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Article

# Fractional-Order PI Control of DFIG-Based Tidal Stream Turbine

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**Abstract:** This study mainly investigates the current and speed control strategies of a doubly-fed induction generator (DFIG), which is applied to a tidal stream turbine (TST). Indeed, DFIG using integer-order PI (IOPI) controller has been widely proposed in the applications with a similar system, especially in wind energy conversion system (WECS). However, these conventional controllers cannot deal with the problems caused by the parameter variations satisfactorily under complex and harsh operation conditions, and may even deteriorate the performance. As a result, a fractional-order PI (FOPI) controller is considered to improve the efficiency and performance of DFIG-based TST in this paper. The FOPI controller, developed from the traditional IOPI controller and the fractional calculus theory, has a lot of prominent merits in many aspects, such as robustness, stability, and dynamic performance. In this paper, the proposed control strategies are embedded into the whole TST model which contains the tidal stream turbine, and the generator. The obtained simulation results demonstrate the prominent effectiveness and advantages of the proposed strategies compared with the conventional IOPI controller in terms of overshoot, static error, adjustment time, and robustness. It implies that FOPI controller could be a good candidate in TST applications.

Keywords: DFIG; fractional-order PI control; tidal stream turbine; robustness

#### 1. Introduction

Due to serious environmental problems caused by fossil fuels, renewable energy has become more and more attractive in recent years. As a result, renewable technologies have been improved continuously. The ocean, much larger than the land surface, is considered as an abundant energy resource which can theoretically provide five times the global energy demand [1,2]. Thus, there is increasing interest in exploiting energies from the ocean. Unfortunately, among the five mainly ocean energy forms, only marine current energy attracts the most attention owing to present technological and economic considerations.

TST is very similar to WECS. Many mature technologies used in WECS can be employed in TST partially, such as the generators and the control methods. Indeed, DFIG, which is always used in WECS, is considered as a good candidate for TST [3]. Meanwhile, IOPI controller is also proposed due to its prominent advantages, such as simple structure, good performance, and convenience to tune

the parameters. The related research results have fully demonstrated that it can achieve satisfactory effects for many objects in both theoretical analysis and actual operation. Indeed, the IOPI controller is the most mature control method with a 90% share in control systems and widely used in industrial processes such as metallurgy, chemical industry, electric power, and machinery [4]. Many researchers have adopted the IOPI controller for TST with different generators in their studies [5–19]. However, these papers mainly focused on the control strategies regarding the swell effect, flux-weakening strategy, power smoothing strategy, MPPT strategy, loss minimization strategy, dispatching and frequency strategies, etc.; and do not pay great attention to the robustness and dynamic performance of the system. All these studies hardly considered the possible variation in the system parameters due to the complicated underwater condition. Normally, an IOPI controller prefers an accurate model to tune the parameters for better performance. Although it does overcome the variation in the system parameters to a certain extent, this is at the cost of deteriorating system performance. It implies that it has poor robustness (sensitive to parameter variations and external disturbances) and it is hard to control the system with uncertainties.

Considering TST always operates under the complicated and uncertain underwater environment, accurate models of the electrical and mechanical systems are hard to obtain and the parameters may vary due to the external environment. Numerous different controllers were proposed by the researchers for the different causes; most controllers were applied in the current loop.

In [20,21] HOSMC was developed for both PMSG and DFIG, validated in the experimental bench, and compared with classical PI control. These studies mainly focused on the sensitivity of the system regarding the tidal turbulence and swell effect. Afterward, HOSMC was adopted in the five-phase PMSG based TST. This system was fully compared with three-phase PMSG-based TST under healthy mode and open-circuit faults [22,23]. The achieved results showed that the five-phase PMSG system would appear better performance than the classical three-phase PMSG system; HOSMC had superiority in terms of fault-tolerant control effectiveness compared to PI control. Furthermore, HOSMC was also selected for DSPM-based TST in [24] to deal with the nonlinear time-varying system. HOSMC indeed has very good robust characteristics due to its independence on the model; however, the characteristics of HOSMC itself introduced chattering which may degrade the system performance [25].

In [26], Gu Y.J. proposed one new fuzzy logic SMC strategy to track the maximum power point accurately and smooth the power fluctuations. MPC and backstepping control were applied to deal with the open-circuit fault in the three- and five-phase PMSG based TST [27,28]. All the results showed good performance of the system in both the transient process and steady-state, even in a faulty condition. However, these papers did not give any relative stability and robustness analyses, neither did they provide time-domain nor frequency-domain characteristics. In [29], the authors proposed NPC for hydrostatic transmission based TST. This proposed NPC could cope with the nonlinearities and uncertainties of the system and had sufficient robustness to the uncertainties and disturbances. Nevertheless, this system was hydrostatic transmission based-TST, neither direct-driven system nor gear-driven system. Yin X.Y. presented a new adaptive backstepping control with uncertainty and disturbance estimation [30]. This control was evaluated for maximum power and appeared better performance compared to the classical backstepping control. Although this paper analyzed the system robustness, it mainly focused on the external uncertainty and disturbance. Some other researchers also applied adaptive backstepping control/fuzzy control for a standalone TST which used three-phase full bridge diode rectifier [31–33]. The adaptive backstepping control was selected to regulate the duty cycle of a DC-DC boost converter to extract the maximum power.

Besides, these references mainly focused on the current loop, there are still a few papers paying attention to the speed loop. In [34], Ghefiri K, et al. developed a fuzzy gain scheduling-PI controller to improve the rotational speed performance with a variable marine tidal current speed. The obtained results showed that this control had good speed tracking performance and improved output power. In [35–37], the authors chose ADRC for TST due to the ability to estimate the entire disturbance by a nonlinear state observer and to compensate them in the control signal. All the simulation results

showed that ADRC appeared faster convergence speed, smallest overshoot, and tracking errors compared to PI and HOSMC controllers. However, this control would bring higher computational cost and time due to its complex structure and calculating process.

In the last few years, the FOPI controller, the combination of the fractional calculus theory and IOPI controller, has become increasingly attractive for control systems and applied successfully in many practical systems such as power electronic converters and hard disk drive servo systems [38,39]. The FOPI controller has one additional control dimension with the order of integral  $\lambda$  to deal with the problems such as: parameter uncertainty, external disturbance, robustness, and stability [40,41]. If the actual systems are described with their fractional properties, the nature and behavior of the object can be better revealed due to the memory and hereditary effects of fractional calculus, and the models should be more precise [42,43]. The fractional-order controller is not only suitable for the fractional-order system model, but also fully demonstrates its superiority for the integer-order system model [44,45].

Some researchers have already focused on the application of FOPI controller in the machine system [39,41,46–59]. These references mainly focused on the controller parameters tuning methods according to different criteria.

