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Stéphane Bertin, Heide Friedrich, Patrice Delmas, Edwin Chan, Georgy Gimel'farb

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1 **Digital Stereo Photogrammetry for Grain-Scale**
2 **Monitoring of Fluvial Surfaces: Error Evaluation**
3 **and Workflow Optimisation**

4 By Stephane BERTIN (sber081@aucklanduni.ac.nz), Heide FRIEDRICH
5 (h.friedrich@auckland.ac.nz),
6 *Department of Civil and Environmental Engineering*
7 *The University of Auckland*

8 Patrice DELMAS (p.delmas@auckland.ac.nz), Edwin CHAN (ycha171@aucklanduni.ac.nz)
9 and Georgy GIMEL'FARB (g.gimelfarb@auckland.ac.nz)
10 *Department of Computer Science*
11 *The University of Auckland*

12 **Abstract**

13 Grain-scale monitoring of fluvial morphology is important for the evaluation of river system
14 dynamics. Significant progress in Remote Sensing and computer performance allows rapid
15 high-resolution data acquisition, however, applications in fluvial environments remain
16 challenging. Even in a controlled environment, such as a laboratory, the extensive acquisition
17 workflow is prone to the propagation of errors in digital elevation models (DEMs). This is
18 valid for both of the common surface recording techniques: digital stereo photogrammetry
19 and terrestrial laser scanning (TLS). The optimisation of the acquisition process, an effective
20 way to reduce the occurrence of errors, is generally limited by the use of commercial
21 software. Therefore, the removal of evident blunders during post processing is regarded as
22 standard practice, although this may introduce new errors. This paper presents a detailed
23 evaluation of a digital stereo-photogrammetric workflow developed for fluvial hydraulic
24 applications. The introduced workflow is user-friendly and can be adapted to various close-
25 range measurements: imagery is acquired with two Nikon D5100 cameras and processed
26 using non-proprietary "on-the-job" calibration and dense scanline-based stereo matching
27 algorithms. Novel ground truth evaluation studies were designed to identify the DEM errors,
28 which resulted from a combination of calibration errors, inaccurate image rectifications and
29 stereo-matching errors. To ensure optimum DEM quality, we show that systematic DEM

30 errors must be minimised by ensuring a good distribution of control points throughout the
31 image format during calibration. DEM quality is then largely dependent on the imagery
32 utilised. We evaluated the open access multi-scale Retinex algorithm to facilitate the stereo
33 matching, and quantified its influence on DEM quality. Occlusions, inherent to any
34 roughness element, are still a major limiting factor to DEM accuracy. We show that a careful
35 selection of the camera-to-object and baseline distance reduces errors in occluded areas and
36 that realistic ground truths help to quantify those errors.

37 **Keywords:** Photogrammetry; digital; application; DEM/DTM; close range; high resolution;
38 performance; accuracy

39 **1. Introduction**

40 1.1. Fluvial Morphology Remote Sensing

41 In situ characterisation of grain-scale fluvial morphology is challenging for hydraulic
42 engineers and fluvial geomorphologists. In a riverine environment, the interactions between
43 the sediment surface (characterised by the grain size distribution, the particle shapes and the
44 arrangement of the particles) and the water flow significantly control the riverbed. Hence, an
45 understanding of the river system dynamics, and associated habitats, relies on the ability to
46 accurately describe the riverbed morphology.

47 Using 2.5D digital elevation models (DEMs) is increasingly becoming more common to
48 represent the grain-scale surface morphology for gravel-bed rivers. This is enabled by the
49 advent of new measurement techniques and improved PC performances. DEM analysis
50 reveals the flow history (Mao et al., 2011, Ockelford and Haynes, 2013) and allows the
51 parameterisation of the surface roughness for flow resistance equations (Smart et al., 2002,
52 Aberle and Smart, 2003, Smith et al., 2011, Qin and Ng, 2012). DEMs are also essential for
53 detailed computational fluid dynamics (CFD) simulations (Lane et al., 2002, Hardy, 2008,
54 Hardy et al., 2009). In future, field collection of DEMs will help improve flood modelling by
55 reducing the need to calibrate the surface roughness, a key parameter in flow simulations
56 over rough surfaces.

57 Whilst both digital stereo photogrammetry and terrestrial laser scanning (TLS) support
58 high-resolution data acquisition, measurement errors, which can affect data reliability and
59 subsequent findings (Lane et al., 2005, Hodge et al., 2009), remain a major issue. For this
60 reason, the majority of previously surveyed close-range fluvial environments are exposed

61 riverbeds in a controlled environment, such as the laboratory. At present, it is thus important
62 to identify, quantify and reduce measurement error sources to improve the quality of grain-
63 scale DEMs and allow using the techniques in more sophisticated experiments in future. For
64 TLS applications, previous users scanned fluvial surfaces repeatedly to average out the errors
65 (Hodge et al., 2009, Smith et al., 2012). However, there is still the need of significant post-
66 processing in the form of filtering to obtain accurate metrics from exposed gravel beds in the
67 field. Practical applications have shown that data post-processing should be avoided as it can
68 introduce other errors (Hodge et al., 2009).

69 The most viable approach to minimise measurement errors is the optimisation of the data
70 collection process. Workflow optimisation is of particular concern to stereo-photogrammetric
71 users, as the DEM collection workflow is long, complex, and the source of various error
72 types (Lane et al., 2000, Carbonneau et al., 2003, Bouratsis et al., 2013). However, improving
73 data collection is generally limited by the use of commercial photogrammetric software.

74 To put the introduced workflow in context, we provide a review of previous hydraulic
75 stereo-photogrammetric applications in the next Section. Attention is focused on the DEM
76 collection workflow, the error sources and the solutions previously adopted.

77 1.2. Stereo Photogrammetry for Hydraulic Experiments

78 Stereo photogrammetry of fluvial environments covers a wide range of scales. DEM
79 scales vary from several kilometres for the study of large braided rivers (Westaway et al.,
80 2003), to several metres for mountainous streams (Bird et al., 2010) and to a mere metre for
81 gravel-bed roughness characterisation (Butler et al., 2001, Bertin and Friedrich, 2014). The
82 variety of stereo-photogrammetric applications is also reflected in the hardware and
83 software/workflow selection for DEM reconstruction.

84 The advent of high-resolution digital cameras has led to the replacement of metric film
85 cameras, allowing low-cost and versatile surveys (Chandler et al., 2001, Lane et al., 2001).

86 Metric film cameras are provided with a calibration certificate that includes the parameters of
87 the interior orientation (also called intrinsic parameters), although regular re-calibrations are
88 recommended to ensure optimal accuracy (Cooper and Robson, 2001). Off-the-shelf digital
89 cameras, as used in our experiments, require detailed calibration (see Section 3.4), if accurate
90 metrics are to be extracted from imagery. In contrast, automatic stereo matching is now
91 easier, which ensures an efficient DEM collection process and high data resolution. However,
92 where a human operator previously ensured correct matching, automatic stereo matching now

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95 relies on image quality, and a lack thereof can result in additional errors (Lane, 2000). Very
96 recently, multi-view stereo (MVS) and structure-from-motion (SfM) photogrammetry started
97 to be implemented in medium to large scale experiments (Westoby et al., 2012, Javernick et
98 al., 2014). Even though these novel methods have the potential to better capture occlusions,
99 they are not discussed here, as the workflow departs substantially from the more conventional
100 binocular stereo (also called two-view) photogrammetry.

101 To date, most environmental and fluvial applications of stereo photogrammetry have
102 relied on proprietary stereo-photogrammetric products. OrthoMAX module of Erdas
103 Imagine® (later Leica photogrammetry suite, LPS, now IMAGINE Photogrammetry) is the
104 most used commercial software, with AICON 3D Systems® a more recent product
105 (Schmocker, 2011). [Other commercial software, such as Trimble Inpho®, Intergraph
106 ImageStation® and BAE Systems SOCET SET®, enable DEM reconstruction from stereo
107 images, and have been tested for civil engineering and geomorphic purposes](#) (González-Díez
108 et al., 2014, Murillo-García et al., 2014, Stoter et al., 2015). As noted by Chandler et al.
109 (2001), the use of proprietary software constrains the photogrammetric design. OrthoMAX
110 requires conventional photogrammetric control targets to be placed in the region of interest.
111 The control targets' 3D coordinates are recorded separately, using an independent device, and
112 registered within the stereo model by bundle adjustment. This was shown to be a potential
113 source of errors (Carbonneau et al., 2003). The tangential distortion is ignored in OrthoMAX
114 for the calibration, which may be tolerable for high quality lenses and medium accuracy work
115 (Fraser, 1997, Chandler et al., 2001). Furthermore, OrthoMAX's DEM reconstruction
116 algorithm is limited, with substantial surface smoothing and poor results over rough surfaces
117 and in occlusions (Chandler et al., 2001, Carbonneau et al., 2003), as it relies on area-based
118 stereo matching. Substantial post-processing is needed when using those proprietary stereo-
119 photogrammetric products for fluvial roughness studies (Carbonneau et al., 2003).

120 Attempts to optimise the DEM reconstruction process in OrthoMAX were first made by
121 varying the DEM collection parameters, such as the minimum threshold of normalised cross-
122 correlation and the template size for area-based stereo matching (Butler et al., 1998, Gooch et
123 al., 1999). Butler et al. (1998, 2002) also changed the camera settings to obtain optimal
124 exposures with maximum contrast; however, the image quality effect on stereo matching was
125 not evaluated. As outlined by Aber et al. (2010), low image noise is expected to increase the
126 DEM accuracy, which has been tested in specific application areas, such as
127 stereomicroscopy. In Chandler et al. (2001), two different methods to obtain the calibration
128 parameters were tried: (i) an in situ self-calibration with GAP software and (ii) an "on-the-

129 job” calibration with a 3D test field consisting of 70 retro-reflective targets, both resulting in
130 similar DEM accuracy. Chandler et al. (2001) concluded that self-calibration is perhaps the
131 preferable method, since it only requires the measurement of imagery used for the DEM
132 extraction. However, the number and [spatial arrangement](#) of calibration control targets was
133 found critical, with a need to have numerous (minimum of 15) and well-surveyed control
134 targets evenly distributed throughout the x, y and z volume of the study site, which enables
135 the recovery of reliable lens parameters (Chandler et al., 2001, Carbonneau et al., 2003).

