

# Solute effects on dynamics and deformation of emulsion droplets during freezing

Sidhanth Tyagi, Cécile Monteux, Sylvain Deville

# ► To cite this version:

Sidhanth Tyagi, Cécile Monteux, Sylvain Deville. Solute effects on dynamics and deformation of emulsion droplets during freezing. Soft Matter, 2022, 10.1039/D2SM00226D. hal-03274394v1

# HAL Id: hal-03274394 https://hal.science/hal-03274394v1

Submitted on 8 Oct 2021 (v1), last revised 7 Jul 2022 (v3)

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

1	Solute effects on dynamics and deformation of
2	emulsion droplets during freezing
3	Sidhanth Tyagi <sup>1,2</sup> , Cécile Monteux <sup>2,3</sup> , and Sylvain Deville <sup>4</sup>
4	<sup>1</sup> Laboratoire de Synthèse et Fonctionnalisation des Céramiques, UMR 3080
5	CNRS/Saint-Gobain CREE, Saint-Gobain Research Provence, Cavaillon, France.
6	<sup>2</sup> Sciences et Ingénierie de la Matiére Molle, ESPCI Paris, PSL Research University,
7	CNRS, Sorbonne Universités, UPMC Univ Paris 06, Paris, France.
8	<sup>3</sup> Global Station for Soft Matter, Global Institution for Collaborative Research and
9	Education, Hokkaido University, Sapporo, Japan.
10	<sup>4</sup> Université de Lyon, Université Claude Bernard Lyon1, CNRS, Institut Lumière
11	Matière, 69622 Villeurbanne, France.

June 25, 2021

# 13 Abstract

12

Soft or rigid particles, suspended in a liquid melt, interact with an advancing 14 solidification front in various industrial and natural processes, such as fabrica-15 tion of particle-reinforced-composites, growth of crystals, cryopreservation, frost 16 heave, and growth of sea ice. The particle dynamics relative to the front de-17 termine the microstructure as well as the functional properties of the solidified 18 material. The previous studies have extensively investigated the interaction of 19 foreign objects with a moving solid-liquid interface in pure melts while in most 20 real-life systems, solutes or surface active impurities are almost always present. 21 22 Here we study experimentally the interaction of spherical oil droplets with a

moving planar ice-water interface, while systematically increasing the surfac-23 tant concentration in the bulk liquid, using in situ cryo-confocal microscopy. 24 We demonstrate that a small amount of surfactant in the bulk liquid can insti-25 gate long-range droplet repulsion, extending over a length scale of 40 to 100  $\mu m$ , 26 in contrast to the short-range predicted previously  $(< 1 \ \mu m)$ . We report on the 27 droplet deformation, while they are in contact with the ice-water interface, as a 28 function of the bulk surfactant concentration, the droplet size, and the crystal 29 growth rate. We also depict the dynamic evolution of solute-enriched premelted 30 films ( $\approx 5 \ \mu m$ ). Our results demonstrate how an increasing concentration of 31 surfactant in the bulk and its subsequent segregation during solidification can 32 dramatically alter the solidification microstructures. We anticipate that our 33 experimental study can serve for the development of theoretical models incor-34 porating solute effects. 35

<sup>&</sup>lt;sup>36</sup> Keywords: solidification, solute, droplets, deformation, dynamics

### 37 1 Introduction

The interaction of particles with an approaching solid-liquid interface is of spe-38 cial relevance in nature, like frost heave, glacial motion [1], and in engineering 39 sciences, such as food freeze-thaw stability [2], cryopreservation [3, 4], metal-40 lurgy [5], and crystal growth [6]. This dynamic problem consists of particles, 41 soft or hard, dispersed in a liquid melt interacting with a solid-liquid interface. 42 The objects can be biological cells in cryopreservation [3, 4], colloids in freezecasting [7], droplets in food preservation [8], gas bubbles in growth of single crystals [6,9] and metallurgy [5], or reinforcing particles in material-matrix-45 composites [10]. The outcome of the particle-interface confrontation determines 46 the solidified microstructure and hence, the functional properties of the solidi-47 fied material. Thus, it is essential to understand the underlying mechanisms of 48 solidification (or freezing) to forge the required material microstructure. The 49 particle can interact with an advancing solidification interface with diverse out-50 comes; it can be engulfed instantaneously upon contact, pushed ahead in the 51 remaining liquid by the interface indefinitely, or it may undergo engulfment after 52 being pushed over a certain distance [11]. 53

The dynamics of interaction and spatial distribution of particles are essential 54 features in several material fabrication routes. In particle-reinforced-composites, 55 an instantaneous engulfment in solid phase is desired as it facilitates a homo-56 geneous distribution of the suspended objects [10]. In metallurgy and crystal 57 growth, a continuous repulsion of the impurities by the interface is required to 58 obtain impurity-free-solids [5]. In freeze-casting, a segregation of the colloidal 59 particles by the growing solid enables a porous material structure [7]. The 60 shape of the particle (deformed or undeformed) becomes an equally important 61 processing criterion in applications where soft deformable objects (droplets or 62 bubbles) encounter a moving solid-liquid interface. In cryobiology, utmost care 63 should be taken to avoid physical injury inflicted to the cells from the growing ice crystals [12]. In food preservation, freezing is conducted to conserve the 65

size, shape, and distribution of the dispersed droplets, thereby preserving the
original taste and appearance [8]. Thus, numerous interaction scenarios, still
poorly understood, can exist during solidification.

The role and concentration of solute in the solidifying liquid is often signifi-69 cant and a dominating factor in determining, amongst others, the shape of the 70 solid-liquid interface in the vicinity of the suspended particles [13–15]. Solutes, 71 render the interfacial curvature concave, thereby promoting engulfment of ob-72 jects at growth rates lower than those predicted for planar curvatures [16, 17]. 73 The solutes can be either desired, like additives (e.g. cryoprotectant used in 74 preservation of biological cells), or be present as an undesired impurity, such as 75 dissolved gases  $(H_2)$  in liquid metals or surface active impurities. The segrega-76 tion of solutes at the interface is instigated by their relatively low solubility in the solid phase and enhanced further by the approaching objects obstructing 78 their diffusion field [13]. This local solute enrichment is of particular impor-79 tance in understanding the nucleation and growth of macroporosity in solid-80 ifying melts [14], studying the constitutional supercooling with formation of 81 premelted films [18, 19], and in determining the osmotic stresses acting on a 82 freezing biological cell [4, 12] to give a few examples. Moreover, the morphology 83 of a solid-liquid interface (planar, columnar, or dendritic), determined by the 84 magnitude of solute concentration gradient build-up ahead of the growing solid, 85 plays a major role on the final microstructure [13, 20]. 86

The study of solidification mechanisms such as the particle dynamics, shape 87 evolution, and the local solute concentration are complex and require in situ in-88 vestigations. The major problem associated with studying solidification in situ 89 arises from the need of high space and temporal resolution in conjunction with 90 elevated temperatures especially for metals. For the object dynamics, past stud-91 ies have formulated a plethora of analytical and numerical models expressing 92 the outcome (engulfment or rejection) of objects interacting at close distances 93 (< 10 nm) with the solid-liquid interface [16, 21–24]. The models vary in the 94 mathematical formulation of the features taken into account (e.g. the inclusion 95

of object-melt thermal conductivity mismatch, solute effects etc...), while using 96 a similar approach (balance of repulsive and attractive forces between the object 97 and front) to describe the interaction [11]. The study of particle deformation has been of particular interest in the prediction of pore shape evolution during 99 directional solidification of crystals to avoid or control porosity defects. Much 100 of the progress in this domain has been achieved through numerical simulations 101 and post-solidification analysis [25, 26]. In situ experimental evidence of solidi-102 fication dynamics (repulsion or engulfment) and shape modification have been 103 facilitated using transparent analogs (e.g. succinonitrile-acetone) with optical 104 microscopes at ambient temperatures [20,27] and X-ray transmission microscope 105 at elevated temperatures [14, 28]. However, the volume investigated along with 106 the temporal resolution is limited, while the local solute segregation cannot be 107 visualized. Hence, the tracking of microstructures where objects interact with 108 a solid-liquid interface in the presence of solute effects remains challenging. 109

