

Sea-Spray-Generation Dependence on Wind and Wave Combinations: A Laboratory Study

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William Bruch, Jacques Piazzola, Hubert Branger, Alexander M J van Eijk, Christopher Luneau, et al.. Sea-Spray-Generation Dependence on Wind and Wave Combinations: A Laboratory Study. Boundary-Layer Meteorology, 2021, 180, pp.477 - 505. 10.1007/s10546-021-00636-y . hal-03344241

HAL Id: hal-03344241 https://hal.science/hal-03344241v1

Submitted on 6 May 2022

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Sea Spray Generation Dependence on Wind and 1

Wave Combinations : A Laboratory Study 2

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Received: DD Month 2020 / Accepted: DD Month YEAR 7

Abstract This paper investigates the effect of interacting winds and waves 8 on the surface sea spray generation flux. To this end, the Marine Aerosol 9 Tunnel Experiment (MATE2019) was conducted at the OSU-Pytheas large 10 wind-wave tunnel facility at Luminy, Marseille (France), in June-July 2019. 11 A unique range of air-sea boundary conditions was generated by configuring 12 the laboratory with four types of wave forcing and five wind speeds ranging 13 from 8 to 20 m s⁻¹. The configurations included both young and developed

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waves spanning a wave age (defined in terms of phase speed and friction ve-15 locity) range between 1.3 and 9.5. Sea spray concentrations were measured 16 over the 0.1-47.5 μ m radius range at different heights above water, and a flux-17 profile method using Monin and Obukhov (1954) theory allowed to estimate 18 the sea spray generation flux from concentration profiles. Results show that 19 the flux increases for increased wind-induced wave breaking, and the highest 20 flux is found for steep and heavily-breaking wind-forced waves. Scaling analysis 21 shows that the sea spray generation is best correlated with the wave slope vari-22 ance $(\langle S^2 \rangle)$ for larger droplets (20 μ m and above, assumed predominantly 23 spume droplets generated by surface tearing). For smaller droplets (7-20 μ m, 24 presumed predominantly jet droplets generated by bubble bursting) highest 25 correlation is found with a non-dimensional number combining $\langle S^2 \rangle$ and 26 the friction velocity cubed u_*^3 . This is reflected in the formulation of two wave 27 state dependent sea spray generation functions (SSGFs), each valid for wind 28 speeds 12-20 m s⁻¹ and droplet radii 3-35 μ m, thereby covering both jet and 29 spume droplet production. 30

Keywords Sea spray generation · Air-sea interaction · Wave slope variance ·
 Friction velocity cubed

33 1 Introduction

Sea spray aerosols formed by the interaction between air and water represent
a major component of the natural aerosol mass (Jaenicke, 1984; Yoon et al.,
2007) with a major role in the Earth radiation budget (Mallet et al., 2003;
Mulcahy et al., 2008). In turn, the light scattering by sea spray aerosols is an
important factor in the context of climate change (Lewis et al., 2004). Sea spray

³⁹ also has a significant impact on air quality, particularly in coastal regions where

⁴⁰ anthropogenic emissions are high (Piazzola et al., 2016; Johansson et al., 2019).

41 However, it remains difficult to numerically model these effects. Significant

⁴² predictive uncertainties remain for sea spray aerosol in numerical models with

43 significant biases observed for commonly used emission schemes (Tsyro et al.,

44 2011; Chen et al., 2016; Neumann et al., 2016). Therefore, sea spray aerosol

45 generation and subsequent transport in the atmosphere models need to be

⁴⁶ improved (Canepa and Builtjes, 2017).

Sea spray can be produced both directly and indirectly from the water 47 surface. Indirect generation is associated with the relatively small bubble-48 mediated jet and film droplets produced by wave breaking, effective for wind 49 speeds around 4 m s⁻¹ and above (Blanchard, 1963; Spiel, 1994). The transition 50 from film to jet droplet dominance is thought to occur at radii 2 - 4 μ m 51 (Cipriano and Blanchard, 1981; Woolf, 1997) with jet droplets dominating 52 over the 2 - 20 μ m range and sometimes reaching 50 μ m or more (Newitt, 53 1954; Andreas, 1998). The direct sea spray generation mechanisms activated 54 at wind speeds higher than 10 - 12 m s⁻¹ (Monahan et al., 1986; Andreas et al., 55 2010) consist of surface-tearing of larger (radius $r > 20 \ \mu m$) spume droplets 56 that are directly ejected into the air flow. 57

The direct generation mechanisms have proven to be elusive. Anguelova 58 et al. (1999) noted the tearing of spume drops at the wave crests by the wind, 59 and found spume droplet generation to be strongly related to the whitecap 60 coverage. On a microphysical scale the bag breakup of small canopies of water 61 produced by wind surface friction at the wave crests is a potential mecha-62 nism for spume droplet generation (Mueller and Veron, 2009; Veron et al., 63 2012; Troitskaya et al., 2018). All in all, little is known about the generation 64 of particles of radii > 20 μ m (Veron et al., 2012; Veron, 2015). A better pa-65

rameterization of the droplet generation flux and transport over this range is urgently needed, since a major portion of the total volume of sea spray droplets is thought to be within the 10-200 μ m radius range, as stressed by authors such as Andreas (1992).

The sea spray flux or sea spray generation function (SSGF) is known to 70 depend on numerous environmental parameters such as the wind and wave 71 fields (De Leeuw, 1986; Iida et al., 1992; Smith et al., 1993), the sea surface 72 temperature (Mårtensson et al., 2003), and the composition and salinity of the 73 seawater (Sellegri et al., 2006; Mehta et al., 2019). Although wind speed alone 74 was traditionally used to parameterize the aerosol generation - cf. the SSGFs of 75 Monahan et al. (1986); Smith et al. (1993); Andreas (1998) - there is increasing 76 evidence that this is not sufficiently accurate, and additional environmental 77 conditions have to be taken into account, wave parameters especially. Various 78 authors have also considered scaling droplet generation with non-dimensional 79 numbers such as wave age (Lafon et al., 2007; Laussac et al., 2018), or the 80 windsea Reynolds number R_B (Zhao et al., 2006; Ovadnevaite et al., 2014; 81 Troitskaya et al., 2018). The wave age is defined as the ratio between the wave 82 phase velocity c_p and a wind parameter (for example the wind friction velocity 83 u_*), and is generally used to describe wave-field development and wave-wind 84 equilibrium. R_B , first introduced by Toba and Koga (1986) as $u_*^2/(\nu_a \omega_p)$ with 85 the air kinetic viscosity ν_a and the windsea spectrum peak angular frequency 86 ω_p , thus describing turblence at the wind-wave boundary. The role of wave 87 breaking mechanisms on generation has also been a focus of study with the 88 use of whitecap coverage to scale film, jet (Laussac et al., 2018) and spume 89 droplet generation (Anguelova et al., 1999). In a similar fashion, wave energy 90 dissipation - considered proportional to u_*^3 (the third power of the friction 91 velocity u_*) by several authors - has also been considered for the study of 92

droplet and bubble generation (Newell and Zakharov, 1992; Zhao and Toba,
2001; Zhao et al., 2006; Andreas, 1998, 2002; Fairall et al., 2009).

Of the different wave parameters used to scale sea spray generation, the 95 wave slope has not yet been considered. Nevertheless, it is an interesting can-96 didate because of its strong relation to wave breaking (Stokes, 1880; Duncan, 97 1981; Ramberg and Griffin, 1987), whitecap production (Banner et al., 2002; 98 Brumer et al., 2017), and therefore to sea spray bubble-bursting and surface-99 tearing generation mechanisms. The wave slope, however, is also thought to 100 modulate the air flow at the wave crest (Veron, 2015; Richter et al., 2019; 101 Husain et al., 2019), which is of crucial importance for air-sea momentum 102 transfer and surface tearing mechanisms. Finally, the relationship between the 103 wave slope variance and the wind speed at the wind-wave boundary is rela-104 tively well documented (Cox and Munk, 1956; Plant, 1982; Vandemark et al., 105 2004; Bringer et al., 2013; Lenain et al., 2019). 106

With the advantage of easier instrumentation and control over important 107 environmental parameters compared to the complexity of the field, the labo-108 ratory has proven to be a valuable alternative to the field (open ocean) for the 109 study of wave-wind boundary processes and sea spray generation (Toba and 110 Koga, 1986; Fairall et al., 2009; Ortiz-Suslow et al., 2016; Troitskaya et al., 111 2018). Therefore, we conducted a series of experiments in the wave-wind tunnel 112 at the OSU Pytheas (Observatoire Sciences de L'Univers) Ocean-Atmosphere 113 laboratory in Luminy, France. In the field, a wide range of wind and wave 114 combinations can be encountered. To reproduce a similar range in environ-115 mental conditions the laboratory experiments also included a unique range of 116 wind and wave conditions, which, to the knowledge of the authors, is the most 117 extensive range ever used for studying the SSGF in a laboratory configura-118 tion. The aim is to develop a universal wind and sea state-dependent SSGF 119

applicable for radii typical of jet and spume droplets. To this end, from June 120 to July 2019, sea spray aerosol size concentrations were measured for a total 121 of twenty wind and wave combinations as part of the Marine Aerosol Tunnel 122 Experiment (MATE2019). The experiment is described in Sect. 2, wind and 123 wave results are discussed in Sect. 3, and sea spray results in Sect. 4. Study 124 results include a comparison between the laboratory data and other labora-125 tory and field SSGFs presented in the literature. Finally, two new SSGFs are 126 introduced in Sect. 5, one depending on the wave slope variance alone, and a 127 second on both the wave slope variance and u_*^3 . Both SSGFs combine labora-128 tory and field data, and are valid for wind speeds 12-20 m $\rm s^{-1}$ and radii 3-35 129 $\mu m.$ 130

131 2 Methods

132 2.1 The wind-wave tunnel

The UMS Pytheas ocean-atmosphere interactions facility at Luminy (Mar-133 seille, France), schematically represented in Fig. 1, consists of a water tank 134 with a wind tunnel on top of it. The facility currently allows the use of fresh 135 water only. The water tank is 40 meters long, 2.6 meters wide, and has a 136 wave-dissipating beach at the downwinde end to avoid wave reflection. On the 137 upwind end, the facility is equipped with a programable submerged piston-138 like wavemaker located at the bottom of a cavity below the air tunnel and 139 controlled by an electrohydraulic motor. Wave properties such as amplitude, 140 frequency and slope can therefore be selected. Waves can attain amplitudes 141 reaching 15 cm, approximately. The air channel ceiling is slightly inclined to 142 the fetch to avoid the airflow acceleration and the related longitudinal pressure 143

gradient generated by the thickening of the wall and water surface boundary layers (Coantic et al., 1981). To reduce turbulence as the air flow encounters the water surface, a thin buoyant sheet is placed at the surface of the water at the entrance of the tunnel. The wind speed in the facility is adjustable, with winds reaching 15 m s⁻¹, approximately. Glass walls on either side of the laboratory made it possible to monitor the experiment at the location of the instruments (given below).





