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When Do Opposites Attract? A Model Uncovering the Evolution of Disassortative Mating

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ABSTRACT: Disassortative mating is a rare form of mate preference that promotes the persistence of polymorphism. While the evolution of assortative mating and its consequences for trait variation and speciation have been extensively studied, the conditions enabling the evolution of disassortative mating are still poorly understood. Mate preferences increase the risk of missing mating opportunities, a cost that can be compensated by a greater fitness of offspring. Heterozygote advantage should therefore promote the evolution of disassortative mating, which maximizes the number of heterozygous offspring. From the analysis of a two-locus diploid model with one locus controlling the mating cue under viability selection and the other locus coding for the level of disassortative preference, we show that heterozygote advantage and negative frequency-dependent viability selection acting at the cue locus promote the evolution of disassortative preferences. We predict conditions of evolution of disassortative mating coherent with selection regimes acting on traits observed in the wild. We also show that disassortative mating generates sexual selection, which disadvantages heterozygotes at the cue locus, limiting the evolution of disassortative preferences. Altogether, our results partially explain why this behavior is rare in natural populations.

Keywords: sexual selection, mate choice, genetic load, self-referencing, theory.

Introduction

The evolution of mate preferences is puzzling because preferences increase the risk of missing mating opportunities, which may incur significant fitness costs. While

the evolution of assortative mating has been reported in many species, disassortative mating is more scarcely observed (Jiang et al. 2013; Janicke et al. 2019), suggesting that the ecological conditions enabling its evolution could be more restrictive. Here, using a general approach, we investigate the selection regimes allowing the evolution of disassortative mating using a mathematical model.

The multiple costs associated with mate choice tend to generate direct selection against the evolution of mate preferences (for a review, see Pomiankowski 1987) and may further limit the evolution of disassortative mating (for theoretical studies, see Pomiankowski 1987; Schneider and Bürger 2006; Kopp and Hermisson 2008; Otto et al. 2008). These costs of choosiness are generally separated into fixed and relative costs (Otto et al. 2008). Relative costs depend on the distribution of the mating cue within the population. For example, relative costs of choosiness may emerge from the increased investment in mate searching because an individual needs to investigate several mates to find a suitable one. Increased sampling effort can be costly in time (Kruijt and Hogan 1967) and energy (as empirically estimated in antilopes; Byers et al. 2005), and it may enhance predation risk (e.g., in patrolling animals; Hughes et al. 2012). Evaluation effort increases with the proportion of unpreferred males, implying growing relative costs of choosiness when the preferred cue is rarely displayed in the population. In addition, mate rejection by choosy individuals can also incur relative fitness costs, as in the case of male harassment: in the fly species *Musca domestica*, males jump on females' back to initiate mating, and choosy females have to kick unpreferred males to avoid mating (Sacca 1964). The number of males to kick out decreases

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with the proportion of preferred males. By contrast, fixed costs associated with mate choice do not depend on the composition of the population. For instance, metabolic costs may emerge from the mechanisms underlying mate choice, requiring specialized morphological, physiological, and cognitive changes (for a review, see Rosenthal 2017). For example, in the self-incompatibility system in the genus *Brassica*, mate choice involves a specialized receptor-ligand association (Hiscock and McInnis 2003), so that the evolution of self-incompatibility is associated with metabolic costs induced by the production of the specific proteins.

Despite these costs, mate choice is ubiquitous in nature (Barrett 1990; Backwell and Passmore 1996; Cisar 1999; Jiggins et al. 2001; Hiscock and McInnis 2003; Savolainen et al. 2006; Merrill et al. 2014), indicating that mate preference evolves readily and that choosy individuals enjoy benefits compensating those costs. Choosy individuals may enjoy direct benefits (Wagner 2011)—for instance, through beneficial sexually transmitted microbes (Smith and Mueller 2015) or by decreasing risk of precopulatory cannibalism (Pruitt and Riechert 2009)—as well as indirect benefits associated with mate preferences through an enhanced quality of their offspring (Petrie 1994; Sheldon et al. 1997; Welch et al. 1998; Drickamer et al. 2000; Jiggins et al. 2001; Byers and Waits 2006).

Viability selection acting on mating cues by generating indirect selection on preferences may thus promote their evolution (Fisher 1930). Such indirect selection is caused by genetic associations between mating preference and mating cues (linkage disequilibrium; Ewens 1979; Barton and Turelli 1991; Kirkpatrick and Ravigné 2002) generated during zygote formation because of mate preferences. The indirect effect of viability selection, which acts directly on mating cues, on the evolution of mate preferences, first identified by Fisher, has now been confirmed in many theoretical studies (O'Donald 1980a; Heisler 1984; Barton and Turelli 1991). Preference based on a selectively neutral mating cue may also evolve if the cue is correlated with an adaptive trait due to linkage disequilibrium between preference and an adaptive trait (Heisler 1985). A growing amount of empirical evidence showing that female choice does improve offspring fitness has been reported (Petrie 1994; Sheldon et al. 1997; Welch et al. 1998; Drickamer et al. 2000; Byers and Waits 2006), suggesting that preferences generate linkage disequilibria between preference alleles and other combinations of alleles favored by viability selection. Indirect selection may thus be a major driver of the evolution of mate choice.

Once mate preferences are established in the population, they generate sexual selection on the traits exhibited by individuals during courtship, which may drive the evolution of extravagant traits in males, following a Fisherian runaway (Fisher 1930; O'Donald 1980b; Lande 1981;

Kirkpatrick 1982; Gomulkiewicz and Hastings 1990; Otto 1991; Greenspoon and Otto 2009; Veller et al. 2020). The evolution of mate preferences thus involves complex evolutionary processes where preferences coevolve with the cues displayed by the chosen individuals. This coevolution has been observed in natural populations (Grace and Shaw 2011; Higginson et al. 2012) and in experimental studies (Brooks and Couldridge 1999; Miller and Pitnick 2002), underpinning the importance of sexual selection feedbacks on the evolution of mate preferences.

The different selection regimes acting on mating cues can therefore drive the evolution of different mating patterns through indirect selection. Disruptive selection on mating cues has been demonstrated to promote assortative preferences (Kirkpatrick 2000; Dieckmann 2004; Gavrillets 2004; de Cara et al. 2008; Otto et al. 2008; Bank et al. 2012). By contrast, selection conferring fitness advantages to intermediate phenotypes is often thought to promote disassortative mating (Kondrashov and Shpak 1998; Kirkpatrick and Nuismer 2004). Nevertheless, the selection regimes enabling the evolution of disassortative mating are much less studied than the selective pressures involved in the evolution of assortative mating, which have been extensively investigated in the context of speciation (Gavrillets 2004; Kopp et al. 2018).

Disassortative mating has been documented in only a few cases. The best-documented cases are the major histocompatibility complex (MHC) loci in humans and mice, where females prefer males with a genotype different from their own (Wedekind et al. 1995). MHC genes are involved in specific recognition of pathogens, and host-pathogen interactions classically generate negative frequency-dependent selection and/or heterozygote advantage (recognition of a larger range of pathogens; Piertney and Oliver 2006). Such balancing selection regimes are thought to promote disassortative mating at MHC loci (Slade and McCallum 1992; Penn and Potts 1999; Ihara and Feldman 2003). Using numerical simulations in a haploid model, Howard and Lively (2003, 2004) confirm that host-pathogen interactions at MHC loci promote the emergence of disassortative mating, although they never observed the fixation of this mating behavior in the population. In a more general model, Nuismer et al. (2008) observe that sexual selection due to nonrandom mating generates indirect selection on preference that hampers the fixation of disassortative mating in the population. Despite this limitation, the frequency of disassortative mating can be high when viability selection strongly promotes this behavior. In an extension of Nuismer et al.'s (2008) model, Greenspoon and M'Gonigle (2014) show that maternal transmission of pathogens leads to higher levels of disassortative mating. Since transmitted pathogens tend to be adapted to the MHC genotype of the mother, disassortative preferences targeting the MHC locus may be advantageous:

the resulting offsprings have MHC genotypes differing from their mother and are thus more likely to efficiently eliminate transmitted pathogens.

