

# Laboratory experiments on rain-driven convection: Implications for planetary dynamos

Peter Olson, Maylis Landeau, Benjamin H Hirsh

#### ▶ To cite this version:

Peter Olson, Maylis Landeau, Benjamin H Hirsh. Laboratory experiments on rain-driven convection: Implications for planetary dynamos. Earth and Planetary Science Letters, 2017, 457, pp.403-411. 10.1016/j.epsl.2016.10.015 . hal-03271246

## HAL Id: hal-03271246 https://hal.science/hal-03271246v1

Submitted on 25 Jun 2021

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés. 3

4

5

# Laboratory experiments on rain-driven convection: implications for planetary dynamos

Peter Olson<sup>\*</sup>, Maylis Landeau, & Benjamin H. Hirsh Department of Earth & Planetary Sciences Johns Hopkins University, Baltimore, MD 21218

#### August 22, 2016

#### Abstract

Compositional convection driven by precipitating solids or immiscible liquids has been 6 invoked as a dynamo mechanism in planets and satellites throughout the solar system, including Mercury, Ganymede, and the Earth. Here we report laboratory experiments 8 on turbulent rain-driven convection, analogs for the flows generated by precipitation 9 within planetary fluid interiors. We subject a two-layer fluid to a uniform intensity 10 rainfall, in which the rain is immiscible in the upper layer and miscible in the lower 11 layer. Rain falls through the upper layer and accumulates as a two-fluid emulsion in the 12 interfacial region between the layers. In experiments where the rain is denser than the 13 lower fluid, rain-injected vortices evolve into small-scale plumes that rapidly coalesce 14 into larger structures, resulting in turbulent convection throughout the lower layer. 15 The turbulent convective velocity in our experiments increases approximately as the 16 cube root of the rain buoyancy flux, implying little or no dependence on viscous and 17 chemical diffusivities. Applying diffusion-free scaling laws for magnetic field generation, 18 we find that precipitation-driven convection can be an effective dynamo mechanism in 19 planetary cores provided the precipitation buoyancy flux is large and the convecting 20 region is deep and nearly adiabatic. 21

<sup>22</sup> Key words: Rain-driven convection, planetary dynamos, iron snow, magnesium precip-

<sup>23</sup> itation, convection experiments, scaling laws

<sup>24</sup> \* Corresponding author: *olson@jhu.edu* 

### <sup>25</sup> 1 Introduction

Multi-phase flows involving liquids plus solids or several immiscible liquids have been pro-26 posed as power sources for a number of planetary dynamos, both large and small (Breuer 27 et al., 2015). Examples include iron-snow precipitation in the iron alloy cores of Mercury 28 (Villim et al., 2010; Dumberry and Roldovini, 2015) and Ganymede (Hauck et al., 2006; 29 Rückriemen et al., 2015; Christensen, 2015), in terrestrial exoplanets (Gaidos et al., 2010), 30 precipitation of low-density constituents near the top of Earth's iron-rich core for the early 31 geodynamo (Buffett et al., 2000; O'Rourke and Stevenson, 2016; Badro et al., 2016), and 32 helium rain in Saturn and other hydrogen-rich giant planets (Stevenson, 1980; Fortney and 33 Hubbard, 2004). 34

Although the compositions of both the precipitate and the core fluid, and the ways envisioned to generate fluid motions differ among the planets and satellites, the underlying mechanics are fundamentally similar in each case, as Figure 1 illustrates. First, cooling of the planet leads to saturation of one or more components of the conducting fluid. Nucleation of that component produces liquid drops or solid grains, which precipitate as the equivalents of rain, sleet, graupel, or snow.

In Mercury and Ganymede, the usual assumption is that dense iron-snow precipitates downward through the upper, cooler portions of their molten iron alloy cores (Dumberry and Roldovini, 2015; Christensen, 2015). Falling into the deeper and warmer portions of the core, the iron-snow melts, increasing the density and destabilizing the fluid there. The core then consists of a two-layer system, with a precipitation-dominated region overlying a convectiondominated region, shown in Figure 1a. More complex layering is possible, including staircase structures, particularly if the melting curve and the temperature profile are irregular (Vilim et al., 2010; Dumberry and Roldovini, 2015), or if double diffusive process occur. In general, however, it is usually concluded that the precipitating regions are stable and that dynamo action is concentrated in the convective region (Christensen and Wicht, 2008). The process is similar to convective turbulence in Earth's troposphere, when precipitation falling from clouds as virga snow sublimates before reaching the ground, cooling and destabilizing the air below the cloud base (Kudo, 2013).

