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## **Archeomagnetic intensity investigations of French medieval ceramic workshops: Contribution to regional field modeling and archeointensity-based dating**

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1 **Archeomagnetic intensity investigations of French Medieval ceramic workshops:**  
2 **Contribution to regional field modeling and archeointensity-based dating**

3

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19

20 **Keywords**

21 Archeointensity, Medieval period, Western Europe, Field intensity modeling, Archeointensity  
22 dating

23

24

25

## 26 **Highlights**

- 27 • 7 new Triaxe archeointensity data are obtained from French medieval pottery
- 28 workshops
- 29 • They allow a refinement of the evolution of intensities during the High Middle Ages
- 30 • A set of available intensity data is re-examined based on cooling rate correction
- 31 • We illustrate the sensitivity of regional intensity models to modeling strategies
- 32 • We discuss two different procedures for archeointensity dating

33

## 34 **Abstract**

35 Seven new archeointensity data are obtained through the analysis of groups of pottery and  
36 kiln fragments from ceramic workshops unearthed in France, precisely dated from the High  
37 Middle Ages. The measurements are carried out using the Triaxe magnetometer, following a  
38 dedicated experimental protocol that takes into account the effects of anisotropy and cooling  
39 rate (CR) on thermoremanent magnetization acquisition. The new data are consistent with the  
40 evolution of intensity variations described by our previous data obtained in France and  
41 Northern Italy, which display between the 5<sup>th</sup> and 10<sup>th</sup> c. a pronounced camel-back shape. In  
42 particular, they provide supporting evidence of an intensity minimum that occurred around  
43 the transition between the 7<sup>th</sup> and 8<sup>th</sup> century. These data, combined with a selection of  
44 previously published results within a 700 km radius of Beaune and re-examined based on CR  
45 correction, formed the basis of new regional mean intensity variation curves based on two  
46 independent modeling approaches. The first algorithm developed by Thébault and Gallet  
47 (2010) based on bootstrapping and now irregularly spaced knots according to the data  
48 distribution gives rather smooth intensity variations, while the second approach proposed by  
49 Livermore et al (2018) based on a transdimensional Bayesian technique shows more abrupt  
50 variations with sometimes stronger amplitudes. We explore the dating potential of these two

51 variations curves, which have an unprecedented resolution, by studying two medieval pottery  
52 workshops. Six fragment groups (three per workshop) are analyzed using the Triaxe protocol,  
53 providing mean archeointensity values for each of the two sites. Two different procedures are  
54 used for their dating, either by comparing the intensity value to be dated with the reference  
55 intensity variation curves obtained from the two modeling techniques or by analyzing the  
56 marginal posterior probability distribution of the age values derived from the method of  
57 Livermore et al (2018). For France, the two techniques yield very similar results. The  
58 archeointensity dating results combined with archeological arguments and radiocarbon data,  
59 make it possible to better constrain the age of the end of activity of the two workshops.  
60 Archeointensity investigation of displaced materials thus appears as an effective means to  
61 obtain original chronological constraints on the age of their production, paving the way for a  
62 wide range of complementary research on Medieval pottery.

63

## 64 **1. Introduction**

65 Archeomagnetism is a method now commonly implemented in the field of archeology  
66 throughout the European area to provide chronological constraints on fired clay artifacts  
67 whose dating requires refinement. This tool is based on the use of local reference curves of  
68 the temporal variations of the geomagnetic field in direction and/or intensity, either directly  
69 obtained from the analysis of numerous dated structures in the region of interest, or, when not  
70 available, deduced from regional or even global time-dependent geomagnetic field models. In  
71 Europe, one may rely on the regional SCHA-DIF.4K field model covering the past four  
72 millennia recently constructed by Pavón-Carrasco et al. (2021), which updates and extends  
73 the previous SCHA-DIF.3K model (Pavón-Carrasco et al. 2009). The following studies  
74 indicate the breadth of existing research and interests in a variety of European countries:  
75 Belgium, Ech-Chakrouni et al. (2013); Bulgaria, Herries et al. (2008); England, Batt et al.



76 (2017); France, Gallet et al. (2009) and Hervé and Lanos (2017); Austria, Schnepp et al.  
77 (2015); Greece, Aidona et al. (2017); Italy, Tema et al. (2014) and Principe et al. (2018);  
78 Spain, Gómez-Paccard and Beamud (2008) and Catanzariti et al. (2007).

79 In France, archeomagnetism is so well integrated into the archeological fabric that this  
80 method is now included in the prescription files of preventive (rescue) excavations when  
81 heating structures are detected in situ at the time of archeological diagnosis prior to  
82 excavation. In the archeomagnetic laboratory founded in the 1930s by Emile Thellier in Saint-  
83 Maur, for instance, several hundred pottery and domestic kilns have been studied since the  
84 early 1990s, and the results used for dating purposes based on the reference directional  
85 variation curve available for the past two millennia (i.e. Thellier, 1981, Bucur, 1994, Gallet et  
86 al. 2002, Le Goff et al., 2002; 2020 in this volume).

87 Compared to in-situ burnt structures, the materials discovered displaced from the  
88 location where they were fired have been much less investigated archeomagnetically, in  
89 particular with the purpose of providing chronological constraints. However, archeomagnetic  
90 studies of large ensembles of architectural bricks or tiles have made it possible to refine the  
91 age of buildings from the inclination information (e.g. Lanos, 2019). On the other hand, the  
92 possibility of using the archeointensity as the only dating element for displaced objects has  
93 not yet been really exploited (Gallet et al., 2014a; Shaar et al., 2020). There are two main  
94 reasons for this: firstly, intensity data have long remained much less numerous than  
95 directional data and knowledge of intensity variations was thus very fragmentary. Secondly,  
96 and despite significant progress in intensity data acquisition all over Europe, the available  
97 data often show a dispersion that de facto limits their application for dating. A recent study by  
98 Casas and Tema (2019) explored the dating potential in Europe of the SCHA-DIF.3K model  
99 and highlighted the low added value of intensity measurements for dating. France, however,  
100 benefits from a relatively dense archeointensity dataset covering the past 1600 years, showing

101 little dispersion (Genevey et al., 2009; 2013; 2016; 2019). These results describe smooth  
102 millennial-scale variations punctuated by a pseudo-periodic (~260 years) succession of  
103 intensity peaks of roughly the same amplitude and each lasting ~200 years (Genevey et al.,  
104 2016; Livermore et al., 2018). Maxima are observed at the beginning of the 7<sup>th</sup> c., during the  
105 9<sup>th</sup> c., the 12<sup>th</sup> c., at the end of the 14<sup>th</sup> c. and at the beginning of the 17<sup>th</sup> century. Genevey et  
106 al. (2016) suggested that this recurrence in intensity peaks could be related to a wave motion  
107 at the top of the core, for example due to stable stratification (see discussion in, e.g., Buffett et  
108 al., 2016). Although the reality of these peaks seems now well established, their description  
109 needs to be improved through the acquisition of new data. A densification of the  
110 archeointensity database is therefore still required, with the same effort being made for the  
111 archeomagnetic directions (see for instance Le Goff et al., 2020 in this volume).

112         With this objective, we present seven new Medieval archeointensity results obtained  
113 from the analysis of precisely dated groups of pottery and kiln fragments. These results allow  
114 a refinement of the reference intensity variation curve available in France. We then explore  
115 the potential of this curve for dating purposes through the study of two ceramic production  
116 sites of the High Middle Ages located in the Centre and Ile-de-France regions. The  
117 construction of the reference curve of geomagnetic field intensities and archeomagnetic  
118 dating are both carried out using two different techniques (Thébault and Gallet, 2010;  
119 Livermore et al., 2018), which allows us to compare them and to illustrate the implications of  
120 selecting one single regional modeling and/or dating option rather than the other.

121

## 122 **2. Description of the collected archeological fragments.**

### 123 **2.1 Dated ceramic sets**

124 Among the new groups of fragments, five come from two ceramic production areas largely  
125 exploited in our previous intensity studies i.e. Saran in the Centre region of France and

126 Vanves located close to Paris, in the Ile de France region (Fig. 1a). At Saran, the analysis of  
127 groups SAR19 and SAR21 completes the archeointensity study of the material from the  
128 excavation zone known as La Guignace (Bouillon, 2015). Another group (SAR36) is  
129 associated with a small production unit known as “la voie nouvelle”, which was discovered  
130 more recently and dated from the first half of the 7<sup>th</sup> century (Jeset, to be published). The two  
131 groups from Vanves, referred to as VAN03 and VAN09, come from the excavations  
132 conducted in Rue Gaudray (Lefèvre and Peixoto, 2015), from which some materials were  
133 already studied for archeointensity (Gallet et al. 2009; Genevey et al. 2016). The VAN03  
134 group has been re-sampled with fragments taken from almost complete pots isolated by A.  
135 Lefèvre because they have a morphology typical of the production of the associated kiln. The  
136 numbering of the fragments from this group thus starts at number 23 (Supp. Table1). The  
137 dating of these five groups is mainly based on typo-chronological constraints previously  
138 described in Genevey et al. (2016). For that reason, we exclusively collected fragments of  
139 pottery lips whose shape is clearly identified and characteristic of the production.

140         The other groups are associated with two ceramic production sites recently unearthed  
141 and both located in the Ile-de-France region, at Hermé (c. 85 km south-east of Paris) and  
142 Chamigny (c. 60 km east of Paris, Fig. 1a). The rescue excavations at the site known as  
143 “Hermé Les Malletons (S.P.M. carrière)” were carried out in 2014 by the French National  
144 Institute for Preventive Archeological Research (INRAP), being motivated by the  
145 establishment of a new quarry. These excavations revealed a discontinuous occupation of the  
146 site from Prehistory to the beginning of the 11<sup>th</sup> c. (Chaudriller, 2019). Focusing on the High  
147 Middle Ages period, the site was a rural settlement during the 7<sup>th</sup> c. with a husbandry activity.  
148 Towards the middle of the 9<sup>th</sup> c. the site evolved and two types of workshop were developed,  
149 linked to metallurgical and ceramic productions. Four pottery kilns document this later  
150 activity. Three phases of production were evidenced: during the second half of the 9<sup>th</sup> c., at

151 the beginning of the 10<sup>th</sup> c., and finally around the end of the 10th century. Only the last two  
152 phases were sampled for archeointensity analysis. Three groups of ceramic fragments (called  
153 HERME01 to HERME03) are respectively associated with the productions of kilns F1621  
154 and F3160 of the intermediate phase (beginning of the 10<sup>th</sup> c.) and with kiln F3060 of the last  
155 phase (end of the 10<sup>th</sup> c.). Unfortunately, none of these pottery fragments provided  
156 archeointensity results (*infra.*). For the last phase, we doubled the sampling with a group of  
157 fragments collected from Kiln 3060 (HERME04). The fragments were taken all along the  
158 central tongue support of the kiln particularly well preserved and made of limestone covered  
159 with a thin clay layer (Fig. 1b). The potsherds that were found inside the kiln show a clear  
160 rupture with respect to the previous productions of the site, whether it concerns the profile,  
161 the edge, or the handle of the pots. Based on the form of the pottery, all fragments were dated  
162 prior to the end of the 10<sup>th</sup> century and a dating between c. 970 and 1000 is thus retained for  
163 the last activity of the kiln (and thus for the HERME04 group). It should be noted that  
164 archeomagnetic dating based on directions was conducted on the same kiln (N. Warmé in  
165 Chaudriller, 2019). A 95%-confidence level dating between 900 and 1080 was obtained using  
166 the new reference curve determined by Le Goff et al. (2020 in this volume). Within this time  
167 window, the interval [940-990] appears however as being the most probable with a maximum  
168 probability c. 960 (see description of the method in Le Goff et al., 2002), which is in good  
169 agreement with the ceramological constraints.

170 At Chamigny, the excavations at the place called "la grande maison" are recent,  
171 carried out in the summer of 2017. Conducted by INRAP, they were prescribed following a  
172 project for the construction of individual houses. Two distinct occupation phases have been  
173 observed on this site: The first is dated to the Neolithic period, then, after a long period of  
174 abandonment, a re-occupation is documented from the end of the 6<sup>th</sup>-early 7<sup>th</sup> c. until the end  
175 of the 10<sup>th</sup> century (Mahé, 2020). It is mainly characterized by metallurgical and pottery

176 activities. Several groups of fragments from the different pottery production units (five kilns  
177 in total) were sampled for archeointensity measurements but only one group (CHAM03) has  
178 provided successful results so far. This group consists of fragments from the working area of  
179 kiln 2629 (Fig. 1c). The dating of this production is constrained by morphological and  
180 stylistic elements given by the numerous fragments found inside the kiln. Among other  
181 elements, one may mention the absence of carinated bowls, the importance of deep shapes  
182 with short collar and re-entrant rim or jugs with a shamrock-shaped tubular spout. They  
183 indicate a dating around the end of the 7<sup>th</sup> c. - very beginning of the 8<sup>th</sup> century (Mahé, 2020).

184

## 185 **2.2 Sets of ceramics collected in order to provide chronological constraints**

186 The first site studied was excavated during the fall-winter of 2015-2016 by the  
187 archeological service of the urban community of the city of Bourges (in the center of France,  
188 Fig. 1a). These excavations were carried out before the construction of a housing estate in the  
189 city La Chapelle Saint Ursin (Bourges's suburbs) at the place called "l'angoulaire, chemin des  
190 vallées aux fruscades" (Marot, 2017). This site mainly revealed the existence of a Roman villa  
191 constructed *ex nihilo* at the beginning of the 1<sup>st</sup> century AD. The villa remained in activity  
192 until the 6<sup>th</sup> c. with successive modifications and enlargements. The last phase saw the  
193 installation of a small ceramic production unit for the inhabitants of the villa and surrounding  
194 area. The objective of our work was to provide chronological constraints about the end of this  
195 pottery activity. To this purpose, we sampled fragments of pottery characteristic of the  
196 production found in the kiln, as well as fragments of the kiln itself. For the pottery, two  
197 groups were collected corresponding to pottery wasters showing deformations for the first set  
198 (BOUR01), and evidence of overfiring for the second (BOUR02). The samples from the kiln  
199 itself correspond to fired clay fragments from the dome that were found in the filling

200 (BOUR03). It may be stressed that no archeomagnetic directional study was carried out at the  
201 time of the excavations.

202         The second site was excavated in 1997 after the fortuitous discovery of a burial site on  
203 private land in Vienne-en-Arthies in the hamlet of Chaudry (50 km northwest of Paris, Fig.  
204 1a). The excavations, made over a small area, were entrusted to the Centre de Recherches  
205 Archéologiques du Vexin Français (CRAVF; Regnard 1999). They revealed the existence of a  
206 pottery kiln of which only the heating chamber was unearthed (the rest of the kiln being  
207 located outside the excavated area). It was filled by a largely standardized ceramic production  
208 of pots for cooking, with a mainly sandy and, to a lesser extent, granular paste. This site is the  
209 only witness currently known of a production in the Vexin Français region (Fig. 1a: area in  
210 yellow) during the Carolingian period, although archeologists presume the existence of a  
211 more important pottery production in this region. Three groups of potsherds were selected  
212 with the objective of better constraining the period of activity of this pottery production,  
213 especially its end. The first two groups consist of fragments with a grey sandy paste  
214 (CHAU01) and grey-brown sandy paste (CHAU02) which are typical of this production,  
215 while the last group comprises fragments with red granular re-baked paste (CHAU03). These  
216 later potsherds were most probably used for the construction of the kiln. We note that this  
217 kiln, only partially excavated, was not sampled for archeomagnetic directional analysis.

218

### 219 **3. Measurements workflow**

220 The workflow in this study is identical in all respects to the one used in our previous  
221 archeointensity studies conducted on Western European artifacts (Genevey et al. 2009, 2013,  
222 2016, 2019). All experiments were carried out at the paleomagnetic laboratory of the Institut  
223 de Physique du Globe de Paris (IPGP).

224           The evolution of magnetic susceptibility in weak field was first measured for each  
225 fragment during heating-cooling cycles between room temperature and c. 500°C. These  
226 measurements were performed using an Agico Kappabridge KLY3-S coupled with a CS3  
227 furnace. The reversibility of the susceptibility curves, evaluated visually, allowed the  
228 selection of the fragments that are *a priori* most favorable for intensity measurements (carried  
229 out over the same temperature range).

230           For each fragment, a first specimen was then measured for intensity determination  
231 using the Triaxe protocol. If the observed behavior met our quality criteria or was promising  
232 for intensity determination, other specimens were then measured. This is also the case if the  
233 chosen temperature range was not adequate for the first specimen. The Triaxe experimental  
234 method and our quality criteria have been extensively detailed in previous publications (e.g.  
235 Le Goff and Gallet, 2004, Gallet and Le Goff, 2006, Genevey et al., 2009, Hartmann et al.,  
236 2010, Gallet et al. 2014b) and recently by Troyano et al. (2021 in this volume). We remind  
237 the reader that the magnetization measurements are performed automatically at high  
238 temperatures following a protocol that takes into account the anisotropy and cooling rate  
239 effects on thermoremanent remanent magnetization (TRM) acquisition, and minimizes  
240 possible effect related to the presence of multidomain grains (Genevey et al., 2009, Hartmann  
241 et al., 2010; 2011, Hervé et al., 2017, Shaar et al., 2020). As for the quality criteria, they aim  
242 to test the stability on heating of the magnetic mineralogy (thanks in particular to magnetic  
243 susceptibility vs. temperature curves), the quality of the individual determination and the  
244 consistency of the results both at the fragment (with a minimum of two specimens per  
245 fragment and an error between them of less than 5%) and fragment group levels. A minimum  
246 of three fragments successfully analyzed per group and an error on the mean intensity value  
247 of less than 10% and 5 $\mu$ T are required. The purpose of the 5%-coherence test is to exclude  
248 fragments for which we can suspect a reliability problem in the recording of the geomagnetic

249 signal. At the site level, our quality criteria aim mainly at assessing the temporal homogeneity  
250 of the fragments forming a group.

251 After the archeointensity experiments, a fragment from each retained group was subjected  
252 to Lowrie's (1990) test to provide further constraints on the magnetic mineralogy of the  
253 archeological collection. The three orthogonal IRM were acquired in a field of 1.5T, 0.4T and  
254 0.2T using a pulse magnetometer MMPM10.

255

#### 256 **4. Results**

257 We analyzed 157 ceramic shards and two groups of kiln fragments. Applying our quality  
258 criteria, three groups (SAR19, SAR21 and HERME04) yield a reasonable success rate  
259 between 50% and 60%. For the rest of the collection, the rate is lower, ranging between 16%  
260 and 36%, the lowest percentages being obtained for the groups studied for dating (i.e. BOUR#  
261 and CHAU#). It should be noted that these rates were calculated in relation to the number of  
262 fragments actually measured on the Triaxe. Several fragments were indeed too weakly  
263 magnetized ( $< \sim 30 \cdot 10^{-8} \text{ Am}^2$ ) with respect to the sensitivity of this magnetometer (Supp. Table  
264 1).

265 The mean intensity values obtained for the different groups of fragments are reported  
266 in Table 1. Here the groups BOUR01 and BOUR02 on one hand, and CHAU01 and CHAU02  
267 on the other hand have been merged for the computation of a mean value as these pairs are  
268 representative of the same pottery production. The eleven mean values hence determined are  
269 well defined with a maximum standard deviation of  $2.9 \mu\text{T}$  (or 3.9% of the corresponding  
270 mean; BOUR01/02 group). The consistency of the intensity results for each group of  
271 fragments is further shown in Figure 2, which presents the data at the specimen level obtained  
272 for six different groups of pottery (SAR36, CHAM03, BOUR01/02 and CHAU01/02) and  
273 kiln fragments (HERME04; BOUR03). Concerning the BOUR03 group, which consists of



274 fired clay fragments from the kiln dome, significant variations in colour were observed at the  
275 fragment scale, from bright red, to wine-red and brown. Of the 33 specimens tested, only the  
276 browns provided suitable results. For HERME04, the 30 specimens analyzed were taken  
277 exclusively from the limestone part of the fragments. The thin clay layer was indeed too  
278 weakly magnetized to allow analyses using the Triaxe. Such weak magnetization appears to  
279 be a characteristic of the majority of the potsherds collected at Hermé. Other shards from this  
280 site were further discarded due to strong alteration detected during the magnetic susceptibility  
281 measurements with the consequence, as previously mentioned, that no intensity results were  
282 obtained for the Hermé pottery production.

283         The alteration of the magnetic mineralogy revealed by the non-reversibility between  
284 the heating and cooling magnetic susceptibility curves is one of the reasons for the exclusion  
285 of several fragments (Figs. 3a,b). In almost equal proportions (i.e., 16% versus 14%),  
286 fragments were also discarded when it was impossible to isolate reliably their primary  
287 magnetization component. This is illustrated in Figure 3c where the thermal demagnetization  
288 of specimen CHAU01-10A reveals two magnetization components with widely overlapping  
289 unblocking temperature spectra, which prevented the ancient TRM from being clearly  
290 isolated. In the intensity diagram, this results in complex evolutions in the  $R'(Ti)$  data  
291 between  $T_1$  (or  $T_1'$ ) and  $T_2$ , with significantly varying values (Fig. 3d). In general, however,  
292 most failures in intensity determination at the specimen level (70%) are related to “non-ideal”  
293 Triaxe behavior, as defined by our quality criteria, observed in the intensity diagrams, i.e.,  
294 with non-constant  $R'(Ti)$  ratios over the temperature range where the primary magnetization is  
295 isolated. Specimen HERM04-08A illustrates this problem with a single component  
296 demagnetized between 150°C to 520°C (Fig. 3e) while decreasing  $R'(Ti)$  ratios are observed  
297 over the same temperature range (Fig. 3f). In rare other cases, the  $R'(Ti)$  ratios have a concave  
298 shape, also leading to the rejection of the specimen.

299           The thermal demagnetization of the 3-axis IRMs (recall that one fragment among  
300 those successfully analyzed was chosen for each group) shows a very classical magnetic  
301 mineralogy for baked clay artifacts (Fig. 4). The latter is first characterized by the  
302 predominance of low coercivity minerals (less than 0.2 T) with unblocking temperatures of  
303 less than 600 °C. These minerals are likely from the magnetite family with a different level of  
304 impurities. The thermal demagnetization of the hard component (1.25 T) also indicates the  
305 presence in various proportions of a high-coercivity magnetic phase with unblocking  
306 temperatures lower than 200-250 °C. These properties are compatible with those of the  
307 epsilon iron oxide, which is widespread in the materials analyzed in archeomagnetism (e.g.  
308 Chauvin et al. 2000; Hartmann et al. 2011; Genevey et al. 2016; López-Sánchez et al. 2017;  
309 2020 in this volume). Note that the presence of hematite is not clearly attested in our  
310 collection. Finally, Figure 4 shows several examples of magnetic susceptibility vs  
311 temperatures curves. Although these measurements do not provide additional information on  
312 the magnetic mineralogy (since the heating is only conducted up to 500-520 °C), they  
313 illustrate the reversibility criterion applied on magnetic susceptibilities which is taken into  
314 account in our archeomagnetic studies.