136 More recently, stereo-photogrammetric solutions using non-proprietary algorithms are
137 implemented in hydraulic experiments (e.g. Bouratsis et al. (2013) for the laboratory study of
138 bridge pier scouring). The calibration parameters (including the tangential distortion) were
139 obtained by using the freely accessible camera calibration toolbox for MATLAB® developed
140 by Bouguet (2010). The stereo matching was performed on rectified images with a self-
141 programmed correlation-based algorithm, using a window size of 35 x 35 pixels. Although a
142 smooth surface was investigated, three geometrical filters were needed to process the data
143 and remove blunders in a satisfactory manner. DEM errors were associated with the
144 inadequate stereo setup design (baseline and the flying-height of cameras), which did result in
145 substantial oclusions and thus stereo matching errors. Bouratsis et al. (2013) stressed the
146 importance of image quality for stereo matching and suggested a structured light approach
147 (whereby patterns are projected on the surface) to improve on the initially poor stereo
148 matching results based on the riverbed texture only.

149 1.3. Paper Overview

150 This paper presents in detail a non-proprietary stereo-photogrammetric workflow
151 developed for the grain-scale measurement of fluvial surfaces. The workflow is described and
152 evaluated. Imagery acquired with two consumer-grade DSLRs and processed with non-
153 proprietary algorithms form the basis of the DEM reconstruction. Details of the “on-the-job”
154 MATLAB® calibration toolbox are presented and discussed. Dense scanline-based stereo
155 matching is implemented and it is shown that it improves on the traditional area-based
156 methods in terms of resolution and occlusion suitability. The presented stereo-
157 photogrammetric technique was successfully applied to monitor the morphological changes
158 of water-worked gravel beds, both in air and through-water (Bertin et al., 2013), with sub-
159 millimetre sampling distances and vertical accuracies.

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161 In this study, DEM errors resulting from a combination of calibration errors, inaccurate
162 image rectifications and stereo-mismatches are identified by purposely-designed tests. A
163 framework to evaluate the calibration and the image rectification accuracy is presented.
164 Relevant objects of known geometry, ground truths, were designed, produced and tested for
165 the quantitative DEM quality assessment, enabling the identification of the error propagation.
166 For this paper, we concentrate on presenting the evaluation of the technique for in-air
167 measurement, with the presented concepts being valid also for through-water measurements.

168 This evaluation study will be useful to other researchers using non-proprietary digital
169 stereo photogrammetry and optimisation for their projects, and for the development of
170 camera calibration and image matching techniques.

171 **2. Measurement Environment and Instrumentation**

172 The workflow is designed for experiments in a hydraulic flume (Bertin and Friedrich,
173 2014). The flume in use is 19 m long, 0.45 m wide and 0.5 m deep, with a slope of 0.5%. For
174 hydraulic experiments, a gravel bed is prepared over a one metre long full-width sediment
175 recess (called the “test section”), located 14 m downstream from the inlet (Figure 1). During
176 the experiments, the sediment is water-worked, and the evolving topography is recorded
177 either through-water, or in air after the flume is drained. The data used for this paper are from
178 in-air tests.

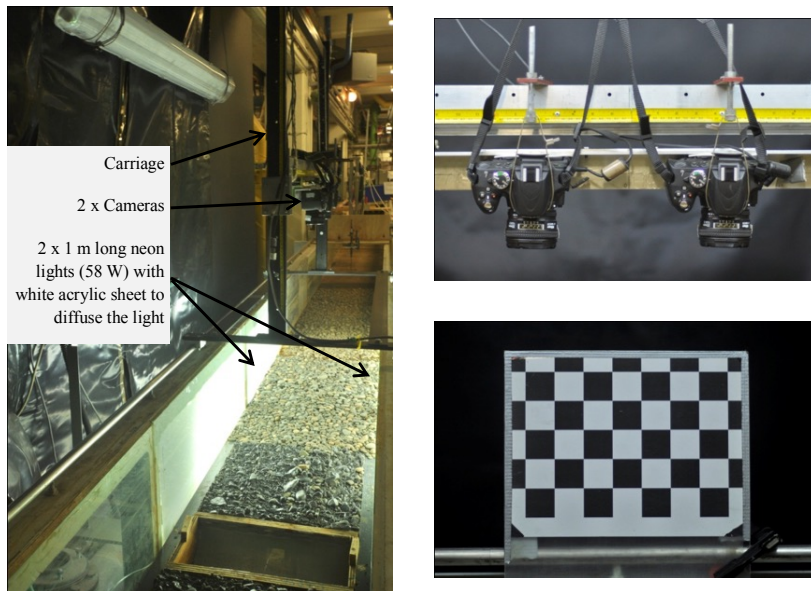
179 Two Nikon D5100 cameras with 16.2 Mpixel complementary metal oxide semiconductor
180 (CMOS) sensors (4928 x 3264 pixels) and Nikkor 20 mm fixed-focus lenses are used for
181 stereo-photogrammetric measurements. The cameras are rigidly attached above the test
182 section, using a gantry-mounting system sliding on a rail (Figure 1). Baseline and height can
183 be adjusted depending on the design needs. Even lighting conditions are ensured (Bertin et
184 al., 2014). An Alienware laptop with Intel core CPU @ 2.20GHz, 8GB memory and
185 MATLAB® 2013b allows on-the-spot processing.

186 **3. DEM Reconstruction Workflow with Stereo Photogrammetry**

187 **3.1. Stereo-photogrammetric Design**

188 The stereo-photogrammetric design is the first step in a stereo-photogrammetric project.
189 It defines the theoretical accuracy achievable by the setup, and is thus critical to the
190 measuring performance (Lane et al., 2001). In this step, the camera placement is optimised

191 for the application. Three parameters are adjusted: (i) the baseline between the two cameras,
192 (ii) the orientation of the cameras, and (iii) the distance between the cameras and the gravel-
193 bed. Additionally, a margin can be accounted for around the measurement window and
194 removed from the DEM during analysis, as it is well known that DEM errors increase near
195 the edges (Butler et al., 2002, Bertin et al., 2014). Compromises often have to be made when
196 finalising the stereo-photogrammetric design. For example, increasing the baseline for a fixed
197 flying height improves the theoretical depth resolution, but also increases the risk of
198 occlusions. Similarly, increasing the flying height to account for a margin reduces the
199 theoretical resolution.



200 **Figure 1.** Hydraulic flume with stereo photogrammetry installed for gravel-bed monitoring
201 (main). The inserts on the right show how cameras are mounted onto the bar using cordons to secure
202 the camera position (top), and the chequerboard with alternating black and white 30 mm squares
203 used for the calibration and the evaluation of image rectification (bottom).

204 To simplify image rectification and uniformly account for partial occlusions by gravel
205 particles protruding and shadowing the surroundings, the camera pair in our experiments is
206 mounted in canonical configuration, where the two optical axes are parallel with each other
207 and perpendicular to the baseline (Figure 1). The standard central perspective projection

208 equations (pin-hole camera model) are used to determine the optimal flying height for the
 209 targeted measurement window size. Experimental heuristics are used to determine the
 210 optimal baseline. Not knowing the exact morphology of the studied area, such as encountered
 211 when recording a gravel bed, it is not possible to design the baseline in the same way as if
 212 one would know the occlusion structure.

213 The setup evaluated in this study was designed for a measurement window of size 450 x
 214 450 mm, which is suited to study gravel-bed roughness (Mao et al., 2011, Ockelford and
 215 Haynes, 2013, Bertin and Friedrich, 2014). No margin was accounted for in this evaluation
 216 study, to enable the identification of the spatial distribution of stereo-photogrammetric errors.
 217 The baseline was set experimentally to 200 mm, requiring a distance between the cameras
 218 and the gravel-bed of 575 mm to cover the measurement window. The resulting common
 219 field of view (CFoV) between the two cameras, where 3D information can be extracted, is
 220 478 x 450 mm in the object space, which results in a theoretical sampling distance of
 221 approximately 0.14 mm, which equals 1 pixel in the image domain. A theoretical depth
 222 resolution (distance between two disparity layers) of 0.39 mm can be achieved (Table I).

223 **TABLE I.** Summary of the stereo-photogrammetric setup used (desired measurement window of size
 224 450 x 450 mm). Computed values were determined using the pin-hole camera model and the rounded
 225 flying height.

Rounded flying height (mm)	575
Baseline (mm)	200
CFoV (mm)	478 x 450
Range of disparity for 50 mm elevation range (pixels)	[1396-1523]
Overlap (%)	70
Pixel size (mm) / resolution (pixel/mm ²)	0.14 / 53
Sampling distance in DEM (mm)	0.25
Theoretical depth resolution or minimum measurable depth (mm)	0.39
Number of pixels in the 450 x 450 mm measurement window (-)	≈ 10,300,000

226 3.2. Setup Preparation

227 The cameras are connected to a computer, allowing remote control and live view using
 228 Nikon's Camera Control Pro 2 software, which is helpful to manually focus on the measured
 229 surface and to mechanically align the cameras. The latter is important to minimise the effect
 230 of image warping during image rectification to epipolar geometry. Easily identifiable feature
 231 points (e.g. chequerboard corners) are used to adjust the alignment until the corresponding

232 points are approximately on the same scanline. Once cameras are correctly focused and
233 mechanically aligned, it is necessary to ensure no modification is made to the physical setup
234 for the duration of the experiment.