In this study, we analyse the interaction of spherical oil droplets with an ad-110 vancing ice-water interface using in situ cryo-confocal microscopy. Our custom 111 solidification setup enables a small temporal resolution (1.7 s) and high spatial 112 resolution  $(1024 \times 1024 \text{ pixels})$  with laser-induced fluorescence to distinguish the 113 accumulation of a fluorescent water-soluble dye rejected by the ice. We prepare 114 oil-in-water emulsions using microfluidics stabilized with a varying amount of 115 surfactant Tween 80 in the aqueous phase. We further characterise and report 116 on the in situ droplet dynamics, droplet deformation, and the role of surfactant 117 on the droplet behaviour. 118

We investigate the impact of an increasing surfctant concentration on the mechanisms involved at three different stages: droplets in water (water) far from the solidification front, droplets in contact with an approaching solidliquid interface, and droplets captured in the growing ice. For the droplet-front interaction dynamics, we depict distinct behaviours such as instantaneous engulfment and repulsion-engulfment transition. While confronting a solid-liquid interface, the droplet shape evolution depends on the imposed growth rate and the surfactant concentration. Furthermore, we show the impact of surfactant on the evolution of premelted films surrounding the oil droplets in ice. Finally, we depict that the three interaction stages are crucial in determining the droplet spatial distribution and shape evolution, and hence, the solidification microstructure.

## $_{131}$ 2 Methods

#### 132 2.1 Materials

We purchased the oil (propyl benzoate), surfactant (Tween 80), oil fluorophore 133 (Difluoro2-[1-(3,5-dimethyl-2H-pyrrol-2-ylidene-N)ethyl]-3,5-dimethyl-1H-pyrro 134 lato-Nboron), and aqueous fluorophore (Sulforhodamine B) from Sigma-Aldrich. 135 The fluorophores are referred to as BODIPY (incorporated in oil) and SRhB 136 (incorporated in water) in the study. We cycled the deionized water through 137  $0.45 \ \mu m$  Nylon membrane filters (VWR International) to remove traces of im-138 purities and ensure purity of the emulsions prepared. The solidification ex-139 periments were conducted to study the interaction of dispersed phase with the 140 ice-water interface. Hence, we prepared oil-in-water emulsions to ensure the 141 dispersed phase remained liquid, while the continuous phase underwent solidi-142 fication. Thus, we chose propyl benzoate owing to its low melting temperature 143  $(T_m = -51.6^{\circ} C)$ , low solubility in water (0.035 g/100 g), and similar density 144 to water  $(\rho_{oil} = 1.023 \ g \cdot cm^{-3}).$ 145

#### <sup>146</sup> 2.2 Sample Preparation



Figure 1: Diameter of monodisperse droplets with radii  $(R_1, R_2)$  of 7.2  $\pm$  0.4  $\mu m$  and 30.9  $\pm$  1.2  $\mu m$  respectively, generated using microfluidics. The size of droplets remained stable during the experimental time-scale, which varied from 15 min to 4 h.  $^{\odot}$  (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

We prepared the oil-in-water emulsions using a microfluidic setup, as explained 147 in our previous study [15]. The monodisperse droplets have radii  $(R_1, R_2)$  of 148 either  $7.2 \pm 0.4 \ \mu m$  or  $30.9 \pm 1.2 \ \mu m$ , as shown in Fig.1. The oil phase consisted 149 of propyl benzoate with  $10^{-4}$  M BODIPY to obtain clear imaging of dispersed 150 droplets at 1% laser power. For the aqueous phase, we used  $10^{-5} M$  SRhB 151 solution, as self-quenching was reported at concentrations above  $2 \times 10^{-4} M$  [29]. 152 We added Tween 80 (HLB = 15 [30]), a non-ionic surfactant, to the aqueous 153 phase to stabilise the oil droplets. The surfactant Tween 80 ( cmc = 13 - 15 mg. 154  $l^{-1}$  [31]) also acts as a solute and hence colligatively depresses the freezing point 155 of solutions, when its concentration increases locally [15]. We prepared three 156 aqueous solutions with 0.01, 0.1, and 1 wt.% Tween 80 to study the impact of 157 solute concentration on the solidification dynamics and behaviour of oil droplets 158 dispersed in an aqueous phase. The surfactant is added as wt.% of the aqueous 159 solution to have an equal concentration in all the solutions prepared. 160

The concentration of surfactants in the bulk solution at which micelles start 161 forming is known as the *cmc*. Individual surfactant molecules that are in the 162 system but are not part of a micelle are called monomers [32]. At 1wt.% of 163 Tween 80 in aqueous solution we are  $\approx 600 \times cmc$ . All experiments are therefore 164 performed above the *cmc* and increasing the surfactant concentration results 165 in an increase of the number of micelles in solution while the concentration 166 of surfactant monomers remains approximatively equal to the cmc. The oil-167 in-water emulsion stabilized by the surfactant is represented schematically in 168 Fig.2. The presence of micelles at the given concentration was confirmed by 169 dynamic light scattering (DLS) analysis. A typical micelle size of 9 nm with a 170 corresponding diffusion coefficient of 30  $\mu m^2 \cdot s^{-1}$  at 273 K was obtained from 171 the DLS analysis. The prepared emulsions were filled through capillarity and 172 solidified in a rectangular Hele-Shaw cell (height =100  $\mu m$  and volume =100  $\mu l$ ). 173 We fabricated the Hele-Shaw cell using two glass slides (Menzel,  $24 \times 60 \ mm$ , 174 thickness 0.13 - 0.16 mm), and sealed it with nail-polish at one end to prevent 175 evaporation and leakage. 176



Figure 2: Schematic depicting a monodisperse oil-in-water emulsion with the surfactant Tween 80 and fluorophore SRhB added to the aqueous phase (not to scale). The oil phase is incorporated with the fluorophore BODIPY. The surfactant form micelles. © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

#### 177 2.3 Imaging & Analysis

We used a Leica TCS SP8 confocal laser scanning microscope (Leica Microsys-178 temes SAS, Germany) equipped with 488 nm (blue), 552 nm (green) lasers and 179 two photodetectors (PMT) for image acquisition. The images were captured 180 for the emission spectra of BODIPY (oil phase) and SRhB (aqueous phase), 181 using a non-immersive objective (Leica HCX PL APO CS  $20\times$ ) with a working 182 distance of 590  $\mu m$ . Ice does not fluoresce and hence, we can simultaneously 183 detect three phases (oil droplets, unfrozen aqueous phase, and ice) with two 184 photodetectors. In 2D, we used the microscope at a scanning speed of 600 Hz, 185 with  $1024 \times 1024$  pixels for imaging  $775 \times 775 \ \mu m$ , resulting in 1.7 s per frame. 186 We used Fiji [33] for image thresholding in conjunction with Python [34] for 187 image and data analysis. 188

