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To cite this version:

Raphael Mermet-Lyaudoz, Pierre Combeau, Emmanuel Drouard, Anne Julien-Vergonjanne, Christian Seassal, et al.. Multiscale Simulation for Visible Light Communication using Perovskite Metasurface. 2021 17th International Symposium on Wireless Communication Systems (ISWCS), Sep 2021, Berlin, Germany. pp.1-6, 10.1109/ISWCS49558.2021.9562213. hal-03443483

HAL Id: hal-03443483 <https://hal.science/hal-03443483>

Submitted on 23 Nov 2021

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Multiscale Simulation for Visible Light Communication using Perovskite Metasurface

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Abstract—This article presents an original multi-scale simulation approach, enabling to rigorously compute the far-field radiation from emerging halide perovskite light-emitting diodes integrating a metasurface active layer, and subsequently to evaluate its impact on the propagation channel characteristics at the scale of an indoor environment, both in terms of coverage and time dispersion. Our results show that the high versatility of the metasurface design parameters allows the outage probability to be divided up to a factor 2 without degrading the temporal dispersion of the optical channel in visible light communication scenarios.

Index Terms—Halide perovskite, nanophotonics, metasurface, multi-scale simulation, visible light communications, Monte-Carlo Ray-Tracing.

I. INTRODUCTION

About 10 years ago [1], the solid-state lighting revolution for indoor illumination has promoted the emergence of visible light communications (VLC) or related light fidelity (LiFi), where light-emitting diode (LED) can provide both illumination and communication. Communication performance of theses systems are significantly impacted by the optical characteristics of the source, in both terms of lighting levels and radiation pattern [2].

Recently, the use of organic light emitting diodes (OLEDs) have been proposed mainly due to their integration flexibility and large active areas [3], [4]. However, their modulation bandwidth is low, limiting their use for high data rates applications.

Halide perovskites, as emerging materials with excellent optical and electrical properties, are prominent candidates for active medium in optoelectronic devices. The popularity of halide perovskites is often symbolized by its rising in photovoltaic applications as an alternative to silicon [5], with the power conversion efficiency of perovskite based solar cells now exceeds 25%. On the other hand, as direct-bandgap semiconductors, they are now also considered as an alternative to III-V semiconductor for emitting devices such as microlasers [6] and LED [7]. The record of halide perovskite based LED external efficiency has recently exceeded the 20% milestone [8]. Indeed, these materials combine strengths of the inorganic semiconductors and organic semiconductors, likely to solve the contradiction that high charge carrier mobility and large stimulated emissions are required for lasing devices but are not found generally in the same material. In particular, unlike OLEDs, halide perovskites LEDs exhibit key properties like long carrier diffusion lengths [9] and high refractive index, which is an important prerequisite to control lightmatter interaction. Moreover, unlike inorganic materials like GaN-based heterostructure, halide perovskite layers can be directly patterned at the sub-wavelength scale using scalable and high throughput technological processes like nanoimprint lithography [10]. The integration of such patterns in LEDs enables to control both the light emission spectra of halide perovskite thin films and their far-field emission pattern [11].

To evaluate communication performance, these light emission properties are first predicted using electromagnetic simulations. These characteristics are then used as input data in simulation tools of light propagation to assess the propagation

This work was funded by the french National Research Agency under the grant agreement no ANR-18-CE24-0016.

Fig. 1. Schemes of the (a) flat and (b) structured metasurface halide perovskite LED. Band diagram of the absorption within a (c) flat and (d) 1D grating structured perovskite layer. (e): Spectra of the absorption and the photoluminescence of the $CH_3NH_3PbBr_3$ perovskite.

channel in realistic environments. The main tools are based on Monte-Carlo ray-tracing (MCRT) algorithms which, from a 3D geometrical model of the propagation environment and the optical properties of the materials, allow computing the line-of-sight (LOS) and multi-reflected contributions between the source and the receiver [12].

