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Trust in complex actions

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Abstract. Current formal models of trust are limited since they only consider an agent's trust in the atomic action of another agent and therefore do not apply to trust in complex actions where the elements in the complex action are atomic actions of different agents. Our aim is to present a logical formalization of trust in complex actions, and to show that this formalization can be useful for the formal characterization of trust in composite services, where trust in a composed service is defined in a compositional way from trust in the components of that service.

1 Introduction

According to Castelfranchi and Falcone (C&F henceforth), the trust relation involves a truster *i*, a trustee *j*, an action *a* that is performed by *j* and a goal φ of *i* [5, 7]. They defined the predicate Trust as a goal together with a particular configuration of beliefs of the trustee. Precisely, *i* trusts *j* to do *a* in order to achieve φ if and only if:

- 1. *i* has the goal that φ and
- 2. *i* believes that:
 - (a) j is capable to perform a,
 - (b) j is willing to perform a,
 - (c) *j* has the power to achieve φ by doing *a*.

C&F distinguish external from internal conditions in trust assessment: *j*'s capability to perform *a* is an external condition, while *j*'s willingness to perform *a* is an internal condition (being about the trustee's mental state). Finally, *j*'s power to achieve φ by doing *a* relates internal and external conditions: if *j* performs *a* then φ will result. Observe that in the power condition the result is conditioned by the execution of *a*; therefore the power condition is independent from the capability condition. In particular, *j* may well have the power to achieve φ without being capable to perform *a*: for example, right now I have the power to lift a weight of 50kg, but I am not capable to do this because there is no such weight at hand.¹

C&F did not investigate further how goals, capabilities, willingness and power have to be defined; their definition might therefore be called semi-formal. Recently Herzig,

¹ Together, capability to perform *a* and power to achieve φ by doing *a* amount to having a strategy to achieve φ . Similar modalities were studied in Coalition Logic CL [17], Alternating-time Temporal Logic ATL [1], and STIT theory [2]. However, these logics focus on game-theoretic situations where an agent has the power to achieve φ whatever the other agents choose to do. While this latter aspect will not be captured in our analysis here, we have shown in [12, 15] how it could be integrated into our logical framework.

Lorini et al. analysed these predicates in more detail in [13, 14, 16]. First of all they defined the predicate Trust₀ as follows:

$$\operatorname{Trust}_{0}(i, j:a, \varphi) \stackrel{\operatorname{def}}{=} \operatorname{Goal}(i, \varphi) \wedge \operatorname{Bel}_{i}(\operatorname{CExt}(i:a) \wedge \operatorname{CInt}(i:a) \wedge \operatorname{Res}(i:a, \varphi))$$

. .

where Goal(i, φ) corresponds to item 1 and CExt(i:a), CInt(i:a) and Res($i:a, \varphi$) respectively correspond to items 2a, 2b and 2c in C&F's definition (and CExt and CInt stand for the external and the internal conditions in trust assessment).²

They then defined the predicates CExt(j:a), CInt(j:a) and $Res(j:a, \varphi)$ in terms of the concepts of belief, choice, action and time. They draw a distinction between occurrent trust —*i*'s trust that *j* is going to perform *a* here and now— and dispositional trust: *i* trusts that *j* is going to perform *a* whenever suitable conditions obtain. The above definition is that of occurrent trust.

Both C&F and Herzig, Lorini et al. only considered trust in the atomic action of another agent and did not consider trust in complex actions where the elements in the complex action are atomic actions of different agents. Our aim in this article is to extend their definition to complex actions, and to show that a definition of trust in complex actions is extremely important in the context of composite services.

In the context of services architecture, some provider agents publish atomic services; however, when a client agent needs to implement a more complex business process, it must chain service calls, according to a specific workflow structure. Automating the service calls is called service composition: given the business process to implement, the control flow has to be computed in order to guarantee that the goal of the service caller is satisfied.

Since services are provided by agents, users may trust some agents for certain actions but not for other actions which they deem critical, usually depending on the nature of the information they have to send to this agent for the service action to perform the action.

In current literature, for example in [18], service selection for composition assumes the existence of a central authority guaranteeing the non-functional properties of the services. In practice, such an authority might not exist, for example in P2P networks [20], or may not itself be trustworthy.

To resolve the aforementioned problem, trust in complex action, supported by the introduction of beliefs and trust in the description of services, could be used. With a model for trust in the services world, one may express composition objectives as dynamic logic formulas with trust component. The service composition problem would then reduce to the satisfaction of such a formula. This method would ensure that the composition is correct and compatible with the beliefs of the user, thus ensuring a trust-worthy sequence of service call for achieving the goal of the user.

The rest of the paper is organized as follows. In Section 2 we introduce a modal logic of belief, goal, time, and complex actions. In Section 3 we define the trust predicate for complex actions and study its constituents. In Section 4 we relate trust in complex

² They used a 4-ary predicate $\text{Trust}(i, j, a, \varphi)$ instead of our ternary $\text{Trust}_0(i, j:a, \varphi)$. Moreover, their trust definition was in terms of the predicates Capable(j:a), Willing(j:a) and $Power(j:a, \varphi)$ instead of our CExt(j:a), CInt(j:a) and $\text{Res}(j:a, \varphi)$. We preferred our terms and notations because they better generalize to complex actions.

actions to trust in atomic actions, providing thus a way to construct trust in complex actions. In Section 5 we then discuss how this applies to service composition.

