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Expected evolution of disk wind properties along an X-ray binary outburst

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ABSTRACT

Blueshifted X-ray absorption lines (preferentially from Fe XXV and Fe XXVI present in the 6–8 keV range) indicating the presence of massive hot disk winds in black hole (BH) X-ray binaries (XrB) are most generally observed during soft states. It has been recently suggested that the nondetection of such hot signatures in hard states could be due to the thermal instability of the wind in the ionization domain consistent with Fe XXV and Fe XXVI. Studying the wind thermal stability does require, however, a very good knowledge of the spectral shape of the ionizing spectral energy distribution (SED). In this paper, we discuss the expected evolution of the disk wind properties during an entire outburst by using the RXTE observations of GX 339-4 during its 2010–2011 outburst. While GX 339-4 never showed signatures of a hot wind in the X-rays, the dataset used is optimal for the analysis shown in this study. We computed the corresponding stability curves of the wind using the SED obtained with the jet-emitting disk model. We show that the disk wind can transit from stable to unstable states for Fe XXV and Fe XXVI ions on a day timescale. While the absence of wind absorption features in hard states could be explained by this instability, their presence in soft states seems to require changes in the wind properties (e.g., density) during the spectral transitions between hard and soft states. We propose that these changes could be partly due to the variation of the heating power release at the accretion disk surface through irradiation by the central X-ray source. The evolution of the disk wind properties discussed in this paper could be confirmed through the daily monitoring of the spectral transition of a high-inclination BH XrB.

Key words. X-rays: binaries – accretion, accretion disks – magnetohydrodynamics (MHD)

1. Introduction

Low mass X-ray binaries (XrB) are binary systems containing a main sequence star and a compact object (neutron star or black hole). Due to Roche lobe overflow, the matter is pulled off from the star and forms an accretion disk around the compact object (see Tauris & van den Heuvel 2006 for a review). XrBs spend most of their time in a quiescent state at very low mass accretion rates. Occasionally, they come out of the quiescent state and undergo outbursts that last from a few months to a year, during which their flux rises by several orders of magnitude across the whole electromagnetic spectrum (e.g., Remillard & McClintock 2006). This release of gravitational power is believed to result from disk instabilities in the outer part of the accretion flow, driven by the ionization of hydrogen above a critical temperature (e.g., Meyer & Meyer-Hofmeister 1981; Smak 1984; Hameury 2020 for a recent review).

During the outburst, XrBs exhibit a large panel of spectral and timing properties. Black hole (BH) XrB (which are the one we are interested in this paper and labeled BH XrB or simply XrB in the following) can be easily distinguished in the so-called hardness-intensity diagram (HID) where the X-ray luminosity is plotted against the hardness ratio of the X-ray spectrum, producing a hysteresis with a typical Q-shaped track. All BH XrBs generally follow the same spectral evolution (e.g., Homan & Belloni 2005; Dunn et al. 2010, and see Remillard & McClintock 2006 or Done et al. 2007 for reviews). At the beginning and end of the outburst, the system is in the so-called hard state. During this state, the X-ray spectrum has a hard power-law shape up to a few tens of keV, which is a signature of nonthermal processes in a very hot, optically thin, plasma (the so-called corona). The radio emission observed in this state, which extends up to the infrared (IR), is believed to be entirely produced by a steady jet. During the middle part of the outburst, the system is in the so-called soft state where the spectrum is dominated by a bump in the soft X-rays (<2 keV) commonly interpreted as the thermal emission from the inner region (close to the innermost stable circular orbit, hereafter ISCO) of an optically thick accretion disk. In this state, the radio and IR emission is strongly reduced (e.g., Coriat et al. 2009) and even undetectable in most cases, suggesting the disappearance (or strong fading) of the jet component. In between these two main states, the system transitions within a few days through the so-called (hard and soft) intermediate states. The spectral shape evolves from hard to soft in the
first part of the outburst and then from soft to hard at the end of the outburst before turning back to the quiescent state (e.g., Remillard & McClintock 2006; Done et al. 2007).

In the last 15 years, it has been realized that, while soft states do not show signatures of a jet, the presence of blue shifted absorption lines, generally from Fe XXV and Fe XXVI, indicates the existence of massive hot disk winds (see Díaz Trigo & Boirin 2016 and Ponti et al. 2016 for recent reviews). While not detected in the hard states, these winds are generally present in the soft states of inclined systems (e.g., Ponti et al. 2012). But the picture is certainly more complicated than a simple on-off wind process between spectral states (e.g., Muñoz-Darias et al. 2016; Homan et al. 2016; Sánchez-Sierras & Muñoz-Darias 2020), and recent results during the (hard and soft) intermediate states show a large variety of wind properties and signatures (Miller et al. 2008b; Kallman et al. 2009; Rahoui et al. 2014; Neilsen et al. 2016; Shidatsu et al. 2016; Muñoz-Darias et al. 2017; Mata Sánchez et al. 2018; Gauzzi et al. 2019). The physical processes at the origin of these disk winds are not completely understood, but observations favored thermal or magnetic driving (or a combination of the two) as the most probable launching mechanisms (e.g., Díaz Trigo & Boirin 2016; Tetarenko et al. 2018b). The dependence of the wind detection with the spectral state of the X-ray source is, however, not straightforward. Indeed, assuming that the outflow velocity is on the order of the escape velocity of the absorbing material, the observed blue-shifts generally put the absorbing wind at up to a few or hundreds of thousand of gravitational radii away from the X-ray emitting region located close to the black hole (Schulz & Brandt 2002; Ueda et al. 2004; Kubota et al. 2007; Miller et al. 2008a; Kallman et al. 2009). In XRBs, such distances correspond to the outer part of the accretion disk. This connection between the inner and outer part of the accretion flow cannot occur on accretion (i.e., viscous) timescale since it is expected to be on the order of several weeks to months, that is to say the typical duration of the observed outbursts. This is much longer than the duration of a few days for a typical transition between a hard (windless) state to a soft (windy) state (e.g., Dunn et al. 2010). To explain the observations, the communication between the X-ray corona and the wind must, therefore, be much faster than the accretion timescale. It has been pointed out that over-ionization, as a consequence of the much harder illuminating spectral energy distribution during hard states might play a role (see e.g., Shidatsu & Done 2019), but in several instances it may not be sufficient (e.g., Neilsen & Homan 2012; Ponti et al. 2015).

