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Low temperature study of phase equilibria in the Co–Ni–W ternary system: evidence of a new intermetallic phase Co₃W-D0_a

Nicolas Bouliez^{1,2}, Jérôme Andrieux², Rodica Chiriac², François Toche², Jean-Claude Crivello³, Bruno Gardiola², Sophie Cazottes⁴, Florence Robaut⁵, Rafael Cury¹, Olivier Dezellus²

ABSTRACT

Tungsten heavy alloys (Co–Ni–W) of different compositions were prepared by powder metallurgy (solid sintering), heat treated at 800°C and 1000°C and subsequently analyzed. The experimental phase identifications and composition measurements emphasized discrepancies compared to the isothermal ternary sections simulated with commercial thermodynamic databases.

The isothermal sections at 800° C and 1000° C were found more complex than expected since a new intermetallic phase appeared to be stable ($D0_a$ structure - Cu_3 Ti prototype). Likewise, an interpretation of phase equilibria evolution with temperature was established to reach agreement with high temperature data. Formation enthalpies associated with the new phase were obtained through first-principles calculations and supported experimental results as they confirmed the stabilizing role of Ni addition for the $D0_a$ structure.

Keywords

A. Intermetallics

B. Powder metallurgy

C. Phase diagrams

D. Thermal analysis; X-ray diffraction

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1. Introduction

The Co–Ni–W system is involved in many industrial applications including Co-based and Ni-based superalloys, cemented carbide materials or tungsten heavy alloys (WHAs). Ni-based superalloys are fit for turbojet engines and marine propulsion turbines. The alloying elements found in nickel based superalloys are chosen for solid solution and Y/Y' precipitation strengthening [1]. The nickel-based superalloys may comprise 10 alloying elements including Co and W and the resulting constitutional complexity must be controlled with care to avoid deleterious phase precipitation (σ , μ , and Laves phases) after long time operation at elevated temperatures [2]. WHAs are employed as balance weights, radiations shields and kinetic energy penetrators amongst other applications. Their W content may reach 96wt%. These alloys have a composite microstructure described by *Fig 1*. The hard tungsten nodules with a body-centered cubic lattice (called σ phase or BCC_A2) are surrounded by a matrix which is a ternary solid solution with face-centered cubic lattice composed mostly of W, Ni, Co (called σ phase or FCC_A1). The mechanical properties of WHAs are mainly driven by the interfacial strength between the σ and σ phases. Thus, it is of utmost importance to avoid intermetallic precipitation at interfaces during manufacturing processes as it causes severe embrittlement.

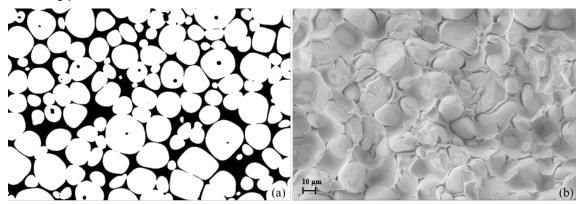


Fig 1. (a) WHAs composite microstructure (SEM/BSE) and (b) rupture analysis of an embrittled alloy (SEM/SE2) observed with magnification x500. - Source: Plansee Tungsten Alloys.

Nowadays alloy designs are computer assisted thanks to the CALPHAD method [3] which enables the assessment of phase equilibria and may predict the microstructure. However, CALPHAD modeling requires experimental data collected in the whole range of thermodynamic variables (mostly compositions and temperature). In the case of the Co–Ni–W system, several CALPHAD models were suggested for the binary subsystems Ni–W [4,5], Co–W [6–11] and Co–Ni [12], whereas only one attempt to model the ternary Co–Ni–W system is reported in the literature by Guillermet in 1988 [13]. At that time, few experimental results were available and most of them corresponded to high temperature phase equilibria at temperatures above 1300°C. Since then, new experimental results, obtained from diffusion multiples at intermediate temperatures (800 and 900°C), were reported [14] and are in contradiction with available thermodynamic description [13]. One of the most striking discrepancy is the Ni/Co substitution ratio in the Co₃W phase that is lower than 0.63 (29 at% Ni) according to Guillermet's model [13], while Zhu et al. [14] reported a maximum value of about 4 (62 at% Ni) at 800°C.

If confirmed, this extension of the Co_3W-DO_{19} phase might have important consequences, preventing for example the precipitation of Co_7W_6 - μ phase in FCC phase during heat treatment in this temperature range. Hence, new experimental data at intermediate temperatures are needed to improve the knowledge on phase stability in composition and temperature and phase equilibria in the ternary system. It is a mandatory step before any improvement of the CALPHAD model initially proposed by Guillermet.

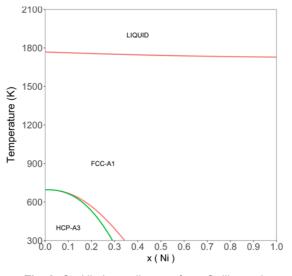
In order to resolve this discrepancy concerning extension in composition of the Co₃W-DO₁₉ phase below 1000°C, samples with different Ni/Co ratios and a constant tungsten content (30 at%) were synthesized and heat treated at 800°C and 1000°C. The samples were characterized by X-ray diffraction and electron diffraction, scanning electron microscopy, electron probe micro analysis and thermogravimetric - differential scanning calorimetric (TGA-DSC) analysis. Also, in order to sustain experimental results, formation enthalpies of intermetallic structures were obtained by electronic Density Functional Theory (DFT) calculations at 0 K.

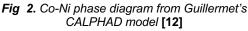
2. Available thermodynamic descriptions

The Co–Ni binary system is characterized by a complete solid solubility in the FCC_A1 phase. It goes from the solidus to the allotropic transformation into the HCP_A3 ε phase in Co-rich side of the diagram. By modelling separately the magnetic and non-magnetic contributions to the Gibbs energy, Guillermet [12] carried out a CALPHAD Co–Ni system assessment (*Fig* 2).

