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► **To cite this version:**

Ikenna Chinazaekpere Ijeh, Mohammad Ali Khalighi, Steve Hranilovic. Parameter Optimization for an Underwater Optical Wireless Vertical Link Subject to Link Misalignments. *IEEE Journal of Oceanic Engineering*, 2021, 46 (4), pp.1424-1437. 10.1109/JOE.2021.3069046 . hal-03452616

HAL Id: hal-03452616

<https://hal.science/hal-03452616v1>

Submitted on 27 Nov 2021

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Parameter Optimization for an Underwater Optical Wireless Vertical Link Subject to Link Misalignments

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Abstract—We consider transmitter-receiver (Tx-Rx) parameter optimization for a vertical underwater wireless optical communication link under misalignment conditions. The Tx is assumed to use a light-emitting diode while the Rx uses a silicon photomultiplier that allows a high Rx sensitivity. We consider two typical application scenarios and investigate optimization of the Tx and the Rx parameters to optimize the link performance in terms of outage probability. We derive accurate analytical expressions for the distribution of the channel attenuation accounting for link misalignments, which allows for the evaluation of the link performance in terms of bit-error-rate and outage probability without resorting to costly Monte Carlo simulations. Through numerical results, we show and discuss the impact of parameter optimization on the link performance in different link configurations and for various misalignment conditions. In particular, the presented results show the significant performance improvement resulting from optimizing the Tx beam divergence and the Rx FoV in the presence of pointing errors.

Index Terms—Underwater wireless optical communications; Link misalignment; Parameter optimization; Silicon photomultiplier; Vertical underwater links.

I. INTRODUCTION

In underwater environments, there is an essential need for efficient wireless communication techniques in a number of applications, including installation monitoring, underwater robotics, port security, etc. Underwater wireless optical communications (UWOC) offer low implementation cost, low latency, high data rate, and energy efficiency, compared with the traditional acoustic communications [1]–[5]. Extensive research has been realized in the past few years in order to address the main challenges of the UWOC technology [6]. Among these, one important issue is to deal with link misalignments, which are particularly problematic in underwater applications where precise localization and tracking of mobile units is very challenging [6]. Other issues include accurate modeling of signal degradation due to water absorption and scattering [7]–[11], solar background noise [12], and channel turbulence [13]–[17], as well as developing efficient transmission techniques to ascertain the reliability of the communication link [18], [19]. In particular, to increase the transmission range of UWOC links, the use of high sensitivity detectors including photo-multiplier tubes (PMTs), single-photon avalanche diodes (SPADs), and arrays of SPADs, also known as silicon photo-multipliers (SiPMs) or multi-pixel

photon counters (MPPCs), has received particular attention [20].

In this paper, we focus on the effect of Tx-Rx misalignment errors and propose optimization of the link parameters to minimize the link performance degradation. Indeed, although the impact of beam misalignment and pointing errors is a well-explored topic in free-space optical (FSO) communications [21], [22], the past literature on UWOC systems mostly considered perfectly aligned line-of-sight (LoS) horizontal or vertical links. However, misalignment is, of course, one of major issues in underwater wireless optical links, which can considerably impact the link reliability. Misalignments can be due to different phenomena in practical link deployment scenarios. For instance, for the case of communication with a underwater mobile unit, they can arise from its positioning inaccuracy or instability. Also, in the case of transmission from a fixed node, e.g., at the sea surface, they can be due to node movements as a results of surface waves.

A few works have considered misalignment considerations for UWOC links. For instance, [23] presented a theoretical and experimental study of the effect of displacement in the Rx position and the inclination angle with respect to the main optical axis on the detected signal. The effect of beam divergence angle on the received power was investigated in [24], taking into consideration the Tx-Rx lateral offset. Also, for the case of turbid waters, [25] studied the effect of Rx angular misalignments and its field-of-view (FoV) on the received signal. Furthermore, for some special link configurations, e.g., a bottom-surface-bottom link in [26] or a surface-to-bottom link in [27], [28], the link performance was evaluated taking into account the effect of random sea surface, based on the verified experimental model of [29]. More recently, [30], [31] proposed an angular multiple-input multiple-output (MIMO) technique for relatively short UWOC links to relax the beam alignment requirements.

Our aim in this work is to focus on the system design for UWOC links corrupted by misalignments in order to minimize their impact on the link performance. As we will explain later, the main parameters that we consider here are the Tx beam divergence and the Rx FoV. Note that a few works have considered a similar approach in the contexts of outdoor FSO systems and indoor optical wireless systems. For instance, for a Gaussian beam propagating through an FSO channel subject

to atmospheric turbulence and pointing errors, [32] proposed joint optimization of beam width and spatial coherence length of the Tx to maximize the average channel capacity. For FSO links deployed in high-altitude platforms subject to angle-of-arrival (AoA) fluctuations and pointing errors, [33] proposed an adaptive beam optimization technique at the Tx and at the Rx using a variable focus lens. Also, [34] considered optimization of the Tx Gaussian beam-waist and the Rx FoV for unmanned aerial vehicle (UAV)-based FSO links under channel turbulence and pointing error conditions. On the other hand, optimized Tx beam width was proposed in [35] for an indoor cellular optical wireless communication (OWC) and positioning system, which allowed a higher channel bandwidth (BW) and a higher position accuracy.

Given the substantially different beam propagation (including scattering), channel characteristics, Tx-Rx types, and operational particularities between FSO, indoor OWC and UWOC systems, there is the need for a unique study into the optimization of UWOC link parameters, which constitutes our motivation behind this work.

We consider a typical scenario for an UWOC link, employing light-emitting diodes (LEDs) at the Tx and a high-sensitivity photo-detector, i.e., an SiPM at the Rx. The interest of using LEDs is their relatively high output power and the flexibility of being arranged in arrays to further increase the transmit power, and hence, the link span [36], [37]. Also, the SiPM, which is an array of Geiger mode biased APDs (SPADs), offers the advantages of high sensitivity, low implementation complexity, low operating bias voltage, mechanical robustness, and magnetic fields insensitivity, as compared to the PMT counterparts [20], [37], [38].

More specifically, in our case study, communication takes place between a buoy at the water surface and an AUV beneath it, as illustrated in Fig. 1. The typical application is high-speed data transfer from a sea surface observation station to an AUV (download mode), or transmitting the collected data by an AUV to a surface station for further long-range through-the-air transmission (upload mode), e.g., for data muling. The position and orientation of the buoy in this scenario are subject to sea surface waves, while those of the AUV are subject to water currents and AUV instability in its *dynamic* positioning (i.e., static position, used when establishing a communication link with the buoy).

To the best of our knowledge, the study of UWOC link optimization for a limited Rx FoV with a high-sensitivity photo-detector (PD) has not been considered in the literature thus far. We provide an accurate and computationally efficient analytical framework for the evaluation of the link performance in terms of the bit-error-rate (BER) and the outage probability (P_{out}). This is based on precise mathematical modeling of angular misalignments and displacements of the AUV, as well as the angular misalignments at the buoy resulting from the sea surface waves. We show that careful selection of the Tx beam divergence and the Rx FoV allows significant performance improvement and substantially improved link reliability. Obviously, the link reliability can be further improved using powerful channel coding and/or more energy-efficient modulation techniques [19], [39].

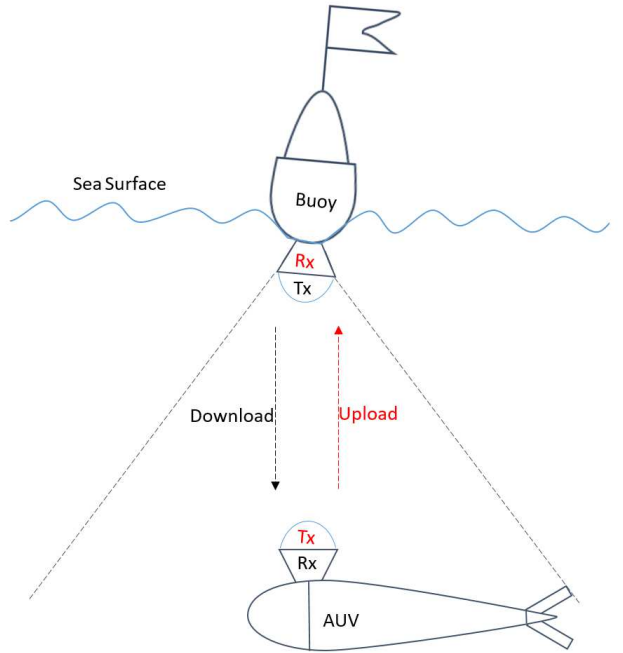


Fig. 1. Buoy-AUV illustration of the considered UWOC link.

The subsequent presentation of this paper is as follows. Section II introduces the considered UWOC link configuration and the related main assumptions. In Section III, we present mathematical modeling for pointing errors. Next, in Section IV, the derivation of the distribution of channel coefficient is provided for the considered link configuration. Then, a set of numerical results are presented in Section V to show the performance improvement achieved by Tx-Rx parameter optimization. Lastly, Section VI concludes the paper.

Notations: Boldface capital letters are used for matrices and boldface small letters for vectors. Also, $(\cdot)^T$ stands for transposition, $\|\cdot\|$ is the Euclidean norm, $\mathbf{a} \cdot \mathbf{b}$ denotes the dot product of vectors \mathbf{a} and \mathbf{b} , and $\delta(\cdot)$ stands for the Dirac delta function. In addition, $\Pr(\cdot)$ denotes probability, and $\text{erfc}(x) = \frac{2}{\sqrt{\pi}} \int_x^\infty e^{-t^2} dt$ and $Q(x) = \frac{1}{2} \text{erfc}(x/\sqrt{2})$ are the well-known complementary error function and Q -function, respectively. Lastly, $\text{sgn}(x)$ is the sign function, which equals 1 for $x \geq 0$ and -1 otherwise.

II. ASSUMPTIONS AND PERFORMANCE METRICS

For the sake of brevity, we provide in the following the system model for the case of downlink transmission for the link configuration shown in Fig. 1, when the Tx is located at the buoy and the Rx at the AUV. The general block diagram of the communication link is shown in Fig. 2.