315

## 316 **5. Selection of data available within a 700 km radius of Beaune with a focus on the** 317 **cooling rate effect**

318 Our seven precisely-dated new results are reported in Figure 5 together with our previous data  
319 obtained mainly in France, but also in Belgium (for one datum) and more recently in Tuscany  
320 in northern Italy. As in our last publication, all data have been reduced to the common site of  
321 Beaune in Burgundy (47.02°N, 4.84°E). At this stage, we observe that the new results are  
322 consistent with the intensity variations described from our previous datasets which display  
323 between the 5<sup>th</sup> and 10<sup>th</sup> c. a pronounced camel-back shape (Genevey et al., 2016). They make

324 it possible to better define the hump that occurred during the 7<sup>th</sup> and 8<sup>th</sup> c., with a maximum  
325 reached around 600 AD followed by a decrease until the beginning of the 8<sup>th</sup> century.  
326 Moreover, Hermé's result dating from the end of the 10<sup>th</sup> c. helps to trace more precisely the  
327 strong and remarkable decrease in intensities, by  $\sim 20 \mu\text{T}$ , which occurred between the  
328 beginning of the 9<sup>th</sup> c. and the end of the 10<sup>th</sup> century.

329         Other archeointensity results dating from the past 1700 years were previously obtained  
330 within the 700 km-radius of Beaune. As in our previous publications, these data were  
331 examined through a set of selection criteria, retaining only those obtained using Thellier and  
332 Thellier (1959) derived protocols including at least two pTRM-checks or with the Shaw  
333 (1974) method. The number of intensity results used to derive the mean is required to be  
334 greater or equal to three and the errors around the mean value must be of less than 15% (this  
335 threshold is therefore less restrictive than the one used for our own data). The TRM  
336 anisotropy must also be taken into account when objects more sensitive to this effect are  
337 analyzed (such as pottery or tiles). An additional criterion concerns the age uncertainties,  
338 which must be less than or equal to  $\pm 50$  years. Applying these criteria, the remaining dataset  
339 comprises results obtained by Chauvin et al. (2000) and Gómez-Paccard et al. (2012) with  
340 respectively seven and four data from France, Casas et al. (2005) (one English result),  
341 Donadini et al. (2008) and Donadini et al. (2012) with respectively one and two data from  
342 Switzerland, and Schnepf et al. (2020 in this volume) with four data from Germany. Eleven  
343 of these data were derived from the study of in-situ burnt structures, i.e., kilns or fireplaces,  
344 with analyzed samples from bricks (five data) and baked clay (five data), while baked rocks  
345 were collected in one case. The eight other results were obtained from the analysis of artifacts  
346 discovered displaced from the location where they were produced: bricks in seven cases and  
347 tiles in the last one.

348           The cooling rate (CR) effect is another parameter whose importance has been  
349 discussed in several studies (for a general discussion see Brown et al. (2021) in this volume,  
350 but also Genevey et al. 2003, 2008, Hervé et al., 2019; Kostadinova-Avramova and  
351 Jordanova, 2019; Jones-Cervantes et al., 2020). With regard to the correction of this effect,  
352 different strategies were implemented for the 19 data above. In particular, it was not  
353 considered by Casas et al. (2005), whereas it was evaluated for each analyzed fragment by  
354 Chauvin et al. (2000). The mean values per group of fragments were then computed using  
355 only CR-corrected data. The situation is more complex for the other studies. For the data  
356 obtained by Gómez-Paccard et al. (2012), the CR effect is evaluated for each fragment but a  
357 correction is applied only when the percentage of alteration is lower than the percentage of  
358 CR correction. We recall that the alteration percentage is calculated from a loop-back test  
359 identical to a pTRM-check. It allows us to ascertain the stability of the magnetic mineralogy  
360 from measurements specifically dedicated to the evaluation of the CR effect. The average per  
361 group of fragments was then calculated combining both uncorrected and CR-corrected  
362 intensity determinations. The values concerned are reported in Supplementary Figure 1. For  
363 the result obtained at Angers, the majority of the values (86%) were CR-corrected and the  
364 general mean calculated by Gómez-Paccard et al. (2012) ( $81.3 \pm 10.8 \mu\text{T}$ ) is consistent with the  
365 average obtained using only the CR-corrected data ( $82.7 \pm 11.3 \mu\text{T}$ ). For the other three groups,  
366 only 33 to 38% of the collection were CR-corrected, leading to three different situations. For  
367 the Mont-Saint-Michel site, the CR-corrected values show the same distribution as the  
368 uncorrected ones (supp. Fig. 1). Therefore, the mean value calculated with all the data or with  
369 only the CR-corrected data is fairly similar ( $69.9 \pm 7.0 \mu\text{T}$  versus  $70.0 \pm 7.4 \mu\text{T}$ ). At Pierrefitte-  
370 sur-Sauldre, the CR-corrected data are in the middle of the distribution of all the values (supp.  
371 Fig. 1), and the mean calculated using only these data ( $83.6 \pm 1.1 \mu\text{T}$ ) presents an error much  
372 smaller but within the uncertainty interval of the mean derived from all data ( $89.3 \pm 8.7 \mu\text{T}$ ).

373 Finally, for the fragment group at Saran, the CR-corrected values are all much lower than the  
374 uncorrected ones (supp. Fig. 1). The mean obtained from the CR-corrected values has a  
375 smaller error ( $67.8 \pm 3.6 \mu\text{T}$ ) but, above all, it is not compatible with the average calculated  
376 using all the data ( $79.9 \pm 8.3 \mu\text{T}$ ). It is interesting to note that this group corresponds to  
377 fragments from a kiln sampled at Saran, whose filling has already been analyzed by Genevey  
378 et al. (2016) (A36/SAR08 group) who found a mean intensity of  $72.0 \pm 3.6 \mu\text{T}$ . Genevey et al.  
379 (2016) proposed a possible time gap between the last use of the kiln and its filling to explain  
380 the difference between the results, although there is no archeological evidence to support this  
381 option. Considering only the CR-corrected data obtained by Gómez-Paccard et al. (2012) now  
382 leads to a mean intensity value ( $67.8 \pm 3.6 \mu\text{T}$ ) compatible with that of Genevey et al. (2016). It  
383 thus appears that the strategy used by Gómez-Paccard and co-authors is not adequate in  
384 certain circumstances, in particular when the distributions of the CR-corrected and non-  
385 corrected values are different. Below, for the results of Gómez-Paccard et al. (2012), we  
386 chose to retain only the mean values computed using the CR-corrected data.

387 We also analyzed in more detail the result obtained by Donadini et al. (2008). Here  
388 again the situation is different with fragments from the same medieval kiln analyzed both in  
389 the paleomagnetic laboratory at Helsinki and Sofia. At Helsinki, small (volume  $1 \text{ cm}^3$ ) and  
390 larger (volume  $8 \text{ cm}^3$ ) samples were measured, and a fan was used for cooling the fragments  
391 during the Thellier experiments. At Sofia, only large samples (volume  $8 \text{ cm}^3$ ) were studied  
392 and the oven used for the Thellier experiments was left cooled without a fan. As expected, the  
393 mini-samples systematically gave higher values (Supp. Fig. 1). An arbitrary decrease of 10%  
394 accounting for the CR effect was thus applied to those data by Donadini et al. (2008), which  
395 *de facto* reduced the difference with the other results, but still with higher values (Supp. Fig.  
396 1). The mean intensity value for this medieval kiln was computed by combining the data from  
397 the large samples (Helsinki and Sofia) without changes and those from the mini samples

398 corrected by 10%. This leads to a mean value with a small error ( $86.85 \pm 1.49 \mu\text{T}$ ) which likely  
399 does not express the real uncertainties associated with this determination. We have preferred  
400 to keep only the results from the Sofia analyses (large samples, no fan,  $83.9 \pm 3.9 \mu\text{T}$ ),  
401 assuming they are less affected by the CR effect although a residual CR effect is possible.

402 The next set of two data was acquired by Donadini et al. (2012) from Medieval  
403 fireplaces unearthed in Zurich. The sample's volume is  $8 \text{ cm}^3$ , therefore corresponding to that  
404 of the big samples in the 2008 study (i.e. those for which no CR correction was applied). No  
405 CR experiment was performed; instead, an educated-guess decrease of 10% was applied to  
406 both data. Given the uncertainty about the relevance of this arbitrary correction, we have  
407 preferred not to retain these two values.

408 The last data set recently acquired by Schnepf et al. (2020) includes four data obtained  
409 by the Thellier method, in its original version or in the version modified by Coe (1967), but  
410 only three of them were CR-corrected, with an experimental evaluation of this effect for each  
411 specimen. We therefore retained these three data, while the fourth result for which the CR-  
412 effect was not explored was discarded. For the same reason, we also did not retain the result  
413 of Casas et al. (2005). In our region of interest, Schnepf et al. (2020) also obtained several  
414 intensity results using the multi-specimen method (Biggin and Poidras, 2006; Dekkers and  
415 Böhnell, 2006) according to the so-called MSP-DSC technique developed by Fabian and  
416 Leonhardt (2010). Without prejudging their reliability nor consistency with the other data, we  
417 chose at this stage not to consider them because the CR-effect on the multi-specimen results  
418 would still deserve further investigation (Schnepf et al., 2020).

419 This leaves us with the original dataset of Chauvin et al. (2000), four mean results  
420 from the Gómez-Paccard et al. (2012) study calculated using only the CR-corrected data, one  
421 result from Donadini et al. (2008) derived from the analysis of big samples at Sofia laboratory  
422 where no fan was used and the three CR-corrected data from Schnepf et al. (2020 in this

423 volume). These twelve data are reported in Figure 5. They are all consistent with our own  
424 dataset (e.g., Genevey et al., 2019), thus entering in the same evolutionary trend, albeit often  
425 showing either higher or lower intensity values.

426

## 427 **6. Construction of a secular variation curve**

428 In our previous studies focused on the field intensity variations in Western Europe  
429 over the past 1600 years, we successively applied two modeling strategies to derive a mean  
430 variation curve. Genevey et al. (2013; 2016) used the approach developed by Thébault and  
431 Gallet (2010) based on an iteratively reweighted least-squares inverse technique combined  
432 with a bootstrap algorithm exploring the intensity and dating uncertainties of each data point.  
433 It allows the computation of a large set of individual models using cubic B-splines whose  
434 knots are evenly spaced, according to the average of the time intervals between data. The time  
435 interval between two knots was equal to 70 years in Genevey et al. (2013) and 50 years in  
436 Genevey et al. (2016). A master curve is then provided in the form of probability density  
437 function (pdf) as a function of time. One of the objectives of this approach is to reduce the  
438 effects of possible outliers. This is achieved thanks to the use of Huber weights for the  
439 experimental data errors, the latter being normally distributed within one standard deviation  
440 and less steeped beyond, and a re-weighted least-squares scheme. An important point is that  
441 the algorithm now includes uneven knot positions, according to the temporal distribution of  
442 the data, which allows us to provide a more robust and detailed determination of the intensity  
443 field variations.

444 More recently, Genevey et al. (2019) used the transdimensional Bayesian method  
445 developed by Livermore et al. (2018), which is based on piecewise linear regression of the  
446 available data. The number and temporal distribution of the linear segments are imposed by  
447 the data according to their experimental and dating uncertainties, without a priori hypothesis

448 on the complexity of the intensity variations to be determined (i.e. with a minimum level of  
449 regularization). A perturbation procedure called AH-RJMCMC (for Age Hyperparameter -  
450 Reverse Jump Monte Carlo Markov Chain; see explanations in Livermore et al., 2018) allows  
451 the determination of a large ensemble of models whose distribution (pdf), mean, median,  
452 mode and 95% credible interval are provided, as well as the posterior intensity and age  
453 distributions of each individual datum (Livermore et al., 2018, 2021 in this volume; see also  
454 Lanos, 2004; Helliou and Gillet, 2014; Hervé and Lanos, 2017). All calculations are made  
455 using a wide prior distribution of the intensity values for each knot common to two  
456 consecutive segments, which has been here chosen between 35  $\mu\text{T}$  and 95  $\mu\text{T}$ ; the maximum  
457 number of knots over the entire documented time interval is conservatively set to 150.  
458 Finally, it should be noted that both techniques allow us to take into account a possible time-  
459 order relationship between subsets of the data.

460         The two approaches above were used to calculate the intensity variations within the  
461 700 km-radius of the city of Beaune in France. The computations are carried out using either  
462 our own dataset alone (Figs. 6a,c; supp. Table 2), which has the advantage of being very  
463 homogeneous from an experimental point of view, or our data combined with those described  
464 in Section 5 (Figs. 6b,d; supp. Table 2), the latter being modified along the lines discussed in  
465 this section. A good agreement is observed between the different variation curves displayed in  
466 Figure 6, which all show the same evolution mainly characterized by a series of century-scale  
467 intensity maxima. Such an agreement is not surprising given the density of the data and their  
468 overall good consistency. In detail, however, some differences are observed which are  
469 intimately linked to the methods used for the computations.

470         Firstly, the intensity variations are smooth when derived from the Thébault and Gallet  
471 (2010) method which considers a certain level of regularization and for which each model is  
472 constructed using cubic-B-splines, whereas the use of linear segments in the case of the



473 method developed by Livermore et al. (2018) gives more abrupt variations. Secondly, the pdf  
474 calculated from the two datasets using the Thébault and Gallet (2010) algorithm are fairly  
475 similar, which is expected as they differ by the addition of only twelve results. It is also worth  
476 recalling that the bootstrap algorithm tends to attenuate the effect of deviant results, and thus  
477 to determine the most robust intensity variations. Conversely, in the method developed by  
478 Livermore et al. (2018), a single result can have a significant effect on the pdf, especially if its  
479 uncertainty is small. This is well illustrated by a result at the 6<sup>th</sup>/7<sup>th</sup> c. transition obtained by  
480 Gómez-Paccard et al. (2012), with quite small experimental (1.1 $\mu$ T) and dating (65 years)  
481 uncertainties, which is higher in intensity than the other data available in the same period.  
482 When incorporated in the calculations (compare Figs. 6c and 6d), it significantly increases the  
483 amplitude of the intensity peak, whereas its effect is very minor with the Thébault and Gallet  
484 (2010) method (compare Figs. 6a and 6b). Similarly, three results obtained by Chauvin et al.  
485 (2000) between the end of the 14<sup>th</sup> c. and the first half of the 15<sup>th</sup> c. appear higher than the  
486 other data documenting this period, while one result from Schnepf et al. (2020) dated to the  
487 middle of the 13<sup>th</sup> c. is significantly lower. Here again, the incorporation of these data in the  
488 computations based on the bootstrap algorithm has little effect on the pdf (Figs. 6a,b). On the  
489 other hand, these results significantly modify the pdf obtained from the AH-RJMCMC  
490 method (compare Fig. 6c and 6d). When the data are not taken into account in the calculations  
491 (Fig. 6c), the mode of the pdf shows a linear evolution between  $\sim$ 1000 and  $\sim$ 1500, while two  
492 intensity peaks during the 11<sup>th</sup> c. and the 14<sup>th</sup> c. are only inferred from the medians, averages  
493 (the latter are not shown in Figs. 6c,d) and shape of the 95% confidence intervals of the pdf,  
494 which thus leads to rather ambiguous information. When they are taken into account (Fig.  
495 6d), the modes of the pdf then become similar to the medians and the averages, showing the  
496 same two intensity peaks that are clearly displayed by the method of Thébault and Gallet  
497 (2010) whatever the dataset used (Figs. 6a, b).

498           The example above highlights the fact that a small amount of data can have a  
499 significant influence on the statistics of the models derived from the method developed by  
500 Livermore et al. (2018), in particular over a time interval wider than that strictly covered by  
501 these data. In addition, it should be noted that the 95% credible intervals provided by the AH-  
502 RJMCMC method are often wider than those given by the Thébault and Gallet (2010) method  
503 (see in particular between c. late 10<sup>th</sup> c. and early 13<sup>th</sup> c.), and the individual models are more  
504 dispersed inside the credible interval. This comes from two reasons. One arises from the AH-  
505 RJMCMC method because of the large a priori intensity range considered in the calculations,  
506 which allows for the possibility of fast and ample variations not necessarily seen from the  
507 data distribution. The second reason is that the bootstrap approach, on the contrary, uses a  
508 regularization defined as the best trade-off between the minimum complexity and the data  
509 misfit that reduces the probability of rapid and large variations in the absence of constraints  
510 provided by the data. In this way, the philosophy conveyed by the AH-RJMCMC method is  
511 very suitable to the detection of very rapid or extreme intensity variations (in this case, each  
512 result can have a strong influence on the field intensity evolution; Livermore et al., 2021 in  
513 this volume). Indeed, the method admits all possible time-dependence consistent with both  
514 the prior information and the dataset, although it returns a higher probability for parsimonious  
515 models with the least number of knots.

516

## 517 **7. Contributions and limitations of archeointensity dating: case study of Bourges and** 518 **Chaudry workshops**

519 Two procedures were used to derive chronological constraints based on archeointensity  
520 results, and also considering the reference curves established from the two different modeling  
521 techniques described in section 6 (Thébault and Gallet, 2010; Livermore et al., 2018). The  
522 first method, classical in archeomagnetism (e.g. Pavón-Carrasco et al., 2011) which we refer

523 below as “archeointensity correlation dating”, consists in convolving the pdf of the  
524 geomagnetic intensities defining the reference curve with the pdf of the intensity to be dated  
525 (i.e. a Gaussian) to form a (normalized) pdf of the age. It should be noted that the true pdf of  
526 the reference curves were used in our study and not, for simplification, a series of Gaussian  
527 distributions (e.g. Pavón-Carrasco et al., 2011). In this case, the intensity value to be dated is  
528 independent of the data used to create the reference curve. The second dating method, referred  
529 to as “archeointensity marginalized dating”, was described by Livermore et al (2018) and  
530 already used by Gallet et al (2020) and Shaar et al. (2020). Here, in contrast to the first  
531 method, the archeointensity value (of a priori poorly known age) to be dated is included in the  
532 dataset that constrains the joint age-intensity posterior distribution. The dating is then  
533 determined by the posterior age probability distribution derived for this datum by  
534 marginalization using the AH-RJMCMC method (see also Schnepf et al., 2015; Hervé and  
535 Lanos, 2017). The age distribution of the datum is then constrained by not only its wide prior  
536 age interval, but also by the ages of other data which are close in age. For age distributions  
537 derived either from the correlation or marginalization methods, we construct the most likely  
538 age intervals by calculating the highest density region at a 95.4% threshold (e.g. solid blue  
539 filled region in Fig 7). We will see below that the two dating methods give very similar  
540 results when using the AH-RJMCMC approach.

541

### 542 **7.1 Pottery workshop of La Chapelle Saint Ursin (BOUR# groups)**

543 The sampling of fragments associated with the pottery kiln and its production was carried out  
544 after an initial ceramological overview. At this moment, it was possible to isolate fragments  
545 of lips associated with pots characteristic of the production. The chronological constraints on  
546 the period of activity of this small workshop were, however, still rather loose. The objective

547 of our study was therefore to see whether archeointensity analyses could help to better define  
548 the period of production, which was perceived as being linked to the 5<sup>th</sup> century.

549 The two mean intensity values obtained for the pottery (BOUR01/02) and kiln  
550 (BOUR03) fragments are very consistent (Table 1), indicating that the pottery wasters found  
551 in the kiln filling are most likely associated with the kiln's latest productions. All the results  
552 obtained at the fragment level were therefore used to calculate a mean intensity value, which  
553 should be characteristic of the ambient field that prevailed at the time the kiln was abandoned  
554 (Table 1). The overall mean intensity value was compared to the different intensity variation  
555 curves shown in Figure 6, and the results of the archeointensity correlation dating are  
556 provided in the first two columns of Table 2. While two age intervals are discriminated during  
557 the High Middle Ages with the curves constructed according to the AH-RJMCMC method  
558 (Fig. 7a), a single age interval encompassing almost the entire High Medieval Period is  
559 isolated using the curves derived from the Thébaud and Gallet (2010) approach (Fig. 8a). The  
560 fact that the variation curves are respectively (for the two regional field modeling methods)  
561 more or less smooth and more or less sensitive to a very small number of data easily explain  
562 these differences (see discussion in Section 6). Furthermore, when using the AH-RJMCMC  
563 method, one can see the significant effect on the dating results induced by the choice of the  
564 database used to build the models, which is much less the case with the method of Thébaud  
565 and Gallet (2010) (Table 2). On the other hand, the marginal posterior age distribution of the  
566 intensity value to be dated derived from the approach developed by Livermore et al 2018 (i.e.,  
567 the archeointensity marginalized dating method; last two columns in Table 2; Fig. 7b) gives  
568 almost the same dating results as those provided by the archeointensity correlation dating  
569 method. Such an agreement can be understood by the fact that the French database is quite  
570 dense and the data very coherent, so that the incorporation of a single data point with a wide  
571 dating interval (here of 800 years between 400 and 1200) does not have much influence on

572 the calculated models. At this stage, it is fair to say that the results of archeointensity dating  
573 indicate that the production of this small workshop may have persisted beyond the 5<sup>th</sup> century.

574 This possibility was independently confirmed by the complete study of the ceramic  
575 material, which now places the production between 450 and 550, and by radiocarbon dating  
576 (Fig. 8b). The ceramic dating was first based on the study of the material "out of production"  
577 for which was noted the absence of characteristic elements of the 4<sup>th</sup> c. and early 5<sup>th</sup> c., and of  
578 Merovingian décor with a "molette" (i.e. made by impression with a wood wheel). The kiln  
579 production, with a very limited repertoire, also echoes other ensembles discovered in  
580 occupation contexts dating from the second half of the 4<sup>th</sup> c. and the first half of the 5<sup>th</sup>  
581 century. The radiocarbon dating was carried out on charcoal found in a layer associated with  
582 the last use of the kiln and should therefore be relevant for dating the end of the production. It  
583 gave an uncalibrated age of 1580±30 BP (Lyon-13108 (RICH)) and a calibrated age between  
584 420 and 556 calAD (using OxCal 4.4 and IntCal20, Reimer et al. 2020).

585 These different dating elements, archeology, archeomagnetism (archeointensity  
586 correlation dating) and radiocarbon, can be combined to better constrain this production.  
587 Since the three dating techniques are independent, the product of their pdf is applied, yielding  
588 an age interval during the first half of the 6<sup>th</sup> c. (Fig. 8), whatever the intensity variations  
589 curves used or the method considered for deriving the archeomagnetic age intervals. Note that  
590 the radiocarbon data contributes little to this dating: combining the radiocarbon data with  
591 either the archeological or archeointensity constraints gives an age interval identical or not  
592 significantly different from that provided by archeology. In contrast, the archeointensity result  
593 in combination with the archeological constraints makes it possible to limit the age interval  
594 for the end of the pottery production to ~half a century, which brings a strong constraint for  
595 the age of abandonment of the Roman villa associated with this pottery workshop.

596

## 597 **7.2 Pottery workshop of Chaudry (CHAU# groups)**

598 The archeointensity study was carried out as part of an archeological project aimed at  
599 completely re-examining the ceramic material unearthed on this site in the late 1990s  
600 (Regnard et al. 2021). Since its discovery, this material has been recognized as dating from  
601 the Carolingian period (mid 8<sup>th</sup>-end 10<sup>th</sup> century). The re-examination of the material allowed  
602 us to detail the production, highlighting in particular the highly standardized nature of the  
603 shapes, most of which are closed, and to define several technical groups, the most significant  
604 of which have been sampled for archeointensity analyses. The objective was therefore to  
605 better define the end of the period of activity of this kiln, certainly associated with a pottery  
606 activity extending over a wider spatial area.