Other cases of disassortative mating in traits unlinked to immune functions have been reported, such as disassortative mating based on the plumage coloration in the white throated sparrow (Throneycroft 1975) or on the wing color pattern in the mimetic butterfly *Heliconius numata* (Chouteau et al. 2017). In both cases, one cue allele is linked to a genetic load (Tuttle et al. 2016; Jay et al. 2021), so that disassortative mating may increase offspring fitness through an increased viability of heterozygotes. In both cases, cue alleles associated with a genetic load are dominant to other alleles, suggesting that dominance among cue alleles may play a role in the evolution of disassortative mating. Numerical simulations matching the specific case of the polymorphic mimicry in the butterfly *Heliconius numata* confirm that selection promoting heterozygotes at the mimicry supergene may favor the emergence of disassortative mating (Maisonneuve et al. 2021).

Other theoretical studies have focused on the effect of disassortative mating on the persistence of variations at the cue locus, illustrating that this mate preference may limit the purging of maladaptive cue alleles and therefore promote higher levels of polymorphism at the cue locus (Karlin and Feldman 1968; Falk and Li 1969; Ihara and Feldman 2003). Polymorphism, in turn, maintains conditions favoring this mate preference. These results suggest that the evolution of disassortative preferences is likely to depend on viability selection acting at the cue locus but also on feedbacks between cue polymorphism and mate choice. These complex interactions between selective pressures, identified in different systems where disassortative mating is observed, are now calling for a mathematical framework providing a unifying perspective on the evolution of disassortative preference. Here, we use a modeling approach to draw general predictions about the selection regimes enabling the emergence of this mate preference and to shed light on the feedback generated by sexual selection on the evolution of disassortative mating when this behavior is common.

We thus conduct an analytical exploration of the conditions enabling the evolution of disassortative mating by adapting a previous model of evolution of assortative mating developed by Otto et al. (2008). The model assumes a population of diploid individuals with two key loci: the first locus, C , controls variation in a single mating cue, which may be subject to viability selection. The second locus, P , controls mate preference on the basis of the cue encoded by locus C . We take into account fixed and relative costs associated with choosiness. Contrary to the original model built to understand the evolution of assortative mating, alleles at preference locus P generate

disassortative preference. Moreover, we introduce coefficients that describe the dominance at both loci to identify how the dominance relationships impact the evolution of disassortative mating.

We first analyze the model under quasi-linkage equilibrium (QLE) to derive analytical expressions of changes in genetic frequency at both the cue locus and the preference locus, providing general expectations on the conditions enabling the emergence and persistence of disassortative mating. We then use numerical simulations to explore the evolution of disassortative preferences under strong overdominant selection acting at the cue locus that does not match the QLE assumptions. We finally compare our theoretical predictions with the few documented cases of disassortative mating and discuss why the evolution of disassortative mating may be limited in natural populations.

Methods

Following the theoretical framework developed by Otto et al. (2008), we investigate the evolution of disassortative mating by assuming a diploid sexual species with a balanced sex ratio and considering two loci C and P . The locus C controls for a trait used as a mating cue, and the locus P controls for the mate preference. We consider two different alleles, a and b , at locus C , so that $\mathcal{G}_C = \{aa, ab, bb\}$ is the set of possible genotypes at this locus. The locus C can be under different viability selection regimes. At the mating preference locus P , we assume two alleles: a resident allele M , and a mutant allele m . The set of possible genotypes at locus P is thus $\mathcal{G}_P = \{MM, Mm, mm\}$. The two loci recombine with probability r at each birth event. We consider a discrete time model and follow the genotype frequencies over time.

Mating Cue Locus under Viability Selection

We define $Res(i, j)$ as the phenotypic resemblance between individuals with genotypes i and j at locus C , for all $(i, j) \in \mathcal{G}_C$. Individuals with genotypes aa and bb at locus C display distinct phenotypes, so that $Res(aa, bb) = 0$. Dominance between the cue alleles a and b is controlled by the dominance coefficient at locus C , h_a . This coefficient describes the dominance of the focal allele a with the following rule, for every $i \in \mathcal{G}_C$:

$$\begin{aligned} Res(ab, i) &= Res(i, ab) \\ &= \frac{1 + h_a}{2} Res(aa, i) + \frac{1 - h_a}{2} Res(bb, i). \end{aligned} \quad (1)$$

Hence, if $h_a = 0$, alleles a and b are codominant, and if $h_a = 1$ (resp. -1), the focal allele a is dominant (resp.

recessive) to b . If $0 < h_a < 1$ (resp. $-1 < h_a < 0$), allele a is incompletely dominant (resp. recessive) to b .

The cue induced by the genotype at locus C determines mating success but can also be under viability selection. We explore the evolution of disassortative mating under different viability selective regimes acting on the mating cues, specifically focusing on balancing selection regimes promoting polymorphism at locus C .

Let $f(i, k)$ be the frequency of genotype $(i, k) \in \mathcal{G}_C \times \mathcal{G}_P$. We introduce a selection coefficient $S_i(f, h_a)$ acting on genotype $i \in \mathcal{G}_C$, which may vary depending on genotypic frequencies at locus C and dominance between alleles a and b . This allows exploring different regimes of balancing selection, including negative frequency-dependent selection, that can favor polymorphism at locus C . Let w_i be the fitness of genotype i resulting from viability selection acting at locus C :

$$w_i := 1 + S_i(f, h_a). \quad (2)$$

We assume that viability selection generating changes in genotype frequencies at locus C acts before reproduction. As a consequence, the changes in frequencies due to sexual selection depend on the frequencies at locus C after viability selection, described below. For $(i, k) \in \mathcal{G}_C \times \mathcal{G}_P$,

$$f'_{i,k} = \frac{w_i}{\bar{w}} f_{i,k}, \quad (3)$$

with

$$\bar{w} = \sum_{i \in \mathcal{G}_C} w_i \left(\sum_{k \in \mathcal{G}_P} f_{i,k} \right) \quad (4)$$

being the average fitness of the females.

Mate Choice and Reproduction

Reproduction depends on the mating cues controlled by locus C but also on mate preferences controlled by locus P . Each genotype $k \in \mathcal{G}_P$ is associated with a coefficient ρ_k , which quantifies how much a female of genotype k tends to reject males with the same cue as her own (i.e., the strength of disassortative preference of females). The values of ρ_{MM} and ρ_{mm} are fixed. For the genotype Mm , we introduce a dominance coefficient h_m at locus P . Similarly to the dominance at locus C , the coefficient h_m in $[-1, 1]$ describes the dominance of the mutant allele m .

We assume females to be the choosy sex (Lande 1981; Gavrillets and Boake 1998; de Cara et al. 2008; Kopp and Hermisson 2008; Otto et al. 2008), so that males can mate with any accepting females. We assume a balanced sex ratio and consider the frequencies of females and males with genotype i to be equal (Gavrillets and Boake 1998; de Cara et al. 2008; Otto et al. 2008).

To quantify the mating probability between two individuals, we introduce the preference matrix $Pref(\rho_k)$, $k \in \mathcal{G}_P$. For $(i, j) \in \mathcal{G}_C^2$, $k \in \mathcal{G}_P$, the preference matrix is defined by $Pref_{ij}(\rho_k) = 1 - \rho_k Res(ij)$, which measures the strength of preference of female i with genotype k at locus P for male j . Using equation (1), the preference matrix is given by

$$Pref(\rho_k) = \begin{pmatrix} aa & ab & bb \\ 1 - \rho_k & 1 - \frac{1+h_a}{2}\rho_k & 1 \\ 1 - \frac{1+h_a}{2}\rho_k & 1 - \rho_k & 1 - \frac{1-h_a}{2}\rho_k \\ 1 & 1 - \frac{1-h_a}{2}\rho_k & 1 - \rho_k \end{pmatrix} \begin{matrix} aa \\ ab \\ bb \end{matrix}. \quad (5)$$

With the help of this preference matrix describing disassortative mating behavior in the framework of Otto et al. (2008), which was initially designed to explore the evolution of assortative mating, we investigate the evolution of disassortative mating.