A related but somewhat different precipitation scenario has been proposed for the Earth's 54 core in the deep past. Evidence for a geomagnetic field of similar strength as the present-55 day field extends to 3.4 Ga (Tarduno et al. 2010) and possibly 4.2 Ga (Tarduno et al., 56 2015), whereas current estimates place the age of the inner core at 1 Ga or less (Olson 57 et al., 2015), highlighting the need for geodynamo energy sources other than inner core 58 growth. It has been hypothesized that, as the core cooled from an initially high temperature 59 state, nucleation of weakly soluble magnesium-bearing grains or drops occurred (O'Rourke 60 and Stevenson, 2016; Badro et al., 2016). Positively buoyant in Earth's iron-rich core, the 61 magnesium-bearing compounds precipitated upward and accumulated at the core-mantle 62 boundary (CMB), as shown schematically in Figure 1b. Removal of magnesium left the 63 residual core fluid denser and therefore unstable, enabling a compositional convective region 64 to develop, thereby helping to maintain the early geodynamo. 65

Another example of precipitation-driven flow has been proposed for gas giant planets, Saturn in particular (Stevenson, 1980), but also giant exoplanets (Fortney and Hubbard, 2004). There, cooling produces supersaturated conditions for helium in the outer portion of the hydrogen-rich fluid envelope of the planet, a situation broadly similar to Figure 1a. It is hypothesized that helium rainfall stabilizes the density profile in a precipitation-dominated layer, allowing strong horizontal shear flows to develop. It has been shown that dynamo action driven by strong shear constrains the external magnetic field to be highly axisymmetric
(Stanley, 2010; Cao et al., 2012), as observed on Saturn (Cao et al., 2011).

Thermochemical evolution calculations reveal that the rate of gravitational potential 74 energy release in the saturation-precipitation process is proportional to the cooling rate of 75 the fluid (Rückriemen et al., 2015). For plausible planetary cooling rates, the precipitation 76 mechanisms described above are expected to release substantial amounts of gravitational 77 potential energy per unit time, and therefore hold potential for dynamo action. Yet, little 78 is known about the multi-phase flows involved in precipitation-driven convection, much less 79 their ability to produce efficient planetary dynamos. In particular, there are questions about 80 whether the potential energy released by precipitation converts efficiently to kinetic energy 81 of fluid motion, and whether the kinetic energy is produced at scales that are large enough 82 for dynamo action. 83

Precipitation may also play an important role during late-stage planetary accretion. It 84 has been hypothesized that late-stage giant impacts fragment core-forming metals in a deep 85 magma ocean (Tonks and Melosh, 1993; Nakajima and Stevenson, 2015) that might extend 86 to the core (Labrosse et al., 2007). For some impacts, complete fragmentation could produce 87 iron rainfall from the mantle directly into the core (Ichikawa et al., 2010; Deguen et al., 88 2014; Kraus et al., 2015). In this scenario, high-pressure, high-temperature metal-silicate 89 interactions predict that the metallic rain absorbs large concentrations of lighter elements 90 from the magma (Takafuji et al., 2005; Siebert et al., 2011) and would enter the core with a 91 large density deficit, rather than a density excess, possibly contributing to the stable layering 92 inferred at the top of the present-day outer core (Helffrich and Kaneshima, 2010; Landeau 93 et al., 2016). 94

In this study we investigate these issues using analog laboratory experiments of rain-95 driven convection. We exploit differences in interfacial tension to create a transition from 96 a precipitation-dominated region to a convection-dominated region in a two-layer fluid with 97 geometry shown in Figure 1c. In both the laboratory and in nature, precipitation-driven 98 convection is intrinsically non-uniform on multiple scales. On the smallest scales, it is gran-99 ular in space and time because it originates from the dissolution of individual drops or 100 particles. It is also heterogeneous at intermediate time and length scales, due to variability 101 in the local precipitation rate, which in our experiments comes from random fluctuations 102 in the rain production apparatus in Figure 1c, and in natural systems comes from lateral 103 heterogeneity in temperature, composition, and the velocity of the fluid through which the 104 precipitation falls. A fundamental assumption is that these small and intermediate scale 105 heterogeneities average out, so that on larger scales the precipitation induces a constant and 106 horizontally uniform buoyancy flux, analogous to turbulent Rayleigh-Benard convection with 10 fixed heat flux boundary conditions (Verzicco and Sreenivasan, 2008; Johnston and Doering, 108 2009; Huang et al., 2015). However, because precipitation-driven convection has received so 109 little attention, the validity of this assumption as applied to planetary dynamos is an open 110 question. 111

## 112 2 Rain-driven convection experiments

Figures 2-5 show results of laboratory experiments in which a two-layer fluid is subject to a uniform intensity rainfall of a third fluid. The rain is a dyed aqueous solution, immiscible in the upper fluid, a low-density, low-viscosity silicone oil, but miscible in the lower fluid, pure water in these experiments. The two fluids are confined in a rectangular plexiglass tank with a square 25x25 cm cross-sectional area shown in Figure 1c, above which a 25 cm diameter circular shower head consisting of 100 equally-spaced, 0.75 mm diameter spigots connected via a flow meter and control valve to a head tank containing the rain fluid. Back lighting with a rectangular diode array is used to illuminate the tank. The stochastic drop pattern from the shower head yields a statistically uniform precipitation in the central region of the tank, where we confine our measurements, and slightly reduced precipitation in the corner regions.

