

Co-inoculation with arbuscular mycorrhizal fungi differing in carbon sink strength induces a synergistic effect in plant growth

Maria M Martignoni, Jimmy Garnier, Xinlu Zhang, Daniel Rosa, Vasilis Kokkoris, Rebecca C Tyson, Miranda M Hart

▶ To cite this version:

Maria M Martignoni, Jimmy Garnier, Xinlu Zhang, Daniel Rosa, Vasilis Kokkoris, et al.. Co-inoculation with arbuscular mycorrhizal fungi differing in carbon sink strength induces a synergistic effect in plant growth. Journal of Theoretical Biology, 2021, 10.1016/j.jtbi.2021.110859. hal-03439689

HAL Id: hal-03439689 https://hal.science/hal-03439689

Submitted on 22 Nov 2021

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Co-inoculation with arbuscular mycorrhizal fungi differing in carbon sink strength induces a synergistic effect in plant growth

Maria M. Martignoni^{1,6}, Jimmy Garnier², Xinlu Zhang³, Daniel Rosa³, Vasilis Kokkoris^{4,5}, Rebecca C. Tyson¹, and Miranda M. Hart³

¹Department of Mathematics, University of British Columbia, Kelowna (BC), Canada, maria.martignonimseya@ubc.ca, rebecca.tyson@ubc.ca

²LAboratoire de MAthématiques (LAMA), CNRS, Univ. Grenoble Alpes, Univ. Savoie Mont Blanc, Chambery, France, jimmy.garnier@univ-smb.fr

³Department of Biology, University of British Columbia, Kelowna (BC), Canada,

miranda.hart@ubc.ca, zhangx19262@163.com, daniel.rosa@ubc.ca

⁴Department of Biology, University of Ottawa, Ottawa (ON), Canada, vkokkori@uottawa.ca

⁵Agriculture and Agri-Food Canada, Ottawa Research and Development Centre, Ottawa (ON),

Canada, vasilis.kokkoris@canada.ca

⁶Department of Mathematics and Statistics, Memorial University, St. John's (NL), Canada, mmartignonim@mun.ca

July 28, 2021

Abstract

Arbuscular mycorrhizal (AM) fungi play a key role in determining ecosystem functionality. Understanding how diversity in the fungal community affects plant productivity is therefore an important question in ecology. Current research has focused on understanding the role of functional complementarity in the fungal community when the host plant faces multiple stress factors. Fewer studies, however, have investigated how variation in traits affecting nutrient exchange can impact the plant growth dynamics, even in the absence of environmental stressors. Combining experimental data and a mathematical model based on ordinary differential equations, we investigate the role played by carbon sink strength on plant productivity. We simulate and measure plant growth over time when the plant is associated with two fungal isolates with different carbon sink strength, and when the plant is in pairwise association with each of the isolates alone. Overall, our theoretical as well as our experimental results show that co-inoculation with fungi with different carbon sink strength can induce positive non-additive effects (or synergistic effects) in plant productivity. Fungi with high carbon sink strength are able to quickly establish a fungal community and increase the nutrient supply to the plant, with a consequent positive impact on plant growth rate. On the other side, fungi with low carbon sink strength inflict lower carbon costs to the host plant, and support maximal plant productivity once plant biomass is large. As AM fungi are widely used as organic fertilizers worldwide, our findings have important implications for restoration ecology and agricultural management.

Keywords : Arbuscular mycorrhizal fungi (AMF), multiple mutualist effects (MMEs), carbon sink strength, synergy, productivity, agriculture, nutrient exchange, inoculum, mutualism.

Introduction

Arbuscular mycorrhizal (AM) fungi are microscopic symbionts found inside the roots of 2 the vast majority of terrestrial plants (Smith and Read, 2010). AM fungi exert a strong positive influence on plant growth and fitness, by facilitating plant access to limiting nutrients (e.g., phosphorus) (Jeffries et al., 2003; Smith and Read, 2010), providing 5 pathogen protection (Pozo and Azcón-Aguilar, 2007; Shrivastava et al., 2015), or tol-6 erance to abiotic stress (Latef et al., 2016; Augé et al., 2015). The plant, in exchange, provides AM fungi with fixed carbon (Smith and Read, 2010). In nature, multiple species of AM fungi coexist in the roots of the same host plant (Verbruggen et al., a 2012; Vandenkoornhuyse et al., 2007) and it is proposed that variation of functional traits can be observed among coexisting fungi (Powell and Rillig, 2018; Lee et al., 2013; 11 Mensah et al., 2015; Smith et al., 2000; Feddermann et al., 2010). 12 With functional complementarity among fungi one could expect plant benefit to be 13 higher in the presence of multiple AM fungi than in the presence of any of the species 14

(or isolates) separately (Koide, 2000; Gianinazzi et al., 2010). However, experimental 15 observations on plant growth show that simultaneous colonization by multiple AM fungi 16 does not always lead to a greater benefit for the plant, and in some cases productivity can be larger in the presence of a single, most beneficial fungus (Gustafson and Casper, 18 2006; Jansa et al., 2008; Violi et al., 2007; Thonar et al., 2014; Maherali and Klironomos, 19 2007; Gosling et al., 2016; Jansa et al., 2008; Alkan et al., 2006). As AM fungi play a key 20 role in determining ecosystem productivity and function (Van der Heijden et al., 1998), 21 a better understanding of the relationship between diversity in the fungal community 22 composition and plant productivity is of particular importance. 23

Experimental studies have focused on understanding the link between diversity and 24 productivity in multistressed environments, where the presence of taxonomically distant 25 AM fungal species can act as insurance to support plant growth despite challenging 26 abiotic conditions (Yang et al., 2016; Thonar et al., 2014; Crossay et al., 2019; Gosling et al., 2016; Maherali and Klironomos, 2007). Few studies, however, have looked at 28 how functional complementarity in the fungal community may affect nutrient exchange 29 processes, even in the absence of stress factors (Mensah et al., 2015; Ibrahim, 2018; 30 Jansa et al., 2005). AM fungi can differ in their ability to provide phosphorus to the 31 plant (Drew et al., 2003; Giovannini et al., 2020), or in their access to host carbon (Zhu 32 and Miller, 2003), and these differences should by themselves result into differences in 33 the plant growth dynamics (Afkhami et al., 2014). While some studies have investigated 34 how plant productivity is affected by fungi to plant supply (i.e., phosphorus transfer), 35 (Jansa et al., 2005; Mensah et al., 2015; Ibrahim, 2018; Martignoni et al., 2020a), 36 changes in productivity due to carbon transfer (i.e., plant to fungi supply) have remained 37 unexplored. 38

The need for a framework to study the mechanisms associated with the presence 39 of multiple, functionally different mutualists has been recently highlighted also from 40 the theoretical point of view (Afkhami et al., 2014). Theoretical work, however, has 41 focused on explaining stable coexistence among mutualists (Bachelot and Lee, 2018; 42 Johnson and Bronstein, 2019: Martignoni et al., 2020a), rather than on investigating 43 the consequences of intraguild diversity on productivity. Multiple mutualists effects 44 can potentially increase, reduce or have no repercussion on host performance, but it is 45 unclear how interactions with the environment, direct and indirect interactions among 46

⁴⁷ mutualists, or nutrient exchange may contribute to the final outcome (Afkhami et al.,

⁴⁸ 2014; Stanton, 2003).

Here, we test whether differences in the benefit provided by the plant to fungal mu-49 tualists can induce positive non-additive effects (or synergistic effects) in plant biomass, 50 which in our work will be used as a measure of productivity (Xu and Mage, 2001). The 51 factors driving carbon allocation from host to fungus are largely unknown (di Fossalunga 52 and Novero, 2019), but might be important determinants of plant growth. The level of 53 carbon transfer has been hypothesized to be a result of plant discrimination between 54 associated fungi, where fungi providing more nutrients to the plant are rewarded with 55 more carbon in exchange (Kiers et al., 2011; Kafle et al., 2019). However, it remains 56 challenging to explain how a plant can discriminate between symbionts in natural con-57 ditions, where multiple fungi share a single root system (Walder and van der Heijden, 58 2015). For this reason, in our study we do not assume any association between carbon 59 transfer and the reward received from the fungus. We consider the ability of a fungus 60 to access plant carbon (or its 'carbon sink strength') to be intrinsic characteristic of the 61 fungal species (or fungal isolate), determined by the physiological capacity of the fungus 62 to acquire carbon (Rezáčová et al., 2017; Pearson and Jakobsen, 1993), and linked, for 63 example, to the proportion of intercellular hyphae involved in carbon transfer (Smith 64 and Read, 2010; Hodge et al., 2010). 65 We use an ordinary differential equation (ODE) model to investigate the coupled 66 plant-fungi growth dynamics. The model allows us to disentangle the effects on plant 67 growth driven by differences in fungal carbon sink strength, from effects caused by 68

environmental stressors. We then compare our theoretical predictions with in vivo experiments. We use two fungal isolates with different carbon sink strength and measure plant growth over time in monocultures and in mixed cultures.

