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# Dipole Polarizability of $C_{28}$ and its Counterparts $Nb_4B_{18}$ and $Ta_4B_{18}$ . Insights from a Density Functional Theory (DFT) Endeavour

**Demetrios Xenides\***

Laboratory of Predictive Analytics and Complex Systems, Department of Economics, School of Management and Economics, University of Peloponnese, Tripolis Campus, 22100, Greece

E-mail: [xenides@uop.gr](mailto:xenides@uop.gr)

**Panagiotis Karamanis**

Equipe de Chimie Théorique, ECP Institut des Sciences Analytiques et de Physico-chimie pour l'Environnement et les Matériaux (IPREM) UMR 5254, Hélioparc Pau Pyrénées 2 avenue du Président Angot, 64053 Pau Cedex 09, France

E-mail: [panagiotis.karamanis@univ-pau.fr](mailto:panagiotis.karamanis@univ-pau.fr)

**Abstract.** We report on a preliminary investigation of the non linear optical (NLO) properties and in particular dipole polarizability. The target species are two perfect tetrahedral nanoclusters  $Nb_4B_{18}$  and  $Ta_4B_{18}$ , along with their nanofullerene counterpart that is  $C_{28}$ . Our study based on density functionals (DFs) that have gained popularity among the scientific community. In addition we performed Hartree-Fock calculations known for not including dynamic electron correlation. The DF obtained values are characterized by some dispersion, with maximal differences to be around 5 %, in all three cases. Given that the DFT introduces a fuzzy percentage of electron correlation sets the observed convergence of HF values to DFT ones is at least surprising. Furthermore, it should be said that though the values can be characterized as accurate their reliability should not be taken for granted. Last, we note the smooth convergence of LC-BLYP, LC-BP86, LC-BPW91 to LC- $\omega$ hPBE.

## 1. Introduction

The study of the field of nanoclusters emerged as a need to bridge the gap between molecules and matter. Species of this type are building blocks of larger architectures. As such  $Nb_4B_{18}$  and  $Ta_4B_{18}$  after self-assembling could form the respective face central crystals  $M_4B_{15}$  ( $M=Nb, Ta$ ) [1].

On the other hand the importance of dipole polarizability ( $\alpha_{\alpha\beta}$ ) has been elegantly described in the excellent book by Bonin and Kresin [2]. This list has been extended by studies relate it to hardness-softness [3], aromaticity [4], and other important natural phenomena such as electrostatic interactions that involve molecular polarization [5].

For these reason we have put some effort in calculating dipole polarizabilities of  $Nb_4B_{18}$  and  $Ta_4B_{18}$  in Density Functional Theory (DFT) levels of theory and for the shake of comparison at Hartree-Fock, as well. The DFT methods are still the only alternative as the size of the

architecture grows. Therefore, it seems mandatory to check their accuracy and reliability in such calculations.

