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## **Room Temperature Second Sound in Cumulene**

Claudio Melis,\*a Giorgia Fugallo,b and Luciano Colomboa

Second sound is known as the thermal transport regime occurring in a wave-like fashion, usually identified in a limited number of materials only at cryogenic temperatures. Here we show that second sound in a  $\mu$ m-long carbon chain (cumulene) might occur even at room temperature. To this aim, we calibrate a many-body force field on the first principles calculated phonon dispersion relations of cumulene and, through molecular dynamics, we mimic laser-induced transient thermal grating experiments. We provide evidence that by tuning temperature as well as the space modulation of its initial profile we can reversibly drive the system from a wave-like to a diffusive-like thermal transport. By following three different theoretical methodologies (molecular dynamics, Maxwell-Catteneo-Vernotte equation, heat transport microscopic theory) we estimate for cumulene a second sound velocity in the range [2.4-3.2] km/s.

#### 1 Introduction

Fourier's law of thermal conduction states that the steady-state heat current is proportional to the local temperature gradient applied, the proportionality constant being the material intrinsic thermal conductivity<sup>1</sup>. Even if there is still no rigorous derivation of this law starting from a microscopic Hamiltonian description<sup>2–4</sup>, it has been for 200 years enormously successful in providing a reliable description of heat transport phenomena in bulk, 3D materials. On the opposite, its reliability for low-dimensional structures is far from clear and every evidence of its breakdown is seen as a possibility to shed light on its understanding 5-16. On the one side, the chance to observe divergent thermal conductivity, i.e. infinitely-long ranged ballistic transport, has been experimentally<sup>17</sup> and theoretically<sup>18–20</sup> reported in combination with a lowering of the system dimensionality. On the other side, the last five years have been witnesses of a revival of interest on second sound, namely the propagation of heat as a wave  $^{21-24}$ .

In insulating crystals these anomalous behaviours and the different thermal transport regimes can be explained in terms of dominance of different phonon scattering mechanisms. In particular, the physics of heat conduction is ruled by the intriguing interplay between conserving (Normal) and not conserving (Umklapp, boundary, defects, etc) crystal-momentum scattering processes. More specifically: (i) a predominant role of the boundary scattering identifies the ballistic regime; (ii) strong Umklapp processes dictate the diffusive regime; (iii) in between, when Normal processes are the strongest, Umklapp the weakest and boundaryscattering the intermediate mechanism, the hydrodynamic regime appears. In this latter condition, Normal processes preserve the heat flux creating a correlation between phonons and giving rise to collective phonon-excitations which alone will not be able to relax the system into full thermal equilibrium, but at most they will bring it into a drifted Bose-Einstein distribution<sup>25</sup>. In other words phonons can develop a nonzero drift velocity when subjected to a temperature gradient, very much like the viscous flow of a fluid driven by a pressure gradient. In analogy, such a heat conduction regime is called hydrodynamics phonon transport. Once this drifting distribution  $n_{drift}$  has accumulated, heat propagates as a wave (second sound) that is eventually damped on longer timescales by the resistive processes (Umklapp, isotopes etc). Pouseille and second sound can then be considered typical of this hydrodynamic regime, but pioneering experiments in the 70's were able to detect second sound in Bi, NaF and <sup>4</sup>He only at cryogenic temperature in a narrow [1.5-5 K] temperature range<sup>26–29</sup>, as in bulk 3D systems very low temperatures are required in order to freeze out Umklapp processes<sup>30,31</sup>. These limited temperature conditions made these phenomena fascinating, but not particularly appealing since hard to detect experimentally and unsuitable for relevant technological applications.