⁷² Models, materials, and methods

⁷³ Differences in carbon sink strength and productivity

To investigate plant productivity in the presence of two fungal isolates with different carbon sink strength we compare growth when the plant is in pairwise association with each of the fungi separately (see Fig. 1, left panel), to growth when the plant is in simultaneous association with the two fungi (Fig. 1, right panel). First, we identify the oretically under which circumstances the synergy occurs, using the mathematical model described below. We then compare our theoretical results with in vivo experiments and statistical analysis of experimental data.



Fig. 1: Schematic representation of the scenarios used to address questions 1 (left panel) and 2 (right panel), through numerical simulation. On the left we consider a plant interacting separately with two different isolates of AM fungi, m_1 and m_2 , taken one at a time. On the right the plant interacts with the two fungal isolates simultaneously. Fungi m_1 and m_2 share the carbon supplied by the plant and therefore interact indirectly with each other.

81 Theoretical work:

Model description: To study the plant-fungi growth dynamics we used the mathematical model developed by Martignoni et al. (2020a). This model is based on a consumer-resource framework for mutualisms (Holland and DeAngelis, 2010), and considers the coupled dynamics of a mutualist guild (i.e., the fungal mutualists) sharing a resource supplied by the same host (i.e., plant carbon).

In the model, plant growth depends on the amount of phosphorus that the plant 87 receives from the fungi, on the carbon that the plant provides to the fungi, on plant 88 growth in the absence of mutualism, and on the amount of nutrients that need to be 89 reserved for maintenance of the existing plant biomass. Similarly, the growth of each 90 fungus depends on the amount of carbon received from the plant, on the amount of 91 phosphorus that the fungus transfers to the plant, and on the maintenance costs. We 92 refer to 'fungal isolates' instead of 'fungal species', as for the experimental testing of 93 our hypotheses we will select different isolates of the same fungal species (i.e., different 94 isolates of *Rhizophagus irregularis*, as described in the next section). 95

The system of equations describing the variation over time of plant biomass p and of the biomass of one associated fungal isolate m_i (where i = 1, 2) is given by

$$\underbrace{\frac{dp}{dt}}_{i} = q_{hp} \underbrace{\left(\sum_{i} \alpha_{i} m_{i}\right) \frac{p}{d+p}}_{i} - q_{cp} \underbrace{\left(\sum_{i} \alpha_{i} m_{i}\right) \frac{p}{d+p}}_{i} - q_{cp} \underbrace{\left(\sum_{i} \beta_{i} m_{i}\right) p}_{i} + \underbrace{\left(\sum_{$$

$$\underbrace{\frac{dm_i}{dt}}_{\substack{\text{change in}\\\text{fungal biomass}}} = q_{cm} \underbrace{\frac{\beta_i p m_i}{\alpha_i p m_i}}_{\substack{\text{carbon}\\\text{from plant}}} - q_{hm} \underbrace{\frac{\alpha_i p m_i}{d + p}}_{\substack{\text{phosphorus}\\\text{to plant}}} - \underbrace{\frac{\mu_m m_i^2}{\alpha_i p m_i}}_{\substack{\text{maintenance}\\\text{cost}}}.$$
(1b)

A brief description of all model parameters is given in Table 1. The model assumes nutrient transfer to be biomass dependent, where the functional responses chosen are justified in detail in Martignoni et al. (2020a). We assume a linear relationship between fungal biomass and phosphorus transfer. Indeed the amount of phosphorus transferred is expected to increase with increasing hyphal length and root colonization (Sawers et al., 2017; Treseder, 2013). When plant biomass is low, the amount of phosphorus that can be received by the plant is limited by its small size, and we assume phosphorus

Table 1: Brief description of the variables and parameters of the model of Eq. (1) and default values used for simulations. Default values are based on the statistical analysis of the experimental data (see Appendix C). Values in brackets correspond to case variations shown in Fig. 3.

Symbol	Description	Default value
<i>p</i>	Plant biomass	—
m_i	Fungal biomass	—
p_0	Plant initial biomass	0.08
m_{0i}	Fungal initial biomass of isolate i	0.05(0.1)
μ_p	Plant maintenance rate	1.44 (1.7)
μ_m	Fungal maintenance rate of isolate i	1.05(1.3)
$ q_{hp}$	Conversion phosphorus to plant biomass	2.93
q_{cm}	Conversion carbon to fungal biomass of isolate i	2.93
q_{cp}	Conversion carbon to plant biomass	1
q_{hm}	Conversion phosphorus to fungal biomass of isolate i	1
d	Half-saturation constant	1.07
$ r_p$	Plant intrinsic growth rate	$0.33\ (0.66)$
$\ \alpha_i$	Phosphorus supply from fungal isolate i	2.2(2.0)
β_i	Carbon sink strength of fungal isolate i	1.0-4.0

transfer to depend on both plant and fungal biomass (see 'phosphorus from AM fungi' and 'phosphorus to plant' terms in Eq. (1)). Carbon transfer from the plant to the fungi depends on carbon fixation and on the extent of root colonization by AM fungi (Thomson et al., 1990; Vierheilig et al., 2002), and in the model we assume a linear relationship between carbon transfer and fungal and plant biomass (see 'carbon to AM fungi' and 'carbon from plant' terms in Eq. (1)). Fungal isolates therefore do not directly compete for host carbon, but each fungus accesses a different proportion of host carbon depending on its biomass.

The nutrient transfer terms show the same biomass dependence for all fungi, how-111 ever, the exact amount of nutrients transferred varies among isolates, and depends on 112 the ability of a fungus to transfer phosphorus to the plant (parameter α_i) and on its 113 access to plant carbon (parameter β_i). Fungi with higher carbon sink strength can 114 therefore be characterised by a larger β_i parameter. Other fungal parameters are the 115 carbon and phosphorus to biomass conversion rates $(q_{cm} \text{ and } q_{hm})$, and the rate at which 116 a fungus deviates resources to maintenance of its existing biomass (μ_m) . Parameters characterising plant growth are the phosphorus and carbon to biomass conversion rates 118 $(q_{hp} \text{ and } q_{cp})$, the intrinsic growth rate in the absence of mutualism (r_p) , and the plant 119 maintenance rate (μ_p) . The presence of stress factors can be modeled as an increase in 120 the amount of resources reserved for maintenance, reflected in a higher value of the μ_p and μ_m parameters.

Relating carbon sink strength to plant growth: To investigate how the plant growth rate and final size are affected by carbon sink strength (parameter β) we first considered a plant associated with a single fungus. For this purpose, we solved Eq. (1) for i = 1 and considered a range of β parameters, while other parameters were kept constant at their default value (see Table 1). The final size corresponds to plant biomass ¹²⁸ at equilibrium. The average plant growth rate was computed as

$$\int_{0}^{T_{95}} \frac{1}{T_{95}} \frac{1}{p} \left(\frac{dp}{dt}\right) \mathrm{d}t,\tag{2}$$

129

where T_{95} is the time needed to reach 95% of the plant biomass at equilibrium, and dp/dt represents plant biomass over time (defined in Eq. (1a)).

Additionally, we compared plant growth in the presence of one isolate (with either high or low carbon sink strength) with plant growth in the presence of both isolates simultaneously. In the model, fungal maintenance costs are non-additive as they depend on fungal biomass (see last term in Eq. (1b)). Therefore, in order to compare plant growth in the presence of one and two fungal isolates, we assumed the plant p to be always in association with two fungal isolates (i.e., i = 1, 2), where the two fungi can be the same isolate (i.e., characterised by the same parameters), or different isolates (i.e., characterised by different β_i parameters).

Finally, we compared the effect of variations in the carbon sink strength with variations in phosphorus supply. We repeated the procedure described in the previous two paragraphs to investigate how phosphorus supply (parameter α_i) affects the plant growth rate and final size, and simulated plant growth over time in the presence of one and two fungal isolates differing in their phosphorus supply to the plant.

Sensitivity of parameter values: We solved Eq. (1) for i = 1, 2, where fungus 145 1 and 2 are characterised by different β_1 and β_2 parameters, while other parameters 146 were kept constant at their default values (see Table 1). Default values were based on 147 the statistical analysis of the experimental data described below. We determined the 148 (β_1, β_2) parameter regions where a synergy in plant growth was observed and for each of 149 these we computed the intensity and temporal length of the synergistic effect. We define 150 the synergistic effect as a percentage gain in productivity, quantified as the percentage 151 increase in plant biomass observed when the plant is in combination with two isolates, 152 with respect to when the plant is in combination with the isolate that leads to the 153 highest plant biomass. We found that a synergy in plant growth was observed when 154 the plant was associated with two isolates with higher or lower carbon sink strength, 155 characterised by parameters β_H and β_L respectively. Mathematically, we write: 156

% gain in productivity(t) =
$$\frac{p_{H+L}(t) - \max(p_H(t), p_L(t))}{\max(p_H(t), p_L(t))} \times 100,$$
 (3)

where $p_H(t)$ and $p_L(t)$ refer to plant biomass at each point in time when the plant is 158 associated with the isolate with high or low carbon sink strength respectively, while 159 $p_{H+L}(t)$ refers to plant biomass when the plant is associated with both isolates. When 160 the maximal gain in productivity is positive, i.e., $p_{H+L}(t) > \max(p_H(t), p_L(t))$, we say 161 that a synergistic effect is observed. The temporal length of the synergistic effect refers 162 to the number of days for which the gain in productivity is positive. The intensity of 163 the synergistic effect refers to the maximal gain in productivity observed during the 164 time interval considered. 165

We considered variations from the default scenario, by choosing a higher intrinsic growth rate of the plant (parameter r_p), a higher amount of initial fungal biomass (higher m_{0_i}), higher environmental stress (reflected in an increase in parameters μ_p and μ_m , the plant and fungal maintenance rates), and a reduced ability of the fungal isolate to transfer phosphorus to the plant (lower α_i parameters). Parameter ranges were chosen based on the significance of the results. Simulations were performed using the Matlab (R2020b) solver ode45.

