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Experimental investigation of the effect of moisture on the acoustic properties of lightweight substrates used in green envelopes

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Abstract

Substrates are used in green walls and roofs to supply air and water to the roots of the growing plants. These substrates are porous with micropores which store water and macropores which facilitate drainage and air entry. Effect of moisture on acoustic absorption is studied for two lightweight substrates: coir dust and perlite. Measurement of dry and moistened substrates are conducted to evaluate their effective speed of sound, attenuation, characteristic impedance, compressibility and density between 100 Hz and 1000 Hz using an impedance tube and the three microphone-two load method. Effect of moisture on these quantities is found to depend strongly upon the interaction between water and substrate particles at the microscale. Performance of rigid-frame and limp frame porous models is evaluated when applied to the characterization of dry and moistened lightweight substrates. Finally, sound absorption of substrate layers and composite plant-substrate samples is analyzed for different moisture contents.

Keywords: sound absorption, lightweight substrate, acoustic porous medium, moisture, green envelope

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1. Introduction

For several decades, growing environmental concern in urban areas has stimulated the development of green building envelopes with significant benefits on stormwater management [1], wildlife habitat [1], energy conservation [1, 2], air quality [1, 3], mitigation of urban heat island effect [1], and noise reduction [4]. In the latter case, in-situ measurements demonstrated that the main improvement comes from the increased absorption of sound when highly reflecting building materials are covered by green roofs [5, 6] and green walls [4]. Numerical simulations were also conducted to evaluate how propagation of traffic noise was affected by building enveloppe greening for different urban configurations [7, 8]. Laboratory experiments have shown that the main contribution 11 of this absorption comes from the substrate with a clear dependence to sub-12 strate composition [5, 9, 10, 11], geometry [5, 11, 12, 13] and moisture content [5, 9, 12].14

Substrates are porous materials containing both gas and liquid in order to supply water and air to the roots and achieve growth of plants. Water availability depends upon substrate composition and volume but varies also with plant 17 development and external environmental conditions [14]. The effect of moisture 18 or water content on the acoustic properties of soils (sandstones, clay...) such as airflow resistivity [15], ground impedance [16, 17, 18] speed of sound [19] and attenuation [19] has been widely studied. Long-term in-situ experimentations 21 were also conducted on green roofs incorporating relatively heavy substrates to 22 evaluate the variation of acoustic signal attenuation with substrate water con-23 tent. Van Renterghem and Bottledooren reported variations reaching 10 dB between dry substrate and moistened substrate close to saturation in the 250-1250 Hz frequency range [20]. Liu and Hornikx performed similar experiments for two roofs incorporating different substrates [21]. Correlation between change in 27 acoustic wave attenuation and substrate water content was observed for one roof and not for the other one. The fact that the porosity of the substrate was weakly dependent of water content was suggested to explain the absence of change for the latter case. Connelly and Hodgson [5] evaluated the absorption coefficient at normal incidence of nine different (heavy) substrates in an impedance tube at three levels of volumetric water content: oven-dry, wilting capacity and field capacity. They also observed a decrease of absorption coefficient with moisture content.

Some recent works have also addressed the effect of moisture on low density 36 substrates which are preferred for green walls to reduce total weight. Horoshenkov et al [9] measured in an impedance tube, the absorption coefficient at normal incidence of two dry and moistened substrates: a clay soil and a light substratum made of coir, perlite and polymer gel. In the 100-1500 Hz frequency range, absorption coefficient of clay soil dropped from 0.2-0.7 to 0.1-0.12 for 41 a relatively small amount of added water. For the light substratum, a much smaller decrease was observed from 0.8-0.9 to 0.6-0.75 at a larger moisture content and only above 300 Hz. Different porous models were used for clay soil and substratum in order to evaluate the variation of model parameters under moisture condition. Yang et al [12] measured the absorption coefficient of heavy 46 (topsoil) and light (mixture of coir, perlite and water-retaining polymer) substrate layers for different moisture contents. Average absorption coefficient was obtained in reverberant room for topsoil while absorption coefficient at normal 49 incidence was measured in impedance tube for the mixture. For all frequencies between 100 and 4000 Hz, absorption coefficient of topsoil was found to decrease 51 significantly with increasing moisture while those of the light substrate was increasing slightly. The purpose of this work is to analyze how moisture affects the effective acoustic properties of two different lightweight substrates and to 54 evaluate the consequences of these property changes on the acoustic absorption 55 of substrate and plant-substrate samples. Measurement of substrate effective 56 properties is carried out in an impedance tube using the three microphone-two loads method. The measurement method, which also provides sample absorption coefficient and surface impedance, as well as the considered lightweight 59 substrates, the preparation of the samples and their physical characterization are described in section 2. Measured physical and effective acoustic properties

of the three substrates, dry and moistened, are analyzed in section 3. Performance of rigid-frame and limp frame of porous models is considered in section 4 when applied to the characterization of dry and moistened lightweight substrates. The variation of normal incidence absorption coefficient with moisture contents discussed in section 4 for substrate single layers and in section 5 for composite plant-substrate samples.

68 2. Experimental procedure

9 2.1. Measurement method

Acoustic characterization of substrate samples is performed in an impedance tube (Fig.1) using the three-microphone two-load method [22]. A specific tube of large diameter (192 mm) is used to have a sample diameter significantly larger than the size of sample constituents (substrate particles, leaves).

