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Quantum of Thermal Conductance of Nanofilms due to Surface-Phonon Polaritons

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Based on the Boltzmann transport equation, we demonstrate that the thermal conductance per unit width of a sufficiently thin polar nanofilm supporting the propagation of surface-phonon polaritons along its surfaces is independent of the material properties and is given by $12z(3)k_B^3T^2/ch^2$, where k_B and h are the respective Boltzmann and Planck constants, while c is the light speed in vacuum, T the temperature and $z(3)$ the Riemann zeta function. The huge propagation length of these energy carriers establishes that this quantization holds not only for temperatures much smaller than 1 K, as is the case of electrons and phonons, but also for those comparable to room temperature, which can significantly facilitate its observation and implementation in the thermal management of nanoscale electronics and photonics.

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One-dimensional (1D) heat conduction at low temperature has been extensively investigated due to the existence of a quantum of thermal conductance. This quantization corresponds to the heat flux carried by ballistic phonons or electrons in a single polarization and is given by $\pi^2k_B^2T/3h$, where k_B and h are the respective Boltzmann and Planck constants, and T is the temperature [1–5]. This minimal and universal amount of heat, for a given T , holds for both electrons and phonons, as was theoretically predicted [6–9] and experimentally validated [9, 10]. Given that the typical mean free paths of electrons and phonons are smaller than $1\mu\text{m}$ at room temperature, with lower temperatures leading to longer mean free paths, the observation of this quantization in the ballistic regime typically requires the utilization of nanostructures at temperatures lower than 1 K [10].

The physics of two-dimensional (2D) systems has also become an increasingly important research field due to the fundamental phenomena that have provided the basis for modern device concepts [11, 12]. For instance, a 2D electron gas is typically found in transistor-like structures made from semiconductors that control the mainstream information technologies [13–15]. In addition, with the recent advent of 2D materials, it is now possible to manipulate 2D phonon gases and excite fundamental modes of heat transport [16, 17]. As in the case of 1D heat conduction driven by either electrons or phonons, these 2D ballistic modes appear at very low temperatures, which limits their observation and application. However, ballistic heat transport can be achieved at room temperature by surface phonon-polaritons (SPhPs), which are evanescent electromagnetic waves generated by the hybridization of photons and phonons at the interface of polar materials [18, 19]. This ballistic behavior appears due to the huge SPhP propagation length that was found to be as long as 1 m [20, 21] and hence orders of magnitude longer than the typical mean free paths of electrons and phonons at room temperature. The wavelength of SPhPs

propagating along thin films is usually much larger than the film thickness [20], which makes of these energy carriers a 2D quantum gas. As a result of these relatively long values of the propagation length and wavelength of SPhPs, their contribution to the in-plane heat transport was measured to be comparable to or even higher than the one of phonons [22, 23]. Similar to the case of phonons and electrons, as well as to SPhPs propagating along nanowires [21], the ballistic heat transport of SPhPs along nanofilms is expected to be characterized by a 2D quantum of thermal conductance, however its existence and value have not been explored yet. The temperature scaling of this 2D quantization is expected to be different than that in 1D systems, due to the distinctive features of the density of states.

The purpose of this letter is to demonstrate that the thermal conductance per unit width of a thin enough polar nanofilm supporting the propagation of SPhPs along its surfaces is quantized for any temperature comparable to or lower than room temperature. As the film thickness d decreases, this quantization arises from the convergence of the dispersion relation of SPhPs to that of light in vacuum, while their propagation length ($\propto d^{-2}$) increases, which ensures the ballistic propagation of SPhPs in a wide frequency spectrum. This 2D quantum of thermal conductance appears in thin films of SiN thinner than 50 nm and therefore its observation could be achieved with the current experimental capabilities.

