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## ► To cite this version:

Komlavi Gogoli, Florian Gehring, Christophe Poilâne, Magali Morales. Analysis of morphological variations of flax fibre bundles by Fraunhofer diffraction. Industrial Crops and Products, 2021, 171, pp.113856. 10.1016/j.indcrop.2021.113856. hal-03348176

## HAL Id: hal-03348176 https://hal.science/hal-03348176v1

Submitted on 2 Aug 2023

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Version of Record: https://www.sciencedirect.com/science/article/pii/S0926669021006208 Manuscript\_c0cdedb91073b59129a6a1f70982718a

## 1 Analysis of morphological variations of flax fibre bundles by Fraunhofer

- 2 diffraction
- 3

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5 Abstract

The increasing use of plant fibres in industrial applications requires a better understanding of 6 7 their morphologies. Experimental observations have shown that these fibres are characterized by a complex geometry which could affect their mechanical behaviour. Indeed, it is well 8 known that the size and shape of plant fibres cross-section vary from bundle to bundle and 9 along their length. In this study, the technique of Fraunhofer diffraction was used to 10 characterize this morphological heterogeneity of flax fibre bundles. The analysis of the results 11 12 showed a large scattering of the cross-section area (CSA). Lengthwise morphological variations of the bundles were examined and reveal that the CSA varies by a factor of 3.4 over 13 14 a length of 75 mm. It also appears that the cross-section shape of flax fibre bundle can be 15 better approximated by an elliptical model than by a circular model. The ratio between the 16 maximum and minimum cross-section shape factor was found to be approximately 2 over a length of 75 mm. Moreover, the occurrence of cross-section rotations has been shown in case 17 18 of fibre bundles, i.e., the orientation of the major-axis of the ellipse corresponding to the 19 cross-section may be different from one point to another, causing sometimes visible twists 20 along the bundle. These different results allowed us to build a numerical 3D volume 21 considering the evolution of flax fibre bundles outer contour.

Keywords: f1ax fibre bundle; Fraunhofer diffraction; cross-section area; shape factor; variability; 3D
 reconstruction

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### **1. Introduction**

25 As a response to ecological challenges, there is an increasing use of plant fibres in industry, particularly in the manufacture of composite materials (Dicker et al., 2014; Joshi et al., 2004). 26 27 As they are biodegradable, renewable and naturally abundant, these plant resources offer real alternatives to petrochemical fibres (Goda and Cao, 2007). Used in particular as 28 29 reinforcements in organic matrix composite materials, plant fibres such as flax, sisal or hemp 30 have remarkable specific mechanical properties making them very competitive with man-31 made materials such as glass (Bledzki and Gassan, 1999; Wambua et al., 2003; Yan et al., 2014). In the fight against global warming, these plant fibres are therefore good candidates to 32 replace petrochemicals fibers as their increasing use would help to reduce the ecological cost 33 34 of industrial processes.

35 However, a large scattering of mechanical properties has been observed, in particular in the distribution of rupture stress and Young's modulus of these fibres (Bourmaud et al., 2013; 36 Haag and Müssig, 2016; Lefeuvre et al., 2015; Shah et al., 2016), which could limits their 37 38 massive use for the design of structural or semi-structural composite material parts. Also, unlike glass fibres, plant fibres such as flax and hemp have a non-linear mechanical behaviour 39 (Charlet, 2008; Cisse, 2016; Duval et al., 2011). To explain this variability and this complex 40 41 mechanical behaviour, the morphology, the biochemical composition and the microstructural 42 organization of elementary fibres or bundles are regularly discussed (Del Masto et al., 2017; 43 Placet et al., 2014). Consequently, in-depth understanding of each of these parameters is necessary to allow a more intensive and reliable use of these fibres in industrial processes. 44

45 Concerning the morphology, various studies have highlighted an important variability of 46 morphological characteristics of plant fibres. Experimental observations have clearly shown 47 that their cross-section is very irregular in size and shape (Charlet et al., 2007; Charlet, 2008; 48 Garat et al., 2018; Thuault, 2015) whereas for man-made fibres the cross-section is more

uniform. Moreover, in studies on plant fibres, the cross-section of the bundles is often 49 considered to be circular (Charlet, 2008; Cisse, 2016; Romão et al., 2004; Thuault, 2015). But 50 recent work has shown that the cross-section of flax and hemp bundles can be better assessed 51 52 by an elliptic model. Indeed, the simplified assumption of circular cross-section is suitable for man-made fibre but lead to overestimate the CSA of flax and hemp fibre bundle (Garat et al., 53 54 2018; Haag and Müssig, 2016). It is then clear that the geometric model used to represent the 55 cross-section in the calculations is of major importance and also influences the variability of the mechanical properties of plant fibres (Aslan et al., 2011; Bourmaud et al., 2013; Ilczyszyn, 56 2013). Based on this observation, in this paper, we presented an elliptical model for a better 57 58 assessment of flax fibre bundle cross-section.