Four loudspeakers (type Visaton FRS) are mounted in the PVC front disk located at the front end of the tube. A movable Teflon piston is positionned at the other end. A plastic sample holder contains the substrate maintained by two pieces of textile net. Acoustic pressure measurements are performed with three microphones (Sennheiser MKE 2P with 3.8 mm diameter). Two microphones are located in front of the sample respectively at 80 and 90 cm from the front end of the tube. The third microphone is located at the center of the movable piston behind the sample. The sound card (RME-Fireface 802) control inputs and outputs of the system. The excitation signal is a step by step sine. More details on experimental set-up may be found in reference [11]

Sample transfer matrix parameters are measured in the 100-1000 Hz frequency range. Assuming $e^{+j\omega t}$ time dependency where ω is the circular frequency and t the time, sample transfer matrix $T(\omega)$ relating acoustic pressures P and velocities V at x=0 and x=d is written as

$$\begin{bmatrix} P(0) \\ V(0) \end{bmatrix} = \begin{bmatrix} T_{11}(\omega) & T_{12}(\omega) \\ T_{21}(\omega) & T_{22}(\omega) \end{bmatrix} \begin{bmatrix} P(d) \\ V(d) \end{bmatrix}, \tag{1}$$

In the three-microphone two-load method, the transfer matrix is evaluated by using the three measured transfer functions between the microphones for two different sizes of the backing cavity [22]. Assuming that the sample may be described as an ideal homogeneous fluid medium, the transfer matrix is written as

$$\begin{bmatrix} T_{11}(\omega) & T_{12}(\omega) \\ T_{21}(\omega) & T_{22}(\omega) \end{bmatrix} = \begin{bmatrix} \cos(k(\omega)d) & jZ_c(\omega)\sin(k(\omega)d) \\ \frac{j\sin(k(\omega)d)}{Z_c(\omega)} & \cos(k(\omega)d) \end{bmatrix}, \tag{2}$$

where k and Z_c are the effective wave number and the characteristic impedance of the material constituting the sample. c is the effective speed of sound in the sample. k, Z_c and c are deduced from the transfer measured matrix using

$$k(\omega) = \frac{\arccos(T_{11}(\omega))}{d},\tag{3}$$

$$c(\omega) = \frac{\omega}{k(\omega)},\tag{4}$$

$$Z_c(\omega) = \sqrt{\frac{T_{12}(\omega)}{T_{21}(\omega)}}. (5)$$

As homogeneous samples are symmetric, T_{11} and T_{22} are equal in an homogeneous sample. Therefore, measured values of T_{11} and T_{22} may be compared to strengthen the hypothesis of homogeneity:

$$T_{11}(\omega) \approx T_{22}(\omega).$$
 (6)

Effective compressibility χ and density ρ are obtained using

$$\chi(\omega) = \frac{1}{c(\omega)Z_c(\omega)},\tag{7}$$

$$\rho(\omega) = \frac{Z_c(\omega)}{c(\omega)}.$$
 (8)

Finally, the absorption coefficient α and the specific impedance Z_s of the sample in rigid backing condition are obtained using

$$\alpha(\omega) = 1 - \left| \frac{T_{11}(\omega) - Z_0 T_{21}(\omega)}{T_{11}(\omega) + Z_0 T_{21}(\omega)} \right|^2, \tag{9}$$

$$Z_s(\omega) = \frac{T_{11}(\omega)}{T_{21}(\omega)},\tag{10}$$

where Z_0 is the characteristic impedance of air. More details on experimental set-up and measurement method may be found in reference [11]

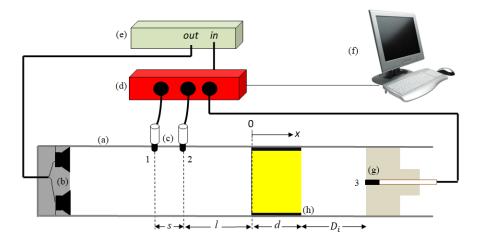


Figure 1: Schematic view of the experimental setup: (a) stainless steel tube; (b) cylindrical PVC disk integrating 4 loudspeakers; (c) microphones; (d) sound card; (e) amplifier; (f) computer; (g) flush mounted microphone on movable piston; (h) sample holder containing the sample.

2.2. Samples description, preparation and physical characterization

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High content of available water and adequate air supply are considered as the most important physical characteristics required for substrates in order to achieve optimal growth of plants. All substrates are composed of three phases: solid, aqueous and gaseous. The capacity of a substrate to store water and air and its ability to provide them to the plant are determined by its porosity characteristics [23, 24]. Water is mainly held by the micropore space of the

	Bulk density (dry) $(kg.m^{-3})$	Effective porosity (%)	Total water holding capacity (%)	Reference
Coir dust	40-80	85-89	73-80	[25]
	25-89	98-94	14-78	[26]
	60	91	64	[27]
Perlite	140	70	25	[27]
	170	66	54	[28]

Table 1: Properties of coir dust and perlite substrates

substrate, while rapid drainage and air entry is facilitated by the macropores 109 [25]. Therefore, an adequate distribution of large and small pores is essential 110 for a good medium. 111

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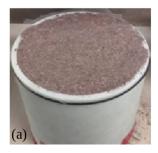
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Two different substrates having low bulk density, high water holding capac-112 ity and low suction are considered in this work: coir dust and perlite. Their microporosity corresponds to the internal porosity of their constituent particules and the macroporosity to the inter-particle porosity. Their main properties found in the literature are given in table 2. The bulk density of the substrate 116 is defined as its dry mass per unit of volume. The effective porosity is the ratio of the total volume of open pores to the total volume of the substrate. It can be 118 determined using a **porosimeter**. The storage of water in a growth substrate is 119 described by the water retention curve which relates volumetric water content 120 to water suction [23, 24]. Container capacity is reached in the **substrate** when 121 water stops draining following saturation. It is usually defined at a suction of 1 122 kPa. The total water holding capacity is the ratio of the total volume of water 123 held in substrate at container capacity to the total volume of substrate. As Young-Lapace equation states that capillary pressure is inversely proportional 125 to channel radius, it is usually admitted that water retention curve is essentially 126 the pore-size distribution curve [23].