We consider two types of rain, distinguished by their density relative to the lower fluid. 124 In high-density rain experiments, hereafter referred to as Type 1 experiments, the rain fluid 125 consists of a water-NaCl solution with organic dye, the salt and dye concentrations adjusted 126 to produce the desired density excess with respect to the lower fluid. In low-density rain 127 experiments, referred to as Type 2, the rain fluid consists of a water-ethanol solution with 128 organic dye, their concentrations adjusted to produce the desired density deficit with respect 129 to the lower fluid. Properties of the experimental fluids and a comparison of the dimensionless 130 parameters in the experiments and in planetary cores are given in Table 1. 131

In the high-density Type 1 rain experiment shown in close-up in Figures 2a and 2b, the rain has an initial density excess of  $\Delta \rho / \rho_L = +1.0\%$  with respect to the lower fluid, the average rainfall intensity is  $R=4.5\times10^{-4}$  m s<sup>-1</sup> (approximately 28 ml s<sup>-1</sup> total rain rate) applied over approximately 120 s. The corresponding rain buoyancy flux, defined as (see Appendix)

$$F = \frac{g\Delta\rho}{\rho_L}R\tag{1}$$

where g is gravity, is  $F = 4.5 \times 10^{-5} \text{ m}^2 \text{ s}^{-3}$  in this experiment. In the low-density Type 2 rain experiment shown in close-up in Figures 2c and 2d, the rain density deficit is -1.0% and the average rainfall intensity is the same as in the accompanying Type 1 experiment, so that the rain buoyancy flux in that case is  $F = -4.5 \times 10^{-5} \text{ m}^2 \text{ s}^{-3}$ . In both Type 1 and 2 experiments, rain precipitates through the upper layer and accumulating as a binary emulsion at the interface with the lower fluid. The drops fall along nearly vertical trajectories in the upper layer. We do not observe substantial lateral deflections or clustering of the drops as they fall, even in the highest rain intensity experiments, as would be the case if the rainfall generated coherent large-scale motions in the upper layer. We emphasize this point because it relates to the question of the capacity for dynamo action in precipitation-dominated regions of planetary cores.

Gravitational separation of the fallen rain and the entrained upper layer fluid occurs 148 within the two-phase emulsion zone shown in Figure 2. The various steps in the gravita-149 tional separation processes within the emulsion are the same as described in detail by Sato 150 and Sumita (2007) and Gilet et al., (2007) for the case in which the negatively buoyant com-151 ponent is discontinuous (localized in drops) and the neutral component forms the connected 152 pore network. Drop dissolution ejects small volumes of the rain fluid downward, forming 153 millimeter-sized ring vortices below the emulsion interface, while the less dense silicone oil 154 percolates back into the upper layer. 155

The behavior of the rain fluid injected into the lower layer depends on its density relative 156 to the lower fluid. In the case of excess density rain in Type 1 experiments, the vortex 157 rings formed by drop dissolution evolve into small-scale, negatively buoyant compositional 158 plumes, as shown in Figure 2a. The time sequence in Figures 2a and 2b shows how these 159 small-scale compositional plumes coalesce into larger plumes that drive a still larger-scale 160 turbulent convective overturn, mixing and homogenizing the entire lower fluid. In contrast, 161 in Type 2 experiments with density-deficient rain, the small-scale compositional plumes are 162 positively buoyant and barely penetrate into the lower fluid, as shown in Figures 2c and 2d. 163 Instead of producing turbulence throughout the lower layer, the rain products accumulate 164

below the emulsion interface, producing a stratified rain product layer that grows with time. The intensity of convection in the lower layer is governed by a flux Rayleigh number defined in terms of F (see Appendix)

$$Ra_F = \frac{Fd_L^4}{\nu^3} \tag{2}$$

where  $d_L$  and  $\nu$  are the initial lower fluid depth and kinematic viscosity, respectively. For the Type 1 experiment shown in Figures 2a and 2b, using the lower fluid depth  $d_L$  given in Table 1, the flux Rayleigh number is  $Ra_F = 4.5 \times 10^{10}$ . We measure the intensity of the convective turbulence in terms of a Reynolds number based on the lower fluid depth and the average velocity of the plumes w (see Appendix)

$$Re = \frac{wd_L}{\nu},\tag{3}$$

The average plume velocity is defined as  $w = d_L/\tau$ , where  $\tau$  is the plume travel time, the average of the measured time intervals between the formation of plumes below the interfacial emulsion and the arrival of those plumes at the base of the tank. For the Type 1 experiments shown in Figures 2a and 2b,  $Re \simeq 1.8 \times 10^3$ .

