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Explicit formulations of adhesive wear extension in fretting interfaces applying the contact oxygenation concept

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Abstract

Adhesive wear extension in metal fretting contacts was previously related to the partial pressure of oxygen gas in a porous third body layer. Below a threshold value, the surface oxidation is no more possible and adhesive wear prevails in the inner part of the interface. The contact oxygenation concept (COC) allowing the prediction of the dioxygen partial pressure profile was recently simulated for a 2D surface analysis (i.e. 3D contact) using a numerical Advection-Dispersion-Reaction (ADR) approach. In this study, a simple explicit formulation is derived to capture COC response using a 1D surface analysis (i.e. 2D contact hypothesis).

Keywords: Abrasive-adhesive fretting wear; Long-flat contacts; Contact oxygenation concept (COC); Advection-Dispersion-Reaction model (ADR).

1. Introduction

Fretting takes place in contact surfaces undergoing micro-displacement oscillatory movements where most of the interface is hidden from the outer environment [1,2]. When relatively large displacement amplitudes are applied, gross slip fretting takes place inducing wear through the formation and expulsion of debris particles.

Several wear mechanisms can be activated during fretting including fatigue, abrasion, adhesion, corrosion, etc. [3]. Adhesion is one of the most drastic aspects of wear as it causes local overstresses triggering nucleation and propagation of incipient fretting cracks in addition to micro-welding process [4].

The extension of adhesive wear in a fretting interface can be illustrated considering the contact oxygenation concept (COC) [5–10]. This latter describes the interfacial oxygen flow such that adhesion prevails in the middle of the interface whenever the oxygen partial pressure (P_{O_2}) falls below a threshold value ($P_{O_2,th}$), otherwise, in the lateral sides, abrasive-oxidational wear is observed (Fig.1). This lateral abrasion zone can be assessed using the “oxygen distance d_o ” parameter [11] which is the distance from the contact edges to the boundaries of adhesion domain (Fig. 1).

Oxygen transport within the interface was recently simulated using an advection-dispersion-reaction approach (ADR) [12] such that the debris bed is considered a porous medium crossed by atmospheric gases namely oxygen and nitrogen. These gases interact with the freshly exposed metal through the friction power dissipated at the interface (Fig. 1) which is formalized through the Archard power density factor $\omega^*=p.v$ (with p being the contact pressure and v being the sliding speed). For such 2D surface analysis (i.e. 3D contact), complex finite difference procedures are required. However, assuming the same hypothesis, it was shown in [13] that this complete model can be reduced to an explicit analytical solution based on Bessel functions for axisymmetric circular interfaces. In this work, it can be shown that ADR model can be further reduced to a simple exponential function for 1D linear contact equivalent for instance to a long

flat contact configuration. This simple closed form of COC is compared with complete 2D simulations and discussed regarding dedicated experiments.

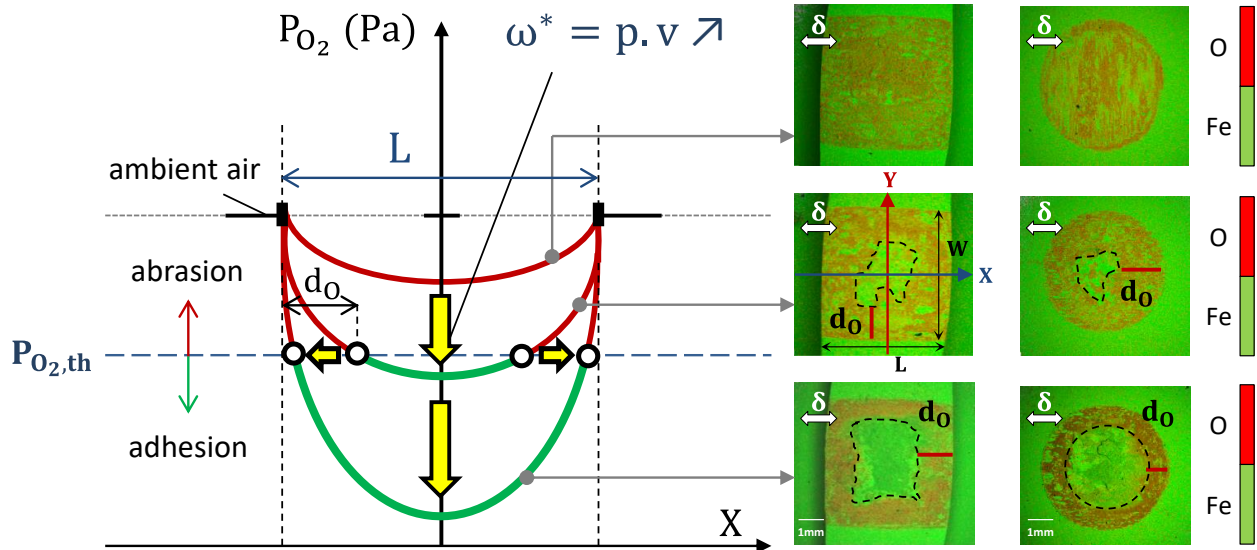


Fig.1. Illustration of the contact oxygenation concept (COC) showing the transition from pure abrasive to a mixed abrasive-adhesive wear and application of the latter on flat circular [13] and square [12] shaped fretting interfaces as reflected by the EDX maps.

2. Description of the ADR approach

ADR approach, being thoroughly illustrated in [12,13], is concisely recapped in this section. This model consists in obtaining the oxygen partial pressure profile within the interface by establishing a balance between the advective and dispersive transport of O_2 from the ambient air within the porous debris layer and the reaction process (i.e. the consumption rate of the available O_2 molecules with the freshly exposed metal surface by friction). The ADR continuity equation of a gas component "i" ($i=O_2$ or N_2) is shown in Eq. 1.

$$a \frac{dP_i}{dt} = -\nabla \cdot (J_i) + R_i = -\nabla \cdot (J_{a,i} + J_{d,i}) + R_i = -\nabla \cdot (-D_i \nabla P_i + v P_i) + R_i \quad (1)$$

Where P_i is the gas partial pressure, J_i the general molar flux, $J_{a,i}$ the advective flux, $J_{d,i}$ the dispersive flux, R_i the reaction rate, a the debris bed porosity, D_i the dispersion coefficient, and v the gas-mixture advection velocity in the porous debris bed. These latter parameters are computed applying the models and equations which are completely detailed in Ref. [12].

