



**HAL**  
open science

# The Event-specific Geomorphological Instantaneous Unit Hydrograph (E-GIUH): The basin hydrological response characteristic of a flood event

Hervé Andrieu, Roger Moussa, Pierre-Emmanuel Kirstetter

## ► To cite this version:

Hervé Andrieu, Roger Moussa, Pierre-Emmanuel Kirstetter. The Event-specific Geomorphological Instantaneous Unit Hydrograph (E-GIUH): The basin hydrological response characteristic of a flood event. *Acta Biológica Colombiana*, 2021, 603 (D), 10.1016/j.jhydrol.2021.127158 . hal-03430447

**HAL Id: hal-03430447**

**<https://hal.science/hal-03430447>**

Submitted on 16 Nov 2021

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

1 **The Event-specific Geomorphological Instantaneous Unit Hydrograph (E-**  
2 **GIUH): The basin hydrological response characteristic of a flood event**

3 Hervé Andrieu<sup>1</sup>, Roger Moussa<sup>2</sup>, Pierre-Emmanuel Kirstetter<sup>3,4,5,6</sup>

4  
5 <sup>1</sup>GERS-LEE, Univ. Gustave Eiffel, IFSTTAR, F-44344 Bouguenais, France

6 <sup>2</sup>LISAH, Univ. Montpellier, INRAE, IRD, Montpellier SupAgro, Montpellier, France

7 <sup>3</sup>School of Civil Engineering and Environmental Science, University of Oklahoma, Norman, OK 73072, USA

8 <sup>4</sup>School of Meteorology, University of Oklahoma, Norman, OK 73072, USA

9 <sup>5</sup>Advanced Radar Research Center, University of Oklahoma, Norman OK 73072, USA

10 <sup>6</sup>NOAA / National Severe Storms Laboratory, Norman OK 73072, USA

11  
12 Submitted for publication in the Journal of Hydrology  
13 <https://doi.org/10.1016/j.jhydrol.2021.127158>

14 Corresponding author: Hervé Andrieu, [AndrieuHerve@orange.fr](mailto:AndrieuHerve@orange.fr)

15 Keywords : GIUH, Flash-flood, rainfall-runoff modeling, Inverse method, Rainfall spatial variability

16  
17 Highlights:

18 - The Width Function-GIUH has been modified to project the spatial distribution of rainfall onto the  
19 hydrological network.

20 - By accounting for the influence of rainfall on the hydrological response of catchments, an Event specific -  
21 GIUH (E-GIUH) is defined for each flood event.

22 - The identification of an E-GIUH from observed data (hydrograph and rain field time series) is treated as an  
23 inverse problem.

24 - The proposed identification method is applied to a sample of flooding events on two catchments within the  
25 OHMCV Observatory territory, in confirming the wide diversity of E-GIUHs.

26 - A sensitivity analysis indicates that the method is fairly robust and easy to use, which is most encouraging  
27 for large-scale applications.

28

29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46

**Abstract:**

In the field of hydrology, the Geomorphological Instantaneous Unit Hydrograph (GIUH) is central to describing a watershed response. The application of GIUH is extended to individual hydrological events by accounting for the influence of rainfall spatial distribution. A method is proposed herein to identify the Geomorphological Instantaneous Unit Hydrograph specific to each flood event (i.e. E-GIUH), when runoff of effective rainfall is the dominant process. The E-GIUH is derived from observational data, namely: rainfall field time series, and a hydrograph. Such an identification process is formulated as an inverse problem with parameters such as the E-GIUH velocity and coefficient of dispersion, as well as the hyetograph of rainfall excess. The proposed method is applied to several flood events across two mountainous catchments within the Cevennes-Vivarais Mediterranean Hydrometeorological Observatory territory prone to flash flooding. Results indicate that the E-GIUHs display significant variability over the two basins, and the E-GIUH parameters appear to be correlated with the flood event magnitude. The E-GIUH synthesizes the basin response to rain forcing and can be considered as a signature of flood events. A sensitivity study suggests that E-GIUH identification is fairly robust, even with respect to the *a priori* hyetograph of effective rainfall.

47 **1. Introduction**

48

49 The concept of the Geomorphological Instantaneous Unit Hydrograph (GIUH), defined as the probability  
50 density function (pdf) of water travel time along the channel links of the hydrographic network, was developed by  
51 (Gupta et al., 1980; Rodriguez-Iturbe and Valdés, 1979) by linking the unit hydrograph (Dooge, 1959; Sherman,  
52 L.K., 1932) to the geomorphological parameters of a catchment. The emergence of GIUH has contributed to the  
53 success of lumped rainfall-runoff models, which are widely used for their parsimony and robustness in both flash  
54 flood prediction and hydrograph analysis when runoff of effective rainfall is the dominant process of floods (Wood  
55 et al., 1990) . More specifically, the GIUH is well suited to treating the ungauged basin modeling problem, which  
56 pertains to the longstanding challenge of regional modeling over large areas, as exposed in the review paper by  
57 (Singh et al., 2014). The widespread use of GIUH within the hydrology community coupled with its development  
58 over the decades attests to its relevance in representing watershed responses and moreover confirms the ability of  
59 this approach to complement distributed models (Fatichi et al., 2016).

60

61 The initial GIUH formulation relies on the channel links in hydrographic networks, as described by the Horton  
62 classification. (Marani et al., 1991) and (Rodriguez-Iturbe and Rinaldo, 1997) extended this formulation to the  
63 probability density function (pdf) of hydrological distances to the basin outlet, as described by the Width Function  
64 (Kirkby, 1976), and went on to propose the Width Function Geomorphological Approach (D’Odorico and Rigon,  
65 2003; Rigon et al., 2016). An assumption of constant velocity is adopted to convert the distribution of flow  
66 distances into a pdf of travel times along flow paths. The travel time pdf may be represented by the Advection  
67 Dispersion Equation (ADE) (Rinaldo et al., 1991) and a unique solution of the Diffusive Wave Equation (Hayami,  
68 1951; Moussa, 1997). The GIUH is thus defined by the Width Function and the two parameters characterizing the  
69 ADE and DWE, i.e. flow velocity and coefficient of dispersion. (Saco and Kumar, 2002a) justified this constant  
70 velocity assumption by showing that varying flow path velocities can be taken into account by means of a  
71 kinematic-geomorphic dispersion that increases the coefficient of dispersion parameter.

72

73 GIUH applications often rely on a unique set of parameters in order to calibrate the model (e.g. (Boudhraâ et  
74 al., 2018; Chen et al., 2019; Choi et al., 2011; Moussa, 1997; Yao et al., 2014), thereby suggesting that a single  
75 representative GIUH can be associated with a catchment. However, several studies have highlighted the influence  
76 on the catchment response of: i) the rain spatial distribution (Emmanuel et al., 2017; Goni et al., 2019; Olivera and  
77 Maidment, 1999; Zoccatelli et al., 2010), and ii) the rain event magnitude (Rodriguez et al., 2005; Saco and Kumar,

78 2002b). These findings have been confirmed by the post-event analysis of floods, (Smith et al., 2005, 2002) among  
79 others, and simulation studies (Emmanuel et al., 2015; Volpi et al., 2012), hence acknowledging the GIUH  
80 limitations listed by (Rigon et al., 2016), who specifically noted these shortcomings when accounting for the  
81 rainfall distribution. Broadly speaking, these results indicate that the GIUH depends on rainfall-runoff processes  
82 that drive the flow dynamics in the hydrograph network. Consequently, every flood event can be characterized by  
83 its own GIUH, hereafter denoted as the E-GIUH, which is capable of enriching the signatures of hydrological  
84 processes driving the basin response to rainfall forcing at the flood event scale (McMillan, 2020).

85

86 This manuscript aims to advance the width function-based GIUH by: i) adapting its formulation in order to  
87 account for the influence of spatial rainfall variability, and ii) proposing a method to determine the E-GIUH for  
88 each flood event. First, the GIUH formulation is adapted to take into account the spatial rainfall pattern by means  
89 of replacing the width function by the rainfall width function (Emmanuel et al., 2015; Woods and Sivapalan, 1999).  
90 This improvement serves to overcome a key limitation of the GIUH, as highlighted by (Rigon et al., 2016). Second,  
91 a novel E-GIUH identification method based on observed data is developed and tested. The typical approach  
92 consists of assuming a production function and jointly calibrating the GIUH and the production function  
93 parameters; hence, results depend on the *a priori* production function. To address this problem, the original method  
94 proposed herein formulates Event-GIUH identification as an inverse problem (Menke, 2012; Tarentola, A., 2005).  
95 Inverse theory was defined by (Menke, 2012) as “a set of mathematical techniques for reducing data to obtain  
96 knowledge about the physical world on the basis of inferences drawn from observations”. Inverse techniques have  
97 been used in hydrology, e.g. by (Pan and Wood, 2013) to derive spatially distributed runoff, by (Fisher et al.,  
98 2020) for the purpose of determining spatially distributed continuous river discharge from discrete flow data, as  
99 well as by (Boudhraâ et al., 2018) to derive the hyetograph of effective rainfall from flow data. The E-GIUH is  
100 identified from the observed hydrograph and from an estimation of the hyetograph of effective rainfall. It is likely  
101 that this hyetograph influences the resulting E-GIUH. The use of an inverse algorithm makes it possible to  
102 explicitly consider the specific role of this hyetograph. It can be done by considering it as a set of parameters of  
103 the problem to solve. The algorithm is initialized by the priori information about this hyetograph which combines  
104 the estimation of the a-posteriori hyetograph and its accuracy. The inverse algorithm will give more or less  
105 importance to the a priori hyetograph according to its accuracy, and will propose an improved shape. More  
106 generally, the adopted framework is well adapted to considering the weight of data, a priori parameter values and  
107 model on the solution based on their accuracy. The proposed approach extends the domain of application of the

108 GIUH. It allows to characterize each event in terms of a specific E-GIUH that can be viewed as the signature of  
109 this event”.

110

111 Section 2 presents an adaptation of the width function-based GIUH, which takes into account the spatial rainfall  
112 variability and develops the approach employed to identify the E-GIUH from observed data, namely the  
113 hydrograph and rainfall field time series. The case study serving to test the proposed E-GIUH identification method  
114 is described in Section 3. This case study combines a set of events affecting two basins located in Southern France.  
115 Section 4 provides the application conditions of this E-GIUH identification approach, and Section 5 discusses the  
116 results obtained. Section 6 concludes the manuscript.

117

## 118 **2. Methods**

### 119 *2.1 The Event-specific Geomorphological Instantaneous Unit Hydrograph (E-GIUH)*

120 This section introduces the spatial variability of rainfall in the derivation of the Width Function-based E-GIUH  
121 (D’Odorico and Rigon, 2003; Rigon et al., 2016). The travel time of water drops and the GIUH both depend  
122 primarily on the hydrological distance  $L$ , defined as the distance to the outlet from any point on the hydrological  
123 network. Let  $w$  be the width function of the basin, defined as the portion of the basin area at the hydrological  
124 distance  $L$ , which in addition represents the transverse extent of the basin at  $L$  (Rodriguez-Iturbe and Rinaldo,  
125 1997). The spatial rainfall variability is represented by the rainfall variability along hydrological paths (Smith et  
126 al., 2005). The flow at the catchment outlet can be expressed as:

$$127 \quad Q(t) = \int_0^{L_{max}} dQ(L, t) dL \quad \text{with} \quad dQ(L, t) = A w(L) dL \int_0^t R_e(L, t - \tau) f(L, \tau) d\tau \quad (1)$$

128 with:  $dQ(L, t)$  denoting the outflow at time  $t$  from surface area  $dA = A w(L)dL$  at hydrological distance  $L$ ;  $R_e$  the  
129 effective rainfall at time  $\tau$  and at hydrological distance  $L$ ;  $L_{max}$  the maximum hydrological distance; and  $f$  the  
130 travel time distribution of water particles from  $dA$ .

