1}{}^{4}c_{1}{}^{10} + a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_{1}{}^{4}a_$ $a_1^4 d_1^{10} + 86400 a_1^4 c_3^2 + 86400 a_1^4 d_3^2 + 777600 a_2^4 c_1^2 + 777600 a_2^4 d_1^2),$

 $d(x,t) = -64 a_1^8 x^6 + (192 a_1^7 d_1 - 192 a_1^7 c_1) x^5 + (-240 a_1^6 d_1^2 - 240 a_1^6 c_1^2 + 480 a_1^6 c_1 d_1) x^4 + (-240 a_1^6 d_1^2 - 240 a_1^6 c_1^2 + 480 a_1^6 c_1 d_1) x^4 + (-240 a_1^6 d_1^2 - 240 a_1^6 d_1^2 (-{160}\,{a_{1}}^{5}{c_{1}}^{3}+480\,{a_{1}}^{5}{c_{2}}-480\,{a_{1}}^{5}{d_{2}}+160\,{a_{1}}^{5}{d_{1}}^{3}+480\,{a_{1}}^{5}{c_{1}}^{2}{d_{1}}-960\,t{a_{1}}^{8}+480\,{a_{1}}^{4}{a_{2}}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{6}{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{2}{a_{2}}^{2}{d_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{2}}{d_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}^{2}{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_{1}}-660\,t{a_$ $480\,{a_1}^4{a_2}{c_1} - 480\,{a_1}^5{c_1}{d_1}^2)x^3 + (-1440\,{t_1}^7{c_1} - 60\,{a_1}^4{d_1}^4 - 720\,{a_1}^4{c_1}{d_2} - 60\,{a_1}^4{c_1}^4 + 1440\,{a_1}^3{a_2}{c_1}{d_1} + 140\,{a_2}^3{a_2}{c_1}{d_2} + 140\,{a_2}^3{a_2}{c$ $720\,{a_1}^4{d_1}{d_2} - 720\,{a_1}^4{c_2}{d_1} - 720\,{a_1}^3{a_2}{d_1}^2 + 720\,{a_1}^4{c_1}{c_2} + 240\,{a_1}^4{c_1}{d_1}^3 + 1440\,{t_1}^7{d_1} + 240\,{a_1}^4{c_1}^3{d_1} - 240\,{a_1}^4{c_1}^3{d_1} - 240\,{a_1}^4{c_1}^2{d_1}^2 + 720\,{a_1}^4{c_1}^2{d_1}^2 + 720\,{a_1}^4{c_1}^2{d_1} + 72$ $360\,{a_1}^4{c_1}^2{d_1}^2 - 720\,{a_1}^3{a_2}{c_1}^2)x^2 + (4320\,{a_1}{a_2}^2{d_1} - 1440\,{a_1}^3{c_3} + 1440\,{a_1}^3{d_3} - 720\,{a_1}^6{d_1}^2t - 640\,{a_1}^2{d_1}^2 + 640\,{a_1}^2{d_1}^2 - 720\,{a_1}^2{d_1}^2 + 640\,{a_1}^2{d_1}^2 - 720\,{a_1}^2{d_1}^2 - 720\,{a_1}^2{d_1} - 720\,{a_1}^$ $720\,{a_1}^6{c_1}^2t - 4320\,{a_1}{a_2}^2{c_1} + {12\,{a_1}}^3{d_1}^5 - {12\,{a_1}}^3{c_1}^5 + 360\,{a_2}{a_1}^2{d_1}^3 - 4320\,{a_2}{a_1}^2{d_2} + 4320\,{a_2}{a_1}^2{c_2} - 4320\,{a_2}{a_1}^2{d_2} + 43$ $360\,a_{2}a_{1}{}^{2}c_{1}{}^{3}-360\,a_{1}{}^{3}d_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{2}d_{1}{}^{3}-360\,a_{1}{}^{3}c_{1}{}^{2}d_{2}+360\,a_{1}{}^{3}d_{1}{}^{2}c_{2}-120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}c_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{2}c_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{3}+120\,a_{1}{}^{3}d_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^{3}+120\,a_{1}{}^$ $360\,{a_{1}}^{3}{c_{1}}^{2}{c_{2}} + 1440\,{a_{3}}{a_{1}}^{2}{c_{1}} - 1440\,{a_{3}}{a_{1}}^{2}{d_{1}} - 60\,{a_{1}}^{3}{d_{1}}^{4}{c_{1}} + 60\,{a_{1}}^{3}{c_{1}}^{4}{d_{1}} + 