It has been recently understood that the spectral state of the central source has a huge impact on the thermal stability of the wind and its ionization state (Chakravorty et al. 2013, 2016; Bianchi et al. 2017; Higginbottom et al. 2020). While illuminated by a soft state spectrum, the wind is always thermally stable regardless of its ionization parameter. When the spectrum is hard, however, large parts of the stability curve are thermally unstable, in particular in the ionization domain required for the production of Fe XXV and Fe XXVI ions. The timescale for the thermal instability to take place depends on the cooling timescale of the gas and, for the expected wind density (see Sect. 2), is expected to be quite fast (<day, see e.g., Gonzáles et al. 2007; Bianchi et al. 2017). These arguments support the importance of the thermal instability process in the changes of the wind ionization state (but see Sect. 2.2 for potential caveats). In this context, the disk wind could be present at all times (as recently suggested by the observation of near-IR emission lines all along the outburst of the black hole transient MAXI J1820+070, Sánchez-Sierras & Muñoz-Darias 2020), but it is detectable only in the soft state, when the relevant (for Fe XXV and Fe XXVI) range of the ionization parameter corresponds to stable thermal equilibrium.

Stability curves are very useful to study, more precisely, the role of thermal stability on the wind properties. They represent the photoionization equilibrium states of a plasma illuminated by a broad band spectral energy distribution (SED). The computation of these stability curves is, however, very sensitive to the spectral shape of the illuminating SED (e.g., Chakravorty et al. 2013; Bianchi et al. 2017). The precise study of the wind thermal stability during an outburst, and especially during the spectral transitions, then requires knowledge of the spectrum in the broadest energy range possible. However, Galactic hydrogen absorbs the soft X-rays (<0.1 keV) and instrumental limitations prevent access to a precise spectra for hard X-rays (>50 keV). With the typical 0.5–10 keV energy range (from e.g., Chandra or XMM), extrapolating from phenomenological models is hazardous and could lead to unphysical broad band spectral shapes and, consequently, erroneous stability curves. With the lack of daily broad band monitoring of XRB, the best alternative is the use of physically motivated models to obtain reasonable extrapolations where the data are missing.

This is the purpose of the present paper. We discuss the expected evolution of the disk wind properties of an XRB by using the detailed observations of the most famous (and thus best monitored) one, that is to say GX 339-4. No wind signature has been detected in this object potentially due to the low inclination of our line-of-sight (Ponti et al. 2012, but see Miller et al. 2015 for the marginal detection of He-like Fe XXV and H-like Fe XXVI emission lines during a high and soft state of this source, which are potential signatures of a wind). Even if GX 339-4 is not the prototype of a windy XRB, we believe that its spectral behavior along an outburst is representative of the one followed by any XRB. As a consequence, its SED can be used to trace the expected evolution of the stability curve of a windy source. GX 339-4 entered several times in outburst in the last 20 years and for which a large amount of data exist (see e.g., the WATCHDOG all-sky database Tetarenko et al. 2016). Its 2010–2011 outburst for example was very well followed in X-rays and radio. It was observed by RXTE for more than 400 days with almost one observation every day. Marcel et al. (2019) recently reproduced the spectral shapes of each observation during the entire outburst with the jet-emitting disk (JED) model (Ferreira et al. 2006; Marcel et al. 2018b,a). The corresponding best-fit SEDs are well constrained by the RXTE/PCA observations. While model dependent, they are however physically motivated and give consistent extrapolations outside the energy window of RXTE. We thus made the choice to use these SEDs to compute the wind stability curves and follow their evolution day by day, keeping in mind however their model-dependency. Assuming GX 339-4 is a typical XRB, this evolution of the stability curves is expected to be quite generic for all XRBs. Moreover, the very good sampling of the hard-to-soft transition of the 2010–2011 outburst of GX 339-4 is optimal for the analysis shown in the present study. None of the sources which show absorption lines in their spectra have coverage that is as extensive of SEDs as a function of state evolution.

\footnote{For an $a$-disk (Shakura & Sunyaev 1973) around a 10 solar-mass black hole characterized by a disk aspect ratio $H/R$, with $H$ being the height of the disk at the radius $R = r_{\text{in}}$, the accretion timescale to reach the black hole from the disk radius $R$ is $t_{\text{visc}} = 5 \times 10^{-3} (H/R)^{-2} r_{\text{in}}^{-1/2} \text{s}$. For $H/R = 10^{-2}$, $a = 0.1$ and $R = 10^5 R_\odot$, $t_{\text{visc}} \approx 60 \text{ days}$. It becomes $\sim 2000 \text{ days}$ for $R = 10^9 R_\odot$.}
2. Stability curves computation

2.1. Methodology

Stability curves are generally plotted in a $\log T - \log \xi/\Gamma$ diagram (e.g., Krolik et al. 1981), where $T$ is the gas temperature and $\xi$ is its ionization parameter\(^2\). In this diagram, an equilibrium state where the slope of the curve is positive is thermally stable, while it is unstable if the slope is negative, and the gas is then expected to rapidly collapse into a different stable equilibrium state.

As said in the introduction, we used the best fit SED obtained by Marcel et al. (2019) in the JED model framework to compute the stability curves. These SED reproduce the RXTE/PCA data of GX 339-4 observed during its 2010–2011 outburst. The JED framework and the way in which the SED were computed are described in a series of papers (Ferreira et al. 2006; Marcel et al. 2018b,a) to which the reader is referred for more details. In Appendix A, we have also reported some of this information. To summarize, the JED framework assumes the presence of a JED in the inner region of the accretion flow, for disk radii $< R_N$, and a standard accretion disk (SAD) beyond $R_N$. The total SED is mainly characterized by $R_N$ and the accretion rate $\dot{M}$ reaching the inner compact object. The high energy emission (above 1–2 keV) is dominated by the emission of the standard accretion disk. Both JED and SAD emissions depend on $R_N$ and $\dot{M}$. The JED emission is generally dominated by the Compton process, the seed photon field being a mix of local bremsstrahlung and synchrotron emission and nonlocal emission from the SAD (see Marcel et al. 2018a). A few SED examples are detailed in Fig. “citeSEDcompMon”.