The current study neglects the metal reaction with nitrogen gas (i.e. $R_{N_2} \approx 0$) despite the observation of nitriding process in some fretting contacts as titanium alloys [6,14]. In contrary, oxygen gas interacts with the metal surface such that the reaction rate (R_{O_2}) is represented as a first-order decay rate of O_2 (Eq. 2) which is consumed due to the oxidation of the metal surface exposed by friction process represented by the oxidation rate coefficient r_{O_2} .

$$R_{O_2} = -r_{O_2} \times P_{O_2} \quad (2)$$

r_{O_2} is estimated using a simple empirical phenomenological expression considering the Archard power density factor ω^* which is equal to the “p.v” factor.

$$r_{O_2} = \beta \left(\frac{\omega^*}{\omega_{ref}^*} \right)^Y \text{ with } \omega^* = p \times v = 4 \cdot p \cdot \delta_g \cdot f \quad (3)$$

This model was applied to investigate the adhesive wear extension for a low-alloyed (34NiCrMo16) flat-on-flat interface [12]. One interest of this flat-on-flat contact configuration is the possibility to maintain a constant contact area and contact pressure

during wear process. The reaction rate parameters (Eq. 3) were calibrated in [12] leading to $\beta=394.63$ and $\gamma=0.47$ [12]. ω_{ref}^* is the Archard power density factor at the reference conditions defined in [12] having a sliding amplitude $\delta_g=\pm 100 \mu\text{m}$, mean contact pressure $p=100 \text{ MPa}$, and a sliding frequency $f=1 \text{ Hz}$ (with a square contact area $A=5 \times 5=25 \text{ mm}^2$ and a test duration=20000 fretting cycles) such that $\omega_{ref}=0.04 \text{ W/mm}^2$. Very nice predictions of the partition between adhesive and abrasive wear domains were achieved taking into account the effect of frequency, contact pressure and contact size. However, 2D surface analysis requires complete numerical simulations which do not permit an explicit correlation between the loading and debris bed parameters and the evolution of O_2 partial pressure profile. Recently [13], assuming a steady state condition of the ADR where the effect of both the nitrogen gas and the advection process are neglected, it was shown that for a flat asymmetrical circular interface of an external radius R , ADR equation can be solved analytically such that the di-oxygen partial pressure versus the radial distance “ r ” ($R_0 < r < R$) can be evaluated using the following simple analytical expression:

$$P_{\text{O}_2}(r) = A \times I_0(\eta r) + B \times K_0(\eta r) \quad (4)$$

$$I_0(\eta r) = \sum_{n=0}^{\infty} \frac{1}{(n!)^2} \left(\frac{1}{2} \eta r\right)^{2n} \quad (5)$$

$$K_0(\eta r) = \int_0^{\infty} \cos(\eta r \sinh(t)) dt = \int_0^{\infty} \frac{1}{\sqrt{t^2 + 1}} \cos(\eta r t) dt \quad (6)$$

$$A = \frac{K_1(\eta R_0) \times P_{\text{O}_2}(R)}{I_1(\eta R_0)K_0(\eta R) + I_0(\eta R)K_1(\eta R_0)} \quad (7)$$

$$B = \frac{I_1(\eta R_0) \times P_{\text{O}_2}(R)}{I_1(\eta R_0)K_0(\eta R) + I_0(\eta R)K_1(\eta R_0)} \quad (8)$$

$$\text{where } \eta = \sqrt{\frac{r_{O_2}}{D_{\text{diffusion}, O_2}}}$$

Due to the singularity existing at $r = R_0 \rightarrow 0$ as detailed in [15], the solution can be further simplified to:

$$P_{O_2}(r) = \frac{I_0(\eta r)}{I_0(\eta R)} \times P_{O_2}(R) \quad (9)$$

$$I_0(\eta r) = \sum_{n=0}^{\infty} \frac{1}{(n!)^2} \left(\frac{1}{2} \eta r\right)^{2n} \quad \text{and } \eta = \sqrt{\frac{r_{O_2}}{D_{\text{diffusion}, O_2}}} \quad (10)$$

This analytical solution depends mainly on the reaction rate coefficient “ r_{O_2} ” and the effective diffusion coefficient “ $D_{\text{diffusion}, O_2}$ ” of oxygen gas in the porous debris bed. A parametric analysis comparing the analytical solution versus the complete numerical simulations confirm the stability of the proposal. Deepening this approach, it will be demonstrated that a simpler expression of O_2 partial pressure can be derived for 1D surface configuration (i.e. 2D flat contact). This 1D surface will be approximated experimentally to a flat geometry having a long “Y” transverse width (W) compared to a collinear “X” contact length (L). A similar 34NiCrMo16 interface will be considered so that the same calibration parameters can be applied to simulate the experiments (i.e. $\beta=394.63$ and $\gamma=0.47$) as detailed in [12]. Additionally, the threshold oxygen partial pressure “ $P_{O_2,th}$ ” and the debris bed porosity will be assumed equal to 0.1 Pa and 0.48 respectively for the same assumptions discussed in [12].

