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Enhanced local viscosity around colloidal nanoparticles probed by Equilibrium Molecular Dynamics Simulations

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ABSTRACT:

Nanofluids -dispersions of nanometer-sized particles in a liquid medium- have been proposed for a wide variety of thermal management applications. It is known that a solid-like nanolayer of liquid of typical thickness 0.5-1 nm surrounding the colloidal nanoparticles can act as a thermal bridge between the nanoparticle and the bulk liquid. Yet, its effect on the nanofluid viscosity has not been elucidated so far. In this article, we compute the local viscosity of the nanolayer using equilibrium molecular dynamics based on the Green-Kubo formula. We first assess the validity of the method to predict the viscosity locally. We apply this methodology to the calculation of the local viscosity in the immediate vicinity of a metallic nanoparticle for a wide range of solid-liquid interaction strength, where a nanolayer of thickness 1 nm is observed as a result of the interaction with the nanoparticle. The viscosity of the nanolayer, which is found to be higher than its corresponding bulk value, is directly dependent on the solid-liquid interaction strength. We discuss the origin of this viscosity enhancement and show that the liquid density increment alone cannot explain the values of the viscosity observed. Rather, we suggest that the solid-like structure of the distribution of the liquid atoms in the vicinity of the nanoparticle contributes to the nanolayer viscosity enhancement. Finally, we observe a failure of the Stokes-Einstein relation between viscosity and diffusion close to the wall, depending on the liquid-solid interaction strength, which we rationalize in terms of hydrodynamic slip.

KEYWORDS: Green-Kubo; Nanofluids; Heterogeneous systems; Diffusion coefficient; nanolayer; Stokes-Einstein

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I. INTRODUCTION

Nanofluids are colloidal solutions in which suspended nanometer-sized particles in the liquid medium¹⁻³ are responsible for enhanced thermophysical properties such as density, thermal conductivity, diffusivity, and viscosity compared to the base fluids⁴⁻⁹. The nanoparticles used in nanofluids are typically made of metals¹⁰⁻¹², oxides¹³⁻¹⁶, carbides¹⁷⁻¹⁹, or carbon nanotubes²⁰⁻²³, which are immersed in base fluids such as water²⁴⁻²⁶, ethylene glycol²⁷⁻²⁹, oil³⁰⁻³³, and refrigerant³⁴⁻³⁶. The main interest behind introducing the nanofluid concept is the increment in the thermal conductivity compared to the conventional fluids³⁷⁻⁴². The thermal conductivity of the nanofluids depends on various factors such as Brownian motion⁴³⁻⁴⁵, thermophoresis⁴⁶⁻⁴⁸, and clustering⁴⁹⁻⁵¹ of the solid particles as well as phonon-based nature of heat transfer within solid nanoparticles^{52,53}. Besides, liquid molecules form a local structured layer around the nanoparticle, known as nanolayer, which acts as a thermal bridge between the nanoparticle surface and the bulk liquid⁵⁴ that can enhance the thermal conductivity of the nanofluids by 10~20% depending on the base fluid type and nanoparticle diameter^{55,56}.

The term nanolayer describes the solid-like interfacial layer between the liquid and the nanoparticle, in which liquid molecules form an ordered layer structure similar to shell on the nanoparticle solid surfaces as a result of intermolecular forces existing between liquid and solid atoms⁵⁷. The thickness of the nanolayer vary between 0.3 *nm* to 1 *nm* (corresponding to 1 to 3 molecular sizes) depending on the interface interaction strength⁵⁸⁻⁶². Numerous studies have attempted to model the thermophysical properties of nanofluid by considering the role of this nanolayer. As an example, the role of nanolayer in the enhanced thermal conductivity of nanofluids was investigated thoroughly in a renovated Maxwell model⁶² for spherical particles suspensions and a renovated Hamilton–Crosser model⁶³ for non-spherical particles suspensions. The effect of nanolayer on the density of nanofluid has been also investigated experimentally and it was shown that in order to reproduce the experimental densities of the nanofluids, the nanolayer should be taken into the account⁶⁴. Molecular dynamics (MD) simulations of silver-water nanofluids were also conducted in order to find the effect of nanolayer on the density of the nanofluid and a new ternary mixture model was proposed for the computation of nanofluids

density. It was shown that the nanolayer density is about 1.6 times that of the bulk fluid. Such high density causes a contraction in the fluid which reduces the volume of the base fluid by 3%⁶⁰.

Considering the viscosity of nanofluids, a few models have been proposed during the past decades⁶⁵. For a dilute suspension of small, rigid, spherical particles in the base fluid, a good approximation of the nanofluid viscosity can be obtained by Einstein model⁶⁶. For a moderate particle concentration, Brinkman has modified Einstein's equation and proposed a new model⁶⁷. Batchelor⁶⁸ proposed a new model to account for the effect of Brownian motion on the viscosity of an isotropic suspension of spherical, rigid particles. There are only a few models that include the nanolayer effect in the viscosity of the nanofluid. Considering an elliptical liquid layer shell around the nanoparticles, the Ward model for calculating the viscosity was proposed⁶⁹. The above-mentioned models for the viscosity of the nanofluid were compared with MD simulations⁶⁰. It was shown that the calculated viscosity based on the models which do not include the nanolayer effect is not consistent with MD while the models which account for a nanolayer shell around nanoparticles follow the MD simulations viscosity well. The key role of the nanolayer viscosity highlighted in this work makes it critical to characterize it for a variety of liquid-solid interfaces.

Liquid Viscosity and diffusivity are known to be affected by the fluid heterogeneity at the molecular scale such as density inhomogeneity⁷⁰. The effects of density heterogeneities at the solid/liquid interface on the shear viscosity profile were investigated thoroughly for a sheared confined fluid by the use of non-equilibrium molecular dynamics (NEMD) simulations⁷¹. It was shown that the local viscosity varied strongly with the distance from the walls for both the dense and dilute fluid, displaying oscillations correlated to the density profile. This work was further developed and a local average density model was developed to describe the distribution of the local shear viscosity in inhomogeneous fluid⁷². It was shown that for a dense inhomogeneous liquid, the proposed model leads to a good description of the viscosity profiles as measured by NEMD. However, some deviations were observed for the low-density inhomogeneous liquid. Such viscosity variation was shown to be able to significantly reduce the flow rate for a Poiseuille flow as the system dimension became smaller than 3~4 nm for water and 1 nm for nonpolar fluids⁷³. The effects of the inhomogeneity length scale on structural and dynamic properties of

the fluid were investigated thoroughly by applying sinusoidal density profiles having various wavelengths⁷⁴. It was shown that for a long-wavelength density distribution, bulk-like relationships between thermodynamics, local structure, and diffusivity were observed. However, as it came to small wavelengths, different correlations should be considered between the local static and dynamic quantities, depending on the wavelength.

Due to the importance of the precise viscosity calculation in the nanofluid, the objective of the present research is to characterize the viscosity of the nanolayer around the nanoparticles. To that aim, we will use equilibrium molecular dynamics (EMD) simulations, where the viscosity of the system is computed with the Green-Kubo (GK) relation. The ability of the GK relation for the calculation of bulk and confined liquid viscosity were investigated by several researchers^{75–83}. The viscosity of confined water inside hydrophilic and hydrophobic nanotubes was computed using the GK method⁸⁴. A great impact of water-wall interactions, confinement size, and density on the viscosity was observed. However, it was shown that for the small nanotube, as the density is increased, the viscosity and the diffusion coefficient are increased together and violates the Stokes-Einstein relation. Zaragoza *et al.*⁸⁵ studied how the planar walls and nanotube confinements affect water viscosity and proposed a confined Stokes-Einstein relation for obtaining the viscosity from diffusivity. It is interesting to note that, while the viscosity computed with the GK method differs from that of the bulk noticeably, the viscosity computed with confined Stokes-Einstein relation is not affected by the confinement. The authors concluded that different methods in calculating the viscosity may provide dramatically different results, which may not easily be related to the standard and experimental definition of viscosity. However, a NEMD simulation of shear-driven liquid argon flow between two graphene walls shows an increment by the factor two for the viscosity of liquid argon in the vicinity of the nanochannel wall compared to the middle of the channel⁸⁶. Recently, Zhou *et al.*⁸⁷ have shown that in the viscosity calculation of the nanoconfined fluid, the wall friction should be decoupled from the fluid viscosity by defining the frictional (near the wall), the transitional, and the viscous (far from the wall) region. This was concluded by a comparison between the fluid viscosities calculated from the GK formula in the entire domain and the viscous region, and the fluid viscosity which was obtained based on the velocity profile of the Hagen–Poiseuille flow. This analogy revealed

that only the viscosity in the viscous region coincides with the one deduced from the velocity profile.