The Ni-W system was studied by various authors and discrepancies in experimental observations arose. Indeed, an intermetallic phase of composition NiW was observed by Walsh and Donachie [15] and later by Hofmann [16] with diffusion couple experiments and heat-treated alloys respectively. Poulsen et al. [17] claimed observing at equilibrium the intermetallic phase NiW2, along with the NiW phase, in sintered samples made of W wires surrounded by a Ni matrix. The indexations performed by these authors from X-ray diffraction were judged as incoherent by Cury et al. [18] who did not detect these intermetallic phases at 950°C for any of the sintered, arc-melted or induction-melted alloys. Cury et al. found very good agreement in terms of position and relative intensity between the XRD patterns obtained by Hofmann [16], Poulsen et al. [17], Walsh and Donachie [15] and a simulated Ni₆W₆C pattern. Cury et al. concluded that NiW and NiW₂ were misidentified with the Ni₆W₆C and Ni₂W₄C carbides whose formation is favored by C contamination of surfaces, a key point in case of diffusion couple experiments. Finally, it was concluded that the only stable intermetallic phase present in the Ni-W system was the body-centered tetragonal phase Ni₄W (s.g. I4/m - MoNi₄ type - D1_a). A thermodynamic assessment, performed by P. Gustafson et al. [4] in 1986, included the both non-existing intermetallic phases NiW and NiW2. More recently, I. Isomäki et al [5] proposed a new modeling of the Ni-W system (Fig 3) taking consideration of Cury et al. results on stable intermetallic phases. Authors also performed DFT calculations combined to phonon calculations to evaluate stability of several compounds. They confirmed the presence of three intermetallic structures on the convex-hull: the bodycentered tetragonal phase Ni₄W; the orthorhombic Ni₃W-D0a phase (s.g. Pmmm, Cu₃Ti prototype considered here as D0a); and the Ni₈W compound with martensitic-like Bravais lattice (s.g. I4/mmm -NbNi₈ type). However the intermetallic phases Ni₃W-D0_a and Ni₈W were experimentally observed only

in extreme conditions [19,20] and their thermodynamic stability under normal condition remains uncertain.





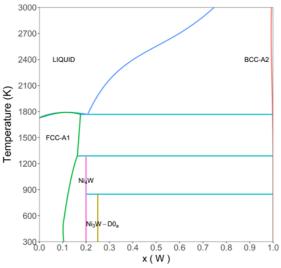


Fig 3. Ni-W phase diagram from Isomäki et al. CALPHAD model [5]

The Co–W binary system was evaluated extensively [6–11] with two intermetallic phases named Co₃W-DO₁₉ (s.g. *P63/mmc* – Ni₃Sn type - *D*O₁₉) and Co₇W₆-μ (or μ phase, s.g. *R-3m* – Fe₇W₆ type - *D*8₅) whose decomposition invariant temperatures were measured as 1093°C [21] and 1689°C [22] respectively. *Sato et al.* [8] simulated the Co₃W-DO₁₉ phase with two sublattices allowing a solubility range and could well reproduce the Co-rich composition side of the intermetallic phase measured in their work. On the contrary, Guillermet [6] chose to model the Co₃W-DO₁₉ phase as a stoichiometric compound. The Co₇W₆-μ phase shows a wider homogeneity range and was modelled, for simplification purposes, with three sublattices by several authors [6–10]. J-M. Joubert and N. Dupin [23] showed the need of different occupancies on the two Wyckoff positions with coordination number 12 for the Co₇W₆-μ phase (3*a* and 18*h*) and therefore recommended the use of a 4 sublattices model. Pure Co magnetic contribution to the Gibbs energy is significant. It must be taken into account for the description of intermetallic endmembers when using formation enthalpies calculated with DFT [9–11]. The FCC_A1 phase magnetic ordering leads to a monotectöid transformation (*Fig 4*) from paramagnetic FCC_A1 to ferromagnetic FCC_A1 and Co₃W-DO₁₉ as predicted by Guillermet's CALPHAD assessment and confirmed experimentally by Östberg [24] and Sato *et al.* [8].

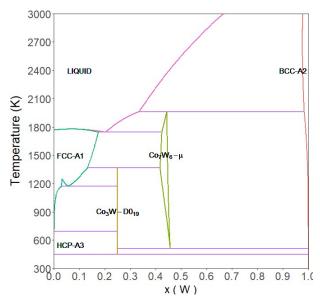


Fig 4. Co-W phase diagram drawn from Guillermet's CALPHAD modeling [6].

The Co-Ni-W ternary system was assessed in the late eighties by Guillermet [13] and the calculated isothermal section at 1000°C is proposed on *Fig 5*.

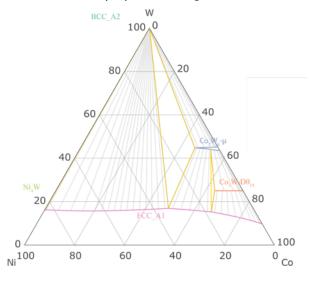


Fig 5. Calculated isothermal section at 1000°C according to Guillermet's assessment [13].

At that time the experimental measurements on the system were very scarce and some unpublished works carried out at the Royal Institute of Technology in Stockholm were used for parameters optimization. Sources for experimental data obtained at 1300° C and 1400° C by several authors could not be all verified. Tungsten content of the Co_7W_6 - μ phase as modelled by Guillermet [13] appears quite low as compared to experimental measurements [25]. Discrepancies at 1000° C from Shipovskov *et al.* [26] experimental results stood out. Indeed, binary phase domains were found from the CALPHAD model located at compositions where ternary phase domains were experimentally found and inversely.

Also, the ternary domain FCC_A1 + $Co_7W_6-\mu$ + Co_3W-D0_{19} defined by Guillermet was too narrow as compared to Shipovskov's experimental results.

Some years later, Zhu *et al.* [14] built diffusion multiples in the Co–Ni–W system which underwent long annealing heat treatments at 800°C and 900°C for 2200 hours and 1010 hours respectively. Diffusion multiples suffered from carbon impurity which formed Ni₂W₄C and Ni₆W₆C carbides at the interface with tungsten and prevented the measurement of most tie-lines. However, tie-lines obtained after EPMA measurements exhibited nickel solubility in Co₃W-DO₁₉ ranging from 13 at% at 900°C to 62 at% at 800°C. These values strongly differed from the ones issued from Guillermet's modeling that were respectively 6.5 at% and 29 at% [13].