This work presents first the use of resonant metasurfaces to engineer the photoluminescence (PL) emission of halide perovskite thin films. These metasurfaces are sub-wavelength periodic lattice which are directly obtained by patterning the halide perovskite thin film by thermal nanoimprint lithography. Their use allows enhancing the PL of perovskite and controlling on-demand the far-field emission pattern from quasi-isotropic emission to highly directional one. Then, these optical source data are considered in MCRT tool [13]–[15] to characterize the propagation channel in terms of optical DC gain and root mean square delay spread (DRMS). Thus, we propose a multi-scale simulation approach, from the device to the far-field propagation, with the perspective of efficient conception of halide perovskite sources in order to match specific VLC applications.

The rest of the article is organized as follows. Section II presents the conception process of the metasurface halide perovskite LED. Section III describes the channel modelling approach by presenting first the integration of metasurface halide perovskite LED characteristics in the MCRT tool in Section III-A, then the considered propagation environment in Section III-B, and finally by discussing the obtained results in Section III-C. Conclusions and perspectives are given in Section IV.

II. METASURFACE HALIDE PEROVSKITE LED

We first introduce the material stack in a standard halide perovskite LED. As depicted in Fig. 1(a,b), the LED stack consists of: Au and Indium Tin Oxyde (ITO) as contacts, $TiO₂$ and Spiro-OMeTAS as transporting layer for respectively electrons and holes, and halide perovskite as the active material where the carrier recombination leading to light emission takes place. As a proof-of-concept, the chosen perovskite is $CH_3NH_3PbBr_3$ which is one of the most popular and stable perovskites with strong emission in the green wavelength range. Emitted light is collected from the ITO side. Thicknesses of each material are kept constant for the different designs (h_{Au} = 200 nm, h_{Spiro} = 150 nm, h_{Perovskite} = 270 nm, $h_{TiO_2} = 20$ nm, $h_{ITO} = 200$ nm) - rather flat or having perovskite layer patterned into metasurface structure.

The rigorous coupled wave analysis (RCWA) [16] suits well for the simulation of the stacks periodically patterned under plane wave illumination. We have used the $S⁴$ code [17] available in the Solcore package [18] to compute the absorption within the perovskite layer. According to Kirchhoff's law of thermal radiation, the emission in the (θ, ϕ) space with $\theta \in$ [0,360] the azimuth and $\phi \in [0,90]$ the elevation equals the absorption in the same space. Such a result is still commonly used for out-of-equilibrium active devices such as LED. Then absorption $A(\theta, \phi, \lambda)$ is obtained using RCWA by applying the Poynting's theorem to the perovskite material area. Far-field of the emitted light is then obtained integrating the product of the absorption and the spectrum of the PL of the perovskite we measured, along the wavelength range of interest $[\lambda_1, \lambda_2] = [535]$ nm, 580 nm] (cf. area delimited by dashed red lines in Fig. 1(ce)), as:

$$
Farfield(\theta,\phi) = \int_{\lambda_1}^{\lambda_2} A(\theta,\phi,\lambda) PL(\lambda) d\lambda \tag{1}
$$

The metasurface designs investigated in this work, in addition to the flat slab, are sub-wavelength periodic lattices of 1D grating, 2D square, 2D triangular and 2D honeycomb whose schemes are depicted in Fig. 2(a-e). The introduction of a periodic pattern in the active material triggers optical resonances to occur enhancing photons absorption and emission phenomena for given θ and ϕ . For patterned LED device, the emitted photons can be coupled to Bloch resonances of the periodic metasurface. Such a coupling has two-fold effects: i) Enhance the extraction efficiency [19] ii) Shape the far-field pattern following the photonic bandstructure. Although an improvement of light extraction with metasurface design is hinted (see Fig. 2(f-j)), here we only focus on the engineering of far-field pattern for VLC applications. The tuning of the geometrical parameters of the pattern is a way to engineer the shape of the

Fig. 2. (a), (b), (c), (d) and (e): Schemes of the different patterns within the perovskite layer. Depths of all patterns is 135 nm. 1D grating exhibits a period of 295 nm and a filling factor of 0.5. 2D square (period = 300 nm, radius = 90 nm). 2D triangular (period = 310 nm, radius = 90 nm). 2D honeycomb $(period = 460 \text{ nm}, \text{ radius} = 80 \text{ nm})$. (f) , (g) , (h) , (i) and (j) : Far-field emission of the corresponding geometries.

