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# Joint stereochemical and ab initio overview of $\mathrm{Sn}^{\mathrm{II}}$ electron lone pairs ( E ) and $\mathrm{F}^{-}(\mathrm{E})$ triplets effects on the crystal networks, the bonding and the electronic structures in a family of tin fluorides 

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#### Abstract

The stereochemistry of $5 s^{2}(\mathrm{E})$ lone pair of divalent $\mathrm{Sn}\left(\mathrm{Sn}^{\mathrm{II}}\right.$ designated by $\mathrm{M}^{*}$ ) and the lone pair triplet around the fluorine ions are examined complementarily with stereo-chemical approach and ab initio quantum investigations focusing on the electron localization and pertaining electronic structure properties, obtained within Density Functional Theory (DFT) and derived Electron Localization Function (ELF) mapping. The review completes a series of former ones focusing on the stereochemical role played by electron lone pairs LP. We start by examining LP-free $\mathrm{Sn}^{\mathrm{IV}} \mathrm{F}_{4}$ then develop on $\mathrm{Sn}^{\mathrm{II}} \mathrm{F}_{2} \mathrm{E}$ in its three crystal varieties ( $\alpha, \beta, \gamma$ ). The investigation then extends to study two mixed-valence fluorides: $\mathrm{Sn}_{2}{ }^{\mathrm{II}} \mathrm{Sn}^{\mathrm{IV}} \mathrm{F}_{6} \mathrm{E}_{2}$ and $\mathrm{Sn}^{\mathrm{II}} \mathrm{Sn}^{\mathrm{IV}} \mathrm{F}_{6} \mathrm{E}$. The lone pair presence is readily detected in the crystalline network by its sphere of influence characterized by a radius rE , and $\mathrm{M}^{*}$ - E directions; all distances are also detailed and assessed. The observations point to significant modifications of the structure which are also analyzed with the electronic density of states DOS projected over the different atomic constituents. Within the selected fluorides details of $\mathrm{Sn}^{\mathrm{II}}$ various coordination numbers ( CN ) generally indicate onesided coordination; specifically: $\mathrm{CN}=4+1 \mathrm{SnF}_{4} \mathrm{E}$ triangular bipyramid, $\mathrm{CN}=5+1 \mathrm{SnF}_{5} \mathrm{E}$ distorted octahedron (square pyramid with E roughly symmetric of its F apex) and $\mathrm{CN}=6$ octahedron [ SnE$] \mathrm{F}_{6}$. In the latter, the rotation speed of E (which increases with Z number due to relativistic effects) and the size of the F polyhedron make it favorable enough to E rotating around $\mathrm{Sn}^{2+}$ with the particularity of its transformation into a large cation $[\mathrm{SnE}]^{2+}$ with a size comparable to $\mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}$ or $\mathrm{Ba}^{2+}$.


## 1. Introduction

The use of Tin metal $(\mathrm{Sn})$ is commonly found in the canning industry for conservation and transportation for food and beverages. Chemically, upon reacting with fluorine, chlorine, sulfur, or oxygen, Sn is identified in two oxidation states: divalent Sn (II) and tetravalent Sn (IV) giving stannous and stannic compounds respectively [1]. Focusing here on $\mathrm{Sn}-\mathrm{F}$ chemical combinations, stannous fluoride $\left(\mathrm{SnF}_{2}\right)$ is most known in its effectiveness against dental caries as a result of the toxicity of the various tin fluoride species that occur in solution towards bacteria which are sometimes carcinogenic. The anti-caries mechanism of $\mathrm{SnF}_{2}$ has been investigated by determining its behavior in aqueous solution and in contact with a hydroxyl-apatite powder [2]. Further
oxidation of divalent tin fluoride leads to stannic fluoride $\mathrm{SnF}_{4}$. From the electronic structure view, the passage from divalent to tetravalent tin is due to the loss of the $5 \mathrm{~s}^{2}$ electron pair LP from $\mathrm{Sn}(\mathrm{II})$ which has been shown to have large stereochemical, electronic structure, and physical effects such in enhanced ionic mobility of fluorine in $\mathrm{PbSnF}_{4}$ [3,4]. Such LP stereo activity was also assessed in Bi (III) and Pb (II) in a review [5]. Also, mixed-valence tin fluorides with $\mathrm{Sn}(\mathrm{II})$ and $\mathrm{Sn}(\mathrm{IV})$ as $\mathrm{Sn}_{3} \mathrm{~F}_{8}$ [6] and $\mathrm{Sn}_{2} \mathrm{~F}_{6}$ [7] have been studied within the solid-state chemistry community to investigate the chemical effects of such mixtures which are further quantified herein.

We here provide an original assessment of tin fluorides electronic structures within coherent crystal chemistry and ab initio analyses. The investigations start from established crystal structures from the litera-

[^0]

Fig. 1. Perspective view of $\mathrm{SnF}_{4}$ tetrafluoride highlighting $\operatorname{SnF} F_{6}$ octahedra.

Table 1
X-ray and DFT-ELF (present work: pw) data of $\mathrm{SnF}_{4}$.
$\mathrm{SnF}_{4}$ [22] Tetragonal, Space group I4/mmm ( $\mathrm{N}^{\circ} 139$ )
Molecular weight: $194.684 \mathrm{~g}, \rho_{\mathrm{x}}=4.88\left(\mathrm{~g} / \mathrm{cm}^{3}\right)$

|  | $\mathrm{a}(\AA)$ | $\mathrm{b}(\AA)$ | $\mathrm{c}(\AA)$ | $\mathrm{V}\left(\AA^{3}\right)$ | Z | $\mathrm{rV}(\mathrm{F}, \mathrm{E})\left(\AA^{3}\right)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| RX [21] | 4.0498 | 4.0498 | 7.9375 | 130.18 | 2 | 16.3 |
| DFT-ELF [pw] | 4.05 | 4.05 | 7.94 | 130.20 | 2 | 16.3 |


| Sn-F1 eq | 2.025 | F1-F1 | 2.864 | Sn-CT | 2.042 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sn-F2 ax | 1.874 | F2-F1 | 2.759 |  |  |
| E2-F2 | 0.560 | E2-CT | 0.534 | Sn -E2 (of \{F2E2 $\left.{ }_{3}\right\}$ ) | 0.560 |
| T. rd.rect.F2 <br> Fig. $3 \mathrm{~L} / \mathrm{H} / \mathrm{R}$ | $\begin{aligned} & 2.13 / \\ & 1.50 / \\ & 0.65 \end{aligned}$ | $\varnothing$ Text. $\left\{\mathrm{F} 2 \mathrm{E} 2_{3}\right\}$ <br> blue dotted <br> circle | 1.94 | Tgyr. yellow circle - radius | 0.534 |
| E2 ellipsoid a/b/c | $\begin{aligned} & 0.49 / \\ & 0.49 / \\ & 0.76 \end{aligned}$ | rE2 <br> Sphere of influence. | 0.57 | CT-F2 | 0.168 |

[pw]: present work.
eq.: equatorial. ax.: axial. Ec2 coordinates: $x, y, z$ (Wy (32o) site), 0.9631/ 0.5135/0.7572.

CT: E2 torus center Wyckoff positions: Wy $x, y, z 0.5 / 0.5 / 0.7573$. T gyr. E2: torus gyration radius $=0.534 \AA$.
ture, followed by calculations based on the quantum density functional theory (DFT) $[8,9]$ targeting data pertaining to the electron localization description based on the electron localization function (ELF) approach by Becke and Edgecomb [10]. As a matter of fact, we have shown in former works [3, 5 and therein cited refs.] that the stereochemistry and metrics of electron lone pairs (LP) can be accurately addressed from merging together quantum chemical calculations within DFT and crystal chemistry rationale.

The purpose of this work is to apply this methodology to examine Sn LP in the three experimental varieties of $\mathrm{SnF}_{2} \alpha, \beta$ and $\gamma[11,12]$ and the above-mentioned mixed-valence fluorides. For the sake of
completeness, the electronic structures are addressed based on the site projected electronic density of states DOS; we also provide a qualitative description of chemical bonding based on the overlap populations.

## 2. Brief description of the computation methodology

Within DFT we used VASP (Vienna ab initio simulation package) code [13,14]. The projector augmented wave (PAW) method [14,15], was used with atomic potentials built within the generalized gradient approximation (GGA) scheme [16].

A major outcome from electronic structure calculations is the electronic charge density and the electron localizations which are addressed based on their localization function ELF [10]. ELF is a scheme firstly devised for Hartree-Fock quantum chemical calculations. Later on, its extension to DFT methods was done by Savin et al. [17] as based on the kinetic energy with explicit account for the Pauli Exclusion Principle: ELF $=\left(1+\chi_{\sigma}{ }^{2}\right)^{-1}$. In this expression the ratio $\chi_{\sigma}=D_{\sigma} / D_{\sigma}{ }^{0}$, where $D_{\sigma}=\tau_{\sigma}-1 / 4\left(\nabla \rho_{\sigma}\right)^{2} / \rho_{\sigma}$ and $D_{\sigma}{ }^{\circ}=3 / 5\left(6 \pi^{2}\right)^{2 / 3} \rho_{\sigma}{ }^{5 / 3}$ correspond respectively to a measure of Pauli repulsion ( $\mathrm{D}_{\sigma}$ ) of the actual system and to the free electron gas repulsion $\left(\mathrm{D}_{\sigma}{ }^{0}\right)$ and $\tau_{\sigma}$ is the kinetic energy density; $\rho$ being the electron density. A normalization of the ELF function between 0 (zero localization) and 1 (strong localization) with the value of $1 / 2$ corresponding to a free electron gas behavior enables analyzing the 2D contour maps following a code: blue zones for zero localization, red zones for full localization and green zone for ELF $=1 / 2$. Besides the 2D ELF representation, we mainly consider the metrics of 3D iso-surfaces enclosing the electrons of LP atomic constituents. We note here that regarding electron localization another choice is to use Wannier localized functions in real space (like ELF) for a chemical insight [18].