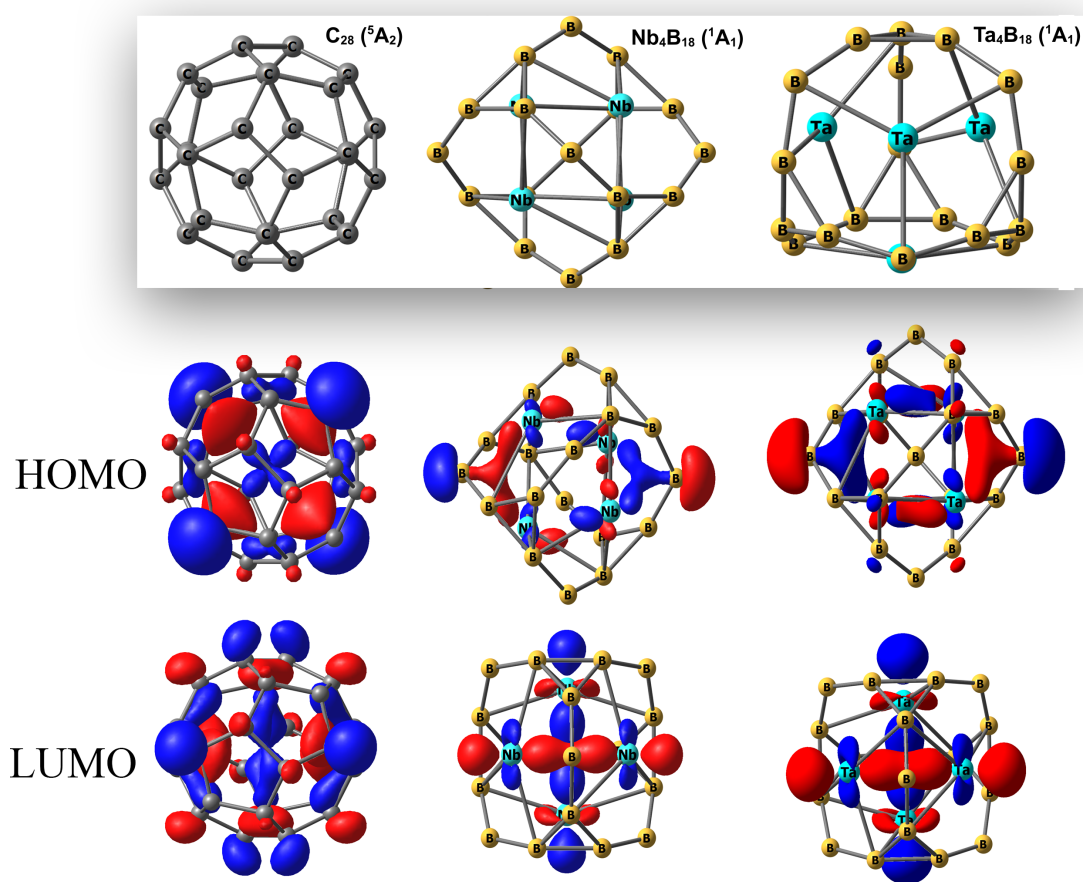
## 2. Computational Details

We have calculated dipole polarizability ( $\alpha_{\alpha\beta}/e^2\alpha_0^2E_h^{-1}$ ) via the Finite Field approach. To ensure the reliability of the method we have used carefully selected field strengths of 0.003 au.

Basis sets of TZVP quality have been used for B, C, Nb and Ta. For the latter two we have also implemented effective core potentials (ECPs) as to take into account the relativistic corrections related to the nature of the two heavy atoms. In particular, these two elements have been described by the def2-TZVP basis set obtained from *Basis Set Exchange* server [6]. All calculations have been performed with Gaussian 16 package [7].

The methods used in the present study are Hartree-Fock (HF) [9], B-[10] and B3-{LYP,P86,PW91} [11, 12, 13, 14], PBE1PBE [15] and HSEH1PBE [16], CAM-B3LYP [17], LC- $\omega$ PBE [18] as well as LC-{BLYP, BP86, BPW91}, M05 [19] and M052x [20], M06 and M062x [21], M08 [22],  $\omega$ B97xD [23] and BMK [25] In the case of  $C_{28}$  ( ${}^5A_2$ ) all the above methods have been applied at the restricted open (RO) formulation.

In Fig. 1 we have drawn the structure of the three nanoclusters under study. We further add a picture of the HOMO and LUMO orbitals of them as to gain information on the shape of the frontier orbitals.