235 3.3. Image Acquisition

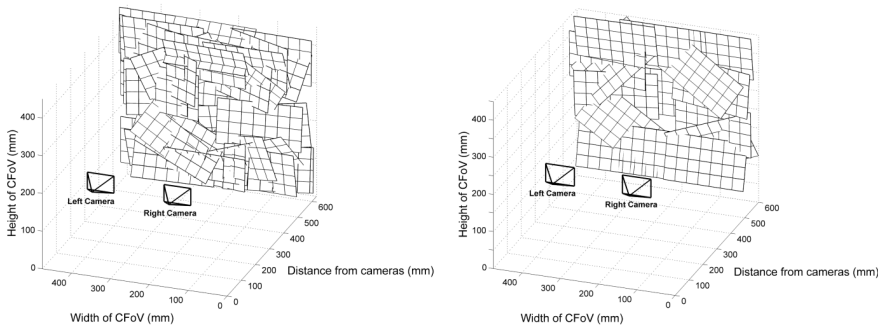
236 Adequate selection of the camera settings for the application is important, as the crucial
237 element to a successful close-range stereo-photogrammetric process is attaining “good
238 images” (Matthews, 2008), where the term “good” refers to sharp images that have uniform
239 exposure with high contrast. Since the lighting environment constrains the cameras’ settings,
240 it is important that both the lighting environment and the exposure settings are optimised
241 interdependently. To obtain the best quality images, the cameras are operated in manual
242 mode. We found that for our environment, using Nikkor 20 mm lenses, a combination of $f/8$
243 aperture (increased to $f/10$ or $f/11$ for selected tests) with a generic sensitivity value such as
244 ISO 200, ensures a good depth of field, a reduced vignette effect and uniform sharpness
245 across the image. Once the aperture and ISO are set, these settings should remain constant
246 throughout the acquisition of all images. For evaluation purposes we changed the shutter
247 speed, as presented later.

248 3.4. Calibration and Image Rectification

249 The calibration method of Zhang (1999), implemented in the calibration toolbox for
250 MATLAB® (Bouguet, 2010), is used to compute the camera calibration and pose parameters
251 (also called intrinsic and extrinsic parameters, respectively) from a series of stereo images
252 (called the “calibration images”) of a planar chequerboard in different orientations (Figure 2).
253 Radial distortion (up to the fourth-order) and tangential distortion are also modelled during
254 calibration for each camera. For simplicity, “calibration parameters” hereafter refer to the
255 ensemble of the camera calibration parameters, the pose parameters and the distortion
256 coefficients. The chequerboard used in this study consists in alternating black and white 30
257 mm squares, prepared on a flat and rigid perspex plate (Figure 1), providing 40 (8 x 5)
258 control points (i.e. the chequerboard corners) per calibration image. A sufficiently accurate
259 checkerboard can be produced from off-the-shelf printers and other materials (Zhang, 1999).

260 Assuming a standard central perspective projection by the cameras, the calibration
261 toolbox extracts the chequerboard’s corners, with distances between corners precisely known,
262 to compute a closed form solution for the calibration parameters and provide separately the

263 intrinsic and the extrinsic parameters of each camera, not including any lens distortion. [The](#)
264 [closed-form estimation of intrinsic parameters explicitly uses a constraint based on the](#)
265 [orthogonality of vanishing points](#) (Bouguet, 2010). Lens distortion is accounted for during the
266 non-linear optimisation step, which minimises the total re-projection error (in the least
267 squares sense) over all other calibration parameters, [and solved with the Levenberg-](#)
268 [Marquardt algorithm](#). The re-projection error (residuals between image measurements) is the
269 difference in (x,y) pixel coordinates between the re-projected corners of the chequerboard,
270 using the calibration results, and their measured locations with sub-pixel accurate corner
271 detection. (x,y) represent the horizontal and vertical directions in an image, respectively.



272 **Figure 2.** Independent sets of (left) 40 “calibration images”, the “parent” set in this research; and
273 (right) 15 “rectification-check” images. The chequerboard corners are alternatively used as control
274 points in calibration images, and as check points for image rectification in rectification-check images.

275 A common procedure to refine the calibration data for each camera separately is to re-
276 compute the chequerboard corners until a minimum re-projection error is attained (Bouguet,
277 2010, Bouratsis et al., 2013). This can be done manually for images where corner detection is
278 initially poor, or automatically on all images. For the automatic re-computation, used
279 thereafter, the toolbox re-computes the positions of every corner by using the re-projected
280 grid as the initial guess locations for the corners.

281 Ultimately, during the stereo calibration step, all calibration parameters are re-evaluated
282 based on the calibration image presenting the minimum re-projection error on both cameras
283 to provide a single set of extrinsic parameters for the stereo setup (Bradley and Heidrich,
284 2010).

285 Once the calibration parameters are known, all stereo images obtained with the setup in
286 the calibrated configuration can be rectified to epipolar geometry to minimise y-parallax in

287 the rectified images. This way, the 2D search of corresponding pixels is reduced to 1D, which
288 assists stereo matching efficiency. Image rectification (Fusiello et al., 2000) is included in the
289 calibration toolbox. It should be noted that the toolbox transforms images to greyscale
290 equivalents during rectification. The code is herewith modified to obtain rectified images in
291 red/green/blue (RGB) format.

292 3.5. Stereo Matching and DEM Reconstruction

293 Stereo matching is performed on rectified images using the conventional and well-
294 established computer stereovision algorithm called symmetric dynamic programming stereo
295 (SDPS) (Gimel'farb, 2002), providing both dense disparity maps and ortho-images of the
296 region covered by the CFoV. The disparity map is then transformed into the depth map using
297 projective geometry and the calibration parameters (the so-called depth triangulation).

298 For each conjugate pair of epipolar lines across a stereo pair, the SDPS algorithm
299 exhausts all continuous epipolar profiles of a single continuous surface to find the profile
300 minimising the total mismatch between both the lines. Individual mismatches between the
301 corresponding pixels, which represent binocularly visible surface points, are measured by the
302 total absolute or squared difference between the pixel intensities. The pixel intensity is
303 defined as the maximum tonal value between the red, green and blue channels, expressed on
304 an 8-bit (0-255) scale. Individual partial occlusions, such that the surface points are observed
305 only in a single image, are taken into account by a special additive penalty. In other words, if
306 a pixel has no counterpart in the other image because of partial occlusion, the latter is
307 penalised in order to regularise the overall matching score, the depth at this point being
308 computed based on the assumption of a single continuous surface.

309 The total line-to-line mismatch is a linear combination of the total intensity mismatch
310 between the corresponding points and a weighted total occlusion penalty for the binocularly
311 observed and partially occluded surface points along the profile, respectively. Compared with
312 previous stereo-photogrammetric applications in hydraulic experiments (see Section 1.2), the
313 SDPS performs pixel-to-pixel signal matching, rather than a "feature-based" or "area-based"
314 one. Hence, the obtained DEM is dense, contrary to the feature-based matching; the DEM's
315 smoothing will be lesser than in the area-based matching, and the sampling distance can be
316 chosen, if necessary, as small as the pixel size at the object's distance.

317 In application to a gravel surface, the more conventional feature-based stereo matchers
318 cannot produce a dense depth map and also may be inaccurate due to the absence of easily

319 detectable and discriminable visual features. The gravel surfaces are highly textured with
320 relatively small occluded areas at borders, ensuring a sufficiently high accuracy of the dense
321 SDPS matcher. However, the employed line-to-line stereo matching needs the more accurate
322 image rectification, as otherwise true correspondences between the pixels may not be found.

323 Post-processing by median filtering, a common practice in stereo-photogrammetric
324 surveys (Carbonneau et al., 2003), is implemented in the SDPS algorithm and is
325 automatically applied to eliminate blunders in the depth maps. Using the default filter width
326 of 3 pixels and height of 11 pixels, each given pixel elevation is replaced by the median value
327 over a 3 x 11 neighbourhood around the corresponding pixel position in the input image. The
328 filter size is such that it is able to smooth the horizontal streaks of disparity error that may
329 result from scanline-based stereo matching. It should be noted that one can opt for this post-
330 processing filter to be skipped and thus true pixel size resolution depth information can be
331 obtained.

332 In terms of matching accuracy, the SDPS algorithm is able to distinguish disparity layers
333 up to 1 pixel. [Since the disparity at a distance Z from the cameras is equal to \$bf/Zp\$](#) the
334 setup's theoretical depth resolution dz in metric units (also called minimum measurable
335 depth; Table I) [can be expressed](#) using the following formula (only valid in case of canonical
336 configuration):

$$337 \quad dz = \frac{Z^2 p}{bf - Zp} \quad [1]$$

338 where (b , f , p and Z) are the baseline, focal length, pixel size in the sensor plane and camera-
339 to-object distance (in mm), respectively.

340 To reconstruct the DEM, all pixels in a depth map are triangulated using projective
341 geometry and the calibration results. A point cloud, containing the (x,y,z) coordinates of all
342 points in metric units, is obtained. The points in the point cloud are not regularly spaced, as
343 they are assigned to different disparity levels. Using the function 'gridfit' in MATLAB®, the
344 point cloud is finally interpolated (using the default triangle interpolation method) onto
345 regular grids with adjustable sampling distance, and represented as 2.5D DEMs. Previous
346 tests showed that the interpolation scheme to transform a point cloud into a regular DEM has
347 very little impact on the data accuracy and that the selection of the sampling distance is
348 critical (Bertin et al., 2014). DEM quality is best preserved when the raw point cloud is
349 interpolated onto a grid with spacing close to the sampling distance of the point cloud (Hodge
350 et al., 2009, Bertin et al., 2014). In this study, raw point clouds were interpolated onto

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352 orthogonal grids with 0.25 mm sampling distance (Table I). Our available computer
353 performance for subsequent analysis was the limiting factor for choosing this resolution.

354 **4. Errors in Digital Stereo Photogrammetry**

355 **4.1. Identification and Quantification**

356 An overview of error causes is provided in Table II. The paper focuses on errors that
357 arise from the stereo-photogrammetric processing steps, i.e. the calibration, the image
358 rectification and the stereo matching. Table II also summarises the identification methods and
359 the implemented solutions to reduce or even eliminate the errors. The error sources and the
360 identification methods are discussed in detail below.

361 **4.1.1. Calibration Error**

362 The calibration toolbox allows evaluating the quality of the calibration based on the
363 numerical uncertainties of the estimated parameters and the re-projection error for each
364 camera. The numerical uncertainties are approximately three times the standard deviation of
365 the parameters after optimisation and are thus equivalent to the precisions of the parameters
366 from the calibration. The toolbox provides the standard deviation of estimated re-projection
367 error over all calibration images along the x and y directions, for both the left and right
368 cameras (four parameters).