2 Background

We recall the logical framework of [13, 14, 16], that we extend towards complex actions.

2.1 A logical language with complex actions

Suppose given three countable sets: a set of propositional variables *Atm*, a set of agents *Agt* and a set of atomic actions *Act*. Complex formulas φ and complex actions α are defined by the following BNF:

```
\varphi ::= p \mid \neg \varphi \mid \varphi \land \varphi \mid \mathsf{Bel}_i \varphi \mid \mathsf{Ch}_i \varphi \mid \mathsf{Feasible}_a \varphi \mid \mathsf{Happens}_a \varphi \mid \mathsf{F} \varphi\alpha ::= i:a \mid \alpha; \alpha \mid \alpha + \alpha \mid \varphi? \mid \alpha^*
```

where *p* ranges over *Atm*, *i* ranges over *Agt*, and *a* ranges over *Act*. Bel_{*i*} φ reads "*i* believes that φ "; Ch_{*i*} φ reads "*i* chooses that φ "; Feasible_{*a*} φ reads "there is a possible execution of α after which φ is true"; Happens_{*a*} φ reads " α happens, and φ is true afterwards"; and F φ reads " φ will eventually be true". Both Feasible_{α} and Happens_{α} are modal operators of the possible kind, and could be written $\langle \alpha \rangle$ as in dynamic logic. Note that they are different: Feasible_{α} \top means that α is execut*able*, while Happens_{α} \top means that α is execut*ed*.

Operators Ch_i are used to denote an agent's current chosen goals, that is, the goals that the agent has decided to pursue here and now. We do not consider how an agent's chosen goals originate through deliberation from more primitive motivational attitudes, called desires, and from moral attitudes, such as ideals and imperatives. Since the chosen goals of an agent result from the its deliberation, they must satisfy two fundamental rationality principles: chosen goals have to be consistent (i.e., a rational agent cannot decide to pursue an inconsistent state of affairs); chosen goals have to be compatible with the agent's beliefs (i.e., a rational agent cannot decide to pursue something that it believes to be impossible). These two principles will be formally expressed in Section 2.2.

Remark 1. In [13, 14, 16] Happens_{*i:a*} was noted *Does*_{*i:a*} and read "*a* is going to be performed by *i*". We preferred Happens in order to allow for complex actions such as *i:a*; *j:b* that are performed by more than one agent.

The atomic action *i*:*a* reads "*i* performs *a*"; the complex action α_1 ; α_2 reads "do α_1 and then α_2 "; $\alpha_1 + \alpha_2$ reads "choose nondeterministically between α_1 and α_2 ", where the choice is understood to be up to the environment (i.e., the other agents and nature), and not up to the agents performing α_1 and α_2 ; φ ? reads "if φ is true then continue, else fail"; and finally, α^* reads "do α an arbitrary number of times".

We define $After_{\alpha}\varphi$ to be an abbreviation of $\neg Feasible_{\alpha}\neg\varphi$, which therefore has to be read "if the execution of α is possible then φ holds afterwards". Moreover, the following standard program constructions are defined as follows:

 $\begin{array}{rll} & {\rm skip} & \stackrel{\rm def}{=} & \top ?\\ & {\rm fail} & \stackrel{\rm def}{=} & \bot ?\\ & {\rm if}\,\varphi\, {\rm then}\,\alpha_1\, {\rm else}\,\alpha_2 & \stackrel{\rm def}{=} & (\varphi?;\alpha_1) + (\neg\varphi?;\alpha_2)\\ & {\rm while}\,\varphi\, {\rm do}\,\alpha & \stackrel{\rm def}{=} & (\varphi?;\alpha)^*; \neg\varphi? \end{array}$

In our application the actions seem never to be joined actions (which here would be something like translating a text together). For that reason we define parallel composition as interleaving, i.e. $\alpha ||\beta| \stackrel{\text{def}}{=} (\alpha; \beta) + (\beta; \alpha)$. In this way we can avoid introducing || as a primitive.

2.2 Semantics

We take over the semantics of [14] and extend it to complex actions, whose semantics we take over from Propositional Dynamic Logic PDL. We call the resulting logic \mathcal{L} . The semantics of \mathcal{L} is in terms of a class of frames that has to satisfy several constraints.

Frames A *frame* is a tuple $M = \langle W, A, B, C, D \rangle$ that is defined as follows.

- W is a nonempty set of possible worlds or states.
- $A: Agt \times Act \longrightarrow 2^{W \times W}$ maps every agent *i* and action *a* to a relation $A_{i:a}$ between possible worlds in *W*.
- $B: Agt \longrightarrow 2^{W \times W}$ maps every agent *i* to a serial, transitive and Euclidean³ relation B_i between possible worlds in W.
- $C: Agt \longrightarrow 2^{W \times W}$ maps every agent *i* to a serial relation C_i between possible worlds in *W*.
- $D: Agt \times Act \longrightarrow 2^{W \times W}$ maps every agent *i* and action α to a deterministic relation (alias a partial function) $D_{i:a}$ between possible worlds in W.⁴

It is convenient to view relations on *W* as functions from *W* to 2^W ; therefore we write $D_{i:a}(w)$ for the set $\{w' | (w, w') \in D_{i:a}\}$, etc.