**Figure 1.** Structure and HOMO LUMO orbitals of and  $C_{28}$   $Nb_4B_{18}$  and  $Ta_4B_{18}$ .

### 3. Results and Discussion

In the case of  $C_{28}$  the majority of DFT methods produce dipole polarizability values that are greater than the respective RO-HF ones. However, there are the LC-BLYP, LC-BP86, LC-BPW91 and LC- $\omega$ hPBE methods that diverge from the trend of the rest of DFT ones. That is the LC correction strongly affects the predictive capability of DF methods. Surprisingly enough the values of the LC methods are closer to ROHF ones, as it can be seen in Fig. 2. In particular the ROHF value is 246.4 when the LC- $\{BLYP, BP86, BPW91, \text{ and } \omega hPBE\}$  are 246.9, 247.7, 245.5 and 246.2, respectively. The others are lying in the vicinity of 255 as it can be also seen in Table 1. The same trend had been observed in a study by Sekino et al [26] on dipole (hyper)polarizabilities of polydiacetylene and polybutatriene.

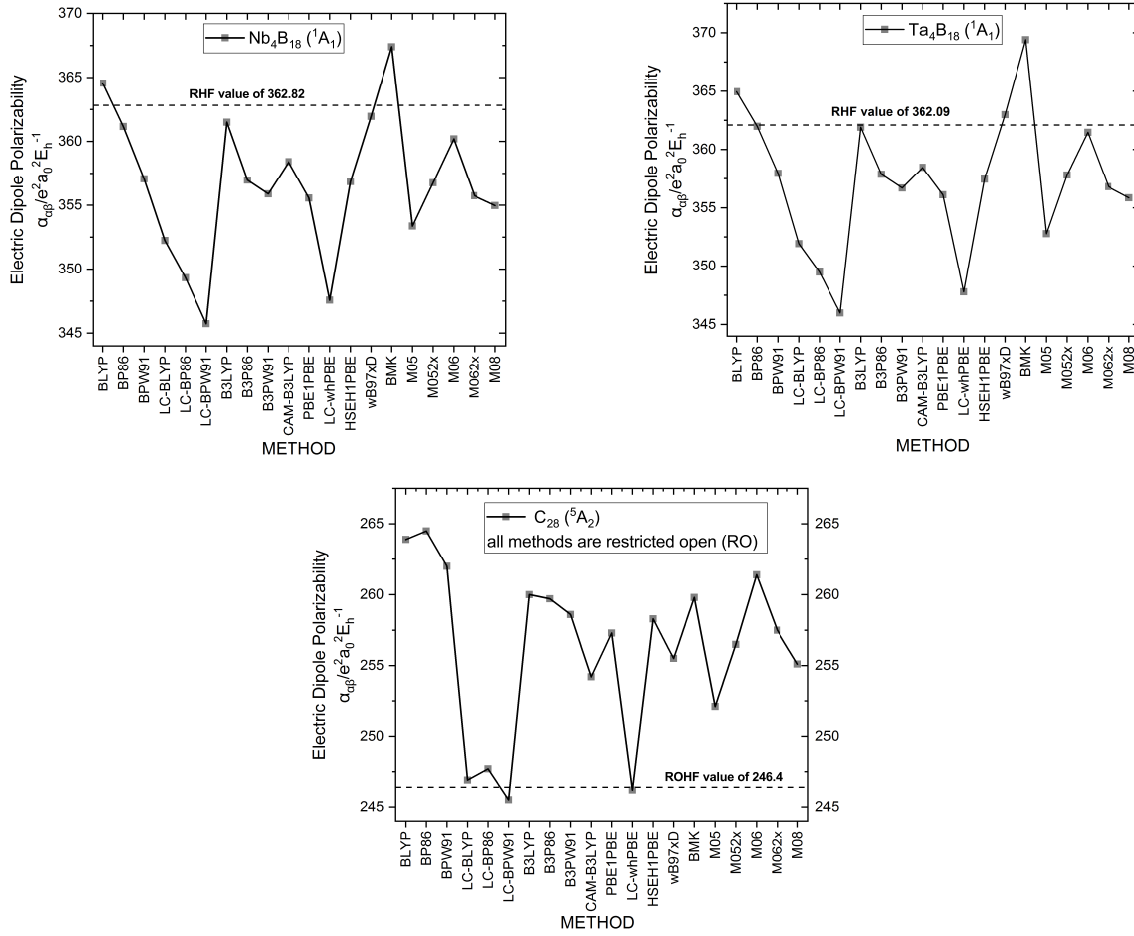
**Table 1.** Dipole polarizability values of  $C_{28}$ ,  $Nb_4B_{18}$ , and  $Ta_4B_{18}$  at HF and DFT levels of theory (*restricted open (RO) shell calculations have been performed in the case of  $C_{28}$* ).