For $(i, k) \in \mathcal{G}_C \times \mathcal{G}_P$, we define $T_{i,k}$ as the probability that a female of genotype (i, k) accepts a male during a mating encounter:

$$T_{i,k} = \sum_{j \in \mathcal{G}_C} Pref_{ij}(\rho_k) p'_j, \quad (6)$$

with

$$p'_j := \sum_{l \in \mathcal{G}_P} f'_{j,l} \quad (7)$$

being the proportion of genotype j at the cue locus C in the population after the viability selection step.

Choosy females of genotype k at locus P are assumed to pay a fixed cost $c_f \rho_k$ for their choosiness (the choosier a female is, the higher this cost is). Mating behavior is indeed thought to be more costly for choosy females than for females mating with the first male encountered, regardless of displayed cue. Choosy females also pay a relative cost of choosiness, depending on the proportion of preferred males and on a coefficient $c_r \in [0, 1]$. This relative cost is small if the preferred mates are abundant in the population. When a female rejects a given male because he displays an unpreferred cue, she can still accept another mate with probability $1 - c_r$.

We define the fertility of a female of genotype $(i, k) \in \mathcal{G}_C \times \mathcal{G}_P$ as

$$F_{i,k} = (1 - c_r + c_r T_{i,k})(1 - c_f \rho_k). \quad (8)$$

The average fertility in the population is thus:

$$\bar{F} = \sum_{(i,k) \in \mathcal{G}_C \times \mathcal{G}_P} f'_{i,k} F_{i,k}. \quad (9)$$

Then changes in genotypes frequencies after reproduction are as follows. For $(i', k') \in \mathcal{G}_C \times \mathcal{G}_P$,

$$f''_{i,k'} = \sum_{(i,k) \in \mathcal{G}_C \times \mathcal{G}_P} \left(f'_{i,k} \frac{F_{i,k}}{F} \sum_{(j,l) \in \mathcal{G}_C \times \mathcal{G}_P} \text{coef}_{i',k',i,k,j,l,r} \frac{\text{Pref}_{ij}(\rho_k) f'_{j,l}}{T_{i,k}} \right), \quad (10)$$

where *coef* controls the Mendelian segregation of alleles during reproduction. The term $\text{coef}_{i',k',i,k,j,l,r}$ describes the proportion of individuals of genotype i' at locus C and k' at locus P in the offspring of a choosing individual of genotype i at locus C and k at locus P and a chosen individual of genotype j at locus C and l at locus P . The Mendelian segregation depends on the recombination probability r between the cue locus C and the preference locus P . All variables and parameters used in the model are described in table 1.

Model Exploration

QLE Approximation Exploring the Evolution of Weak Disassortative Preference. We use the QLE analysis results presented in a previous model of evolution of assortative mating (see app. B in Otto et al. 2008). This approach is valid

when the selection coefficients, the strength of choosiness, and the costs of assortment are small relative to recombination; namely, for all $(i, f, h_a) \in \mathcal{G}_C \times \mathcal{F}_{C,P} \times [0, 1]$ (where $\mathcal{F}_{C,P}$ denotes the space of frequencies on $\mathcal{G}_C \times \mathcal{G}_P$) and k in \mathcal{G}_P , $S_i(f, h_a)$, ρ_k , c_r , and c_f are of order ϵ with ϵ small and the recombination rate r of order 1. Under this hypothesis, the genetic associations (linkage disequilibria and departures from Hardy-Weinberg) are small (of order ϵ). This approach allows us to obtain mathematical expressions of allele frequency changes at the cue and preference loci from Hardy-Weinberg equilibrium. This method highlights the key evolutionary mechanisms shaping the evolution of allele frequencies at these loci. In particular, we assume that the mutant allele m increases disassortative preference (i.e., $\rho_{mm} > \rho_{MM}$) and investigate the evolutionary forces acting on this allele. The QLE approximation assumes a weak viability selection at the cue locus C and is mostly relevant to explore the evolution of a weak tendency to disassortative mating (low values of ρ).

Numerical Simulations. We then use numerical simulations to explore the evolutionarily stable level of strength

Table 1: Description of variables and parameters used in the model

	Description
\mathcal{G}_C	Set of possible genotypes at locus C : $\mathcal{G}_C = \{aa, ab, bb\}$
\mathcal{G}_P	Set of possible genotypes at locus P : $\mathcal{G}_P = \{MM, Mm, mm\}$
$f_{i,k}$	Frequency of genotype (i, k) in the population, $(i, k) \in \mathcal{G}_C \times \mathcal{G}_P$
$f'_{i,k}$	Frequency of genotype (i, k) in the population after viability selection, $(i, k) \in \mathcal{G}_C \times \mathcal{G}_P$
$f''_{i,k}$	Frequency of genotype (i, k) in the population after reproduction, $(i, k) \in \mathcal{G}_C \times \mathcal{G}_P$
p_α	Proportion of allele α at locus C in the population (with $\alpha \in \{a, b\}$)
p_m	Proportion of allele m at locus P in the population (with $m \in \{m, M\}$)
r	Recombination probability between the loci C and P
ρ_k	Strength of disassortative mating within a female of genotype $k \in \mathcal{G}_P$ at locus P as described in preference matrix (5)
h_a/h_m	Dominance coefficient at locus C describing the dominance of allele a/m
$S_i(f, h_a)$	Viability selection coefficient when the allele frequencies are f and the dominance coefficient at locus C is h_a
c_f/c_r	Fixed/relative cost of choosiness
D_C	Genetic diversity at locus C , $D_C = p_a p_b$
D_P	Genetic diversity at locus P , $D_P = p_m p_M$
P_{he}^{HW}	Proportion of heterozygotes at Hardy-Weinberg equilibrium, $P_{he}^{HW} = 2p_a p_b$
P_{ho}^{HW}	Proportion of homozygotes at Hardy-Weinberg equilibrium, $P_{ho}^{HW} = p_a^2 + p_b^2$
H_{ns}/H_{ss}	Heterozygote advantage due to viability/sexual selection
H	Heterozygote advantage
$\bar{\rho}$	Average strength of disassortative mating in the population
Δ_ρ	Effect of allele m on the level of disassortative mating in the population
D_{am}	Linkage disequilibrium between alleles a and m within chromosome (<i>cis</i>); $D_{am} = p_{am} - p_a p_m$, where p_{am} is the proportion of the association between alleles a and m within the chromosome
$D_{a,m}$	Linkage disequilibrium between alleles a and m between homologous chromosomes (<i>trans</i>); $D_{a,m} = p_{a,m} - p_a p_m$, where $p_{a,m}$ is the proportion of the association between alleles a and m between homologous chromosomes
D_{he}	Excess of heterozygotes at locus C , $D_{he} = 1 - p_{aa}^2 - p_{bb}^2$
$D_{he,m}$	Trigenic disequilibrium measuring the association between allele m and the excess of heterozygotes at locus C
δ	Fitness reduction in homozygotes in numerical simulations
μ	Asymmetry in viability selection acting on the two homozygous genotypes in numerical simulations

of disassortative mating when the hypothesis of weak selection is relaxed. We specifically focus on a realistic case of viability selection promoting polymorphism at the cue locus, assuming overdominance. We explore the effect of variations in key parameters, in the range where the QLE analysis is not relevant.

To explore the evolution of disassortative mating acting on the cue locus submitted to overdominance, we model a viability selection regime favoring heterozygotes. We thus set the selection coefficients associated with the different genotypes at the cue locus as

$$S_{aa} = -\frac{1 + \mu}{2}\delta, \quad S_{ab} = 0, \quad S_{bb} = -\frac{1 - \mu}{2}\delta, \quad (11)$$

where δ is the fitness reduction in homozygotes and μ is the asymmetry in viability selection acting on the two homozygous genotypes. If $\mu = 1$ (resp. -1) the disadvantage is applied to genotype *aa* (resp. *bb*) only, and if $\mu = 0$ the disadvantage is the same for both homozygotes. To study the evolutionarily stable level of the strength of disassortative mating, we numerically compute the invasion gradient. First we consider a population without a mutant ($p_m = 0$), and for each value of the strength of disassortative mating of the resident ρ_{MM} we let the initial population evolve until the genotype frequencies at the cue locus *C* reach equilibrium. At equilibrium, we introduce the mutant allele *m* with an initial 0.01 frequency. We call $\Delta^{100}p_m$ the change in the mutant frequency after a hundred generations. We then numerically estimate

$$D(\rho_{MM}) = \frac{\partial \Delta^{100}p_m}{\partial \rho_{mm}}. \quad (12)$$

The evolutionarily stable level of strength of disassortative mating is the value ρ for which $D(\rho) = 0$.