Marcel et al. (2019) showed that $R_N$ and $\dot{M}$, and consequently the broad band JED-SAD SEDs, are quite well constrained all along the outburst thanks to the RXTE/PCA data. In Table 1, we have reported the parameters $R_N$ and $\dot{M}$ as well as the corresponding bolometric and ionizing (i.e., between 1 and 1000 Rydbergs) luminosities (in Eddington units) of a few best fit SEDs at different MJD along the 2010–2011 outburst of GX 339-4. In Fig. 1, we have reported the hardness-intensity diagram (HID) of this outburst with the position of the different observations reported in Table 1. The corresponding SEDs are plotted on the left side of Fig. 2 and are discussed later.

These SEDs were then used in CLOUDY 17.01 (last described in Ferland et al. 2013) to compute the corresponding stability curves all along the outburst.

We adopted Solar abundances (as in Table 7.1 of CLOUDY documentation\(^3\)), a typical disk wind density $n = 10^{12}$ cm\(^{-3}\) (see Sect. 2.2 for a discussion on the effect of the density), a turbulence velocity $v_{\text{turb}} = 500$ km s\(^{-1}\), and a column density $\log(N_H/\text{cm}^{-2}) = 23.5$, as in Bianchi et al. (2017).

Notes. We have also reported the corresponding luminosities between 1 and 1000 Rydbergs and between 1 and 100 keV as well as the bolometric luminosity. The Eddington luminosity $L_{\text{Edd}} = \dot{M} c^2 / (1 - \varepsilon)$, assuming a black hole mass of $5.8 \, M_\odot$.

2.2. Caveats

While the SEDs have a strong impact on the stability curves, other parameters can also affect the heating and cooling equilibrium and modify the stability curve shape. For instance, Bianchi et al. (2017) looked at the effect of chemical abundances and they are marginal. Chakravorty et al. (2013) and Bianchi et al. (2017) looked at the effect of the plasma density and only high densities (above $10^{16}$ cm\(^{-3}\)) have a significant impact on the stability curve shape. In the case of a hard state SED, the slope of the stability curves can even change and the branch consistent with Fe XXV and Fe XXVI ions can move from thermally unstable to thermally stable conditions (see Fig. 5 of Bianchi et al. 2017).

Such high densities are, however, not consistent with the (admittedly rare) observational constraints (e.g., Kallman et al. 2009; Schulz et al. 2008) nor expected from disk wind models in XRBs (e.g., Chakravorty et al. 2016, Higginbottom et al. 2017). Our choice of a wind density of $n = 10^{12}$ cm\(^{-3}\) in our simulations is then coherent with the fact that stability curves do not change drastically for a wind density varying between $10^{8}$ and $10^{16}$ cm\(^{-3}\) (see Chakravorty et al. 2013; Bianchi et al. 2017, and see also Appendix B).

The CLOUDY code also assumes an isolated and static plasma which is obviously not the case for a large-scale wind. The effects such as thermal conduction or adiabatic coolings are thus not taken into account in our computation. Numerical simulations of thermal disk winds indicate, however, that thermal conduction should have a small effect on the heating and cooling equilibrium (e.g., Higginbottom et al. 2017 for thermal winds). Concerning adiabatic coolings, they can also be neglected as long as the time to reach photoionization equilibrium is, locally,
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shorter than the dynamical timescale of the wind. While the observed line widths generally imply that the gas is supersonic, such conditions are actually verified in MHD disk wind solutions such as those discussed by Chakravorty et al. (2016). In fact, even if the plasma wind velocity could be supersonic, its dynamical timescale (see an estimate given by Gonçalves et al. 2007 in their Eq. (8)) is expected to be significantly longer than the other timescales involved in the radiative equilibrium computation (e.g., ionization time, recombination time, and thermal time; see Gonçalves et al. 2007).

While these arguments suggest that the shape of the stability curves discussed in this paper should not strongly depend on our physical and numerical assumptions, precise estimates would require a detailed modeling of the disk wind physical properties and dynamics such as in the recent work by Dannen et al. (2020), Waters et al. (2021) in the case of thermal disk winds. While this is an important step which should also be done in the case of magnetically driven disk winds, this is however out of the scope of the present paper. Some caution is nevertheless required and our results must then be understood with these limitations in mind.

3. Stability curve evolution

The stability curves corresponding to the MJD reported in Table 1 are plotted in the right panels of Fig. 2 in the log \( T \) – \( \log \xi / T \) plane. In this plane, the parts of the stability curves with positive (resp. negative) slopes are thermally stable (resp. unstable). The highlighted areas on each curve correspond to the range of the ionization parameter consistent with Fe XXV and Fe XXVI ions and they can go from \( 10^3 \) to \( 10^7 \) \( \text{erg cm}^{-2} \) depending on the SED. They are colored in gray (resp. blue) if they are located on an unstable (resp. stable) part of the stability

3.1. Hard state: From MJD 55208 to MJD 55293

The first RXTE observation starts at MJD 55208 when the source was already in a rather bright (\( L \approx 2\% L_{\text{Edd}} \)) hard state. GX 339-4 stayed in the hard state until around MJD 55293 when it started transitioning to the soft state. The 1–1000 Ry luminosity increases by a factor of 5–6 during this period (see Table 1). The three best-fit SEDs obtained with the JED model for MJD 55208, 55271, and 55293 are reported in Fig. 2a and information on the corresponding stability curves can be found in Fig. 2b. The SEDs are typical of hard states, dominated by a hard X-ray cut-off power law above \( \sim 1–2 \) keV (produced by the inner JED) and a weak disk black-body component below, produced by the outer SAD. The power-law slope appears roughly constant around 1.4–1.5 and the cut-off energy decreases when the luminosity increases. The disk black body emission increases in flux and temperature, which is in agreement with the decrease in the transition radius \( R_{\text{in}} \) between the JED and the SAD while the accretion rate increases (see Table 1).

The computed stability curves are quite similar for the three MJD 55208, 55271, and 55293. In the three cases, the temperature range that agrees with the right ionization range for Fe XXV and Fe XXVI is unstable. In fact, if the wind exists during this period, its temperature has to be in one of the ranges where the stability curves have a positive slope that is either at a very high temperature \( (\gtrsim 3 \times 10^7 \text{K}) \) or in localized regions around \( 10^6 \text{K} \), \( 2 \times 10^5 \text{K} \), or at a lower temperature \( 3 \times 10^4 \text{K} \). In these temperature ranges, the wind would not produce any Fe XXV and Fe XXVI absorption lines (see Sect. 3.7).