Let us consider a polar nanofilm supporting the simultaneous propagation of SPhPs and phonons due to the temperature difference $T_h > T_c$ set by two thermal baths, as shown in Fig. 1. The resulting steady-state heat transport along the z axis is thus driven by the heat fluxes generated by these two types of energy carriers. Assuming that the phonon heat conduction can be described by an effective thermal conductivity k_{ph} , the principle of energy conservation along with the Fourier’s law establishes that the temperature T inside the nanofilm is given

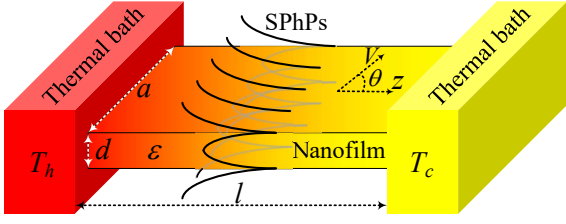


FIG. 1: Scheme of a polar nanofilm supporting the propagation of SPhPs due to the temperature difference $T_h - T_c > 0$ imposed by two thermal baths.

by

$$-k_{ph} \frac{dT}{dz} + q(z) = q_t, \quad (1)$$

where q is the SPhP heat flux and q_t is the total heat flux, a constant independent of the position z . The phonon thermal conductivity k_{ph} includes the contributions of both the acoustic phonon modes, which usually dominate the heat transport, and the optical ones that couple with photons to generate the SPhPs. Taking into account that SPhPs can be treated like bosonic particles [24], q can be determined by means of the Boltzmann transport equation (BTE) under the relaxation time approximation and the intensity representation. For the steady-state heat transport along the z axis shown in Fig. 1, the BTE takes the form

$$I_\omega + \mu\Lambda \frac{\partial I_\omega}{\partial z} = I_\omega^0 \quad (2)$$

where $\mu = \cos(\theta)$ is the cosine of the angle between the SPhP propagation direction and the $+z$ axis, $\Lambda = \Lambda(\omega)$ is the propagation length of SPhPs, I_ω is their intensity, and $I_\omega^0 = V\hbar\omega f_0(T)D(\omega)$ its equilibrium counterpart, with $2\pi\hbar$, $f_0(T)$, and $D(\omega)$ being the Planck constant, Bose-Einstein distribution function and SPhP density of states per unit area, frequency, and angle; respectively. Since SPhPs propagate along the interface of the film and they span over its surface, their 2D density of states is given by [24, 25] $D(\omega) = \beta_R / ((2\pi)^2 V)$, where β_R is the real part of the in-plane SPhP wave vector. After solving Eq. (2) for the intensity I_ω , the SPhP heat flux can be determined by

$$q = \frac{1}{d} \int \int I_\omega \mu d\omega d\theta. \quad (3)$$

Equation (3) is almost identical to the usual 3D expression for the phonon heat flux, except by its integration on $d\theta$ instead of $d\mu$, due to the 2D heat transport of SPhPs. Once I_ω and q are determined either numerically (accurate method) or analytically (approximate solution), as detailed in the supplementary material (SM) [26], the temperature profile $T(z)$ and total heat flux q_t can be determined by integrating Eq. (1) and evaluating its result

with the boundary conditions $T(0) = T_h$ and $T(l) = T_c$. In the very thin film limit of interest in this work, the SPhP heat flux can be described by the approximate analytical solution of Eqs. (2) and (3), which yield [26]

$$q(\xi) = \int \frac{\Delta I_\omega^0}{\lambda d} [\pi - 2(E_4(\xi) + E_4(\lambda - \xi))] d\omega, \quad (4)$$

where $\xi = z/\Lambda$, $\lambda = l/\Lambda$, $\Delta I_\omega^0 = I_\omega^0(T_h) - I_\omega^0(T_c)$, and $E_n(x) = \int_0^{\pi/2} \mu^{n-2} e^{-x/\mu} d\theta$ is a positive function with values between zero and unity for any $n = 1, 2, \dots$. Note that the SPhP heat flux at two equidistant positions from the external film surfaces ($\xi = 0; \lambda$) takes the same value ($q(\xi) = q(\lambda - \xi)$), such that its maximum appears at the middle of the film ($\xi = \lambda/2$). This behavior arises from the non-local dependence of the heat flux on the temperature profile [26], which exhibits a non-linear dependence on position, as established by the integration of Eq. (1) for the heat flux in Eq. (4). The explicit results are