The nanolayer definition in our study coincides with the definition of the frictional plus transitional region, whose viscosity was not discussed in previous studies. A closer look at the nanolayer viscosity is the main motivation of our study. Therefore, we should be able to apply the GK method to the separate liquid layers and as the first step of our research, this feasibility is validated. In addition, the diffusion coefficient of the liquid layers is also calculated, which is then connected to the difference between the viscosity of the different layers. The remainder of this article is organized as follows: In Section II, the methodology of the simulation is described in detail. In Section III, the simulation results are presented. In the first part of this section, a validation is presented to assess the accuracy of the applied simulation method. Then the viscosity of the nanolayer of the copper-argon nanofluid is calculated and the results are thoroughly interpreted. Finally, we conclude in Section IV. It is worth mentioning that the rationale behind choosing copper-liquid argon is that this is a model system that can be used as the initial step in the study of new phenomena. Argon, in practice modeled with a Lennard-Jones potential, may be thought of as the simplest liquid one can model, and whose properties can be mapped to any real liquid using the law of corresponding states. Nevertheless, it would be interesting to extend this work by considering models of more complex liquids such as ethylene glycol or water.

II. COMPUTATIONAL DETAILS AND METHODS

In this study, the viscosity of the liquid argon is calculated by EMD method using LAMMPS⁸⁸ (Large-Scale Atomic/Molecular Massively Parallel Simulator). The Open Visualization Tool (OVITO) is used to visualize and represent atomic configurations⁸⁹. Lennard-Jones (LJ) potential parametrization is considered for interatomic forces between different types of atoms in this study. The Lennard-Jones (LJ) potential parameters that were used in this study are shown in Table 1, in which r_C^{LJ} denotes the cut-off distance of the LJ interactions. While a timestep of 1 fs is used in all simulations, smaller timesteps were also tested and had no significant effect on the results. Considering the temperature of the liquid medium and the walls, a Maxwell–Boltzmann

velocity distribution is used to initialize the velocity of the atoms at the beginning of the simulation. In all sets of simulations, two independent Nosé-Hoover thermostats were applied to liquid and wall for 2 ns to ensure the desired temperature is achieved. After that, the thermostat is removed from the liquid domain while still applied to the walls. Then, the simulation proceeds for 2 ns. This ensured us that no thermostat is applied to the fluid atoms directly and the results are not affected by the selection of thermostat parameters. Additionally, another 2 ns are performed for the averaging process in which the density, temperature, and viscosity of each computational bin are calculated.

The shear viscosity of a fluid, μ , can be computed using the GK relation which is based on the shear stress $\tau_{\alpha\beta}$ autocorrelation function^{90,91}:

$$\mu = \frac{V}{k_B T} \int_0^{+\infty} \langle \tau_{\alpha\beta}(t) \tau_{\alpha\beta}(0) \rangle dt, \quad (1)$$

with $\alpha \neq \beta$,

$$\tau_{\alpha\beta} = \frac{1}{V} \left(\sum_{i=1}^N \frac{P_{\alpha}^i P_{\beta}^i}{m^i} + \sum_{i=1}^N \sum_{j>i}^N r_{ij}^{\alpha} F_{ij}^{\beta} \right), \quad (2)$$

where V and T are the volume and temperature of the system, respectively, k_B the Boltzmann constant, m the mass, P the momentum, as well as r and F , are the distance and the force between two particles, respectively; i and j are the atomic indexes and N is the number of particles. According to the GK relation, the calculated shear viscosity of equation (1) consists of three components, i.e., μ_{xy} , μ_{xz} and μ_{yz} and the shear viscosity of the fluid equals their average.

In order to interpret the result, the diffusion coefficient was also determined using the mean square displacement of the particle⁸⁵:

$$D = \lim_{t \rightarrow \infty} \frac{\langle |r(t_0 + t) - r(t_0)|^2 \rangle}{2 \dim \times t} \quad (3)$$

where r denotes the position vector. The standard formula considering the three-dimensional displacement uses $\dim=3$ while for two-dimensional displacement, $\dim=2$ should be used. However, since in the current study the MSD is calculated separately in each direction and the diffusion coefficients in perpendicular and parallel directions are computed based on them, $\dim=1$ is considered in equation (3). In order to have a reasonable estimate of the intrinsic

diffusion coefficient, the liquid center of mass motion was subtracted before computing the MSD⁹². The validity of the Stokes-Einstein relation was investigated using^{93–95}:

$$\mu = \frac{k_B T}{3\pi D \sigma_h} \quad (4)$$

which relates to the viscosity and the diffusivity of the fluid. In this equation, σ_h denotes the hydrodynamic fluid particle diameter. The above-mentioned equations for calculating the viscosity and diffusion coefficient are for the calculation of the entire volume of the liquid. However, as it comes to layers of liquids, these relations must be used with caution. In particular, since the calculation of the diffusion coefficient is based on the MSD according to equation (3), some restrictions must be considered. Actually, the displacement of an atom is calculated based on its reference position which is normally the original position at the onset of the MSD calculations⁸⁸. Consequently, as an atom moves to the adjacent liquid layer, the validity of the MSD calculations become under question. In order to handle such restriction in our study, the MSD calculation time is chosen smaller than the required time that an atom needs to move to its adjacent liquid layer. Considering the diffusion coefficient of bulk liquid argon⁹⁶ and liquid layer thickness, the required time for an atom to move to its adjacent liquid layer is on the order of 0.3 ns and in order to be cautious in this study, 0.2 ns is considered as the maximum MSD calculation time.

TABLE 1. LJ parameters for non-bonding interactions

<i>interaction</i>	ϵ (kcal/mol)	σ (Å)	r_c^{LJ} (Å)
<i>Ar – Ar</i> ^{97–100}	0.237	3.405	27
<i>Cu – Cu</i> ¹⁰¹	4.72	2.616	10
<i>Ar – Cu</i> ^{102,103}	0.25, 0.5, 1.0, 1.5	3.010	18

III. RESULTS

It should be noted that the GK method is derived for a bulk system^{104,105} and it was verified that for a system with geometrical confinement, in the direction without confinement where the

periodic boundary conditions are applied, calculated thermal conductivity based on the GK equation yields results which agree well with the Non-Equilibrium Molecular Dynamics (NEMD)¹⁰⁶. Therefore, the first step in this paper is to validate the use of GK viscosity calculations for a system with a non-periodic boundary condition.

