



A LOFAR-uGMRT spectral index study of distant radio halos

G. Di Gennaro, R.J. van Weeren, R. Cassano, G. Brunetti, M. Brüggen, M. Hoeft, E. Oasinga, A. Botteon, V. Cuciti, F. de Gasperin, et al.

► To cite this version:

G. Di Gennaro, R.J. van Weeren, R. Cassano, G. Brunetti, M. Brüggen, et al.. A LOFAR-uGMRT spectral index study of distant radio halos. *Astronomy and Astrophysics - A&A*, 2021, 654, pp.A166. 10.1051/0004-6361/202141510 . hal-03339478

HAL Id: hal-03339478


<https://hal.science/hal-03339478>

Submitted on 17 Jun 2022

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

A LOFAR-uGMRT spectral index study of distant radio halos

G. Di Gennaro¹, R. J. van Weeren¹, R. Cassano², G. Brunetti², M. Brüggen³, M. Hoeft⁴, E. Oasinga¹, A. Botteon¹, V. Cuciti³, F. de Gasperin³, H. J. A. Röttgering¹, and C. Tasse^{5,6}

¹ Leiden Observatory, Leiden University, PO Box 9513, 2300 RA Leiden, The Netherlands
e-mail: digennaro@strw.leidenuniv.nl

² Istituto Nazionale di Astrofisica-Istituto di Radioastronomia, Bologna Via Gobetti 101, 40129 Bologna, Italy

³ Hamburger Sternwarte, Universität Hamburg, Gojenbergsweg 112, 21029 Hamburg, Germany

⁴ Thüringer Landessternwarte, Sternwarte 5, 07778 Tautenburg, Germany

⁵ GEPI and USN, Observatoire de Paris, CNRS, Université Paris Diderot, 5 place Jules Janssen, 92190 Meudon, France

⁶ Centre for Radio Astronomy Techniques and Technologies, Department of Physics and Electronics, Rhodes University, Grahamstown 6140, South Africa

Received 9 June 2021 / Accepted 3 August 2021

ABSTRACT

Context. Radio halos are megaparsec-scale diffuse radio sources mostly located at the centres of merging galaxy clusters. The common mechanism invoked to explain their origin is the re-acceleration of relativistic particles caused by large-scale turbulence.

Aims. Current re-acceleration models predict that a significant number of halos at high redshift should be characterised by very steep spectra ($\alpha < -1.5$) because of increasing inverse Compton energy losses. In this paper, we investigate the spectral index properties of a sample of nine clusters selected from the second *Planck* Sunyaev-Zel'dovich catalogue showing diffuse radio emission with the Low Frequency Array (LOFAR) in the 120–168 MHz band. This is the first time that radio halos discovered at low frequencies are followed up at higher frequencies.

Methods. We analysed upgraded Giant Metrewave Radio Telescope (uGMRT) observations in Bands 3 and 4, that is, 250–500 and 550–900 MHz respectively. These observations were combined with existing LOFAR data to obtain information on the spectral properties of the diffuse radio emission.

Results. We find diffuse radio emission in the uGMRT observations for five of the nine high- z radio halos previously discovered with LOFAR. For those, we measure spectral indices in the range of -1 to -1.4 . For the uGMRT non-detections, we estimated that the halos should have a spectral index steeper than -1.5 . We also confirm the presence of one candidate relic.

Conclusions. Despite the small number of clusters, we find evidence that about half of the massive and merging clusters at high redshift host radio halos with a very steep spectrum. This is in line with theoretical predictions, although larger statistical samples are necessary to test models.

Key words. radiation mechanisms: non-thermal – galaxies: clusters: general – galaxies: clusters: intracluster medium

1. Introduction

In the framework of the Λ CDM cosmological model, galaxy clusters form and grow via accretion of less massive systems (e.g., galaxy groups or small galaxy clusters, see [Press & Schechter 1974](#); [Springel et al. 2006](#)). These events release energy up to 10^{64} erg in the intracluster medium (ICM) in a few gigayears. A fraction of this energy is dissipated by shocks and turbulence, and is used in the amplification of magnetic fields and (re)acceleration of particles, producing diffuse radio emission in the form of radio halos and radio relics (see [Brunetti & Jones 2014](#); [van Weeren et al. 2019](#), for recent theoretical and observational reviews). Because of their intrinsic low surface brightness (~ 0.1 – $1 \mu\text{Jy arcsec}^{-2}$ at 1.4 GHz), halos and relics are difficult to detect. In addition, they are characterised by steep spectra (i.e. $\alpha < -1$, with $S_\nu \propto \nu^\alpha$), and are therefore better observed at low radio frequencies (i.e. below GHz).

Radio halos are cluster-size structures that generally follow the distribution of the thermal cluster emission (i.e. the ICM). Their currently favoured formation scenario involves the re-acceleration of electrons via turbulence induced by cluster merger events (e.g., [Brunetti et al. 2001](#);

[Petrosian 2001](#); [Brunetti & Lazarian 2007, 2016](#); [Donnert et al. 2013](#)). In support of this scenario, radio halos are preferentially detected in dynamically disturbed clusters (e.g., [Cassano et al. 2013](#); [Cuciti et al. 2021a](#)). An additional channel may arise from proton–proton collisions, which generate secondary electrons that then emit synchrotron radiation (e.g., hadronic models, [Blasi & Colafrancesco 1999](#); [Dolag & Enßlin 2000](#)). Although the non-detection of γ -ray emission from galaxy clusters rules out a dominant contribution from this channel (e.g., [Reimer et al. 2003](#); [Ackermann et al. 2010](#); [Prokhorov & Churazov 2014](#); [Brunetti et al. 2017](#); [Adam et al. 2021](#)), turbulent re-acceleration of secondary particles is still a viable model ([Brunetti & Lazarian 2011](#); [Pinzke et al. 2017](#); [Brunetti et al. 2017](#)).

Radio relics are elongated structures generally located in the cluster outskirts. It is widely believed that these are associated with propagating shock waves caused by mergers (e.g., [Rottgering et al. 1997](#); [Enßlin et al. 1998](#); [Giacintucci et al. 2008](#); [van Weeren et al. 2010](#); [Pearce et al. 2017](#); [Hoang et al. 2018](#); [Di Gennaro et al. 2018](#)). This is also supported by the detection of strongly polarised emission at the relic position (e.g., [van Weeren et al. 2010](#); [Di Gennaro et al. 2021a](#)), which

Table 1. Physical properties of the galaxy clusters.

Cluster name	z	RA _{J2000} [deg]	Dec _{J2000} [deg]	$M_{\text{SZ},500}$ [$10^{14} M_{\odot}$]	kpc''
PSZ2 G086.93+53.18	0.675	228.50446	+52.81074	5.4 ± 0.5	7.125
PSZ2 G089.39+69.36	0.680	208.43748	+43.48470	5.7 ± 0.7	7.148
PSZ2 G091.83+26.11	0.822	277.78430	+62.24770	7.4 ± 0.4	7.676
PSZ2 G099.86+58.45	0.616	213.6909	+54.78029	6.8 ± 0.5	6.845
PSZ2 G126.28+65.62	0.820	190.5975	+51.43944	5.0 ± 0.7	7.670
PSZ2 G141.77+14.19	0.830	70.27167	+68.22275	7.7 ± 0.9	7.700
PLCK G147.3–16.6	0.645	44.105898	+40.290140	6.3 ± 0.4	6.988
PSZ2 G147.88+53.24	0.600	164.37923	+57.99591	6.5 ± 0.6	6.762
PSZ2 G160.83+81.66	0.888	186.74267	+33.54682	$5.7^{+0.6}_{-0.7}$	7.865

Notes. The cluster masses, $M_{\text{SZ},500}$, are taken from the *Planck*-SZ catalogue (Planck Collaboration XXVII 2016).

suggests amplification and compression of magnetic fields. Nonetheless, the nature of the (re)acceleration mechanism is still unclear (e.g., Vazza & Brüggen 2014). Standard Fermi type-I acceleration of thermal ICM electrons (e.g., Drury 1983; Ensslin et al. 1998; Brunetti & Jones 2014) sometimes requires an unrealistic shock efficiency to justify the relic radio brightness –in the case where electrons are accelerated from the thermal pool– because of the low Mach number of the shocks ($M \lesssim 2$, e.g., Botteon et al. 2016, 2020; Hoang et al. 2017; Di Gennaro et al. 2019). Re-acceleration of pre-existing relativistic plasma at the shock has therefore been proposed (e.g., Markevitch et al. 2005; Bonafede et al. 2014; Kang et al. 2017; van Weeren et al. 2017). Examples that are considered to indicate ongoing re-acceleration are still limited to a few cases (e.g., van Weeren et al. 2017; Di Gennaro et al. 2018).

Most of the statistical studies of diffuse radio emission are limited to the local Universe (i.e. $z \sim 0.1$ – 0.4 ; e.g., Cassano et al. 2013; Kale et al. 2015; Cuciti et al. 2021b,a). A handful of clusters up to $z \sim 0.5$ hosting diffuse radio emission have recently been reported in Giovannini et al. (2020). All these observations were firstly carried out at GHz frequencies, and eventually followed up at lower frequencies (i.e. ~ 100 MHz) to investigate the spectral characteristic of the observed radio halos. This approach however misses a large fraction of (ultra-)steep spectrum halos, because radio halos with $\alpha < -1.5$ are hardly detected at GHz frequencies. At higher redshifts ($z \geq 0.6$), only a few exceptional clusters have been studied so far (e.g., ‘El Gordo’ at $z = 0.87$, Lindner et al. 2014, PLCK G147.3–16.6 at $z = 0.645$, van Weeren et al. 2014 and PSZ2 G099.86+58.45 at $z = 0.616$, Cassano et al. 2019). Recently, in Di Gennaro et al. (2021b), we presented a statistical study of a sample of distant ($z \geq 0.6$) galaxy clusters selected from the second *Planck* Sunyaev-Zel’dovich (SZ) catalogue (Planck Collaboration XXVII 2016) and observed with the LOFAR Two-Metre Sky Survey (LoTSS; Shimwell et al. 2017, 2019). We observed that 9 out of 19 clusters host diffuse radio emission. Available X-ray observations (Chandra and/or XMM-Newton; see Fig. 2 in Di Gennaro et al. 2021b) suggest that the radio halos are located in dynamically disturbed clusters. Assuming turbulent re-acceleration from the radio luminosities, we estimated magnetic field strengths similar to nearby ($z \sim 0.2$) systems in the same mass range. According to the turbulent re-acceleration scenario, a large fraction of distant radio halos should have steep integrated spectral indices ($\alpha < -1.5$) because of the strong synchrotron and inverse Compton (IC) losses. We followed up those clusters hosting diffuse radio emission

in Di Gennaro et al. (2021b) with the upgraded Giant Metre-wave Radio Telescope (uGMRT). This represents the first high-frequency follow up of high- z halos detected at low frequencies. The observed sample is listed in Table 1.

Throughout the paper, we assume a standard Λ CDM cosmology, with $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.3$ and $\Omega_\Lambda = 0.7$.

2. Observations and data reduction

2.1. LOFAR

We use the same dataset presented in Di Gennaro et al. (2021b). The sample was observed together with LoTSS (Shimwell et al. 2017, 2019), which consists of 8 hours of observation for each pointing (see Table 2). We performed standard LOFAR data reduction, which includes direction-independent and direction-dependent calibration and imaging of the full LOFAR field of view using prefactor (van Weeren et al. 2016; Williams et al. 2016; de Gasperin et al. 2019), killMS (Tasse 2014; Smirnov & Tasse 2015), and DDFacet (Tasse et al. 2018, 2021). Additionally, we performed extra phase and amplitude self-calibration loops using the products of the pipeline¹ and subtracting all of the sources outside of a region of $15' \times 15'$ surrounding the target in order to improve the quality of the calibration (van Weeren et al. 2021). Final imaging was done with WSClean v2.10 (Offringa et al. 2014; Offringa & Smirnov 2017) with the wideband deconvolution mode (channelsout=6). The images have a central frequency of 144 MHz. The systematic uncertainty due to residual amplitude errors is set to 15% (Shimwell et al. 2019).

2.2. uGMRT

The clusters presented in this work have been observed with the uGMRT in Band 3 (250–550 MHz) and/or Band 4 (550–900 MHz). The total length of the observation is 6 hours, except for PSZ2 G091.83+26.11 and PSZ2 G141.77+14.19 which have been observed for 5 hours (see Table 2). Data were recorded in 2048 frequency channels with an integration time of 4 s in full Stokes mode. We used 3C286, 3C147, and 3C48 as primary calibrators, depending on the target. To process the data, we ran the Source Peeling and Atmospheric Modeling (SPAM, Intema et al. 2009) on six sub-bands of 33.3 MHz bandwidth each for Band 3, and on four sub-bands of 50.0 MHz bandwidth each for Band 4. For each band, the sub-bands are then imaged together using

¹ <https://github.com/mhardcastle/ddf-pipeline>

Table 2. Radio observation details.

Cluster name	Telescope	Project/pointing	Observation date [dd-mm-yyyy]	Observation length ^(†) [h]	Frequency coverage [MHz]	Configuration
PSZ2 G086.93+53.18	LOFAR	P227+53 P231+53	19-02-2015 19-02-2015	8.33	120–168	HBA Dual Inner
	uGRMT	38_054	30-08-2020	6	550–900	Band 4
PSZ2 G089.39+69.36	LOFAR	P207+45 P209+42	07-05-2015 05-03-2015	8.33	120–168	HBA Dual Inner
	uGMRT	38_054	25-08-2020	6	250–500	Band 3
PSZ2 G091.83+26.11	LOFAR	P275+63 P280+60	22-08-2016 18-01-2019	8.33	120–168	HBA Dual Inner
	uGMRT	36_039	05-05-2019	5	250–500	Band 3
	uGRMT	36_039	29-05-2019	5	550–900	Band 4
PSZ2 G099.86+58.45	LOFAR	P209+55 P214+52 P214+55	30-04-2015 12-05-2015 12-05-2015	8.33	120–168	HBA Dual Inner
	uGRMT	38_054	30-08-2020	6	550–900	Band 4
PSZ21 G126.28+65.62	LOFAR	P29Hetdex19 P30Hetdex06 P33Hetdex08	26-06-2014 30-05-2014 19-06-2014	8.33	120–168	HBA Dual Inner
	uGRMT	38_054	10-07-2020	6	550–900	Band 4
PSZ2 G141.77+14.19	LOFAR	P068+69	08-09-2017	8.33	120–168	HBA Dual Inner
	uGRMT	36_039	07-05-2019	5	550–900	Band 4
PLCK G147.3–16.6	LOFAR	P044+39	29-11-2017	8.33	120–168	HBA Dual Inner
	uGRMT	38_054	20-06-2020	6	250–500	Band 3
	uGRMT	38_054	16-06-2020	6	550–900	Band 4
PSZ2 G147.88+53.24	LOFAR	P165+57 P166+60	11-05-2015 13-10-2017	8.33	120–168	HBA Dual Inner
	uGRMT	38_054	20-06-2020	6	550–900	Band 4
PSZ2 G160.83+81.66	LOFAR	P185+32 P185+35 P188+32 P188+35	11-12-2019 23-02-2017 18-08-2017 28-03-2019	8.33	120–168	HBA Dual Inner
	uGRMT	38_054	12-08-2020	6	550–900	Band 4

Notes. ^(†)The observation length includes also the time on the calibrators.

WSClean v2.10 at the common frequency of 400 and 650 MHz, for Band 3 and 4, respectively. The systematic uncertainties due to residual amplitude errors are set to 8% and 5% for the observations in Bands 3 and 4 respectively (Chandra et al. 2004).

2.3. Imaging and integrated flux densities

For all clusters, we produced the final deep images using WSClean v2.10, with `weighting='Briggs'` and `robust=-0.5`. For the LOFAR images, we applied an inner uv -cut of 80λ to remove the Galactic emission. The final noise levels were found in the ranges ~ 50 – $150 \mu\text{Jy beam}^{-1}$, ~ 20 – $60 \mu\text{Jy beam}^{-1}$, and ~ 7 – $12 \mu\text{Jy beam}^{-1}$ for the 144, 400, and 650 MHz full-resolution images, respectively (see Table 3). This means that the 650 MHz observations are about three times deeper than the LOFAR ones for detecting compact sources, that is, assuming a typical spectral index $\alpha = -0.8$. For steep-spectra sources, that is, $\alpha = -1.3$, the sensitivities of the two arrays are similar. The low-resolution images for both the LOFAR and uGMRT observations were produced by applying a Gaussian taper at different resolutions to downweight the visibilities from longer baselines. We display all the images in Figs. 1–9. Among the nine clusters presented in this work, five of them show extended diffuse radio emission in the uGMRT observations.