	$C_{28}$	$Nb_4B_{18}$	$Ta_4B_{18}$
HF	246.4	362.82	362.09
BLYP	263.9	364.56	364.95
BP86	264.5	361.15	361.98
BPW91	262.0	357.07	357.95
LC-BLYP	246.9	352.24	351.92
LC-BP86	247.7	349.32	349.49
LC-BPW91	245.5	345.74	345.99
B3LYP	260.0	361.49	361.91
B3P86	259.7	356.96	357.87
B3PW91	258.6	355.89	356.69
CAM-B3LYP	254.2	358.40	358.47
PBE1PBE	257.3	355.56	356.12
LC- $\omega$ hPBE	246.2	347.57	347.79
HSEH1PBE	258.3	356.84	357.45
$\omega$ B97xD	255.5	361.95	362.98
BMK	259.8	367.39	369.41
M05	252.1	353.38	352.77
M052x	256.5	356.75	357.81
M06	261.4	360.19	361.46
M062x	257.5	355.74	356.81
M08	255.1	354.97	355.86

Quite opposite is the behaviour of the methods in the case of  $M_4B_{18}$  ( $M=Nb, Ta$ ) nanoclusters.

When  $M=Nb$  the BLYP(364.56), BP86(361.15), B3LYP(361.49) and  $\omega$ B97xD(361.95) values are quite close to the HF(362.82). We note that in contrast to the rest of the methods BLYP(364.56) and BMK(367.39) values are larger than the HF ones. The LC correction affected the most the obtained values. This can be seen as a sharp lowering of the obtained values. In particular LC- $\{BLYP, BP86, BPW91 \text{ and } \omega hPBE\}$  values are 352.24, 349.32, 345.74 and 347.57, respectively. The M05 method produces a value of 353.38, that is the one being close to the LC family. The other functionals produce values that are in between 355 and 360 au.

For  $M$  being  $Ta$ , the BP86(361.98), B3LYP(361.91), M06(361.46) and  $\omega$ B97xD(362.98) are the ones that are noticeable proximal to HF(362.09) one. A smooth convergence of LC-BLYP,



**Figure 2.** Dipole polarizabilities of  $Nb_4B_{18}$ ,  $Ta_4B_{18}$  and  $C_{28}$ .

LC-BP86, LC-BPW91 values (351.92, 349.49, 345.99) to LC- $\omega$ hPBE (347.79) has been also observed. Once again M05 (352.77) resembles the LC family results.

What we have seen from the above made analysis is that in all three cases DFs methods caused a positive (enhancement) or negative (lowering) of the respective HF dipole polarizability values. Furthermore, it is known that DFs methods introducing a (fuzzy) percentage of dynamic electron correlation. That is the reason of gaining their popularity (along with the fact that they need moderate computational resources). In the present study the DFs produced results differ by the most of 5 % from the HF ones. Moreover, it is the nature of them that does not allow for naming one of them as method of preference. That, probably, justifies the question of whether there is a need of a calculation of DFT type when a HF one produces similar results, without the accompanying uncertainty of the DFT methods.

Last but not least, we note the remarkably similarity of dipole polarizability of both  $M_4B_{18}$  ( $M=Nb, Ta$ ). Thus, it is fair to assume that the nature of the heavy atom has a negligible effect on this interesting property.