3.2. Hard-to-soft transition: From MJD 55294 to MJD 55333

From MJD 55294, the source starts to transition to the soft state, that is to say the path in the HID turns to the left. This transition lasts about 40 days, between MJD 55294 to around MJD 55333. During this period, the SEDs still show a power law component in the X-rays but the slope increases from \( \sim 1.5 \) to 2.2 and the high energy cut-off decreases all along the transition (see Fig. 2c). On the other hand, the disk component increases in flux and temperature. At MJD 55333, at the end of the transition, the SED is only dominated by the disk component.

We have reported the corresponding stability curves in Fig. 2d. During this hard-to-soft transition, the stability curves change drastically and at the end of the transition (after MJD 55296), the stability curves become thermally stable in almost the entire temperature range used in the CLOUDY
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Fig. 2. SED (left) and corresponding photoionization stability curves (right) between MJD 55208 and 55293 (hard state, a and b), MJD 55294 and 55303 (hard-to-soft transition, c and d), MJD 55304 and 55592 (soft state, e and f) and MJD 55593 and 55606 (soft-to-hard transition, g and h). The stability curves are labeled with their corresponding MJD. The highlighted (blue and gray) areas on each curve correspond to the range of the ionization parameter consistent with Fe XXV and Fe XXVI. They are colored in blue (resp. gray) if they are located on a stable (resp. unstable) part of the stability curve.

This change occurs in a couple of days (between MJD 55295 and MJD 55297), while the changes of the SED are quite minor. Within a day, from MJD 55295 to MJD 55296, the wind becomes able to produce Fe XXV and Fe XXVI absorption lines. While the bolometric luminosity varies by only a factor of 1.4 during computations. This includes the ionization range compatible with Fe XXV and Fe XXVI ions.

Except in a narrow interval around $3 \times 10^4$–$10^5$ K, a temperature range which is irrelevant for Fe XXV and Fe XXVI because it is too low.
the transition, with a maximum around MJD 55303, the ionizing luminosity varies by a significantly larger factor of \( \sim 3.3 \) due to the increase in the disk flux which dominates the 1–1000 Ry energy range.

### 3.3. Soft state: From MJD 55334 to MJD 55559

In the soft state, which lasts about 225 days here, the SED are mainly characterized by a disk component in this state (see Fig. 2e). The stability curves are very similar to one another during this entire state (see Fig. 2f), while the 1–1000 Ry luminosity decreases by a factor of 4–5. The ionization range compatible with Fe XXV and Fe XXVI ions is always in a stable part of the stability curves, meaning that the associated absorption lines can be present. The presence of a hard tail can, however, significantly impact the thermal equilibrium of the wind (see Sect. 3.6 and Fig. 3).

### 3.4. Soft-to-hard: From MJD 55561 to MJD 55606

At MJD 55559, the path of GX 339-4 starts to turn right in the HID, the source transiting back to the hard state. This transition lasts about 40 days until around MJD 55606. We have reported a few best fit SEDs during this transition in Fig. 2g. The disk component decreases in flux and temperature, while the X-ray power law hardens and the high-energy cut-off increases. The 1–1000 Ry and bolometric luminosities decrease by a factor of \( \sim 2.2 \) and \( \sim 2.6 \), respectively, during this transition.

We have reported the corresponding stability curves in Fig. 2h. As in the hard-to-soft transition, the shape of the stability curves changes drastically during the soft-to-hard transition. Moreover, and again similar to the hard-to-soft transition, the change from stable to unstable conditions for the ionization range compatible with Fe XXV and Fe XXVI ions occurs in a couple of days. While the stability curve is similar to that of soft states at MJD 55592, it becomes the same as hard states at the beginning of the outburst at MJD 55594. Moreover, the temperature ranges of thermal stability after the soft-to-hard transition are also similar to those before the hard-to-soft transition (see Sect. 3.1).

### 3.5. Hard-to-quiescence: From MJD 55607 to MJD 55646

After MJD 55607, GX 339-4 is back to the hard state until the end of the outburst. The bolometric luminosity decreases by more than a factor of 30 during this period. The lower the luminosity is, the bumpier the SED shape (see Fig. 2i). This is a characteristic of the Compton process in a hot, but tenuous plasma, where each scattering order produces well separated spectral bumps.

We have reported the corresponding stability curves in Fig. 2j. They are typical of hard state ones (see Sect. 3.1) and no Fe XXV and Fe XXVI absorption lines are expected. The general shape of the stability curves seems to stiffen when the source flux decreases, the “S” shape then evolves to a “step” function where the upper hot and tenuous branch takes up the large part of the \( \xi/T \) range.

### 3.6. Hard tail

The soft states can also present a low luminosity and steep power law at a high energy (above \( \sim 10 \) keV), the so-called hard tail, whose origin is currently unknown (Remillard & McClintock 2006). It is generally badly constrained due to the lack of statistics, reaching up to a 50% error on the photon index, for example. Marcel et al. (2019) included this hard tail in the SED by adding a power-law component to the synthetic spectra each time the fitting procedure favored a pure blackbody emission (see Marcel et al. 2018a for a detailed discussion). The photon index of this power-law component was set to \( \Gamma = 2.5 \) and it was normalized in order to contribute to a fixed fraction of the 2–20 keV energy range (typically between 1% and 20%, Remillard & McClintock 2006). On the left side of Fig. 3, we report the stability curves for MJD 55410 assuming different hard tails with a different flux (contributing to 1 and 20% of the 2–20 keV flux), but with a fixed photon index \( \Gamma = 2.5 \). In the right panel, we assume hard tails with different spectral indices \( \Gamma = 2.5 \) and 2) but a constant flux (contributing to 10% of the 2–20 keV flux). These different examples show that the presence of this hard tail can have some effects on the stability curves, but it is not sufficient to change a soft state-like into a hard state-like shape. Moreover, its impact on the thermal stability of the hot wind in the soft state should not drastically change the existence of a stable ionization domain for Fe XXV and Fe XXVI.