A. Validation of the GK methodology for the liquid layer

The simulation domain for the validation is presented in FIG. 1. The system is a cube with sides of 6 nm filled with 4280 argon atoms at the temperature of 100 K, which corresponds to a density of 1314 kg/m³. Considering the values of the density and temperature, the viscosity is expected to be 184 $\mu Pa \cdot s$ ¹⁰⁷. It is well-known that in EMD calculations, larger system sizes do not significantly affect the calculated shear viscosity^{108–111}. Therefore, we proceed with the above-mentioned dimensions. Periodic boundary conditions are applied along x, y, and z directions. Regarding this configuration, two sets of simulations were conducted. In the first set of simulations, the viscosity of the whole simulation box is considered as a unit configuration, and the components of the viscosity for the whole simulation box are calculated using equations (1) and (2). In the second set of simulations performed simultaneously, the simulation box is divided into two equal simulation domains considering a virtual plane perpendicular to the x direction. The atoms can freely move between zones from this plane. Since for each instance, the autocorrelation of the shear stress components is used for the calculation of the viscosity, it does not matter if the atoms cross the virtual plane as the calculation is done based on the neighboring atoms. Using such a methodology, the components of the viscosity in each region are calculated separately. The integration time for the viscosity calculation by GK method in this part is 10 ps according to Fig. 2. The calculated viscosity is averaged over twenty-five different initial independent configurations and the reported viscosity deviation is defined based on them. It should be noted that the error bar of the reported viscosity components is the standard deviation of the tail of the final running⁸⁷.

It is observed that as the GK method is applied on the whole simulation box, the computed viscosity, $180 \pm 5 \mu Pa \cdot s$, is close to the expected value while as the GK method is applied on the left or the right box, the calculated viscosity becomes $130 \pm 5.3 \mu Pa \cdot s$ and $127 \pm 6 \mu Pa \cdot s$

respectively where the deviation from the desired value is considerable. To find out the source of such deviations, the autocorrelation of the shear stress components, averaged over all cases, is shown in FIG. 2. This figure clearly implies that the viscosity component in the yz plane should be higher than that of the xy and xz planes. The viscosity components for the left and right boxes are computed based on these autocorrelations. The calculated viscosity components for xy, xz , and yz planes are $111 \pm 5.3 \mu Pa \cdot s$, $112 \pm 4.9 \mu Pa \cdot s$, and $178 \pm 0.9 \mu Pa \cdot s$ respectively for the left simulation box and $108 \pm 6 \mu Pa \cdot s$, $108 \pm 5.7 \mu Pa \cdot s$, and $175 \pm 1.3 \mu Pa \cdot s$ for the right ones. These values show that while the calculated viscosities in the xy and xz planes deviate significantly from $184 \mu Pa \cdot s$, the yz component is in good agreement with the expected value. A closer look at the boundary conditions might reveal the source of such behavior.

Actually, the periodic boundary condition is applied in y and z directions, consequently in yz plane, which leads to the correct viscosity prediction. On the other hand, the GK method underestimates the μ_{xy} and μ_{xz} which should be related to the presence of the non-periodic boundary condition, the imaginary boundary, in the middle of the simulation box along x direction. It can be concluded that similar to the thermal conductivity¹⁰⁶, the viscosity calculation using the GK method can be only applied in a direction having periodic boundary conditions. It is also interesting to notice that the boundary condition in the middle of the box is not a wall or any physical confinement. It is just an imaginary boundary that divides the simulation box into two parts. Besides, it is worth mentioning that the convergence of the autocorrelation function of all the three viscosity components does not guarantee the correctness of calculated viscosity in the GK method, and further criteria should also be checked.

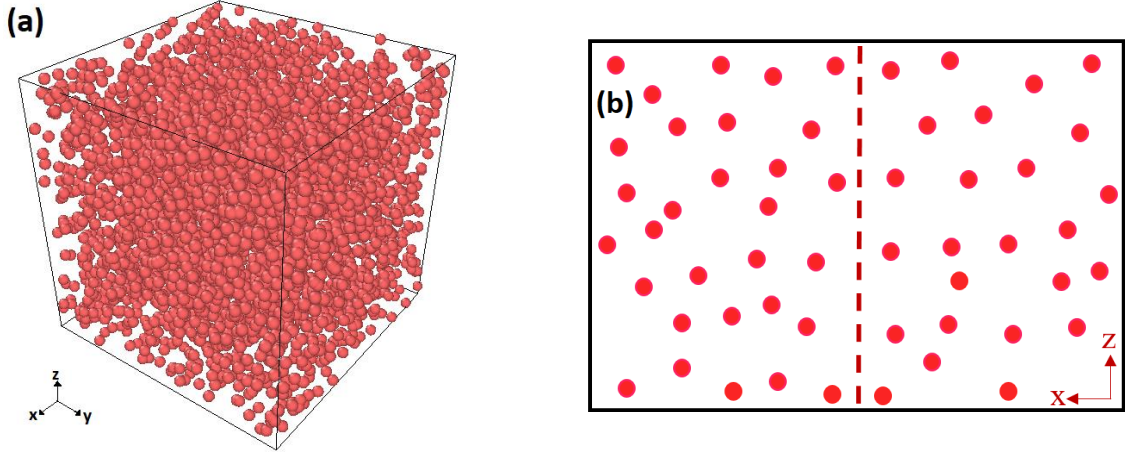


FIG. 1. (a) Simulation domain filled by liquid argon atoms and (b) schematic sketch of the simulation domain which is divided into two parts.

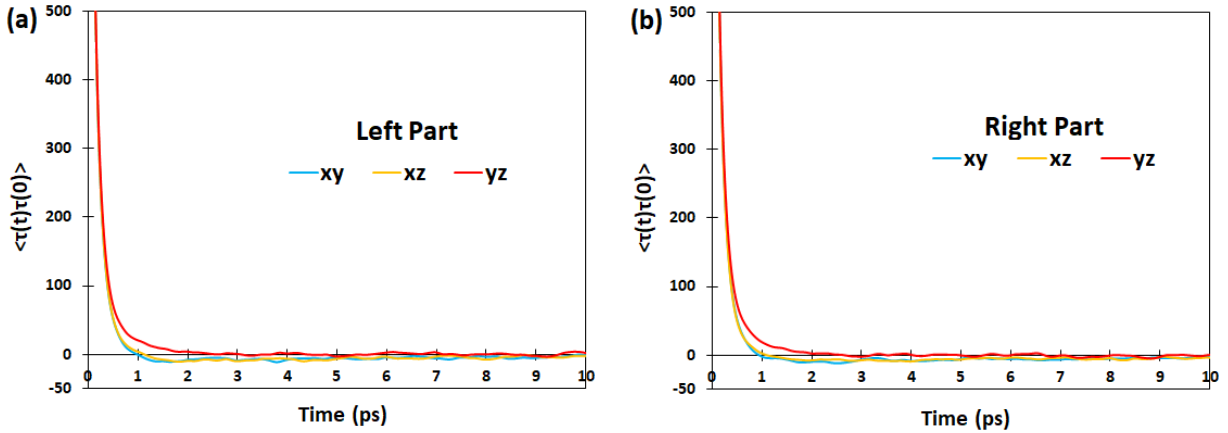


FIG. 2. Autocorrelation of the shear stress components for the (a) left and (b) right simulation box.