131 It is assumed that the probability density function (pdf) of travel time can be modeled by the following law  
132 (Rigon et al., 2016; Rinaldo et al., 1991):

$$133 \quad f(L, t) = \frac{L}{\sqrt{4\pi D(L) t^3}} \exp \left[ -\frac{(L-U(L)t)^2}{4D(L)t} \right] \quad (2)$$

134 with  $U(L)$  and  $D(L)$  denoting the respective parameters of velocity and coefficient of dispersion (sometimes called  
135 diffusivity) of the travel time pdf. Let's note that Eq. (2) is also the (Hayami, 1951) solution of the Diffusive Wave

136 Equation (Moussa, 1997) with  $(U, D)$  standing for the mean velocity and coefficient of dispersion, respectively,  
 137 of the wave flow. The influence of rainfall spatial variability on flow conditions may explain why  $U$  and  $D$  both  
 138 depend on  $L$ .

139 The rainfall variability along flow paths can be introduced by defining the rainfall width function, as inspired  
 140 from (Smith et al., 2005):

$$141 \quad w_R(L, t) = \frac{R_e(L, t)}{\overline{R_e(t)}} w(L) \quad (3)$$

142 with  $w_R$  rainfall width function, and  $\overline{R_e(t)}$  mean value of effective rainfall over the basin at time  $\tau$ .

143 Unlike the width function, the rainfall width function does depend on time. (Emmanuel et al., 2015) showed  
 144 that the influence of spatial rainfall variability on the basin response is well explained by the deviation between  
 145 the width function and the rainfall width function associated to the pattern of rain amount during a time interval  
 146 of approximately two to three times the basin response time, which is thus close to the time of concentration. The  
 147 event rainfall width function  $w_E$  is defined over this duration; it was first introduced by (Woods and Sivapalan,  
 148 1999) to analyze the effect of spatial rainfall variability and runoff formation on catchment response. According  
 149 to these authors, it can be assumed that the spatio-temporal variability of rainfall along flow paths can be written  
 150 as the product of two independent functions, i.e.:

$$151 \quad R_e(L, t) = w_E(L) \overline{R_e(t)} \quad (4)$$

152 with  $w_E$  event rainfall width function which depends only on hydrologic distance and  $\overline{R_e}$  hyetograph of effective  
 153 rainfall which depends only on time.

154 Introducing Eq. (4) into Eq. (1) leads to the following expression of outflow:

$$155 \quad Q(t) = \int_0^{L^{max}} A w_E(L) dL \int_0^t R_e(L, t - \tau) f(L, \tau) d\tau \quad (5)$$

156 which can also be written :

$$157 \quad Q(t) = A \int_0^t \overline{R_e(t - \tau)} f_E(\tau) d\tau \quad \text{with} \quad f_E(\tau) = \int_0^{L^{max}} w_E(L) f(L, \tau) dL \quad (6)$$

158  $f_E$  is the E-GIUH associated with the flood event E. (Saco and Kumar, 2002a) stated that the pdf of travel time  
 159  $f$  can be approximated by replacing the varying parameters  $U$  and  $D$  by an equivalent network velocity ( $U_E$ ) and  
 160 equivalent hydrodynamic coefficient of dispersion ( $D_E$ ), which enable preserving the mean and variance of  $f_E$ .  
 161 They noticed that “although used as spatially invariant parameters, they are estimated to account for the nonlinear  
 162 effects that arise when varying hydrodynamic parameters”.

163 Ultimately, the expression of E-GIUH is:

$$f_E(t) = \int_0^{L_b} \frac{L w_E(L)}{\sqrt{4\pi D_E t^3}} \exp\left[-\frac{(L - U_E t)^2}{4 D_E t}\right] dt \quad (7)$$

In addition, (Rodriguez-Iturbe and Rinaldo, 1997) found that the first two moments of  $f_E$  must satisfy the following expressions:

$$E(T) = \frac{1}{U_E} E(L) \text{ and } Var(T) = 2 \frac{D_E}{U_E^2} E(L) + \frac{1}{U_E^2} Var(L) \quad (8)$$

where  $E(L)$  and  $Var(L)$  are the first two moments of the pdf of hydrological paths.

In sum, the spatial variability of rainfall can be integrated into the width function-based GIUH by replacing the width function by the rainfall width function. This formulation paves the way to determining the E-GIUH, which characterizes the basin response to each rain event forcing.

## 2.2 Principles of the E-GIUH identification process

The problem posed consists of identifying the E-GIUH, specific to flood event E that leads to the best reconstitution of the observed hydrograph at the basin outlet. This E-GIUH is defined by two parameters  $U_E$  and  $D_E$  as well as by the event rainfall width function  $w_E$ . Note that Equation (6) expresses the hydrograph as a function of both E-GIUH and the hyetograph of effective rainfall, meaning that the identification of effective rainfall and Event-GIUH are not independent of one another and moreover that the transformation of observed rainfall data fields into a hyetograph of effective rainfall might influence the identified E-GIUH. For this reason, the components of the hyetograph of effective rainfall are also considered as parameters. Nevertheless, the adopted identification algorithm (Section 4) provides the opportunity to introduce the hyetograph of effective rainfall as an “*a priori*” information to which a level of confidence is ascribed, thus making it possible to control its influence on the result. Lastly, the E-GIUH identification process calls for a model capable of combining the following equations:

i) Flow at the catchment outlet expressed as the convolution product:  $Q = \overline{R}_e * f_E(U_E, D_E)$ , written in a discretized manner:

$$Q_j = A \sum_{k=1}^{k=j} \overline{R}_{e_{j+1-k}} f_{E_k}(U_E, D_E) \quad (9)$$

with:

$$f_{E_k}(U_E, D_E) = \sum_{\gamma=1}^{\gamma=n_w} w_{R\gamma} \int_{(k-1)\Delta t}^{k\Delta t} \frac{\overline{L}_\gamma}{\sqrt{4\pi D_E \tau^3}} \exp\left[-\frac{(\overline{L}_\gamma - U_E \tau)^2}{4 D_E \tau}\right] d\tau \quad (10)$$

where:  $\mathbf{Q} = (Q_1, Q_2, \dots, Q_{m_q})$  is the vector grouping the  $m_q$  components of the event hydrograph,  $\overline{\mathbf{R}}_e = (\overline{R}_{e_1}, \overline{R}_{e_2}, \dots, \overline{R}_{e_{m_r}})$  the vector grouping the  $m_r$  components of the hyetograph of effective rainfall over the basin,



191 and  $\mathbf{w}_E = (w_{E1}, w_{E2}, \dots, w_{En_w})$  the vector grouping the  $n_w$  components of the event rainfall width function at  
 192 distances  $(L_1, L_2, \dots, L_{n_w})$ . The vector  $\mathbf{f}_E = (f_{E1}, f_{E2}, \dots, f_{Em_f})$  regroups the  $m_f$  components of the E-GIUH.

193 ii) A conservation equation stating that runoff volume at the outlet amounts to the effective rainfall:

$$194 \sum_{k=1}^{k=m_q} Q_k = A \sum_{k=1}^{k=m_r} \overline{R}_{e_k} \quad (11)$$

195 iii) The discretized form of Equations (8), which relate the parameters of the E-GIUH with the pdf of  
 196 hydrological distances, in the framework of GIUH theory:

$$197 E(T, U_E, D_E) - \frac{\bar{L}}{U_E} = 0 \quad (12)$$

$$198 Var(T, U_E, D_E) - 2 \frac{D_E}{U_E^2} \bar{L} + \frac{1}{U_E^2} V(L) = 0 \quad (13)$$

199 with:

$$200 \bar{L} = \sum_{\gamma=1}^{\gamma=n_w} w_{E\gamma} L_\gamma \text{ and } V(L) = \sum_{\gamma=1}^{\gamma=n_w} w_{E\gamma} [L_\gamma - \bar{L}]^2 \quad (14)$$

201 Moreover, the vector of parameters to identify is:  $\mathbf{p} = (U_E, D_E, \overline{\mathbf{R}}_e)$ , while the vector grouping the data  
 202 associated with Equations 9, 11, 12 and 13, used to base the identification procedure is:  $\mathbf{d}_0 =$   
 203  $(\mathbf{Q}_0, \sum_{k=1}^{k=m_r} Q_{0k}, 0.0, 0.0)$ .

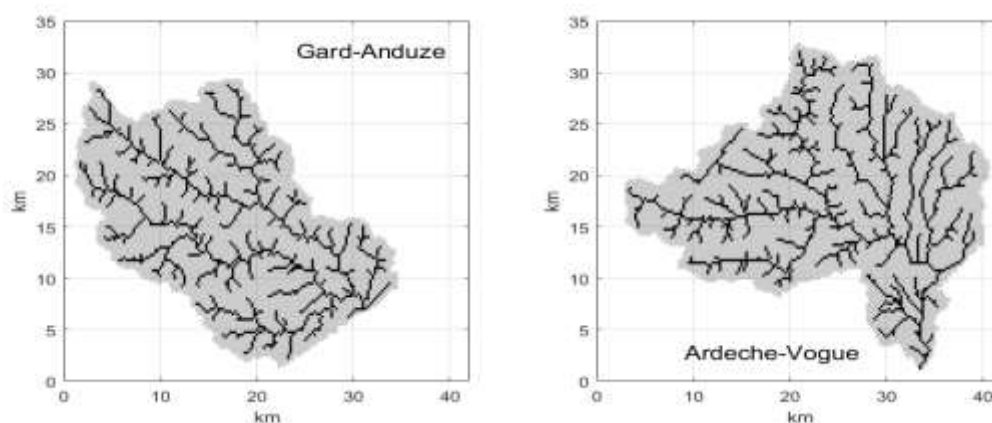
204

### 205 3. Case study and dataset

206 The Cevennes Region encompasses a medium-elevation mountain range located in the southeastern part of  
 207 France's Massif Central sector (Fig. 1). The southeastern end of this range consists of a plateau and a plain area  
 208 extending to the Mediterranean Coast. Several rivers originate in the Cevennes Mountains and cross the  
 209 intermediate plain to empty into the Rhone River or flow into the Mediterranean Sea. This region displays typical  
 210 Mediterranean climate and is subject to heavy rainfall events during the fall, causing flash floods that can result in  
 211 considerable damage and losses. The Cevennes Region is covered by a network of rain gauges at a density of  
 212 roughly 1 gauge every 150 km<sup>2</sup>, complemented by two weather radars that provide quantitative precipitation  
 213 estimates (QPE) at a high spatial (1 km x 1 km) and temporal (5 min) resolution. Hydrometeorological recordings  
 214 in this region are enhanced by the presence of the OHMCV (Cevennes-Vivarais Mediterranean  
 215 Hydrometeorological Observatory) (<http://www.ohmcv.fr>). This long-term observatory has built an integrated  
 216 hydrometeorological database of flash flood events across the Cevennes-Vivarais area. The available operational  
 217 datasets have therefore undergone a thorough quality control and can be considered highly accurate (Boudevillain  
 218 et al., 2011). The OHMCV provides several QPE products. For purposes of this study, the hourly rainfall fields of

219 1 km x 1 km spatial resolution, obtained by means of a radar - rain gauge merging technique proposed by (Delrieu  
220 et al., 2014) have been used; these fields offer a high level of accuracy compared to other QPE products.

221 The basins considered herein are: Gard at the Anduze gauging station (surface area: 545 km<sup>2</sup>), and Ardèche at  
222 the Vogüe gauging station (620 km<sup>2</sup>). Upstream of Anduze, the Gard bedrock consists mainly of schist (61%) and  
223 granite (18%). The Ardèche bedrock upstream of Vogüe is mostly granitic (72%) (Douinot et al., 2018). The  
224 hydrographic network of these two basins has been determined with the TauDem tool (Tarboton, 1997), in using  
225 a DTM at a spatial resolution of 250 m. Both basins are well documented and have been the subject of several  
226 works on rainfall-runoff modeling (Adamovic et al., 2015; Douinot et al., 2018; Moussa et al., 2007; Naulin et al.,  
227 2013; Saulnier and Le Lay, 2009; Trambly et al., 2011; Vannier et al., 2016) and flash flood forecasting (Alfieri  
228 et al., 2011; Dolcine et al., 2001).