To obtain the flux densities of the radio halos, we produced source-subtracted images. We applied a uv -cut to the data to filter out emission associated with sources of linear sizes larger than 500 kpc at the cluster redshift, and to create a clean component model of the compact sources. Given the sizes of the halo, for the LOFAR image of PSZ2 G089.39+69.36 we employed an inner

uv -cut of 400 kpc. During this step, we employed multiscale deconvolution using scales of $[0, 4, 8, 16] \times \text{pixelscale}$ (with the pixel size of $1.5''$, $2''$ and $1''$ for the 144, 400 and 650 MHz images, respectively) to include and subtract the diffuse emission from the radio galaxies. For the automatic deconvolution, we used a mask threshold of $1\sigma_{\text{rms}}$ to subtract the faintest contaminating sources. Finally, we subtracted the compact source models from the visibilities, and tapered the uv -data with different Gaussian tapers (i.e. $6''$, $10''$ or $15''$). In case of an extended radio galaxy with a linear size ≥ 500 kpc, we cannot properly subtract the radio emission from the uv -data. This is the case for the candidate radio relic in PSZ2 G091.83+26.11 and for the radio galaxy northward of PLCK G147.3–16.6, which have been manually excluded from the radio halo region (Di Gennaro et al. 2021b).

We measure the radio halo flux densities for each cluster from same regions in the LOFAR and uGMRT images, encompassing the full extent of the diffuse radio emission (see Appendix A). Uncertainties on the halo flux densities are given by:

$$\Delta S_\nu = \sqrt{(fS_\nu)^2 + N_{\text{beam}}\sigma_{\text{rms}}^2 + \sigma_{\text{sub}}^2}, \quad (1)$$

where f are the systematic uncertainties due to residual amplitude errors, σ_{rms} is the map noise level, N_{beam} is the number of beams covering the halo region, and σ_{sub} is the uncertainty of the source subtraction in the uv plane (i.e. a few percent of the residual flux from compact sources; see, e.g., Cassano et al. 2013; van Weeren et al. 2021). The resulting flux densities are listed in Table 4.

Table 3. Imaging parameters and image properties of the cluster sample.

Cluster name	Central frequency [MHz]	Resolution ["×"]	uv min [λ]	uv -taper ["]	σ_{rms} [$\mu\text{Jy beam}^{-1}$]
PSZ2 G086.93+53.18	144	9.5×4.5	80	–	91.8
		26.0×26.0	80	15	239.4
	650	3.8×3.4	–	–	8.6
		26.0×26.0	–	15	45.5
PSZ2 G089.39+69.36	144	8.3×4.8	80	–	64.3
		29.0×29.0	80	15	138.2
	400	6.4×5.1	–	–	57.2
		29.0×29.0	–	15	416.0
PSZ2 G091.83+26.11	144	6.8×4.5	80	–	92.1
		14.0×14.0	160	6	188.4
	400	13.8×6.2	–	–	64.6
		14.0×14.0	160	–	94.6
	650	4.4×2.8	–	–	11.4
		14.0×14.0	160	6	38.9
PSZ2 G099.86+58.45	144	8.0×4.4	80	–	66.3
		18.0×18.0	180	10	153.2
	650	5.0×2.6	–	–	8.2
PSZ2 G126.28+65.62	144	18.0×18.0	180	10	33.7
		7.6×4.5	80	–	52.3
	650	25.0×25.0	80	15	117.6
		7.6×2.5	–	–	9.8
PSZ2 G141.77+14.19	144	25.0×25.0	–	15	39.9
		7.6×5.0	80	–	119.6
	650	17.0×17.0	150	10	171.0
		6.4×3.3	–	–	9.7
PLCK G147.3–16.6	144	17.0×17.0	150	10	21.3
		7.6×5.9	80	–	152.8
	400	17.0×17.0	150	10	315.6
		8.0×4.1	–	–	22.3
	650	17.0×17.0	150	10	58.1
PSZ2 G147.88+53.24	144	3.4×3.0	–	–	7.3
		17.0×17.0	150	10	25.5
	650	8.6×4.6	80	–	61.7
		14.0×14.0	100	6	123.4
PSZ2 G160.83+81.66	144	5.6×2.6	–	–	8.5
		14.0×14.0	100	6	19.5
	650	13.1×4.6	80	–	138.2
		21.0×21.0	80	15	221.3
	650	4.5×2.6	–	–	9.2
		21.0×21.0	–	15	22.7

2.4. Radio halo injection and upper limits

In those systems with no detection of diffuse emission in the uGMRT images, we derived upper limits injecting mock radio halos directly in the original visibilities (e.g., Venturi et al. 2007, 2008; Kale et al. 2015; Cuciti et al. 2021a). Following Bonafede et al. (2017), we modelled the radio halo brightness with a symmetric exponential profile, $I(r) = I_0 \exp(-r/r_e)$, and including power spectrum fluctuations of the type $P(\Lambda) \propto \Lambda^n$ (with Λ being the spatial scale of the fluctuations and $n = 11/3$; see also Govoni et al. 2005, 2006; Bonafede et al. 2009). In the exponential model, I_0 is the central brightness and r_e the e -folding radius which we assumed to be one-third of the halo radius, R_H ² (Murgia et al. 2009). We injected the mock halo in

a region close to the cluster³ that is free of compact sources in order to avoid the inclusion of possible halo residuals which would bias the upper limits to lower levels (Bonafede et al. 2017; Osinga et al. 2021; Cuciti et al. 2021a). We assumed different I_0 levels, starting from $\sigma_{\text{rms}} \sqrt{N_{\text{beam}}}$ and increasing this value until positive residuals were visible in the image. We define these positive residuals as an upper limit when the largest linear scale above the $2\sigma_{\text{rms}}$ level is about $2r_e$ (Cuciti et al. 2021a). We measured the flux density directly from the image, corresponding to ~ 80 – 90% of the injected flux. An example of the injection procedure is displayed in Fig. 10. All the upper limits on the flux densities are reported in Table 4.

² We define R_H as half of the largest linear size in the LOFAR image (see Table 4).

³ The original image without compact sources is displayed in Appendix A.

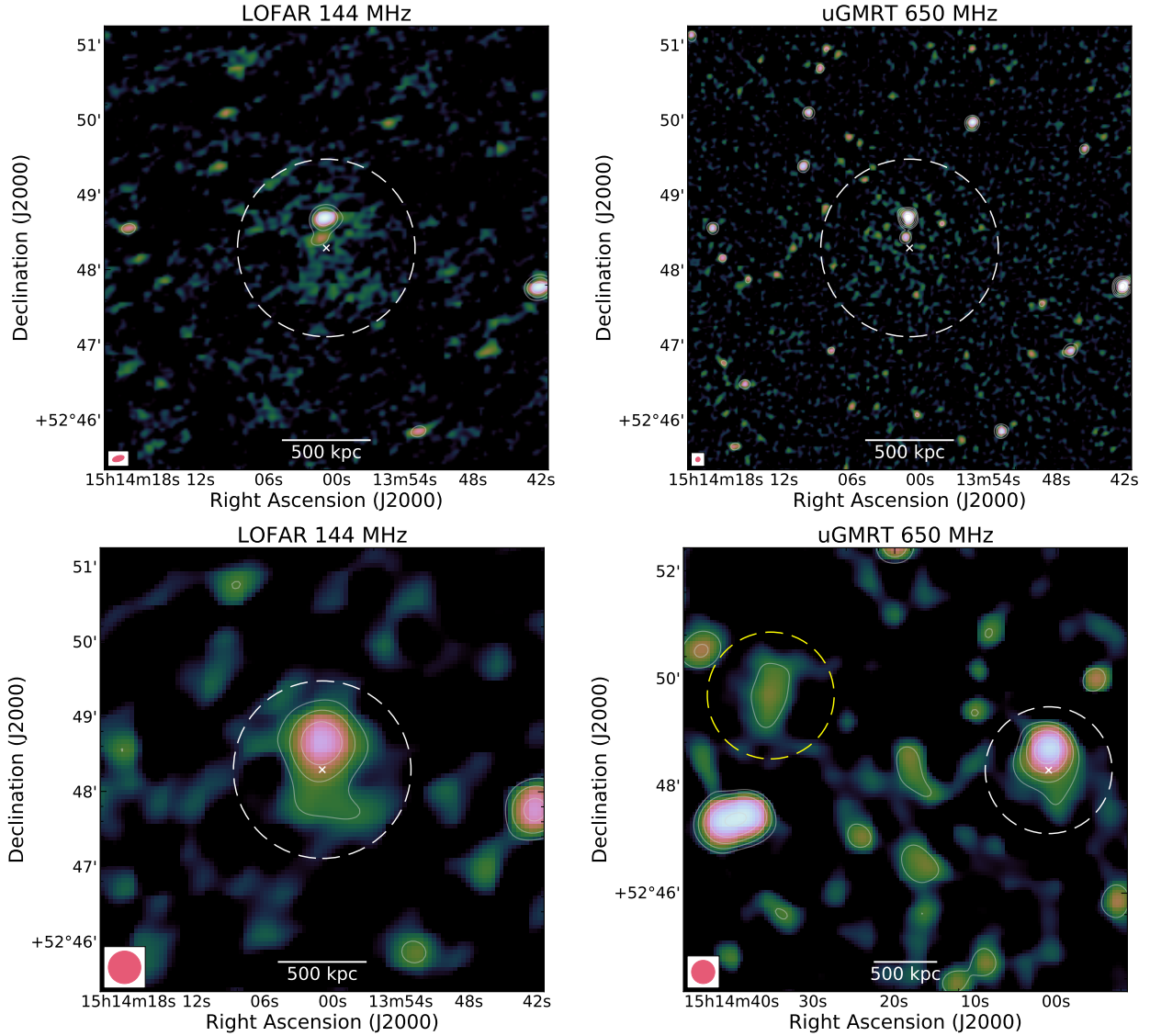


Fig. 1. PSZ2 G086.93+53.18. *Top and bottom rows:* full-resolution and 26'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (left) and 650 MHz (right). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the cross showing the cluster centre. The dashed yellow circle in the *bottom right panel* shows the position of the mock radio halo.

3. Results

3.1. Spectral index maps and integrated spectral indices

To produce the spectral index maps of those clusters with diffuse radio emission in both LOFAR and uGMRT observations, we made images with a common inner uv -cut to compensate for the different interferometer uv -coverage. To emphasise the presence of the radio halo, we also applied a Gaussian taper. The images were then convolved to the same resolution, and re-gridded to the same pixel grid (i.e. the LOFAR image). The effective final resolutions and the noise levels of each image are listed in Table 3. For the clusters with observations at three frequencies, we used the same procedure used in Di Gennaro et al. (2018), where a second-order polynomial fit was used in case of significant curvature (i.e. above the 2σ threshold, where σ is the uncertainty associated with the second-order term). In this case, the spectral index was calculated at 400 MHz, which is the median of the total band. We blanked all the pixels below the $2\sigma_{\text{rms}}$ thresh-

old for each frequency, with σ_{rms} being the noise level reported in Table 3. The spectral index uncertainty maps are obtained via 150 Monte Carlo simulations of the first- and second-order polynomial fit. We assumed the uncertainty of each flux to be given by the sum in quadrature of the noise map and the systematic flux uncertainties, that is $\Delta S_\nu = \sqrt{(fS_\nu)^2 + \sigma_{\text{rms}}^2}$. For the clusters with observations at only two frequencies, we calculate the spectral index analytically, with an uncertainty of:

$$\Delta\alpha = \frac{1}{\ln \frac{\nu_1}{\nu_2}} \sqrt{\left(\frac{\Delta S_1}{S_1}\right)^2 + \left(\frac{\Delta S_2}{S_2}\right)^2}. \quad (2)$$

3.2. Individual clusters

In this section we provide a brief description of each cluster, at all the observing frequencies. The results are summarised in Table 4.

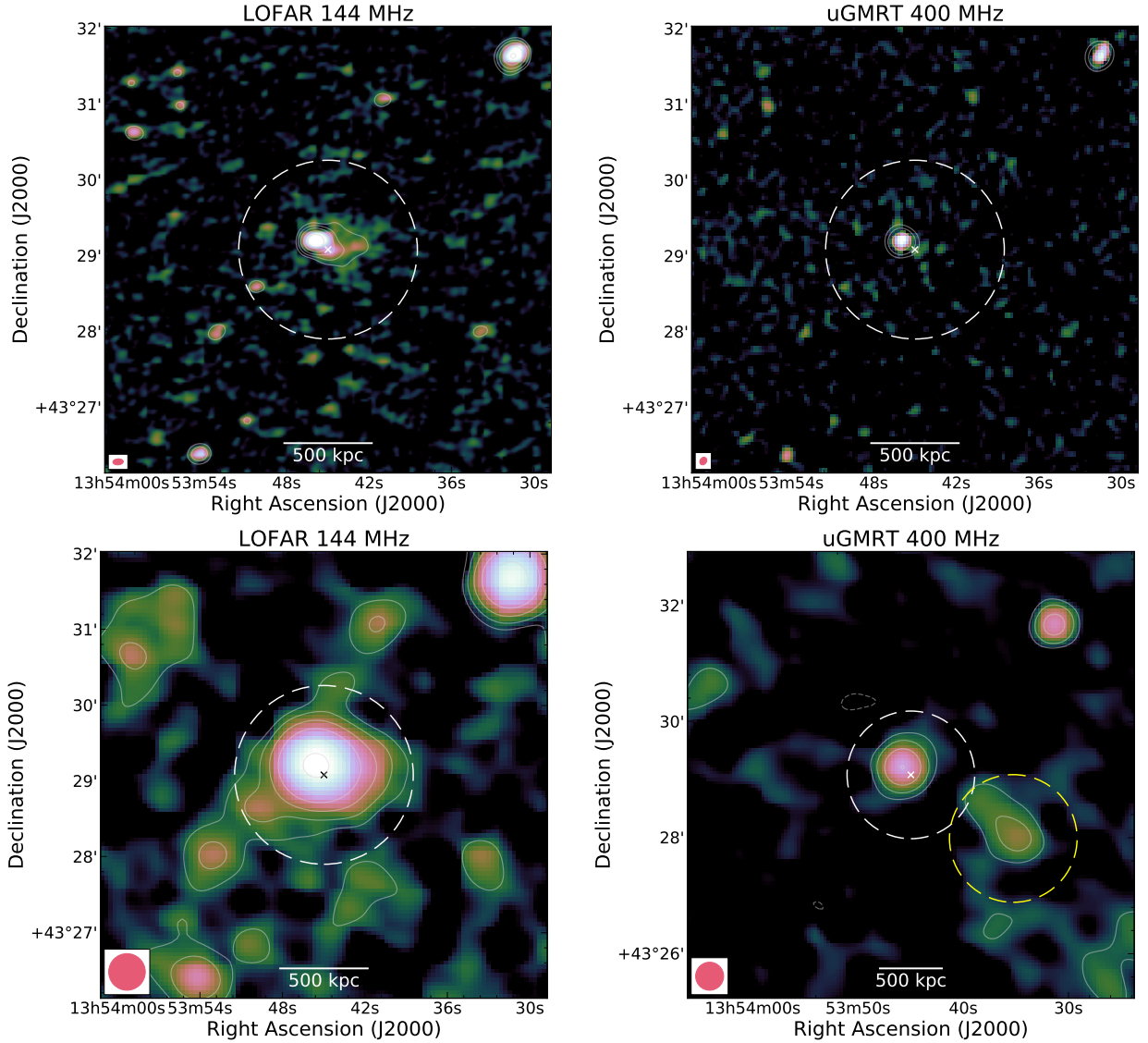


Fig. 2. PSZ2 G089.39+69.36. *Top and bottom rows:* full-resolution and 29'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (left) and 400 MHz (right). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the cross showing the cluster centre. The dashed yellow circle in the *bottom right panel* shows the position of the mock radio halo.

