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# Integrated Laycan and Berth Allocation Problem with conveyor routing constraints and preventive maintenance activities in bulk ports

Hamza Bouzekri<sup>a,b</sup>, Gülgün Alpan<sup>a,b</sup> and Vincent Giard<sup>a,c\*</sup>

<sup>a</sup> EMINES - School of Industrial Management, Mohammed VI Polytechnic University, Ben Guerir, Morocco

<sup>b</sup> Univ. Grenoble Alpes, CNRS, Grenoble INP, G-SCOP, Grenoble, France

<sup>c</sup> Université Paris-Dauphine, Université PSL, CNRS, LAMSADE, Paris, France

## Integrated Laycan and Berth Allocation Problem with conveyor routing constraints and preventive maintenance activities in bulk ports

In this paper, we study the integrated Laycan and Berth Allocation Problem (LBAP) in the context of bulk ports, which considers two problems in an integrated way: the tactical Laycan Allocation Problem and the dynamic hybrid case of the operational Berth Allocation Problem. To make the LBAP closer to reality, we consider tidal bulk ports with conveyor routing constraints between storage hangars and berthing positions, preventive maintenance activities, multiple quays with different water depths and fixed heterogeneous bulk-handling cranes, navigation channel restrictions, vessels with multiple cargo types, charter party clauses and non-working periods. The aim of the proposed integer programming model is to define an efficient schedule for berthing chartered vessels and optimal laycans to new vessels to charter. The model is formulated with predicates that guarantee maximum flexibility in the implementation and greatly improve the computational performance. Finally, the model is tested and validated through a relevant case study inspired by the operations of OCP Group at the bulk port of Jorf Lasfar in Morocco. The results show that the model can be used to solve to optimality instances with up to 60 vessels for a 4-week planning horizon in very reasonable computational time using commercial software.

Keywords: laycan allocation; berth allocation; tidal bulk ports; conveyors; preventive maintenance; integer programming

#### 1. Introduction:

With an estimated 80 per cent of the volume of world merchandise trade by sea, international shipping and ports provide crucial linkages in global supply chains and are essential to enable all countries to access global markets UNCTAD (2019). Although containerization has revolutionized the shipping industry, bulk cargoes are still the fundamental and enduring trades that support the dynamism of maritime transport. Five cargo types can be distinguished: container cargo, liquid bulk, dry bulk, break-bulk cargo, and ro-ro. In container terminals, all cargo is packed into standard containers, and thus there is no need for any specialized equipment to handle any particular type of cargo. In

contrast, cargo is not packaged in bulk ports and a wide variety of loading/unloading equipment and means of transport is used depending on the vessel requirements and cargo properties. For example, dry bulk goods are handled using fixed bulk-handling cranes and are transferred using conveyors between storage hangars and bulkers considering conveyor routing constraints, while liquid bulk goods need pipelines to be handled and transferred between storage tanks and tankers. On the other hand, containers are handled using mobile cranes and are transferred between storage tanks and tankers.

Despite their importance in maritime logistics, bulk ports have received less attention than container terminals in the scientific literature. This research considers tidal bulk ports in which dry bulk goods are transferred from storage hangars to berthing positions using conveyors. Our approach integrates two important decision problems in port management: the tactical Laycan Allocation Problem (LAP) and the operational Berth Allocation Problem (BAP). The LAP assigns berthing time windows to new vessels to charter within a medium-term planning horizon (three to four weeks), considering the availability of cargo and port resources (berthing positions, handling equipment, etc.). Hence, the LAP has a clear interaction with one of the most important operational problems in the seaside area of ports: the BAP. The latter assigns berthing positions and times to every vessel projected to be served within a short-term planning horizon (one to two weeks) such that a given objective function is optimized. To easily manage the integration between these two problems that have different decision levels, we consider a modular decision time-interval inside the planning horizon. This approach was first proposed in Bouzekri et al. (2021) to integrate the LAP with the integrated Berth Allocation and Quay Crane Assignment Problem (BACAP) in the context of container terminals. To the best of our knowledge, the current paper is the first research to integrate the LAP and the BAP in the context of bulk ports, considering conveyor routing constraints with preventive maintenance activities between storage hangars and berthing positions.

This study also considers all common constraints of port management listed below and never considered altogether in bulk ports modeling. These constraints relate to 1) the multiplicity of quays, 2) navigation channel restrictions, 3) the variation of water depth, 4) vessel tide-dependency, 5) the productivity of loading equipment, 6) charter party clauses and 7) non-working periods. These constraints are quite common in real port operations. Including them into the model increases the application potential of the resulting solutions.

Finally, we use predicates in the proposed integer linear programming model to define the feasibility zone of decision variables. This approach permits reducing the number of variables and constraints and hence makes it possible to solve real size problems using commercial software. This type of formulation has successfully been used in Bouzekri et al. (2021). The current paper confirms its efficiency.

The remainder of this paper is organized as follows. In Section 2, we present a literature review of the BAP and the LAP in the context of bulk ports. Section 3 is dedicated to the description of the LBAP, while Section 4 is dedicated to its mathematical formulation. In Section 5, we present a case study with an illustrative example, then we discuss the results. Finally, in Section 6, we draw some conclusions and indicate future research directions.

#### 2. Literature review:

In this section, we review the academic literature on the BAP and the LAP in the context of bulk ports.

#### 2.1.BAP Literature:

The BAP in bulk ports has received little attention in Operations Research literature compared to container terminals until recently. A list of papers that propose new models for the BAP in the context of bulk ports, as an individual problem or using an integrated approach, are described below.

The berth layout can be either discrete, continuous, or hybrid. Barros et al. (2011) propose an integer linear programming model for the discrete BAP considering homogeneous berthing positions with tide and stock level constraints, prioritizing vessels related to the most critical mineral stock level. The authors then propose a Simulated Annealing-based algorithm as a valid alternative to the commercial solver to find good and fast solutions for hard instances. Ribeiro et al. (2016) also solve the discrete BAP by proposing a mixed-integer linear programming model considering maintenance activities. The authors model each maintenance activity as a dummy vessel which must be handled at a precise time by a specific berthing position, which means that this berthing position cannot receive vessels during that time. They then develop an adaptive large neighborhood search heuristic that finds good solutions within low computational times on all instances.

Ernst et al. (2017) solve the continuous BAP with tidal constraints that limit the departure of fully loaded vessels from dry bulk terminals, using a commercial solver. The authors propose two new mixed-integer linear programming models, and then they provide several valid inequalities for both models, which improve both their solution quality and run time. To solve efficiently medium to large-sized instances of Ernst et al. (2017), Cheimanoff et al. (2020) develop a metaheuristic approach based on the Reduced Variable Neighborhood Search. The authors also develop a machine learning algorithm to tune the metaheuristic's hyper parameters.

Umang et al. (2013) study the hybrid BAP by proposing two exact methods based on mixed-integer programming and generalized set partitioning, and a heuristic method based on squeaky wheel optimization. The authors consider the fixed equipment facilities, such as conveyors and pipelines, which are installed at only certain sections along the quay, the cargo type on the vessel and its draft. They also consider the time taken to transfer cargo between its location on the yard and the berthing position of the vessel. de León et al. (2017) propose a Machine Learning-based system to select the best algorithm for solving the BAP model proposed by Umang et al. (2013) in each particular case. The latter depends on factors such as the percentage of vessels that need specialized handling equipment, and the congestion level, which is influenced by the distribution of the estimated time of arrival of vessels and their workload.

Most authors consider dynamic vessel arrivals, while Tang et al. (2016) consider static vessel arrivals. The authors implement a multi-phase particle swarm optimization algorithm to minimize the total service time of vessels or their makespan.

Since the operational problems observed in port terminals are often interrelated, some authors study the BAP using an integrated approach. Indeed, Robenek et al. (2014) extend the work of Umang et al. (2013) by integrating berth allocation and yard assignment problems. The authors propose an exact solution algorithm based on a branch and price framework and a metaheuristic approach based on critical-shaking neighborhood to solve this integrated problem. Al-Hammadi and Diabat (2017) apply the model proposed by Robenek et al. (2014) for Mina Zayed Port in Abu Dhabi in order to test different scenarios as a means of sensitivity analysis, with respect to certain factors such as the congestion level, in terms of the relative arrival time of vessels, the unavailability of certain resources and the addition of new resources.

In the same logic of integrating problems, Unsal and Oguz (2019) propose an exact solution procedure for an integrated problem that consists of three operations: berth allocation, reclaimer (a large machine used to recover bulk material from a stockpile) scheduling and stockyard allocation, considering tide and reclaimers non-crossing constraints. The authors develop a novel logic-based Benders decomposition algorithm in which a master problem and a subproblem are modeled using mixed-integer programming and constraint programming, respectively. The subproblem's role is either to find a feasible schedule for reclaimer schedules and yard allocations given mooring and departure times of vessels or to prove that the problem instance is infeasible.

Note that few papers consider tide with navigation channel restrictions such as the maximum number of vessels to pass simultaneously through the navigation channel and the vessels' incapability to pass in opposing directions. These restrictions are considered by Zhen et al. (2017) and Corry and Bierwirth (2019) in the context of container terminals. In the context of bulk ports, Pratap et al. (2017) develop a decision support system to solve the integrated problem of berth and ship unloader allocation, under the condition that the channel allows only one vessel to pass at a time, using metaheuristics. The authors consider two different approaches: either solving the problem sequentially as a two-phase optimization model, berth allocation and ship unloader allocation or integrating the two phases in a single-phase problem. The integrated approach gives a better result than the sequential approach, but the latter is useful for the port authorities to revise their contract with their clients. Liu et al. (2021) propose a mixed-integer linear programming model for integrated planning of berth allocation and vessel sequencing in tidal seaports with one-way navigation channel, which obliges vessels to queue up to enter or leave the port alternately. The authors also develop a tailored adaptive large neighborhood search algorithm to solve the integrated problem within a reasonable time.