B. Copper nanoparticle in liquid argon

In the previous section, we observed that even in the presence of a non-periodic boundary condition, the viscosity component in a plane with periodic boundary conditions in all its directions still gives the local viscosity of the fluid in that region. Considering a nanoparticle and spherical nanolayer around it to calculate the viscosity, such a plane cannot be defined. For the nanoparticles with a diameter larger than 20 nm , a small part of the nanoparticle surface can be modeled as a flat wall approximately as can be seen in FIG. 3. Therefore, the simulation domain in this part is considered as a flat wall consisting of two layers of FCC copper atoms, which is extended 8 nm in y and z directions, and a 5 nm liquid domain in the x direction. The temperature of the wall and argon is kept at 100 K . The liquid is divided into 5 bins of 1 nm

thickness perpendicular to the wall for the averaging process in the MD method. Therefore, it should be noted that the center of the first, second, third, fourth, and fifth bins is located at 5, 15, 25, 35, and 45 nm from the wall respectively. It should be mentioned that all the presented data for the temperature, density, and viscosity is the value averaged over 20 different initial distributions of the liquid atoms. To find the effect of the interaction strength between nanoparticle surface and the liquid on the density and viscosity of the nanolayer, ϵ_{Cu-Ar} is considered as 0.25, 0.5, 1.0 and, 1.5 *kcal/mol*. Actually, 1 *kcal/mol* approximately equals the case with Lorentz-Berthelot mixing rules for interaction strength; $\sqrt{\epsilon_{Cu-Cu} \times \epsilon_{Ar-Ar}} = 1.05$ *kcal/mol*. Changing the solid-liquid interaction strength varies the number of liquid atoms in the nanolayer, the first layer adjacent to the wall, which consequently affects the liquid density in the other layers. To be able to compare these solid-liquid interaction strengths together, the number of liquid atoms in the simulation domain has been changed, based on a trial-and-error method, in such a way that the density of the liquid remains approximately 1314 *kg/m³* for the third to the fifth layers (which can be considered as the bulk liquid). The calculated number of liquid atoms for each case is shown in Table 4. The integration time for the viscosity calculation based on the autocorrelation of the shear stress components in this section is 50 *ps*. More details about the viscosity calculation can be found in the supporting information (SI).

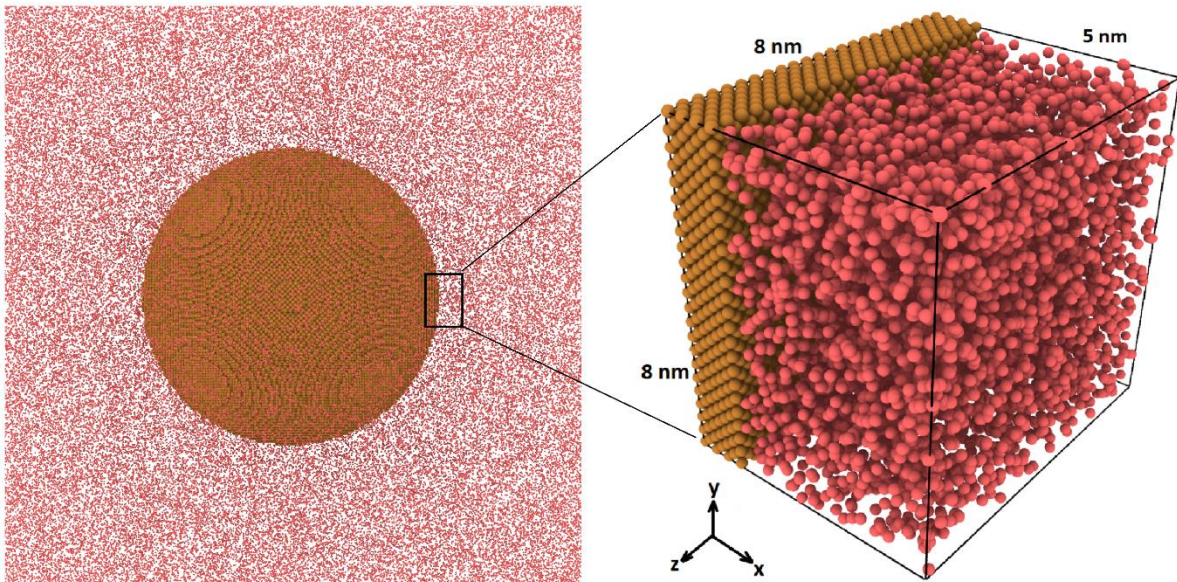


FIG. 3. Simulation domain considered for viscosity calculation, which is a part of 20 *nm* diameter copper nanoparticle surface that is immersed in liquid argon.

TABLE 4. Calculated density of the nanolayer and its corresponding viscosity extracted from Lemmon and Jacobsen¹⁰⁷ and Galliero *et al.*¹¹²

ϵ_{Cu-Ar} (kcal/mol)	# liquid atoms	density (kg/m ³)	viscosity ($\mu Pa \cdot s$)
0.25	6725	1367	227 ¹⁰⁷
0.5	6850	1470	330 ¹⁰⁷
1.0	6950	1540	770 ¹¹²
1.5	7000	1597	1227 ¹¹²

The density distribution of the liquid in different layers is shown in FIG. 4. It can be seen that the liquid density in the first layer around the nanoparticle is enhanced notably to 1367, 1470, 1540 and 1597 kg/m³ as the solid-liquid interaction strength is increased from 0.25 to 1.5 kcal/mol. Interestingly, the second layers also show higher densities which are 1331, 1356, 1369 and 1372 kg/m³ as the solid-liquid interaction strength is increased. Meanwhile, the density of the other layers is about 1314 kg/m³ as expected. The increase in the density of the liquid in the first and second layers corresponds to the well-known density layering phenomenon near solid surfaces,¹¹³ which is a direct consequence of interactions with the wall in the near-wall region⁹⁷.

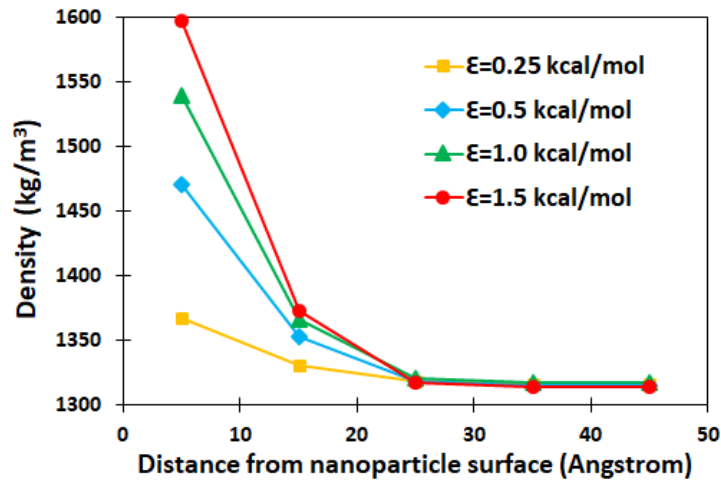


FIG. 4. Local liquid density in the different layers.

As mentioned before, the spatial viscosity distribution in the liquid is calculated using the GK relation as described in the previous section. According to FIG. 3, μ_{yz} is considered as the viscosity of liquid argon in each layer. The autocorrelation function of τ_{yz} for the liquid layers is shown in the SI, and the viscosity of each layer is calculated based on them. It is observed that the viscosity of the first liquid layer becomes 275, 442, 1031, and 2284 $\mu Pa \cdot s$ as the solid-liquid interaction strength is increased from 0.25 to 1.5 $kcal/mol$ while for the second layer, the corresponding viscosities are 182, 184, 190, and 190 $\mu Pa \cdot s$. The viscosities of the other layers are around 184 $\mu Pa \cdot s$ ¹⁰⁷ which is the expected viscosity for 1314 kg/m^3 . By normalizing the viscosity of each layer with respect to 184 $\mu Pa \cdot s$, as done in Fig. 5, it is interesting to notice that the viscosity of the first layer is approximately 1.5, 2, 6, and 12 times the bulk viscosity as the interaction strength increased, which shows the great impact of the solid surface on its adjacent liquid viscosity. Interpreting the main reasons behind such anomalous viscosity increment of the first layer is the main subject of this manuscript.

One reason behind such viscosity increment is related to the denser liquid medium of the first layer compared to the other layers. A denser liquid medium increases the collision between liquid atoms which enhances the viscosity accordingly. This can be also clearly observed in the viscosity enhancement of the second layer compared to the third, fourth, and fifth layers as it has higher liquid density according to Fig. 4. It should be noted that the viscosities of the second to the fifth layer are still in the same order of magnitude which implies that a similar mechanism governs the transport phenomenon in these layers. Meanwhile, the viscosity of the first layer is much higher compared to the other layers, which suggests that a different mechanism might govern the transport phenomenon in this layer.