3.2.1. PSZ2 G086.93+53.18

This is the faintest radio halo found in the LOFAR observations ($S_{144} = 6.9 \pm 1.3$ mJy), with a largest linear size $\text{LLS}_{144} = 0.4\text{--}0.5$ Mpc. No diffuse radio emission is visible at 650 MHz, despite the better depth of the observation (see Fig. 1). Using the mock halo injection, we are able to detect diffuse radio emission with a flux density of $S_{650} < 0.7$ mJy ($I_0 = 1.4 \mu\text{Jy arcsec}^{-2}$ and $r_e = 60$ kpc), corresponding to an integrated spectral index of about -1.5 .

3.2.2. PSZ2 G089.39+69.36

A megaparsec-scale radio halo is found in the LOFAR observations ($S_{144} = 10.0 \pm 1.6$ mJy, $\text{LLS}_{144} = 1$ Mpc). No diffuse radio emission is observed in the 400 MHz image (Fig. 2). Using the mock halo injection, we are able to detect diffuse radio emission with a flux density of $S_{400} < 1.9$ mJy ($I_0 = 3.4 \mu\text{Jy arcsec}^{-2}$ and

$r_e = 160$ kpc), corresponding to an integrated spectral index of about -1.6 .

3.2.3. PSZ2 G091.83+26.11

The radio halo in this cluster is the brightest in our sample at all three frequencies (see Fig. 3). The largest linear size of the radio halo is the same in both the LOFAR and uGMRT observations, namely about 1.2 Mpc. The 650 MHz observation is the deepest among the others, assuming $\alpha = -0.8$. At this frequency, we also see substructures in the halo. We measure a flux density of $S_{144} = 65.4 \pm 9.9$ mJy, $S_{400} = 23.9 \pm 2.0$ mJy, and $S_{650} = 14.5 \pm 0.8$ mJy for the LOFAR, uGMRT Band 3, and uGMRT Band 4 observations. This corresponds to integrated spectral indices of $\alpha_{650}^{144} = -1.00 \pm 0.11$, $\alpha_{400}^{144} = -0.99 \pm 0.17$, and $\alpha_{650}^{400} = -1.03 \pm 0.21$. These values are consistent with a single power-law spectral shape. The spectral index map shows

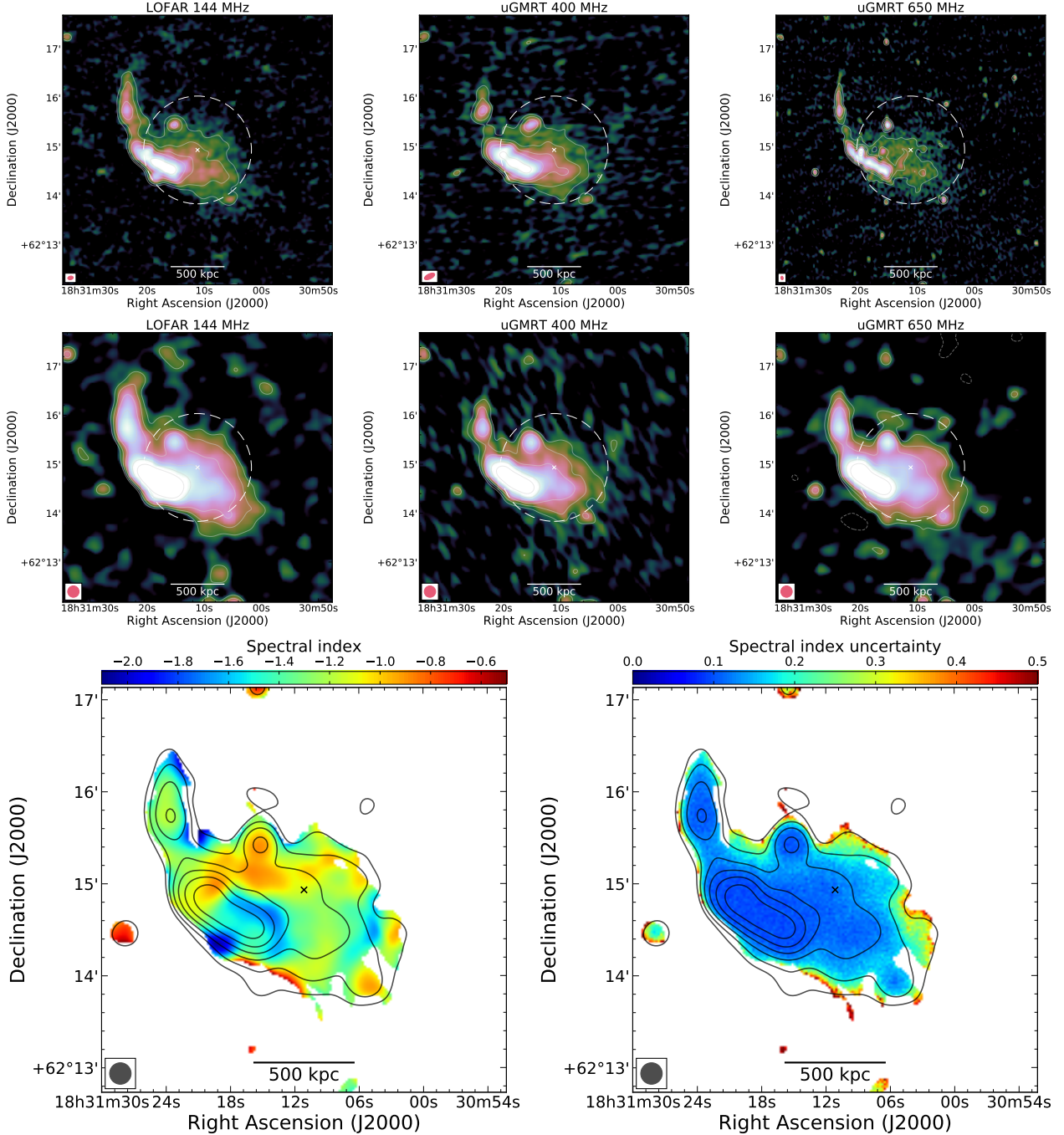


Fig. 3. PSZ2 G091.83+26.11. *Top and central rows:* Full-resolution and 14'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (left), 400 MHz (middle), and 650 MHz (right). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the cross showing the cluster centre. *Bottom row:* spectral index map fitting at 400 MHz (see Sect. 3.1), at 14'' resolution, and the corresponding uncertainty map (left and right panels, respectively). uGMRT radio contours at 650 MHz are drawn in black, at the levels $3\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level (see Table 3).

a steeper spectral index in the central part of the cluster, with α_{400} between ~ -1.2 and ~ -1.4 . Northward, the spectral index gets flatter, with $\alpha_{650}^{144} \sim -0.75$, in correspondence with sources C and D.

In the east and south-east directions, the elongated source that was classified as a candidate radio relic in Di Gennaro et al. (2021b) maintains its morphology. This source can be divided into two pieces: One (R1) located east of the cluster centre, is a faint patchy filament that is 80'' wide and 8'' long, corre-

sponding to $640 \times 60 \text{ kpc}^2$ at the cluster redshift; the other (R2), located southeast of cluster centre, is brighter and extends for about 40'' (i.e. 300 kpc at the cluster redshift). Interestingly, its morphology resembles a double-lobe radio galaxy at 650 MHz. However, no optical counterpart is visible from the available PanSTARRS (Panoramic Survey Telescope and Rapid Response System; Chambers et al. 2016) optical image (see Appendix B). However, we note that the optical image is rather shallow, and might miss faint galaxies. It is possible that R2 combines the

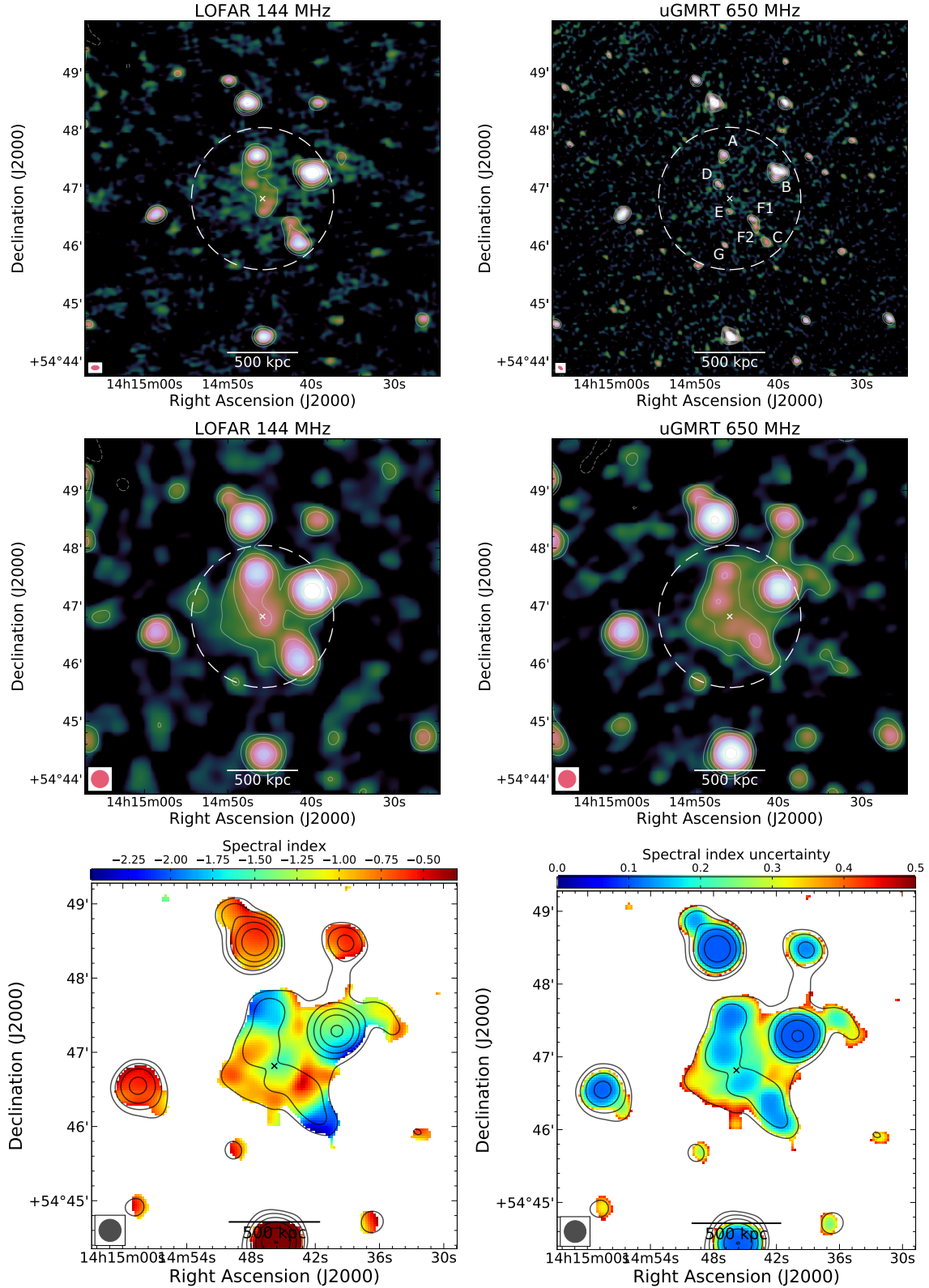


Fig. 4. PSZ2 G099.86+58.45. *Top and central rows:* full-resolution and 18'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (*left*) and 650 MHz (*right*). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. We followed [Cassano et al. \(2019\)](#) for the source labelling (their sources 1, 2, and 3 became D, E, and F1+F2, respectively). The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region obtained from $M_{SZ,500}$, with the cross showing the cluster centre. *Bottom row:* spectral index map between 144 and 650 MHz at 18'' resolution, and correspondent uncertainty map (*left and right panels, respectively*). uGMRT radio contours at 650 MHz are drawn in black, at the levels $3\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} the noise level (see Table 3).

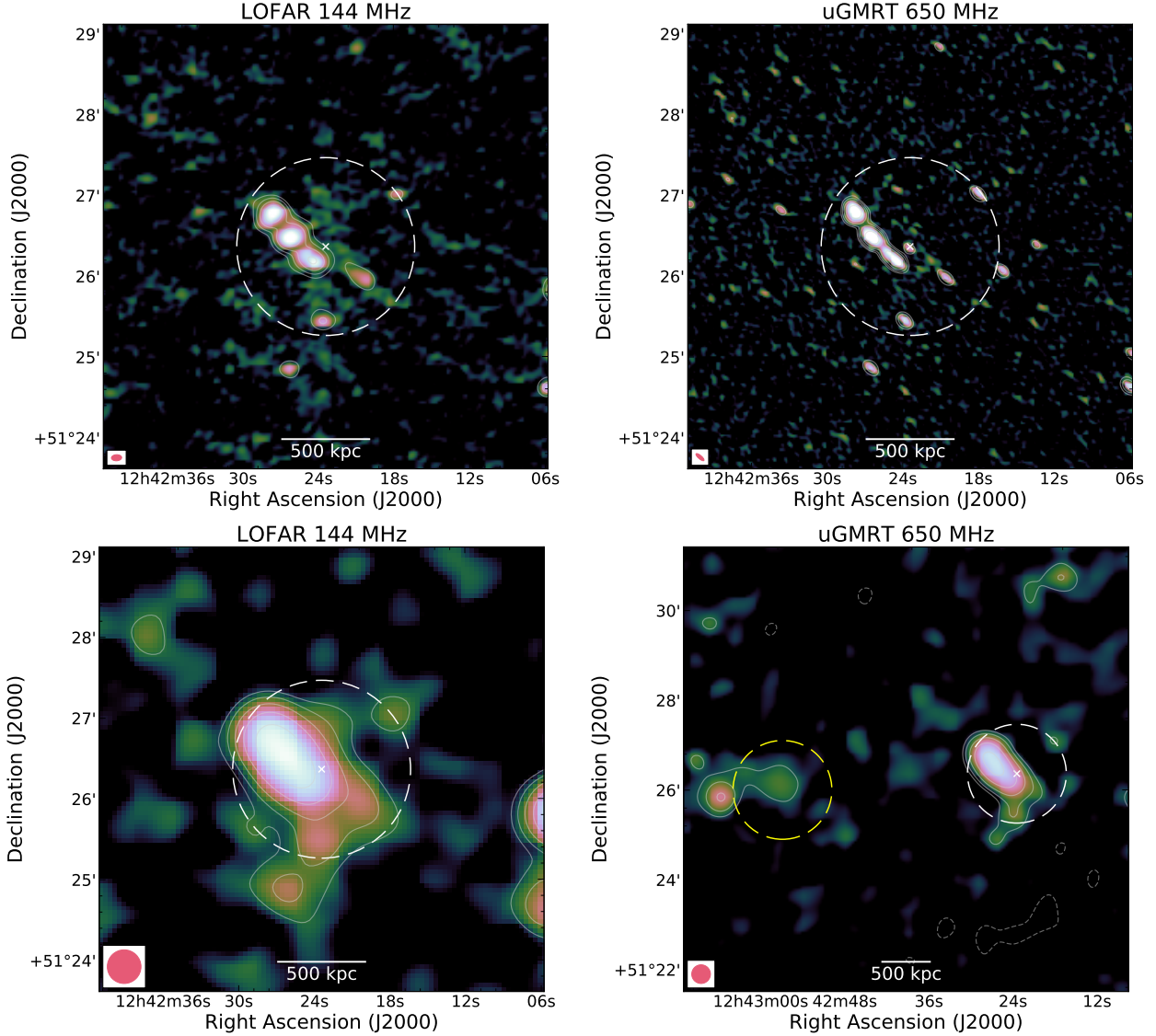


Fig. 5. PSZ2 G126.28+65.62. *Top and bottom rows:* full-resolution and 25'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (*left*) and 650 MHz (*right*). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the cross showing the cluster centre. The dashed yellow circle in the *bottom right panel* shows the position of the mock radio halo.

emission of a radio relic and a double-lobe radio galaxy. Observations with the Karl-Jansky Very Large Telescope (VLA) in the 1–4 GHz band will help in the classification of this elongated piece of emission. In particular, the polarisation characteristics will be crucial and will be presented in a forthcoming paper (Di Gennaro et al., in prep). We measure the flux density for the candidate radio relic from the low-resolution images (i.e. $14'' \times 14''$), considering the full length of the source (i.e. R1+R2). At this resolution, the compact sources B, C, and D are embedded in the candidate relic, and so we measured their flux densities from the full-resolution image and we subtracted them arithmetically from the total flux density. We obtain $S_{144} = 274.8 \pm 45.6$ mJy, $S_{400} = 76.6 \pm 6.5$ mJy, and $S_{650} = 36.3 \pm 2.1$ mJy, corresponding to $\alpha_{650}^{144} = -1.34 \pm 0.12$ ($\alpha_{400}^{144} = -1.25 \pm 0.18$ and $\alpha_{650}^{400} = -1.54 \pm 0.21$). The spectral index map shows hints of steepening for R2 (up to $\alpha_{400} \sim -2$), which is typical of radio relics (e.g., Di Gennaro et al. 2018; Rajpurohit et al. 2018). This

is not observed for R1. Next to the candidate relic, source B is characterised by a very steep spectrum ($\alpha_{400} \sim -2$).