In [41,46], MATLAB optimization toolbox FMINCON was adopted to minimize the phase margin; Newton iteration method was selected to maximize the gain margin in [47]; ITAE was used as the criterion of optimal parameters tuning in [48–51]; reference [48] applied PSO to find the minimum ITAE; Dieng A. utilized PSO to optimize a special objective function which could minimize the torque ripple [52–54]; in [55], a new non-linear function containing ITSE, settling-time, rising time, and maximum overshoot was minimized by PSO and BFO. There are still a few papers studying on the robustness of internal parameter variations and external disturbances [39,56,57]. Indeed, most of these papers compared the performance of IOPI and FOPI controllers. Nevertheless, the parameters of FOPI controller obtained in these papers were all optimized in different ways; while the parameters of IOPI controller were normally achieved by the time-domain design method. Thus, the performance of FOPI controller was undoubtedly much better than that of IOPI controller. According to the literature, in [58,59], the FOPI controller parameters were developed with the same open-loop gain crossover frequency and phase margin as the IOPI controller. However, this paper mainly discussed the starting characteristics of FOPI/IOPI controllers with fractional-order and integer-order model.

In this paper, FOPI controller is applied for both current and speed loops of DFIG-based TST; the robustness of the internal and external disturbances will be analyzed; the performance will be compared systematically with that of IOPI controller; the overall system performance will also be evaluated. Consequently, this paper is organized as follows. TST is firstly introduced. The turbine, and DFIG are modeled respectively. Subsequently, the fundamental principle and design of IOPI controller are introduced briefly. Then, the FOPI controller is implemented by the phase-and-amplitude-margin method. Finally, the performance of DFIG-based TST using IOPI and FOPI controllers is realized, analyzed, and compared.

#### 2. Model of DFIG-Based TST

In order to simply the system, the only turbine and generator will be modeled. The drive train and the converter are assumed to be ideal without any losses.

#### 2.1. Tidal Stream Turbine Modeling

Like wind energy, regardless of turbine design, only a small portion of the hydrodynamic energy can be absorbed from the water. The amount of extractable mechanical power  $P_m$  is expressed by (1) [18,60].

$$P_m = \frac{1}{2} C_p \rho A V_{tide}^3 \tag{1}$$

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where the coefficient  $C_p$  highly depends on TSR/ $\lambda$ , the pitch angle  $\beta$  and the number and the geometry of the blades. The theoretical maximum  $C_p$  is 16/27 (0.59259). For TST, the maximum  $C_p$  is around in the range 0.35–0.5 [61].

Principally, the Betz's coefficient  $C_p$  is determined by the drag ('D') and lift ('L') forces on the blade. These two forces depend on many factors, such as the seawater density  $\rho$ , the resultant velocity 'W' (m/s), the attack angle ' $\alpha$ ' (rad) of the water flow, the blade chord 'chord (r)' (m), the drag and lift coefficients ' $C_D(\alpha)$ ' & ' $C_L(\alpha)$ '. The local drag and lift gradients 'dD' & 'dL' on the blade section between radius r and elementary radius (r + dr) are defined in (2). The simple explanation of the blade section is shown in Figure 1. According to this figure, the resultant velocity 'W' is defined in (3) consequently [62].

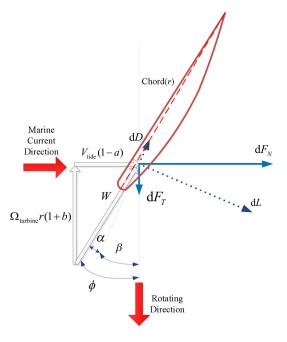


Figure 1. Blade section.

$$\begin{cases} \frac{dD}{dr} = \frac{1}{2}\rho C_D(\alpha)W^2 \text{chord}(r) \\ \frac{dL}{dr} = \frac{1}{2}\rho C_L(\alpha)W^2 \text{chord}(r) \end{cases}$$
 (2)

$$W^{2} = [V_{\text{tide}}(1-a)]^{2} + [\Omega_{\text{turbine}}r(1+b)]^{2}$$
(3)

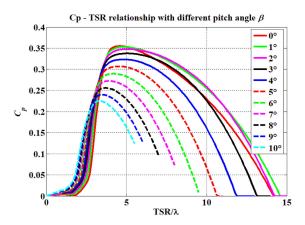
According to the blade element momentum theory, the relation between the  $C_p$  gradients and  $\lambda$  can be easily achieved in (4) [62].

$$\frac{dC_p}{dr} = \frac{\lambda (1-a)^2 \operatorname{chord}(r) N_b r C_{F_T}}{R^3 \pi \sin^2 \varphi}$$
(4)

$$\begin{cases}
C_{F_T} = C_L(\alpha)\sin(\varphi) - C_D(\alpha)\cos(\varphi) \\
C_{F_N} = C_L(\alpha)\cos(\varphi) + C_D(\alpha)\sin(\varphi)
\end{cases}$$
(5)

Based on this theory and the data from NACA0012, the  $C_p$ -TSR/ $\lambda$  variation of the studied three-blade horizontal axis turbine with different  $\beta$  is given in Figure 2. According to this figure, the power coefficient  $C_p$  reached the maximum value at 0.3553 when  $\beta$  equates to 0° and TSR ( $\lambda$ ) is 4.6.

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**Figure 2.** C<sub>p</sub>-TSR/ $\lambda$  curve with different pitch angles *β*.

#### 2.2. DFIG Modeling

For the DFIG-based TST, it has many advantages. Principally, DFIG makes the system easily operate in variable speed, lower the converter costs and power losses [61]. To control the active and reactive power without coupling, DFIG is generally defined in the synchronously d–q frame. Consequently, the model in the d–q coordinate axis of the stator is described in (6) [21,63].

$$\begin{cases}
V_{sd} = R_s i_{sd} + \frac{d}{dt} \phi_{sd} - \omega_s \phi_{sq} \\
V_{sq} = R_s i_{sq} + \frac{d}{dt} \phi_{sq} + \omega_s \phi_{sd} \\
V_{rd} = R_r i_{rd} + \frac{d}{dt} \phi_{rd} - (\omega_s - \omega_r) \phi_{rq} \\
V_{rq} = R_r i_{rq} + \frac{d}{dt} \phi_{rq} + (\omega_s - \omega_r) \phi_{rd} \\
\phi_{sd} = L_s i_{sd} + L_m i_{rd} \\
\phi_{sq} = L_s i_{sq} + L_m i_{rq} \\
\phi_{rd} = L_r i_{rd} + L_m i_{sd} \\
\phi_{rq} = L_r i_{rq} + L_m i_{sq} \\
\Gamma_{em} = \frac{3}{2} n_p L_m (i_{sq} i_{rd} - i_{rq} i_{sd}) \\
J_m \frac{d}{dt} \Omega_m = \Gamma_{em} - \Gamma_m - f_v \Omega_m \\
P_s = 1.5 (V_{sd} i_{sd} + V_{sq} i_{sq}) \\
Q_s = 1.5 (V_{sq} i_{sd} - V_{sd} i_{sq})
\end{cases}$$
(6)