### 3.7. Low temperature phases

All the stability curves plotted in Figs. 2 and 3 show low temperature domains (around \( 10^{4.5} \) and \( 10^{5} \) K), which are thermally stables. If part of the wind plasma is in this range of temperatures, absorption lines from low ionization-level ions could also be observable. Of course, this strongly depends on the total column density of this low temperature plasma on the line of sight. For instance, in the case of the transient accreting neutron star...
AX J1745.6-2901, Bianchi et al. (2017) tested the case where the column density is equal to the one deduced from the Fe XXV and Fe XXVI absorption lines. This low temperature phase, if present on the line of sight, would then block all the radiation in the soft X-rays. On the other hand, Bianchi et al. (2017) estimate the filling factor of this phase to be very low. So this strong absorption would only be observed as a sporadic change in the persistent neutral absorption and, in the case of AX J1745.6-2901, this was tentatively associated to the dips observed in this source by Bianchi et al. (2017). With CLOUDY, we simulated a mate the filling factor of this phase to be very low. So this strong absorption would only be observed as a sporadic change in the persistent neutral absorption and, in the case of AX J1745.6-2901, this was tentatively associated to the dips observed in this source by Bianchi et al. (2017). With CLOUDY, we simulated a few cases with lower column densities and where the absorption is less severe. No absorption lines are present above 1 keV, but some significant absorption is observed below 1 keV and strong absorption is observed in the UV down to the IR. We note that the ionization parameter is quite low in these phases (<10³). This could correspond to an unphysical large distance from the BH. In other words, these low temperature phases may simply not exist for compact systems.

4. Discussion

We used the best fit SED obtained by Marcel et al. (2019) to compute the stability curves presented in Sect. 3. These SEDs were computed in the JED-SAD framework and reproduced the spectral evolution of GX 339-4 during its 2010–2011 outburst. We show that the range of ionization parameters consistent with Fe XXV and Fe XXVI ions is always in a thermally unstable part of the stability curves in the hard state. On the contrary, this range of ionization parameters is always thermally stable in the soft state. Moreover, the observations of hot wind signatures in soft states indicate that the wind properties agree with this stable range of ionization. Assuming that a wind is always present during the entire outburst, as we did in this work, we then wonder how the wind properties should evolve during the state transition while reaching (in the case of the hard-to-soft transition) or leaving (in the case of the soft-to-hard transition) the soft state ionization conditions. Some interesting constraints need to be satisfied as discussed below. As mentioned in Sect. 2.2, however, it is worth keeping in mind that the true evolution of the plasma would require detailed modeling of the disk wind’s physical properties and dynamics (e.g., Dannen et al. 2020; Waters et al. 2021). While out of the scope of the present paper, they could significantly affect the following points raised in the rest of this section.

4.1. Changes in the disk wind properties during spectral transitions

4.1.1. From hard-to-soft

As shown in Sect. 3, only a few temperature domains are thermally stable during hard states (see Fig. 2b) either at very high temperature (>3 × 10⁷ K) or in a localized region around 10⁶ K, 2 × 10⁶ K, or at a low temperature <3 × 10⁴ K. As already mentioned, the ionization range compatible with Fe XXV and Fe XXVI is itself thermally unstable. In the soft state, however, a large part of the temperature domain is thermally stable including the ionization range compatible with Fe XXV and Fe XXVI. In order to become detectable at the end of the hard-to-soft transition, the hot wind properties cannot be just any at the beginning. They have to evolve from the stable temperature domains of the hard states to the “hot wind” domains of the soft states.

Interestingly, this evolution is unlikely to occur at constant wind density distribution (i.e., constant nr²) as shown in Fig. 4. This figure is similar to Fig. 2d, but we over-plotted two different paths (square and dashed line; star and dashed line) which correspond to two different wind evolutions at constant nr². The square and dashed line starts from the stable part of the temperature domain of the hard state around 10⁶ K (indicated by a square on the stability curve of MJD 55294). During the spectral evolution between MJD 55294 and MJD 55333, this path always stays on a stable part of the stability curves, but it never crosses the “hot wind” domain of the soft states. As a consequence, no signature of a hot wind is visible in the soft states at the end of the transition. The same conclusion is obtained if the wind is initially (during MJD 55294) on one of the stable branches existing at a lower temperature (<10⁶ K).

The other path (star and dashed line) starts from the top hot stable branch (T > 3 × 10⁷ K) of the hard state at the very beginning of this temperature domain (indicated by a black star on the stability curve of MJD 55294). During the spectral evolution of the system, this path crosses the stable “hot wind” domains of the soft states only after MJD 55297. In fact, only the constant nr² paths that start in the small temperature domain underlined in red on the stability curve of MJD 55294 will cross the “hot wind” domain of one of the soft states at the end of the transition. Indeed, a plasma at a temperature just below the red segment is unstable. And for a plasma at a temperature larger than the red segment, constant nr² paths will never cross a “hot wind” domain of the soft states and no wind will be detected at the end of the transition. This red segment, however, corresponds to a
very limited range of temperatures and ionization parameters in the hard state. To reach the soft state, it appears more reasonable to assume a change in the physical characteristics of the wind during the transition (i.e., $n r^2$ does not stay constant). As an example, we over-plotted in red dashed lines the paths followed by the wind if its density increases (red star and dashed line) or decreases (red square and dashed line) by a factor of 3 between MJD 55295 and MJD 55296. See Sect. 4.1.1 for the small temperature domain underlined in red on the stability curve of MJD 55294. The arrows indicate the time evolution.

We can repeat a similar procedure to follow the evolution of the wind if its density increases (red star and dashed line) or decreases (red square and dashed line) by a factor of 3.

4.1.2. From soft-to-hard

We can repeat a similar procedure to follow the evolution of the wind thermal state during the transition from the soft to the hard state. This is now illustrated in Fig. 5. We assume that at the beginning of the transition, the wind is in the conditions where Fe XXV and Fe XXVI lines are detectable (black star on the MJD 55593 stability curve). Then a path at constant $n r^2$ (black dashed line) reaches the unstable temperature domain of the stability curve of MJD 55594 (black star on the MJD 55594 stability curve). In fact, looking at the shape of the stability curves, this evolution does not strongly depend on the starting point in the “hot wind” domain of the soft states (MJD < 55594), and, as long as $n r^2$ stays constant, the wind inevitably reaches an unstable state when the X-ray source enters in the hard state at MJD 55594.