We explore the effect of variations in every key parameter (δ , h_a , μ , c_f , and c_r) using independent simulations. The default values for the remaining parameters follow the assumptions: codominance at cue locus $h_a = 0$, $\delta = 1$, pure symmetry in viability selection $\mu = 0$, and low cost of choosiness $c_f = c_r = 0.005$. We assume no recombination $r = 0$ and codominance at preference locus $h_m = 0$.

Results

Sexual Selection at the Cue Locus Generated by Disassortative Mating

Following the QLE approach, the change in frequency of allele *a* at the locus *C* controlling mating cue is (see eq. [B2a] in Otto et al. 2008)

$$\Delta p_a = \underbrace{D_C(p_a(S_{aa}(f, h_a(-S_{ab}(f, h_a))) + p_b(S_{ab}(f, h_a) - S_{bb}(f, h_a))))}_{\text{effect of viability selection}} + \underbrace{\bar{\rho}(1 + c_r)D_C((p_b^4 - p_a^4)/4 + h_a(P_{ho}^{HW} - 2P_{he}^{HW})/4)}_{\text{effect of sexual selection and opportunity cost}} + O(\epsilon^2), \quad (13)$$

where $D_C = p_a p_b$ is the genetic diversity at locus *C*;

$$\bar{\rho} = p_M^2 \rho_{MM} + 2p_M p_m \rho_{Mm} + p_m^2 \rho_{mm} \quad (14)$$

is the average disassortative mate preference at locus *P*; and

$$P_{he}^{HW} = 2p_a p_b, \quad P_{ho}^{HW} = p_a^2 + p_b^2, \quad (15)$$

are respectively the proportion of heterozygotes and homozygotes at Hardy-Weinberg equilibrium. Under the QLE assumption, the departure from Hardy-Weinberg equilibrium is small; hence, the proportions of heterozygotes and homozygotes are close to P_{he}^{HW} and P_{ho}^{HW} .

Equation (13) highlights that the dynamics of the mating cue allele *a* can be affected by viability and sexual selection on males and the relative cost of choosiness impacting females. Contrary to assortative mating, which generates positive frequency-dependent sexual selection, disassortative preferences generate negative frequency-dependent sexual selection on cue alleles (see arrows C and E in fig. 1). The strength of this sexual selection then depends on the average strength of disassortative preference ($\bar{\rho}$). Disassortative mating also generates a relative cost of choosiness on females (see arrow D in fig. 1). Similarly to sexual selection, this cost especially disfavors females displaying a common phenotype because these females tend to prefer males with rare phenotype.

Sexual selection and the relative cost of choosiness also tightly depend on dominance at the cue locus *C*. When $h_a \neq 0$ (departure from codominance), the evolutionary fate of alleles is strongly influenced by their dominance. When heterozygotes are frequent at locus *C*—that is, when allele *a* is neither rare nor common ($P_{ho}^{HW} - 2P_{he}^{HW} < 0$, i.e., $p_a \in (0.21, 0.79)$; see details in app. A [apps. A, B are available online])—allele *a* is favored when recessive ($h_a < 0$) because *aa* homozygotes then display the rarest phenotype and therefore benefit from improved reproductive success. By contrast, when heterozygotes are rare at locus *C* ($2P_{he}^{HW} - P_{ho}^{HW} < 0$), allele *a* is favored when dominant ($h_a > 0$). Indeed, when allele *a* is rare ($p_a < 0.21$), *bb* individuals are numerous and preferentially mate with individuals displaying the phenotype encoded by allele *a* (the rare phenotype). Therefore, when *a* is dominant, *ab* individuals benefit from a greater mating success than *bb* individuals, thereby increasing the frequency of allele *a*. When the cue allele *a* is common ($p_a > 0.79$), the dominance of allele *a* limits the reproductive success of the few remaining heterozygotes *ab* displaying the frequent phenotype shared with homozygotes *aa*, as allele *b* is mostly present

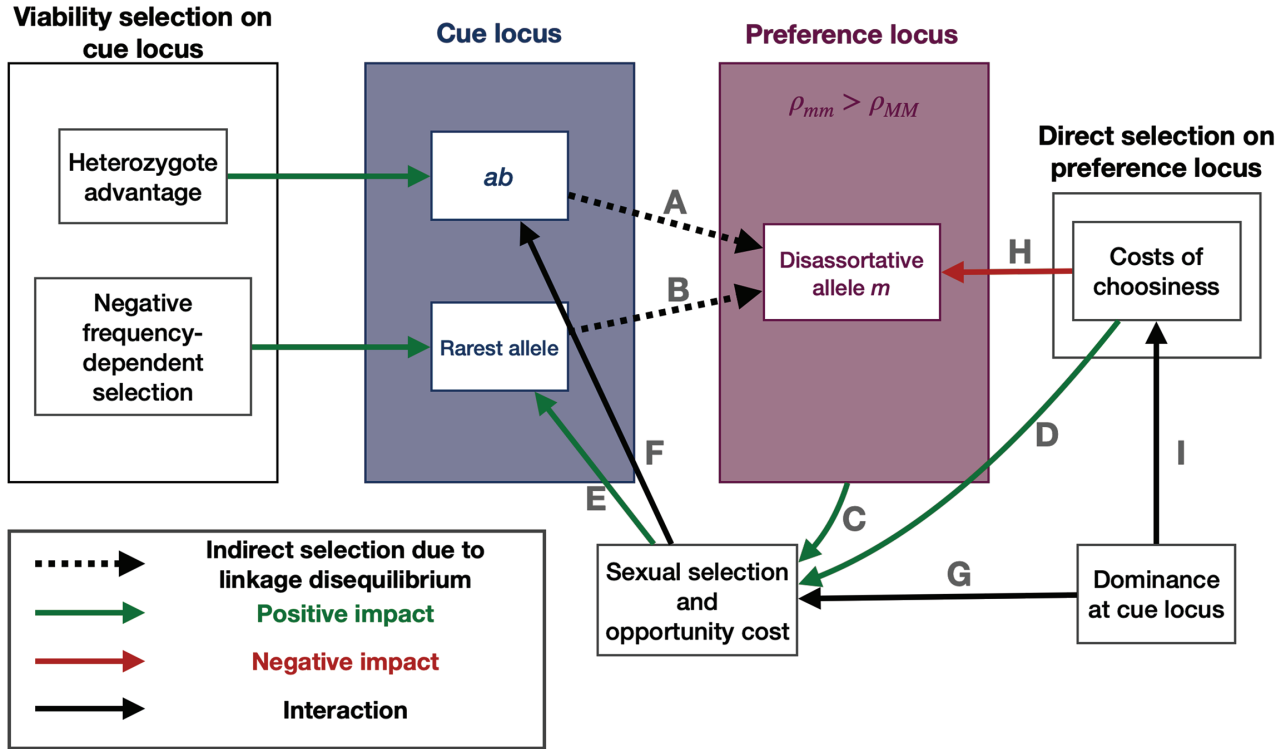


Figure 1: Selective forces acting on cue and preference loci. Dotted arrows represent indirect selection due to positive linkage disequilibrium between cue genotype and preference genotype. Green and red arrows represent the positive and negative impact, respectively. Black arrows represent an impact that is either positive or negative (see text for details). A disassortative allele is promoted by heterozygote advantage (arrow A) and negative frequency-dependent viability selection (arrow B) at the cue locus via indirect selection due to linkage disequilibrium. Disassortative mating triggers sexual selection on males (arrow C) and opportunity costs on females due to a cost of choosiness (arrow D) that generates negative frequency-dependent sexual selection (arrow E) and impacts the fitness of heterozygotes at the cue locus (arrow F). Sexual selection often causes a disadvantage to heterozygotes at the cue locus, hampering the fixation of disassortative mating. However, the dominance relationship at the cue locus impacts sexual selection (arrow G). Under certain conditions, sexual selection favors heterozygotes at the cue locus (arrow C), promoting high levels of disassortative mating. The disassortative allele suffers from costs of choosiness (arrow H). These costs depend on the dominance relationship at the cue locus (arrow I).

in heterozygotes, which leads to the gradual elimination of the alternative allele b .