In this framework, little attention has been paid to this subject for decades; only recently with the theoretical predictions to observe second sound up to 100 K in graphene and other 2D materials<sup>21,22</sup> and carbon nsanotubes<sup>32</sup>, the interest on second sound has risen again up, eventually leading to its experimental observation at 100 K in graphite<sup>23</sup>. From these studies it results that the occurence of Umklapp processes towards low-energy phonons with small phonon wave-vector **q** is severely reduced. These modes, with a large predominance of Normal scat-

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terings, will then carry the majority of the heat flux.<sup>33–35</sup> This is due to the fact that by lowering the dimensionality of the system a softening of the corresponding mode will emerge, and this might effectively reduce the phonon Umklapp scattering phasespace. This result leads to a double gain: first of all, thanks to an extended abundance of Normal processes it is possible to reach extremely high thermal conductivities\*; secondly, the intrinsic limitation of Umklapp scatterings effectively enlarges the temperature window for the observation of hydrodynamic regime up to temperatures where phonon modes with larger  $\mathbf{q}$  will be populated, Umklapp processes eventually activated, and thus the diffusive regime reached. This condition also determines an interesting side effect which misguided some interpretations: in the hydrodynamic regime the main heat carriers are not individual phonons, but rather, collective phonon excitations<sup>36–40</sup> with mean free paths which can be orders of magnitude longer than those of individual phonons; accordingly, ballistic regimes can occur up to length scales that can be orders of magnitudes longer than those expected on the basis of a standard comparison between the actual sample size and the individual phonon mean free paths<sup>17</sup>. For all these reasons, low dimensional systems are then considered crucibles of possible exotic properties.

From an experimental point of view, the observation of phenomena such as Poiseuille flow and second sound means probing a time scale which falls in between the typical Normal and Umklapp relaxation times<sup>22</sup>. This short time scale prevents to use conventional thermal sensors. In this perspective, time-resolved laser based measurements are better suited for measuring thermal responses, due to their much higher time resolution. In particular, thermoreflectance-based techniques<sup>41</sup> use a time modulated laser to heat the surface of a sample. The variation of the surface temperature leads to a corresponding change in reflectance, which is then measured by a probe laser. By comparing the measured reflectance with theoretical calculations, possible deviations in thermal transport with respect to a diffusive regime can be detected. An alternative method named laser-induced transient thermal gratings (TTG)<sup>42</sup> recently allowed to directly observe second sound in graphite at temperatures above 100 K<sup>23</sup>. In this method, two crossing laser pulses are used to create a spatially periodic temperature profile, which is usually set as sinusoidal with a controlled spatial period  $\lambda$ . The transient decay of the amplitude of the imposed sinusoidal temperature profile is then sampled via diffraction by a probe laser beam. Even though the laser-induced TTG technique has recently shown to be very effective to detect wave-like thermal transport features in bulk graphite, there are still many issues that make the use of this technique difficult to study second-sound features on nanomaterials and/or systems with reduced dimensionality. Under this respect, the main issue is the reduced spatial resolution which limits TTG techniques to spatial periods lower than few  $\mu$ m, thus limiting the overall size of the systems to be analyzed. Moreover, TTG shows a time-resolution in the order of the nanosecond, in-

This state of affairs has motivated us to focus on what could be referred to as the prototypical 1D system, namely cumulene, which has been recently identified as the material with the highest lattice thermal conductivity<sup>55</sup> and with a negligible electronic contribution<sup>56</sup>. Cumulene is a carbyne isomer<sup>57</sup>, showing a simple double bonds sequence. It has been synthetized in 2015<sup>58</sup> and its stability has been assessed up to 499 K<sup>59</sup>, above which it transforms into the other carbyne isomer, the semiconducting polyyne, where single alternate to triple bonds. Our goal consists in taking this system as a representative/Gedanken experiment where to identify all the physical elements necessary for observing second sound. In order to do that we develop a procedure based on model-potential Molecular Dynamics (MD) that allows to accurately simulate laser-induced TTG by spanning time-, lengthand temperature- ranges significantly larger than the experimental ones. Using this procedure, we predict second sound at room temperature for cumulene chains with lengths up to hundreds of microns. We, as well, estimate the second sound velocity  $v_{ss}$  as large as 2.680 Km/s, in good agreement with the one estimated using the microscopic derivation of Hardy<sup>36</sup>.