#### <sup>189</sup> 2.4 Freezing Stage



Figure 3: Cryo-confocal microscope setup to perform in situ solidification experiments. A Hele-Shaw cell containing an oil-in-water emulsion is pulled at a constant velocity  $(V_{sl})$  through a constant linear temperature gradient (G), established by two Peltier elements. In steady-state, the solidification interface is at a constant position under the microscope objective. In the sample frame, the interface is moving at a solidification velocity of  $V_{sl}$ , imposed by the motor.<sup>©</sup> (2020) S. Tyagi *et al.* (10.6084/m9.figshare.12046560) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

- <sup>190</sup> We conducted unidirectional solidification experiments, translating the sample
- <sup>191</sup> cell at a constant velocity  $(V_{sl})$  along a constant linear temperature gradient (G)

of  $10^4 K \cdot m^{-1}$ , using the cryo-confocal stage described in detail previously [35]. 192 We imposed the temperature with two Peltier modules, and controlled it with 193 high precision ( $< 0.01 \,^{\circ}C$ ) using TEC-1122 Dual Thermo Electric Cooling Tem-194 perature Controller from Meerstetter Engineering, Switzerland. The Peltier el-195 ements were separated by a distance of 2 mm to establish a linear temperature 196 gradient along  $\vec{x}$ . The *in situ* observation of objects interacting with the solid-197 liquid interface was achieved using a confocal microscope mounted vertically 198 over the gap (2 mm) between the two Peltier modules, as shown in Fig.3. The 199 solidification interface appears immobile in the frame of observation, however, 200 in the sample frame, a solidifying front at the velocity  $V_{sl}$  is advancing in the 201 sample (along  $\vec{x}$ ). We utilised the VT-80 translation stage (Micos Pollux Drive 202 PI, USA) to impose the rate at the which the sample cell is pulled through the 203 temperature gradient. The rate of translation was verified to be in agreement 20 with the measured solidification velocity  $(V_{sl})$ , using posterior image analysis 205 (error < 1 %). Thus, we can decouple and control independently the solidifica-206 tion velocity  $(V_{sl})$  and the thermal gradient (G) in our system. 207

We performed the solidification experiments in the velocity range of 208  $1.0 \leq V_{sl} \leq 10.0 \ \mu m \cdot s^{-1}$ . We wait for  $20 - 30 \ mins$  to ensure a steady-209 state diffusion controlled regime before starting the acquisition at a given so-210 lidification velocity. The time needed for a steady-state to establish scales as 211  $2D/V_{sl}^2 \approx 60 \ s$ , where D is the solute diffusion coefficient. We do not expect 212 forced convection in our experiments as they are performed in a closed Hele-213 Shaw cell of small thickness (100  $\mu m$ ) and at low solidification velocity with 214 a steady linear temperature gradient. The solid-liquid interface is stable over 215 extended time periods ( $\approx 4-5$  hours) and the interface does not accelerate or 216 decelerate during the solidification experiments. In addition, we do not observe 217 a transient unsteady regime and the interface morphology is stable for the given 218 experimental parameters. 219

## 220 3 Results & Discussions

We performed horizontal solidification experiments by displacing a Hele-Shaw 221 cell, containing an oil-in-water emulsion, in a custom cryo-confocal stage, at a 222 velocity of  $V_{sl}$ . A typical 2D confocal image of a freezing emulsion with the 223 distinct features observed is shown in Fig.4A. The confocal image enables us 224 to distinguish three phases; oil phase in cyan (fluorophore BODIPY), water in 225 colormap viridis (fluorophore SRhB), and a dark ice phase. As solidification 226 progresses, the growing ice phase rejects the dissolved dye, SRhB, owing to its 227 low solubility and hence appears black, which enables us to visualize the solid-228 liquid interface. In the frame of the ice-water interface, the interface is stationary 229 and the droplets far from the ice-water interface are translated at a velocity 230  $V_{sl}$  toward the ice-water interface. In the frame of the sample, the interface 231 is advancing through the sample at a velocity of  $V_{sl}$  along  $\vec{x}$  and eventually 232 encounters droplets which velocity, noted  $U_r$  (defined in Fig. S2) is indicated 233 in Fig.4A. We also note the premelted films between two ice surfaces as well as 234 around the oil droplets captured in the ice phase, which are due to the rejection 235 of the dye by the ice and subsequent depression of the freezing point. 236

A typical time-lapse evolution of an isolated oil droplet interacting with 237 the ice-water interface obtained for an oil-in-water emulsion with 1wt.% Tween 238 80 in the aqueous phase is shown in Fig.4B. The interaction of oil droplets 239 with the solid-liquid interface can be divided in three different stages, which are 240 described below in three different sections. First, we investigate the solidification 241 mechanisms at play when the oil droplets are far from the advancing interface. 242 We investigate the role of an increasing bulk surfactant concentration and the 243 different solidification parameters (growth rate, droplet size) on the droplet 244 dynamics in water ( $t < 44 \ s$  in Fig.4B). Second, we look into the impact of 245 the approaching solid-liquid interface on the droplet shape upon their mutual 246 contact  $(44 \le t \le 57 \ s \text{ in Fig.4B})$ . Third, we analyse the droplets captured in 247 ice and report on the evolution of premelted films with the associated ice-water 248

249 meniscus (99  $\leq t \leq 111 \ s \text{ in Fig.4B}$ ).



Figure 4: 2D cryo-confocal image of freezing an oil-in-water emulsion in the presence of 1wt.% Tween 80 in the aqueous phase. (A) Typical features observed for a planar growth at  $V_{sl} = 2 \ \mu m \cdot s^{-1}$  (B) Time-lapse evolution of an oil droplet encountering an approaching solid-liquid interface with three distinct regimes of interaction at  $V_{sl} = 2 \ \mu m \cdot s^{-1}$ . Ice is in black, oil droplets in cyan, and the aqueous phase is in colormap viridis (fluorescence bar).  $^{\odot}$  (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

#### 250 3.1 Droplets in water

We track the trajectories of the oil droplets which enables us to deduce the 251 isolated droplet velocity  $U_r$  in the sample frame (see details in Fig. S1 and 252 S2). Our Hele-Shaw cell of length 4 cm facilitates an acquisition of 50 - 400253 isolated droplet velocities and we deduce the mean droplet velocity as  $\overline{U} = \langle U_r \rangle$ 254 (The python script employed can be found in a previous study [19]). A positive 255 magnitude of  $\overline{U}$  implies that the droplets are repelled or pushed by the moving 256 ice-water interface towards the remaining liquid. 257 In Fig.5, we present the mean droplet velocity,  $\overline{U}$ , with the distance to 258

interface for an interface velocity of  $V_{sl}$  of  $3 \ \mu m \cdot s^{-1}$ . We define the distance to interface as  $0 \ \mu m$  when the front edge of the droplet comes in contact with the absolute detected position of the ice-water interface.