A. Signal Transmission Modeling

Figure 3 shows the corresponding link geometry, where the Rx is located at depth D , exactly beneath the Tx (i.e., when there is no displacement between the Tx and the Rx). The link distance L is then equal to D . At the Tx, the LED is assumed to follow a Lambertian model with order m , which

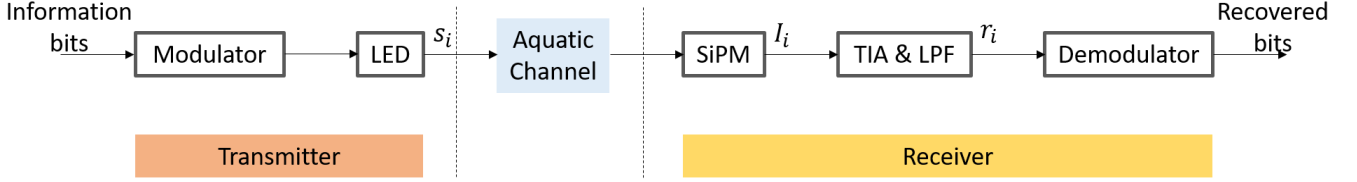


Fig. 2. The block diagram of the UWOC communication link.

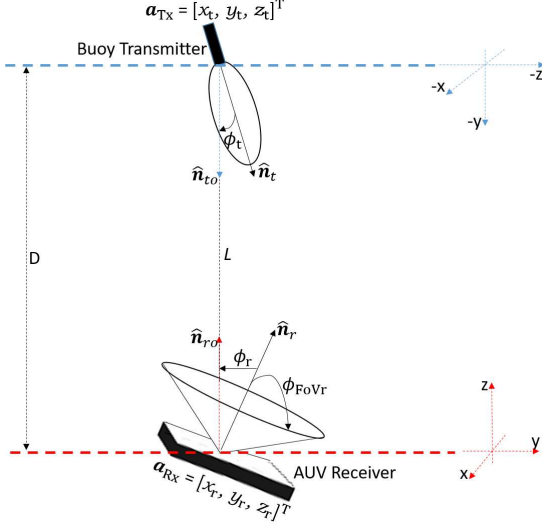


Fig. 3. Geometry of the buoy-AUV downlink UWOC system (inspired from [40]).

specifies the optical beam directionality [40]. At the Rx, prior to the PD, we consider the use of an optical filter with signal transmission $T_s(\phi_r)$ in order to reject the background noise as far as possible [12], as well as a non-imaging concentrator of refractive index n_r and gain $g(\phi_r)$ with $\phi_r \in \{0, \frac{\pi}{2}\}$ being the incidence angle [40]. Defining the active area of the PD by A_{PD} , the effective Rx light collection area A_{eff} is then given by [40]:

$$A_{\text{eff}}(\phi_r) = \begin{cases} A_{PD} T_s(\phi_r) g(\phi_r) \cos(\phi_r), & \phi_r \leq \phi_{\text{FoVr}} \\ 0, & \phi_r > \phi_{\text{FoVr}}, \end{cases} \quad (1)$$

where

$$g(\phi_r) = \frac{n_r^2}{\sin^2(\phi_{\text{FoVr}})}, \quad (2)$$

and ϕ_{FoVr} is the Rx FoV. For a given transmit optical power P_{Tx} , the received intensity P_{Rx} on the PD can then be expressed as [41]:

$$P_{Rx} = P_{Tx} \frac{m+1}{2\pi} \cos^m(\phi_t) e^{-(L K_d)} \frac{A_{\text{eff}}(\phi_r)}{L^2} \Pi\left(\frac{\phi_r}{\phi_{\text{FoVr}}}\right) \quad (3)$$

where, $\phi_t \in \{-\frac{\pi}{2}, \frac{\pi}{2}\}$ is the angle of irradiance at the Tx. We have used the definition of $\Pi(u) = 1$ if $u \leq 1$, and zero otherwise, which allows accounting for link interruption when the beam incident angle falls out of the Rx FoV. Also, K_d denotes the diffuse attenuation coefficient (taking into account

both beam absorption and scattering in water) that depends on the beam wavelength and the concentration of the particulates in water (chlorophyll concentration for the so-called Case-1 waters [42]). The exponential term in (3) is an approximate model to the beam attenuation due to seawater absorption and scattering when using a relatively wide beam [43], which is typically the case when considering LEDs at the Tx [12].

Define the aggregate channel coefficient, which includes the effects of the Tx, the Rx, and the aquatic channel as:

$$h = P_{Rx}/P_{Tx}. \quad (4)$$

In general, h is a random variable due to channel turbulence and Tx-Rx random misalignments.

As we use an LED at the Tx, we consider intensity modulation and direct detection for signal transmission. Without loss of generality, the non-return-to-zero (NRZ) on-off keying (OOK) is considered. At the Rx, the generated photo-current at the SiPM output is passed through a trans-impedance amplifier (TIA) followed by a low-pass filter (LPF) to limit the thermal noise variance (see Fig. 2).

The transmitted OOK signal s_i , $i \in \{0, 1\}$, takes two values of P_{Tx0} and P_{Tx1} , given the average transmitted optical power P_{Tx} and the extinction ratio, defined as $\xi = P_{Tx0}/P_{Tx1}$. The generated photo-current I_i at the SiPM output is:

$$I_i = \underbrace{\mathcal{R}_e s_i h}_{I_{s,i}} + I_d + n_{s_i} = \check{I}_i + n_{s_i}, \quad (5)$$

where $I_{s,i}$ represents the useful signal, I_d is the dark current, and n_{s_i} is the photo-current noise, including background noise, shot noise, and dark current noise. Also, $I_i = I_{s,i} + I_d$, which includes the constant component of the dark current, and \mathcal{R}_e is the SiPM responsivity, given by [38]:

$$\mathcal{R}_e = \left(\frac{\Upsilon_{\text{PDE}}}{E_{\text{ph}}} \right) (1 + P_{\text{AP}} + P_{\text{CT}}) e G. \quad (6)$$

Here, E_{ph} is the photon energy and e is the electron charge. Also, G , Υ_{PDE} , P_{AP} , P_{CT} denote the SiPM gain, photon detection efficiency, probability of after-pulsing, and probability of cross-talk, respectively (see [20], [44] for detailed description of SiPM parameters). The SiPM dark current is given by:

$$I_d = f_{\text{DCR}} (1 + P_{\text{AP}} + P_{\text{CT}}) e G, \quad (7)$$

where f_{DCR} denotes the SiPM dark count rate.

Denote the signal (voltage) at the LPF output by r_i :

$$r_i = R_L I_i + n_{\text{th}} = \underbrace{R_L \check{I}_i}_{\check{r}_i} + R_L n_{s_i} + n_{\text{th}} \quad (8)$$

with R_L being the load resistance of the TIA, and n_{th} denotes the thermal noise component in r_i , arising from the TIA and LPF circuitry (mainly related to R_L). The corresponding total noise variance $\sigma_{n_i}^2$ (in units of V^2) is given by:

$$\sigma_{n_i}^2 = R_L^2 (\sigma_{n_{s_i}}^2 + \sigma_{\text{th}}^2) = R_L^2 (\sigma_{\text{sh},i}^2 + \sigma_d^2 + \sigma_b^2) + \sigma_{\text{th}}^2, \quad (9)$$

where $\sigma_{\text{sh},i}^2$, σ_d^2 , σ_b^2 , and σ_{th}^2 (in V^2) denote the variances of the signal shot noise, dark noise, background noise, and thermal noise, respectively, where,

$$\begin{cases} \sigma_{\text{sh},i}^2 &= 2 e G F B I_{s,i}, \\ \sigma_d^2 &= 2 e G F B I_d, \\ \sigma_{\text{th}}^2 &= 4 K_Z T B R_L. \end{cases} \quad (10)$$

Here, K_Z , T , F , and B denote the Boltzmann constant, the Rx equivalent temperature in kelvin, the PD excess noise factor, and the BW of the Rx LPF, respectively. Let $B \approx R_b/2$, with R_b being the bit rate [45].

In this work, channel delay dispersion is neglected, which is valid in practice when working in low-to-moderate turbidity waters [9], [11]. Also, we neglect the channel turbulence, which implies that sea currents and the gradient of salinity and temperature variations are considered as negligible. Furthermore, for simplicity, we will neglect the effect of background noise from solar radiations, i.e., we set $\sigma_b^2 \approx 0$. In fact, considering a worst-case scenario, with a relatively high level of radiation when the sun is at zenith and assuming no shadowing for a vertical downlink transmission, [46] showed that an SiPM-based Rx is highly impacted by the background noise in relatively shallow waters, despite using a narrow-band optical filter. However, in our considered scenario these worst-case conditions are not likely to happen: the more critical case is the downlink (from the buoy-based Tx to the AUV Rx), where the buoy installation would shadow the sunlight, for example, when the sun is at the zenith. For the uplink case, the Rx performance could be limited by the laterally-diffused sunlight in water. However, the major part of this noise can be rejected by using a spatial filter at the buoy Rx.

B. Performance Evaluation

Given that channel variations due to misalignments occur in a much slower rate than the link bit-rate, the channel is modeled as non-ergodic for which the outage probability P_{out} is an appropriate performance metric. Define P_{out} as the probability that the link BER falls below a target BER. We further consider the probability of link interruption P_{int} as the probability that the incident angle of the incoming beam at the Rx falls outside the Rx FoV, i.e., $\phi_r > \phi_{\text{FoVr}}$. Notice that interruption events are included in outage.