Consequently, the available thermodynamic description of the ternary Co–Ni–W system is inconsistent mostly at temperatures lower than 1300°C where experimental measurements are both scarce and in disagreement. From the results presently obtained and the past investigations, the phases considered for the Co–Ni–W ternary system are listed in

Table 1.

Phase name	Space Group	Prototype	Number of sublattices
FCC_A1 (Y)	Fm-3m	Cu	1
BCC_A2 (α)	Im-3m	W	1
HCP_ <i>A</i> 3 (ε)	P6₃/mmc	Mg	1
Ni_4W	14/m	Ni ₄ Mo	2
(Co,Ni) ₃ W- <i>D</i> 0 ₁₉	P6₃/mmc	Ni₃Sn	2
(Co,Ni) ₃ W-D0 _a	Pmmn	Cu₃Ti	3
Co_7W_6 - μ	R-3m	Fe ₇ W ₆	5

Table 1. Phases reported in the Co-Ni-W ternary system.

3. Experimental procedure

Samples were prepared from pure Co, Ni and W powders which chemical compositions are described in *Table 2*. The compositions of most samples (except sample 51W) were chosen with a fixed W (30 at%) and variable Ni content (from 15 to 40 at%, see *Table 3*). The powders were blended for 30 min to get homogeneous distribution of the elements and then milled with Co–Ni–W WHA balls for 30 min. Milled powders were isostatically pressed at 190 MPa. Samples were solid-state sintered at 1440°C for one hour under a pure hydrogen atmosphere to reduce the oxide layer on the powder surface. The samples were then cooled at a controlled 5°C.min⁻¹ rate down to 800°C and then, inertially.

	Maximum impurity										
content (ppm)											
Element	Element Ni Co										
С	800	300	30								
S	10	50	5								
Fe	100	200	100								
Ni	1	100	/								
Ca	1	100	/								
Na	1	100	10								
Si	1	100	30								
Мо	1	1	30								

Table 2. Chemical composition of elemental powders used in this work.

Sample	Initial	Compos (at%)	sition	Phases identified by	Composition	determined by E	PMA (at%)
identification	Со	Ni	W	XRD	$Co_{(\sigma)}$	$Ni_{(\sigma)}$	$W_{(\sigma)}$
Ni15	55	15	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 ₁₉	46,86 _(0.19) 58.05 _(0.58)	8.51 _(0.32) 18.94 _(0.65)	44,63 _(0.26) 23.00 _(0.32)
Ni17.5	53.5	17.5	30	Co ₇ W ₆ - µ Co ₃ W- <i>D</i> 0 ₁₉	/ /	/ /	/ /
Ni20	50	20	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 ₁₉	43.11 _(0.53) 52.53 _(0.43)	11.43 _(0.46) 23.91 _(0.34)	45.46 _(0.17) 23.56 _(0.13)
Ni21.5	48.5	21.5	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 _a	43.37 _(0.69) 50.66 _(0.45)	11.28 _(0.71) 25.75 _(0.44)	45.35 _(0.24) 23.59 _(0.10)
Ni23	47	23	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 _a	/ /	/ /	/ /
Ni25	45	25	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 _a	40.13 _(0.36) 47.08 _(0.27)	14.32 _(0.21) 29.60 _(0.27)	45.55 _(0.21) 23.32 _(0.07)
Ni30	40	30	30	Co_7W_6 - μ Co_3W - DO_a	35.51 _(0.61) 40.58 _(0.27)	17.78 _(0.62) 35.10 _(0.32)	46.71 _(0.42) 24.32 _(0.31)
Ni40	30	40	30	Co ₇ W ₆ - μ Co ₃ W-D0 _a BCC_A2	32.32 _(0.59) 31.70 _(0.38)	21.23 _(0.40) 44.46 _(0.34)	46.46 _(0.32) 23.84 _(0.09)
51W	23.1	52.1	24.8	FCC_A1 Co₃W-D0₃ BCC_A2	24.39 _(0.54) 24.09 _(1.27)	59.00 _(1.23) 52.49 _(0.98) -*	16.61 _(0.41) 23.42 _(0.41) -*

^{*:} High uncertainties on EPMA measurements.

Table 3. Samples initial composition and composition of the phases formed in Co–Ni–W powder mixtures after 720h at 1000°C.

A 15 mm diameter slice of each as-sintered cylinder was cut using electrical discharge machining. Slices were wrapped in tantalum foils. Samples were then sealed in a silica bulb under residual argon

^{/:} EPMA measurements not performed on the sample.

atmosphere and underwent a 1500 hours long annealing heat treatment at 800±5°C or a 720 hours long annealing heat-treatment at 1000°C±5°C followed by rapid quenching in water.

Afterwards each slice was cut in two pieces to conduct different characterizations. Half of the samples was resin-mounted, grinded and meticulously polished (finish with colloidal silica solution) to enable EDS and WDS composition measurements. Scanning Electron Microscopy (SEM) on a Zeiss Merlin Compact was conducted under 15 kV accelerating voltage to observe the samples microstructure. EDS point measurements were performed with an Oxford Instruments X-Max^N detector using electronic standards to approximate the composition of the phases involved in the equilibria at 800°C and 1000°C. In order to measure the chemical compositions accurately, the samples heat treated at 1000°C were also characterized using electron probe microanalysis (EPMA) and pure standards for the 3 elements (Co, Ni and W). The measurements were carried out on a SX100 Cameca microprobe with a 18 kV accelerating voltage, a 60 nA probe current, LiF monochromators for Co and Ni K_{α} radiations and a TAP monochromator for W M_{α} radiation. Quantitative procedure for analysing the samples used the PAP $\Phi(pz)$ model from Pouchou and Pichoir [27].