It might be helpful to find the viscosity of the liquid at the corresponding bulk density for the first layer. This information will show us whether the viscosity increment of the nanolayer is only related to the increase in the liquid density or if some other phenomenon is also involved. The viscosities based on the liquid density for the first layer are presented in Table 4. Lemmon and Jacobsen¹⁰⁷ presented these viscosities for the bulk liquid medium based on a combination of the theoretical models and the empirical equations. For density higher than 1481.5 kg/m^3 (melting density at $T = 100K$), the viscosity is taken from Galliero *et al.*¹¹² in which an accurate

correlation is presented for the viscosity of the Lennard-Jones fluid. The ratio of this viscosity to the calculated one can be considered as the contribution of the density to the total viscosity. It is observed that the viscosity of the first liquid layer based on its density is 227, 330, 770, and 1227 $\mu Pa.s$ as the solid-liquid interaction strength is increased from 0.25 to 1.5 $kcal/mol$, which shows a notable difference compared to the viscosity of the nanolayer. Therefore, it is concluded that in addition to the liquid density, there must be some other phenomenon that increase the viscosity of the nanolayer.

TABLE 5. Calculated viscosity ($\mu Pa.s$) for the different liquid argon layers as a function of the interaction strength between the wall and liquid atoms

ϵ_{Cu-Ar} ($kcal/mol$)	First	Second	Third	Fourth	Fifth
0.25	275 \pm 2.1	182 \pm 2.7	173 \pm 6.6	172 \pm 2.1	174 \pm 2.0
0.5	442 \pm 1.0	184 \pm 1.5	175 \pm 1.5	173 \pm 3.9	174 \pm 2.5
1.0	1031 \pm 2.3	190 \pm 0.8	178 \pm 1.7	171 \pm 2.4	173 \pm 1.2
1.5	2284 \pm 2.5	190 \pm 2.5	170 \pm 5.0	174 \pm 2.6	172 \pm 1.8

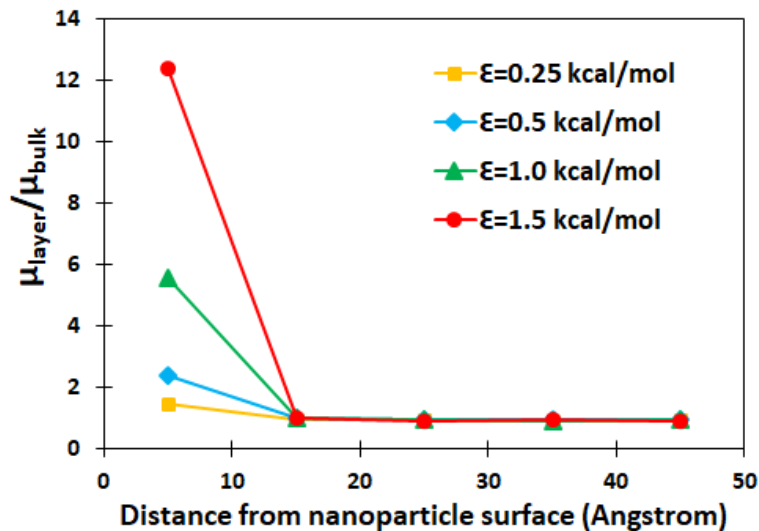


FIG. 5. Normalized viscosity distribution in the liquid argon normalized with $\mu_{bulk} = 184 \mu Pa.s$.

In the liquid nanolayer adjacent to a nanoparticle, the liquid atoms are under the strong attraction of the nanoparticle atoms on the surface. On the other hand, the reported values in Table 4 are for the bulk condition where the liquid atoms can move and interact with each other freely. Therefore, a closer look at the liquid structure and transport properties of the atoms in the nanolayer might reveal the main reason behind such discrepancy between the calculated viscosity of the nanolayer and the expected viscosity based on its density.

Figure 6 displays the distribution of the liquid atoms near the nanoparticle surface. As it can be observed, the liquid atoms in the nanolayer form two ordered liquid atoms layers for the interaction strength of 0.25 kcal/mol while three layers are formed for higher interaction strength. Note that the contact layer always remains liquid: as detailed below, atoms are still diffusing, both within and between the layers. We suggest that the anomalous viscosity enhancement of the nanolayer compared to the other layers can be assigned to such liquid atoms ordering, and we will refer to it as the contribution of the liquid structure to viscosity. This can be computed by subtracting the contribution of the liquid density from total viscosity. Figure 7 compares the contribution of the liquid density and the layered structure in the total viscosity of the nanolayer which shows a greater role played by the liquid structure as the liquid-solid interaction strength increased.

The definition of the nanolayer in our study coincides with the sum of the frictional (distance lower than 1.5σ from the wall) and transitional (distance between 1.5σ and r_c^{LJ} from the wall) regions defined by Zhou *et al.*⁸⁷. It was observed that in the frictional and transitional regions, the liquid atoms are attracted by the wall atoms, inducing additional friction on the liquid atoms compared to the bulk. This was shown to be intensified as the solid-liquid interaction energy increased. The same phenomenon is observed in our study considering Fig. 7 in which the contribution of the liquid structure to the total viscosity is enhanced as the solid-liquid interaction energy increased. It seems that besides the induced wall friction on the liquid atoms in the frictional region which is enhanced as the solid-liquid interaction energy increased, the formation of the ordered liquid structure in the transitional region is another source for the friction increment. This might be related to an increment in the friction between the neighboring liquid atoms as the liquid structure becomes ordered.

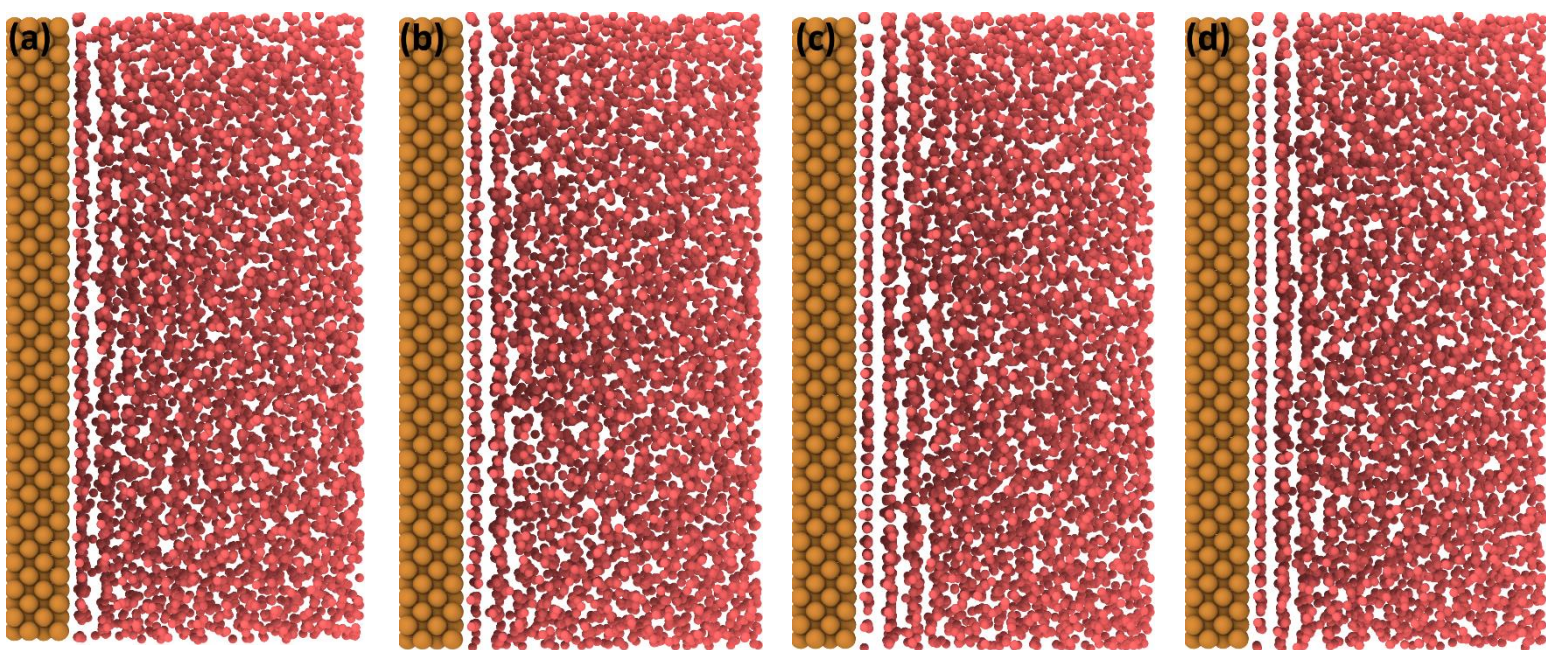


FIG. 6. Distribution of the liquid atoms near the nanoparticle surface in the steady state for liquid-solid interaction strength of 0.25 (a), 0.5 (b), 1.0 (c), and 1.5 kcal/mol(d).