Figure 5: Droplet dynamics in presence of 0.01, 0.1, and 1wt.% solute in solution, deduced from the droplet trajectories at  $V_{sl} = 3 \ \mu m \cdot s^{-1}$ . Mean droplet velocity versus distance to interface for (A)  $R_1 = 7.2 \pm 0.4 \ \mu m$ and (B)  $R_2 = 30.9 \pm 1.2 \ \mu m$ . The droplets accelerate as the solidification front approaches, and decelerate as they are engulfed into the ice. © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

At large distances from the interface, larger than 100  $\mu m$  the droplets in 262 water are unperturbed and their mean velocity  $\overline{U}$  in the sample frame is zero. 263 As they get closer to the interface, they start getting repelled. The mean droplet 264 velocity  $(\overline{U})$  increases and exhibits a maximum  $(U_{max})$ , when the leading edge 265 of the droplets coincides with the initial position of the growing crystal. We note 266 that the droplet velocity  $\overline{U}$  is lower than  $V_{sl}$ , which means that the droplets are 267 finally captured in ice after a typical time, called interaction time (defined in 268 Fig. S1), which is discussed later. As the droplets are captured in ice, their 269 velocity  $\overline{U}$  returns to zero. As shown in Fig.5,  $\overline{U}$  decreases for a larger droplet 270 size, while it increases with an increasing surfactant concentration. 271

In Fig.6, we report the evolution of the maximum velocity  $U_{max}$  with the surfactant concentration, the droplet size, and the solid liquid interface velocity  $V_{sl}$ . Similar to  $\overline{U}$ , we observe an increase of  $U_{max}$  with an increasing surfactant concentration and that the larger  $R_2$  droplets get pushed away from the growing solid at lower velocities as compared to the smaller  $R_1$  droplets. Furthermore,





Figure 6: Maximum mean droplet velocity  $(U_{max})$  when the droplet front edge coincides with the ice-water interface (distance to interface = 0  $\mu$ m) for (A)  $R_1 = 7.2 \pm 0.4 \ \mu$ m and (B)  $R_2 = 30.9 \pm 1.2 \ \mu$ m. In general, the magnitude of  $U_{max}$  is greater for higher surfactant concentrations and smaller droplet sizes. An increasing growth rate  $V_{sl}$  as well as droplet radius promote a smaller magnitude of  $U_{max}$ . The dotted lines are for visualization and do no represent an extrapolation of the results denoted by the circular markers. © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.



Figure 7: Characteristic length scale  $L_v$  in the plane of Solute Concentration (*wt.*%) versus Solidification Velocity ( $V_{sl}$ ). Contour plots denoting the magnitude of  $L_v$  for (A)  $R_1 = 7.2 \pm 0.4 \ \mu m$  and (B)  $R_2 = 30.9 \pm 1.2 \ \mu m$ . Each contour line denotes a constant magnitude of  $L_v$  equivalent to the value shown on the calibration bar. The distance  $L_v$ , where droplets in water start getting repelled by the interface, increases significantly with the solute concentration, while it decreases with an increasing growth rate. © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

From the evolution of  $\overline{U}$  with the distance to the interface, we define a char-278 acteristic length scale,  $L_v$ , corresponding to the distance at which the droplets 279 attain a mean velocity  $(\overline{U})$  of  $0.1 \ \mu m \cdot s^{-1}$ , which is shown in Fig.7. This distance 280 corresponds to the range of interaction between the droplets and the interface. 281 We find that the droplets get repelled over distances ranging between 10 and 282 100  $\mu m$ , often larger than their diameter, especially for the largest surfactant 283 concentrations. Smaller droplets with radius  $R_1$  are repealed at greater distances 284 from the interface as compared to the larger  $R_2$  droplets. Increasing the growth 285 rate decreases the characteristic distance  $L_{v}$ . 286

We also depict in Fig.8 the interaction time  $\tau$  (defined in SI), which repre-287 sents the time during which the velocity of the droplets is different from zero 288 before and after crossing the interface. In general, we notice that the interaction 289 time diminishes with an increasing solidification velocity  $(V_{sl})$  and reduces to 290 zero at higher growth rates  $(V_{sl} \ge 5 \ \mu m \cdot s^{-1})$ , independent of the surfactant 291 concentration. An interaction time of  $0 \ s$  implies that the droplets get engulfed 292 into the ice instantaneously and hence, are not repelled by the advancing solid-293 liquid interface. In contrast, the interaction time increases strongly with the 294 surfactant concentration at relatively lower growth rates  $(V_{sl} \leq 3 \ \mu m \cdot s^{-1})$ . 295

In Fig.9 we present the droplet displacement  $\delta$  due to their repulsion by the front (defined in Fig. S1), which represents the distance moved by the droplets during the interaction time. We again observe that increasing the surfactant concentration leads to higher displacements while increasing the growth rate leads to a lower displacement.

The results described so far emphasize that an increasing amount of surfactant induces a repulsion of the droplets by the interface over large distances, of the order ten to a hundred of microns away from the interface and that the droplet dynamics is influenced by the bulk surfactant concentration, the growth rate and the droplet size. These three parameters control the local gradient of surfactant concentration close to the solidification front. Indeed the surfactant concentration close to the solid-liquid interface is higher as compared to the



Figure 8: Interaction time for oil droplets dispersed in water at three distinct solute concentrations. Plot of characteristic interaction time for (A)  $R_1 = 7.2 \pm 0.4 \ \mu m$  and (B)  $R_2 = 30.9 \pm 1.2 \ \mu m$ . Droplets tend to interact or feel the presence of an approaching ice-water interface during 10 to 100 s at high solute concentrations ( $\geq 0.1 \ wt.\%$ ) and low growth rates ( $\leq 5 \ \mu m \cdot s^{-1}$ ). The dotted lines are for visualization and do no represent an extrapolation of the results denoted by the circular markers. <sup>©</sup> (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

<sup>308</sup> bulk concentration far from the interface because of its low solubility in ice.
<sup>309</sup> For *steady-state* planar growth, the concentration field of rejected solutes in the
<sup>310</sup> remaining liquid writes

$$C_L = C_0 + C_0 \left(\frac{1 - K_0}{K_0}\right) exp\left[\frac{-V_{sl}}{D}|x|\right]$$
(1)

where  $C_L$  is the solute concentration at a distance x from the interface,  $C_0$ is the bulk solute concentration in the liquid far from the interface, D is the solute diffusion coefficient and  $K_0$ , the partition coefficient defined as the ratio of surfactant concentration in the solid phase to the one in the liquid [36].

In a previous article [19], we suggested that the displacement of the droplets is caused by surfactant concentration gradients close to the ice-water interface, possibly through a phenomenon called diffusiophoresis [37]. Diffusiophoresis is provoked by solute concentration gradients and can lead to displacement of



Figure 9: Displacement of oil droplets dispersed in water at three distinct solute concentrations, while interacting with the ice-water interface. Plot of droplet displacement for (A)  $R_1 = 7.2 \pm 0.4 \ \mu m$  and (B)  $R_2 = 30.9 \pm 1.2 \ \mu m$ . The interaction of droplets with an advancing ice-water interface can displace them by increasing distances ( $\geq 10 \ \mu m$ ) owing to a high amount of surfactant ( $\geq 0.1 \ wt.\%$ ) in the bulk solution. The dotted lines are for visualization and do no represent an extrapolation of the results denoted by the circular markers.  $^{\odot}$  (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

micrometric particles with velocities of the order of a few micron per second, 319 comparable to the droplet velocities that we measure in our study. From Eq. (1), 320 it is expected that the local gradient of surfactant concentration spans over a 321 typical distance  $L_d = D/V_{sl}$  [36]. Hence an increasing growth rate  $(V_{sl})$  will de-322 crease the distance at which the solute field can be perceived by the droplets and 323 can qualitatively account for the decreasing values of  $L_v$  measured (see Fig.7) 324 at high growth rates  $(V_{sl} \ge 5 \ \mu m \cdot s^{-1})$ . Moreover the concentration gradient 325  $C_L - C_0$  depends linearly on  $C_0$  which can possibly account for the strong influ-326 ence of the surfactant concentration on the droplet displacement. We note that 327 diffusiophoretic displacements of particles have been studied theoretically and 328 experimentally for simple solutes such as ionic salts, dissolved gas or charged 329 surfactants such as Sodium dodecylSulfate [37-40] but was never reported for 330 non-ionic species. 331