173 Experimental work:

Selection of AM fungal isolates: To identify isolates with different carbon sink 174 strength but similar ability to transfer phosphorus to the plant, we conducted a prelim-175 inary study using nine isolates of *Rhizophagus irregularis* (Schenck and Smith, 1982). 176 Additional information about this experiment is available in Appendix A. We identi-177 fied two isolates of R. *irregularis* that matched the needed requirements: 1) Cuba8, 178 which demonstrated a high carbon sink strength under the growing conditions of our study, and 2) CC4 (DAOM 229457), which demonstrated significantly lower carbon 180 sink strength. No statistically significant difference was found in the phosphorus trans-181 fer ability of Cuba8 and CC4 (Fig. A.1). 182

AM fungal inoculum: Isolates Cuba8 and CC4 were grown with Ri T-DNA trans-183 formed carrot roots on Petri plates (60-mm diameter and 15-mm height) (VWR) with 184 M medium as described by Bécard and Fortin (1988), solidified with 1% gellan gum 185 (Alfa Aesar). The Petri plates were incubated inverted at 26°C (CONVIRON ADAP-186 TIS CMP6010) in the dark, until numerous spores were produced. Mature spores were 187 extracted after solubilizing the medium with sterile 10 mM, pH=6 sodium citrate buffer 188 solution (Doner and Bécard, 1991). Cuba8 has a germination rate of 20% while CC4 189 has a significantly higher germination rate of 60% (Kokkoris et al., 2019). To ensure 190 standard inoculum density throughout the experiment we accounted for the variation 191 in the germination rates to ensure the presence of at least six viable spores per pot. 192 For this reason we used 30 Cuba8 spores or 10 CC4 spores per pot when the plant 193 was inoculated with a single isolate, and 30 spores of Cuba8 and 10 spores CC4 when 194 the plant was inoculated with a mix of both isolates. To avoid runoff of spores post 195 inoculation and to attain successful colonization we applied a novel inoculation system 196 that involved the creation of 'inoculation disks' (see Appendix B, Fig. B.1). 197

Growing conditions: For the main experiment, AM fungal isolates and host plants 198 of Linum usitatissimum (Flax) were grown in 2L pots containing (v/v=1:1) sterilized 199 medium-fine sand (SAKRETE Play Sand) and vermiculate (in identical conditions as 200 in the preliminary study, see Appendix A). Flax seeds were surface sterilized with 70%201 ethanol for 1 min, followed by 5 min in 9.6% bleach. Seeds were then washed six times 202 for 1 min each, in sterilized distilled water. The surface sterile seeds were germinated 203 in Petri dishes on wet sterile 11 cm filter papers (VWR) and kept in an incubator 204 (CONVIRON ADAPTIS CMP6010) at 26°C (no light) until a radicle was observed. 205 Inoculated pots were placed in the greenhouse where the temperature ranged from 26 206 to 20°C (day/night) with a photoperiod of 18 h per day, of 200 μ mol s-1 m-2 per μ A 207 as measured with a LI-250A light meter (Biosciences). Two weeks post inoculation 208 and weekly thereafter, plants were fertilized with Low P fertilizer (Miracle-gro 24-8-16) 209 (50mL per plant of 5 mL fertilizer dissolved in 4L water) until harvest. Additional 210

water was applied with emitters directly above the straws, supplying 2 l hr-1 to each pot, \sim 35 ml every two days.

After the first month, eight plants per week and per treatment were harvested from each treatment for the duration of eight weeks, for a total growing period of 12 weeks. At each harvest, roots were washed, dried of excess water and the fresh root weight was recorded. Shoots were weighed for fresh weight.

217 Statistical analysis:

230

251

Analysis of experimental data: Our first goal was to analyse the experimental 218 data to understand whether a synergy in productivity has occurred, and if so to quantify 219 its duration and intensity. We compared the total biomass of randomly chosen replicates from each experiment with only one fungal isolate (either Cuba8 or CC4), with the total plant biomass of a random replicate from the experiments with a combination of both 222 isolates (Cuba8 and CC4). We computed the number of weeks for which plant biomass from the experiments with both AM fungal isolates was greater than the maximal 224 plant biomass measured when only one AM fungal isolate was present. In addition, we 225 computed the percentage gain in productivity per week (or weekly percentage increase 226 in plant biomass) measured when a synergy occurs (Figs. 5a and 5b). For each weekly measurement of plant biomass in the presence of both isolates $(p_{H+L}(t))$ the gain in 228 productivity was computed as: 229

% gain in productivity(t) =
$$\frac{p_{H+L}(t) - \max(M(p_H)(t), M(p_L)(t))}{\max(M(p_H)(t), M(p_L)(t))} \times 100, \quad (4)$$

where $M(p_H)(t)$ and $M(p_L)(t)$ refer to the median of the plant biomass weekly measurements collected in the presence of a single isolate with high or low carbon sink strength. A synergy is observed if the % gain in productivity is positive.

Parametrization from experimental data: Our second goal was to recover resource exchange parameters from the experimental data (such as the carbon sink strength β_i and phosphorus transfer ability α_i of the fungal isolates used), to test whether our theoretical predictions could explain experimental findings (Fig. 5c). To do so, we used a statistical model, which describes the experimental measurements, and a mechanistic-statistical model based on the mathematical model of Eq. (1), which describes plant-fungal growth. The model projects the biomass of the plant p(t) at any time t, in association with AM fungi.

During our experiments, we measured the biomass of the plant Y_i every week $t_i \in$ 242 $\{1, \ldots, I\}$ during I = 8 weeks. Depending on the experiments, the plant was associated 243 with only one fungal isolate (either Cuba8 or CC4) or with the two different isolates 244 simultaneously (Cuba8 and CC4). The measurement protocol was identical for all 245 the experiments and the measures are independent from each other for any of the 246 experiments. Thus, conditionally on the plant biomass p and the harvesting time $\mathbf{t} =$ 247 $\{t_i | 1 \leq i \leq I\}$, the plant biomass measurements Y_i for $i \in \{1, \ldots, I\}$ are assumed to be 248 independent random variables following a Gamma distribution with a mean $p(t_i)$ and 249 a variance proportional to the actual biomass of the plant $p(t_i)$. We obtain: 250

$$Y_i | p, \mathbf{t} \sim \text{Gamma}\left(\frac{p(t_i)}{\sigma}, \sigma\right) ,$$
 (5)

where $\sigma > 0$ is the proportionality constant that determines the variance of the biomass measurements and p(t) depends on the parameters of the model given in Table 1.

We denote by θ the parameters of our mechanistic-statistical model: $\theta = (\beta_1, \beta_2, \alpha_1, \alpha_2, r_p, p_0, m_{1,0}, m_{2,0}, d, \mu_p, \mu_m, q_{hp}, q_{cm}, \sigma)$. Using the definition of the random variables Y_i , we can state the likelihood function associated to our mechanistic-statistical model with unknown parameters θ :

258

$$\mathcal{L}(\theta) = \mathbb{P}(Y|\theta, \mathbf{t}) = \prod_{i=1}^{8} \frac{1}{Y_i} \left(\frac{Y_i}{\sigma}\right)^{p(t_i)/\sigma} \Gamma\left(\frac{p(t_i)}{\sigma}\right)^{-1} e^{-Y_i/\sigma} \,. \tag{6}$$

For each of the three experiments (plant with Cuba8, plant with CC4, and plant with Cuba8 and CC4), we have 8 replicates, which therefore provide us with 24 data sets. For each data set, we obtain an estimator $\hat{\theta}$ of the parameters θ by minimizing the function $-\log(\mathcal{L}(\theta))$. The minimization was performed using the Matlab[®] constrained gradient-based minimization algorithm, fmincon, with the constraint:

$$\hat{\theta} \in [0, 10]^2 \times [0, 20]^2 \times [0, 0.5] \times [0, 0.3] \times [0, 0.5]^2 \times [0, 2] \times [0.01, 10]^2 \times [1, 6] \times [0.5, 5] \times [0, 0.65]$$

In the computation of $-\log(\mathcal{L}(\theta))$, the numerical evaluation of the quantities $(p(t_i))_{i=1,\dots,8}$

was based on the numerical computation of the ODE model using the Matlab (R2020b)

²⁶⁷ ode45 solver.

$_{268}$ **Results**

²⁶⁹ Differences in carbon sink strength and plant productivity:

Overall, our theoretical as well as our experimental results show that a temporal synergy in productivity can be observed when associated fungi present differences in their carbon sink strength. Below we discuss model predictions and their comparison to experimental data.