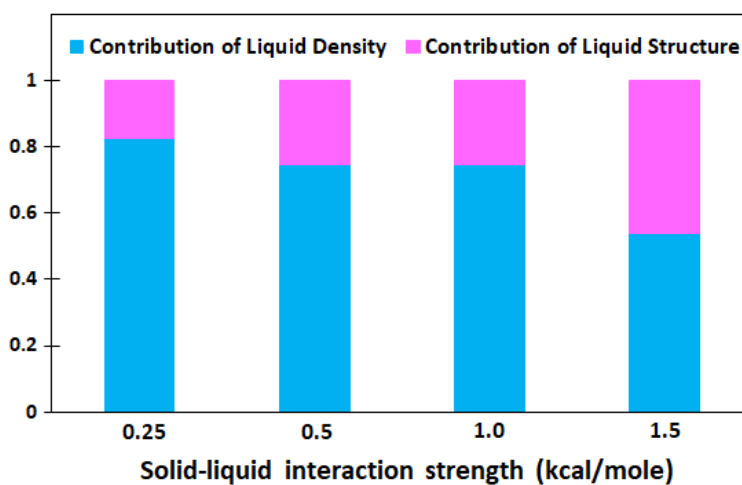


FIG. 7. Contribution of liquid density and liquid structure in the total viscosity for different interaction strengths of solid/liquid.

To go further, the mean square displacement (MSD) and the diffusion coefficient can be considered as the main criteria of the transport characteristics of the liquid atoms. Therefore, a more detailed evaluation of these parameters might help us to have a better understanding of the underlying physics in the nanolayer. The diffusion coefficients are calculated based on the

MSD of the liquid atoms using equation (3). According to Fig. 3, the diffusion coefficient perpendicular to the nanoparticle surface is D_x and the average of D_y and D_z is considered as the diffusion coefficient parallel to the surface. Figure 8 shows the variation of the diffusion coefficient parallel and perpendicular to the nanoparticle surface as a function of solid-liquid interaction strength for liquid layers. These values are also shown in Table 6 and Table 7. It is observed in Fig. 8a that as the liquid-solid interaction energy increases from 0.25 to 1.5 kcal/mol, the diffusion coefficient parallel to the nanoparticle surface in the third to the fifth layers, is about $3.35 \times 10^{-9} m^2 s^{-1}$ while a reduction from 3.02×10^{-9} to $2.76 \times 10^{-9} m^2 s^{-1}$ and 1.86×10^{-9} to $0.65 \times 10^{-9} m^2 s^{-1}$ is observed for the second and first layers respectively. Figure 8b clearly shows that for the same increment of interaction energy, the diffusion coefficient perpendicular to the nanoparticle surface is approximately $3.30 \times 10^{-9} m^2 s^{-1}$ for the fourth and the fifth layers, while it decreases from 2.92×10^{-9} to $2.72 \times 10^{-9} m^2 s^{-1}$ for the third layer. For the second and first layers, the diffusion coefficient decreases more, from 2.16×10^{-9} to $1.83 \times 10^{-9} m^2 s^{-1}$ and 1.09×10^{-9} to $0.5 \times 10^{-9} m^2 s^{-1}$ respectively. The diffusion coefficient perpendicular direction to the nanoparticle surface is inversely related to the residence time of the liquid atoms in the layers. Therefore, it can be concluded that the liquid atoms remain more time in the first liquid layer compared to the other layers for all interaction strength according to Fig. 8b. More details about the MSD and diffusion coefficient of the different layers are shown in the SI.

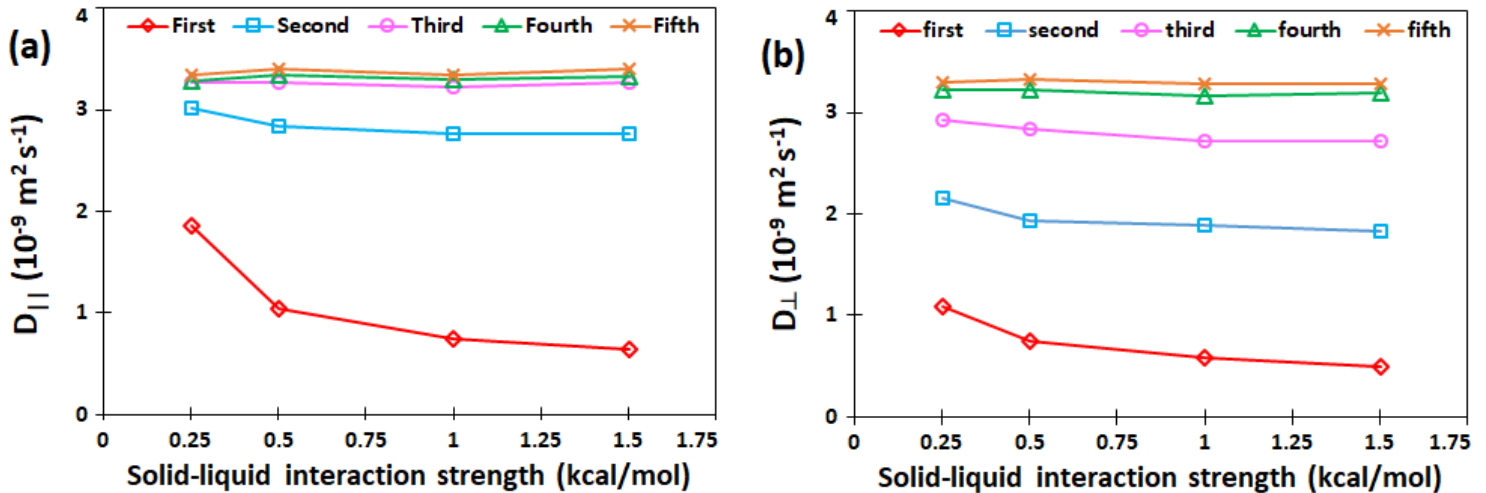


FIG. 8. Variation of the diffusion coefficient parallel (a) and perpendicular (b) to the nanoparticle surface as a function of solid-liquid interaction strength for liquid layers

TABLE 6. Calculated diffusion coefficient parallel to the nanoparticle surface ($10^{-9}\text{m}^2\text{s}^{-1}$) for the different liquid argon layers as a function of the interaction strength between the wall and liquid atoms

ϵ_{Cu-Ar} (kcal/mol)	First	Second	Third	Fourth	Fifth
0.25	1.87±0.42	3.02±0.15	3.26±0.16	3.28±0.16	3.34±0.13
0.5	1.04±0.08	2.84±0.11	3.26±0.2	3.34±0.13	3.4±0.19
1.0	0.75±0.09	2.76±0.14	3.22±0.13	3.3±0.18	3.34±0.18
1.5	0.65±0.06	2.76±0.15	3.26±0.13	3.32±0.18	3.4±0.15