The image sequence in Figure 3 shows large-scale views of the development of the con-177 vecting region in an 0.1% excess density (Type 1) rain experiment at  $Ra_F = 4.5 \times 10^9$ . The 178 emergence of large-scale flows through plume growth and coalescence is evident in this se-179 quence. At 9 s after rain injection begins (Figure 3a) the small size of the plumes corresponds 180 to the scale at which vorticity is injected into the lower layer following the coalescence of 181 individual rain drops. At 24 s after the initial injection (Figure 3b), clusters of the small 182 plumes have merged to form larger plumes. Plume mergers continue as the mixing layer and 183 the large-scale circulation approach the base of the lower layer at 39 s (Figure 3c). The final 184

image Figure 3d shows nearly complete homogenization on the lower layer by the overturning circulation. The progressive upward displacement of the emulsion at the rain-convection
interface in Figures 3a-d is due to filling of the lower layer by the rain fluid.

The two images in Figure 4 compare Ty pe 1 rain-driven turbulent convection with large 188 and small density excess, respectively. In Figure 4a, the rain density excess is 0.03% and the 189 flux Rayleigh number is  $Ra_F = 1.35 \times 10^9$ , whereas in Figure 4b the rain density excess is 190 2.5% and the flux Rayleigh number is approximately  $Ra_F = 1.13 \times 10^{11}$ , nearly two orders 191 of magnitude larger. Note the increase in turbulent mixing from the higher density rainfall 192 and the shorter growth time of the plumes in Figure 4b compared to Figure 4a. But in terms 193 of their large-scale structure, the two flows are remarkably similar, despite the nearly two 194 orders of magnitude difference in  $Ra_F$ . 195

Figure 5 shows the relationship between the plume Reynolds number defined in (3) and the flux Rayleigh number, from five different Type 1 rain convection experiments. Figure 5 also shows a power-law fit to the data of the form

$$Re = cRa_F^\beta \tag{4}$$

in which  $c = 0.17 \pm 0.02$  and  $\beta = 0.32 \pm 0.02$ . Within experimental error, (4) is indis-199 tinguishable from the  $\beta = 1/3$ -power law exponent that corresponds to ideal inertial scaling 200 (see Appendix). In terms of dimensional variables, a 1/3-power law relationship between 201 Re and  $Ra_F$  implies  $w \propto (Fd_L)^{1/3}$ , i.e., the plume velocity is independent of the viscosity 202 and the diffusivity, and depends only on the buoyancy flux and the convective layer depth. 203 In our experiments, we mostly varied the buoyancy flux, by independently varying the rain 204 density and the precipitation rate. In contrast, the lower layer depth was varied only by 205 small amounts, so the implied  $d_L^{1/3}$ -dependence of w was not actually tested. 206

We can compare our plume Reynolds number scaling with the plume Reynolds numbers measured in thermal convection experiments of the classical Rayleigh-Benard type, in which the top and bottom boundaries are rigid and isothermal. Figure 5 shows a semi-theoretic scaling law for the plume Reynolds number derived by Grossmann and Lohse (2001), which has the form

$$Ra_F = (Nu - 1)Pr^{-2}Ra = c_1 \frac{Re^2}{f(Re)} + c_2 Re^3,$$
(5)

in which Ra and Nu are the Rayleigh number and the Nusselt number in Rayleigh-Benard convection defined in terms of the temperature difference across the fluid (defined in the Appendix), Pr is the Prandtl number,  $f(x) = (1 + x^2)^{1/4}/x^{1/2}$ , and  $c_1$  and  $c_2$  are empirical coefficients that depend on the experimental geometry and boundary conditions (Grossmann and Lohse, 2003), and also on the technique used to measure the plume velocities (Ahlers et al., 2009).

Fitting (5) to turbulent Rayleigh-Benard convection experiments in a variety of fluids, 218 Grossmann and Lohse (2002) obtain  $c_1 \simeq 8.7$  and  $c_2 \simeq 1.45$ . The resulting scaling law is 219 indicated by the dashed line in Figure 5. A similar scaling has been found to hold for 220 Rayleigh-Benard convection in cylindrical domains, but with some variations in the coeffi-221 cients (Ahlers and Xu, 2001; Funfschilling et al., 2005). In Figure 5 we indicate the sensitivity 222 to geometry and boundary conditions with the background gray shading. We note that the 223 trend of our data is hardly distinguishable from (5), and the offset is only about 40%, an 224 amount which can be expected in light of the differences in boundary conditions, geometry, 225 and the fact that we measure the overall plume travel time in our rain convection experi-226 ments versus mid-depth plume travel times in the conventional Rayleigh-Benard convection 22 experiments. 228

### <sup>229</sup> 3 Implications for precipitation-driven dynamos

We quantify the dynamo capacity of precipitation-driven convection in planetary core using 230 scaling laws for the fluid velocity and the magnetic field intensity generated by thermochemi-231 cal convection obtained from numerical dynamo systematics (Christensen and Aubert, 2006; 232 Aubert et al. 2009). These scaling laws include the effects of sphericity, self-gravitation, 233 and planetary rotation, which are missing from our experiments, and assume that the fluid 234 velocity and the magnetic induction are independent of diffusive effects, including the vis-235 cosity. The fact that our experimental convective velocities are consistent with inertial (i.e., 236 viscosity-independent) scaling provides some justification for using such diffusion-free dy-237 namo scaling laws in this application. 238