According to the stator flux oriented vector control adopted in this paper, the voltage vector coinciding with the q-axis is  $90^{\circ}$  ahead of the flux vector which coincides with d-axis when the stator resistance is neglected. Therefore, the flux and voltage equations of the stator can be simplified via (7). Then, the flux and the voltage of the rotor can be rewritten in (8).

$$\begin{cases}
\phi_{sd} = \phi_s \\
\phi_{sq} = 0 \\
V_{sd} = 0 \\
V_{sq} = V_s = \omega_s \phi_{sd}
\end{cases}$$
(7)

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$$\begin{cases}
\phi_{rd} = L_{r}\sigma i_{rd} + \frac{L_{m}V_{s}}{L_{s}\omega_{s}} \\
\phi_{rq} = L_{r}\sigma i_{rq} \\
V_{rd} = R_{r}i_{rd} + L_{r}\sigma \frac{di_{rd}}{dt} - sl\omega_{s}L_{r}\sigma i_{rq} = R_{r}i_{rd} + L_{r}\sigma \frac{di_{rd}}{dt} - \omega_{sl}L_{r}\sigma i_{rq} \\
V_{rq} = R_{r}i_{rq} + L_{r}\sigma \frac{di_{rq}}{dt} + sl\omega_{s}L_{r}\sigma i_{rd} + sl\frac{L_{m}V_{s}}{L_{s}} = R_{r}i_{rq} + L_{r}\sigma \frac{di_{rq}}{dt} + \omega_{sl}L_{r}\sigma i_{rd} + sl\frac{L_{m}V_{s}}{L_{s}} \\
\sigma = 1 - \frac{L_{m}^{2}}{L_{r}L_{s}} \\
\omega_{sl} = sl\omega_{s} = \omega_{s} - \omega_{r} = \omega_{s} - n_{p}\Omega_{m} \\
\Omega_{m} = N_{\text{gear}}\Omega_{\text{turbine}}
\end{cases} \tag{8}$$

According to the equations (6), (7) and (8), the stator current equations can be easily obtained in (9). The d-axis stator flux transfer function can be rewritten in (10).

$$\begin{cases}
i_{sd} = \frac{\phi_s}{L_s} - \frac{L_m}{L_s} i_{rd} \\
i_{sq} = -\frac{L_m}{L_s} i_{rq}
\end{cases}$$
(9)

$$\phi_{sd}(s) = \frac{L_m}{\frac{L_s}{R}s + 1} i_{rd}(s) \tag{10}$$

# 3. Conventional Integer-Order PI Controller

## 3.1. Control Strategy

For DFIG-based TST, the controller of the machine side mainly aims to extract the maximum energy from marine current flow. Generally speaking, DFIG has several control strategies, such as torque-speed control strategy and power control strategy. These two strategies have a quite similar double closed-loop structure which can easily control the torque-speed/active power and reactive power respectively without coupling. Due to the intuitiveness of the torque-speed control strategy, it is proposed in this paper.

For this strategy, the turbine speed, which would extract the maximum power from the tidal current, is deduced by the optimal tip-speed ratio method. Subsequently, the rotor current reference  $i_{rq}^*$  is achieved by ASR; the rotor current reference  $i_{rd}^*$  can be obtained in (11) which is developed from the stator reactive power and stator flux equations. Then, RSC realizes the excitation control with the control signal of ACR. ASR and ACR can be either FOPI controller or IOPI controller. The processes to obtain the controllers are detailed in the following sections. The basic diagram of this control strategy is given in Figure 3.

$$i_{rd} = \frac{L_s}{L_m} \left( \frac{\phi_s}{L_s} - \frac{Q_s}{1.5\omega_s \phi_s} \right) = \frac{L_s}{L_m} \left( \frac{V_s}{\omega_s L_s} - \frac{Q_s}{1.5V_s} \right) \tag{11}$$

# 3.2. Current Loop

Based on (8), the current open-loop transfer function is represented in (12).

$$G_{e,op}(s) = \left(k_{pe} + \frac{k_{ie}}{s}\right) \frac{1}{\sigma L_r s + R_r} = \frac{\frac{k_{pe}}{\sigma L_r} s + \frac{k_{ie}}{\sigma L_r}}{s\left(s + \frac{R_r}{\sigma L_r}\right)}$$
(12)

For IOPI controller of ACR, the parameters are determined by the pole placement method in this paper [64,65]. Thus, the relative closed-loop transfer function can be later simply developed in the following (13). When the time trends to zero, the first item of the molecule will be zero. Consequently, according to the automatic control theory, the settling time  $t_{se}$  of this second-order system can be

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approximated in (14) for  $\pm 5\%$  error bandwidth [39,64,66]. Then, the parameters  $k_{pe}$  and  $k_{ie}$  are deduced in (15) subsequently [63].

$$G_{e,cl}(s) = \frac{G_{e,op}}{1 + G_{e,op}} = \frac{\frac{k_{pe}}{\sigma L_r} s + \frac{k_{ie}}{\sigma L_r}}{s^2 + \frac{R_r + k_{pe}}{\sigma L_r} s + \frac{k_{ie}}{\sigma L_r}} \approx \frac{\omega_{ne}^2}{s^2 + 2\xi \omega_{ne} s + \omega_{ne}^2}$$
(13)

$$t_{se} = \frac{3}{\xi \omega_{ne}} \tag{14}$$

$$\begin{cases} k_{pe} = \frac{6\sigma L_r}{t_{se}} - R_r \\ k_{ie} = \frac{9\sigma L_r}{\xi^2 t_{se}^2} \end{cases}$$
 (15)

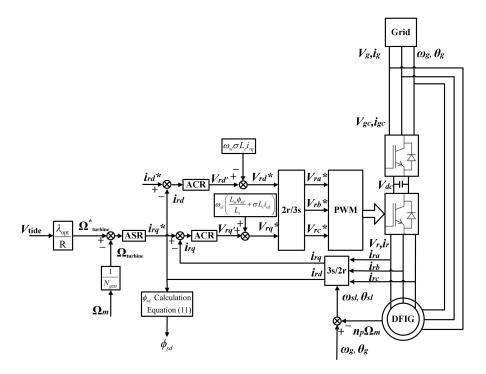


Figure 3. Diagram of torque-speed control strategy of DFIG.