3.2.4. PSZ2 G099.86+58.45

We detect diffuse radio emission in the 650 MHz observations, similar to what is visible at 144 MHz (Fig. 4, $\text{LLS}_{144} = 1.2$ and $\text{LLS}_{650} = 0.95$ Mpc). We measure a flux density of $S_{144} = 18.1 \pm 2.9$ mJy and $S_{650} = 4.0 \pm 0.4$ mJy for the LOFAR and uGMRT Band 4 observations. This corresponds to an integrated spectral index of $\alpha_{650}^{144} = -1.00 \pm 0.13$. The spectral index map in Fig. 4 shows steeper values at the cluster centre (i.e. $\alpha_{650}^{144} \sim -1.6$) and flatter at the cluster outskirts (i.e. $\alpha_{650}^{144} \sim -0.9$). For this cluster, L-band VLA observations are also available (Cassano et al. 2019). In these observations, hints of a halo are present only at the $2\sigma_{\text{rms}}$ level (with $\sigma_{\text{rms,VLA}} = 20 \mu\text{Jy beam}^{-1}$). We repeated the flux measurement, covering the same region as the LOFAR

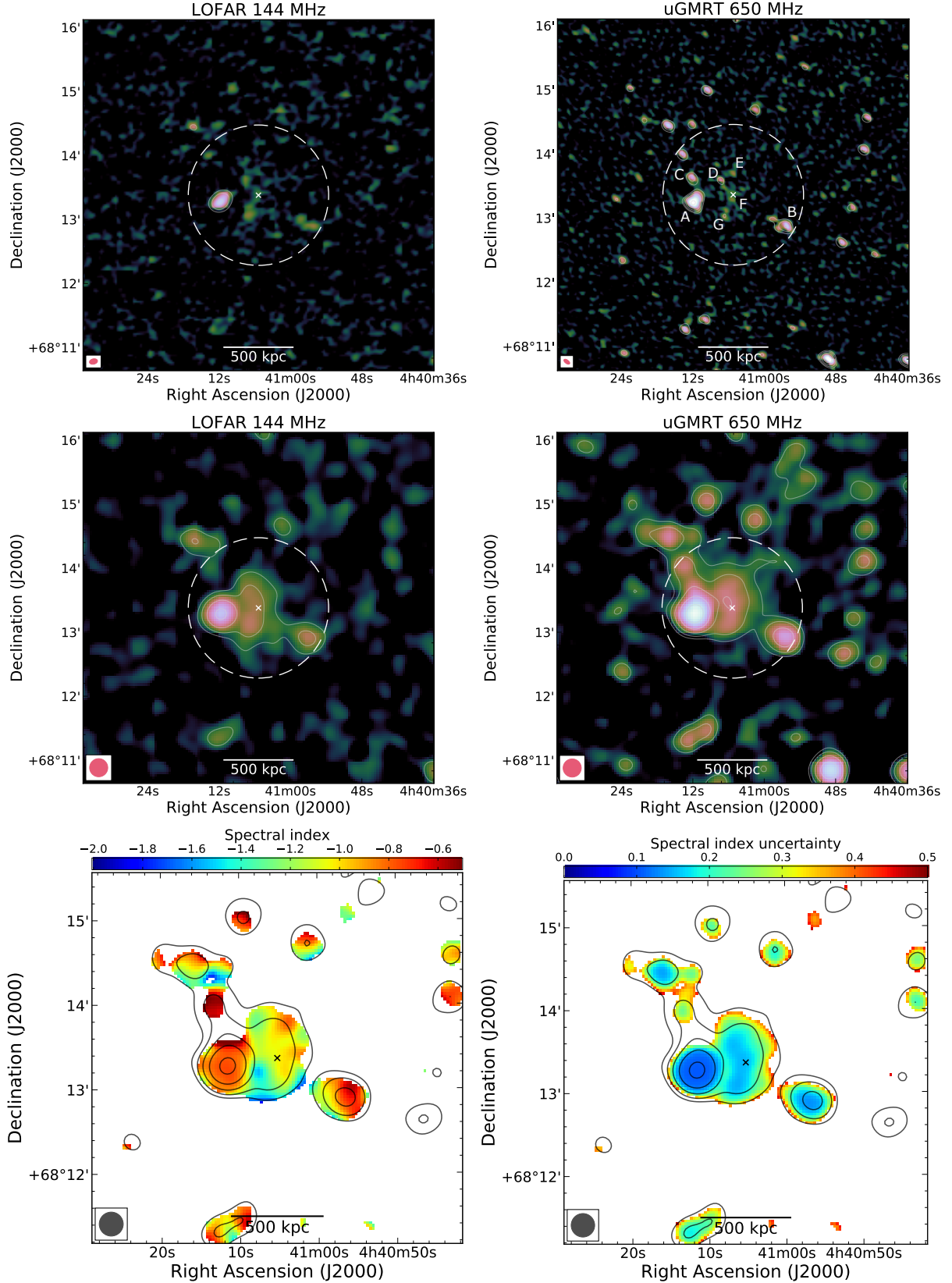


Fig. 6. PSZ2 G141.77+14.19 . *Top and central rows:* full-resolution and 17'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (left) and 650 MHz (right). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region obtained from $M_{SZ,500}$, with the cross showing the cluster centre. *Bottom row:* spectral index map between 144 and 650 MHz at 17'' resolution, and correspondent uncertainty map (left and right panels, respectively). uGMRT radio contours at 650 MHz are drawn in black, at the levels $3\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level (see Table 3).

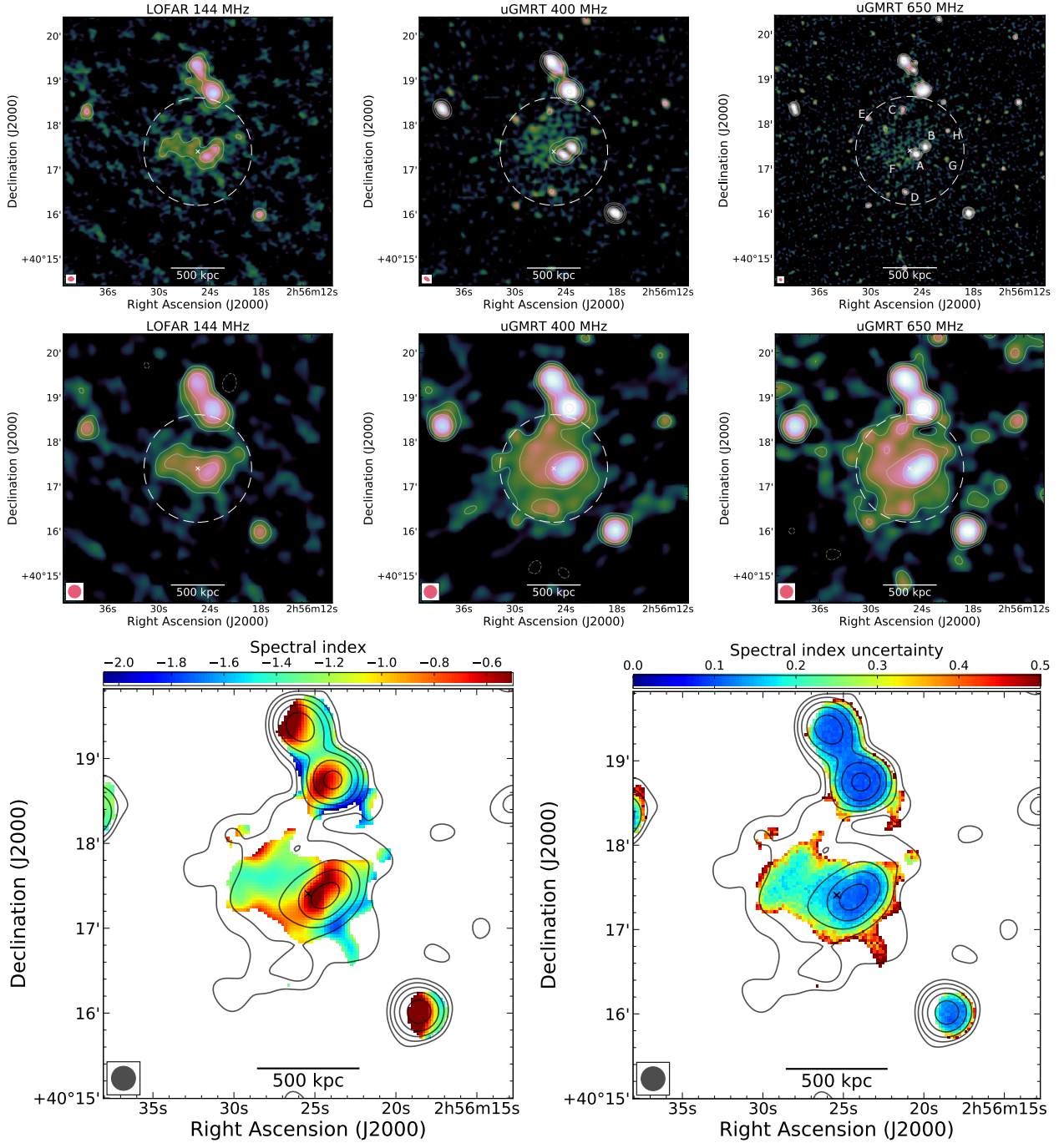


Fig. 7. PLCK G147.3–16.6. *Top and central rows:* full-resolution and 17'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (*left*), 400 MHz (*middle*) and 650 MHz (*right*). Radio contours are drawn in white at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. We followed van Weeren et al. (2014) for the source labelling. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region, obtained from $M_{\text{SZ},500}$, with the cross showing the cluster centre. *Bottom row:* spectral index map at 400 MHz (see Sect. 3.1), at 17'' resolution, and correspondent uncertainty map (*left and right panels*, respectively). uGMRT radio contours at 650 MHz are drawn in black, at the levels $3\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} the noise level (see Table 3).

halo and finding a flux of $S_{1500} \sim 1.0 \pm 0.4$ mJy, in agreement with the flux density reported in Cassano et al. (2019). This VLA flux density suggests a steepening towards GHz frequencies, with $\alpha_{1500}^{650} \sim -1.7 \pm 0.5$.

As for PSZ2 G091.83+26.11, we also detect ultra-steep spectra from source A ($\alpha_{600}^{144} \sim -1.7$) and source C ($\alpha_{650}^{144} \sim -2.5$) in this cluster, as was also mentioned by Cassano et al. (2019).

3.2.5. PSZ2 G126.28+65.62

No diffuse radio emission is found in the uGMRT 650 MHz observations (see right panel Fig. 5, $\text{LLS}_{144} = 0.8$ Mpc). We measure $S_{144} = 8.9 \pm 1.2$ mJy for the radio halo. Using the mock halo injection, we are able to detect diffuse radio emission with a flux density of $S_{650} < 1.0$ mJy ($I_0 = 1.0 \mu\text{Jy arcsec}^{-2}$

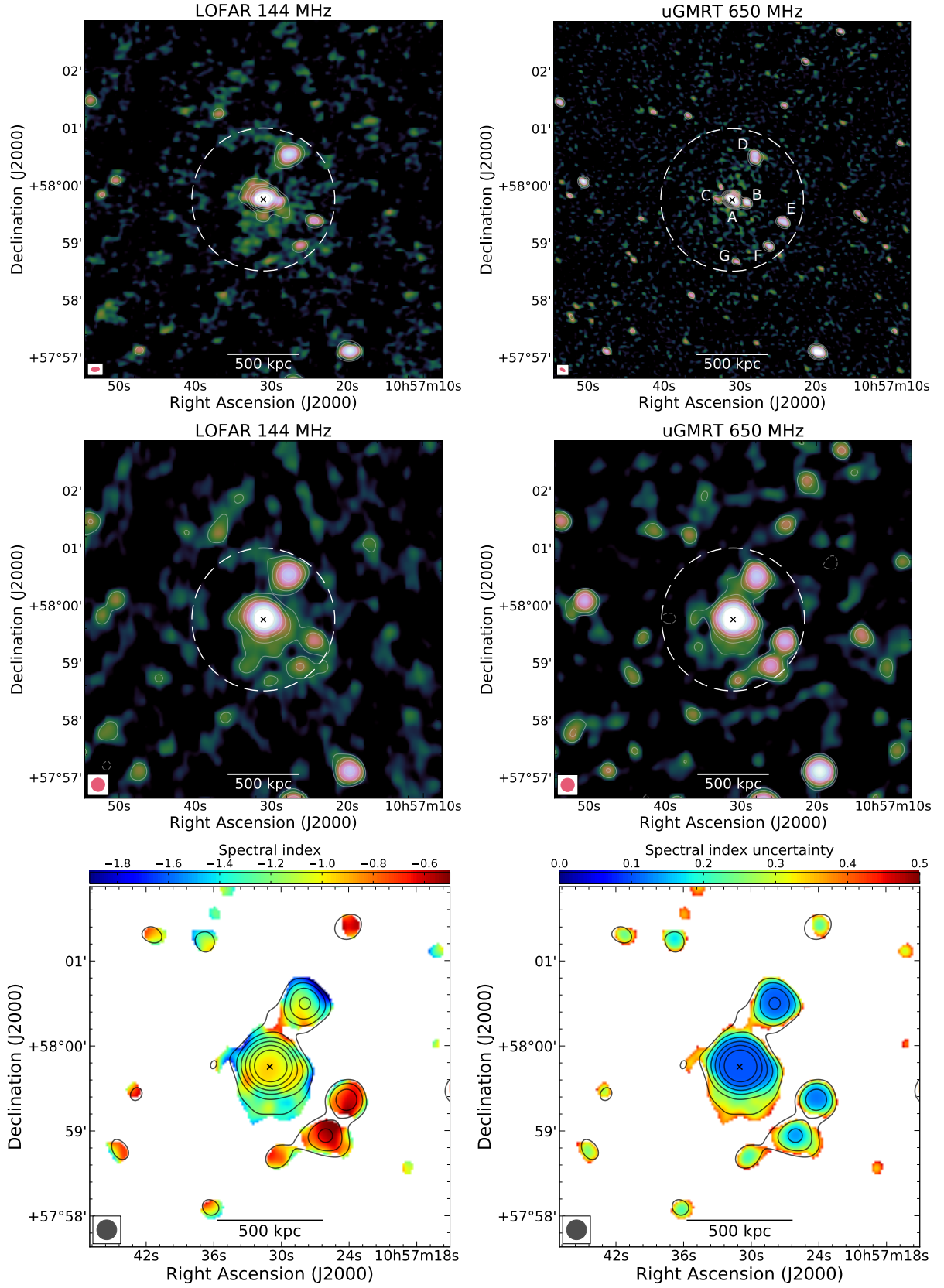


Fig. 8. PSZ2 G147.88+53.24. *Top and central rows:* full-resolution and 14'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (*right*) and 650 MHz (*left*). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region, obtained from $M_{SZ,500}$, with the cross showing the cluster centre. *Bottom row:* spectral index map between 144 and 650 MHz at 14'' resolution, and corresponding uncertainty map (*left and right panels, respectively*). uGMRT radio contours at 650 MHz are drawn in black, at the levels $3\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level (see Table 3).