When $w' \in A_{i:a}(w)$ then *if* at *w* agent *i* performs α then this *might* result in *w'*. $B_i(w)$ is the set of worlds that are compatible with agent *i*'s beliefs at *w*; the conditions of seriality, transitivity and Euclideanity are those of the standard logic of belief KD45. $C_i(w)$ is the set of worlds that are compatible with agent *i*'s choices at *w*; seriality corresponds to consistency of choices, which is the only condition that is generally imposed on choices. $D_{i:a}(w)$ is the set of worlds w' that can be reached from *w* through the occurrence of agent *i*'s action *a*. If $(w, w') \in D_{i:a}$ then *w'* is the unique actual *successor* world of *w*, that will be reached from *w* through the occurrence of agent *i* performs an action *a*, resulting in the next state *w'*. (We might also say that $D_{i:a}$ is a partial function.) If $D_{i:a}(w) \neq \emptyset$ then we say that $D_{i:a}$ is defined at *w*.

³ A relation B_i on W is Euclidean if and only if, if $(w, w') \in B_i$ and $(w, w'') \in B_i$ then $(w', w'') \in B_i$.

⁴ A relation $D_{i:a}$ is deterministic iff, if $(w, w') \in D_{i:a}$ and $(w, w'') \in D_{i:a}$ then w' = w''.

Constraints on frames Frames will have to satisfy some constraints in order to be legal \mathcal{L} -frames. For every $i, j \in Agt, \alpha, \beta \in Act$ and $w \in W$ we suppose:

C1 if $D_{i:a}$ and $D_{j:b}$ are defined at w then $D_{i:a}(w) = D_{j:b}(w)$.

Constraint **C1** says that if w' is the *next* world of w which is reached from w through the occurrence of agent *i*'s action α and w'' is also the *next* world of w which is reached from w through the occurrence of agent *j*'s action β , then w' and w'' denote the same world. Indeed, we suppose that one agent acts at a time, and that every world can only have one *next* world. Note that **C1** implies determinism of every $D_{i:a}$ (so we might have omitted that from the above constraints on D).

Therefore, when $w' \in A_{i:a}(w)$ but $D_{i:a}(w) = \emptyset$ then at *w* agent *i* does not perform α , but if it did so it might have produced another outcome world *w'*.

Moreover, for every $i \in Agt$, $\alpha \in Act$ we suppose:

C2 $D_{i:a} \subseteq A_{i:a}$.

The constraint **C2** says that if w' is the *next* world of w which is reached from w through the occurrence of agent *i*'s action α , then w' must be a world which is *reachable* from w through the occurrence of agent *i*'s action α .

The next constraint C3 links the agents' choices with what they do: if a is executable and i chooses to do a then a is going to happen.

C3 if $A_{i:a}$ is defined at w and $D_{i:a}$ is defined at w' for all $w' \in C_i(w)$ then $D_{i:a}$ is defined at w.

The following semantic constraint **C4** is also about the relationship between an agent *i*'s choices (i.e., chosen worlds) and the actions performed by *i*. For every $i \in Agt$, $\alpha \in Act$ and $w \in W$, we suppose that:

C4 if $w' \in C_i(w)$ and $D_{i:a}$ is defined at w, then $D_{i:a}$ is defined at w'.

In other words, if it is not the case that *i* performs *a* in all of *i*'s chosen worlds then *i* is not going to perform *a*.

The next constraint relates worlds that are compatible with agent *i*'s beliefs and worlds that are compatible with *i*'s chosen goals: as motivated in the beginning of Section 2.1, they should not be disjoint. For every $i \in Agt$ and $w \in W$:

C5 $C_i(w) \cap B_i(w) \neq \emptyset$.

The next constraint on \mathcal{L} -frames is one of introspection w.r.t. choices. For every $i \in Agt$ and $w \in W$:

C6 if $w' \in B_i(w)$ then $C_i(w) = C_i(w')$.

The next two constraints on \mathcal{L} -frames are what is called 'no learning' and 'no forgetting' for beliefs in the literature [6]. For every $i, j \in Agt, a \in Act$ and $w \in W$:

C7 if $(w, v) \in A_{j:a} \circ B_i$ and there is *u* such that $(w, u) \in B_i \circ A_{j:a}$ then $(w, v) \in B_i \circ A_{j:a}$ **C8** if $(w, v) \in B_i \circ A_{j:a}$ and there is *u* such that $(w, u) \in A_{j:a}$ then $(w, v) \in A_{j:a} \circ B_i$, where \circ is the standard composition operator between two binary relations. Thus, we suppose that events are always uninformative, in the sense: *i should not forget* anything about the particular effects of *j*'s action *a* that starts at a given world *w*, and *i should not learn* anything new due to the occurrence of *j*'s action *a* that starts at a given world *w* (except the occurrence of that very action). In other words, what an agent *i* believes at a world *v* after the occurrence of *j*'s action *a*, only depends on what *i* believed at the previous world *w* and on the action which has occurred and which was responsible for the transition from *w* to *v*. Note that the 'no forgetting' and 'no learning' constraints rely on an additional assumption that actions are public: it is supposed that *j*'s action *a* occurs if and only if every agent is informed of this fact.