To further study the influence of the surfactant concentration gradients on



Figure 10: Solute rejected by the growing solid phase and segregated at the solid-liquid interface during steady-state directional solidification. (A) Model sketch depicting the concentration profile evolution of a solute (in magenta) in the remaining liquid, rejected by a solidification front advancing at  $V_{sl}$ , during steady-state planar growth. (B) Mean fluorescence intensity (magenta) of SRhB, acquired using a confocal microscope, is fit with a theoretical diffusion-type exponential (black line). The predicted steady-state diffusion of SRhB (green line), using the model from Tiller et al. [36], corresponds closely to the experimental data fit. A steady-state planar growth is thus verified. The corresponding steady-state diffusion profile of Tween 80 micelles (blue) shows a significant difference in length scales over which the two molecules (SRhB and Tween 80) diffuse. All data presented was recorded for a growth rate of 3  $\mu m \cdot s^{-1}$ . © (2020) S. Tyagi et al. (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

the droplet dynamics, it would be useful to measure in situ the surfactant 333 concentration close to the front. However Tween 80 does not fluoresce, hence 334 we cannot measure its concentration profile. However it is in principle possible 335 to predict it from Equation 1 provided a steady state regime is reached in our 336 experiments. Therefore we examine the validity of Equation 1 by recording the 337 fluorescence intensity of the dye, SRhB, which can be obtained easily with the 338 confocal microscope (see Fig. 10A). The concentration profile of SRhB rejected 339 by the ice-water interface, deduced from the fluorescence intensity profile for a 340 growth rate of 3  $\mu m \cdot s^{-1}$  is given in Fig.10B. At 3  $\mu m \cdot s^{-1}$ , the concentration 341 profile obtained is in agreement with the *steady-state* diffusion profile predicted 342

from Eq.1 (see Fig.10B). However we note that the *steady-state* approximation is not valid at higher velocities (not shown) probably because constitutional undercooling modifies the local temperature of the front hence the diffusion coefficient of the dye.

Interestingly, we see from Fig.10B which is obtained for a velocity of 3  $\mu m$ . 347  $s^{-1}$ , that the distance at which the dye concentration profile starts increasing is 348 of the order of 150  $\mu m$ . This value is much higher than the typical distance  $L_v$ 349 over which both the large and small droplets get repelled from the interface at 350 the same velocity, ranging between 40 and 80  $\mu m$  depending on the surfactant 351 concentration and the droplet size. As the surfactant monomers and the dye 352 have the same diffusion coefficient, we would expect that the distance  $L_d$  is 353 similar for both species. 354

To account for the discrepancy between the measured values of  $L_v$  and the 355 theoretical  $L_d = D/V_{sl}$ , one may suggest that the droplet dynamics may be 356 controlled by the concentration gradient of surfactant micelles, which diffusion 357 coefficient is lower than that of the monomers and for which we expect a lower 358 value of  $L_d$ . Using DLS, we measured the diffusion coefficient of the micelles 359 and calculated the corresponding concentration profile using Eq.1. As shown 360 in Fig.10B, at a growth rate of 3  $\mu m \cdot s^{-1}$ , we obtain a typical distance  $L_d$  of 361 10  $\mu m$ , which is lower than the distance  $L_v$  measured experimentally at this 362 growth rate. Hence it turns out that the experimentally measured value of  $L_v$ 363 ranges between the  $L_d$  values calculated either for the surfactant micelles or for 364 the monomers. However we note that the monomer and micelle concentration 365 profiles close to ice-water front depends on the exchange dynamics between the 366 surfactants and the micelles, hence may not be at equilibrium. 367

#### <sup>368</sup> 3.2 Droplets at the interface

We now focus on the behaviour of droplets when they come in contact (distance to interface = 0  $\mu m$ ) with the solid-liquid interface. We observe three typical behaviours of oil droplets as they encounter an approaching front, as shown



Figure 11: Typical time-lapse montage depicting the three types of deformation behaviour of oil droplets while undergoing directional planar front solidification. (A) The droplets elongate at the ice-water interface and remain deformed in the ice phase, scale bar =  $50 \ \mu m$  (B) The droplets deform in a transient manner ( $t = 13 \ s$ ) at the ice-water interface and recover their shape as they are captured by the growing ice phase, scale bar =  $10 \ \mu m$  (C) The droplets do not undergo deformation and preserve their shape during their interaction and further engulfment in the growing crystal. Scale bar =  $50 \ \mu m$ . Oil is in cyan, water is in colormap viridis (fluorescence bar), and ice is in black. © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

- in Fig.11. The droplets can elongate permanently as they get engulfed in the 372 growing ice (Fig.11A), the droplets may deform transiently  $(t = 13 \ s)$  at the 373 ice-water interface and subsequently relax to their original spherical shape as 374 they move further into the ice phase (Fig.11B), or the droplets remain mostly 375 spherical during their engulfment by the growing crystal (Fig.11C). We notice 376 that the deformation behaviour depends on the droplet size R, the imposed 377 growth rate  $V_{sl}$ , and the bulk surfactant concentration. Therefore, we need to 378 systematically study the effect of these solidification parameters to understand 379 the different types of deformation observed. 380
- The droplet deformation is estimated from the analysis of 2D shape elongation, as shown in the schematic in Fig.11A, taking the ratio of droplet diameters along  $\vec{x}$  and  $\vec{y}$ . In Fig.12, we depict the mean elongation profiles calculated for 50 to 400 (depending on R and  $V_{sl}$ ) droplet interactions in 0.01 wt.% and 1 wt.%



solute solution at varying growth rates for two different droplet sizes  $(R_1, R_2)$ .

Figure 12: Mean elongation profiles for oil droplets encountering an approaching ice-water interface. Planar solidification front induced permanent deformation of oil droplets dispersed in a solution with (A,B) 0.01 wt.% solute concentration having a size of (A)  $R_1 = 7.2 \pm 0.4 \ \mu m$  (B)  $R_2 = 30.9 \pm 1.2 \ \mu m$ . The transient and no deformation regimes for droplets in (C,D) 1 wt.% solute concentration having a size of (C)  $R_1 = 7.2 \pm 0.4 \ \mu m$  (D)  $R_2 = 30.9 \pm 1.2 \ \mu m$ .  $^{\odot}$  (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

We observe from Fig.12A and Fig.12B that the droplets undergo permanent 386 elongation for the two droplet sizes  $(R_1, R_2)$ , when the bulk surfactant concen-387 tration is 0.01 wt.%. The elongation is  $\approx 1.0$ , representing a circle, when the 388 droplets are in the remaining liquid far from the interface. The droplets start 389 getting elongated as their front edge touches the interface (distance = 0  $\mu m$ ) 390 and their shape transforms into an ellipse (elongation > 1.0). The droplet de-301 formation evolves further and reaches a constant magnitude when the front edge 392 is located at a distance of  $2R \times Elongation$ . Once the droplets are completely 393 engulfed in the ice, their shape does not evolve any more (Fig.12A,B). Interest-394 ingly, we notice that the elongation reduces with an increasing growth rate for 395

<sup>396</sup> both the droplet sizes investigated. However, the maximum elongation for the <sup>397</sup> smaller  $R_1$  droplets is lower as compared to the larger  $R_2$  droplets at the given <sup>398</sup> 0.01 wt.% solute concentration.