Krimi et al. (2019, 2020) study the integrated Berth allocation and Quay Crane Assignment Problem in tidal bulk ports with multiple quays, vessels with multiple cargo types, and unavailability constraints due to preventive maintenance of quay cranes and bad weather conditions. The authors develop a general variable neighborhood searchbased approach to solve instances the commercial solver failed to solve optimally.

We also note that we found no papers that consider the BAP with conveyor routing constraints between storage hangars and berthing positions. Some authors consider conveyor routing constraints in other problems. For example, Menezes et al. (2017) study the production planning and scheduling problem in bulk ports which defines the amount and destination of each product and simultaneously establishes a set of feasible routes from storage subareas to vessels, where there is no conflict regarding equipment allocation. However, the authors consider the berthing positions of vessels as inputs in the problem.

The journal papers cited above are summarized in Table 1, in which the following information is presented.

- Port type: either import or/and export ports.
- Spatial attribute: it concerns the berth layout (either discrete, continuous or hybrid), the number of quays (either a single quay or multiple quays), and it specifies if the BAP considers the draft of berthing positions and the restrictions of the navigation channel and the conveyor system when deciding on a vessel's berthing position.
- Temporal attribute: it describes the arrival process of vessels (either static or dynamic), and it specifies if the BAP considers tide constraints and non-working periods (e.g., non-working days and maintenance activities) when deciding on a vessel's berthing time.

- Handling time attribute: it describes the productivity of handling equipment (either homogeneous or heterogeneous). In the case of homogeneous handling equipment, handling time of vessels is fixed, while it is variable in the case of heterogeneous handling equipment. The attribute also specifies if the BAP considers the distance between berthing positions and storage locations when calculating a vessel's handling time.
- Performance measure attribute: it specifies the optimization criteria used in the objective function (either efficiency or effectiveness). Most models consider minimizing various times or costs.
- Vessel cargo types: it specifies if a vessel carries only a single type or multiple types of cargo.
- Problems integrated with the BAP: it specifies the problems that are integrated with the BAP when the latter is studied using an integrated approach.
- Resolution approach: either exact methods, heuristics, or/and metaheuristics.
- Modeling choices: it specifies if the conditions of the BAP (berthing time and space, draft, tide, navigation channel, non-working periods) are modeled as either constraints or predicates using binary variables.

For detailed reviews of the BAP literature in the context of container terminals, we refer readers to Bierwirth and Meisel (2010, 2015).

#### 2.2.LAP Literature:

While BAP literature is abundant, only two papers were found that deal with the LAP.

Lorenzoni et al. (2006) develop a mathematical model, based on a multi-mode resource-constrained scheduling problem improving the attendance of vessels. The proposed model determines laycans in a way that avoids simultaneous or nearly simultaneous arrivals of vessels competing with the same port resources (berthing positions, handling equipment, etc.), under the first come first served regime of attendance. However, the authors consider only time windows for resources' availability, without considering spatial constraints such as vessel and berth lengths.

Bouzekri et al. (2021) study the integrated Laycan and Berth Allocation and timeinvariant Quay Crane Assignment Problem in tidal ports with multiple quays. Then, they extend the integrated problem to the Specific Quay Crane Assignment, which includes the assignment of a set of specific quay cranes to each vessel. This research is more suitable for container terminals since it does not specify the cargo type, which is an important point in bulk ports.

As a conclusion to this section, we highlight that in this paper, we propose a new integer linear programming model for a new integrated problem: the LBAP in the context of bulk ports. Moreover, we consider numerous conditions related to port management in the definition of the LBAP, which reduces the gap between the abstract representation of the studied problem and its applicability in real situations. Indeed, our model considers tidal bulk ports that have conveyor routing constraints between storage hangars and berthing positions with preventive maintenance activities, a navigation channel, multiple quays with different water depths and heterogeneous loading equipment, vessels with multiple cargo types, charter party clauses and non-working periods.

Table 1. BAP literature in the context of bulk ports.

	Po ty			Sp	oatia	ıl attı	ibut	e		Ter	npor	al a	ttrib	ute		lling ti tribute		m	formance neasure tribute	Ve: cargo		Pro	blen with	ns int the	tegra BAP	ited	Resol appr	lution oach	Mo	deli	ng c	hoice	s
			num ofqu			erth vout				ves arri				s	hand equip	lling ment							ment	ling				ics				0	2
Authors	import	export	ouou	multi	discrete	continuous hvhrid	draft	navigation channel	conveyor system	static	dynamic	tide	maintenance	non-working periods	homogeneous	heterogeneous	distance	efficiency	effectiveness	mono	multi	laycan allocation	quay equipment assignment	yard equipment scheduling	yard assignment	vessel sequencing	exact methods	heuristics/metaheuristics	berthing time	berthing space	draft	tide non-working neriods	10
Barros et al. (2011)	x	x	х		x						х	х			х			V		х								х	С	С		С	
Umang et al. (2013)		x	х			Х	X				х				Х		х		S	х							х	х	С	С	C		
Robenek et al. (2014)	x	x	х			х	x				х				х		х		S	х					х		х	х	С	С	С		
Ribeiro et al. (2016)	x	x	х		x						х		х			х		V		х								х	С	С		C	4 7
Tang et al. (2016)	х	x	х		x					х						х			S, M	х								х	С	С			
Pratap et al. (2017)	х		Х		х			х			х				Х				W, H, R	Х			Х					х	С	С			_
Al-Hammadi and Diabat (2017)	х	x	х			x	x				х				х		х		S	Х					х		х		С	С	С		
Ernst et al. (2017)		x	Х			х					х	х			Х				D	Х							Х		С	С		С	_
Unsal and Oguz (2019)		x	х		x						х	х			х		х		D	Х				x	х		х		С	С		С	
Krimi et al. (2019, 2020)		x		х		х					х	x	х			х			Т		x		х					х	С	С		CC	-
Cheimanoff et al. (2020)		x	х			х					х	х			х				D	х								х	С	С		С	
Liu et al. (2021)	х	x	х		x		x	x			х	x			х				S	х						х		х	С	С	Р	С	
Our paper		x		х		x	x	x	х		х	x	x	х		х		V	D		x	x					х		Р	Р	Р	P P	

Performance measure attribute: D: Departure times; T: Tardiness; W: Waiting times; H: Handling times; S: Total service times; M: Makespan; R: Priority deviation; V: Demurrage vs despatch Modelling choices: P: Predicate; C: Constraint

#### 3. Problem description:

In this section, we present all the constraints considered in the problem modelling. These constraints include both general port constraints and specific bulk port constraints. Then we present some possible optimization criteria related either to efficiency or to effectiveness.

#### 3.1. General port constraints:

We consider a tidal port with multiple quays. Each quay has as hybrid layout where large vessels may occupy more than one berthing position, however, small vessels cannot share a berthing position. In Figure 1, the vessel 3 occupies the berthing position 5 that is the union of the berthing positions 3 and 4, however, the vessels 2 and 2' cannot share the berthing position 2.

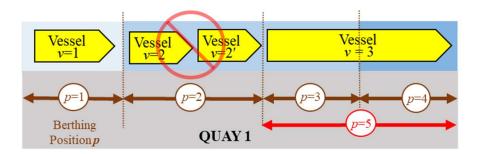


Figure 1. Hybrid berth layout.

Each berthing position is characterized by a length and a water depth. All the berthing positions of a quay can have the same water depth, or the water depth increases seaward by berthing positions, as in Figure 2. The indexation of berthing positions is independent of the quays.

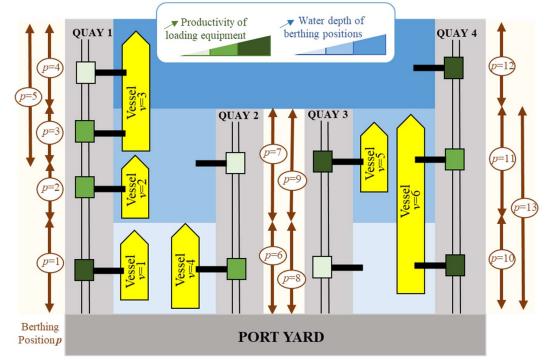


Figure 2. Example of a bulk port.

We consider three types of vessels:

- Already berthed vessels: these vessels have residual handling time and a predetermined berthing time and position.
- Chartered vessels: the charter party of these vessels is already signed. Consequently, their expected arrival time is fixed. The decisions remaining to take are when and where to berth.
- New vessels to charter: the charter party of these vessels is under negotiation. Consequently, their laycan is not yet fixed. The decisions to take are the first layday and where to berth.

We assume dynamic vessel arrivals which means that expected arrival times are given for chartered vessels. Each vessel is characterized by a length and a draft. A maximum waiting time in the harbor per vessel is also introduced to circumvent solutions with very high waiting times. The port manager can fix this parameter based on what he judges acceptable. Besides this practical relevance, it also plays an interesting role in the computational performance by limiting the search space. We also consider the technical constraints of vessels that prohibit their berthing at some berthing positions or oblige them to berth at a specific berthing position.

In tidal ports, the use of the navigation channel is impacted by the tide cycle. We assume that large loaded vessels that have deep drafts are not able to pass through the navigation channel, while leaving the port during low tides, and thus have to wait for high tide cycles where the sea level is superior to their drafts (Figure 3). The detailed calculation of tide parameters is shown in the file <u>Tide.xlsx</u>. Moreover, a maximum number of vessels must not be exceeded in a given period of time while passing simultaneously through the navigation channel.

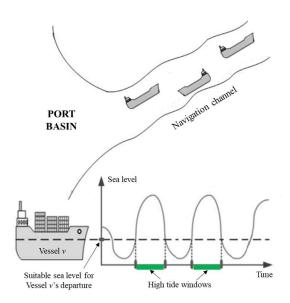


Figure 3. Navigation channel restrictions.