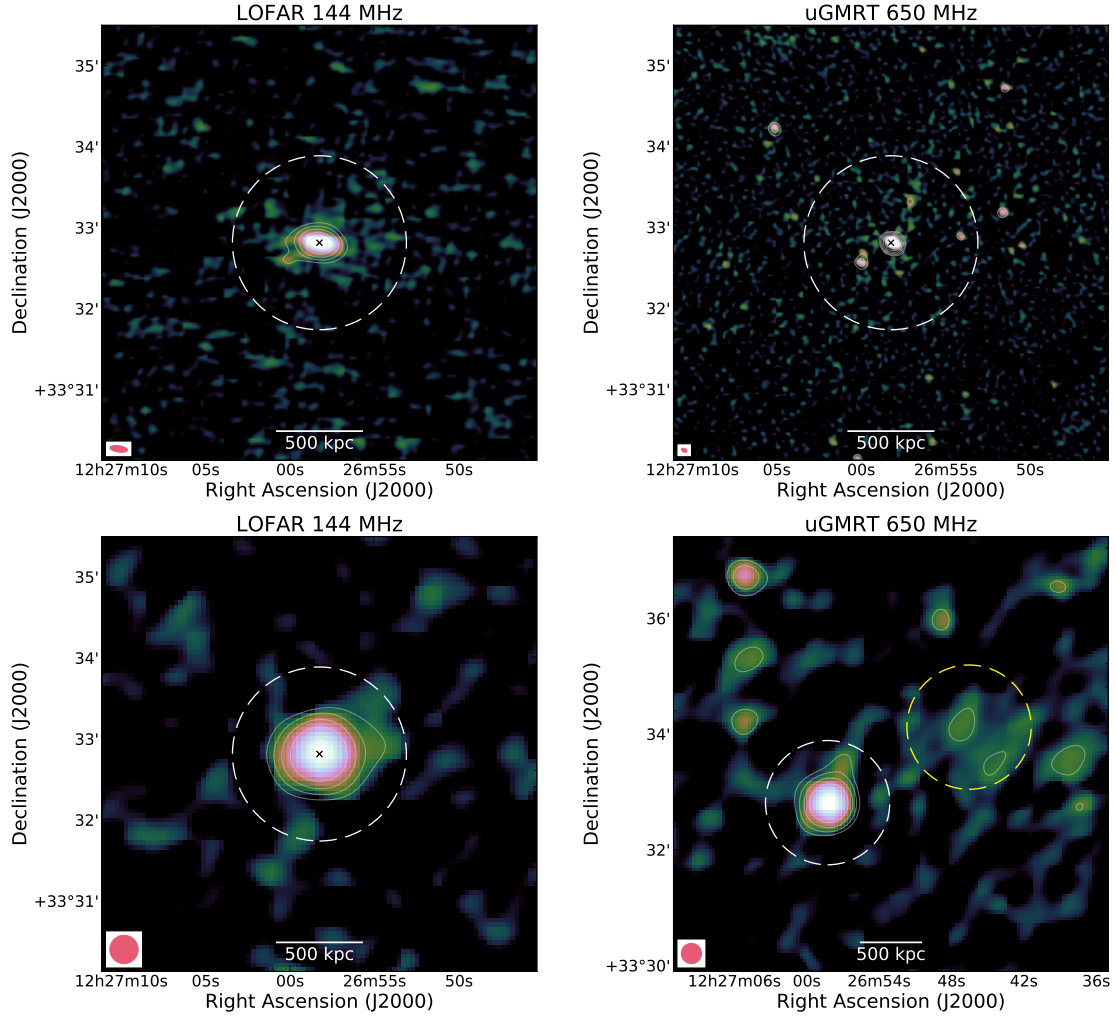


Fig. 9. PSZ2 G160.83+81.66. *Top and bottom rows:* full-resolution and 21'' images (weighting='Briggs' and robust=-0.5) at 144 MHz (*left*) and 650 MHz (*right*). White-coloured radio contours are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} being the noise level at each frequency (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region, obtained from $M_{\text{SZ},500}$, with the cross showing the cluster centre. The dashed yellow circle in the *bottom right* panel shows the position of the mock radio halo.

and $r_e = 130$ kpc). This corresponds to a spectral index of about -1.5 .

3.2.6. PSZ2 G141.77+14.19

Hints of the presence of diffuse emission are present in the uGMRT 650 MHz data around sources D, E, F, and G (see right panel Fig. 6, $\text{LLS}_{144} = 0.6$ and $\text{LLS}_{650} = 0.55$ Mpc). We measure a flux density of $S_{144} = 6.5 \pm 1.2$ mJy and $S_{650} = 1.2 \pm 0.1$ mJy from the same halo region. This corresponds to a spectral index of $\alpha_{650}^{144} = -1.12 \pm 0.13$, and it agrees with the values found in the spectral index map.

3.2.7. PLCK G147.3-16.6

Observations at 610 MHz with the GMRT were published by van Weeren et al. (2014), where a radio halo was discovered. With the new wide-band GMRT observations we confirm the presence of a megaparsec-size radio halo at both 400 and 650 MHz (Fig. 7). Interestingly, in the two uGMRT observations, the diffuse emission appears to be larger than on the LOFAR

image ($\text{LLS}_{144} = 0.8$, $\text{LLS}_{400} = 1$ and $\text{LLS}_{650} = 1$ Mpc). However, we note that this observation is less deep, which is probably due to a bad ionosphere. The flux densities encompassed in the area covered by the halo in the LOFAR images (i.e. solid yellow region, see Appendix A) are $S_{144} = 21.0 \pm 3.7$ mJy, $S_{400} = 5.4 \pm 0.6$ mJy, and $S_{650} = 2.8 \pm 0.3$ mJy for the 144 MHz, 400 MHz, and 650 MHz observations. Increasing the region to cover the full extension of the halo in the uGMRT images (i.e. dashed yellow region, see Appendix A), we obtain $S_{144} = 26.6 \pm 4.4$ mJy, $S_{400} = 10.0 \pm 0.9$ mJy, and $S_{650} = 5.6 \pm 0.4$ mJy. We note that the 650 MHz flux we report is slightly below the one found by van Weeren et al. (2014). This is probably due to a better subtraction of the contribution of the compact sources with the deeper wide-band observations. Given the integrated flux densities, we obtain spectral indices of $\alpha_{650}^{144} = -1.34 \pm 0.15$, $\alpha_{400}^{144} = -1.33 \pm 0.20$, and $\alpha_{650}^{400} = -1.35 \pm 0.37$, in the small area, and $\alpha_{650}^{144} = -1.03 \pm 0.12$, $\alpha_{400}^{144} = -0.96 \pm 0.19$, and $\alpha_{650}^{400} = -1.19 \pm 0.23$, in the big area. The spectral index map in Fig. 7 shows steeper spectral index in the halo centre, with $\alpha_{400} \sim -1.4$, in agreement with the integrated spectral indices in the small halo region.

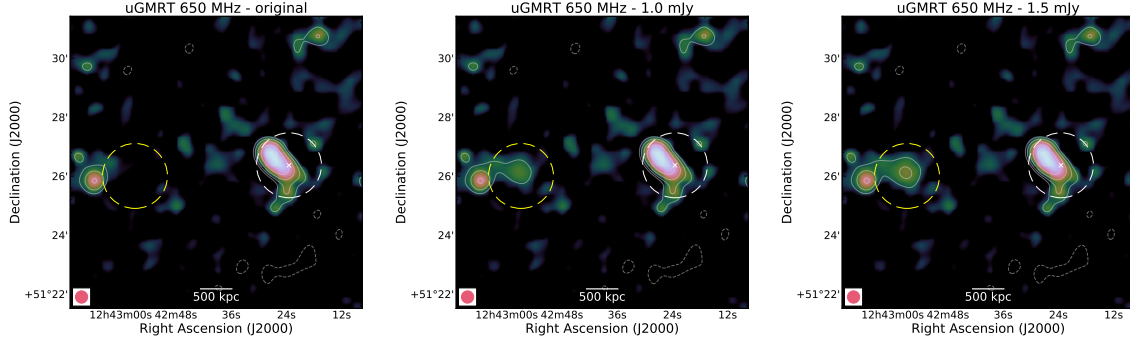


Fig. 10. Example of injection of mock radio halos in PSZ2 G126.28+65.62. *Left:* original image. *Middle:* injected radio halo with a flux density of 1.0 mJy. *Right:* injected radio halo with a flux density of 1.5 mJy. Radio contours are displayed starting from the $2\sigma_{\text{rms}}$ level. The two circles display the R_{500} area, with the white one centred on the cluster (see cross) and the yellow one centred on the injected halo.

Table 4. Flux densities and largest linear sizes (LLS) of the radio halos in our sample.

Cluster name	S_{144}	LLS ₁₄₄ [mJy]	S_{400} [Mpc]	LLS ₄₀₀ [mJy]	S_{650} [Mpc]	LLS ₆₅₀ [mJy]	α_{650}^{144}
PSZ2 G086.93+53.18	6.9 ± 1.3	0.4–0.5	–	–	<0.7	N/A	–
PSZ2 G089.39+69.36	10.0 ± 1.6	1.0	<1.9	N/A	–	–	–
PSZ2 G091.83+26.11	65.4 ± 9.9	1.2	23.9 ± 2.0	1.2	14.5 ± 0.8	1.2	-1.00 ± 0.11
PSZ2 G099.86+58.45	18.1 ± 2.9	1.2	–	–	4.0 ± 0.4	1.0	-1.00 ± 0.13
PSZ2 G126.28+65.62	8.9 ± 1.2	0.8	–	–	<1.0	N/A	–
PSZ2 G141.77+14.19	6.5 ± 1.2	0.6	–	–	1.2 ± 0.1	0.55	-1.12 ± 0.13
PLCK G147.3–16.6	21.0 ± 3.7	0.8	5.4 ± 0.6	1.0	2.8 ± 0.3	1.0	-1.34 ± 0.20
PSZ2 G147.88+53.24	8.2 ± 1.3	0.6	–	–	1.1 ± 0.2	0.5	-1.33 ± 0.17
PSZ2 G160.83+81.66	9.5 ± 1.5	0.7	–	–	<1.0	N/A	–

Notes. In the last column, we report the measured integrated spectral index of the radio halos between 144 MHz and 650 MHz. The LOFAR flux densities agree within 1σ with the values reported in Di Gennaro et al. (2021b). The flux densities reported for PLCK G147.3–16.6 refer to the small halo region (see Appendix A).

3.2.8. PSZ2 G147.88+53.24

Diffuse radio emission at 144 MHz was reported in Di Gennaro et al. (2021b), with $\text{LLS}_{144} = 0.6$ Mpc. This is also confirmed by deep observations at the same frequency (Osinga et al. 2021). Hints of diffuse radio emission are visible in the 650 MHz image (see Fig. 8, $\text{LLS}_{650} = 0.5$ Mpc). Excluding sources D, E, F, and G from the halo region, we measure $S_{144} = 8.2 \pm 1.3$ mJy and $S_{650} = 1.1 \pm 0.2$ mJy for the LOFAR and uGMRT Band 4 observation respectively. This corresponds to a spectral index of $\alpha_{650}^{144} = -1.33 \pm 0.17$. The spectral index map for PSZ2 G147.88+53.24 is mostly dominated by the central compact source (i.e. source A, see Fig. 8), which is characterised by a spectral index $\alpha_{650}^{144} \sim -1$. Just south of this, we detect steeper spectral index values ($\alpha_{650}^{144} \sim -1.3$) that can be associated with the radio halo.

3.2.9. PSZ2 G160.83+81.66

This cluster represents the most distant radio halo found so far, at a redshift of 0.888 ($S_{144} = 9.5 \pm 1.5$ mJy, $\text{LLS}_{144} = 0.7$ see Fig. 9). No diffuse radio emission is visible at 650 MHz. Using the mock halo injection, we are able to detect diffuse radio emission with a flux density of 1.0 mJy ($I_0 = 0.8 \mu\text{Jy arcsec}^{-2}$ and $r_e = 110$ kpc). This corresponds to a spectral index of about -1.5 .

4. Discussion

Investigating the spectral index properties of distant radio halos is crucial to understanding the mechanism of particle acceleration in these radio sources. So far, spectral studies in radio halos have been carried out starting from high-frequency (i.e. \sim GHz) observations, which were then followed up at lower frequencies. However, this approach tends to miss a large fraction of steep-spectra sources simply because they are not detected in the GHz observations. This issue is particularly important for high-redshift clusters, as a large fraction of these halos, especially the low-mass systems, should have a steep spectral index ($\alpha < -1.5$, see Cassano & Brunetti 2005; Cassano et al. 2006). This is due to the larger contribution of inverse Compton energy losses (i.e. $dE/dt_{\text{IC}} \propto (1+z)^4$), which is expected to hamper the acceleration of high-energy electrons. As a consequence, the ensuing synchrotron luminosity should be reduced. The LoTSS survey will help to avoid this bias towards flat-spectra halos. This survey at low frequencies is expected to observe a large number of previously undiscovered radio halos (e.g., Cassano et al. 2010; van Weeren et al. 2021), which can be followed up at higher frequencies.

In Di Gennaro et al. (2021b) we presented the first statistical study of diffuse radio emission with LOFAR (120–168 MHz) of a sample of 19 distant ($z \geq 0.6$) galaxy clusters selected from the *Planck* SZ catalogue (Planck Collaboration XXVII 2016). In the present work, we present a follow-up study at higher fre-

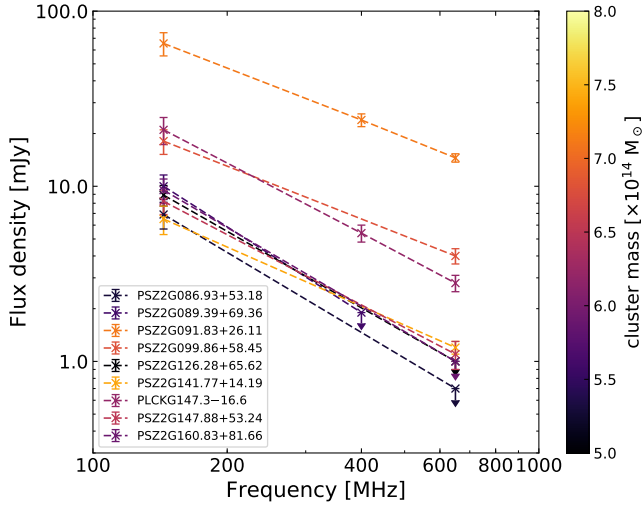


Fig. 11. Radio spectra of the clusters in our sample (Table 4). The arrows show the upper limits on the flux densities.

quencies of the nine radio halos detected in the LOFAR observations. Our observations were carried out with the uGMRT, mainly at 550–900 MHz (Band 4), but for two clusters (i.e. PSZ2 G091.83+26.11 and PLCK G147.3–16.6) we also obtained observations at 250–550 MHz (Band 3). At these higher frequencies, we find the presence of diffuse radio emission in five of the nine clusters discovered in LOFAR. These are PSZ2 G091.83+26.11, PSZ2 G099.86+58.45, PSZ2 G141.77+14.19, PLCK G147.3–16.6, and PSZ2 G147.88+53.24. While we note that these clusters are also the most massive objects in our sample, with $M_{500,\text{SZ}} \sim 6\text{--}8 \times 10^{14} M_{\odot}$, the low-mass clusters in our sample (i.e. $M_{500,\text{SZ}} = 5\text{--}6 \times 10^{14} M_{\odot}$; PSZ2 G086.93+53.18, PSZ2 G089.39+69.36, PSZ2 G126.28+65.62 and PSZ2 G160.83+81.66) do not show diffuse radio emission at the uGMRT frequencies and we could only derive upper limits on the flux density (Fig. 11).

For the uGMRT-detected radio halos, we measure integrated spectral indices between -1 and -1.4 (see Table 4). These values are similar to those found for classical halos in local clusters (e.g., Feretti et al. 2012; van Weeren et al. 2019). We also note that for those targets with three observing frequencies (i.e. PSZ2 G091.83+26.11 and PLCK G147.3–16.6), no spectral curvature is present. This means that the steepening frequency ν_s has to be at higher frequencies (i.e. $\nu_s > 650$ MHz). Hints of spectral steepening are indeed suggested with archival 1.4 GHz VLA observations of PSZ2 G099.86+58.45 (Cassano et al. 2019). For the non-detections, we tested the sensitivity of our uGMRT data by injecting mock halos with spectral indices of -1.5 (Sects. 3.2.1, 3.2.5 and 3.2.9) or -1.6 (Sect. 3.2.2). In this case, we found that diffuse radio emission is observed above the $2\sigma_{\text{rms}}$ level. As these halos are not detected in our uGMRT images, this implies that they should have a steeper spectral index.