Fig. 3. Radiation patterns of the different LED structure: (a) flat, (b) 1D grating, (c) 2D square, (d) 2D triangular, and (e) 2D honeycomb.

LEDs beam. For instance, dealing with symmetries, the shapes of the far-field in Fig. 2(f-j) exhibit the same symmetries as the patterns in Fig. 2(a-e). Moreover, the photonic bandstructure can be engineered on-demand within the spectral region of interest to exhibit various characteristics such as slow-light and linear dispersion [20], or even peculiar ones such as flatband, Dirac cones and multivalley characteristics [21], [22].

III. CHANNEL MODELLING

A. Propagation simulation

To evaluate the impact of those metasurface halide perovskite LEDs, we simulate the channel impulse response (CIR) $h(t)$ for a given link between a couple of emitter and receiver. We adopt a modelling approach based on a stochastic Monte-Carlo method, associated with ray-tracing algorithm, to numerically determine, from analytical models of reflection (bidirectional reflectance distribution function (BRDF)) and propagation, the propagation delay and the received power for LOS and non-LOS (NLOS) paths, i.e. reflected paths over all the elements inside the propagation environment. In this paper, we consider the MC ray-shooting [23] simulation algorithm, with 10e6 launched rays, a maximum reflection depth of 3 and a time resolution of 0.2 ns.

Thus, the simulation process consists first in integrating in the light propagation simulator the simulated radiation patterns of the different developed LED structures presented in Fig. 3, which have been computed based on the process presented in Section II. Corresponding to the flat slab structure, Fig. 3(a) exhibits a pattern very close to the standard Lambertian one.

It can be viewed as a reference case. These radiation patterns are computed for a set of incident directions, deterministically determined with a constant angular step, in both elevation and azimut. Since the MCRT algorithm leads to consider random incident directions from the optical source, in which the radiated luminance is usually not known, it is simply interpolated from the known values in neighboring directions. Finally, The radiation patterns are obviously normalized by the total radiated power computed by MC integration over the hemisphere covering the LED.

In [24], a recent study highlighted the impact of the area of the transmitter's excitation surface onto the channel DC gain, which becomes significant with its increase. Its shape, circular or rectangular, can also be of importance. These two parameters are taken into account in our MCRT simulations. Next lines present the corresponding process in case of only LOS link.

 $G_{T_x}(\vec{v})$ being the normalized radiation pattern of the optical source T_x , defining so the relative radiated power in direction \vec{v} , the overall received power P_{R_x} by the receiver R_x is given by:

$$
P_{R_x} = P_t \iint_{A_{T_x}, A_{R_x}} G_{T_x}(\overrightarrow{xy}) V(x, y) \frac{|\overrightarrow{xy}, \overrightarrow{n_r}|}{||\overrightarrow{xy}||^3} d\mu(x) d\mu(y), \quad (2)
$$

where P_t is the total emitted optical power, A_{T_x} and A_{R_x} are the areas of the emitter/receiver, x and y two given points onto the emitter/receiver' surfaces, \overrightarrow{xy} the vector from x to y, $\overrightarrow{n_r}$ the normal at the receiver' surface at y, $d\mu(x)$ and $d\mu(y)$ two elementary areas around x and y , and V the visibility function defined as:

$$
V(x, y) = \begin{cases} 1 & \text{if } x \text{ and } y \text{ are visible from each other} \\ 0 & \text{else} \end{cases}
$$
 (3)