Sample N, of specific composition (Ni/Co ratio of 0.7 and 25.5 at% W) was also included in the heat treatments at 1000°C. From this sample, a thin foil was prepared using Focused Ion Beam and a JEOL 2010 LaB6 Transmission Electron Microscope operated at 200kV was used in order to characterize the Co₃W-D0_a like intermetallic phase using Electron Diffraction.

The other half of samples treated at 1000°C were crushed into powders at room temperature using a dedicated jar along with a ball both made of tungsten carbide. The powders were sieved to reach a particle size below 20 μ m in diameter. Sieved powder was suspended in 5 mL ethanol with silicon powder (XRD internal reference) and the resulting suspension was sonicated for 5 minutes. Droplets of this suspension were deposited on a zero background monocrystalline corundum substrate for XRD. The diffractograms were acquired on a Bruker D8 advance using the Cu radiation ($\lambda_{\alpha 1}$ = 1,54060 Å and $\lambda_{\alpha 2}$ = 1,54439 Å) for 8 hours with a 20 step of 0.008° in 0-0 Bragg Brentano geometry over the 20 range 10-60°. The divergence slits were fixed to 0.3° opening for radial divergence and a 4mm mask was used for axial divergence. Le Bail refinement was performed with the Fullprof software [28] to confirm phase identification and to measure the lattice parameters of the intermetallic phases. Le Bail refinements were conducted in isotropic conditions to achieve a satisfactory profile matching. The samples heat treated at 800°C were characterized as bulk specimen after removing surface layers and polishing to sharply reduce the surface roughness. The diffractograms were acquired in the same conditions as the ones selected for samples heat treated at 1000°C.

Sample	Sample Initial Compositio		sition	Phases identified by	Composition determined by EDS (at%)			
identification	Co	(at%) Ni	W	XRD	$Co_{(\sigma)}$	$Ni_{(\sigma)}$	$W_{(\sigma)}$	
Ni20	50	20	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 ₁₉	43.11 _(0.28) 52.86 _(1.10)	11.50 _(0.28) 22.62 _(1.26)	45.39 _(0.19) 24.52 _(0.33)	
Ni21.5	48.5	21.5	30	Co ₇ W ₆ - µ Co ₃ W- <i>D</i> 0 ₁₉	<i>I I</i>	<i>I</i>	<i>l</i>	
Ni23	47	23	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 ₁₉	41.22 _(0.59) 49.57 _(0.54)	12.94 _(0.70) 25.78 _(0.70)	45.84 _(0.22) 24.65 _(0.32)	
Ni25	45	25	30	Co ₇ W ₆ - μ Co ₃ W- <i>D</i> 0 ₁₉	39.91 _(0.49) 47.05 _(0.61)	14.23 _(0.49) 28.70 _(0.76)	45.86 _(0.28) 24.24 _(0.64)	
Ni30	40	30	30	Co ₇ W ₆ - µ Co ₃ W- <i>D</i> 0 _a	35.59 _(0.48) 41.07 _(0.53)	$17.99_{(0.47)} \\ 34.43_{(0.73)}$	46.42 _(0.41) 24.50 _(0.50)	
Ni40	30	40	30	BCC_A2 Co ₃ W- <i>D</i> 0 _a	_* 32.29 _(0.34)	-* 43.14 _(0.53)	-* 24.57 _(0.61)	
Ni54.5	15.5	54.5	30	BCC_A2 Co ₃ W-D0 _a	-* 16.84 _(0.47)	-* 58.68 _(0.34)	-* 24.48 _(0.42)	

^{*:} Uncertainties on EDS measurements are high because of the size of the phases and operating conditions leading to a risk of an interaction volume bigger than the size of the phase.

Table 4. Samples initial composition and composition of the phases formed in Co–Ni–W powder mixtures after 1500h at 800°C.

TGA-DSC analyses were performed on the crushed powders of samples heat treated at 1000°C. For all analyses, the TGA/DSC3+ device from Mettler-Toledo was used and samples were put into 150 μL alumina crucibles. Temperature calibration was achieved with the melting temperature measurements of In, Al and Au standards. Analyses were run under a purified argon flow using a type N Subtronic purifier and the tested sample masses were very close to each other. The cycle consisted in a 20°C.min⁻¹ heating ramp to 950°C, an isothermal dwell at 950°C for 30 minutes followed by a 5°C.min⁻¹ heating ramp to reach 1200°C. The decomposition onset temperature of the Co₃W like phases was assessed as the temperature for which a fixed value for the baseline deviation was reached as illustrated in *Fig 9.a.* TGA-DSC analyses were also done for several samples heat treated at 800°C on bulk specimens. The isothermal dwell was set at 780°C for 30 minutes and was followed by a 5°C.min⁻¹ heating ramp up to 1200°C.

First principle calculations were performed using the Density Functional Theory (DFT) under the General Gradient Approximation (GGA) with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation energy functionals expression [29]. The VASP code was used with the Projector Augmented Wave (PAW) approach [30]. The energy cut-off for the PAWs was set to 600 eV. The ZenGen script [31] was used to automatically organize the input files for every end-member and adopt progressive relaxation steps. Magnetic moments were calculated using a spin polarized model once all relaxation steps for the non-magnetic state were achieved. The irreducible Brillouin zone (BZ) was sampled using high-density k meshing of 0.05 Å-1 points for each primitive cell. The formation enthalpy at 0 K of every ternary

^{/ :} EDS measurements not performed on the sample.

end-members for the Co₇W₆-µ phase with its 5 sublattices (3⁵=243 configurations), the Co₃W-DO_a phase with its 3 sublattices (3³=27 reduced to 14 unique configurations, since the crystal sites present similar environment and the permutation of atoms leads to some degenerated configurations) and the Co₃W-DO₁₉ phase with its 2 sublattices (3²=9 configurations) were calculated by total energy differences of compound with their weighted elements in their stable reference state. Special Quasirandom Structure (SQS) using MCSQS [32,33] tool were considered to generate cells with a mixing of atoms for the Co₃W-DO_a phase to compare relative stability of partial occupancies. The clusters considered for the SQS study were limited to 9 pairs, 7 triangles and 4 tetrahedra to design 48 to 72-atoms SQS cells depending of the studied compositions.