Theoretical work: Our theoretical study predicts that plant final size decreases with 274 increasing carbon sink strength, while plant average growth rate responds nonmono-275 tonically to changes in carbon sink strength (β), increasing when carbon sink strength 276 is low and decreasing when carbon sink strength is high (Fig. 2a). Thus, if the plant is 277 in simultaneous association with two isolates of AM fungi differing only in their carbon sink strength, when the plant growth rate is enhanced by the isolate with low carbon sink strength, and the plant final size is enhanced by the isolate with high carbon sink 280 strength, the plant will do better when both isolates are present than in association 281 with either of the isolates alone (Fig. 2c). A fungus with low carbon sink strength (e.g., 282 $\beta \sim 1$) will benefit productivity when plant biomass is large, by increasing the plant 283 final size. A fungus with higher carbon sink strength (e.g., $\beta \sim 1.5$) will maximize the 284 average plant growth rate when plant biomass is small. If the plant is in simultaneous 285 association with two isolates of AM fungi differing only in their carbon sink strength, 286 the plant final size is enhanced by the isolate with low carbon sink strength, and the 287 plant final size is enhanced by the isolate with high carbon sink strength. Thus, adding 288 an isolate with high carbon sink strength to an isolate with low carbon sink strength 289

will lead to an increase in the plant growth rate, and a decrease in the plant final size. Adding an isolate with low carbon sink strength to an isolate with high carbon sink strength will decrease the plant growth rate, but increase the plant final size. Additionally, for a certain period of time, co-inoculation of two isolates with different carbon sink strength can lead to higher productivity than when the plant is in association with either isolate separately, and drive a temporal synergistic effect in plant growth, as shown in Fig. 2c.

Our theoretical predictions suggest that differences in phosphorus supply do not lead to a synergistic effect on plant growth. The plant growth rate and final size both increase with increasing fungi to plant supply (Fig. 2b) and productivity at any point in time is always higher when the plant is associated with the isolate with the higher phosphorus transfer ability (Fig. 2d).

From Fig. 3 we see that the synergistic effect is stronger and can be observed for a longer period of time when the difference in carbon sink strength of the two fungal isolates is large. High initial fungal biomass and high intrinsic growth rate of the plant can reduce the intensity and duration of the synergy. Stress factors, quantified in an increase of the maintenance rates μ_p and μ_m , and the phosphorus transfer ability of the fungi (parameter α) do not affect the synergy duration or intensity.

From numerical simulations we expect a synergy to be observed also in the presence of multiple isolates differing in their carbon sink strength (Fig. E.1). Our analysis shows that the gain in productivity is affected by the average as well as by the variability in carbon sink strength observed among isolates (see Appendix E). A comprehensive analysis of the synergistic effect in the presence of multiple fungi is complex, and will be left for future work.

Experimental work & Statistical analysis: Our theoretical model with the in-314 ferred parameters from our statistical analysis predicts plant biomass over time to follow 315 a logistic growth curve, where a synergy due to differences in the carbon sink strength of 316 the isolates is expected to occur around weeks 4 or 5 (Fig. 2c). Experimental data also 317 show a tendency toward logistic growth, and a synergy at weeks 4, 5 and 6 was indeed 318 detected in most of the experiments (Fig. 4). Although the statistical significance is 319 low, other statistics performed considering the mean of the experimental observations, 320 instead of the median, show a statistically significant synergy at week 4 (see Appendix 321 D). Our analysis suggests therefore that the synergy predicted by our simulations is 322 also present in the experimental data. 323

A synergy at weeks 1 and 2 was also observed. This early synergy was not expected to occur theoretically, as our model is linear at low density, and non-additive effects (such as a synergy) are not expected to occur when the fungal biomass is small. We can therefore not draw any conclusion from the gain in productivity observed in weeks 1 and 2. No synergy was detected at week 3, which suggests that the synergy at weeks 1 and 2 and the synergy at weeks 4, 5 and 6 might be due to different mechanisms.

In Fig. 5a we can see that a temporary synergy in plant growth in Cuba8-CC4 mixed inocula was observed in 75% of the experiments conducted. In half of the cases the synergy was observed for at least 3 out of 8 weeks of measurements. When the synergy occurred, the increase in productivity (or % gain in plant biomass) was higher than 33% in half of the cases (Fig. 5b). The medians of the phosphorus and carbon transfer parameters recovered from the statistical analysis are $\alpha_1 = 2.06$ and $\beta_1 = 1.94$

for isolate 1 (Cuba8) and $\alpha_2 = 2.39$ and $\beta_2 = 1.64$ for isolate 2 (CC4) (Fig. 5c). 336 The two fungal isolates Cuba8 and CC4 were selected because of their different carbon 337 sink strength and potentially similar phosphorus transfer ability (see Appendix A). 338 The medians of the resource exchange parameters obtained by fitting our model to the 339 experiments reflect this difference in carbon sink strength, with Cuba8 having a larger 340 carbon sink strength than CC4 (β_1 (Cuba8) > β_2 (CC4)). However, the median of the 341 recovered phosphorus transfer ability of Cuba8 is lower than CC4 (α_1 (Cuba8) < α_2 342 (CC4)), although the statistical test conducted in the preliminary analysis suggest that 343 the phosphorus transfer ability of the two isolates might be similar on average (Fig. A.1). 344



Fig. 2: Projections of plant final size (blue dotted line) and average growth rate (red dashed line) (see Eq. (2)), as a function of (a) carbon sink strength β and (b) phosphorus supply α , when the plant is considered in pairwise association with a single AM fungal isolate. (c) Numerical simulations showing plant biomass over time when the plant is associated with a fungal isolate with high carbon sink strength (β_H , dashed curve), with an isolate with low carbon sink strength (β_L , dotted curve), or with a combination of both isolates (β_{L+H} , solid curve). We assume that the isolates have the same phosphorus exchange ability ($\alpha = (2.06 + 2.39)/2$) and differ only in their carbon sink strength ($\beta_H = 1.94$, $\beta_L = 1.64$). (d) Numerical simulations of plant biomass over time when the plant is associated with a fungal isolate with low phosphorus supply (α_L , dashed curve), with an isolate with low phosphorus supply (α_L , dashed curve), with an isolate with low phosphorus supply (α_{L+L}). We assume that the isolates have the same carbon sink strength ($\beta = (1.94 + 1.64)/2$) and differ only in their phosphorus supply ($\alpha_H = 2.39$, $\alpha_L = 2.06$). The chosen parameter values correspond to the parameters recovered from the statistical analysis of the experimental data (Fig. boxplots(c) and Table 1).



Fig. 3: (a) Maximal gain in productivity (see Eq. (3)) and (b) duration for which a synergy in plant growth is observed (in days) as functions of the carbon sink strength of the two associated fungi (parameters β_1 and β_2 , incremented in steps of size 0.1). (i) Parameters at their default values (see Table 1), (ii) higher plant intrinsic growth rate r_p , (iii) higher initial fungal biomass m_{0_i} , (iv) higher plant and fungal maintenance rates μ_p and μ_m , (v) lower phosphorus transfer ability α_i . The darker colors indicate a smaller gain in productivity and a shorter duration of the synergistic effect. Note that figures are symmetric about the $\beta_1 = \beta_2$ diagonal.



Fig. 4: The red curves represent the median of experimental measurements of plant biomass over 8 weeks when the plant is grown in association with an isolate with high carbon sink strength (Cuba8), with an isolate with low carbon sink strength (CC4), or with a mix of both isolates. The boxplots show the first and third quartile (box edges), the median (bar plots), and the range of the data of the gain in productivity at each sampling date, computed as described in Eq. (4)).



Fig. 5: (a) Average duration of the synergy in plant biomass observed when the plant is associated with two different fungal isolates. (b) Increase in productivity (expressed as % gain in plant biomass) observed when a synergy occurs. (c) Estimation of the α_i parameters (quantifying phosphorus exchange) and the β_i parameters (quantifying carbon exchange) of fungal isolates Cuba8 and CC4, recovered by fitting our model to the experimental data. Boxplots show the first and third quartile (box edges), the median (middle red line), the range of the data (whiskers), and data outliers (red crosses). Other parameters estimated from the statistical analysis are provided in Fig. (C.1).

345 Discussion

It has been proposed that complementarity in the reward provided by fungi to their 346 host plant (i.e., phosphorus transfer) positively correlates with increased plant biomass 347 (Mensah et al., 2015; Jansa et al., 2005). This hypothesis is supported by studies on 348 tripartite interactions of legumes with AM fungi and rhizobia, showing that minimal 349 functional overlap in the rewards provided might not only benefit plant growth, but 350 also microbe growth, as a fitter host would be able to provide a higher reward in return 351 (Afkhami et al., 2014; Afkhami and Stinchcombe, 2016) (but see Franklin et al. (2020); 352 Martignoni et al. (2020a)). Less intuitive, however, is how functional differences in 353 the reward received from the host (e.g., carbon supply) might ultimately affect host 354 benefit. It is likely that species providing very distinct rewards to different mutualists 355 (such as a plant providing pollen to bees and nectar to butterflies) should experience 356 enhanced benefit (such as pollination from both bees and butterflies) (Afkhami et al., 357 2014). However, empirical evidence assessing those potential productivity benefits is 358 lacking. 359

In our work, the amount of plant carbon supplied by the host to each fungal mu-360 tualist is determined by an intrinsic characteristic of the fungus (i.e., its carbon sink 361 strength), and it is independent of the amount of phosphorus that each fungus provides 362 in return. We show that differences in the rates at which plant carbon is supplied to the 363 AM fungi can effectively lead to plant productivity benefits, regardless of phosphorus 364 supply. Fungal isolates with high carbon sink strength are most beneficial when the 365 total fungal biomass is low. In this case, a higher amount of carbon per biomass intake 366 by the fungi helps the quick establishment of an abundant fungal community, with a 367 consequent increase in fungi to plant nutrients supply and thus in the plant growth 368 rate. Fungal isolates characterised by low carbon sink strength are not able to support 369

plant growth when fungal biomass is low, but by reducing the carbon cost to the plant they help the plant to reach a higher final size. We expect the synergistic effect to be stronger when fungal biomass is initially low, and when the plant is highly dependent on the AM symbiosis for nutrient provision, as in this case quick establishment of a fungal community is particularly important.