Recall that we consider NRZ-OOK modulation scheme. We do not consider any channel coding [19] in this work. We assume the Rx has perfect knowledge of the random channel attenuation coefficient h , based on which it sets the optimal detection threshold for signal demodulation.¹ Note from the

¹Note that this is a quite reasonable assumption since the channel varies slowly with respect to the bit duration, and can easily be estimated using pilot symbols [47].

previous subsection that, an important point is that the Rx noise is signal dependent, given the use of an SiPM PD. The instantaneous BER $P_e(e|h)$ can be written as [48]:

$$P_e(e|h) = \frac{1}{4} \operatorname{erfc} \left(\frac{\gamma_{\text{th}} - \check{r}_0}{\sqrt{2\sigma_{n_0}^2}} \right) + \frac{1}{4} \operatorname{erfc} \left(\frac{\check{r}_1 - \gamma_{\text{th}}}{\sqrt{2\sigma_{n_1}^2}} \right), \quad (11)$$

where γ_{th} stands for the optimal detection threshold, and \check{r}_0 and \check{r}_1 denote the signals input to the demodulator, corresponding to bits ‘0’ and ‘1’, respectively. The corresponding noise variances are denoted by $\sigma_{n_0}^2$ and $\sigma_{n_1}^2$, calculated from (9). The optimal threshold γ_{th} is calculated as [48]:

$$\begin{aligned} \gamma_{\text{th}} = & \frac{\check{r}_0 \sigma_{n_1}^2 - \check{r}_1 \sigma_{n_0}^2}{\sigma_{n_1}^2 - \sigma_{n_0}^2} + \left[\frac{\check{r}_1^2 \sigma_{n_0}^2}{\sigma_{n_1}^2 - \sigma_{n_0}^2} + \right. \\ & \left. \left(\frac{\check{r}_0 \sigma_{n_1}^2 - \check{r}_1 \sigma_{n_0}^2}{\sigma_{n_1}^2 - \sigma_{n_0}^2} \right)^2 - \frac{\check{r}_0^2 \sigma_{n_1}^2}{\sigma_{n_1}^2 - \sigma_{n_0}^2} \right. \\ & \left. - \frac{\sigma_{n_0}^2 \sigma_{n_1}^2}{\sigma_{n_1}^2 - \sigma_{n_0}^2} \ln \left(\frac{\sigma_{n_0}^2}{\sigma_{n_1}^2} \right) \right]^{0.5}. \end{aligned} \quad (12)$$

The average BER² can then be calculated as:

$$P_e = \int_0^\infty P_e(e|h) f_h(h) dh, \quad (13)$$

where $f_h(h)$ is the PDF of h . Also, the outage probability can be defined as:

$$P_{\text{out}} = \Pr(h < h_{\text{th}}) = \int_0^{h_{\text{th}}} f_h(h) dh, \quad (14)$$

where h_{th} is defined so that $\text{BER}_{\text{th}} = P_e(e|h_{\text{th}})$. Lastly, the link interruption probability is:

$$P_{\text{int}} = \Pr(\phi_r > \phi_{\text{FoVr}}). \quad (15)$$

C. Analytical Outage Probability Calculation

As will be explained in Section V, the link performance can be evaluated through a statistical Monte Carlo (MC) approach. Obviously, there is interest to calculate these quantities analytically to avoid timely MC simulations. We provide here details on the derivation of the average BER and the outage probability. Whereas closed form expressions can readily be derived for the case of using a simple PIN PD [27], [34], the signal dependent noise in our case (resulting in a complex form for $P_e(e|h)$ and for the optimal detection threshold γ_{th} in (11) and (12)) and the relatively complex expressions for the PDF of h (as will be shown later in Section IV) make derivation of closed form expressions for P_{out} very complex. For this reason, we propose here to make some simplifying assumptions. Firstly, we assume that the shot noise $R_L^2 \sigma_{\text{sh},i}^2$ in (8) is the dominant noise factor at the Rx. This implies that we have a large PD gain G (which is actually the case), and that for OOK signaling, a relatively large³ extinction ratio ξ is used, which implies that even for ‘‘off’’ OOK symbols, the thermal and dark noises are negligible, compared with the

²Although our channel is non-ergodic and the appropriate metric is the outage probability, P_e is also given for the sake of completeness.

³We have verified by numerical simulations that the obtained solution is quite accurate for $\xi \gtrsim 30\%$, and even provides a good accuracy for ξ as small as $\sim 10\%$.

corresponding signal-dependent shot noise. As a result, given that $I_{s,0} = \xi I_{s,1}$, we set $\check{r}_0 \approx \xi \check{r}_1$ and also $\sigma_{n_0}^2 \approx \xi \sigma_{n_1}^2$. Then, considering optimal thresholding for signal detection, the error probability in (11) can be simplified as:

$$P_e(e|h) = \frac{1}{2} \operatorname{erfc} \left(\frac{R_L I_{s,1} - \gamma_{\text{th}}}{\sqrt{2 \sigma_{n_1}^2}} \right) = Q \left(\frac{R_L I_{s,1} - \gamma_{\text{th}}}{\sqrt{\sigma_{n_1}^2}} \right). \quad (16)$$

Also, with the considered approximations, the expression of γ_{th} in (12) can be simplified as follows:

$$\gamma_{\text{th}} = R_L \sqrt{\xi I_{s,1}^2 - \frac{\xi \sigma_{n_1}^2}{1 - \xi} \log \xi} \approx R_L I_{s,1} \sqrt{\xi} \quad (17)$$

Now, to calculate P_{out} for a given h_{th} (which corresponds to a BER_{th}), we have $\sigma_{n_1}^2 = R_L^2 (2eGFB \mathcal{R}_e s_1 h_{\text{th}} + \sigma_d^2) + \sigma_{\text{th}}^2$ and $I_{s,1} = \mathcal{R}_e s_1 h_{\text{th}}$. Then, from (16) we can define:

$$A \triangleq Q^{-1}(\text{BER}_{\text{th}}) = \frac{R_L \mathcal{R}_e s_1 h_{\text{th}} - R_L \mathcal{R}_e s_1 h_{\text{th}} \sqrt{\xi}}{\sqrt{R_L^2 (2eGFB \mathcal{R}_e s_1 h_{\text{th}} + \sigma_d^2) + \sigma_{\text{th}}^2}} \quad (18)$$

A can be calculated, for instance, using the Matlab *qfuncinv* function [49]. We also define for notation simplicity $\mu = R_L \mathcal{R}_e s_1$ and $\beta = 2eR_L GFB \mu$. We can then rewrite (18) as:

$$A = \frac{\mu h_{\text{th}} (1 - \sqrt{\xi})}{\sqrt{\beta h_{\text{th}} + R_L^2 \sigma_d^2 + \sigma_{\text{th}}^2}} \quad (19)$$

It can be easily shown that h_{th} can be calculated from the following equation:

$$h_{\text{th}} = \frac{\mathcal{B} + \sqrt{\mathcal{B}^2 + 4\mathcal{D}\mathcal{C}}}{2\mathcal{D}}, \quad (20)$$

where $\mathcal{B} = \mathcal{A}^2 \beta$, $\mathcal{C} = \mathcal{A}^2 (R_L^2 \sigma_d^2 + \sigma_{\text{th}}^2)$, and $\mathcal{D} = \mu^2 (1 - \sqrt{\xi})^2$. The accuracy of this approach will later be quantified by numerical results in Section V.

III. POINTING ERROR MODELING

Consider the downlink configuration as the default case, i.e., when the Tx is on the buoy and the Rx is on the AUV. For the mathematical derivations, we assume that the buoy's position is nearly fixed, whereas its orientation is primarily affected by the surface waves as a result of wind. The orientation of the Rx is deviated by underwater currents and the instability of the AUV, whereas its displacement is due to positioning inaccuracies. To account for pointing errors, we consider the perfect alignment case when the AUV is exactly beneath the buoy and there is no orientation deviation with respect to the optical axis. Figure 3 illustrates the scenario where there is no position displacement between the Tx and the Rx but there are orientation deviations at both the Tx and the Rx with respect to the optical axis. A more general scenario is illustrated in Fig. 4, where there is also a position displacement of the Rx with respect to the Tx.

Consider the more general misalignment case as illustrated in Fig. 4. Under perfect Tx-Rx alignment, denote the normal vectors to the Tx and the Rx by $\hat{\mathbf{n}}_{t_0}$ and $\hat{\mathbf{n}}_{r_0}$, respectively, where $\hat{\mathbf{n}}_{t_0} = [0, 0, -1]^T$ and $\hat{\mathbf{n}}_{r_0} = [0, 0, 1]^T$. Under misaligned beam conditions, these normal vectors are denoted by

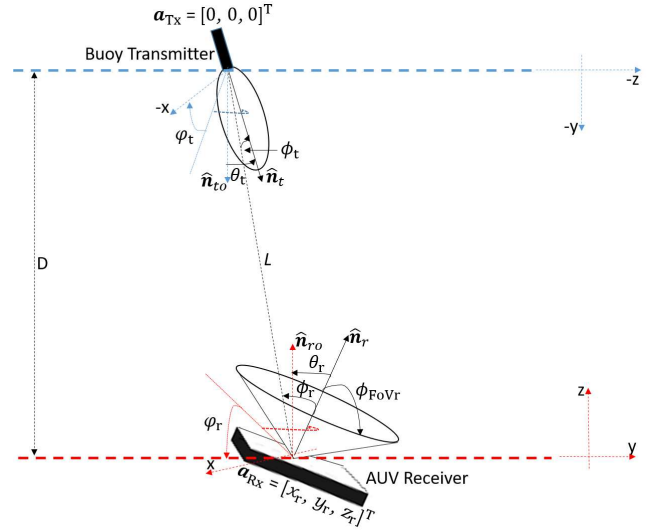


Fig. 4. Transmitter and Receiver with Orientation and Position Deviations (inspired from [40]).