4. Results and discussions

4.1. Phase Equilibria

X-rays diffraction was performed on each sample. The diffractograms obtained from suspended powders deposition for sample Ni15 to sample Ni25 are shown in $\it Fig. 6$. Profile matchings achieved in isotropic conditions with Fullprof were characterized by the reliability R-factors related to points with Bragg contributions corrected for background. These R-factors are characterized by R_p <25, R_{wp} <18 and Chi2 <4.

For low Ni content (samples Ni15, Ni17.5 and Ni20), the Co_7W_6 - μ phase was identified together with Co_3W - DO_{19} at 1000°C. According to diffraction peaks positions and Le Bail refinement, the later phase crystallizes in the $P6_3/mmc$ space group with a=5.125 Å, c=4.148 Å as refined lattice parameters for sample Ni20.

A change is observed in diffraction peaks existence and position between sample Ni20 and sample Ni21.5. This is visible from the triplet found between 25 ° and 30 °20 or the doublet around 35 °20 on *Fig* 6. These diffraction peaks can be attributed by Le Bail refinement to a Co_3W-DO_a phase. This phase is isostructural to the Ni₃Mo compound and it crystallizes in the *Pmmn* space group with a=5.113 Å, b=4.141 Å and c=4.463 Å as refined lattice parameter for sample Ni21.5. Consequently, X-ray diffraction analysis reveals a structural transition at 1000°C from Co_3W-DO_{19} to Co_3W-DO_a caused by nickel addition with nominal concentration from 20 at% to 21,5 at%.

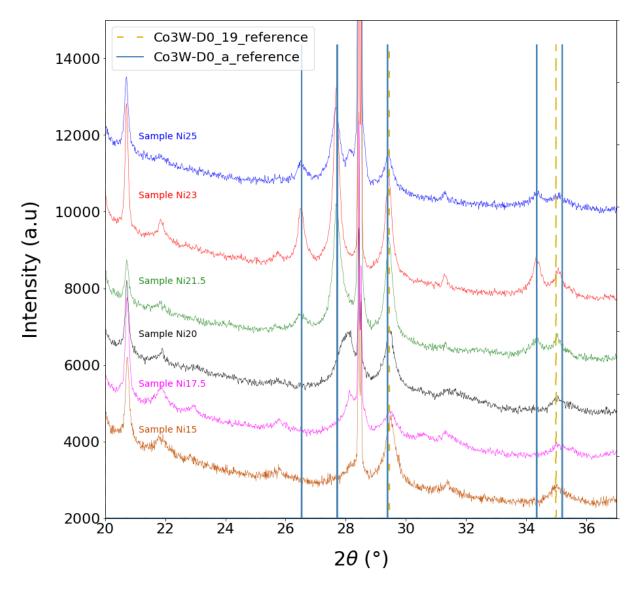


Fig 6. Evolution of powder diffractograms obtained in a serie of W–Ni–Co samples with constant 30 at%.W and increasing Ni content after 720 h at 1000 °C. Samples are crushed after heat treatment and sieved powders deposited on monocrystalline corundum substrate. Characteristic lines for Co₃W-DO_a and Co₃W-DO₁₉ structures are added for lecture. Diffraction peak at 20.7 °2θ is from Co₇W₆-μ phase. Addition of Si XRD internal reference is observed at 28.47 °2θ.

Sample N (heat treated at 1000° C) TEM measurements confirmed the Co_3W-D0_a structure. The FIB sample location is illustrated on *Fig* 7.(a) and was extracted in an area containing only Co_3W-D0_a phase. As Co_3W-D0_a and Co_3W-D0_{19} present very similar structures, most of the electron diffraction pattern recorded could be indexed with both phases, except the $<1\bar{1}0>$ presented in *Fig* 7.(c). This specific orientation allowed to discriminate between the two phases, since the (110) and $(00\bar{1})$ planes of the Co_3W-D0_a structure are in diffraction conditions. Triplet of plans $\{101\}$ are used in X-ray diffraction analysis to distinguish between the two phases as the diffractograms were very similar and many peaks were convolved with the ones from the Co_7W_6 - μ phase.

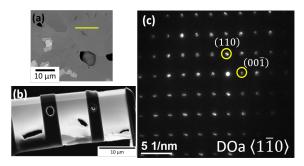


Fig 7. (a) Location of the extraction zone of the FIB sample used for electron diffraction study, (b) SEM-SE observation of the thin foil and (c) Small Area Electron Diffraction pattern of one of the grain oriented $\langle 1\overline{1}0 \rangle$ and indexed as Co_3W-DO_a phase.

The annealing heat treatments at 800°C and 1000°C led to thermodynamic equilibrium as it is illustrated in *Fig 8* for sample Ni40. Three phases in contact with each other are observed at 1000°C, illustrating the existence of a three-phase equilibrium. X-rays powder diffraction performed on the crushed sample allows the identification of the phases BCC_A2, Co₃W-D0_a and Co₇W₆-µ. EPMA measurements reveal that the maximum Ni solubility in the Co₇W₆-µ phase is 21.23 at%.Ni at 1000°C (*Table 3*). In addition, this sample emphasizes the stability of a Co₃W-D0_a structure with a Ni content of 44.46 at%.

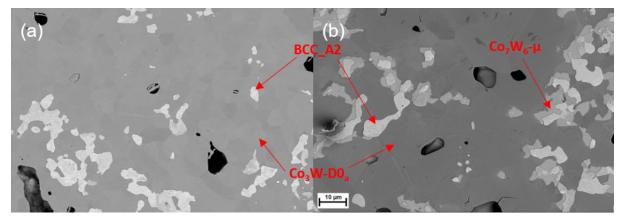


Fig 8. Microstructure of sample Ni40 after 1500 h at 800 °C (a) and after 720 h at 1000°C (b) observed with SEM in BSE mode (magnification x1000).