These conclusions are drawn from the QLE approximation and are relevant for moderate levels of disassortative mating (low values of ρ). Stronger levels of disassortative mating may lead to contrasted outcomes because some crosses (e.g., $aa \times aa$) will occur at very low frequency.

Evolutionary Fate of Disassortative Mating Mutants

To understand the conditions enabling the evolution of disassortative mating, we now approximate the change in frequency of the mutant allele m at the preference locus P associated with an increased level of disassortative preference compared with the resident allele M . The QLE analysis highlights that the evolution of disassortative mating depends on (1) the heterozygote advantage, (2) the genetic variation at the cue locus C , and (3) the costs of choosiness,

described by the terms $\Delta^{he}p_m$, Δ^Cp_m , and $\Delta^{cost}p_m$, respectively. Assuming that ϵ is small, we get (see eq. [B3a] in Otto et al. 2008)

$$\Delta p_m = \Delta^{he}p_m + \Delta^Cp_m + \Delta^{cost}p_m + O(\epsilon^3). \quad (16)$$

In the following sections we define these three terms and dissect the evolutionary mechanisms acting on preference alleles.

Disassortative Mating Is Promoted by Heterozygote Advantage at the Cue Locus. The impact of heterozygote advantage on the frequency of the mate choice allele m is given by

$$\Delta^{he}p_m = D_{he,m}H, \quad (17)$$

where $D_{he,m}$ (see eq. [20]) is the trigenic disequilibrium describing the association between the mutant m at the mate choice locus P and heterozygotes at the cue locus C and

H is the heterozygote advantage at the cue locus C (see eq. [18]). The fitness advantage of heterozygotes H can be influenced by both viability and sexual selection, as detailed below:

$$H = \underbrace{2S_{ab}(f) - S_{aa}(f) - S_{bb}(f)}_{\text{viability selection acting on cues } (H_v)} + \underbrace{\frac{1}{2}(p_a^2 H_{aa} + 2p_a p_b H_{ab} + p_b^2 H_{bb})}_{\text{sexual selection acting on cues } (H_s)} \quad (18)$$

The sexual selection promoting heterozygotes at the cue locus C depends on mate preferences for heterozygotes over homozygotes expressed by the different genotypes $i \in \mathcal{G}_C$ at locus C (H_i):

$$H_i = 2\text{Pref}(\bar{\rho})_{i,ab} - \text{Pref}(\bar{\rho})_{i,aa} - \text{Pref}(\bar{\rho})_{i,bb}. \quad (19)$$

The effect of heterozygote advantage at the cue locus C on the disassortative mating allele m is then modulated by the association between the mutant m and heterozygotes at the cue locus (i.e., the trigenic disequilibrium $D_{he,m}$), as described by equation (17). At QLE, the trigenic disequilibrium satisfies

$$D_{he,m} = \frac{1}{2} D_p \Delta D_{he} + O(\epsilon^2), \quad (20)$$

where D_{he} is the excess of heterozygotes at locus C due to allele m and $D_p = p_M p_m$ is the genetic diversity at locus P .

The trigenic disequilibrium depends on the change in the excess of heterozygotes due to allele m following a single round of mating. This change depends on (1) the fraction of homozygotes at the cue locus C , determined by allele frequencies (p_a and p_b) and dominance relationships (h_a) and (2) the increase in disassortative preferences in the population Δ_p (eq. [21]):

$$\Delta D_{he} = D_C^2 \Delta_p (P_{ho}^{HW} + h_a(p_b - p_a)) + O(\epsilon^2). \quad (21)$$

The increase in disassortative preferences Δ_p depends on the effect of the mutant m at the preference locus P and its frequency (eq. [22]):

$$\Delta_p = p_m(\rho_{mm} - \rho_{Mm}) + p_M(\rho_{Mm} - \rho_{MM}). \quad (22)$$

The change ΔD_{he} has the same sign as the increase in disassortative preferences Δ_p (for details, see app. A). As the mutant m increases the strength of disassortative preferences (i.e., $\rho_{mm} > \rho_{MM}$), $\Delta D_{he} > 0$, meaning that individuals with disassortative preferences tend to produce more heterozygotes at locus C . As a consequence, mutant alleles m , increasing disassortative preferences, are preferentially associated with heterozygotes at the cue locus C . The disassortative mutant m is thus promoted when viability and sexual selection both favor heterozygotes at the mating cue locus C (see arrow A in fig. 1). This contrasts

with the assortative mating model of Otto et al. (2008), where the assortative allele is preferentially associated with homozygotes at the cue locus, suggesting that assortative mating can be promoted when homozygotes are favored.

Dominance relationships affect the change in the frequency of heterozygotes. For instance, when a rare cue allele is dominant, a round of moderate disassortative mating (i.e., ρ_{MM} and ρ_{mm} are small) produces more heterozygotes than when the rarer cue allele is recessive. Indeed, when the dominant allele is rarer, individuals with disassortative preferences have a higher fecundity because dominance reduces the cost of choosiness (see an explanation for this phenomenon in the section “The Costs of Choosiness Limit the Fixation of Disassortative Mating”).

Sexual Selection Produced by Disassortative Mating Generates a Heterozygote Disadvantage, Limiting the Evolution of Such a Behavior. As described above, the disassortative alleles m tend to be preferentially associated with heterozygotes at locus C . Because ab heterozygotes with disassortative preferences (i.e., carrying an m allele) mate preferentially with either of the aa or bb homozygotes (depending on the dominance relationship), the evolution of disassortative preferences is likely to generate a sexual selection disfavoring heterozygotes at locus C . This mechanism may hamper the fixation of allele m and limit the evolution of disassortative mating in natural populations. This effect is determined by the mating success of heterozygotes at locus C . From equation (18), this sexual selection term can be written as

$$H_{ss} = \bar{\rho} \left(-\frac{P_{he}^{HW}}{2} + \frac{h_a}{2}(p_b - p_a) \right). \quad (23)$$

Sexual selection on heterozygotes depends on the strength of disassortative mating ($\bar{\rho}$), the allele frequencies at locus C (p_a and p_b), and the dominance of allele a (h_a). Assuming codominance at the cue locus ($h_a = 0$), sexual selection always disfavors heterozygotes at the cue locus (see arrow F in fig. 1). The more common disassortative preferences are in the population, the higher this sexual selection acting against heterozygotes is. Since the disassortative allele m is preferentially associated with heterozygotes at the cue locus, it suffers from sexual selection caused by disassortative mating. The spread of a disassortative allele is thus limited by this negative feedback.

However, the sexual selection acting against heterozygotes at the cue locus depends on the dominance relationship at the cue locus (see arrow G in fig. 1). Assuming strict dominance at the cue locus ($h_a = -1$ or $h_a = 1$), heterozygous individuals are indistinguishable from homozygotes, thus modifying the proportion of phenotypes in the population. Heterozygote advantage at the cue locus due to sexual

selection increases when the most common allele is recessive: when allele a is recessive and common heterozygous males ab have the same phenotype as homozygotes bb , ab males then display the rarest phenotype and benefit from negative frequency-dependent selection. When the dominant cue allele is sufficiently rare, sexual selection favors heterozygotes (see app. A), generating a positive feedback loop favoring the evolution of disassortative mating (see arrow F in fig. 1). However, this effect should often be transient because negative frequency-dependent sexual selection rapidly balances phenotypic cue frequencies. In the general case where allele frequencies are balanced at the cue locus, sexual selection is thus expected to limit the evolution of disassortative mating.

Such a negative effect of sexual selection has already been described for the evolution of assortative mating (Otto et al. 2008). Nevertheless, since (1) the assortative allele is preferentially associated with homozygotes at the cue locus and (2) assortative mating promotes homozygotes, the negative effect of sexual selection on the evolution of assortative mating is expected to be more limited than for disassortative mating, where (1) the disassortative allele is preferentially associated with heterozygotes at the cue locus and (2) disassortative mating disfavors heterozygotes.