We have similar principles of no learning and no forgetting for the relations $D_{i:a}$. For every $i, j \in Agt, a \in Act$ and $w \in W$:

C9 if $(w, v) \in D_{j:a} \circ B_i$ and there is *u* such that $(w, u) \in B_i \circ A_{j:a}$ then $(w, v) \in B_i \circ D_{j:a}$; **C10** if $(w, v) \in B_i \circ D_{j:a}$ and there is *u* such that $(w, u) \in D_{j:a}$ then $(w, v) \in D_{j:a} \circ B_i$.

Models and truth conditions A *model* is a tuple $M = \langle W, A, B, C, D, V \rangle$ where the tuple $\langle W, A, B, C, D \rangle$ is a frame and $V : Atm \rightarrow 2^W$ is a valuation.

Formulas and events are interpreted according to the following clauses.

 $\begin{aligned} R_{\alpha;\beta} &= R_{\alpha} \circ R_{\beta} \\ R_{\alpha+\beta} &= R_{\alpha} \cup R_{\beta} \\ R_{\varphi?} &= \{\langle v, v \rangle \mid v \in W \text{ and } M, v \models \varphi \} \\ R_{\alpha^{*}} &= (R_{\alpha})^{*} \\ M, w \models p \text{ iff } w \in V(p) \\ M, w \models \text{Bel}_{i}\varphi \text{ iff } M, w' \models \varphi \text{ for every } w' \in B_{i}(w) \\ M, w \models \text{Ch}_{i}\varphi \text{ iff } M, w' \models \varphi \text{ for every } w' \in C_{i}(w) \\ M, w \models \text{Feasible}_{a}\varphi \text{ iff } M, w' \models \varphi \text{ for some } w' \in A_{\alpha}(w) \\ M, w \models \text{Happens}_{a}\varphi \text{ iff } M, w' \models \varphi \text{ for some } w' \in D_{\alpha}(w) \\ M, w \models F\varphi \text{ iff } M, w' \models \varphi \text{ for some } w' \text{ such that } w(\bigcup_{a \in Act} D_{a})^{*}w' \end{aligned}$

The clauses for the Boolean operators are as usual. The last clause is based on the hypothesis that time flow is determined by the actions that are performed (where the D_a and $\bigcup_{a \in Act} D_a$ are understood as relations). $\bigcup_{a \in Act} D_a(w)$ is the set of worlds w' that are in the future of w: w' can be attained from w by some D-chain, i.e. by some sequence of actions.

2.3 Some useful validities

We now state some validities of our logic that will be useful later.⁵

Proposition 1. The following formulas are valid:

⁵ We do not give a completeness result: there is such a result (albeit for a simpler language) in [14], which should be extended in order to account for complex actions; in particular the Kleene star "*" requires a fixpoint axiom and a least fixpoint axiom, which makes that the completeness proof is not straightforward.

1. After $_{\varphi?}\psi \leftrightarrow (\varphi \rightarrow \psi)$ 2. Happens $_{\varphi?}\psi \leftrightarrow (\varphi \wedge \psi)$ 3. Happens $_{\alpha;\beta}\varphi \leftrightarrow (\text{Happens}_{\alpha} \top \land \neg \text{Happens}_{\alpha} \neg \text{Happens}_{\beta}\varphi)$ 4. Happens $_{\alpha;\beta}\varphi \leftrightarrow (\varphi \land \text{Happens}_{\alpha}\varphi \lor \text{Happens}_{\beta}\varphi)$ 5. Happens $_{\alpha^*}\varphi \leftrightarrow (\varphi \land \text{Happens}_{\alpha}\text{Happens}_{\alpha^*}\varphi)$ 6. $(F \neg \varphi \land \text{After}_{\alpha^*}(\varphi \rightarrow \text{Happens}_{\alpha} \top)) \rightarrow \text{Happens}_{\text{while }\varphi \text{ do }\alpha} \top$ 7. Happens $_{\alpha}\varphi \rightarrow \text{Feasible}_{\alpha}\varphi$ 8. Feasible $_{\alpha}\varphi \rightarrow F\varphi$ 9. $(\text{Happens}_{\alpha}\varphi \land \text{After}_{\alpha}\psi) \rightarrow \text{Happens}_{\alpha}(\varphi \land \psi)$ 10. $\neg(\text{Ch}_{i}\varphi \land \text{Bel}_{i}\varphi)$ 11. $(\text{Feasible}_{i:\alpha}\varphi \land \text{Ch}_{i}\text{Happens}_{i:\alpha}\top) \rightarrow \text{Happens}_{i:\alpha}\top$ 12. $(\neg \text{Bel}_{i} \neg \text{Feasible}_{\alpha} \top \land \text{Bel}_{i}\text{After}_{\alpha}\varphi) \rightarrow \text{After}_{\alpha}\text{Bel}_{i}\varphi$

13. (Feasible_{α} \top \land After_{α}Bel_{*i*} φ) \rightarrow Bel_{*i*}After_{α} φ

14. $(\neg \text{Bel}_i \neg \text{Happens}_{\alpha} \top \land \text{Bel}_i \neg \text{Happens}_{\alpha} \neg \varphi) \rightarrow \neg \text{Happens}_{\alpha} \neg \text{Bel}_i \varphi$

15. (Happens_{α} $\top \land \neg$ Happens_{α} \neg Bel_{*i*} $\varphi) \rightarrow$ Bel_{*i*} \neg Happens_{α} $\neg \varphi$

Formula 11 is a principle of intentional action **IntAct**. The last four are principles of no forgetting (**NF**, alias perfect recall) and no learning (**NL**, alias no miracles) for beliefs. Similar principles have been studied in [8, 19, 11].