For the experiments in June-July 2019, the water depth was set to 90 cm, 151 leaving 150 cm between the water surface and the ceiling of the wind tunnel. 152 As schematically represented in Fig. 1, instruments used for the measurements 153 of air, water, wind and wave characteristics were placed at the 27.2 meter fetch 154 mark. A sensor positioned 81 cm above the mean water level (MWL) was used 155 to measure air relative humidity (RH) and temperature (T_a) . Vertical profiles 156 of horizontal wind speed and air temperature between 15 and 66 cm above 157 MWL were obtained using sensors mounted on a telescopic arm. The water 158 temperature was measured at both 20 and 60 cm depth beneath the MWL. 159 A camera with 60 Hz sampling frequency placed on the tunnel ceiling allowed 160 estimating the whitecap coverage during the experiments from color images. 161 Though not schematically represented in Fig. 1 a higher-frequency 128 Hz 162 camera was used to film through the glass wall of the tunnel for monitoring 163 purposes only. Finally, at the 30 meter fetch mark, vertical profiles of the sea 164

spray number concentration were measured using two particle probes mounted
 onto a vertically displaceable frame.

¹⁶⁷ 2.2 Wave generation and characterisation

The water surface elevation was measured by an array of two calibrated capacitance wave gauges placed at the 27.2 meter fetch mark. The sample frequency for the wave gauges was 256 Hz allowing to sample a wide range of wave surface elevation and slope frequency spectra. The sensors were aligned orthogonally to the general wave direction, and were placed 1 cm from each other to ensure accurate wave slope measurements.

In the present study, four types of waves were generated. Five different wind 174 speeds between 8-20 m s⁻¹ were applied over each wave type, in a total of 20 175 laboratory wind-wave configurations. A first type of waves was generated solely 176 by the wind, resulting in pure wind waves. The other three types of waves were 177 generated using the piston wavemaker and are referred to as short wave forcing 178 (peak frequency $f_p = 1.3$ Hz and wavelength $\lambda = 0.92$ m), intermediate wave 179 forcing $(f_p = 1.1 \text{ Hz and } \lambda = 1.29 \text{ m})$, and long wave forcing $(f_p = 0.8 \text{ Hz and } \lambda$ 180 = 2.4 m). These conditions were selected to ensure that near-equilibrium with 181 the overlying wind field was either never met, or met at different wind speeds. 182 Deep water conditions are theoretically confirmed for all types of forcing except 183 the long wave case. This is also the wave type that is least forced by the wind 184 and can be considered representative of the wind over swell condition that can 185 be found in the field. Together, the 20 tunnel wind and wave combinations 186 span a range of wave ages $\frac{c_p}{u_*}$ between 1.3 and 9.6. 187

The wave sensor array provides several parameters that are useful to relate the wave properties measured at the 27.2 m fetch mark to the sea spray concentrations measured at the 30 m fetch mark. The significant wave height H_S is determined using:

 $H_s = 4\sigma_\eta$

where σ_{η} is the standard deviation of the surface elevation (η) time series measured by the wave sensor array.

The wave slope variance $\langle S^2 \rangle$ is considered equal to the wave mean square slope (MSS). It is calculated from the time series of the wave slope S, for wavelengths $\lambda > 1$ cm (strong majority of waves dominated by gravity). The use of classical Fourier analysis allows to determine the peak frequency f_p from the wave elevation energy spectra. Finally, the wave phase speed c_p is determined from the phase shift between the wave gauges as the waves propagated along the wave sensor array.

202 2.3 Whitecap measurements

To quantify the wave breaking, the whitecap coverage W(%) is estimated from 203 video colour images taken by a camera mounted at the tunnel ceiling (cf. Fig. 204 1). The system takes images at 60 Hz frequency with dimensions 2704×2028 . 205 These images are spatially referenced to allow to estimate the approximate 206 surface area of each pixel. To identify the whitecaps, a separation method is 207 used that applies a greyscale conversion and a subsequent intensity threshold 208 to the image. The surface areas of the pixels above threshold are subsequently 209 added and divided by the total image surface area for an estimate of the 210

whitecap surface coverage W(%). Using a time series of images, it was found that W(%) estimates converge to an average value within approximately 120 frames. This method for whitecap estimation is commonly used (e.g. Lafon et al. (2007); Lenain and Melville (2017); Brumer et al. (2017)), and although the selection of the intensity threshold may be subjective, we expect that our whitecap coverage estimates capture the relative amount of wave breaking induced by various wind and wave conditions.

218 2.4 Wind measurements

A hot film wind sensor (E+E Elektronik, Langwiesen, Austria) mounted onto 219 a telescopic arm was used to measure vertical profiles of horizontal wind speed 220 U at the 27.2 meter fetch mark (cf. Fig. 1). This sensor was calibrated against a 221 reference sonic anemometer on several occasions during the experiments. Some 222 subsets of wind data obtained at 15 cm of the MWL were eliminated from the 223 dataset to avoid erroneous measurements caused by large droplets impacts on 224 the hot film sensor. To ensure representative wind statistics, convergence of 225 the wind speed time-averages was achieved for each height z along the U(z)226 profiles, with averages spanning over 20 to 80 minutes in accordance with the 227 sea spray aerosol sample durations. 228

The wind speed reference used in this study is U_{10} , i.e. the wind speed at 10 meters above MWL. Assuming a logarithmic wind profile and neutral conditions, Monin and Obukhov (1954) scaling allows evaluation of U_{10} (m s⁻¹) and the friction velocity u_* (m s⁻¹) from the measured U(z) profile values U(z):

$$U(z) = \frac{u_*}{k} ln(\frac{z}{z_0}) \tag{1}$$

where k = 0.4 the von Kármán constant, z is the measurement height above MWL, and z_0 the roughness length. The latter is retrieved by extending the wind profile with data from the more elevated part of the wind profile that is not significantly affected by the wave field. During the experiments, z_0 estimates varied between 0.2 and 2.5 mm.

Figure 2 presents the experimental wind profiles for all 20 laboratory config-239 urations (data points with horizontal error bars) as well as the corresponding 240 theoretical profiles obtained with Eq. 1. For clarity and indicative purposes 241 only, are also presented the average friction velocities $\langle u_* \rangle$ calculated over 242 the 4 different wave types for each individual tested wind speed. The experi-243 mental profiles exhibit near-logarithmic behaviour, and the gradient increases 244 for increasing reference wind speed U_{10} , in accordance with a fully developed 245 turbulent layer near the water surface as encountered in the field. This is fur-246 ther evidenced by the windsea Reynolds number (R_B) found greater than 10^3 247 in the laboratory for reference wind speeds U_{10} of 12 m s⁻¹ or more, thereby 248 signifying that the air flow in the boundary layer is in a fully turbulent regime 249 and windsea breaking occurs (Toba et al., 2006). 250



Fig. 2 Measured U(z) profiles for all twenty laboratory configurations (horizontal bars) with associated theoretical profiles (lines) calculated with Eq. 1. Average friction velocities values $\langle u_* \rangle$ pertain to the five wind speeds set in the laboratory.

251 2.5 Sea spray aerosol measurements

The measurement of sea spray in the tunnel was carried out using two CSASP 252 (Classical Scattering Aerosol Spectrometer) probes (Particle Measurement 253 Systems, Boulder, Colorado, USA). This type of probes has been proven re-254 liable in numerous experiments by the authors and others (e.g., Frick and 255 Hoppel (2000); Savelyev et al. (2014); Petelski et al. (2014)). Our two probes 256 have overlapping particle radius ranges allowing a combined range of 0.1 to 257 47.5 μ m. Prior to the experiments, both probes were calibrated with latex 258 particles of known sizes. The CSASP-100-HV-ER probe samples by rotating 259 over 4 sets of 15 size bins at a time, in total spanning from 0.5 to 47.5 μ m 260 radius. The CSASP-200, samples over a single set of 31 size bins ranging from 261

0.1 to 10 μ m radius. The probes send data to the controller every second, 262 and aerosol number concentrations for each bin size are obtained by averaging 263 over a chosen sample (integration) time. Since number concentrations were 264 expected to decrease with increasing height above the water surface, sample 265 times varied from a minimum of 20 minutes at z = 35 cm to a maximum of 266 80 minutes at z = 82 cm in order to improve droplet count statistics. Never-267 theless, particle concentrations for radii greater than 35 μ m were statistically 268 unreliable and had to be discarded. It was verified that droplet concentrations 269 were stationary over the duration of the experiment once equilibrium for a 270 particular laboratory configuration was established. 271