We also consider non-working periods, which can either be included or excluded in the counting of the laytime. For example, in SSHEX (Saturdays/Sundays/Holidays Excluded), the time lost in port on Saturdays, Sundays and Holidays does not count as laytime (from 5 pm on Friday until 8 am on Monday, and on holidays from 5 pm of the day preceding a holiday until 8 am of the next working day), while in SSHINC (Saturdays/Sundays/Holidays Included), no exception periods are in effect and the laytime will count seven days a week as well as during holidays.

#### 3.2. Specific bulk port constraints:

Each berthing position in the port is characterized by a fixed bulk-handling crane also characterized by a productivity (see Figure 2). Berthing positions are linked to storage hangars by a conveyor system, which can be divided into sections composed of identical parallel conveyors. The number of the latter differs from the number of conveyors linked directly before each section (e.g., in Figure 4, the section 1 is linked upstream to four storage hangars by four conveyors but has only three identical parallel conveyors).

Berthing positions are linked to storage hangars by a conveyor system, as shown in Figure 4. The conveyor system is a set of identical parallel conveyors (represented by horizontal bars) connected together by switches (represented by dots) and identical feeding/transfer conveyors (represented by vertical bars). The black box represents a flexible transfer system that connects the upstream conveyors linked to the hangars to the downstream conveyors linked to each berthing position on the quays. A route is a collection of interconnected horizontal and vertical conveyors that links a hangar to a berthing position. The number of possible routes is quite high (e.g., more than 1.3 million combinations in the example of Figure 4). It must be noted that all potential routes cannot be operational at the same time since a conveyor cannot transport two different bulk products at a time. This particularity is used to circumvent the combinatorial nature of the problem by defining compatible routes Menezes et al. (2017). Two routes are said to be compatible if and only if they do not share a conveyor (or a switch). This reduces considerably the number of routes to consider in assigning conveyors. However, it is a delicate task to list all compatible routes without errors.

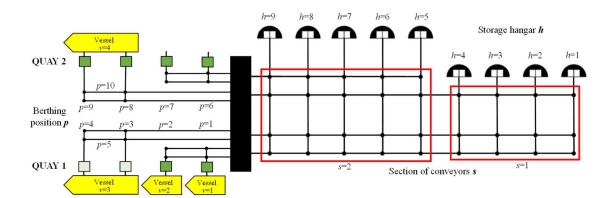


Figure 4. Sections of the port conveyor system.

Therefore, in this paper we adapt another approach. Instead of considering a conveyor assignment problem, we consider conveyor capacity allocation. To this end, we divide the port conveyor system into sections (for example, two sections, s=1 and 2, in Figure 4). We define two parameters: the first one gives the number of identical parallel conveyors in each section that expresses the maximum number of bulk products that can be transported simultaneously in the given section (e.g. in Figure 4, maximum 3 in section 1 and 4 in section 2). The second one is a Boolean parameter with three indices (storage hangars, berthing positions and sections) that specifies which section is needed to transfer a product from a given hangar to a given berthing position (e.g., in Figure 4, the conveyors of any route between berthing position 1 and storage hangar 3 belong to sections 1 and 2). This allows replacing a list of compatible routes that is hard to build free of errors, by a simple constraint that limits the number of identical parallel conveyors to use simultaneously in a section, at a given time period. The solution to our model will provide which bulk product to be transported from which hangar to which berthing position at a time, respecting this capacity constraint. Given this solution, the allocation of conveyors and the maintenance of the model in case of infrastructural changes in the conveyor system can be done easily a posteriori.

We also consider scheduled preventive maintenance activities to be performed at the conveyors and berthing positions over a period of time or at a fixed date. Maintenance activities at conveyors in the same section can overlap with each other, while they are disjoint at a berthing position. Some berthing positions can also be unavailable due to bad weather. We note that the conveyor system is the bottleneck of the port since it limits the number of vessels that can be handled simultaneously (e.g., in Figure 4, only four out of ten vessels can be handled simultaneously).

Handling times of vessels depend on loading equipment's productivity in the berthing positions, and a vessel can be served by more than one loading equipment depending on its length. Each vessel is also characterized by a number of cargo types with different amounts to load on it. These amounts of cargo types can be expressed as batches. Each batch is characterized by an availability date and a storage hangar. It has to be noted that the batches to load on a single vessel can be stored in the same hangar or different hangars. We assume that only one batch at most can leave a storage hangar at a time and that two (or more) batches cannot be loaded at the same time on a vessel, but they can be loaded in any order without downtime. This assumption favors the waiting of vessels in the harbor until their continuous loading is guaranteed to minimize their berthing time in the port.

In Figure 5, the vessel 3 is a chartered vessel that is berthed in berthing position 5. The vessel is represented by a large rectangle placed in the area of berthing position 5 starting from its berthing time with a length equal to its handling time. Small rectangles inside the big rectangle represent the batches to load on the vessel according to a loading sequence chosen by the optimal solution. Each small rectangle starts from the loading start time of the batch with a length equal to its handling time. Vertical bars represent high tide windows.

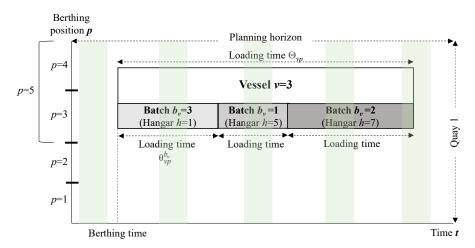


Figure 5. Representation of a chartered vessel and the batches to load on it.

#### 3.3. Optimization criteria:

#### 3.3.1. Efficiency criteria:

The LAP defines some major contractual terms that are found in a maritime contract between a *shipowner* and a *charterer* for the hire of a vessel (called *charter party*). Some of these contractual terms are the following: *laycan, laydays, laytime, demurrage,* and *despatch*. All these chartering terms are shown in Figure 6 and will be used for expressing the objective function and some decision variables in the mathematical model proposed in this paper.

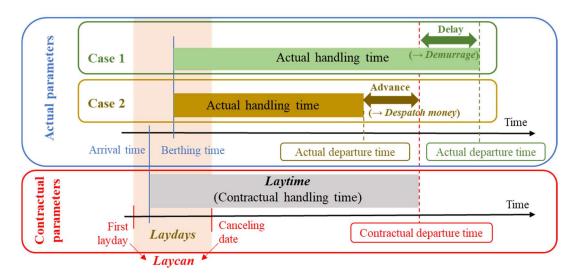


Figure 6. Contractual vs actual parameters of vessels (adapted from Bouzekri et al. (2021)).

One of the efficiency criteria that could be applied is to find an efficient schedule for berthing chartered vessels that maximizes the sum of the difference between the despatch money and the demurrage charges for each vessel (i.e., minimize the demurrage charges and maximize the despatch money) while proposing optimal laycans for new vessels to charter considering all the characteristics and constraints described above.

#### 3.3.2. Effectiveness criteria:

We note that other objective functions based on physical criteria could be considered such as the minimization of the sum of expected vessel departure times or vessel stay times. These sums can be weighted to consider vessels priority. This does not require any change in the model, except in the objective function's formula.

#### 4. Model formulation:

#### 4.1.Notation:

The sets are represented by calligraphic letters, the parameters by Greek letters or capital Latin letters, the variables by italic letters, and the indices by italic lowercase letters. The latter are always written as subscripts, except for the indices  $b_v$ ,  $m_p$  and  $m_s$ , that are related to the indices v, p and s, which are always written as superscripts.

Index	Description
t	Index of time periods $\mathcal{T} = \{1,, T\}$ .
v	Index of vessels $\mathscr{V} = \{1,, V\}$ with $\mathscr{V} = \mathscr{V}_1 \cup \mathscr{V}_2 \cup \mathscr{V}_3$ and $V = V_1 + V_2 + V_3$ ,
	where:
	• $\mathscr{V}_1 = \{1,, V_1\}$ is the set of already berthed vessels.
	• $\mathscr{V}_2 = \{V_1 + 1,, V_1 + V_2\}$ is the set of chartered vessels.
	• $\mathscr{V}_3 = \{V_1 + V_2 + 1,, V\}$ is the set of new vessels to charter.
$b_{v}$	Index of batches to load on vessel $v \mathscr{B}_v = \{1,, B_v\}$ .

р	Index of berthing positions $\mathscr{P} = \{1,, P\}$ .
$m_p$	Index of maintenance activities to be performed at berthing position $p$
	$\mathcal{M}_p = \left\{1, \dots, \mathbf{M}_p\right\}.$
S	Index of sections composed of identical parallel conveyors $\mathcal{S} = \{1,, S\}$ .
$m_s$	Index of maintenance activities to be performed at a conveyor in section $s$
	$\mathcal{M}_{s} = \left\{1, \dots, M_{s}\right\}.$
h	Index of storage hangars $\mathcal{H} = \{1,, H\}$ .
Parameter	Description
Navigation c	hannel
G	Maximum number of vessels allowed to pass simultaneously through the
	navigation channel.
Time decision	
K <sub>t</sub>	Boolean parameter that equals 1 if a decision of berthing vessels can be taken
	during time period $t$ , 0 otherwise (see Section 4.3).
<u>Tide cycle</u>	
O <sub>t</sub>	Boolean parameter that equals 1 if time period $t$ is within a high tide cycle, 0 otherwise.
Berthing pos	<u>itions</u>
Q <sub>p</sub>	Length of berthing position <i>p</i> .
$W_p$	Minimum water depth of berthing position <i>p</i> .
$\mathbf{E}_{p}^{p'}$	Boolean parameter that equals 1 if berthing positions $p$ and $p'$ share a berthing
P	position, 0 otherwise (e.g., in Figure 1, berthing positions 3 and 5 share
	berthing position 3). When $p = p'$ , $E_p^{p'} = 1$ .
<u>Sections</u>	
U <sub>s</sub>	Number of identical parallel conveyors in section <i>s</i> .
F <sub>sh</sub>	Boolean parameter that equals 1 if one of the conveyors belonging to the route
	that links a berthing position to storage hangar $h$ belongs to section $s$ , 0 otherwise.
<u>Preventive m</u>	aintenance activities
$\mathbb{R}_p^{m_p}$	Duration of maintenance $m_p$ to be performed at berthing position $p$ .