As AM fungal inoculants are being used as organic fertilizers worldwide (Gianinazzi 375 and Vosátka, 2004), our findings constitute an important contribution for agricultural 376 management (Ryan and Graham, 2018). We suggest that to maximize plant productiv-377 ity in depleted soils (i.e., where fungal biomass is low), plants should ideally associate 378 with multiple fungal species or isolates with high and low carbon sink strengths, where 379 fungi with high carbon sink strength contribute to an initial increase in the plant growth 380 rate, and fungi with low carbon sink strength support maximal productivity once plant 381 biomass is large. 382

Synergistic effects in productivity due to the presence of a diverse AM fungal commu-383 nity have been found in plants subjected to multiple stress factors and in the presence 384 of taxonomically distant AM fungal species (Yang et al., 2016; Thonar et al., 2014; 385 Crossay et al., 2019; Gosling et al., 2016; Maherali and Klironomos, 2007). While the 386 context of these papers is different from the one we studied, they provide evidence of 387 synergistic effects arising from the presence of multiple fungi. Here we show that syn-388 ergies can be explained by an interaction mechanism that does not require any stress 389 factors. We propose that, even in the absence of stress, differences in fungal carbon 390 sink strength can drive a synergistic effect in productivity. Indeed, our theoretical work 391 shows that variations in environmental stress did not affect the overall dynamics. 392

Competition between fungi is also known to affect productivity benefits (Berruti et al., 2016; Gosling et al., 2016; Koch et al., 2017). In particular, our previous studies have shown that strong competition between fungi can negatively affect productivity benefits in mixed cultures (Martignoni et al., 2020b). If the observed dynamics were due to competitive interactions alone, we would have expected to see a reduction in plant productivity in the presence of two isolates over the whole time window considered, which was not the case in our experimental results.

The similarities found between the experimental results and our simulations suggest 400 that, despite its simplicity, our model can be an efficient tool in predicting, and explain-401 ing the mechanisms behind, the response of plant productivity to a fungal community. 402 Our results lend support to the benefits of having redundancy in biological systems, 403 even if symbionts are ecologically similar, as both the average plant growth rate as well 404 as final plant biomass can be important determinants of productivity. Whether our 405 findings are valid for all conditions is not clear. For example, it would be worthwhile to 406 consider plant growth when resources are limiting, or in the presence of multiple plants. 407 The model could be expanded to consider the consequences of temporal variation in 408 carbon and phosphorus allocation strategies over time (Lekberg et al., 2013), the influ-409 ence of enemies on plant performance (Morris et al., 2007), potential anastomosis and 410 cytoplasmic exchange between the isolates (Novais et al., 2017), or competition between 411 fungi (Martignoni et al., 2020b; Franklin et al., 2014; Hammarlund et al., 2020). Inves-412 tigation of these factors is an important avenue of future work. We hope that the work 413 presented here will call for further studies to understand how productivity responds to 414 co-inoculation with multiple symbionts differing in their resource exchange capacity. 415

416 Authors contribution

- ⁴¹⁷ MMM developed the theory, developed and analysed the model, helped to design the ⁴¹⁸ experiment, interpreted the results, wrote the manuscript.
- ⁴¹⁹ JG performed the statistical analysis, performed the analysis of the experimental data,
- interpreted the results, contributed to discussions, contributed to writing of the final manuscript.
- ⁴²² XZ executed the experiment, performed measurements, collected experimental data,
- ⁴²³ and wrote the experimental part of the manuscript.
- ⁴²⁴ DR helped with measurement and analysis of the experimental study.
- VK designed preliminary and main experiment, executed and analysed the preliminary study, helped to analyze the main study, and wrote Appendix A.
- RCT funded the modelling portion of the project, helped with initial model development, contributed to discussions, contributed to the writing of the final manuscript.
- ⁴²⁹ MMH funded the experimental portion of the project, supervised the experimental
- aspect of the project, designed the experiment, contributed to discussions, helped to
- analyze the main study, contributed to the writing of the final manuscript.

432 Acknowledgement

- ⁴³³ JG was funded by GLOBNETS project (ANR-16-CE02-0009).
- RCT was funded by NSERC Discovery Grant RGPIN-2016-05277
- ⁴³⁵ MMH was funded by NSERC Discovery Grant (no grant number).

436 **References**

- ⁴³⁷ Afkhami, M. E., Rudgers, J. A., and Stachowicz, J. J. (2014). Multiple mutualist effects: ⁴³⁸ conflict and synergy in multispecies mutualisms. *Ecology*, 95(4):833–844.
- Afkhami, M. E. and Stinchcombe, J. R. (2016). Multiple mutualist effects on
 genomewide expression in the tripartite association between medicago truncatula,
 nitrogen-fixing bacteria and mycorrhizal fungi. *Molecular Ecology*, 25(19):4946–4962.
- Alkan, N., Gadkar, V., Yarden, O., and Kapulnik, Y. (2006). Analysis of quantitative interactions between two species of arbuscular mycorrhizal fungi, glomus mosseae and g.
 intraradices, by real-time pcr. *Applied and Environmental Microbiology*, 72(6):4192–4199.
- Augé, R. M., Toler, H. D., and Saxton, A. M. (2015). Arbuscular mycorrhizal symbiosis
 alters stomatal conductance of host plants more under drought than under amply
 watered conditions: a meta-analysis. *Mycorrhiza*, 25(1):13–24.
- Bachelot, B. and Lee, C. T. (2018). Dynamic preferential allocation to arbuscular
 mycorrhizal fungi explains fungal succession and coexistence. *Ecology*, 99(2):372–384.
- ⁴⁵² Baon, J., Smith, S., and Alston, A. (1993). Mycorrhizal responses of barley cultivars differing in p officiency. *Plant and Soil*, 157(1):07, 105
- differing in p efficiency. *Plant and Soil*, 157(1):97–105.

⁴⁵⁴ Bécard, G. and Fortin, J. (1988). Early events of vesicular–arbuscular mycorrhiza ⁴⁵⁵ formation on ri t-dna transformed roots. *New Phytologist*, 108(2):211–218.

Berruti, A., Lumini, E., Balestrini, R., and Bianciotto, V. (2016). Arbuscular mycorrhizal fungi as natural biofertilizers: let's benefit from past successes. Frontiers in *microbiology*, 6:1559.

⁴⁵⁹ Crossay, T., Majorel, C., Redecker, D., Gensous, S., Medevielle, V., Durrieu, G., Cav⁴⁶⁰ aloc, Y., and Amir, H. (2019). Is a mixture of arbuscular mycorrhizal fungi better
⁴⁶¹ for plant growth than single-species inoculants? *Mycorrhiza*, 29(4):325–339.

- di Fossalunga, A. S. and Novero, M. (2019). To trade in the field: the molecular determinants of arbuscular mycorrhiza nutrient exchange. *Chemical and Biological Technologies in Agriculture*, 6(1):1–12.
- Doner, L. W. and Bécard, G. (1991). Solubilization of gellan gels by chelation of cations.
 Biotechnology techniques, 5(1):25–28.

Drew, E., Murray, R., Smith, S., and Jakobsen, I. (2003). Beyond the rhizosphere:
growth and function of arbuscular mycorrhizal external hyphae in sands of varying
pore sizes. *Plant and Soil*, 251(1):105–114.

Feddermann, N., Finlay, R., Boller, T., and Elfstrand, M. (2010). Functional diversity in arbuscular mycorrhiza-the role of gene expression, phosphorous nutrition and symbiotic efficiency. *Fungal Ecology*, 3(1):1–8.

Franklin, J. B., Hockey, K., and Maherali, H. (2020). Population-level variation in
host plant response to multiple microbial mutualists. *American Journal of Botany*,
107(10):1389–1400.

Franklin, O., Näsholm, T., Högberg, P., and Högberg, M. N. (2014). Forests trapped in
nitrogen limitation-an ecological market perspective on ectomycorrhizal symbiosis. *New Phytologist*, 203(2):657–666.

Gianinazzi, S., Gollotte, A., Binet, M.-N., van Tuinen, D., Redecker, D., and Wipf, D.
(2010). Agroecology: the key role of arbuscular mycorrhizas in ecosystem services.
Mycorrhiza, 20(8):519–530.