From a theoretical point of view a predictive theory resides on the good description of the harmonic (i.e. the phonon distribution, population and group velocities) and the anharmomic (i.e. phonon lifetimes and scatterings rates) properties of the system under study. By just considering first order anharmonicity and so three phonons scatterings, the only possible processes <sup>†</sup> are those in which two phonons combine to give a third one and viceversa  $\mathbf{q}_1 + \mathbf{q}_2 \rightleftharpoons \mathbf{q}_3$ . At the same time, conservation of energy requires  $E_1 + E_2 = E_3$  where  $\mathbf{q}_{1,2,3}$  and  $E_{1,2,3}$  are the wave-vectors and the

deed a feature limiting the frequencies of the detectable second sound signal to just few GHz. All the above issues are even more severe when dealing with 1D materials, where the limitations in time- and length- resolution (as well as the the difficulties in their synthesis) make the experimental detection of second-sound very difficult. In this perspective, the atomistic simulations are an alternative tool to address phenomena occurring at time and length scale which are experimentally hard to address. It is worth stressing that 1D systems are extensively investigated since they represent a convenient playground for both analytical and computerbased investigations; furthermore, the thermal conductivities  $\kappa$  in 1D systems are found to depend on the system length L and will eventually diverge in the thermodynamic limit  $L \rightarrow \infty$ . This issue has captured the attention of the community and 1D systems are considered perfect test cases for better understanding the condition for the non-validity of the Fourier's heat conduction law. The overall momentum conservation appears to be a key factor for the anomalous behaviour<sup>43-49</sup>, even with some exceptions such as 1D coupled rotator system 50-52 and the chain with a double-well potential<sup>53</sup>, however only a few studies have focused their attention on second sound<sup>32,51</sup>: besides ideal single chains described with different model potentials<sup>54</sup> and carbon nanotubes<sup>32</sup>, no other studies described wave-like transport on these systems.

 $<sup>\</sup>ast$  Unless the presence of other phonon scattering mechanisms becomes effective in the region of small  ${\bf q}.$ 

<sup>†</sup> Conservation of energy forbids the simultaneous creation or annihilation of phonons even-though terms to this effect appear in the interaction Hamiltonian.





**Fig. 1** Phonon dispersion curves of cumulene obtained via first principles Density Functional Theory (DFT) calculations (black solid lines) a standard Class II model potential (MP) (blue solid lines)<sup>55</sup> and the present optimized Class II MP with the inclusion of cross-coupling terms (red solid lines).

energies of the three individual phonons. As long as  $\mathbf{q}_1$ ,  $\mathbf{q}_2$  and  $\mathbf{q}_3$  stay all inside the 1st Brillouin Zone (BZ) this process will be called Normal scattering. If, on the opposite,  $\mathbf{q}_1$  and  $\mathbf{q}_2$  are so large to make their sum  $\mathbf{q}_3$  to lie outside the 1BZ, it will become necessary the addition of a reciprocal lattice vector  $\mathbf{G}$  in order to fold  $\mathbf{q}_3$  back to its equivalent wave-vector within the 1BZ ( $\mathbf{q}_1 + \mathbf{q}_2 = \mathbf{q}_3 + \mathbf{G}$ ). This corresponds to an Umklapp process. On the basis of this definition, it is evident the need to accurately reproduce the phonon dispersion over the entire first BZ in order to correctly mimic the good momentum and energy conservation conditions associated with each scattering event.

#### 2 Results and discussion

We developed and implemented in LAMMPS<sup>60</sup> a specific Class II force field<sup>61</sup> able to reproduce the phonon dispersion curves calculated at the Density Functional Theory (DFT) level (see the ESI<sup>†</sup> for all the technical details). Fig.1 shows the comparison between the phonon dispersion curves obtained by the adopted model potential (red lines) and DFT (black lines). For sake of comparison we also report the phonon dispersion previously obtained by a different force field 55 showing a much less satisfactory agreement with DFT. Such an unsatisfactory description of the phonon spectrum might lead to an incorrect description of i) Umkapp/Normal relative proportion, ii) mean free paths lengths of the heat-carriers and iii) intrinsic thermal conductivity (see the ESI<sup>†</sup>). We stress that our potential (containing anharmonic and cross-coupling terms) allows to describe the quadraticity of the degenerate trasversal acoustic modes (TA) as well as the Kohn anomaly occurring in the longitudinal acoustic mode (LA), both important features missing in Ref. 55. It is then of fundamental importance to accurately describe all the interatomic interactions within the system since thermal transport features (e.g wavelike/anomalous, diffusive transport) are sensitive to the specific intrinsic and extrinsic source of scattering included <sup>50,51,62,63</sup>.