# 3.3. Speed Loop

The external speed loop aims to follow the optimal speed reference for the maximum power extraction from the tidal current flow. In this section, the current loop is considered as 1 for simplification. Based on the assumption, the relative speed open and closed loops transfer functions are presented in (16) and (17) separately. Then, the controller parameters of ASR could be developed by the same method as the current loop in (18).

$$G_{m,op}(s) = \left(k_{pm} + \frac{k_{im}}{s}\right) \frac{1}{J_m s + f_v} = \frac{\frac{k_{pm}}{J_m} s + \frac{k_{im}}{J_m}}{s\left(s + \frac{f_v}{J_m}\right)}$$
(16)

$$G_{m,cl}(s) = \frac{\frac{k_{pm}}{J_m} s + \frac{k_{im}}{J_m}}{s^2 + \frac{f_v + k_{pm}}{J_{uv}} s + \frac{k_{im}}{J_{uv}}} \approx \frac{\omega_{nm}^2}{s^2 + 2\xi \omega_{nm} s + \omega_{nm}^2}$$
(17)

$$\begin{cases} k_{pm} = \frac{6J_m}{t_{syn}} - f_v \\ k_{im} = \frac{9J_m}{\xi^2 t_{syn}^2} \end{cases}$$
 (18)

#### 4. Fractional-Order PI Controller

Although the fractional calculus is quite an ancient mathematical subject, it is usually applied to develop more practical and accurate models and to improve the traditional control algorithms right now. Consequently, the researchers regard it as one powerful and effective instrument for ameliorating engineering solutions [40].

Until now, many researchers have proposed various fixed structures for the fractional-order controller, such as: different generations of CRONE controller proposed by A. Oustaloup [67], TID controller [68], FOPID controller and the fractional-order lead-lag compensator [69,70]. According to the algorithms of the different generations of the CRONE controller, FOPID controller has a strong suppression effect on high-frequency and low-frequency disturbances; that is to say, the robustness of the fractional-order controller is much better than the traditional IOPID controller [71].

# 4.1. Basic Introduction of Fractional-Order PID Controller

FOPID controller is also known as the PI $^{\lambda}$ D $^{\mu}$  controller. For this controller, the fractional-order integrator  $1/s^{\lambda}$  and differentiator  $s^{\mu}$  replace the integer-order integrator 1/s and differentiator s of IOPID controller. Thus, the relative general form is simplified in (19).  $\lambda$  and  $\mu$  are bounded between 0 and 2:  $0 < \lambda < 2$ ,  $0 < \mu < 2$  [72,73].

$$C(s) = K_p + \frac{K_i}{s^{\lambda}} + K_d s^{\mu} \tag{19}$$

The relationship between the IOPID and FOPID controllers are presented in Figure 4. If  $\lambda = \mu = 1$ , FOPID controller becomes IOPID controller. Therefore, FOPID controller can be considered as an exception of IOPID controller. When  $K_d = 0$  or  $K_i = 0$ , FOPID controller turns to be FOPI or FOPD controller. As a result, they can simply be regarded as a subclass of FOPID controller and an extension of the traditional IOPI or IOPD controller.

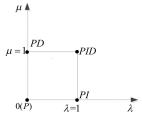


Figure 4. Range of IOPID and FOPID controllers.

From this figure, IOPID controller can only change the parameters at the four points; while for the FOPID controller, it can take the values in this quadrant. Because of these two adjustable parameters  $\lambda$  and  $\mu$ , they can highly improve the performance and robustness of the whole system. However, it undoubtedly makes the process of parameter tuning more complex [69].

Theoretically, the fractional-order system is an infinite dimension system. The conventional analysis approach of the integer-order system cannot be applied directly. Therefore, some appropriate methods are proposed by the researchers to analyze the fractional-order systems. Right now, the discretization and approximation of the rational functions of the fractional-order systems becomes one of the main methods [74]. In this paper, the Oustaloup approximation method is selected to solve the fractional-order problem [75].

#### 4.2. Design of FOPI Controller

There are many different parameter tuning algorithms for FOPID controller. At present, the mainly used methods include optimization method, dominant pole algorithm, phase-and-amplitude-margin method, etc. [45,63,76,77].

In this paper, phase-and-amplitude-margin method is applied to design this robust controller. For this method, the phase margin must be regarded as the most important criterion to obtain the relative stability of the system. If the gain crossover frequency  $\omega_c$  and the phase margin  $\gamma_c$  are determined, the controller parameters can be easily achieved according to the tuning rules. The parameter tuning process is detailed in the following steps [56–58,63,78,79].

(1) Determination of the phase-frequency characteristics at  $\omega_c$ :

$$Arg[G(j\omega_c)] = Arg[C(j\omega_c)P(j\omega_c)] = -\pi + \gamma_c$$
(20)

(2) Determination of the amplitude-frequency characteristics at  $\omega_c$ :

$$\left| G(j\omega_c) \right|_{dB} = \left| C(j\omega_c) \right| \left| P(j\omega_c) \right|_{dB} = 0 dB \tag{21}$$

(3) Robustness to the variations of the system gain:

The robust stability condition must be added to ensure the robust characteristics of the system. Thus, the phase in the open-loop Bode diagram should be flat near the gain crossover frequency  $\omega_c$ . When the gain of the system increases or decreases by 20%, the phase-to-frequency derivative in Bode diagram is 0 dB at the gain crossover frequency  $\omega_c$  and the overshoot of the dynamic response almost remains the same. To obtain such good robustness characteristics, the transfer function of the open-loop must satisfy (22).

$$\frac{\mathrm{d}(Arg[C(j\omega_c)P(j\omega_c)])}{\mathrm{d}\omega}\bigg|_{\omega=\omega_c} = 0 \tag{22}$$

Usually, the unified FOPI controller is simply described as (23). Then, the relative frequency response can be developed in the following (24).

$$C(s) = K_p \left( 1 + \frac{K_i}{s^{\lambda}} \right) \tag{23}$$

$$C(j\omega) = K_p \left( 1 + K_i \omega^{-\lambda} \cos\left(\frac{\lambda \pi}{2}\right) - jK_i \omega^{-\lambda} \sin\left(\frac{\lambda \pi}{2}\right) \right)$$
 (24)

According to the transfer functions in (12) and (16), they can be all approximated as a first-order system. The standard transfer function is given in (25).

$$P'(s) = \frac{K}{Ts+1} \tag{25}$$

where:  $T = \sigma L_r/R_r$  for the current loop and  $T = J_m/f_v$  for the speed loop.