During the experiments, the probes were placed on top of each other. 272 Droplet number concentrations were measured at five different heights for each 273 of the twenty laboratory configurations. For the CSASP-100-HV-ER, samples 274 were made at heights z = 35, 41, 51, 65 and 82 cm above the MWL. These 275 heights are used as reference in this study, and the CSASP-200 concentrations 276 are interpolated to these heights. The air flow inside a long wind-tunnel is not 277 completely homogenous, and very slight transverse counter-rotating stream-278 wise vortices or cells may appear (Holmes et al., 1996; Pope, 2000), with a 279 very weak divergence or convergence zone along the middle of the width of the 280 tunnel. As it is usually done in the IRPHE wind-wave facility, the probes were 281 slightly shifted away from the middle axe line of the facility. For all laboratory 282 configurations, both aerosol probes were temporarily positioned at the tunnel 283 entrance to verify that no background aerosols entered the tunnel, which im-284 plies that all particles detected at the 30 m fetch mark are solely produced 285 over the upwind 30 meter fetch length. 286

After generation at the water surface, the hygroscopic aerosols adjust their size to the ambient humidity and temperature of the air flow. This process is

different for salt water than for the fresh water used in the tunnel, as freshwater 289 droplets can evaporate more quickly and completely than saltwater droplets 290 that reach an equilibrium size (e.g. Pruppacher and Klett (1978); Andreas 291 (1989); Fairall (1990); van Eijk et al. (2001); Mueller and Veron (2014); Mehta 292 et al. (2019)). During the experiments, the relative humidity (RH) in the 293 laboratory varied between 79 and 82%, with an average water temperature at 294 0.2 m depth of 18°C, and an average air temperature T_a at 85 cm height of 295 25°C. We therefore assume that sea spray number concentrations correspond 296 (roughly) to RH = 80%. Since the rate of freshwater droplet evaporation at 297 RH = 80% is relatively small, we assume that out measured droplets are 298 representative for saltwater droplets at their RH = 80% equilibrium radii. 299 However, this assuption will fail if the freshwater droplets are relatively small 300 or have long residence times before reaching the aerosol probes, as evaporation 301 can become substantial (Veron, 2015). To avoid such evaporation effects over 302 the length of the wave-wind facility, only radii greater than 7 μ m are considered 303 for the source functions proposed in this study (see Sect. 5) in accordance with 304 Fairall et al. (2009). 305

Aerosol concentrations are often expressed as number concentrations dN/dr(cm⁻³ μ m⁻¹; the number of particles N of a given radius r measured per unit air) or volume concentrations dV/dr (the volume for a given radius measured per unit air). In this study, we use mostly number concentrations, with a single exception (Sect. 4, Fig. 6). The conversion from number to volume concentrations (cm⁻³ cm⁻³ μ m⁻¹) is made by assuming that the droplets are spherical:

$$\frac{dV}{dr} = \frac{dN}{dr}\frac{4}{3}\pi r^3 \tag{2}$$

As discussed above, we may consider that the freshwater droplet distributions measured in the tunnel are analogous to salt water droplets at RH = 80%. Since the processes that generate the freshwater droplets in the tunnel are the same as for sea spray in the field, we will denote the droplets in the tunnel as sea spray in the remainder of this paper.

318 3 Tunnel wave and wind results

319 3.1 Wave measurements

Table 1 characterises all 20 laboratory configurations in terms of the significant 320 wave height H_s , the wave slope variance $\langle S^2 \rangle$, the friction velocity u_* , 321 and the whitecap coverage W(%). The table shows that the wind field forces 322 the wave field, resulting in increased wave height, wave slope variance and 323 breaking, as evidenced by H_s , $< S^2 >$ and W(%). In some cases however, 324 significant wave height and wave slope decrease for high wind speeds as wave 325 energy dissipation by wind-induced breaking becomes temporarily greater than 326 the energy input from the wind to the waves. This is especially the case for 327 the intermediate wave forcings for wind speeds increasing from 16 to 18 m s⁻¹ 328 (Table 1) where wave breaking was especially high. Further evidence of the 329 forcing of the wave field by the wind is the decrease in f_p for increasing wind 330 speed observed at the 27.2 fetch mark, with the exception of the long wave 331 forcing which conserves the 0.8 Hz frequency prescribed by the wavemaker 332 throughout the experiments. The momentum transfer from the wind to the 333 waves is therefore relatively low for the long wave forcing in comparison to 334 the other wave forcings, resulting in relatively low U(z) gradients (Fig. 2) and 335 whitecap coverages W(%) (Table 1). 336

							10.5			
Forcing		$U_{10} = 8 \text{ m s}^{-1}$				$U_{10} = 12 \text{ m s}^{-1}$				
	H_s	$< S^{2} >$	u_*	c_p	W(%)	H_s	$< S^{2} >$	u_*	c_p	W(%)
Wind	3.2	0.026	0.32	0.78	0.13	5.5	0.039	0.54	0.99	0.29
Short	9.7	0.037	0.28	1.19	0.28	12.4	0.053	0.52	1.29	0.62
Inter.	13.2	0.033	0.21	1.42	0.32	16.7	0.047	0.46	1.49	0.53
Long	12.0	0.024	0.23	2.2	0.16	13.8	0.03	0.48	1.7	0.25
		$U_{10} = 16 \text{ m s}^{-1}$				$U_{10} = 18 \text{ m s}^{-1}$				
Wind	8.3	0.056	0.75	1.1	0.8	9.63	0.062	0.89	1.25	1.25
Short	13.7	0.063	0.76	1.33	1.17	15.4	0.066	0.85	1.54	1.45
Inter.	20.1	0.087	0.8	1.50	2.55	18.4	0.08	0.89	1.59	4.65
Long	16.5	0.046	0.66	2.1	0.73	19.6	0.055	0.79	2.14	0.84
$U_{10} = 20 \text{ m s}^{-1}$										
Wind	11.3	0.073	1.05	1.32	2.0					
Short	15.2	0.072	1.01	1.63	2.25					
Inter.	17.6	0.078	1.0	1.57	3.19					
Long	21.6	0.065	0.9	2.15	1.19					

Table 1 Wave-wind boundary characteristics for the different laboratory configurations: significant wave height H_s (cm), wave slope variance ($\langle S^2 \rangle$), friction velocity u_* (m s⁻¹), wave phase speed c_p (m s⁻¹) and whitecap coverage W(%)

This non-linear behaviour of the parameters listed in Table 1 highlights 337 the importance of correctly understanding the boundary processes, such as 338 the state of wind-wave equilibrium. Though not shown here, f^{-5} and f^{-4} 339 spectral shapes were identified for the individual wave spectra, but it proved 340 difficult to quantify the wave-wind equilibrium this way. We therefore abide by 341 the heuristic idea that when the phase speed c_p is greater than the overlying 342 wind speed (e.g. the friction velocity u_*) then the underlying waves are no 343 longer forced by the wind field. Thus we use the wave age defined as c_p/u_* to 344 quantify the wind-wave equilibrium. 345

Our laboratory configurations yield wave age c_p/u_* values ranging from 1.3 to 9.6 where the higher values correspond to the long wave forcing combined with the lowest wind speed (8 m s⁻¹). These values are generally lower than those recorded in the field because of the comparatively much shorter fetch length in the laboratory.

351 3.2 Whitecap measurements

As previously noted, several studies have related whitecapping to the genera-352 tion of film, jet and spume droplets. For comparison, it is therefore important 353 to ascertain whether the whitecap production in the laboratory differs from 354 the field. To this end, we use data collected during the EMMA campaign which 355 took place in Toulon-Hyeres bay, yielding wave, wind and whitecap coverage 356 data for wind speeds in the 10 - 18 m s⁻¹ range and wave ages c_n/u_* in the 14 -357 28 range Lafon et al. (2007). We compare our laboratory whitecap coverage to 358 that measured in fetch-limited field conditions during EMMA, using a similar 359 image-processing technique with intensity threshold separation (data available 360 in Lafon et al. (2007)). Laboratory data obtained at 8 m s⁻¹ wind speed are 361 not included in this comparison because the relatively small amount of wave 362 breaking may reduce the accuracy of the whitecap coverage estimates. 363

Multiple independent scaling studies have proven R_B to be a successful 364 scaling tool for W(%) (Zhao and Toba, 2001). However, the evaluation of 365 R_B requires the wave peak frequency ω_p , which differs significantly between 366 the laboratory and the field. The relatively short fetch in the laboratory and 367 the wavemaker settings lead to shorter wavelengths and a relatively greater 368 number of wave crests per unit area (Mueller and Veron, 2009). To allow 369 a better comparison between the laboratory and the field, the W(%) value 370 are therefore normalised by the wave peak frequency. Figure 3a shows the 371 relationship between the normalised W(%) and R_B . The data from both the 372 laboratory (+) and the field $(\mathbf{\nabla})$ display a very similar trend yielding nearly 373 identical slopes when fitted by a power law. In absolute magnitude there is a 374 factor 1.5 difference between the laboratory and the field with the lower W(%)375 values for the laboratory. A possible explanation is the absence of surfactants 376

and salt in the laboratory, which in the field contribute to whitecap formation and increase whitecap lifetime (Callaghan et al., 2012). Consequently, the lower rate of whitecap formation and lifetime in the laboratory may signify that our whitecap coverage is more representative for the process of active wave breaking, which we refer to as the wave breaking coverage.



Fig. 3 Comparison between laboratory and field (Lafon et al., 2007) (a) f_p -normalised whitecap coverage W(%) estimates as function of the windsea Reynolds number R_B , and (b) W(%) as function of the wave slope variance $\langle S^2 \rangle$. Lines and corresponding R^2 statistics represent power laws fitted to the data.

A further comparison between the laboratory and the field is obtained by 382 scaling W(%) to the wave slope variance $\langle S^2 \rangle$. In this case, W(%) does 383 not need to be normalised by the peak frequency as the wave slope variance 384 $< S^2 >$ integrates a very large part of the wave frequency spectrum and 385 corresponding wave slopes, unlike the peak wave characteristics required for 386 windsea Reynolds number R_B . For the EMMA campaign data (Lafon et al., 387 2007), < $S^2\,>$ is estimated from the measured wind speed data (Cox and 388 Munk, 1956) : 389

$$\langle S^2 \rangle = 0.003 + 5.12 \times 10^{-3} U_{12.5} \pm 0.004$$
 (3)

where the wind speed $U_{12.5}$ is calculated from the EMMA campaign U_{10} measurements using classical Monin and Obukhov (1954) theory. It is worth noting that Eq. 3 (Cox and Munk, 1956) was determined from airborne observations of sun glitter resulting in the contribution of a wide range of wave scales including non-breaking waves, which is to some extent comparable to the wide range of wavelengths included in the laboratory wave slope variance.