In Fig.12C, we report the transient deformation of the oil droplets as they 399 confront the ice-water interface with 1 wt.% bulk solute concentration. Here, 400 the oil droplets undergo elongation at the interface (distance =  $0 \ \mu m$ ) but even-401 tually recover their shape as they are completely engulfed in the ice. In contrast, 402 from Fig.12D we notice that the larger  $R_2$  droplets do not undergo any type 403 of deformation at the same solute concentration of 1 wt.%. Hence, the elon-404 gation profile of  $R_2$  droplets remains unmodified during the droplet-interface 405 confrontation. 406

We deduce from these observations that the droplets confronting an approaching interface have distinct behaviours depending on the concentration of solute in the bulk solution. In particular, an increasing solute concentration tends to decrease the droplet elongation significantly.

Several experimental and theoretical studies devoted to the shape of bubbles 411 during solidification in the absence of surfactant can be found in the literature 412 [41–43]. Highly elongated bubbles along with the formation of a highly curved 413 tip at the bubble-ice interface were observed [41, 42] and are controlled by 414 the contact angle between the bubbles and the ice-water interface [43]. In 415 the case of the low surfactant concentrations, we see from Fig.11A that the 416 contact angle between the droplets and the ice-water interface remains close to 417 90° during engulfment, similarly to bubbles, because of the weak thermal flux 418 in the droplets owed to their low thermal conductivity in comparison to water 419 [44]. This results in tear-shaped drops which are very similar to those reported 420 in the literature for bubbles. 421

At higher surfactant concentration we observe much lower elongations. According to Eq.1, an increasing bulk solute concentration  $(C_0)$  implies a higher concentration of the solute segregated  $(C_0/K_0)$  at the solid-liquid interface. The segregation of solute is further enhanced owing to an obstruction of their diffu-

sion field by the droplets in the vicinity of the solid-liquid interface [13, 45]. The 426 segregated solute, trapped in the layer between the droplet and the interface, 427 induces solute premelting [46, 47] (Fig.4B at  $t = 44 \ s$ , Fig.11B at  $t = 8 \ s$ , in 428 Fig.11C at t = 3 s) which in turn causes a lowering of the equilibrium melt-429 ing temperature of water. Therefore these premelted films are stable below the 430 solid's bulk melting temperature,  $T_m$  and the thickness of the premelted films 431 increases with the solute concentration [18, 46]. As a premelting film interca-432 lates between the droplets and the solid liquid interface, the situation is very 433 different from the literature studies discussed above as no finite contact angle 434 between the drops and the interface can be defined. Here we suggest that the 435 liquid-liquid interfacial tension between the droplet and the premelting film fa-436 vors spherical shapes to minimize the interfacial area. Interestingly we note that 437 the effect of size is different at low and high surfactant concentrations. At low 438 surfactant concentrations, smaller droplets undergo a lower deformation, prob-439 ably because of a higher capillary pressure inside the drops that opposes the 440 deformation. At opposite, for large surfactant concentrations, smaller droplets 441 present a transient deformation, while larger droplets remain mostly spheri-442 cal. This effect may be linked to the stronger segregation of solute in the films 443 between the droplets and the ice in the case of larger films. 444

#### 445 3.3 Droplets in Ice

We have discussed so far the dynamics and consequences of oil droplets interacting with an approaching ice-water interface. In the last section, we investigate the fate of droplets after their engulfment by the ice front.

At 1 wt.% solute in the aqueous solution, at a growth rate of 1  $\mu m \cdot s^{-1}$ , the droplets undergo an elongation process after engulfment whereby the two radii, along  $\vec{x}$  and  $\vec{y}$ , are stretched in magnitude as the droplets progress further in ice. This means that the droplets flatten in the z direction as they are engulfed in the ice. We depict this phenomenon with a time-lapse montage, highlighting the deformation, in Fig.13. Interestingly, we observe this phenomenon only at



Figure 13: Crushing of oil droplets during their engulfment in ice at a growth rate of  $V_{sl} = 1 \ \mu m \cdot s^{-1}$  with  $1 \ wt\%$  solute in solution.  $R_2 = 30.9 \pm 1.2 \ \mu m$ . Typical time-lapse montage depicting the crushing of an oil droplet, scale bar = 50  $\mu m$ . The dashed circle indicate the shape of the droplet before encapsulation. Note that in the crushing regime, the droplets are elongated in a direction parallel to the front, unlike in the other regimes (elongation perpendicular to the front). © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.

a growth rate of  $1 \ \mu m \cdot s^{-1}$  in the presence of  $1 \ wt.\%$  bulk solute concentration for both droplets radii R1 and R2.

We currently have no definitive explanations for this behavior. One possibility could be that the shape of the water/ice meniscus in these conditions (curved meniscus) may favor entrapment and flattening of the droplets between the ice and the glass surface. However, this particular point would deserve additional experiments, in particular in 3D, which are beyond the scope of the current study.

Furthermore we note that once the droplets are trapped in the ice, we do 463 not observe any thermal regelation, i.e the droplets do not manifest any motion 464 relative to the ice. Moreover the liquid layer between the droplet from the 465 growing solid decreases in thickness as the droplets move along the temperature 466 gradient in ice towards an increasing undercooling  $(\Delta T = T_m - T)$ , where T is 467 the temperature of the substrate) [1]. The study of particle migration in ice is an 468 important topic of research to understand frost heave, glacier motion, and ice-469 core dating among other technological applications [1]. Recent studies suggest 470 that the presence of impurities or solutes tend to accelerate the *regelation* of 471 trapped particles in ice. Typical migration velocities of  $0.1 \ \mu m \cdot s^{-1}$  at  $\Delta T$  of  $1 \ K$ 472 have been reported for micron sized particles in the presence of impurities [48]. 473 Another recent study highlights the major impact of impurities on the rapid 474 displacement (0.5 cm) over small time scales (120 s) of 1  $\mu m$  silicon particles 475 trapped in ice [49]. The objects investigated here are 1 order of magnitude (or 476 more) larger, which could explain why no regelation was observed. The use of 477 cryo-confocal microscopy with the ability to image the solute segregation has 478 a promising prospect for investigating such mechanisms. We believe the high 479 space and temporal resolution can be used effectively to resolve the dynamics 480 of individual colloidal particles to gain further insight into regelation. 481

## 482 4 Conclusions

In the first section, we have investigated the role of solutes on the dynamics of 483 freezing oil droplets using in situ cryo-confocal microscopy. We have reported 484 on the significant magnitude of droplet-front interaction time and the resulting 485 droplet displacement owing to the solute effects. We believe this can be an 486 important criterion for controlling the spatial distribution of objects, especially 487 in multiple object scenarios. The control of the material microstructure has 488 been a topic of interest in alloy solidification (especially in particle-reinforcedcomposites) and for impurity control in castings and single crystal growth. The 490 object dynamics and impact of solute (or impurity) are still complex to quantify 491 as the observation of solidification in situ remains challenging. We have tried 492 to advance towards an *in situ* quantification of the solute mechanisms at play 493 and further work is required to correlate the dye fluorescence intensity to the 494 absolute solute concentration gradient. The latter can be useful in predicting 495 thermal convection and non *steady-state* solidification regimes. 496

In the second section, we have shown that the deformation of droplets at 497 the ice-water interface depends strongly on the growth rate  $(V_{sl})$  and the cor-498 responding bulk solute concentration  $(C_0)$ . Furthermore, the addition of solute 499 increases the thickness of the observable premelted films, which appears to act 500 as a protection mechanism against the interface initiated droplet deformation. 501 The local solute environment and deformation are two important criterion for 502 cryopreservation in particular. In cryobiology, the excess of solute causes severe 503 osmotic stresses that can instigate cell membrane rupture and hence, cryoinjury 504 to cells and tissues [4, 12]. In food engineering, alterations to the continuous 505 phase concentration or to the shape and size of dispersed droplets is detrimen-506 tal to the freeze-thaw stability of consumable emulsions [8]. Hence, a complete 507 understanding of the solute redistribution mechanisms along with the associ-508 ated object deformation at the corresponding freezing conditions is desired. 509 Our multi-dimensional approach highlights the importance of different solidifi-510

cation parameters and the ubiquitous role of solute in dominating the various
aspects of object deformation behaviour. Further work is required to accurately
estimate the direction and magnitude of forces at the origin of the observed
deformation.