Subsequently, the standard form of the system could be rewritten in (26) and the open-loop transfer function is presented in (27).

$$P(s) = \frac{1}{Ts+1} \tag{26}$$

$$G(s) = C(s)P(s) = K_p \left(1 + \frac{K_i}{s^{\lambda}}\right) \left(\frac{1}{Ts+1}\right)$$
(27)

According to the expressions in (25) to (27), the tuning rules in (20) to (22) could be rearranged in (28) to (30).

$$Arg[G(j\omega_c)] = -\arctan\left(\frac{K_i\omega_c^{-\lambda}\sin\frac{\lambda\pi}{2}}{1 + K_i\omega_c^{-\lambda}\cos\frac{\lambda\pi}{2}}\right) - \arctan(\omega_c T) = -\pi + \gamma_c$$
 (28)

$$\left|G(j\omega_c)\right| = \left|C(j\omega_c)\right| \left|P(j\omega_c)\right| = \frac{K_p \sqrt{\left(1 + K_i \omega_c^{-\lambda} \cos\left(\frac{\lambda \pi}{2}\right)\right)^2 + \left(K_i \omega_c^{-\lambda} \sin\left(\frac{\lambda \pi}{2}\right)\right)^2}}{\sqrt{1 + \left(\omega_c T\right)^2}} = 1$$
 (29)

$$\frac{\mathrm{d}(Arg[G(j\omega)])}{\mathrm{d}\omega}\bigg|_{\omega=\omega_c} = \frac{K_i\lambda\omega_c^{\lambda-1}\sin\left(\frac{\lambda\pi}{2}\right)}{\omega_c^{2\lambda} + 2K_i\omega_c^{\lambda}\cos\left(\frac{\lambda\pi}{2}\right) + K_i^2} - \frac{T}{1 + (T\omega_c)^2} = 0$$
 (30)

For this method, the phase margin  $\gamma_c$  and the gain crossover frequency  $\omega_c$  are required. For the sake of comparing the performance between two controllers, FOPI controller would choose the same phase margin and gain crossover frequency as IOPI controller.

Based on the open-loop transfer functions with IOPI controller for the current and speed loops in (12) and (16), the relative frequency characteristics could be achieved in (31) and (32) subsequently.

$$G_{e,op}(j\omega) = \frac{\frac{k_{pe}}{\sigma L_r}(j\omega) + \omega^2}{(j\omega)(j\omega + \frac{R_r}{\sigma L_r})},$$
(31)

$$G_{m,op}(j\omega) = \frac{\frac{k_{pm}}{J_m}(j\omega) + \omega^2}{(j\omega)\left(j\omega + \frac{f_v}{J_m}\right)},$$
(32)

According to the phase-frequency characteristic at the gain crossover frequency  $\omega_c$ , the amplitude-margins of the current and speed loops must be 0 dB:  $|G_{e,op}(j\omega_{ce})| = 1 \& |G_{m,op}(j\omega_{cm})| = 1$ . Consequently, the frequencies ( $\omega_{ce}$  and  $\omega_{cm}$ ) and the relative phases [ $\varphi(\omega_{ce})$  and  $\varphi(\omega_{cm})$ ] can be obtained by (33) to (36) respectively. Then, the phase margins ( $\gamma_{ce}$  and  $\gamma_{cm}$ ) are developed in (37) and (38) consequently.

$$\omega_{ce} = \sqrt{\frac{-\left(\frac{R_r^2}{\sigma^2 L_r^2} - \frac{k_{pe}^2}{\sigma^2 L_r^2}\right) + \sqrt{\left(\frac{R_r^2}{\sigma^2 L_r^2} - \frac{k_{pe}^2}{\sigma^2 L_r^2}\right)^2 + 4\omega_{ne}^4}}{2}}$$
(33)

$$\omega_{cm} = \sqrt{\frac{-\left(\frac{f_v^2}{J_m^2} - \frac{k_{pm}^2}{J_m^2}\right) + \sqrt{\left(\frac{f_v^2}{J_m^2} - \frac{k_{pm}^2}{J_m^2}\right)^2 + 4\omega_{nm}^4}}{2}}$$
(34)

$$\varphi(\omega_{ce}) = \arctan \frac{k_{pe}\omega_{ce}}{\sigma L_r \omega_{ne}^2} - \frac{\pi}{2} - \arctan \frac{\sigma L_r \omega_{ce}}{R_r}$$
(35)

$$\varphi(\omega_{cm}) = \arctan \frac{k_{pm}\omega_{cm}}{J_m\omega_{nm}^2} - \frac{\pi}{2} - \arctan \frac{J_m\omega_{cm}}{f_v}$$
(36)

$$\gamma_{ce} = \pi + \varphi(\omega_{ce}) = \frac{\pi}{2} + \arctan \frac{k_{pe}\omega_{ce}}{\sigma L_r \omega_{ne}^2} - \arctan \frac{\sigma L_r \omega_{ce}}{R_r}$$
(37)

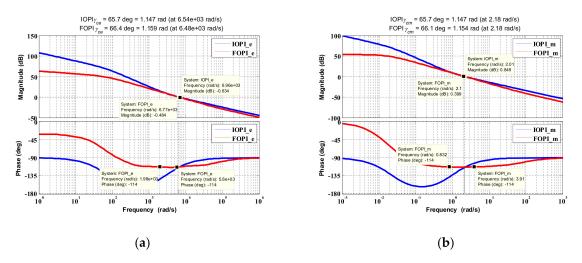
$$\gamma_{cm} = \pi + \varphi(\omega_{cm}) = \frac{\pi}{2} + \arctan \frac{k_{pm}\omega_{cm}}{J_m\omega_{nm}^2} - \arctan \frac{J_m\omega_{cm}}{f_v}$$
(38)

If the damping ratio  $\xi$  for these two loops equates to 0.707, the settling times of the current and speed loops are 0.001 s and 3 s respectively, consequently, the relative gain crossover frequencies are  $\omega_{ce} = 6536$  rad/s and  $\omega_{cm} = 2.18$  rad/s, the phase margins for the two loops are  $\gamma_{cm} = \gamma_{ce} \approx 1.147$  rad.