Figure 3b presents the W(%) scaling by $\langle S^2 \rangle$, demonstrating that laboratory (+) and field ($\mathbf{\nabla}$) data almost overlap. The laboratory data is well fitted ($R^2 = 0.75$) by a the power law:

$$W(\%) = 6.02 \times 10^3 < S^2 >^{3.025}$$
⁽⁴⁾

The good fit of this power law to field data (Fig. 3b) suggests that Eq. 4 may 399 have a validity range extending to both the laboratory and the field. The strong 400 correlation between $\langle S^2 \rangle$ and W(%) suggests that the wide range of the 401 wave slope spectrum inherent to $\langle S^2 \rangle$ allows to separate breakers and non 402 breakers. This corroborates conclusions from a north-Pacific field campaign 403 (Schwendeman and Thomson, 2015), where the wave slope variance amongst 404 the different existing slope parameterizations is found to scale best with W(%)405 by considering the slopes of the shorter waves, thought to be important for 406 whitecap production. In contrast, the scaling of whitecap coverage with wave 407 steepness (often written as $H/(2\lambda)$) has proven difficult (Schwendeman and 408 Thomson, 2015) or even unsuccessful (Holthuijsen and Herbers, 1986). 409

410 4 Laboratory sea spray results

411 4.1 Sea spray aerosol size distribution spectra

Figure 4 presents two typical size distributions as measured in the laboratory. 412 The figure shows the sea spray distributions for wind speeds $U_{10} = 16 \text{ m s}^{-1}$ 413 and $U_{10} = 20 \text{ m s}^{-1}$, measured 55 cm above MWL and during the intermediate 414 wave forcing. For convenience, polynomial functions (solid and dashed lines for 415 16 and 20 m s⁻¹, respectively) have been fitted to the distributions. The poly-416 nomial functions show that the number concentration of all but the smallest 417 particles increases with increasing wind speed. This behaviour is observable 418 at any height above MWL and for all four types of wave forcing. The con-419 centration increase is consistent with the increased W(%) for increasing wind 420 speeds (cf. Table 1) and hence, the enhanced droplet generation. Furthermore, 421 the size distribution shows a relative abundance of particles with sizes around 422 1 and 10 μ m. This corroborates the established size ranges of film and jet 423 droplets, respectively. The droplet spectra for larger radii change markedly at 424 wind speeds lower than 12 m s⁻¹, where number concentrations for $r > 15 \ \mu m$ 425 are negligible. This corroborates the assumption that these larger droplets are 426 predominantly spume droplets, and that their generation mechanism activates 427 at wind speeds around 12 m s⁻¹. This was confirmed by our high-speed video 428 footage, which revealed surface tearing and bag break-up only for wind speeds 429 higher than 12 m s⁻¹. In conclusion, the above observations suggest that sim-430 ilar droplet generation mechansisms are active in the laboratory and in the 431 field. 432



Fig. 4 Sea spray number concentration size distribution at 55 cm above the MWL for the intermediate wave forcing.

Let us now consider the vertical distribution of the freshly generated parti-433 cles. Figure 5 shows number concentration profiles obtained at $U_{10} = 20 \text{ m s}^{-1}$ 434 as a linear function of the natural logarithm of height ln(z). Two sets of profiles 435 are shown, for droplets of 10 and 20 μ m radius, and each set contains data for 436 the four different types of wave forcing. The symbols of individual data points 437 refer to the type of wave forcing. The lines denote linear functions fitted on 438 the experimental data. Figure 5 suggests that the vertical number concentra-439 tion profiles of sea spray are near-logarithmic with height above MWL. This 440 behaviour is general for all radii in the 7-35 μ m range. For the three highest 441 wind speeds, R^2 values of the individual fits all exceed 0.95. Though not pre-442 sented in Fig. 5 for clarity, the standard deviation in number concentrations is 443

highest closest to the water surface, especially for intermediate and short wave 444 forcing, but remains very small with a maximum value approaching $10^{\text{-5}}\ \mathrm{cm}^{\text{-3}}$ 445 μ m⁻¹ at z = 0.35 m. As the environmental conditions were stationary during 446 the measurements for each individual laboratory configuration, this greater 447 variability (standard deviation) in near-surface concentrations could be asso-448 ciated with wave-induced and phase-locked modulation of the airflow, which 449 can lead to flow separation. These mechanisms have recently been observed in 450 microphysical laboratory experiments (Buckley and Veron, 2019; Richter et al., 451 2019; Husain et al., 2019). Whether this modulation effect also caused stronger 452 fluctuations in the near-surface sea spray concentrations in the laboratory re-453 mains hypothetical as the maximum sample frequency of the particle probes 454 does not allow to resolve these fluctuations assumed to occur at frequencies 455 approaching f_p or higher. 456



Fig. 5 Sea spray number concentration profiles at 20 m s⁻¹ winds as function of height, represented as ln(z). Symbols denote experimental data, lines linear fits to the data.

Figure 5 also demonstrates that the type of forcing affects the vertical 457 concentration gradients. The stronger gradients are observed for intermediate 458 and short wave forcings, whereas the forcing by wind alone results in a less 459 pronounced concentration decrease with height. To further investigate the ef-460 fect of sea state, Fig. 6 focuses on the aerosol size distributions over the 6 -461 47.5 μ m radius range obtained at z = 35 cm, and for wind speed $U_{10} = 20$ m 462 s⁻¹. Individual datapoints represent an average over several particle bin sizes 463 (spanning $\pm 4 \ \mu m$) for clarity, and horizontal and vertical error bars illustrate 464 the standard deviations in average size and concentration, respectively. The 465 data is presented on a log-log scale, and individual datapoints are connected 466

⁴⁶⁷ by lines to provide an indication of the volume spectrum. As identified by the
⁴⁶⁸ legend in Fig. 6, we present data for the four types of wave forcings using in
⁴⁶⁹ the laboratory.



Fig. 6 Sea spray volume concentrations for $U_{10} = 20 \text{ m s}^{-1}$ at 35 cm above the mean water level, for the four forcings used in the laboratory. SPANDEX data measured at 31.5 cm above MWL corresponding to their nominal condition is presented for comparison.

Figure 6 depicts volume rather than number concentrations. Comparing with Fig. 4 reveals that while large droplets are less numerous, they represent the larger part of the volume (or mass). Presenting the data as volume concentrations allows us to better detail the differences between the four types of wave forcing. Visual comparison of the four curves reveals that wind forcing alone results in the lowest concentrations (dashed curve) and a distribution that strongly decreases for $r > 20 \ \mu$ m. The three wavemaker forcings all result in higher volume concentrations than the wind forcing: the order long, short and intermediate for increasing concentration corresponds well with the increase in whitecap W(%) and wave slope variance $\langle S^2 \rangle$ for these three types of forcing (cf. Table 1), and hence, the production of droplets.

A literature survey for comparison laboratory data identified the SPAN-481 DEX dataset (Fairall et al., 2009) as the most suitable. These authors also 482 used a wind-wave interaction tunnel with freshwater and a mechanical wave 483 paddle for the wave forcings. The triangles in Figure 6 (connected by the thin 484 dashed line) represent the volume concentrations reported by Fairall et al. 485 (2009), obtained at 31.5 cm height for 16.7 m s⁻¹ wind speed (corresponding 486 to their nominal forcing) measured at 40 cm above MWL (roughly equivalent 487 to 28 m s⁻¹ at U_{10}), 1.36 Hz peak wave frequency (same as our short wave 488 forcing), and friction velocity $u_* = 1.44$ m s⁻¹. Though the wind speed and 489 friction velocity were 50 % greater than for the present study, the SPANDEX 490 volume concentrations are of the same order of magnitude as our wave-forced 491 data (cf. Fig. 6). This unexpected overlap may be explained by experimental 492 differences such as tunnel dimensions (more than three times the height be-493 tween the water surface and the tunnel ceiling during MATE2019 compared 494 with SPANDEX) leading to possibly different boundary effects. Another ex-495 planation maybe also be related to the different wave amplitudes between 496 both experiments (≈ 5 times greater in the present study) resulting in shorter 497 distances between the probes and the wave crests in the case of MATE2019 498 despite comparable sample heights in the present comparison. 499

⁵⁰⁰ 4.2 Scaling parameters for the sea surface sea spray generation

In the previous section we have demonstrated that the sea spray concentra-501 tion depends on properties of both the air flow and the sea state. To bridge 502 these two domains, we will scale the sea spray surface generation using non-503 dimensional numbers representing the physical processes on the wind and wave 504 side of the wave-wind boundary. The non-dimensional numbers determined 505 from the set of parameters $(u_*, \omega_p, c_p, H, \lambda, X, g, \rho_a, \rho_w, \nu_a, \nu_w, \Gamma)$, where 506 u_* is the friction velocity, ω_p is the wave peak angular frequency, c_p is the 507 wave phase speed, H is the wave height, λ is the wavelength, X is the fetch 508 length, g is gravitational acceleration, ρ_a and ρ_w are air and water densities 509 respectively. Furthermore, ν_a and ν_w are air and water kinematic viscosities, 510 respectively, and Γ is the water surface tension. 511