We assume that the planet's core is divided into a outer precipitation-dominated re-239 gion and a central convection-dominated region, separated at a radius  $r_c$ . We can write 240 the precipitation buoyancy flux at the top of the convective region as (1), where now g is 241 gravity at radius  $r_c$ ,  $\rho_L$  is the convecting region density,  $\Delta \rho$  is the density difference be-242 tween the convecting region and the precipitation, and R is the rate of precipitation, solid 243 or liquid, evaluated at the top of the convecting region. Magnetic field generation depends 244 on F through the magnetic Reynolds number of the convection Rm. In an entirely molten 245 convecting sphere with radius  $r_c$ , 246

$$Rm = \frac{ur_c}{\eta} \tag{6}$$

where  $\eta$  is the magnetic diffusivity of the fluid and u is the rms fluid velocity. For full-sphere geometries and assuming an adiabatic heat flux at the CMB, dynamo scaling relationships (Aubert et al., 2009) yield

$$Rm \simeq 1.3p^{0.42} PmE^{-1} \tag{7}$$

where  $Pm = \nu/\eta$  is the magnetic Prandtl number,  $E = \nu/\Omega r_c^2$  is the Ekman number,

$$p = \frac{3F}{5\Omega^3 r_c^2} \tag{8}$$

is the convective power, and  $\Omega$  is angular velocity of planetary rotation. The critical magnetic Reynolds number for convective dynamo onset is  $Rm_{crit} \simeq 40$  (Christensen et al., 1999).

We first consider magnesium precipitation in Earth's core prior to inner core nucleation. 253 recently proposed by O'Rourke and Stevenson (2016) and later considered by Badro et al. 254 (2016). Rising precipitation in the form of buoyant magnesium oxides and silicates would 255 leave behind a dense iron-rich residual fluid, promoting compositional convection deeper in 256 the core. If we assume that the background state of the core is well mixed (i.e., adiabatic), 257 then very low intensity precipitation of this type could initiate the geodynamo. According 258 to (1), (7), (8) and the data in Table 2, a precipitation rate of just a few m Gyr  $^{-1}$  produces 259  $Rm_{crit}$  under these conditions. 260

More intense magnesium precipitation is needed to maintain a finite intensity magnetic field, even if the background state of the core is well mixed. According to dynamo model systematics (Olson and Christensen, 2006) the dipole magnetic moment  $\mathcal{M}$  in the dipoledominated regime depends on the buoyancy flux from precipitation F approximately as

$$\mathcal{M} \simeq 1.8 (\frac{\rho}{\mu_0})^{1/2} r_c^{10/3} F^{1/3},\tag{9}$$

where  $\mu_0$  is free-space magnetic permeability. In order to sustain a magnetic field with dipole moment  $\mathcal{M}=50$  ZAm<sup>2</sup>, comparable to the time-averaged Proterozoic geomagnetic field intensity (Biggin et al., 2015), (9) along with the data in Table 2 predict that a precipitation rate of  $R \simeq 400$  m Gyr<sup>-1</sup> is required. This is a negligibly small magnesium addition to the mantle and would not materially affect geochemical tracers such as Hf-W isotopic ratios (Rudge et al., 2010) or mantle siderophiles (Chabot et al., 2005). It would slightly increase Earth's rotation rate, but by less than 1%, far too small to counteract the angular deceleration from
tidal braking (Denis et al., 2011).

Far more intense precipitation would be needed for dynamo action if the core was strat-273 ified, either thermally or by composition. If the heat loss from the convective region is less 274 than the heat conducted down the core adiabat, a plausible situation in view of the high 275 thermal conductivity of the core (Gomi et al., 2013; Labrosse, 2015), then an additional 276 compositional buoyancy flux must be added to balance the negative thermal buoyancy flux 277 due to the subadiabatic thermal gradient, in order to homogenize the core fluid. In terms 278 of the total heat loss from the convecting region Q, the additional thermal buoyancy flux 279 is given by  $F_T = (Q - Q_{ad})/\rho A_c H_c$ , where  $Q_{ad}$  is the adiabatic heat loss,  $A_c = 4\pi r_c^2$  is the 280 surface area of the convecting region, and  $H_c$  is its temperature scale height. The net buoy-281 ancy flux that enters into the expression for the convective power (8) then becomes  $F + F_T$ . 282 If the thermal buoyancy flux  $F_T$  is negative because  $Q < Q_{ad}$ , then a larger rain-produced 283 buoyancy flux F is required in order to compensate for the subadiabatic heat loss. 284