Experimental measurements in *Table 3* confirm the stability of the BCC_A2+Co₃W-D0_a binary phase domain at 1000°C as well as the two ternary phase domains BCC_A2+Co₃W-D0_a+FCC_A1 and BCC_A2+Co₃W-D0_a+Co₇W₆-μ. From EPMA compositions for both Co₃W-D0_a and Co₃W-D0₁₉, a shift from stoichiometry is observed since the tungsten content is slightly lower than 25 at%. (*Table 3*). There is also a trend for an increase in tungsten content of the Co₇W₆-μ phase in equilibrium with Co₃W-D0_a or Co₃W-D0₁₉ with nickel addition. The composition obtained at 1000°C with EDS were in very good agreement with the ones measured with EPMA. Thus, EPMA measurements for samples heat treated at 800°C were not necessary provided that EDS measurements were performed in the same conditions as the ones already compared with EPMA at 1000°C.

Composition measurements and phase identification obtained for the samples treated at 800°C (*Table* 4) show a decrease in the maximum Ni dissolution for the Co₇W₆-µ phase (<21,23 at% Ni) and a shift

towards lower Co content for the ternary phase domain BCC_A2+Co₃W-D0_a+FCC_A1 if compared with samples treated at 1000°C.

TGA-DSC analyses on samples heat treated at 1000°C defined the decomposition onset temperature of the Co₃W-like phases as the kinetics for the monovariant reactions are fast. The decomposition onset temperature for sample Ni30 heat treated at 1000°C is shown on *Fig 9.a* by a vertical line. The evolution in the onset temperatures as a function of the samples nominal Ni/Co ratio is shown on *Fig 9.b*. In this figure, a previous measurement is included and was obtained on a sample richer in Co than sample Ni20, obtained from an arc melted pellet heat treated at 1000°C. The phase transition between Co₃W-D0₁₉ and Co₃W-D0_a is conspicuous since the onset decomposition temperature first decreases with low Ni addition and then increases when the nominal Ni content is higher than 21.5 at%. Indeed, there is a fall in the Co₃W-D0₁₉ decomposition onset temperature from 1093°C in the Co–W binary system to 1035°C for sample Ni20 heat treated at 1000°C. The decomposition onset temperature for the Co₃W-D0_a phase from sample Ni25 to sample Ni40 around 1045°C is stable. The onset decomposition temperature for higher Ni content decreases as illustrated for sample 51W.

Samples Ni21.5, Ni23 and Ni25 heat treated at 800°C were studied with TGA-DSC to show the Co₃W-DO₁₉ to Co₃W-DO_a phase transition between 800°C and 1000°C. As illustrated in *Fig 10* for sample Ni25, the DSC curves did not allow the identification of any phase transition below 1000°C. It may be caused either by sluggish kinetics below 1000°C or by the nature of the phase transition. The later may be of the second order and thus corresponds to an athermal structure transition. Sluggish kinetics were confirmed for the Co₃W-DO_a decomposition with sample Ni54.5 (Ni/Co=3.52) treated at 800°C. The onset decomposition temperature was measured around 995°C, which is inconsistent with EPMA measurements of sample 51W (Ni/Co=1.83) heat treated at 1000°C. Phase change kinetic limitations was also observed with sample Ni40 heat treated at 800°C for which two thermal phenomena were expected from structural data shown in *Table 3* and *Table 4*. However, there was only the Co₃W-DO_a phase decomposition that was detected with the DSC curve. The onset decomposition temperatures of samples heat treated at 1000°C must be considered as maximum temperatures for phase transition in thermodynamic assessment. Therefore, delay in temperature due to sluggish kinetics must be accounted for.

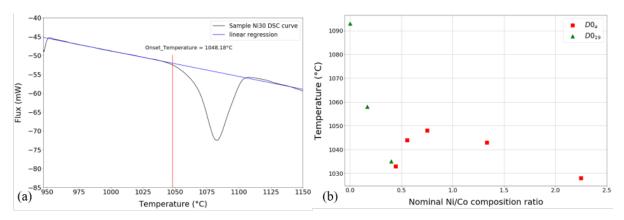


Fig 9. (a) DSC onset decomposition temperature assessment for sample Ni30 heat treated 720 hours at 1000°C and (b) onset decomposition temperature evolution of Co₃W like phases as a function of the nominal Ni/Co composition ratio obtained from samples equilibrated at 1000°C.

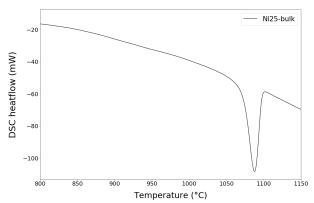


Fig 10. DSC curve of sample Ni25 heat treated at 800°C.

An isothermal section at 1000°C of the ternary Co–Ni–W system is suggested in *Fig 11*. The change in tie-line orientation between sample Ni20 and sample Ni21.5 (as well as a common measured composition for the Co_7W_6 - μ phase for both samples) draw a thin Co_7W_6 - μ + Co_3W - $D0_a$ + Co_3W - $D0_{19}$ ternary phase domain perimeter. It is consistent with TGA-DSC and XRD measurements performed on samples heat-treated at 1000°C . The sample compositions Ni17.5, Ni20, Ni21.5, Ni23 were used to verify experimentally the Co_7W_6 - μ + Co_3W - $D0_a$ + Co_3W - $D0_{19}$ ternary phase domain existence. Ternary phase domain occurrence is supported in this work, even though the attempt to check its existence was unfruitful. XRD and EDS measurements performed on samples heat-treated at 800°C and 1000°C as well as TGA-DSC analyses show a shift towards the Co rich side of the Co–Ni–W system of the expected ternary phase domain $(\text{Co}_7\text{W}_6$ - μ + Co_3W - $D0_a$ + Co_3W - $D0_1$ 9) when the temperature increases. From these observations, an invariant phase transformation Co_3W - $D0_a$ + Co_3W - $D0_1$ 9 when the ternary phase domain FCC_A1+ Co_7W_6 - μ + Co_3W - $D0_a$ should shift quickly towards Ni rich side of the Co–Ni–W system when temperature increases beyond 1030°C.