For the measurement of the CSA or the study of plant fibre morphology, there is no 59 standardised technique. Different methods are used by the authors: optical microscopy 60 61 (Charlet, 2008; Ilczyszyn, 2013; Yue et al., 2019), Scanning Electron Microscopy (Charlet, 2008; Thygesen et al., 2006), laser scan (Garat et al., 2018; Haag and Müssig, 2016), 62 63 Fraunhofer diffraction (Romão et al., 2004), X-ray tomography (Del Masto et al., 2018) or mathematical modelling combined with experimental data (Grishanov et al., 2006). In the 64 presented study, Fraunhofer diffraction has been chosen because - as non-destructive 65 66 technique using a laser beam – it allows the morphological study of a sample and the subsequent mechanical testing of the same sample. Also, Fraunhofer diffraction requires less 67 68 time than tomography and therefore allows more samples to be analyzed.

The aim of our investigations is to study the morphological variations of flax fibre bundles and to propose a non-destructive methodology to better assess the morphological characteristics of plant fibres. Thanks to Fraunhofer diffraction, the inter-bundle variability of cross-section and its lengthwise non-uniformity along bundle have been characterised and the non-circularity of the cross-section was investigated by using an elliptical model to calculate

the CSA of the bundles. Furthermore, it is also known that the characterization of the 3D 74 morphology of plant fibres and in particular that of their bundles is a real challenge because of 75 the small size of these samples and the difficulties linked to experimental manipulations. 76 Based on our cross-section measurements, a numerical 3D reconstruction of external contour 77 of flax fibre bundle is finally proposed. The interest of such approach of three-dimensional 78 morphology is to propose a 3D model of a bundle respecting the dispersion of the measured 79 parameters. Also in further studies, by including elementary fibres in the bundle 3D 80 81 reconstructions as done by (Baley et al., 2018), these models can be introduced into a mesher for finite element method studies that could help to improve the understanding of the 82 83 mechanics of flax fibre bundles.

### 84 **2. Materials and Methods**

#### 85 **2.1. Materials**

The flax fibre bundles used to perform this morphological analysis were supplied by Natup 86 company and come from different flax varieties and batches. Since the origin of flax could 87 impact fibre bundles morphology and properties (Booth et al., 2004; Pisupati et al., 2021), a 88 batch of flax from the same origin could be used to exclude the influence of the plant variety. 89 90 Such specific study could be used in the futur with the methodology proposed here. The usual 91 treatment stages of plant fibres: retting, scutching and then combing were applied. These bundles have the particularity of having been treated with water spray, to make the natural 92 pectins more flexible and to use them as glue between millions of parallel bundles to form a 93 94 roll. For the purposes of the study, the bundles are randomly and manually extracted from the roll. The extraction was done carefully to avoid bundle damage. A total of 100 fibre bundles 95 were characterized and their outer shape were reconstructed. 96

97

## 98 2.2. Method used to characterize the flax fibre bundle cross-section

99 To determine the dimensions of the cross-sections, the Fraunhofer diffraction technique as 100 illustrated in **Figure 1a** was used. This technique consists in focusing a laser beam 101 (wavelength  $\lambda$ ) on the cross-section to be characterized and collecting diffraction pattern 102 composed of several horizontal spots on a display table placed at a given distance *D* from the 103 fibre bundle. A visible green laser (class 3B,  $\lambda = 532nm$ , maximum power = 100mW) was 104 used for the tests.

Each fibre bundle whose morphology is to be analysed is glued to a windowed cardboard 105 frame with a free length between the edges of 100 mm. According to (Lefeuvre, 2014), a 106 minimum of 6 measurements is required to have a sufficiently representative cross-section of 107 an elementary fibre. Despite the longer length of our samples, the same method was used in 108 the absence of more precise indication concerning the fibre bundles. Moreover, this number 109 of measurements per bundle allows us to optimize the experiment time as the number of 110 samples to be tested is high. Based on this assumption, along the free length of each bundle, 111 112 the dimensions of the cross-section are determined at 6 locations equidistant by 15 mm (15 113 mm, 30 mm, 45 mm, 60 mm, 75 mm, 90 mm).

Since the cross-section of fibre bundle is considered to be ellipsoidal in our investigations, the axes (minor-axis and major-axis)  $d_1$  and  $d_2$  of the ellipse must then be determined to assure a reliable elliptical CSA calculation (**Table 1**). In accordance to that geometry and the mathematical definition of an ellipse, the axes  $d_1$  and  $d_2$  must be determined in two orthogonal directions.