$\underline{\mathbf{R}}_{p}^{m_{p}}$	Earliest time to perform maintenance $m_p$ at berthing position $p$ .
$\overline{R}_p^{m_p}$	Latest time to perform maintenance $m_p$ at berthing position $p$ .
$\mathbf{R}_{s}^{m_{s}}$	Duration of maintenance $m_s$ to be performed at a conveyor in section s.
$\underline{\mathbf{R}}_{s}^{m_{s}}$	Earliest time to perform maintenance $m_s$ at a conveyor in section s.
$\overline{R}_{s}^{m_{s}}$	Latest time to perform maintenance $m_s$ at a conveyor in section s.
Vessels	
A <sub>v</sub>	Expected arrival time of chartered vessel $v$ and earliest time a new vessel to charter $v$ can arrive to the port.
I <sub>v</sub>	Maximum waiting time in the harbor of vessel v.
$\lambda_{v}$	Length of vessel <i>v</i> .
D <sub>v</sub>	Draft of vessel v when it is fully loaded.
ω <sub>v</sub>	Boolean parameter that equals 1 if vessel $v$ is tide-dependent, 0 otherwise.
$\gamma_{\nu}$	Boolean parameter that equals 1 if the handling of vessel $v$ is restricted to working periods, 0 otherwise.
$L_v$	Laydays of vessel v.
$J_{v}$	Contractual handling time of vessel v.
$\delta_{v}$	Contractual finishing time of vessel v, $\delta_v = A_v + J_v - 1, \forall v \in \mathscr{V}$ .
$\eta_{\nu}$	Contractual demurrage by hour of vessel v. $\eta_v = 0, \forall v \in \mathscr{V}_1$ and
	$\eta_{\nu} = 1, \forall \nu \in \mathscr{V}_{3}.$
$\beta_{v}$	Contractual despatch by hour of vessel <i>v</i> . $\beta_v = 0, \forall v \in \mathscr{V}_1$ and $\beta_v = 1, \forall v \in \mathscr{V}_3$ .
N <sub>vp</sub>	1 if vessel $v$ can berth at berthing position $p$ , 0 otherwise.
<u>Batches</u>	
$\mathrm{H}_{\mathcal{V}}^{b_{\mathcal{V}}}$	Storage hangar of batch $b_v$ to load on vessel v.
$C_v^{b_v}$	Date of availability of batch $b_v$ to load on vessel v.
$ heta_{ up}^{b_{ u}}$	Loading time of batch $b_v$ on vessel v when the latter is berthed at berthing
	position <i>p</i> . $\theta_{vp}^{b_v}$ = tonnage of batch $b_v$ / productivity of berthing position <i>p</i> .

$$\begin{split} \Theta_{vp} & \text{Loading time of vessel } v \text{ when the latter is berthed at berthing position } p, \\ & \text{which equals the sum of loading times of all the batches to load on this vessel,} \\ & \text{in any order without downtime: } \Theta_{vp} = \sum_{b_v \in \mathscr{R}_v} \Theta_{vp}^{b_v}, \forall v \in \mathscr{V}, \forall p \in \mathscr{P}. \end{split}$$

#### Time framework

$\Psi_{vt}$	Boolean parameter that equals 1 if the handling of vessel $v$ should not be carried out during time period $t$ , 0 otherwise (see Section 4.2).
$\Gamma_{vt}$	Relative period of the absolute time period $t$ of vessel $v$ considering non- working periods (see Section 4.2).
Υ <sub>vt</sub>	Absolute period of the relative time period $t$ of vessel $v$ considering non-
	working periods (see Section 4.2).
Decision	Description
variable	
x <sub>vpt</sub>	1 if vessel $v$ starts berthing at berthing position $p$ in time period $t$ , 0 otherwise.
$y_{vpth}^{b_v}$	1 if batch $b_v$ stored in hangar h starts loading on vessel v at berthing position
·F	p in time period $t$ , 0 otherwise.
$z_{pt}^{m_p}$	1 if maintenance $m_p$ starts performing at berthing position $p$ in time period $t$ ,
r ·	0 otherwise.
$z_{st}^{m_s}$	1 if maintenance $m_s$ starts performing at a conveyor in section s in time period
	t, 0 otherwise.
<i>u<sub>v</sub></i>	Delay of vessel $v$ , which is the number of time periods exceeding its laytime,
	$u_v \in \mathbb{Z}^+$ (since the planning horizon is divided into equal-sized time periods).
W <sub>V</sub>	Advance of vessel v, which is the number of time periods saved in its laytime,
	$w_v \in \mathbb{Z}^+.$

Intermediary	Description
variable	
$\mu_v, \tau_v^{b_v}$	Berthing position of vessel v in the decision variables $x_{vpt}$ and $y_{vpth}^{b_v}$
	respectively.
$\mathcal{E}_{V}$	Berthing time of vessel <i>v</i> .
$\pi_v$	Finishing time of vessel v.
$ ho_v^{b_v}$	Loading start time of batch $b_v$ .

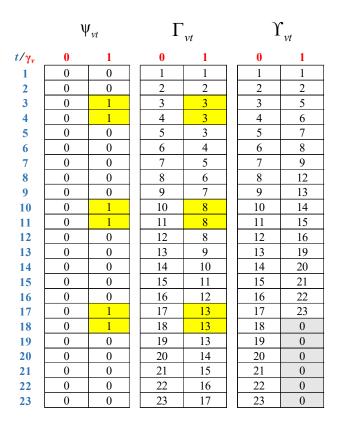
#### 4.2. Representation of time:

Port operations might be unavailable at some periods for some vessels (e.g. non-working days). If such periods coincide with the berthing period of the related vessel, they must be considered to estimate the ending time of berthing for this vessel. This requires adjusting index t for this vessel in the mathematical model. We use the approach proposed by Bouzekri et al. (2021) to this end.

We define four parameters;  $\gamma_v$  to indicate if the handling of vessel v is restricted to some working periods  $(\gamma_v = 1)$  or not  $(\gamma_v = 0)$ . The second one is,  $\psi_{vt}$ , which is used to indicate the non-working periods for the vessels for which  $\gamma_v = 1$ .  $\psi_{vt}$  is equal to 1 in this case, and will be equal to zero for all other situations. The third parameter  $\Gamma_{vt}$  is a relative time scale that keeps track of the non-working periods and accounts for them in advancing time. It is written follows as when  $\gamma_{v} = 1$ :  $\Gamma_{vt|\psi_{vt}=0} = t - \sum_{t'=1}^{t'=t} \psi_{vt'}, \forall t \in \mathcal{T}, \forall v \in \mathcal{V} \text{ and } \Gamma_{vt|\psi_{vt}=1} = \Gamma_{vt'}, \forall t \in \mathcal{T}, \forall v \in \mathcal{V}, \text{ where}$ t' is the first working period after t, as it is the first  $t' > t | \psi_{vt'} = 0$ . Obviously,  $\Gamma_{vt} = t, \forall t \in \mathcal{T}, \forall v \in \mathcal{V}$ , when  $\gamma_v = 0$ . Finally, the fourth parameter  $\Upsilon_{vt}$  records the calendar time t for vessel v.

An example of these parameters is shown in Table 2, where each time period is one hour long and non-working periods last two hours. A realistic assignment of two day-long non-working periods is provided in the file <u>Time.xlsx</u>.

Table 2. Calculation of non-working periods parameters.



To consider non-working periods in the calculation of the contractual finishing time of vessel v,  $\delta_v = A_v + J_v - 1$  becomes  $\delta_v = \Upsilon_{v(\Gamma_{vA_v} + J_v - 1)}$ . Indeed,  $\Gamma_{vA_v}$  gives the relative period of the absolute expected arrival time of vessel v considering non-working periods, then  $\Upsilon_{v(\Gamma_{vA_v} + J_v - 1)}$  gives the absolute period of the relative contractual finishing time of vessel v also considering non-working periods. If vessel v is not restricted to working periods,  $\Upsilon_{v(\Gamma_{vA_v} + J_v - 1)} = A_v + J_v - 1$ , therefore  $\delta_v = \Upsilon_{v(\Gamma_{vA_v} + J_v - 1)}$  is used in both cases.

#### 4.3. Decision time-interval:

To reduce the computational complexity and consider the increasing uncertainty of inputs as the length of planning horizon increases, we follow the approach proposed by Bouzekri et al. (2021) which modulates decision time-interval through the planning horizon. So, we define a Boolean parameter  $K_t$ , that equals 1 if vessels can berth during time period *t* (without considering other constraints). Thanks to this parameter, we are able to restrict berthing decision periods inside the planning horizon, and hence to change the decision time-interval.

The user of the model is free to define the values of  $K_t$ . For example, during the first week, chartered vessels can berth every hour « 1 », hence  $K_t = 1, \forall t$ ; during the second week, every four hours « 0 - 0 - 0 - 1», hence  $K_t = 1, \forall t | (t)_{mod4} = 0$  and  $K_t = 0$  otherwise; during the third week, every eight hours « 0 - 0 - 0 - 0 - 0 - 0 - 0 - 1», hence  $K_t = 1, \forall t | (t)_{mod8} = 0$  and  $K_t = 0$  otherwise. New vessels to charter can be planned during the second and third week, providing for them an estimated position in the schedule. Then, as we advance in the planning horizon, the schedule is refined: some chartered vessels ( $\mathscr{V}_2$ ) will become berthed vessels ( $\mathscr{V}_1$ ), and some new vessels to charter ( $\mathscr{V}_3$ ) will become chartered vessels ( $\mathscr{V}_2$ ), and hence their laydays will be replaced by an expected arrival time. The decisions related to the loading of batches are constrained by the decisions related to the berthing of vessels, as they must be done during the vessel's stay which starts from the berthing time, but they can be taken at any period without considering the parameter  $K_t$ .