229  
230  
231

Figure 1: Case study of the two basins studied

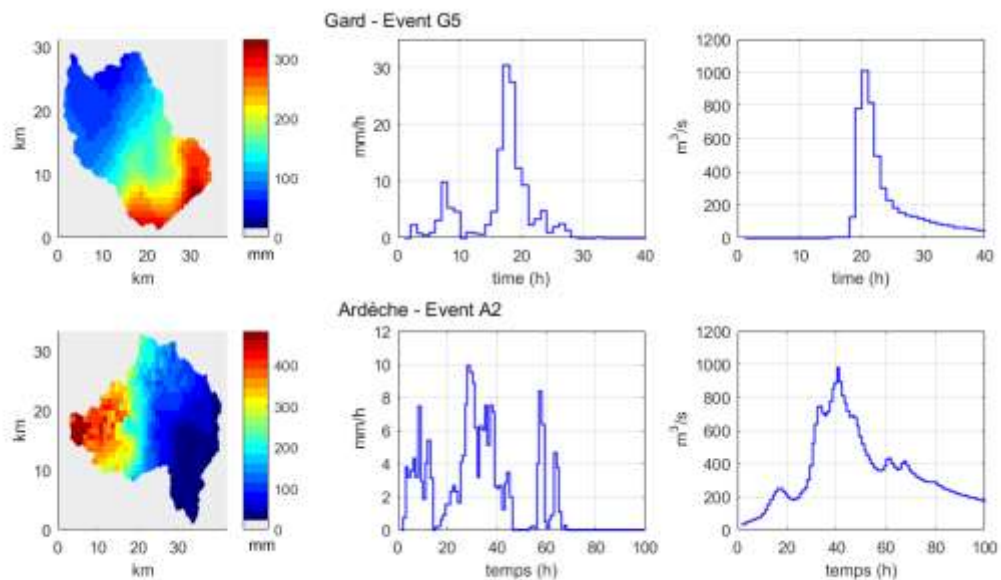
232 The QPE product covers a time period from 2011 to 2014 and includes one very intense and significant rain  
233 event in September 2002 (Delrieu et al., 2005). A sample of six flood events at each basin have been selected,  
234 comprising both rain and flow data. All these events are single-peak hydrographs, which are more easily adapted  
235 to characterizing a unit hydrograph. Some selected events occurred during long rainy periods, which explains the  
236 high flow values observed upon their initiation. The main features of these flood events are summarized in Table  
237 1. The peak flow of a two-year return period is, respectively,  $Q_2 = 630 \text{ m}^3/\text{s}$  for Gard-Anduze and  $Q_2 = 740 \text{ m}^3/\text{s}$   
238 for Ardèche-Vogüe, thus indicating that the dataset contains flow events of various magnitudes. The coefficient  
239 of variation in the spatial rainfall amount ranges from 0.08 to 1.04 for Gard-Anduze and from 0.22 to 0.76 for  
240 Ardèche-Vogüe, which confirms the varied characteristics of the selected flood events.

241  
242

Basin	Flood Event		Peak flow (m <sup>3</sup> /s)	Rainfall duration (h)	Rainfall amount (mm)	Rainfall variability (coef. var)
Gard (Anduze) 545 km <sup>2</sup>	G1	Oct 8-9, 2002	2,744	23	294.6	0.44
	G2	Oct 20-23, 2008	933	10	125.8	1.04
	G3	Oct 31 - Nov 3, 2008	1,010	61	287.8	0.25
	G4	Oct 29 - Nov 1, 2010	306	41	191.1	0.08
	G5	Sept 17-21, 2014	1,010	25	148.8	0.50
	G6	Nov 14, 2014	616	17	98.9	0.38
Ardèche (Vogüe) 620 km <sup>2</sup>	A1	Oct 20-23, 2008	953	26	158.6	0.31
	A2	Oct 31 - Nov 3, 2008	983	44	169.3	0.76
	A3	Sept 6-8, 2010	1,270	30	225.1	0.22
	A4	Dec 21-24, 2010	571	56	153.6	0.22
	A5	Oct 22-25, 2013	850	28	126.1	0.27
	A6	Oct 9-15, 2014	1,090	48	181.4	0.66

243

Table 1: Characteristics of the selected flood event



244

245 Figure 2: Examples of flood events – Map of total rainfall (left) – Hyetograph (center) – Hydrograph (right)

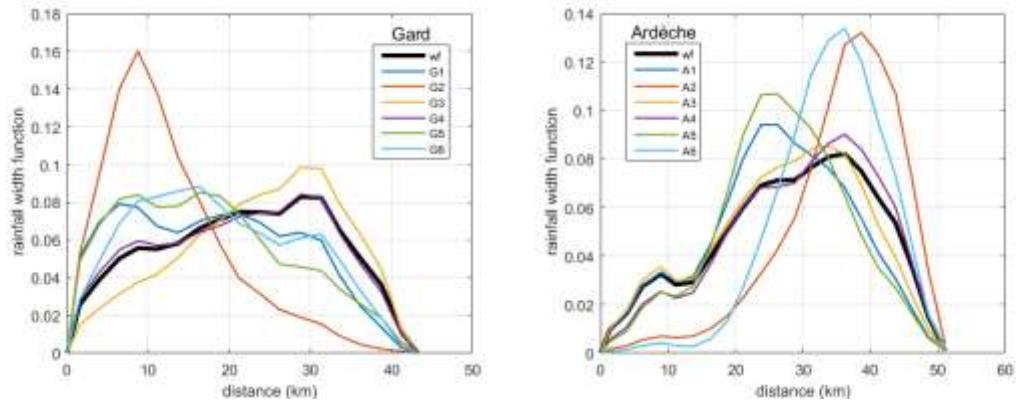
246

(The 12 flood events of the data set are displayed in supplementary material)

247

248

249



250

251 Figure 3: Rainfall width functions of the studied flood events - the left graph combines the six Gard-Anduze  
 252 Basin events and the right graph the Ardèche-Vogüe Basin event. The thick black continuous line provides the  
 253 width function of each basin.

254

255 Figure 2 illustrates one event for each basin: G5 for Gard A2 for Ardèche. The other events of each basin are  
 256 displayed in the Supplementary Information section. It can be noted that the rainfall map of Event G5 indicates  
 257 that the maximum rainfall occurs downstream, as confirmed by the corresponding rainfall width function shown  
 258 in Figure 3 (left graph). The rainfall map of Event A2 is quite different, with the maximum rainfall being located  
 259 upstream, which has been clearly confirmed by the associated rainfall width function (Fig. 3, right graph). The  
 260 rainfall width functions presented in Figure 3 reveal that most rain events feature significant variability along the  
 261 hydrological path, and moreover the events of the two basins are of a different nature. For Gard-Anduze (left  
 262 graph), all events but one are characterized by a higher rainfall amount downstream, while for Ardèche-Vogüe  
 263 most rain events are characterized by a higher rainfall amount upstream or in the central part of the basin. It is  
 264 clear that these rainfall features can influence the basin response to rainfall forcing, along with the E-GIUH  
 265 summarizing this response.

266

## 267 4. Application and results

### 268 4.1 The identification algorithm

269 It has been proposed to treat E-GIUH identification within the framework of inverse theory, as detailed in the  
 270 textbooks by (Menke, W. 2012; Tarentola, A., 2005).

271 The solution minimizes the following expression:

$$272 \Phi(\mathbf{d}, \mathbf{p}) = [\mathbf{m}(\mathbf{d}) - \mathbf{d}]^t \mathbf{C}_Q^{-1} [\mathbf{m}(\mathbf{p}) - \mathbf{d}_0] + [\mathbf{p} - \mathbf{p}_0]^t \mathbf{C}_P^{-1} [\mathbf{p} - \mathbf{p}_0] \quad (15)$$

273  $\mathbf{d} = m(\mathbf{p})$

274 where:  $\Phi$  is the likelihood function,  $t$  signifies transpose,  $m$  denotes the model relating data and parameters,  $\mathbf{p}_0$  is  
 275 the vector of *a priori* parameters,  $\mathbf{C}_p$  is the covariance matrices of residuals between truth (and unknown) and *a*  
 276 *priori* parameters, and  $\mathbf{C}_{dm}$  the covariance matrix combining data and modeling uncertainties (Tarentola, A.,  
 277 2005).

278 The statistical distributions of both  $[\mathbf{d} - \mathbf{d}_0]$  and  $[\mathbf{p} - \mathbf{p}_0]$  are assumed to be unbiased and Gaussian. Menke  
 279 (1989) demonstrated that the solution vector  $\mathbf{p}'$  satisfies:

280 
$$\mathbf{p}' = \mathbf{p}_0 + \mathbf{C}_p \mathbf{M}^t [\mathbf{M}^t \mathbf{C}_p \mathbf{M} + \mathbf{C}_{dm}]^{-1} [\mathbf{d}_0 - m(\mathbf{p}') + \mathbf{M}(\mathbf{p}' - \mathbf{p}_0)] \quad (16)$$

281 where  $\mathbf{M}$  is the matrix of (first-order) partial derivatives of model  $m$ . If model  $m$  is nonlinear, (Tarentola, A., 2005)  
 282 demonstrated that the solution can be obtained using a quasi-Newton method by means of the following algorithm  
 283 (Equation 3.51, p. 69):

284 
$$\mathbf{p}_{n+1} \approx \mathbf{p}_n - \mu_n [\mathbf{M}_n^t \mathbf{C}_p^{-1} \mathbf{M}_n + \mathbf{C}_d^{-1}]^{-1} [\mathbf{M}_n^t \mathbf{C}_{dm}^{-1} \langle m(\mathbf{p}_n) - \mathbf{d}_0 \rangle + \mathbf{C}_p^{-1} \langle \mathbf{p}_n - \mathbf{p}_0 \rangle] \quad (17)$$

285 in which  $\mathbf{P}_n$  constitutes the result of the  $n^{\text{th}}$  iteration,  $\mathbf{M}_n = \frac{\partial m(\mathbf{p}_n)}{\partial (\mathbf{p}_n)}$  is the matrix of (first-order) partial derivatives  
 286 of the model at point  $\mathbf{p}_n$ , and  $\mu_n < 1$  serves to control the convergence. More information regarding the resolution  
 287 of such nonlinear problems can be found in (Menke, 2012; Tarentola, A., 2005).

288 The *a priori* information, introduced in terms of  $(\mathbf{p}_0, \mathbf{C}_p)$ , contains the initial knowledge of the parameters to  
 289 be identified, along with the confidence ascribed to this knowledge. If the observed data are insufficient or if the  
 290 level of confidence in the data is low, then the problem becomes underdetermined and the *a priori* information  
 291 assumes a dominant role. If the problem is over-determined (i.e. availability of very high quality data in sufficient  
 292 quantity), the solution would only depend very little on the *a priori* information.

293 The next section presents the application conditions of this inverse algorithm in order to identify the E-GIUH  
 294 by focusing on the *a priori* information that initializes the identification process.

## 295 4.2 Identification algorithm – *A priori* information

### 296 4.2.1 Data and associated covariance matrix

297 The data vector, which regroups  $n_d = m_q + 3$  components,  $\mathbf{d}_0 = (\mathbf{Q}_0, \sum_{k=1}^{k=m_r} Q_{0k}, 0.0, 0.0)$ , was introduced  
 298 in Section 2.2. Its covariance matrix  $\mathbf{C}_{dm}$  characterizes the uncertainties on both the data and model equations.

299 This matrix is assumed to be diagonal, and the standard deviations associated with both the data and model  
 300 equations have been assembled in the vector  $\boldsymbol{\sigma}_{\mathbf{d}_0} = (\boldsymbol{\sigma}_{Q_0}, \sigma_{\Sigma Q_0}, \sigma_E, \sigma_V)$ , with:

$$301 \quad \boldsymbol{\sigma}_{Q_0} = (\sigma_{Q_1}, \dots, \dots, \sigma_{Q_{m_q}}) \text{ and } \sigma_{Q_{0i}} = \max[\alpha_Q Q_{0i}, \sigma_{Q_{min}}] \quad (17)$$

$$302 \quad \sigma_{\Sigma Q_0} = \alpha_{\Sigma} \left[ \sum_{k=1}^{k=m_q} Q_k \right]$$

$$303 \quad \sigma_E = \alpha_E E(T, U_e, D_e)$$

$$304 \quad \sigma_V = \alpha_V \text{Var}(T, U_e, D_e)$$

305  $\alpha_{\Sigma}, \alpha_E, \alpha_V$  are the coefficients of variation of the errors associated with Equations (11), (12) and (13), respectively.