We can affirm that the highest Ni/Co nominal ratio to avoid precipitation of any intermetallic phase between 800°C and 1000°C is higher than 3.52 in the Co–Ni–W system. This is in agreement with the results from Zhu et al. [14] but is in contradiction with the CALPHAD modeling from Guillermet [13].

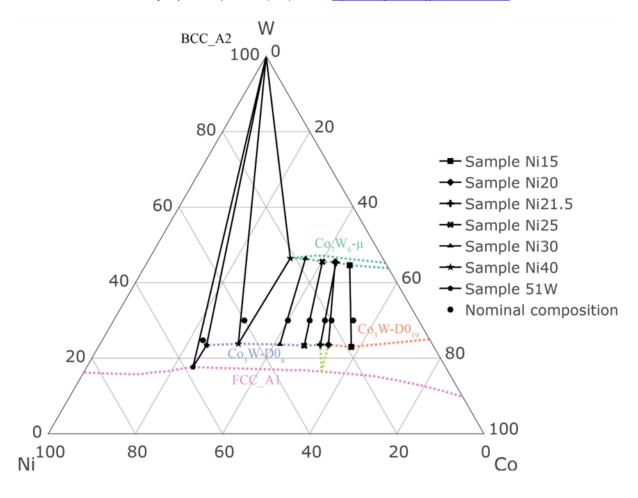


Fig 11. Experimental EMPA composition measurements of samples heat treated 720 hours at 1000°C superimposed on the proposed isothermal section of the W–Ni–Co system at 1000°C.

4.2. DFT calculations and phase stability

	Composition		Lattice parameters (Å)			Atomic positions					
Phase	x(Co)	x(Ni)	x(W)	а	b	С	Site label	x	у	Z	
Co ₃ W-D0 ₁₉	I-D0 ₁₉ 0.75 0 0.25 5.0965 5.0965 4.0835	4.0835	6 <i>h</i> -Co	0.162	0.324	0.75					
CO3 VV- DO19	0.75	0	0.25	0.0000 0.0	J.0303 J.0303 4.0	4.0633	5.0965 4.0835	2 <i>c</i> -W	1/3	2/3	0.25
C- W D0	0.50	0.25	0.25	5.1653	4.0889	4.3998	4e-Co	0.25	0.00	0.672	
Co ₃ W-D0 _a	0.50	0.25	0.25	5. 1053	4.0889	4.3998	2a-Ni	0.25	0.25	0.182	

Table 5 summarizes the crystallographic data obtained from DFT calculation in a given ordered configuration for both Co₃W-D0₁₉ and Co₃W-D0_a. In Co₃W-D0₁₉ structure, Co and W atoms are located on Wyckoff position 6*h* and 2*c* respectively since Co₃W-D0₁₉ is a thermodynamically stable ordered structure from the HCP_A3 solid solution at 1000°C. Ni substitution to Co is expected on atomic site 6*h* until the solubility limit of Ni in this phase is reached. In Co₃W-D0_a structure, Ni and Co atoms occupy Wyckoff positions 2*a* and 4*e* respectively whereas W atoms are located on 2*b* Wyckoff position.

	Composition		Lattice parameters (Å)			Atomic positions						
Phase	x(Co)	x(Ni)	x(W)	а	b	С	Site label	x	у	Z		
Co ₃ W-D0 ₁₉	0.75	0	0.25	5.0965	5.0965	4.0835	6 <i>h</i> -Co	0.162	0.324	0.75		
CO3 VV- DO19	0.73	U	0.23	3.0903	3.0903	4.0633	4.0000	4.0000	2 <i>c</i> -W	1/3	2/3	0.25
C - W D0	0.50	0.05	0.05	E 46E0	4.0000	4 2000	4e-Co	0.25	0.00	0.672		
Co ₃ W-D0 _a	0.50	0.25	0.25	5.1653	4.0889	4.3998	2a-Ni	0.25	0.25	0.182		

Table 5. Structure comparison from DFT calculations.

Formation enthalpies for both intermetallic phases Co₃W-DO_a and Co₃W-DO₁₉ are provided in *Table* 6 and *Table* 7Erreur! Source du renvoi introuvable. respectively. Formation enthalpies in Co₃W-DO_a of the X:A:B and X:B:A configurations were found identical when A and B atoms were swapped between sites 2a and 2b since coordination distances of the 12 nearest neighbors for sites 4e, 2a and 2b were the same. Likewise, A:B:B and B:A:A configurations led to the same formation enthalpies. This degeneracy caused the reduction from 27 to 14 unique configurations as indicated in *Table* 6.

Comparable samples	Atom on site 4e	Atom on site 2 <i>a</i>	Atom on site 2b	x(Co)	x(Ni)	x(W)	ΔH (kJ/mol)
1	Co	Со	Со	1	0	0	-0.025
1	Co	Co	W	0.75	0	0.25	-5.215
1	Co	W	W	0.5	0	0.5	5.113
1	W	Co	W	0.25	0	0.75	32.303
1	W	Ni	W	0	0.25	0.75	25.864
1	W	Ni	Ni	0	0.5	0.5	3.479
1	Ni	Ni	W	0	0.75	0.25	-10.380
1	Ni	Ni	Ni	0	1	0	2.192
Ni23	Co	Ni	W	0.5	0.25	0.25	-6.587
51W	Ni	Co	W	0.25	0.5	0.25	-8.283
1	W	W	W	0	0	1	48.995
1	Co	Co	Ni	0.75	0.25	0	-1.869
1	Ni	Co	Co	0.5	0.5	0	-0.782
1	Ni	Ni	Со	0.25	0.75	0	0.596

Table 6. DFT calculated formation enthalpies for end-members of the Co₃W-DO_a phase.