Modulating time interval in this manner helps integrating short-term decisions (BAP) and medium-term decisions (LAP) in a single model. As time approaches to present, the decisions are taken in a finer granularity (every hour), while for decisions that concern the planning in a few weeks from now a rough decision is taken (every 8 hours). Besides facilitating integration of LAP and BAP, this approach also helps controlling the number of variables (i.e. the number of variables is lower for medium-term decisions).

#### 4.4.Predicates:

A predicate is a logical statement that returns either a value of "True" or "False", based on the parameter values used in the statement. We will use these logical statements to describe the validity domain of decision variables. In our model, a decision variable exists only when the associated set of predicates returns "True". In this section, we present how predicates are implemented in our mathematical model.

The decision variable  $x_{vpt}$  determines for each chartered vessel  $(v \in \mathscr{V}_2)$ , the berthing time t and berthing position p. Each already berthed vessel  $(v \in \mathscr{V}_1)$  has a residual handling time and a predetermined berthing position. For the sake of simplicity, we assume that the berthing time t = 1 for these latter vessels.

The decision variable  $y_{vpth}^{b_v}$  determines for each chartered vessel  $(v \in \mathscr{V}_2)$  berthed in berthing position p, the loading start time t of batch  $b_v$ , stored in hanger h. The first batch to load on each already berthed vessel  $(v \in \mathscr{V}_1)$  has a residual handling time with a loading start time assumed at t = 1.

For each new vessel to charter  $(v \in \mathscr{V}_3)$ , the berthing position will be reserved from its latest berthing time decreased by its laydays,  $t - L_v + 1$ , until its latest finish date,  $\Upsilon_{v(\Gamma_{vt}+\Theta_{vp}-1)}$  (Figure 7). Similarly, the conveyors used to transport each batch  $b_v$  from storage hangar *h* to berthing position *p* will be reserved from the latest loading start time of the batch decreased by the vessel's laydays,  $t - L_v + 1$ , until the latest finish date of the batch,  $\Upsilon_{v(\Gamma_{vt}+\theta_{vp}^{h_v}-1)}$ , depending on the loading sequence chosen by the optimal solution. This assures that, any time during their laydays, new vessels to charter can be berthed at the reserved berthing position, and thus all the batches can be loaded, in any order without downtime, using the reserved conveyors.

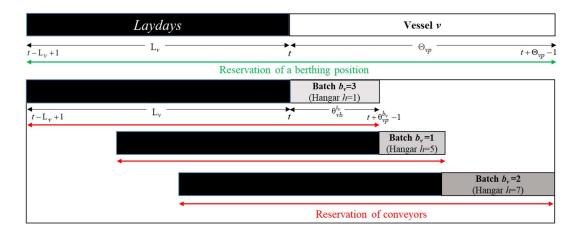


Figure 7. Reservation of port resources for new vessels to charter.

The existence of the decision variable  $x_{vpt}$  is subject to seven conditions:

- (1) Vessel v must be able to berth at berthing position p:  $N_{vp} = 1$ .
- (2) The length of vessel v must not exceed the length of berthing position p:  $\lambda_v \leq Q_p$ .
- (3) The draft of vessel v must not exceed the water depth of berthing position p:  $D_v \leq W_p$ .
- (4) Vessel v can berth only after its expected arrival time without exceeding its maximum waiting time in the harbor:  $A_v \le t \le A_v + I_v$ . To allow new vessels to charter  $(v \in \mathscr{V}_3)$  to berth at their first layday, t is replaced by  $t L_v + 1$ , then condition 4 becomes  $A_v \le t L_v + 1 \le A_v + I_v$ . Already berthed and chartered vessels have fictitious laydays equal to one hour  $(L_v = 1)$  since they have fixed expected arrival times, and hence they are not concerned by the decision of fixing laycans as in the case of new vessels to charter. Hence, the new condition is valid for all the types of vessels. The same applies to the following conditions. This modelling approach allows to merge LAP and BAP decision.

- (5) Vessel *v* can berth only during time periods where a decision of berthing vessels can be taken:  $K_{(t-L_v+1)}=1$ .
- (6) If the handling of vessel v is restricted to working periods  $(\gamma_v = 1)$ , it can enter the port only during working periods:  $\psi_{v(t-L_v+1)} = 0$ .
- (7) If vessel v is tide-dependent  $(\omega_v = 1)$ , it can leave the port at time period  $t = \Upsilon_{v(\Gamma_{vt} + \Theta_{vp} - 1)}$  if the latter is within a high tide  $(O_t = 1)$ :  $(1 - \omega_v) + \omega_v \cdot O_{\Upsilon_{v(\Gamma_{vt} + \Theta_{vp} - 1)}} = 1$ .

Similarly, the existence of the decision variable  $y_{vpth}^{b_v}$  is subject to seven conditions:

(1) Conditions 1, 2 and 3 of the existence of the decision variable  $x_{vpt}$ :

$$\mathbf{N}_{vp} = \mathbf{1} \wedge \lambda_v \le \mathbf{Q}_p \wedge \mathbf{D}_v \le \mathbf{W}_p \,.$$

(2) Batch  $b_v$  can be loaded on vessel v between the expected arrival time of this vessel and its finishing time as it reaches its maximum waiting time in the harbor, minus the loading time of this batch:

$$\mathbf{A}_{v} \leq t - \mathbf{L}_{v} + 1 \leq \Upsilon_{v\left(\Gamma_{v\left(\mathbf{A}_{v}+\mathbf{I}_{v}\right)}+\Theta_{vp}-\theta_{vp}^{b_{v}}\right)}.$$

(3) Batch  $b_v$  can be loaded on vessel v only after its date of availability:

$$t - \mathcal{L}_{v} + 1 \ge \mathcal{C}_{v}^{b_{v}}.$$

- (4) If the handling of vessel v is restricted to working periods  $(\gamma_v = 1)$ , batches can start loading only during working periods:  $\psi_{v(t-L_v+1)} = 0$ .
- (5) Batch  $b_v$  is loaded on vessel v from its storage hangar h:  $h = H_v^{b_v}$ .

Regarding the preventive maintenance activities, the decision variables  $z_{pt}^{m_p}$  and

 $z_{st}^{m_s}$  determine the starting time t of performing maintenance  $m_p$  at berthing position p and maintenance  $m_s$  at a conveyor in section s, respectively. The existence of these two decision variables is subject to only one condition each which states that each maintenance must be performed between its earliest and latest time:  $\underline{R}_p^{m_p} \le t \le \overline{R}_p^{m_p}$  for berthing positions and  $\underline{R}_s^{m_s} \le t \le \overline{R}_s^{m_s}$  for sections. When the maintenance has a fixed date, the indices of the decisions variables are predetermined.

To facilitate the readability of the mathematical model, we represent each predicate by a simplified notation given in Table 3.

Predicate	Notation
$N_{vp} = 1 \land \lambda_v \le Q_p \land D_v \le W_p$	$\mathbf{P}_{vp}$
$A_{\nu} \le t - L_{\nu} + 1 \le A_{\nu} + I_{\nu} \land K_{(t - L_{\nu} + 1)} = 1 \land \psi_{\nu(t - L_{\nu} + 1)} = 0 \land (1 - \omega_{\nu}) + \omega_{\nu} \cdot O_{\Upsilon_{\nu(\Gamma_{\nu t} + \Theta_{\nu p} - 1)}} = 1$	<b>P</b> <sub>vpt</sub>
$\mathbf{A}_{\nu} \leq t - \mathbf{L}_{\nu} + 1 \leq \Upsilon_{\nu\left(\Gamma_{\nu\left(\mathbf{A}_{\nu}+\mathbf{I}_{\nu}\right)} + \Theta_{\nu p} - \theta_{\nu p}^{b_{\nu}}\right)} \wedge t - \mathbf{L}_{\nu} + 1 \geq \mathbf{C}_{\nu}^{b_{\nu}} \wedge \Psi_{\nu\left(t - \mathbf{L}_{\nu} + 1\right)} = 0$	$\mathbf{P}_{vpt}^{b_v}$
$h = \mathrm{H}_{\mathcal{V}}^{b_{\mathcal{V}}}$	$\mathbf{P}_{vh}^{b_v}$
$\underline{\mathbf{R}}_{p}^{m_{p}} \leq t \leq \overline{\mathbf{R}}_{p}^{m_{p}}$	$\mathbf{P}_{pt}^{m_p}$
$\underline{\mathbf{R}}_{s}^{m_{s}} \leq t \leq \overline{\mathbf{R}}_{s}^{m_{s}}$	$\mathbf{P}_{st}^{m_s}$

Table 3. Notation of predicates.