Site projected density of states PDOS analyses were carried out using scalar relativistic full potential augmented spherical wave ASW method (for more details cf [19,20]. and cited refs therein). Also when pertinent for further argumentation, the chemical bonding is addressed following Hoffmann with the COOP criterion (crystal orbital overlap population) based on the overlap integral $\mathrm{S}_{\mathrm{ij}}$; i and j being two chemical species, ex. Sn and F [21].

## 3. Tin (IV) fluoride: $\mathrm{SnF}_{4}$

### 3.1. Description and crystal chemistry rationale

There is only one tin fluoride phase with a maximum IV oxidation state, $\mathrm{SnF}_{4}$; it is a hygroscopic white powder. In its crystal structure, the fourfold axes of the $\mathrm{SnF}_{6}$ octahedra are parallel to [001] and cornershared via their entire equatorial apices parallel to (001) plane. They form $\left[\mathrm{SnF}_{4}\right]_{\mathrm{n}}$ monolayers parallel to this plane. These layers are packed along [001] with $\mathrm{c} / 2$ periodicity and a shift of $1 / 2 \vec{a}+1 / 2 \vec{b}$ (Fig. 1). The relevant X-ray data from Bork and Hoppe [22] are reported in Table 1 and the perspective view of the structure highlighting the $\mathrm{SnF}_{6}$ octahedra is represented in Fig. 1.

The $\mathrm{SnF}_{6}$ octahedra, opposite to regular $\mathrm{SnO}_{6}$ ones are flattened with shorter apical bonds Sn-F2 $(\mathrm{x} 2)=1.874 \AA$ versus longer equatorial ones $\mathrm{Sn}-\mathrm{F} 1(\mathrm{x} 4)=2.025 \AA$. The fluorine equatorial plane is perfectly tetragonal with ( 4 x ) $\mathrm{F} 1-\mathrm{F} 1=2.864 \AA$, the remaining apicalequatorial bonds being smaller ( $8 x$ ) $F-F=2.759 \AA$. It is relevant to note that both Sn atoms and F 2 sit onto fourfold rotation axis with Wy 2a 4/ $\mathrm{mmm}(0,0,0)$ for the former and Wy $4 e 4 m m$ for the second ( $W y=$ Wyckoff position).

These pieces of data are significant upon assessing the evolution of cell volumes and interatomic distances when fluorides of crystal Tin II structures are considered and particularly the role played by the $5 \mathrm{~s}^{2}$ lone pair of $\mathrm{Sn}(\mathrm{II})$ and also by $\left\{2 \mathrm{~s}^{2} 2 \mathrm{p}^{4}\right\}$ configuration of 3 LP 's (triplets)


b)
d)

a)

C)


Fig. 2. $\mathrm{SnF}_{4}$ a) Perspective view of the packing of monolayers $\left[\mathrm{SnF}_{4}\left\{\mathrm{E}_{3}\right\}_{2}\right]_{\mathrm{n}}$; b) Detail of the most important piece of the network the $\mathrm{Sn}-\mathrm{F} 2\{\mathrm{E} 3\}$ with the electronic torus (pale blue) generated by fluorine $2 s^{2} 2 p^{4}$ lone pair triplet whirling around Sn E 2 direction at CT level at $0.168 \AA$ from F 2 ( $\mathrm{Sn}-$ $\mathrm{CT}>\mathrm{Sn}-\mathrm{F} 2$ ) (CT: indicates E2 torus center). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

Fig. 3. $\mathrm{SnF}_{4}$ a) ELF section by (SnF1F2) plane which is parallel to [001] with A4 fourfold rotation axis coiling to $\mathrm{Sn}-\mathrm{F} 2$ bond. Note the symmetric high densities below F2 where E2 whirling around leaves its trace (CT middle of the symmetric Ec-Ec); Ec white-red circle exact position and circle white-blue E2 the center of ellipse section of the electronic cloud accompanying Ec. b) Planar section perpendicular to $\mathrm{Sn}-\mathrm{F} 1$ in F 1 ; note the regular electronic ring with IDC $=0.84$. c) The same type of section but perpendicular to $\mathrm{Sn}-\mathrm{F} 2$ in F 2 ; note the large ring with the highest IDC $=0.82$. d) The section passing by CT remarkably different with, in the domain of the ring with $\mathrm{IDC}=0.82$, eight domains with IDC $=0.84$ these domains perfectly described by tetragonal space group $14 / \mathrm{mmm}$ and designed by dark-grey circles in Fig. 2b. E's then move continuously along the gyration circle (yellow trace).


Fig. 4. $\mathrm{SnF}_{4}$ : Site projected DOS (top) and chemical bonding using COOP criterion (bottom) based on the overlap integrals.
which are all non-bonding in "apical" fluorine atoms.
Therefore while examining Sn fluorides it is important to focus also on the stereochemistry and the topology of $\mathrm{F}^{-}$electron pair triplets derived from ab initio calculations. For this purpose performing calculations of the electronic structure within DFT and deriving the Electronic Localization Function (ELF) on fluorine lone pair triplet within $\mathrm{SnF}_{4}$ were carried out and their experimental [22] and calculated data are listed in Table 1.

In $\mathrm{SnF}_{4}$ network there is an important feature concerning the monolayers, F1 the equatorial atom, in between two Sn atoms design a planar two-dimensional network while F2 strongly connected to Sn (Sn-F2 $=1.874 \AA$ ) points apart this plane. This is shown in Fig. 2a and b.

Two F2 levels (F2z and F2a) pertaining to two successive $\mathrm{SnF}_{4}$ layers do not interpenetrate and show a thin interspace of 0.221 A (F2z ( $z=0.7361$ ) and F2a ( $z=0.7639$ ) left to F-F interactions.

Therefore it was important to localize precisely the lone pair triplet $\left\{\mathrm{E}_{3}\right\}$ potentially associated with F 2 atoms to understand the $\left[\mathrm{SnF}_{4}\right]_{\mathrm{n}}$ layer packing. Note that we have shown the stereochemical importance of $\{\mathrm{E}\}_{3}$ triplets whirling around their atom in preceding compounds like $\mathrm{XeF}_{2} \mathrm{E}_{3}$ [23], $\mathrm{OF}_{2} \mathrm{E}_{8}$ or $\mathrm{Cl}-\mathrm{FE}_{3}$ [24] as revealed by similar DFT-ELF calculations.

### 3.2. Electron localization function ELF

The $\{\mathrm{E}\}_{3}$ triplets around F 2 z were derived and refined from ELF data. So in a first attempt, a search of a maximum E 2 z density around F 2 z in the three-dimensional electron localization was done and E2z coordinates determined and refined. These coordinates correspond to the general position Wyckoff position Wy 32 o $x, y, z$ (see Table 1). Fig. 3a shows a section of $\mathrm{SnF}_{4}$ layer by a plane SnF 1 F 2 ; it gives information of paramount importance concerning the two independent crystallographic sites of F atoms. F1 assuming a connection of Sn atoms in a square net shows an ellipsoid well centered on it, and confirmed by a section in Fig. 3b where a regular ring of iso-density curve IDC $=0.84$ is centered on F1 (IDC = isodensity curve). Then F2 appears immediately more complex in Fig. 3a with two symmetric maxima (whitered) circles showing a line perpendicular to $\mathrm{Sn}-\mathrm{F} 2$ but clearly noncentered on F2 but in CT onto the fourfold axis.

After space group symmetry operations the triplet of lone pairs around $\mathrm{F} 2 \mathrm{z}\{\mathrm{E} 2 \mathrm{z}\}_{3}$ shows eight equivalent positions (marked by dark grey circles - see Fig. 2a) around the fourfold rotation axis, forming a

Table 2
Crystallographic [11] and DFT -ELF [pw] data of $\alpha \mathrm{SnF}_{2} \mathrm{E}$.
$\alpha \mathrm{SnF}_{2}-[11]$ Monoclinic - Space group C2/c ( $\mathrm{N}^{\circ} 15$ ) - Molecular weight: $156.686-\rho_{\mathrm{x}}=4.88\left(\mathrm{~g} / \mathrm{cm}^{3}\right)$.

|  | a ( $\AA$ ) | b ( A $^{\text {) }}$ | c (Å) | $\beta\left({ }^{\circ}\right)$ | $\mathrm{V}\left(\AA^{3}\right)$ | Z | $\mathrm{rV}(\mathrm{F}, \mathrm{E})\left(\AA^{3}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Crystal [11] | 13.3532 | 4.9073 | 13.7860 | 109.29 | 852.66 | 16 | 17.8 |
| DFT-ELF [pw] | 13.3532 | 4.910 | 13.786 | 109.30 | 854.40 | 16 | 17.8 |
| Interatomic distances $(\AA)$ \& angles $\left.\left({ }^{\circ}\right)-1\right)$ crystal - 2) ELF analyses |  |  |  |  |  |  |  |
| 1) Sn1-F2 eq $2.102 \quad$ Sn2-F1ap $2.048 \quad$ 86.7 |  |  |  |  |  |  |  |
| 2) | Sn1-F3c eq | 2.057 | Sn2-F1 |  | 2.386 | $\angle \mathrm{F} 3 \mathrm{iSn} 1 \mathrm{~F} 4 \mathrm{a}$ ax | 142.7 |
|  | Sn1-F4a ax | 2.156 | Sn2-F2 |  | 2.197 | $\angle \mathrm{Sn} 1 \mathrm{~F} 2 \mathrm{Sn} 2$ | 172.0 |
|  | Sn1-F3i ax | 2.671 | Sn2-F4 |  | 2.276 | $\angle \mathrm{Sn} 2 \mathrm{~F} 4 \mathrm{Sn} 1 \mathrm{a}$ | 131.3 |
|  | F1ap- F1 | 2.890 | Sn2-F3 |  | 2.494 | F3i-F3c | 2.737 |
|  | Sn1-E1 | 0.86 | Sn2-E2 |  | 0.99 | $\angle \mathrm{E} 2 \mathrm{Sn} 2 \mathrm{~F} 1$ ap | 175.2 |
|  | E1-F2 eq | 2.45 | E2-F1 |  | 2.70 |  |  |
|  | E1-F3c eq | 2.90 | E2-F2 |  | 2.60 |  |  |
|  | E1-F4a ax | 2.55 | E2-F3 |  | 2.83 |  |  |
|  | E1-F3i ax | 3.00 | E2-F4 |  | 2.69 |  |  |
|  | E1a-E2 | 2.55 | E2-E2a |  | 2.91 |  |  |
|  | E1 ellipsoid a/b/c | 1.27/1.14/0.80 | E2 ellipsoid a/b/c |  | 1.30/1.10/0.84 | rE1 | 1.05 |
|  |  |  |  |  |  | rE2 | 1.06 |

eq: equatorial; ax: axial. Ec coordinates: 0.1205/0.1476/0.4145 (Ec1); 0.0624/0.3442/0.1814(Ec2).
$\mathrm{E} \mathrm{a} / \mathrm{b} / \mathrm{c}$ ellipsoid size - rE: radius of the sphere of influence.
$\mathrm{rV}(\mathrm{F}, \mathrm{E})$ : reduced volume $=$ cell volume divided by number of $\mathrm{F}+\mathrm{E}$.