#### 306 4.2.2 *A priori E-GIUH parameters*

307 The two E-GIUH parameters are velocity ( $U_E$ ) and the coefficient of dispersion ( $D_E$ ). Nevertheless, the E-  
 308 GIUH components also depend on the event rainfall width function ( $\mathbf{w}_E$ ), which reveals the spatial pattern of  
 309 effective rainfall. The rainfall width function is derived from radar time series data; let's note that this choice is  
 310 associated with the measured rainfall width function and not the effective rainfall width function. Such caution is  
 311 exercised in seeking to maintain the E-GIUH independent of the *a priori* effective rainfall, which may be  
 312 erroneous. Comparison tests conducted between rainfall width functions and effective rainfall width functions, by  
 313 means of the Kolmogorof-Smirnov protocol, have confirmed that the two pdfs are not significantly different.

314 The *a priori* velocity ( $U_{E0}$ ) and *a priori* hydrodynamic coefficient of dispersion ( $D_{E0}$ ) are both set by the user  
 315 and accompanied by their standard deviations of  $\sigma_U$  and  $\sigma_D$ , respectively.

316 The total coefficient of dispersion of the GIUH is expressed as follows (Rodriguez-Iturbe and Rinaldo, 1997):

$$317 \quad D_{G0} + D_{E0} = \frac{U_{E0}^2 \text{Var}(T)}{2L} \text{ and } D_{G0} = \frac{U_{E0} \text{Var}(L)}{2L} \quad (18)$$

#### 318 4.2.3 *A priori parameters: Hyetograph of effective rainfall $\mathbf{R}_e$*

319 The GIUH expresses the transformation of effective rainfall over the basin to flow at its outlet. It is worth  
 320 considering the accuracy of effective rainfall. The hydrograph of effective rainfall is incorporated into the  
 321 parameters of the inverse algorithm and moreover defined by its *a priori* components ( $\mathbf{R}_{n0}$ ) as well as the  
 322 associated error covariance matrix. The inverse algorithm offers a flexibility that enables taking the effective  
 323 rainfall into account in various ways, ranging between two extreme situations, namely:

324 i) the basin production function, giving rise to a vector grouping the *a priori* hyetograph of effective rainfall  
 325 components ( $\mathbf{R}_{e0}$ ), is considered to be accurate, and the associated covariance terms are very weak. The inverse  
 326 algorithm does not significantly modify the *a priori* hyetograph of effective rainfall, and its functioning is nearly  
 327 the equivalent to the calibration of the two parameters defining the E-GIUH;

328 ii) the production function is unknown, and the hyetograph of effective rainfall components are the parameters  
 329 to be determined. In this case, ( $\mathbf{R}_{e0}$ ) is not considered to be accurate, and the associated covariance terms are  
 330 assigned large values. The inverse algorithm identifies both the net hyetograph and E-GIUH and moreover may  
 331 be viewed as an evolution of the method developed by (Duband et al., 1993) to simultaneously identify the unit  
 332 hydrograph common to all events and the hyetograph of effective rainfall of each of them.

333 The matrix of error covariance of the effective rainfall hyetograph is defined as follows:

$$334 \text{cov}(R_{e0i}, R_{e0j}) = \sigma_{Ri} \sigma_{Rj} \exp\left[-\left(\frac{|i-j|\Delta t}{T_R}\right)^2\right] \text{ with } \sigma_{Ri} = \max(\alpha_R R_{e0i}, \sigma_{Rmin}) \quad (19)$$

335 with  $i$  and  $j$  being time indices,  $\sigma_{Ri}$  and  $\sigma_{Rj}$  the error standard deviation of  $R_{e0i}$  and  $R_{e0j}$ , respectively.  $\alpha_R$  is the  
 336 coefficient of variation in the error characterizing the hyetograph of effective rainfall,  $\beta_R$  denotes the minimum  
 337 value assigned to the error standard deviation, and  $T_R$  is the decorrelation time controlling the temporal structure  
 338 of the errors affecting successive components of the *a priori* net hyetograph.

339 The role of the *a priori* net hyetograph in the E-GIUH identification is defined by the value assigned to  $\alpha_R$ . A  
 340 very weak value, e.g. 0.05, means that the *a priori* net hyetograph is assumed to be highly accurate, whereas a  
 341 larger value, e.g. 0.2 to 0.3, indicates that the *a priori* net hyetograph is assumed to be inaccurate.

### 342 4.3 Reference E-GIUHs

#### 343 4.3.1 Data and model description

344 The flow data are assumed to be of good quality. The coefficient of variation of the flow measurement error  
 345 has been set at  $\alpha_Q = 0.10$ , with a minimum value of  $2m^3s^{-1}$ . Equation (9) is assumed to be exact and free of any  
 346 error. Equation (11), which expresses the budget equation and is assumed to be associated with a weak error  
 347 characterized by its small coefficient of variation,  $\alpha_\Sigma = 0.05$ . The theoretical GIUH framework coupled with the  
 348 introduction of the spatial rainfall variability accurately depicts the true E-GIUH (Equations 12 and 13). This  
 349 modeling error is then defined by weak coefficients of variations:  $\alpha_E = 0.05$  and  $\alpha_V = 0.05$ , respectively.

350

351 4.3.2 *A priori E-GIUH*

352 A constant *a priori* velocity has been adopted for all flow events of the same basin. The standard deviation  
 353 values retained are  $\sigma_U = 0.5ms^{-1}$  and  $\sigma_D = 1000 m^2s^{-1}$ , in order to leave a wide interval of variation with  
 354 respect to the *a priori* values. The *a priori* E-GIUH also depends on the rainfall width function  $w_{E0}$ , which has  
 355 been derived from radar time series data. Let's note once again that this choice is associated with the measured  
 356 rainfall width function and not the effective rainfall width function. Such an exercise of caution aims to maintain  
 357 the E-GIUH independent of the *a priori* effective rainfall, which may be erroneous. In addition, the comparison of  
 358 rainfall width functions and effective rainfall width functions for these case study events, by means of the  
 359 Kolmogorof-Smirnov test, have confirmed that they do not differ significantly.

360 The SCS model has been adopted to provide the *a priori* values of the net hyetograph. This classical model is  
 361 widely used, and recent tools have been developed to derive the curve number values from remote sensing data  
 362 (Ross et al., 2018; Zeng et al., 2017). The SCS model has been successfully applied to basins subject to flooding  
 363 in this Mediterranean region (Naulin et al., 2013). It is being used herein by considering a parameter,  $S_{moy}$ , that  
 364 represents the mean storage capacity of the basin for a given event. The runoff volume is defined by:

$$365 Vr = \sum_{k=1,p} \frac{(Rt_k - Ia_k)^2}{(Rt_k - Ia_k) + S_k} \quad (20)$$

366 with  $Vr$  denoting the runoff volume at the basin outlet,  $p$  the number of meshes in the basin grid,  $Rt_k$  the rainfall  
 367 amount,  $S_k$  the storage capacity, and  $Ia_k = 0.2 S_k$  the initial loss of mesh  $k$ . The CN values are then transformed  
 368 into a map of relative storage capacity, from which the storage capacity of each mesh is derived:  $S_k = S_{moy} \gamma_k$ ,  
 369 with  $\gamma_k$  being the relative storage capacity of mesh  $k$ .  $S_{moy}$  has been calibrated for each flood event so that the  
 370 effective rainfall volume is equal to the runoff volume. As runoff generated by the effective rainfall is assumed to  
 371 be the dominant process of flow generation, the base flow is removed from the observed flow values. The pre-  
 372 event base flow is the measured flow at the beginning of the rain event. At the end of the event, it is assumed that  
 373 the runoff contribution becomes negligible after the rain has stopped for a period equal to the basin time of  
 374 concentration. The post-event base flow is the flow measured at this time. It is assumed that the base flow varies  
 375 linearly between these values during the flood event. The time of concentration is estimated to be 18h for the Gard-  
 376 Anduze basin and 24 h for the Ardèche-Vogüe basin. Changing the concentration times by a few hours don't  
 377 significantly affect the obtained results. The net hyetograph ( $R_{e0}$ ) is thus deduced from the time series of hourly  
 378 effective rainfall maps.



379 For the identification of the reference E-GIUH, it is assumed that the *a priori* effective rainfall is highly  
 380 accurate. The coefficient of variation of each net hyetograph component is then given by the value  $\alpha_R = 0.10$ . In  
 381 addition,  $T_R = 2 h$  controls the temporal structure of the error on the *a priori* net hyetograph.

382 The application conditions selected to derive the reference E-GIUHs are collated in Table 2

Hydrological distance increment: $\Delta L = 2500 m$ <i>Data and model errors:</i> Error on flow: $\alpha_Q = 0.10$ Conservation of flux – Eq. (17): $\alpha_\Sigma = 0.05$ E-GIUH equation – Eq. (17): $\alpha_E = 0.05$ E-GIUH equation – Eq. (17): $\alpha_V = 0.05$ <i>A priori parameter values:</i> Velocity: $U_{E0} = 1.2 m s^{-1}$ (Gard-Anduze), $U_{E0} = 1.0 m s^{-1}$ (Ardèche-Vogüe), $\sigma_U = 0.5 m s^{-1}$ Coef. of dispersion provided by Eq. (18) $D_{E0} \approx D_{G0}/2$ and $\sigma_D = 1200 m^2 s^{-1}$ A priori net hyetograph: SCS - $\alpha_R = 0.10$ and $T_R = 2 h$
---

383 Table 2: Summary of the reference applications conditions

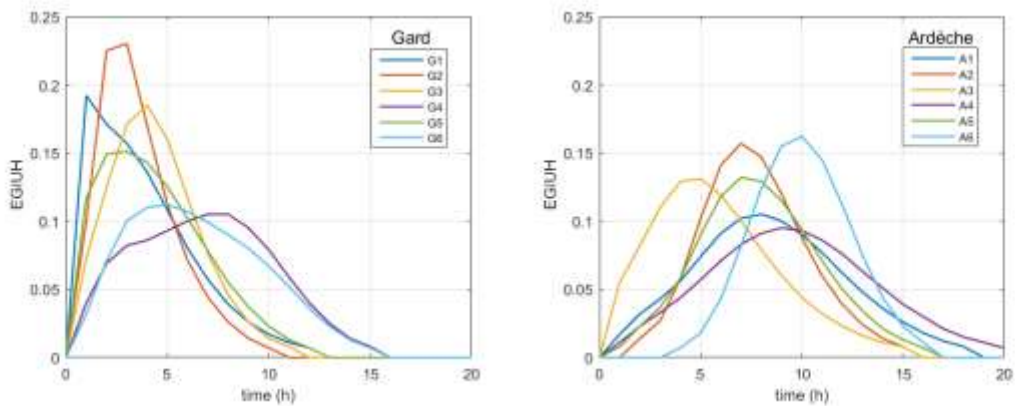
384 *4.4 Results and discussion*

385 The accuracy of the identified E-GIUH can only be evaluated indirectly. The classical Nash-Sutcliffe efficiency  
 386 criterion (denoted NSE) is used for such a purpose:

387 
$$NSE_x = 1 - \frac{\sum_{i=1}^n (x_{ref i} - x_{tes i})^2}{\sum_{i=1}^n (x_{ref i} - \bar{x})^2} \quad (21)$$

388 with  $[x_{ref i}]$  reference vector of  $n$  components of mean  $\bar{x}_{tes}$ ,  $[x_i]$  vector to be tested.