The logical conditions of the existence of the decision variables  $x_{vpt}$ ,  $y_{vpth}^{b_v}$ ,  $z_{pt}^{m_p}$ 

and  $z_{st}^{m_s}$  are the following ones. For instance, the variable  $x_{vpt}$  exists only when the predicates  $\mathbf{P}_{vp}$  and  $\mathbf{P}_{vpt}$  are both "True".

$$x_{vpt} \in \{0,1\}, \forall v \in \mathcal{V}, \forall p \in \mathcal{P} | \mathbf{P}_{vp}, \forall t \in \mathcal{T} | \mathbf{P}_{vpt}\}$$

$$\begin{aligned} y_{vpth}^{b_{v}} \in \{0,1\}, \forall v \in \mathcal{V}, \forall b_{v} \in \mathcal{R}, \forall p \in \mathcal{P} \left| \mathbf{P}_{vp}, \forall t \in \mathcal{T} \right| \mathbf{P}_{vpt}^{b_{v}}, \forall h \in \mathcal{H} \left| \mathbf{P}_{vh}^{b_{v}} \right| \\ z_{pt}^{m_{p}} \in \{0,1\}, \forall p \in \mathcal{P}, \forall m_{p} \in \mathcal{M}_{p}, \forall t \in \mathcal{T} \left| \mathbf{P}_{pt}^{m_{p}} \right| \\ z_{st}^{m_{s}} \in \{0,1\}, \forall s \in \mathcal{S}, \forall m_{s} \in \mathcal{M}_{s}, \forall t \in \mathcal{T} \left| \mathbf{P}_{st}^{m_{s}} \right| \end{aligned}$$

#### 4.5.Mathematical model:

First, we define the intermediary variables  $\mu_v$  and  $\tau_v^{b_v}$ , which give for each vessel v the berthing position in the decision variables  $x_{vpt}$  and  $y_{vpth}^{b_v}$ , respectively.

$$\begin{split} \mu_{v} &= \sum_{p \in \mathscr{P} \mid \mathbf{P}_{vp}} \sum_{t \in \mathscr{T} \mid \mathbf{P}_{vpt}} p \cdot x_{vpt}, \forall v \in \mathscr{V} \\ \tau_{v}^{b_{v}} &= \sum_{p \in \mathscr{P} \mid \mathbf{P}_{vp}} \sum_{t \in \mathscr{T} \mid \mathbf{P}_{vpt}^{b_{v}}} \sum_{h \in \mathscr{H} \mid \mathbf{P}_{vh}^{b_{v}}} p \cdot y_{vpth}^{b_{v}}, \forall v \in \mathscr{V}, \forall b_{v} \in \mathscr{B}_{v} \end{split}$$

Similarly, we define for each vessel v the berthing and finishing times  $\varepsilon_v$  and  $\pi_v$ , by replacing  $b \cdot x_{vpt}$  in  $\mu_v$  by  $t \cdot x_{vpt}$  and  $\Upsilon_{v\left(\Gamma_{v(t-L_v+1)}+\Theta_{vp}-1\right)} \cdot x_{vpt}$ , respectively. Likewise, we define for each batch  $b_v$  to load on vessel v, the loading start and finishing times  $\rho_v^{b_v}$  and  $\sigma_v^{b_v}$  by replacing  $p \cdot y_{vpth}^{b_v}$  in  $\tau_v^{b_v}$ , respectively, by  $t \cdot y_{vpth}^{b_v}$  and  $\Upsilon_{v\left(\Gamma_{v(t-L_v+1)}+\theta_{vp}^{b_v}-1\right)} \cdot y_{vpth}^{b_v}$ .

The mathematical model can be formulated as follows:

$$\begin{aligned} &Max \sum_{v \in \mathscr{V}} \left( \beta_{v} \cdot w_{v} - \eta_{v} \cdot u_{v} \right) (1) \text{ or } Min \sum_{v \in \mathscr{V}} \pi_{v} (1') \\ &\sum_{p \in \mathscr{P} \mid \mathbf{P}_{vp}} \sum_{t \in \mathscr{T} \mid \mathbf{P}_{vpt}} x_{vpt} = 1, \forall v \in \mathscr{V} \qquad (2) \\ &\sum_{p \in \mathscr{P} \mid \mathbf{P}_{vp}} \sum_{t \in \mathscr{T} \mid \mathbf{P}_{vpt}^{b_{v}}} \sum_{h \in \mathscr{H} \mid \mathbf{P}_{vh}^{b_{v}}} y_{vpth}^{b_{v}} = 1, \forall v \in \mathscr{V}, \forall b_{v} \in \mathscr{R}_{v} \qquad (3) \\ &\sum_{t \in \mathscr{T} \mid \mathbf{P}_{pt}^{m_{p}}} z_{pt}^{m_{p}} = 1, \forall p \in \mathscr{P}, \forall m_{p} \in \mathscr{M}_{p} \qquad (4) \end{aligned}$$

$$\begin{split} \sum_{t \in \mathscr{T}} \left| \mathbf{P}_{st}^{m_{s}} z_{st}^{m_{s}} = 1, \forall s \in \mathscr{T}, \forall m_{s} \in \mathscr{M}_{s} \quad (5) \right. \\ \mu_{v} = \tau_{v}^{b_{v}}, \forall v \in \mathscr{V}, \forall b_{v} \in \mathscr{R}_{v} \quad (6) \\ \rho_{v}^{b_{v}} \geq \varepsilon_{v}, \forall v \in \mathscr{V}, \forall b_{v} \in \mathscr{R}_{v} \quad (7) \\ \sigma_{v}^{b_{v}} \leq \pi_{v}, \forall v \in \mathscr{V}, \forall b_{v} \in \mathscr{R}_{v} \quad (8) \\ \sum_{b_{v} \in \mathscr{R}_{v}} \sum_{p \in \mathscr{P}} \left| \mathbf{P}_{vp} \sum_{t' \in \mathscr{T}} \left| \mathbf{P}_{vpt'}^{b_{v}} \wedge \Gamma_{vt'} + \theta_{vp}^{b_{v}} - 1 \leq T \wedge t' \leq t \leq \Upsilon_{v} (\Gamma_{vt'} + \theta_{vp}^{b_{v}} - 1) \right. \right. \\ \sum_{b_{v} \in \mathscr{R}_{v}} \sum_{b_{v} \in \mathscr{R}_{v}} \left| \mathbf{P}_{vh}^{b_{v}} \sum_{p \in \mathscr{P}} \left| \mathbf{P}_{vp} \sum_{t' \in \mathscr{T}} \left| \mathbf{P}_{vpt'}^{b_{v}} \wedge \Gamma_{vt'} + \theta_{vp}^{b_{v}} - 1 \leq T \wedge t' - \mathbf{L}_{v} + 1 \leq t \leq \Upsilon_{v} (\pi_{v} - b_{v}^{b_{v}}) \right. \right. \\ \end{split}$$

$$\sum_{v \in \mathscr{V}} \sum_{v \in \mathscr{X}_{v}} |\mathbf{P}_{vh}^{\circ v} \sum_{p \in \mathscr{P}} |\mathbf{P}_{vp} \sum_{t' \in \mathscr{T}} |\mathbf{P}_{vpt'}^{\circ v} \wedge \Gamma_{vt'}^{\circ} + \theta_{vp}^{\circ v} - 1 \le \Gamma \wedge t' - L_{v} + 1 \le t \le \Gamma_{v} (\Gamma_{vt'} + \theta_{vp}^{b_{v}} - 1)^{2} \text{ where } h$$

$$(10)$$

$$\sum_{v \in \mathscr{T}} \sum_{b_v \in \mathscr{R}_v} \sum_{p \in \mathscr{P} \mid \mathbf{P}_{vp}} \sum_{t' \in \mathscr{T}} \left| \mathbf{P}_{vpt'}^{b_v} \wedge \Gamma_{vt'} + \theta_{vp}^{b_v} - 1 \le \mathsf{T} \wedge t' - \mathsf{L}_v + 1 \le t \le \Upsilon} \sum_{v \left( \Gamma_{vt'} + \theta_{vp}^{b_v} - 1 \right)} \sum_{h \in \mathscr{H} \mid \mathbf{F}_{sh} = 1 \wedge \mathbf{P}_{vh}^{b_v}} y_{npt'h}^{b_v} \le \mathsf{U}_s - \sum_{m_s \in \mathscr{M}_s} \sum_{t' \in \mathscr{T}} \left| t - \mathsf{R}_s^{m_s} + 1 \le t' \le t \wedge \mathbf{P}_{st}^{m_s}} z_{st'}^{m_s}, \forall t \in \mathscr{T}, \forall s \in \mathscr{S}$$
(11)

$$\sum_{v \in \mathscr{V}} \sum_{p' \in \mathscr{P}} \left| \mathbf{E}_{p}^{p'} = 1 \wedge \mathbf{P}_{vp'} \sum_{t' \in \mathscr{T}} \left| \mathbf{P}_{vp't'} \wedge \Gamma_{vt'} + \Theta_{vp'} - 1 \leq T \wedge t' - \mathbf{L}_{v} + 1 \leq t \leq \Upsilon_{v(\Gamma_{vt'} + \Theta_{vp'} - 1)} x_{vp't'} \leq 1 - \sum_{p' \in \mathscr{P}} \left| \mathbf{E}_{p}^{p'} = 1 \sum_{m_{p'} \in \mathscr{M}_{p'}} \sum_{t' \in \mathscr{T}} \left| t - \mathbf{R}_{p'}^{mp'} + 1 \leq t' \leq t \wedge \mathbf{P}_{p't}^{mp'} x_{p't'}^{mp'}, \forall t \in \mathscr{T}, \forall p \in \mathscr{P}$$

$$(12)$$

$$\begin{bmatrix} \sum_{v \in \mathscr{V}_{2} \cup \mathscr{V}_{3}} \sum_{p \in \mathscr{P}} |\mathbf{P}_{vp} \sum_{t' \in \mathscr{T}} |\mathbf{P}_{vpt'} \wedge t' = t + \mathcal{L}_{v} - 1} x_{vpt'} \end{bmatrix} + \begin{bmatrix} \sum_{v \in \mathscr{V}} \sum_{p \in \mathscr{P}} |\mathbf{P}_{vp} \sum_{t' \in \mathscr{T}} |\mathbf{P}_{vpt'} \wedge \Gamma_{vt} - \Theta_{vp} \ge 0 \wedge t' = \Upsilon_{v(\Gamma_{vt} - \Theta_{vp} + 1)} x_{vpt'} \end{bmatrix} \le \mathbf{G}, \forall t \in \mathscr{T}$$
(13)  
$$u_{v} \ge \pi_{v} - \delta_{v}, \forall v \in \mathscr{V}$$
(14)  
$$w_{v} \ge \delta_{v} - \pi_{v}, \forall v \in \mathscr{V}$$
(15)  
$$u_{v} - w_{v} = \pi_{v} - \delta_{v}, \forall v \in \mathscr{V}$$
(16)  
$$u_{v}, w_{v} \ge 0, \forall v \in \mathscr{V}$$
(17)