Fig. 5. Perspective view along [010] direction of a three-dimensional network of $\alpha \mathrm{SnF}_{2}$. Sn 1 (blue circle) with $\mathrm{CN}=4+1$ shows a triangular bipyramid $\mathrm{Sn}^{2} \mathrm{~F}_{4} \mathrm{E} 1$. Sn 2 (blue-red circle) with $\mathrm{CN}=5+1$ is inside a distorted octahedron $\mathrm{Sn}_{2} \mathrm{~F}_{5} \mathrm{E}_{2} . \mathrm{Sn} 2 \mathrm{~F}_{5} \mathrm{E} 2$ designs a distorted octahedron. Sn2-F1ap the shortest bond is easily recognized by its red stick. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)


Fig. 6. $\alpha-\operatorname{SnF}_{2}$ a) ELF section of the equatorial plane of $\mathrm{Sn}_{1} \mathrm{~F}_{4} \mathrm{E}$ TBP shows the presence of $\mathrm{E} 1 ; \mathbf{b}$ ) Ec1F3cF2 plane allowed to get some geometric parameters of E1 in this equatorial EcF3cF2 triangular base. c) The axial plane Sn1F4aF3i shows a lone pair section less deformed. d) The section based on Ec1F4aF3i gives the last parameters of the so-called ellipsoidal E1 lone pair form (see Table 1).


Fig. 7. $\alpha \mathrm{SnF}_{2 .}$ a), b), c), d) ELF sections depicting planes with diagonal F2F3 and F1F4 of the fluorine square pyramid with Sn2 and E2. e) plane containing the Ec2-Sn2-F1ap the pseudo fourfold axis of the ${\mathrm{Sn} 2 \mathrm{~F}_{5} \mathrm{E} 2 \text { octahedron, also showing one section of } \mathrm{E} 2 \text { (pale blue ellipse). f) A planar section Ec2F2F4 showing another section }}^{2}$ of E2 giving a second parameter set of lone pair ellipse (pale blue). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)
circle which center CT on fourfold axis shows E2z coordinates clearly of center from F 2 z further from $\mathrm{Sn}(\mathrm{CT}-\mathrm{F} 2=0.168 \AA, \mathrm{Sn}-\mathrm{CT}>\mathrm{Sn}-\mathrm{F} 2 \mathrm{z}$ by $0.221 \AA$ ). So important to note that if the layers $\left[\mathrm{SnF}_{4}\right]_{\mathrm{n}}$ along [001], bordered by F2 do not interpenetrate, leaving an "empty" two-dimensional space, in fact, this space is filled up by two E2 layers, E2z and E 2 a , therefore with a sequence $\mathrm{F} 2 \mathrm{z} / \mathrm{E} 2 \mathrm{a} / \mathrm{E} 2 \mathrm{z} / \mathrm{F} 2 \mathrm{a}$ and $\Delta(\mathrm{F} 2 \mathrm{z}-$ $\mathrm{E} 2 \mathrm{a})=0.052 \AA, \Delta(\mathrm{E} 2 \mathrm{a}-\mathrm{E} 2 \mathrm{z})=0.116 \AA$ and $\Delta(\mathrm{E} 2 \mathrm{z}-\mathrm{F} 2 \mathrm{a})=0.052 \AA$. The $\left\{\mathrm{E}_{3}\right\}$ triplet, in principle, cannot accept a fourfold axis, so, the best solution is to consider that the three doublets are whirling around it
(drawn as a torus including all the eight dark-grey circles (Fig. 2a and b)). Now the $\left\{\operatorname{SnF}_{4}\left\{\mathrm{E}_{3}\right\}_{2}\right\}$ n layers are held together by these E 2 z and E2a which interpenetrate. This association cannot be very strong and it is not surprising to note its high hygroscopicity which makes it difficult to handle, but in return its high reactivity can be directly reliable to these (001) planes whose surface presents very active whirling electron doublets being capable to play as chemical scissors in contact with another material.

Fig. 2b shows the detail of $\mathrm{Sn}-\mathrm{F} 2\left\{\mathrm{E}_{3}\right\}$ bonding. E lone pair

Table 3
X-ray and DFT-ELF data of $\beta$ SnF2E.
$\beta \mathrm{SnF}_{2} \mathrm{E}$ - [11] Orthorhombic - Space group $\mathrm{P}_{1} 2_{1} 2_{1}\left(\mathrm{~N}^{\circ} 19\right)$ - Phase transition 339K. Molecular weight: $156.686-\rho_{x}=5.25\left(\mathrm{~g} / \mathrm{cm}^{3}\right)$.

|  | a (Å) | b (Å) | c (Å) | $\mathrm{V}\left(\AA^{3}\right)$ | Z | $\begin{aligned} & \text { rV(F,E) } \\ & \left(\AA^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| RX [3] | 4.9889 | 5.1392 | 8.4777 | 217.36 | 4 | 18.1 |
| DFT-ELF | 4.8030 | 5.1300 | 8.0460 | 198.25 | 4 | 16.5 |
| Interatomic distances ( A ) \& angles ( ${ }^{\circ}$ ) - DFT - ELF analyses -* average |  |  |  |  |  |  |
| Sn-F1 ap | 2.131 | Sn-F2 | 2.358 | Sn-F*eq |  | 2.379* |
| Sn-F1a | 2.336 | Sn-F2c | 2.668 | F1ap-F* |  | 2.888* |
| Sn-F2b | 2.153 | F1a-F2b | 3.122 | $\angle \mathrm{F} 1 \mathrm{apSnF}$ * |  | 79.5* |
| F2b-F2 | 2.862 | F2-F2c | 3.868 | $\angle \mathrm{ESnF} *$ |  | 101.1* |
| F2cF1a | 3.386 | F1-F1a | 2.823 | $\angle \mathrm{ESnF} 1 \mathrm{ap}$ |  | 162.7 |
| Sn - E | 1.019 | Ec ... Eb | 2.941 | E-F* |  | 2.756* |
| E ellipsoid a/b/c |  | 1.13/1.07/1.00 |  | rE |  | 1.07 |

Eq.: quadrilateral equatorial. $\mathrm{F}^{*}$ equatorial for averages.
Ec coordinates: 0.9643/0.3917/0.3368.
$\mathrm{E} \mathrm{a} / \mathrm{b} / \mathrm{c}$ ellipsoid size - rE: the sphere of influence.
dimension has been evaluated with its center dark-grey surrounded by an electronic cloud in form of an ellipsoid (pale blue ellipse, a/b/c parameters derived from Fig. 3a,c,d). It is reasonable to postulate that the three E's would be separated by $120^{\circ}$. In Fig. 3d the ring of IDC $=0.82$ E's leaves eight preferential spots of various sizes with IDC $=0.84$ during their whirling around Sn-CT axis. $\left\{\mathrm{E}_{3}\right\}$ triplet is set into a torus whose size and gyration circle have been precisely delimitated. In the torus E's are reasonably separated by $120^{\circ}$; three green radii (green sticks) being drawn to note that during the jumps of E from one large density "island" to another the three sticks are roughly
continuously pointed onto a domain of maximum density $\operatorname{IDC}=0.84$. So the whirling around A4 axis of E's is self-propelling to overcome a potential little difference when $\left\{\mathrm{E}_{3}\right\}$ doublets jump from one IDC domain to another (at the vicinity of $45^{\circ}$ the symmetric domains with $\operatorname{IDC}=0.84$ are reduced) .

### 3.3. Electronic density of states and chemical bond

The upper panel of Fig. 4 shows the site-resolved projected DOS (density of states) PDOS projected on Sn and the two fluorine sites Feq. (F1) and Fap. (F2z). In this plot and all the following ones, the zero of energy is with respect to the top of the valence band (VB) at $\mathrm{E}_{\mathrm{V}}$. This is why VB energies are negative whereas those of the empty conduction band (CB) are positive. The energy gap between VB and CB amounts to 4 eV . Then the tetrafluoride can be qualified as a wide gap insulator. The DOS in the VB spans two regions from -7 to -4 eV for low energy lying s-like states and from -4 eV up to $\mathrm{E}_{\mathrm{V}}$ for p-like states. In the former region, there can be seen quite similar Sn and F-eq (F1) PDOS skylines, which are different from those of Fap showing lower magnitude. This is also observed for the p-like states for the Sn-Feq (F1) albeit with much larger intensity for $F$ states especially for Fap (F2z) which show the largest intensity especially at the top of VB.

The lower panel shows the comparative bonding between Sn and the two F sites. The $\mathrm{Sn}-\mathrm{F} 2 \mathrm{z}$ (equatorial fluorine) bonding is clearly stronger especially around -4 eV in spite of negative antibonding COOP between -2 and the top of VB. Oppositely Sn-Fap. COOPs are lower in intensity but keep bonding (positive COOP) up to VB-top. This highlights the nonbinding character of the intense states of Fap. which are actually responsible for the development of tori around F as shown in Fig. 2.