369 **4.1.2. Rectification Error**

370 For image rectification, the essential parameters to consider are the relative translation
371 and rotation between the two cameras, as well as the calibrated principal distances and the
372 positions of the principal points for each camera. Any calibration error on the above
373 parameters will prevent a correct image rectification and will result in residual y-parallax in
374 the rectified images, called rectification error. Although the two steps should be regarded as
375 separate, the removal of image distortion is performed simultaneously with the image
376 rectification.

377 To compute the rectification error, an independent set of calibration images, called the
378 “rectification check” images (Figure 2), is recorded, providing check points (i.e. the
379 chequerboard corners, 40 per images) covering the whole CFoV. Per definition, the
380 rectification error is the absolute difference in vertical (y) pixel coordinates between the
381 measured check points of the left-hand and right-hand rectification-check images after image
382 rectification. For the quantitative evaluation of the calibration quality in this study, the mean

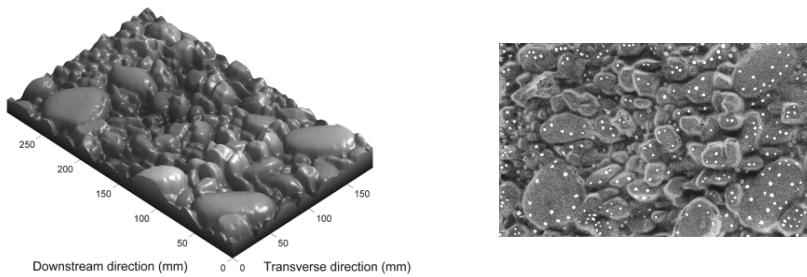
383 (unsigned) rectification error and the maximum (unsigned) rectification error were computed
384 as the average and the maximum of the rectification errors over all check points in all
385 rectification check images (i.e. 600 check points covering the CFoV), respectively. The
386 maximum rectification error at the 99.7 % level was computed as the sum of the mean error
387 and three times the standard deviation of error.

388 **4.1.3. DEM Quality**

389 Ground truths were essential to DEM evaluation to understand the links between
390 calibration, image rectification, stereo matching and thus the resulting DEM error. The latter
391 is evaluated by measuring a ground truth and comparing measured and “truth” elevations on a
392 point-by-point basis, after mutual alignment. The mean unsigned error (MUE), the standard
393 deviation of error (SDE), and the maximum unsigned error were used for the evaluation in
394 this study. At several occasions, the maximum error at the 99.7 % level was computed as the
395 sum of the MUE and three times the SDE.

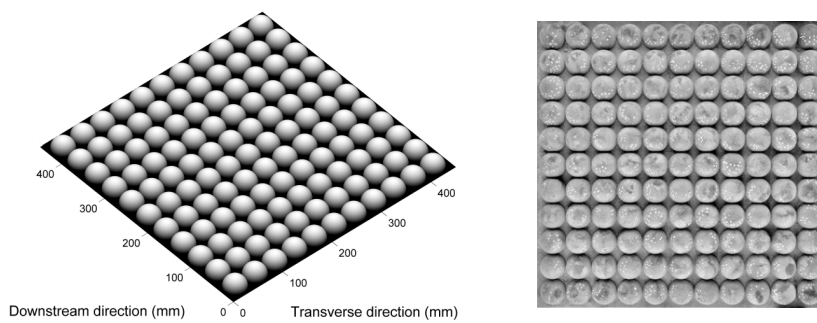
396 Two different ground truths were used (Figures 3 and 4). Both of them lacked initially
397 the texture and contrast of a real gravel-bed (Bertin et al., 2014). To compensate for this, the
398 ground truth surfaces were finished with a light layer of paint, and the addition of differently
399 coloured fine sand (diameter less than 0.2 mm, which is smaller than the 0.39 mm theoretical
400 depth resolution achievable by the setup). For the assessment of the measured DEMs,
401 manufacturing imprecisions and the effect of the surface finishing were neglected.

402 The first ground truth, hereafter referred to as the “gravel-bed model”, was prepared with
403 a 3D printer based on the DEM of a water-worked gravel bed as measured during a previous
404 experiment. The ground truth elevations are produced with the manufacturer’s specified
405 accuracy range of 0.033 to 0.066 mm every 0.25 mm in both directions over a surface of size
406 296 x 184 mm (Figure 3). The preparation of the realistic ground truth and the method to
407 automatically align measured and “truth” data before elevation differences can be computed
408 on a point-by-point basis at more than 800,000 known locations is described in Bertin et al.
409 (2014).



410 **Figure 3.** “Truth” DEM of the gravel-bed model (left); greyscale ortho-image of the model after the
 411 surface was finished to maximise the stereo matching performance (right). Elevations are known at
 412 every 0.25 mm over 296 x 184 mm. DEM quality is evaluated by measuring the ground truth and
 413 comparing measured and “truth” elevations, after mutual alignment, at over 800,000 locations.

414 A second ground truth, called the “hemisphere model” (Figure 4), the same size as our
 415 measurement window (450 x 450 mm), was prepared to evaluate the full spatial distribution
 416 of DEM errors. A digital model was prepared with MATLAB®, taking the form of a “truth”
 417 DEM, with elevations known at every 0.25 mm (Figure 4). To produce the actual model, an
 418 aluminium sheet (450 x 450 mm) was machined with a DOOSAN DNM 650 milling
 419 machine, 30 mm thick and perfectly flat. 121 adjoining cylinders (40 mm in diameter, 20 mm
 420 deep) were drilled onto the plate to allow ping pong balls (40 mm diameter) to be fitted half-
 421 way through. When reversed and laid down on a surface plate (flatness guaranteed with
 422 accuracy of 250 nm), no rocking due to uneven ping pong balls’ protrusions was observed,
 423 satisfying the criteria of a precise ground truth.



424 **Figure 4.** “Truth” DEM of the hemisphere model (left); greyscale ortho-image of the model after the
 425 surface was finished to maximise the stereo matching performance (right). Elevations are known at

426 *every 0.25 mm over 450 x 450 mm. DEM quality is evaluated by measuring the ground truth and*
427 *comparing measured and “truth” elevations, after mutual alignment, at over 3,200,000 locations.*

428 **4.1.4. Dome Effect**

429 The presence of systematic errors in DEMs obtained with stereo photogrammetry, taking
430 the form of a cubic surface centred on the photo base, called a dome, was noticed in previous
431 studies and explained by the incorrect removal of the radial distortion (Chandler et al., 2005,
432 Wackrow and Chandler, 2011). To detect the presence of domes in our data, a flat surface
433 (450 x 450 mm, 250 nm specified flatness) is measured with the setup. After alignment of the
434 obtained DEM with the photo base, the dome effect is estimated by fitting a bi-quadratic
435 surface to the detrended DEM by least-squares.

436 **TABLE II.** A summary of the causes of stereo-photogrammetric errors evaluated in the paper, the identification methods and the solutions adopted.

Causes	Description	Identification and quantification	Mitigation / *removal
Inaccurate calibration (IP/EP/distortion)	Conjugate points are not a same scan line after image rectification (rectification error or y-parallax), which may result in systematic matching errors	Compute rectification error Ground truth measurement	Optimise calibration strategy (number spatial arrangement of control points) Apply a margin during design *Median filtering
	Dome effect in the measured elevations due to the introduction of x-parallax in the stereo model	Measurement of a flat surface Ground truth measurement	Optimise calibration strategy (spatial arrangement of control points) Apply a margin during design *Bi-quadratic surface detrending if dome shape is known
Image quality and stereo matching	Gross errors due to incorrect matches	Internal reliability test using different imagery Ground truth measurement	Optimise image quality (change camera settings and/or lighting environment, use image processing techniques) *Median filtering

437 IP for intrinsic parameters. EP for extrinsic parameters.

440 4.2. Workflow Optimisation Methodology

441 Using the identification/quantification methods presented in Table II, we evaluated each
442 DEM reconstruction step and quantified errors for each step and configuration. In test 1, the
443 effect of the number of calibration images and the effect of automatically re-computing the
444 corners to refine the calibration data were evaluated. The influence of the 3D spatial
445 distribution (both horizontal and vertical) of the control points was evaluated in test 2. Test 3
446 was designed to provide a better understanding of what is image quality and how it influences
447 stereo matching.

448 Unless otherwise mentioned, chequerboard calibration images were obtained inside the
449 illuminated hydraulic flume, using manual focus, f/8 aperture setting, 1/50 s shutter speed,
450 ISO 200 and JPEG (1:4) fine image format for both cameras. The chequerboard was held in
451 position by supports underneath, to avoid any movement. Stereo images of the gravel-bed
452 and hemisphere models were recorded in JPEG (1:4), using 1/20 s shutter speed, and
453 transformed with Retinex. Detailed information on Retinex is given in Section 4.2.3.

454 4.2.1. Test 1: Calibration Quantity and Automatic Corner Re-computation

455 40 stereo images of the chequerboard were recorded, with the chequerboard in different
456 positions and orientations, with care being taken to have control points (chequerboard
457 corners) distributed throughout the CFoV (Figure 2). A maximum of 40 was chosen to verify
458 the statement that 20 to 30 views are required (Bradley and Heidrich, 2010). Furthermore,
459 performing a calibration using 40 calibration images still allows for a time-efficient process,
460 which is tolerable for applications in both the laboratory and the field. Smaller subsets
461 containing 10, 20 and 30 calibration images were created by randomly selecting images from
462 the “parent” set of 40 calibration images. The chosen subsets ensured a decent CFoV
463 chequerboard coverage. The calibration toolbox algorithms were successively applied for all
464 calibration image sets individually, with and without automatic corner re-computation,
465 resulting in eight different sets of calibration parameters, for which the stereo-
466 photogrammetric errors were computed.

467 4.2.2. Test 2: Calibration Spatial Distribution

468 Two subsets, both containing 15 calibration images but covering different CFoV areas,
469 were created from the “parent” set of 40 calibration images to enable the evaluation of the
470 effect of the control points’ planar distribution during calibration. The first subset comprised
471 images presenting control points on one half of the CFoV only (Figure 9). The obtained

472 calibration data is hereafter referred to as the “partial” calibration. The second subset, called
473 the “complete” calibration, presented control points distributed throughout the CFoV (Figure
474 9). Stereo-photogrammetric errors were computed for both calibration subsets. Based on the
475 results of test 1, corner re-computation during calibration was not used in this test.