The conventional MC estimator P_{R_x} of P_{R_x} computed for N samples is:

$$
\widehat{P}_{R_x} = \frac{P_t}{N} \sum_{i=1}^N \frac{G_{T_x}(\overrightarrow{x_i y_i}) V(x_i, y_i) \frac{|\overrightarrow{x_i y_i}, \overrightarrow{n_r}|}{||\overrightarrow{x_i y_i}||^3}}{p_x(x_i) p_y(y_i)},
$$
(4)

where x_i and y_i are two random points onto the T_x and R_x ' surfaces, computed from the considered probability density functions (PDF) p_x and p_y respectively. The genericity of MC integration method leads to the fact that the MC estimator given in (4) is valid for any PDF. Although the estimator's variance is impacted by the choice of a specific PDF and as we have no a priori information on $G_{T_x}(\vec{v})$, we have adopted conventional uniform PDF, i.e.:

$$
p_x(x_i) = \frac{1}{A_{T_x}}, \qquad p_y(y_i) = \frac{1}{A_{R_x}}.
$$
 (5)

Finally, the algorithms to uniformly sample a point onto a rectangular or circular surface are obvious. There expressions can be found in [25].

B. Propagation environment

The simulation environment, illustrated in Fig. 4, is the Barry-A scene first proposed in [26]. It consists of a paralepipedic room of $5 \times 5 \times 3$ m. The optical source is at the ceiling center and points towards the ground. The receivers are photodiodes with a 1 cm² sensitive area and a 60° field of view (FoV), defined as the half-detection power semi-angle. We consider a set of receiving positions on the ground, located on a discrete grid with a fixed 20 cm step, corresponding to a set of 625 reception positions. All the geometrical and optical parameters of the environment are detailed in Table I.

C. Results

The CIRs have been simulated between the emitter and the set of receiving positions presented in Fig. 4, according to each of the five LED structures presented in Section II, allowing to draw in Fig. 5 maps of channel DC gain H_0 defined as:

$$
H_0 = \int_0^\infty h(t) \, \mathrm{d}t. \tag{6}
$$

Based on the central limit theorem, H_0 was found in the confidence interval $[0.99H_0, 1.01H_0]$ with a probability of 95%, H_0 being the MC estimator of H_0 . Theses maps have a similar behavior according to the different LEDs, as indicated as example for flat and 2D honeycomb structures in Fig. 5(a) and (c) respectively, which present very close gain distributions inside the room. This is confirmed by the PDFs of the channel DC gain presented in Fig. 6 (plain line curves). This figure highlights a minimum gain of about -59 dB.

Fig. 4. Simulation environment.

TABLE I PARAMETERS OF THE PROPAGATION ENVIRONMENT [?].

Parameters	values
Room size	$5 \times 5 \times 3$ m
BRDF of all surfaces	Lambertian, <i>i.e.</i> purely diffuse
Reflectance of walls and ceiling	0.8
Reflectance of floor	0.3
Tx coordinates	(2.5, 2.5, 2.99)
T_x power	1W (normalized)
Tx geometrical shape / area	Rectangular $/ 1$ cm ²
Number of receiving positions	625 (25 \times 25)
Spacing of neighboring receiver positions	20 cm
R_x geometrical shape / area	Circular $/1$ cm ²
FoV of the receivers	60°

Even though it cannot be guaranteed in a real environment, due to mobility for instance, the best communication performance level is obviously obtained when the LOS link exists. Fig. 6 also illustrates the PDFs of the LOS contribution to the channel DC gain (dashed line curves). It appears that the LOS gain can be lower that the minimum channel gain (-59 dB), and in this case it is compensated by the reflections over the room surfaces. Also, the maximum occurrence of gain value is still about -59 dB (dotted line).