TABLE 7. Calculated diffusion coefficient perpendicular to the nanoparticle surface ($10^{-9}\text{m}^2\text{s}^{-1}$) for the different liquid argon layers as a function of the interaction strength between the wall and liquid atoms

ϵ_{Cu-Ar} (kcal/mol)	First	Second	Third	Fourth	Fifth
0.25	1.09±0.24	2.16±0.08	2.92±0.11	3.22±0.1	3.3±0.14
0.5	0.75±0.06	1.94±0.1	2.84±0.1	3.22±0.1	3.32±0.19
1.0	0.59±0.07	1.89±0.07	2.72±0.09	3.14±0.18	3.28±0.16
1.5	0.5±0.04	1.83±0.09	2.72±0.12	3.2±0.15	3.28±0.19

Using equation (4), the validity of the Stokes-Einstein relation for each layer is also investigated in Fig. 9. Considering the nanolayer, it is interesting to notice that the Stokes-Einstein relation is valid for the low and intermediate solid-liquid interaction strength as $D_{||} \times \mu$ is approximately constant for all liquid layers in Fig. 9a. However, it should also be noted that a small reduction in the first layer is observed. The Stokes-Einstein relation implies a hydrodynamic radius which should depend on the local density, but if we take into account this correction as $D_{||} \times \mu \times \rho^{-1/3}$, we still have a small deviation for the first layer according to Fig. 9b. On the other hand, Figs. 9a and 9b clearly show that for stronger interaction, the violation of the Stokes-Einstein relation becomes noticeable. This violation is mainly related to the different structural and transport properties of the first layer compared to the others as the solid-liquid interaction strength increased which indicates the decoupling of viscosity and diffusion.

It is important to notice that the breakdown of the Stokes-Einstein relation has been also observed for a wide range of glassy systems¹¹⁴. While Stokes-Einstein breakdown was shown to be related to the fluctuation dominance in the dynamics of the glass formers at low-temperature¹¹⁵, it was also shown that the atomic dynamics is dramatically slowed down¹¹⁶ for the glassy system. The dynamics slowing down is usually accompanied by the emergence of heterogeneous dynamics, which can manifest in the existence of solid-like clusters characterized by dynamics slower than the average¹¹⁷ and whose size depends on the temperature¹¹⁸. In such a heterogeneous environment, the Stokes-Einstein relation may be broken as a result of the different spatial averages underlying liquid viscosity and diffusivity^{117,119}.

The changes in local liquid atomic structure and dynamic of liquid atom motion of the first liquid atom layer in our study are somehow similar to what was observed in the glassy system while their origin is different. In fact for the glassy system, it was shown that as the temperature lowered close to the glass transition, the diffusion coefficient $D_{||}$ and T/μ have different functional dependence on the temperature¹²⁰. It should be noted that in our current study violation of the Stokes-Einstein relation is only observed in the first layer and for the strong interaction energy between solid-liquid, 1.0 and 1.5 kcal/mol. Considering Fig. 8a, it is obvious that the diffusion coefficient for 1.0 and 1.5 kcal/mol are even lower than the corresponding values for 0.25 and 0.5 kcal/mol. Therefore, the violation of the Stokes-Einstein relation should be attributed to the anomalous viscosity increment for interaction energy of 1.0 and 1.5 kcal/mol as is shown in Fig. 5.

The variation of the viscosity and the diffusivity of the nanolayer against the interaction strength are shown in Fig. 10 in which the solid lines show the exponential behavior. It is observed that the viscosity and the diffusion coefficient of the nanolayer parallel to the nanoparticle surface vary as $\left[73e^{\left(\frac{\varepsilon}{k_B T}\right)^{0.61}}\right] \times 10^{-6} Pa.s$ and $\left[0.8e^{\left(\frac{\varepsilon}{k_B T}\right)^{-1.33}}\right] \times 10^{-9} m^2s^{-1}$ respectively as the solid-liquid interaction strength increases.

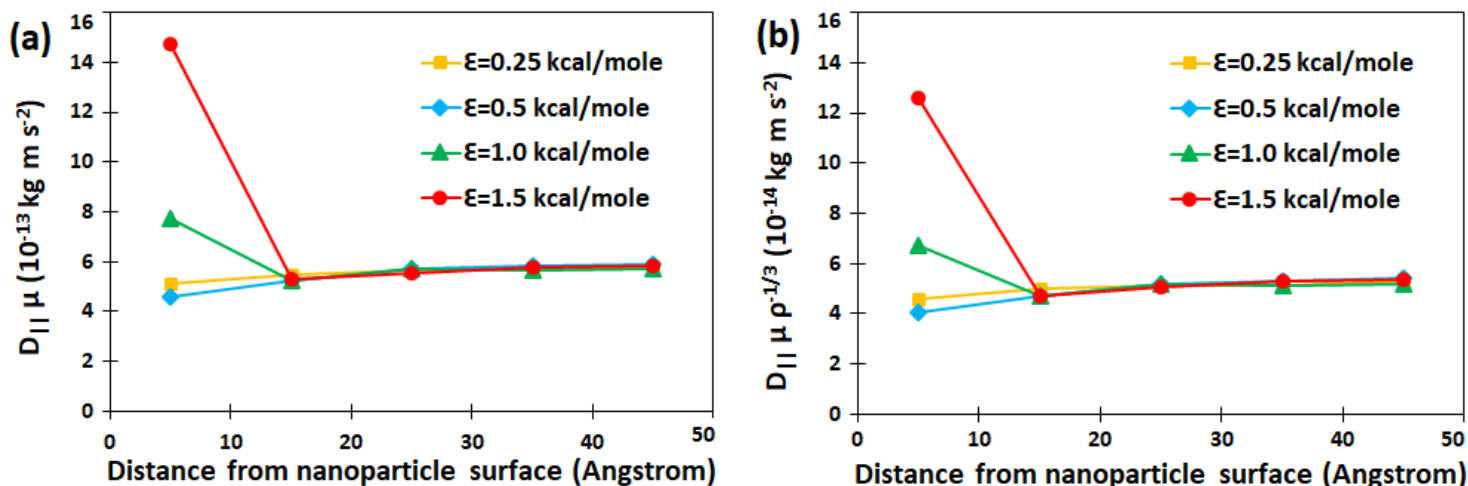


FIG. 9. The evolution of the Stokes-Einstein $D_{||} \times \mu$ (a) and modified Stokes-Einstein with a hydrodynamic radius $D_{||} \times \mu \times \rho^{-1/3}$ (b) relation as a function of distance from the nanoparticle surface.

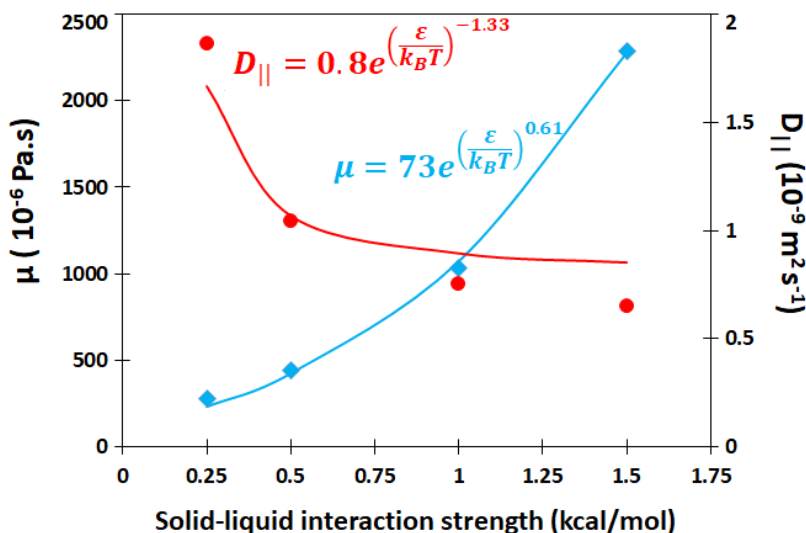


FIG. 10. Viscosity and diffusion of the nanolayer as a function of liquid-solid interaction strength.