476 To investigate on the importance of the calibration distance (i.e. the distance between the
477 cameras and the control points), the rectification error was measured at distances that
478 encompass the calibration distance (Figure 12). Calibration was completed using control
479 points distributed throughout the CFoV at distances from the cameras between 510 mm and
480 630 mm. The rectification error was measured at distances from the cameras between 430
481 mm and 700 mm. To avoid any bias due to different horizontal [arrangements](#) of the check
482 points at the various distances, only check points in the central region of the CFoV were
483 utilised. To enable this test, the image acquisition settings were changed to f/20 aperture and
484 1/20 s shutter speed.

485 4.2.3. Test 3: Image Quality

486 Stereo images of the gravel-bed model were recorded with five different shutter speeds
487 (1/5 s, 1/10 s, 1/20 s, 1/40 s and 1/60 s) in both RAW and JPEG (1:4) image formats. The
488 other camera settings (f/8, ISO 200) remained identical to those used for the acquisition of the
489 calibration images. We purposely obtained images with varied histograms (Figure 13).
490 Before the stereo matching, RAW images were exported to JPEG using the default encoding
491 parameters and the two lowest compression rates applicable (JPEG (1:2.6) and JPEG (1:15)
492 for “highest quality” and “high quality” JPEG compressions, respectively). The stereo images
493 directly recorded in JPEG (1:4) were subject to transformations, such as greyscale and
494 Retinex. Retinex is a popular human-perception-based image processing technique,
495 increasing the sharpness and compressing the dynamic range of images by reducing flares
496 and enlightening shadows. The Retinex theory (Land, 1986) postulates that a given image can
497 be decomposed into two different images, a reflectance image and an illumination image, on
498 which transformations (e.g. normalising illumination and increasing the local contrast in the
499 dark zones) can be operated to mimic direct scene viewing. Following the emergence of the
500 Retinex theory, different Retinex algorithms were developed; the most widely used being the
501 multi-scale Retinex with colour restoration (MSRCR) algorithm that combines dynamic
502 range compression and tonal rendition (Jobson et al., 1997). Retinex methods have common
503 advantages that they do not require training images and have low computational complexity.
504 A possible defect is the colour greying of images, either globally or in regions where the

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506 grey-world assumption is violated (Rahman and Woodell, 2004). Retinex was used for
507 medical image enhancement (Meng et al., 2012), shadow detection and removal (Sun et al.,
508 2008), illumination-invariant face recognition (Park and Kim, 2008) and point selection in 3D
509 shape registration (Liu et al., 2014). To the best of our knowledge, Retinex was never
510 employed to improve image quality before stereo matching. Using GIMP®
511 (<http://www.gimp.org/>), the MSRCR algorithm was uniformly applied with the following
512 parameters: 240 (scale), 3 (scale division) and 4 (dynamic). These parameters were chosen to
513 provide the best DEM accuracy based on preliminary tests.

514 To enable a realistic comparison between obtained DEMs of the gravel-bed model, where
515 image quality is the only difference, the same calibration data was used to rectify all images
516 and to triangulate all depth information, leading to DEM reconstruction.

517 **5. Results and Discussion**

518 **5.1. Test 1: Calibration Quantity and Corner Re-computation**

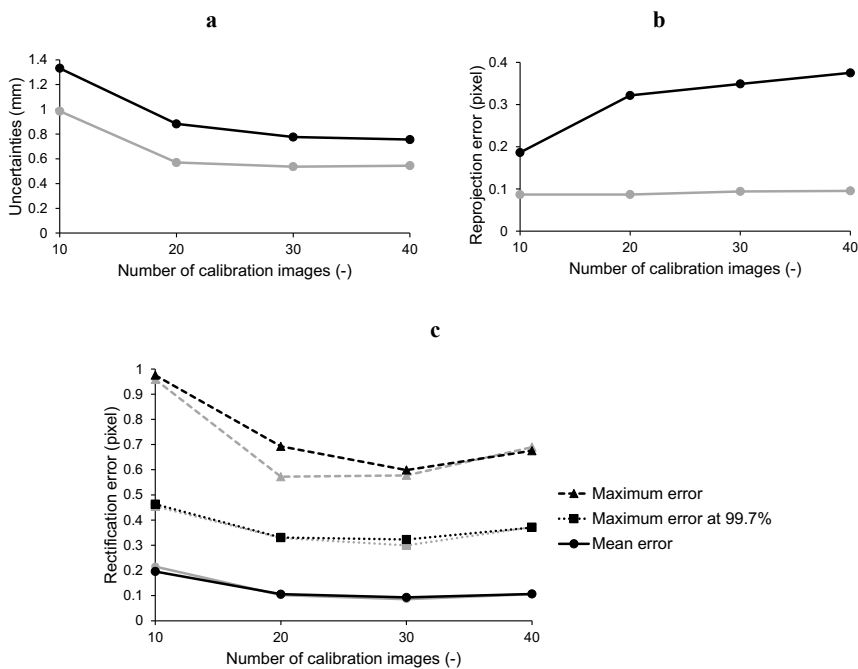
519 Figure 5a shows the numerical uncertainties on the baseline after calibration with
520 different numbers of calibration images, with and without automatic corner re-computation.
521 The uncertainty/precision on the camera baseline was calculated as the square root of the sum
522 of the squared (x,y,z) uncertainties given by the toolbox. Other parameters, such as the focal
523 length (or principal distance), the principal point and the distortion coefficients are not
524 shown, but presented a similar shape of uncertainties. The precisions of the calibrated
525 parameters are reduced with increasing number of calibration images, with a substantial jump
526 between 10 and 20 images (Figure 5a). Corner re-computation also reduced the uncertainties,
527 resulting in around 20 % improvement for all data sets.

528 The re-projection error presented in Figure 5b is the average of the re-projection errors
529 given by the toolbox in the horizontal (x) and vertical (y) directions in an image, averaged
530 between the left and the right camera. It represents the overall precision with which the
531 calibration is able to re-project the chequerboard corners on the calibration images. Figure 5b
532 shows that the re-projection error is significantly reduced (about 3-fold) by automatically re-
533 computing the corners during calibration.

534 The rectification error (Figure 5c) is reduced with increasing calibration images. A
535 minimum rectification error was obtained with 30 images, after which the rectification error
536 slightly increased again. Although re-computing the corners during calibration improved the
537 precisions of the calibration parameters (Figure 5a), it did not improve image rectification.

538 This suggests that the automatic corner re-computation had minimal effect on the calibration
 539 parameters, and thus on image rectification. For all calibrations, the mean and the standard
 540 deviation of rectification error are small (about 0.2 pixel and smaller), indicating that most
 541 conjugate points are on the same scanline after image rectification, ensuring minimal
 542 systematic matching error throughout the CFoV.

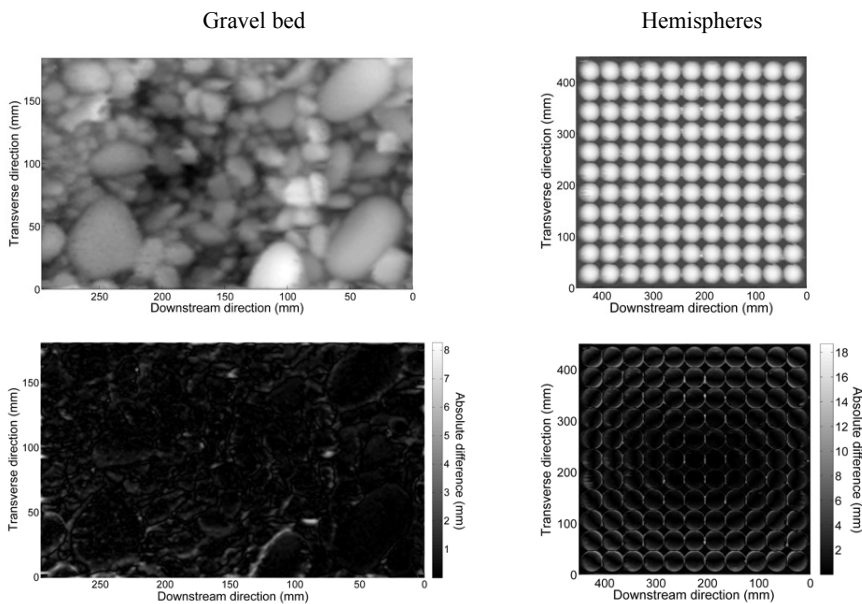
543



544 **Figure 5.** Influence of the automatic corner re-computation and the number of calibration images on
 545 (a) the numerical uncertainties on the calibrated baseline; (b) the re-projection error; and (c) the
 546 rectification error. Calibrations with corner re-computation (grey), calibrations without corner re-
 547 computation (black).