As a first step, we focus our attention on the air kinematic viscosity. Sev-512 eral studies have indicated that water droplets and water vapor can alter the 513 air viscosity, but the effect on the momentum flux is thought to be small, 514 less than 3% (Fairall et al., 2009). We therefore consider the non-dimensional 515 groups ν_a/ν_w and ρ_a/ρ_w to be constants. We also expect the surface tension 516 Γ to be constant and remain negligible due to the relatively long wavelengths 517 considered here (strong majority of gravity waves). Then, we can express the 518 sea spray aerosol generation flux as a function of the non-dimensional numbers 519 that are the inverse wave age $(= u_*/c_p)$, the windsea Reynolds number R_B 520 $(= u_*^2/(\nu_a \omega_p))$, determined from both wind (u_*) and peak wave (ω_p) charac-521 teristics), and the wave steepness. In continuity with the previous sections, 522 the wave slope variance $\langle S^2 \rangle$ is used instead of the wave steepness $(H/2\lambda)$. 523 The inverse wave age is preferred to the wave age out of physical coherence, as 524 the former is expected to increase for increasing R_B and $\langle S^2 \rangle$. We create 525

⁵²⁶ a fourth scaling parameter by combining the inverse wave age, the windsea ⁵²⁷ Reynolds number and the wave slope variance:

528

$$P_S = R_B < S^2 > \frac{c_p}{u_*}^{-1}$$

which, considering the deep water dispersion relation $c_p = \frac{g}{2\pi}T$ (*T* the wave period), reduces to:

$$P_{S} = \frac{u_{*}^{3}}{\nu_{a}g} < S^{2} > \tag{5}$$

where P_S , adding to the P threshold for the activation of droplet and bub-531 ble formation at the water surface (Newell and Zakharov, 1992; Fairall et al., 532 2009), describes the wave slope variance-modulated wind energy input to the 533 waves. This number combines two experimental quantities, $\langle S^2 \rangle$ provided 534 by the wave sensor array, and u_*^3 provided by the wind speed vertical profiles, 535 providing information on the wind-dependent sea state and wind-induced dis-536 sipation, respectively. This allows to study air-sea interaction processes from 537 a multiscale point of view, assuming that the smaller and larger scale wind 538 and wave components significantly contribute to boundary layer mechanisms 539 responsible for sea spray generation. 540

⁵⁴¹ 4.3 Scaling of the sea spray generation

This section discusses the scaling of the sea spray by the four scaling parameters introduced above. For this, we use the concentrations measured 35 cm above the MWL, i.e., the lowest height of our aerosol samplers, assumed the most representative of the generation flux and the least affected by sizedependent vertical dispersion effects similar to Wu (1993) and Andreas (1998). The scaling relationships are presented for droplet radii of 7.5 μ m (Fig. 7) and ⁵⁴⁸ 25 μ m (Fig. 8), which are considered representative of the behaviour of the ⁵⁴⁹ droplets in the 7-20 μ m and the 20-35 μ m size range, respectively. In this man-⁵⁵⁰ ner, we provide separate scaling for the sea spray predominantly produced by ⁵⁵¹ bubble bursting (7-20 μ m) and surface-tearing (20-35 μ m) mechanisms.

Figures 7a and 8a report the scaling with wave age. The presented data 552 correspond to the wind-wave (blue dots), long wave (pink dots), intermediate 553 wave (red dots) and short wave (green dots) forcing at 16, 18 and 20 m s⁻¹ U_{10} 554 wind speeds. Data of the same type of forcing are fitted to a linear function, 555 denoted by a dashed line of the same colour. The black solid line represents a 556 linear fit to all 12 datapoints, and the R^2 value of the fit is given in the graphs 557 $(R^2 = 0.13$ for scaling with wave age for particles of 7.5 μ m). Although the 558 wave age seems to correctly scale concentrations for individual wave forcings, 559 no clear relationship is found between the measured concentrations and wave 560 age when all data is included. Therefore, we conclude that wave age is not 561 well suited for the scaling of sea spray generation for both young wind-forced 562 waves, and older swell-type waves. 563

Nevertheless, it is interesting to further discuss Figs. 7a and 8a. The overall 564 decrease in near-surface concentrations for increasing wave age (Figs. 7a and 565 8a) corroborates observations made in the field, as less whitecap is produced 566 by older swell-type waves or wind waves modulated by older waves in contrast 567 with wind waves alone (Schwendeman and Thomson, 2015; Brumer et al., 568 2017). Both figures show that relatively high sea spray concentrations are 569 found for the intermediate and short forcings, with corresponding wave age 570 values of approximately 1.7. This can be expected considering the high values 571 of W(%) and $\langle S^2 \rangle$ for these types of forcing (cf. Table 1). High droplet 572 concentrations associated with young, steep and strongly breaking waves is 573 typical of fetch-limited wave fields (Lafon et al., 2007). Specifically, for the 574

⁵⁷⁵ larger 25 μ m particles (cf. Fig. 8a) such a peak can be related to droplet ⁵⁷⁶ ejection microphysics as younger steeper waves induce airflow separation (Reul ⁵⁷⁷ et al., 2008), thought to play an important role in droplet ejection from the ⁵⁷⁸ wave crests (Mueller and Veron, 2009; Veron et al., 2012; Richter et al., 2019).



Fig. 7 Scaling of dN/dr with (a) wave age, (b) R_B , (c) $< S^2 >$ and (d) $P_S = \frac{u_*^3}{\nu_{ag}} < S^2 >$ for particles of radius 7.5 μ m, 35 cm above MWL. Individual types of wave forcing are represented in color, with U_{10} wind speeds ranging from 16 to 20 m s⁻¹. Solid black lines in all panels represent linear fits to all 12 datapoints.

⁵⁷⁹ We now turn our attention to Figs. 7b and 8b, which present the windsea ⁵⁸⁰ Reynolds number R_B as a scaling parameter for the sea spray concentration. ⁵⁸¹ The Reynolds number has proven to be strongly related to whitecap coverage ⁵⁸² and wave breaking (cf. Sect. 3.2) as well as sea spray concentrations for wind ⁵⁸³ waves especially (Iida et al., 1992; Toba et al., 2006; Troitskaya et al., 2018). ⁵⁸⁴ This seems confirmed by the overall (solid black line) trend line in Figures

7b and 8b, which is relatively close to the data corresponding to wind waves. 585 The data show less spread than for scaling with wave age, and most types 586 of forcing follow the overall trend, despite systematic differences in droplet 587 concentrations. The overall fit quality for the 7.5 μ m particles amounts to R^2 588 = 0.49 and similar values were noted for other radii in the 7-20 μ m range. 589 The windsea Reynolds number R_B does not perform as well over the 20-590 35 μ m radius range, as demonstrated by $R^2 = 0.31$ for the 25 μ m particles 591 (Fig. 8b). The better performance for smaller radii can find explanation in 592 the information contained in R_B about the flow velocity and more specifically 593 the turbulence intensity at the wind-wave boundary layer. We expect this to 594 be key for the smaller droplets that are more subject to turbulent diffusion 595 and less affected by gravitational settling than the larger spume droplets (e.g. 596 Andreas et al. (2010)). 597

The scaling of spray concentrations by the wave slope variance $\langle S^2 \rangle$ 598 is presented in Figs. 7c and 8c. The most striking feature of these figures 599 is the bahaviour for the intermediate wave forcing, which yields decreasing 600 aerosol concentrations with $\langle S^2 \rangle$, whereas the other types of forcing all 601 yield increasing concentrations. This behaviour can be traced back to the ear-602 lier observation (Sect. 3.1) that the intermediate forcing yields a decrease in 603 significant wave height with increasing $\langle S^2 \rangle$ (and a less clear increase of 604 W(%), which was attributed to (exceptionally) efficient wave energy dissipa-605 tion that for the other three types of forcing. This contrasting behaviour for 606 the intermediate forcing causes the overall fit quality for smaller particles to 607 be less than when scaling with R_B (R^2 of 0.34 versus 0.49). Over the 20-35 μ m 608 range however, the wave slope variance offers the best scaling performance for 609 all four scaling parameters ($R^2 = 0.55$). The wave slope variance thus appears 610

⁶¹¹ well adapted for the scaling of near-surface spume droplet concentrations (Fig.

612 8c).



Fig. 8 Scaling of dN/dr with (a) wave age, (b) R_B , (c) $\langle S^2 \rangle$ and (d) $P_S = \frac{u_*^3}{\nu_a g} \langle S^2 \rangle$ for particles of radius 25 μ m, 35 cm above MWL. Individual wave forcings are denoted by colours, for U_{10} wind speeds ranging from 16 to 20 m s⁻¹. Solid black lines in all panels represent linear fits to all 12 datapoints.

Finally, we scale near-surface concentrations as a function of the combina-613 tion of non-dimensional numbers $\frac{u_*^3}{\nu_{ag}} < S^2 >$. Results show that the combined 614 number P_S scales the particle concentrations better than either the wave age 615 or the windsea Reynolds number. In comparison with the wave slope variance 616 the combined number performance is better over the 7-20 $\mu{\rm m}$ range $(R^2=0.60$ 617 versus $R^2 = 0.34$ for $r = 7.5 \ \mu m$), but about equal for particles greater than 618 20 μ m ($R^2 = 0.5$ versus $R^2 = 0.55$ for $r = 25 \mu$ m). However, the combined 619 number results in similar trends for all four types of wave forcing, including 620

the intermediate forcing (compare panels c and d). This suggests that the combined number is capable of scaling sea spray generation for a wider range of environmental conditions than $\langle S^2 \rangle$ alone. We therefore conclude that the combined number is well suited for the simultaneous scaling of breaking wave (bubble bursting) and surface tearing mechanisms.