Fig. 8. a) The $\beta \mathrm{SnF}_{2}$ three-dimensional network built up by $\left[\mathrm{SnF}_{5} \mathrm{E}\right]$ octahedra sharing apices but the E one; the apical bonds Sn-F1ap opposite to Sn-E are shown by red sticks. b) A projection onto (010) plane allows to enlighten the tetramer $\left[\mathrm{Sn}_{4} \mathrm{~F}_{4}\right]$ shaded in pale green and the presence of two Sn-F1ap over the eight $\mathrm{Sn}-\mathrm{F}$ surrounding it; worthy to note that the green tetramer $\left[\mathrm{Sn}_{4} \mathrm{~F}_{4}\right]$ is centered around a twofold screw axis developing a channel welcoming two lone pairs sites (E and Ec). . (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)


Fig. 9. $\beta \mathrm{SnF}_{2}$. a) ELF data section by F1ap-Sn-Ec plane underlines E position on the line of F1ap-Sn apical bond. b) EcF2bF2c and the presence F1ap trace are roughly in the same plane. c) \& d). These sections show that Sn-F1a, F2, F2b bonds are linked by the continuity of electron density while Sn-Fc clearly longer is attracted by two Sn atoms (Fig. 9d). e) A section in the double endless chain of E in the tetramer channel depicted in Fig. 9b f) The typical one-sided $\mathrm{CN}=5+1$ of tin in the form of distorted octahedron $\mathrm{SnF}_{5} \mathrm{E}$ with Sn (II) and its E being opposite to F1ap.

## 4. Tin (II) fluorides

## 4.1. $\alpha S n F_{2}$

Focusing firstly on the base centered monoclinic difluoride $\alpha \mathrm{SnF}_{2}$, the structure shows all atoms at (8f) Wyckoff positions with two different Sn and four F . Cell data are reported in Table 2; same atomic coordinates for all atoms in both X-ray and DFT-ELF data.
$\alpha \mathrm{SnF}_{2}$ exhibits an original three-dimensional network of two tin atoms occupying independent crystallographic sites $\operatorname{Sn} 1$ and $\operatorname{Sn} 2$. Moreover both Sn atoms show different coordination type with fluorine atoms both distorted and one-sided, Sn 1 with $\mathrm{CN}=4+1$ making a fluorine triangular bipyramid $\mathrm{Sn} 1 \mathrm{~F}_{4} \mathrm{E} 1$ the lone pair sitting at the apex of equatorial triangle, while Sn 2 with $\mathrm{CN}=5+1$ exhibits an octahedron $\mathrm{Sn} 2 \mathrm{~F}_{5} \mathrm{E} 2$, E2 being at opposite apex of the summit of the fluorine square pyramid. A perspective view of $\alpha \mathrm{SnF}_{2}$ along [010] is

Table 4
X-ray [12] and DFT-ELF data of $\gamma \mathrm{SnF}_{2} \mathrm{E}$.
$\gamma \mathrm{SnF}_{2} \mathrm{E}$ - [12] Tetragonal - Space group $\mathrm{P} 4_{1} 2_{1} 2\left(\mathrm{~N}^{\circ} 92\right)$
Phase transition $\sim 460 \mathrm{~K}$. - Molecular weight: $156.686-\rho_{\mathrm{x}}=4.64\left(\mathrm{~g} / \mathrm{cm}^{3}\right)$.

|  | $\mathrm{a}(\AA)$ | $\mathrm{b}(\AA)$ | $\mathrm{c}(\AA)$ | $\mathrm{V}\left(\AA^{3}\right)$ | Z | $\mathrm{V}(\mathrm{F}, \mathrm{E})\left(\AA^{3}\right)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| X-ray [3] | 5.0733 | 5.0733 | 8.4910 | 218.54 | 4 | 18.2 |
| DFT-ELF [pw] | 5.130 | 5.130 | 8.516 | 224.12 | 4 | 18.7 |

Interatomic distances ( $\AA$ ) and angles ( ${ }^{\circ}$ ) - DFT - ELF analyses -* average

| Sn-Fa, Fb eq | 2.115 | Fc-Fa $=$ Fd-Fb | 2.911 | $\angle$ Fa-Sn-Fb eq | 91.3 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sn-Fc, Fd ax | 2.327 | Fc-Fb $=$ Fd-Fa | 2.907 | $\angle$ Fc - Sn-Fd ax | 156.1 |
| Sn-E | 0.97 | E-E | 3.530 |  |  |
| E-Feq | 2.878 | E-Fax | 2.700 | Mean E-F* | $2.789^{*}$ |
| E ellipsoid a/b/c | $1.24 / 1.14 / 0.95$ |  | rE | 1.103 |  |

eq:equatorial; ax: axial. $\mathrm{F}^{*}$ equatorial for averages.
Coordinates: E: $0.6367 / 0.3633 / 0.25$. Sn: $0.5029 / 0.4971 / 0.25$. F: $0.1375 /$ 0.2643/0.1691.
$\mathrm{E} a / \mathrm{b} / \mathrm{c}$ ellipsoid size - rE: the radius of the sphere of influence.
given in Fig. 5.
All coordination details of both Sn 1 and Sn 2 are summarized in Table 2 and each polyhedron is shown in the right part of Fig. 5. Sn1 exhibits a triangular bipyramid (TBP) Sn1F $\mathrm{F}_{4} \mathrm{E} 1$ with four fluorine atoms one-sided and a lone pair E1 at the apex of the equatorial plane (F2F3cE). The TBP Sn1F2F3cF4aF3iE2 shows two strong covalent
equatorial bonds as reported in Table 2 delimitating the equatorial base (average Sn1-F* $=2.080 \AA$ ), one axial bond Sn1-F4a being slightly bigger ( $+0.08 \AA$ ) than Sn1-F* while the second Sn1-F3i introducing more distortion with $0.52 \AA$ elongation. The lone pair E1 with Sn1$\mathrm{E} 1=0.862 \AA$ appears slightly below the equatorial plane Sn1F2F3c and the average distance E1-F* $=2.73 \AA$.

Sn 2 with its lone pair E2, is outside a square pyramid formed by five fluorine atoms F1apF1F2F3F4, the lone pair E2 being opposite to the apical fluorine (F1ap) ( $\angle \mathrm{E} 2 \mathrm{Sn} 2 \mathrm{~F} 1 \mathrm{ap}=175.2^{\circ}$ ). Sn2 below the base of the square pyramid is inside a distorted octahedron.

Four Sn and four F atoms are formed around twofold A 2 axis a fourfold ring $\left[\mathrm{Sn}_{4} \mathrm{~F}_{4}\right]$ shaded in yellow for clarity. $\alpha \mathrm{SnF}_{2}$ develops a tunnel along [010] occupied by E2 lone pairs, E1 being close to its wall. It also designs the skeleton of $\left[\mathrm{Sn}_{4} \mathrm{~F}_{8}\right]$ tetramer which results from solid $\mathrm{SnF}_{2}$ sublimation. Worthy to note that $\left[\mathrm{Sn}_{4} \mathrm{~F}_{4}\right]$ rings are held together along [100] and [010] by fluorine corner-sharing F1, F1ap, F3 and F3i of the ${\mathrm{Sn} 2 \mathrm{~F}_{5} \mathrm{E} 2 \text { octahedra and along the third direction by a couple of }}^{2}$ Sn1F $\mathrm{F}_{4} \mathrm{E} 1$ triangular bipyramids sharing an edge F3c-F3i also corner shared with ${\mathrm{Sn} 2 \mathrm{~F}_{5} \mathrm{E} 2 \text { octahedra. }}^{2}$

### 4.1.1. Electron localization function

Looking to lone pairs Sn1-E1 and Sn2-E2 distances a deformation of the first one is noted which can be related to its surrounding being squeezed close to the center of symmetry in a quadrilateral tunnel formed along [010] by F2F4aF3cF3i.

E1 lone pair domain, marked by its electronic cloud covers Sn1; it appears "blown" towards F3c direction by fluorine network (Fig. 6a). Therefore sections based on Sn1, Ec1 and associated fluorine atoms of equatorial and axial planes of TBP (Sn1F2F3cF4aF3iE2) have shown in


Fig. 10. a) View of $\gamma \mathrm{SnF}_{2}$ three-dimensional network built up by [ $\mathrm{SnF}_{4} \mathrm{E}$ ] TBP's sharing all fluorine apices; b) Detail of one-sided coordinated Sn atom to fluorine atoms making a triangular bipyramid [ $\mathrm{SnF}_{4} \mathrm{E}$ ] (equatorial bonds in red). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)


Fig. 11. $\gamma \mathrm{SnF}_{2}$. a) b) ELF sections showing the electronic density of equatorial and axial planes of $\mathrm{SnF}_{4} \mathrm{E}$ TBP. E (white blue circle) marks the center of the elliptic section of the electronic cloud around the lone pair core Ec (max. isodensity curves IDC white red circle). c) d) Sections EcFaFb and EcFcFd allow to check the Ec coordinates and to show two sections at $90^{\circ}$ showing the influence of F atoms on the electronic cloud testifying its plasticity. Refinement of Ec coordinates shows a perfect set up with isodensity curves. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)
these ELF sections the possibility to settle E1. We notice that E1 (blue ring) is clearly displaced from Ec1 (red ring) by Ec1-E1 $=0.55 \AA$. A similar analysis has been done using axial plane Sn1F4aF3i (Fig. 5c). It is worth to note that the electronic cloud around E1 is less disturbing in that direction and that its E1 gravity center coils are closer to Ec1. The size of E1 with its electronic cloud is concentrated and deformed in a large ellipsoidal volume, giving a volume of influence rE1 $=1.05 \AA$, almost the size of a fluorine atom.

E2 on its own does not show in sections reported in Fig. 7 same constraints inside the endless tunnel delimitated by $\left[\mathrm{Sn} 2{ }_{4} \mathrm{~F}_{4}\right]_{\mathrm{n}}$ tetramer ring along [010], then E2 size corresponds to an ellipsoid of roughly the same sphere of influence size rE2 $=1.06 \AA$ (cf. Table 2). To extract the E 2 dimensions the diagonal planes of the fluorine square pyramid Sn2F2F3 and Sn2F1F4 of the Sn2F1apF1,2,3,4E octahedron have been calculated (Fig. 3a,b,c,d) two other sections were also particularly interesting SnEc2F1ap and Ec2F2F4 plane. They are reported in Fig. 7 and analyzed alike previously. Fig. 7e and f are detailed showing the Ec 2 LP center (red circle) in its electronic cloud (pale transparent blue ellipse). Fluorine atoms F1ap and F2, F4 of the tetramer link with Sn2 exhibit a solid bonding (2.048, 2.197, $2.276 \AA$ ), while the remaining ones F1 and F3 engaged to connect with the next tetramer ring via Sn2c and Sn1a ( $2.386 \AA$ and $2.494 \AA$ ), show a small rupture of the electron density (see Fig. 7).