607         The two technical groups associated with the kiln's production (CHAU01/02) yielded  
608 very consistent intensity values. The results obtained from two shards (of eleven measured)  
609 used in the construction of the kiln (third technical group; group CHAU03) appeared also  
610 very close to those obtained for the CHAU01/02 group, and their incorporation does not  
611 change the mean, nor its precision (CHAU01/02:  $77.3 \pm 0.5$  versus CHAU01/02/03:  
612  $77.4 \pm 0.4 \mu\text{T}$ ). For the archeomagnetic dating, we used the mean intensity value calculated  
613 from the data obtained for the three Chaudry groups, thus assuming that the fragments of  
614 CHAU03 were completely refired during the last use of the kiln. The archeointensity dating  
615 results obtained from this value are reported in Table 2. We find the same characteristics as  
616 before: while a single (long) age interval is obtained by correlation dating using the field  
617 evolution given by the Thébault and Gallet (2010) method (Fig. 9a), despite the very low  
618 (rather unusual) value of the standard deviation of the archeointensity data point, several  
619 distinct intervals (up to three) are observed from the AH-RJMCMC technique. For the latter,  
620 this is the case either by performing a correlation dating or by analyzing the marginal

621 posterior age distribution of this data point (Supp. Fig. 2), again with a significant effect of  
622 the database used on the results (Table 2).

623 The age interval provided by the archeological constraints is rather large, as it  
624 encompasses the entire Carolingian period (Fig. 9b). However, based on the recognition of  
625 certain regional stylistic elements, Lefèvre and Mahé (2004) proposed to narrow the  
626 production period to the first decades of the 10<sup>th</sup> century. All the results of archeointensity  
627 dating imply that the production would not have persisted beyond the very beginning of the  
628 10<sup>th</sup> century. To test whether this observation is related to the very small standard deviation  
629 (0.4 $\mu$ T), we increased its value to 1.5 $\mu$ T. This leads to the same conclusion for the 10<sup>th</sup>  
630 century (Table 2).

631 Radiocarbon data from charcoal are also available for the kiln (uncalibrated age,  
632 1255 $\pm$ 30 BP giving a 95.4%-calibrated age range between 671 and 876; Ref. Lyon-16233  
633 (RICH), Fig. 9b). However, the charcoal was not found at the bottom of the kiln, thus raising  
634 the question of the significance of the age obtained. As a result, neither the archeointensity  
635 (due to the nature of the intensity variations during the High Middle Ages) nor the  
636 radiocarbon data (and their combination) make it possible to constrain the age of the  
637 beginning of ceramic production (Fig. 9). In particular, it seems useful to ask whether the  
638 stylistic features that led to the early dating of the 10<sup>th</sup> century could in fact have appeared  
639 somewhat earlier (last decades of the 9<sup>th</sup> c. or first decade of 10<sup>th</sup> c.) in the Vexin Français  
640 area than in other parts of the Ile-de-France region. This issue is still unresolved. Clearly, only  
641 additional archeological constraints, from the excavation of other kilns in the Vexin Français  
642 or the recognition of this ceramic production in occupation contexts, would further limit the  
643 age span of the production.

644

645

646 **8. Conclusions**

647 Seven new archeointensity values with accurate dating in the High Middle Ages further  
648 improved our knowledge of the variations in geomagnetic intensities in France, and more  
649 generally in Western Europe, over the past 1700 years.

650 Two regional modeling approaches were used to trace these variations, the first  
651 derived from the method of Thébault and Gallet (2010), which now considers irregularly  
652 spaced knots according to the data distribution, the second developed by Livermore et al.  
653 (2018) based on a transdimensional Bayesian technique. In addition, two databases were used  
654 that differ according to a criterion of data homogeneity, all of which are located within a 700  
655 km circle around the city of Beaune. This dual approach allowed us to illustrate the sensitivity  
656 of the mean curves, based on the distribution of a large set of individual models, to the  
657 principles of each of the two modeling approaches. While the first method gives a very  
658 regular and smooth evolution in intensity variation, with a weighting of the effects linked to  
659 slightly discordant data, the second approach shows more abrupt variations with sometimes  
660 stronger amplitudes.

661 We also illustrated two examples of dating integrating the constraints resulting from  
662 the archeointensity results, in addition to those of the available archeological and radiocarbon  
663 data. For this, we also used two different dating techniques, either by classically comparing  
664 the intensity value to be dated with the reference geomagnetic variation curve, or by  
665 analyzing the marginal posterior age distribution of the data point given by the method of  
666 Livermore et al (2018). We showed that for France, the two techniques give very similar  
667 results. In this respect, the consideration of two different approaches for both regional field  
668 modeling and dating strengthens the interpretation of archeointensities for archeological  
669 dating.



670 Finally, beyond the information provided to the archeologists, our study showed that it  
671 would certainly be illusory to consider archeointensities as a fully independent “absolute”  
672 dating method (e.g. Aitken, 1990; Korte et al., 2019), especially in the absence of direction-  
673 based archeomagnetic constraints. On the contrary, archeointensities may provide  
674 chronological constraints, which in combination with other archeological and/or radiocarbon  
675 dating elements, can be very valuable in refining the dating of the structures/artifacts studied,  
676 opening the way to a wide range of complementary research on Medieval pottery production.

677

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684

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943

944 **Figure captions:**

945 Figure 1: (a) Location of the archeological sites discussed in this paper. The pink circles  
946 indicate the sites associated with the seven new precisely-dated archeointensity results. The  
947 two pink circles bordered with purple indicate the sites where groups were collected for  
948 dating (the yellow area represents the so-called “Vexin Français” region). The blue circles  
949 indicate the geographical distribution of our intensity dataset (Genevey et Gallet, 2002; Gallet  
950 et al. 2009; Genevey et al., 2009, 2013, 2016, 2019). The green squares correspond to the  
951 sites of the selected data obtained by Chauvin et al. (2000), Donadini et al. (2008), Gómez  
952 Paccard et al. (2012) and Schnepf et al. (2020 in this volume). The circle with a radius of  
953 700km is centered on the city of Beaune (Burgundy) to where the different intensity results  
954 were reduced. (b) Kiln 3060 unearthed at Hermé. Sampling for direction and intensity was  
955 concentrated on the central tongue of the Kiln (Group HERME04) ©N. Warmé, Inrap (c)  
956 Close-up of the pottery fragments found in kiln 2629 unearthed in Chamigny (Group  
957 CHAM03) ©C. Seng, Inrap.

958

959 Figure 2: Archeointensity results obtained for six groups (or pairs of groups) of fragments.  
960 Each curve corresponds to the analysis of a specimen and represents the intensity values (i.e.  
961 the  $R'(T_i)$  data) obtained over the temperature range  $T_{min}$ - $T_{max}$  where the primary TRM  
962 component was isolated (given in Supp Tab. 1). These examples show that for each specimen,  
963 the  $R'(T_i)$  data are nearly constant over the  $T_{min}$ - $T_{max}$  temperature interval, indicating that  
964 the magnetic mineralogy has maintained the same acquisition capability for both the NRM  
965 and the laboratory-TRM. Enhanced scatter observed at low temperatures, when the running  
966 temperature  $T_i$  is close to  $T_{min}$ , is due to the small NRM and laboratory-TRM fractions  
967 involved in the  $R'(T_i)$  ratios.

968

969 Figure 3: Examples of magnetic behavior for rejected fragments. (a, b) Two fragments for  
970 which a major alteration of the magnetic mineralogy was detected from low-field magnetic  
971 susceptibility versus temperature measurements. (c, d) Fragment for which the primary TRM  
972 component could not be reliably isolated in the thermal demagnetization diagram (c) and  
973 corresponding intensity diagram with non-constant intensity values (d). (e, f) Fragment with a  
974 single magnetization component observed between 100°C and 520°C in the thermal  
975 demagnetization diagram (e) but with decreasing intensity values over the same temperature  
976 range (f). In the demagnetization diagrams (c, e), the solid (resp. empty) circles represent the  
977 declinations (resp. inclinations) in specimen coordinates.

978

979 Figure 4: Thermal demagnetization of three-axis IRM components acquired in fields of 1.25,  
980 0.4 and 0.2 T for six different fragments successfully analyzed in intensity and low-field  
981 magnetic susceptibility versus temperature curves (up to 500-520°C) for the same fragments.

982

983 Figure 5: Archeointensity data available within a 700 km radius around Beaune combining  
984 our dataset and other selected results (see details in the figure). The results of Donadini et al  
985 (2008) and Gómez Paccard et al. (2012) were modified as discussed in the text. Direct  
986 measurements are from <http://www.bcmf.fr/>. All data were reduced to the latitude of Beaune  
987 (47.03°N, 4.83°E)

988

989 Figure 6: Intensity variations curves in Western Europe over the past 1700 years. (a,b)  
990 Variation curves obtained using the Thébaud and Gallet (2010) method considering our  
991 dataset only (a) and our data combined with the other selected data (b). The curve in pink  
992 indicates the probability maxima and the pink dotted lines the 95% credible interval. (c,d)  
993 Variation curves obtained using the AH-RJMCMC method (Livermore et al., 2018)  
994 considering only our data (c) and together with the other selected data (d). The curves in red  
995 and blue show the probability maxima and the median values, respectively; the thin dotted  
996 lines in blue show the 95% credible interval. More details are given in the text and in supp  
997 Table 2. In all diagrams, the density distribution of individual models is shown according to a  
998 grey colour code scale (maximum probability of 0.15). Direct measurements are from  
999 <http://www.bcmf.fr/>. All data were reduced to the latitude of Beaune (47.03°N, 4.83°E).

1000

1001 Figure 7: Archeomagnetic dating obtained for the pottery workshop discovered at La Chapelle  
1002 Saint Ursin site (BOUR# groups). (a) Archeointensity correlation dating: The variation curve  
1003 is calculated using the AH-RJMCMC method developed by Livermore et al (2018) method  
1004 and taking into account all the selected data (see text) available within 700 km radius of the  
1005 city of Beaune (see Fig. 6d). The horizontal area in orange shows the intensity value ( $\pm 2\sigma$ ) to  
1006 be dated. The dating is carried out by direct comparison with the calculated models ensemble.  
1007 The age intervals (light blue area, right y-scale; see Table 2) are determined according to a

1008 95.4% threshold value (horizontal blue line) which defines a highest density region. (b)  
1009 Archeointensity marginalized dating (Livermore et al., 2018): The intensity value to be dated  
1010 is incorporated with a large age interval (here between 400 and 1200) into the database used  
1011 for the construction of the models using AH-RJMCMC. The diagram presents the marginal  
1012 posterior age distribution derived for the data point concerned. As previously, different age  
1013 intervals (light blue area; Table 2) are obtained according to a 95.4% threshold (horizontal  
1014 blue line). The picture shows the kiln once excavated © E. Marot, Bourges plus.

1015

1016 Figure 8: Dating elements available for the pottery workshop discovered at La Chapelle Saint  
1017 Ursin. (a) Archeointensity correlation dating. The variations curve displayed is calculated  
1018 using the Thébault and Gallet (2010) method and all the data selected within the 700 km  
1019 radius of the city of Beaune (see Fig. 6b). The Gaussian curve in red next to the intensity axis  
1020 represents the intensity value to be dated. The age probability derived from the comparison of  
1021 the BOUR overall mean value with the reference curve, taking into account their error bars, is  
1022 represented both directly on the variation curve using a colour code and by a probability  
1023 density curve reported along the age axis. The age interval shown between brackets is the  
1024 most likely age range at a 95.4% threshold. The drawing represents a characteristic form of  
1025 the production to be dated (©E. Marot, Bourges Plus). (b) This panel presents the  
1026 archeological age interval, with a uniform probability density considered for the pottery  
1027 production (black line), the probability density of the C14 data after calibration (in red) and  
1028 the final age probability (in green) derived by combining the pdfs of the three dating elements  
1029 (archeomagnetism of figure (a), archeological and C14).

1030



1031 Figure 9: Same legend as in Fig. 8 but the archeointensity value to be dated was obtained for  
1032 the pottery workshop discovered at Chaudry. The drawing represents a characteristic form of  
1033 this production ©S. Regnard, CRAVF.

1034

### 1035 **Table captions**

1036 Table 1: New archeointensity results obtained for the seven dated groups of fragments and for  
1037 the two series of groups investigated for dating.

1038

1039 Table 2: Results of archeomagnetic dating obtained for the pottery workshops discovered at  
1040 La Chapelle Saint Ursin (BOUR#) and Chaudry (CHAU#). Dating is carried out using two  
1041 field modeling techniques, according to Thébault and Gallet (2010) and Livermore et al.  
1042 (2018), two databases and two different dating approaches, here referred to as  
1043 “archeointensity correlation dating” and “archeointensity marginalized dating”. For Chaudry,  
1044 the calculations are performed using the standard error of mean intensity value and by  
1045 artificially increasing this error up to 1.5  $\mu$ T. See the text for more explanation. All age  
1046 intervals are given with a 95.4% confidence level.

1047

### 1048 **Supplementary information**

1049 Supp. Figure 1: Cooling rate (CR) effect on the intensity data obtained by Donadini et al.  
1050 (2008) and Gómez- Paccard et al. (2012). The results are reported at the site location, both at  
1051 the specimen (spec.) and group levels. The description of the different symbols is given in the  
1052 Figure. The “Nblue/Npink” numbers for the data obtained by Gómez- Paccard et al. (2012)  
1053 indicate the number of results used to derive the mean value when using all the data, i.e.  
1054 combining CR corrected and uncorrected values (Nblue), and the number of CR-corrected  
1055 values used to derive the mean (Npink). The “Ngrey/Nyellow” number for the result of

1056 Donadini et al. (2012) indicates the number of results obtained from small samples (volume  
1057  $1\text{cm}^3$ ) analyzed at the Helsinki paleomagnetic laboratory (Ngrey) and the number of large  
1058 samples (volume  $8\text{ cm}^3$ ) analyzed in the paleomagnetic laboratory at Sofia (Nyellow).

1059

1060 Supp. Figure 2: Archeomagnetic dating obtained for the pottery workshop discovered at the  
1061 Chaudry site (CHAU# groups). (a) Archeointensity correlation dating: The variation curve is  
1062 calculated using the AH-RJMCMC method developed by Livermore et al (2018) method and  
1063 taking into account all the selected data (see text) available within the 700 km radius of the  
1064 city of Beaune (see Fig. 6d). The horizontal area in orange shows the intensity value ( $\pm 2\sigma$ ) to  
1065 be dated. The dating is carried out by direct comparison with the calculated models. The age  
1066 intervals (light blue area, right y-scale; see Table 2) are determined according to a 95.4%  
1067 threshold value (horizontal blue line). (b) Archeointensity marginalized dating (Livermore et  
1068 al. 2018): The intensity value to be dated is incorporated with a large age interval (here  
1069 between 400 and 1200) in the database used for the construction of the models. The diagram  
1070 presents the marginal posterior age distribution derived for the data point concerned. As  
1071 previously, different age intervals (light blue area; Table 2) are obtained according to a 95.4%  
1072 threshold (horizontal blue line). The picture shows the kiln being excavated with its filling. ©  
1073 S. Regnard, CRAVF.

1074

1075 Supp. Table 1: Intensity results obtained at the specimen level and mean values obtained at  
1076 the fragment level. ‘Natural magnetic moment’: Magnetic moment before demagnetization  
1077 for each specimen in  $\text{A.m}^2$ . The volume of each specimen is of the order of  $0.75\text{ cm}^3$  or  
1078 slightly less. ‘Tmin-Tmax’: Interval of temperature involved for the intensity computation. ‘F  
1079 lab’: Intensity of the laboratory field in  $\mu\text{T}$ . ‘NRM T1 (T1’)’: Fraction in % between the  
1080 magnetization unblocked between Tmin and Tmax, thus used for intensity determination, and

1081 the magnetization with unblocking temperatures  $\geq T_{min}$ . ‘Slope R’: Slope of the straight line  
1082 computed by linear regression from the  $R'(T_i)$  data between  $T_{min}$  and  $T_{max}$ . It is calculated  
1083 as follows (see also Gallet and Le Goff 2006): Slope  $R'=(R'(T_{max})-R'(T_{min})) / (\text{Mean}$   
1084  $(R'(T_i)$  data) where  $R'(T_{max})$  and  $R'(T_{min})$  are here the values at  $T_{max}$  and  $T_{min}$  deriving  
1085 from the linear regression of the  $R'(T_i)$  data. It is expressed in %. ‘F Triaxe’: Intensity values  
1086 obtained at the specimen level in  $\mu T$ . It is estimated by computing the arithmetic mean from  
1087 all  $R'(T_i)$  ratios obtained for a specimen over the  $T_{min}$ - $T_{max}$  temperature range. ‘F Triaxe  
1088 mean value per fragment  $\pm \sigma F$ ’: Mean intensity value obtained at the fragment level with its  
1089 standard error when computed from 2 values or its standard deviation when computed from 3  
1090 values.  $(N1/N2/N3/N4)^*$  indicates respectively the number of fragments collected, the  
1091 number of fragments whose magnetization was strong enough relative to the Triaxe  
1092 sensitivity, the number of fragments measured on the Triaxe for which no sign of magnetic  
1093 mineralogy alteration was observed during the susceptibility measurements and the number of  
1094 fragments retained to estimate a mean value at the group level.  $(n1/n2)^{**}$  indicates  
1095 respectively the number of specimens measured using the Triaxe and the number of retained  
1096 specimens. Note that we usually test two to three specimens per fragment to reject or retain  
1097 the fragment based on our set of quality criteria.

1098

1099 Supp. Table 2: Intensity values derived from the method of Thébault and Gallet (2010;  
1100 maximum probability and 95% credible interval) and that of Livermore et al (2018; maximum  
1101 probability, median, 95% credible interval). For the latter technique, the following  
1102 computational parameters were considered:  $\sigma_{move}=30$  years,  $\sigma_{change}= 5 \mu T$ ,  $\sigma_{birth}=5 \mu T$ ,  
1103  $K_{max}=150$ , prior intensities between  $35 \mu T$  and  $95 \mu T$  and a chain length of 200 million  
1104 samples. One datum age is perturbed per age-resampling. All the calculations are carried out

1105 using our data alone or our dataset combined with a selection of other results (see text). These  
1106 values trace the different curves shown in Fig. 6.

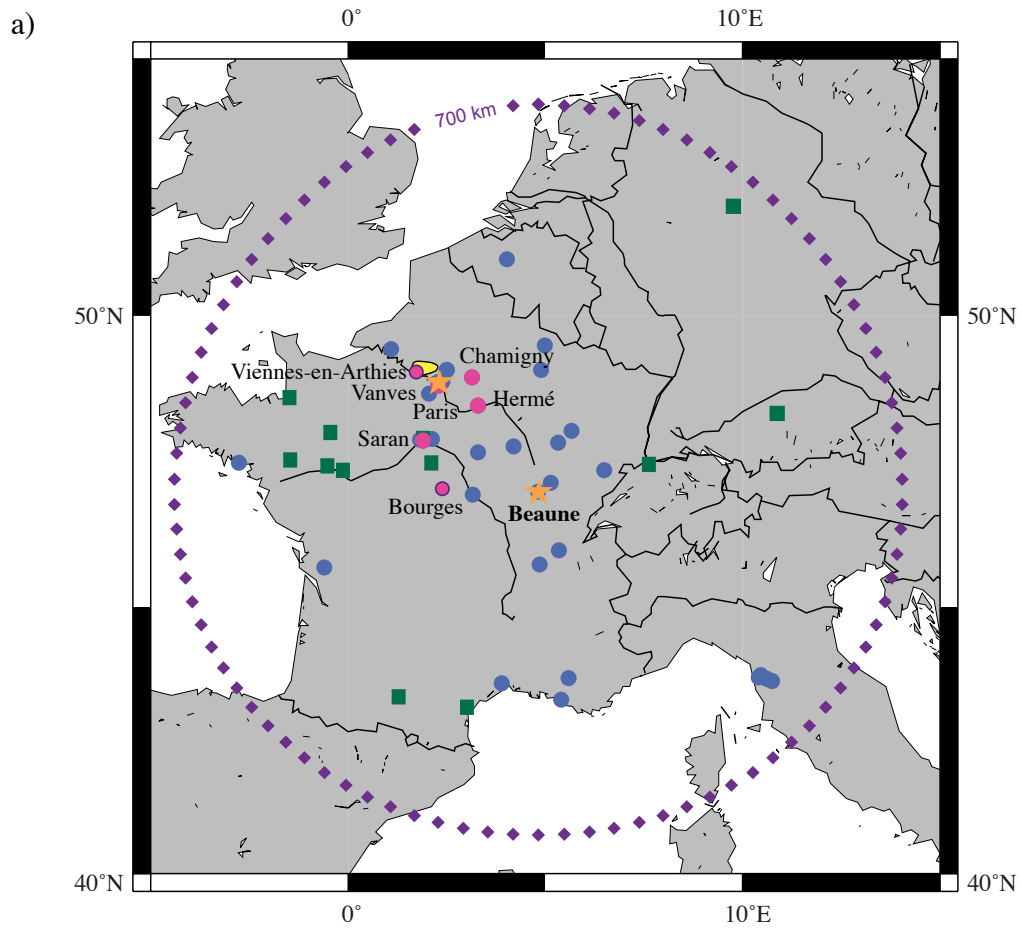


Figure 1.