#### 4. Conclusion

Having performed restricted open shell calculations on the  $C_{28}$  ( $^5A_1$ ) fullerene we found that most of the functionals enhance the value of dipole polarizability. In striking difference is the LC-({BLYP, BP86, BPW91,  $\omega$ hPBE}) family of functionals that produces results quite similar

to ROHF ones. The inverse has been observed in  $M_4B_{18}$  ( $M=Nb, Ta$ ) nanoclusters. In particular DF methods lower the value of Hartree-Fock polarizability. This is most intense in the case of LC family. However, in all cases the DFT values are around 5 % lower or greater than the HF ones. This could raise the question whether there is a need of calculation of DF type instead of a pure HF one, that it is known for its limitations. Last, we note that both heavy metal including moieties are characterized by almost identical dipole polarizability values. Therefore, it is fair to assume that there is a negligible effect of the nature of heavy atom on the value of dipole polarizability.

## 5. References

- [1] Zhang Y and Lu X and Yan M and Li S-d, Perfect Spherical Tetrahedral Metallo-Borospherene  $Ta_4B_{18}$  as a Superatom Following the 18-Electron Rule (2021), *ACS Omega* **6**, 10991–10996.
- [2] Bonin K D and Kresin V V, Electric-Dipole Polarizabilities of Atoms, Molecules, and Clusters (1997), World Scientific.
- [3] Hati S and Datta D, Hardness and Electric Dipole Polarizability. Atoms and Clusters (1994), *J. Phys. Chem. A* **98**, 10451–10454.
- [4] Jartín R. S. Cuesta I G and Sánchez de Merás A and Lazzeretti P, Can aromaticity be connected with molecular polarizability? A theoretical study of benzene isomers and five-membered heterocyclic molecules (2004), *J. Comp. Methods in Sc. Eng.* **4**, 665–676.
- [5] Israelachvili J N, Interactions Involving the Polarization of Molecules, in Intermolecular and Surface Forces (Third Edition) (2011), pp 91–106, Academic Press, San Diego.
- [6] Pritchard B P and Altarawy D and Didier B and Gibson T D and Windus T L, A New Basis Set Exchange: An Open, Up-to-date Resource for the Molecular Sciences Community , *J. Chem. Inf. Model.* (2019), **59**, 481–4820.
- [7] Gaussian 16, Revision C.01, M. J. Frisch et al, Gaussian, Inc., Wallingford CT, 2019.
- [8] Becke A D, A new mixing of Hartree-Fock and local density-functional theories (1993), *J. Chem. Phys.* **98**, 1372–77.
- [9] Roothaan C C J, New Developments in Molecular Orbital Theory (1951), *Rev. Mod. Phys.* **23**, 69–89.
- [10] Becke A D, Density-functional exchange-energy approximation with correct asymptotic-behavior (1988), *Phys. Rev. A* **38**, 3098-100.
- [11] Becke A D, Density-functional thermochemistry. III. The role of exact exchange (1993), *J. Chem. Phys.* **98**, 5648–52;
- [12] Lee C, Yang W and Parr E G, Development of the Colle-Salvetti correlation-energy formula into a functional of the electron density (1988), *Phys. Rev. B* **37**, 785–9; Miehlich B et al, Results obtained with the correlation-energy density functionals of Becke and Lee, Yang and Parr (1989), *Chem. Phys. Lett.* **157**, 200–206.
- [13] Perdew J P, Density-functional approximation for the correlation energy of the inhomogeneous electron gas (1986), *Phys. Rev. B* **33**, 8822–4.
- [14] Perdew J P, in Electronic Structure of Solids (1991), Akademie Verlag, Eds Ziesche P and Eschrig H, Berlin; Perdew J P et al, Atoms, molecules, solids, and surfaces: Applications of the generalized gradient approximation for exchange and correlation (1992) *Phys. Rev. B* **46**, 6671–87; Perdew A J et al, Erratum: Atoms, molecules, solids, and surfaces: Applications of the generalized gradient approximation for exchange and correlation (1993), *Phys. Rev. B* **48**, 4978; Perdew J P, Burke K and Wang Y, Generalized gradient approximation for the exchange-correlation hole of a many-electron system (1996), *Phys. Rev. B* **54**, 16533–9; Burke K, Perdew J P and Wang Y, in Electronic Density Functional Theory: Recent Progress and New Directions (1998), Eds Dobson J F, Vignale G and Das M P, Akademie Verlag (Plenum).
- [15] Perdew J P, Burke K and Ernzerhof M, Generalized gradient approximation made simple (1996), *Phys. Rev. Lett.* **77**, 3865–8; Perdew J P, Burke K and Ernzerhof M, Errata: Generalized gradient approximation made simple (1996), *Phys. Rev. Lett.* **78**, 1396; Errata: Generalized gradient approximation made simple, *Phys. Rev. Lett.* **78**, 1396.
- [16] Heyd J and Scuseria G E and Ernzerhof M, Erratum: Hybrid functionals based on a screened Coulomb potential (2006) , *J. Chem. Phys.* **124** 219906; Henderson T M and Izmaylov A F and Scalmani G and Scuseria G E, Can short-range hybrids describe long-range-dependent properties? (2009), *J. Chem. Phys.* **131**, 044108
- [17] Yanai T, Tew D, and Handy N, A new hybrid exchange-correlation functional using the Coulomb-attenuating method (CAM-B3LYP) (2004), *Chem. Phys. Lett.* **393**, 51–57.
- [18] Vydrov O A, Scuseria G E, Assessment of a long range corrected hybrid functional (2006), *J. Chem. Phys.*