4.1. Comparison with theoretical models

Although our sample is not designed to test the occurrence of radio halos in high-redshift systems (because of its small size and low completeness), we can compare our results with model expectations. According to re-acceleration models, the possibility to detect diffuse radio emission depends on the steepening frequency ν_s of the synchrotron spectra. Therefore, halos can be

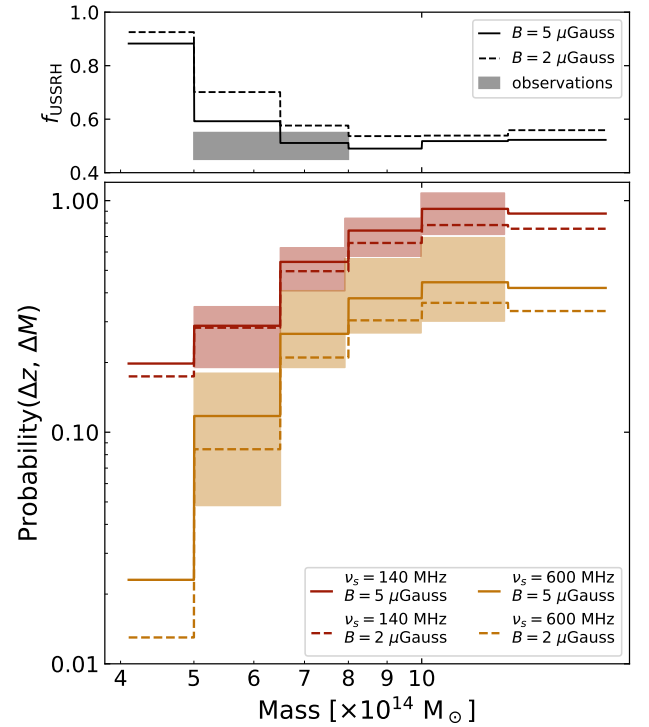


Fig. 12. Probability of forming radio halos with $\nu_s > 140$ and $\nu_s > 600$ MHz (red and yellow lines, respectively) as a function of the cluster virial mass in the redshift range $0.6\text{--}0.7$. Magnetic fields of $B = 5 \mu\text{Gauss}$ and $B = 2 \mu\text{Gauss}$ are assumed (solid and dashed lines, respectively). The shadowed regions represent the 1σ uncertainty derived through Monte Carlo calculations. *Top panel:* expected fraction of USSRH visible at 144 MHz with steepening frequency $\nu_s < 600$ MHz as a function of the cluster virial mass, assuming $B = 5 \mu\text{Gauss}$ and $B = 2 \mu\text{Gauss}$ (solid and dashed lines, respectively). The shadowed area indicates the observed fraction of USSRH in our sample.

observed only at $\nu \leq \nu_s$, with ν being the observing frequency. Following the procedure in Cassano et al. (2019), we estimated the probability of forming a radio halo as a function of cluster mass at a median redshift of $z = 0.7$ and with a steepening frequency of $\nu_s \geq 140$ MHz and $\nu_s \geq 600$ MHz (see Fig. 12). The formation probability takes into account the cluster merger history (merger trees), the generation of turbulence, particle acceleration (including energy losses) and the resulting cluster synchrotron spectrum. In these models, the turbulent energy, acceleration rate, and magnetic field per volume unit are considered constant (i.e. homogeneous models, Cassano et al. 2010). Here we consider magnetic field strengths of 2 and 5 μGauss (solid and dashed lines in Fig. 12), which matches the range of results in Di Gennaro et al. (2021b). The highest value for the magnetic field strength is based on the value that maximises the lifetime of relativistic electrons at the system redshift, that is, $B = B_{\text{CMB}}/\sqrt{3}$ (where $B_{\text{CMB}} = 3.25(1+z)^2 \mu\text{Gauss}$ is the magnetic field strength equivalent to the energy density of the cosmic microwave background). We assumed that the radio emission encompasses a region $R_H = 400$ kpc, which is the median size of the halos in our sample (see Table 4). The value of R_H is smaller than the typical radio halos found in the local Universe (i.e. $z \sim 0.2$). This is probably due to the fact that, for the same mass, distant clusters have smaller virial radii (Kitayama & Suto 1996). The uncertainty of the estimated fraction of halos is obtained via 1000 Monte Carlo extractions of galaxy cluster samples from the pool of simulated merger trees

(Cassano et al. 2010, see yellow shaded areas in Fig. 12). We find that, in the mass interval of our sample $M_{500} = 5.0\text{--}8.0 \times 10^{14} M_{\odot}$, and assuming $B = 5 \mu\text{Gauss}$, the probability of observing a radio halo with steepening frequency $\nu_s \geq 140$ MHz is between 60% and 30% (Fig. 12 red line), while it decreases down to 13–30% for $\nu_s \geq 600$ MHz (Fig. 12 yellow line), with a clear dependence on cluster mass. This agrees with our observations, where we detect a radio halo in about 47% of the total sample (9/19) at 144 MHz (Di Gennaro et al. 2021b) and in about 26% (5/19) at 650 MHz. Assuming $B = 2 \mu\text{Gauss}$, the expected fractions of halos are consistent with the uncertainties given the Monte Carlo simulations (see dashed lines in Fig. 12).

These expectations imply the presence of a population of ultra-steep spectra radio halos (USSRHs) with $140 \leq \nu_s < 600$ MHz, which will be missed by observations at frequencies higher than 600 MHz because of their ultra-steep radio spectra. In the top panel of Fig. 12, we show the fraction of these USSRH with respect to the total number of radio halos expected at 140 MHz, f_{USSRH} , as a function of the cluster mass, assuming $B = 5 \mu\text{Gauss}$ and $B = 2 \mu\text{Gauss}$ (solid and dashed lines, respectively). Given the mass range of our clusters, namely $M_{500} = 5.0\text{--}8.0 \times 10^{14} M_{\odot}$, we expect 50–60% ($B = 5 \mu\text{Gauss}$) or 65–60% ($B = 2 \mu\text{Gauss}$) of these to be ultra steep (i.e. $\alpha < -1.4$). Despite the low statistics, the estimate using higher magnetic fields is in good agreement with our observations, where we estimate about 45% USSRHs (see Table 4). Increasing the number of distant radio halos will help to better determine the magnetic field levels in these clusters.

4.2. Occurrence of radio relics at high redshift

According to the predictions by Nuza et al. (2012), about 800 radio relics should have been observed at $0.5 < z < 1$ in the full LoTSS survey. However, Nuza et al. (2017) showed in a follow-up work that the majority of these relics, if physical and not artefacts due to a simplified modelling of the ICM, would have small angular extensions ($\lesssim 2'$ when the image is smoothed with a $45''$ beam). Therefore, they would be challenging to detect and classify correctly. The results by Nuza et al. (2017) confirm that relics as extended as the one in PSZ2 G091.83+26.11 and sufficiently bright to be detected are rare in distant clusters.

In our total sample of 19 clusters at $z \geq 0.6$ we found one candidate radio relic, in PSZ2 G091.83+26.11. This source has a linear size of larger than 1 Mpc. Although our sample is not complete and is rather small, we are likely observing the most violent mergers in the distant Universe (i.e. $M > 5 \times 10^{14} M_{\odot}$) and we would have expected to detect more relics. However, a reliable prediction which includes a proper analysis of the probability of identifying and classifying relics, and their number to be detected in LoTSS, is still missing. At $z > 0.5$, five additional radio relics, namely PLCK G004.5-19.5 ($z = 0.52$, Dec = -33° , Albert et al. 2017), MACS J1149.5+2223 ($z = 0.544$, Bonafede et al. 2012), MACS J0717.5+3745 ($z = 0.546$, Bonafede et al. 2009; van Weeren et al. 2009), MACS J0025.4-1222 ($z = 0.584$, Dec = -12° , Riseley et al. 2017), and ACT-CL J0102-4915 (“el Gordo”; $z = 0.87$, Dec = -49° ; Lindner et al. 2014), and two candidate radio relics, namely ACT-CL J0014.9-0057 ($z = 0.533$, Dec = -1° , Knowles et al. 2019) and ACT-CL J0046.4-3912 ($z = 0.592$, Dec = -39° , Knowles et al. 2021), are known in the literature⁴. Among these, MACS J0717.5+3745, MACS J1149.5+2223, and ACT-

CL J0046.4-3912 host relics with linear sizes of about 1 Mpc. The small number of detections available to date does not allow a clear comparison with the current models. Despite that, the findings we present in this paper and future observations of high- z relics will be crucial to developing more stringent predictions of the magnetic properties of the ICM at the location of the shock, acceleration efficiency, and seed populations when the first structure formed (Brüggen & Vazza 2020).

5. Conclusions

In this paper, we present follow-up observations of the high-redshift *Planck*-SZ clusters hosting diffuse radio sources presented in Di Gennaro et al. (2021b). Our observations were taken with the upgraded GMRT (uGMRT) in Band 4 (550–900 MHz) and, for two clusters (i.e. PSZ2 G091.83+26.11 and PLCK G147.3–16.6) also in Band 3 (250–500 MHz)⁵. These observations were combined with LOFAR data at 144 MHz. Below we summarise our findings.

- About 50% (5/9) of the clusters presented show the presence of a radio halo in the uGMRT observations, up to $\nu = 650$ MHz.
- For these systems, we measure integrated spectral indices of between -1 and -1.4 . We note that these clusters are also the most massive in our sample, and at these redshifts ($M > 6 \times 10^{14} M_{\odot}$). This also implies more energetic merger events.
- The injection of mock radio halos reveals that diffuse radio emission with $\alpha \sim -1.5$ is detectable in our uGMRT data. Therefore, for those clusters with a radio halo in the LOFAR images but not in the uGMRT ones, we estimate that they should have integrated spectral indices steeper than -1.5 , in line with the predictions of re-acceleration models (Cassano et al. 2010).
- Although our sample is not complete, the fraction of clusters hosting halos and the spectral indices agree with expectations from theoretical models of re-acceleration (Cassano & Brunetti 2005; Cassano et al. 2006, 2010).
- We confirm the presence of a single candidate radio relic in this sample of distant clusters, in PSZ2 G091.83+26.11, as reported in Di Gennaro et al. (2021b). This is possibly contaminated by a double radio galaxy, although no optical counterparts have been observed in the PanSTARRS data. A future polarisation analysis with the VLA will provide further information on the nature of this radio source.

Observing distant diffuse radio emission is particularly important for the investigation of the evolution of magnetic fields over cosmic time and Universe magnetogenesis. Given the small size of the sample presented in this work, comparison with cosmological simulations is difficult. Upcoming observations with the X-ray satellite eROSITA (Extended Roentgen Survey Imaging Telescope Array; Merloni et al. 2012, 2020) will help in finding new distant galaxy clusters that can be easily followed up by low-frequency radio observations.

Acknowledgements. We thank the anonymous referee for useful comments which have improved the quality of the manuscript. This paper is based on data obtained with the Giant Metrewave Radio Telescope (GMRT). GMRT is run by the National Centre for Radio Astrophysics of the Tata Institute of Fundamental Research. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc. We thank the staff of the GMRT that made these observations possible. LOFAR (van Haarlem et al. 2013) is the Low Frequency Array designed and constructed by ASTRON. It has observing, data processing, and

⁴ Only MACS J1149.5+2223 and MACS J0717.5+3745 are observed with LOFAR (Bruno et al. 2021; Bonafede et al. 2018, respectively).

⁵ PSZ2 G089.39+69.36 was observed only in Band 3.

data storage facilities in several countries, which are owned by various parties (each with their own funding sources), and which are collectively operated by the ILT foundation under a joint scientific policy. The ILT resources have benefited from the following recent major funding sources: CNRS-INSU, Observatoire de Paris and Université d'Orléans, France; BMBF, MIWF-NRW, MPG, Germany; Science Foundation Ireland (SFI), Department of Business, Enterprise and Innovation (DBEI), Ireland; NWO, The Netherlands; The Science and Technology Facilities Council, UK; Ministry of Science and Higher Education, Poland; The Istituto Nazionale di Astrofisica (INAF), Italy. This research made use of the Dutch national e-infrastructure with support of the SURF Cooperative (e-infra 180169) and the LOFAR e-infra group. The Jülich LOFAR Long Term Archive and the German LOFAR network are both coordinated and operated by the Jülich Supercomputing Centre (JSC), and computing resources on the supercomputer JUWELS at JSC were provided by the Gauss Centre for Supercomputing e.V. (grant CHTB00) through the John von Neumann Institute for Computing (NIC). This research made use of the University of Hertfordshire high-performance computing facility and the LOFAR-UK computing facility located at the University of Hertfordshire and supported by STFC [ST/P000096/1], and of the Italian LOFAR IT computing infrastructure supported and operated by INAF, and by the Physics Department of Turin university (under an agreement with Consorzio Interuniversitario per la Fisica Spaziale) at the C3S Supercomputing Centre, Italy. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc. GDG and RJvW acknowledge support from the ERC Starting Grant ClusterWeb 804208. RC and GB acknowledge support from INAF through the mainstream project "Cluster science with LOFAR". HJAR acknowledges support from the ERC Advanced Investigator programme NewClusters 321271. AB and RJvW acknowledge support from the VIDI research programme with project number 639.042.729, which is financed by the Netherlands Organisation for Scientific Research (NWO). VC acknowledges support from the Alexander von Humboldt Foundation.