$\hat{\mathbf{n}}_t$ and $\hat{\mathbf{n}}_r$, respectively. Let θ_t denote the polar angle between $\hat{\mathbf{n}}_{t_0}$ and $\hat{\mathbf{n}}_t$, and φ_t the azimuthal angle to $\hat{\mathbf{n}}_t$. Similarly, the polar and azimuthal angles of the Rx are denoted by θ_r and φ_r , respectively. Like in Fig. 3, here, ϕ_t and ϕ_r denote the polar angles with respect to the optical axis. We have:

$$\cos(\phi_t) = \frac{\hat{\mathbf{n}}_t \cdot (\mathbf{a}_{\text{Rx}} - \mathbf{a}_{\text{Tx}})}{\|\mathbf{a}_{\text{Rx}} - \mathbf{a}_{\text{Tx}}\|}, \quad (21)$$

$$\cos(\phi_r) = \frac{\hat{\mathbf{n}}_r \cdot (\mathbf{a}_{\text{Tx}} - \mathbf{a}_{\text{Rx}})}{\|\mathbf{a}_{\text{Tx}} - \mathbf{a}_{\text{Rx}}\|} \quad (22)$$

where $\|\mathbf{a}_{\text{Tx}} - \mathbf{a}_{\text{Rx}}\| = L$. Denote the Cartesian coordinates of the Tx and the Rx by vectors $\mathbf{a}_{\text{Tx}} = [x_t, y_t, z_t]^T$ and $\mathbf{a}_{\text{Rx}} = [x_r, y_r, z_r]^T$, respectively. Also, without loss of generality, in the following, consider the buoy's position as the origin of the Cartesian coordinates, i.e., $\mathbf{a}_{\text{Tx}} = [0, 0, 0]^T$. Note that when there is no Rx displacement, like in Fig. 3, we have $\phi_t = \theta_t$ and $\phi_r = \theta_r$.

A. Modeling Tx Orientation

The buoy at the sea surface swerves as wind blows across it from different directions. A set of experimental measurements were carried out in [29] to measure the sea surface slope. A close linearity was then deduced between the variance of sea surface slopes and the wind speed U for an approximate range of $1 \text{ m/s} < U < 14 \text{ m/s}$. This model was later validated in [50] based on a derived and experimentally-validated omni-directional wind-dependent sea surface spectrum. It was adopted in [27], [28] for a buoy-based vertical UWOC link, where the distribution of the random sea surface slope was expressed in terms of spherical coordinates as follows:

$$f_{\theta, \varphi}(\theta, \varphi) = \frac{\tan(\theta) \sec^2(\theta)}{2\pi\sigma_u^2} \exp\left(-\frac{\tan^2(\theta)}{2\sigma_u^2}\right), \quad (23)$$

where the variance σ_u^2 of the omni-directional sea surface slope (which is independent of the wind direction) is given by [29]:

$$\sigma_u^2 = 0.003 + 0.00512U \pm 0.004, \quad (24)$$

with U being in units of m/s. Note that in (23), φ_t is assumed to be uniformly distributed between 0 and 2π .

B. Modeling Rx Orientation and Displacement

We model the orientation of the Tx and the Rx by a rotation matrix \mathbf{R} applied to their initial vectors $\hat{\mathbf{n}}_{to}$ and $\hat{\mathbf{n}}_{ro}$ (corresponding to the perfect link alignment, see Fig. 3), respectively [51]. This way, $\hat{\mathbf{n}}_t = \mathbf{R}\hat{\mathbf{n}}_{to}$, and $\hat{\mathbf{n}}_r = \mathbf{R}\hat{\mathbf{n}}_{ro}$. Matrix \mathbf{R} accounts for rotations around z , x , and y axes (yaw γ , pitch α , and roll β) through rotation matrices \mathbf{R}_γ , \mathbf{R}_α , and \mathbf{R}_β , respectively:

$$\mathbf{R}_\gamma = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad \mathbf{R}_\alpha = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{bmatrix},$$

$$\mathbf{R}_\beta = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix},$$

here, α and β represent the sea surface slope effect from the up/downwind and the crosswind directions [29].

Given $\hat{\mathbf{n}}_{to} = [0, 0, -1]^T$, $\hat{\mathbf{n}}_t$ can be written as:

$$\hat{\mathbf{n}}_t = \mathbf{R}\hat{\mathbf{n}}_{to} = \mathbf{R}_\gamma \mathbf{R}_\alpha \mathbf{R}_\beta \hat{\mathbf{n}}_{to}$$

$$= \begin{bmatrix} -\cos \beta \sin \gamma \sin \alpha - \cos \gamma \sin \beta \\ \cos \gamma \cos \beta \sin \alpha - \sin \gamma \sin \beta \\ -\cos \alpha \cos \beta \end{bmatrix} = \begin{bmatrix} -\sin \theta_t \cos \varphi_t \\ -\sin \theta_t \sin \varphi_t \\ -\cos \theta_t \end{bmatrix}. \quad (25)$$

Similarly,

$$\hat{\mathbf{n}}_r = \mathbf{R}\hat{\mathbf{n}}_{ro} = \mathbf{R}_\gamma \mathbf{R}_\alpha \mathbf{R}_\beta \hat{\mathbf{n}}_{ro}$$

$$= \begin{bmatrix} \cos \beta \sin \gamma \sin \alpha + \cos \gamma \sin \beta \\ \sin \gamma \sin \beta - \cos \gamma \cos \beta \sin \alpha \\ \cos \alpha \cos \beta \end{bmatrix} = \begin{bmatrix} \sin \theta_r \cos \varphi_r \\ \sin \theta_r \sin \varphi_r \\ \cos \theta_r \end{bmatrix}. \quad (26)$$

Based on the illustration of Fig. 4, and given that $z_t = D$, (21) and (22) can be expressed as:

$$\cos(\phi_t) = \underbrace{\left(-\frac{x_r}{L} \cos(\varphi_t) - \frac{y_r}{L} \sin(\varphi_t)\right)}_{a_t} \sin(\theta_t) + \underbrace{\frac{D}{L}}_b \cos(\theta_t) \quad (27)$$

$$\cos(\phi_r) = \underbrace{\left(-\frac{x_r}{L} \cos(\varphi_r) - \frac{y_r}{L} \sin(\varphi_r)\right)}_{a_r} \sin(\theta_r) + \underbrace{\frac{D}{L}}_b \cos(\theta_r), \quad (28)$$

where we have defined the parameters a_t , a_r , and b for notation simplicity, similar to the approach in [51]. We model x_r and y_r by zero-mean independent Gaussian random variables (RVs) with variance σ_{pr}^2 . Also, for simplicity, θ_r is modeled as a zero-mean Gaussian-distributed RV with variance $\sigma_{\theta r}^2$.

IV. CHANNEL COEFFICIENT DISTRIBUTION

In order to analytically evaluate the link performance, we need the probability density function (PDF) of the received signal in the general case of a link subject to Tx-Rx angular misalignments and displacements. For the sake of simplicity, we assume that the concentrator gain $g(\phi_r)$ and the optical filter transmittance $T_s(\phi_r)$ are independent of ϕ_r , and denote them simply by T_s and g , respectively. Regarding the optical filter, this simplification could be equivalent to removing the optical filter, as we assume negligible background noise, see the last part of Subsection II-A.⁴ From (3) and (4), we have:

$$h = h_c \cos^m(\phi_t) \cos(\phi_r) \Pi\left(\frac{\phi_r}{\phi_{\text{FoVr}}}\right), \quad (29)$$

where h_c denotes the deterministic part of h :

$$h_c = \frac{m+1}{2\pi} \frac{A_{\text{PD}} T_s g}{L^2} e^{-(L K_d)}. \quad (30)$$

Let us further separate in (29) the parts depending only on ϕ_t and ϕ_r , that we denote by h_{ϕ_t} and h_{ϕ_r} , respectively:

$$h = h_c h_{\phi_t} h_{\phi_r}, \quad (31)$$

$$h_{\phi_t} = \cos^m(\phi_t), \quad (32)$$

$$h_{\phi_r} = \cos(\phi_r) \Pi\left(\frac{\phi_r}{\phi_{\text{FoVr}}}\right). \quad (33)$$

To derive the PDF of h , we consider the following cases in the subsequent subsections. First, in Subsection IV-A, only Tx angular misalignments are considered (without any displacement) while assuming a fixed Rx (orientation and position) and a (fixed) large Rx FoV. Then, in Subsection IV-B, both Tx and Rx angular misalignments are taken into account without any displacement, i.e., as illustrated in Fig. 3. The PDF is then modified in Subsection IV-C to account for Rx displacements, i.e., as in Fig. 4. Lastly, the generalization to the case of limited Rx FoV is considered in Subsection IV-D.

A. Tx Angular Misalignment and Fixed Rx

The key point here is to relate the distribution of h back to the random angular misalignment of the buoy. For this case, $\phi_t = \theta_t$ and $\phi_r = \theta_r = 0$, thus $h_{\phi_r} = 1$, and $h = h_c h_{\phi_t}$ that we denote by h_0 whose cumulative density function (CDF) can be obtained as:

$$F_{h_0}(h_0) = \Pr(h_c h_{\phi_t} \leq h_0) = \Pr(h_c \cos^m(\theta_t) \leq h_0)$$

$$= \Pr\left(\theta_t > \cos^{-1}\left(\sqrt[m]{\frac{h_0}{h_c}}\right)\right) = 1 - F_{\theta_t}\left(\cos^{-1}\left(\sqrt[m]{\frac{h_0}{h_c}}\right)\right), \quad (34)$$

where $F_{\theta_t}(\cdot)$ denotes the CDF of θ_t . From (34), the PDF of h_0 can be obtained as follows:

⁴Note that, in general, the approximation of a constant T_s is justified when the FoV is relatively small, with the range depending on the filter bandwidth. Nevertheless, recent techniques have shown the possibility of designing relatively wide FoV optical filters using metamaterials, e.g. [52]. Investigation of link parameter optimization while taking into account the dependence of T_s on ϕ_r , which is particularly interesting when background noise effect cannot be neglected (e.g., in downlink), can be subject of future research.

$$f_{h_0}(h_0) = \frac{C_1}{mh_0 \sqrt{\left(\sqrt{\frac{h_0}{h_c}}\right)^{-2} - 1}} f_{\theta_t} \left(\cos^{-1} \left(\sqrt{\frac{h_0}{h_c}} \right) \right), \quad (35)$$

where C_1 is a normalization coefficient to have $F_{h_0}(\infty) = 1$, and $f_{\theta_t}(\cdot)$ is the PDF of θ_t that is obtained from (23) as $f_{\theta_t}(\theta_t) = 2\pi f_{\theta_t, \varphi_t}(\theta_t, \varphi_t)$.