## 4.2. $\beta S n F_{2}$

The synthesis mode needed to obtain $\beta \mathrm{SnF}_{2}$ leads to a metastable
phase. Its structure was determined and refined using X-ray powder pattern data [11] (Table 3 and Fig. 8). Therefore taking advantage of this piece of information a refinement of the network was realized using DFT-ELF calculations. The results showing a little condensation of the network and various interatomic distances are reported in Table 3.

In $\beta \mathrm{SnF}_{2}$ there is one independent Sn atom bonded to five F making a distorted quadrilateral pyramid (Fig. 8). Taking into account its lone pair $\mathrm{E}, \mathrm{CN}=5+1$ coordination $\left[\mathrm{SnF}_{5} \mathrm{E}\right.$ ] occurs in the form of a distorted octahedron, particularly its equatorial plane F2bF2F2cF1a (Fig. 9a \& f). As usual, the shortest Sn-F1ap bond (red stick) extends towards the apex of the fluorine square pyramid and all the angles are in between $73.8^{\circ} \angle \mathrm{F} 1-\mathrm{Sn}-\mathrm{F} 2 \mathrm{~b}, \mathrm{~F} 1 \mathrm{a}, \mathrm{F} 2<83.7^{\circ}$ but the angle $\angle \mathrm{F} 1-\mathrm{Sn}-\mathrm{F} 2 \mathrm{c}=104.0^{\circ}$ thereby reflecting the pronounced puckering of the equatorial plane, the dihedral angle F1a-F2bF2-F2c $=23.8^{\circ}$. After locating $E$ one finds that $S n-E=1.019 \AA$, a value very close to the one of Sn 2 in $\alpha \mathrm{SnF}_{2}$ having the same octahedral coordination with Sn 2 $\mathrm{E} 2=0.987 \AA$. The $\mathrm{Sn}-\mathrm{F} 1 \mathrm{ap}=2.131 \AA$, apical bond in $\beta \mathrm{SnF}_{2}$, is slightly bigger than in $\alpha \mathrm{SnF}_{2}\left(2.048 \AA\right.$ ) and averaged $\mathrm{Sn}_{\circ} \mathrm{F}$ distances of the equatorial plane are similar $2.379 \AA$ against $2.337 \AA$.

A projection of the structure along [010] shows, alike in $\alpha$ phase, a kind of fourfold ring making a tunnel along [010] (Fig. 9b). Its section shaded in pale green color looks like the yellow one of the $\alpha$ phase, therefore two Sn-F1ap bonds participate to bordering the tetramer while they were uniquely engaged in interconnecting bonding previously. It is also noted that two lone pairs E point towards the inside of the tunnel where they find enough space, $\mathrm{Ec} . . \mathrm{Eb}=2.941$ Å. Repeated by the twofold screw axis they design an endless double chain along

Sn8F16, monoclinic base-centred

$\alpha \mathrm{SnF}_{2}$

Sn4F8, orthorhombic primitive


$\gamma \mathrm{SnF}_{2}$
Fig. 12. Site projected density of states (DOS) of divalent tin fluoride $\mathrm{Sn}^{\mathrm{II}} \mathrm{F}_{2}$ three varieties.
[010].
Each [ $\left.\mathrm{SnF}_{5} \mathrm{E}\right]$ octahedron share corners with five other octahedra thereby creating a three-dimensional network as illustrated in Fig. 9a. There is a strong connection between Sn and Snc via $\mathrm{Sn}-\mathrm{F} 1 \mathrm{ap}=2.131 \AA$ and Snc-F1a $=2.336 \AA$ bonds. They show around the twofold screw axes located in $y=1 / 4$ and $3 / 4$ and parallel to [010] a condensation of the network which leaves along this direction a channel in which lone pairs chains extend. The average distance of E with surrounding fluorine atoms making a distorted quadrilateral is 2.756 A.

### 4.2.1. Electron localization function

A series of sections in ELF data allowed appreciating the nature of bonding. All $\mathrm{Sn}-\mathrm{F}$ bonds appear well associated with F by covalent bonding but $\mathrm{Sn}-\mathrm{F} 2 \mathrm{c}=2.668 \AA$, longer than the four others $\mathrm{Sn}-\mathrm{F} 1 \mathrm{ap}$, F1a, F2, F2b, and therefore more relevant of iono-covalent character (Fig. 9b and d). The coordinates of the Ec core of Sn lone pair (little red circle) have been refined in Fig. 9a,b,c,d sections.

Fig. 9 e is a section by a plane containing three E immediate neighbors of Ec; showing that they are free of constraints. An ellipsoidal ( $\mathrm{a} / \mathrm{b} / \mathrm{c}$ ) envelop for E has been determined (see Table 3) Ec being accompanied by an electronic cloud, giving finally a sphere of influence with radius $\mathrm{rE}=1.013 \AA$. Its center (little blue circle) as ever is slightly off Ec position ( $0.2-0.3 \AA$ ) its plasticity being sensitive to the various network interactions.

## 4.3. $\gamma S n F_{2}$

X-ray powder data needed to determine the structure of this $\gamma \mathrm{SnF}_{2}$ phase were collected after heating at $190^{\circ} \mathrm{C}$, followed by slow cooling down to $80^{\circ} \mathrm{C}$, where the temperature was maintained to stabilize this variety of tin II fluoride (Table 4).

The salient feature of the $\gamma \mathrm{SnF}_{2}$ structure is a new change of Sn II to coordination polyhedron $\mathrm{CN}=4+1$, a triangular bipyramid (TBP) [ $\left.\mathrm{SnF}_{4} \mathrm{E}\right]$ alike Sn 1 in $\alpha \mathrm{SnF}_{2} \mathrm{E}$. This TBP as shown in Fig. 10a is the onesided coordination of Sn with four Fs, the lone pair E at the apex of the equatorial triangle making up the triangular bipyramid. Equatorial bonds $\mathrm{Sn}-\mathrm{Fa}, \mathrm{Fb}$ (red sticks in Fig. 10), equivalent by symmetry $2.115 \AA$, are slightly bigger than mean Sn1-Feq $=2.080 \AA$ of $\alpha$ allotrope while the two $\mathrm{Sn}-\mathrm{Fax}=2.327 \AA$ are very different in $\alpha$ phase alike $\angle \mathrm{Fa}-\mathrm{Sn}-\mathrm{Fb}$ equatorial ( $91.3^{\circ}$ ) and $\angle \mathrm{Fc}$-Sn-Fd axial ( $156.1^{\circ}$ ) angles are more open instead of $86.7^{\circ}$ and $142.7^{\circ}$ due to strong E-bond pairs repulsions. $\mathrm{Sn}-\mathrm{Fc}$, Fd are longer than the equatorial ones by $0.2 \AA$, a value already found in such type of $\left[\mathrm{M}^{*} \mathrm{X}_{4} \mathrm{E}\right]$ TBP ( $\mathrm{X}=\mathrm{O}$ or F ). Each $\left[\mathrm{SnF}_{4} \mathrm{E}\right]$ TBP shares apices with four different homologs. Equatorial apices are systematically linked to axial ones, the short bond being followed by a longer one; for example, Sn -Fa-Sna with $\mathrm{Sn}-\mathrm{Fa}=2.132 \AA$ and Fa $S n a=2.323 \AA$, Fa equatorial for Sn becomes an axial F for the $\left[\mathrm{SnaF}_{4} \mathrm{E}\right.$ ] TBP. Such a bonding scheme generates a three-dimensional network as illustrated in Fig. 10b in which, as in the previous allotropic phases a large rectangular tunnel can be seen parallel to [100], defined here by a pseudo ring $\left\{\mathrm{Sn}_{6} \mathrm{~F}_{6}\right\}$, a tunnel which welcomes the lone pairs of tin II (see Fig. 11).

### 4.3.1. Electron localization function

Opposite to $\alpha$ and $\beta$ the $\gamma \mathrm{SnF}_{2}$ variety does not show a $\mathrm{CN}=6$ in form of $\left[\mathrm{SnF}_{5} \mathrm{E}\right]$ octahedron but to the triangular bipyramid $\mathrm{CN}=5$ alike the one centered on Sn 1 of $\alpha$ form. Both $\mathrm{Sn}-\mathrm{F}$ equatorial and axial bonds show IDC continuity indicating a stable $\mathrm{SnF}_{4} \mathrm{E}_{2}$ unit in this threedimensional network.

The density maximum close to Sn atom is shown in Fig. 11 by a little white-red circle which gives Ec centroid of the lone pair. The associated electronic cloud with its E center (white-blue circle) is delimitated and


Fig. 13. a) Projection onto [010] plane of the $\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}$ crystal structure. $\mathrm{Sn}^{4+}$ and $\mathrm{Sn}^{2+}$ are shown in black and blue circles, $\mathrm{Sn}^{4+}-\mathrm{F}$ and $\mathrm{Sn}^{2+}-\mathrm{F}$ bonds in red and blue sticks, E in a pale blue ellipse. The [ $\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}$ ] layer formed by $\mathrm{Sn} 1^{4+} \mathrm{F}_{6}$ and $\mathrm{Sn} 2^{2+} \mathrm{F}_{5} \mathrm{E}$ octahedra F corner shared is parallel to (101) plane (shaded in yellow); worthy to note that a double plane of $E$ separate $\left[\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}\right]_{\mathrm{n}}$ layers. b) Detail of an isolated $\left[\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}\right]_{\mathrm{n}}$ layer, parallel to (101) plane, showing the endless zigzag string of ... Sn2-F4ap-Sn2-F4ap ... along [010]. c) Perspective view of the $\mathrm{Sn} 2 \mathrm{~F}_{5} \mathrm{E}$ distorted octahedron. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

Table 5
X-rays [6] and DFT-ELF (pw) data of $\mathrm{SnSn}_{2} \mathrm{~F}_{8} \mathrm{E}_{2}$.