- 125**, 234109; Vydrov O A et al, Importance of short-range versus long-range Hartree-Fock exchange for the performance of hybrid density functionals (2006), *J. Chem. Phys.* **125**, 074106; Vydrov O A et al, Tests of functionals for systems with fractional electron number (2007), *J. Chem. Phys.* **126**, 154109.
- [19] Zhao Y, Schultz N E and Truhlar D G, Exchange-correlation functional with broad accuracy for metallic and nonmetallic compounds, kinetics, and noncovalent interactions (2005), *J. Chem. Phys.* **123**, 161103.
- [20] Zhao Y and Schultz N E and Truhlar D G, Design of density functionals by combining the method of constraint satisfaction with parametrization for thermochemistry, thermochemical kinetics, and noncovalent interactions (2006), *J. Chem. Theory and Comput.* **2**, 364–82.
- [21] Zhao Y and Truhlar D G, The M06 suite of density functionals for main group thermochemistry, thermochemical kinetics, noncovalent interactions, excited states, and transition elements: two new functionals and systematic testing of four M06-class functionals and 12 other functionals (2008), *Theor. Chem. Acc.* **120**, 215–41.
- [22] Zhao Y and Truhlar D G, Exploring the limit of accuracy of the global hybrid meta density functional for main-group thermochemistry, kinetics, and noncovalent interactions (2008), *J. Chem. Theory Comput.* **4**, 1849–68.
- [23] Grimme S, Semiempirical GGA-type density functional constructed with a long-range dispersion correction (2006), *J. Comp. Chem.* **27**, 1787–99.
- [24] Chai J D and Head-Gordon M, Long-range corrected hybrid density functionals with damped atom-atom dispersion corrections (2008), *Phys. Chem. Chem. Phys.* **10**, 6615–20.
- [25] Boese A D and Martin J M L, Development of Density Functionals for Thermochemical Kinetics (2004), *J. Chem. Phys.* **121**, 3405–3416.
- [26] Kirtman B and Bonness S and Ramirez-Solis A and Champagne B and Matsumoto H and Sekino H, Calculation of electric dipole (hyper)polarizabilities by long-range-correction scheme in density functional theory: A systematic assessment for polydiacetylene and polybutatriene oligomers (2008), *J. Chem. Phys.* **128**, 114108.