389 The E-GIUHs identified according to the reference application conditions are displayed in Figure 4.



390

391

Figure 4: Identified Event-GIUHs relative to the reference application conditions

392

393 These results have been assessed by calculating four criteria: 1)  $NSE_Q$  between observed hydrographs and  
394 hydrographs modeled using *a priori* E-GIUH and an *a priori* net hyetograph; 2)  $NSE_Q$  between observed  
395 hydrographs and hydrographs modeled using the identification results; 3)  $NSE_{Rn}$  between the *a priori* net  
396 hyetograph and the identified net hyetograph; and 4)  $NSE_{GIUH}$  between the *a priori* E-GIUH and the identified E-  
397 GIUH. These criteria are calculated for each flood event; their average value is computed for the two basins so as  
398 to provide an overview of the results obtained. These criteria have been compiled in Table 3, leading to the  
399 following comments:

400 - The identified E-GIUHs allow improving the simulation of observed hydrographs. This improvement seems  
401 as more pronounced as the identified values of  $(U_E, D_E)$  differ from the *a priori* values. The average increase in  
402  $NSE_Q$  is significant, from 0.72 to 0.83 for Gard-Anduze and from 0.65 to 0.84 for Ardèche-Vogüe.

403 - This increase primarily results from an evolution in E-GIUHs. Indeed, a comparison of the net hyetographs  
404 indicates that the *a priori* ones slightly differ from the identified ones. The average value of  $NSE_{Rn}$  equals 0.97  
405 for Gard-Anduze and 0.96 for Ardèche-Vogüe; in all cases, the criterion is above 0.92.

406 - A comparison of the *a priori* and identified E-GIUHs confirms quite well that based on the reference  
407 conditions, the identification method acts primarily on E-GIUHs. Indeed, the average values of  $NSE_{GIUH}$ , 0.74 for  
408 Gard-Anduze and 0.65 for Ardèche-Vogüe, underscore that *a priori* E-GIUHs differ considerably from identified  
409 ones.

410 Beyond these criteria, it is very interesting to note the wide diversity and wide variability of the E-GIUHs of  
411 each basin. For instance, the time to peak for Gard-Anduze flood events (left graph) ranges from one hour to seven  
412 hours, while the time to peak for Ardèche-Vogüe flood events ranges from 5 to 10 hours. These results confirm  
413 not only the influence of rainfall variability on the E-GIUH, but also the fact that the E-GIUH could be well  
414 adapted to serve as a signature characteristic of a flood event.

415

416

417

418

419

420

421

422

Basin	Flood event	<i>A priori</i> parameters		Identified parameters		Evaluation criteria			
		$U_{E0}$ (m/s)	$D_{E0}$ (m <sup>2</sup> /s)	$U_E$ (m/s)	$D_E$ (m <sup>2</sup> /s)	1 $NSE_Q$ A <i>priori</i>	2 $NSE_Q$ Identified	3 $NSE_{Rn}$	4 $NSE_{GIUH}$
Gardo (Anduze) 545 km <sup>2</sup>	G1	1.2	1,700	1.54	5,180	0.77	0.83	0.92	0.72
	G2	1.2	1,219	1.24	958	0.86	0.88	0.99	0.99
	G3	1.2	1,129	1.78	4,209	0.73	0.92	0.99	0.06
	G4	1.2	1,476	1.03	873	0.51	0.75	0.97	0.87
	G5	1.2	1,693	1.47	2,323	0.69	0.75	0.97	0.90
	G6	1.2	1,464	0.93	1,000	0.76	0.92	0.96	0.83
	Average	1.2	1,447	1.33	2,425	0.72	0.84	0.97	0.73
Ardèche (Vogüe) 620 km <sup>2</sup>	A1	1.0	970	1.00	1,548	0.80	0.89	0.96	0.98
	A2	1.0	493	1.45	2,605	0.71	0.94	0.97	-0.31
	A3	1.0	1,059	1.36	4,330	0.50	0.79	0.93	0.33
	A4	1.0	937	0.96	1,540	0.80	0.87	0.99	0.97
	A5	1.0	768	1.13	1,460	0.64	0.85	0.93	0.87
	A6	1.0	383	1.09	652	0.46	0.77	0.92	0.90
	Average	1.0	768	1.17	2,022	0.65	0.85	0.95	0.63

423

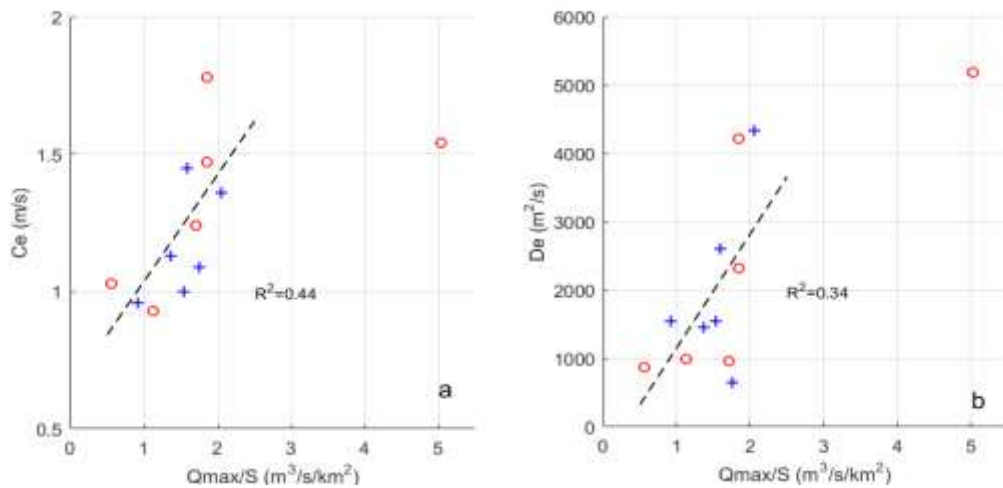
424 Table 3: Results for the 12 studied events – Comparison of *a priori* and final parameters and evaluation  
425 criteria

426

427 The *a priori* values of the E-GIUH parameters ( $U_{E0}$ ,  $D_{E0}$ ) have been chosen regardless of the event features.  
428 What conclusions can be drawn from their resulting values? For the sake of simplicity, the hydrological features  
429 of a flood event are summarized by its specific flow peak ( $q_{max}$ ), considered as an indicator of the event  
430 magnitude. The use of a specific flow peak allows regrouping the events of both catchments on the same graph in  
431 order to study a possible relationship between this indicator and the E-GIUH parameters. The scattergrams  
432 ( $U_E$ ,  $q_{max}$ ) and ( $D_E$ ,  $q_{max}$ ) with  $q_{max}$  as the specific flow peak are displayed in Figure 5. It can be observed that a  
433 significant correlation exists between the two E-GIUH parameters and the specific flow peak. Let's note that the  
434 coefficient of determination ( $R^2$ ) has been calculated without accounting for the exceptional flow event that  
435 occurred on Sept 20-21, 2002. The limited size of the dataset and the fairly low value of  $R^2$  do not offer the basis  
436 for a more detailed analysis. This result however could suggest that:

- 437 - The mean flow velocity  $U_E$  increases with the magnitude of the flood event, which appears to be logical and  
438 consistent with previous results. It is interesting to note that taking the rainfall width function into consideration  
439 does not alter this mean trend, even though it could be surmised that flood events displaying a strong rainfall  
440 variability also exhibit a stronger variability in flow velocity within the hydrological network.

441 - Results regarding the coefficient of dispersion  $D_E$  are not simple to analyze. The model equations relate  $D_E$   
 442 and  $U_E$ , which would contribute to the link between  $q_{max}$  and  $D_E$ . Similarly, the average values of  $D_E$  and  $U_E$   
 443 (Table 2) indicate a strong increase in  $D_E$  values with respect to the *a priori* values, thereby likely to generate an  
 444 accurate restitution of the observed hydrographs. Lastly, the sensitivity study (next section) suggests that this  
 445 identification procedure is not highly sensitive to  $D_E$ . Moreover, it is not yet possible to draw a clear conclusion,  
 446 and studying a larger sample of events would allow progressing in this effort.



447  
 448 Figure 5: Relationship between the specific peak flow and the E-GIUH parameters of the flood events

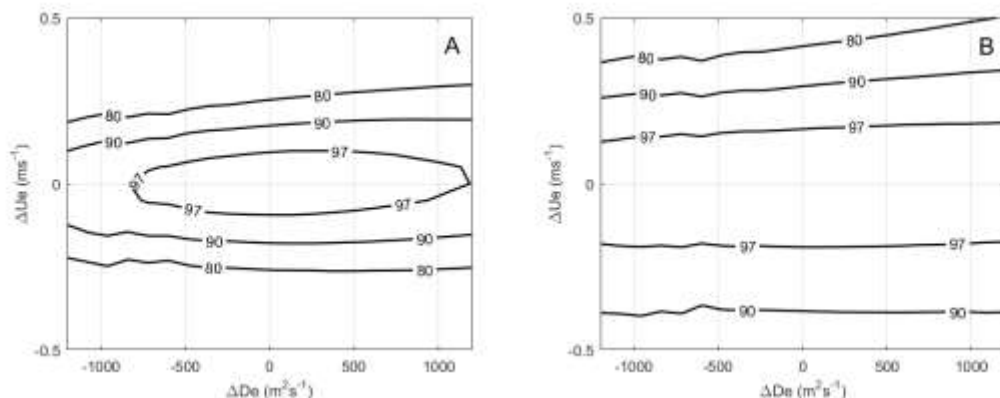
449 *4.5 Sensitivity study of the E-GIUH identification*

450 This sensitivity study addresses the influence of the application conditions on the identified E-GIUHs. This  
 451 section provides the main results and conclusions of the sensitivity study; a detailed presentation can be found in  
 452 the Supporting Information. Note that special attention has been paid to the influence of the *a priori* hyetograph  
 453 of effective rainfall.

454 *4.5.1 Sensitivity to ( $U_E$ ,  $D_E$ ) variations*

455 This test examines the influence of ( $U_E$ ,  $D_E$ ) variations on the simulated E-GIUHs and hydrographs. The E-  
 456 GIUHs and hydrographs obtained by varying ( $U_E$ ,  $D_E$ ) values with respect to the reference solution are compared  
 457 to the E-GIUHs and hydrographs of this reference solution by calculating the NSE values. Figure 5 illustrates the  
 458 results of this test, which yields two key indications: i) the influence of  $D_E$  is much weaker than that of  $U_E$ ; and ii)  
 459 the simulated hydrographs are much less influenced by ( $U_E$ ,  $D_E$ ) variations than the simulated E-GIUHs. This  
 460 latter result proves to be important, given that the identification procedure is mostly based on observed

461 hydrographs. This sensitivity study confirms that a reliable estimation of  $(U_E, D_E)$  from hydrographs is far from  
 462 being straightforward.



463  
 464 Figure 6: Sensitivity of E-GIUHs (A) and simulated hydrographs (B) to variations in  $(U_E, D_E)$

465

#### 466 4.5.2 Sensitivity of the E-GIUH to inverse algorithm application conditions

467 This part of the sensitivity study comprises: i) the confidence assigned to flow data (coefficient of variation  
 468  $\alpha_Q$ ), ii) the confidence assigned to the GIUH theoretical model (coefficients of variation  $\alpha_E$  and  $\alpha_V$ ), iii) the  
 469 influence of the *a priori* value of  $D_{E0}$ , iv) the influence of the *a priori* value of  $U_{E0}$ , and lastly v) the confidence  
 470 assigned to the *a priori* hyetograph of effective rainfall (coefficient of variation  $\alpha_R$ ). It is performed by running  
 471 the E-GIUH identification in varying one of these factors with respect to the reference conditions. The results  
 472 obtained are summarized in Table 4 and then detailed in the Appendix.

473 It is interesting to emphasize the influence of an increase of  $\alpha_R$  which controls the error variance on the *a*  
 474 *priori* hyetograph of effective rainfall. It is confirmed that an increase of  $\alpha_R$  results in an improvement of the  
 475 restitution of the observed hydrograph. The overall improvement is obtained by changes in the resulting effective  
 476 rainfall hyetograph, thus confirming the capability of this method to identify both the E-GIUH and the hyetograph  
 477 of effective rainfall ( $R_n$ ). This result might extend the application domain of the proposed method, but this subject  
 478 is out the scope of the present work which focuses on the identification of E-GIUHs.