The effects of core heat flux and magnesium precipitation rate on the dynamo structure and the induced dipole moment are shown in Figure 6, where we have assumed a convecting zone radius of  $r_c$ =3480 km, equal to the present-day core radius, and an adiabatic heat flux of 0.1 W m<sup>-2</sup>, equivalent to  $Q_{ad} \simeq 15$  TW. Line contours indicate the induced dipole moment in ZAm<sup>2</sup> from (9) and the local Rossby number  $Ro_{\ell}$ , which controls the transition from dipolar to multipolar dynamo states (Christensen and Aubert, 2006; Aubert et al., 2009):

$$Ro_{\ell} \simeq 0.54 p^{0.48} E^{-0.32} (PrPm)^{0.19},$$
 (10)

where  $Pr = \nu/\kappa$  is the Prandtl number. Shadings indicate dynamo regimes that are subcritical (labeled no-dynamo), convection driven by precipitation against stable thermal strat<sup>294</sup> ification (labeled precipitation dynamo), and convection driven by precipitation acting in <sup>295</sup> concert with unstable thermal stratification (labeled thermo-precipitation dynamo).

Magnesium precipitation can maintain a strong dipolar dynamo even under subadiabatic 296 conditions, provided the precipitation rate is high enough. Suppose, for example, that Q = 1229 TW, equivalent to  $q_{cmb} \simeq 0.08 \text{ W m}^{-2}$  for the average local heat flux at the CMB. To maintain 298 a dipole moment of 50 ZAm<sup>2</sup> with this core heat flux, Figure 6 indicates that a magnesium 299 rain rate of approximately R=2.8 km Gyr<sup>-1</sup> is required. For purposes of comparison, this 300 is approximately the same as the present-day mean rate of sediment accumulation on the 301 Pacific ocean floor (Olson et al., 2016), a modern analog that demonstrates how sparse this 302 type of precipitation would be in the Earth's core. 303

With these properties,  $Ro_{\ell} < 0.1$ , indicating the dynamo would be dipolar, consistent with most Proterozoic paleomagnetic data (Biggin et al., 2015). However, a precipitation dynamo with these parameters lies perilously close to the subcritical regime in Figure 6, such that a modest reduction in core heat flux would cause it to fail. The situation is made worse by the fact that the precipitation rate R is coupled to Q through the cooling rate of the core, so that a reduction in Q also reduces R, further increasing the chances of dynamo failure.

The results in Figure 6 assume the convective region occupies the entire Earth's core. In other planets the convective region may occupy only a fraction of the core, and if so, the precipitation rate required for dynamo action can be very high. For example, Figure 7 shows contours of magnetic Reynolds number from (7) and local Rossby number from (10) as functions of convecting radius and iron-snow precipitation rate for Mercury, based on the parameter values in Table 2 and assuming a solid inner core is absent or negligibly small. If the convective radius exceeds 200 km, a minimum precipitation rate near 30 km Gyr<sup>-1</sup> is needed for dynamo onset, but in a smaller convective region, with  $r_c < 100$  km, dynamo action would require implausibly high precipitation rates.

Another implication of Figure 7 is that iron-snow precipitation can generate high mag-320 netic Reynolds number conditions in a deep convective region in Mercury, but according 321 to (10), this convection would induce a multi-polar field because of the planet's slow ro-322 tation. This is seemingly in contradiction with the offset dipolar field observed in orbit 323 around Mercury (Anderson et al., 2011). It is, however, consistent with a proposed deep dy-324 namo mechanism for Mercury by Christensen (2006), which postulates that the non-dipolar 325 components of the dynamo magnetic field generated deep within the Mercury's core are elec-326 tromagnetically screened in an overlying stable layer. According to our experiments, such 327 electromagnetic screening might occur in the precipitation-dominated layer because it lacks 328 large-scale circulation. 329

Figure 8 shows the dynamo regimes for Ganymede, calculated according to the same 330 scaling laws as for Earth and Mercury, but using the property values for Ganymede in Table 331 2. The model for Ganymede differs from Mercury in having a smaller convective region and 332 a lower thermal conductivity, following Christensen (2015). A convective dynamo driven 333 by iron snow precipitation, possibly aided by an unstable thermal gradient, is predicted for 334 most precipitation rates, including the nominal precipitation rate of 10 km  $Gyr^{-1}$ . The no-335 dynamo regime in Figure 8 consists of two part. In region (a) the convection is subcritical, 336 i.e., the magnetic Reynolds number is below 40, whereas in the no-dynamo region (b) the 337 heat loss is less than the latent heat released by melting the precipitation (assumed to be 338  $5 \times 10^5$  J kg<sup>-1</sup>), so that steady-state convection is not sustainable. 339