In order to get the fractional-order coefficient, equations (28) and (30) must be combined as a set of simultaneous equations. Then, the coefficients  $\lambda$  and  $K_i$  can be calculated. Finally, the coefficient  $K_p$  can be achieved by (29). According to this solving process, the FOPI controllers of the two loops ( $G_{fopim}$  and  $G_{fopie}$ ) can be designed in (39) and (40). Subsequently, the open-loop transfer functions could be future developed with the Oustaloup approximation algorithm. The corresponding Bode diagrams of the current and speed open-loops are shown in Figure 5. From these figures, the phases of the two systems near each gain crossover frequency  $\omega_c$  are almost the same (equal to  $-\pi + \gamma_c$ ). It means that these two FOPI controllers are well designed and they all have strong gain robustness characteristics.

$$G_{fopie}(s) = 10.4952 \left( 1 + \frac{86.1313}{s^{0.3372}} \right) \tag{39}$$

$$G_{fopim}(s) = 0.0535 \left(1 + \frac{14.94}{s^{0.299}}\right)$$
 (40)



**Figure 5.** Bode diagrams of the open–loops with two controllers: (a) current loop; (b) speed loop.

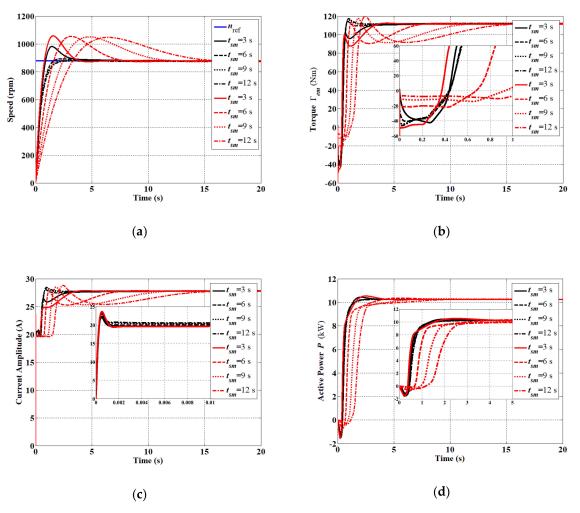
#### 5. Simulation and Comparison

To verify the proposed control method, the simulation is accomplished by MATLAB/SIMULINK in this part. The performance of the two controllers is analyzed and compared subsequently.

In this section, the settling time  $t_{se}$  of the current loop IOPI controller is fixed as 1 ms. Then, the parameters of FOPI controller are designed according to the relative phase margin  $\gamma_{ce}$  and crossover frequency  $\omega_{ce}$  of IOPI controller.

# 5.1. Comparison of the Two Controllers

This part will analyze the performance with the different settling times  $t_{sm}$  of the speed loop. According to the tuning method detailed above, the relative parameters of FOPI controller could be obtained with the gain crossover frequency and phase margin of every settling time. Consequently, the performance with IOPI and FOPI controllers for the different speed settling times  $t_{sm}$  is presented in Figure 6. All the black lines indicate the response of FOPI controller; meanwhile, the red lines imply that of IOPI controller. The different styles of lines (solid line, dashed line, dotted line, and dash-dot line) represent the different settling times.



**Figure 6.** Performance of DFIG for FOPI (black) and IOPI (red) controllers with different settling time  $t_{sm}$ : (a) DFIG speed; (b) electromagnetic torque; (c) rotor current amplitude; (d) active power.

From Figure 6a, with the different  $t_{sm}$ , FOPI and IOPI controllers can follow the reference in the given time. However, for each condition, FOPI controller always appears much quicker response compared with IOPI controller. Moreover, the overshoots of FOPI controller are much smaller than that of IOPI controller for each  $t_{sm}$ . In addition, the overshoot of FOPI controller will decrease with the increasing settling time from this figure.

Figure 6b,c shows the electromagnetic torques and rotor current amplitudes of two controllers with different  $t_{sm}$ . As the tidal current speeds are the same for these two systems, the final electromagnetic torques and rotor current amplitudes must be the same respectively. However, due to the different speed responses, the torque and current amplitude of IOPI controller will have bigger oscillations and reach their desired values in a longer time. What should be mentioned is that there is a shock in the current at the starting stage for both two controllers, while there is a shock in the torque only for IOPI controller. Indeed, this torque shock can be weakened by the increasing settling time. Nevertheless, the FOPI controller always presents smoother starting performance compared with the IOPI controller. As TST may have big rotor inertia and the inertia may increase due to the adhesion of marine fouling organisms, this characteristic can greatly avoid some mechanical faults that may occur during system start-up [80–82].

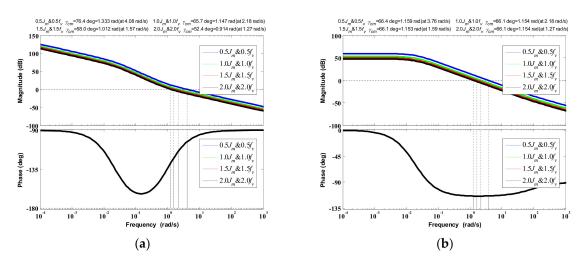
Due to the better performance of the speed and current FOPI controllers, the corresponding active power is presented in Figure 6d. From this figure, FOPI controller is always much faster than IOPI controller to reach the maximum active power.

#### 5.2. Robustness Analysis

In this section, the robustness of the speed loop is analyzed. For the speed loop, the mechanical equation contains two parameters: rotor inertia  $J_m$  and viscosity coefficient  $f_v$  and can be considered as one low-pass filter after Laplace transformation. In order to simplify the analysis, the rotor inertia and viscosity coefficient would have the same variation.

In this part, the settling time  $t_{sm}$  is fixed at 3 s. Then, the performance comparisons are presented in the following figures. The annotations in these figures imply the different rotor inertia and viscosity coefficient compared with the initial values.

Firstly, bode diagrams of the two systems with different rotor inertia and viscosity coefficient are given in Figure 7. Apparently, if the system parameters vary, the phase-and-amplitude-margin characteristics must change. Although the system gain crossover frequencies will all change with these new modified system models and the same controllers, the FOPI controller can almost keep the same phase margin as the original case. It implies that it can maintain the system stability under these conditions. While for IOPI controller, the stability will be changed with these different system parameters.

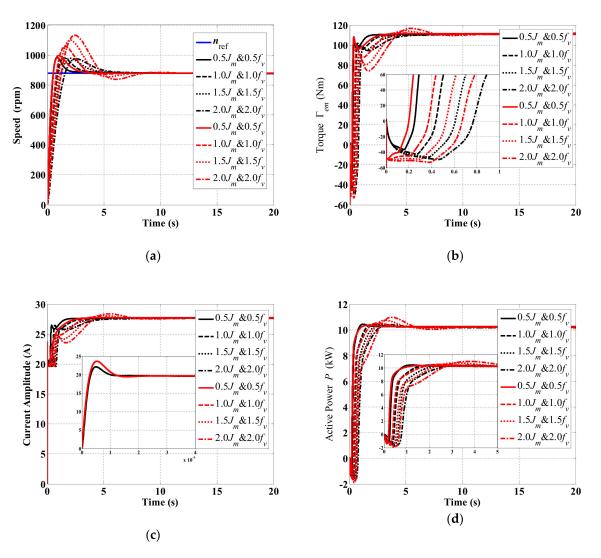


**Figure 7.** Bode diagrams of the speed open-loop with inaccurate mechanical model: (a) IOPI controller; (b) FOPI controller.