The simulation procedure used to mimic time-resolved opti-



**Fig. 2** Top: time evolution of the of the normalized amplitude  $A(t)/A_0$  of the temperature profile along a cumulene chain with length  $L_x$ =1.228  $\mu$ m. The red line is obtained by fitting the A(t) decays with the approximate 1D solution of the heat and Maxwell, Cattaneo, and Vernotte equation. The inset shows the initial temperature profile imposed along the cumulene chain with the corresponding spatial period  $\lambda$  and amplitude  $A_0$ .

cal measurements proceeds through two steps. At first, an initial sinusoidal temperature profile  $T(x,t) = T_0 - A_0 \cos(qx)$  (where  $q = 2\pi/\lambda$ ,  $\lambda$  the spatial period,  $A_0 = 10$  K the initial profile amplitude and  $T_0$  the average temperature) was imposed to a single cumulene chain with length  $L_x$ . Thermalization was next performed by ideally (i) dividing the system in segments, (ii) exciting all the allowed vibrational modes of each segment at a local value of temperature by means of a white Langevin thermostat, (iii) periodically varying the local value of temperature along the chain backbone. As a matter of fact, such an initial non-equilibrium condition corresponds to white Langevin thermostatting. The second step consisted in the removal of the Langevin thermostat. The following transient relaxation of the cumulene chain towards a stationary temperature profile was studied in a microcanonical ensemble by monitoring the time evolution of the amplitude A(t)and the temperature profile T(x,t) with a time-resolution as small as 10 ps. All the simulations have been performed by integrating the equation of motions using the velocity-Verlet algorithm with a time step of 0.1 fs. In order to suppress statistical fluctuations, an average over N trajectories (where N varies from 40 up to 1600, depending on the chain length) was performed to obtain the final A(t) profiles. Each simulation corresponding to a specific  $\lambda$  value has been performed using periodic boundary conditions in a simulation box with length  $L_x = 3\lambda$ . In detail, for  $\lambda = 0.0409$ , 0.409, 4.090 and 40.90  $\mu$ m the corresponding lengths  $L_x$  of the simulation box were 0.1228 (10<sup>3</sup> atoms), 1.228 (10<sup>4</sup> atoms), 12.28 and  $(10^5 \text{ atoms})$  and 122.80  $\mu m$  (10<sup>6</sup> atoms) respectively. The corresponding maximum simulation times were 50, 200, 1800 and 15000 ps. Fig.2 shows the time evolution of the normalized amplitude  $A(t)/A_0$  of the temperature profile along a cumulene chain with length  $L_x = 1.228 \ \mu m$ . The spatial period of the temperature profile was set as  $\lambda = 0.41 \ \mu m$ . Damped oscillations are observed with a sign flip in A(t) after  $\sim 27$  ps. As pointed out in Ref. 23, this behaviour implies that the spatial phase of the initial sinusolidal temperature profile has shifted by  $\pi$ ; or, equivalently, the



**Fig. 3** Time evolution of the sinusoidal temperature profile for cumulene. The sinusoidal temperature profile is initially flattened during the first  $\sim$ 27 ps. During the next 10 ps we observe a  $\pi$  shift of the sinusoidal temperature profile which is eventually damped out being definitely flat at t $\sim$ 200 ps. For the sake of clarity the temperature profile at t=37 and 200 ps have been multiplied by a factor 2.5.

local maxima converted into minima and viceversa, key feature of wave-like propagation since in principle, in the diffusive regime maxima and minima should not switch simply because the heat moves only from hotter to colder regions. This scenario is fully confirmed in Fig.3, where we clearly observe that the sinusoidal temperature profile is at first quickly flattened (corresponding to A(t) = 0) during the first ~27 ps; next, the signal amplitude undergoes a  $\pi$  phase shift reaching its maximum negative amplitude at t~37 ps. The following profile evolution consists in similar phase oscillations with increasingly damped amplitude. Eventually at t~200 ps the temperature profile becomes definitely flat.