479

480

481

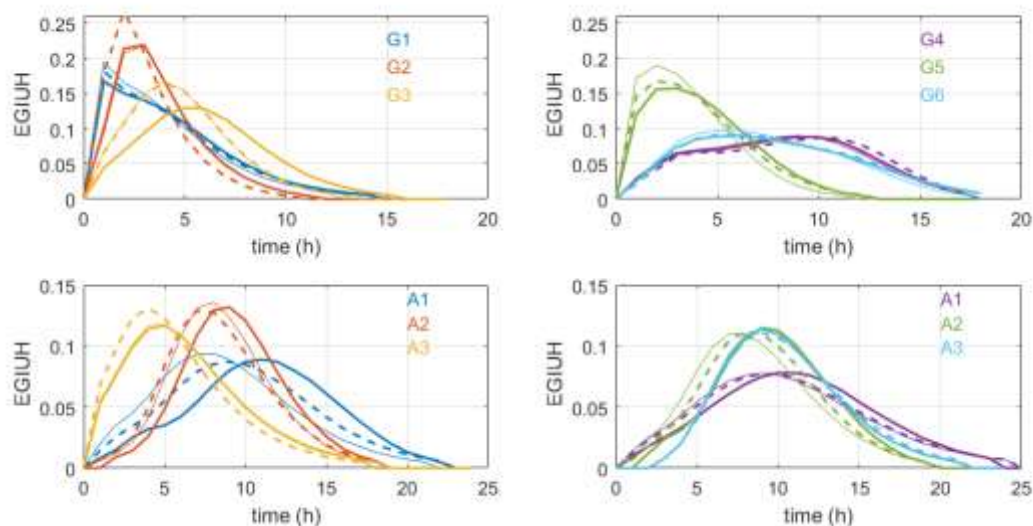
Variable	Sensitivity of the identification result	Comment
$\alpha_Q$	Strong	Decrease in $NSE_Q$ as $\alpha_Q$ increases.
$\alpha_E, \alpha_V$	Weak	Significant increase in the mean value of $D_E$ as both $\alpha_E$ and $\alpha_V$ increase.
$D_{E0}$	Weak	Increase in the mean value of $D_E$ as $D_{E0}$ increases. This result is consistent with the previous section.
$U_{E0}$	Moderate	An <i>a priori</i> underestimation seems to be more detrimental than an overestimation. A conservative <i>a priori</i> value seems to be preferable.
$\alpha_R$	Moderate to strong	The increase in $\alpha_R$ results in an increase of $NSE_Q$ . The identified E-GIUHs are only slightly affected. The overall improvement is obtained by changes in the resulting effective rainfall hyetograph.

483 Table 4: Conclusions drawn from the sensitivity study

484 4.5.3 Influence of the *a priori* hyetograph of effective rainfall

485 The previous results have been obtained by considering that the widely used SCS production function  
486 accurately represents basin operations. The question raised then is whether the choice of an *a priori* hyetograph of  
487 effective rainfall affects the identified E-GIUHs. This test is conducted by running the method with an *a priori*  
488 hyetograph of effective rainfall that's very different from the SCS one, so as to introduce a sharp contrast with the  
489 reference application conditions. The selected production function (denoted CR-PI) assumes initial losses of 20  
490 mm in each mesh of the basin, along with a constant runoff coefficient. For each flood event, this coefficient is  
491 estimated such that the effective rainfall volume is equal to the runoff volume. The choice of the *a priori* net  
492 hyetograph is the only modification adopted with respect to the reference application conditions. The two *a priori*  
493 net hyetographs are assumed to be rather inaccurate, with an error covariance  $\alpha_R = 0.25$ . It then becomes possible  
494 to compare the E-GIUHs identified based on the SCS and CR-PI production function, respectively. The *a priori*  
495 E-GIUHs turn out to be similar for both cases. The comparison results are detailed in the Supporting Information  
496 section and illustrated in Figure 6, which displays the 12 E-GIUHs obtained from the SCS (continuous line) and  
497 the CR-PI (dashed line) net hyetographs, respectively. The reference E-GIUH (thin continuous line) has been  
498 added to this comparison. The sensitivity test shows that for 9 of the 12 flood events, the identified E-GIUH is  
499 very weakly affected by the change in *a priori* net hyetograph ( $NSE_{GIUH} > 0.94$ ), only moderately affected for 2  
500 of them ( $NSE_{GIUH} = 0.88$ ) and significantly affected for 1 other event ( $A1-NSE_{GIUH} = 0.80$ ). More specifically,

501 Figure 7 indicates that the differences between the 12 E-GIUHs remain quite pronounced and much larger than  
 502 the fluctuations of each E-GIUH. In addition, it is confirmed that the identification method serves to improve the  
 503 net hyetograph, with the identified ones lying much closer than the *a priori* ones.



504  
 505 Figure 7: Sensitivity of the E-GIUHs to the production function (SCS and Cr-PI). For each of the 12 flow  
 506 events, three E-GIUH of the same color are displayed: E-GIUH obtained with the SCS ( $\alpha R = 0.25$ ; plain line);  
 507 E-GIUH obtained with CR-PI ( $\alpha R = 0.25$ ; dashed line); reference (thin line). The two upper graphs are for  
 508 Gard-Anduze and the lower for Ardèche-Vogüe

509  
 510 **5. Summary and conclusion**

511 The GIUH has become a classical representation of the rapid response of a basin when adapted to rainfall-  
 512 runoff modeling. If the GIUH depends on the morphological features of a basin, then it is also influenced by the  
 513 characteristics of rainfall patterns as well as by the variability of flow path velocities. We have therefore considered  
 514 that an Event-specific GIUH (or E-GIUH) exists that actually characterizes the catchment response under the  
 515 specific conditions of each flood event. The method proposed herein to identify this E-GIUH relies on the width  
 516 function-based GIUH (Rigon et al., 2016), as adapted to take into account the spatial variability of rainfall through  
 517 replacing the width function by the rainfall width function (Emmanuel et al., 2015; Woods and Sivapalan, 1999).  
 518 The E-GIUH is identified from data combining time series of rain fields and observed hydrographs. This E-GIUH  
 519 identification has been tested on a dataset composed of 12 flood events that occurred on catchments within the  
 520 OHMCV Observatory territory. Despite being of limited range, this evaluation has provided interesting insights,  
 521 namely:

522 - The concept of E-GIUH appears to be relevant, and moreover the proposed identification method seems easily  
523 applicable and flexible for users, who are now able to define the adapted application conditions;

524 - The E-GIUHs associated with the various flood events of a catchment display very distinct characteristics,  
525 thus confirming that E-GIUH shape depends on the GIUH model parameters, as well as on the rainfall width  
526 function, both of which are specific to the flood events;

527 - For both basins, the two E-GIUH parameters ( $U_E$ ,  $D_E$ ) lie within the range [0.9 m/s, 1.8 m/s] for  $U_E$  and [600  
528  $\text{m}^2/\text{s}$ , 5,200  $\text{m}^2/\text{s}$ ] for  $D_E$ . These two parameters appear to be correlated with the event peak flow, which serves as  
529 an indicator of flow magnitude, even though this tenuous link needs to be confirmed and warrants further  
530 investigation. The identification procedure is more sensitive to parameter  $U_E$  than to parameter  $D_E$ , mainly because  
531 the direct model is not highly sensitive to this latter parameter.

532 - The results obtained appear to be fairly robust and in most cases remain relatively independent of the *a priori*  
533 rainfall hyetograph. This result indicates that representative E-GIUHs could be derived by defining the *a priori*  
534 effective rainfall from a widely used production function and then calibrating the two E-GIUH parameters.

535

536 This work would need to be pursued in several directions, in order to improve our knowledge and develop  
537 applications relying on the E-GIUH concept, including:

538 - A more robust assessment of the proposed method seems to be a priority. This could be achieved by  
539 application to a large numbers of catchments located in various climatic zones;

540 - The E-GIUH, which is mostly based on observed data, could be considered as a signature characterizing flood  
541 events;

542 - The flood events that affect a basin stem from diverse conditions: moisture status of the basin, spatial and  
543 temporal characteristics of the rain event. The E-GIUH associated with a given basin summarizes the basin  
544 response under such conditions. An analysis of the population of E-GIUHs would pave the way to a hydro-  
545 climatological catchment response to rainfall forcing;

546 - The relatively small number of basins and flood events described here does not allow a complete assessment  
547 of the limitations of the method under all circumstances. For instance, the method might be less suitable if the  
548 rainfall influence results from moving rainfall fields interacting with the basin (Volpi et al., 2013). In addition, the  
549 method might be less efficient when the statistical framework is outside of its application domain, e.g. when the  
550 distribution of error is not Gaussian or at least unimodal, or when the *a priori* conditions are not relevant.

551 - The E-GIUH represents a signature of the basin response that could prove useful for various applications.  
552 First, it can be used to diagnose basin responses to rainfall forcing. The E-GIUH summarizes the basin response



553 that stems from diverse physiographic, climatological, and meteorological conditions, such as moisture status of  
 554 the basin and the spatial and temporal distribution of rainfall forcing. The E-GIUH signature can be used to  
 555 compare and classify basin responses for different forcing rain events, or to analyse the influence of land use and  
 556 change (e.g. recovery after wildfire) among other factors. Analysing populations of E-GIUHs that represent  
 557 various conditions opens the way to hydro-climatological studies of catchment responses. Finally, it could  
 558 contribute to improving lumped rainfall-runoff modelling through transfer function adapted to rainfall patterns.

## 559 **Nomenclature**

560	$A$	Surface area
561	$D$	Coefficient of dispersion -
562	$E$	Flood Event
563	$f(L, t)$	Probability density function of travel time to the catchment outlet
564	$f_E$	Event specific – GIUH
565	GIUH	Geomorphological Instantaneous Unit Hydrograph
566	E-GIUH	Event specific GIUH
567	$L$	Distance to catchment outlet along hydrological paths
568	$L_{max}$	Maximum hydrological distance of the basin
569	$NSE$	Nash-Sutcliffe efficiency criterion
570	pdf	Probability Density Function
571	$Q(t)$	Hydrograph at the outlet
572	$R(t)$	Hyetograph
573	$R_n(t)$	Effective rainfall, part of rainfall contributing to runoff
574	$\overline{R}_e(t)$	Areal Mean value of the effective rainfall
575	$t$	Time
576	$U$	Velocity
577	$w$	Width function at a distance
578	$w_E$	Event rainfall width function

## 579 **Acknowledgments**

580 The authors would like to express their gratitude to O.Payraastre for providing the maps of CN values for the  
 581 Cevennes Region. Pierre Kirstetter acknowledges support through the NASA Ground Validation Program award  
 582 NNX16AL23G.