626 4.4 Combined scaling parameters

Our fourth scaling parameter is similar to the non-dimensional numbers sug-627 gested by Brumer et al. (2017) and Lenain and Melville (2017). The latter 628 authors combine the wave steepness, the wave age and a Reynolds number 629 depending on the significant wave height $H_s (R_H = \frac{H_s u_*}{\nu})$. A similar number 630 was also used by Brumer et al. (2017) for the scaling of whitecap coverage. 631 Preliminary laboratory studies on the scaling of sea spray concentrations in 632 the 7-35 μ m radius range by the number proposed by Lenain and Melville 633 (2017) suggest that the scaling does not significantly change when substitut-634 ing R_H with R_B . However, significantly better scaling is achieved when the 635 wave steepness $(H/2\lambda)$ is replaced with $\langle S^2 \rangle$. 636

As mentioned in the introduction, u_*^3 has proven to be a worthy candidate 637 to scale wave energy dissipation and input from the wind field necessary for 638 bubble and droplet production (Newell and Zakharov, 1992; Zhao and Toba, 639 2001; Zhao et al., 2006; Andreas, 1998, 2002; Fairall et al., 2009). Though not 640 detailed in the present scaling analysis, a preliminary study allowed to evaluate 641 the scaling performance of u_*^3 for near-surface concentrations. Results reveal 642 similar performance to the combined number with good scaling results over the 643 7-20 μ m range ($R^2 = 0.56$ for $r = 7.5 \mu$ m) with less satisfactory performance 644 for larger droplets ($R^2 = 0.23$ for $r = 25 \ \mu m$). Associating scaling performances 645

of u_*^3 (best for $r < 20 \ \mu m$) with $\langle S^2 \rangle$ (best for $r > 20 \ \mu m$) in the combined number (Eq. 5) allows good scaling of sea spray aerosol generation over the 7-35 μm range, suggesting that the combination of both allows to scale production in a wider range of conditions than $\langle S^2 \rangle$ alone.

⁶⁵⁰ 4.5 The laboratory generation flux

In this section, we will consider a suitable scaling parameter for the spray generation flux (dF/dr). We will derive this flux from the sea spray concentration profiles measured in the laboratory (cf. Fig. 5), at each resolved particle size. We only use the data obtained for the higher wind speeds (16, 18 and 20 m s⁻¹), but we include all four types of wave forcing. As a first step we approach the vertical concentration profiles with a function depending on the natural logarithm of measurement height (cf. Sect. 4.1 and Fig. 5):

$$N^r(z) = N^r_* ln(z) + C^r \tag{6}$$

where radius-dependent the aerosol concentration at the surface N_*^r (m⁻³) is determined by extending the measured aerosol concentration profiles to MWL. *r* denotes the dependence on the droplet radius. The sea spray flux dF/dr (m⁻² s⁻¹) is subsequently obtained by multiplication with the friction velocity u_* :

$$\frac{dF}{dr} = N_*^r u_* \tag{7}$$

We evaluate N_*^r for each radius (bin) greater than 7 μ m measured by our aerosol probes. This method is commonly used for the estimation of the sea spray flux in the field (Petelski et al., 2014), as well as for numerical LES (Large Eddy Simulation) data (Richter et al., 2019). However, the use of a logarithmic ⁶⁶⁶ function to describe the concentration gradient is debated, and other authors
⁶⁶⁷ have prefered a power law (e.g., Fairall et al. (2009); Ortiz-Suslow et al. (2016)).
⁶⁶⁸ Rather than entering this debate, we abide by the adequate fit of logarithmic
⁶⁶⁹ functions to our data (cf. Fig. 5).

As discussed in the previous section, both the wave slope variance and 670 the combined number are good candidates to scale droplet generation. The 671 combined number is found suitable over the entire study radius range, and 672 the wave slope variance for spume droplets. Thus, Figure 9 shows the size-673 dependent sea spray generation flux dF/dr (evaluated using Eq. 7) as function 674 of both the combined number (panel (a)) and the wave slope variance (panel 675 (b), for various representative droplet radii between 8.5 and 30 μ m. Individual 676 data for a specific radius was fitted to a power law presented as lines in Fig. 677 9. As expected, the figure demonstrates that the combined number and the 678 wave slope variance are also good scaling parameters for the generation flux. 679 In accordance with the positive slopes in Figs. 7 and 8 (panels c and d), 680 increasing values of combined number or wave slope variance lead to a stronger 681 flux. Although it is difficult to conclude visually from Fig. 9, a comparison of 682 panels a and b reveals the better scaling performance of the combined number 683 for smaller radii, as reflected in the quality of the fit for 8.5 particles μ m. 684 Finally, and interesting feature in both Figs. 9a and 9b is the increase in the 685 curve slopes for increasing radius as function of the scaling parameters. The 686 lower slopes are found for the larger droplets. These slopes, seem to converge 687 towards a maximum slope in the jet droplet range as the curves become almost 688 parallel for $r < 15 \ \mu m$. This suggests uneven radius-dependent flux strength 689 variations over the sea spray spectrum according to the forcing. 690



Fig. 9 The laboratory dF/dr sea spray flux as a function of (a) the combined number $\frac{u*^3}{\nu_a g} < S^2 >$ and (b) the wave slope variance $< S^2 >$. Lines denote power law fits to data for individual radii.

⁶⁹¹ 4.6 Comparison with other studies

This section presents a comparison of our generation flux to others reported 692 in the literature. Since most existing fluxes rely on data acquired in the field, 693 we must ascertain that our laboratory data can be compared to the field. 694 Comparing air-sea interaction processes and resulting sea spray generation in 695 laboratory conditions to the field is not a straightforward task, due to the 696 greater complexity of the natural environment. It is important that physical 697 mechanisms at play in the laboratory, as well as the resulting sea spray gen-698 eration fluxes, be similar to those observed in the field. The former question 699 has already been discussed in this paper; the wind flow (Sect. 2.4), the wave 700 field (Sect. 3.1), and the whitecap coverage (Sect. 3.2) were all found to fol-701 low the same physics as in the field. As for the sea spray concentrations, Sect. 702 4.1 demonstrated the expected behaviour with increasing concentrations for in-703 creasing wind speed, a dependence on wave state, as well as a near-logarithmic 704

⁷⁰⁵ concentration profile later used to calculate the laboratory generation fluxes⁷⁰⁶ (Eqs. 6 and 7).

The above reasoning leads us to compare our laboratory sea spray gen-707 eration flux to four (field and laboratory) flux formulations published in the 708 literature. For this comparison we have evaluated our generation flux for the 709 laboratory pure wind forcing for 18 probe size bins over the 5-30 μ m radius 710 range, with friction velocity $u_* = 1.05 \text{ m s}^{-1}$ and wind speed $U_{10} = 20 \text{ m s}^{-1}$ (cf. 711 Table 1). The flux is depicted in Fig. 10 as the black solid line. The triangles 712 denote the radii for which the dF/dr was evaluated, to which a polynomial 713 function is fitted to facilitate comparison with the other generation spectra. 714 Figure 10 also represents fluxes from the literature; Smith et al. (1993) denoted 715 by S93 and the grey solid line, Andreas (1998) denoted by A98 and the dotted 716 line, Laussac et al. (2018) denoted by L18 and the dashed line, and Fairall 717 et al. (2009) denoted by F09 and the grey dashed line. The latter flux was 718 obtained from laboratory data, the other three from field data. The Andreas 719 (1998) and Smith et al. (1993) flux models solely depend on wind speed U_{10} 720 and are evaluated here for $U_{10} = 20 \text{ m s}^{-1}$. The F09 flux is estimated for $u_* =$ 721 1.35 m s⁻¹, and is only valid for $r \ge 24 \ \mu$ m. Finally, L18 flux strength depends 722 on the whitecap coverage, in turn defined in terms of the wave age, and has a 723 $0.5-20 \ \mu m$ radius validity range. The closest match with laboratory conditions 724 (wave age equal to 1.25) was obtained by estimating the L18 flux for a wave 725 age value of 3.9 using a fetch model adapted to the north-west Mediterranean 726 (Lafon et al., 2004), corresponding with a MIRAMER campaign sample point 727 located at 12 km fetch (Demoisson et al., 2013; Laussac et al., 2018) used to 728 parameterise the L18 SSGF. 729



Fig. 10 Vertical sea spray concentration fluxes at $U_{10} = 20 \text{ m s}^{-1}$.

Figure 10 shows that the various flux estimates have a spread of an order 730 of magnitude. While this may seem significant, the spread is quite typical as 731 evidenced by reviews of the various source functions reported over the years 732 (Andreas, 1998; Lewis et al., 2004; Veron, 2015). Our flux function has the same 733 strength as S93, A98 and L18 for particles of 5 μ m, but suggests a stronger 734 flux than these other functions as radius increases. Specifically, our flux curve 735 includes a shoulder (or peak) around 10-15 μ m, also seen in S93, which we 736 attribute to a peak in jet droplet production. A similar shoulder is observed 737 in the aerosol size distributions measured at 55 cm height above the surface 738 (cf. Fig. 4). Moving forward to radii in excess of 15 μ m, the typical domain 739 of spume droplets, the strength of L18 and S93 generation functions decrease 740 rapidly. In both cases, this decrease was attributed to an underestimation of 741

spume droplet production, for L18 because the experiment was hampered by 742 the near-absence of high wind speed events, and because for L18 and S93 the 743 height of the measurement towers prevented efficient dispersion of the spume 744 droplet location. In each case this can result in poor count statistics, and the 745 larger droplet concentrations are often discarded as done for $r > 35 \ \mu m$ in 746 the present study. Examples of efforts to compensate such effects include the 747 reformulation of S93 in A98, where the generation flux was corrected over the 748 spume droplet range (Andreas, 1998). For the larger radii (r > 25 μ m), our flux 749 function yields equal strength as F09. Because these largest particles reflect 750 the limits of our PMS probes it is difficult to conclude, but both our flux curve 751 and F09 seem to indicate that the decrease in strength becomes less strong 752 with radius. This may point to the presence of another shoulder around 30 753 μ m, reflecting a peak in spume droplet generation. 754