$$T(\xi) = T_h - \Delta T \frac{z}{l} + \frac{\Delta T}{k_{ph}} \int k_\omega \left[\frac{\pi\xi + 2\Delta\psi(\xi)}{\pi\lambda - 4\psi(0)} - \frac{\xi}{\lambda} \right] d\omega, \quad (5a)$$

$$q_t = (k_{pol} + k_{ph}) \frac{\Delta T}{l}, \quad (5b)$$

where $\Delta T = T_h - T_c$, $\Delta\psi(\xi) = \psi(\xi) - \psi(0)$, $\psi(x) = E_5(x) - E_5(\lambda - x)$ and the spectral SPhP thermal conductivity k_ω is defined in terms of its integrated counterpart $k_{pol} = \int k_\omega d\omega$ given by

$$k_{pol} = \frac{1}{4\pi d} \int \left(1 - \frac{4\psi(0)}{\pi\lambda} \right) \hbar\omega\beta_R\Lambda \frac{\partial f_0}{\partial T} d\omega. \quad (6)$$

Equation (6) was derived by considering that the average temperature $T = (T_h + T_c)/2 \gg \Delta T$, such that $f_0(T_h) - f_0(T_c) = \Delta T \partial f_0 / \partial T$. The rigorous solution of SPhP BTE developed in this work considers the boundary scattering more accurately than the semi-empirical Matthiessen's rule and hence the predictions of k_{pol} in Eq. (6) are expected to be more precise than those based on this latter rule, as detailed in the Supplementary Material [26]. According to Eq. (5a), the deviation of the temperature profile from the usual linear dependence (first two terms) on position is driven by the ratio k_{pol}/k_{ph} between the SPhP and phonon thermal conductivities. Interestingly, regardless of the values of this ratio, the SPhP contribution to the temperature profile disappears at the middle of the film ($\xi = \lambda/2$). This behavior is related to the symmetry of the SPhP heat flux around this position and is well confirmed by accurate numerical results, as shown below. As a result of this symmetry, the sum of temperatures at two equidistant points from the external film surfaces is an invariant of heat conduction given by $T(\xi) + T(\lambda - \xi) = T_h - T_c$, as established by Eq. (5a). This feature of temperature is generated by the

non-local behavior of the heat conduction and is analogous to the characteristic temperature profiles found in radiative heat transfer [27].

As the heat transport in a polar nanofilm is driven by both phonons and SPhPs, the total heat flux is determined by the sum of thermal conductivities related to these two energy carriers, as established by Eq. (5b). This fact indicates that, as the film thickness scaled down, the usual reduction of k_{ph} could be offset by the increasing values of k_{pol} , due to the predominant surface effects driving the propagation of SPhPs. In the SPhP diffusive approximation ($\lambda = l/\Lambda \gg 1$), the ratio $\psi(0)/\lambda \rightarrow 0$ and Eq. (6) reduces to the previous expression derived by Chen *et al.*[24], as expected. In the ballistic limit ($\lambda \ll 1$), on the other hand, $1-4\psi(0)/\pi\lambda \approx 2\lambda/\pi$ and the SPhP thermal conductance $G = adk_{pol}/l$ of the nanofilm is given by

$$G = \frac{a\sqrt{\varepsilon_0}}{2\pi^2c} \int \hbar\omega^2 \frac{\partial f_0}{\partial T} d\omega, \quad (7)$$

where c is the speed of light in vacuum and ε_0 ($= 1$ for air) is the relative permittivity of the medium surrounding the nanofilm. Equation (7) was derived by using the fact that the ballistic regime characterized by long propagation lengths ($\Lambda \gg l$) appears for very thin films along which the SPhPs propagate with a wave vector $\beta_R = \sqrt{\varepsilon_0}\omega/c$ independent of the film properties [19, 20, 24]. By contrast, the SPhP propagation length for this photon-like mode does depend on the material properties and is generally non-zero in some discrete frequency intervals [22, 23, 28] $\omega_n^{\min} \leq \omega \leq \omega_n^{\max}$, with ω_n^{\min} and ω_n^{\max} being the minimum and maximum frequencies supporting the SPhP propagation for the segment $n = 1, 2, \dots, N$. The integration in Eq. (7) for this allowed frequency intervals can then be written as follows