The evolution of the wind after MJD 55294 is thus quite unknown. The thermal instability forces the wind plasma to leave the thermally unstable temperature domain and to reach the other stable branches of the stability curve. This necessarily requires a change in the wind temperature and density. Locally, as soon as the plasma reaches a new (stable) temperature, the new ionization equilibrium is expected to settle in almost immediately (Gonçalves et al. 2007). Of course, the complete migration of the gas from a thermally unstable to a thermally stable state, which is itself a mix of hot and cold phases in interaction, takes some time. This is expected to occur on a timescale $t_{\text{migr}}$ on the order of $\Delta H/c_s$ where $\Delta H$ is the thickness of the thermally unstable region and $c_s$ is the sound velocity in the cold phase (see discussion in Gonçalves et al. 2007). This translates to

$$t_{\text{migr}} \lesssim 2 \times 10^4 \frac{\N_23}{T_5^{1/2} n_{12}} \quad \text{(in units of s)},$$

where $N_{23}$ is the column density in units of $10^{23}$ cm$^{-2}$, $n_{12}$ is the hydrogen density in units of $10^{12}$ cm$^{-3}$, and $T_5$ is the temperature of the cold gas in units of $10^5$ K. Assuming a maximal extension of the disk wind on the order of the binary separation in GX 339-4, that is $\sim 10^{12}$ cm (Zdziarski et al. 2004, 2019), and an optically thin wind, $t_{\text{migr}}$ is shorter than a day. Thus the migration can easily occur between two RXTE pointings (generally separated by 1 day).

The vertical dotted segments in Fig. 5 indicate the cases where the evolution of the gas after MJD 55594 occurs at a constant pressure (isobaric evolution i.e., a constant $\xi/T$) and is fast enough to assume that the average distance of the gas to the X-ray source would not change. In this case, the wind plasma can transition to two different stable solutions, one hotter and the other colder, indicated by the upper and lower red squares, respectively, on the MJD 55594 stability curve. It is also possible that the wind evolves into a mix of these two different plasma phases where colder (and denser) structures are embedded in a hotter (less dense) gas. This situation would be very similar to the one discussed by Bianchi et al. (2017) in the case of the wind evolution observed in the neutron star AX J1745.6-2901 between its soft and hard state. After MJD 55594, each of the two possible wind phases keep on evolving depending on the spectral evolution of the X-ray source. As examples, we over-plotted in Fig. 5 in red dashed lines the two possible paths where $n r^2$ is assumed to be constant.

Fig. 4. Colored lines are the photoionization stability curves during the hard-to-soft transition (see Fig. 2 for the meaning of the blue and gray segments). The black dashed lines (squares and dashed line; star and dashed line) correspond to different paths with constant $n r^2$. The red lines are the paths followed by the wind assuming an increase (red dotted path) or decrease (red dashed path) in the wind density by a factor of 3 between MJD 55295 and MJD 55296. See Sect. 4.1.1 for the small temperature domain underlined in red on the stability curve of MJD 55294. The arrows indicate the time evolution.

Fig. 5. Colored lines are the photoionization stability curves during the soft-to-hard transition (see Fig. 2 for the meaning of the blue and gray segments). The black stars and dashed line correspond to a path of constant $n r^2$ from MJD 55595 until MJD 55594. The vertical red dotted lines correspond to isobaric (constant $\xi/T$) evolutions of the wind. The black square and dashed lines correspond to a path of constant $n r^2$ starting from MJD 55594. The arrows indicate the time evolution.
4.1.3. A very favorable configuration for disk wind detection

Interestingly, during the soft-to-hard and hard-to-soft transitions, the shape of the stability curve becomes almost vertical in the ionization range compatible with Fe XXV and Fe XXVI ions (see e.g., the stability curve of MJD 55296 in Fig. 2h). This corresponds to a situation where the pressure equilibrium is satisfied in this ionization domain and this is a quite favorable mechanical configuration for the wind. This could explain why we generally observe the strongest wind absorption features in the middle of the transition states (see Ponti et al. 2012).

4.2. Disk irradiation as a potential driver of the change in the disk wind properties during the hard-to-soft transition

As shown in Sect. 4.1.1, if we want to observe a hot wind at the end of the hard-to-soft transition, an increase (or a decrease depending on the wind phase at the beginning of the transition) in the wind density seems to be needed to make the wind evolve into the stable ionization range for Fe XXV and Fe XXVI ions. It is hard to estimate the timescale for such evolution given the lack of long (several days) and continuous monitoring of a hard-to-soft state transition of an XRB. But the fact that absorption features are regularly observed in soft states suggests that the wind properties should evolve rapidly (for approximately days) after its entry in the soft state. This is somewhat problematic if the wind density scales only with the local disk density. Since the latter scales with the disk accretion rate, the wind density would be expected to increase and then decrease during the outbursting cycle. However, the disk wind region is estimated to be located quite far away, beyond $10^4 R_g$. There is, therefore, no reason why the slow time evolution of the far-out wind driving zone should always be contemporaneous with the rapid spectral changes of the SED emitted from the innermost disk regions. Irradiation of the outer disk by the inner X-ray emission seems to be performed (e.g., Casse & Ferreira 2000) and thermally-driven (e.g., Higginbottom & Proga 2015) outflows.

The amount of X-ray luminosity incident on the disk at a radius $r = R/R_g$ in a ring of thickness $\Delta r$ depends on the exact geometry. Estimates from a simple radial profile of the disk aspect ratio provide an X-ray irradiation that is too low; this does not fit with the required disk accretion transport to explain the XRB outburst light curve durations (e.g., Dubus et al. 2001; Tetarenko et al. 2018a, 2020). Following Dubus et al. (2001), the intercepted and reprocessed X-ray irradiation (which corresponds to the heating power deposit $Q$) at the disk surface leads to the enhancement of mass loss, both in magnetically-driven (e.g., Casse & Ferreira 2000) and thermally-driven (e.g., Higginbottom & Proga 2015) outflows.