Objective function (1) is based on an efficiency criteria that maximizes the difference between the despatch money and the demurrage charges of each vessel v while objective function (1') is based on an effectiveness criteria that minimizes the finishing

time (departure time) of each vessel v. Equation (2) ensures that each vessel v starts berthing at a unique berthing position p, and in a unique time period t. Equation (3) ensures that each batch  $b_v$  starts loading in a unique vessel v at a unique berthing position p, in a unique time period t, and is stored in a unique hangar h. Equation (4) ensures that maintenance  $m_p$  to be performed at a berthing position p has a unique start time. Similarly, equation (5) ensures that maintenance  $m_s$  to be performed at a conveyor in section s has a unique start time. Equation (6) ensures that berthing position p is the same in both decision variables  $x_{vtp}$  and  $y_{vtph}^{b_v}$ . Equation (7) ensures that the loading of each batch  $b_v$  can only begin once vessel v has been berthed. Equation (8) ensures that each vessel v can only leave the port when all batches have been loaded. Equation (9) ensures that at most one batch can be loaded at the same time on each vessel v. Equation (10) ensures that only one batch at most can leave at a time each storage hangar h. Equation (11) limits the number of identical parallel conveyors used simultaneously in a section s during the loading time of each batch due to the limit or/and the maintenance of conveyors. Equation (12) avoids the overlapping of vessels in each berthing position p, the simultaneous use of berthing positions that share a space of the quay since the berth layout of each quay is hybrid and the use of berthing positions where maintenance activities are performed (e.g., in Figure 1, berthing positions 3 and 5 share berthing position 3, consequently, they cannot be used simultaneously. Moreover, if maintenance is performed at berthing position 3, it will also be formed at berthing position 5. The opposite is also true.). Equation (13) limits the number of incoming and outgoing vessels to pass simultaneously through the navigation channel. Equations (14-17) determine the delay and the advance of each vessel.

#### 5. Case study:

In this section, we describe the test instances of the case study and report the computational results. An example schedule obtained using the model is also given to illustrate a typical output. The formulations are written on Mosel and implemented in Xpress IVE Version 1.24.24, with 64 bits. All the tests are run on a server with an Intel® Xeon® Gold 6138 processor (8 cores) of 2.00 GHz processing speed and 32 GB of memory using the Xpress Optimizer Version 33.01.05 with the default options.

#### 5.1. Generation of test instances:

Test instances are based on a sample of data obtained from OCP group, a world leader in the phosphate industry, which operates six quays in the bulk port of Jorf Lasfar in Morocco, recognized as the largest bulk port in Africa. We focus on the first two quays that are dedicated to the export of phosphate rock and fertilizers. The data provides information about all the vessels that were berthed during the first half of 2016, such as the arrival time, the berthing time and position, the cargo type and tonnage, and the handling time of vessels. Given the limited access to real bulk port data, test instances are designed to have the same characteristics as the sample of data obtained from OCP group, to test and validate the effectiveness of the proposed model.

Three sets are designed for  $V = \{20, 40, 60\}$ . Each set is composed of 15 instances. Hence, we have 45 instances in total. Every 5 instances in a set represent a level of congestion (congested, mildly congested, and uncongested), which is determined by the interarrival time of vessels. Indeed, for the same number vessels, the level of congestion in the port increases as the interarrival time of vessels decreases and then the problem becomes harder to solve.

For all instances:

- We assume a 4-week planning horizon discretized into 1-hour intervals, hence T=672. We vary the decision time interval inside this planning horizon to handle short term and medium-term decisions as explained in Section 4.3. For the short-term planning (e.g. during the first week in our instances) the accuracy of the planning is set to every hour. The decision time interval is set to four, eight and twelve hours for weeks two, three and four, respectively. Characteristics related to time periods (decision time-intervals, high-tide cycles and non-working periods) can be found in <u>Time.xlsx</u>.
- We consider a navigation channel in which the maximum number of vessels allowed to pass simultaneously is limited to three vessels. We also consider two quays with hybrid berth layout, partitioned into five berthing positions each. Table 4 gives respectively for each berthing position the length (m), the minimum water depth (m), the productivity (t/h), the incompatibilities and the number of maintenance activities with the duration (h), the earliest and latest time (h) to perform each one.

Table 4.	Character	istics of	berthing	positions.
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	p	$Q_p$	$W_p$	Productivity					E	р' р					M <sub>p</sub>	R	$p^{p}$	R	т <sub>р</sub> :р	R	$p^{p}$
	P	$\checkmark_p$	•• <i>p</i>		p'=l	p'=2	<i>p′=3</i>	<i>p'</i> =4	<i>p'</i> =5	<i>p'=6</i>	<i>p'</i> =7	<i>p'=8</i>	p'=9	<i>p′=10</i>	mp	$m_p=1$	$m_p=2$	$m_p=1$	$m_p=2$	$m_p=1$	$m_p=2$
	1	180	13.5	2000	1	0	0	0	0	0	0	0	0	0	2	12	10	24	328	48	328
-	2	255	14.5	2000	0	1	0	0	0	0	0	0	0	0	1	7	0	405	0	450	0
Quay	3	150	15.6	1000	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0
	4	150	15.6	1000	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0
	5 (3 U 4)	300	15.6	2000	0	0	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0
	6	180	13.5	2000	0	0	0	0	0	1	0	0	0	0	2	29	14	266	320	266	320
2	7	235	14.5	2000	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0
Quay	8	125	14.5	2000	0	0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	0
$ \circ $	9	125	15.6	2000	0	0	0	0	0	0	0	0	1	1	2	10	6	10	360	53	382
	10 (8 U 9)	250	14.5	4000	0	0	0	0	0	0	0	1	1	1	1	23	0	300	0	320	0

• We consider nine storage hangars which are linked to all the berthing positions via a conveyor system (Figure 4). The latter is divided into two sections composed of different numbers of identical parallel conveyors. Table 5 gives respectively for each section of the port conveyor system the number of identical parallel

conveyors, the conveyors that belong to it and the number of maintenance activities with the duration (h), the earliest and latest time (h) to perform each one. Table 5. Characteristics of sections of the port conveyor system.

_																					
	c					F <sub>sh</sub>					TT	M		$\mathbf{R}_{s}^{m_{s}}$			$\underline{\mathbf{R}}_{s}^{m_{s}}$			$\overline{R}_{s}^{m_{s}}$	
		h = 1	h=2	h=3	h=4	h = 5	h=6	h = 7	h = 8	h=9	U <sub>s</sub>	M <sub>s</sub>	$m_s = 1$	$m_s = 2$	$m_s=3$	$m_s = 1$	$m_s=2$	$m_s=3$	$m_s = 1$	$m_s = 2$	$m_s = 3$
	1	1	1	1	1	0	0	0	0	0	3	2	12	8	0	282	284	0	282	286	0
	2	1	1	1	1	1	1	1	1	1	4	3	6	10	9	213	290	362	213	290	390

- The length of vessels varies between 100 and 300 meters.
- The draft of vessels varies between 5 and 15 meters. Vessels that have a draft over 14 meters are tide-dependent while leaving the port.
- The number of batches to load on each vessel varies between one and three batches.
- The tonnage of batches varies between 2,000 and 36,000 tones.
- 10% of vessels have a SSHEX clause.
- The laydays are set arbitrarily at 48 hours for new vessels to charter, while already berthed and chartered vessels have fictitious laydays equal to one hour.
- For chartered vessels, the contractual demurrage is chosen randomly from a Uniform distribution between 50 and 150. The contractual dispatch is assumed half the demurrage. For new vessels to charter, we assume negligible demurrage and dispatch per hour. Note that these are fictitious values and are only used in order not to impact the economic results of already chartered vessels. Finally, for already berthed vessels, hourly demurrage and dispatch rates are assumed zero since no decisions need to be made for this group of vessels; they are already berthed.
- The maximum waiting time in the harbor is set arbitrarily at 72 hours for all the chartered vessels and one week for all the new vessels to charter. The latter have

high maximum waiting times in the harbor in order not to affect the economic results of chartered vessels.

Thanks to these conventions, all the vessels are dealt with together since there is no need to define specific constraints for each type of vessels (already berthed vessels, chartered vessels, and new vessels to charter). All instances are accessible in the file Instances.xlsx.

#### 5.2.Illustrative example:

In this section, we present a typical schedule that the port manager can obtain by using the proposed model. We consider the same characteristics of time periods, berthing positions, conveyor sections and vessels presented in the previous section. Table 6 gives the characteristics of six chartered vessels and one new vessel to charter.