- 584 Adamovic, M., Braud, I., Branger, F., Kirchner, J.W., 2015. Assessing the simple dynamical systems approach  
585 in a Mediterranean context: Application to the Ardèche catchment (France). *Hydrology and Earth*  
586 *System Sciences* 19, 2427–2449. <https://doi.org/10.5194/hess-19-2427-2015>
- 587 Alfieri, L., Smith, P.J., Thielen-Del Pozo, P.J., Beven, K.J., 2011. A staggered approach to flash flood  
588 forecasting - Case study in the Cévennes region. *Advances in Geosciences* 29, 13–20.  
589 <https://doi.org/10.5194/adgeo-29-13-2011>
- 590 Boudevillain, B., Delrieu, G., Galabertier, B., Bonnifait, L., Bouilloud, L., Kirstetter, P.E., Mosini, M.L., 2011.  
591 The Cévennes-Vivarais Mediterranean Hydrometeorological Observatory database. *Water Resources*  
592 *Research* 47, 1–6. <https://doi.org/10.1029/2010WR010353>
- 593 Boudhraâ, H., Cudennec, C., Andrieu, H., Slimani, M., 2018. Net rainfall estimation by the inversion of a  
594 geomorphology-based transfer function and discharge deconvolution. *Hydrological Sciences Journal*.  
595 <https://doi.org/10.1080/02626667.2018.1425801>
- 596 Chen, Y., Shi, P., Ji, X., Qu, S., Zhao, L., Dong, F., 2019. New method to calculate the dynamic factor–flow  
597 velocity in Geomorphologic instantaneous unit hydrograph. *Scientific Reports* 9, 1–13.  
598 <https://doi.org/10.1038/s41598-019-50723-x>
- 599 Choi, Y.-J., Lee, G., Kim, J.-C., 2011. Estimation of the Nash Model Parameters Based on the Concept of  
600 Geomorphologic Dispersion. *Journal of Hydrologic Engineering* 16, 806–817.  
601 [https://doi.org/10.1061/\(ASCE\)HE.1943-5584.0000371](https://doi.org/10.1061/(ASCE)HE.1943-5584.0000371)
- 602 Delrieu, G., Ducrocq, V., Gaume, E., Nicol, J., Payrastre, O., Yates, E., Kirstetter, P.-E., Andrieu, H., Ayrat, P.-  
603 A., Bouvier, C., Creutin, J.-D., Livet, M., Anquetin, S., Lang, M., Neppel, L., Obled, C., Parent-Du-  
604 Châtelet, J., Saulnier, G.-M., Walpersdorf, A., Wobrock, W., 2005. The catastrophic flash-flood event  
605 of 8-9 September 2002 in the Gard Region, France: A first case study for the Cévennes-Vivarais  
606 Mediterranean Hydrometeorological Observatory. *Journal of Hydrometeorology* 6.  
607 <https://doi.org/10.1175/JHM-400.1>
- 608 Delrieu, G., Wijbrans, A., Boudevillain, B., Faure, D., Bonnifait, L., Kirstetter, P.E., 2014. Geostatistical radar-  
609 raingauge merging: A novel method for the quantification of rain estimation accuracy. *Advances in*  
610 *Water Resources* 71, 110–124. <https://doi.org/10.1016/j.advwatres.2014.06.005>
- 611 D’Odorico, P., Rigon, R., 2003. Hillslope and channel contributions to the hydrologic response. *Water*  
612 *Resources Research* 39, 1–9. <https://doi.org/10.1029/2002WR001708>
- 613 Dolcine, L., Andrieu, H., Sempere-Torres, D., Creutin, D., 2001. Flash food forecasting with coupled  
614 precipitation model in mountainous Mediterranean Basin. *Journal of Hydrologic Engineering* 6.  
615 [https://doi.org/10.1061/\(ASCE\)1084-0699\(2001\)6:1\(1\)](https://doi.org/10.1061/(ASCE)1084-0699(2001)6:1(1))
- 616 Dooge, J.C.I., 1959. A General Theory of the Unit Hydrograph. *Journal of Geophysical Research* 64, 241–256.
- 617 Douinot, A., Roux, H., Garambois, P.A., Dartus, D., 2018. Using a multi-hypothesis framework to improve the  
618 understanding of flow dynamics during flash floods. *Hydrology and Earth System Sciences* 22, 5317–  
619 5340. <https://doi.org/10.5194/hess-22-5317-2018>
- 620 Duband, D., Obled, C., Rodriguez, J.Y., 1993. Unit hydrograph revisited: an alternate iterative approach to UH  
621 and effective precipitation identification. *Journal of Hydrology* 150, 115–149.  
622 [https://doi.org/10.1016/0022-1694\(93\)90158-6](https://doi.org/10.1016/0022-1694(93)90158-6)

623 Emmanuel, I., Andrieu, H., Leblois, E., Janey, N., Payrastra, O., 2015. Influence of rainfall spatial variability on  
624 rainfall – runoff modelling : Benefit of a simulation approach ? *Journal of Hydrology* 531, 337–348.  
625 <https://doi.org/10.1016/j.jhydrol.2015.04.058>

626 Emmanuel, I., Payrastra, O., Andrieu, H., Zuber, F., 2017. A method for assessing the influence of rainfall  
627 spatial variability on hydrograph modeling. First case study in the Cevennes Region, southern France.  
628 *Journal of Hydrology* 555. <https://doi.org/10.1016/j.jhydrol.2017.10.011>

629 Fatichi, S., Vivoni, E.R., Ogden, F.L., Ivanov, V.Y., Mirus, B., Gochis, D., Downer, C.W., Camporese, M.,  
630 Davison, J.H., Ebel, B., Jones, N., Kim, J., Mascaro, G., Niswonger, R., Restrepo, P., Rigon, R., Shen,  
631 C., Sulis, M., Tarboton, D., 2016. An overview of current applications, challenges, and future trends in  
632 distributed process-based models in hydrology. *Journal of Hydrology* 537, 45–60.  
633 <https://doi.org/10.1016/j.jhydrol.2016.03.026>

634 Fisher, C.K., Pan, M., Wood, E.F., 2020. Spatiotemporal assimilation-interpolation of discharge records through  
635 inverse streamflow routing. *Hydrology and Earth System Sciences* 24, 293–305.  
636 <https://doi.org/10.5194/hess-24-293-2020>

637 Goni, M., López, J.J., Gimena, F.N., 2019. Geomorphological instantaneous unit hydrograph model with  
638 distributed rainfall. *Catena* 172, 40–53. <https://doi.org/10.1016/j.catena.2018.08.010>

639 Gupta, V.K., Waymire, E., Wang, C.T., 1980. A representation of an instantaneous unit hydrograph from  
640 geomorphology. *Water Resources Research* 16, 855–862. <https://doi.org/10.1029/WR016i005p00855>

641 Hayami, S., 1951. On the propagation of Flood Waves. *Disaster Prevention Research Institute Bulletin* 1, 1–16.

642 Kirkby, M.J., 1976. Tests of the random network model, and its application to basin hydrology. *Earth Surface*  
643 *Processes* 1, 197–212. <https://doi.org/10.1002/esp.3290010302>

644 Marani, A., Rigon, R., Rinaldo, A., 1991. A Note on Fractal Channel Networks. *Water Resources Research* 27,  
645 3041–3049. <https://doi.org/10.1029/91WR02077>

646 McMillan, H., 2020. Linking hydrologic signatures to hydrologic processes: A review. *Hydrological Processes*  
647 34, 1393–1409. <https://doi.org/10.1002/hyp.13632>

648 Menke, W., 2012. *Geophysical Data Analysis: Discrete Inverse Theory MATLAB edition, Book*.  
649 <https://doi.org/10.1016/B978-0-12-397160-9.00001-1>

650 Moussa, R., 1997. Geomorphological transfer function calculated from digital elevation models for distributed  
651 hydrological modelling. *Hydrological Processes* 11, 429–449. [https://doi.org/10.1002/\(SICI\)1099-1085\(199704\)11:5<429::AID-HYP471>3.0.CO;2-J](https://doi.org/10.1002/(SICI)1099-1085(199704)11:5<429::AID-HYP471>3.0.CO;2-J)

652

653 Moussa, R., Chahinian, N., Bocquillon, C., 2007. Distributed hydrological modelling of a Mediterranean  
654 mountainous catchment – Model construction and multi-site validation. *Journal of Hydrology* 337, 35–  
655 51. <https://doi.org/10.1016/j.jhydrol.2007.01.028>

656 Naulin, J.-P., Payrastra, O., Gaume, E., 2013. Spatially distributed flood forecasting in flash flood prone areas:  
657 Application to road network supervision in Southern France. *Journal of Hydrology* 486, 88–99.  
658 <https://doi.org/10.1016/j.jhydrol.2013.01.044>

659 Olivera, F., Maidment, D., 1999. Model for Runoff Routing. *Water Resources Research* 35, 1155–1164.  
660 <https://doi.org/10.1029/1998WR900104>

661 Pan, M., Wood, E.F., 2013. Inverse streamflow routing. *Hydrology and Earth System Sciences* 17, 4577–4588.  
662 <https://doi.org/10.5194/hess-17-4577-2013>

663 Rigon, R., Bancheri, M., Formetta, G., DeLavenne, A., 2016. The geomorphological unit hydrograph from a  
664 historical-critical perspective. *Earth Surface Processes and Landforms* 41, 27–37.  
665 <https://doi.org/10.1002/esp.3855>

666 Rinaldo, A., Marani, A., Rigon, R., 1991. Geomorphological Dispersion. *Water Resources Research* 27, 513–  
667 525.

668 Rodriguez, F., Cudennec, C., Andrieu, H., 2005. Application of morphological approaches to determine unit  
669 hydrographs of urban catchments. *Hydrological Processes* 19. <https://doi.org/10.1002/hyp.5643>

670 Rodriguez-Iturbe, I., Rinaldo, A., 1997. *Fractal River Basins: Chance and Self-Organization*, Cambridge  
671 University Press. ed.

672 Rodriguez-Iturbe, I., Valdés, J.B., 1979. The geomorphologic structure of hydrologic response. *Water Resources*  
673 *Research* 15, 1409–1420. <https://doi.org/10.1029/WR015i006p01409>

674 Ross, C.W., Prihodko, L., Anchang, J., Kumar, S., Ji, W., Hanan, N.P., 2018. Global Hydrologic Soil Groups  
675 (HYSOGs250m) for Curve Number-Based Runoff Modeling.  
676 <https://doi.org/10.3334/ORNLDAAC/1566>

677 Saco, P.M., Kumar, P., 2002a. Kinematic dispersion in stream networks 1. Coupling hydraulic and network  
678 geometry. *Water Resources Research* 38, 26-1-26–14. <https://doi.org/10.1029/2001wr000695>

679 Saco, P.M., Kumar, P., 2002b. Kinematic dispersion in stream networks 2. Scale issues and self-similar network  
680 organization. *Water Resources Research* 38, 27-1-27–15. <https://doi.org/10.1029/2001wr000694>

681 Saulnier, G.-M., Le Lay, M., 2009. Sensitivity of flash-flood simulations on the volume, the intensity, and the  
682 localization of rainfall in the Cévennes-Vivarais region (France). *Water Resources Research* 45.  
683 <https://doi.org/10.1029/2008WR006906>

684 Sherman, L.K., 1932. Stream flow from rainfall by the unit hydrograph method. *Engineering News Record* 501–  
685 505.

686 Singh, P.K., Mishra, S.K., Jain, M.K., 2014. A review of the synthetic unit hydrograph: from the empirical UH  
687 to advanced geomorphological methods. *Hydrological Sciences Journal* 59, 239–261.  
688 <https://doi.org/10.1080/02626667.2013.870664>

689 Smith, J.A., Baeck, M.L., Meierdiercks, K.L., Nelson, P.A., Miller, A.J., Holland, E.J., 2005. Field studies of the  
690 storm event hydrologic response in an urbanizing watershed. *Water Resources Research* 41.  
691 <https://doi.org/10.1029/2004WR003712>

692 Smith, J.A., Baeck, M.L., Morrison, J.E., Sturdevant-Rees, P., Turner-Gillespie, D.F., Bates, P.D., 2002. The  
693 Regional Hydrology of Extreme Floods in an Urbanizing Drainage Basin. *Journal of Hydrometeorology*  
694 3, 267–282. [https://doi.org/10.1175/1525-7541\(2002\)003<0267:TRHOEF>2.0.CO;2](https://doi.org/10.1175/1525-7541(2002)003<0267:TRHOEF>2.0.CO;2)

695 Tarboton, D.G., 1997. A new method for the determination of flow directions and upslope areas in grid digital  
696 elevation models. *Water Resources Research* 33, 309–319. <https://doi.org/10.1029/96WR03137>

697 Tarentola, A., 2005. *Inverse Problem Theory*, SIAM, Society for Industrial and Applied Mathematics. ed.  
698 Philadelphia.