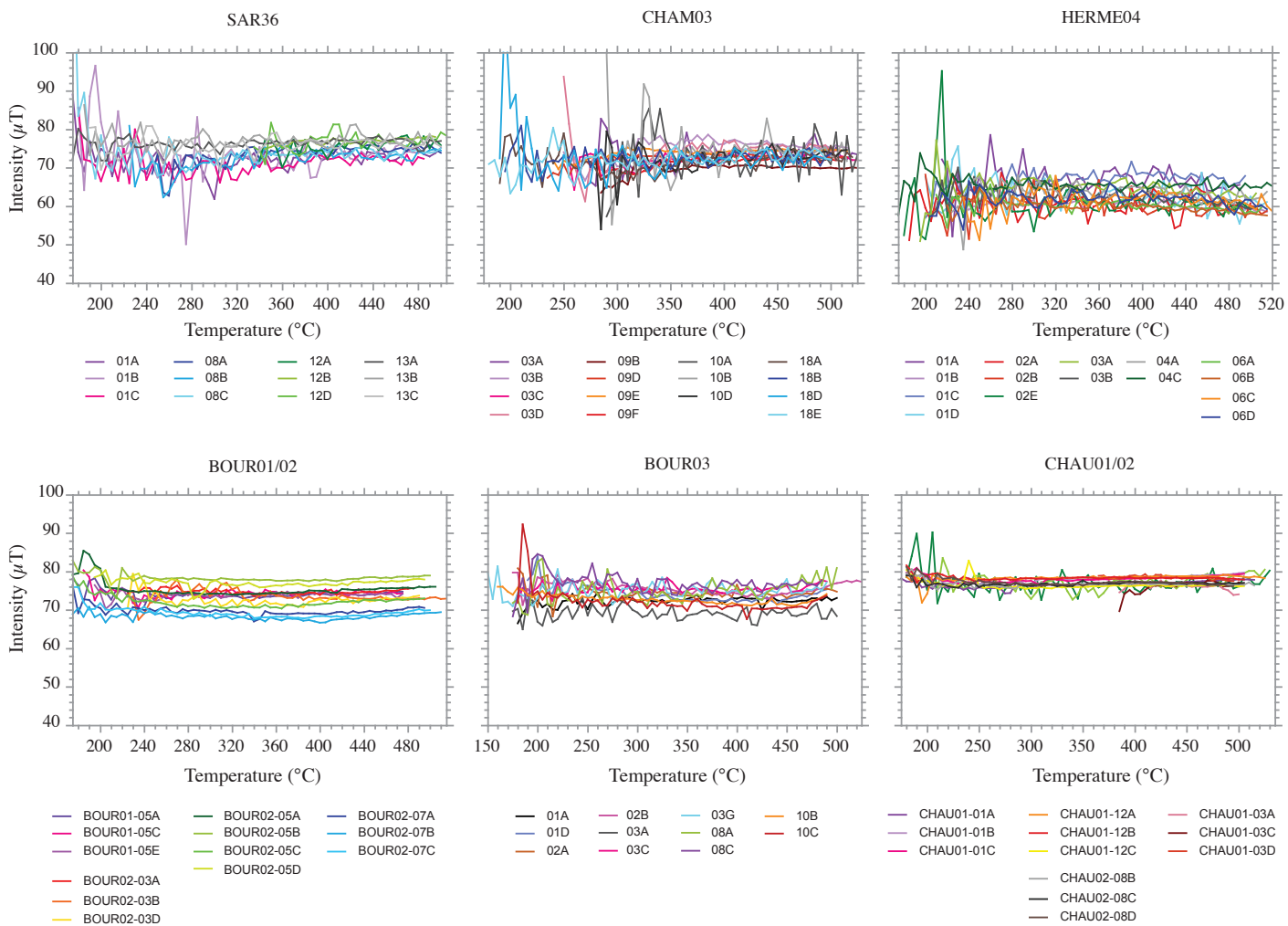


Figure 2.

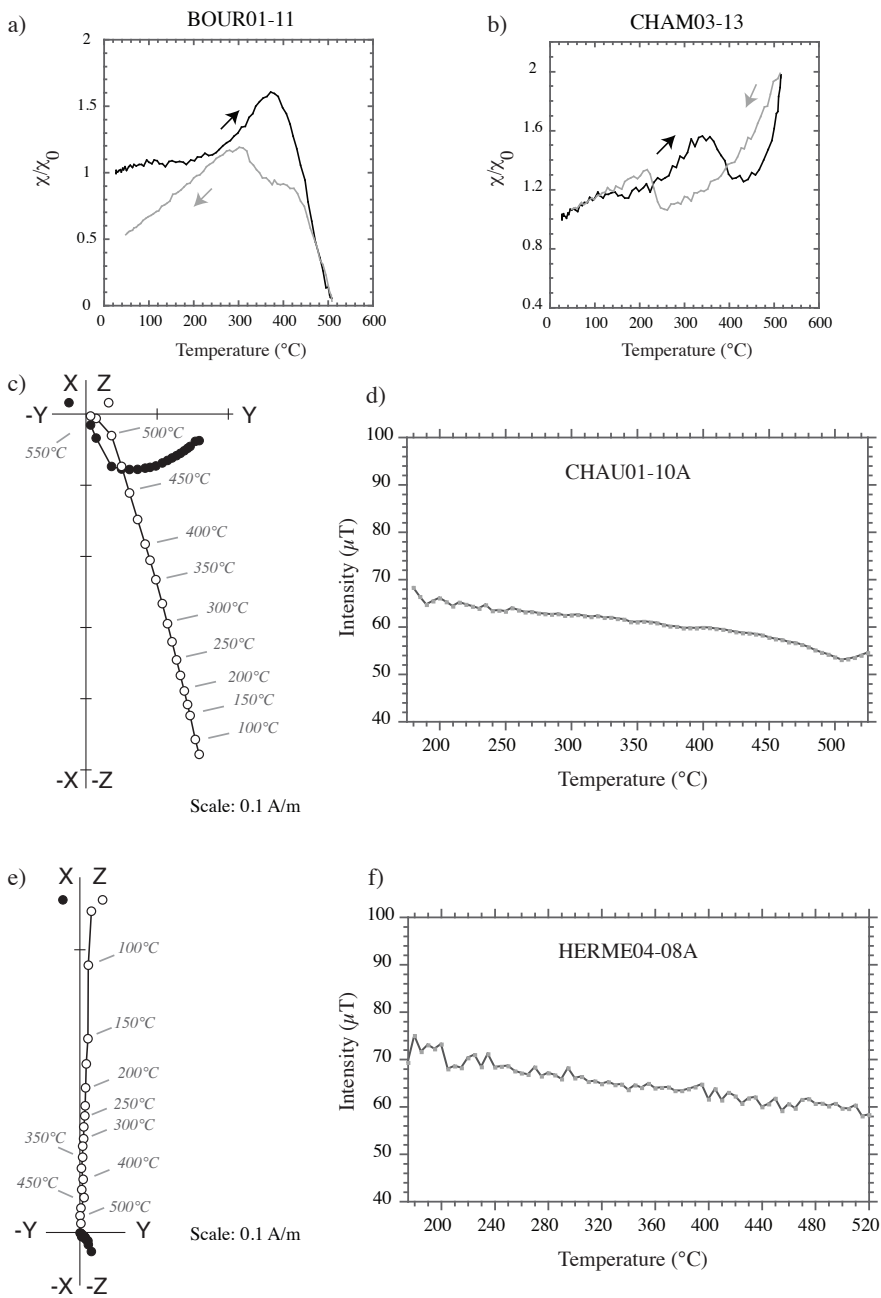


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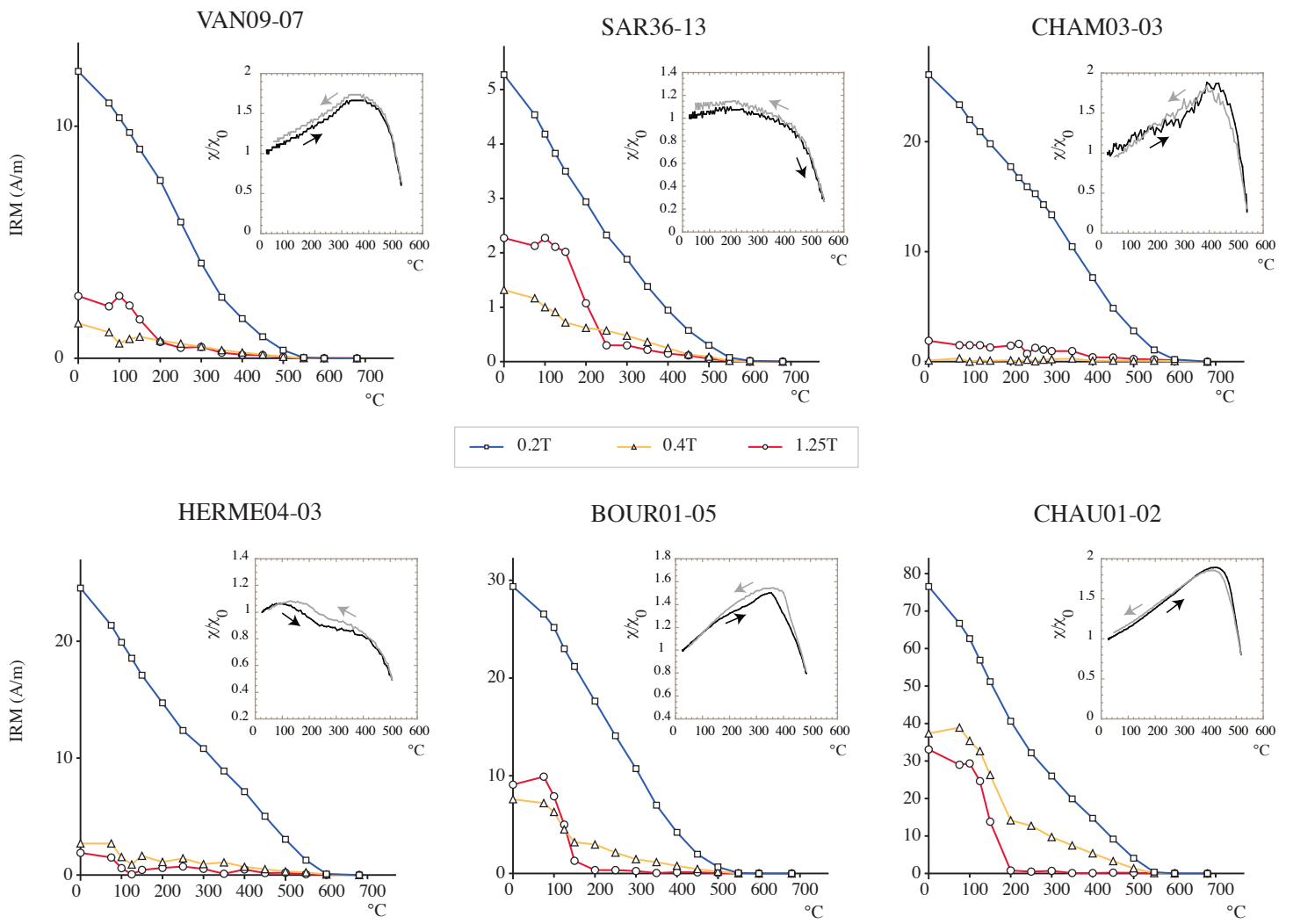


Figure 4.



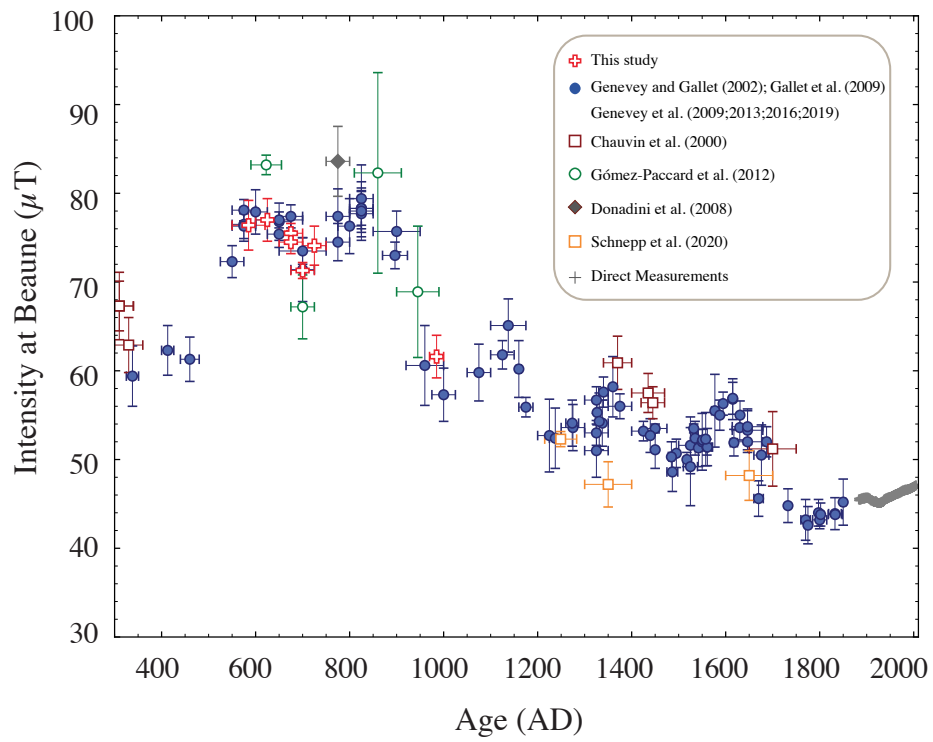
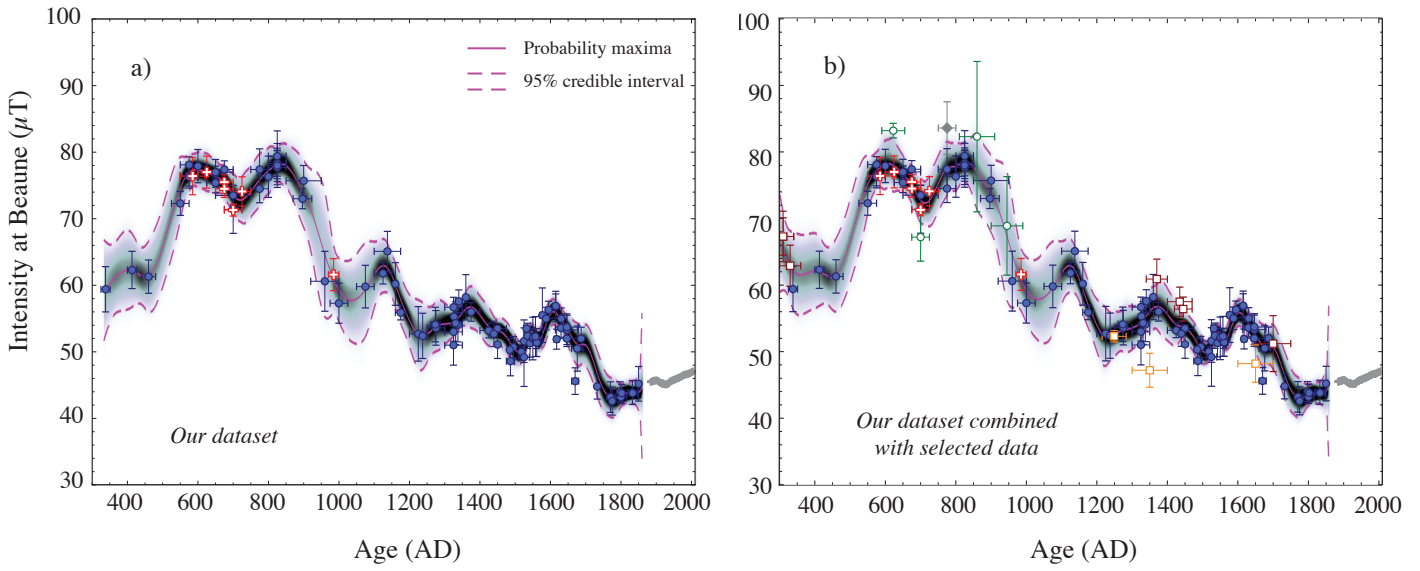


Figure 5.

- + This study
  - Genevey and Gallet (2002); Gallet et al. (2009); Genevey et al. (2009;2013;2016;2019)
  - + Direct Measurements
- Chauvin et al. (2000)
  - Gómez-Paccard et al. (2012)
  - ◆ Donadini et al. (2008)
  - Schnepf et al. (2020)

### Bootstrap algorithm



### Transdimensional bayesian technique

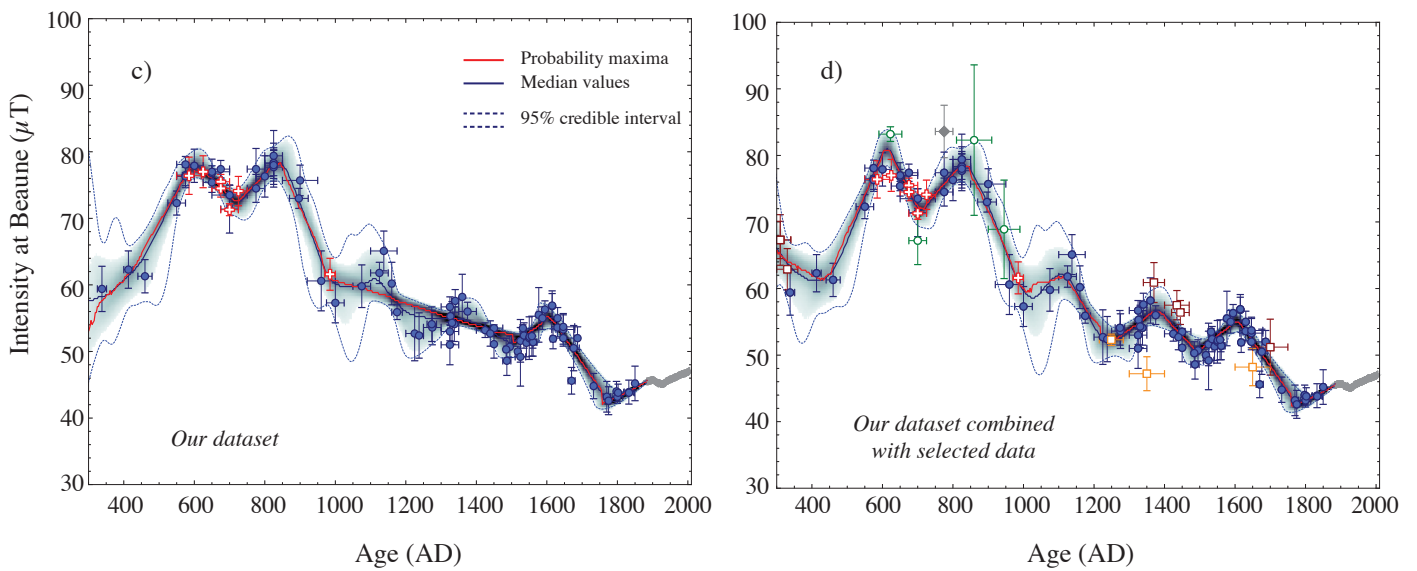


Figure 6.

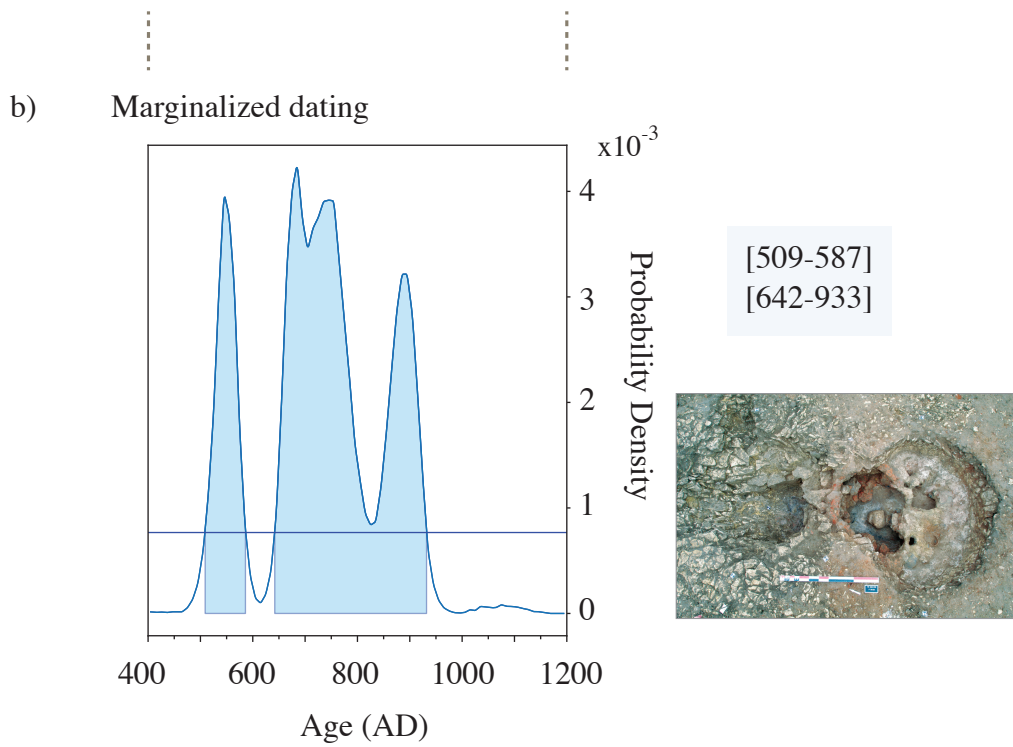
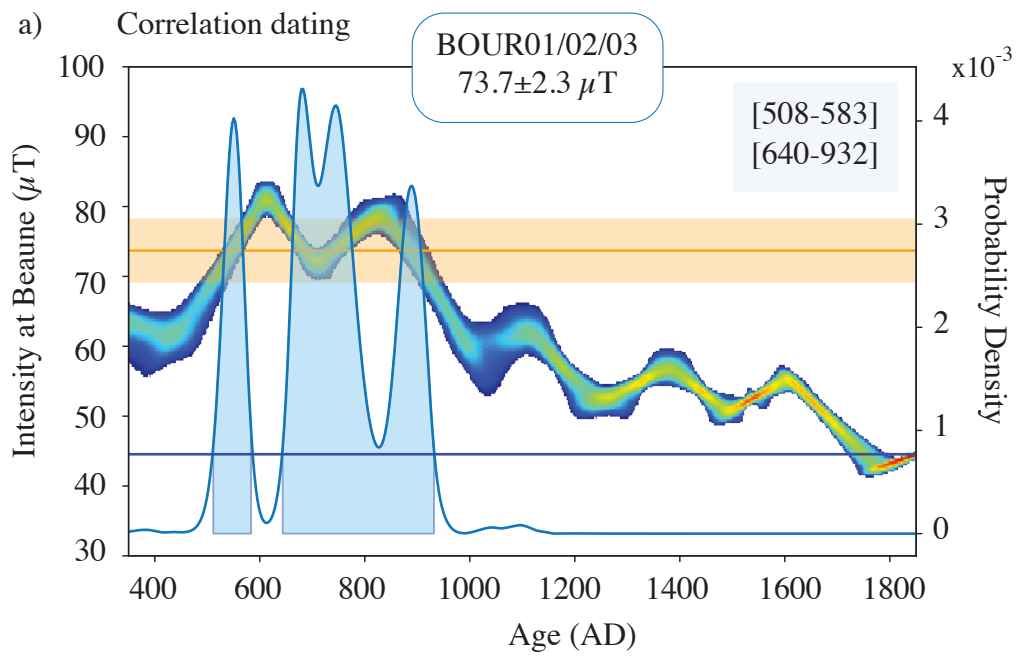


Figure 7

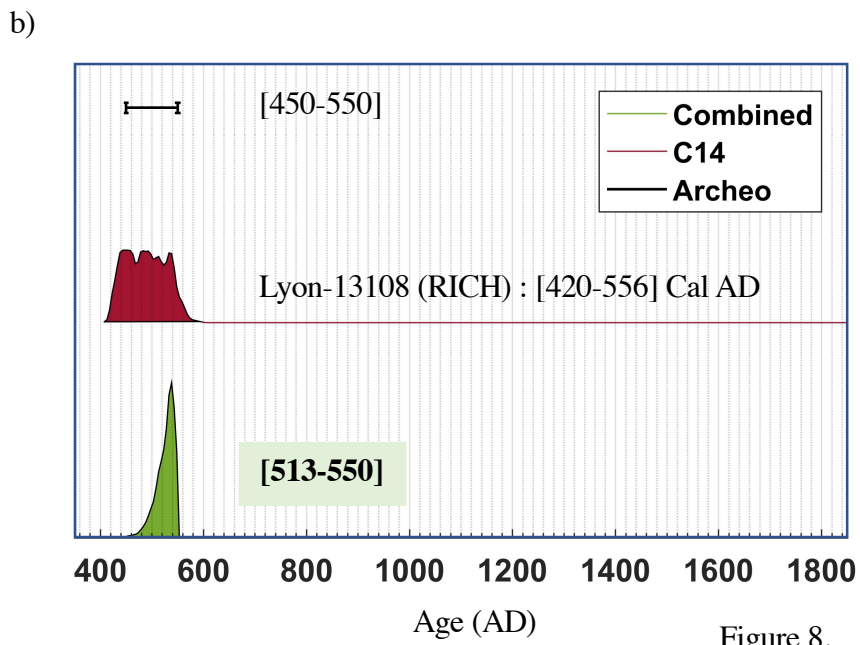
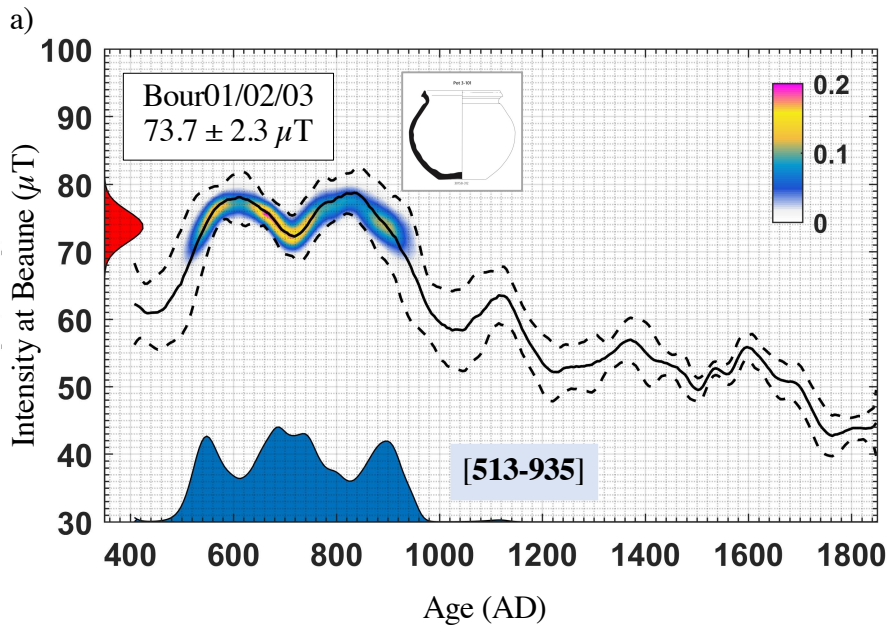


Figure 8.