3. One dimensional analytical solution of the ADR approach

Cartesian ADR continuity equation was solved numerically in [12] leading to a good description of the adhesive wear extension. However, in order to explicitly understand the role of the debris bed parameters and the oxidation reaction coefficient on the partition of abrasive and adhesive wear, numerical solution is not sufficient and an analytical solution is requested. Nonetheless, deriving the analytical solution is not straightforward and requires many simplifications of the highly-coupled parameters in the ADR equation. Thus, the following assumptions are suggested:

-The analytical solution will be estimated at steady state, hence:

$$\frac{dP_{O_2}}{dt} = 0 \Rightarrow -\nabla \cdot (-D_{O_2} \nabla P_{O_2} + vP_{O_2}) + R_{O_2} = 0 \quad (11)$$

-One dimensional contact is assumed such that the dispersion, advection and reaction coefficients are supposed to be constant (i.e. $D_{O_2}=\text{constant}$, $v=\text{constant}$, $r_{O_2}=\text{constant}$):

$$D_{O_2} \nabla^2 P_{O_2} - v \nabla P_{O_2} - r_{O_2} P_{O_2} = 0 \Rightarrow D_{O_2} \frac{d^2 P_{O_2}}{dx^2} - v \frac{dP_{O_2}}{dx} - r_{O_2} P_{O_2} = 0 \quad (12)$$

Eq. 12 is a second order ordinary differential equation whose solution is as follows (A & B are constants):

$$P_{O_2}(x) = A \times \exp \left\{ \left(\frac{v}{2D_{O_2}} - \sqrt{\left(\frac{v}{2D_{O_2}} \right)^2 + \frac{r_{O_2}}{D_{O_2}}} \right) x \right\} + B \times \exp \left\{ \left(\frac{v}{2D_{O_2}} + \sqrt{\left(\frac{v}{2D_{O_2}} \right)^2 + \frac{r_{O_2}}{D_{O_2}}} \right) x \right\} \quad (13)$$

In order to further simplify the above analytical solution and reduce the number of parameters in the model, the relative importance of advection to diffusion is estimated.

This can be done using Peclet number "Pe" which is the ratio of the time necessary for

the gas molecules to traverse a characteristic length L by advection and the time required to travel the same length by diffusion (Eq. 14) [16]. The characteristic length L represents the distance the gas molecules can travel which is equal to the contact size and $D_{\text{diffusion}, O_2}$ is the effective diffusion coefficient of O_2 . Based on this, oxygen gas flow will be diffusion-controlled if $Pe < 1$ [16].

$$Pe = \frac{|v|L}{D_{\text{diffusion}, O_2}} \quad (14)$$

Former study [13] linked to this work involving fretting tests of 34NiCrMo16 circular flat-on-flat contact revealed that the average Peclet number “ Pe ” does not exceed one for a wide range of fretting loadings investigated within the same study. Besides, varying the advection speed by several orders of magnitude by changing the debris bed intrinsic permeability and particle size had no significant effect on the oxygen distance parameter and adhesive wear extension as shown in [12]. Hence, keeping the same parameters in this study, it can be suggested that the relative importance of oxygen gas advection to diffusion is weak implying a negligible advection speed ($v \approx 0$). Doing so, the analytical solution can be simplified to this very simple exponential function expressing the O_2 partial pressure profile as a function of the axial position “ x ”:

$$P_{O_2}(x) = A \times \exp\left(-\sqrt{\frac{r_{O_2}}{D_{O_2}}}x\right) + B \times \exp\left(\sqrt{\frac{r_{O_2}}{D_{O_2}}}x\right) \quad (15)$$

In the absence of advection, the dispersion coefficient D_{O_2} will be equal to the effective molecular diffusion $D_{\text{diffusion}, O_2}$ of the gas component which is the random spreading of the gas molecules due to concentration gradients. $D_{\text{diffusion}, O_2}$ is equal to the product of the oxygen gas diffusion coefficient “ $D_{O_2,m}$ ” in a homogeneous mixture of gases and the

tortuosity “ τ ” which depicts the diminution of the effective diffusion coefficient caused by the solid-phase that reduces the cross-sectional area available for diffusion. These parameters are estimated previously in [12,13]. The tortuosity “ τ ” is expressed empirically as a function of the debris bed porosity “ a ” considering Moldrup et al. model [17] (Eq. 16).

$$D_{O_2} = D_{\text{diffusion},O_2} = \tau D_{O_2,m} = 0.66 \times a \times D_{O_2,m} \quad (16)$$

The constants “A” and “B” (Eq. 17 & 18) are estimated assuming the oxygen partial at the borders equal to the oxygen partial pressure in the ambient air (i.e. $P_{O_2(\text{atm})} = 21278.25 \text{ Pa}$).

$$A = \frac{1 - \exp\left(\sqrt{\frac{r_{O_2}}{D_{O_2}}} L\right)}{\exp\left(-\sqrt{\frac{r_{O_2}}{D_{O_2}}} L\right) - \exp\left(\sqrt{\frac{r_{O_2}}{D_{O_2}}} L\right)} \times P_{O_2(\text{atm})} \quad (17)$$

$$B = \frac{\exp\left(-\sqrt{\frac{r_{O_2}}{D_{O_2}}} L\right) - 1}{\exp\left(-\sqrt{\frac{r_{O_2}}{D_{O_2}}} L\right) - \exp\left(\sqrt{\frac{r_{O_2}}{D_{O_2}}} L\right)} \times P_{O_2(\text{atm})} \quad (18)$$

4. Comparison between 1D analytical and 2D numerical solutions of the ADR

As detailed previously, the 1D description of the ADR model is only valid comparing the P_{O_2} profile along the median “X” axis (i.e. L contact length) applied for large W/L ratios so that the ADR process generated along the transverse side can be neglected. To illustrate the W/L ratio effect, $P_{O_2}(x)$ profiles are compared in Fig. 2 for two contact geometries W/L=1 and W/L=4 (fixing L at 5 mm). The graphs compare the complete 2D model considering advection process, the 2D model without advection and the 1D

approximation which neglects both the transverse ADR contribution and the advection effect. A first global overview of the log scale graphs reveals a very good prediction provided by the 1D analytical solution. However, a deeper analysis of the oxygen partial pressure for $W/L=1$ condition underlines a scattering regarding the minimum P_{O_2} value at the contact center. Note that this difference is mainly due to the 1D hypothesis (i.e. transverse ADR contribution) such that 2D P_{O_2} profiles with and without advection are very close. However, if we consider the prediction of the oxygen distance “ d_o ” when $P_{O_2} < P_{O_2,th}=0.1$ Pa, the error is clearly smaller. This suggests that even for the limit condition $L=W$, the 1D approximation provides a very good estimation of the partition between adhesive and abrasive wear domains at least for the studied contact.