548 Figure 6 presents the DEMs of the gravel-bed and hemisphere models obtained with the
 549 “parent” calibration (40 images) and their associated DEMs of difference (DoDs) after
 550 comparison of the DEMs with the “truth” elevations. Figure 6 shows clearly that most DEM
 551 errors occur at the edges and troughs, due to occlusions. Edges and troughs also cause poor
 552 image correspondences because of shadows and uniform colouring of the surface (i.e. low-
 553 textured areas). For occlusions, the at-a-point elevation is based on the assumption of a

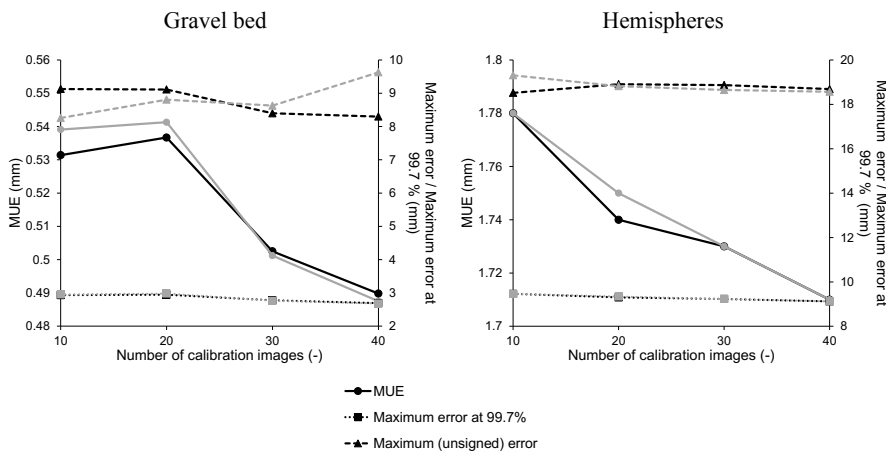
554 continuous surface, generally resulting in over-smoothed deep holes. The DoD of the
 555 hemisphere model shows that DEM errors increase both in frequency and magnitude with the
 556 radial distance from the centre of the CFoV because of occlusions, since oblique rays are less
 557 able to reach areas shadowed by higher grounds. This is not observed in the DEM of the
 558 gravel-bed model, which can partly be attributed to its smaller size. Additionally, the decision
 559 to set the baseline parallel to the downstream direction resulted in errors preferentially
 560 aligned with the transverse direction. When recording surfaces similar to the hemisphere
 561 model, increasing the setup flying-height would likely reduce the occlusions and improve the
 562 DEM quality. A poorer resolution would result as a consequence, as mentioned previously.



563 **Figure 6.** (Top) measured DEMs, aligned with the truth DEMs; and (bottom) associated DoDs
 564 (absolute differences are shown for clarity). Calibration was performed with the “parent” set of
 565 images without corner re-computation; stereo matching was done on JPEG (1:4) images obtained
 566 with 1/20 s and transformed with Retinex.

567 Figure 7 shows the quantitative evaluation of the DEM quality, computed over the
 568 gravel-bed and hemisphere models, for the eight calibrations tested. All gravel-bed model
 569 DEMs have optimal accuracy with MUE equal to 0.51 ± 0.03 mm and a maximum absolute
 570 error of 8.90 ± 0.7 mm. In Bertin et al. (2014), a MUE of 0.43 mm and a maximum absolute

571 error of 8.16 mm was obtained with a baseline distance of 250 mm and a flying-height of 636
 572 mm, suggesting that the DEM errors can be reduced by changing the stereo-photogrammetric
 573 design. As Figure 6 suggested, the DEMs of the hemisphere model are of lesser quality than
 574 the DEMs of the gravel-bed model, with an overall three-fold increase in the MUE and two-
 575 fold increase in the maximum absolute error. Figure 7 shows that the MUE and the maximum
 576 error at the 99.7 % level tend to decrease with the number of calibration images for all
 577 DEMs. This may be explained by the joint reduction of the uncertainties on the calibration
 578 parameters and the rectification error with the number of calibration images, which was
 579 observed in Figure 5a and Figure 5c. Similarly to previous observations (Figure 5c), the
 580 effect of the corner re-computation on the DEM quality is small, and no clear trend is
 581 observable. We nevertheless believe that corner re-computation is useful when chequerboard
 582 image quality prevents accurate corner detection, e.g. in the case of through-water
 583 photogrammetry.

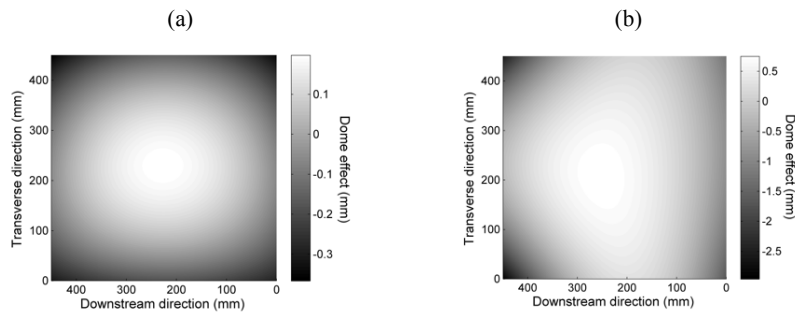


584 **Figure 7.** Influence of the automatic corner re-computation and the number of calibration images
 585 on the DEM quality. Calibrations with corner re-computation (grey), calibrations without corner re-
 586 computation (black).

587 A small dome (elevation span of $0.64 \text{ mm} \pm 0.08$; mean absolute elevation when centred
 588 on zero of $0.12 \text{ mm} \pm 0.02$) was noticed in the DEM of a flat surface ($450 \times 450 \text{ mm}$) for all
 589 calibrations (Figure 8a). Increasing the number of calibration images and re-computing the
 590 corners during the calibration did not reduce the dome effect.

591 Wackrow and Chandler (2011) showed that the mildly convergent imagery provides
592 means to reduce the dome effect. Similarly to the optimisation of the baseline distance,
593 deciding between a convergent and a vertical image configuration is difficult and is surface-
594 dependent.

595 A counter measure to minimise the dome effect in DEMs is the application of a margin
596 during the design to limit the DEM analysis to a more central region where the dome is
597 smaller. But again, to be effective, the minimisation of the dome effect by accounting a
598 margin has to be balanced against a deteriorated depth resolution when the camera-to-object
599 distance is increased.

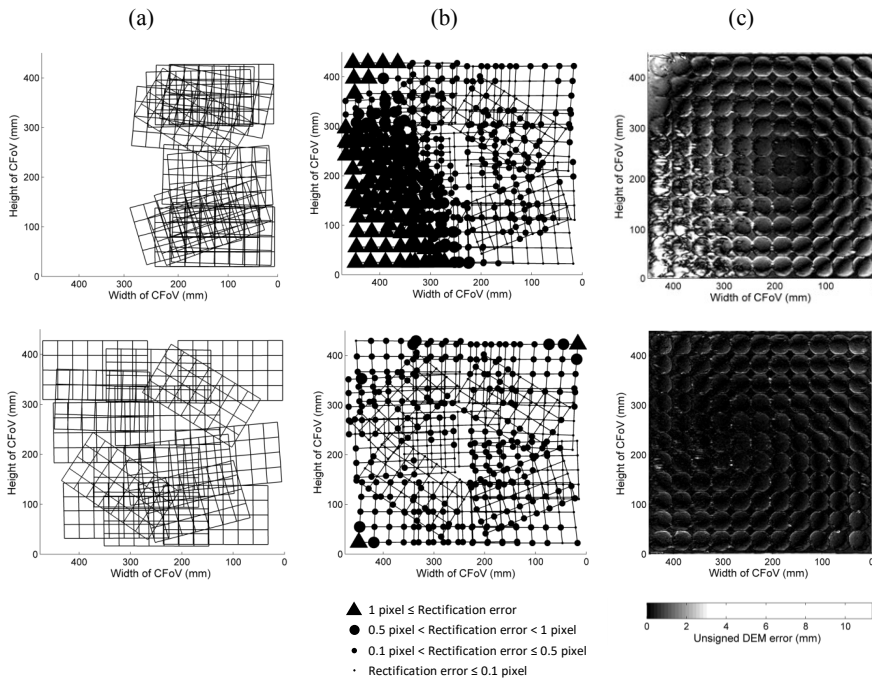


600 **Figure 8.** Dome observed in the DEM of a flat surface (450 x 450 mm). (a) The dome effect was
601 similar for all calibrations tried in test 1. (b) Dome in the case of the “partial” calibration (test 2).
602 The dome was measured by fitting a bi-quadratic surface to the DEM by least-squares, after the DEM
603 was aligned with the photo base.

604 5.2. Test 2: Calibration Spatial Distribution

605 Figure 9 and Table III show that both the rectification error and the DEM error are
606 increased in the regions where control points were missing during calibration. This is valid
607 for the “partial” calibration, but is also visible for the “complete” calibration. For the “partial”
608 calibration, rectification error statistics are severely increased (about 10 times) between
609 regions with control points (called the “calibration region”) and regions without control
610 points (Table III). This in turn results in a two-fold increase in the DEM error between the
611 two regions (Table III). The degradation of the DEM quality is less than the difference in
612 rectification error would suggest. Firstly, only large rectification errors (> 0.5 pixel) have an
613 impact on the stereo matching, and thus on the DEM quality, since SDPS stereo matching is
614 performed along lines of 1 pixel width. Secondly, point cloud to DEM transformation, during

615 which the DEM errors due to solitary large rectification errors are smoothed by interpolation,
 616 reduces the final DEM error. And thirdly, DEM errors are bounded by the relief of the
 617 hemisphere model.



618 **Figure 9.** Plan-view of control points location in calibration images (a); associated rectification
 619 error (b); and associated DEM error over the hemisphere model (c). The top row corresponds to the
 620 “partial” calibration. The bottom row corresponds to the “complete” calibration. In order to
 621 emphasise the effect of a “partial” calibration, the internal reliability of the DEMs was evaluated by
 622 doing a comparison with the DEM obtained with the “parent” calibration, not the “truth” DEM.