3 Trust about complex actions

We now generalize the definition of (occurrent) trust about atomic actions of [13, 14, 16] to trust about complex actions and study its constituents. Among all possible complex actions we here only consider deterministic actions [9]: actions built with "skip", "fail", ";", "if φ then α_1 else α_2 ", and "while φ do α ". Their BNF is:

 $\alpha ::= i:a \mid \text{skip} \mid \text{fail} \mid \alpha; \alpha \mid \text{if } \varphi \text{ then } \alpha \text{ else } \alpha \mid \varphi? \mid \text{while } \varphi \text{ do } \alpha$

Tests φ ? can be defined as if φ then skip else fail. In our analysis of trust in complex actions we do not consider the other program operators of PDL, viz. nondeterministic composition and iteration.

Let us first recall the definition of the original trust predicate in [13, 14, 16]. There, the goal condition Goal(i, φ) was defined as Ch_iF φ , i.e. as i's choice of futures where φ holds. The external condition CExt(j:a) was defined as Feasible_{$j:a}<math>\top$ (j:a is executable), and the internal condition CInt(j:a) as Ch_jHappens_{$j:a}<math>\top$ (j chooses that j:a is going to occur). Finally, the power condition Res($j:a, \varphi$) was defined as After_{$j:a}<math>\varphi$ (φ will hold immediately after every possible performance of j:a).</sub></sub></sub>

It turns out that our move from trust in atomic actions to trust in complex actions requires some adjustments.

3.1 Definition of trust

First of all, here is our official definition of trust in a complex action:

daf

$$Trust(i, \alpha, \varphi) \stackrel{\text{def}}{=} Goal(i, \varphi) \land Bel_i(CExt(\alpha) \land CInt(\alpha) \land Res(\alpha, \varphi))$$

where *i* is an agent, α is a deterministic action, and φ is a formula. As before, CExt and CInt stand for the external and the internal conditions in trust assessment; they will be defined in the sequel. We have thus simply replaced the atomic actions in our definition of Section 1 by complex actions.

Observe that trust in atomic actions involved a single trustee *j*. Here we have to account for trust in complex actions that may be performed by several agents; we therefore consider trust in a group of agents.

Note also that before, the trustee j —which here would be a set of agents J—appeared explicitly in the definition of the predicate Trust. However, one may consider that J is implicitly already there: it is the set of agents occurring in α . Therefore the agent argument need not appear as a separate argument in the definition.

It remains to explain the predicates on the right hand side of the definition of trust.

3.2 Defining the ingredients of trust

We now reduce the predicates on the right hand side of the definition of trust.

Goal The definition of the Goal predicate transfers straightforwardly because no action occurs in it:

$$Goal(i,\varphi) \stackrel{\text{def}}{=} Ch_i F\varphi$$

So it remains to define CExt, CInt and Res.

Result The original power condition $\text{Bel}_i\text{After}_{j:a}\varphi$ stipulated that *i* believes φ immediately results from *j*'s performance of atomic action *a*. However, consider *i*'s trust in j_1 and j_2 to perform the sequence of actions $j_1:a_1$; $j_2:a_2$ in order to achieve *i*'s goal φ . With respect to which goal should *i* trust j_1 ? The truster *i* typically does not bother about the direct effect of j_1 's action a_1 and is only interested in the overall effect φ of the complex action $j_1:a_1$; $j_2:a_2$. In other words, we have to account for the case where φ is not achieved immediately, but only at some time point in the future. We therefore redefine

$$\operatorname{\mathsf{Res}}(\alpha,\varphi) \stackrel{\operatorname{der}}{=} \operatorname{\mathsf{After}}_{\alpha} \operatorname{\mathsf{F}} \varphi$$

Under the other definitions to come, the original $\text{Trust}_0(i, j:a, \varphi)$ will be equivalent to our $\text{Trust}(i, j:a, F\varphi)$.

External and internal condition Up to now, all our definitions were directly in terms of well-defined formulas of our logic. Things are not as simple for the external condition CExt and for the internal condition CInt.

In [13, 14, 16], using axiom **IntAct** it was proved that

 $(CExt(i:a) \land CInt(i:a)) \rightarrow Happens(i:a)$

is valid. That is, if both the external condition and the internal condition for the execution of action a by agent i obtain —i.e., i is capable to perform action a and is willing (has the intention) to perform a— then i performs a. We would like to keep this principle of intentional action, and therefore need a definition of the CExt and CInt predicates validating

$(CExt(\alpha) \land CInt(\alpha)) \rightarrow Happens(\alpha)$

In particular, we will have to include a condition guaranteeing that while-loops are exited (because Happens_{while ψ do α \top implies that F $\neg \psi$).}

As to the external condition, $Cext(\alpha)$ means that the complex action α is executable whatever the other agents and nature choose to do. This means that the preconditions of α must obtain at every step of every execution of α . It follows that while $Cext(\alpha)$ implies $Feasible_{\alpha} \top$, it should not be equivalent to it. For example, the complex action (i:a+i:a'); *i*:*b* cannot be said to be executable (in the above sense) when just $Feasible_{i:a+i:a';i:b} \top$ holds. Indeed, a situation where $Feasible_{i:a'}$ After*i*:*b* \top is compatible with the latter formula, and if nature chooses *i*:*a'* when executing the nondeterministic *i*:*a*+*i*:*a'* then it cannot be said that $Feasible_{i:a+i:a':i:b} \top$ is executable.