B. Tx-Rx Angular Misalignments and Fixed Rx Position

We consider now random $\phi_t = \theta_t$ and $\phi_r = \theta_r$, while considering $\phi_{\text{FoVr}} > \phi_r$. In this case, $h = h_c \cos^m(\theta_t) \cos(\theta_r) = h_0 h_{\phi_r}$. The CDF of h_{ϕ_r} , $F_{h_{\phi_r}}(\cdot)$, can be written as:

$$F_{h_{\phi_r}}(h_{\phi_r}) = \Pr(\cos(\theta_r) \leq h_{\phi_r}) = 1 - F_{\theta_r}(\cos^{-1}(h_{\phi_r})). \quad (36)$$

Subsequently, the PDF of h_{ϕ_r} , $f_{h_{\phi_r}}(\cdot)$, is:

$$f_{h_{\phi_r}}(h_{\phi_r}) = \frac{C_2}{\sqrt{1 - h_{\phi_r}^2}} f_{\theta_r}(\cos^{-1}(h_{\phi_r})), \quad (37)$$

where C_2 is a normalization coefficient. Afterwards, the PDF of h can be obtained as:

$$f_h(h) = \int f_{h|h_{\phi_r}}(h|h_{\phi_r}) f_{h_{\phi_r}}(h_{\phi_r}) dh_{\phi_r}, \quad (38)$$

where

$$\begin{aligned} f_{h|h_{\phi_r}}(h|h_{\phi_r}) &= \frac{1}{h_{\phi_r}} f_{h_0} \left(\frac{h}{h_{\phi_r}} \right) \\ &= \frac{C_3}{mh \sqrt{\left(\sqrt{\frac{h}{h_c h_{\phi_r}}}\right)^{-2} - 1}} f_{\theta_t} \left(\cos^{-1} \left(\sqrt{\frac{h}{h_c h_{\phi_r}}} \right) \right), \end{aligned} \quad (39)$$

and C_3 is a normalization coefficient.

C. Tx-Rx Angular Misalignments and Rx Displacements

In this case, $\phi_t \neq \theta_t$ and $\phi_r \neq \theta_r$. We assume that the Rx displacements are negligible, compared to the link range, which is reasonable in practice. Consequently, we assume $D \approx L$, and hence, consider h_c as almost constant. Given that we have six RVs that are involved in h (i.e., x_r , y_r , φ_t , φ_r , θ_t , and θ_r), the derivation of the general form of $f_h(h)$ is quite complex. Therefore, for simplicity, and similar to the approach considered in [51], we derive the PDF of h by fixing the Rx position (x_r and y_r) and the azimuthal angles⁵ φ_t and φ_r . According to (27), we have $\cos(\phi_t) = a_t \sin(\theta_t) + b \cos(\theta_t)$, which can be written as [51]:

$$\cos(\phi_t) = \text{sgn}(a_t) \sqrt{a_t^2 + b^2} \sin\left(\theta_t + \tan^{-1}(b/a_t)\right). \quad (40)$$

⁵As suggested in [53], this would correspond to the case where the Rx only tilts to front and back while the Rx normal $\hat{\mathbf{n}}_r$ faces the Tx.

We consider in the following the case of $a_t < 0$, i.e., $\text{sgn}(a_t) = -1$, which allows a simpler derivation⁶ of $f_h(h)$. Recall our notation of $h = h_c h_{\phi_t} h_{\phi_r} = h_0 h_{\phi_r}$. Thus,

$$f_{h|h_{\phi_r}}(h|h_{\phi_r}) = \frac{1}{h_{\phi_r}} f_{h_0} \left(\frac{h}{h_{\phi_r}} \right). \quad (41)$$

The CDF of h_0 can be written as:

$$\begin{aligned} F_{h_0}(h_0) &= \Pr(h_c \cos^m(\phi_t) \leq h_0) \\ &= \Pr\left(\theta_t > -\sin^{-1} \left(\frac{\sqrt{\frac{h_0}{h_c}}}{\sqrt{a_t^2 + b^2}} \right) - \tan^{-1} \left(\frac{b}{a_t} \right)\right) \\ &= 1 - F_{\theta_t} \left(-\sin^{-1} \left(\frac{\sqrt{\frac{h_0}{h_c}}}{\sqrt{a_t^2 + b^2}} \right) - \tan^{-1} \left(\frac{b}{a_t} \right) \right). \end{aligned} \quad (42)$$

Consequently,

$$\begin{aligned} f_{h_0}(h_0) &= \frac{-C_4 \sqrt{\frac{h_0}{h_c}}}{mh_0 \sqrt{a_t^2 + b^2 - \left(\sqrt{\frac{h_0}{h_c}}\right)^2}} \\ &\times f_{\theta_t} \left(-\sin^{-1} \left(\frac{\sqrt{\frac{h_0}{h_c}}}{\sqrt{a_t^2 + b^2}} \right) - \tan^{-1} \left(\frac{b}{a_t} \right) \right), \end{aligned} \quad (43)$$

where C_4 is a normalization coefficient. Similarly, using (28), we can write $\cos(\phi_r) = a_r \sin(\theta_r) + b \cos(\theta_r)$. Then, the PDF of h_{ϕ_r} can be given as:

$$\begin{aligned} f_{h_{\phi_r}}(h_{\phi_r}) &= \frac{-C_5}{\sqrt{a_r^2 + b^2 - h_{\phi_r}^2}} \\ &\times f_{\theta_r} \left(-\sin^{-1} \left(\frac{h_{\phi_r}}{\sqrt{a_r^2 + b^2}} \right) - \tan^{-1} \left(\frac{b}{a_r} \right) \right), \end{aligned} \quad (44)$$

where C_5 is a normalization coefficient. Therefore for this case,

$$\begin{aligned} f_{h|h_{\phi_r}}(h|h_{\phi_r}) &= \frac{-C_6 \sqrt{\frac{h}{h_c h_{\phi_r}}}}{mh \sqrt{a_t^2 + b^2 - \left(\sqrt{\frac{h}{h_c h_{\phi_r}}}\right)^2}} \\ &\times f_{\theta_t} \left(-\sin^{-1} \left(\frac{\sqrt{\frac{h}{h_c h_{\phi_r}}}}{\sqrt{a_t^2 + b^2}} \right) - \tan^{-1} \left(\frac{b}{a_t} \right) \right), \end{aligned} \quad (45)$$

and C_6 is a normalization coefficient. Lastly, $f_h(h)$ is obtained from (38) by marginalization.

⁶The PDF of h for the case of $a_t > 0$ is much more complex but can be obtained using the proposed approach in [51].

D. Limited Rx FoV; Tx-Rx Angular Misalignments and Rx Displacements

Now we apply to the last stage the FoV limitation. Inspired by the approach in [54], the CDF of h_{ϕ_r} needs to be modified as follows:

$$\begin{aligned}
 F_{h_{\phi_r}}(h_{\phi_r}) &= \Pr\left(\cos(\phi_r) \Pi\left(\frac{\phi_r}{\phi_{\text{FoVr}}}\right) \leq h_{\phi_r}\right) \\
 &= \underbrace{\Pr\left(\cos^{-1}(h_{\phi_r}) < \phi_r \leq \phi_{\text{FoVr}}\right)}_{1 - F_{\phi_r}(\cos^{-1}(h_{\phi_r}))} + \underbrace{\Pr(\phi_r > \phi_{\text{FoVr}})}_{1 - F_{\phi_r}(\phi_{\text{FoVr}})} \\
 &= 1 - F_{\theta_r}\left(-\sin^{-1}\left(\frac{h_{\phi_r}}{\sqrt{a_r^2 + b^2}}\right) - \tan^{-1}\left(\frac{b}{a_r}\right)\right) \\
 &\quad + \left(1 - F_{\phi_r}(\phi_{\text{FoVr}})\right).
 \end{aligned} \tag{46}$$

In the right side of the first line of (46), the first term accounts for the probability that an incident ray falls within the Rx FoV, while the second terms corresponds to a link interruption. The resulting PDF is then:

$$\begin{aligned}
 f_{h_{\phi_r}}(h_{\phi_r}) &= \frac{-C_7}{\sqrt{a_r^2 + b^2 - h_{\phi_r}^2}} \\
 &\quad \times f_{\theta_r}\left(-\sin^{-1}\left(\frac{h_{\phi_r}}{\sqrt{a_r^2 + b^2}}\right) - \tan^{-1}\left(\frac{b}{a_r}\right)\right) \\
 &\quad + \left(1 - F_{\phi_r}(\phi_{\text{FoVr}})\right) \delta(h_{\phi_r}),
 \end{aligned} \tag{47}$$

where the Dirac delta function accounts for the discontinuity of the CDF at $h_{\phi_r} = 0$ [54], and C_7 is a normalization coefficient. The PDF of h can be obtained by marginalization from (38) using (45) and (47).

V. NUMERICAL RESULTS

This section presents numerical results to study the link performance and the impact of link parameter optimization.

A. Parameter Specification

We consider a vertical link operating at depth Z in clear ocean waters having a chlorophyll concentration of $C_{\text{cl}} = 0.5 \text{ mg/m}^3$. At the Tx, we use a blue LED of wavelength 470 nm with a spectral half-width of 20 nm [55]. For this wavelength and the considered C_{cl} , K_d is approximately 0.08 m^{-1} [56], [57]. At the Rx, we use an optical filter of BW $\Delta\lambda = 20 \text{ nm}$, where for the sake of simplicity, we assume that its signal transmission T_s is nearly constant and equal to 1 [58]. Also, a blue-sensitive SiPM with reference SensL B-series MicroSB 30020 [59] is considered. Note that the deadtime of the SiPM is $\tau_d = 90 \text{ ns}$, during which the detector is unable to detect a new incoming photon [20], [60]. The extinction ratio for OOK Off/On symbols is set to $\xi = 0.4$ and the bit rate to $R_b = 1 \text{ Mbps}$. It is worth mentioning that τ_d is much smaller than the considered symbol duration, i.e., $1 \mu\text{s}$, and furthermore, the typical modulation BWs of the LED and the SiPM are assumed to be much higher than the

signal BW [37]. Hence, no inter-symbol interference affects the transmitted signal.⁷ Unless otherwise specified, the link range (i.e., the AUV operational depth in our case study) is set to 100 m, and the average Tx power is set to $P_{\text{Tx}} = 20 \text{ W}$ that can be obtained by using multiple LEDs at the Tx [36], [37]. Table I summarizes the considered parameters used for the link performance evaluation.