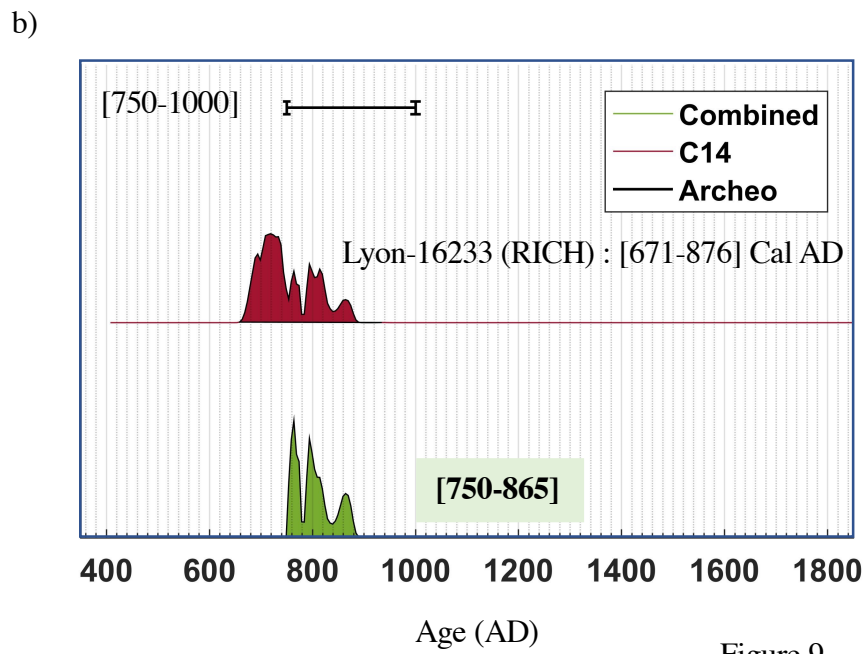
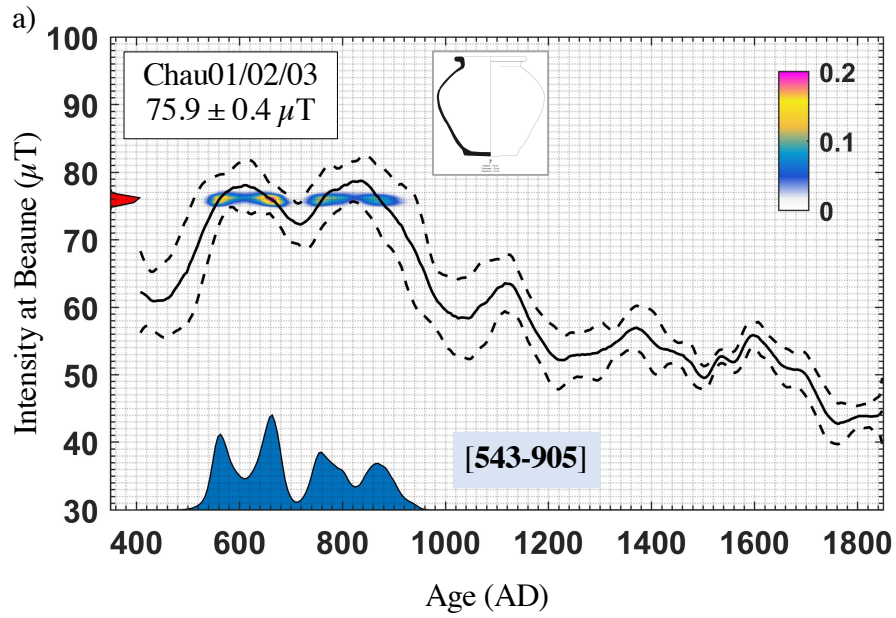


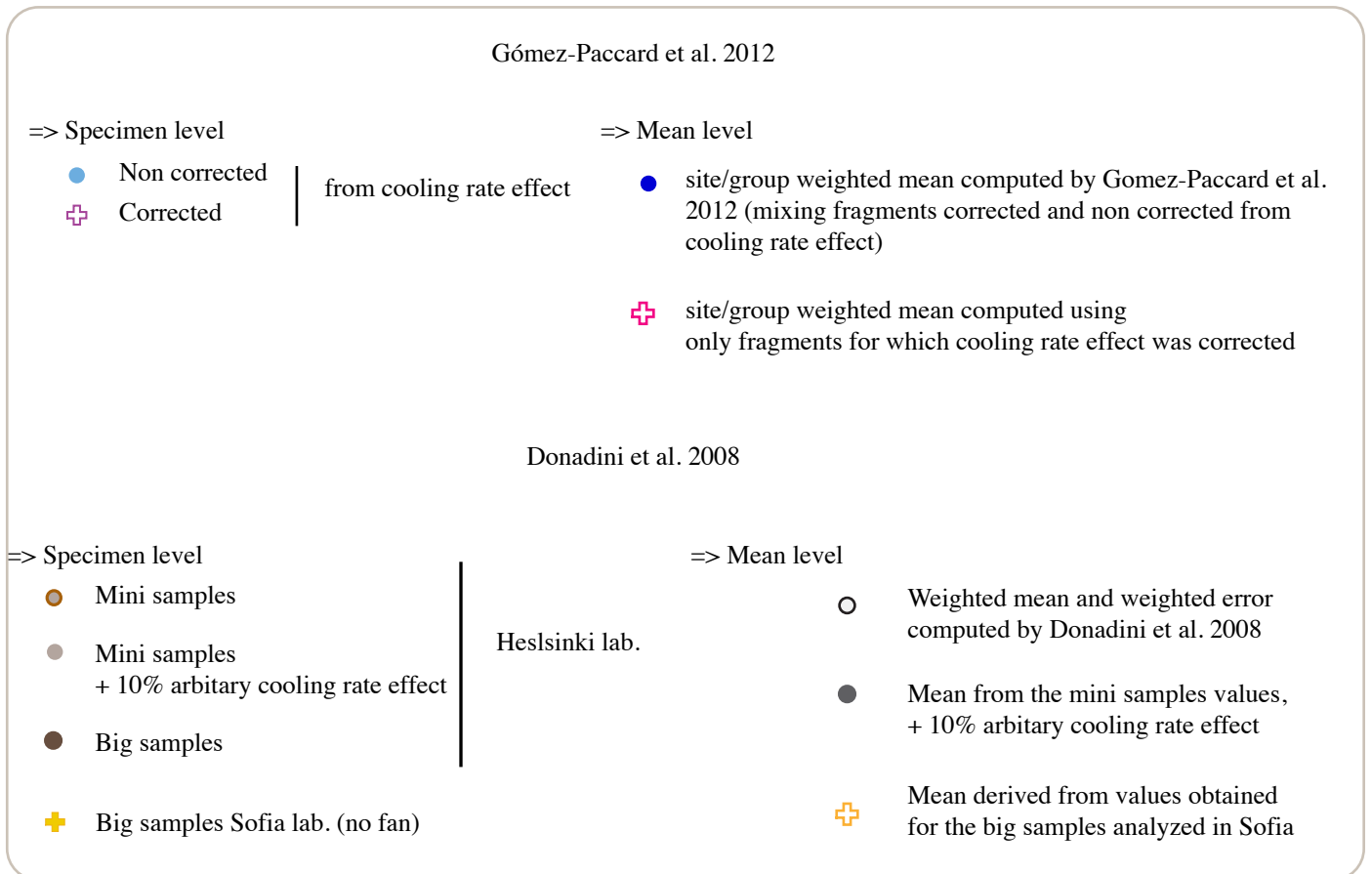
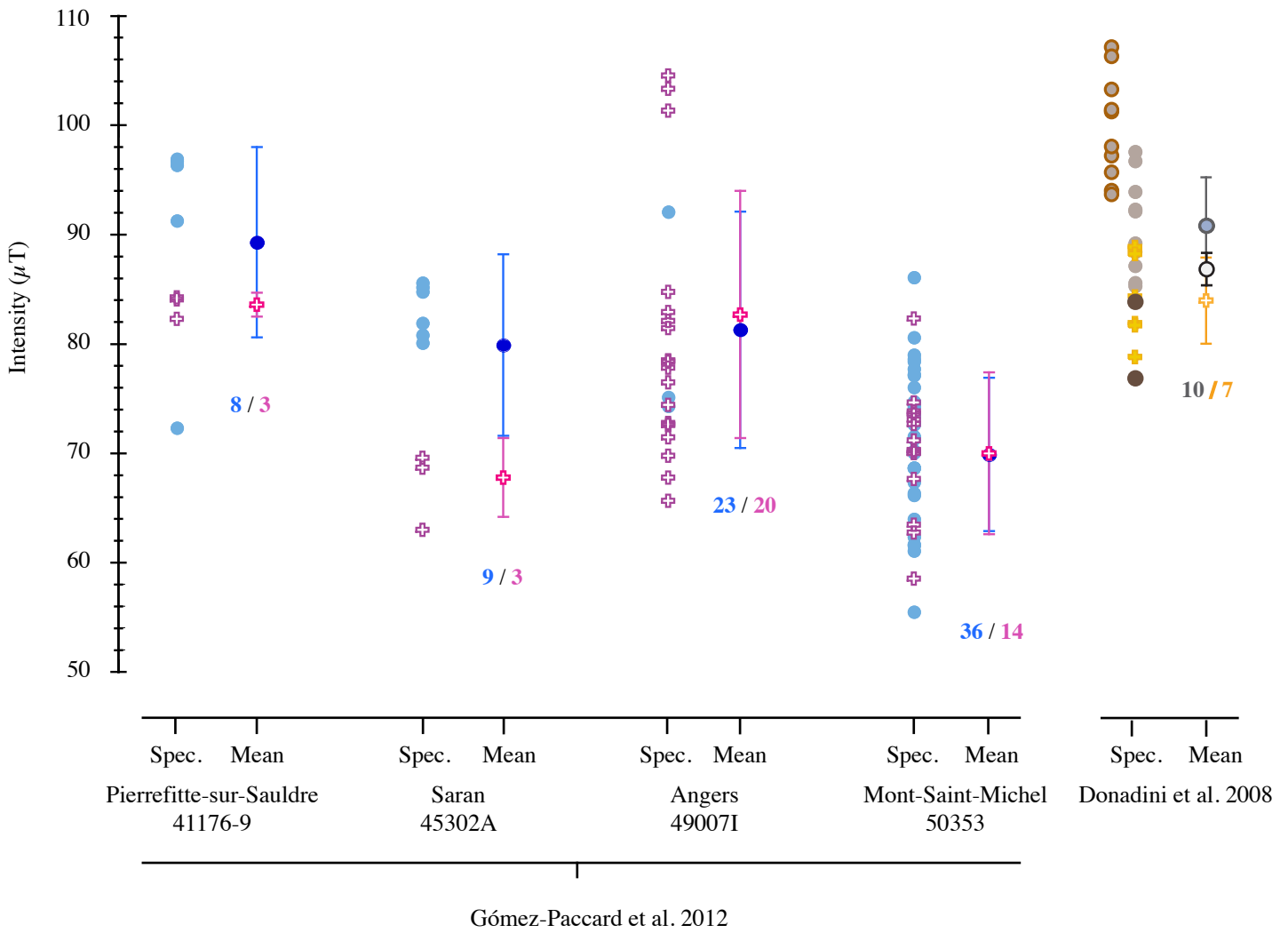
Figure 9.

Table 1

# Group	Site (Location, Archeological excavation)	Archeological description	Type of material	Age (AD.)	N Thermal unit(s) (n specimens)	F ± σF (μT)	F <sub>Beaune</sub> (μT)
<b>► Groups analyzed to provide new reference intensity values</b>							
SAR19	Saran, La Guignace (47.9°N, 1.9°E)	Kiln 10 (SU 2761)	Potsherd	[550-620]	N=12 (n=26)	77.1±2.8	76.4
SAR21	Saran, La Guignace (47.9°N, 1.9°E)	Kiln 5 (SU 2064)	Potsherd	[600-650]	N=5 (n=16)	77.7±2.4	77.0
VAN03	Vanves, rue Gaudray (48.83°N, 2.30°E)	Kiln 3039 (SU 3304 & SU 3305)	Potsherd	[650-700]	N=4 (n=10)	76.9±1.1	75.5
VAN09	Vanves, rue Gaudray (48.83°N, 2.30°E)	Kiln 1138 (SU 1141)	Potsherd	[650-700]	N=4 (n=9)	75.8±1.3	74.5
CHAM03	Chamigny, La Grande Maison (48.97°N, 3.15°E)	Kiln 2629 (Structure 2116)	Potsherd	[675-725]	N=4 (n=15)	72.7±0.9	71.3
SAR36	Saran, Voie Nouvelle (47.9°N, 1.9°E)	F 24 (SU 1073)	Potsherd	[700-750]	N=4 (n=12)	74.7±2.2	74.1
HERME04	Hermé, Les Malletons carrière SPM (48.5°N, 3.3°E)	Kiln 3060; fragments from the central (and elongated) support of the floor in the firing chamber	Baked clay fragment	[970-1000]	N=1 (n=15)	62.5±2.4	61.6
<b>► Groups analyzed for dating</b>							
BOUR01/02	La Chapelle Saint-Ursin, L'angoulaire, chemin des vallées aux fruscades (47.08°N, 2.4°E)	Kiln 3004 (SU 30121 & SU 30145)	Potsherd		N=4 (n=13)	73.2±2.9	73.2
BOUR03	La Chapelle Saint-Ursin, L'angoulaire, chemin des vallées aux fruscades (47.08°N, 2.4°E)	Kiln 3004, fragments from the kiln floor in the firing chamber	Baked clay fragment		N=1 (n=11)	73.9±2.2	73.9
BOUR01/02/03	La Chapelle Saint-Ursin, L'angoulaire, chemin des vallées aux fruscades (47.08°N, 2.4°E)				N=5 (n=24)	73.7±2.3	73.7
CHAU01/02	Viennes-en-Arthies, Chaudry (49.07°N, 1.73°E)	Filling unit of the kiln	Potsherd		N=4 (n=12)	77.3±0.5	75.8
CHAU03	Viennes-en-Arthies, Chaudry (49.07°N, 1.73°E)	Pottery fragments associated with debris of the kiln walls	Potsherd		N=2 (n=6)	77.6±0.3	76.1
CHAU01/02/03	Viennes-en-Arthies, Chaudry (49.07°N, 1.73°E)				N=6 (n=18)	77.4±0.4	75.9

Table 2

	Archeointensity correlation dating		Archeointensity marginalized dating	
	Our dataset	All selected data	Our dataset	All selected data
▶ <i>BOUR01/02/03</i> : $73.7 \pm 2.3 \mu T$				
Bootstrap algorithm Thébault and Gallet (2010)	[513 – 930]	[513 – 935]	X	X
AH-RJMCMC method Livermore et al. (2018)	[502 – 824] & [839– 926]	[508 – 583] & [640– 932]	[505 – 826] & [844 – 926]	[509 – 587] & [642 – 933]
▶ <i>CHAU01/02/03</i> : $75.9 \pm 0.4 \mu T$				
Bootstrap algorithm Thébault and Gallet (2010)	[543 – 895]	[543 – 905]	X	X
AH-RJMCMC method Livermore et al. (2018)	[541 – 683] & [752 – 899]	[544 – 586] & [643 – 683] & [740 – 902]	[543 – 686] & [752 – 899]	[545 – 589] & [642 – 685] & [742 – 907]
▶ <i>CHAU01/02/03</i> : $75.9 \pm 1.5 \mu T$				
Bootstrap algorithm Thébault and Gallet (2010)	[538 – 905]	[538 – 915]	X	X
AH-RJMCMC method Livermore et al. (2018)	[535 – 707] & [731 – 905]	[535 – 595] & [628 – 698] & [722 – 911]	[535 – 708] & [732 – 905]	[536 – 598] & [631 – 700] & [720 – 913]



Supp. Figure1



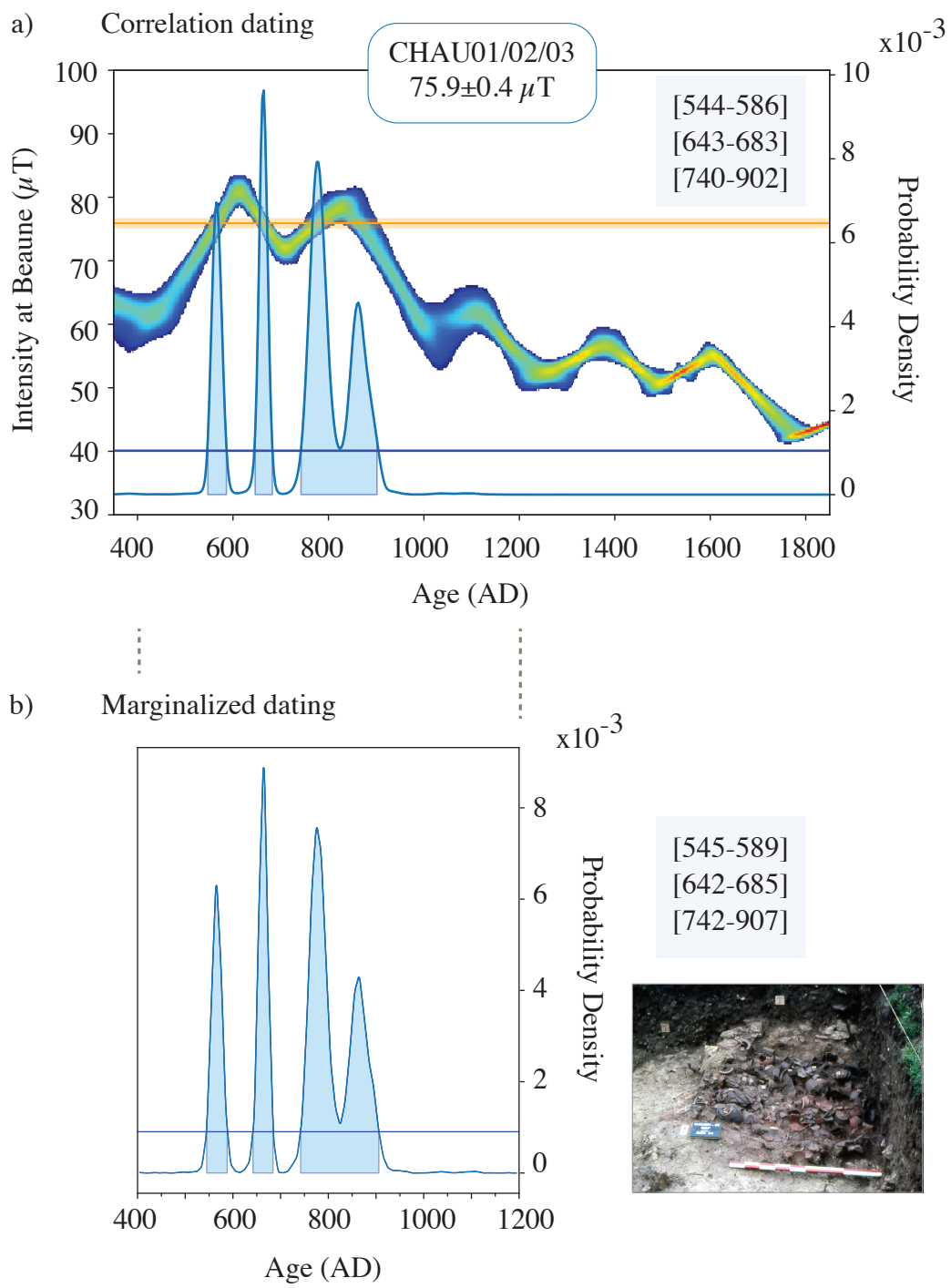


Figure S2.