119 To achieve these goals, thanks to a device designed in the laboratory, the laser beam is first 120 focused on the point of the bundle whose cross-section is to be characterised and the width 121  $\delta_1$  of the central diffraction spot on the display table is measured (Figure 1b). 122 Then, keeping the laser beam always focused on the same point, the support on which the 123 cardboard is mounted is rotated by 90° around the longitudinal axis of the bundle and the 124 width  $\delta_2$  of the central spot of the second diffraction pattern is also measured. The same 125 operation is repeated for each of the 6 cross-sections along the bundle. This gives a total of 126 twelve axis calculations per bundle. The two orthogonal directions named "Direction 1" and 127 "Direction 2" are fixed in advance and are therefore identical for all samples.

## Table 1: Geometric model and formula used to calculate the CSA from diffraction measurements



```
132
```

## Figure 1: (a) Schematic diagram of the Fraunhofer diffraction principle and (b) Diffraction pattern recorded on the display table

133

134 After recording the widths  $\delta_1$  et  $\delta_2$ , the axes  $d_1$  and  $d_2$  are then calculated using equation (2):

135

$$d = \frac{2D\lambda}{\delta}$$
(2)

137 with:

138  $\lambda$ : laser beam wavelength

139 D: distance between the fibre bundle and the display table

 $\delta$ : width of the central spot formed by the first two nodes of the diffraction pattern (Figure 140 141 **1b**)

The smallest axes between  $d_1$  and  $d_2$  is considered to be the minor-axis of the ellipse and the 142 143 largest one is considered to be the major-axis. Finally, the elliptical CSA is determined using the equation (1) shown in the **Table 1**. 144

145 For scientific accuracy of later results discussion, it is useful here to recall some significant consequences of the assumptions made about the cross-sections measurements: 146

Since the measurement directions are taken randomly, it is not certain that the two 147 \_ 148 orthogonal dimensions measured correspond to the real axes (major and minor) of the 149 ellipse that would best fit the real cross-section. With the used method, the crosssection is a projection in two orthogonal directions of the real cross-section. 150

151 Using Fraunhofer diffraction, the disadvantage is that the measure neglects the lumens of elementary fibres which form the bundle. The space occupied by the interfacial 152 lamella between elementary fibres is also not taken into account. However, knowing 153 154 that in a bundle cross-section, there are usually ten to forty elementary fibres, it follows that the CSA calculated by neglecting the lumen and the interfacial lamella 155 will be slightly overestimated compared to the real CSA. We propose here an estimate 156 of the error made by neglecting the lumens. 157

Let us assume that at a given point, a bundle is composed of n elementary fibres. The CSA 158 159 measured at this point, neglecting the lumens is:

160 
$$CSA = \sum_{i=1}^{n} CSA_i$$
(3)  
161 with:

 $CSA_i$ : the cross-section area of the elementary fibre of rank i measured by neglecting the area 162 of its lumen. 163

164 The real CSA of the bundle if the total area occupied by the lumens of the elementary fibres is165 removed become:

$$CSA' = \sum_{i=1}^{n} (1 - p_i) CSA_i$$
 (4)

167 with:

166

168  $p_i$ : the surface proportion occupied by the lumen of the elementary fibre of rank i.

169 
$$CSA' = \sum_{i=1}^{n} CSA_i - \sum_{i=1}^{n} p_i CSA_i$$
(4)

170

171 Since it is impossible for us to know the surface proportion of lumen for each elementary 172 fibre in a given cross-section of the bundle, we can take an average value from the literature 173 to estimate the overestimation caused by not taking lumens into account. Let's attribute this 174 average to all the fibres, in this case:  $p_i = p$ .

$$CSA' = CSA - \sum_{i=1}^{n} p CSA_i$$
(4)

176 
$$CSA' = CSA - p \times \sum_{i=1}^{n} CSA_i$$
(4)

$$CSA' = CSA - p \times CSA \tag{4}$$

$$CSA' = (1-p)CSA \tag{5}$$

Combining different studies (Charlet, 2008; Charlet et al., 2010; Richely et al., 2021), it appears that on average the lumen area is between 0.4 and 10.5% of the CSA of the elementary fibre. In this case the CSA of the bundle measured by neglecting only the lumens of its elementary fibre would be on average overestimated by 0.4 to 10.5% compared to the real CSA (calculated by taking into account the interfacial lamella between the elementary fibres). This gives an idea of the overestimation of the cross-section area due to the negligence of the lumens. According to (Charlet et al., 2012) the length of the interfacial lamellae is between 5  $\mu$ m and 15  $\mu$ m and the thickness is about 0.5  $\mu$ m. With such data, one could try to estimate a theoretical surface proportion of the interfacial lamella, but the latter depends strongly on the arrangement of the elementary fibres in a given section of the bundle. Therefore, an accurate estimate will need the use of optical methods to measure on several samples: the CSA of a bundle, the CSA of its constituent elementary fibres, the area of the lumens and the thickness of the interfacial lamella between elementary fibres. This is beyond the scope of this work.