1080\,{a_{1}}^{2}{c_{1}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{1}}^{2}{c_{1}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{1}}^{2}{c_{1}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{1}}^{2}{c_{1}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{1}}^{2}{c_{1}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{1}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{2}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{1}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{2}}^{2}{a_{2}}{d_{1}} + 1080\,{a_{2}}^{2}{a_{2}}{d_{2}}{d_{1}} + 1080\,{a_{2}}^{2}{a_{2}}{d_{2}}{d_{2}} + 1080\,{a_{2}}^{2}{a_{2}}{d_{2}}{d_{2}} + 1080\,{a_{2}}^{2}{a_{2}}{d_{2}}{d_{2}}{d_{2}}{d_{2}} + 1080\,{a_{2}}^{2}{a_{2}}{d_$ $720\,a_{1}^{3}d_{1}d_{2}c_{1} - 720\,a_{1}^{3}c_{1}c_{2}d_{1} + 1440\,ta_{1}^{6}c_{1}d_{1} - 1080\,a_{1}^{2}d_{1}^{-2}a_{2}c_{1})x + 60\,a_{1}^{-2}d_{1}^{-3}d_{2} + 720\,a_{1}a_{3}d_{1}^{-2} + 720\,a_{1}^{-2} + 720\,$ $120 t a_1{}^5 d_1{}^3 + 2880 t^2 a_1{}^8 + 720 a_1 a_2 d_1 d_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1 a_2 d_1{}^4 - 2880 t a_1{}^4 d_1 a_2 + 2880 t a_1{}^4 a_1 a_2 + 2880 t a_1{}^4 a_2 c_1 - 60 a_1{}^4 a_1 a_2 - 60 a_1{}^4 a_2 - 60 a_1{}^4 a_1 a_1 a_1 - 60 a_1{}^4 a_1 a_1 - 60 a_1{}^4 a_1 a_2 - 60 a_1{}^$ $720\,{a_{1}}{a_{3}}{c_{1}}^{2}-{d_{1}}^{6}{a_{1}}^{2}+720\,{a_{1}}{a_{2}}{c_{1}}{c_{2}}-{c_{1}}^{6}{a_{1}}^{2}-15\,{a_{1}}^{2}{c_{1}}^{2}{d_{1}}^{4}-15\,{a_{1}}^{2}{c_{1}}^{4}{d_{1}}^{2}+720\,{d_{3}}{a_{1}}^{2}{c_{1}}+10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-10\,{d_{1}}^{2}-1$ $720 c_3 a_1^{\ 2} d_1 + 6 d_1^{\ 5} a_1^{\ 2} c_1 + 6 c_1^{\ 5} a_1^{\ 2} d_1 - 60 c_2 a_1^{\ 2} d_1^{\ 3} - 1440 c_2 a_1^{\ 2} d_2 + 20 d_1^{\ 3} a_1^{\ 2} c_1^{\ 3} - 60 d_2 a_1^{\ 3} c_$ $2880 \, ta_{1}{}^{5}c_{2} - 720 \, a_{1}{}^{2}c_{1}c_{3} + 60 \, a_{1}{}^{2}c_{1}{}^{3}c_{2} - 120 \, ta_{1}{}^{5}c_{1}{}^{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}{}^{5}d_{2} - 720 \, a_{1}{}^{2}d_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}{}^{4} + 2880 \, ta_{1}a_{2}c_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}d_{3} - 60 \, a_{1}a_{2}c_{1}d_{3$ $1440\,{a_{2}}^{2}{d_{1}}^{2} + 720\,{a_{1}}^{2}{c_{2}}^{2} + 720\,{a_{1}}^{2}{d_{2}}^{2} + 2880\,{d_{1}}{a_{2}}^{2}{c_{1}} + 180\,{d_{1}}{a_{1}}^{2}{c_{1}}^{2}{d_{2}} - 1440\,{d_{1}}{a_{3}}{a_{1}}{c_{1}} - 1440\,{d_{1}}{a_{2}}{a_{1}}{c_{1}} - 1440\,{d_{1}}{a_{2}}{a_{1}}{c_{1}} - 1440\,{d_{1}}{a_{2}}{a_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}} - 1440\,{d_{1}}{a_{2}}{a_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_{1}}{c_$ $360\,a_1c_1^{\,\,2}a_2d_1^{\,\,2} + 180\,a_1^{\,\,2}c_1c_2d_1^{\,\,2} - 180\,d_1^{\,\,2}d_2a_1^{\,\,2}c_1 - 180\,c_1^{\,\,2}c_2a_1^{\,\,2}d_1 - 360\,d_1^{\,\,2}ta_1^{\,\,5}c_1 + 360\,c_1^{\,\,2}ta_1^{\,\,5}d_1 - 360\,d_1^{\,\,2}ta_1^{\,\,5}d_1 - 360\,d_1^{\,\,5}d_1 - 360\,d_1^{\,\,5}d$ $720 c_2 a_1 a_2 d_1 + 240 d_1^3 a_1 a_2 c_1 - 720 d_2 a_1 a_2 c_1 + 240 c_1^3 a_1 a_2 d_1 - 1440 a_2^2 c_1^2$