Supp. Table 1

Fragment	Specimen	Natural magnetic moment	Tmin-Tmax	F Lab	NRM T1 (T1')	Slope R'	F Triaxe	F Triaxe mean value per fragment $\pm \sigma F$
		$10^{-8} \text{ A.m}^2$	(°C)	( $\mu\text{T}$ )	(%)	(%)	( $\mu\text{T}$ )	( $\mu\text{T}$ )
<b>SAR19, Saran - La Guignace [550-620] AD, (23/20/18/12)*, (42/26)**</b>								
SAR19-02	SAR19-02A	52	315-495	75	87	0	80.7	80.2 $\pm$ 0.5
	SAR19-02B	85	350-495	75	89	1	79.6	
SAR19-04	SAR19-04A	43	210-495	75	88	0	78.4	78.9 $\pm$ 0.5
	SAR19-04C	49	180-485	75	86	-2	79.4	
SAR19-05	SAR19-05A	49	195-495	75	89	0	78.3	76.4 $\pm$ 1.4
	SAR19-05B	37	180-485	75	86	0	75.5	
SAR19-06	SAR19-06A	87	180-495	75	94	-3	76.3	74.8 $\pm$ 1.7
	SAR19-06B	94	180-485	75	90	6	74.1	
	SAR19-06C	101	180-485	75	92	1	72.8	
	SAR19-06D	71	180-470	75	84	-2	76.1	
SAR19-07	SAR19-07A	102	180-495	75	90	-1	74.6	76.2 $\pm$ 1.6
	SAR19-07B	116	180-485	75	91	-2	77.8	
SAR19-12	SAR19-12A	54	180-495	75	90	3	72.8	72.5 $\pm$ 0.4
	SAR19-12B	59	175-480	75	90	3	72.1	
SAR19-13	SAR19-13A	122	180-485	75	91	4	76.0	76.7 $\pm$ 0.7
	SAR19-13B	130	180-475	75	89	5	77.3	
SAR19-14	SAR19-14A	117	225-485	75	80	5	75.1	74.6 $\pm$ 0.5
	SAR19-14B	96	235-485	75	86	3	74.1	
SAR19-16	SAR19-16A	268	180-485	75	91	1	78.6	78.2 $\pm$ 0.4
	SAR19-16B	227	180-470	75	88	1	77.7	
SAR19-18	SAR19-18A	67	265-485	75	86	-6	74.6	75.3 $\pm$ 0.7
	SAR19-18B	69	245-490	75	84	1	76.0	
SAR19-21	SAR19-21A	200	180-485	75	78	4	82.1	82.6 $\pm$ 0.5
	SAR19-21B	195	180-485	75	81	-2	83.1	
SAR19-23	SAR19-23A	212	180-485	75	91	-2	77.9	78.4 $\pm$ 0.5
	SAR19-23C	210	190-470	75	86	-3	78.9	
<b>SAR21, Saran - La Guignace [600-650] AD, (16/10/10/5)*, (28/16)**</b>								
SAR21-02	SAR21-02A	73	200-495	75	92	4	78.3	77.8 $\pm$ 1.1
	SAR21-02B	65	200-495	75	79	1	76.5	
	SAR21-02C	57	180-490	75	84	0	78.6	
SAR21-03	SAR21-03A	72	260-495	75	90	6	74.6	76.0 $\pm$ 1.3
	SAR21-03B	50	260-495	75	83	0	77.3	
SAR21-05	SAR21-05B	62	220-505	75	83	2	77.6	76.1 $\pm$ 2.1
	SAR21-05C	71	190-495	75	90	3	73.7	
	SAR21-05E	95	200-505	75	91	-1	77.0	
SAR21-11	SAR21-11A	52	180-480	75	80	5	80.8	81.7 $\pm$ 1.9
	SAR21-11B	61	180-485	75	85	1	84.6	
	SAR21-11C	37	205-485	75	81	1	80.5	
	SAR21-11D	40	195-480	75	90	-3	80.9	
SAR21-15	SAR21-15A	43	280-480	75	71	-6	76.4	77.0 $\pm$ 1.3
	SAR21-15B	39	265-505	75	80	-4	77.5	
	SAR21-15C	47	270-505	75	79	3	78.4	
	SAR21-15D	50	270-505	75	81	0	75.5	

**VAN03, Vanves - rue Gaudray [650-700] AD, (13/11/10/4)\*, (25/10)\*\***

VAN03-23	VAN03-23A	547	265-510	75	99	4	76.7	77.7±1.0
	VAN03-23B	668	265-490	75	98	4	78.7	
VAN03-28	VAN03-28A	145	285-490	75	90	7	77.1	77.6±1.2
	VAN03-28C	138	260-475	75	81	4	79.0	
	VAN03-28D	115	275-490	75	84	6	76.7	
VAN03-30	VAN03-30A	134	225-490	75	86	5	77.5	77.1±0.5
	VAN03-30D	95	200-500	75	81	1	76.6	
VAN03-31	VAN03-31B	56	175-485	75	78	0	76.1	75.3±0.7
	VAN03-31C	75	180-500	75	82	5	75.1	
	VAN03-31D	84	190-500	75	79	3	74.8	

**VAN09, Vanves - rue Gaudray [650-700] AD, (11/11/10/4)\*, (22/9)\*\***

VAN09-06	VAN09-06A	65	250-510	75	90	3	75.7	75.9±0.2
	VAN09-06C	60	250-500	75	80	3	76.1	
VAN09-07	VAN09-07A	103	185-510	75	94	1	76.3	75.9±0.4
	VAN09-07B	90	175-495	75	91	3	75.5	
VAN09-08	VAN09-08A	161	195-510	75	95	5	76.0	77.3±1.3
	VAN09-08B	108	175-495	75	94	1	78.6	
VAN09-11	VAN09-11A	89	175-510	75	91	7	73.5	74.1±0.7
	VAN09-11B	94	175-495	75	85	-4	74.9	
	VAN09-11C	52	175-495	75	81	3	74.0	

**CHAM03, Chamigny - La Grande Maison [675-725] AD, (19/12/9/4)\*, (24/15)\*\***

CHAM03-03	CHAM03-03A	70	275-525	75	73	3	73.2	73.7±1.3
	CHAM03-03B	131	250-515	75	73	8	75	
	CHAM03-03C	89	255-525	75	78	5	72.1	
	CHAM03-03D	126	250-510	75	72	4	74.3	
CHAM03-09	CHAM03-09B	319	285-525	75	85	4	69.6	71.8±1.8
	CHAM03-09D	191	235-515	75	82	-3	72.3	
	CHAM03-09E	257	250-515	75	91	4	73.9	
	CHAM03-09F	204	280-505	75	75	5	71.3	
CHAM03-10	CHAM03-10A	36	290-520	75	78	3	72.8	73.1±1.0
	CHAM03-10B	34	290-515	75	75	0	74.3	
	CHAM03-10D	39	280-515	75	80	6	72.3	
CHAM03-18	CHAM03-18A	67	190-520	75	89	3	71.6	72.2±0.5
	CHAM03-18B	76	195-500	75	85	1	72.5	
	CHAM03-18D	47	190-500	75	84	-6	72.6	
	CHAM03-18E	66	180-500	75	84	5	72.2	

**SAR36, Saran - Voie nouvelle [700-750] AD, (12/7/7/4)\*, (30/12)\*\***

SAR36-01	SAR36-01A	41	175-500	75	92	1	72.5	72.3±1.1
	SAR36-01B	32	180-485	75	88	-5	73.3	
	SAR36-01C	37	180-485	75	86	-2	71.2	
SAR36-08	SAR36-08A	48	245-500	75	92	9	73.5	73.4±1.2
	SAR36-08B	43	225-500	75	89	8	72.2	
	SAR36-08C	39	175-500	75	90	-7	74.5	
SAR36-12	SAR36-12A	39	340-500	75	85	5	75.7	76.5±0.7
	SAR36-12B	155	340-500	75	86	3	76.9	
	SAR36-12D	69	330-500	75	89	3	76.9	
SAR36-13	SAR36-13A	120	175-500	75	87	2	76.4	76.5±0.6
	SAR36-13B	68	185-490	75	78	0	77.1	
	SAR36-13C	42	190-500	75	89	2	76.0	

**HERME04, Hermé - Les Malletons carrière SPM [970-1000] AD, (30/15)\*\***

HERME04-01A	76	215-490	65	66	-1	66.8
HERME04-01B	143	220-515	65	84	-2	60.4
HERME04-01C	145	200-495	60	75	7	66.6
HERME04-01D	61	200-515	60	74	-7	62.9
HERME04-02A	74	185-500	65	73	-2	60.8
HERME04-02B	56	200-515	65	76	-3	60.5
HERME04-02E	61	180-500	60	75	-3	60.7
HERME04-03A	113	195-505	65	74	-2	64.7
HERME04-03B	82	205-510	65	76	-6	62.5
HERME04-04A	91	225-520	65	82	0	63.3
HERME04-04C	103	175-520	65	79	-1	65.5
HERME04-06A	145	210-520	65	76	-4	60.3
HERME04-06B	129	220-515	65	74	-5	59.9
HERME04-06C	110	235-520	60	69	3	61.3
HERME04-06D	98	205-515	60	66	0	61.8

**BOUR01/02, La Chapelle Saint-Ursin, L'angoulaire, chemin des vallées aux fruscades, (26/20/17/4)\*, (29/13)\*\***

BOUR01-05	BOUR01-05A	243	175-475	70	88	-1	74.0	74.1±0.3
	BOUR01-05C	135	185-475	75	93	0	74.4	
	BOUR01-05E	227	195-475	75	93	-1	73.9	
BOUR02-03	BOUR02-03A	743	225-485	75	57	-1	74.8	73.6±1.1
	BOUR02-03B	515	225-510	75	86	-2	73.5	
	BOUR02-03D	479	225-490	75	58	-1	72.6	
BOUR02-05	BOUR02-05A	702	175-505	75	94	-4	75.5	75.8±2.6
	BOUR02-05B	610	175-500	75	84	-1	78.3	
	BOUR02-05C	449	175-495	75	94	-3	72.2	
	BOUR02-05D	646	195-495	75	76	-1	77.1	
BOUR02-07	BOUR02-07A	785	175-495	75	66	-2	69.8	69.1±0.8
	BOUR02-07B	805	175-510	75	75	4	68.2	
	BOUR02-07C	810	175-500	75	81	-1	69.3	

**BOUR03, La Chapelle Saint-Ursin, L'angoulaire, chemin des vallées aux fruscades, (33/11)\*\***

BOUR03-01A	236	180-500	75	68	3	72.3
BOUR03-01D	172	190-490	75	82	-7	74.2
BOUR03-02A	265	180-500	75	88	-1	74.4
BOUR03-02B	318	175-525	75	94	-3	75.7
BOUR03-03A	143	175-505	75	72	-1	69.2
BOUR03-03C	380	180-490	75	81	-1	75.5
BOUR03-03G	200	150-490	75	68	1	75.2
BOUR03-08A	175	175-500	75	66	5	75.0
BOUR03-08C	120	180-490	75	79	-2	76.9
BOUR03-10B	550	160-490	75	59	-5	72.8
BOUR03-10C	200	180-490	75	79	-8	72.2

**CHAU01/02, Viennes-en-Arthies - Chaudry, (25/25/24/4)\*, (48/12)\*\***

CHAU01-01	CHAU01-01A	891	175-515	75	90	2	76.7	77.7±0.8
	CHAU01-01B	900	180-505	75	83	3	78.2	
	CHAU01-01C	840	180-505	75	83	1	78.1	
CHAU01-03	CHAU01-03A	438	385-500	75	80	2	76.0	76.8±1.4
	CHAU01-03C	342	385-505	75	88	6	76.0	
	CHAU01-03D	496	365-495	75	81	-2	78.4	
CHAU01-12	CHAU01-12A	751	180-525	75	97	2	78.3	77.7±1.1
	CHAU01-12B	840	180-505	75	92	-1	78.4	
	CHAU01-12C	658	185-505	75	93	-2	76.5	
CHAU02-08	CHAU02-08B	385	180-515	75	95	-1	76.8	77.0±0.3
	CHAU02-08C	441	180-505	75	89	0	76.8	
	CHAU02-08D	316	180-495	75	88	-3	77.3	

**CHAU03, Viennes-en-Arthies - Chaudry, (12/11/9/2)\*, (20/6)\*\***

CHAU03-05	CHAU03-05A	85	180-530	75	81	3	77.1	77.8±0.9
	CHAU03-05B	276	180-525	75	88	0	78.9	
	CHAU03-05C	123	175-505	75	73	3	77.5	
CHAU03-08	CHAU03-08A	87	180-535	75	81	-6	77.7	77.3±0.3
	CHAU03-08B	42	185-525	75	70	2	77.1	
	CHAU03-08C	124	210-525	75	83	3	77.2	

Supp. Table 2

Age (AD)	Bootstrap algorithm						Transdimensional bayesian technique								
	Fig. 6a			Fig. 6b			Fig. 6c				Fig. 6d				
	Probability Maximum ( $\mu T$ )	Lower Limit ( $\mu T$ )	Upper Limit ( $\mu T$ )	Probability Maximum ( $\mu T$ )	Lower Limit ( $\mu T$ )	Upper Limit ( $\mu T$ )	Age (AD)	Probability Maximum ( $\mu T$ )	Median ( $\mu T$ )	Lower Limit ( $\mu T$ )	Upper Limit ( $\mu T$ )	Probability Maximum ( $\mu T$ )	Median ( $\mu T$ )	Lower Limit ( $\mu T$ )	Upper Limit ( $\mu T$ )
300.00				66.70	74.87	58.61	298.02	52.85	57.65	44.91	81.16	65.45	66.05	59.76	76.93
303.00				66.38	73.99	58.77	301.03	53.15	57.65	45.58	79.92	65.75	66.05	60.24	75.73
306.00				66.04	73.13	58.94	304.03	53.75	57.65	46.24	78.68	65.15	65.75	60.50	74.58
309.00				65.68	72.29	59.07	307.03	54.65	57.65	46.82	77.44	65.45	65.45	60.60	73.51
312.00				65.30	71.45	59.14	310.04	54.05	57.65	47.41	76.22	65.15	65.15	60.56	72.46
315.00				64.91	70.65	59.17	313.04	54.35	57.65	47.96	74.96	64.85	65.15	60.43	71.46
318.00				64.53	69.93	59.13	316.05	54.65	57.95	48.48	73.62	64.85	64.85	60.20	70.55
321.00				64.16	69.31	59.02	319.05	55.85	57.95	49.00	72.30	64.55	64.55	59.90	69.70
324.00				63.78	68.79	58.75	322.05	55.85	57.95	49.49	70.94	64.55	64.25	59.54	68.97
327.00				63.42	68.44	58.41	325.06	56.75	57.95	49.98	69.64	64.25	64.25	59.07	68.35
330.00				63.09	68.19	57.98	328.06	56.75	58.25	50.42	68.50	64.25	63.95	58.54	67.87
333.00				62.80	68.06	57.55	331.06	57.35	58.25	50.82	67.63	63.95	63.65	57.96	67.48
336.00				62.54	67.96	57.12	334.07	57.35	58.25	51.13	66.98	63.95	63.65	57.36	67.17
339.00				62.30	67.89	56.71	337.07	57.65	58.25	51.38	66.58	63.95	63.35	56.75	66.95
342.00				62.09	67.83	56.35	340.08	57.65	58.25	51.57	66.36	63.95	63.05	56.10	66.78
345.00				61.91	67.77	56.04	343.08	57.95	58.25	51.66	66.29	63.65	63.05	55.45	66.66
348.00				61.76	67.72	55.79	346.08	57.95	58.25	51.66	66.36	63.65	62.75	54.80	66.58
351.00	60.18	54.39	65.99	61.64	67.66	55.61	349.09	58.25	58.55	51.63	66.53	63.65	62.75	54.16	66.51
354.00	60.37	54.75	65.99	61.55	67.61	55.48	352.09	58.55	58.55	51.51	66.91	63.65	62.45	53.57	66.50
357.00	60.56	55.06	66.06	61.49	67.56	55.41	355.09	58.55	58.55	51.34	67.42	63.35	62.45	53.03	66.49
360.00	60.74	55.32	66.15	61.45	67.52	55.38	358.10	58.55	58.55	51.21	67.98	63.05	62.45	52.61	66.53
363.00	60.91	55.53	66.29	61.42	67.46	55.39	361.10	59.15	58.85	51.10	68.54	63.35	62.15	52.26	66.57
366.00	61.06	55.68	66.44	61.42	67.43	55.41	364.11	58.55	58.85	51.09	69.01	63.05	62.15	52.01	66.61
369.00	61.21	55.80	66.62	61.45	67.42	55.48	367.11	58.85	59.15	51.12	69.45	63.05	62.15	51.86	66.64
372.00	61.35	55.88	66.81	61.50	67.43	55.58	370.11	59.15	59.15	51.22	69.73	62.75	61.85	51.80	66.71
375.00	61.49	55.95	67.02	61.57	67.45	55.69	373.12	59.15	59.45	51.39	70.02	62.75	61.85	51.79	66.81
378.00	61.63	56.01	67.25	61.62	67.47	55.78	376.12	59.45	59.45	51.67	70.10	62.75	61.85	51.86	66.83
381.00	61.75	56.05	67.46	61.68	67.49	55.87	379.12	59.75	59.75	52.00	70.09	62.75	61.55	52.01	66.88
384.00	61.86	56.07	67.65	61.74	67.53	55.96	382.13	60.05	59.75	52.37	69.99	62.75	61.55	52.20	66.89
387.00	61.96	56.09	67.82	61.81	67.58	56.05	385.13	60.05	60.05	52.79	69.76	62.45	61.55	52.47	66.84
390.00	62.03	56.11	67.96	61.88	67.63	56.13	388.14	60.35	60.05	53.21	69.42	62.45	61.25	52.80	66.75
393.00	62.10	56.14	68.06	61.93	67.67	56.19	391.14	60.35	60.35	53.66	68.97	62.45	61.25	53.17	66.62
396.00	62.16	56.18	68.13	61.98	67.70	56.26	394.14	60.35	60.35	54.12	68.39	62.15	61.25	53.57	66.47
399.00	62.19	56.23	68.15	62.02	67.72	56.33	397.15	60.35	60.65	54.60	67.81	62.15	61.25	53.99	66.26
402.00	62.21	56.29	68.13	62.06	67.71	56.40	400.15	60.65	60.65	55.04	67.21	61.85	61.25	54.41	66.05
405.00	62.21	56.36	68.07	62.08	67.68	56.48	403.15	61.25	60.95	55.45	66.74	61.85	61.25	54.81	65.89
408.00	62.20	56.46	67.94	62.08	67.61	56.56	406.16	61.25	60.95	55.82	66.40	61.85	61.25	55.20	65.75
411.00	62.16	56.56	67.76	62.06	67.48	56.65	409.16	61.55	61.25	56.13	66.14	61.85	61.25	55.52	65.64
414.00	62.10	56.67	67.53	62.02	67.30	56.74	412.17	61.55	61.25	56.37	65.98	61.85	61.25	55.78	65.57
417.00	62.03	56.80	67.26	61.96	67.09	56.84	415.17	61.85	61.55	56.56	65.90	61.55	61.25	55.99	65.52
420.00	61.94	56.93	66.96	61.89	66.84	56.94	418.17	62.15	61.55	56.72	65.89	61.55	61.25	56.13	65.47
423.00	61.84	57.03	66.65	61.80	66.56	57.03	421.18	62.15	61.85	56.84	65.92	61.55	61.25	56.23	65.45
426.00	61.72	57.12	66.33	61.70	66.30	57.10	424.18	62.15	61.85	56.89	66.02	61.25	61.25	56.27	65.46
429.00	61.61	57.16	66.06	61.60	66.05	57.16	427.18	62.45	62.15	56.92	66.16	61.55	61.25	56.27	65.51
432.00	61.50	57.17	65.82	61.51	65.84	57.16	430.19	62.75	62.15	56.92	66.33	61.55	61.25	56.27	65.57
435.00	61.40	57.15	65.66	61.42	65.69	57.15	433.19	63.05	62.45	56.95	66.50	61.25	61.55	56.27	65.65
438.00	61.31	57.06	65.56	61.33	65.59	57.08	436.20	63.05	62.75	56.99	66.66	61.55	61.55	56.32	65.73
441.00	61.23	56.93	65.56	61.25	65.57	56.95	439.20	63.65	62.75	57.08	66.83	61.85	61.55	56.40	65.83
444.00	61.17	56.76	65.57	61.18	65.60	56.78	442.20	63.65	63.05	57.16	67.00	61.85	61.85	56.49	65.95
447.00	61.12	56.56	65.68	61.13	65.67	56.59	445.21	64.25	63.35	57.25	67.18	62.15	61.85	56.63	66.09
450.00	61.10	56.35	65.82	61.09	65.81	56.38	448.21	64.25	63.35	57.31	67.38	62.15	62.15	56.73	66.26
453.00	61.09	56.15	66.02	61.11	66.00	56.20	451.21	64.85	63.65	57.38	67.59	62.15	62.15	56.84	66.45
456.00	61.12	55.99	66.24	61.15	66.24	56.06	454.22	65.15	63.95	57.43	67.80	62.15	62.45	56.93	66.66
459.00	61.20	55.90	66.50	61.24	66.51	55.96	457.22	65.45	64.25	57.48	68.03	63.05	62.45	57.04	66.88
462.00	61.31	55.86	66.78	61.36	66.80	55.95	460.23	65.75	64.55	57.48	68.26	63.35	62.75	57.13	67.13
465.00	61.47	55.87	67.06	61.53	67.10	55.96	463.23	66.05	64.85	57.50	68.51	63.65	63.05	57.19	67.38
468.00	61.66	55.96	67.35	61.73	67.42	56.05	466.23	66.35	65.15	57.50	68.77	63.95	63.35	57.25	67.64
471.00	61.90	56.11	67.68	61.98	67.76	56.21	469.24	66.65	65.45	57.48	69.03	64.55	63.65	57.29	67.91
474.00	62.18	56.34	68.02	62.29	68.13	56.45	472.24	66.95	65.75	57.45	69.30	64.85	63.95	57.31	68.20
477.00	62.50	56.62	68.39	62.60	68.50	56.71	475.24	67.25	66.05	57.40	69.60	65.45	64.25	57.29	68.50
480.00	62.86	56.95	68.78	62.94	68.88	57.01	478.25	67.55	66.35	57.28	69.90	65.75	64.55	57.27	68.81
483.00	63.25	57.32	69.19	63.33	69.31	57.36	481.25	67.55	66.65	57.13	70.22	66.05	64.85	57.25	69.11
486.00	63.66	57.71	69.61	63.75	69.75	57.75	484.26	67.85	66.95	57.02	70.54	66.35	65.15	57.26	69.42
489.00	64.09	58.12	70.06	64.19	70.22	58.16	487.26	68.15	67.25	56.96	70.86	66.65	65.45	57.30	69.73
492.00	64.55	58.57	70.53	64.66	70.72	58.60	490.26	68.45	67.55	56.92	71.21	67.25	66.05	57.36	70.04
495.00	65.04	59.04	71.04	65.17	71.26	59.07	493.27	68.75	67.85	56.92	71.59	67.85	66.35	57.46	70.34
498.00	65.56	59.54	71.58	65.67	71.79	59.54	496.27	69.05	68.15	57.00	71.97	68.15	66.65	57.60	70.65
501.00	66.07	60.02	72.12	66.18	72.35	60.01	499.27	69.35	68.45	57.14	72.35	68.45	66.95	57.80	70.94
504.00	66.60	60.52	72.67	66.72	72.93	60.51	502.28	69.65	68.75	57.35	72.73	68.45	67.55	58.04	71.24
507.00	67.15	61.04	73.26	67.27	73.52	61.02	505.28	69.95	69.05	57.63	73.10	69.35	67.85	58.35	71.54
510.00	67.71	61.57	73.85	67.83	74.12	61.54	508.29	70.25	69.35	57.99	73.45	69.35	68.15	58.72	71.84
513.00	68.28	62.11	74.45	68.39	74.72	62.07	511.29	70.25	69.65	58.41	73.79	69.65	68.75	59.14	72.14
516.00	68.85	62.66	75.04	68.96	75.31	62.61	514.29	70.55	70.25	58.93	74.13	69.95	69.05	59.58	72.43
519.00	69.42	63.22	75.62	69.52	75.88	63.17									