References

- Ackermann, M., Ajello, M., Allafort, A., et al. 2010, *ApJ*, **717**, L71
- Adam, R., Goksu, H., Brown, S., Rudnick, L., & Ferrari, C. 2021, *A&A*, **648**, A60
- Albert, J. G., Sifón, C., Stroe, A., et al. 2017, *A&A*, **607**, A4
- Blasi, P., & Colafrancesco, S. 1999, *Astropart. Phys.*, **12**, 169
- Bonafede, A., Feretti, L., Giovannini, G., et al. 2009, *A&A*, **503**, 707
- Bonafede, A., Brüggén, M., van Weeren, R., et al. 2012, *MNRAS*, **426**, 40
- Bonafede, A., Intema, H. T., Brüggén, M., et al. 2014, *ApJ*, **785**, 1
- Bonafede, A., Cassano, R., Brüggén, M., et al. 2017, *MNRAS*, **470**, 3465
- Bonafede, A., Brüggén, M., Rafferty, D., et al. 2018, *MNRAS*, **478**, 2927
- Botteon, A., Gastaldello, F., Brunetti, G., & Dallacasa, D. 2016, *MNRAS*, **460**, L84
- Botteon, A., Brunetti, G., Ryu, D., & Roh, S. 2020, *A&A*, **634**, A64
- Brüggén, M., & Vazza, F. 2020, *MNRAS*, **493**, 2306
- Brunetti, G., & Jones, T. W. 2014, *Int. J. Mod. Phys. D*, **23**, 1430007
- Brunetti, G., & Lazarian, A. 2007, *MNRAS*, **378**, 245
- Brunetti, G., & Lazarian, A. 2011, *MNRAS*, **410**, 127
- Brunetti, G., & Lazarian, A. 2016, *MNRAS*, **458**, 2584
- Brunetti, G., Setti, G., Feretti, L., & Giovannini, G. 2001, *MNRAS*, **320**, 365
- Brunetti, G., Zimmer, S., & Zandanel, F. 2017, *MNRAS*, **472**, 1506
- Bruno, L., Rajpurohit, K., Brunetti, G., et al. 2021, *A&A*, **650**, A44
- Cassano, R., & Brunetti, G. 2005, *MNRAS*, **357**, 1313
- Cassano, R., Brunetti, G., & Setti, G. 2006, *MNRAS*, **369**, 1577
- Cassano, R., Etti, S., Giacintucci, S., et al. 2010, *ApJ*, **721**, L82
- Cassano, R., Etti, S., Brunetti, G., et al. 2013, *ApJ*, **777**, 141
- Cassano, R., Botteon, A., Di Gennaro, G., et al. 2019, *ApJ*, **881**, L18
- Chambers, K. C., Magnier, E. A., Metcalfe, N., et al. 2016, *ArXiv e-prints* [ArXiv:1612.05560]
- Chandra, P., Ray, A., & Bhatnagar, S. 2004, *ApJ*, **612**, 974
- Cuciti, V., Cassano, R., Brunetti, G., et al. 2021a, *A&A*, **647**, A51
- Cuciti, V., Cassano, R., Brunetti, G., et al. 2021b, *A&A*, **647**, A50
- de Gasperin, F., Dijkema, T. J., Drabent, A., et al. 2019, *A&A*, **622**, A5
- Di Gennaro, G., van Weeren, R. J., Hoeft, M., et al. 2018, *ApJ*, **865**, 24
- Di Gennaro, G., van Weeren, R. J., Andrade-Santos, F., et al. 2019, *ApJ*, **873**, 64
- Di Gennaro, G., van Weeren, R. J., Brunetti, G., et al. 2021a, *Nat. Astron.*, **5**, 268
- Di Gennaro, G., van Weeren, R. J., Rudnick, L., et al. 2021b, *ApJ*, **911**, 3
- Dolag, K., & Enßlin, T. A. 2000, *A&A*, **362**, 151
- Donnert, J., Dolag, K., Brunetti, G., & Cassano, R. 2013, *MNRAS*, **429**, 3564
- Drury, L. O. 1983, *Rep. Prog. Phys.*, **46**, 973
- Enßlin, T. A., Biermann, P. L., Klein, U., & Kohle, S. 1998, *A&A*, **332**, 395
- Feretti, L., Giovannini, G., Govoni, F., & Murgia, M. 2012, *A&ARv*, **20**, 54
- Giacintucci, S., Venturi, T., Macario, G., et al. 2008, *A&A*, **486**, 347
- Giovannini, G., Cau, M., Bonafede, A., et al. 2020, *A&A*, **640**, A108
- Govoni, F., Murgia, M., Feretti, L., et al. 2005, *A&A*, **430**, L5
- Govoni, F., Murgia, M., Feretti, L., et al. 2006, *A&A*, **460**, 425
- Hoang, D. N., Shimwell, T. W., Stroe, A., et al. 2017, *MNRAS*, **471**, 1107
- Hoang, D. N., Shimwell, T. W., van Weeren, R. J., et al. 2018, *MNRAS*, **478**, 2218
- Intema, H. T., van der Tol, S., Cotton, W. D., et al. 2009, *A&A*, **501**, 1185
- Kale, R., Venturi, T., Giacintucci, S., et al. 2015, *A&A*, **579**, A92
- Kang, H., Ryu, D., & Jones, T. 2017, in *35th International Cosmic Ray Conference (ICRC2017)*, International Cosmic Ray Conference, 301, 283
- Kitayama, T., & Suto, Y. 1996, *ApJ*, **469**, 480
- Knowles, K., Baker, A. J., Bond, J. R., et al. 2019, *MNRAS*, **486**, 1332
- Knowles, K., Pillay, D. S., Amodeo, S., et al. 2021, *MNRAS*, **504**, 1749
- Lindner, R. R., Baker, A. J., Hughes, J. P., et al. 2014, *ApJ*, **786**, 49
- Markevitch, M., Govoni, F., Brunetti, G., & Jerius, D. 2005, *ApJ*, **627**, 733
- Merloni, A., Nandra, K., & Predehl, P. 2020, *Nat. Astron.*, **4**, 634
- Merloni, A., Predehl, P., Becker, W., et al. 2012, *ArXiv e-prints* [arXiv:1209.3114]
- Murgia, M., Govoni, F., Markevitch, M., et al. 2009, *A&A*, **499**, 679
- Nuza, S. E., Hoeft, M., van Weeren, R. J., Gottlöber, S., & Yepes, G. 2012, *MNRAS*, **420**, 2006
- Nuza, S. E., Gelszinnis, J., Hoeft, M., & Yepes, G. 2017, *MNRAS*, **470**, 240
- Offringa, A. R., & Smirnov, O. 2017, *MNRAS*, **471**, 301
- Offringa, A. R., McKinley, B., Hurley-Walker, N., et al. 2014, *MNRAS*, **444**, 606
- Osinga, E., van Weeren, R. J., Boxelaar, J. M., et al. 2021, *A&A*, **648**, A11
- Pearce, C. J. J., van Weeren, R. J., Andrade-Santos, F., et al. 2017, *ApJ*, **845**, 81
- Petrosian, V. 2001, *ApJ*, **557**, 560
- Pinzke, A., Oh, S. P., & Pfrommer, C. 2017, *MNRAS*, **465**, 4800
- Planck Collaboration XXVII. 2016, *A&A*, **594**, A27
- Press, W. H., & Schechter, P. 1974, *ApJ*, **187**, 425
- Prokhorov, D. A., & Churazov, E. M. 2014, *A&A*, **567**, A93
- Rajpurohit, K., Hoeft, M., van Weeren, R. J., et al. 2018, *ApJ*, **852**, 65
- Reimer, O., Pohl, M., Sreekumar, P., & Mattox, J. R. 2003, *ApJ*, **588**, 155
- Riseley, C. J., Scaife, A. M. M., Wise, M. W., & Clarke, A. O. 2017, *A&A*, **597**, A96
- Röttgering, H. J. A., Wieringa, M. H., Hunstead, R. W., & Ekers, R. D. 1997, *MNRAS*, **290**, 577
- Shimwell, T. W., Röttgering, H. J. A., Best, P. N., et al. 2017, *A&A*, **598**, A104
- Shimwell, T. W., Tasse, C., Hardcastle, M. J., et al. 2019, *A&A*, **622**, A1
- Smirnov, O. M., & Tasse, C. 2015, *MNRAS*, **449**, 2668
- Springel, V., Frenk, C. S., & White, S. D. M. 2006, *Nature*, **440**, 1137
- Tasse, C. 2014, *A&A*, **566**, A127
- Tasse, C., Hugo, B., Mirmont, M., et al. 2018, *A&A*, **611**, A87
- Tasse, C., Shimwell, T., Hardcastle, M. J., et al. 2021, *A&A*, **648**, A1
- van Haarlem, M. P., Wise, M. W., Gunst, A. W., et al. 2013, *A&A*, **556**, A2
- van Weeren, R. J., Röttgering, H. J. A., Brüggén, M., & Cohen, A. 2009, *A&A*, **505**, 991
- van Weeren, R. J., Röttgering, H. J. A., Brüggén, M., & Hoeft, M. 2010, *Science*, **330**, 347
- van Weeren, R. J., Intema, H. T., Lal, D. V., et al. 2014, *ApJ*, **781**, L32
- van Weeren, R. J., Williams, W. L., Hardcastle, M. J., et al. 2016, *ApJS*, **223**, 2
- van Weeren, R. J., Andrade-Santos, F., Dawson, W. A., et al. 2017, *Nat. Astron.*, **1**, 0005
- van Weeren, R. J., de Gasperin, F., Akamatsu, H., et al. 2019, *Space Sci. Rev.*, **215**, 16
- van Weeren, R. J., Shimwell, T. W., Botteon, A., et al. 2021, *A&A*, **651**, A115
- Vazza, F., & Brüggén, M. 2014, *MNRAS*, **437**, 2291
- Venturi, T., Giacintucci, S., Brunetti, G., et al. 2007, *A&A*, **463**, 937
- Venturi, T., Giacintucci, S., Dallacasa, D., et al. 2008, *A&A*, **484**, 327
- Williams, W. L., van Weeren, R. J., Röttgering, H. J. A., et al. 2016, *MNRAS*, **460**, 2385

Appendix A: Source-subtracted images

In this section we present the source-subtracted images and the region used to determine the radio halo flux densities reported in

Table 4 (solid yellow polygons). The positions of the subtracted compact sources are shown with a red cross.

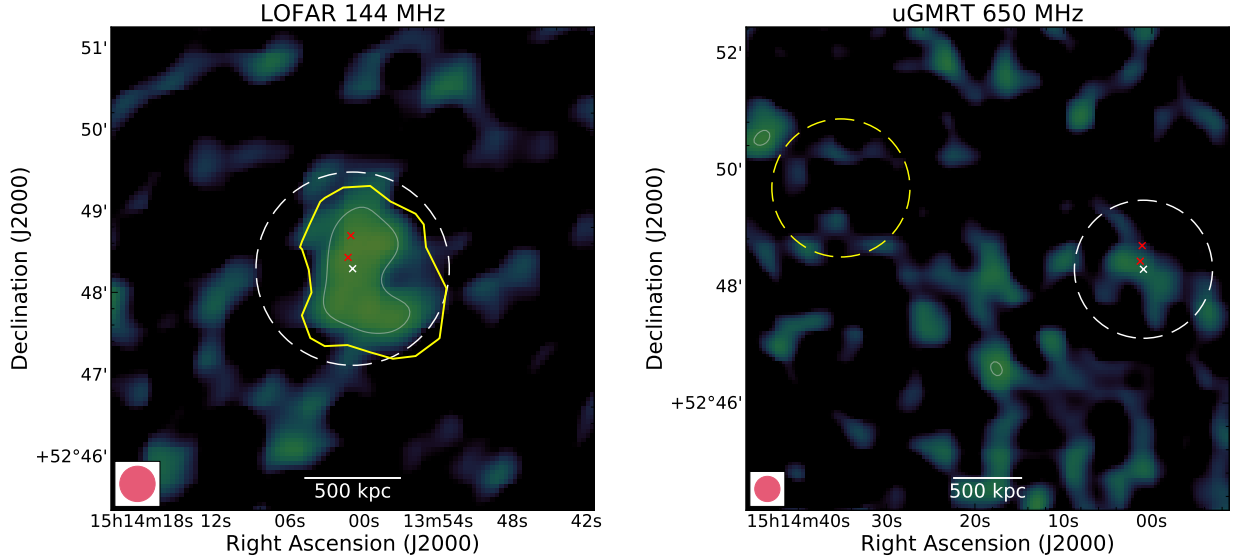


Fig. A.1. PSZ2 G086.93+53.18. 26''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left) and 650 MHz (right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 260 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},650} = 50 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region obtained from $M_{SZ,500}$, with the white cross showing the cluster centre, while the dashed yellow circle shows the position of the injected mock halo. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygon represents the area where the flux densities were measured.

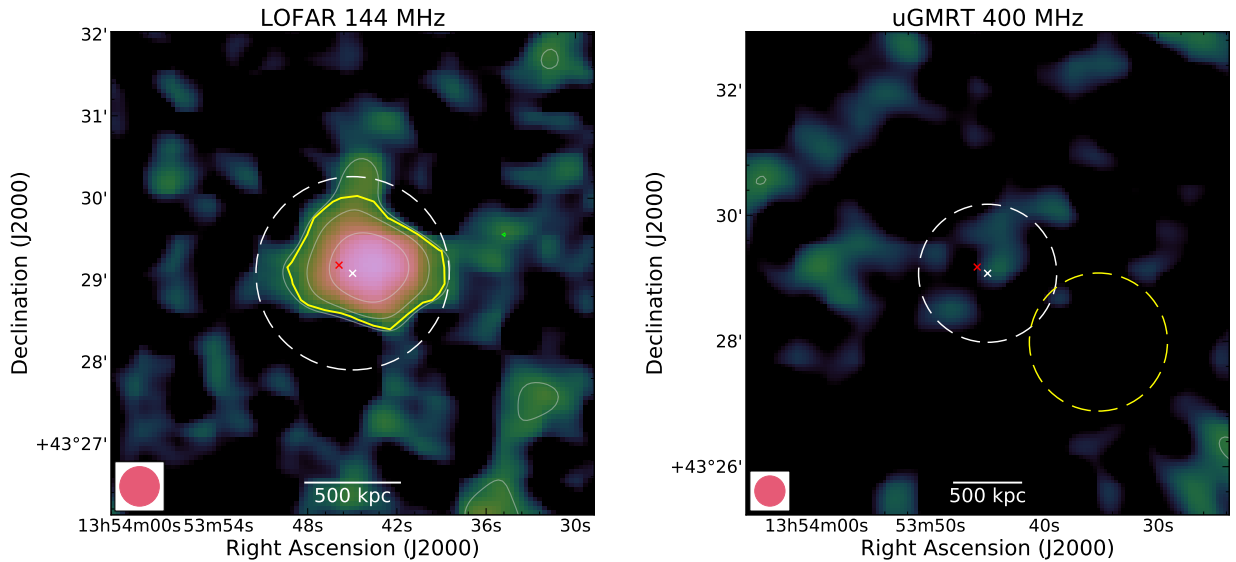


Fig. A.2. PSZ2 G089.39+69.36. 29''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left) and 650 MHz (right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 150 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},400} = 416 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region obtained from $M_{SZ,500}$, with the white cross showing the cluster centre, while the dashed yellow circle shows the position of the injected mock halo. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygon represents the area where the flux densities were measured.

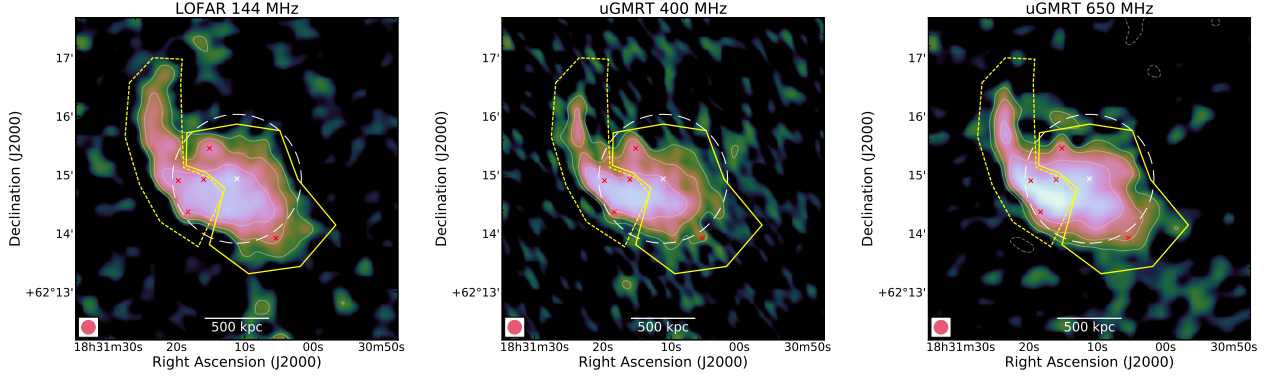


Fig. A.3. PSZ2 G091.83+26.11. 14''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left), 400 MHz (middle) and 650 MHz(right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 180 \mu\text{Jy beam}^{-1}$, $\sigma_{\text{rms},400} = 90 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},650} = 38 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the white cross showing the cluster centre. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygons represent the area where the flux densities were measured for the halo (solid) and the relic (dashed).

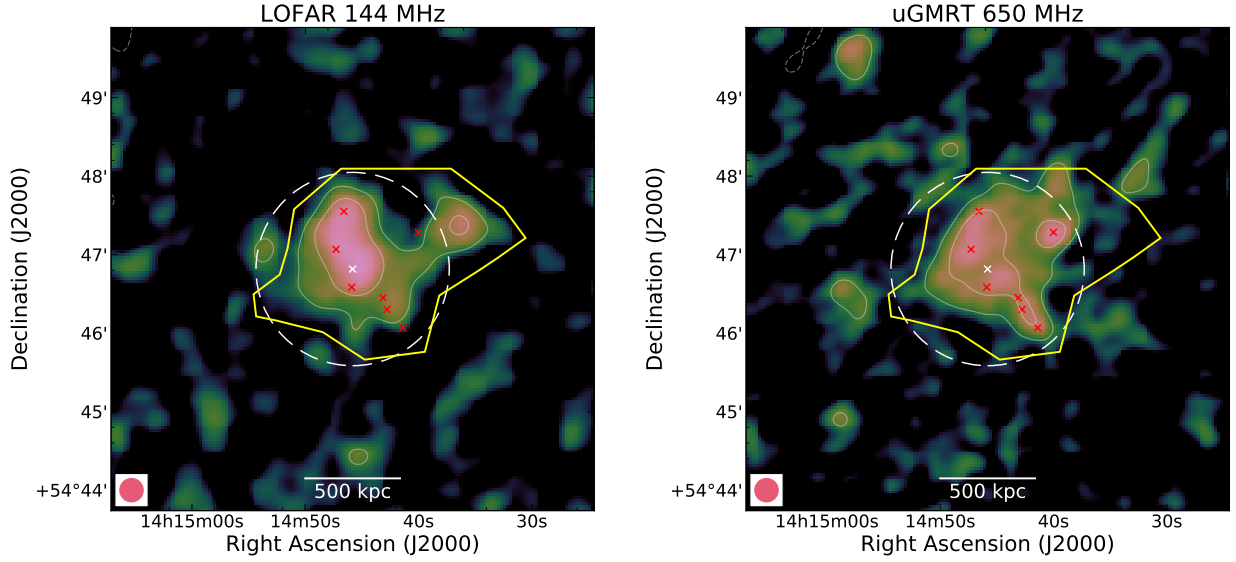


Fig. A.4. PSZ2 G099.86+58.45 18''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left) and 650 MHz(right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 140 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},650} = 32 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the white cross showing the cluster centre. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygon represents the area where the flux densities were measured.