We do not consider any forward error correction (FEC) and set the target BER to the FEC threshold $\text{BER}_{\text{th}} = 2 \times 10^{-3}$ [63]. To calculate P_{out} , we use statistical and analytical approaches. By the statistical approach, in the general case of misaligned link illustrated in Fig. 4, for instance, we generate independent RVs $\theta_t, \phi_t, \varphi_t, \theta_r, \phi_r, \varphi_r, x_r$, and y_r according to the considered distributions, and use them to calculate the corresponding channel attenuation h . Then, for each channel realization h , the BER is calculated from (11). The outage probability P_{out} is calculated based on more than 10^7 channel realizations and for a given BER_{th} . On the other hand, by the analytical method, we calculate the approximate P_{out} from (14) using the derived analytical PDFs $f_h(h)$ in Section IV, through numerical integration [64].

Concerning the parameters related to angular misalignment and displacement of the AUV, we consider a range of a few degrees for $(\sigma_{\theta_t}, \sigma_{\theta_r})$ and a range of a few meters for σ_{pr} , which are close to practical uplink and downlink scenarios.⁸

In what follows, we first illustrate the effect of different factors that result in pointing errors in the considered case studies. Then, we focus on Tx/Rx parameter optimization, i.e., m and θ_{FoV} , and investigate its effect on the overall link performance.

B. Effect of Misalignment Parameters on Outage Probability, Buoy-to-AUV Downlink

First, to get an idea of the effect of wind speed and AUV angular misalignments and displacements, consider the downlink configuration, i.e., from the buoy to the AUV, and see the impact of different parameters. Consider a (fixed) LED Lambertian order of $m = 20$, corresponding to a beam divergence of about 15° , a (fixed) large Rx FoV $\phi_{\text{FoVr}} = \pi/2$, and a link range of 65 m. For the three cases specified in Subsections IV-A, IV-B, and IV-C, are presented in Fig. 5 the outage probability versus the corresponding misalignment parameter, i.e., U , σ_{θ_r} , and σ_{pr} , respectively.

Notice the good match between the simulation-based (statistical MC) and analytical results, which shows the accuracy of the approximate analytical formulas. Indeed, they provide a tight lower bound on P_{out} for the considered operating conditions. From Fig. 5(a), for fixed (and exact) AUV position

⁷For very high data rates where the deadtime limitation induces inter-symbol interference, [61] proposed an optimal signal detection approach, based on the number of counts and arrival times of the photons. Also, appropriate signaling schemes were proposed in [37], [62] for the case of limited Tx/Rx modulation BW with respect to the data rate.

⁸For instance, some ultra-short baseline (USBL) underwater acoustic positioning systems used for AUVs, such as the Subsonus USBL and its corresponding transponder, Subsonus tag, have their respective pitch and roll accuracies as $\sim 0.1^\circ$ and $\sim 1^\circ$ [65], [66]. Also, the position accuracies of Subsonus USBL and Subsonus tag are around 0.5 and 1.5 m, respectively, at a typical range of 100 m [65], [66].

TABLE I
Simulation Parameters

Parameter	Value
Tx wavelength λ	470 nm
Tx average transmit power P_{Tx}	20 W
OOK extinction ratio ξ	0.4
Bit rate R_b	1 Mbps
Optical filter BW	20 nm
SiPM active area A_{PD}	9 mm ²
SiPM, number of SPADs	10998
SiPM, fill factor	48 %
SiPM gain G	10 ⁶
SiPM photon detection efficiency Υ_{PDE}	24 %
SiPM dark count rate f_{DCR}	6.6 MHz
SiPM dark current I_d	1.10 μ A
SiPM prob. of cross-talk P_{CT}	0.03 %
SiPM prob. of after-pulsing P_{AP}	0.2 %
SiPM deadtime τ_d	90 ns
SiPM excess noise factor F	1.1
TIA load resistance R_L	1 k Ω
Target BER, BER_{th}	2×10^{-3}

and orientation, notice a significant impact of the wind speed U on the link performance. Comparing this with Fig.5(b), notice that AUV angular misalignments have a less significant impact on P_{out} ; it is almost unaffected for σ_{θ_r} up to 10° corresponding to little angular deviations of the Rx from the beam LoS. For angular deviations larger than $\sim 15^\circ$ (which is close to the considered Tx beam divergence), a significant P_{out} degradation is noticed as the Rx largely turns away from the beam spot.

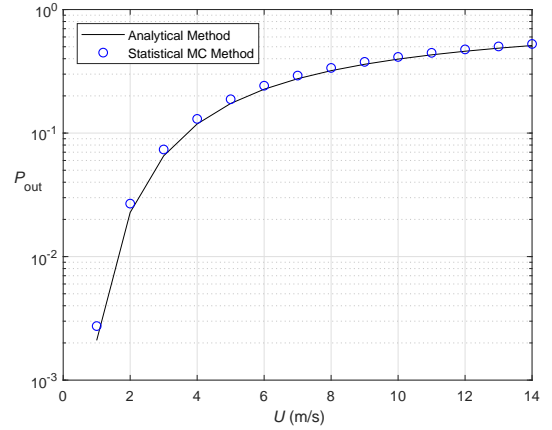
For Fig. 5(c), following our approach in Subsection IV-C for the derivation of the analytical PDF of h , we have set $\varphi_t = \varphi_r = 30^\circ$, and calculated P_{out} for a fixed displacement $x_r = y_r$. Notice a significant performance degradation with displacement error. For $x_r = y_r \gtrsim 5$ m, P_{out} is almost equal to one, meaning that the Rx is completely away from the transmitted beam LoS.

Similar to Fig. 5(a), we have further presented in Fig.6 P_{out} as a function of the average transmit power P_{Tx} and the sea surface wind speed U , assuming exactly positioned Rx. We notice that with increase in U , an increase in P_{Tx} can only marginally compensate for this P_{out} degradation. However, it will be shown in the following subsection that the optimization of the Tx/Rx parameters can improve the link performance considerably.

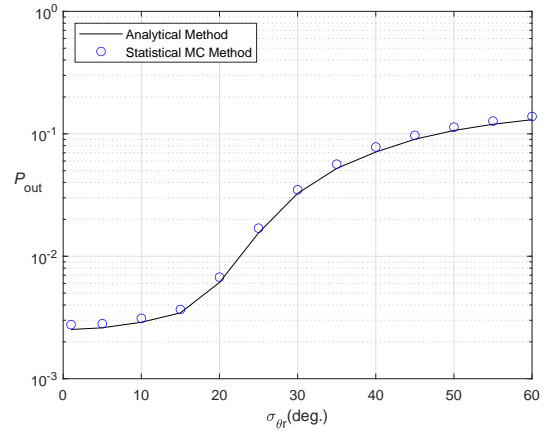
C. Effect of Tx/Rx Parameter Optimization, Buoy-to-AUV Downlink

For different link conditions, we investigate the effect of optimizing Tx and Rx parameters, i.e., m and ϕ_{FoVr} for limited Rx FoV. Two scenarios are considered: without and with Rx position displacement. The presented results are obtained using MC simulations.

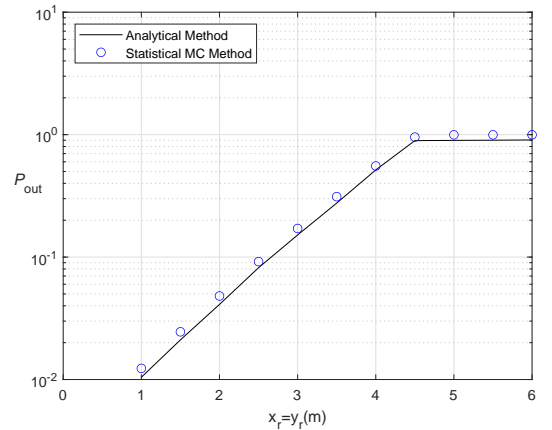
1) *Scenario 1: Negligible Rx position displacement:* Consider first the case where there is no position displacement for the Rx, see Fig.3. Figure7 shows the 3D plot of P_{out} versus m and ϕ_{FoVr} for $U = 3$ m/s and $\sigma_{\theta_r} = 5^\circ$. We notice that significant performance improvement can be obtained by



(a) Tx angular misalignments and fixed Rx



(b) Tx-Rx angular misalignments and fixed Rx



(c) Tx-Rx angular misalignments and Rx displacements

Fig. 5. Effect of misalignment parameters on P_{out} performance using the analytical and statistical MC approaches; Downlink transmission with $m = 20$, $P_{Tx} = 20$ W, $\xi = 0.4$, $\phi_{FoVr} = \pi/2$, and $Z = 65$ m; (a) $\sigma_{\theta_r} = 0$, $\sigma_{pr} = 0$; (b) $U = 1$ m/s, $\sigma_{pr} = 0$; (c) $U = 1$ m/s, $\sigma_{\theta_r} = 5^\circ$.