Gianinazzi, S. and Vosátka, M. (2004). Inoculum of arbuscular mycorrhizal fungi for production systems: science meets business. *Canadian Journal of Botany*, 82(8):1264–
1271.

Giovannini, L., Sbrana, C., Avio, L., and Turrini, A. (2020). Diversity of a phosphate
 transporter gene among species and isolates of arbuscular mycorrhizal fungi. *FEMS Microbiology Letters*, 367(2):fnaa024.

Gosling, P., Jones, J., and Bending, G. D. (2016). Evidence for functional redundancy
 in arbuscular mycorrhizal fungi and implications for agroecosystem management.
 Mycorrhiza, 26(1):77–83.

- ⁴⁹¹ Gustafson, D. J. and Casper, B. B. (2006). Differential host plant performance as a
- ⁴⁹² function of soil arbuscular mycorrhizal fungal communities: experimentally manipu-
- lating co-occurring glomus species. *Plant Ecology*, 183(2):257–263.
- Hammarlund, S. P., Gedeon, T., Carlson, R. P., and Harcombe, W. R. (2020). Limitation by a shared mutualist promotes coexistence of multiple competing partners. *bioRxiv*.
- Hodge, A., Helgason, T., and Fitter, A. (2010). Nutritional ecology of arbuscular
 mycorrhizal fungi. *Fungal Ecology*, 3(4):267–273.
- Holland, J. N. and DeAngelis, D. L. (2010). A consumer–resource approach to the
 density-dependent population dynamics of mutualism. *Ecology*, 91(5):1286–1295.
- ⁵⁰¹ Ibrahim, M. (2018). Response of seeds quality of sunflower to inoculation with single ⁵⁰² and mixed species of indigenous arbuscular mycorrhizal fungi. *The Open Agriculture* ⁵⁰³ *Journal*, 12(1).
- Jansa, J., Mozafar, A., and Frossard, E. (2005). Phosphorus acquisition strategies within arbuscular mycorrhizal fungal community of a single field site. *Plant and Soil*, 276(1-2):163–176.
- Jansa, J., Smith, F. A., and Smith, S. E. (2008). Are there benefits of simultaneous root colonization by different arbuscular mycorrhizal fungi? *New Phytologist*, 177(3):779– 789.
- Jeffries, P., Gianinazzi, S., Perotto, S., Turnau, K., and Barea, J.-M. (2003). The contribution of arbuscular mycorrhizal fungi in sustainable maintenance of plant health and soil fertility. *Biology and Fertility of Soils*, 37(1):1–16.
- Johnson, C. A. and Bronstein, J. L. (2019). Coexistence and competitive exclusion in mutualism. *Ecology*, page e02708.

Kafle, A., Garcia, K., Wang, X., Pfeffer, P. E., Strahan, G. D., and Bücking, H. (2019).
 Nutrient demand and fungal access to resources control the carbon allocation to the
 symbiotic partners in tripartite interactions of medicago truncatula. *Plant, Cell & Environment*, 42(1):270–284.

Kiers, E. T., Duhamel, M., Beesetty, Y., Mensah, J. A., Franken, O., Verbruggen, E.,
Fellbaum, C. R., Kowalchuk, G. A., Hart, M. M., Bago, A., et al. (2011). Reciprocal
rewards stabilize cooperation in the mycorrhizal symbiosis. *Science*, 333(6044):880–
882.

Koch, A. M., Antunes, P. M., Maherali, H., Hart, M. M., and Klironomos, J. N. (2017).
 Evolutionary asymmetry in the arbuscular mycorrhizal symbiosis: conservatism in
 fungal morphology does not predict host plant growth. New Phytologist, 214(3):1330–
 1337.

Koide, R. T. (2000). Functional complementarity in the arbuscular mycorrhizal symbiosis. *The New Phytologist*, 147(2):233–235.

Kokkoris, V., Miles, T., and Hart, M. M. (2019). The role of in vitro cultivation on
 asymbiotic trait variation in a single species of arbuscular mycorrhizal fungus. *Fungal*

Biology, 123(4):307-317.

Latef, A. A. H. A., Hashem, A., Rasool, S., Abd_Allah, E. F., Alqarawi, A., Egamberdieva, D., Jan, S., Anjum, N. A., and Ahmad, P. (2016). Arbuscular mycorrhizal symbiosis and abiotic stress in plants: A review. *Journal of Plant Biology*, 59(5):407–426.

Lee, E.-H., Eo, J.-K., Ka, K.-H., and Eom, A.-H. (2013). Diversity of arbuscular mycorrhizal fungi and their roles in ecosystems. *Mycobiology*, 41(3):121–125.

Lekberg, Y., Rosendahl, S., Michelsen, A., and Olsson, P. A. (2013). Seasonal carbon allocation to arbuscular mycorrhizal fungi assessed by microscopic examination, stable isotope probing and fatty acid analysis. *Plant and Soil*, 368(1-2):547–555.

Lenth, R. V., Lenth, M. R. V., and Vdgraph, S. (2020). Package 'rsm'.

Maherali, H. and Klironomos, J. N. (2007). Influence of phylogeny on fungal community
 assembly and ecosystem functioning. *science*, 316(5832):1746–1748.

Martignoni, M. M., Hart, M. M., Garnier, J., and Tyson, R. C. (2020a). Parasitism
within mutualist guilds explains the maintenance of diversity in multi-species mutualisms. *Theoretical Ecology*, pages 1–13.

Martignoni, M. M., Hart, M. M., Tyson, R. C., and Garnier, J. (2020b). Diversity within mutualist guilds promotes coexistence and reduces the risk of invasion from an alien mutualist. *Proceedings of the Royal Society B*, 287(1923):20192312.

Mensah, J. A., Koch, A. M., Antunes, P. M., Kiers, E. T., Hart, M., and Bücking, H.
(2015). High functional diversity within species of arbuscular mycorrhizal fungi is associated with differences in phosphate and nitrogen uptake and fungal phosphate metabolism. *Mycorrhiza*, 25(7):533–546.

Morris, W. F., Hufbauer, R. A., Agrawal, A. A., Bever, J. D., Borowicz, V. A., Gilbert,
G. S., Maron, J. L., Mitchell, C. E., Parker, I. M., Power, A. G., et al. (2007).
Direct and interactive effects of enemies and mutualists on plant performance: a
meta-analysis. *Ecology*, 88(4):1021–1029.

⁵⁵⁸ Murphy, J. and Riley, J. P. (1962). A modified single solution method for the determi-⁵⁵⁹ nation of phosphate in natural waters. *Analytica chimica Acta*, 27:31–36.

Novais, C. B. d., Pepe, A., Siqueira, J. O., Giovannetti, M., and Sbrana, C. (2017).
 Compatibility and incompatibility in hyphal anastomosis of arbuscular mycorrhizal
 fungi. *Scientia Agricola*, 74(5):411–416.

Pearson, J. and Jakobsen, I. (1993). Symbiotic exchange of carbon and phosphorus be tween cucumber and three arbuscular mycorrhizal fungi. New phytologist, 124(3):481–
 488.

Powell, J. R. and Rillig, M. C. (2018). Biodiversity of arbuscular mycorrhizal fungi and
 ecosystem function. New Phytologist, 220(4):1059–1075.

Pozo, M. J. and Azcón-Aguilar, C. (2007). Unraveling mycorrhiza-induced resistance.
 Current Opinion in Plant Biology, 10(4):393–398.

Řezáčová, V., Konvalinková, T., and Jansa, J. (2017). Carbon fluxes in mycorrhizal
 plants. In *Mycorrhiza-eco-physiology, secondary metabolites, nanomaterials*, pages
 1–21. Springer.

Ryan, M. H. and Graham, J. H. (2018). Little evidence that farmers should consider
 abundance or diversity of arbuscular mycorrhizal fungi when managing crops. New
 Phytologist, 220(4):1092–1107.

Sawers, R. J., Gutjahr, C., and Paszkowski, U. (2008). Cereal mycorrhiza: an ancient symbiosis in modern agriculture. *Trends in Plant Science*, 13(2):93–97.

Sawers, R. J., Svane, S. F., Quan, C., Grønlund, M., Wozniak, B., Gebreselassie, M.N., González-Muñoz, E., Chávez Montes, R. A., Baxter, I., Goudet, J., et al. (2017).
Phosphorus acquisition efficiency in arbuscular mycorrhizal maize is correlated with
the abundance of root-external hyphae and the accumulation of transcripts encoding
pht1 phosphate transporters. New Phytologist, 214(2):632–643.

Schenck, N. and Smith, G. S. (1982). Additional new and unreported species of myc orrhizal fungi (endogonaceae) from florida. *Mycologia*, 74(1):77–92.

Shrivastava, G., Ownley, B. H., Augé, R. M., Toler, H., Dee, M., Vu, A., Köllner, T. G.,
and Chen, F. (2015). Colonization by arbuscular mycorrhizal and endophytic fungi
enhanced terpene production in tomato plants and their defense against a herbivorous
insect. Symbiosis, 65(2):65–74.

Smith, F., Jakobsen, I., and Smith, S. (2000). Spatial differences in acquisition of
 soil phosphate between two arbuscular mycorrhizal fungi in symbiosis with medicago
 truncatula. *The New Phytologist*, 147(2):357–366.