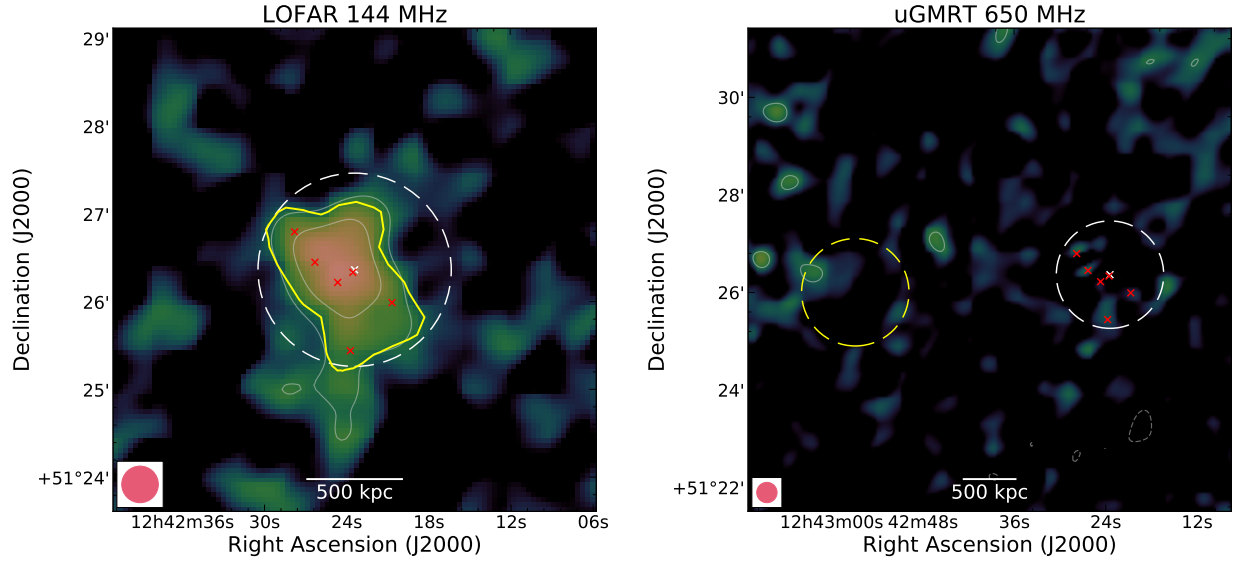


Fig. A.5. PSZ2 G126.28+65.62. 25''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left) and 650 MHz(right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 130 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},650} = 80 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region obtained from $M_{SZ,500}$, with the white cross showing the cluster centre, while the dashed yellow circle shows the position of the injected mock halo. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygon represents the area where the flux densities were measured.

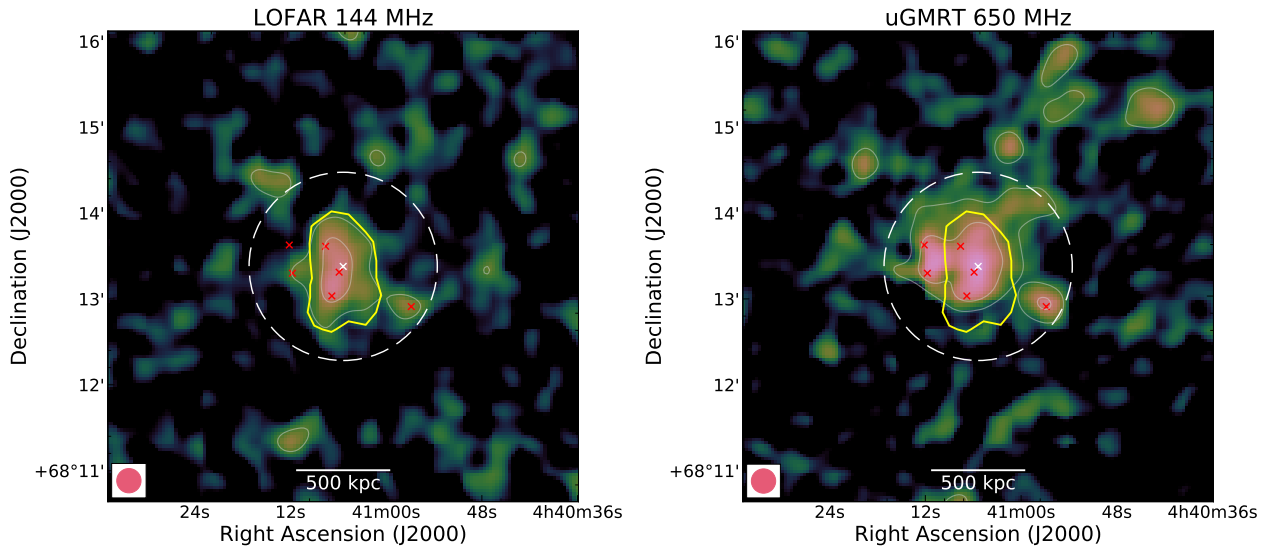


Fig. A.6. PSZ2 G141.77+14.19. 17''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left) and 650 MHz(right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 165 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},650} = 20 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region obtained from $M_{SZ,500}$, with the white cross showing the cluster centre. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygon represents the area where the flux densities were measured.

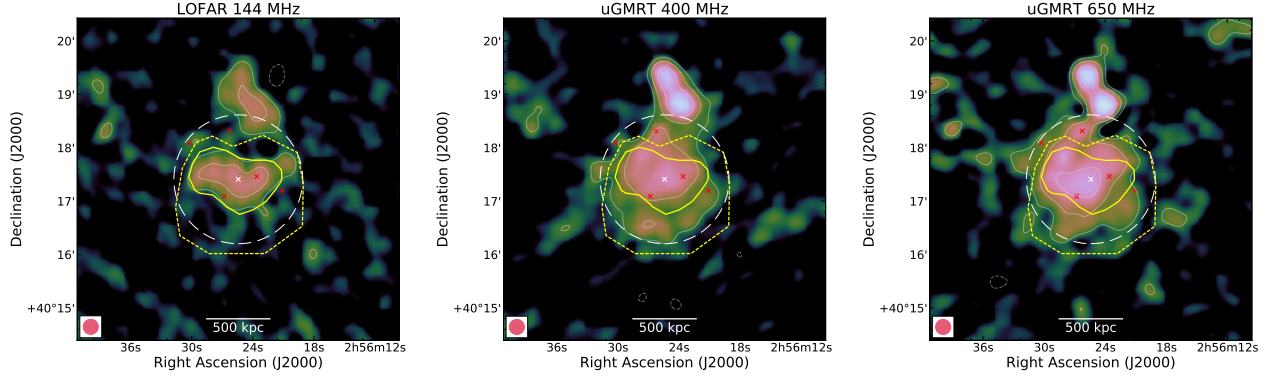


Fig. A.7. PLCK G147.3–16.6. 17''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left), 400 MHz (middle) and 650 MHz(right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 300 \mu\text{Jy beam}^{-1}$, $\sigma_{\text{rms},400} = 61 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},650} = 25 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the white cross showing the cluster centre. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow solid and dashed polygons represent the area where the flux densities were measured.

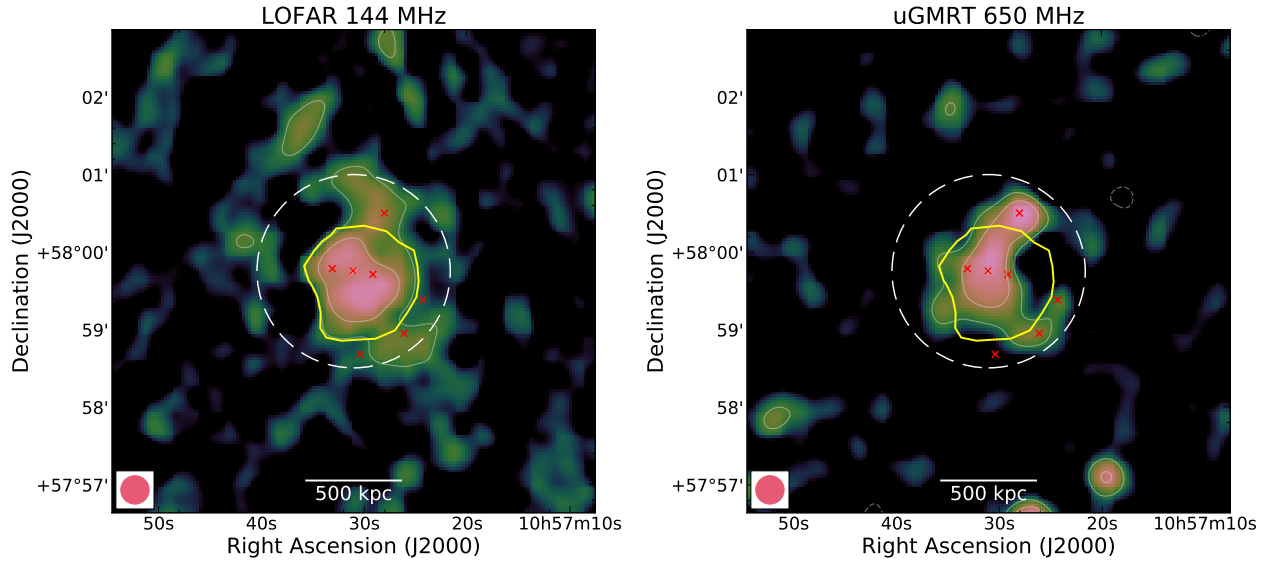


Fig. A.8. PS22 G147.88+53.24. 22''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left) and 650 MHz(right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with $\sigma_{\text{rms},144} = 140 \mu\text{Jy beam}^{-1}$ and $\sigma_{\text{rms},650} = 35 \mu\text{Jy beam}^{-1}$ the maps noise. The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{\text{SZ},500}$ region obtained from $M_{\text{SZ},500}$, with the white cross showing the cluster centre. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygon represents the area where the flux densities were measured.

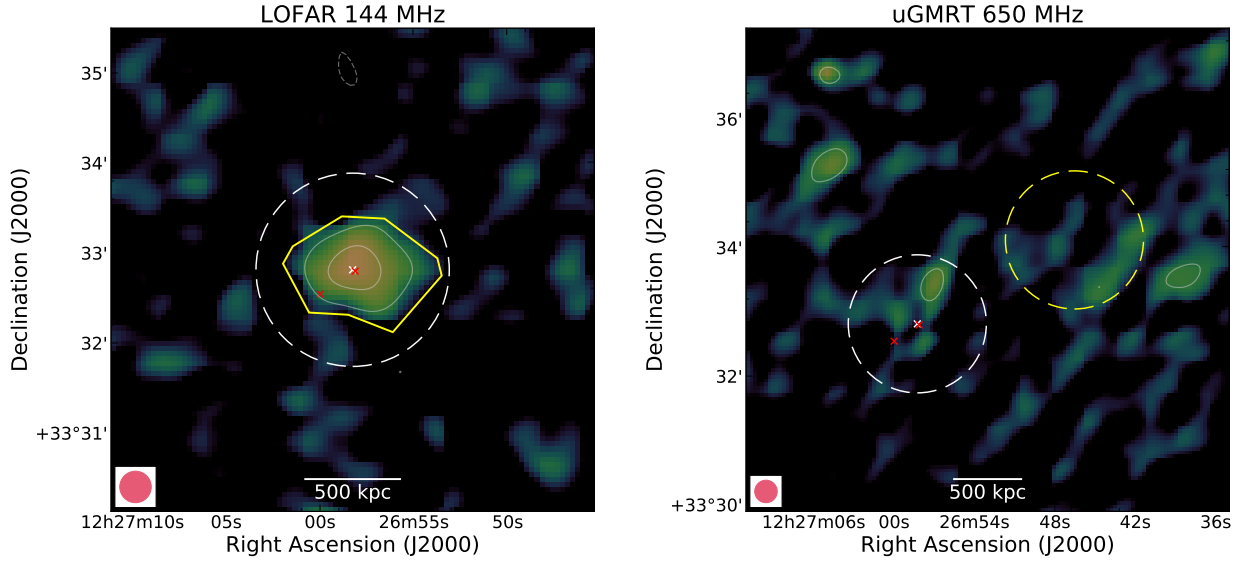


Fig. A.9. PS22 G160.83+81.66. 22''-resolution compact source-subtracted LOFAR and uGMRT images at 144 MHz (left) and 650 MHz (right). White-coloured radio contours at the same resolution are drawn at levels of $2.5\sigma_{\text{rms}} \times [-1, 1, 2, 4, 8, 16, 32]$, with σ_{rms} the noise map (see Table 3). The negative contour level is drawn with a dashed white line. The dashed white circle in each map shows the $R = 0.5R_{SZ,500}$ region obtained from $M_{SZ,500}$, with the white cross showing the cluster centre, while the dashed yellow circle shows the position of the injected mock halo. The positions of the subtracted sources in the cluster region are highlighted with red crosses. The yellow polygon represents the area where the flux densities were measured.

Appendix B: Optical–radio overlays for PSZ2 G091.83+26.11

Here we present the optical *irg* image of PSZ2 G091.83+26.11 taken from the PanSTARRS archive⁶ (Chambers et al. 2016). We

overlay the radio contours of the uGMRT 650 MHz image after removing the contribution of the halo emission in order to investigate possible optical counterparts that generate the radio emission of the candidate radio relic.

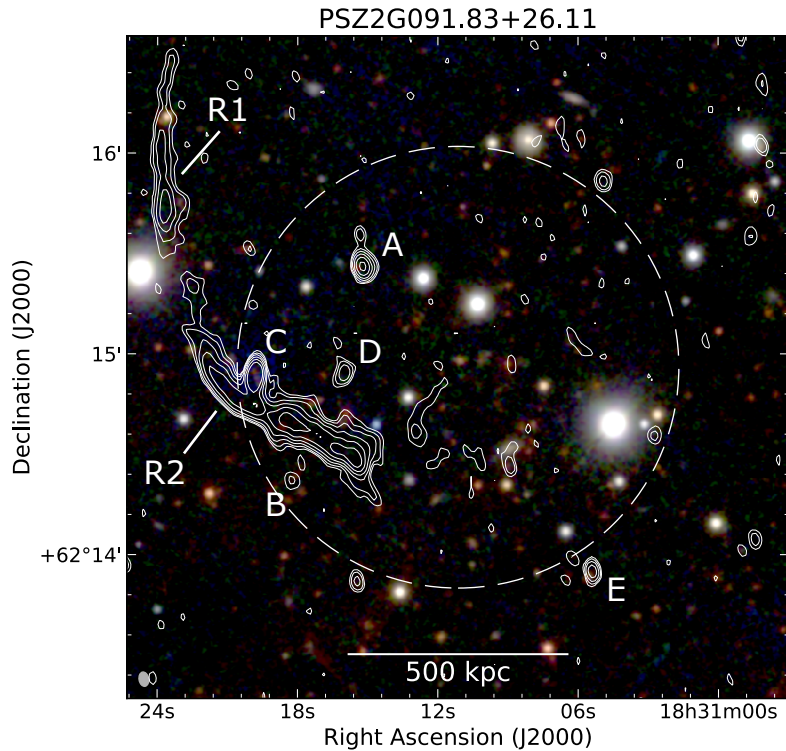


Fig. B.1. PanSTARRS optical *irg* image of PSZ2 G091.83+26.11. Radio contours at 650 MHz without the contribution of the radio halo (i.e. with the *uw*-cut at 500 kpc, see Sect. 2.3) are overlaid in white. The white dashed circle represents the R_{500} region. Labels follow Fig. 3.

⁶ <https://ps1images.stsci.edu/cgi-bin/ps1cutouts>