#### 340 4 Conclusions

In this paper we describe a new class of convective flows, driven by buoyancy acquired 341 through precipitation. This form of convection has been proposed for evolving planetary 342 cores, where cooling results in nucleation, precipitation, and dissolution of buoyant con-343 stituents. Our rain-driven experiments are analogous to precipitation-driven systems in 344 planetary interiors in several respects, although there are important differences. Similarities 345 include (1) the basic two-layer dynamical structure, with a precipitation region separated 346 from a region where the precipitation is dissolved, with the possibility of compositional 347 convection; (2) a thin multi-component transition zone separating these regions where the 348 buoyancy for convection originates; and (3) buoyancy production on the scale of the indi-349 vidual precipitates, followed by plume coalescence. Significant differences include, for the 350 experiments (1) lack of phase changes (solidification and melting) and latent heat exchange, 351 which could contribute to the convection; (2) absence of rotational and magnetic field effects, 352 which tend to stabilize the convection; and (3) the idealized plane-layer geometry, which ig-353 nores the changes in fluid volume and gravity with radius. In addition, there are structural 354 differences between our experiments and some of the scenarios envisioned for planetary in-355 teriors. 356

In Earth's core, for example, it is supposed that extraction of upward precipitating magnesium or other light constituants would yield a negatively buoyant residual liquid, whereas in our experiments, the negatively buoyant liquid is produced through addition of downward precipitation. In cores dominated by the Fe-FeS system, the geometry might be inverse of our experiment. For example, for core compositions on the FeS side of the eutectic, convection might be due to sulfur-rich fluid rising from a deep iron snow zone (Hauck et al. 2006; <sup>363</sup> Chen et al. 2008). In spite of these differences, we claim that the fundamental effects of <sup>364</sup> precipitation on the dynamics of these system are captured in our experiments.

A key finding of our study is the process by which stochastic precipitation self-organizes to generate larger-scale convective motions. In our experiments, this organization begins during gravitational separation within multi-component emulsion layers, whereas in planetary interiors it is generally hypothesized to occur near the pressure-temperature horizon that corresponds to a phase transition. In both situations, however, the fluid buoyancy develops on the scale of the isolated particles or drops, generating micro-scale plumes that must coalesce in order to form the larger plume structures that induce convective overturn.

Although substantial gravitational potential energy may be released in the precipitation-372 dominated region of a planetary core, this does not guarantee that large scale magnetic 373 induction occurs there. If the only fluid motions in the precipitation zones are in particle 374 wakes, which have lateral dimensions on the scale of the particles themselves ( $\sim 1 \text{ mm}$ ), 375 these will be quickly dissipated by viscous or Lorentz forces, and will contribute little (if 376 anything) to dynamo action. In contrast, our experiments show that the convective regions 377 have far more capacity for dynamo action. In planetary cores, the rates of precipitation 378 needed to maintain a dynamo are not excessive, especially if the precipitation is intense and 379 strongly buoyant and the convective region is deep. 380

Lastly, we note that previous studies have found that diffusive boundary layer effects, including viscosity, remain controlling factors in heat transfer in Rayleigh-Benard convection when planetary rotation is included, even at high Rayleigh numbers (King et al., 2009, Stellmach et al., 2014). It would be revealing, therefore, to determine how the velocity scaling for precipitation-driven convection changes when rotation is added. Acknowledgements: We gratefully acknowledge support from grant EAR-0909622 and FESD grant EAR-1135382 from the National Science Foundation. This paper benefitted from helpful comments by two anonymous referees.

Author contributions: BH, ML, and PO jointly conducted the experiments; PO and ML jointly made the calculations; PO and ML prepared the figures, tables, and references; PO and ML jointly wrote the paper.

Conflicts of interest: The authors have no conflicts of interest to disclose regarding this
 research or this paper.

## 394 Appendix

The steady-state mechanical energy equation for non-rotating, non-magnetic Boussinesq convection can be written

$$\frac{1}{2}\nabla \cdot (u^2 \mathbf{u}) = \mathbf{F} + \nu \mathbf{u} \cdot (\nabla^2 \mathbf{u})$$
(11)

<sup>397</sup> where  $\rho$  is the mean density, **u** is the fluid velocity, nu is kinematic viscosity, and

$$F = \rho'(\mathbf{g} \cdot \mathbf{u})/\rho \tag{12}$$

is the buoyancy flux, in which **g** is the vector gravity and  $\rho'$  is the density perturbation, respectively. From left to right, the terms in (11) represent fluid inertia, production of kinetic energy by buoyancy, and dissipation of kinetic energy by viscosity, respectively. At convective onset, buoyancy production balances viscous dissipation. Using d and  $\nu/d$  to scale length and velocity in the dissipation term, the ratio of the second to the third term in (11) defines the Rayleigh number used in our experiments:

$$Ra_F = Fd^4/\nu^3 \tag{13}$$

Ideal inertial scaling, appropriate for fully-developed turbulent convection corresponds to a balance between the inertia of the fluid and the buoyancy force driving the motion, the first and second terms in (11). For this balance, by choosing w and d for the velocity and length scales, (11) can be written in terms of non-dimensional variables (denoted by asterisks) as

$$\frac{w^3}{2d}\nabla^* \cdot (u^{*2}\mathbf{u}^*) = F \tag{14}$$

<sup>409</sup> where . In order for this force balance to hold, the convective velocity must scale like

$$w \sim (Fd)^{1/3},$$
 (15)

<sup>410</sup> as given in the text.