⁵⁹² Smith, S. E. and Read, D. J. (2010). *Mycorrhizal symbiosis*. Academic press.

Stanton, M. L. (2003). Interacting guilds: moving beyond the pairwise perspective on
 mutualisms. *The American Naturalist*, 162(S4):S10–S23.

Thomson, B., Robson, A., and Abbott, L. (1990). Mycorrhizas formed by gigaspora calospora and glomus fasciculatum on subterranean clover in relation to soluble carbohydrate concentrations in roots. *New Phytologist*, 114(2):217–225.

Thonar, C., Frossard, E., Šmilauer, P., and Jansa, J. (2014). Competition and facilitation in synthetic communities of arbuscular mycorrhizal fungi. *Molecular Ecology*,
23(3):733-746.

Treseder, K. K. (2013). The extent of mycorrhizal colonization of roots and its influence on plant growth and phosphorus content. *Plant and Soil*, 371(1):1–13.

Van der Heijden, M. G., Klironomos, J. N., Ursic, M., Moutoglis, P., Streitwolf-Engel,
 R., Boller, T., Wiemken, A., and Sanders, I. R. (1998). Mycorrhizal fungal diver-

sity determines plant biodiversity, ecosystem variability and productivity. Nature,

⁶⁰⁶ 396(6706):69.

Vandenkoornhuyse, P., Mahé, S., Ineson, P., Staddon, P., Ostle, N., Cliquet, J.-B.,
Francez, A.-J., Fitter, A. H., and Young, J. P. W. (2007). Active root-inhabiting microbes identified by rapid incorporation of plant-derived carbon into rna. *Proceedings*of the National Academy of Sciences, 104(43):16970–16975.

Verbruggen, E., Van der Heijden, M. G., Weedon, J. T., Kowalchuk, G. A., and Röling,
 W. F. (2012). Community assembly, species richness and nestedness of arbuscular
 mycorrhizal fungi in agricultural soils. *Molecular Ecology*, 21(10):2341–2353.

Vierheilig, H., Bago, B., Lerat, S., and Piché, Y. (2002). Shoot-produced, lightdependent factors are partially involved in the expression of the arbuscular mycorrhizal (am) status of am host and non-host plants. Journal of Plant Nutrition and
Soil Science, 165(1):21–25.

Violi, H. A., Treseder, K. K., Menge, J. A., Wright, S. F., and Lovatt, C. J. (2007). Density dependence and interspecific interactions between arbuscular mycorrhizal fungi
mediated plant growth, glomalin production, and sporulation. *Botany*, 85(1):63–75.

⁶²¹ Walder, F. and van der Heijden, M. G. (2015). Regulation of resource exchange in the ⁶²² arbuscular mycorrhizal symbiosis. *Nature Plants*, 1(11):15159.

Xu, W. and Mage, J. A. (2001). A review of concepts and criteria for assessing agroe cosystem health including a preliminary case study of southern ontario. Agriculture,
 Ecosystems & Environment, 83(3):215–233.

Yang, Y., Liang, Y., Han, X., Chiu, T.-Y., Ghosh, A., Chen, H., and Tang, M. (2016).
 The roles of arbuscular mycorrhizal fungi (amf) in phytoremediation and tree-herb
 interactions in pb contaminated soil. *Scientific reports*, 6:20469.

⁶²⁹ Zhu, Y.-G. and Miller, R. M. (2003). Carbon cycling by arbuscular mycorrhizal fungi ⁶³⁰ in soil-plant systems. *Trends in Plant Science*, 8(9):407–409.

Appendix A: Preliminary analysis for the selection of AM fungal isolates

Experimental design: In order to test the carbon and phosphorus sink strength 633 of multiple *Rhizophaqus irregularis* isolates we performed a greenhouse experiment in 634 a completely randomized block design (n = 10, total 100 experimental units) where 635 we used a single spore-single plant inoculation approach (as described by Kokkoris 636 et al. (2019)) for nine R. irregularis isolates and pre-germinated plantlets of Linum usi-637 tatissimum (Flax, var. Bethune). This experiment was conducted at UBC Okanagan 638 greenhouse from May 2018 to September 2018 and was part of a larger study (of 400 639 experimental units) designed to assess life history variation among R. irregularis iso-640 lates. Variation in plant biomass reflects differences between the carbon sink strength 641 of the isolates while % shoot P reflects differences between the P sink strength of each 642 isolate. 643

Growing conditions: AM fungal isolates and host plants were grown in 2L pots containing (v/v=1:1) sterilized medium-fine sand (SAKRETE Play Sand) and vermiculate. Plants were grown for approximately three months (to flowering stage). Water and fertilizer were as described for the main experiment. The temperature ranged from 26 to 20°C (day/night) with a photoperiod of 18 h per day, of 200 μ mol s-1 m-2 per μ A as measured with a LI-250A light meter (Biosciences).

Harvest and Plant responses: Upon harvest, roots were separated from shoots and wet weight of each part was obtained. Roots were fragmented and stained for AM fungal colonization status assessment (positive vs negative) and shoots were dried at 60°C until weight stability was achieved (approximately after 72h). After recording the dry shoot weight, the tissue was pulverized, homogenized, and was used to calculate the % P in the flax shoot using the color development method described in the main manuscript (Murphy and Riley, 1962).

Statistical analysis: To evaluate the carbon and phosphorus sink strength of each isolate we first calculated the mycorrhizal response (MR) for the total plant biomass and % shoot P. MR describes any benefit or detriment for a specific plant trait (e.g. biomass and phosphorus in our case) as a result of AM fungal inoculation (Baon et al., 1993; Sawers et al., 2008). The MR was calculated as: MR = $\ln (X/Y)$ where X= response of mycorrhizal plants and Y= mean response of non-mycorrhizal (control) plants.

We used a mixed effect linear model to examine the variation between the isolates with AM fungal isolate identity as a fixed factor and block as a random factor followed by pairwise comparison (emmeans package – Lenth et al. (2020)) (Fig. A.1). The package uses a p-value adjustment method by default, to ensure that the confidence interval remains large enough when performing multiple comparisons. The analysis was performed in R studio (Version 1.0.136–2009–2016 RStudio, Inc.).



Fig. A.1: Linum usitatissimum (Flax) mycorrhizal response of (A) total biomass and (B) % shoot P, for different fungal isolates (x-axis). Cuba8 has a higher carbon sink strength compared to CC4 since the plant biomass was significantly lower (p < 0.05) but the two isolates are not different in their P sink strength (p = 0.99). Blue line indicates the mean value of the non-mycorrhizal plants. Boxplots show the third and first quartile (box edges), the median (middle black line), the range of the data (whiskers) and data outliers (black open circles).

⁶⁶⁹ Appendix B: Inoculation method



Fig. B.1: (1a) AM fungal inoculation method. 'Inoculation Discs' were created by mixing sterile quartz sand with 1% gellan gum - H_2O solution. We then inoculated each disc with 30 Cuba8 spores or/and 10 CC4 spores to ensure a minimum of 6 viable spores per pot. (1b) After filling each pot halfway with the growing media (sand-vermiculite) an inoculation disc containing the spores) was embedded in the middle. (1c) To ensure the physical interaction of plant-AM fungi, we placed a straw (5mm diameter and 5cm length) filled with wet sand on the top of the disc and completed the volume of the pot with our substrate. (1d) The germinated seed was placed into the straw, positioning it directly above the AM fungal inoculum disc.

Appendix C: Inferred parameters



Fig. C.1: Parameters recovered from fitting our model to the experimental data. Median values: $r_0 = 0.33$, $p_0 = 0.08$, $m_{0_1} = 0.14$, $m_{0_2} = 0.11$, d = 1.07, $\mu_p = 1.44$, $\mu_m = 1.05$, $q_{hp} = 2.93$, $q_{cm} = 2.93$, $\sigma = 0.02$. Parameters q_{cp} and q_{hm} have been set equal to 1.

⁶⁷¹ Appendix D: Statistical analysis based on the mean ⁶⁷² average of the experimental observations

In this appendix we present the analysis of the experimental data resulting when considering the mean, instead of the median, of the experimental observations. The mean of the synergistic effect is computed as

⁶⁷⁶ % gain in productivity(w) =
$$\frac{p_{H+L}(t) - \max(mean(p_H)(t), mean(p_L)(t)))}{\max(mean(p_H)(t), mean(p_L)(t))} \times 100,$$
 (7)

where p_{H+L} represent the weekly measurements of plant biomass in the presence of both isolates, $mean(p_H)(t)$ and $mean(p_L)(t)$ refer to the mean of the plant biomass weekly measurements collected in the presence of a single isolate with high or low carbon sink strength. A synergy is observed if the % gain in productivity is positive. Note that Eq. (7) corresponds to Eq. (4) where the median of the experimental measurements has been substituted with the mean.