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The heat equation best describing mesoscopic wave-like thermal transport is the phenomenological hyperbolic Maxwell-Cattaneo-Vernotte (MCV) equation:

$$\tau_{ss}\frac{\partial^2 T}{\partial t^2} + \frac{\partial T}{\partial t} = \alpha \nabla^2 T \tag{1}$$

where is  $\alpha$  is the thermal diffusivity and  $\tau_{ss}$  is the thermal relaxation time. The MCV equation describes the propagation of a temperature wave with a damping term equal to  $\partial T/\partial t$  and a corresponding velocity  $v_{ss} = \sqrt{\alpha/\tau_{ss}}$ . The MCV 1D solution under periodic boundary conditions is <sup>64</sup>:  $A(t) \sim \exp(-t/2\tau_{ss})\cos(qv_{ss}t)$ , where  $q = 2\pi/\lambda$  is the wavevector and  $v_{ss}$  is the second sound velocity. We observe from Fig.2 (full red line) that such a solution provides a pretty accurate fit of the amplitude decay generated by the above MD simulations, further confirming the wave-like nature of thermal transport in this case. Moreover, the present fitting procedure allows us to estimate  $v_{ss}$  and  $\tau_{ss}$  for different spatial periods and temperatures (see the ESI<sup>†</sup>). As mentioned above the occurrence of a wave-like thermal transport is due to the dominance of Normal over border and Umklapp phonon scattering events. By rising the temperature an increase in the occurrence of Umklapp processes is expected with then a corresponding transition towards the diffusive regime. We investigated this phenomenon by studying the time evolution of the amplitude A(t)in a chain with length  $L_x$ =12.280  $\mu$ m at three different average temperatures 30 K, 300 K, and 450 K. In these simulations we set  $\lambda\!=\!4.09~\mu\text{m}.$ 

In order to quantitatively analyse the transition from the hydrodynamic to the diffusive transport, we perform the Fourier transform  $F^A(\omega)$  of the time dependent amplitude as shown in Fig. 4. At T=30 K, we observe a peak at a frequency ~0.6 GHz in the same range of the "second sound" peaks observed in graphite<sup>23</sup> for similar spatial periods. At T=300 K this peak is significantly damped, while at T=450 K it disappears. In this latter case we observe the typical functional form  $F^A(\omega) \sim a/(a^2 + \omega^2)$  corresponding to the Fourier transform of an exponential decay  $e^{(-at)}$ . Other details of the calculated  $F^A(\omega)$  are discussed in the ESI†.

In general, the experimental limitation in time-resolution prevents also to probe the system response for initial spatial periods lower than few  $\mu$ m. Instead, by exploiting the extremely high resolution (100 GHz) of our MD simulations, we can address the system response for initial spatial periods spanning 4 order of magnitudes (from 0.04  $\mu$ m up to 40  $\mu$ m). The results in Fig.4 show that second sound occurs in cumulene at T=300 K provided that a suitably short modulation of the initial temperature profile is set up. More specifically, Fig.4 shows a clear peak at T=300 K at a frequency  $\sim$ 12 GHz for  $\lambda$  =0.409  $\mu$ m. For  $\lambda$  =4.090  $\mu$ m, we observe a shift of the peak down to  $\sim$ 0.6 GHz and a corresponding damping of the intensity. Finally, for  $\lambda = 40.900 \ \mu m$ , the peak completely disappears. In general, we observe a shift towards lower frequencies by increasing  $\lambda$  as shown in Fig. 5. As reported for graphite<sup>23</sup>, we observe a nearly linear dependence  $\omega = \omega(q)$ , which allows us to estimate the corresponding second sound velocity  $v_{ss} = 2.680 \pm 0.055$  Km/s at T=30K in remarkable agreement with the  $v_{ss} = 2.470 \pm 0.18$  Km/s obtained at the same temperature by fitting the A(t) time-decay with the approximate solution of the Maxwell-Cattaneo-Vernotte as explained above. Interestingly, this value is also comparable with the one of graphene (1.9-2.0 Km/s) at the same temperature<sup>21,24</sup>. As expected, this velocity is much lower with respect to the sound velocity in cumulene, which we estimated from the phonon dispersion curves