Coir dust (Fig.2 (a)) is a residual waste of coir processing. The main part of coir dust is constituted by pithy tissue particles sizing between 1 and 4 mm for more than 90% of the particles [29]. Pithy tissue particles have an internal porosity of approximately 40% and exhibit round-shaped external pores (average diameter of 40 μ m) accounting for a relative surface porosity of about 40%

(Fig.3.(a)). Internal and surface porosities are interconnected. The high water storage capacity of coir dust is associated to high surface porosity and larger openings in coarse pithy tissue which facilitate the water penetration into the cells [28]. Remaining particles of larger size are short coir fibers. Coir dust properties differ significantly between sources (table 1). This variation is closely 137 related to the particle size distribution [30], substrates with smaller particles 138 exhibiting higher bulk density, smaller effective porosity and a larger proportion 139 of micropores.

Perlite is an amorphous aluminum silicate glassy volcanic rock which traps crystalline water into its mass. When heated above 900°C, entrapped water molecules turn to steam. Perlite expands up to 4-20 times of its original volume and become porous [31]. Expanded perlite (Fig.2(b)) is composed of millimetersize particles having a crystal-like porous and glassy structure with countless number of pores sizing from 20 to 100 μ m (Fig. 3(b)) [28, 32]. Properties of expanded perlite substrates also vary with particle size distribution [27, 28, 33]. Compared to coir dust substrates, expanded perlite substrates tend to have higher bulk density, lower effective porosity and lower total water holding capacity. Expanded perlite is used in hydroponics and green systems alone as a medium or as a soil amendment to retain moisture and lighten compact soils.



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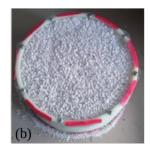
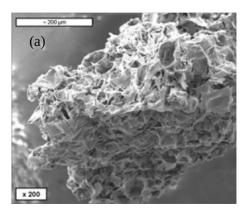




Figure 2: (a) Coir dust; (b) Perlite; (c) Japanese spindle.

Each substrate is dried in an oven at 130°C during 15 hours and then mixed with a controlled amount of water. Moisture content is defined as the ratio of the mass of added water to the mass of the dry substrate. Substrate and water



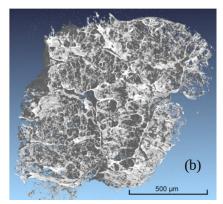


Figure 3: (a) Coir dust pithy tissue particle (image by scanning electron microscopy) from [29]; (b) microstructure of an expanded perlite particle (pseudo-image by computer micrography) from [32].

are mixed mechanically in order to homogeneize the distribution of water.

The dry or wet substrate is then placed in the 8 cm thick sample holder as evenly as possible and without compaction. Textile nets are stretched on the top and bottom ends of the sample holder to maintain the soil-air interfaces perpendicular to tube axis [17]. Acoustic measurements are made on four different substrate samples for each moisture content.

Additional characterizations of dry and wet substrates properties are also conducted. Density, effective porosity and airflow resistivity are directly measured using an electronic balance, a porosimeter and a resistivimeter. An inverse method is also used to determine the parameters of the porous model (porosity, airflow resistivity, tortuosity, viscous and thermal lengths) from absorption curves measured in an impedance tube. It relies on the minimization of a least square cost function between measurements and simulation with a Johnson Allard-Champoux [34, 35] or limp [36] porous models.

The plant considered in this work is Japanese spindle (Euonymus japonicus), a small shrub with oval leaves which are about 5 cm long and 3 cm wide (Fig. 2(c)). Plant samples have an air-filled porosity of 95% which is evaluated by dividing the total volume of the plant by the internal volume of the sample

holder. The volume of the plant is obtained by submerging branches and leaves in a graduated cylinder filled with water and measuring the water level variation. Plant samples are constituted by a set of small branches introduced in the sample holder. The foliage is disposed in the whole volume of the sample holder to obtain the most homogeneous distribution possible. Textile nets are added on the top and bottom of the sample holder to keep the air/plants interface perpendicular to tube axis and serve as reference surfaces.

3. Measurement of dry and wet substrates

3.1. Physical properties of substrates

Measurement are performed on three different samples for each substrate and 182 each moiture content. Average value and standard deviation of measured poros-183 ity ϕ , density ρ and airflow resistivity σ are reported in table 2 for perlite and 184 coir dust at different moisture contents τ . As airflow resistivity of coir dust with 185 15 % moisture content was found to be highly sensitive to the substrate-water 186 mixing process, results are reported for three different processes. Variations of 187 these quantities (normalized to their value at dry state) with respect moisture 188 content are displayed in Fig.4. Simulated variations of these quantities assum-189 ing a constant volume of the substrate are also reported. If the decrease of 190 porosity is due to the added volume of water, the theoretical porosity of the wet substrate is written as 192

$$\phi_{wet} = \phi_{dry} - \tau \frac{\rho_{dry}}{\rho_{water}},\tag{11}$$

193 If the increase of density is due to the added mass of water, the theoretical
194 density of the wet substrate is

$$\rho_{wet} = \rho_{dry}(1+\tau). \tag{12}$$

For perlite, the decrease of porosity is larger than expected from Eq.(11).