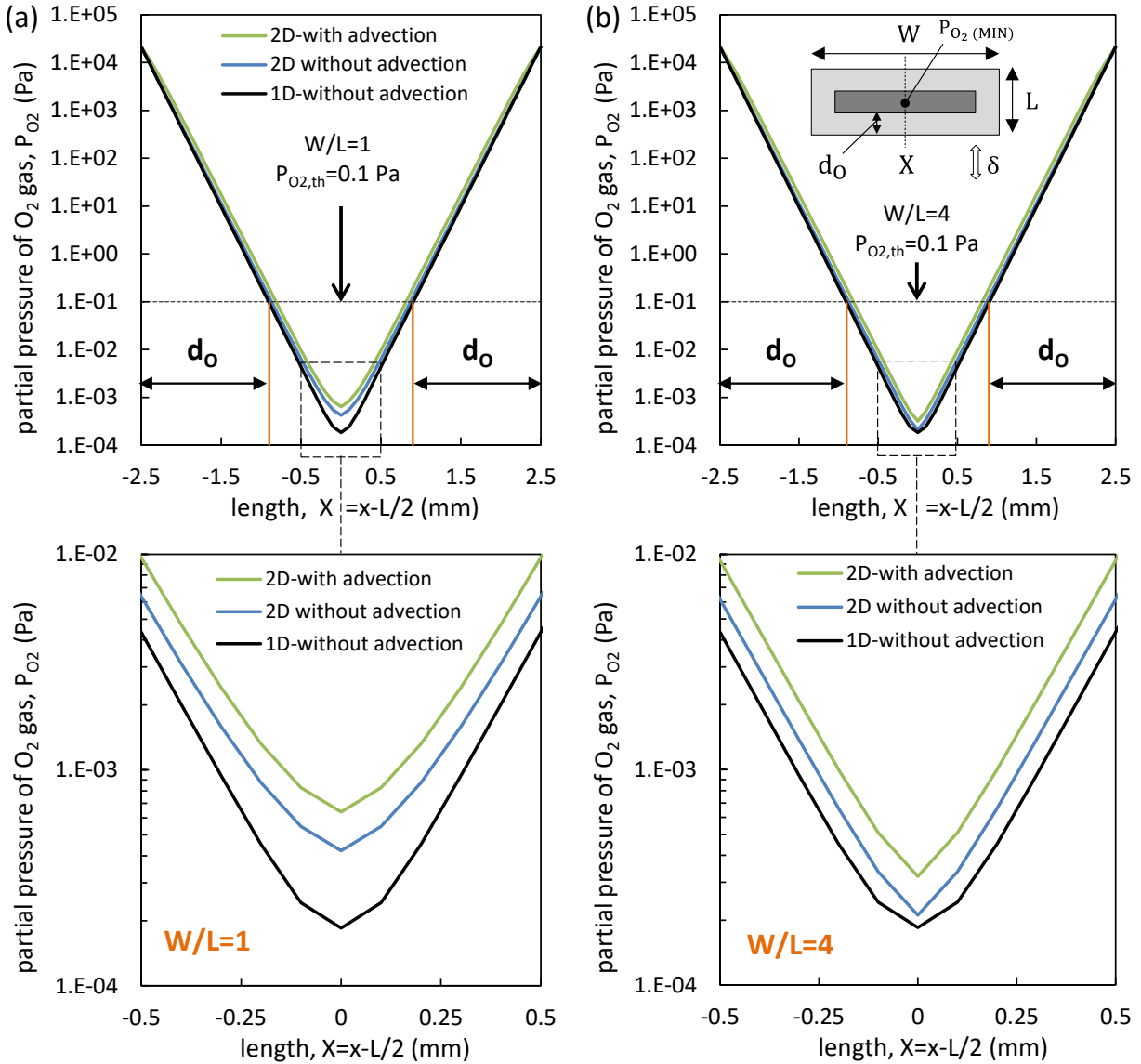


Fig.2. (a) Evolution of the P_{O_2} profiles along the X median axis for $W/L=1$; (b) evolution of the P_{O_2} profiles along the X median axis for $W/L=4$ and $L=5$ mm ($p=100$ MPa, $\delta_g=\pm 100$ μ m, and $f=1$ Hz corresponding to the reference condition in [12,13]).

This comparison of the P_{O_2} profiles given for $W/L=4$ (with $L=5$ mm) confirms a smaller scattering even for the central part of the contact. Indeed, increasing the W/L ratio, the ADR transverse effect along the X median axis is reduced and the contact evolves toward a 1D analytical approximation. However, a log scale graph tends to flatten this

scattering. Therefore, to better quantify the comparison, two index errors comparing the minimum O_2 partial pressure in the contact center and the oxygen distance “ d_O ”, assuming $P_{O_2,th}=0.1$ Pa, are computed.

$$\Delta P_{O_2 (1D)} = |P_{O_2,2D} (x = 0) - P_{O_2,1D} (x = 0)| \quad (19)$$

$$\% d_{O (1D)} = \left| \frac{d_{O,2D} (P_{O_2,th} = 0.1 \text{ Pa}) - d_{O,1D} (P_{O_2,th} = 0.1 \text{ Pa})}{d_{O,2D} (P_{O_2,th} = 0.1 \text{ Pa})} \right| \times 100 \quad (20)$$

To evaluate the relative influence of the advection contribution two additional index errors are estimated using the 2D numerical simulations with and without advection process.

$$\Delta P_{O_2 (adv)} = |P_{O_2,2D} (x = 0) - P_{O_2,2D} (x = 0, adv = 0)| \quad (21)$$

$$\% d_{O (adv)} = \left| \frac{d_{O,2D} (P_{O_2,th} = 0.1 \text{ Pa}) - d_{O,2D} (P_{O_2,th} = 0.1 \text{ Pa}, adv = 0)}{d_{O,2D} (P_{O_2,th} = 0.1 \text{ Pa})} \right| \times 100 \quad (22)$$