Given these considerations we recursively define $CExt(\alpha)$ as follows:

$$\begin{array}{rcl} \mathsf{CExt}(i:a) & \stackrel{\mathrm{def}}{=} & \mathsf{Feasible}_{i:a} \top \\ \mathsf{CExt}(\mathsf{skip}) & \stackrel{\mathrm{def}}{=} & \top \\ \mathsf{CExt}(\mathsf{fail}) & \stackrel{\mathrm{def}}{=} & \bot \\ \mathsf{CExt}(\alpha;\beta) & \stackrel{\mathrm{def}}{=} & \mathsf{CExt}(\alpha) \land \mathsf{After}_{\alpha}\mathsf{CExt}(\beta) \\ \mathsf{CExt}(\mathsf{if}\,\varphi\,\mathsf{then}\,\alpha_1\,\mathsf{else}\,\alpha_2) & \stackrel{\mathrm{def}}{=} & (\varphi \land \mathsf{CExt}(\alpha_1)) \lor (\neg \varphi \land \mathsf{CExt}(\alpha_2)) \\ \mathsf{CExt}(\mathsf{while}\,\psi\,\mathsf{do}\,\alpha) & \stackrel{\mathrm{def}}{=} & \mathsf{F}\neg\psi \land \mathsf{After}_{(\psi?;\alpha)^*;\psi?}\mathsf{CExt}(\alpha) \end{array}$$

It is the clause for ";" that makes that $CExt(\alpha)$ stronger than $Feasible_{\alpha} \top$.

As to the (internal) willingness condition, it is tempting to define $CInt(\alpha)$ as $\bigwedge_{j \in Agt(\alpha)} Ch_j Happens_{\alpha} \top$,

where $Agt(\alpha)$ is the set of agent names occurring in α : every agent involved in the complex action α chooses that α happens. However, this would be too strong. Indeed, consider the scenario where $j_1:a_1$ is j_1 's action of requesting j_2 to do a_2 , and where j_2 initially prefers not to be asked by j_1 , i.e. $Ch_{j_2} \neg Happens_{j_1:a_1} \bot$, but intends to perform $j_2:a_2$ after j_1 's request. In symbols, we have a situation where $Happens_{j_1:a_1;j_2:a_2} \top$ and $\neg Ch_{j_2}Happens_{j_1:a_1;j_2:a_2} \top$ is true.

Such considerations lead to the following recursive definition of the predicate CInt.

$$\begin{array}{rcl} \operatorname{CInt}(i:a) & \stackrel{\mathrm{def}}{=} & \operatorname{Ch}_{i}\operatorname{Happens}_{i:a}\top\\ \operatorname{CInt}(\operatorname{fail}) & \stackrel{\mathrm{def}}{=} & \top\\ \operatorname{CInt}(\operatorname{skip}) & \stackrel{\mathrm{def}}{=} & \top\\ \operatorname{CInt}(\alpha;\beta) & \stackrel{\mathrm{def}}{=} & \operatorname{CInt}(\alpha) \wedge \operatorname{After}_{\alpha}\operatorname{CInt}(\beta)\\ \operatorname{CInt}(\operatorname{if}\varphi \operatorname{then} \alpha_{1} \operatorname{else} \alpha_{2}) & \stackrel{\mathrm{def}}{=} & (\varphi \wedge \operatorname{CInt}(\alpha_{1})) \lor\\ & & (\neg \varphi \wedge \operatorname{CInt}(\alpha_{2}))\\ \operatorname{CInt}(\operatorname{while} \psi \operatorname{do} \alpha) & \stackrel{\mathrm{def}}{=} & \operatorname{After}_{(\psi';\alpha)^{*};\psi'}\operatorname{CInt}(\alpha) \end{array}$$

3.3 A principle of intentional action for complex actions

We are now going to relate the predicates CExt and CInt with the modal operator Happens. We prove that when α is complex then one half of the axiom IntAct remains valid.

Proposition 2. The formula $CExt(\alpha) \rightarrow Feasible_{\alpha} \top$ is valid.

Proof. The proof is by induction on the structure of α .

As mentioned above, the other direction $\text{Feasible}_{\alpha} \top \rightarrow \text{CExt}(\alpha)$ is guaranteed to be valid only when α is atomic.

Proposition 3. The formula $(CExt(\alpha) \land CInt(\alpha)) \rightarrow Happens_{\alpha} \top$ is valid.