The mean of the 6 calculated CSAs of the bundle was taken as its representative mean CSA:  $CSA_{EM}$ . In total we characterised 100 bundles. For 7 of these bundles, however, the measurements were carried out at 5 points due to elementary fibre detachments along the bundle resulting in 593 cross-sections measurements.

## 197 **3. Results and discussion**

#### 198 **3.1.Scattering of flax fibre bundle axes**

With 593 cross-sections characterized by two axes  $d_1$  and  $d_2$ , there are a total of 1186 measurements. Analysis of the results reveals a large scattering of the axes with respectively a mean value of 104±38 µm for minor-axis and 158±54 µm for major-axis (Figure 2a and 2b). The distribution of the axes was characterised by testing different statistical distribution laws using the Anderson-Darling test implemented in Matlab software. Only the log-normal distribution (6) seems to be suitable for the distribution of the axes (\*\*P≤0.01).

$$Log(\mu,\sigma): f(x) = \frac{1}{x\sigma\sqrt{2\pi}} exp\left[-\frac{((lnx)-\mu)^2}{2\sigma^2}\right]$$
(6)

206 with:

207  $\mu$  and  $\sigma$  the parameters of the log-normal distribution

208

205

This large scattering is quite characteristic of plant fibres because they grow in natural conditions which imply a heterogeneity of their cross-section dimensions, unlike man-made 211 fibres whose dimensions can be standardised during their industrial production. Compared to 212 other studies on "flax fibre bundle apparent diameter", the mean value of our calculated axes is higher than that obtained by (Haag and Müssig, 2016) and (Garat et al., 2018). Apart from 213 214 natural causes, the significantly higher length of the bundles tested in our case and the number of cross-sections analysed may be the cause of this discrepancy. This difference may also be 215 216 due to the treatments applied to the fibre bundles used in the different studies. Harvesting and processing conditions can also influence the geometry of these fibres. Indeed, the more the 217 218 bundles undergo individualization operations – according to the use that will be made of them - the more the number of elementary fibres per bundle decreases, thus lowering the 219 220 dimensions of the resulting bundle.

Furthermore, it should be noted that other factors such the measurement technique accuracy can also influence the results of calculated cross-section dimensions of plant fibres. In fact, for the same batch of flax bundles, the difference in technique used to measure the crosssection dimensions can lead to an error of up to 175% in the calculation of the tensile stress, due to the bias introduced by each technique (automated laser, microscopy, flat-bed scanning) in the measure (Haag and Müssig, 2016).

Simultaneous lengthwise evolution of some bundle axis dimension highlights the non-227 circularity of the cross-section (Figure 2c). This clearly shows that when the cross-section is 228 229 considered circular, the "mean apparent diameter" of the bundle which will be calculated will 230 depend on the direction of measurement. For the batch of 100 bundles the relative difference 231 between the two "mean apparent diameters" calculated according to Direction 1 and Direction 2 (considering the cross-section to be a circle of diameter  $d_1$  in Direction 1 or  $d_2$  in Direction 232 2) respectively is around 20  $\% \pm 17$ . This implies that the mechanical properties which will be 233 obtained using each of "mean apparent diameter" will be impacted by this difference. The 234

random measurement angle of characterisation chosen by the experimenter is hence a source of variability reported by many studies (Aslan et al., 2011; Bourmaud et al., 2013) in both the cross-section dimensions calculation and the mechanical properties that will be attributed to the bundle. Indeed, the rupture stress and Young's modulus depend directly on the mean CSA of the bundle. This conclusion is obviously valid for elementary fibres.

## Figure 2: Characteristics of the axes of the cross-section: (a) Distribution of the minoraxes, (b) Distribution of the major-axes and (c) Lengthwise evolution of cross-section axis for two bundles

240

## **3.2.** Scattering and lengthwise variation of CSA along the bundle

The 593 cross-sections calculated from the axis measurements were analysed and again revealed a large variability inherent to plant fibres. This cross-section scattering is the logical consequence of the axis scattering discussed in **section 3.1**. In terms of distribution, the crosssection distribution also follows a log-normal distribution ( $^{*}P \le 0.05$ ) (**Figure 3a**).