$$G = \frac{2a\sqrt{\varepsilon_0}k_B^3T^2}{ch^2} \sum_{n=1}^N \int_{A_n/T}^{B_n/T} \frac{x^3 e^x}{(e^x - 1)^2} dx, \quad (8)$$

where $A_n = \hbar\omega_n^{\min}/k_B$ and $B_n = \hbar\omega_n^{\max}/k_B$. The SPhP thermal conductance is thus determined by the relative values of these normalized cutoff frequencies, characteristic of the film material, with respect to temperature. The analytical calculation of the integral in Eq. (8) yields

$$G = \frac{2a\sqrt{\varepsilon_0}k_B^3T^2}{ch^2} \sum_{n=1}^N [J(A_n/T) - J(B_n/T)], \quad (9a)$$

$$J(x) = \frac{x^3}{e^x - 1} - 3x^2 \ln(1 - e^{-x}) + 6xL_2(e^{-x}) + 6L_3(e^{-x}), \quad (9b)$$

where $L_s(z) = \sum_{m=1}^{\infty} \frac{z^m}{m^s}$ is the polylogarithm function. Taking into account the behavior of the positive function J for small [$J(x \ll 1) \approx 6z(3) - 0.5x^2$] and large [$J(x \gg 1) \approx (x^3 + 3x^2 + 6x + 6)e^{-x}$] arguments, Eq. (9a)

establishes that if, for a given temperature T , there exists a frequency interval large enough ($A_n \ll T \ll B_n$), the SPhP thermal conductance per unit width of a nanofilm suspended in air ($\varepsilon_0 = 1$) is quantized and given by

$$\frac{G_0}{a} = 12z(3) \frac{k_B^3 T^2}{ch^2}, \quad (10)$$

where $z(3) = \sum_{m=1}^{\infty} m^{-3} \approx 1.2021$ is the Riemann zeta function. The maximum contribution of SPhPs to the nanofilm thermal conductance is thus independent of the material properties and determined by universal constants only. G_0 increases with the square of temperature due to the 2D density of states ($D(\omega) \propto \beta_R \propto \omega$) of SPhPs propagating along a nanofilm, as indicated in Eq.(7). This quadratic increase is thus faster than the linear one exhibited by the ballistic thermal conductance of SPhPs [21], phonons [2, 3, 10], and electrons [9, 29] propagating in a 1D nanowire. The quantization of the SPhP thermal conductance of nanofilms supporting the ballistic propagation of SPhPs is analogous to its phonon and electron counterparts observed for 2D structures at low temperatures ($T < 10$ K), in which the temperature dependence is generally different than T^2 , due to the non-linear dispersion relations [16, 17, 30].

Note that if the temperature rise $\Delta T = T - T_0$ is much smaller than room temperature ($\Delta T \ll T_0$), $T^2 \approx T_0^2 + 2T_0\Delta T$ and hence k_{pol} in Eq. (6) increases linearly with ΔT . This linear increase of the SPhP thermal conductivity is consistent with the one observed for the thinnest (30 nm) SiN nanofilm studied in our previous work [31], for temperatures between 300 and 400 K. However, for higher temperatures or thicker films with a stronger phonon heat transport, the temperature dependence of k_{pol} will be nonlinear and different than that of the measured thermal conductivity [31], because this latter one represents the total (phonon+polariton) thermal conductivity.

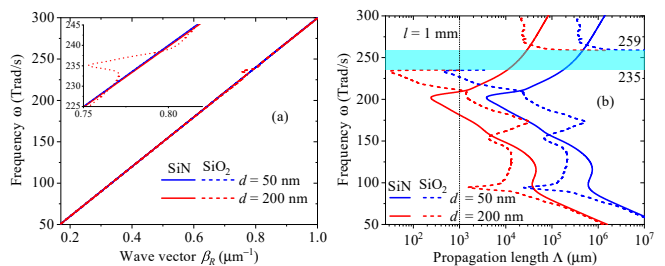


FIG. 2: Frequency spectra of the (a) wave vector and (b) propagation length of SPhPs propagating along nanofilms of SiN and SiO₂ of two thicknesses.