In conclusion, we report that the oil droplets undergoing directional solidifi-515 cation feel the impact of solute at every stage, from being in the liquid phase to 516 getting captured by the growing ice-water interface. The solute plays an impor-517 tant role in determining the droplet shape (deformed or not), droplet behaviour 518 (engulfment or rejection), and eventually the droplet spatial distribution. To 519 predict the solidified microstructure, an understanding of the several in-situ 520 mechanisms at play is therefore indispensable. The use of rapid cryo-confocal 521 microscopy facilitates an in situ investigation and quantification of solidifica-522 tion mechanisms with visualization of the local solute segregation. To represent 523 the observations in real-life systems, we need to explore models incorporating 524 interaction dynamics and object behaviour with solute effects. Current theories 525 do not encompass all the factors required for explaining the long-range solute 526 effects on the objects during solidification. We hope our experimental data can 527 serve to improve the existing theoretical models. Finally, we suggest that the 528 freezing of oil-in-water emulsions may serve as an analogue for studying the in 529 situ interaction of foreign objects with an advancing solid-liquid interface in the 530 presence of solute effects. 531

## 532 Acknowledgements

The research leading to these results has received funding from the ANRT and Saint-Gobain through a CIFRE fellowship ( $N^{\circ} 2017/0774$ ). We would like to thank Alban Sauret and Virgile Thievenaz for discussing the deformation of droplets.

## 537 Author contributions

S.D. and C.M. designed and supervised the project, S.D, C.M. and S.T. designed
the experiments, S.T. carried out the confocal microscopy, S.T., C.M. and S.D.
analyzed the data. All authors discussed the results and implications and wrote
the manuscript.

## 542 Corresponding Authors

543 Correspondence should be sent to Cécile Monteux (Cecile.Monteux@espci.fr)

<sup>544</sup> and Sylvain Deville (sylvain.deville@univ-lyon1.fr)

## 545 Conflict of interest

546 The authors declare no conflict of interest.

## 547 Availability of materials and data

The datasets generated during and/or analysed during the current study are available from the corresponding author on reasonable request.

## 550 References

- <sup>551</sup> [1] J. G. Dash, A. W. Rempel, and J. S. Wettlaufer. The physics of pre-
- melted ice and its geophysical consequences. *Reviews of Modern Physics*,
   78(3):695–741, 2006.
- [2] M Shafiur Rahman. Handbook of food preservation. CRC press, 2007.
- <sup>555</sup> [3] VL Bronstein, YA Itkin, and GS Ishkov. Rejection and capture of cells
   <sup>556</sup> by ice crystals on freezing aqueous solutions. *Journal of Crystal Growth*,
   <sup>557</sup> 52:345–349, 1981.

- [4] C Körber. Phenomena at the advancing ice-liquid interface: solutes, parti-
- cles and biological cells. *Quarterly reviews of biophysics*, 21:229–298, 1988.
- Lifeng Zhang. Nucleation, growth, transport, and entrapment of inclusions
   during steel casting. Jom, 65(9):1138–1144, 2013.
- <sup>562</sup> [6] H Li, EA Ghezal, A Nehari, G Alombert-Goget, A Brenier, and K Lebbou.
   <sup>563</sup> Bubbles defects distribution in sapphire bulk crystals grown by czochralski
   <sup>564</sup> technique. *Optical Materials*, 35(5):1071–1076, 2013.
- <sup>565</sup> [7] Sylvain Deville. Freeze-casting of porous ceramics: a review of current
   <sup>566</sup> achievements and issues. Advanced Engineering Materials, 10(3):155–169,
   <sup>567</sup> 2008.
- [8] Supratim Ghosh and John N Coupland. Factors affecting the freeze-thaw
   stability of emulsions. *Food Hydrocolloids*, 22(1):105–111, 2008.
- [9] OM Bunoiu, Th Duffar, and I Nicoara. Gas bubbles in shaped sapphire.
   Progress in crystal growth and characterization of materials, 56(3-4):123–145, 2010.
- <sup>573</sup> [10] D. Shangguan, S. Ahuja, and D. M. Stefanescu. An analytical model for
  <sup>574</sup> the interaction between an insoluble particle and an advancing solid/liquid
  <sup>575</sup> interface. *Metallurgical Transactions A*, 23(2):669–680, 1992.
- [11] R. Asthana and S. N. Tewari. The engulfment of foreign particles by a
  freezing interface. *Journal of Materials Science*, 28(20):5414–5425, 1993.
- [12] Gregory M. Fahy. The relevance of cryoprotectant "toxicity" to cryobiology.
   *Cryobiology*, 23(1):1–13, 1986.
- J. K. Kim and P. K. Rohatgi. The effect of the diffusion of solute between
   the particle and the interface on the particle pushing phenomena. Acta
   Materialia, 46(4):1115–1123, 1998.

- <sup>583</sup> [14] Adrian V. Catalina, Subhayu Sen, Doru M. Stefanescu, and William F.
- Kaukler. Interaction of porosity with a planar solid/liquid interface. Met allurgical and Materials Transactions A, 35(5):1525–1538, 2004.
- [15] Sidhanth Tyagi, Hélène Huynh, Cécile Monteux, and Sylvain Deville. Objects interacting with solidification fronts: Thermal and solute effects. Materialia, 12(April):100802, 2020.
- <sup>589</sup> [16] Justin C. T. Kao and Alexander A. Golovin. Particle capture in binary
   <sup>590</sup> solidification. Journal of Fluid Mechanics, 625(September 2008):299, 2009.
- [17] Yi Yang, JW Garvin, and HS Udaykumar. Sharp interface numerical simulation of directional solidification of binary alloy in the presence of a ceramic
   particle. International journal of heat and mass transfer, 51(1-2):155–168,
   2008.
- <sup>595</sup> [18] JS Wettlaufer and M Grae Worster. Premelting dynamics. Annu. Rev.
   <sup>596</sup> Fluid Mech., 38:427–452, 2006.
- [19] Dmytro Dedovets, Cécile Monteux, and Sylvain Deville. Five-dimensional
   imaging of freezing emulsions with solute effects. *Science*, 360(6386):303–
   306, 2018.
- [20] J. A. Sekhar and R. Trivedi. Solidification microstructure evolution in the
   presence of inert particles. *Materials Science and Engineering A*, 147(1):9–
   21, 1991.
- <sup>603</sup> [21] Jürgen Pötschke and Volker Rogge. On the behaviour of foreign particles at
  <sup>604</sup> an advancing solid-liquid interface. Journal of Crystal Growth, 94(3):726–
  <sup>605</sup> 738, 1989.
- [22] A. W. Rempel and M. G. Worster. Interaction between a particle and an
  advancing solidification front. *Journal of Crystal Growth*, 205(3):427–440,
  1999.