A possible mechanism would be the trapping of water at the surface of perlite

particles that could **obstruct** the micropores of the particule without occupying
their entire volume. The increase of measured density is correctly described
by Eq.(12) confirming that the volume of perlite substrate remains constant
when it is moistened. Measured airflow resistivity of perlite substrate is found
to decrease with moisture content contrary to previous mesurements on sand
showing an opposite effect [15, 17]

For coir dust, measured variations depend strongly upon considered mois-203 ture content range. For moisture content between 0 and 15 %, variations of porosity and density are correctly described by Eqs.(11) and (12). Airflow re-201 sistivity rises by 28 to 124 % with high sensitivity to substrate-water mixing 206 process. For moisture contents between 15 and 65 %, porosity and density stay 207 relatively constant despite the additional volume and mass of water brought to the substrate. This effect can be explained by the penetration of water in pithy tissue cells [29] which produces an increase of their volume and also of 210 volume of the whole sample. This observation is also consistent with the con-211 tinuous decrease of airflow resistivity as the pore size is assumed to increase 212 when particle size increases. It is possible that water also penetrates in pithy 213 tissue cells at moisture between 0 and 15 % with a different macroscopic effect. 214 Initially, expansion of pithy tissue particles could tend to diminish pore size be-215 fore reaching an equilibrium through contact forces with neighboring particles. 216 When moisture content keeps increasing, particles tend to expand and contact 217 forces generate an internal pressure and therefore an increase of sample volume. For a 200 % moisture content close to saturation, direction of variations 219 predicted by Eqs.(11) and (12) are recovered as porosity decreases and density 220 increases. Further decrease of airflow resistivity is also observed. 221

3.2. Effective acoustic properties of substrates

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Measurement of acoustic properties are performed on four different samples for each substrate and each moiture content. Average value and standard deviation are reported on Figure 5 to 8. Symmetry of the sample is also verified

Substrate	Moisture content	Porosity average	Porosity standard deviation (%)	Density average (kg.m ⁻³)	Density standard deviation (%)	Airflow resistivity average $(Ns.m^{-4})$	Airflow resistivity standard deviation (%)
Perlite	0	0,773	1,7	290,1	7,6	3562	11,1
	0,15	0,710	0,6	334,2	2,9	2663	8,1
	0,30	0,651	3,1	398,1	1,5	2038	4,5
Coir dust	0	0,920	0,2	133,6	2,3	39615	5,2
	0,15	0,899	0,7	152,5	4,1	50879	13,8
						67343	13,3
						88948	0,6
	0,30	0,900	0,2	148,2	0,6	46647	11,2
	0,65	0,886	1	147,6	0,6	25261	4,4
	2,00	0,804	1,3	234,8	7	13209	8,6

Table 2: Porosity, density and airflow resistivity of coir dust and perlite substrates measured at different moisture contents

by comparing measured values of T_{11} and T_{22} . As measured T_{11} and T_{22} are different above 500 Hz for coir dust sample at 15 % and 30 % moisture content effective properties are not evaluated at these frequencies and water contents.

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Measured spectra of effective speed of sound, attenuation, characteristic impedance, compressibility and density are reported in Figs. 5 to 8 for dry and moistened coir dust and perlite substrates between 100 and 1000 Hz. Frequency spectra of the real and imaginary parts of the effective speed of sound (Fig. 5) show that both substrates, wet or moistened, are dispersive. For dry substrates, effective speed of sound is lower than speed of sound of air and effective attenuation (Fig. 6) is higher than attenuation in air, the lower the speed of sound, the higher the attenuation. For frequencies varying between 100 and 1000 Hz, speed of sound and attenuation ranges measured on dry substrates are respectively 60-100 m.s⁻¹ and 4-30 m⁻¹ for coir dust, 70-135 m.s⁻¹ and 4-14 m⁻¹ for perlite. Different changes of effective properties with moisture content are observed depending on the considered substrate. In coir dust with 15 and 30% moisture contents, speed of sound drastically decreases to 40-60 m.s⁻¹ and attenuation strongly increases to 7-30 m⁻¹. Only very small change of these properties are observed when moisture content is increased from 15% and 30%. For a moisture content of 200%, real part of speed of sound and attenuation spectra are very close to those of dry coir dust. Imaginary part undergoes large oscillations with peaks at 270, 600 and 900 Hz.

Real part of effective characteristic impedance (Fig. 6) is also frequency-248 dependent and decreases with frequency for both substrates. Characteristic impedance of dry perlite, 1000-2000 $Pa \ s \ m^{-1}$, and dry coir dust, 1000-2500 250 $Pa\ s\ m^{-1}$ are much larger than air characteristic impedance. Different varia-251 tions with moisture content are observed according to the substrate. Compared 252 to the dry case, characteristic impedance of perlite decreases for all frequencies 253 with a 15% moisture content and then barely changes when increasing moisture content to 30%. For moistened coir dust, effective characteristic impedance 255 increases continuously with moisture content from 15 to 200 %. 256

Real and imaginary parts of effective compressibility and effective density are 257 displayed in Fig.7 and 8 respectively. For perlite, main changes with moisture are found for the real and imaginary parts of effective density which decreases by 25 to 50% in the whole frequency range. Real part of compressibility is 260 barely modified for a 15% moisture content but decreases by 7 to 30% for a 30% 261 moisture content. Coir dust exhibits a different behaviour under moisture condi-262 tions: for 15 or 30% moisture contents, the increase of real and imaginary parts 263 of effective density reaches 100% between 200 and 400 Hz and progressively diminishes at higher frequencies. For a 200% moisture content, a smaller increase 265 of the real part of effective density is observed at low frequency. Changes of 266 compressibility depend both on moisture level and frequency. The decrease of 267 the real part of effective compressibility is more pronounced near complete saturation while a larger increase of the magnitude of the imaginary part is obtained in the case of lower moisture contents. 270

3.3. Acoustic properties of substrate samples in rigid backing condition

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Two **independent** measurements of the acoustic absorption by dry and wet substrate samples are presented. The first one is based on transfer matrix measurements using the three microphone-two loads method and calculation of absorption coefficient and surface impedance using equations 9 and 10. The second one is carried out with a commercial impedance tube (diameter 100)

mm) according to the International Standard ISO 10534-2 [37]. Measurements are performed on substrates of the same origin and with the same preparation 278 process. However, they are made with different samples because experimental 279 set-ups are in different locations.

Absorption coefficient (measured with both methods) and surface impedance (measured with first method) are displayed in Fig.9 for 8 cm thick substrate samples in rigid backing conditions.