Disassortative Preferences Are Favored When the Rarer Allele Is Promoted. The change in the frequency of cue alleles impacts the evolution of preference alleles. This impact is described by the term

$$\Delta^c p_m = (D_{am} + D_{a,m}) \frac{\Delta p_a}{D_C}. \quad (24)$$

As highlighted in equation (24), the invasion of a disassortative mutant m depends on its linkage with the cue allele a (either in *cis* or in *trans*, described by D_{am} and $D_{a,m}$, respectively) and on the variation in the frequency of allele a (Δp_a). If allele m is associated with allele a , the frequency of allele m increases with the rise of frequency of allele a . The QLE approximates the *cis* and *trans* linkage disequilibria between the mutant allele m and the cue allele a as

$$\begin{aligned} D_{am} &= D_{a,m} + O(\epsilon^2) \\ &= \frac{D_p D_C}{2} \Delta \rho \left((p_b^4 - p_a^4) + \frac{h_a}{2} (P_{ho}^{HW} - P_{he}^{HW}) \right) \\ &\quad + O(\epsilon^2). \end{aligned} \quad (25)$$

The terms D_{am} and $D_{a,m}$ have the same sign as $p_b - p_a$ (for more details, see app. A); thus, D_{am} and $D_{a,m}$ are positive (resp. negative) when allele a is the rarer (resp. most common). Contrary to assortative alleles preferentially associated with the most common cue allele (Otto et al. 2008),

equation (25) indicates that the disassortative mating allele m tends to be linked with the rarer allele at locus C . This predicts that disassortative mating is likely to emerge when viability selection on the cue provides fitness benefit to rare alleles (see arrow D in fig. 1), while assortative mating is promoted when the most common cue alleles are favored.

Disassortative allele m also tends to be more tightly linked either to the dominant cue allele when the frequency of homozygotes is high or to the recessive allele when the frequency of heterozygotes is high (i.e., when $(h_a/2)(P_{ho}^{HW} - P_{he}^{HW}) \geq 0$), increasing the association between alleles a and m . The effect of dominance can thus modulate the association between allele m and the rarer cue allele.

Given that (1) the disassortative allele m is associated with the rarer cue allele and (2) disassortative mating promotes the rarer allele via sexual selection, the disassortative mating allele m could benefit from a positive feedback loop promoting the evolution of disassortative mating. However, negative frequency-dependent sexual selection rapidly increases the frequency of the initially rare allele, limiting the spread of the m allele in the population. The initially rarer allele may become as common as the other allele, breaking the linkage disequilibrium between allele m and alleles at the cue locus. Thus, this positive effect of sexual selection on the evolution of disassortative mating could be broken with the increase of the initially rarer allele frequency.

The Costs of Choosiness Limit the Fixation of Disassortative Mating. The evolution of mate preferences is generally limited by the costs associated with choosiness. Equation (26) shows that both fixed and relative costs of choosiness indeed limit the fixation of the disassortative mutant m (see arrow H in fig. 1):

$$\begin{aligned} \Delta^{cost} p_m &= -\frac{\Delta_p}{2} D_p \left(c_f + c_r \left(\text{mate}_0 + \frac{1}{2} \text{mate}_1 \right. \right. \\ &\quad \left. \left. + \frac{h_a}{2} (\text{mate}_1^a - \text{mate}_1^b) \right) \right), \end{aligned} \quad (26)$$

where mate_i , $i \in \{0, 1\}$, and mate_1^α , $\alpha \in \{a, b\}$, describe the proportion of mating partners sharing different numbers of alleles (see eqq. [27] and [29]). The costs of choosiness disfavor preference alleles, increasing disassortative choices (i.e., when $\rho_{mm} > \rho_{MM}$; for details, see app. A). The relative cost of choosiness then crucially depends on the proportion of preferred mates. This effect can be captured by the parameters mate_k , $k \in \{0, 1\}$, representing the probability that a female encounters a male differing by k alleles at locus C at Hardy-Weinberg equilibrium:

$$mate_0 = p_a^2 p_a^2 + 2p_a p_b 2p_a p_b + p_b^2 p_b^2, \quad (27)$$

$$mate_1 = p_a^2(2p_a p_b) + 2p_a p_b(p_a^2 + p_b^2) + p_b^2(2p_a p_b). \quad (28)$$

The mating between individuals differing by zero ($mate_0$) or one cue allele ($mate_1$) may be partially avoided when individuals have a disassortative preference, resulting in a cost c , for the choosy female that may fail to find a suitable male. The term $mate_0 + (1/2)mate_1$ is minimal when $p_a = p_b$, so that the impact of the relative cost of choosiness is weaker when the cue alleles are in similar proportions in the population, maximizing the opportunities for females to find a male displaying the preferred cue. The dominance at the cue locus C then modulates the crosses at Hardy-Weinberg equilibrium between individuals carrying at least one allele a ($mate_1^a$) and between individuals carrying at least one allele b ($mate_1^b$)

$$mate_1^a = p_a^2(2p_a p_b) + 2p_a p_b(p_a^2), \quad (29)$$

$$mate_1^b = p_b^2(2p_a p_b) + 2p_a p_b(p_b^2). \quad (30)$$

When a is dominant ($h_a > 0$), matings between individuals sharing at least one allele a ($mate_1^a$) are limited by disassortative preference, leading to an increased cost of choosiness. By contrast, matings between individuals sharing at least one allele b ($mate_1^b$) are promoted by disassortative preference, therefore limiting the cost of choosiness. The difference between $mate_1^a$ and $mate_1^b$ is thus crucial to understanding the impact of the dominance relationship at locus C on the cost of choosiness. This difference is given by

$$mate_1^a - mate_1^b = 4p_a p_b(p_a - p_b). \quad (31)$$

Thus, when a is dominant ($h_a > 0$), the relative cost of choosiness is limited when allele a is rare because bb homozygotes will frequently meet ab heterozygotes displaying their preferred cue. Symmetrically, the cost of choosiness acting on the mutant allele m is higher when the most common cue allele is dominant. The dominance relationship therefore also influences the evolution of disassortative mating by modulating the costs of choosiness (see arrow I in fig. 1).

Recombination Rate Does Not Impact the Evolution of Disassortative Mating Based on a Matching Rule under the QLE Hypothesis. The QLE approximation revealed no effect of the recombination rate r between cue and preference alleles on allelic frequency changes, suggesting that it does not impact the evolution of disassortative mating. Similarly, recombination does not impact the analytical results brought by the QLE approach applied to the evolution of assortative mating (Otto et al. 2008). These two models

assume mate preferences based on a matching rule—that is, that females use their own cue to choose their mate (Kopp et al. 2018). Under this assumption, a mutant allele m immediately translates into disassortative mating in any female carrying it, independently from her genotype at the cue locus. By contrast, assuming a trait/preference rule—that is, when females choose their mate independently of their own cue—any preference allele in a female does not always generate a disassortative behavior, depending on her genotype at the cue locus. Under such a preference/trait hypothesis, the recombination rate would likely impact the evolution of disassortative preference.

Evolution of Disassortative Mating Assuming Strong Overdominance at the Cue Locus

The QLE approximation allows us to draw analytic approximations for the change in frequencies at both loci, assuming low levels of selection. Appendix B shows that QLE approximations are relevant when the parameters $S_i(f, h_a)$ for all $(i, f, h_a) \in \mathcal{G}_C \times \mathcal{F}_{C,P} \times [0, 1]$, ρ_i for all $i \in \mathcal{G}_C$, c_r and c_f are small but are not valid outside these conditions. Since we could not perform a local stability analysis using analytical derivation, we run numerical simulations to study ecological situations where viability selection at the cue locus can be strong and/or marked mate preferences lead to high rate of disassortative mating.

Well-documented cases of disassortative mating in a natural population present a strong heterozygote advantage (Tuttle et al. 2016; Jay et al. 2021). We thus focus on the evolution of disassortative mating acting on a cue locus where strong overdominance is operating (fig. 2).