623 A closer look at Figure 9 and Table III shows that the “partial” calibration not only
 624 affected the point measurements outside the “calibration region”, but to a lesser extent has a
 625 global effect over the whole measurement window. Indeed, the DEM error inside the
 626 “calibration region” in the case of the “partial” calibration (MUE of 0.66 mm and SDE of
 627 0.90 mm) is larger than the overall (over the whole CFoV) DEM error in the case of the
 628 “complete” calibration (MUE of 0.30 mm and SDE of 0.42 mm). Since the rectification error
 629 was only increased outside the “calibration region” for the “partial” calibration, we conclude

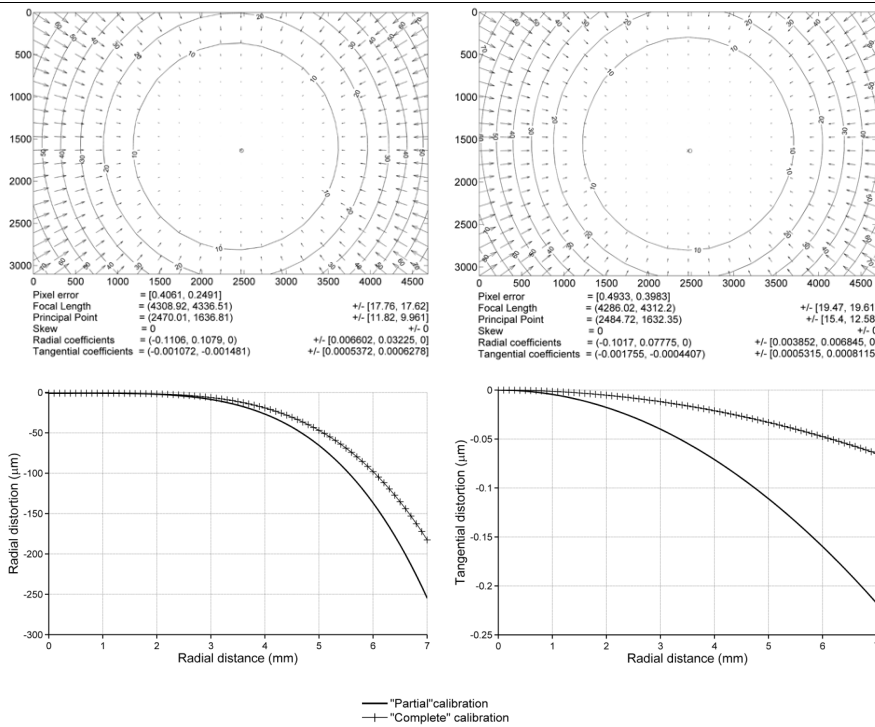
630 that there must be other DEM error sources in addition to those from inaccurate image
 631 rectification.

632 **TABLE III.** Rectification error and DEM error (using the hemisphere model) in the case of the
 633 “partial” and the “complete” calibrations. In order to emphasise the effect of a “partial”
 634 calibration, the internal reliability of the DEMs was evaluated by doing a comparison with the DEM
 635 obtained with the “parent” calibration, not the “truth” DEM.

	Spatial distribution of control points	Partial coverage of CFOV			Complete coverage of CFOV
	Region where errors are calculated	Inside calibration region	Outside calibration region	Whole CFOV	Whole CFOV
Rectification error (pixel)	Mean	0.13	1.18	0.60	0.14
	Standard deviation	0.12	1.25	0.99	0.08
	Maximum	0.76	10.11	10.11	0.78
DEM error (mm)	MUE	0.66	1.09	0.88	0.30
	SDE	0.90	1.51	1.25	0.42
	Maximum (unsigned)	5.60	11.34	11.34	4.21

636
 637 Figure 10 presents the complete distortion model, the intrinsic parameters and the re-
 638 projection errors for the “partial” and the “complete” calibrations. Observations for both
 639 cameras were identical; therefore only results for the left camera are presented. Firstly, the re-
 640 projection errors are smaller for the “partial” calibration, which disagrees with the
 641 rectification error and the DEM error observations (Table III). This suggests that the re-
 642 projection error is not adequate to characterise the calibration effect onto the stereo matching.
 643 Other studies showed that the rectification error is more suitable than the re-projection error
 644 to evaluate the quality of a calibration for binocular systems (Bradley and Heidrich, 2010,
 645 Bertin et al., 2012). Secondly, the shape of the distortion model is modified for the “partial”
 646 calibration, with a lateral displacement and a change in curvature. The computed distortion

647 coefficients and the profiles of radial and tangential distortion confirm this change, showing
 648 an increase in distortion for the “partial” calibration (Figure 10).

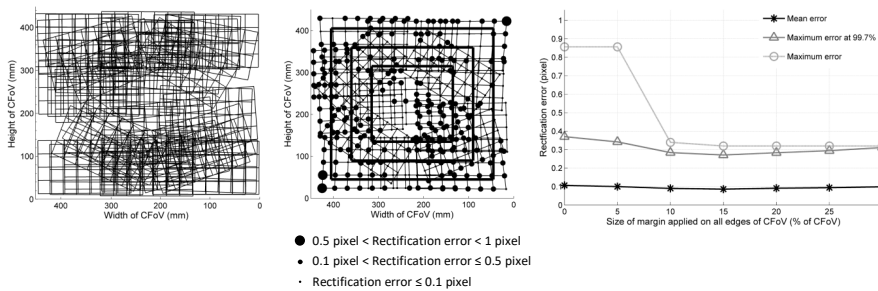


649 **Figure 10.** (Top row) Complete distortion model, intrinsic parameters and re-projection errors
 650 obtained during calibration of the left camera for (left) the “partial” calibration; and (right) the
 651 “complete” calibration. (Bottom row) Profiles of radial (left) and tangential (right) distortion of the
 652 left camera. Similar observations were made with the right camera.

653 Resulting from the inaccurate distortion model obtained with the “partial” calibration, a
 654 large dome (elevation span of 3.71 mm and mean absolute elevation when centred on zero of
 655 0.47 mm; compared with 0.64 mm and 0.12 mm, respectively, for a “complete” calibration)
 656 was observed in the DEM of a flat surface (Figure 8b), explaining why DEM errors not only
 657 increased outside the “calibration region”, but globally over the CFoV.

658 Figure 11 presents the results obtained with the “parent” calibration. We recall the
 659 “parent” calibration was completed using 40 calibration images, which was the largest image
 660 set in this study. As shown, it is difficult to place the chequerboard (and thus obtaining

661 control points) to cover the whole CFoV (Figure 11). Rectification errors larger than 0.5 pixel
 662 are found in the two corners of the measurement window where only one control point was
 663 available for calibration. Hence, to enable correct stereo matching throughout the
 664 measurement window, it is essential to obtain sufficient control points (our results suggest at
 665 least two).

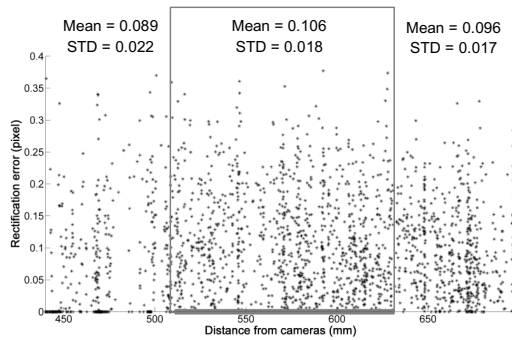


666 **Figure 11.** Plan-view of control points location in the case of the “parent” calibration: 40 calibration
 667 images (left); and associated rectification error (middle). The lines delimit the regions after a margin
 668 of size 10, 20 and 30% the size of the CFoV, respectively, has been applied. The graph on the right
 669 shows the rectification error as a function of the margin size.

670 Accounting for a margin around the CFoV, where the rectification error is not counted,
 671 can be helpful to remove marginal pixels with large rectification errors (Figure 11), thus
 672 reducing the risk to have large DEM errors at these same locations. Median filtering during
 673 the stereo matching may also smooth the effects of solitary large rectification errors.

674 With no loss in accuracy, image rectification to epipolar geometry can be performed for
 675 points with a camera distance outside the range of control points (Figure 12). As previously
 676 found, control points should be evenly distributed throughout the 3D volume covered by the
 677 object of interest (Chandler et al., 2001, Carboneau et al., 2003). Figures 9 and 12 show that
 678 in our case control points only need to cover the 2D area of interest. For hydraulic
 679 experiments this implies that calibration images can be obtained above the gravel-bed
 680 surface, without increasing the rectification error at the distance of the gravel bed.
 681 Subsequent stereo matching performance will not be decreased. This is a major advantage, as
 682 the setup does not need to be moved for the calibration, which minimises the risk to alter the
 683 validity of the calibration over time. Our results support and extend the early findings of
 684 Weng et al. (1992), who showed that calibrated cameras are able to measure points at
 685 distances beyond the range of control points with minimal (1.3 %) loss in accuracy. However,

686 caution needs to be taken when generalising these results to a much larger range of camera
687 distances, as only a narrow distance strip was tested.

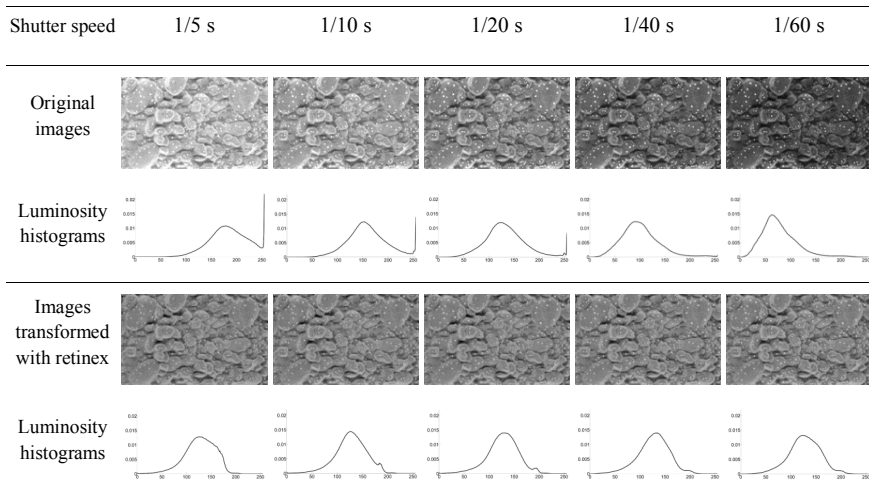


688
689 **Figure 12.** Rectification error, determined at each corner of the chequerboard in 65 rectification-
690 check images (i.e. at 2600 check points), versus the distance from the cameras. The grey markers on
691 the horizontal axis and the box delimit the range of control points' distances during calibration.

692 5.3. Test 3: Image Quality

693 Figure 13 presents the original images of the gravel-bed model, directly recorded in
694 JPEG (1:4) using various shutter speeds (other camera settings remained constant), and their
695 Retinex equivalents, all cropped to the size of the model (296 x 184 mm), with their
696 respective luminosity histograms. Pixel luminosity corresponds to the sum of 0.299, 0.587,
697 and 0.114 times the intensity in the red, green and blue tones, respectively. As evidenced in
698 Figure 13, the MSRCR algorithm implemented in GIMP® is able to re-centre the distribution
699 of pixel luminosity for all images tested. Whilst original images look very different, the
700 images transformed with Retinex are very similar visually. As observed in previous works, a
701 colour greying happened during the Retinex transformations (Jobson et al., 1997, Rahman
702 and Woodell, 2004).