| $\mathrm{Sn}_{3} \mathrm{~F}_{8}$ - [6] Monoclinic - Space group P2 ${ }_{1} / \mathrm{n}\left(\mathrm{N}^{\circ} 14\right)$ - Molecular weight: $508.06 \mathrm{~g} \rho_{\mathrm{x}}=4.86\left(\mathrm{~g} / \mathrm{cm}^{3}\right)$. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | a (A) | b (Å) | c ( A $^{\text {) }}$ | $\alpha\left({ }^{\circ}\right)$ | $\beta\left({ }^{\circ}\right)$ | $\gamma\left({ }^{\circ}\right)$ | $\mathrm{V}\left(\AA^{3}\right)$ | Z | $\mathrm{V}(\mathrm{F}, \mathrm{E})\left(\AA^{3}\right)$ |
| X-rays | 5.2155 | 5.3208 | 12.483 | 90 | 90.38 | 90 | 345.97 | 2 | 19.3 |
| DFT-ELF [pw] | 5.217 | 5.318 | 12.473 | 90 | 90.36 | 90 | 346.04 | 2 | 19.3 |
| Interatomic distances $(\AA)$ and angles $\left(^{\circ}\right.$ ) - [ $\left.\mathrm{Sn}^{4+}(\mathrm{Sn} 1)-\mathrm{Sn}^{2+}(\mathrm{Sn} 2)\right]$ |  |  |  |  |  |  |  |  |  |
| Sn1-F1 (x2) |  |  | Sn2-F4a ap |  | 2.097 |  | F4a.ap-Sn2a |  | 2.169 |
| Sn1-F2 (x2) |  |  | Sn2-F4 |  | 2.169 |  | Sn2-F1a |  | 2.555 |
| Sn1-F3 (x2) |  |  | Sn2-F2 |  | 2.253 |  | Sn2-F3 |  | 2.651 |
| Sn2-E2 |  |  | E2a-F1b |  | 2.721 |  | $\angle \mathrm{ESn} 2 \mathrm{~F} 4 \mathrm{ap}$ |  | 157.7 |
| E2-F2 |  |  | E2a-F3b |  | 2.578 |  | $\angle \mathrm{F} 4 \mathrm{apSn} 2 \mathrm{~F} *$ |  | $80.4 \pm 5.2$ |
| E2-F4 |  |  | E2a-E2b |  | 3.900 |  | $\angle \mathrm{E} 2 \mathrm{Sn} 2 \mathrm{~F} 1 \mathrm{a}$ |  | 89.1 |
| E2b-E2c |  |  | Mean E-F |  | 2.766 |  | $\angle \mathrm{E} 2 \mathrm{Sn} 2 \mathrm{~F} 3$ |  | 100.3 |
| E ellipsoid a/b/c |  |  | 1.15/1.10/0 |  |  |  | rE |  | 1.04 |

eq.: equatorial; ax: axial. F* equatorial averages. E a/b/c ellipsoid size.
Coordinates: E: 0.3600/0.5743/0.1407-rE: sphere of influence.
marked by a dotted pale blue ellipse. E is moved out from Ec by $\sim 0.3 \AA$ because interactions of network requesting its plasticity.

### 4.3.2. Electronic density of states of the three Sn(II) fluorides

The site projected electronic density of states DOS is shown for the three $\mathrm{SnF}_{2}$ varieties in Fig. 12. Along the x -axis, the energy zero is at the top of the valence band VB, separated from the conduction band CB by a large bandgap. Then $\mathrm{SnF}_{2}$ is insulating in its three phases.

The bandgap magnitude increases along with the series going from $\sim 3 \mathrm{eV}$ for $\alpha \mathrm{SnF}_{2}$ then $\sim 3.3 \mathrm{eV}$ for $\beta \mathrm{SnF}_{2}$ and $\sim 3.8 \mathrm{eV}$ for $\gamma \mathrm{SnF}_{2}$. The change of bandgap magnitude is likely due to the different local surroundings of Tin as shown in Figs. 5, 8 and 10.

The energy low lying F-s states are not taken into account in the explicit basis set. This is also the case of full $\mathrm{Sn} 4 \mathrm{~d}^{10}$ states.

From this, Sn explicit basis set is of s and p character while F valence states are of p character. Due to the large filling of F p subshell ( $\mathrm{F}-\mathrm{is}$ $2 \mathrm{p}^{6}$-like) the F PDOS are of large intensity and are found dominating VB. The Sn s and p states mix with those of F p to ensure for the bonding. Within the valence band, the similar DOS skylines indicate the quantum mixing between the valence states. This is particularly so for the extent of the VB up to its top. Note the different DOS of the two Sn sites in the $\alpha$ phase due to the local surrounding of $\mathrm{Sn} 1 / \mathrm{Sn} 2$ detailed in Fig. 5.

## 5. Tin (II-IV) mixed-valence fluorides

## 5.1. $\mathrm{Sn}_{3} \mathrm{~F}_{8}$ or $\mathrm{Sn}_{2}^{2+} \mathrm{Sn}^{4+} F_{8} E_{2}$

Single crystals of this tin fluoride were obtained by direct oxidation of an HF solution of $\mathrm{SnF}_{2}$. After analysis using various techniques, in particular, Mössbauer spectroscopy, the mixed valent formula of this fluoride was precisely established as $\mathrm{Sn}_{2}^{2+} \mathrm{Sn}^{4+} \mathrm{F}_{8}$ [23]. Following the introduction into a glass capillary, the X-ray analysis showed that it belongs to the monoclinic system (Table 4).

Tin atoms are located on two crystallographic sites, Sn 1 which accommodates $\mathrm{Sn}^{4+}$ onto symmetry center, $\mathrm{Sn}^{2+}$ being on Sn 2 site. A projection of the framework onto (010) plane is given in Fig. 13a.
$\mathrm{Sn} 1^{4+}$ with six fluorine atoms creates a flattened $\mathrm{Sn} 1 \mathrm{~F}_{6}$ octahedron sharing all these apices with six independent $\mathrm{Sn}^{2+}{ }^{2+}$ ions (Fig. 13b). The Sn1-F1,2,3 are quasi identical at $1.963 \pm 0.013 \AA$. Note the major differences with $\mathrm{Sn}-\mathrm{F}_{\mathrm{ax}}=1.874 \AA$ bonds which assume the connection into endless $\left[\mathrm{SnF}_{4}\right]_{\mathrm{n}}$ strings and free $\mathrm{Sn}-\mathrm{F}_{\mathrm{eq}}=2.025 \AA$ bonds in $\mathrm{SnF}_{4}$ fluoride.
$\mathrm{Sn} 2^{2+}$ exhibits a sterical active lone pair and a $\mathrm{CN}=5+1$ co-
 $\mathrm{E} 2=0.938 \AA$ is in agreement with previous cases therefore smaller than $\mathrm{Sn} 2-\mathrm{E} 2=0.987 \AA$ in $\alpha \mathrm{SnF}_{2} \mathrm{E}$ and $\mathrm{Sn}-\mathrm{E}=1.019 \AA$ in $\beta \mathrm{SnF}_{2} \mathrm{E}$.

These $\mathrm{Sn} 2{ }^{2+} \mathrm{F}_{5} \mathrm{E}$ octahedra are associated along [010] by F4p atoms along [010] developing an endless zigzag string ... Sn2-F4ap-Sn2-F4ap ... the remaining fluorines F1, F2 and F3 assuming the layer formation by interconnection with $\mathrm{Sn}^{2} \mathrm{~F}_{6}$ octahedra. Such bonding develops an $\left[\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}\right]_{\mathrm{n}}$ layer parallel to the plane (101). E lone pairs border these layers filling the interspace between them via a double layer, van der Waals interactions assuming the stability of the packing. In this space, the closest interatomic distances between consecutive layers are E2$\mathrm{F} 1 \mathrm{~b}=2.708 \AA$ and $\mathrm{E} 2-\mathrm{F} 3 \mathrm{~b}=2.966 \AA$ while $\mathrm{F}-\mathrm{F}$ distances are above $3 \AA$ as well as Sn2a-F1 or F3i making an improbable weak interaction. So the stability of $\mathrm{Sn}_{3} \mathrm{~F}_{8}$ framework appears to be provided via lone pairfluorine inter-actions.

An isolated $\left[\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}\right]_{\mathrm{n}}$ layer is shown together with the distorted $\left[\mathrm{Sn} 2 \mathrm{~F}_{5} \mathrm{E}\right]$ octahedron (O) in Fig. 13b and c. One can see that $\left[\mathrm{Sn}_{2} \mathrm{FF}_{5} \mathrm{E}\right]_{\mathrm{n}}$ make infinite zigzag strings along [010] by corner-sharing of their equatorial apices; they are held together by $\mathrm{Sn}_{\mathrm{F}} \mathrm{F}_{6}$ octahedra. Note the twofold role of E which, at the level of the $\left[\mathrm{Sn}_{2} \mathrm{~F}_{5} \mathrm{E}\right](\mathrm{O})$, via the strong repulsion lone pair-bond pair, pulls down the angles $\angle \mathrm{F} 4 \mathrm{apSn} 2 \mathrm{~F}^{*}$ to $80.4^{\circ}$ and $\angle \mathrm{ESn} 2 \mathrm{~F} 4$ ap to $157.7^{\circ}$ and which at the level of the framework holds together $\left[\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}\right]_{\mathrm{n}}$ layers via $\mathrm{E}-\mathrm{F}$ interactions. Note also the bond lengths of Sn2-F1a and Sn2-F3 and angles E2Sn2F1a and E2Sn2F3 which are impacted by E pair-bond pair repulsion (Table 5).