Atom on site	Atom on site	x(Co)	x(Ni)	x(W)	ΔH (kJ/mol)
6 <i>h</i>	2 <i>d</i>	X(OO)	A(141)	X(VV)	ΔΙΤ (ΚΟ/ΠΙΟΙ)
Со	Со	1	0	0	-0.014
Ni	Ni	0	1	0	2.345
W	W	0	0	1	48.957
Со	Ni	0.75	0.25	0	-2.260

Ni	Co	0.25	0.75	0	1.445
Co	W	0.75	0	0.25	-8.098
W	Co	0.25	0	0.75	33.145
W	Ni	0	0.25	0.75	24.102
Ni	W	0	0.75	0.25	-3.511

Table 7. DFT calculated formation enthalpies for end-members of the Co₃W-DO₁₉ phase.

Calculated formation enthalpies at 0 K for ordered configurations are represented in \it{Fig} 12 as a function of Ni/Co ratio for the $\it{D0}_a$ and $\it{D0}_{19}$ intermetallic phases along the isopleth ideal composition line between Ni₃W and Co₃W. DFT calculations demonstrate that Ni substitution for Co leads to a stability inversion favorable to $\it{D0}_a$ formation. Consequently DFT calculations support the experimental evidence that Ni addition tends to stabilize the $\it{D0}_a$ intermetallic phase at the expense of the $\it{D0}_{19}$ phase in the Co–Ni–W ternary system.

For a better understanding of the Co/Ni substitution mechanism in the Co₃W-DO_a intermetallic phase, SQS calculations enabled partial sublattice site occupancy of sites 2a and 4e to be studied. Formation enthalpies calculated with SQS (

Table 8) for x(Ni)=0.25 and x(Ni)=0.50 show that full substitutional models with a common Ni site occupancy for sites 2a and 4e are energetically alike when compared to ordered configurations. It is also shown for x(Ni)=0.50 that Ni in 2a and half 4e is preferred to the ordered phase with Ni in 4e. Hence it may be assumed that substitution of Co by Ni in the Co_3W-DO_a phase proceeds by filling site 2a and when full occupancy is reached, substitution would continue on site 4e.

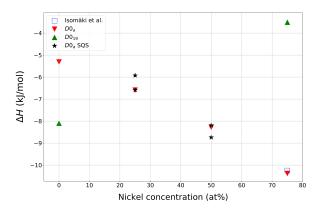


Fig 12. Formation enthalpy evolution calculated with DFT as a function of Ni concentration for Co₃W-D0_a and Co₃W-D0₁₉ structure with a fixed 25 at%.W at 0 K.

Co₃W-D0_a phase lattice parameters calculated by DFT and obtained with Le Bail refinements on sample Ni21.5 to Ni40 diffractograms are plotted in *Fig* 13. The lattice parameters found experimentally at 1000°C are in good agreement with DFT relaxed structure and comprised between the values calculated for 25 at%.Ni and 50 at%.Ni concentrations in Co₃W-D0_a. The experimental lattice parameter evolution with nickel addition does not feature any discernible trend.

x(Ni)	Ordered formation enthalpy (kJ/mol)	SQS superlattice formation enthalpy (kJ/mol)	Number of atoms for SQS calculations	Ni site occupancy on site 2a	Ni site occupancy on site 4e
0.25	-6.587	-5.931	48	0	1/2
0.25	-6.587	-6.536	72	1/3	1/3
0.50	-8.283	-8.740	48	1	1/2
0.50	-8.283	-8.194	72	2/3	2/3

Table 8. SQS formation enthalpies for the Co₃W–D0_a phase with 2b sublattice fully occupied by W.

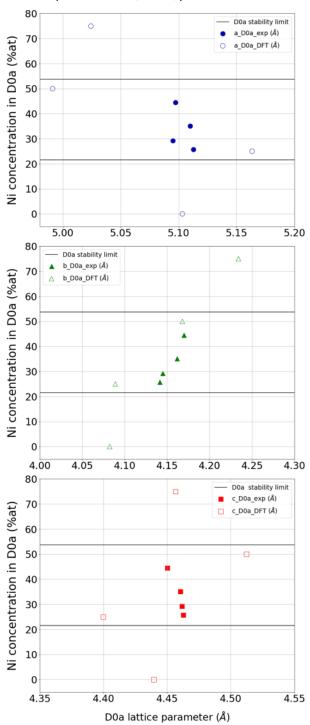


Fig 13. Co₃W-D0_a lattice parameter evolution with Ni content as found from DFT calculations and Le Bail refinements on samples equilibrated at 1000°C.

5. Conclusions

Samples within the Co–Ni–W system along the 30 at% W isocompositional line were prepared, heat-treated at 800°C and 1000°C and characterized through different methods: X-ray diffraction, electronic diffraction, SEM observations, EPMA composition measurements, TGA-DSC analysis, DFT and SQS calculations. New experimental data were provided to assess phase equilibria evolution as a function of chemical composition and temperature between 800°C and 1000°C.

Zhu *et al.* [14] pointed out the significant Ni solubility of the (Co,Ni)₃W like structures at 800°C but could not identify with certainty the phases at equilibrium since they relied on chemical compositions. The intermetallic phase called Co₃W-D0_a was found stable over a wide composition range in Ni (52.49 at% at 1000°C and more than 58.68 at% at 800°C) and the transition from Co₃W-D0₁₉ to Co₃W-D0_a with nickel addition was studied in terms of temperature and composition. Further experiments are necessary to better understand the phase transition between Co₃W-D0₁₉ to Co₃W-D0_a which is located around 30 at% Ni at 800°C and around 25 at% Ni at 1000°C.

Besides the presence of several ternary phase domains were established including BCC_A2+Co₃W-D0_a+Co₇W₆-µ and BCC_A2+Co₃W-D0_a+FCC_A1 and assumptions on phase domain evolution with temperature were put forward based on all the obtained experimental results. The obtained results emphasize the lacks of the previous thermodynamic descriptions for the Co–Ni–W system at temperatures lower than 1300°C. Therefore, there is a conspicuous need for a revamped CALPHAD model. Thermodynamic data extracted from DFT calculations are consistent with experimental results and will help to establish a better description of intermetallic phases involved in the Co–Ni–W system. More experimental investigations are being conducted to achieve a better understanding of phase equilibria over a wide range of compositions and temperatures and a CALPHAD optimization of the ternary Co–Ni–W system is ongoing.

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