703 Table IV presents the MUE computed after differentiation of the DEMs reconstructed
704 with the images obtained for the test and the “truth” DEM of the gravel-bed model. We recall
705 that the same calibration data was used throughout the test to ensure a consistent comparison
706 between the DEMs, where image quality is the only difference. HHQ and HQ correspond to
707 images recorded in RAW exported to “highest quality” (1:2.6 compression ratio) and “high
708 quality” (1:15 compression ratio) JPEG, respectively.



709 **Figure 13.** Left-hand images of the gravel-bed model, cropped to the size of the ground truth (296 x
710 184 mm), and their associated luminosity histograms. Only the shutter speed was changed, other
711 settings (ISO, aperture) remained constant. The original images, recorded in JPEG (1:4), and their
712 Retinex transformations are presented.

713 Image transformations (greyscale and Retinex) have a considerable impact on the stereo
714 matching and thus on the DEM accuracy (Table IV). The most accurate DEMs were those
715 obtained with images transformed with Retinex, with an average 40 % reduction of the MUE
716 compared with the DEMs reconstructed using the original images. This finding is significant,
717 as to the authors' knowledge it is the first time the MSRCR algorithm is implemented to
718 facilitate the stereo matching. In contrast, the stereo matching performed on the greyscale
719 equivalent images provided the worst results. We therefore recommend other users of the
720 calibration toolbox to modify the code to obtain rectified images in RGB format to enable
721 superior stereo matching results.

722 Table IV shows that RAW to JPEG transformation reduced the DEM quality in terms of
723 the MUE (about 5 % for HHQ, 10 % for HQ), compared to DEMs collected using images
724 directly recorded in JPEG (1:4). It suggests that the in-camera and the camera software JPEG
725 encodings are different. Here, the in-camera JPEG compression provided better quality
726 images for the stereo matching. We still believe RAW imagery will be useful for other
727 studies, where there is no a-priori knowledge of the optimum stereo matching camera
728 settings, since exposure changes can be made on RAW images.

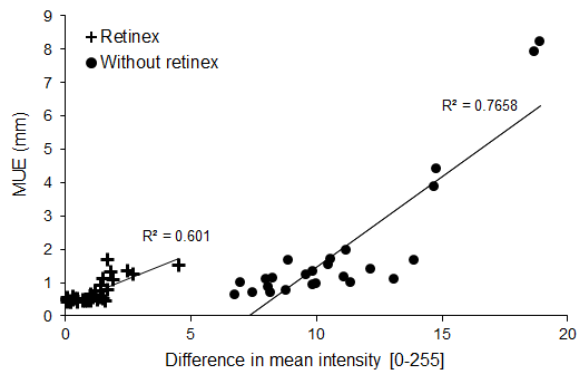
729 **TABLE IV.** Mean unsigned error (MUE) in millimetre measured on the DEMs of the gravel-bed
730 model, reconstructed using images recorded with various shutter speeds (other camera settings
731 constant) in both JPEG(1:4) and RAW format. Images recorded in RAW were converted to HHQ and
732 HQ JPEG (JPEG (1:2.6) and JPEG (1:15), respectively) before the stereo matching. Original images
733 directly recorded in JPEG (1:4) were transformed with Retinex and greyscale. To allow a realistic
734 comparison between DEMs, where the differences are only due to the image quality, the image
735 rectification prior to the stereo matching and the depth triangulation were performed using the same
736 calibration data. Image file size is indicated, and was determined on the left-hand images recorded
737 with 1/20 s shutter speed.

Transformation	Shutter speed (s)				
	1/5	1/10	1/20	1/40	1/60
Retinex (7.8Mb)	0.54	0.51	0.49	0.49	0.51
Original (6.6 Mb)	0.96	0.69	0.62	1.08	1.64
HHQ (9.1 Mb)	1.02	0.72	0.64	1.12	1.59
HQ (1.8 Mb)	1.09	0.73	0.66	1.13	1.57
Greyscale (4.7 Mb)	1.43	1.16	0.98	2.01	2.57

738 The tested shutter speed camera setting impacted the stereo matching performance and
739 the DEM quality substantially (Table IV). All other camera settings were unchanged in this
740 test. The stereo pair recorded with 1/20 s shutter speed always provided the best DEMs in
741 terms of the MUE. It is important to note that this finding is specific to this study, as the
742 shutter speed selection depends on various parameters, such as the lighting environment and
743 the shininess of the surface. For all images except the Retinex equivalents, the correct
744 selection of the shutter speed was essential, since a change of the shutter speed from 1/20 s to
745 1/60 s resulted in DEMs with a large difference in MUE (about 60 % change). For images
746 transformed with Retinex, the representation of the MUE for various shutter speeds is less
747 widely spread (Table IV), suggesting that a larger range of shutter speeds has a lesser effect
748 on stereo matching. Still, a 9 % difference in MUE is observed between two DEMs collected
749 using Retinex imagery (DEMs reconstructed with 1/5 s and 1/20 s, respectively). Therefore,
750 whilst image transformation techniques like Retinex have the potential to facilitate the stereo
751 matching, the careful selection of the camera settings must still be regarded as a key element

752 in a stereo-photogrammetric project. According to the results obtained in this test, a good
753 image for stereo matching is represented by a luminosity histogram with a pronounced
754 central peak before any transformation.

755 Figure 14 presents a summary of the MUE for 62 gravel-bed model DEMs. The
756 horizontal axis shows the difference in mean pixel intensity between the two images,
757 calculated over the size of the gravel-bed model (296 x 184 mm). Even in a controlled
758 environment such as the laboratory, exposure difference between the left and right images
759 forming a stereo pair may be observed, often due to the lighting source. Neon lights (Figure
760 1), which were used for the study, have the advantage of producing an even illumination of
761 the test section. The known disadvantage is that they cause a “flicker effect” with light pulsed
762 at twice the supply frequency. Figure 14 shows clearly that the difference in mean pixel
763 intensity between the two images forming a stereo pair is reduced when transformed with
764 Retinex.



765
766 **Figure 14.** Effect of the image quality (here described in terms of the difference in mean pixel
767 intensity between the two images forming a stereo pair) on the DEM accuracy, represented by the
768 MUE. The results obtained on 62 DEMs of the gravel-bed model (37 Retinex and 25 original images)
769 are summarised in this graph.

770 Furthermore, the results show that the MUE and the difference in mean pixel intensity are
771 correlated, with a distinct relationship for each image type (i.e. with or without Retinex). For
772 both original images and their Retinex equivalents, the MUE increases with an increased
773 difference in mean pixel intensity between the two images used for the stereo matching. To
774 evaluate image quality, the difference in mean pixel intensity between the two images

775 forming a stereo pair, needs to be an important parameter to judge the pair's suitability for
776 stereo matching.

777 **6. Conclusions**

778 This paper presented a digital stereo-photogrammetric workflow for close-range
779 measurement, in application to grain-scale fluvial surfaces. Processing steps (calibration,
780 image rectification and stereo matching) were introduced and discussed. A controlled
781 laboratory evaluation was carried out to identify the cause of processing errors and to find
782 means to reduce their impact on DEM quality.

783 The introduced workflow can be described as user-friendly, low-cost and versatile.
784 Imagery was acquired with two consumer-grade DSLRs and processed using non-proprietary
785 algorithms. Compared with previous fluvial applications, "on-the-job" calibration using
786 stereo images of a 2D chequerboard does not require the placement of fixed control targets on
787 the riverbed surveyed with an independent device, and enables both radial and tangential
788 distortion coefficients to be recovered. Scanline-based stereo matching resulted in dense
789 DEMs with the possibility to have sampling distances as small as the pixel size at the object's
790 distance, which improves substantially on traditional area-based methods. Limited post-
791 processing was applied and prevented the introduction of new errors.

792 Consequently, our DEMs have high point densities (0.25 mm sampling distance) and high
793 vertical accuracies (MUE close to 0.5 mm), which are required to realistically represent
794 water-worked riverbed roughness. To the authors' knowledge this represents one of the most
795 precise and accurate topography measurement solution for hydraulic research, which rivals
796 results obtained with laser-scanning (Hodge et al., 2009).

797 Using the presented evaluation strategy, it is shown that errors are systematically
798 introduced to the workflow, starting with the calibration. Evenly distributed control points
799 throughout the measurement window improve DEM quality, by ensuring a smaller than 0.5
800 pixel homogeneous rectification error and removing most of the optical imagery distortion. In
801 general terms, an increasing number of calibration images improved DEM quality, whilst re-
802 computing corners had no observable effect outside the re-projection error reduction.
803 Following on previous works, our studies confirm that the calibration quality for binocular
804 systems is best expressed in terms of the rectification error, rather than the more commonly
805 used re-projection error (Bradley and Heidrich, 2010, Bertin et al., 2012). Image quality, a
806 function of the dynamic range in the imagery, as well as the similarity between the two

807 images forming a stereo pair, was shown critical to stereo-matching success. We presented
808 how image transformation techniques, such as Retinex, provide means to heighten the
809 similarity between the images forming a stereo pair and thus to improve stereo matching.
810 Given suitable calibration parameters, image enhancement and stereo matching were the
811 steps where optimisation resulted in the most significant DEM accuracy improvement in our
812 study. We therefore recommend considering these steps carefully to achieve optimal
813 accuracy.

814 Ongoing work is required on how best to address the existence of occlusions, which are
815 still a major source of photogrammetric errors. Recent studies use multi-view stereo (MVS)
816 and structure-from-motion (SfM) photogrammetry techniques for medium to large scale
817 experiments (Westoby et al., 2012, Javernick et al., 2014), but not for the very small scales.
818 Those techniques are potentially more suited to capture occlusions. In the present study,
819 occlusion errors could not be removed completely, although calibration and image quality
820 optimisation improved stereo-matching results. Occlusions are the direct consequence of the
821 photogrammetric design. The use of realistic ground truths, such as the ones presented in this
822 study, is shown to be useful for the experimental determination of the optimum stereo-
823 photogrammetric design. The next step is acquiring multiple depth maps of the same scene
824 from different viewpoints, which can then be fused to improve data quality.

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