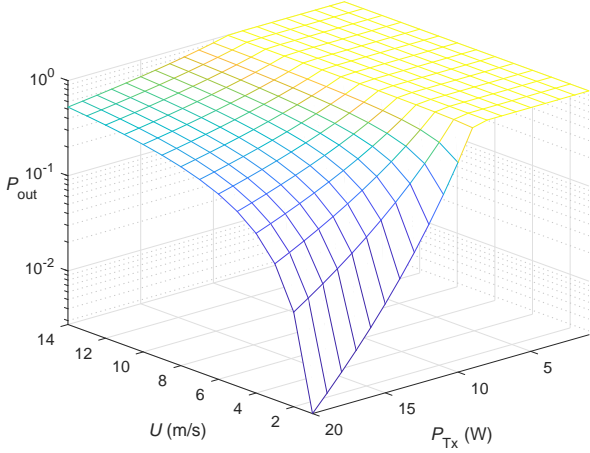


Fig. 6. Effect of wind speed U and the average transmit power P_{Tx} on the P_{out} ; $\sigma_{\theta_r} = 0$, $\sigma_{pr} = 0$, $m = 20$, $\xi = 0.4$, $\phi_{FoVr} = \pi/2$, and $Z = 65$ m.

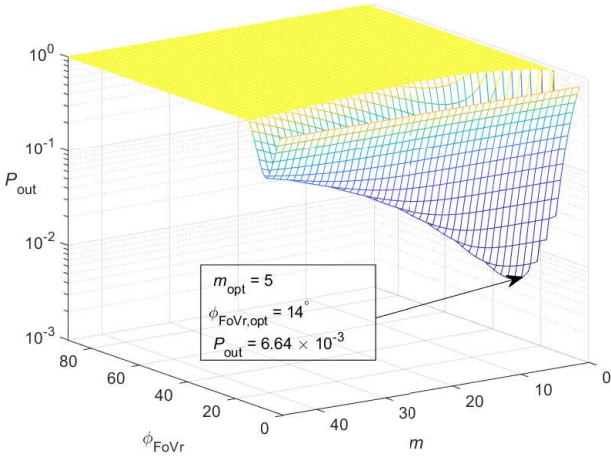


Fig. 7. Scenario 1: Effect of m and ϕ_{FoVr} (in degrees) on P_{out} for $U = 3$ m/s and $\sigma_{\theta_r} = 5^\circ$. $Z = 100$ m, $P_{Tx} = 20$ W.

using the optimal parameters in terms of reducing the outage probability, here, $m_{opt} \approx 5$ and $\phi_{FoVr,opt} \approx 14^\circ$ resulting in the minimum $P_{out} = 6.64 \times 10^{-3}$.

Subsequently, for increased wind speeds of $U = 6$ and 9 m/s and $\sigma_{\theta_r} = 5^\circ$, we have shown in Fig. 8 plots of P_{out} versus m . To simplify the presentation in a 2D plot, we have considered for each m the corresponding $\phi_{FoVr,opt}$ resulting in the minimum P_{out} . As reference to the results in Fig. 7, we have also shown the P_{out} plot for $U = 3$ m/s. These results clearly show the destructive impact of U on the link performance. Also, optimized Tx-Rx parameters allow a significant improvement in the link performance; the optimum parameters and the corresponding P_{out} values are indicated in the figure. We notice that for increased U , a smaller m should be used. This is quite rational, since by increased Tx angular misalignments, we should use a wider Tx beam to minimize the probability of receiving a too weak signal at the Rx. In other words, surface waves are more likely to direct the signal

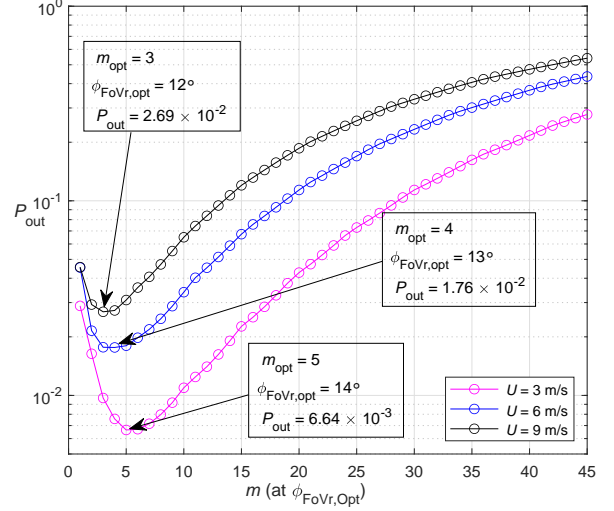


Fig. 8. Scenario 1: Effect of m on P_{out} using optimum ϕ_{FoVr} for $U = 3, 6,$ and 9 m/s and $\sigma_{\theta_r} = 5^\circ$. $Z = 100$ m, $P_{Tx} = 20$ W.

TABLE II
SCENARIO 1 (DOWNLINK): OPTIMUM PARAMETERS FOR DIFFERENT σ_{θ_r} OF AUV RX DISORIENTATION; $U = 3$ m/s, $Z = 100$ m, $P_{Tx} = 20$ W.

σ_{θ_r} (deg.)	m_{opt}	$\theta_{FoVr,opt}$ (deg.)	P_{out}	P_{int}
5	5	14	6.64×10^{-3}	5.1×10^{-3}
7	6	15	3.84×10^{-2}	3×10^{-2}
10	8	16	1.17×10^{-1}	8.9×10^{-2}

away from the Rx FoV, thus the beam should be widened to insure the signal reaches the Rx. The optimum Rx FoV values are rather close; yet, $\phi_{FoVr,opt}$ decreases by increasing U : it equals 14° , 13° , and 12° , for $U = 3, 6,$ and 9 m/s, respectively. To explain this, we note from (1) and (2) that the effective Rx area A_{eff} is inversely related to ϕ_{FoVr} due to the use of a non-imaging concentrator. Hence, a decrease in $\phi_{FoVr,opt}$ arising from an increased U is justified by achieving a larger effective light collection area, compensating for more pointing errors.

To see the effect of the Rx's σ_{θ_r} , we have fixed U at 3 m/s and increased σ_{θ_r} to 7° and 10° . Results are summarized in Table II, where we have also provided the corresponding values of P_{int} . From these results, we notice a rather low sensitivity of m_{opt} and $\theta_{FoVr,opt}$ to σ_{θ_r} . Interestingly, as σ_{θ_r} increases, the beam needs to be more directive (m should be increased) and the Rx FoV should increase. Indeed, increasing m increases the directivity of the transmit beam towards the normal of the Rx, while the increase in the Rx FoV aims to improve signal reception for larger Rx deviations.

Let us now investigate the effect of the average transmit power on the parameter optimization. We have summarized the results in Table III, where we notice that by decrease in P_{Tx} , m_{opt} is increased, i.e., the beam is made more directive to reduce the effect of geometric loss, while $\phi_{FoVr,opt}$ is decreased to increase the Rx effective area of light collection. Overall, these two factors compensate for the reduced signal-to-noise

TABLE III
SCENARIO 1 (DOWNLINK): OPTIMUM PARAMETERS FOR
DIFFERENT P_{Tx} ; $U = 3$ m/s, $\sigma_{\theta_r} = 5^\circ$, $Z = 100$ m.

P_{Tx} (W)	m_{opt}	$\phi_{FoVr,opt}$ (deg.)	P_{out}	P_{int}
30	4	16	1.5×10^{-3}	1.4×10^{-3}
20	5	14	6.64×10^{-3}	5.1×10^{-3}
10	7	11	4.67×10^{-2}	2.78×10^{-2}

TABLE IV
SCENARIO 1 (DOWNLINK): OPTIMUM PARAMETERS FOR
DIFFERENT LINK SPANS Z ; $U = 3$ m/s, $\sigma_{\theta_r} = 5^\circ$, $P_{Tx} = 20$ W.

Z (m)	m_{opt}	$\theta_{FoVr,opt}$ (deg.)	P_{out}	P_{int}
90	3	20	3.39×10^{-5}	3.1×10^{-5}
100	5	14	6.64×10^{-3}	5.1×10^{-3}
110	6	9	7.81×10^{-2}	7.17×10^{-2}

ratio (SNR) with decrease in P_{Tx} . We have further presented in Table IV the results for different link ranges. Logically, the trend in m_{opt} and $\phi_{FoVr,opt}$ with increase in Z is the same as with decrease in P_{Tx} . We notice that, as the Tx-Rx distance increases, m_{opt} is increased while $\phi_{FoVr,opt}$ is decreased.

2) *Scenario 2: Considering Rx position displacement:* Let us now include in the considered link configuration the deviations in the position of the AUV Rx with respect to the buoy Tx. We have presented in Table V the results for $U = 3$ m/s, $\sigma_{\theta_r} = 5^\circ$, and different values of the Rx displacement standard deviation σ_{pr} . The case of $\sigma_{pr} = 0$ corresponds to the results previously presented in Fig. 7. Reasonably, with an increase in σ_{pr} , the corresponding P_{out} and P_{int} increase. For more important displacements, i.e., higher σ_{pr} , we need to widen the Tx beam (by decreasing m) and increase the effective Rx area (by decreasing ϕ_{FoVr}). Meanwhile, notice the small change in the optimum parameters m_{opt} and $\phi_{FoVr,opt}$ with increase in σ_{pr} . This can be explained by the fact that, given the Tx beam divergence and the link range, the Rx displacements are not significant compared to the beam spot radius. This latter is considered as the radius where we get the half intensity with respect to the beam center, which is around 30 m for $m = 5$, for instance.

D. Effect of Tx/Rx Parameter Optimization, AUV-to-Buoy Uplink

For the case of uplink transmission, i.e., from the AUV to the buoy, the angular misalignments are modeled by σ_{θ_t} (for

TABLE V
SCENARIO 2 (DOWNLINK): OPTIMUM PARAMETERS FOR
DIFFERENT σ_{pr} OF AUV RX DISPLACEMENTS; $U = 3$ m/s, $\sigma_{\theta_r} = 5^\circ$,
 $Z = 100$ m, $P_{Tx} = 20$ W.