Hence, $\Delta P_{O_2 (1D)}$ and $\% d_{O (1D)}$ index errors measure the maximum error between the complete ADR model versus the 1D analytical expression. However, $\Delta P_{O_2 (adv)}$ and $\% d_{O (adv)}$ measure the relative errors induced when neglecting the advection process in the 2D numerical solutions. Finally, the error differences between these two errors ($\Delta P_{O_2 (1D)} - \Delta P_{O_2 (adv)}$) and ($\% d_{O (1D)} - \% d_{O (adv)}$) illustrate the effect of transverse contributions on the minimum P_{O_2} and $\% d_{O}$ values respectively. This index error analysis is generalized to plot the evolution of $\Delta P_{O_2 (1D)}$ and $\Delta P_{O_2 (adv)}$ then $\% d_{O (1D)}$ and $\% d_{O (adv)}$ versus W/L in Fig. 3a and Fig. 3b respectively.

Asymptotic decreasing evolutions are observed confirming that when W/L exceeds 1, the given 1D analytical formulation provides rather good estimation of the minimum oxygen partial pressure and above all a good prediction of the oxygen distance. Note

that in addition to the P_{O_2} variable, the oxygen distance d_o was established by previous study [11] as a key parameter to quantify the partition of adhesive and abrasive wear domains in the fretting interface. The very good prediction of the d_o values for $W/L > 1$ suggests that despite its simplicity, the 1D analytical formulation appears as a very useful strategy to quantify the contact oxygenation process under gross slip fretting interface.

Besides, the comparison between $\Delta P_{O_2 (1D)}$ and $\Delta P_{O_2 (adv)}$ and then $\% d_{O (1D)}$ and $\% d_{O (adv)}$ respectively suggests that most of the error is in fact induced by the transverse ADR contribution rather than by the advection effect whose contribution appears negligible compared with the diffusion process.

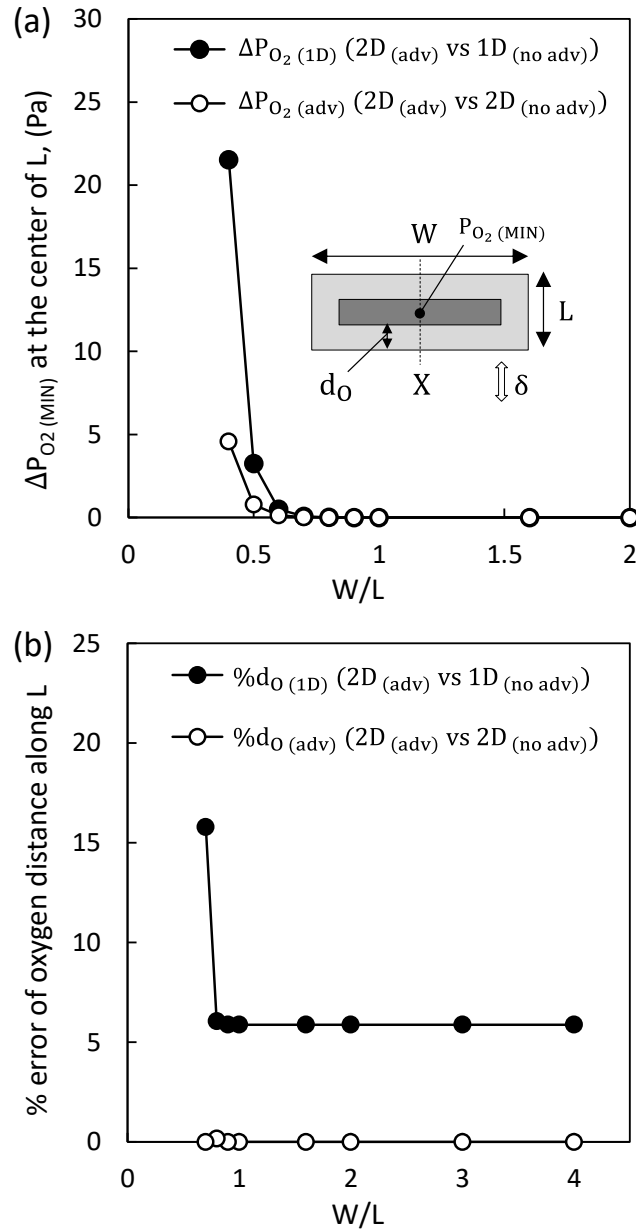


Fig.3. (a) Evolution of $\Delta P_{O_2(1D)}$ and $\Delta P_{O_2(adv)}$ index errors versus W/L ratio; (b) evolution of % $d_{O(1D)}$ and % $d_{O(adv)}$ index errors versus W/L ratio estimated for a nonzero adhesion zone ($p=100$ MPa, $\delta_g=\pm 100$ μ m, and $f=1$ Hz).

5. Experimental validation of the analytical solution of the ADR model

The 1D analytical approximation of the ADR model previously validated after being compared with a complete 2D numerical simulation is now confronted with experiments.

The studied contact geometry consists in a rectangular 34NiCrMo16 flat-on-flat configuration such that the transverse width ($W=10$ mm) is chosen at least three times longer than the collinear contact length ($L=3$ mm) leading to a W/L ratio=3.33 with an apparent contact area $A=30$ mm². This contact configuration permits assuming a one-dimensional evolution of the interfacial oxygen flow along the collinear contact length “L” by considering that the transverse width “W” is sufficiently large with respect to “L”. A hydraulic test machine, specific for testing large flat contacts (see Ref. [12,18]) is used to perform the experiments.