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**Fig. 4** Fourier transform  $F^A(\omega)$  of the amplitude A(t) for three different average temperatures: 30 K (blue lines), 300 K (black lines) and 450 K (red lines) at three different spatial period:  $\lambda$ =0.404  $\mu$ m (dashed lines), 4.090  $\mu$ m (solid lines) and 40.900  $\mu$ m (dash dot line).

of Fig. 1 as large as 36 Km/s, in very good agreement with the value of 31.5 km/s obtained by DFT<sup>65</sup>. In order to assess the validity of this procedure, we independently estimate  $v_{ss}$  according to Ref. 36

$$(v_{ss})^2 = (C_0 V^{-1}) \sum_k \frac{d\langle N_k \rangle_0}{dT_0} \hbar \omega_k \frac{1}{3} v_k \cdot v_k$$
(2)

where  $C_0$  is the system specific heat at temperature  $T_0$ , V the system volume,  $\langle N_k \rangle_0$  the equilibrium phonon distribution,  $\omega_k$  and  $v_k$  the phonon frequencies and the corresponding group velocities. We estimated  $v_k$  and  $\omega_k$  by diagonalizing the cumulene dynamical matrix whose elements have been obtained by the adopted potential. The get  $v_{ss}$ =2.538 Km/s is in excellent agreement with the MD value. This result finally assess the reliability of the presented MD procedure to estimate the second sound velocity.

Standard features of wave propagation in nonlinear optical media are also higher harmonic generation and sum-frequency generation. At the present stage our simulation procedure does not in principle allow to detect any nonlinear phononic phenomena due to the fact that the spatial sinusoidal temperature profile is initialized by a "white" thermalization, i.e. by exciting all the vibrational degrees of freedom. An alternative procedure, which could in principle detect any nonlinear phononic behaviour, should initially thermalize the cumulene chain by selecting a specific phonon mode, e.g. by exciting the displacement pattern of a specific mode, see for example our implementation in Ref. 66. Then, by monitoring the time evolution of the spectral energy density, it is in principle possible to detect nonlinear phonic behaviours such as second harmonic generation or sum-



**Fig. 5** Black circles: frequencies of the second-sound peaks as a function of the wavevector q (equal to  $2\pi/\lambda$ ) at T=30 K and for  $\lambda$  ranging from 0.04  $\mu$ m up to 40  $\mu$ m. The red dashed line represents the corresponding linear fitting function.

frequency generation, see e.g. Ref. 67.

#### 3 Conclusions

In conclusion, by means of molecular dynamics we have simulated time-resolved optical measurements aimed at unveiling wave-like features in the transport of heat. We applied this procedure to a single  $\mu$ m-long cumulene chain predicting for such system second sound even at room temperature. The transition is observed by raising the temperature and activating the Umklapp process connected with the dynamical interactions between CC stretching vibrational coordinates. This behaviour finds complete analogy with the transition from anomalous to normal behavior observed in other 1D chains where by tuning the temperatures it is possible to switch on/off channels of scattering which destroy the momentum conservation <sup>50,51,63</sup>. Moreover we have also been able to prove how by tuning the length of the initial sinusoidal spatial period  $\lambda$ , it is possible to modulate the transition from the hydrodynamic to the diffusive regime. The present procedure allows also to estimate via three different theoretical methodologie a cumulene second sound velocity  $v_{ss}$  in the range [2.4-3.2] Km/s.

#### **Conflicts of interest**

There are no conflicts to declare.

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