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For dry coir dust samples, absorption coefficient is found to be almost constant above 200 Hz, between 0.5 and 0.7, for both measurement methods (Figs. 285 9(a) and 9(b)). In the presence of moisture, only small variations of absorption 286 coefficient are observed with the first measurement method while the second one shows an absorption peak appearing progressively between 400 and 600 Hz with increasing moisture content. Attenuation remains high in the presence of moisture. Thickness resonances do not build up and a large mismatch is found 290 between air characteristic impedance and the surface impedance of the sample that remain almost constant in the whole frequency range (Fig. 9(c)). 292

For dry perlite, a peak appears in the absorption spectrum near 450 Hz 293 with an absorption coefficient approximately equal to 0.9 for the first method 294 (Fig.9(d)) and near 650 Hz with an absorption coefficient close to 1 for the sec-295 ond method (Fig.9(e)). In moistened perlite, this peak shifts up in frequency 296 due to the increase of speed of sound. It may be noted that acoustic absorp-297 tion remains close to 1 at resonance although attenuation drops in moistened perlite (Fig. 6(c)). This result is explained by the improved matching of surface impedance with air characteristic impedance near resonance (Fig.9(f)) which is 300 related to the decrease of the characteristic impedance in the presence of mois-301 ture (Fig. 6(d)). It may noted that radial effects could appear in the samples for 302 the considered frequency range due to the low speed of sound in perlite and coir 303 dust. Absorption coefficients measured by both methods could therefore differ because samples of different diameters are used [38].

⁵⁶ 4. Applicability of porous model

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In this section, the performance of two models of porous media, rigid-frame Johnson-Champoux-Allard model [34, 35], and limp frame model [36], is considered when applied to the characterization of dry and moistened coir dust and perlite substrates.

In ${\bf the}$ rigid-frame model, effective density and compressibility are written as

$$\rho_{rigid}(\omega) = \frac{\alpha_{\infty}\rho_0}{\phi} \left[1 - j \frac{\sigma\phi}{\omega\alpha_{\infty}\rho_0} \sqrt{1 + j \frac{4\alpha_{\infty}^2 \eta \rho_0 \omega}{\sigma^2 \Lambda^2 \phi^2}} \right], \tag{13}$$

$$\chi(\omega) = \frac{\gamma - (\gamma - 1) \left[1 - j \frac{8\kappa}{\omega \rho_0 C_p \Lambda'^2} \sqrt{1 + j \frac{\omega \rho_0 C_p \Lambda'^2}{16\kappa}} \right]^{-1}}{\frac{\gamma P_0}{\phi}}, \tag{14}$$

where γ is the heat capacity ratio, ρ_0 , η , C_p and κ are the density, the dynamic viscosity, the heat capacity and the heat conductivity of air, P_0 is the static pressure, ϕ , α_{∞} and σ are the open porosity, the high frequency limit of the tortuosity and the static air flow resistivity of the substrate, Λ and Λ' are the viscous and thermal characteristic lengths of the substrate. In **the** limp frame model, the effective density is modified to take into account the inertia added by the limp solid phase:

$$\rho_{limp}(\omega) = \frac{(\rho_s + \phi \rho_0)\rho_{rigid}(\omega) - \rho_0^2}{(\rho_s + \phi \rho_0) + \rho_{rigid}(\omega) - 2\rho_0}$$
(15)

Model parameters are evaluated for each substrate and each moisture content using an iterative optimization process which minimizes for each measurement the error between the measured absorption coefficient spectrum (Fig.9(b) or 9(c)) and the calculated one with rigid-frame or limp frame model. A genetic algorithm is used on ten different starting populations in order to verify its convergence. For perlite, similar results are obtained with rigid-frame and limp frame models. Best results for coir dust are obtained with limp frame model. Final parameters are reported in table 3 for coir dust and table 4 for perlite. Effective density and compressibility simulated with these parameters are displayed in Fig.9 and 10.

Variation of coir dust parameters obtained for different samples of the same substrate and same moisture content do not exceed 7 % excepted for thermal 329 length at a moisture content of 30 %. Calculated porosities agree with mea-330 surements made with the porosimeter excepted for a 200 % moisture content. 331 Calculated airflow resistivities are smaller than those measured with the **flow** 332 resistivity meter. In particular, the increase of resistivity measured with 333 the resistivimeter for a moisture content of 15 % (table 2 and Fig.4(c)) is not 334 found. The monotoneous decrease of resistivity with moisture content above 335 15 % is consistent with previous measurements. Calculated effective densities 336 (Fig. 10(a) and 10(b)) exhibit variations with moisture content of the same order of magnitude than the measured ones (Figs. 8(a) and 8(b)). However, the fine evolution is not correctly described. Differences on real part of density 339 for moisture contents of 15 and 30 % can originate from the high sensitivity of 340 substrate resistivity to substrate-water mixing process mentionned previously. 343 Calculated imaginary parts of density are also very different from measured ones 342 at moisture contents of 0 % and 200 %. Real parts of calculated effective compressibility (Fig.10(c)) are slightly overestimated and their decrease between 344 low (0 to 30%) and high (200%) moisture contents is correctly described. 345

Perlite parameters display larger variations between samples than that of coir dust in particular for airflow resistivity. Calculated porosities are much lower than measured ones with the porosimeter at any moisture content. Calculated airflow resistivities decrease with increasing moisture contents contrary to the values measured with the resistivimeter. Calculated effective densities (Fig. 12(a) and 12(b)) are the same order of magnitude than the measured ones (Figs. 8(c) and 8(d)). The largest calculated densities (real and imaginary parts) are obtained for a moisture content of 30 % whereas the largest measured densities correspond to dry perlite. Calculated real parts of effective compressibility (Fig. 12(c)) display similar orders of magnitude and similar decrease with moisture contents. However, the model predicts constant **compressibilities** value in