If one consider this value as a target limit to guarantee the best level of performance, even in case of LOS blockage, the cumulative density function (CDF) of the multi-reflected contributions according to the LED structures, presented in Fig. 7, allows determining the outage probability P_{out} , i.e. the probability to have a channel gain value less than this targeted one. Theses curves clearly indicate significant gap between the P_{out} values, which are summarized in Table II. The 2D triangular and flat LED structures give the highest P_{out} values of 82.24 and 79.84% respectively. The 1D structure is a little better with 71.52 %, whereas the 2D square and honeycomb structures are the most interesting, with a significantly weaker P_{out} values of 62.72 and 44.16% respectively. Thus, the best structure, i.e 2D honeycomb, allows to divide the P_{out} by a factor of about 2 with regards to flat one.

Fig. 5. Maps of Channel DC gain according to: (a) only LOS contribution and Flat structure, (b) only multi-reflected contributions and Flat structure, (c) only LOS contributions and 2D honeycomb structure, and (d) only multi-reflected contributions and 2D honeycomb structure.

Fig. 6. PDFs of the channel DC gain (plain lines) and the LOS contribution (dashed lines) to the channel DC gain according the LED structures.

Fig. 7. CDFs of the only multi-reflected contributions to the channel DC gain according the LED structures.

This interesting result is obtained thanks to the reflected contributions which are the highest for the 2D honeycomb structure, as Fig. 5(b) and (d) illustrate it for flat and 2D honeycomb structures respectively.

As last part of this study, we now present the impact of LEDs' structure onto the time dispersive character of the channel, by computing its DRMS [12] expressed for recall by:

$$
DRMS = \sqrt{\frac{\int (t - \mu)^2 h^2(t)dt}{\int h^2(t)dt}}, \mu = \frac{\int th^2(t)dt}{\int h^2(t)dt}, \quad (7)
$$

TABLE II OUTAGE PROBABILITY FOR A NLOS TARGET GAIN OF -59 DB ACCORDING TO THE LED STRUCTURES.

LED structures	$P_{out}: P(H_0 < -59 \text{ dB})$
Flat	79.84 %
1D grating	71.52%
2D square	62.72%
2D triangular	82.24%
2D honeycomb	44.16 %

Fig. 8. CDFs of the DRMS according the LED structures.

Fig. 9. CDFs of only multi-reflected contributions to the DRMS according the LED structures.

with μ the mean excess delay.

Fig. 8 shows the CDF of the DRMS according to the LED structures. It appears that the structure of the LEDs has very little impact on the DRMS with a maximum difference of only 0.2 ns which corresponds to 0.1% of the maximum DRMS value. Even if this first result is interesting, since it shows that the LED structuring does not degrade the channel performance in terms of temporal dispersion, it is obtained in the favorable configuration where the LOS link is always existing.

Because reflected contributions have more similar power levels between each other, NLOS configurations are more conducive to high levels of DRMS. To check the impact of the LED structuration in the NLOS case, Fig. 9 shows the CDF of the only multi-reflected contributions. As expected, the levels of DRMS are significantly higher than in LOS case, but the difference between the different LED structures are still weak, with a maximum difference of about 0.4 ns, being only 0.05% of the maximum DRMS value.

IV. CONCLUSION

By implementing a modeling approach, we investigated the impact of metasurface halide perovskite LED design on the characteristics of the optical wireless propagation channel. The optical properties of the designed components were included in an optical propagation simulator based on the MCRT method to determine the characteristics of the transmission channel. Overall, we have underlined that the structuring of the LED, considering normalized radiation patterns, allows optimizing the coverage by dividing the outage probability up to a factor 2, without degrading the temporal dispersion of the channel. These first results illustrate the interest of such a multi-scale approach that we will deepen by studying the impact of other parameters related to the design of LEDs. Beyond its influence on the emission pattern, we will for instance investigate the impact of perovskite metasurface geometrical parameters on the emitted power and the electrical consumption, and take it into account in propagation simulation to evaluate its impact on communication performance in more complex optical transmission scenarios.

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