- [23] A. W. Rempel and M. G. Worster. Particle trapping at an advancing
   solidification front with interfacial-curvature effects. *Journal of Crystal Growth*, 223(3):420-432, 2001.
- [24] Min S. Park, Alexander A. Golovin, and Stephen H. Davis. The encapsulation of particles and bubbles by an advancing solidification front. *Journal*of Fluid Mechanics, 560:415–436, 2006.
- [25] P. S. Wei and S.Y. Y. Hsiao. Pore shape development from a bubble captured by a solidification front. Int. J. Heat Mass Transf., 55(25-26):8129–8138, dec 2012.
- [26] E. A. Ghezal, H. Li, A. Nehari, G. Alombert-Goget, A. Brenier, K. Lebbou, M. F. Joubert, and M. T. Soltani. Effect of pulling rate on bubbles
  distribution in sapphire crystals grown by the micropulling down (μ-PD)
  technique. Crystal Growth and Design, 12(8):4098–4103, 2012.
- [27] H. Jamgotchian, R. Trivedi, and B. Billia. Interface dynamics and coupled growth in directional solidification in presence of bubbles. *Journal of Crystal Growth*, 134(3-4):181–195, 1993.
- [28] S. Sen, W. F. Kaukler, P. Curreri, and D. M. Stefanescu. Dynamics of
  solid/liquid interface shape evolution near an insoluble particle An X-ray
  transmission microscopy investigation. *Metallurgical and Materials Trans- actions A: Physical Metallurgy and Materials Science*, 28(10):2129–2135,
  1997.
- [29] F López Arbeloa, P Ruiz Ojeda, and I López Arbeloa. Flourescence selfquenching of the molecular forms of rhodamine b in aqueous and ethanolic
  solutions. Journal of luminescence, 44(1-2):105–112, 1989.
- [30] Rex Malcolm Chaplin Dawson, Daphne C Elliott, William H Elliott, and
  Kenneth M Jones. *Data for biochemical research*, volume 3. Clarendon
  Press, 2002.

- [31] Eleanor LV Harris, S Angal, and Simon Roe. Protein purification applica-
- tions: a practical approach, volume 71. IRL press Oxford, 1990.
- [32] Alan D McNaught, Andrew Wilkinson, et al. Compendium of chemical
   terminology, volume 1669. Blackwell Science Oxford, 1997.
- [33] Johannes Schindelin, Ignacio Arganda-Carreras, Erwin Frise, Verena
  Kaynig, Mark Longair, Tobias Pietzsch, Stephan Preibisch, Curtis Rueden,
  Stephan Saalfeld, Benjamin Schmid, et al. Fiji: an open-source platform
  for biological-image analysis. *Nature methods*, 9(7):676, 2012.
- [34] Stéfan van der Walt, Johannes L. Schönberger, Juan Nunez-Iglesias,
  François Boulogne, Joshua D. Warner, Neil Yager, Emmanuelle Gouillart,
  Tony Yu, and the scikit-image contributors. scikit-image: image processing
  in Python. *PeerJ*, 2:e453, 6 2014.
- [35] Dmytro Dedovets, Cécile Monteux, and Sylvain Deville. A temperature controlled stage for laser scanning confocal microscopy and case studies in
   materials science. Ultramicroscopy, 195(August):1–11, 2018.
- [36] W. A. Tiller, K. A. Jackson, J. W. Rutter, and B. Chalmers. The redistribution of solute atoms during the solidification of metals. *Acta Metallurgica*,
  1(4):428–437, 1953.
- <sup>654</sup> [37] JL Anderson, ME Lowell, and DC Prieve. Motion of a particle generated by
   <sup>655</sup> chemical gradients. part 1. non-electrolytes. J. Fluid Mech, 117(1):107–121,
   <sup>656</sup> 1982.
- [38] Rodrigo Nery-Azevedo, Anirudha Banerjee, and Todd M Squires. Diffusio phoresis in ionic surfactant gradients. *Langmuir*, 33(38):9694–9702, 2017.
- [39] Trevor J Shimokusu, Vanessa G Maybruck, Jesse T Ault, and Sang woo Shin. Colloid separation by co2-induced diffusiophoresis. *Langmuir*,
   36(25):7032-7038, 2019.

- [40] Suin Shim and Howard A Stone. Co2-leakage-driven diffusiophoresis causes
- spontaneous accumulation of charged materials in channel flow. *Proceedings* of the National Academy of Sciences, 117(42):25985–25990, 2020.
- [41] P. S. Wei, C.C. Huang, Z.P. Wang, K.Y. Chen, and C.H. Lin. Growths
  of bubble/pore sizes in solid during solidification—an in situ measurement
  and analysis. J. Cryst. Growth, 270(3-4):662–673, 2004.
- [42] Norizaku Maeno. Air bubble formation in ice crystals. *Phys. Snow Ice Proc.*, 1(1):207–2181, 1967.
- <sup>670</sup> [43] P. S. Wei and C.Y Ho. An Analytical Self-Consistent Determination of a
  <sup>671</sup> Bubble with a Deformed Cap Trapped in Solid during Solidification. *Metall.*<sup>672</sup> *Mater. Trans. B*, 33(February):91–100, 2002.
- [44] AA Chernov, DE Temkin, and AM Mel'Nikova. The influence of the thermal conductivity of a macroparticle on its capture by a crystal growing
  from a melt. Sov. Phys. Crystallogr, 22(6):656–658, 1977.
- [45] R. Sasikumar and T. R. Ramamohan. Distortion of the temperature and
  solute concentration fields due to the presence of particles at the solidification front-effects on particle pushing. Acta Metallurgica Et Materialia,
  39(4):517–522, 1991.
- [46] J. Wettlaufer. Impurity Effects in the Premelting of Ice. *Physical Review Letters*, 82(12):2516-2519, 1999.
- [47] A. W. Rempel, J. S. Wettlaufer, and M. G. Worster. Interfacial Premelt ing and the Thermomolecular Force: Thermodynamic Buoyancy. *Physical Review Letters*, 87(8):088501, 2001.
- [48] Julia Schollick. Real space study of pattern formation in freezing colloidal
   suspensions. PhD thesis, University of Oxford, 2012.
- [49] Navaneeth K. Marath and J. S. Wettlaufer. Impurity effects in thermal
   regelation. Soft Matter, 16(25):5886–5891, 2020.

# **<sup>609</sup>** 5 Supplementary Information



Figure S1: Measurement of interaction time and apparent droplet velocity U' in the observation frame. In the observation frame, far from the solid-liquid interface in water the droplet moves at the imposed growth rate  $U' = V_{sl}$ , as the droplet approaches the interface it gets repelled  $U' \neq V_{sl}$ , and as the droplet is engulfed in the ice it doesn't get repelled anymore, thereby recovering  $U' = V_{sl}$ . The interaction time is the total duration over which a droplet gets repelled by the solidification interface. Relative time is zero when the front edge of the droplet hits the solidification front. Experimental conditions for which the curve was recorded:  $V_{sl} = 3 \ \mu m \cdot s^{-1}$ ,  $G = \nabla T = 10^4 \ K \cdot m^{-1}$ , Droplet size  $R_1 = 7.2 \pm 0.4 \ \mu m$ . © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.



Figure S2: Deducing the isolated droplet velocity  $U_r$  and the mean droplet velocity  $\overline{U}$  in the sample frame. In the sample frame, the isolated droplet velocity  $U_r$  is zero far from the interface, it increases and reaches a maximum when the droplet gets repelled by the interface and subsequently, reduces to zero as the droplet is engulfed in the ice. Experimental conditions for which the curve was recorded:  $V_{sl} = 3 \ \mu m \cdot s^{-1}$ ,  $G = \nabla T = 10^4 \ K \cdot m^{-1}$ , Droplet size  $R_1 = 7.2 \pm 0.4 \ \mu m$ . © (2020) S. Tyagi *et al.* (10.6084/m9.figshare.14815083) CC BY 4.0 license https://creativecommons.org/licenses/by/4.0/.