Recombination Between Cue and Preference Loci Does Not Impact the Evolution of Disassortative Mating. We demonstrate using the QLE approach that the recombination rate between cue and preference alleles does not impact the evolution of disassortative mating. However, QLE assumes that recombination is strong compared with the strengths of preference and selection. We numerically evaluate the effect of the recombination rate on the evolutionarily stable level of disassortative mating when this assumption is violated and find consistent results (fig. 2a). These results certainly emerge from the matching rule used in the model.

Disassortative Mating Is Favored by Asymmetrical Overdominance. Our simulations show that the difference between the fitness of heterozygotes and homozygotes has a strong effect on the evolution of disassortative mate preferences (fig. 2b, 2c). Higher levels of disassortative mating are favored when heterozygotes at the cue locus are advantaged by viability selection (i.e., when homozygotes

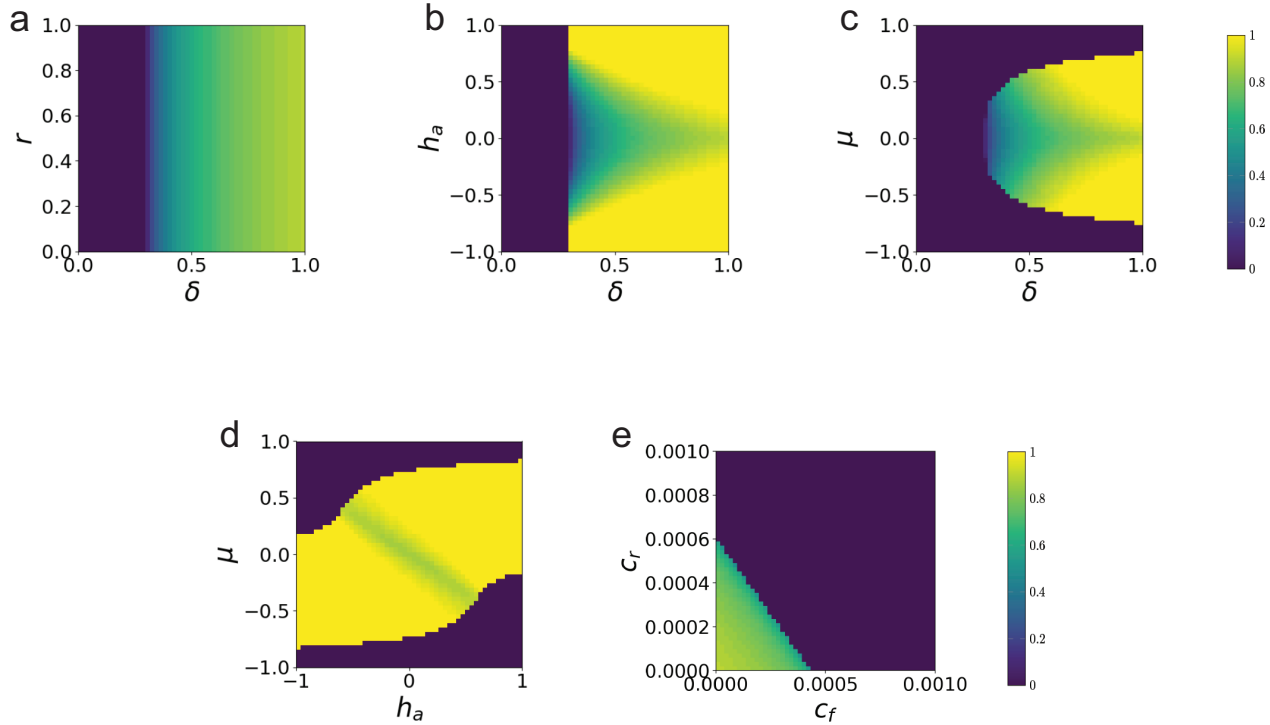


Figure 2: Evolutionarily stable level of strength of disassortative mating ρ acting on a cue locus submitted to overdominance. We plotted the evolutionarily stable level of the strength of disassortative mating ρ . The effects of key parameters on the evolution of the disassortative mating acting on the cue loci submitted to overdominance are explored in the different panels. *a*, Effect of fitness reduction in homozygotes δ and of dominance coefficient at the cue locus C h_a . *b*, Effect of fitness reduction in homozygotes δ and asymmetry in this reduction on the two homozygotes μ . *c*, Effect of dominance coefficient at the cue locus C h_a and asymmetry in the fitness reduction on the two homozygotes μ . *d*, Effect of fixed cost of choosiness (c_f) and relative cost of choosiness (c_r). The default parameters values are as follows: $h_a = h_m = 0$, $r = 0$, $\delta = 0.9$, $\mu = 0$, and $c_r = c_f = 0.005$.

suffer from a significant genetic load δ ; fig. 2*b*, 2*c*), consistent with the predictions brought by the QLE approximation. Interestingly, higher levels of disassortative mating are favored when there is a moderate asymmetry (μ) in the negative selection acting on homozygotes at the cue locus, that is, when one of the two cue alleles is associated with a stronger genetic load (fig. 2*c*). Selection indirectly acting on mating preference indeed crucially depends on genotypic frequencies at the cue locus C , which become unbalanced under asymmetrical selection. Unbalanced cue allele frequencies tend to increase the frequency of homozygotes compared with the frequency of heterozygotes, increasing the relative advantage of heterozygotes due to viability selection, to sexual selection, and to opportunity cost. As disassortative preference tends to be linked with heterozygotes, high levels of disassortative mating are favored by the unbalanced cue allele frequencies.

Because disassortative mating mutants are preferentially associated with the rare allele (carrying the recessive genetic load), once the asymmetrical selection against the rare allele is too strong, it prevents the emergence of the

disassortative mating alleles associated with this maladaptive cue allele. When the negative viability selection on the rare allele is lower than a threshold, viability selection allows the emergence of the disassortative mating mutant and even favors the evolution of stronger levels of disassortative mating because as the level of disassortative behavior increases, the disadvantage of being associated with the rarer allele becomes weaker.

Asymmetrical overdominance therefore promotes the evolution of disassortative mating preference, but only when the asymmetry in the genetic load associated with cue alleles is not too high.

Interactions between Dominance and Fitness of Cue Alleles Determine the Evolution of Disassortative Mate Preferences. High levels of disassortative mating are favored when dominance relationships at the cue locus are strict (i.e., when allele a [resp. b] is fully dominant to b [$h_a = 1$] [resp. a ($h_a = -1$)], as highlighted in figure 2*b*). The dominant allele is disfavored by sexual selection generated by disassortative mating. When the dominant allele is rare, the

association between disassortative preference and cue heterozygosity increases, promoting high levels of disassortative mating. Moreover, when the dominant allele is rare, the impact of the costs of choosiness on frequency changes is lower, further promoting high levels of disassortative mating.

When combining both effects leading to unbalanced cue allele frequencies (i.e., dominance and asymmetrical negative selection on cue alleles), we show that high levels of disassortative mating are strongly favored when the fitness reduction in homozygotes is associated with the dominant cue allele (fig. 2*d*). This numerical result is consistent with the prediction drawn from the QLE approximation because the dominant allele is here present at a low frequency (because of both viability and sexual selection).

The Challenging Evolution of Disassortative Mating. Numerical simulations confirm that the evolution of disassortative mating is challenging when moderate overdominance (enhancing the fitness of heterozygotes) is at play at the cue locus. In most cases, strict disassortative mating is not favored. The higher the disassortative preferences, the more sexual selection acts against heterozygotes. When heterozygote advantage is not strong enough, sexual selection caused by mating preferences can overcome heterozygote advantage, favoring an intermediate level of disassortative mating (see the green areas in fig. 2*b*, 2*c*). By contrast, when viability selection produces a strong heterozygote advantage (δ is high) that can compensate sexual selection, complete disassortative preferences can be fixed (see fig. 2*b*, 2*c*).

The costs of choosiness may further limit the evolution of the disassortative mutant. Figure 2*e* shows that disassortative mating is under positive selection only when the costs of choosiness are limited (at least inferior to 0.03).