The speed responses of the two controllers are shown in Figure 8a. Absolutely, the speed performance of the two systems varies with the different rotor inertia  $J_m$  and viscosity coefficient  $f_v$ . In general, the speed rising times of the two controllers will all rise with the increasing  $J_m$  and  $f_v$ . The difference is that the rising times of FOPI controller are always relative smaller than that of IOPI controller. Significantly, the speed overshoots of the FOPI controller will remain almost the same. This phenomenon just verifies the robustness to the variations of the system gain which has already been mentioned in the tuning process. For the IOPI controller, its overshoot will grow with the increasing rotor inertia and viscosity coefficient.

Figure 8b,c indicates the electromagnetic torque and rotor current amplitude. From these two figures, there is always a shock for IOPI controller at the beginning. Meanwhile, its oscillations will be bigger with the bigger rotor inertia  $J_m$  and viscosity coefficient  $f_v$ . While for the active power in Figure 8d, these two controllers have similar performance during the start-up. However, the IOPI controller will bring a slight fluctuation. Its value will increase with the raising  $J_m$  and  $f_v$ , and can reach nearly 10% when  $J_m$  and  $f_v$  are twice the original values.

Consequently, from these figures, the FOPI controller can ensure the robustness to parameter variations and system uncertainties. All the simulation results also demonstrate that the FOPI controller always appears much better performance compared with the IOPI controller under these conditions.

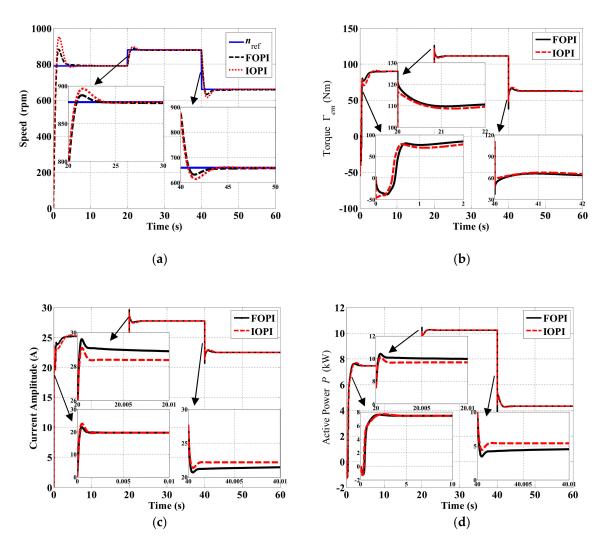


**Figure 8.** Performance of DFIG for FOPI (black) and IOPI (red) controllers with the inaccurate mechanical model: (a) DFIG speed; (b) electromagnetic torque; (c) rotor current amplitude; (d) active power.

# 5.3. Performance Analysis with the Tidal Current Variation

The marine tidal current speed could be regarded as constant in a short time. However, because of the turbulence and swell effects, the speed is always changing. In this part, the performance analysis and comparison of two controllers will be presented considering varying tidal current speeds.

Firstly, the tidal current speed is considered to have step changes. In the simulation, the marine tidal current speed is 1.8 m/s at the beginning, rises to 2 m/s at 20 s, and then decreases to 1.5 m/s at 40 s. As the two systems are analyzed based on the same condition and parameters, the final values of the rotor current amplitude, torque, and active power must be the same. The relative mechanical speeds with the two controllers are shown in Figure 9a. According to this figure, the overshoot of the FOPI controller is always much smaller than that of the IOPI controller. From Figure 9b–d, when the marine tidal current speed changes suddenly, the torque, current amplitude, and active power will be different in the transient process due to the different responses of the controllers. Moreover, the relative oscillations and the current overshoot will be a little smaller if FOPI controller is employed.



**Figure 9.** Performance of DFIG for FOPI and IOPI controllers with variable marine tidal current speed: (a) DFIG speed; (b) electromagnetic torque; (c) rotor current amplitude; (d) active power.

Secondly, the swell effect is applied to simulate the continual variable speed. Indeed, the swell effect is the most important perturbation to vary the flow speed [19]. According to the literature, the simple first-order Stokes model is selected and shown in (41). In order to get this swell effect, some parameters must be obtained beforehand. In this section, the JONSWAP spectrum is adopted because of its sharp peak characteristic which is given in (42). Then, the amplitude of each frequency component  $a_i$  can be calculated in (43). The other important parameter, each swell length  $L_i$ , can be achieved by the sea wave dispersion relation in (44) [7,8,19]. If the average marine current is 2 m/s, the total speed including the swell effect is shown in Figure 10 as an example. As can be seen from this figure, if the swell effect is considered, the marine tidal current speed will vary within a certain range continuously.

$$V_{\text{swell}}(t) = \sum_{i} \frac{2\pi a_{i}}{T_{i}} \frac{\cosh\left(2\pi \frac{z + depth}{L_{i}}\right)}{\sinh\left(2\pi \frac{depth}{L_{i}}\right)} \cos 2\pi \left(\frac{t}{T_{i}} - \frac{x}{L_{i}} + \varphi_{i}\right) \tag{41}$$

$$S(f) = \frac{k_J g^2}{(2\pi)^4 f^5} \exp\left[-\frac{5}{4} \left(\frac{f_m}{f}\right)^4\right] \gamma^{\alpha}$$
(42)

$$a_i = \sqrt{2S(f_i)\Delta f} \tag{43}$$

$$L_{i} = \frac{gT_{i}^{2}}{2\pi} \tanh\left(2\pi \frac{depth}{L_{i}}\right) \tag{44}$$

where:

$$\gamma = 3.3$$

$$k_{J} = \frac{0.076}{x^{0.22}} = 0.076 \left(\frac{gL_{F}}{V_{wind}^{2}}\right)^{-0.22}$$

$$\alpha = \exp\left[-\frac{(f - f_{m})^{2}}{2\sigma^{2}f_{m}^{2}}\right] \text{ with } \sigma = \begin{cases} 0.07f \le f_{m} \\ 0.09f > f_{m} \end{cases}$$

$$f_{m} = 3.5 \left(\frac{gL_{F}}{V_{wind}^{2}}\right)^{-0.33}$$

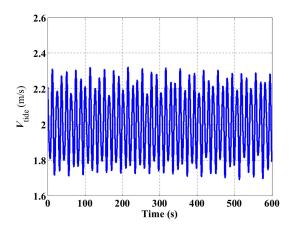
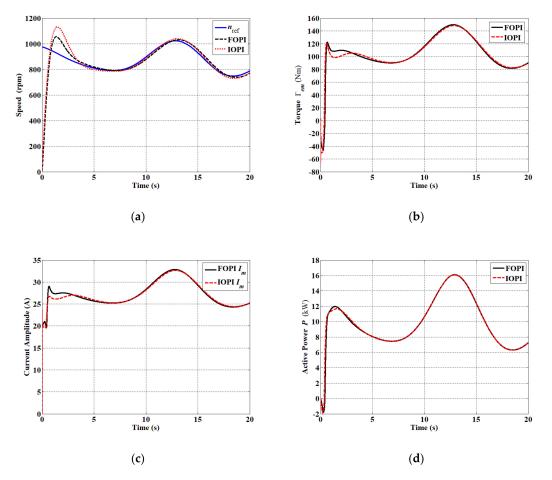


Figure 10. Marine tidal current speed regarding swell effect.