The confident intervals of the synergistic effect in Fig. 4 are obtained by computing (684)

% gain in productivity'(w) =
$$\frac{p_{H+L} - \max(p_H(w), p_L(w))}{\max(p_H(w), p_L(w))} \times 100.$$
 (8)

We make this choice for two reasons: First, the confident intervals obtained when considering Eq. (7) are large because of the small amount of data (8 data points per weeks), while in Eq. (8) we do have more data available ($8 \times 64 = 512$ data points per weeks). Secondly, the mean of the gain in productivity obtained by using Eqs. (7) and (8) are similar, as the variance of max(p_H, p_L) is small. We can write:

⁶⁹¹ mean(% gain in productivity'(w)) =
$$\left(mean\left[\frac{p_{H+L}(w)}{\max(p_H(w), p_L(w))}\right] - 1\right) \times 100$$
, (9)

⁶⁹² and we can show that, at each week,

$$\frac{mean(p_{H+L})}{mean(max(p_H, p_L))} \le \frac{mean(p_{H+L})}{max(mean(p_L), mean(p_H))}.$$
(10)

⁶⁹⁴ From the Jensen's inequality we know that, at each week,

$$\frac{mean(p_{H+L})}{mean(\max(p_H, p_L))} \le mean\left(\frac{p_{H+L}}{\max(p_H, p_L)}\right).$$
(11)

Given that the variance of $\max(p_H, p_L)$ is small, we can assume that $\max(p_H, p_L)$ follows a normal distribution. We obtain:

$$mean\left(\frac{p_{H+L}}{\max(p_H, p_L)}\right) \sim \frac{mean(p_{H+L})}{mean(\max(p_H, p_L))} \pm \frac{Var(\max(p_H, p_L))}{mean(\max(p_H, p_L))^2} \times mean(p_{H+L}).$$
(12)

698

693

695

685

As $Var(\max(p_H, p_L)) \ll 1$, we obtain that at each week:

$$mean(\% \text{ gain in productivity}') = \frac{mean(p_{H+L})}{mean(\max(p_H, p_L))} - 1 + Var\left(\frac{\max(p_H, p_L)}{mean(\max(p_H, p_L))^2}\right) \times mean(p_{H+L}) \leq mean(\% \text{ gain in productivity}).$$
(13)

So if mean(% gain in productivity') is significantly larger than zero, so does mean(% gain)in productivity) and the confidence intervals of (% gain in productivity') can be used

⁷⁰⁰ in productivity) and the confidence intervals of (% gain in productivity). ⁷⁰¹ to describe the confidence intervals of (% gain in productivity).

In Fig. D.1 we see that the mean is significantly above zero in weeks 1, 2, and 4, and significantly below zero in weeks 6, 7 and 8. The gain in productivity at week 3 is not significantly different than zero, while when considering the median (Fig. 4) we obtained a significant loss in productivity at week 3.



Fig. D.1: Equivalent of Fig. 4 when considering the mean instead of the median of the experimental observations. The red curves represent the mean of experimental measurements of plant biomass over 8 weeks when the plant is grown in association with an isolate with high carbon sink strength (Cuba8), with an isolate with low carbon sink strength (CC4), or with a mix of both isolates. The boxplots show the first and third quartile (box edges), the median (bar plots), and the range of the data of the gain in productivity at each sampling date, computed as described in Eqs. (7) and (8).

⁷⁰⁶ Appendix E: Multiple fungal partners



Fig. E.1: Plant growth over time when the plant is associated with five AM fungal partners (i.e., i = 1, ..., 5) with (a) different carbon sink strength and identical phosphorus supply (with $\alpha_i = 2.2$ for all *i*) or (b) different phosphorus supply and identical carbon sink strength (with $\beta_i = 1.4$ for all *i*). (a) The solid line represents plant growth when the fungal partners have mixed carbon sink strength ($\beta_1 = 1.0, \beta_2 = 1.2, \beta_3 = 1.4, \beta_4 = 1.6, \beta_5 = 1.8$). The dotted curve represents plant growth when fungal partners have low carbon sink strength ($\beta_i = 1.0$ for all *i*), and the dashed curve represents plant growth when the fungal partners provide mixed phosphorus supply ($\alpha_1 = 1.6, \alpha_2 = 1.8, \alpha_3 = 2.0, \alpha_4 = 2.2, \alpha_5 = 2.4$). The dotted curve represents plant growth when fungal partners provide high phosphorus supply ($\alpha_i = 2.4$ for all *i*), and the dashed curve represents plant growth when fungal partners provide high phosphorus supply ($\alpha_i = 1.6$ for all *i*).

Analysis of plant final size: We assume that all fungi provide the same amount of phosphorus to the plant (i.e., $\alpha_i = \alpha$) but differ in their access to carbon (i.e., β_i differ, where $\boldsymbol{\beta} = (\beta_1, \ldots, \beta_N)$). We want to understand how the plant final size p^* depends on the carbon sink strength of all mutualists. From Martignoni et al. (2020a) we know that

$$p^{*}(\boldsymbol{\beta}) = \frac{q_{hm}\alpha}{q_{cm}\overline{\beta}}P^{*}(\boldsymbol{\beta}) - d$$
with $P^{*}(\boldsymbol{\beta}) = \frac{(1+Q)\sum_{i=1}^{N}\frac{1}{\eta_{M_{i}}} + \sqrt{(1+Q)^{2}(\sum_{i=1}^{N}\frac{1}{\eta_{M_{i}}})^{2} - 4Q\sum_{i=1}^{N}\frac{\overline{\beta}}{\beta_{i}\eta_{M_{i}}}(\sum_{i=1}^{N}\frac{\beta_{i}}{\overline{\beta}\eta_{M_{i}}} + \eta_{P_{i}})}{2\left(\sum_{i=1}^{N}\frac{\beta_{i}}{\overline{\beta}\eta_{M_{i}}} + \eta_{P_{i}}\right)},$

$$(14)$$

712

where the non-dimensionalized variables P^* and M_i are defined as $P^* = \frac{q_{cm}\beta}{q_{hm}\alpha}p^*$ and $M_i = \frac{q_{cp}\beta_i}{q_{hm}\alpha}m_i$ (Martignoni et al., 2020a). Non-dimensionalized parameters Q, η_{M_i} and η_P are defined as $Q = \frac{q_{cm}q_{hp}}{q_{cp}q_{hm}}$, $\eta_{P_i} = \frac{\mu_p}{q_{cm}\beta_i}$, and $\eta_{M_i} = \frac{\mu_m}{q_{cp}\beta_i}$ (Martignoni et al., 2020a). To go further, we need to come back to the original variable for η_{M_i} and η_{P_i} . We 717 define $\overline{\beta} = mean(\beta)$ and we obtain

$$P^{*}(\boldsymbol{\beta}) = \frac{(1+Q)\frac{Nq_{cm}}{\mu_{m}}\overline{\beta} + \sqrt{(1+Q)^{2}(\frac{Nq_{cm}}{\mu_{m}}\overline{\beta})^{2} - 4Q\frac{Nq_{cm}\overline{\beta}}{\mu_{m}}(\sum_{i=1}^{N}\frac{q_{cm}\beta_{i}^{2}}{\overline{\beta}\mu_{m}} + \frac{\mu_{p}}{q_{cm}\overline{\beta}})}{2\left(\sum_{i=1}^{N}q_{cm}\frac{\beta_{i}^{2}}{\overline{\beta}\mu_{m}} + \frac{\mu_{p}}{q_{cm}\overline{\beta}}\right)}$$
$$= \frac{(1+Q)\overline{\beta} + \overline{\beta}\sqrt{(1+Q)^{2} - 4Q(\frac{1}{N}\sum_{i=1}^{N}\frac{\beta_{i}^{2}}{\overline{\beta}^{2}} + \frac{\mu_{p}\mu_{m}}{q_{cm}^{2}\overline{\beta}^{2}N})}}{2\left(\frac{1}{N}\sum_{i=1}^{N}\frac{\beta_{i}^{2}}{\overline{\beta}^{2}} + \frac{\mu_{p}\mu_{m}}{q_{cm}^{2}\overline{\beta}^{2}N}\right)}.$$
(15)

718

720

⁷¹⁹ We can see that

$$\frac{1}{N}\sum_{i=1}^{N}\frac{\beta_i^2}{\overline{\beta}^2} = 1 + \frac{Var(\boldsymbol{\beta})}{\overline{\beta}^2}.$$
(16)

721 Thus we obtain

$$P^{*}(\boldsymbol{\beta}) = \overline{\boldsymbol{\beta}} \frac{(1+Q) + \sqrt{(1+Q)^{2} - 4Q\left(1 + \frac{\mu_{p}\mu_{m}}{q_{cm}^{2}\overline{\boldsymbol{\beta}}^{2}N} + \frac{Var(\boldsymbol{\beta})}{\overline{\boldsymbol{\beta}}^{2}}\right)}}{2\left(1 + \frac{\mu_{p}\mu_{m}}{q_{cm}^{2}\overline{\boldsymbol{\beta}}^{2}N} + \frac{Var(\boldsymbol{\beta})}{\overline{\boldsymbol{\beta}}^{2}}\right)}, \qquad (17)$$

723 and

724

$$p^*(\boldsymbol{\beta}) = \frac{q_{hm}\alpha}{q_{cm}\overline{\beta}} P^*(\boldsymbol{\beta}) - d.$$
(18)

Eq. (18) shows that $p^*(\beta)$ is decreasing with respect to the mean $\overline{\beta}$ of β and decreases with respect to the variance $Var(\beta)$.