is a rational solution to the KdV equation (1), quotient of two polynomials with the numerator of order 10 in x, 3 in t, the denominator of degree 12 in x, 4 in t.

2.6 Another orders

For greater orders, the solutions become very complex and we cannot give them here. We only give solutions with parameters a_j equal to 1 and all other parameters equal to 0.

 $\mathbf{Order}\ 4$

Proposition 2.4 The function v defined by

$$v(x,t) = -2 \frac{n(x,t)}{d(x,t)^2},$$
(10)

 $n(x,t) = -10 x^{18} - 360 t x^{15} - 14175 t^2 x^{12} + 330750 t^3 x^9 + 5953500 t^4 x^6 - 22325625 t^6,$

 $d(x,t) = x^{10} + 45 \, tx^7 + 4725 \, t^3 x$

is a rational solution to the KdV equation (1), quotient of two polynomials with numerator of degree 18 in x, 6 in t, and denominator of degree 20 in x, 6 in t.

$\mathbf{Order}\ 5$

Proposition 2.5 The function v defined by

$$v(x,t) = -2 \frac{n(x,t)}{d(x,t)^2},$$
(11)

$$\begin{split} n(x,t) &= -15\,x^{28} - 1890\,tx^{25} - 113400\,t^2x^{22} - 84837375\,t^4x^{16} - 7501410000\,t^5x^{13} - 64699661250\,t^6x^{10} - 168781725000\,t^7x^7 - 4430520281250\,t^8x^4 + 8861040562500\,t^9x, \end{split}$$

 $d(x,t) = -x^{15} - 105 tx^{12} - 1575 t^2 x^9 - 33075 t^3 x^6 + 992250 t^4 x^3 + 1488375 t^5$ is a rational solution to the KdV equation (1), quotient of two polynomials with numerator of degree 28 in x, 9 in t, and denominator of degree 30 in x, 10 in t.

$\mathbf{Order}\ 6$

Proposition 2.6 The function v defined by

$$v(x,t) = -2 \frac{n(x,t)}{d(x,t)^2},$$
(12)

$$\begin{split} n(x,t) &= -21\,x^{40} - 6300\,tx^{37} - 793800\,t^2x^{34} - 39690000\,t^3x^{31} - 1909585125\,t^4x^{28} - 43320642750\,t^5x^{25} + \\ 8174661547500\,t^6x^{22} + 376889591925000\,t^7x^{19} + 5541251715759375\,t^8x^{16} + 60042410851500000\,t^9x^{13} - \\ 1339696292124093750\,t^{10}x^{10} + 2026431366238125000\,t^{11}x^7 - 88656372272917968750\,t^{12}x^4 - \\ 106387646727501562500\,t^{13}x, \end{split}$$

 $\begin{array}{l} d(x,t)\,=\,-x^{21}-210\,tx^{18}-10395\,t^2x^{15}-264600\,t^3x^{12}+5457375\,t^4x^9-343814625\,t^5x^6-3438146250\,t^6x^3+5157219375\,t^7 \end{array}$

is a rational solution to the KdV equation (1), quotient of two polynomials with numerator of degree 40 in x, 13 in t, and denominator of degree 42 in x, 14 in t.

3 Conclusion

We have given three types of representations of solutions to the KdV equation. First, solutions in terms of elementary exponential functions have been constructed. In particular, performing a passage to the limit when one parameter goes to 0 we get rational solutions to the KdV equation. We give another representation in terms of determinants without the presence of a limit. So we obtain an infinite hierarchy of multi-parametric families of rational solutions to the KdV equation as a quotient of a polynomials depending on 3N real parameters.

We can formulate some remarks about the structure of these solutions. For the N-order solution, the numerator of the solution is a polynomial of degree N(N = 1) - 2 in x and the denominator a polynomial of degree N(N + 1) in x. The structure relative to t seems more complicated. It would be relevant to study these polynomials in more details.

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