In this part, the system will be simulated only 20 s for simplification. The mechanical settling time is also equal to 3 s as before. The system performance is presented in Figure 11. If the marine current speed varies continuously, both FOPI and IOPI controllers cannot track the speed reference perfectly due to the limitation of PI controller and always have a static error. However, FOPI controller has better starting characteristics compared to IOPI controller in the speed (see in Figure 11). For the torque, current amplitude and active power, two controllers have similar response characteristics except for the start-up process. IOPI controller will have a little bigger fluctuation during the transient process.

Overall, all the analysis in this section only demonstrates the good starting performance of FOPI controller with the variable tidal speed. Nevertheless, it cannot prove its good characteristics during the steady-state process. Furthermore, the IOPI controller seems to have a bigger step pulse when the reference changes suddenly. Considering the possible strong current speed variations/disturbances, it is very important to ensure the TST to have smoother reactions. From this point of view, FOPI controller's low overshoot characteristic can be advantageous in TST applications.

It should also be noted that all the research in this section is based on the precise model of the system and a shorter settling time. According to the analysis in the previous two sections, the FOPI controller has already demonstrated its prominent advantage in the aspects of different settling time and robustness. Therefore, it is reasonable to believe that if the system model is inaccurate and the marine tidal current has a big variation, the FOPI controller must have better performance compared to the IOPI controller.



**Figure 11.** Performance of DFIG for FOPI and IOPI controllers with swell effect: (a) DFIG speed; (b) electromagnetic torque; (c) rotor current amplitude; (d) active power.

#### 6. Conclusions

This paper compares the conventional IOPI and proposed FOPI controllers in a DFIG-based TST. The obtained simulation results are very interesting. They show that the FOPI controller can obtain desired results and present better performance than IOPI controller in the FOC control strategy. (1) The FOPI controller will get smaller overshoot and static error, less adjustment time, and better robustness with variable marine current speed and uncertain system parameters. (2) The FOPI controller can significantly improve the start-up performance and make the system into steady-state without a big impact.

From the system simulation, the FOPI controller demonstrates high effectiveness in terms of speed tracking and current regulation. It implies that the FOPI controller could be a very good candidate in TST applications for the normal operation condition even the system model is inaccurate due to the complex working environment. In the future, a system in faulty condition using a FOPI controller will be studied because of its prominent advantage in the overshoot and robustness.

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#### Nomenclature

TST Tidal Stream Turbine

WECS Wind Energy Conversion System

 $egin{array}{ll} \hbox{IOPI} & \hbox{Integer-Order PI} \\ \hbox{FOPI} & \hbox{Fractional-Order PI} \\ \hbox{TSR} & \hbox{Tip Speed Ratio/} \lambda \\ \end{array}$ 

PMSG Permanent Magnet Synchronous Generator

DFIG Doubly-Fed Induction Generator

DSPM Doubly Salient Permanent Magnet machine

SMC Sliding Mode Control

HOSMC High-Order Slide Mode Control
MPC Model Predictive Control
NPC Nonlinear Predictive Control

ADRC Active Disturbance Rejection Control

ITAE Integral of Time multiplied by Absolute Error

PSO Particle Swarm Optimization

ITSE Integral of the Time multiplied Square Error

BFO Bacterial Foraging Optimization
ASR Automatic Speed Regulator
RSC Rotor-Side Converter

ACR Automatic Current Regulator

CRONE Commande Robuste d'Ordre Non Entier

TID Tilt-Integral Derivative FOPID Fractional-Order PID

ρ Seawater density (1024 kg/m<sup>3</sup>)

*C<sub>p</sub>* Power coefficient, also called Betz's coefficient

λ Tip Speed Ratio (TSR)

 $\Omega_{
m turbine}$ ,  $\Omega_m$  Mechanical speed of the turbine/DFIG (rad/s) a, b Axial and tangential flow induction factors

 $dF_N$ ,  $dF_T$  Axial and tangential components of the blade element hydrodynamic forces (N)

R, R Radius of the turbine (m), the resistance ( $\Omega$ )

 $N_b$  Number of the blades s, r Stator/rotor index

*d*, *q* Synchronous reference frame index

V, i,  $\varphi$ ,  $\omega$  Voltage (V), current (A), flux (Wb) and electrical speed (rad/s)

sl Slip

 $\omega_{sl}$  Rotor current speed (rad/s)

 $L_s$ ,  $L_r$ ,  $L_m$  Self inductances of the stator and rotor, and mutual inductances (H, H, H)

 $\Gamma_{em}$  Electromagnetic torque (Nm)  $n_p$  Number of the pole pair

 $J_m$  Inertia (kg\*m²)  $f_v$  Viscosity coefficient

 $P_{s}$ ,  $Q_{s}$  Stator active and reactive powers (W, VAR)

 $N_{\rm gear}$  Ratio of the gearbox  $V_s$  Voltage amplitude (V)  $\xi$  Damping ratio

e, m electrical/mechanical index  $t_s$  Settling time of the closed-loop (s)

 $k_p$ ,  $k_i$  Proportional and integral coefficients

 $\omega_c$ ,  $\gamma_c$  Gain crossover frequency and the phase margin for the open-loop (rad/s, rad)

 $K_p$ ,  $K_i$ ,  $K_d$  Proportional, integral and differential constants

 $\lambda$  and  $\mu$  Integral and differential orders

K Amplification coefficient which can be integrated into the proportional coefficient  $K_p$ 

*T* Time constant

Peak enhancement factor which indicates the ratio of the maximal spectral energy to the

maximum of the corresponding Pierson-Moskowitz spectrum

 $L_{\rm F}$  Fetch length (m)  $V_{\rm wind}$  Wind speed (m/s)

g Acceleration of gravity (m/s<sup>2</sup>)

f, f<sub>m</sub> Wave frequency and the frequency at the maximum of the spectrum (Hz, Hz)

 $k_I$  Usual Phillips constant

 $T_i$  Swell period of each component (s)

 $\varphi_i$  Initial phase of each term which is given randomly (rad)

depth Sea depth (m)

x, z Horizontal and vertical point for the calculation (m)

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