246

Table 2: Calculated geometric parameters of flax fibre bundles CSA

	Min	~Mean	Max
$\mathrm{CSA}\left(\mu m^2\right)$	836	14062	68267
Minor-axis ( μm)	27.8	121.7	251.4
Major-axis ( $\mu m$ )	38.3	147.2	345.9

247

The mean CSA is  $13947 \pm 9331 \,\mu\text{m}^2$ . Our results are quite similar to those of (Charlet, 2008) who found respectively on two different batches of bundles, mean CSA of  $14107 \pm$ 4555  $\mu\text{m}^2$  and  $13881 \pm 4496 \,\mu\text{m}^2$  by image analysis. On the other hand, compared to the mean CSA of  $6148 \,\mu\text{m}^2$  found by (Garat et al., 2018) using optical microscopy, the mean cross-section of this present study is more than the double. To explain the important

difference with the results of (Garat et al., 2018), one can mention again the origin of samples 253 254 and the individualisation processes they underwent before being characterised. In fact, it is really difficult to conclude on this point because few precise indications are given on this 255 information in the different publications. The variety of flax used in the studies may also be 256 the source of this high difference. But it is unlikely in the light of our knowledge that the 257 258 difference in variety can justify such a large difference. (Thuault, 2015) studied the "apparent diameters" of seven varieties of flax and concluded from his statistical results that there is no 259 significant different between diameter from one variety to another. 260

There is also strong intra-bundle heterogeneity in the cross-sections. The characterisation of this heterogeneity is crucial to set-up the 3D outer contour of the bundles. Here, two levels of study are required: on the one hand, the evolution of the size (CSA) of the cross-section and, on the other, the evolution of its shape. In the actual section, the first level of the study is discussed. For a sample, the cross-section heterogeneity ratio  $r_s$  – which represents the multiplication factor of the CSA over 75 mm (15 mm to 90 mm) – is calculated by equation (7). It is worth noting that this ratio is computed for each of the six sections of the bundle:

268 
$$r_s = \frac{\max(CSA_i)}{\min(CSA_i)}$$
 i = 1; 2 ...; 6

269 (7)

270 On average the CSA is multiplied by 3.4 over 75 mm. Table 3 gives the  $r_s$  values for 10 representative samples from the batch of 100 bundles characterised. The ratio of the 271 272 maximum CSA to the minimum CSA can reach values of the order of ten. However, it should be noted that 90% of the  $r_s$  values are below 6. Despite the small number of measurement 273 274 points compared to the length of our samples, this result shows the high variability of CSA along the bundle (Figure 3b). This variation in cross-section can cause stress concentrations 275 that would add to the elementary inter-fibre friction that occurs in a tensile test on a plant 276 277 fibre bundle. Once again, the CSA scattering is one of the reasons which could explain the 278 scattering of mechanical properties since each bundle has a unique morphology that influences its mechanical properties whatever the sample length, notably through thecalculation of the mean CSA.

## Figure 3: (a) Cross-Section Area distribution and (b) Lengthwise variations of flax fibre bundle CSA

281

282

The explications of this CSA lengthwise variation can be multiple. As the elementary fibres are not continuous and given the length of the bundles tested, the number of elementary fibres per cross-section is very likely to be different. This would result in CSA high variations. Even if between two measuring points, the number of elementary fibres would be identical, the consistency of the CSA is not at all guaranteed. **Table 3: Analysis of CSA heterogeneity for 10 representative bundles of the total batch** 

289

 Table 3: Analysis of CSA heterogeneity for 10 representative bundles of the total batch

Bundle	L1	L2	L3	L4	L5	L6	L7	L8	L9	L10
Mean CSA (µm <sup>2</sup> )	10288	15917	16250	15461	15567	10322	8998	8215	29975	14875
Standard- deviation	1277	5086	5780	9612	10419	6729	6231	6899	22946	13368
r <sub>s</sub>	1.4	2.2	3.5	4.1	5.4	6.7	7.2	8.6	9.2	12.0

<sup>290</sup> 

It should be remembered here that even elementary fibre do not have a constant CSA (Charlet, 2008; Thuault, 2015). Using a camera equipped with lenses that can see details at the micrometer scale, the bundles were photographed to highlight these strong lengthwise variations of the CSA (**Figure 4**).

295

#### Figure 4: Two different flax fibre bundles section seen in profile

Let now  $d_{1m}$  ou  $d_{2m}$  be the mean axes of the bundle in the Direction 1 and Direction 2 respectively. A power regression correlation law between the "maximum mean axis"  $d_m =$  298  $\max(d_{1m}, d_{2m})$  and the mean elliptical cross-section area  $CSA_{EM}$  of the bundle was 299 developed (Figure 5a):

$$CSA_{EM} = k \times d_m^{\ n} \tag{8}$$

301 When the "maximum mean axis" is less than 100  $\mu$ m, the calculated mean elliptical CSA 302 given by the power law given in equation (8) is very close to the experimental results. This 303 law deviates from calculated mean elliptical CSA for high "maximum mean axis".