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au		φ	$\sigma \ (N.s.m^{-4})$	α_{∞}	Λ (m^{-1})	$\Lambda^{'}$ (m^{-1})
0	average	0.62	1371	1.79	$1.94.10^{-4}$	$3.35.10^{-4}$
	variation	< 0.01	531	< 0.01	$0.07.10^{-4}$	$0.15.10^{-4}$
0.15	average	0.54	1477	1.53	$2.10.10^{-4}$	$3.52.10^{-4}$
	variation	0.04	917	0.07	$0.30.10^{-4}$	$0.25.10^{-4}$
0.30	average	0.28	2402	1	$1.43.10^{-4}$	$3.15.10^{-4}$
	variation	< 0.01	649	< 0.01	$0.01.10^{-4}$	$0.03.10^{-4}$

Table 3: Parameters of rigid-frame Johnson-Champoux-Allard model of dry and moistened perlite substrates.

au		ϕ	σ	α_{∞}	Λ	$\Lambda^{'}$
0	average	0.89	32316	1.02	$1.04.10^{-5}$	$4.98.10^{-5}$
	variation	0.01	65	0.01	$0.01.10^{-5}$	$0.1.10^{-5}$
0.15	average	0.82	22273	1.04	$7.98.10^{-6}$	$5.03.10^{-5}$
	variation	< 0.01	134	< 0.01	$0.15.10^{-5}$	$0.24.10^{-5}$
0.3	average	0.98	29551	1.03	$1.42.10^{-5}$	$2.26.10^{-4}$
	variation	0.02	148	< 0.01	$0.05.10^{-5}$	$0.75.10^{-4}$
2	average	0.6	5730	1.17	$9.26.10^{-5}$	$2.39.10^{-4}$
	variation	< 0.01	395	< 0.01	$0.19.10^{-5}$	$0.06.10^{-4}$

Table 4: Parameters of limp frame model of dry and moistened coir dust substrates.

the considered frequency range whereas measurements display an increase of compressibility with frequency.

5. Effect of moisture content on the acoustic properties of green envelopes

To evaluate the impact of moisture content on the acoustic performance of a green envelope, simulations are conducted on a composite sample composed of a 8 cm thick layer of spindle (95% porosity) atop a 8 cm thick layer of substrate using two methods: 1) transfer matrix method using effective properties obtained

experimentally for dry and moistened substrates and for plants [11]; 2) transfer matrix method using porous model for substrates and effective properties ob-366 tained experimentally for plants. Variation of absorption coefficient and surface impedance with moisture contents for plant-perlite and plant-coir dust composite samples are displayed in Figs. 12 and 13 for both calculation methods. For a 369 composite sample with dry perlite, an acoustic absorption coefficient above 0.95 370 is obtained between 400 and 1000 Hz (Fig. 12(c)). High absorption coefficient 371 and broad band of absorption may be attributed to both quarter-wavelength 372 thickness resonance of the envelope and the impedance matching provided by 373 the plant layer which acts as a quarter-wavelength transformer between the air 374 and the substrate [11]. For moisture contents of 15 or 30%, a slight degradation 375 of absorption band is found with model 1 between 300 and 900 Hz due to the 376 lower attenuation and the higher characteristic impedance of moistened perlite that detunes the matching effect provided by the plant layer. Slight variations 378 of absorption coefficient are also predicted when using rigid-frame porous model 379 2 but with better absorption for 15 % moisture content than for dry perlite. The 380 main differences between the models are observed on surface impedance below 38: 500 Hz. 382

For a composite sample with dry coir dust, an acoustic absorption coefficient 383 above 0.8 is obtained between 200 and 1000 Hz (Fig. 12(a)) with both models. 384 For moistened coir dust, the absorption coefficient calculated with model 1 is 385 degraded between 150 and 700 Hz for any moisture contents. The lower speed of sound in moistened coir dust shifts down below 100 Hz the quarter-wavelength thickness resonance of the envelope. Therefore, an anti-resonance peak appears 388 near 200 Hz and the impedance mismatch between air characteristic impedance 389 and envelope surface impedance increases (Fig. 12(b)). A much more limited 390 shift of thickness resonance is obtained with limp frame porous model 2 with 391 smaller changes in acoustic absorption for moisture contents of 15 and 30 %. Again, the main differences between the models concern the surface impedance 393 below 400 Hz. 394

95 Summary and conclusion

Different variations of effective density and compressibility with moisture 396 content are measured for the two considered substrates. In perlite, a sharp drop 397 of real and imaginary parts of density and a slight decrease of real part of com-398 pressibility with some oscillations are observed in the presence of moisture. Coir dust exhibits a much more complex behaviour. Real and imaginary parts of its 400 effective density increase at low moisture contents. At high moisture content, 401 real part of density decreases (at a value that remains higher than the value for 402 dry coir dust) and the imaginary part of density remains stable. For effective 403 compressibility, real part decreases monotonously with increasing moisture content while imaginary part strongly increases for low moisture content and then 405 decreases (at a value that remains higher than the value for dry coir dust) at 406 high moisture content. In addition, large oscillations with frequency of real and 407 imaginary parts of density and imaginary part of compressibility are observed 408 in moistened coir dust. These different variations may be analyzed using complementary measurements of dry and moistened substrate porosity, density and 410 the knowledge of perlite and coir dust particles microstructure. Perlite particles 411 are stiff and can only trap water in their micropores. On the contrary, pithy 412 tissue particles constituting most of coir dust substrate are soft and can store 413 water into their cells. Therefore, coir dust particles constitute a soft frame and 414 have a volume which tends to increase with moisture content. 415 Two different porous models are considered to predict properties of these lightweight 416 substrates: rigid-frame Johnson-Champoux-Allard model for perlite and limp 417 frame for coir dust. Estimation of model parameters is difficult in the case of 418 perlite. Large differences are found between measured static values of porosity 419 and airflow resistivity and values of these parameters issued from an optimiza-420 tion process using a measured acoustic absorption spectrum. Consequently, 421 422 rigid-frame model fails to predict the variations of effective density with moisture content. For coir dust, variation of real parts of density and compressibility 423 with moisture content is well captured by the limp frame model qualitatively. 424