$$Q \approx C_{ir} \frac{L_X}{4\pi r^2} 2\pi r d r = C_{ir} L_X \frac{\Delta r}{2r},$$  \hspace{1cm} (2)

with $C_{ir}$ being a parameter which encapsulates our ignorance concerning the irradiation geometry, the X-ray albedo, and X-ray irradiating spectral shape. We note that $C_{ir}$ is estimated to be $\approx 0.05$ to explain the XRB outburst light curve durations (see Tetarenko et al. 2018b and references therein). Actually, a (weak) radial dependence of $C_{ir}$ is expected due to the radial variation of the disk aspect ratio (see Dubus et al. 2019 and references therein). The scattering of the X-rays by the disk wind itself can also have some impact on the disk irradiation (Dubus et al. 2019; Kimura & Done 2019). But for the present discussion, we assume $C_{ir}$ to be constantly equal to 0.05. Equation (2) then shows that heating through irradiation is directly related to the X-ray luminosity. The thermal timescale on which the disk matter is heated is given by (e.g., Gonçalves et al. 2007)

$$t_{th} \sim \frac{T_s}{n_{12} A_{23}} \text{ sec},$$  \hspace{1cm} (3)

where, as in Eq. (1), $n_{12}$ is the density expressed in $10^{12}$ cm$^{-3}$, $T_s$ is the temperature in $10^5$ K, and $A_{23}$ is the cooling function in $10^{-23}$ erg cm$^{-3}$ s$^{-1}$. It is thus reasonable to expect thermalization timescales of seconds to minutes. The travel time for the X-ray photons produced at a few $R_g$ from the black hole and then to the outer disk ($R > 10^4 R_g$) is of the same order of magnitude. Finally the density adjustment of the wind follows the thermal adjustment of the underlying disk on, typically, the local Keplerian timescale which is less than a day even at a disk radius of $10^4 R_g$ (assuming a 10 solar mass black hole). Overall the entire process (irradiation and wind density adjustment) is expected to occur in less than a day.

We have reported the X-ray luminosity $L_X$ computed from the SED between 1 and 100 keV in Table 1. The luminosity $L_X$ increases rapidly at the beginning of the transition with an increase of a factor of $\sim 1.5$–2 between MJD 55294 and MJD 55303, while the accretion rate stays roughly constant (see Table 1). Our qualitative estimates then suggest an increase in the disk surface heating through irradiation by the inner X-ray source during the hard-to-soft transition and, consequently, a potential increase of the disk wind mass loading and wind density in a short (less than a day) timescale. Thus, looking at Fig. 4, our result supports the scenario with an increase in the wind density during the transition. A more quantitative impact on the wind density would require, however, a precise modeling of the thermal balance of the disk outflowing disk surface layers which is out of the scope of the present paper.

5. Concluding remarks

We studied the expected evolution of the thermal properties of a hot disk wind (e.g., characterized by the presence of absorption lines of Fe XXV and Fe XXVI ions) in a low-mass X-ray binary assuming it is present during the entire outburst (e.g., Sánchez-Sieras & Muñoz-Darias 2020). For that purpose, we have used the best fit SEDs obtained by Marcel et al. (2019) to reproduce the RXTE/PCA data of GX 339-4 during the 2010–2011 outburst of the source. These broad-band SEDs have been obtained in the JED framework described in Ferreira et al. (2006), Marcel et al. (2018a,b). For each of the 274 SEDs, we computed the corresponding stability curve using the CLOUDY software. We were then able to follow the evolution of these stability curves all along the outburst. Our main conclusions are as follows.

- All hard-state observations are characterized by stability curves where the ionization domain that is compatible with Fe XXV and Fe XXVI ions is thermally unstable. On the contrary, in all the soft state observations, this ionization domain is thermally stable.

- During the spectral state transitions, the evolution of the stability curve from stable to unstable conditions (in the soft-to-hard transition) and reversely (in the hard-to-soft transition) can occur rapidly (a day timescale) due to the change in the illuminating ionizing SED.

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During the hard-to-soft transition, the common observations of hot wind signatures in the soft states and their absence in the hard states suggests a rapid evolution of the disk wind properties, most likely a significant increase (or decrease depending on the ionization state of the wind at the beginning of the transition) in its density. Moreover, this evolution must occur quasi simultaneously with the change in the spectral state of the inner X-ray source located $10^{23}$–$10^{24}$m around from the wind production site.

During the soft-to-hard transition, if a hot wind is present in the soft states, the hardening of the X-ray emission unavoidably puts the hot wind into an unstable part of the stability curve in the hard states. Then the wind plasma necessarily moves to a hotter or a colder (or a mix of the two) phase where Fe XXV and Fe XXVI ions cannot exist and, in consequence, cannot be detected.

We note that the first item is also consistent with our initial assumption that hot winds are always launched from the outskirt of the accretion disk, regardless of the spectral state of the innermost region. But they are only observable in soft states during which the required thermal stability occurs.

Recent numerical simulations (e.g., Zhu & Stone 2018; Jacquemyn-Ide et al. 2019 and references therein) show that disk winds are expected from low magnetized turbulent accretion disks threaded by a large-scale magnetic field, which would correspond to our SAD. For high magnetization, however, which would correspond to our JED, powerful jets are rather produced (e.g., Liska et al. 2020). Our results thus provide a case for the presence in XRBs of a large-scale magnetic field throughout the entire accretion disk whose largescale magnetization would evolve from high values in the inner regions (i.e., Liska et al. 2020 configuration), to much lower values in the outer regions, where a disk wind would be launched (i.e., Zhu & Stone 2018 or Jacquemyn-Ide et al. 2019 configuration). In recent 3D simulations (Jacquemyn-Ide et al. 2021), such a radial stratification of the magnetization is expected as the outcome of a global readjustment of the disk (see also Scepi et al. 2019, 2020). If true, this could have a significant impact on the secular evolution of the accretion flow.

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References

Diaz Trigo, M., & Boirin, L. 2016, Astron. Nachr., 337, 368
Done, C., Gierlinski, M., & Kubota, A. 2007, A&ARv, 15, 1

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Appendix A: The JED-SAD framework

The SEDs used in this study were computed in the JED-SAD framework described in detail in Marcel et al. (2018b,a, 2019). While the reader is referred to these papers for more details, we briefly recall the main characteristics of this model here.

JED solutions assume the existence of a large-scale vertical magnetic field B, threading the disk. The JED magnetization \( \mu = B_z / (\varepsilon_0 P_{\text{rad}}) \), where \( P_{\text{rad}} \) includes the plasma and radiation pressures, is in the range from \([0.1–1]\). In these conditions, in a JED, part of the accreted matter is ejected and the accretion pressures, is in the range from \([0.1–1]\). In these conditions, in a JED, part of the accreted matter is ejected and the accretion rate is a function of the radius, that is to say \( \dot{M}(R) \propto R^p \) with \( p \) being the ejection parameter\(^6\). In contrast with the ADIOS model (Blandford & Begelman 1999; Begelman 2012), the ejection efficiency \( p \) is not a free parameter in the JED model, but it is a consequence of the disk properties (magnetization, turbulence). Its value results from the resolution of the full set of MHD equations governing the interdependent accretion-ejection physics in the presence of a large-scale magnetic field (see Ferreira 2002, 2008 for reviews).