## **304 3.3. Ellipticity of flax fibre bundle cross-section**

300

The measurements also confirm the ellipticity of the cross-sections. For each of the 593 crosssections, the ellipticity *e* is calculated to better characterization of the cross-section shape (9):

307 
$$e = 1 - \frac{\min(d_1, d_2)}{\max(d_1, d_2)} = 1 - \frac{\min(d_1, d_2)}{\max(d_1, d_2)}$$
(9)

308 From a mathematical point of view, this definition makes it possible to identify the flattening 309 degree of an elliptical curve. The more circular the characterized cross-section is, the more e 310 tends towards 0 since in this case  $d_1$  and  $d_2$  are quite close. Otherwise, the flatter the ellipse corresponding to the cross-section is, the more e tends towards 1. With a range of values 311 from 0 to 0.77, the distribution the ellipticity is highly random compared to those of axes and 312 313 cross-sections. The mean ellipticity is 0.32 and confirms the relevance of the elliptical model for determining the CSA of flax fibre bundles. On the basis of this result, it can therefore be 314 concluded that, compared to the circular model, the elliptical model seems to be more suitable 315 for determining the CSA of flax fibre bundles. 316

The comparison with other similar works (Garat et al., 2018; Haag and Müssig, 2016) on plant fibre shape requires the calculation of the shape factor f defined as ratio between the major and minor axis of the ellipse:

320 
$$f = \frac{\max(d_1, d_2)}{\min(d_1, d_2)}$$
(10)

It was found for all 593 cross-sections:  $f_{mean} = 1.6$ ,  $f_{min} = 1$  et  $f_{max} = 4.3$ . Our result is 321 similar to that of (Haag and Müssig, 2016) for whom the  $f_{mean}$  is 1.76. but lower than the 322 value of 2.58 found by (Garat et al., 2018) for fibre bundle cross-sections. Nevertheless, the 323 three studies lead to the same conclusion: the cross-section of flax fibre bundles is rather 324 elliptical. The ellipse corresponding to the mean shape factor  $f_{mean}$  of the present study is 325 326 drawn on the Figure 5b in comparison with a circle whose diameter would be the major axis 327 of the ellipse. The flattening degree of the ellipse close to the real cross-section clearly illustrates the non-circularity of the flax fibre bundle. 328

The second level of study required to perform the 3D reconstruction of the bundle outer contour is the lengthwise evolution of the cross-section shape. The analysis of the intrabundle heterogeneity shows that the shape factor doubles on average over 75 mm. Not only can the CSA be multiplied by 3.4 over 75 mm, but the cross-section shape factor can be multiplied by 2 on average. These results illustrate the important irregularity exhibited by the morphology of flax fibre bundles.

## Figure 5: (a) Power law correlation between "maximum mean axis" and mean CSA of the bundle and (b) Illustration of the ellipticity of flax fibre bundle : curves drawn with major axis of the ellipse = diameter of the comparison circle = 100 μm

335

Although the study of the influence of the geometrical model used to calculate the CSA on the mechanical properties is beyond the scope of this works, these findings confirms that the geometric model directly influences the mechanical properties of the sample (Aslan et al., 2011). For example, in our case, when the mean cross-section of the bundle is calculated by considering a circular cross-section (assuming that the cross-section is a circle of diameter  $d_1$ in Direction 1 or  $d_2$  in Direction 2), there is an average overestimation of 12% compared to the mean cross-section calculated using the elliptical model. Therefore, as suggested by (Virk, 343 2010), if the circular model is used when measuring cross-section, it would be relevant to 344 determine a "correction factor" for the CSA to take into account the overestimation induced 345 by the geometrical model. This correction factor, which according to our study would be the 346 mean shape factor of 1.6 for flax bundle, is slightly lower than the value of 1.76 proposed by 347 (Haag and Müssig, 2016) but greater than the value of 1.42 proposed for jute fibre bundles by 348 (Virk, 2010).