### 5.1.1. Electron localization function ELF

A series of sections in ELF data allows determining E coordinates and also lone pair shape in Fig. 14. The distance Sn2-E is closed to preceding values found for $\alpha$ and $\beta \operatorname{SnF}_{2}$. The E electronic volume,


Fig. 14. ELF of $\mathrm{Sn}_{3} \mathrm{~F}_{8}$. a) Sn 2 via $\mathrm{Sn} 2-\mathrm{F} 1 \mathrm{a}$ and $\mathrm{Sn} 2-\mathrm{F} 2$ equatorial bonds assume the bridging between two ( $\mathrm{Sn}_{1} \mathrm{~F}_{6}$ ) octahedra (see Fig. 13a and b) a section of Sn2 lone pair is clearly marked; b) this section based on the same fluorine atoms F1a and F2 and Ec2 electron density maximum of E2 lone pair allows determining two parameters of E2 ellipsoid. c) F4ap strongly tighten the thickness of $\left[\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}\right]_{\mathrm{n}}$ layer. d) The section Sn2F4F3 almost at $90^{\circ}$ of b) offers the possibility to check again E2 shape. e) E section by a plane perpendicular in Ec to $\mathrm{Sn} 2-\mathrm{Ec} 2$ vector shown in $\mathbf{f}$ ).
which always accompanies the core Ec of the lone pair, has been determined to make at the summit of $\operatorname{Sn} 2 \mathrm{~F}_{5} \mathrm{E}$ octahedron a helmet density on Sn2. Therefore owing to various repulsive interactions the $\angle \mathrm{FSn} 2 \mathrm{~F}$ angles of the octahedron have been somewhat shacked. Anyhow the various sections show a large coherence with crystal data as shown in Fig. 14.

They show that $\mathrm{Sn} 2-\mathrm{F} 1$ a bond is not covalent like $\mathrm{Sn}-\mathrm{F} 2$ but it
participates in layer coherence by bridging two $\mathrm{Sn}_{\mathrm{F}}^{\mathrm{F}} 6$ octahedra along [101] (Fig. 14a).

In Fig. 14b, E2F1aF2 allows us to determine Ec2 coordinates of lone pair and to draw its elliptic section (pale blue color) and to precise its center (blue-white circle) slightly distant from Ec $<0.02$ Å. Fig. 14c shows the link between to $\mathrm{Sn}^{2+}$ and $\mathrm{Sna}^{2+}$, i.e. $\mathrm{Sn} 2-\mathrm{F} 4 \mathrm{ap}-\mathrm{Sn} 2 \mathrm{a}$, in fact, doubled by Sn2a-F4-Sn2 fixing strongly the thickness of $\left[\mathrm{Sn}_{3} \mathrm{~F}_{8} \mathrm{E}_{2}\right]_{\mathrm{n}}$


Fig. 15. $\mathrm{Sn}_{3} \mathrm{~F}_{8}\left(\mathrm{Sn}_{6} \mathrm{~F}_{16}\right)$ : Site projected DOS with all constituents (top) and focus on the $\mathrm{Sn}^{2+} / \mathrm{Sn}^{4+}$ partial DOS (bottom).
layer. The network of this layer is the result of an endless double zigzag string [... Sn2-F4-Sn2-F4ap-Sn2a ...] $]_{n}$ parallel to [010] (b periodicity)
 odicity, making endless piling along [010] [... [Sn1F6]-empty trigonal antiprism- $\left.\left[\mathrm{Sn}_{1} \mathrm{~F}_{6}\right] \quad \ldots\right]_{\mathrm{n}}$. The E's produce not only distortions on $\mathrm{Sn}-\mathrm{F} 1,2,3$ bonds but also, with their double plane between the layers, they assume their packing by Van der Waals-like interactions.

### 5.1.2. Site projected density of states

The site project DOS of $\mathrm{Sn}_{3} \mathrm{~F}_{8}$ is shown in two panels in Fig. 15. Due to a large number of fluorine sites the valence band VB has a rather complex character but it is clearly dominated by the F p states (low
energy s states not shown). F-p is prevailing from -12 to -6 eV within VB and shown some bonding (similar skylines) with the two Sn valences.

The gap between VB and CB is very small, which is concomitant with the mixed-valence compound. Focusing on the Sn states is shown on a smaller scale DOS at the lower panel. Clearly, the simultaneous presence of divalent and tetravalent Sn leads to a reduced bandgap. $\mathrm{Sn}^{2+}$ with two lore electrons than $\mathrm{Sn}^{4+}$ has the PDOS larger throughout the VB and especially at the top of the VB. However, there can be noticed differences of magnitudes such as in the $-4,-2 \mathrm{eV}$ energy window, where $\mathrm{Sn}^{4+}$ PDOS are larger. This translates complex bonding features with F substructures illustrated above in the ELF maps.

## 5.2. $\mathrm{Sn}_{2} \mathrm{~F}_{6}$ or $\mathrm{Sn}^{2+} \mathrm{Sn}^{4+} F_{6}$

This second mixed-valence fluoride was obtained by direct synthesis of stoichiometric $\mathrm{SnF}_{4}$ and $\mathrm{SnF}_{2}$. It is sensible to moisture. It crystallizes in the cubic system as revealed by neutron diffraction patterns (Table 6). Its structural network is simply a doubling of the well known $\mathrm{ReO}_{3}$ structure, therefore, evidencing an order between Sn II (Sn1) and Sn IV (Sn2) [7]. A view of the structure is given in Fig. 16a and b.

The main feature of this di-fluoride is a marked difference in the volume of octahedra $\operatorname{Sn} 1^{2+} \mathrm{F}_{6}\left(16.2 \AA^{3}\right)$ and $\mathrm{Sn} 2^{4+} \mathrm{F}_{6}\left(13.0 \AA^{3}\right)$ and to find $\mathrm{Sn}^{2+}$ and its lone pair E together onto a symmetry center. This particular situation can be related to the relativistic effect due to important electron speed at such a high atomic number: $\mathrm{ZSn}=50$ and the space provided by the large fluorine octahedron of the network. In this particular case, the centroid Ec of the lone pair is at its maximum velocity transforming $\mathrm{Sn}^{\mathrm{II}}$ in a large cation $[\mathrm{SnE}] 1^{2+}$ roughly analogous to $\mathrm{Sr}^{2+}$ for example. Based on $\mathrm{rF}^{-}=1.19 \AA, \mathrm{r}[\mathrm{SnE}] 1^{2+} \sim 1.11 \AA$ a size smaller than [SnE] $3^{2+} \sim 1.30 \AA$ (close to $\mathrm{Ba}^{2+}$ ) in the fluoride cube of the mixed-valence oxyfluoride [ SnE$]^{2+} \mathrm{Sn}_{3}^{4+} \mathrm{O}_{2} \mathrm{~F}_{10}$ [25], allowing to appreciate the constraints of an octahedral surrounding against a hexahedral one, therefore showing also the plasticity of the sphere of influence of E .

Again in this double $\mathrm{ReO}_{3}$ type unit, there are empty distorted cuboctahedra. The square faces are now rectangular, two opposite faces being in anti position. The trigonal faces have edge lengths corresponding to those of $[\mathrm{SnE}] 1 \mathrm{~F}_{6}$ and $\mathrm{Sn} 2 \mathrm{~F}_{6}$ octahedra. The distances between its center marked by the star to the twelve fluorine atoms amount to $2.950 \AA$; it suggests that a large cation like $\mathrm{Ba}^{2+}$ could be introduced giving eventually non-stoichiometric mixed-valence phases $\mathrm{Ba}_{\mathrm{x}}[\mathrm{SnE}]$ $1_{1+x} \mathrm{Sn} 2_{1-\mathrm{x}} \mathrm{F}_{6}$.

### 5.2.1. Electron localization function ELF

[ SnE ]1- $\mathrm{F}_{6}$ bonds are $0.433 \AA$ bigger than $\mathrm{Sn} 2-\mathrm{F}$ ones showing for the former ionic interactions while the second shows clearly covalent character. Anyhow it is interesting to have a look also onto the particular case of the lone pair triplet of the fluorine atom sandwiched by [ SnE ]1 and Sn 2 . Fig. 17 gives some data on both $\mathrm{Sn}^{\mathrm{II}}$ and $\mathrm{Sn}^{\mathrm{IV}}$ cations and lone pair triplet of F .

Fig. 17a shows a planar section Sn1FaFb of ELF data. A large high electron density curves appear concentrated onto Sn1 crystallographic site testifying that $\mathrm{Sn}^{\mathrm{II}}$ and its $\mathrm{E}\left(5 \mathrm{~s}^{2}\right)$ lone pair make a unique large cation $[\mathrm{SnE}] 1^{2+}$. Fig. 17b shows a drastic difference; the bonding $\mathrm{Sn} 2-\mathrm{F}_{4}$ is marked its association showing directly its impact on F density curves. Note that maximum intensity IDC $=0.83$ underlined by a white red circle in the two "crescent moon density" (IDC $=0.80$ ) open by Sn2-F bond indicate respectively the centroid Eca trace (section of

Table 6
Crystal data of $\mathrm{Sn}_{2} \mathrm{~F}_{6} \mathrm{E}$.
$\mathrm{Sn}_{2} \mathrm{~F}_{6} \mathrm{E}$ - [6] Z Anorg. Allg. Chemie, 590, 173-180, 1990.
Cubic, Space group Fm $\overline{3} \mathrm{~m}\left(\mathrm{~N}^{\circ} 225\right)$, Molecular weight: $351.37, \rho_{\mathrm{x}}=4.05\left(\mathrm{~g} / \mathrm{cm}^{3}\right)$.

| $\mathrm{a}(\AA) \quad \mathrm{b}(\AA)$ | c (A) | $\alpha\left({ }^{\circ}\right)$ | $\beta\left({ }^{\circ}\right)$ | $\gamma\left({ }^{\circ}\right)$ | $\mathrm{V}\left(\AA^{3}\right)$ | Z | $\begin{aligned} & \mathrm{V}(\square, \mathrm{~F}) \\ & \left(\AA^{3}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8.321 8.321 | 8.321 | 90 | 90 | 90 | 576.1 | 4 | 18.0 |
| Interatomic distances $(\AA)$ and angles $\left({ }^{\circ}\right)\left[\mathrm{Sn}^{2+}(\mathrm{Sn} 1)-\mathrm{Sn}^{4+}(\mathrm{Sn} 2)\right]$ |  |  |  |  |  |  |  |
| [SnE]1-F (x6) | 2.297 |  | Sn2-F (x6) |  | 1.864 | - F (x12) | 2.950 |
| F-F (oct. [SnE]1) (x12) | 3.248 |  | F-F (oct. Sn2) (x12) |  | 2.636 |  |  |
| [SnE]1-Ea | 2.237 |  | Sn2-Ea |  | 2.068 | Fa-Ea | 0.566 |
| [SnE]1-CT | 2.167 |  | Sn2-CT |  | 1.993 | CT-Fa | 0.129 |
| T. rd.rect.Fa <br> Fig. $16 \mathrm{~L} / \mathrm{H} / \mathrm{R}$ | 2.13/1.50/0.65 |  | $\varnothing$ Text.\{F2E2 ${ }_{3}$ \} blue dotted circle |  | 1.93 | T.gyr. yellow circle-radius | 0.552 |
| Ea ellipsoid a/b/c | 0.46/0.46/0.64 |  | rE2 <br> sphere of influence. |  | 0.51 |  |  |

eq.: equatorial. ax.: axial. Eca coordinates: $x, y, z$ ( $W y$ (192l) site), 0.4343/0.4913/0.7395.
CT: E2 torus center: Wy (24e) $x, y, z$ 0.5/0.5/0.7395. T gyr. Ea: torus gyration radius.
gyration core of the electronic torus (CT center)). The associated electron cloud around Eca is somewhat displaced (white blue circle of the pale blue ellipse). Fig. 17c Then the electronic torus with its circle pathway (yellow) made by the triplet is not centered on Fa but repulsed towards [SnE]1 with Fa-CT $=0.129$ Å. A little scheme of Sn2,Fa, Ea and [SnE]1 is done in Fig. 17d.