The SEDs of a JED-SAD configuration combine the emission of the JED, which is present between \( R_{\text{ISCO}} \) and a transition radius \( R_{\text{tr}} \), and the emission of the nonejecting SAD extending beyond \( R_{\text{ISCO}} \). The JED thermal structure was computed taking into account the local turbulent heating, coulomb heat exchange (i.e., a two-temperature plasma), heat advection, and cooling using a bridge formula for optically thick and thin plasmas. The optically thin cooling processes are bremsstrahlung, synchrotron and local, and nonlocal (on the soft photons emitted by the outer SAD) Compton scattering processes. The SED mainly depends on two parameters: the transition radius \( R_{\text{tr}} \) and the inner disk accretion rate \( M(R_{\text{ISCO}}) \) (simply noted \( M \) hereafter) at \( R_{\text{ISCO}} \). The global spectrum emitted by a JED-SAD disk configuration characterized by \( (R_{\text{tr}}, M) \) was self-consistently computed along with the disk thermal and dynamical states. It appears that the JED can play the role of the hot corona needed to explain the hard X-ray emission in XRB. Its emission dominates the high energy part of the SED, while the multicolor disk emission from the SAD dominates at low energy (Marcel et al. 2018a). We note that for \( R_{\text{tr}} = R_{\text{ISCO}} \), there is no JED. The entire accretion flow, then, is a SAD and the source is in a soft state. On the contrary, large \( R_{\text{tr}} \) (\( > R_{\text{ISCO}} \)) characterize hard states, while \( R_{\text{tr}} \) on the order of a few \( R_{\text{ISCO}} \) are typical of (either hard or soft) intermediate states.

This model was applied with success to the RXTE/PCA data of the 2010–2011 outburst of GX 339-4. In this case, for \( R_{\text{ISCO}} \), a black-hole mass of 5.8 solar masses\(^7\) and a black hole spin \( a = 0.94 \) are assumed (see references in Marcel et al. 2019). The distance of GX 339-4 is also assumed to be 8 kpc (Hynes et al. 2004; Zdziarski et al. 2004; Parker et al. 2016). These results are discussed in detail in Marcel et al. (2019) (the three other outbursts of this source during the RXTE era have been analyzed in Marcel et al. 2020). We have reported the comparison between the observations and the model in Fig. A.1. The observed values of the \( 3–200 \) keV total luminosity, the power-law luminosity fraction \( L_{\text{pl}} / L_{\text{3–200}} \) (defined as the ratio of the power-law flux to the total flux in the \( 3–200 \) keV range), and the power-law index \( \Gamma \) obtained by Clavel et al. (2016) are reported with black markers at the top, middle, and bottom panels, respectively. The corresponding values produced by the best fit SED obtained by Marcel et al. (2019) are over-plotted with colored markers. The MJD of Table 1 are also indicated with dashed vertical lines. The best fit SEDs reproduce the observations very well except in the soft state for what concerns the power law component (middle and bottom panels, red markers). In the soft states, however, the statistics at high energy (\( > 10 \) keV) of the RXTE/PCA data is too low to provide good constraints on this power law and the comparison is not relevant. In Fig. A.2, we have also reported the SED for MJD 55617, 55208, and 55297, detailing the importance of the different radiative processes (bremsstrahlung, synchrotron, and Compton).

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\(^6\) The ejection parameter is labeled \( \xi \) in Marcel et al. (2019). It was changed to \( p \), which is not to be confused with the ionization parameter of the wind.

\(^7\) Multiple studies have been performed to constrain the BH mass in GX 339-4 and have led to different estimations (e.g., Hynes et al. 2003; Muñoz-Darias et al. 2008; Parker et al. 2016; Heida et al. 2017). For simplification, and since there is no consensus about the GX 339-4 mass, we chose for it to be the central value.

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Fig. A.1. Results of the fitting procedure of Marcel et al. (2019) applied to the 2010–2011 outburst of GX 339-4. The black markers are fits taken from Clavel et al. (2016) reported with their error bars when reliable, while color lines display the best fit values obtained with the JED-SAD SED: Green, blue, yellow, and red correspond to hard, hard-intermediate, soft-intermediate, and soft states, respectively. From top to bottom: 3–200 keV total luminosity, \( L_{\text{3–200}} \) (in Eddington units), the power-law luminosity fraction \( L_{\text{pl}} / L_{\text{3–200}} \), defined as the ratio of the power-law flux to the total flux in the \( 3–200 \) keV range, and the power-law index \( \Gamma \). The transparent colored areas correspond to the confidence intervals of a 5% and 10% error margin (see Marcel et al. 2019). The vertical dashed line corresponds to the MJD reported in Table 1.
Appendix B: Effect of density on the stability curve shape

In Fig. B.1, we have reported the stability curves computed with CLOUDY for MJD 55293 (top) and MJD 55297 (bottom) for different values of the plasma density varying between $10^8$ and $10^{15}$ cm$^{-3}$. If differences at low $\xi$ are visible, although not large enough to qualitatively change the general behavior of the curves, at high $\xi$ the stability curves are almost independent of the density. The reason for this is that Compton scattering dominates there and both heating and cooling terms scale with density in the same way.
Appendix C: Ion fraction

Fig. C.1. Fe XXV (solid lines) and Fe XXVI (dashed lines) ion fractions for three MJD of the 2010–2011 outburst of GX 339-4. They were computed by using the SED of Marcel et al. (2019). The vertical dotted lines define, for each curve, the range in log $\xi$ used to create the highlighted (blue or gray) areas on the stability curves presented in this paper. The lower limit in log $\xi$ for each range corresponds to an ionic fraction equal to 90 percent of the ionic fraction peak of Fe XXV, while the upper limit corresponds to an ionic fraction equal to 90 percent of the ionic fraction peak of Fe XXVI. If this upper limit is larger than five (like for MJD 55450), it is put equal to five.

In Fig. C.1, we have reported three examples of ion fractions for three MJD of the 2010–2011 outburst of GX 339-4.