Discussion

Predicted Selection Regimes Promoting Disassortative Mating Match Empirical Observations

Our results show that disassortative mating is promoted either (1) when heterozygotes at the cue locus are on average fitter than homozygotes or (2) when viability selection on the cue favors the rarest cue allele. These selection regimes promoting disassortative mating are opposed to the selection regimes promoting assortative mating, such as homozygote advantage at the cue locus or viability selection on the cue favoring the most common allele (Otto et al. 2008; see table 2).

Interestingly, our simulations also show that higher levels of disassortative mating are promoted when one cue allele is dominant. The dominance relationship can indeed decrease sexual selection and the relative cost of choosiness, impairing the evolution of disassortative preferences.

Simulations also highlight that higher levels of disassortative mating are promoted when the dominant allele is disfavored when homozygous. This effect is consistent with the observed cases of disassortative mating. For instance, the butterfly *Heliconius numata* displays strong disassortative mating based on wing pattern phenotype (in a tetrad experiment, three-fourths of the realized crosses involved disassortative pairs; Chouteau et al. 2017). In this species, the variation in wing pattern morphs is controlled by a supergene with three main haplotypes (Joron et al. 2011). The dominant haplotypes are associated with a low survival of homozygous larvae (Jay et al. 2021). This case of disassortative mating seems to gather the conditions pinpointed by our model to enable the evolution of higher levels of disassortative mating.

Similarly, in the white-throated sparrow *Zonotrichia albicollis*, an almost strict disassortative mating based on

Table 2: Comparison between the evolution of disassortative mating based on the present study and the evolution of assortative mating based on Otto et al.'s (2008) study

	Present model studying the evolution of disassortative mating	Otto et al. (2008) model studying the evolution of assortative mating
Viability selection on mating cue that promotes preferences	Heterozygote advantage Negative frequency-dependent viability selection	Homozygote advantage Positive frequency-dependent viability selection
Sexual selection on mating cue due to preferences	Is expected to disadvantage heterozygotes unless one type of homozygote is common and heterozygotes display the same mating cue as rare homozygotes Negative frequency-dependent sexual selection	Is expected to disadvantage homozygotes unless females sufficiently reject males differing by one cue allele and homozygotes are common Positive frequency-dependent sexual selection
Relative cost of choosiness	Lower when one type of homozygote is common and heterozygotes display the same mating cue as rare homozygotes	Lower when one type of homozygote is common

alternative cues on the evolution of disassortative mating will then depend on viability selection. Cotto and Servedio (2017) show that contact between populations promotes a higher level of assortative mating because individuals adapted to different habitats produce intermediate offspring maladaptive in each habitat. Contact between locally adapted populations may thus limit the evolution of disassortative mating because it generates viability selection against hybrids, disfavoring such preferences.

Mating opportunities also depend on the distribution of cues in the population. A more balanced cue distribution within a population often increases the negative effect of sexual selection on the evolution of assortative preferences (Otto et al. 2008). For instance, migration between populations has been shown to limit the evolution of further assortative mating because it promotes a more balanced polymorphism within populations and therefore increases the negative effect of sexual selection (Servedio 2011). Similarly, migration between populations may limit the evolution of disassortative mating because the resulting more balanced polymorphism increases the negative sexual selection.

Negative Feedback in the Evolution of Disassortative Mating Contrasts with the Evolution of Assortative Mating

A striking result from our analyses stems from the role of sexual selection generated by disassortative preferences on its evolution, which contrasts with the evolutionary dynamics of assortative mating. Our results confirm that the sexual selection generated by disassortative mating often limits its own spread, as already mentioned by Nuismer et al. (2008). Indeed, the disassortative mating allele is generally associated with heterozygotes at the cue locus. Individuals with such allelic combinations tend to preferentially mate with homozygotes, generating sexual selection disfavoring heterozygotes at the cue locus. However, this sexual selection acting against heterozygotes depends on the distribution of cue allele frequency (for more details, see table 2).

Similarly, the evolution of assortative mating is thought to be limited by sexual selection (Otto et al. 2008), although sexual selection can promote the evolution of assortative mating in some cases (for more details, see table 2). However, this negative effect of sexual selection decreases when the proportion of homozygotes at the cue locus is high. Assortative mating usually produces more homozygotes than random mating: a decrease in the level of heterozygosity at the cue locus is thus expected when assortative preferences are spreading within a population. During the evolution of assortative mating, the negative effect of sexual selection on the evolution of assortative mating decreases as the proportion of homozygotes increases. The evolution

of disassortative mating may therefore be more severely impaired by sexual selection than the evolution of assortative mating.

In two meta-analyses (Jiang et al. 2013; Janicke et al. 2019) covering 1,116 and 1,447 measures of strength of assortment, respectively, most of the values corresponding to disassortative mating range from -0.5 to 0 (but see the exception below), suggesting that high values of strength of disassortative mating are rarely observed. By contrast, most values corresponding to assortative mating behavior range from 0 to 1 , suggesting that the evolution of strict assortative mating is observed in a wide range of organisms.

Jiang et al. (2013) and Janicke et al. (2019) also show that weak disassortative mating is rare. This observation is unlikely to reflect the negative feedback of sexual selection on the evolution of disassortative preferences precisely because this effect is weak when preferences are weak. The rarity of weak disassortative mating may instead reflect the effect of a cost of choosiness, which increases with the proportion of heterozygotes in the population, which is itself promoted by the selection regimes that favor disassortative mating.

Alternative Genetic Architectures of Mate Preferences May Limit the Evolution of Disassortative Mating

The genetic architecture of preference may also have an impact on the evolution of disassortative mating. Theoretical studies of the evolution of assortative mating usually rely on two main types of matching rules (Kopp et al. 2018): (1) when mate choice of an individual depends on its own phenotype (matching rule) and (2) when preference is independent from the phenotype of the chooser (preference/trait rule). The evolution of assortative mating is strongly promoted either when assuming the matching rule or when the cue and preference/trait loci are tightly linked (Kopp et al. 2018). Here, our results on the evolution of disassortative mating are obtained assuming a matching rule, and we expect that assuming a preference/trait rule might limit such an evolution because selection might break the nonmatching allelic combinations. In the specific case of polymorphic mimicry, Maisonneuve et al. (2021) showed that under the preference/trait rule, disassortative mating can emerge only if the preference and the cue loci are fully linked.

Moreover, here we consider only a single choosy sex. However, when both sexes are choosy (Servedio and Lande 2006), the positive selection on the evolution of mate preference in one sex may be relaxed when strong mate preferences are fixed in the other sex (Aubier et al. 2019). Drift then leads to periodic cycles where males and females alternatively become the most choosy sex (Aubier et al. 2019).

Conclusions

Our analytical and numerical results provide a general theoretical framework establishing the conditions enabling the evolution of disassortative mating. Our results pinpoint two selective regimes on mating cues that promote disassortative mating through indirect selection: heterozygote advantage and negative frequency-dependent selection. We also observe that disassortative mating generates sexual selection that often hampers its own fixation, leading to an intermediate level of disassortative mating. This sexual selection depends on the dominance at the cue locus: if one type of homozygote at the cue locus is common and if heterozygotes display the same cue as the rare homozygote, sexual selection promotes the evolution of disassortative mating. We also show that this condition reduces the costs associated with choosiness. Interestingly, the favorable selective conditions predicted by our model match with two well-characterized cases of strong disassortative mating.

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Statement of Authorship

L.M., V.L., C.S., and T.B. conceived and designed the study. L.M. analyzed the model. L.M. wrote the manuscript with contributions from all authors. V.L. and C.S. supervised the thesis of L.M. M.J. and V.L. obtained funding from ANR SUPERGENE (ANR-18-CE02-0019).

Data and Code Availability

Code is available online at <https://github.com/Ludovic-Maisonneuve/when-do-opposites-attract> (Zenodo: <https://doi.org/10.5281/zenodo.5091606>; Ludovic-Maisonneuve 2021).

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“The illustrations of the peccary and American bison are examples of the wood cuts, a large proportion of which are borrowed from Brehm’s *Thierleben*.” Figured: “The American Bison.” From the review of the *Standard Natural History* (*The American Naturalist*, 1884, 18:808–809).