Proof. We use induction on the structure of α . The base cases are ensured by the axiom **IntAct** and by Proposition 1. For the induction step we have: $CExt(\alpha; \beta) \wedge CInt(\alpha; \beta)$

(by I.H.)
(by Prop. 1)

$CExt(if\psithen\alphaelse\beta)\wedgeCInt(if\psithen\alphaelse\beta)$	
$\leftrightarrow (\psi \to (CExt(\alpha) \land CInt(\alpha)) \land (\neg \psi \to (CExt(\beta) \land CInt(\beta)))$)
$\rightarrow (\psi \rightarrow \text{Happens}_{\alpha} \top) \land (\neg \psi \rightarrow \text{Happens}_{\beta} \top)$	(by I.H.)
\rightarrow Happens _{if ψ then α else β \top}	(by Prop. 1)

 $\mathsf{CExt}(\mathsf{while}\,\psi\,\mathsf{do}\,\alpha)\wedge\mathsf{CInt}(\mathsf{while}\,\psi\,\mathsf{do}\,\alpha)$

 $\begin{array}{l} \leftrightarrow \mathsf{F} \neg \psi \land \mathsf{After}_{(\psi?;\alpha)^*;\psi?}(\mathsf{CExt}(\alpha) \land \mathsf{CInt}(\alpha)) \\ \rightarrow \mathsf{F} \neg \psi \land \mathsf{After}_{(\psi?;\alpha)^*}(\psi \rightarrow \mathsf{Happens}_{\alpha} \top) \\ \rightarrow \mathsf{F} \neg \psi \land \mathsf{After}_{(\psi?;\alpha)^*}(\psi \rightarrow \mathsf{Happens}_{\psi?;\alpha} \top) \\ \rightarrow \mathsf{Happens}_{\mathsf{while}} \psi \text{ do } \alpha \top \qquad (\mathsf{by Prop. 1}) \end{array}$

As said above, the other direction of Proposition 3

 $\mathsf{Happens}_{i_1:a_1;i_2:a_2} \top \rightarrow (\mathsf{CExt}(i_1:a_1;i_2:a_2) \land \mathsf{CInt}(i_1:a_1;i_2:a_2))$

is invalid because i_1 's performance of a_1 may cause i_2 's performance of a_2 .

We finally observe that when the truster's goal is \top then trust in α amounts to the conjunction of external and internal condition.

Proposition 4. The formula $\text{Trust}(i, \alpha, \top) \leftrightarrow \text{Bel}_i(\text{CExt}(\alpha) \land \text{CInt}(\alpha))$ is valid.

4 Properties of trust

In this section we state the properties of trust in complex actions, alias workflow constructs.

First of all and as announced in Section 3.2 we observe that our and the original definition coincide for atomic actions, except that we have relaxed the result condition:

for us it suffices that the result φ obtains at some point in the future, and not immediately after the action. We therefore have $\text{Trust}(i, j:a, \varphi) \leftrightarrow \text{Trust}_0(i, j:a, F\varphi)$.

For complex actions we are going to have reductions in terms of equivalences for the cases of skip, fail, if-then-else conditionals and while loops. For trust in sequential compositions we only give a sufficient condition. We only give some of the proofs.

4.1 Atomic actions

Theorem 1. The formulas $\text{Trust}(i, \text{fail}, \varphi) \leftrightarrow \perp and$ $\text{Trust}(i, \text{skip}, \varphi) \leftrightarrow (\text{Goal}(i, \varphi) \land \text{Bel}_i F \varphi)$

are valid.

4.2 Sequential composition

Our first theorem allows to construct trust in a sequence $\alpha; \beta$ from trust in α and trust in β .

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Theorem 2. The formula

(\operatorname{Trust}(i, \alpha, \varphi) \land \operatorname{Bel}_i \operatorname{After}_\alpha \operatorname{Trust}(i, \beta, \varphi)) \to \operatorname{Trust}(i, (\alpha; \beta), \varphi)

is valid.
```

The next two theorems are about the consequences of trust in a sequence of actions.

Theorem 3. The formula

 $\operatorname{Trust}(i, (\alpha; \beta), \varphi) \to \operatorname{Trust}(i, \alpha, \varphi)$

is valid.

Proof. We have:

Our last theorem says that trust persists under the condition that the goal persists.

Theorem 4. The formula

 $\mathtt{Trust}(i,(\alpha;\beta),\varphi) \to \mathtt{After}_{\alpha}(\neg \mathtt{Goal}(i,\varphi) \lor \mathtt{Trust}(i,\beta,\varphi))$

is valid.

Proof. First, observe that

 $\operatorname{Trust}(i, (\alpha; \beta), \varphi) \rightarrow \operatorname{Bel}_i \operatorname{Feasible}_{\alpha} \top (*)$

is valid by Proposition 3 and Proposition 1. Now: $Trust(i, (\alpha; \beta), \varphi)$ $\rightarrow Bel_iAfter_{\alpha}(CExt(\beta) \land CInt(\beta) \land After_{\beta}F\varphi)$ $\rightarrow Bel_iAfter_{\alpha} \bot \lor After_{\alpha}Bel_i(CExt(\beta) \land CInt(\beta) \land After_{\beta}F\varphi) \quad (by NF of Prop. 1)$ $\rightarrow After_{\alpha}Bel_i(CExt(\beta) \land CInt(\beta) \land After_{\beta}F\varphi) \quad by (*)$

4.3 If-then-else

Theorem 5. *The formula*

$$\begin{split} \operatorname{Trust}(i, \operatorname{if} \psi \operatorname{then} \alpha \operatorname{else} \beta, \varphi) &\leftrightarrow \operatorname{Bel}_i(\ (\psi \to \operatorname{Trust}(i, \alpha, \varphi)) \wedge \\ (\neg \psi \to \operatorname{Trust}(i, \beta, \varphi)) \) \end{split}$$

is valid.