Calculations were done with the SPhP dispersion relation[20, 24] for thin films suspended in air and the material permittivities reported in the literature [28]. The light blue region stands for the band gap of SiO₂.

To analyze the frequency spectrum supporting the

propagation of SPhPs, the frequency dependence of the wave vector (β_R) and propagation length (Λ) of SPhPs propagating along the surfaces of nanofilms of SiN and SiO₂ suspended in air are shown in Figs. 2(a) and 2(b), respectively. In both of these typical polar materials, β_R increases linearly with frequency through values practically equal to those of the light line (ω/c), specially for the 50 nm-thick films. The slight deviations from this photon-like behavior characterized by a group velocity close to that of light in vacuum ($V \rightarrow c$), show up for the 200 nm-thick films due to the increased energy absorption by the material. The relatively weak absorption of thinner films enables SPhPs to propagate distances as long as 1 m, as shown in Fig. 2(b). The peaks (dips) of Λ are related to the minima (maxima) of the energy absorption driven by the imaginary part of the film permittivity [20, 28]. These Λ values are comparable to the experimental ones reported for SiO₂ [32] and longer than those measured for hBN [33]. Considering that as the film thickness d decreases, the energy absorption reduces and the coupling of SPhPs propagating along both surfaces of the thin film strengthens, the SPhP propagation length scales as $\Lambda \propto \text{Im}(\varepsilon)^{-1}d^{-2}$ [20, 23], where $\text{Im}(\varepsilon)$ is the imaginary part of the film permittivity that drives the energy absorption by the material from the electromagnetic field. This fact along with the photon-like nature of SPhPs ($\beta_R \approx \omega/c$) explains their relatively long propagation length compared to that of phonons and electrons. Note that the SiN nanofilms support the propagation of SPhPs for all displayed frequencies, while the SiO₂ ones have a forbidden frequency band (235; 259)Trad/s, in which SPhPs do not propagate [28]. In addition, the fact that $\Lambda \gg l = 1$ mm, for the 50 nm-thick films, indicates that the SPhPs propagate ballistically along them, which is a condition to reach the 2D quantum of thermal conductance in Eq. (10).

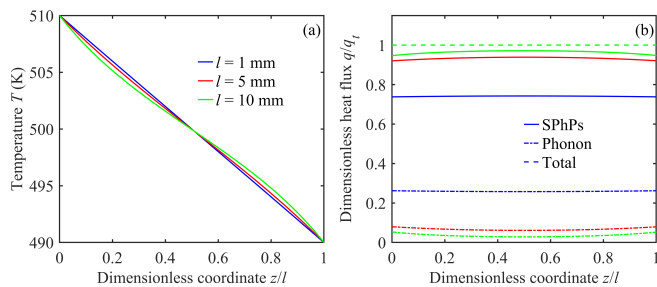


FIG. 3: Numerical results for the (a) temperature profile and (b) heat fluxes in a 50 nm-thick SiN film at 500 K. Calculations were done for three film lengths of practical interest.

Figures 3(a) and 3(b) show the respective temperature and heat flux profiles predicted by the numerical solution of the BTE for the simultaneous propagation of SPhPs and phonon in a 50 nm-thick SiN film with an average

temperature of 500 K. For the shortest film, T approaches to the linear profile predicted by the Fourier's heat diffusion equation without heat source, as a result of the ballistic propagation of SPhPs ($\Lambda \gg l = 1$ mm) with very weak absorption and negligible energy exchange with phonons. The heat generation rate by SPhPs is thus small and their contribution to the heat flux is pretty much independent of position, as shown in Fig. 3(b). For longer films with a length ($l = 5$ and 10 mm) comparable to the SPhP propagation length, on the other hand, the quasi-ballistic propagation of SPhPs fosters their energy exchange with phonons, which generates a nonlinear temperature profile similar to that predicted by the heat diffusion equation with a heat sink for $z/l \leq 0.5$ and a heat source for $z/l \geq 0.5$, as seen in Fig. 3(a). The apparent heat sink and heat source terms in the nanofilm arise from the predominant emission and adsorption of SPhPs near its hot and cold sides, respectively. Therefore, the SPhP heat flux increases with position until $z/l = 0.5$ and decreases afterwards, while the phonon counterpart shows the opposite trend, as established by the principle of energy conservation (Eq. (1)). The increase of the SPhP heat flux with the nanofilm length provides a pathway to enhance the in-plane heat transport along polar films by means of the combined dynamics of SPhPs and phonons, which has never been reported, to the best of our knowledge. Furthermore, as the nonlinearity of the temperature profile represents the fingerprints of SPhPs, its experimental observation can give a conclusive and easy way to detect the SPhP heat transport. For instance, for the 10 mm-long SiN nanofilm shown in Fig. 3(a), the largest temperature deviation from the linear profile is about 1 K, which is measurable by the current state-of-the-art infrared thermometers.