## **349 3.4. Possible rotation of the cross-section along the fibre bundle**

350 The lengthwise evolution of the cross-section has been finely analysed and it was noted that the orientation of the major axis of the ellipse can be different from one cross-section to 351 another. Indeed, for each of the cross-sections, we named  $d_1$  the axis measured along 352 Direction 1 and  $d_2$  the one measured along Direction 2. Considering 2 consecutive cross-353 sections and assuming that for the first one  $d_1 > d_2$  there is no guarantee that in the second 354 cross-section we will have  $d_1 > d_2$  but rather the opposite. When this reasoning is extended to 355 each pair of consecutive cross-sections, according to our method of measurements, the 356 orientation of the cross-section can be different from one point to another (Figure 6a). 357

For the 100 bundles, this change in cross-section orientation between two consecutive points occurs on average 2 times when considering 75 mm over a bundle. As evidence of this, we have taken high precision pictures of bundles, where it is clear that some bundles are twisted (**Figure 6b**).

362

# Figure 6: (a) Illustration of the change of orientation between two consecutive sections and (b) Bundle with local twisting

Using Fraunhofer diffraction or any other laser technique, the number of measurement points per cross-section and per bundle would have to be increased to get an average value closer to reality. The results of our study are indicative since – as we have already reminded – the

ellipse by which we assessed the cross-section corresponds to a view along two orthogonal 368 369 directions. The change of orientation observed can have several origins according to the following two scenarios. Since a bundle is an assembly of discontinuous elementary fibres, 370 371 this change in the orientation of the cross-section may be due to the difference in the arrangement of the elementary fibres between two consecutive points (Figure 7a). In other 372 words, depending on the appearance and disappearance of the elementary fibres, the 373 orientation of the cross-section considered as an ellipse could change. In this case, there 374 375 would be no twisting of the bundle, but just a change in orientation corresponding to the ellipse that best approximates the cross-section. If two consecutive cross-sections of a bundle 376 have an elementary fibre arrangement, as shown in the Figure 7a, it is clear that the 377 orientation of the major-axis of the ellipse corresponding to the cross-section changes 378 between Cross-Section i and Cross-Section i+1. Our calculation method would in this case 379 380 show a twisting when there is no twisting but only a different disposition of elementary fibre. The other possible scenario is that the growth conditions of the bundles in flax stem or the 381 382 processing conditions may have favoured an irregular evolution of the orientation of the 383 cross-sections, thus causing twisting along the bundle. Furthermore, the scenario of a bundle of fibres which twists himself after combing should not be a surprise if all the microfibril 384 helices - which act at the main rigid elements inside elementary fibre - are orientated in the 385 same direction (S-helice) (Baley, 2002; Bergfjord and Holst, 2010). In that case, it can be 386 hypothesized that the twisting is due to stress relaxation once the bundle is released. As the 387 microfibrillar angle is much higher in defect areas such as kink-bands than in the rest of the 388 389 flax fibres (Melelli et al., 2021), it is conceivable that a difference in relaxation ratio may induce or increase such twisting. This twisting revealed by the numerical analysis and the 390 391 optical observations would probably explain the rotation of the bundle at the beginning of the tensile load observed by (Ahmed and Ulven, 2018) using in-situ Scanning ElectronMicroscopy.

## **394 3.5. 3D** reconstruction of flax fibre bundles outer contour

The knowledge of the exact morphology of plant fibre bundles and its lengthwise evolution is 395 a very important issue. Indeed, more and more studies are focusing on the propagation of the 396 mechanical behaviour of elementary fibre to the bundle. When performing numerical 397 simulations of bundle mechanical behaviour, taking into the account the disposition of 398 399 elementary fibres in a circle or ellipse can have an influence on the resulting behaviour of the bundle. For example, numerical simulations by (Del Masto et al., 2017) have shown that the 400 401 more the ellipticity of a hemp elementary fibre tends towards 0, the more the tensile 402 behaviour of the fibre is non-linear. In addition, a better knowledge of bundle morphology 403 could allow an in-depth study of the effect of twisting on their mechanical behaviour. It is quite possible that there is a mechanical coupling (tensile-torsion) or high stress-concentration 404 405 during the elongation of these samples. Due to the size of the bundle or elementary fibre the 406 fine description of the morphology remains little investigated. To overcome this experimental 407 difficulty, numerical approaches are increasingly being considered (Mattrand et al., 2014; Ntenga and Beakou, 2011) and make it possible to study the relationship between the 408 409 complex morphology of plant fibres and their mechanical behaviour (Del Masto et al., 2017). 410 So, based on the results of our morphological analysis, the outer contour of the fibre bundles 411 as made possible by our measurement method was reconstructed numerically. The following basic assumptions are made: 412

In accordance with the model adopted for our measurements, the cross-section is
assumed to be elliptical and the bundle is assumed to have perfect symmetry around its
longitudinal axis.

The morphology reconstructed ignores the disposition of elementary fibres whichconstitute the bundles. So the bundle is considered as a homogeneous medium.