Some differences remains on the imaginary part of density for dry coir dust and moistened coir dust with a 200% content. In addition, the low speed of sound of 426 the considered substrates, 40-100 ms-1 for coir dust and 80-220 ms-1 for perlite, questions the validity of plane-wave hypothesis used in the models. Differences 428 between absorption coefficient of the same substrate and moisture content mea-429 sured with impedance tube of different diameters could be explained by radial 430 effects. 431 Finally, simulations of plant-substrate envelopes designed to have a high and broadband acoustic absorption in dry condition show that moisture tends to 433 reduce absorption coefficient as reported in previous works [3, 5, 7, 8, 10]. This 434 degradation of absorption spectrum has different origins according to the con-435 sidered substrate: a lower attenuation and a higher characteristic impedance of the substate in the case of moistened perlite; a lower speed of sound of the substrate that shifts down the first absorption peak below 100 Hz in the case 438 of moistened coir dust. The considered porous models evaluate correctly the 439 measured absorption spectrum of plant-subtrate envelopes in dry condition. 440 However, they failed to estimate their surface impedance spectrum below 500 Hz and the changes of their absorption coefficient due to moisture.

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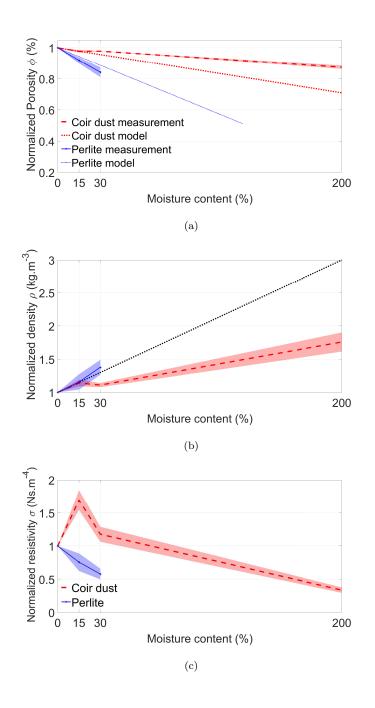


Figure 4: Variation of coir dust and perlite physical parameter with moisture content: (a) normalized porosity, (b) normalized density, (c) normalized airflow resistivity

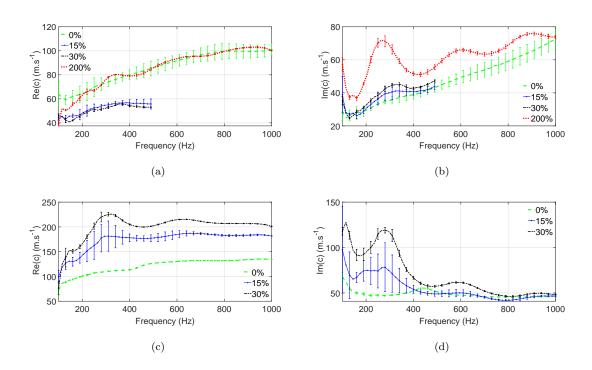


Figure 5: Measured real and imaginary parts of effective speed of sound of substrates for moisture contents varying between 0 and 30% or 200%. Coir dust: (a) and (b) and Perlite (c) and (d). Full line: average value; error bars: standard deviation.

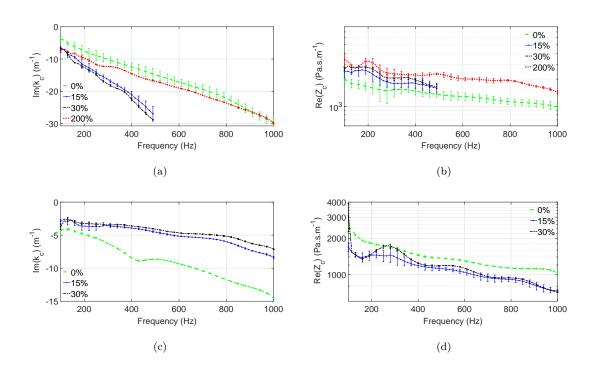


Figure 6: Measured effective attenuation and real part of characteristic impedance of substrates for moisture contents varying between 0 and 30% or 200%. Coir dust: (a) and (b). Perlite: (c) and (d). Full line: average value; error bars: standard deviation.

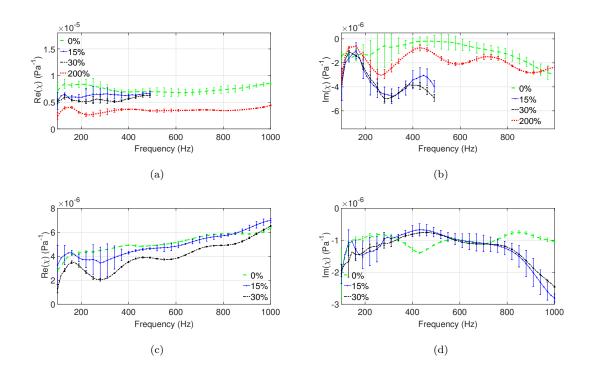


Figure 7: Measured effective real and imaginary parts of substrates compressibility for moisture contents varying between 0 and 30% or 200%. Coir dust: (a) and (b). Perlite: (c) and (d). Full line: average value; error bars: standard deviation.