The SPhP thermal conductance per unit width G/a of SiN and SiO₂ nanofilms is comparatively shown in Fig. 4, as a function of the film thickness. As a result of the predominance of surface effects, thinner films exhibit a higher G/a , whose values increase with temperature. The analytical (solid lines) and numerical (dashed lines) predictions exhibit a very good agreement for both materials and three temperatures, which confirms the high accuracy of Eq. (6) for quantifying the thermal conductance of SPhPs with ballistic propagation (Fig. 2(b)). More importantly, the upper bounds of G/a , in the ballistic regime ($d < 50$ nm), are well confirmed by the analytical and numerical approaches and their values for the SiN films coincide with the quantum of thermal conductance in Eq. (10), for the three considered temperatures. This is due to the fact that SiN is able to support the propagation of SPhPs in a single branch (Fig. 2) spanning from a very low frequency ($A_1 \rightarrow 0$) to a high one ($\omega_n^{\max} > 300$ Trad/s ($B_1 > 2283$ K)). This fact ensures the SPhP energy transport over the full frequency spectrum relevant for temperatures comparable to or smaller than room temperature. By contrast, the frequency band gap

of SiO₂ (Fig. 2(b)) reduces this spectrum and therefore the ballistic SPhP thermal conductance to values slightly smaller than the quantum of thermal conductance, as shown in Fig. 4. This quantization can thus only be achieved in nanofilms without frequency band gaps for the propagation of SPhPs and could be observed by using an experimental setup sensitive to the SPhPs energy transport [34].

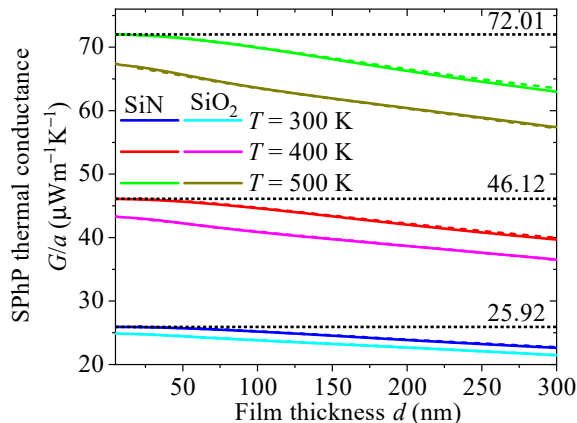


FIG. 4: SPhP thermal conductance per unit width of 1 mm-long nanofilms of SiN and SiO₂, as a function of their thickness. The solid and dashed lines represent the respective analytical (Eq. (6)) and numerical [26] predictions, while the dotted ones stand for the quantum of thermal conductance predicted by Eq. (10). Calculations were done for three temperatures.

In summary, the existence of the universal quantum of thermal conductance $12z(3)k_B^3T^2/ch^2$ per unit width of a thin enough polar nanofilm supporting the propagation of SPhPs along its surfaces has been demonstrated for temperatures comparable to or lower than room temperature. This quantization arises from the ballistic behavior of SPhPs and represents the upper bound for their heat transport, which in SiN, is reached for a film thinner than 50 nm. The obtained results for the SPhP thermal conductance and SPhP thermal conductivity as well as for the temperature and heat flux profiles driven by the combined dynamics of phonons and SPhPs, thus quantify the potential of the latter heat carriers to improve the thermal performance of nanomaterials and facilitate its observation, as these four parameters are measurable.

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