v	A	I,	λ	$D_{\nu}$	0	2	I	I	, η		β,					١	J <sub>up</sub>					B	h	$H^{b_{v}}$	$C_v^{b_v}$					θ	$b_v \\ vp$				
1	1.	1	100	$D_{v}$	w v	IV	<sup>L</sup> v	1	1 10	·	Pv	p=1	p=2	p=3	p=4	p=5	p=6	p=7	p=8	p=9	p=10	Dv	Uv	v	r	p=1	p=2	p=3	p=4	p=5	<i>p</i> =6	p=7	p=8	p=9	p = 10
																							1	6	277	12	12	24	24	12	12	12	12	12	6
1	245	48	170	12.5	0	0	1	22	2 10	5 5	52.5	1	1	1	1	0	1	1	1	1	0	2	2	2	268	10	10	20	20	10	10	10	10	10	5
																							3	0	0	0	0	0	0	0	0	0	0	0	0
																							1	3	250		28	56	56	28	28	28	28	28	14
2	264	48	245	13.0	1	0	1	6	5 13	2	66	0	0	0	0	0	0	0	0	0	1	3	2	7	284		14	28	28	14	14	14	14	14	7
																							3	9	277		24	48	48	24	24	24	24	24	12
																							1	-	269		7	14	14	7	7	7	7	7	4
3	268	48	290	15.5	1	1	1	10	5 70	5   3	38	0	0	0	0	1	0	0	0	0	0	2	2	8	260	9	9	18	18	9	9	9	9	9	5
																							3	0	0	0	0	0	0	0	0	0	0	0	0
																							1	4	297	21	21	42	42	21	21	21	21	21	11
4	298	48	100	10.1	0	0	1	2	1 6	7   3	33.5	1	1	1	1	0	1	1	1	1	0	1	2	0	0	0	0	0	0	0	0	0	0	0	0
									-	_	_												3	0	0	0	0	0	0	0	0	0	0	0	0
										_													1	6	320		8	16	16	8	8	8	8	8	4
15	308	48	250	11.5	0	0	1	34	4 14	97	4.5	1	1	1	1	0	1	1	1	1	0	3	2	7	332	6	6	12	12	6	6	6	6	6	3
$\vdash$					-	-	-	-	-	+	-											-	3	9	308	<u> </u>	20	40	40	20	20	20	20	20	10
	220	40	120	15.2			1		112			1	1	1	1	0	1	1	1	1	0		2		316 331		10	20 26	20 26	10 13	10 13	10 13	10 13	10 13	5
0	320	48	120	15.3	0	0	1	2.	5 13	4	0/	1	1	1	1	0	1	1	1	1	0	2	2	0	551										
$\vdash$							-	-	+	+													1	1	274	0 25	0 25	0	0 50	0 25	0	0 25	0 25	0 25	0
1,	274	160	210	14.2			10		5 1		1	1	1	1	1	0	1	1	1	1	0	1	2	0	0	25	25	50 0	50	25	25	25	25	25	0
11	2/4	108	210	14.2	0	0	48	12:	5 1		1	1	1	1	1	0	1	1	1	1	0	1	2	0	0	0	0	0	0	0	0	0	0	0	0
			1					1		1													13	0	0	0	0	0	0	0	0	0	0	0	0

Table 6. Characteristics of vessels.

Figure 8 shows the Gantt chart of vessel and batch schedule. A complete Gantt chart of 60 vessels and a 4-week planning horizon is shown in the file <u>Gantt.xlsx</u>. At its bottom, there is a time line in hours and a one-week time frame (from Friday of week 2 to Monday of week 3) with high tide hours. The decision time-intervals are highlighted every four hours for week 2 and every eight hours for week 3. All constraints are respected by the solution given by the LBAP model:

- All vessels are berthed at restricted time periods for which a decision can be made and do not occupy berthing positions where a maintenance is performed.
- The batches of each vessel are loaded in any order without downtime after their date of availability and only one batch at most leaves at a time each storage hangar.
- Vessels 2 and 3 have high drafts and thereby are tide-dependent, so they occupy berthing sections with high water depth and leave the port during high tides.
- The handling of vessel 3 stops during non-working hours because it has a SSHEX clause.
- The handling time of vessel 2 is shorter than its contractual handling time since it occupies a berthing position with high productive loading equipment.
- The number of vessels passing through the navigation channel and used parallel conveyors per section do not exceed their limits. The number of allowed parallel conveyors per section can decrease due to maintenance.
- The optimal laycan proposed for the new vessel to charter 7 is [276, 323]. This vessel can berth at any time period during its laydays. We note that, a precise berthing time will be assigned to this vessel as its status changes from new vessel to chartered one and as the time progresses from week two towards week one.

Thanks to the integration of the LAP and the BAP, the port managers can propose laycans for the new vessels to charter considering the allocation of berthing positions to already chartered vessels and conveyors to batches, thereby avoiding the payment of demurrage charges, and knowing when to accept or refuse a new vessel to charter.

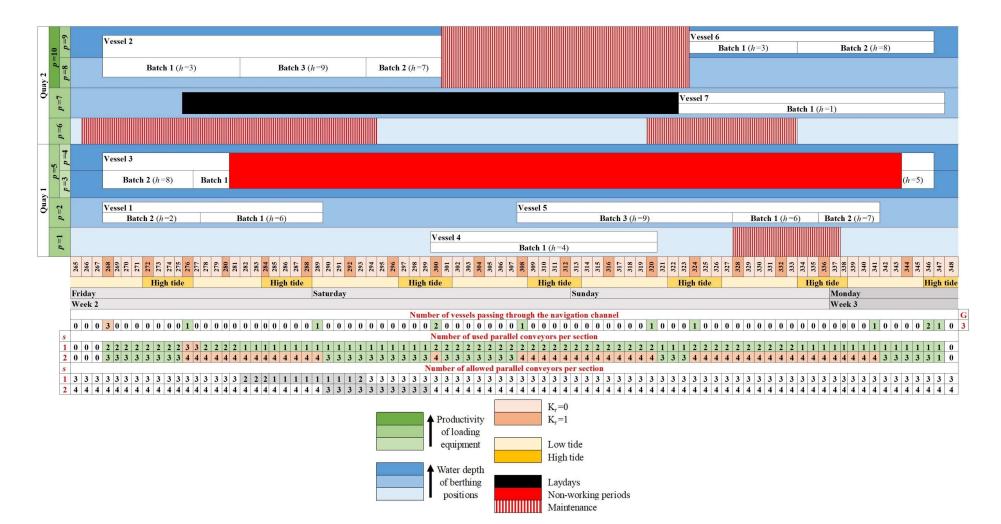


Figure 8. Gantt chart of vessel and batch schedule.

#### 5.3. Computational results:

In this section, we explore the computational performance of the proposed model. One of the objectives is to verify if the proposed model can be solved in a reasonable time using commercial software. The other objective is to test the sensitivity of the results with respect to the different input parameters in the model,

For each instance, Table 7 shows the number of already berthed and chartered vessels and the new ones to charter, the level of congestion, the computation time in seconds, and the optimality gap in percentages. The computation time was limited to 1 hour. The empty fields indicate that no feasible solutions were found within the time limit, and thus, it was not possible to calculate the statistics. Xpress calculates the gap as follows:  $100 \cdot (ub - lb) / ub$ , where ub is the best upper bound obtained within the time limit, and lb is the value of the objective function corresponding to the best integer solution achieved. The detailed results of each instance are shown in the file <u>Results.xlsx</u>. Table 7. Computational results.

		V=	20	V=	-40	V=	=60
		$V_1=2, V_2=$	=16, V <sub>3</sub> =2	V <sub>1</sub> =3, V <sub>2</sub> =	=34, V <sub>3</sub> =3	V <sub>1</sub> =4, V <sub>2</sub> =	=52, V <sub>3</sub> =4
Instance	Congestion	Time	Gap	Time	Gap	Time	Gap
1		3.1	0	13.0	0	52.7	0
2		6.3	0	13.9	0	453.3	0
3	No	6.1	0	15.4	0	243.6	0
4		8.5	0	79.1	0	1366,0	0
5		6.4	0	10.2	0	163.4	0
Av	/erage	6.1	0	26.3	0	455.8	0
6		14.9	0	23.0	0	1356.6	0
7		3.0	0	26.5	0	84.6	0
8	Mild	2.9	0	31.7	0	320.8	0
9		2.4	0	35.4	0	63.6	0
10		9.6	0	30.7	0	840.3	0
Av	/erage	6.6	0	29.5	0	533.2	0
11		12.4	0	9.0	0	2722.1	0
12		13.1	0	106.6	0	3231.9	0
13	Yes	17.7	0	37.4	0	235.3	0
14		23.9	0	27.2	0	3603.5	7.9
15		6.0	0	15.9	0	263.6	0
Av	/erage	14.6	0	39.22	0	1706.1	1.6

We can make several observations based on these results:

First, for a fixed number of vessels, increasing the level of congestion increases the average computation time. Similarly, for a fixed level of congestion, increasing the number of vessels increases the average computation time. Hence, we can conclude that the computation time is very related to the busyness of the port.

Second, we are able to solve to optimality instances of realistic size, up to 60 vessels, 10 berthing positions, and 9 storage hangars for a 4-week planning horizon in computation times not exceeding one hour. For only one instance, Xpress could not find an optimal solution due to the time limit. We note that the maximum number of vessels that were berthed in the port of Jorf Lasfar during a period of 4 weeks in the first half of 2016 is 30 vessels. Hence, we can conclude that the integer linear programming model proposed for the LBAP can easily be used in bulk ports where such decisions need to be made frequently, with only commercial software. Thus, developing a heuristic for the problem is not necessary.

#### 6. Conclusions:

In this paper, we integrate the Laycan Allocation Problem and the dynamic hybrid Berth Allocation Problem in the context of tidal bulk ports with multiple quays and a conveyor system between storage hangars and berthing positions. While laycans concern only vessels for export, a symmetric approach can be applied for berthing decisions in the context of import ports. Our research is motivated by the bulk port of Jorf Lasfar but it is also valid for any other bulk port. A new integer linear programming model is proposed to solve this integrated problem. The latter integrates two problems with different decision levels (tactical and operational) thanks to the modulation of the time-interval between decisions and the introduction of fictitious laydays for already berthed and chartered vessels. Several characteristics are addressed in the definition of the LBAP to make it closer to reality, such as the multiplicity of quays, navigation channel restrictions, conveyor routing constraints with preventive maintenance activities, the variation of water depth, vessel tide-dependency, the productivity of bulk-handling cranes, the multiplicity of cargo types on the same vessel, charter party clauses and non-working periods. Instead of expressing these characteristics by a set of constraints in the model, we used predicates to formulate them. This approach is quite handy since predicates are easy to modify in the model. Furthermore, they reduce the number of variables and constraints in the model and improve the computational performance. Moreover, the port conveyor system is modeled in a new way that does not list each route of conveyors between storage hangars and berthing positions, which makes easier the formulation of the problem.

Computational tests of a case study are performed using a commercial solver. The results show that our model is able to solve problem instances of realistic size, up to 60 vessels, 10 berthing positions, and 9 storage hangars for a 4-week planning horizon, in a reasonable computation time.

In this study, we assumed that the cargo to load on vessels is always available in the hangars. In practice, this depends on the upstream supply chain. An extension to this study could be to integrate storage locations decisions and inventory management at the hangars.

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