Three types of bundles were reconstructed (**Figure 7b, 7c and 7d**): a bundle with little morphological variation; a bundle with strong morphological variations, and a bundle reconstructed with mean lengthwise evolution of the cross-section.

Figure 7: (a) Example of elementary fibre disposition which could induce a change of orientation of the cross-section according to our calculation method, (b) 3D reconstruction of the outer contour of bundle with little morphological variation, c) 3D reconstruction of the outer contour of bundle with strong morphological variations, d) A 3D reconstructed bundle with the average values of lengthwise evolution of the crosssection and e) 3D reconstruction of a bundle outer contour by X-ray nanotomography (Del Masto, 2018)

It is possible to compare this purely numerical 3D reconstruction by X-ray nanotomography 3D reconstruction of a bundle outer contour (**Figure 7e**). Note that the number of characterized cross-sections per bundle should be increased to approach more realistic description. However, the heterogeneity of the cross-section highlighted by the measurements is well illustrated in these reconstructions. The models obtained here will be refined and can be used to study by numerical simulations the relationship between the complex morphology of bundles and their tensile behaviour.

#### 421 **4. Conclusion**

In this paper, we investigated the morphological variations of flax fibre bundles cross-section using the Fraunhofer diffraction technique. A particular focus was made on the heterogeneity of the morphology of a hundred flax fibre bundles. The first finding is the confirmation of the high intra-bundle and inter-bundle scattering of the cross-section. Over 75 mm of a 100 mm 426 length bundle, the cross-section area (CSA) is on average multiplied by 3.4 and the shape 427 factor of cross-section doubles. This clearly shows that it is imperative to determine a mean 428 CSA per bundle for later calculation of mechanical properties. Our method has also 429 highlighted the elliptical shape of the bundles cross-sections. Compared to the elliptical 430 model, using a circular model to obtain an "mean apparent diameter" of the bundle is a less 431 relevant method for a reliable estimation of flax fibre bundles CSA.

432 The morphological scattering coupled with the method geometrical model of the cross-section 433 & measurement technique) used to characterize the cross-sections is one of the reasons which explain the dispersion of the mechanical properties reported by different studies on flax fibre 434 435 bundles. A standardisation of the method using to determine the CSA of plant fibres is strongly required to eliminate the variability introduced by the different techniques used. This 436 would allow a more reliable comparison of results from different studies. The method 437 438 proposed here for plant fibres is of particular interest if it is essential that the analysed 439 samples keep their morphology undamaged for further testing.

Additionally, a possible change in cross-section orientation between two consecutive measurement points along the bundle was revealed. Local twisting of some bundles was thus observed. More detailed analyses, such as an increase in the number of measurement points per cross-section and per – which is possible with automated laser scanning device – would be needed to gain in-depth knowledge of these local bundle twists.

These different results allowed us to reconstruct the 3D evolution of the outer contour of flax fibre bundles. Although performed numerically with a low number of cross-sections per bundle given the length of our samples, the reconstruction helps to highlight the significant heterogeneity in the size and shape of the flax fibre bundle cross-section. In future works, by incorporating elementary fibres in the 3D reconstructions, the use of finite element method could help to better understand the mechanical behaviour of the bundles: especially stress 451 concentration phenomena and the shear occuring at the interface of elementary fibres during a452 tensile test.

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454 Funding: This research did not receive any specific grant from funding agencies in the455 public, commercial, or not-for-profit sectors.

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Figure 1: (a) Schematic diagram of the Fraunhofer diffraction principle and (b) Diffraction pattern recorded on the display table

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Figure 2: Characteristics of the axes of the cross-section: (a) Distribution of the minoraxes, (b) Distribution of the major-axes and (c) Lengthwise evolution of cross-section axis for two bundles





587 Figure 3: (a) Cross-Section Area distribution and (b) Lengthwise variations of flax fibre

588 **bundle CSA** 



Figure 4: Two different flax fibre bundles section seen in profile



Figure 5: (a) Power law correlation between "maximum mean axis" and mean CSA of
the bundle and (b) Illustration of the ellipticity of flax fibre bundle : curves drawn with
major axis of the ellipse = diameter of the comparison circle = 100 μm

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Figure 6: (a) Illustration of the change of orientation between two consecutive sections
 and (b) Bundle with local twisting



Figure 7: (a) Example of elementary fibre disposition which could induce a change of orientation of the cross-section according to our calculation method, (b) 3D reconstruction of the outer contour of bundle with little morphological variation, c) 3D reconstruction of the outer contour of bundle with strong morphological variations, d) A 3D reconstructed bundle with the average values of lengthwise evolution of the crosssection and e) 3D reconstruction of a bundle outer contour by X-ray nanotomography (Del Masto, 2018)