⁷⁵⁵ 5 Formulation of the new sea spray generation function

The previous sections demonstrated that the laboratory generation flux de-756 pends on both wind and wave characteristics, with different responses for 757 individual radii. The dependence on radius is traditionally accounted for by 758 parameterising the SSGF with one or more modes centered around modal radii 759 (Monahan et al., 1986; Demoisson et al., 2013; Ovadnevaite et al., 2014; Laus-760 sac et al., 2018). These modes can be represented with normal, log-normal, 761 or other distributions that are commonly used to reproduce measured aerosol 762 distribution characteristics. Modes are often associated with specific aerosol 763 processes, such as the generation of jet or spume droplets. We adopt this 764 methodology by introducing two modes at 7 and 25 μ m radius, which we 765 consider representative for jet and spume droplets, respectively. The choice 766

of these centre radii was inspired by the shapes of the flux and concentration 767 curves shown in Figs. 4 and 10, respectively. As mentioned in Sect. 2.5, we have 768 excluded droplets with radii less than 7 μ m radius for our analysis, but these 769 droplets are evidently present in the tunnel (Fig. 4). On the basis of the shape 770 of the aerosol size distribution shown in Fig. 4, we add a third mode centered 771 around 2.5 μ m. Taking 3 μ m as the lower limit, the flux strength of the L18 772 SSGF is used over 3-7 μ m. A smooth transition between the field-determined 773 L18 and the laboratory data is attained by seeking a best fit between L18 flux 774 distributions over the 3-7 μ m range, and the laboratory flux distributions. The 775 7 μ m radius marks the transition between both fluxes (cf. Fig. 11). To achieve 776 this combination of flux functions, the whitecap coverage used in L18 (origi-777 nally calculated from the wave age) (Laussac et al., 2018) is recalculated here 778 as a function of present study scaling parameters (cf. Sect. 4.2). In the follow-779 ing, the L18 W(%) is estimated from $\langle S^2 \rangle$ using Eq. 4. Section 4.3 revealed 780 that the flux can be successfully scaled by a combined number P_S , but that the 781 $< S^2 > {\rm also}$ yields acceptable results, especially for larger particles. Therefore, 782 we formulate two SSGFs in terms of three normally distributed modes, valid 783 for droplets between 3-35 μ m radius and wind speeds U_{10} ranging from 12-20 784 m s⁻¹: 785

$$\frac{dF_X}{dr_{80}} = \sum_{i=1}^n \frac{F_i(X)\tau^{-1}}{\sigma_i\sqrt{2\pi}} exp(-\frac{1}{2}(\frac{r_{80}-\mu_i}{\sigma_i})^2)$$
(8)

where X is the scaling parameter (P_S or $\langle S^2 \rangle$), r_{80} is the particle radius at RH = 80%, $\frac{dF_X}{dr_{80}}$ is the size dependent SSGF determined from environmental parameters contained in $F_i(X)$, and τ is the whitecap decay rate. μ_i and σ_i are the mean radius and standard deviation of each of the three modes. The SS-GFs can be given in terms of r_{80} , because the underlying laboratory data was obtained for 80% humidity (cf. the discussion in Sect. 2.5). In formulating the SSGFs, we found best results were obtained using normal modes, whereas other

authors have preferred lognormal modes (e.g. Ovadnevaite et al. (2014)). Pos-793 sibly, this signals that normal modes are more suitable for the larger droplets 794 studied here. Numerical values for Eq. 8 are specified in Table 2. In addition, 795 the whitecap decay rate was given a value of 3.53 (Laussac et al., 2018). De-796 spite a focus on the 16-20 m s⁻¹ range in Sect. 4, we are confident that the 797 SSGFs are valid over the 12-20 m s⁻¹ range as a result of the strong relation-798 ship between numbers $\langle S^2 \rangle$ and P_S and the physical mechanisms known to 799 drive production (cf. sects. 2.4 and 3.2) for these wind speeds. 800

Table 2 shows that flux amplitudes are expressed as power laws of $\langle S^2 \rangle$ and P_S , as suggested with the apparent power law behaviour between scaling parameters and fluxes presented in Fig. 9.

i	σ_i	μ_i	$F_i(\frac{u*^3}{\nu_a g} < S^2 >)$	$F_i()$
1	2.1	2.5	$4.37 \times 10^2 (\frac{u*^3}{\nu_a g} < S^2 >)^{0.92}$	$4.94 \times 10^7 (\langle S^2 \rangle)^{2.45}$
2	7	7	$6.84 \times 10^1 (\frac{u*^3}{\nu_a g} < S^2 >)^{1.41}$	$7.88 \times 10^7 (< S^2 >)^{2.3}$
3	12	25	$4.75 \times 10^1 (\frac{u*^3}{\nu_a g} < S^2 >)^{1.11}$	$1.3 \times 10^7 (< S^2 >)^{2.39}$

Table 2Parameters for the two SSGFs.

The two new SSGFs are presented in Figure 11 as two series of solid lines, 804 where panels a and b denote results for the SSGF in terms of the combined 805 number P_S and $\langle S^{\rangle}$ respectively. These lines are colour-coded according to 806 the values of the scaling parameters; the colour scale is indicated on the right 807 of the individual panels. The range of values was chosen to correspond with 808 the laboratory configurations for all types of wind speeds between 16 and 20 m 809 s⁻¹. The experimental flux data obtained in these configurations is visualised 810 by the color-coded plus signs in Fig. 11. Finally, Figure 11 also presents the 811 flux spectra prescribed by the L18 SSGF (Laussac et al., 2018) over the 3-812 7 μ m range, which, as mentioned above, was modified so that the whitecap 813 coverage W(%) scaling parameter (originally calculated from the wave age), 814

was recalculated to depend on either P_S or $\langle S^2 \rangle$. The recalculated L18 flux spectra are represented by the color-coded dashed lines.



Fig. 11 The altered L18 SSGF (dashed lines) and the (a) combined number P_S and (b) wave slope variance $\langle S^2 \rangle$ SSGFs. Line colors depend on respective non-dimensional (a) P_S and (b) $\langle S^2 \rangle$ values.

Figure 11 demonstrates that the two SSGFs reproduce the experimental flux data obtained in the tunnel quite well, although differences of up to a factor 2 remain. In view of the already noted significant spread in individual flux functions reported in the literature (Tsyro et al., 2011; Chen et al., 2016; Neumann et al., 2016), we consider this performance adequate. The figure

also demonstrates that the two modes at 7 and 25 μ m adequately reproduce 822 the shape of the tunnel spectra, and this better than flux functions with less 823 modes in the large particle size domain (e.g., S93 and L18). Finally, Fig. 11 824 also shows that both SSGFs connect reasonably well to L18. While this was 825 expected with a 2.5 μ m mode inspired by L18 flux strengths, this result offers 826 a perpective for a future coupling between the new SSGFs and L18, thereby 827 extending a universal function to the 0.1-35 μ m range. These results also offer 828 a perspective for future improvements on the combination of laboratory and 829 field sea spray measurements. 830

831 6 Discussion and conclusion

832 6.1 Generation mechanisms

The aim of this study is to investigate the sea spray generation processes for 833 different wind and wave combinations. We performed our studies in a wave-834 wind interaction laboratory and thus, our first task was to demonstrate that 835 important generation mechanisms such as wave breaking (cf. Sect. 3.2) and 836 airflow characteristics (cf. Sect. 2.4) are similar in the laboratory and in the 837 field. Sea spray concentrations over the 7-35 μ m radius range are found to 838 depend on both wind speed and the sea state, and are found to decrease near-839 logarithmically for increasing distance from the water surface. The concentra-840 tion spectra (Fig. 4) exhibit peaks at approximately 2.5 and 7 μ m similar to 841 observations in the field (Laussac et al., 2018), attributed to regimes of film 842 and and jet droplet generation predominance, respectively. A third peak was 843 identified from the volume concentration spectra (Fig. 6) and corresponds to 844 the spume droplet size range. This peak was absent for wind speeds under 12 m 845

s⁻¹ (Sect. 4.1), in accordance with the threshold for spume droplet production
(Monahan et al., 1986; Andreas et al., 2010). The larger droplet concentrations
are found in conditions with high values for whitecap coverage and wave slope
variance. These conditions correspond to intermediate and short wave forcing
in the laboratory (cf. Table 1). In contrast, long wave forcing or forcing by
wind alone result in lower concentrations.

$_{852}$ 6.2 Scaling sea spray generation with $\langle S^2 \rangle$

The sea spray generation flux is calculated assuming logarithmic concentration 853 profiles (Sect. 4.5), motivated by the near-logarithmic profiles obtained in the 854 laboratory (Fig. 5). The sea spray generation is scaled against four parameters 855 that reflect the wind-wave conditions: wave age, windsea Reynolds number R_B , 856 wave slope variance $\langle S^2 \rangle$, and a combined number $\frac{u^{*^3}}{\nu_{\alpha g}} \langle S^2 \rangle$, denoted 857 P_S , describing the wave slope variance-modulated wind energy input to the 858 waves. Whilst the wave age is a useful heuristic tool to estimate wave-wind 859 equilibria, our results indicate that it does not allow satisfactory scaling of 860 sea spray generation for different wind and wave combinations (cf. Figs. 7 and 861 8). The windsea Reynolds number R_B , also combining wind and peak wave 862 characteristics, provides good results for smaller droplets (7-20 μ m range), 863 comparable to the performance for $\langle S^2 \rangle$. However, $\langle S^2 \rangle$ significantly 864 outperforms R_B for spume droplets with radii greater than 20 μ m (cf. Fig. 8). 865 This difference may be expected because R_B only includes information about 866 peak wave statistics, whereas $\langle S^2 \rangle$ is related to turbulence strength at the 867 air-sea interface and wave breaking phenomena on a range of spatial scales. 868 This is in agreement with an increasing number of microphysical studies that 869 relate wave slope to turbulent events such as airflow separation and wind shear, 870

which are thought to drive the surface tearing of spume droplets at the wave
crests (Banner and Melville, 1976; Kawai, 1981; Reul et al., 2008; Mueller and
Veron, 2014; Buckley and Veron, 2019).