597.00	77.26	74.63	79.91	77.82	81.35	74.31	595.39	77.45	77.75	75.98	80.08	79.25	79.85	77.05	83.23
600.00	77.25	74.54	79.94	77.91	81.54	74.28	598.40	77.45	77.75	76.06	80.18	79.85	80.15	77.36	83.42
603.00	77.22	74.49	79.94	77.99	81.63	74.34	601.40	77.75	77.75	76.11	80.27	80.45	80.45	77.66	83.56
606.00	77.18	74.46	79.91	78.05	81.68	74.42	604.40	77.45	77.75	76.12	80.34	80.75	80.75	77.95	83.69
609.00	77.15	74.45	79.85	78.11	81.72	74.48	607.41	77.45	77.75	76.10	80.39	80.75	80.75	78.21	83.78
612.00	77.10	74.40	79.79	78.11	81.77	74.45	610.41	77.45	77.75	76.07	80.42	80.75	80.75	78.39	83.84
615.00	77.04	74.32	79.76	78.09	81.84	74.33	613.42	77.15	77.75	76.02	80.43	80.75	81.05	78.45	83.87
618.00	76.97	74.21	79.74	78.02	81.88	74.15	616.42	77.15	77.75	75.96	80.41	80.75	80.75	78.37	83.87
621.00	76.91	74.11	79.71	77.94	81.89	74.00	619.42	76.85	77.45	75.90	80.38	80.75	80.75	78.20	83.84
624.00	76.85	74.04	79.67	77.85	81.79	73.90	622.43	76.85	77.45	75.83	80.30	80.45	80.75	77.96	83.78
627.00	76.78	74.01	79.56	77.76	81.62	73.92	625.43	76.85	77.15	75.75	80.20	80.15	80.45	77.71	83.67
630.00	76.70	74.00	79.41	77.66	81.34	73.98	628.43	76.85	77.15	75.66	80.06	79.55	80.15	77.46	83.51
633.00	76.62	74.01	79.23	77.53	81.02	74.05	631.44	76.55	77.15	75.57	79.90	79.25	79.85	77.22	83.34
636.00	76.54	74.01	79.07	77.39	80.70	74.08	634.44	76.55	76.85	75.48	79.69	78.95	79.25	76.98	83.11
639.00	76.45	73.97	78.94	77.24	80.41	74.06	637.45	76.55	76.85	75.37	79.45	78.65	78.95	76.75	82.83
642.00	76.37	73.89	78.84	77.06	80.14	73.99	640.45	76.25	76.55	75.27	79.19	78.35	78.65	76.51	82.46
645.00	76.28	73.81	78.75	76.87	79.90	73.84	643.45	76.25	76.55	75.15	78.89	78.05	78.35	76.27	81.98
648.00	76.20	73.74	78.66	76.68	79.65	73.69	646.46	76.25	76.25	75.03	78.58	77.75	78.05	76.03	81.42
651.00	76.12	73.74	78.51	76.49	79.38	73.61	649.46	75.95	76.25	74.91	78.29	77.45	77.45	75.76	80.78
654.00	76.04	73.75	78.32	76.32	79.05	73.59	652.46	75.95	75.95	74.78	78.00	77.15	77.15	75.47	80.11
657.00	75.95	73.78	78.11	76.16	78.72	73.59	655.47	75.65	75.95	74.63	77.74	76.85	76.85	75.15	79.47
660.00	75.88	73.78	77.99	76.01	78.44	73.59	658.47	75.65	75.65	74.48	77.49	76.25	76.55	74.78	78.88
663.00	75.80	73.68	77.93	75.87	78.25	73.50	661.48	75.35	75.65	74.30	77.26	76.25	76.25	74.36	78.34
666.00	75.72	73.51	77.95	75.72	78.14	73.31	664.48	75.35	75.35	74.11	77.06	75.95	75.95	73.88	77.84
669.00	75.63	73.26	78.00	75.54	78.08	73.01	667.48	75.05	75.05	73.88	76.88	75.35	75.35	73.36	77.39
672.00	75.50	73.26	77.99	75.33	77.98	72.68	670.49	75.05	75.05	73.62	76.71	75.05	75.05	72.80	76.97
675.00	75.34	73.24	77.95	75.09	77.84	72.33	673.49	74.75	74.75	73.33	76.56	75.05	74.75	72.22	76.59
678.00	75.12	72.51	77.74	74.81	77.59	72.04	676.49	74.75	74.75	72.99	76.40	74.75	74.45	71.66	76.24
681.00	74.89	72.28	77.49	74.51	77.27	71.74	679.50	74.45	74.45	72.61	76.25	74.45	74.15	71.18	75.92
684.00	74.63	72.03	77.23	74.18	76.94	71.41	682.50	74.45	74.15	72.22	76.08	74.15	73.85	70.77	75.60
687.00	74.36	71.70	77.02	73.87	76.68	71.05	685.51	74.15	74.15	71.86	75.89	73.85	73.55	70.43	75.30
690.00	74.09	71.32	76.87	73.57	76.49	70.65	688.51	73.85	73.85	71.52	75.68	73.55	73.25	70.13	75.01
693.00	73.82	71.02	76.77	73.27	76.34	70.19	691.51	73.85	73.85	71.25	75.45	73.25	72.65	69.90	74.74
696.00	73.56	70.45	76.67	72.98	76.20	69.77	694.52	73.55	73.55	71.03	75.21	72.65	72.65	69.71	74.47
699.00	73.33	70.08	76.57	72.74	76.06	69.40	697.52	73.55	73.25	70.85	74.98	72.65	72.35	69.57	74.23
702.00	73.13	69.85	76.41	72.54	75.89	69.19	700.52	73.25	73.25	70.72	74.77	72.35	72.05	69.45	74.02
705.00	72.97	69.72	76.22	72.39	75.69	69.08	703.53	73.25	72.95	70.62	74.61	72.05	72.05	69.35	73.86
708.00	72.84	69.66	76.03	72.28	75.50	69.06	706.53	72.95	72.95	70.55	74.47	72.05	72.05	69.27	73.78
711.00	72.76	69.61	75.91	72.23	75.43	69.03	709.54	72.95	72.65	70.49	74.36	72.05	71.75	69.21	73.78
714.00	72.71	69.57	75.85	72.21	75.43	69.00	712.54	72.65	72.65	70.43	74.29	72.05	72.05	69.17	73.88
717.00	72.70	69.47	75.91	72.22	75.51	68.92	715.54	72.65	72.65	70.37	74.26	72.05	72.05	69.14	74.01
720.00	72.70	69.35	76.05	72.28	75.76	68.81	718.55	72.65	72.65	70.29	74.27	72.05	72.05	69.10	74.20
723.00	72.76	69.23	76.28	72.40	76.08	68.72	721.55	72.65	72.65	70.20	74.32	72.35	72.05	69.06	74.39
726.00	72.84	69.19	76.52	72.57	76.44	68.70	724.55	72.65	72.65	70.09	74.41	72.65	72.35	69.03	74.62
729.00	72.96	69.17	76.75	72.79	76.81	68.78	727.56	72.65	72.65	69.97	74.54	72.95	72.65	69.00	74.88
732.00	73.09	69.23	76.95	73.05	77.16	68.92	730.56	72.95	72.65	69.88	74.68	72.95	72.65	68.98	75.18
735.00	73.24	69.34	77.13	73.33	77.49	69.16	733.57	72.95	72.65	69.81	74.85	73.25	72.95	69.01	75.50
738.00	73.40	69.52	77.28	73.64	77.83	69.46	736.57	73.25	72.95	69.77	75.02	73.55	73.25	69.05	75.86
741.00	73.58	69.72	77.45	73.98	78.16	69.81	739.57	73.25	72.95	69.74	75.21	73.55	73.55	69.14	76.25
744.00	73.78	69.95	77.62	74.33	78.49	70.17	742.58	73.55	73.25	69.75	75.41	73.85	73.55	69.30	76.63
747.00	73.98	70.17	77.80	74.69	78.84	70.55	745.58	73.85	73.25	69.79	75.63	73.85	73.85	69.52	76.99
750.00	74.19	70.38	77.99	75.06	79.20	70.92	748.58	73.85	73.55	69.85	75.87	74.15	74.15	69.85	77.36
753.00	74.41	70.59	78.23	75.40	79.56	71.25	751.59	74.15	73.85	69.95	76.12	74.15	74.45	70.33	77.74
756.00	74.63	70.79	78.48	75.74	79.92	71.57	754.59	74.15	73.85	70.06	76.40	74.45	74.45	70.89	78.09
759.00	74.85	70.97	78.74	76.08	80.29	71.87	757.60	74.45	74.15	70.22	76.69	74.75	74.75	71.45	78.46
762.00	75.07	71.14	79.00	76.40	80.63	72.16	760.60	74.45	74.45	70.42	76.98	74.75	75.05	71.99	78.81
765.00	75.29	71.33	79.24	76.69	80.94	72.44	763.60	74.75	74.45	70.65	77.27	75.05	75.05	72.47	79.16
768.00	75.50	71.53	79.46	76.93	81.17	72.70	766.61	74.75	74.75	70.93	77.56	75.35	75.35	72.89	79.47
771.00	75.69	71.76	79.63	77.14	81.32	72.96	769.61	75.05	74.75	71.24	77.84	75.35	75.65	73.24	79.79
774.00	75.88	72.01	79.75	77.32	81.41	73.24	772.61	75.05	75.05	71.59	78.13	75.65	75.65	73.57	80.06
777.00	76.07	72.31	79.82	77.45	81.40	73.51	775.62	75.35	75.35	71.98	78.42	75.65	75.95	73.86	80.31
780.00	76.24	72.61	79.87	77.54	81.34	73.75	778.62	75.35	75.35	72.38	78.68	75.95	76.25	74.11	80.53
783.00	76.40	72.88	79.92	77.59	81.25	73.93	781.63	75.65	75.65	72.79	78.95	75.95	76.25	74.34	80.74
786.00	76.56	73.12	80.00	77.62	81.21	74.03	784.63	75.65	75.95	73.18	79.21	76.25	76.55	74.54	80.93
789.00	76.73	73.32	80.14	77.64	81.20	74.08	787.63	75.95	75.95	73.55	79.47	76.55	76.85	74.74	81.07
792.00	76.89	73.46	80.31	77.65	81.22	74.06	790.64	76.25	76.25	73.88	79.71	76.55	76.85	74.92	81.16
795.00	77.04	73.59	80.49	77.65	81.28	74.03	793.64	76.25	76.55	74.18	79.91	76.85	77.15	75.08	81.22
798.00	77.18	73.72	80.65	77.68	81.32	74.05	796.64	76.55	76.55	74.44	80.08	76.85	77.45	75.24	81.23
801.00	77.32	73.90	80.73	77.72	81.33	74.10	799.65	76.55	76.85	74.66	80.21	77.15	77.45	75.39	81.22
804.00	77.45	74.14	80.76	77.79	81.29	74.29	802.65	76.85	76.85	74.86	80.32	77.45	77.75	75.53	81.19
807.00	77.59	74.44	80.74	77.88	81.22	74.53	805.66	76.85	77.15	75.04	80.41	77.45	77.75	75.66	81.15
810.00	77.73	74.76	80.70	77.97	81.14	74.79	808.66	77.15	77.45	75.21	80.47	77.75	78.05	75.78	81.11
813.00	77.86	75.06	80.65	78.06	81.10	75.03	811.66	77.45	77.45	75.35	80.53	77.75	78.05	75.88	81.07
816.00	77.96	75.29	80.64	78.15	81.09	75.20	814.67	77.45	77.75	75.48	80.60	78.05	78.05	75.97	

921.00	70.39	63.59	77.20	71.16	78.46	63.86	919.80	69.35	69.35	60.06	74.88	69.35	69.95	62.46	74.83
924.00	69.92	62.71	77.13	70.69	78.41	62.97	922.80	69.05	69.05	59.38	74.47	69.05	69.35	61.67	74.48
927.00	69.43	61.80	77.05	70.21	78.35	62.07	925.81	68.75	68.45	58.80	74.10	68.75	69.05	60.97	74.19
930.00	68.91	60.87	76.95	69.71	78.26	61.16	928.81	68.45	68.15	58.30	73.77	68.45	68.45	60.30	73.94
933.00	68.38	59.94	76.81	69.21	78.12	60.29	931.81	68.15	67.55	57.88	73.41	68.15	68.15	59.74	73.67
936.00	67.84	59.05	76.64	68.69	77.92	59.46	934.82	67.85	67.25	57.55	73.07	67.85	67.85	59.25	73.41
939.00	67.30	58.20	76.41	68.15	77.61	58.69	937.82	67.25	66.95	57.24	72.68	67.25	67.25	58.84	73.12
942.00	66.78	57.43	76.13	67.63	77.22	58.05	940.82	67.25	66.35	56.98	72.26	66.95	66.95	58.49	72.80
945.00	66.26	56.75	75.78	67.12	76.71	57.53	943.83	66.65	66.05	56.76	71.77	66.65	66.35	58.22	72.41
948.00	65.75	56.15	75.35	66.58	76.04	57.12	946.83	66.35	65.45	56.62	71.27	66.35	66.05	57.99	71.98
951.00	65.24	55.65	74.83	66.04	75.26	56.84	949.84	65.75	65.15	56.51	70.72	65.75	65.75	57.78	71.50
954.00	64.72	55.24	74.18	65.51	74.36	56.65	952.84	65.45	64.55	56.48	70.12	65.45	65.15	57.61	70.99
957.00	64.21	54.99	73.43	64.97	73.39	56.56	955.84	65.15	64.25	56.51	69.52	64.85	64.85	57.47	70.40
960.00	63.72	54.87	72.58	64.43	72.34	56.52	958.85	64.55	63.65	56.54	68.91	64.55	64.25	57.38	69.78
963.00	63.22	54.88	71.58	63.90	71.27	56.54	961.85	63.95	63.35	56.62	68.33	64.25	63.95	57.32	69.21
966.00	62.73	54.93	70.51	63.39	70.20	56.58	964.85	63.05	63.05	56.73	67.78	63.95	63.65	57.32	68.62
969.00	62.24	55.09	69.39	62.89	69.16	56.63	967.86	62.45	62.75	56.85	67.25	63.55	63.05	57.32	68.03
972.00	61.79	55.28	68.30	62.41	68.18	56.63	970.86	62.15	62.15	56.96	66.76	63.05	62.75	57.32	67.45
975.00	61.36	55.46	67.27	61.94	67.28	56.59	973.87	61.85	61.85	57.03	66.30	62.45	62.45	57.27	66.93
978.00	60.95	55.54	66.33	61.50	66.51	56.49	976.87	61.55	61.55	57.04	65.89	61.85	61.85	57.18	66.44
981.00	60.56	55.56	65.56	61.10	65.88	56.32	979.87	61.55	61.55	56.97	65.49	61.55	61.55	57.01	65.99
984.00	60.21	55.45	64.95	60.73	65.39	56.07	982.88	60.95	61.25	56.81	65.14	61.25	61.25	56.77	65.60
987.00	59.89	55.26	64.53	60.38	65.00	55.76	985.88	60.95	60.95	56.57	64.83	60.95	60.95	56.43	65.25
990.00	59.60	54.97	64.23	60.04	64.69	55.39	988.88	60.95	60.65	56.26	64.56	60.65	60.65	55.99	64.97
993.00	59.33	54.64	64.02	59.74	64.46	55.02	991.89	60.65	60.65	55.84	64.34	60.35	60.35	55.48	64.76
996.00	59.07	54.27	63.88	59.46	64.26	54.65	994.89	60.65	60.35	55.36	64.19	60.35	60.05	54.90	64.64
999.00	58.84	53.90	63.77	59.19	64.10	54.28	997.90	60.65	60.35	54.84	64.10	60.05	59.75	54.29	64.62
1002.00	58.63	53.71	63.71	58.95	63.96	53.94	1000.90	60.65	60.05	54.27	64.07	60.05	59.75	53.66	64.71
1005.00	58.44	53.23	63.65	58.73	63.85	53.61	1003.90	60.65	60.05	53.71	64.13	59.75	59.45	53.03	64.92
1008.00	58.25	52.90	63.59	58.53	63.75	53.31	1006.91	60.65	60.05	53.17	64.20	59.45	59.15	52.41	65.21
1011.00	58.08	52.61	63.55	58.35	63.68	53.03	1009.91	60.35	60.05	52.64	64.37	59.45	59.15	51.77	65.59
1014.00	57.94	52.35	63.53	58.20	63.63	52.78	1012.91	60.35	59.75	52.11	64.58	59.75	58.85	51.17	65.96
1017.00	57.82	52.13	63.53	58.08	63.63	52.55	1015.92	60.35	59.75	51.59	64.87	59.45	58.85	50.54	66.35
1020.00	57.73	51.92	63.54	57.99	63.63	52.34	1018.92	60.35	59.75	51.10	65.25	60.05	58.85	49.95	66.90
1023.00	57.66	51.75	63.58	57.91	63.67	52.15	1021.93	60.35	59.75	50.61	65.65	59.45	58.55	49.35	67.50
1026.00	57.62	51.60	63.65	57.85	63.73	51.97	1024.93	60.35	59.75	50.13	66.12	60.35	58.55	48.79	68.05
1029.00	57.60	51.46	63.74	57.80	63.81	51.80	1027.93	60.05	59.75	49.70	66.49	60.65	58.55	48.30	68.56
1032.00	57.60	51.35	63.85	57.79	63.93	51.64	1030.94	60.05	59.75	49.30	66.89	60.65	58.55	47.85	68.95
1035.00	57.62	51.25	63.99	57.79	64.07	51.51	1033.94	60.05	59.75	49.01	67.19	60.65	58.85	47.52	69.28
1038.00	57.67	51.17	64.16	57.81	64.24	51.39	1036.94	60.05	59.75	48.80	67.34	60.65	58.85	47.28	69.49
1041.00	57.73	51.12	64.35	57.86	64.43	51.30	1039.95	60.05	59.75	48.61	67.50	60.95	58.85	47.13	69.52
1044.00	57.81	51.07	64.55	57.94	64.64	51.23	1042.95	60.05	59.75	48.50	67.61	60.95	59.15	47.07	69.48
1047.00	57.92	51.07	64.77	58.03	64.86	51.22	1045.96	60.05	59.75	48.48	67.64	60.95	59.15	47.04	69.38
1050.00	58.04	51.09	65.00	58.15	65.09	51.21	1048.96	59.75	59.75	48.53	67.58	60.95	59.45	47.05	69.25
1053.00	58.18	51.14	65.22	58.27	65.31	51.23	1051.96	59.75	59.75	48.66	67.53	60.95	59.75	47.23	69.08
1056.00	58.33	51.22	65.45	58.40	65.52	51.29	1054.97	59.75	59.75	48.87	67.47	60.95	59.75	47.40	68.90
1059.00	58.51	51.36	65.67	58.56	65.72	51.40	1057.97	59.75	59.75	49.13	67.46	60.95	60.05	47.67	68.76
1062.00	58.70	51.53	65.86	58.74	65.92	51.57	1060.97	59.75	59.75	49.46	67.50	60.95	60.35	48.01	68.71
1065.00	58.89	51.74	66.03	58.95	66.10	51.79	1063.98	59.75	60.05	49.90	67.56	60.95	60.35	48.40	68.74
1068.00	59.12	52.03	66.20	59.16	66.26	52.07	1066.98	59.75	60.05	50.36	67.71	60.95	60.65	48.87	68.82
1071.00	59.36	52.38	66.34	59.39	66.38	52.40	1069.99	59.75	60.05	50.92	67.88	60.95	60.65	49.51	68.97
1074.00	59.60	52.78	66.43	59.64	66.48	52.80	1072.99	59.45	60.05	51.57	68.05	60.95	60.95	50.18	69.11
1077.00	59.87	53.25	66.48	59.89	66.52	53.26	1075.99	59.45	60.05	52.25	68.22	61.25	61.25	50.91	69.25
1080.00	60.15	53.78	66.52	60.15	66.54	53.76	1079.00	59.45	60.05	52.96	68.42	61.25	61.25	51.65	69.45
1083.00	60.43	54.34	66.51	60.43	66.54	54.31	1082.00	59.45	60.05	53.71	68.60	61.25	61.55	52.39	69.64
1086.00	60.71	54.93	66.50	60.70	66.53	54.88	1085.00	59.45	60.35	54.46	68.79	61.25	61.55	53.21	69.81
1089.00	60.99	55.51	66.47	60.98	66.50	55.46	1088.01	59.45	60.35	55.26	68.92	61.25	61.55	54.07	69.91
1092.00	61.26	56.08	66.44	61.25	66.48	56.03	1091.01	59.15	60.35	56.03	69.07	61.55	61.85	54.89	70.04
1095.00	61.53	56.63	66.43	61.51	66.46	56.56	1094.02	59.15	60.35	56.75	69.13	61.55	61.85	55.73	70.09
1098.00	61.78	57.13	66.43	61.75	66.47	57.04	1097.02	59.15	60.65	57.21	69.14	61.55	61.85	56.56	70.03
1101.00	62.02	57.57	66.46	61.98	66.48	57.48	1100.02	59.15	60.65	57.43	69.10	61.85	62.15	57.25	69.93
1104.00	62.24	57.96	66.53	62.21	66.55	57.87	1103.03	59.15	60.65	57.53	68.96	61.55	62.15	57.77	69.74
1107.00	62.43	58.26	66.61	62.41	66.64	58.18	1106.03	58.85	60.95	57.58	68.85	61.55	62.15	58.06	69.52
1110.00	62.59	58.49	66.70	62.58	66.73	58.42	1109.03	58.85	60.95	57.60	68.66	61.55	62.15	58.24	69.26
1113.00	62.71	58.64	66.78	62.70	66.81	58.60	1112.04	58.85	60.95	57.59	68.44	61.85	62.15	58.34	68.94
1116.00	62.79	58.74	66.84	62.79	66.86	58.71	1115.04	58.85	60.95	57.57	68.21	61.55	61.85	58.37	68.63
1119.00	62.84	58.82	66.86	62.84	66.87	58.79	1118.05	58.85	60.65	57.55	67.98	61.55	61.85	58.37	68.34
1122.00	62.84	58.85	66.84	62.83	66.84	58.84	1121.05	58.85	60.65	57.51	67.74	61.55	61.85	58.32	68.08
1125.00	62.78	58.86	66.71	62.80	66.72	58.87	1124.05	58.55	60.65	57.46	67.47	61.55	61.85	58.25	67.73
1128.00	62.68	58.85	66.50	62.69	66.51	58.86	1127.06	58.55	60.35	57.41	67.17	61.25	61.55	58.15	67.39
1131.00	62.51	58.81	66.20	62.53	66.22	58.73	1130.06	58.55	60.35	57.35	66.88	60.65	61.25	58.04	67.10
1134.00	62.31	58.75	65.86	62.30	65.86	58.74	1133.06	58.55	60.05	57.29	66.59	60.65	61.25	57.91	66.78
1137.00	62.06	58.64	65.48	62.04	65.47	58.61	1136.07	58.55	59.75	57.21	66.29	60.35	60.95	57.77	66.48
1140.00	61.76	58.45	65.06	61.73	65.06										