```
\begin{array}{l} Proof. \text{ We have:} \\ \textbf{Trust}(i, \text{ if } \psi \text{ then } \alpha \text{ else } \beta, \varphi) \\ \leftrightarrow \texttt{Goal}(i, \varphi) \land \\ & \texttt{Bel}_i((\psi \to \texttt{CExt}(\alpha)) \land (\neg \psi \to \texttt{CExt}(\beta))) \land \\ & \texttt{Bel}_i((\psi \to \texttt{CInt}(\alpha)) \land (\neg \psi \to \texttt{CInt}(\beta)))) \land \\ & \texttt{Bel}_i((\psi \to \texttt{After}_a F \varphi) \land (\neg \psi \to \texttt{After}_\beta F \varphi)) \\ \leftrightarrow \texttt{Bel}_i\texttt{Goal}(i, \varphi) \land \\ & \texttt{Bel}_i(\psi \to (\texttt{CExt}(\alpha) \land \texttt{CInt}(\alpha) \land \texttt{After}_\alpha F \varphi)) \land \\ & \texttt{Bel}_i(\neg \psi \to (\texttt{CExt}(\beta) \land \texttt{CInt}(\beta) \land \texttt{After}_\beta F \varphi)) \\ \leftrightarrow \texttt{Bel}_i((\psi \to \texttt{Trust}(i, \alpha, \varphi)) \land (\neg \psi \to \texttt{Trust}(i, \beta, \varphi))) \end{array}
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4.4 While

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Theorem 6. The formula

\operatorname{Trust}(i, (\operatorname{while} \psi \text{ do } \alpha), \varphi) \leftrightarrow (\operatorname{Bel}_i \operatorname{After}_{(\psi?;\alpha)^*}(\psi \to (\operatorname{CExt}(\alpha) \land \operatorname{CInt}(\alpha))) \land
```

 $Goal(i,\varphi) \land Bel_iAfter_{while \psi \text{ do } \alpha}F\varphi \land Bel_iF\neg\psi)$

is valid.

```
\begin{array}{l} \textit{Proof. We have:} \\ \texttt{Trust}(i, (\texttt{while } \psi \texttt{ do } \alpha), \varphi) \leftrightarrow \texttt{Goal}(i, \varphi) \land \texttt{Bel}_i\texttt{After}_{\texttt{while } \psi \texttt{ do } \alpha}\texttt{F}\varphi \land \\ \texttt{Bel}_i(\texttt{CExt}(\texttt{while } \psi \texttt{ do } \alpha) \land \texttt{CInt}(\texttt{while } \psi \texttt{ do } \alpha)) \\ \leftrightarrow \texttt{Goal}(i, \varphi) \land \texttt{Bel}_i\texttt{After}_{\texttt{while } \psi \texttt{ do } \alpha}\texttt{F}\varphi \land \texttt{Bel}_i\texttt{F}\neg\psi \land \\ \texttt{Bel}_i\texttt{After}_{(\psi?;\alpha)^*}(\psi \rightarrow (\texttt{CExt}(\alpha) \land \texttt{CInt}(\alpha))) \end{array}
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5 Application

Services-oriented architectures (SOA) allow to develop dynamic business processes and agile applications spanning across organisations and computing platforms to quickly adapt to ever changing requirements. By their modular nature, services can be composed to implement processes of various complexities.

Actors of SOA are divided into two rules, the client, having specific requirements, and the provider advertising its services. Non-functional parameters, such as quality of service (QoS) become important when selecting among a range of functionally equivalent services. However, in certain cases, discrepancies between advertised and observed QoS can occur, either because of temporary failures or voluntary over-rating from the provider. When facing such uncertainties, trust mechanisms should be used to select services matching the goals of the clients and providers.

Trust becomes even more crucial in composite services, where not only the client must trust the composite service but also where each provider involved in the composition must trust its partners [4]. Composite services can be modelled as a set of workflow patterns [10], which are equivalent to the complex action framework described in Section 4. Indeed, trust in a composite service depends on the services involved but also on the structure workflow. For example, a provider might agree to participate in a composite service is used at the end of a sequence, notably for data privacy concerns [3].

In the aforementioned paper, a multi-agent protocol is developed to entice providers to take part in composite web services. This protocol is centered around data privacy in composite services. Basically, and according to Theorem 4, a provider is willing to enter a composite service if and only if it trusts the providers of subsequent services to not mishandle its data. In other words the goal "not mishandle the data" only holds after its won service invocation thus fostering the need for trust.

6 Conclusion

We have presented in this work a logical formalization of trust in complex actions, and have sketched how this formalization could be useful for the formal characterization of trust in composite services, where trust in a composed service is defined in a compositional way from trust in the components of that service. Directions of future research are manifold. In the present article we only gave a semantics for a logic of complex actions. On the one hand, future works will be devoted to find a complete axiomatization of the logic of Section 2 and to study the computational properties of this logic (decidability and complexity). On the other hand, we plan to extend the PDL-based formalism of Section 2 by parallel actions in order to be able to formalize services whose components might work in parallel.

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