Following this, a cross-experimental campaign is considered to evaluate the capacity of the analytical solution of the ADR to predict the oxygen distance “ d_o ” and the partition between adhesive and abrasive wear domains. All the tests are performed at ambient temperature (25 °C \pm 5 °C) and relative humidity ($RH=40\%$ \pm 10%). Starting from a reference test having number of fretting cycles $N=20000$ cycles, sliding amplitude $\delta_g=\pm 100$ μ m, contact pressure $p=100$ MPa, sliding frequency $f=1$ Hz, contact transverse width $W=10$ mm and collinear length $L=3$ mm ($A=30$ mm²), two parameters are tested. First, the sliding frequency is varied from 1 to 15 Hz while maintaining the other parameters the same as the reference condition. Following this, the contact pressure is varied from 25 to 150 MPa while fixing the other parameters (Fig. 4b). Then, oxygen partial pressure is estimated by applying Eq. 15 along the collinear length $L=3$ mm from which the numerical oxygen distance can be computed (Fig. 3). This permits estimating adhesive wear area which is compared to the experimental results obtained using EDX maps as detailed in [12] assuming isotropic oxygen distance.

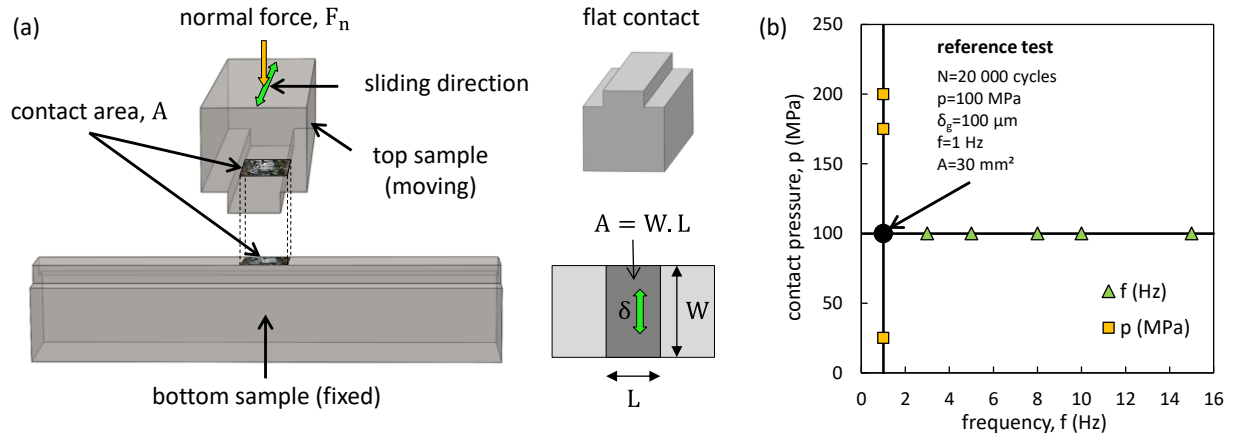


Fig. 4. (a) Schematic illustration of the rectangular crossed flat-on-flat configuration; (b) cross-experimental campaign used to validate the analytical solution of the ADR.

6. Results

Fig. 5 compares the experimental and the predicted evolution of the fretting scar and the adhesive wear extension by the ADR analytical solution as a function of the Archard power density factor while varying the contact pressure and the sliding frequency. It appears that by increasing the friction power dissipated at the interface, the contact shifts from pure abrasive to mixed abrasive-adhesive wear with a noticeable growth of the internal adhesion zone with the increase of ω^* . As suggested by the contact oxygenation concept (COC), this is due to the higher consumption of oxygen at the borders induced by the oxidation of the freshly exposed metal surface by friction process. Hence, there will be oxygen gas depletion towards the center favoring adhesive wear (Fig. 1 & 2). Such tendency is elegantly captured by the analytical solution of the ADR model which mimics the expansion of the internal rectangular adhesion zone at a wide range of loading conditions.

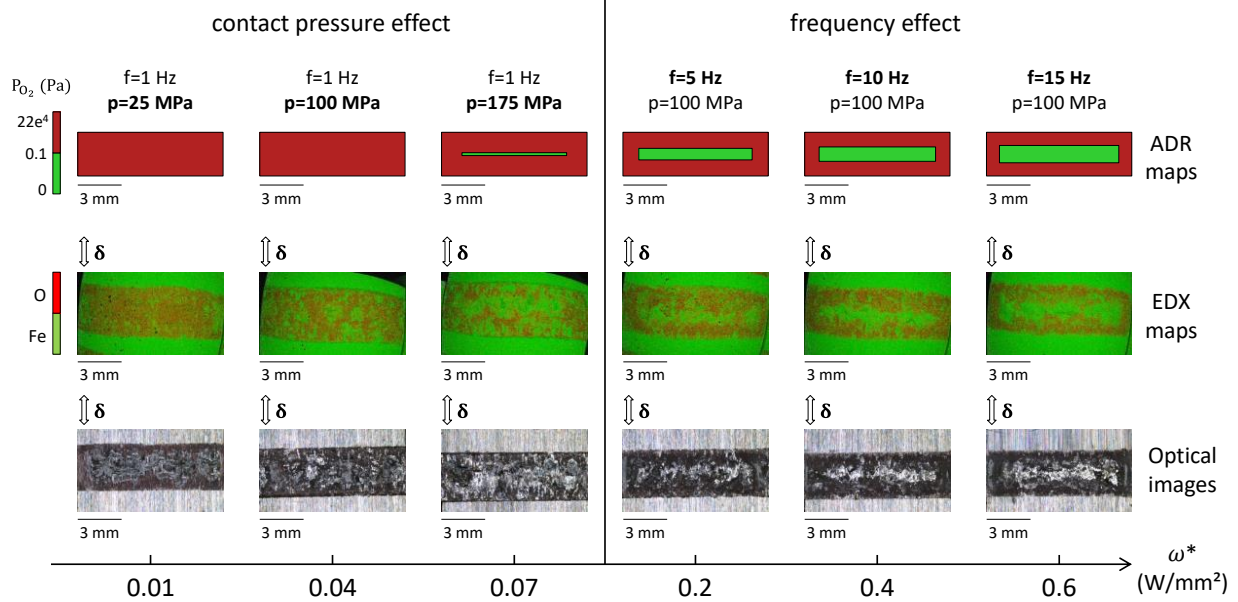


Fig. 5. Comparison between the optical images, EDX maps and the analytical ADR maps for the top samples displaying the growth of the adhesion zone with the increase in the Archard power density factor $\omega^* = p \times v = 4 \cdot p \cdot \delta_g \cdot f$ from 0.01 to 0.6 W/mm² (N=20000 cycles, $\delta_g = \pm 100 \mu\text{m}$, and $A = 3 \times 10 = 30 \text{ mm}^2$).