699 Trambly, Y., Bouvier, C., Ayral, P.A., Marchandise, A., 2011. Impact of rainfall spatial distribution on rainfall-  
700 runoff modelling efficiency and initial soil moisture conditions estimation. *Natural Hazards and Earth*  
701 *System Science* 11, 157–170. <https://doi.org/10.5194/nhess-11-157-2011>

- 702 Vannier, O., Anquetin, S., Braud, I., 2016. Investigating the role of geology in the hydrological response of  
703 Mediterranean catchments prone to flash-floods: Regional modelling study and process understanding.  
704 Journal of Hydrology 541, 158–172. <https://doi.org/10.1016/j.jhydrol.2016.04.001>
- 705 Volpi, E., Di Lazzaro, M., Fiori, A., 2012. A simplified framework for assessing the impact of rainfall spatial  
706 variability on the hydrologic response. Advances in Water Resources 46, 1–10.  
707 <https://doi.org/10.1016/j.advwatres.2012.04.011>
- 708 Wood, E.F., Sivapalan, M., Beven, K., 1990. Similarity and scale in catchment storm response. Reviews of  
709 Geophysics 28, 1–18. <https://doi.org/10.1029/RG028i001p00001>
- 710 Woods, R., Sivapalan, M., 1999. A synthesis of space-time variability in storm response: Rainfall, runoff  
711 generation, and routing. Water Resources Research 35, 2469–2485.  
712 <https://doi.org/10.1029/1999WR900014>
- 713 Yao, C., Zhang, K., Yu, Z., Li, Z., Li, Q., 2014. Improving the flood prediction capability of the Xinanjiang  
714 model in ungauged nested catchments by coupling it with the geomorphologic instantaneous unit  
715 hydrograph. Journal of Hydrology 517, 1035–1048. <https://doi.org/10.1016/j.jhydrol.2014.06.037>
- 716 Zeng, Z., Tang, G., Hong, Y., Zeng, C., Yang, Y., 2017. Development of an NRCS curve number global dataset  
717 using the latest geospatial remote sensing data for worldwide hydrologic applications. null 8, 528–536.  
718 <https://doi.org/10.1080/2150704X.2017.1297544>
- 719 Zoccatelli, D., Borga, M., Zanon, F., Antonescu, B., Stancalie, G., 2010. Which rainfall spatial information for  
720 flash flood response modelling? A numerical investigation based on data from the Carpathian range,  
721 Romania. Journal of Hydrology 394, 148–161. <https://doi.org/10.1016/j.jhydrol.2010.07.019>

## 723 **Appendix – Sensitivity study**

724 This sensitivity analysis has focused on the influence of the application conditions on the identified E-GIUHs.  
725 More specifically, it has concerned: the confidence assigned to flow data (coefficient of variation  $\alpha_Q$ ), the  
726 confidence assigned to the GIUH theoretical model (coefficients of variation  $\alpha_E$  and  $\alpha_V$ ), the influence of the *a*  
727 *priori* value of  $D_{E0}$ , the influence of the *a priori* value of  $U_{E0}$ , and lastly the influence of this error on the *a priori*  
728 net hyetograph.

729 This study has been performed by running the E-GIUH identification method while varying one of these factors  
730 with respect to the reference conditions. The influence was then assessed by calculating: i) the mean Nash  
731 efficiency criterion between the observed and resulting hydrographs ( $NSE_Q$ ), ii) the mean Nash efficiency criterion  
732 between the resulting E-GIUHs and the reference E-GIUH ( $NSE_{GIUH}$ ), and iii) the mean absolute deviation  
733 between the series of reference values of  $U_E$  and  $D_E$ , respectively. The results of this sensitivity analysis are  
734 displayed in Figure 8 and lead to the following conclusions:

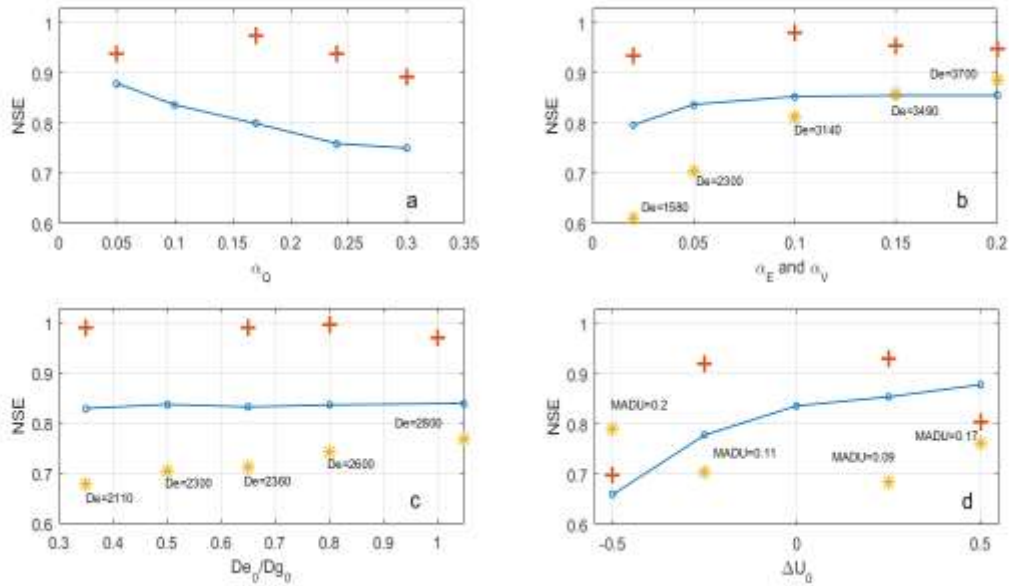
735 - *Confidence assigned to flow data (Fig. A1-a)*: The increase in the coefficient of variation  $\alpha_Q$ , which reflects  
736 a loss of confidence in the measured flow data, clearly yields a reduced quality of the resulting hydrographs (blue  
737 line). The value of  $NSE_{GIUH}$  remains above 0.94, which denotes a moderate influence on the identified E- GIUH

738 with respect to the reference one, except for  $\alpha_Q = 0.3$ , where the E-GIUH change is more pronounced ( $NSE_{GIUH} =$   
739 0.89).

740 - *Confidence assigned to the GIUH model (Fig. A1-b)*: A very strong confidence in GIUH theory ( $\alpha_E = \alpha_V =$   
741 0.02) results in a lower quality of the obtained hydrographs. This quality improves and stabilizes quickly at  
742  $NSE_Q \approx 0.85-0.86$  as  $\alpha_E$  and  $\alpha_V$  increase. The value of  $NSE_{GIUH}$  is higher than 0.95 when  $\alpha_E$  and  $\alpha_E \geq 0.05$ ,  
743 which denotes a weak influence on the identified E- GIUH with respect to the reference one. The more noteworthy  
744 effect pertains to the mean identified value of  $D_E$ , which rises from  $1560 \text{ m}^2\text{s}^{-1}$  to  $3700 \text{ m}^2\text{s}^{-1}$ , at which point  
745 the constraints on GIUH theory are relaxed without the quality criteria being significantly modified. This finding  
746 confirms that the identification of  $D_E$  is far from being straightforward based on the available observations.

747 - *Influence of the a priori value of  $D_{E0}$  (Fig. A1-c)*: The *a priori* value of  $D_{E0}$  has been increased from  $0.35 D_{G0}$   
748 to  $D_{G0}$ . The influence of this value appears to be very weak, while the values of  $NSE_Q$  and  $NSE_{GIUH}$  remain nearly  
749 constant at respectively 0.83-0.84 and 0.99. The mean identified value of  $D_E$  increases from  $2110 \text{ m}^2\text{s}^{-1}$  to  
750  $2800 \text{ m}^2\text{s}^{-1}$  with respect to  $D_{E0}$ ; this influence is less marked than that for  $\alpha_E$  and  $\alpha_V$ .

751 - *Influence of the a priori value of  $U_{E0}$  (Fig. A1-d)*: This influence is tested by defining the *a priori* value  $U_{E0} =$   
752  $U_E^* + \Delta U$ , with  $U_E^*$  being the solution obtained according to the reference application conditions, and  $\Delta U =$   
753  $[-0.5, 0.25, 0.0, 0.25, 0.5] \text{ (m/s)}$ . Note that a modification of  $U_{E0}$  also de facto affects  $D_{E0}$ . The results obtained  
754 indicate that: i) a strong underestimation of  $U_E^*$  ( $\Delta U = -0.5 \text{ m/s}$ ) cannot be corrected by the identification  
755 procedure ( $NSE_Q = 0.66, NSE_{GIUH} = 0.7$  and  $MAD_U = 0.2 \text{ m/s}$ ); ii) the situation is more satisfactory for a  
756 moderate underestimation or overestimation ( $\Delta U = \pm 0.25 \text{ m/s}$ ), for which the final GIUHs do not differ  
757 substantially from the reference solutions ( $NSE_{GIUH} = 0.92$  and  $0.93$  and  $MAD_U = 0.11$  and  $0.09 \text{ m/}$   
758  $s$ , respectively), and iii) an initial overestimation of velocity by the *a priori* value appears to be less detrimental  
759 than an underestimation.



760

761 Figure A1: Sensitivity study of the E-GIUH identification: (A) influence of  $\alpha_Q$ , (B) : influence of  $\alpha_E$  and  $\alpha_V$ ,  
 762 (C) : influence of the *a priori* value  $D_{E0}$ ; (D) : Influence of the *a priori* celerity  $U_{E0}$   
 763  $NSE_Q$  ( blue line),  $NSE_{GIUH}$  (red crosses),

764

765 - Influence of this error covariance on the *a priori* net hyetograph.

766 The E-GIUH identification has been performed by varying the value of  $\alpha_R$  from  $\alpha_R = 0.03$  (excellent  
 767 confidence in the *a priori* net hyetograph) to  $\alpha_R = 0.30$  (weak confidence). These results are illustrated in Figure  
 768 A2, in its display of the evolution in  $NSE_Q$  between the observed hydrographs and the hydrographs simulated  
 769 using the final set of parameters, in offering the following insights:

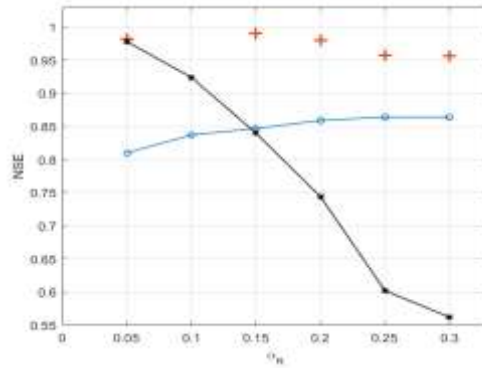
770 - The increase of  $\alpha_R$  results in an increase of  $NSE_Q$ , which rises from  $NSE_Q = 0.83$  for  $\alpha_R = 0.03$  to  $NSE_Q = 0.88$   
 771 for  $\alpha_R = 0.24$ , meaning that the set of parameters characterizing basin operations ( $\overline{R}_n, EGIUH$ ) is globally better  
 772 determined.

773 - This improvement is not correlated with significant changes in the identified E-GIUHs, which do not differ  
 774 significantly from the E-GIUH reference application conditions. Indeed, the value of  $NSE_{GIUH}$  remains above 0.97  
 775 for  $\alpha_R = 0.17$  and  $\alpha_R = 0.24$ .

776 - This improvement is mainly derived from changes in the resulting net hyetographs, in comparison with the *a*  
 777 *priori* net hyetographs, as confirmed by the value of  $NSE_{Rn}$  calculated between the *a priori* and identified net  
 778 hyetographs, which decreases from 0.99 to 0.55 as  $\alpha_R$  increases from 0.05 to 0.3.

779 This sensitivity analysis has confirmed that relaxing the constraint on the *a priori* net hyetograph yields an  
 780 overall more efficient functioning of the identification algorithm, which leads to a coupled identification of the

781  $(\overline{R}_n, EGIUH)$  couple without modifying the resulting E-GIUH by considering the *a priori* net hietograph to be  
782 accurate.



783

784 Figure A2 : Sensitivity study of the E-GIUH identification to the application conditions : influence of  $\alpha_R$

785  $NSE_Q$  ( blue line),  $NSE_{GIUH}$  (red crosses),  $NSE_{Rn}$  (black line)