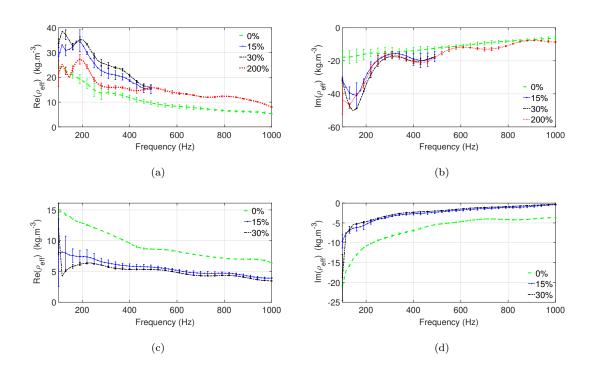


Figure 8: Measured effective real and imaginary parts of substrates density for moisture contents varying between 0 and 30% or 200%. Coir dust: (a) and (b).Perlite: (c) and (d). Full line: average value; error bars: standard deviation.

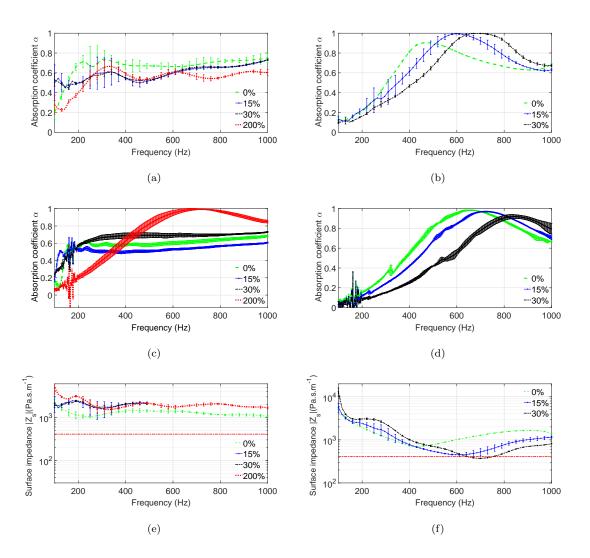


Figure 9: Measured absorption coefficients and surface impedance of 8 cm thick substrate samples for different moisture contents. Absorption coefficient measured with first method: (a) coir dust, (b) perlite. Absorption coefficient measured with second method: (c) coir dust, (d) perlite. Surface impedance measured with first method: (c) coir dust, (f) perlite. Full line: average value; error bars: standard deviation

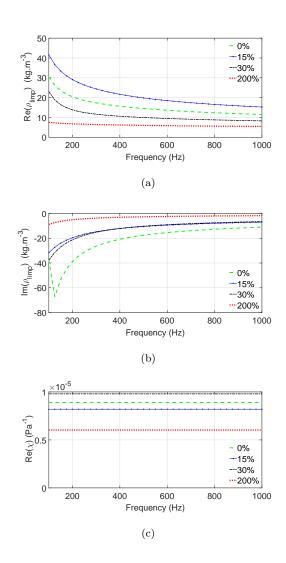


Figure 10: Effective density and compressibility of dry and moistened coir dust calculated using limp frame model. Density: real part (a); imaginary part (b). Compressibility: real part (c); imaginary part negligible (not drawn).

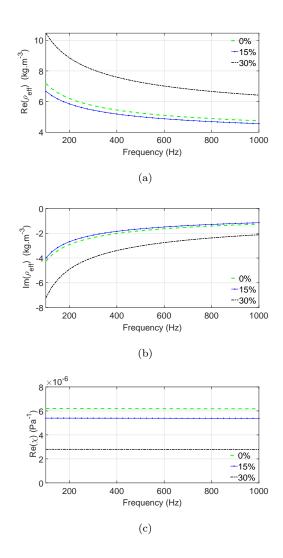


Figure 11: Effective density and compressibility of dry and moistened perlite calculated using rigid-frame model. Density: real part (a); imaginary part (b). Compressibility: real part (c); imaginary part negligible (not drawn).

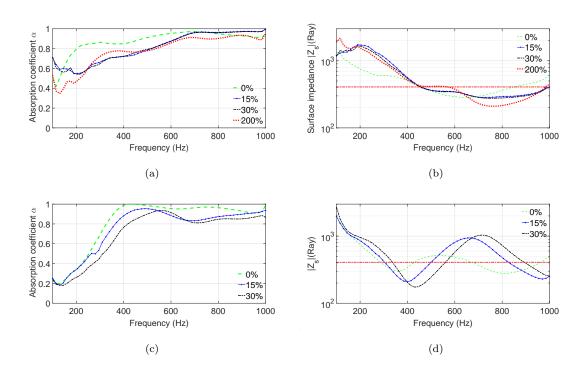


Figure 12: Absorption coefficient and surface impedance of composite samples (8 cm thick plant atop 8cm thick substrate) calculated with method 1 for different moisture contents . Coir dust: (a) and (b). Perlite: (c) and (d).

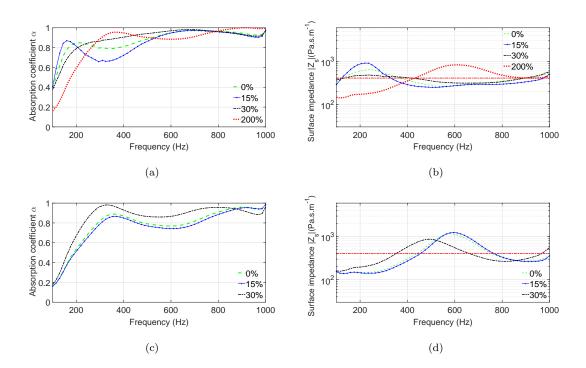


Figure 13: Absorption coefficient and surface impedance of composite samples (8 cm thick plant atop 8 cm thick substrate) calculated with method 2 for different moisture contents. Coir dust: (a) and (b). Perlite: (c) and (d).