The above evolution is quantified in Fig. 6 where the experimental oxygen distance values ($d_{O,exp}$) are compared with those predicted by the 1D ADR simplified analytical solution ($d_{O,1D}$) extracted from Eq. 15. Note that the evolution of $d_{O,1D}$, which corresponds to the distance from the contact borders to the position where $P_{O_2}(x) = P_{O_2,th} = 0.1 \text{ Pa}$, can be approximated by a simple power law function such that $d_{O,1D} = 0.89 \times \omega^{*-0.14}$. As expected, both experiments and simulations display an asymptotic decrease versus the Archard power density factor (i.e. “ $\omega^* = p \cdot v$ ” factor). Combining the effects of the contact pressure and the sliding frequency, it appears clearly that the given “ $d_{O,1D}$ ” formulation provides a very good estimation of the experiments “ $d_{O,exp}$ ”. However, the analytical solution appears to better predict the effect of the sliding

frequency than the contact pressure. The overestimation of the contact pressure effect could be attributed to the fact that the given ADR model assumes a constant debris bed porosity which is not the case when varying the contact pressure as the latter compacts the debris bed leading to lower porosity values.

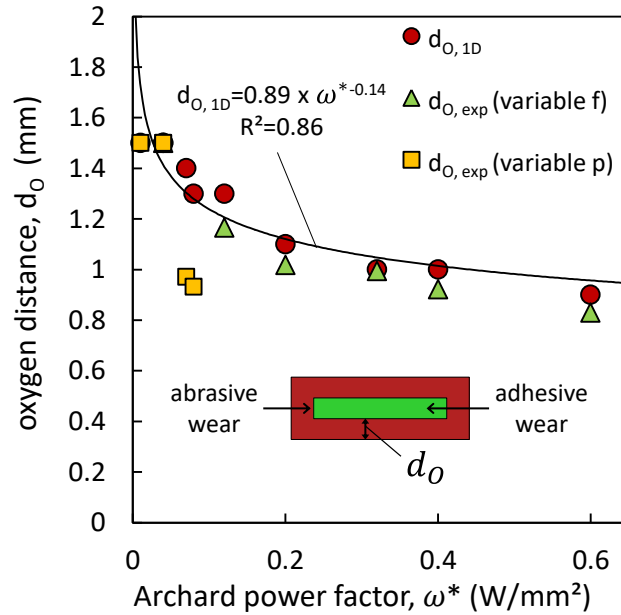


Fig. 6. Correlation between the experimental ($d_{o,exp}$) and the predicted oxygen distance from ADR approach ($d_{o,1D}$) as a function of the Archard power density factor $\omega^* = p \times v = 4 \cdot p \cdot \delta_g \cdot f$ ($N=20000$ cycles, $\delta_g=\pm 100 \mu m$, and $A=3 \times 10=30 \text{ mm}^2$).

The ADR model predictions through the one dimensional analytical solution proposed in Eq. 15 for rectangular and square contacts are combined with the predictions of the ADR axisymmetric analytical solution for circular flat contacts (formerly proposed in [13]) in Fig. 7a, b & c. The results of 50 tests considering variable contact pressure, sliding frequency, and contact size for flat circular, rectangular (linear) and square contacts are compiled. Such combination uncovers a strong correlation between the experimental

and the given ADR analytical oxygen distance prediction which definitively confirms the interest of such simple closed form expressions. This indirectly lends support to the fact that advection contribution can be neglected at least for the studied conditions. It also suggests that using these simple expressions a direct link can be established between contact loadings and the adhesive/abrasive wear distributions within fretting interface. This development is expected to allow basic multiphysics analysis of the fretting wear contacts.