σ_{pr} (m)	m_{opt}	$\theta_{FoVr,opt}$ (deg.)	P_{out}	P_{int}
0	5	14	6.64×10^{-3}	5.1×10^{-3}
2	5	14	1.02×10^{-2}	6.5×10^{-3}
6	4	13	4.66×10^{-2}	4.03×10^{-2}
12	4	13	2.8×10^{-1}	2.33×10^{-1}

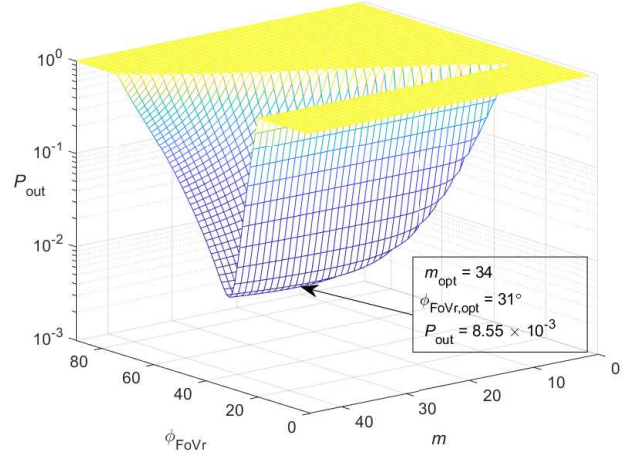


Fig. 9. Scenario 3: Effect of m and ϕ_{FoVr} on P_{out} for the uplink. AUV's Tx with $\sigma_{\theta_t} = 5^\circ$ and Buoy's Rx with $U = 3$ m/s, $Z = 100$ m, $P_{Tx} = 20$ W.

the Tx) and U (for the Rx), respectively.

1) *Scenario 3: Negligible Tx position displacement:* Figure 9 shows the 3D plots of P_{out} versus m and ϕ_{FoVr} for $\sigma_{\theta_t} = 5^\circ$ at the Tx and $U = 3$ m/s at the Rx side. The optimum parameters⁹ are $m_{opt} = 34$ and $\phi_{FoVr,opt} = 31^\circ$, resulting in the minimum achievable $P_{out} = 8.55 \times 10^{-3}$.

Similar to Subsection V-C, keeping U at 3 m/s, we have presented in Fig. 10 the 2D plots of P_{out} versus m for $\sigma_{\theta_t} = 5^\circ$, 7° , and 10° . For each m , ϕ_{FoVr} is selected so as to result in the minimum P_{out} . Like for the downlink case in the previous subsection, as σ_{θ_t} is increased (from 5° to 7° and 10°), the beam needs to be widened (i.e., m_{opt} decreases from 34 to 30, and 26), and the effective area of light collection should be increased (i.e., $\phi_{FoVr,opt}$ decreases from 31° to 29° , and 27°). Once again, the Tx-Rx parameter optimization trades off geometric loss (related to beam divergence) with the Rx concentrator gain (related to the Rx FoV).

To see better the impact of U , we set σ_{θ_t} to 5° and vary U from 3 to 6 and 9 m/s. The optimum parameters together with the minimum P_{out} and P_{int} are given in Table VI. We notice that for increased U , the respective m_{opt} and $\phi_{FoVr,opt}$ increase as well, which is consistent with the results presented for Scenario 1 in the previous subsection: The increase in the Rx angular misalignments is compensated by the increase in m (to make the beam more directive, and hence reduce the geometric loss), and an increase in ϕ_{FoVr} (to improve signal reception for larger Rx deviations although this also results in a smaller concentrator gain).

2) *Scenario 4: Considering Tx position displacement:* Including now into the link configuration the position displacements of the AUV Tx, Table VII shows the optimum parameters and the performance metrics for $U = 3$ m/s, $\sigma_{\theta_t} = 5^\circ$, and four values of $\sigma_{pr} = 0, 2, 6$, and 12 m. Notice the

⁹Note that the larger values of optimum parameters, compared to those of the previously discussed downlink, is due to the difference in the Tx distribution, and subsequently the parameters affecting their angular misalignment.

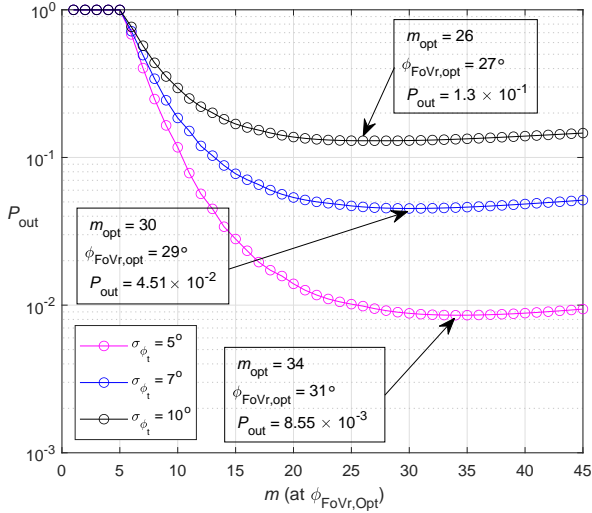


Fig. 10. Scenario 3: Effect of m for an optimum $\phi_{\text{FoVr,opt}}$ on P_{out} for AUV's Tx σ_{θ_t} of 5° , 7° , and 10° at Buoy's Rx $U = 3$ m/s. $Z = 100$ m, $P_{\text{Tx}} = 20$ W.

TABLE VI

SCENARIO 3 (UPLINK): OPTIMUM PARAMETERS FOR DIFFERENT WIND SPEEDS U AFFECTING THE BUOY RX. NEGLIGIBLE TX (AUV) DISPLACEMENT; $\sigma_{\theta_t} = 5^\circ$. $Z = 100$ m, $P_{\text{Tx}} = 20$ W.

U (m/s)	m_{opt}	$\theta_{\text{FoVr,opt}}$ (deg.)	P_{out}	P_{int}
3	34	31	8.55×10^{-3}	2×10^{-3}
6	44	35	2.05×10^{-2}	5×10^{-3}
9	45	38	3.34×10^{-2}	7.7×10^{-3}

TABLE VII

SCENARIO 4 (UPLINK): OPTIMUM PARAMETERS FOR DIFFERENT AUV TX DISPLACEMENT STANDARD DEVIATIONS σ_{pt} ; $\sigma_{\theta_t} = 5^\circ$, $U = 3$ m/s. $Z = 100$ m, $P_{\text{Tx}} = 20$ W.

σ_{pt} (m)	m_{opt}	$\theta_{\text{FoVr,opt}}$ (deg.)	P_{out}	P_{int}
0	34	31	8.55×10^{-3}	2×10^{-3}
2	37	32	1.29×10^{-2}	2.2×10^{-3}
6	40	33	5.8×10^{-2}	1.28×10^{-2}
12	43	34	3.15×10^{-1}	1.19×10^{-1}

relatively close optimum parameters for the considered cases. This can be justified by the fact that such small displacements impact negligibly the signal reception, given the relatively large size of the beam spot at the Rx side (which is around 17.5 m for $m = 34$, for instance; see also Subsection V-C2). In fact, with increase in σ_{pt} , m_{opt} and $\phi_{\text{FoVr,opt}}$ should increase to make the beam more directional on one hand (to decrease the geometric loss), and increase the Rx FoV on the other hand (to improve signal reception). For instance, by increasing σ_{pt} from 0 to 2 m, m_{opt} and $\phi_{\text{FoVr,opt}}$ are increased from 34 to 37, and from 31° to 32° , respectively.

VI. CONCLUSIONS

This paper studies the design of a bi-directional UWOC link between the sea surface and a mobile underwater unit. The presented analysis revealed that a substantial improvement in the link performance can be obtained by optimizing the main

link parameters, namely the Tx Lambertian order and the Rx FoV. The corresponding optimal parameters depend on the channel and link deployment parameters including the sea-surface wind speed, AUV stability and positioning accuracy, and the received power. Note that the received power depends on the the link range (here, the operation depth of the AUV) and the transmit power, for which the dependence of the optimal parameters was shown.

In practice, these link parameters can be estimated either at the Tx or at the Rx and be shared with the other side of the link in real time in order to adapt Tx-Rx parameters. This assumes, of course, a bi-directional transmission between the two ends of the link. Note that in the case that one of the terminals is not equipped with an optical transmitter, sending the estimated channel parameters to the other side of the link can be done using an acoustic link given the corresponding required low data rate.

The buoy can use a gyroscope or an accelerometer in order to estimate the underlying conditions (i.e., the wind surface speed) in real time. Also, depending on the positioning system used by the AUV and the operational conditions, the displacement and angular misalignment variances can be estimated. Lastly, given the estimated link parameters, the Tx beam divergence can be adjusted using a diffuser in front of the LED, whereas the Rx FoV can be changed using a mechanical iris in front of the Rx lens. For a practical implementation, the Tx beam-width and the Rx FoV could be selected amongst a discrete set of available values (using the closest values to the optimally calculated ones).

Future research concerns Tx/Rx parameter optimization taking into account the effect of other channel impairments such as oceanic turbulence and solar background noise, as well as the dependence of the optical filter transmittance on the incidence angles of the optical rays.

ACKNOWLEDGMENT

This work was partly supported by Alex Ekwueme Federal University Ndufu-Alike (AE-FUNAI) in partnership with the Embassy of France in Nigeria and Campus France. The authors also acknowledge the support received from the French Embassy in Canada under the France Canada Research Funds program. The authors would like to thank Dr. Mohammad Taghi Dabiri from the Iran Telecommunication Research Center, Tehran, Iran, Mr. Oussama Haddad and Mr. Taha Essalih from Fresnel Institute, Marseille, France, and Mr. Abdallah S. Ghazy and Mr. Tau Raphael Rasethunsa from McMaster University, Hamilton, Canada, for the fruitful discussions on channel modeling and analytical derivations, as well as Dr. Fabien Lemarchand from Fresnel Institute for discussions on the practical design of optical filters. They are also very grateful to Mr. Yves Chardard from SubseaTech Co., Marseille, and Mr. Christian Marfia from IFREMER, La Seyne-sur-Mer, France, for the practical considerations concerning practical AUV positioning parameters. This publication is also based upon work from COST Action CA19111 (European Network on Future Generation Optical Wireless Communication Technologies, NEWFOCUS), supported by COST (European Cooperation in Science and Technology).

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