Again it is noticed that the lone pair triplet resembling a crown, of the fluoride anion is not aligned with F center like in $\mathrm{SnF}_{4}$ ( F 2 $\mathrm{CT}=0.168 \AA$ ) where the space above CT is free, but here Fa-CT faces directly [SnE]1. So, there is a competition for the coordinate of $\left\{\mathrm{E}_{3}\right\}$ torus between repulsive effect of the strong bond $\mathrm{Sn} 2-\mathrm{Fa}$ and the ionic attraction by [SnE]1 cation which amounts only +0.129 A giving Sn2-$\mathrm{CT}=\mathrm{Sn}-\mathrm{Fa}+0.129 \AA=1.869+0.129=1.993 \AA$. It shows the remarkable mobility and adaptability of the \{E3\} torus along the bond axis of $\mathrm{Sn}-\mathrm{F}$.

### 5.2.2. Site projected density of states

Fig. 18 shows the site projected density of states (DOS).
The same calculation framework as for the above-studied $\mathrm{SnF}_{4}, \mathrm{SnF}_{2}$ and $\mathrm{Sn}_{3} \mathrm{~F}_{8}$ DOS have been considered especially regarding the valence basis sets of Sn and F . The valence band (VB full) is separated from the conduction band (CB empty) by an energy gap of 2 eV . The compound is thus a small gap insulator. We note here that the bandgap is smaller than in $\mathrm{SnF}_{4}$ and $\mathrm{SnF}_{2}$ phases but larger than in $\mathrm{Sn}_{3} \mathrm{~F}_{8}$ in Fig. 15. Then mixed-valence compounds -here fluorides- are expected with smaller band gaps than single valence ones.

VB is dominated by F states (blue dotted lines) but likewise in other $\mathrm{Sn}-\mathrm{F}$ studied compounds.

We further examine the bonding in view of the two different Sn valences. The lower panel of Fig. 18 shows the crystal orbital overlap population (COOP) of $\mathrm{Sn}_{2} \mathrm{~F}_{6}$. For a reminder, COOPs are in shorthand notation the overlap integral $\mathrm{S}_{\mathrm{ij}}$ ( i and j designate two chemical species). Positive, negative and nil intensity along the COOP axis are

a)

b)

Fig. 16. a) Perspective view of $\mathrm{Sn}_{2} \mathrm{~F}_{6} \mathrm{E}$ crystal network (left). Dark blue octahedra built up by fluorine atoms (green circles) receive $\mathrm{Sn} 2^{\mathrm{IV}}$ atoms while [SnE]1 ${ }^{\text {II }}$ large atoms, "dilated" by their lone pairs are set up in pale blue transparent octahedra. b) The sub-cube formed by [SnE] 1 and Sn 2 atoms show edges occupied by fluorine atoms forming an empty distorted cuboctahedron centered at $1 / 4,1 / 4,1 / 4$, designed by a star. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)


Fig. 17. a) Section [SnE]1FaFb showing the dilated [SnE] $1^{2+}$ cation due to the spherical environment of Sn 1 core by its lone pair $5 \mathrm{~s}^{2}$. b) $\mathrm{Sn} 2^{4+}$ in its fluorine equatorial plane showing the section of fluorine atoms with the detail of Fa electronic environment crowned by $\left\{\mathrm{Ea}_{3}\right\}$ triplet lone pair torus. c) Section by a plane orthogonal to Sn2-CT in CT showing in the median plane of Ea torus domains of highest density (IDC $=0.831$ ) indicating the pathway of the lone pair triplet on the gyration radius (yellow circle). The pale blue circle of Ea is separated by $120^{\circ}$ in agreement with their size. d) The sequence of Sn 2 -Fa-CT(torus)-[SnE]1 of the edge of the subcube. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)
relevant to bonding, antibonding and non-bonding interactions respectively. Clearly, the two Sn valences present different $\mathrm{Sn}-\mathrm{F}$ interaction results. The main part of the VB is of bonding character (positive intensity COOP) with an energy shift leading to lower energy $\mathrm{Sn}^{\mathrm{IV}}-\mathrm{F}$ (more ionic) versus $\mathrm{Sn}^{\mathrm{II}}-\mathrm{F}$ (less ionic), the latter characterized by an antibonding red line in the CB designating the $5 \mathrm{~s}^{2}$ lone pair LP character.

Therefore we can propose that the electronic structure results (DOS and COOP) together with those pertaining to stereochemistry and LP metrics present altogether a rationale of tin fluoride compounds within a holistic view.

## 6. Concluding notes

The aim of the present work on tin fluorides was to provide further illustration of $\mathrm{Sn} 5 \mathrm{~s}^{2}$ LP spatial extension and metrics within single and mixed-valence fluorides. At the same time the important role of fluorine ligand was precisely depicted, particularly when terminating a covalent bond with its lone pair triplet designing an electronic torus, which center is repulsed after F center of $\mathrm{Sn}-\mathrm{F}$ bond (case of $\mathrm{Sn}-\mathrm{F} 2$ bond, of $\mathrm{SnF}_{4}\left\{\mathrm{E}_{3}\right\}_{2}$ ) but also in $\mathrm{Sn}_{2} \mathrm{EF}_{6}\left\{\mathrm{E}_{3}\right\}_{6}$ or $[\mathrm{Sn} 1 \mathrm{E}]^{2+} \mathrm{Sn}^{4+}\left[\mathrm{F}\left\{\mathrm{E}_{3}\right\}\right]_{6}$.
$\mathrm{SnF}_{4} \mathrm{E}$ (TBP) or $\mathrm{SnF}_{5} \mathrm{E}$ (O) but for $\alpha \mathrm{Sn}_{\mathrm{F}}^{\mathrm{F}} 4 \mathrm{E}$ TBP this distance is more compelled by the network the value being $\mathrm{Sn} 1-\mathrm{E} 1=0.862 \AA$. Therefore E-F distances equal $2.75 \pm 0.05 \AA$ in all cases.

- $\mathrm{Sn}_{2} \mathrm{~F}_{6} \mathrm{E}$ has given the opportunity to evaluate the size [ SnE ] $1^{2+}$ cation in its fluorine octahedron which is $\mathrm{R}=0.93 \AA$.

Another important result deals with the lone pair triplet $\left\{\mathrm{E}_{3}\right\}$ brought by fluorine atoms as emphasized in the previous papers [3-5]. Therefore another characteristic is provided here by comparing $\mathrm{SnF}_{4}$ (or $\mathrm{Sn}^{4+} \mathrm{F1}_{2}\left[\mathrm{~F}_{2}\left\{\mathrm{E}_{3}\right\}\right]_{2}$ ) and $\mathrm{Sn}_{2} \mathrm{~F}_{6}$ (or $[\mathrm{SnE}] 1^{2+} \mathrm{Sn} 2^{4+} \mathrm{F}_{6}\left\{\mathrm{E}_{3}\right\}_{6}$ ) fluorides. The $\left\{\mathrm{E}_{3}\right\}$ triplet around F plays a dynamic role according to network opportunities. In $\mathrm{SnF}_{4}\left\{\mathrm{E}_{3}\right\}$ triplet a torus centered in CT on $\mathrm{Sn}-\mathrm{F} 2$ bond axis is facing an empty space (Fig. 2) allowing a $\mathrm{F} 2-\mathrm{CT}=0.168 \AA$ or $\mathrm{Sn}-\mathrm{CT}=\mathrm{Sn}-\mathrm{F} 2+0.168 \AA=2.042 \AA$; this $\{\mathrm{E} 3\}$ torus displacement has been attributed to repulsive effect of covalent bond $\mathrm{Sn}-\mathrm{F} 2$. In $\mathrm{Sn}_{2} \mathrm{~F}_{6}$, Fa is sandwiched by $[\mathrm{Sn} 1 \mathrm{E}]^{2+}$ and $\mathrm{Sn} 2^{4+}$, so $\mathrm{Sn} 2-\mathrm{CT}=\mathrm{Sn} 2-\mathrm{Fa}+$ $0.129 \AA=1.993 \AA$ showing that $[\mathrm{SnE}] 1^{2+}$ with its large size maintains an attractive force on $\{\mathrm{E} 3\}$ torus and correlatively weakens $\mathrm{Sn} 2-\mathrm{Fa}$ bonding repulsive effect. This situation shows that in various networks \{E3\} F torus can play an adjustment role in network architecture building.

- The Sn-E average distance appears around $0.98 \pm 0.05 \AA$ for both


Fig. 18. $\mathrm{Sn}_{2} \mathrm{~F}_{6}$ : Site projected DOS (top) and differentiated $\mathrm{Sn}(\mathrm{II})-\mathrm{F} / \mathrm{Sn}(\mathrm{IV})-\mathrm{F}$ chemical bonding based on overlap integral $\mathrm{S}_{\mathrm{ij}} \mathrm{COOP}$ criterion (bottom).

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