The effect of liquid-solid slip on the diffusion coefficient close to the wall of the nanoconfined liquid medium was investigated thoroughly^{121,122}. Sauguey *et al.*¹²³ studied the effect of slip length at the solid-liquid interface on the diffusion of the confined liquid numerically, using a hydrodynamic approach based on the Stokes equation. It was shown that for the no-slip boundary condition, the diffusion coefficient in the vicinity of the wall decreased up to 50% compared with the bulk diffusion, while as the slip on the boundary increased, the diffusion coefficient was enhanced by the same amount. Interestingly, the authors have also derived an

analytical expression for low and high confinement limits, which were in good agreement with numerical data. Using this analytical approach, we have proposed a similar analytical formula for our simulation domain as:

$$D_{||}(x) = D_{bulk} \left\{ 1 - \left(\frac{9}{16} \right) \frac{\sigma}{x + b - \sigma} \right\} \quad (5)$$

where σ is the diameter of the liquid atoms which is 3.405 Angstrom in our case, b is the slip length, and D_{bulk} is the diffusion coefficient in the bulk region away from the solid surface. It should also mention that according to the simulation domain in Fig. 3, we have also considered the full formula accounting for periodic boundary conditions, and this does not lead to a better agreement. The diffusion coefficients derived based on the MD simulation are shown in Fig. 11a along with the fitted analytical formula for different interaction energy. The bulk diffusion coefficient D_{bulk} and the slip length b in equation (5) is considered as the fitting parameters and their corresponding values are obtained for each interaction energy and shown in Fig. 11b. It can be observed that D_{bulk} is around $3.5 \times 10^{-9} m^2s^{-1}$, independently of the interaction energy. Meanwhile, Fig. 11b shows that the slip length declines from 2.51 to 0.75 Å as the interaction energy increases which can be attributed to the increment of the induced friction on the frictional region in liquid by the wall⁸⁷.

The difference between D_{bulk} based on the analytical formula, equation (5), and the calculated $D_{||}$ for the fourth and fifth layers based on our numerical simulation presented in Figs. 8a can be considered as a possible manifestation of finite size effect for each layers^{92,123}. It should be although noted, however, that for the fourth and fifth layers, the ratio of the distance from the nanoparticle surface to the radius of the argon atom is in the order 25. Therefore, it is expected that no confinement effect exists for the single wall configuration¹²³. Considering 3.5×10^{-9} and $3.3 \times 10^{-9} m^2s^{-1}$ as the diffusion coefficients of the D_{bulk} and $D_{||}$ respectively, the finite size effect of each layer should be about $0.2 \times 10^{-9} m^2s^{-1}$. It is difficult to provide a better estimate of possible finite size effects, as analytical formulas in the literature only describe 3D periodic systems¹⁰⁹ or liquids confined by no-slip walls⁹².

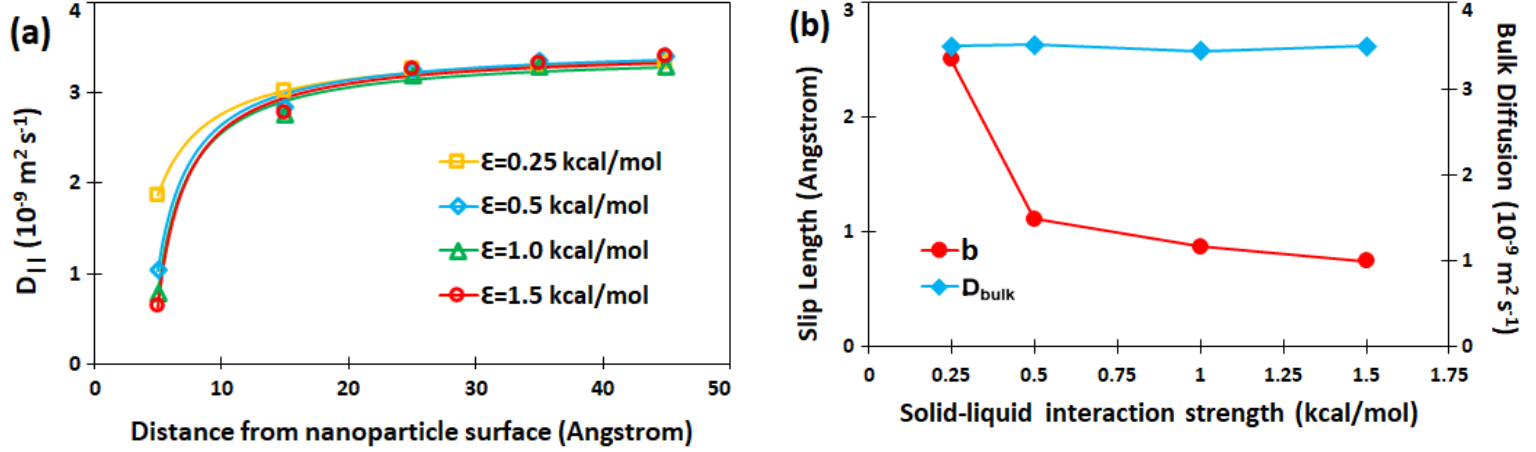


FIG. 11. Variation of the diffusion coefficient in different layers and its corresponding fitted analytical formula which is shown by the solid lines (a) and the variation of calculated slip length and bulk diffusion (b) as a function of solid-liquid interaction strength based on the proposed analytical formula

IV. SUMMARY AND CONCLUSION

The EMD simulation of liquid argon around a copper nanoparticle reveals that the density increments can be observed at 2 nm from the nanoparticle surface, while it is much more intense in the first 1 nm known as the nanolayer. In this study, we characterize the corresponding viscosity increase using the Green-Kubo approach. It is known that the GK method is traditionally derived for the bulk medium in which all the boundary conditions are periodic. Considering the liquid medium adjacent to the nanoparticle surface, we have shown that the GK method can be applied for such configuration with non-periodic boundary conditions provided that only the viscosity component in the normal plane to the non-periodic direction is considered in the calculation. Then, the viscosity of each layer is calculated and it was shown that for the liquid-solid interaction strength of 0.25, 0.5, 1.0 and, 1.5 kcal/mol, the viscosity is multiplied by approximately 1.5, 2, 6, and 12. We have shown that a fraction of this anomalous viscosity enhancement originates from the increment in the liquid density of the nanolayer. The further increment is suggested to be related to the ordered structure of the distribution of the liquid atoms in the nanolayer. We have shown that the contribution of the liquid structure to the total viscosity of the nanolayer is increased as the solid-liquid interaction strength is enhanced. Generally, it was inferred that for the low and intermediate interaction energy systems, the enhanced viscosity of the nanolayer can be assigned to the small increase of the local density.

For these systems, the Stokes-Einstein relation -linking viscosity and diffusion- holds approximately in the nanolayer and the effect of the wall friction is small. On the other hand, for the strong interaction energy systems, the increase of the density cannot explain the enhancement of the local viscosity. This enhancement should be rather controlled by the friction with the wall and other neighboring liquid atoms. In this regime, one expects deviations to the Stokes-Einstein relation as it was observed. Finally, we rationalized the deviations from the Stokes-Einstein relation by accounting for the effect of liquid-solid slip-on diffusion close to the wall, with a slip length that decreases with increasing liquid-wall interaction.

SUPPORTING INFORMATION

Autocorrelation of the shear stress components in different layers of the liquid and the Evolution of the MSD and the diffusion coefficient of the liquid atoms are presented in this section.

CONFLICT OF INTEREST

There are no conflicts to declare.

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