Of the four tested scaling parameters the combined number P_S gives the 874 best overall performance: it is particularly well suited for the scaling of sea 875 spray generation for radii in the 7-20 μ m range, where bubble bursting gen-876 eration dominates, but the larger spume droplets are also well scaled. The 877 spume droplet scaling performance reflects the presence of $\langle S^2 \rangle$, and the 878 scaling performance for smaller droplets may be attributed to u_*^3 as a result 879 of its well documented relationship with wave energy dissipation. The con-880 cept of combined scaling parameters has also been explored by other authors 881 (Brumer et al., 2017; Lenain and Melville, 2017) (cf. Sect. 4.4). A comparative 882 study (Sect. 4.3) shows that minor differences in the definition of the com-883 bined number (e.g. by using a Reynolds number defined in terms of significant 884 wave height) do not impact on the performance, in contrast to the significant 885 difference obtained when replacing wave steepness with the multiscale wave 886 slope variance. 887

From a practical point of view, it is interesting to compare scaling perfor-888 mance to the difficulty to measure the scaling parameters. Both wave age and 889 the windsea Reynolds number R_B require a wind parameter and relatively 890 common wave parameters. The wave age does not scale the flux properly for 891 the range of tested forcings, and R_B scaling performances are mainly limited 892 to the smaller jet droplet particles. The measurement difficulty increases when 893 considering the multiscale information (wave spectrum) required for $\langle S^2 \rangle$, 894 and the combined number P_S adds further complexity by requiring the wind 895 friction velocity u_* . The use of approximate equations to estimate $\langle S^2 \rangle$ from 896

more readily-accessible parameters (e.g. Eqs. 3 and 4) may thus be considered, albeit with loss of scaling performance.

$_{899}$ 6.3 < S^2 > and traditional scaling parameters

As mentioned in the previous section, it may be difficult to measure $\langle S^2 \rangle$ 900 in the field. The use of the approximate equations to infer $\langle S^2 \rangle$ from more 901 accessible parameters such as wind speed U_{10} (Eq. 3), or whitecap coverage 902 W(%) (Eq. 4) may then be considered, as the wave slope variance $\langle S^2 \rangle$ 903 has often been considered proportional to both the wind speed at U_{10} and the 904 friction velocity u_* (Cox and Munk, 1956; Lenain et al., 2019). In a similar 905 fashion, tt is important to note that many authors obtain W(%) from wind 906 speed Monahan and Muircheartaigh (1980). Though not explicitly presented 907 here, $\frac{u*^3}{\nu_a q} < S^2 >$ and $< S^2 >$ (and to a lesser extent R_B) outperform the 908 measured U_{10} , u_* and W(%) for the scaling of sea spray generation in the 909 tested laboratory configurations, especially for larger droplets. W(%) presents 910 R^2 values ranging between 0.2 and 0.45 over the 7-35 μ m range, with best 911 results over the jet droplet range. U_{10} and u_* scaling performances are lower 912 than for W(%) overall, except for the smaller radii of the jet droplet range 913 where U_{10} and u_* show good correlation with spea spray generation, with R^2 914 values reaching maxima of 0.49 and 0.54 (for $r = 7 \ \mu m$), respectively. These 915 better results over the jet droplet range are coherent with the performances 916 of the combined number P_S with the u_*^3 term. Furthermore, this shows that 917 $< S^2 >$ carries additional information (despite the good correlation between 918 $\langle S^2 \rangle$ and W(%) - cf. Eq. 4) about the wave field relative to these three 919 parameters, such as the presumed role of the wave slope in the modulation of 920 the air flow and surface tearing mechanisms, as discussed in Sect 4.1. 921

Unlike $\langle S^2 \rangle$, U_{10} and u_* are not found to be appropriate tools for the 922 upscaling and extrapolation of sea spray generation and whitecap coverage 923 from the laboratory to the field, similar to observations made by Toba et al. 924 (2006) when comparing tunnel and field data. Altough $\langle S^2 \rangle$ outperforms 925 U_{10} and u_* , there are conditions in which the wind parameters scale the aerosol 926 concentrations as successfully. This pertains to smaller droplets (r < 12.5 μ m) 927 and relatively low wind speeds of 8 and 12 m s⁻¹, and a wave field that is forced 928 by the wind. In these circumstances, sea spray consists almost exclusively of 929 the bubble-mediated jet droplets produced from breaking waves under condi-930 tions of strong wave-wind equilibrium. Further analysis of our laboratory data 931 reveals that the linear relation between U_{10} and $\langle S^2 \rangle$ presented by Cox and 932 Munk (1956) (Eq. 3) is best observed for the conditions corresponding to pure 933 wind forcing. This is coherent with the good scaling performance of U_{10} and u_* 934 under these conditions, as mentioned above. However, notable deviations from 935 this linear relationship are observed with other types of wave forcing, which we 936 attribute to the sensitivity of $\langle S^2 \rangle$ to wave-wind equilibria (quantified here 937 with wave age). The monochromatic properties of the longer wave conditions 938 that experience less wind forcing, resulting in low wave energy at the higher 939 frequencies of the wave spectrum, thereby affecting the value of $\langle S^2 \rangle$. In 940 this respect, a future laboratory study with more realistic wave fields such as 941 the JONSWAP spectra (Hasselmann et al., 1973) would be worthwhile. 942

943 6.4 Validation against field data

The sea spray generation fluxes measured in the laboratory are compared to other existing source functions obtained in the field and in laboratory conditions. Our data compare favourably with the SPANDEX laboratory data

reported by Fairall et al. (2009). Flux estimates differ typically by less than 947 an order of magnitude when compared to flux functions obtained in the field 948 (Smith et al., 1993; Andreas, 1998), which is in accordance with the typi-949 cal spread in the literature (Andreas, 1998; Veron, 2015). More substantial 950 differences are noted from the spume droplet domain, when we compare our 951 flux estimates to a function that does not accommodate these large particles 952 explicitly (Laussac et al., 2018). These results prove that the laboratory is a 953 good instrument for determining generation fluxes. This inspires us to continue 954 the tunnel experiments, since the tunnel is better suited for the study of sea 955 spray production for a wide range of wave fields and in high winds represen-956 tative of extreme events. Also, the tunnel facilitates the complex experiments 957 required to understand the generation processes at the microphysical scale, 958 such as airflow separation, and the effects of sea spray on heat, moisture and 959 momentum fluxes at the air-sea interface. Ideally, such experiments should be 960 performed with salt water, for easier comparison with field experiments, be-961 cause saltwater and freshwater lead to differences in the aerosol concentrations 962 and distributions (Fairall et al., 2009; Mehta et al., 2019). 963

6.5 Sea spray generation functions (SSGFs) derived from laboratory
 experiments

The laboratory experiments culminated in two sea spray generation functions (SSGFs) (cf. Fig. 11 and Table 2). These SSGFs describe the droplet generation spectrum as a sum of three normally distributed modes, and are validated for wind speeds ranging from 12-20 m s⁻¹ and droplet radii 3-35 μ m. The radius range spans the major part of the film and jet ranges, as well as an appreciable start of the spume droplet range. One SSGF solely dependent on the wave

slope variance, and to our knowledge is the first of its kind. Wave slope vari-972 ance measurements in the field are scarce, and for practical purposes it may 973 be necessary to estimate the wave slope variance from more readily available 974 variables such as wind speed (Eq. 3, Cox and Munk (1956)), or from mea-975 sured or modelled wave spectra (Elfouhaily et al., 1997). As shown in Section 976 6.3, such approximations may reduce the accuracy of the SSGF. The second 977 SSGF depends on a combined scaling parameter in terms of both $\langle S^2 \rangle$ 978 and u_*^3 . Though obtaining accurate measurements or predictions of u_*^3 may 979 be challenging in the field (and thus renders the use of the second SSGF even 980 more difficult than the one depending solely on $\langle S^2 \rangle$), this non-dimensional 981 number is undeniably the best scaling tool for the generation of film and jet 982 droplets, and also scales the larger spume droplets satisfactorily. In extrapolat-983 ing the P_S -dependent SSGF down to 12 m s⁻¹ the flux may be underestimated 984 at these lower wind speeds, following the suggestion by Andreas (1998) that 985 the rate of spume droplet generation increases with u_*^2 and not u_*^3 for winds 986 below 15 m s⁻¹. 987

988 6.6 Outlook

Recent improvements in the integration of higher order wave field properties 989 in numerical wave models (Cathelain, 2017) and the coupling of wave, atmo-990 spheric and circulation models (Pianezze et al., 2018) provide an impetus for 991 the study of sea spray generation processes. Present study results have shown 992 that the integration of the wave field is essential for the better scaling of the sea 993 spray generation. As we work towards universal SSGFs valid for a wide range 994 of (complex) environmental conditions, a further understanding is required 995 of the effect of multiscale (i.e. millimeter to meter scale) boundary processes 996

sea spray fluxes. This may include first and higher order statistics, such as 997 for the consideration of overlapping wave fields, the directional spreading of 998 wave spectra (Peureux et al., 2018) and wave-current interactions affecting 999 surface wave properties (Ardhuin et al., 2017). As the present study has high-1000 lighted the importance of the wave slope variance in modelling droplet fluxes, 1001 we signal an urgent need for a better understanding of small-scale sea surface 1002 characteristics (Jähne and Riemer, 1990). Unfortunately, field measurements 1003 of these characteristics have been relatively sparse (Munk, 2009), not in the 1004 least because the spatial resolution of airborne and satellite-based sensors is 1005 limited and the presence of whitecaps complicates the retrieval of slope vari-1006 ance estimates (Cox and Munk, 1956; Lenain et al., 2019). 1007

Finally, having demonstrated that the tunnel is a good proxy to the field in determining sea spray fluxes, we would now like to extend the comparison to the aerosol concentrations at some height above the water surface. However, this is not a simple task since the differences in dispersion characteristics, background concentrations and production footprints between the tunnel and the field need to be elucidated. Efforts to do so are underway, and will be reported elsewhere.

1015 Acknowledgements

A special thanks to engineer Rémi Chemin (University of Toulon) for his thoughts and contribution during the laboratory experiment. We are grateful for the sponsorship by the Agence Innovation Défense (AID-DGA) under contract 2018-60-0038 and the Region SUD contract 2018-06085. This work also benefitted from the MATRAC research effort sponsored by ANR-ASTRID under contract ANR-18-ASTR-0002.

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