1245.00	52.60	48.55	56.65	52.52	55.86	49.17	1244.20	56.45	55.25	49.74	57.24	52.55	52.25	49.71	54.46
1248.00	52.73	48.86	56.62	52.61	55.93	49.31	1247.21	56.45	55.25	49.85	57.18	52.55	52.25	49.76	54.35
1251.00	52.87	49.14	56.61	52.71	55.95	49.46	1250.21	56.45	55.25	49.97	57.12	52.55	52.25	49.80	54.27
1254.00	53.02	49.38	56.66	52.80	55.94	49.66	1253.21	56.45	55.25	50.09	57.07	52.55	52.25	49.84	54.21
1257.00	53.16	49.57	56.75	52.88	55.93	49.84	1256.22	56.15	54.95	50.22	57.01	52.55	52.25	49.85	54.16
1260.00	53.30	49.71	56.88	52.95	55.92	49.99	1259.22	56.15	54.95	50.35	56.95	52.55	52.25	49.87	54.15
1263.00	53.43	49.82	57.04	53.02	55.96	50.07	1262.23	56.15	54.95	50.50	56.89	52.55	52.25	49.87	54.16
1266.00	53.56	49.91	57.22	53.07	56.04	50.09	1265.23	56.15	54.95	50.64	56.84	52.55	52.25	49.85	54.19
1269.00	53.67	49.97	57.38	53.10	56.18	50.02	1268.23	56.15	54.95	50.76	56.78	52.55	52.25	49.81	54.23
1272.00	53.77	50.03	57.51	53.13	56.33	49.93	1271.24	55.85	54.95	50.89	56.73	52.85	52.55	49.75	54.29
1275.00	53.86	50.12	57.61	53.16	56.48	49.85	1274.24	55.85	54.95	51.02	56.67	52.85	52.55	49.68	54.35
1278.00	53.93	50.22	57.62	53.20	56.60	49.81	1277.24	55.85	54.95	51.15	56.62	52.85	52.55	49.59	54.42
1281.00	53.97	50.33	57.61	53.25	56.69	49.81	1280.25	55.85	54.95	51.29	56.57	53.15	52.85	49.50	54.49
1284.00	54.01	50.47	57.55	53.30	56.75	49.85	1283.25	55.85	54.95	51.43	56.52	53.15	52.85	49.41	54.56
1287.00	54.04	50.62	57.45	53.34	56.76	49.92	1286.26	55.85	54.95	51.58	56.47	53.45	52.85	49.31	54.63
1290.00	54.05	50.78	57.33	53.39	56.76	50.01	1289.26	55.55	54.95	51.71	56.42	53.45	53.15	49.22	54.71
1293.00	54.07	50.95	57.19	53.44	56.75	50.13	1292.26	55.55	54.95	51.87	56.37	53.45	53.15	49.13	54.79
1296.00	54.08	51.12	57.04	53.50	56.74	50.25	1295.27	55.55	54.95	52.04	56.33	53.75	53.45	49.07	54.87
1299.00	54.10	51.29	56.90	53.56	56.73	50.39	1298.27	55.55	54.95	52.20	56.28	53.75	53.45	49.07	54.95
1302.00	54.11	51.45	56.77	53.63	56.73	50.52	1301.27	55.55	54.95	52.39	56.24	53.75	53.45	49.10	55.04
1305.00	54.13	51.60	56.66	53.70	56.74	50.66	1304.28	55.25	54.95	52.58	56.19	54.05	53.75	49.22	55.13
1308.00	54.16	51.74	56.58	53.78	56.75	50.81	1307.28	55.25	54.95	52.77	56.16	54.05	53.75	49.42	55.23
1311.00	54.21	51.88	56.54	53.88	56.77	50.99	1310.29	55.25	54.95	52.98	56.13	54.35	54.05	49.73	55.33
1314.00	54.27	52.02	56.53	53.99	56.78	51.19	1313.29	55.25	54.95	53.19	56.11	54.35	54.05	50.15	55.44
1317.00	54.35	52.17	56.52	54.10	56.78	51.43	1316.29	55.25	54.95	53.40	56.11	54.35	54.05	50.73	55.56
1320.00	54.45	52.34	56.56	54.24	56.76	51.71	1319.30	55.25	54.95	53.58	56.13	54.35	54.05	51.40	55.70
1323.00	54.57	52.54	56.60	54.40	56.75	52.05	1322.30	54.95	54.95	53.74	56.17	54.65	54.35	52.12	55.85
1326.00	54.71	52.76	56.66	54.58	56.75	52.41	1325.30	54.95	54.95	53.86	56.23	54.65	54.65	52.77	56.03
1329.00	54.88	53.01	56.74	54.77	56.81	52.76	1328.31	54.95	54.95	53.93	56.33	54.95	54.95	53.31	56.29
1332.00	55.06	53.26	56.86	54.98	56.97	52.98	1331.31	54.95	54.95	53.98	56.45	54.95	54.95	53.65	56.66
1335.00	55.25	53.49	57.03	55.20	57.31	53.09	1334.32	54.95	54.95	54.00	56.60	55.25	55.25	53.87	57.13
1338.00	55.46	53.66	57.25	55.42	57.76	53.06	1337.32	54.95	54.95	53.99	56.77	55.25	55.25	54.02	57.59
1341.00	55.66	53.79	57.54	55.63	58.27	53.00	1340.32	54.95	54.95	53.98	56.94	55.25	55.55	54.14	58.02
1344.00	55.86	53.83	57.88	55.85	58.77	52.93	1343.33	54.95	54.95	53.96	57.11	55.55	55.55	54.23	58.41
1347.00	56.04	53.84	58.24	56.05	59.18	52.94	1346.33	54.65	54.95	53.94	57.27	55.55	55.85	54.30	58.74
1350.00	56.21	53.81	58.62	56.23	59.48	52.99	1349.33	54.65	54.95	53.91	57.41	55.85	55.85	54.35	59.01
1353.00	56.36	53.76	58.97	56.39	59.62	53.14	1352.34	54.65	54.95	53.88	57.54	55.85	56.15	54.40	59.22
1356.00	56.48	53.69	59.28	56.50	59.70	53.30	1355.34	54.65	54.95	53.84	57.67	56.15	56.15	54.44	59.41
1359.00	56.57	53.62	59.51	56.58	59.74	53.43	1358.35	54.65	54.95	53.81	57.77	56.15	56.45	54.47	59.55
1362.00	56.61	53.56	59.66	56.65	59.83	53.43	1361.35	54.35	54.95	53.77	57.85	56.15	56.45	54.48	59.65
1365.00	56.62	53.51	59.74	56.68	59.99	53.38	1364.35	54.35	54.95	53.73	57.92	56.45	56.45	54.48	59.75
1368.00	56.60	53.45	59.74	56.68	60.18	53.21	1367.36	54.35	54.65	53.69	57.96	56.45	56.45	54.46	59.84
1371.00	56.52	53.39	59.65	56.67	60.36	52.98	1370.36	54.35	54.65	53.65	58.01	56.45	56.75	54.43	59.94
1374.00	56.43	53.32	59.53	56.62	60.49	52.76	1373.36	54.35	54.65	53.61	58.03	56.45	56.75	54.40	60.03
1377.00	56.31	53.25	59.36	56.54	60.50	52.55	1376.37	54.35	54.65	53.57	58.03	56.45	56.75	54.36	60.11
1380.00	56.15	53.15	59.15	56.43	60.49	52.37	1379.37	54.05	54.65	53.53	58.03	56.45	56.75	54.31	60.18
1383.00	55.97	53.02	58.92	56.30	60.39	52.21	1382.38	54.05	54.65	53.48	58.02	56.45	56.75	54.26	60.22
1386.00	55.77	52.87	58.68	56.15	60.22	52.07	1385.38	54.05	54.35	53.43	58.00	56.45	56.75	54.21	60.25
1389.00	55.57	52.69	58.45	55.98	60.02	51.94	1388.38	54.05	54.35	53.39	57.96	56.45	56.45	54.16	60.26
1392.00	55.36	52.49	58.23	55.79	59.77	51.81	1391.39	54.05	54.35	53.34	57.90	56.15	56.45	54.11	60.23
1395.00	55.14	52.27	58.02	55.58	59.50	51.66	1394.39	54.05	54.35	53.29	57.82	56.15	56.45	54.06	60.19
1398.00	54.92	52.02	57.81	55.37	59.22	51.52	1397.39	54.05	54.35	53.24	57.73	56.15	56.15	54.01	60.09
1401.00	54.69	51.76	57.61	55.16	58.94	51.37	1400.40	53.75	54.05	53.19	57.61	55.85	56.15	53.96	59.95
1404.00	54.47	51.51	57.43	54.95	58.68	51.22	1403.40	53.75	54.05	53.13	57.48	55.55	55.85	53.91	59.78
1407.00	54.26	51.28	57.24	54.75	58.43	51.08	1406.40	53.75	54.05	53.08	57.30	55.25	55.85	53.84	59.56
1410.00	54.06	51.07	57.04	54.57	58.18	50.96	1409.41	53.75	54.05	53.02	57.10	55.25	55.55	53.78	59.33
1413.00	53.87	50.91	56.83	54.39	57.93	50.86	1412.41	53.75	54.05	52.96	56.86	54.95	55.55	53.70	59.04
1416.00	53.70	50.79	56.61	54.24	57.66	50.82	1415.42	53.75	53.75	52.90	56.57	54.95	55.25	53.62	58.71
1419.00	53.55	50.76	56.35	54.09	57.37	50.83	1418.42	53.75	53.75	52.84	56.27	54.65	54.95	53.53	58.35
1422.00	53.41	50.75	56.07	53.98	57.06	50.89	1421.42	53.45	53.75	52.77	55.95	54.35	54.95	53.42	57.93
1425.00	53.30	50.84	55.77	53.88	56.71	51.05	1424.43	53.45	53.75	52.70	55.61	54.35	54.65	53.30	57.46
1428.00	53.22	50.98	55.45	53.81	56.32	51.29	1427.43	53.45	53.45	52.62	55.27	54.05	54.35	53.16	56.94
1431.00	53.15	51.16	55.13	53.77	55.96	51.57	1430.43	53.45	53.45	52.51	54.95	54.05	54.05	52.99	56.41
1434.00	53.10	51.32	54.87	53.75	55.65	51.85	1433.44	53.45	53.45	52.38	54.65	53.75	54.05	52.78	55.88
1437.00	53.06	51.40	54.72	53.72	55.48	51.95	1436.44	53.15	53.15	52.21	54.39	53.75	53.75	52.51	55.42
1440.00	53.03	51.38	54.68	53.69	55.40	51.98	1439.45	53.15	53.15	51.99	54.16	53.45	53.45	52.15	55.01
1443.00	53.00	51.32	54.69	53.64	55.44	51.86	1442.45	53.15	53.15	51.69	53.97	53.45	53.45	51.70	54.68
1446.00	52.98	51.15	54.81	53.57	55.47	51.66	1445.45	53.15	52.85	51.33	53.84	53.15	53.15	51.18	54.41
1449.00	52.93	50.97	54.90	53.46	55.48	51.44	1448.46	53.15	52.85	50.92	53.74	52.85	52.85	50.61	54.18
1452.00	52.86	50.78	54.94	53.33	55.45	51.22	1451.46	52.85	52.85	50.48	53.65	52.85	52.55	50.06	53.99
1455.00	52.75	50.61	54.89	53.18	55.33	51.02	1454.46	52.85	52.55	50.05	53.59	52.55	52.55	49.57	53.82
1458.00	52.62	50.43	54.81	53.00	55.18	50.81	1457.47	52.85	52.55	49.69	53.52	52.55	52.25	49.18	53.67
1461.00	52.45	50.24	54.66	52.80	54.99	50.60	1460.47	52.85	52.25	49.41	53.47	52.25	51.95	48.90	53.54
1464.															

1569.00	52.64	50.53	54.76	52.60	54.72	50.48	1568.61	53.45	53.45	51.09	55.08	53.75	53.75	50.92	54.99
1572.00	53.10	50.75	55.44	53.04	55.38	50.70	1571.61	53.75	53.75	51.17	55.99	53.75	53.75	51.15	55.42
1575.00	53.58	51.09	56.08	53.52	56.01	51.03	1574.61	53.75	53.75	51.29	56.92	53.75	54.05	51.48	56.10
1578.00	54.06	51.54	56.57	53.99	56.48	51.50	1577.62	54.05	54.05	51.48	57.23	54.05	54.05	51.98	56.64
1581.00	54.51	52.11	56.91	54.43	56.81	52.04	1580.62	54.05	54.05	51.82	57.31	54.05	54.35	52.57	56.83
1584.00	54.92	52.69	57.15	54.83	57.03	52.64	1583.63	54.05	54.35	52.53	57.28	54.35	54.35	52.90	56.87
1587.00	55.28	53.22	57.34	55.19	57.24	53.15	1586.63	54.35	54.65	52.98	57.20	54.35	54.65	53.10	56.86
1590.00	55.58	53.62	57.54	55.48	57.43	53.53	1589.63	54.65	54.65	53.15	57.16	54.65	54.65	53.23	56.86
1593.00	55.78	53.86	57.69	55.70	57.64	53.75	1592.64	54.65	54.95	53.25	57.14	54.65	54.95	53.30	56.87
1596.00	55.91	54.00	57.81	55.79	57.75	53.82	1595.64	54.95	54.95	53.31	57.11	54.95	54.95	53.37	56.86
1599.00	55.91	54.01	57.81	55.81	57.79	53.82	1598.64	55.25	55.25	53.37	57.06	54.95	54.95	53.42	56.83
1602.00	55.87	54.00	57.75	55.77	57.76	53.78	1601.65	55.25	55.25	53.42	56.97	54.95	54.95	53.47	56.76
1605.00	55.77	53.89	57.65	55.64	57.65	53.62	1604.65	55.25	55.25	53.46	56.83	54.95	54.95	53.51	56.65
1608.00	55.61	53.70	57.51	55.46	57.51	53.40	1607.66	54.95	54.95	53.49	56.66	54.95	54.95	53.52	56.51
1611.00	55.41	53.46	57.36	55.25	57.34	53.15	1610.66	54.95	54.95	53.49	56.46	54.95	54.95	53.50	56.35
1614.00	55.20	53.24	57.17	55.02	57.12	52.90	1613.66	54.65	54.65	53.45	56.25	54.65	54.65	53.42	56.16
1617.00	54.98	53.03	56.93	54.78	56.85	52.71	1616.67	54.65	54.65	53.36	56.03	54.65	54.65	53.31	55.96
1620.00	54.75	52.87	56.62	54.53	56.51	52.55	1619.67	54.35	54.35	53.22	55.82	54.35	54.35	53.16	55.76
1623.00	54.51	52.71	56.31	54.28	56.14	52.41	1622.67	54.35	54.35	53.05	55.62	54.05	54.05	52.99	55.57
1626.00	54.26	52.53	55.99	54.03	55.81	52.24	1625.68	54.05	54.05	52.87	55.44	54.05	54.05	52.80	55.39
1629.00	54.02	52.28	55.76	53.79	55.55	52.02	1628.68	53.75	53.75	52.67	55.28	53.75	53.75	52.60	55.21
1632.00	53.76	51.94	55.58	53.54	55.38	51.70	1631.69	53.45	53.75	52.46	55.13	53.45	53.45	52.39	55.04
1635.00	53.51	51.53	55.48	53.27	55.28	51.27	1634.69	53.45	53.45	52.24	55.00	53.15	53.45	52.18	54.88
1638.00	53.24	51.07	55.40	53.01	55.22	50.80	1637.69	53.15	53.15	52.01	54.86	53.15	53.15	51.96	54.71
1641.00	52.96	50.60	55.33	52.74	55.16	50.32	1640.70	52.85	52.85	51.78	54.71	52.85	52.85	51.73	54.51
1644.00	52.69	50.15	55.22	52.45	55.06	49.85	1643.70	52.55	52.55	51.54	54.52	52.55	52.55	51.50	54.29
1647.00	52.41	49.74	55.07	52.17	54.90	49.44	1646.70	52.25	52.55	51.29	54.30	52.25	52.25	51.25	54.03
1650.00	52.12	49.37	54.87	51.89	54.71	49.07	1649.71	52.25	52.25	51.04	54.05	52.25	52.25	51.01	53.77
1653.00	51.84	49.02	54.67	51.63	54.51	48.75	1652.71	51.95	51.95	50.79	53.77	51.95	51.95	50.75	53.50
1656.00	51.59	48.69	54.49	51.39	54.34	48.44	1655.72	51.65	51.65	50.52	53.48	51.65	51.65	50.50	53.21
1659.00	51.36	48.36	54.36	51.16	54.20	48.13	1658.72	51.35	51.65	50.25	53.18	51.35	51.35	50.23	52.94
1662.00	51.16	48.07	54.26	50.97	54.09	47.85	1661.72	51.35	51.35	49.97	52.88	51.35	51.35	49.96	52.66
1665.00	51.01	47.83	54.18	50.83	54.00	47.65	1664.73	51.05	51.05	49.69	52.60	51.05	51.05	49.69	52.40
1668.00	50.92	47.73	54.11	50.73	53.92	47.56	1667.73	50.75	50.75	49.42	52.32	50.75	50.75	49.43	52.14
1671.00	50.89	47.76	54.02	50.70	53.83	47.56	1670.73	50.45	50.45	49.14	52.06	50.45	50.45	49.16	51.89
1674.00	50.89	47.84	53.94	50.74	53.74	47.73	1673.74	50.45	50.45	48.86	51.80	50.45	50.45	48.89	51.65
1677.00	50.94	48.01	53.86	50.80	53.71	47.90	1676.74	50.15	50.15	48.58	51.56	50.15	50.15	48.62	51.43
1680.00	50.99	48.10	53.87	50.86	53.70	48.02	1679.75	49.85	49.85	48.31	51.33	49.85	49.85	48.35	51.21
1683.00	51.01	48.12	53.90	50.93	53.81	48.01	1682.75	49.55	49.55	48.04	51.12	49.55	49.55	48.09	51.01
1686.00	50.98	48.00	53.98	50.94	53.93	47.97	1685.75	49.55	49.25	47.76	50.93	49.55	49.25	47.81	50.81
1689.00	50.92	47.82	54.00	50.88	54.02	47.75	1688.76	49.25	49.25	47.46	50.74	49.25	49.25	47.52	50.63
1692.00	50.75	47.55	53.95	50.77	54.01	47.51	1691.76	48.95	48.95	47.14	50.54	48.95	48.95	47.21	50.43
1695.00	50.52	47.25	53.80	50.57	53.92	47.23	1694.76	48.65	48.65	46.82	50.32	48.65	48.65	46.91	50.23
1698.00	50.23	46.91	53.55	50.33	53.73	46.93	1697.77	48.35	48.35	46.49	50.10	48.65	48.35	46.59	50.02
1701.00	49.89	46.55	53.22	50.03	53.46	46.61	1700.77	48.35	48.05	46.17	49.89	48.35	48.35	46.28	49.82
1704.00	49.50	46.16	52.83	49.68	53.11	46.25	1703.78	48.05	48.05	45.83	49.69	48.05	48.05	45.96	49.62
1707.00	49.06	45.74	52.39	49.28	52.70	45.86	1706.78	47.75	47.75	45.50	49.48	47.75	47.75	45.64	49.42
1710.00	48.60	45.28	51.92	48.85	52.26	45.43	1709.78	47.45	47.45	45.16	49.26	47.75	47.45	45.31	49.21
1713.00	48.12	44.80	51.44	48.40	51.82	44.99	1712.79	47.45	47.15	44.81	49.05	47.45	47.15	44.98	49.01
1716.00	47.62	44.29	50.95	47.95	51.38	44.52	1715.79	47.15	46.85	44.46	48.84	47.15	47.15	44.65	48.80
1719.00	47.12	43.76	50.48	47.48	50.93	44.03	1718.79	46.85	46.85	44.11	48.63	46.85	46.85	44.31	48.60
1722.00	46.62	43.23	50.01	47.01	50.50	43.53	1721.80	46.55	46.55	43.76	48.42	46.85	46.55	43.98	48.39
1725.00	46.13	42.72	49.55	46.56	50.07	43.04	1724.80	46.25	46.25	43.39	48.20	46.55	46.25	43.63	48.18
1728.00	45.67	42.24	49.10	46.11	49.65	42.58	1727.81	46.25	45.95	43.03	47.99	46.25	45.95	43.28	47.98
1731.00	45.24	41.81	48.66	45.69	49.22	42.17	1730.81	45.95	45.65	42.66	47.77	45.95	45.95	42.92	47.77
1734.00	44.84	41.46	48.22	45.30	48.79	41.81	1733.81	45.65	45.35	42.24	47.56	45.95	45.65	42.53	47.57
1737.00	44.48	41.17	47.79	44.93	48.36	41.51	1736.82	45.65	45.35	41.87	47.38	45.65	45.35	42.12	47.39
1740.00	44.17	40.95	47.40	44.59	47.93	41.25	1739.82	45.35	45.05	41.68	47.20	45.35	45.05	41.82	47.21
1743.00	43.90	40.76	47.04	44.28	47.53	41.04	1742.82	45.05	44.75	41.56	47.01	45.05	44.75	41.66	47.03
1746.00	43.66	40.60	46.72	44.01	47.18	40.85	1745.83	44.75	44.45	41.47	46.83	45.05	44.75	41.56	46.85
1749.00	43.46	40.46	46.46	43.78	46.88	40.68	1748.83	44.75	44.15	41.41	46.65	44.75	44.45	41.49	46.67
1752.00	43.30	40.34	46.27	43.59	46.64	40.53	1751.84	44.45	44.15	41.37	46.47	44.45	44.15	41.43	46.49
1755.00	43.18	40.22	46.13	43.42	46.45	40.38	1754.84	44.15	43.85	41.34	46.28	44.45	43.85	41.40	46.31
1758.00	43.08	40.12	46.04	43.27	46.31	40.23	1757.84	42.05	43.55	41.33	46.10	44.15	43.85	41.39	46.13
1761.00	42.99	40.02	45.97	43.16	46.19	40.13	1760.85	42.35	43.25	41.34	45.92	42.35	43.55	41.40	45.96
1764.00	42.95	40.00	45.91	43.08	46.10	40.06	1763.85	42.35	43.25	41.36	45.74	42.35	43.25	41.40	45.78
1767.00	42.93	40.01	45.85	43.04	46.00	40.07	1766.85	42.35	42.95	41.40	45.56	42.35	42.95	41.42	45.60
1770.00	42.93	40.09	45.76	43.01	45.89	40.14	1769.86	42.35	42.65	41.44	45.39	42.35	42.95	41.46	45.43
1773.00	42.96	40.27	45.65	43.02	45.74	40.29	1772.86	42.35	42.65	41.48	45.21	42.35	42.65	41.50	45.26
1776.00	43.00	40.51	45.49	43.04	45.57	40.51	1775.87	42.65	42.65	41.53	45.04	42.65	42.65	41.54	45.09
1779.00	43.06	40.79	45.34	43.09	45.39	40.79	1778.87	42.65	42.65	41.59	44.88	42.65	42.65	41.60	44.93
1782.00	43.13	41.08	45.18	43.15	45.23	41.08	1781.87	42.65	42.65	41.65	44.72	42.65	42.65	41.66	44.77
1785.00	43.21	41.36	45.06	43.24	45.11	41.36	1784.88	42.65	42.65	41.72	44.56	42.65	42.65	41.73	44.62
1788.															