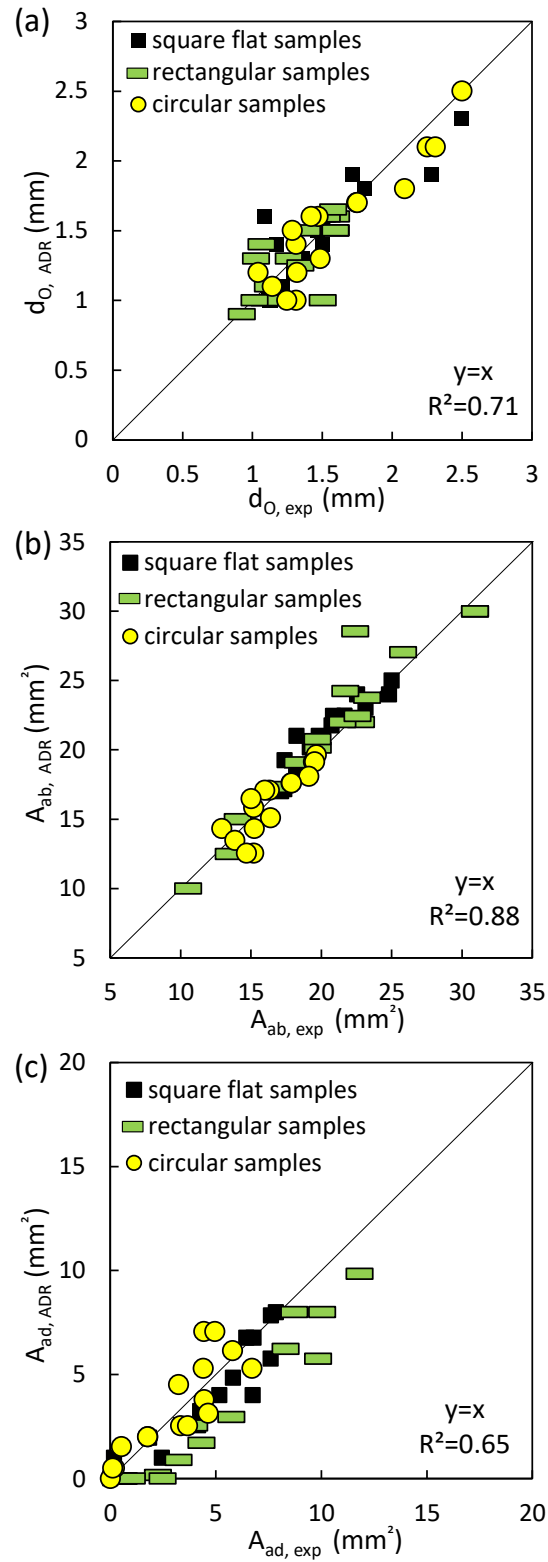


Fig. 7. Comparison between the experimental and the analytical ADR prediction given by 1D (Eq. 15) and axisymmetric (Eq. 4) formulations (i.e. Eq. 15 for rectangular and

square contacts and Eq. 4 for axisymmetric circular contact) for (a) the oxygen distance “ d_o ”; (b) the abrasion area “ A_{ab} ”; and (c) the adhesion area “ A_{ad} ”.

7. Discussion

Explicit closed-form expressions of the ADR modelling are derived for axisymmetric and 1D contact configuration. Using this approach, the oxygen distance d_o (i.e. the extension of the abrasive wear domain) as well as the partition between the inner adhesive wear domain and the surrounding abrasion zone can be estimated. A very good correlation with the experimental results suggest that despite the simplifications made, the given explicit formulations of the COC modeling appear reliable and above all efficient to predict the extension of the adhesive wear domain in fretting interfaces. The model considers a steady state hypothesis which is indirectly supported by a stable evolution of the friction coefficient and a linear increase of the wear volume above 5000 cycles [18].

However, the long term stability of the partition between adhesive and abrasive wear domain (i.e. d_o length) is still an open question. A dynamic description of the fretting scar morphology should be considered to better interpret COC process. Indeed, at the beginning of the fretting test, the native oxide layer is progressively removed inducing direct metal-metal interactions and formation of the first metal debris. Note that this process is activated even for very low mean contact pressures since incipient damage processes are activated at the asperity scale where plasticity occurs as depicted by Greenwood’s theory.

Then, as suggested by COC, the morphology of the wear debris and the related wear mechanisms will depend on the local contact oxygenation condition:

- If these worn debris particles are located in a domain where the contact oxygenation is effective (i.e. $P_{O_2}(x,y) > P_{O_2,th}$), this metallic wear debris will oxidize leading to oxidative abrasive wear process.

- If these incipient metallic wear debris are located in a contact domain where the contact oxygenation is deprived (i.e. $P_{O_2}(x,y) < P_{O_2,th}$), these metallic wear debris will agglomerate leading to an adhesive metallic third body structure.

The partition between these two third-body structures (i.e. d_o) depends on the contact loading conditions but can also evolve with the test duration and the structure of the third-body layer. Zhu et al. [10,19,20], investigating very long cylinder-on-flat contact fretting tests, suggested that above 10^6 fretting cycles the inner adhesive wear domain observed at the beginning of the test disappears. To interpret this result, it must be underlined that for a non-conformal contact like cylinder-on-flat, the surface wear promotes an extension of the contact area which tends to expand the inner adhesive wear domain. However, in the meantime, the mean contact pressure decreases which favors the contact oxygenation process. Therefore, the evolution of d_o (i.e. the partition of adhesive and abrasive wear domains) can be related to the balance between these two opposite effects which can explain that for very long tests, where P_{O_2} becomes lower than $P_{O_2,th}$ over the whole fretted interface, the interface shifts toward a pure abrasive wear scar. In the present flat-on-flat contact investigation, contact area and mean contact pressure remain nearly constant and therefore the composite adhesive-abrasive fretting scar morphology is more stable.

The dynamic evolution of d_0 parameter not only depends on the global contact loadings but also on the local wear process as depicted by Arnaud et al. [21]. Indeed, in this multiphysics research work, both the surface wear and COC processes were coupled to simulate the wear profiles and adhesive/abrasive wear partition of TA6V cylinder-on-flat contact. This work suggests that steady state wear extension implies a homogeneous increment of the wear depth over the whole wear regime is achieved. Therefore, to compensate the lower rate of the inner adhesive wear domain, higher friction energy density and consequently higher contact pressures should operate in the adhesive wear domain compared to the lateral abrasive zones. This generates peak pressure at the d_0 boundary between adhesive and abrasive wear domains (Fig. 16 in [21]). These local peak pressures reduce the oxygen diffusion and in turn stabilize the presence of an inner adhesive domain in the fretting interface as suggested by Fig. 17 in [21].

Hence, the adhesive wear domain remains constant in size although the lateral abrasive wear domains extend with the surface wear extension. To conclude, the long term evolution of the partition between the adhesive and the abrasive wear domain is a complex process, involving a local description of COC but also a local surface wear analysis. Future research works coupling local multiphysics simulations and very long fretting wear experiments will be undertaken to clarify this subject.

8. Conclusion

This paper provides analytical solutions of the Advection-Dispersion-Reaction (ADR) modelling of the contact oxygenation concept. The analytical solution of the ADR is

obtained by assuming one dimensional contact configuration. Results show that despite the simplifications made, the analytical solutions provide a very good approximation of the predictions given by the complete 2D numerical simulations. If the ratio between the transverse and the longitudinal lengths is larger than 1 (i.e. $W/L \geq 1$), these basic formulations not only capture the extension of adhesive wear but also the transition from pure abrasive to a composite abrasive-adhesive wear for a broad range of fretting loadings and flat contact geometries.

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