Traditional Rayleigh-Benard thermal convection experiments use a different Rayleigh number, defined as

$$Ra = \alpha g \Delta T d^3 / \kappa \nu \tag{16}$$

where  $\alpha$  and  $\kappa$  are thermal expansion and thermal diffusivity, respectively, and  $\Delta T$  is the temperature difference across the fluid. Heat transfer in Rayleigh-Benard convection is usually measured in terms of the Nusselt number, defined as

$$Nu = qd/k\Delta T \tag{17}$$

where q and k are heat flux (conventionally measured on the fluid layer boundary) and thermal conductivity of the fluid, respectively. The definitions (16) and (17) are used in the r.h.s. of equation (5).

## **References**

420	Ahlers, G., Xu, X., 2001. Prandtl-number dependence of heat transport in turbulent
421	Rayleigh-Benard convection. Phys. Rev. Lett. 86, 3320-3323.
422	Ahlers, G., Grossmann, S., Lohse, D., 2009. Heat transfer and large scale dynamics in
423	turbulent Rayleigh-Benard convection. Rev. Mod. Phys. 81(2), 503-537.
424	Anderson, B. J., et al., 2011. The global magnetic field of Mercury from MESSENGER
425	orbital observations. Science 333.6051, 1859-1862.
426	Aubert, J., Labrosse, S., Poitou, C., 2009. Modelling the paleo-evolution of the geodynamo.
427	Geophys. J. Int. 179, 1414-1428.
428	Badro, J., Siebert, J., Nimmo, F., 2016. An early geodynamo driven by exsolution of mantle
429	components from Earths core. Nature doi:10.1038/nature18594.
430	Biggin, A., Piispa, E., Pesonen, L., Holme, R., Paterson, G., Veikkolainen, T., Tauxe,
431	L., 2015. Palaeomagnetic field intensity variations suggest Mesoproterozoic inner-core
432	nucleation. Nature 526 (7572), 245-248.
433	Breuer, D., Rueckriemen, T., Spohn, T., 2015. Iron snow, crystal floats, and inner-core
434	growth: modes of core solidification and implications for dynamos in terrestrial planets
435	and moons. Prog. Earth Planet. Sci. $2(1)$ , 1.
436	Buffett, B.A., Garnero, E.J., Jeanloz, R., 2000. Sediments at the top of the core. Science
437	290, 1338-1342.
438	Cao, H., Russell, C. T., Christensen, U. R., Dougherty, M. K., Burton, M. E., 2011. Saturn's
439	very axisymmetric magnetic field: No detectable secular variation or tilt. Earth Planet.

- 440 Sci. Lett. 304(1), 22-28.
- Cao, H., Russell, C. T., Wicht, J., Christensen, U. R., Dougherty, M. K., 2012. Saturns high
  degree magnetic moments: Evidence for a unique planetary dynamo. Icarus 221(1),
  388-394.
- Chabot, N. L., Draper, D. S., Agee, C. B., 2005. Conditions of core formation in the
  Earth: constraints from nickel and cobalt partitioning. Geochim. Cosmochim. Acta
  69, 2141-2151.
- <sup>447</sup> Chen, B., Li, J., Hauck, S.A., 2008. Non-ideal liquidus curve in the FeS system and
  <sup>448</sup> Mercurys snowing core. Geophys. Res. Lett. 35, L07201.
- <sup>449</sup> Christensen, U.R., 2006. A deep dynamo generating Mercury's magnetic field. Nature 444,
  <sup>450</sup> 1056-1058.
- <sup>451</sup> Christensen, U. R., 2015. Iron snow dynamo models for Ganymede. Icarus 247, 248-259.
- <sup>452</sup> Christensen, U. R., Olson, P., Glatzmaier, G. A., 1999. Numerical modelling of the geody<sup>453</sup> namo: a systematic parameter study. Geophys. J. Int. 138, 393-409.
- <sup>454</sup> Christensen, U. R., Aubert, J., 2006. Scaling properties of convection-driven dynamos in
  <sup>455</sup> rotating spherical shells and application to planetary magnetic fields. Geophys. J. Int.
  <sup>456</sup> 166, 97-114.
- <sup>457</sup> Christensen, U.R., Wicht, J., 2008. Models of magnetic field generation in partly stable
  <sup>458</sup> planetary cores: Applications to Mercury and Saturn. Icarus 196, 16-34.
- <sup>459</sup> Deguen, R., Landeau, M., Olson, P., 2014. Turbulent metal-silicate mixing, fragmentation,
  <sup>460</sup> and equilibration in magma oceans. Earth Planet. Sci. Lett. 391, 274-287.

461	Deng, L., Deagle, C., Fei, Y., Shahar, A., 2013. High pressure and temperature electrical
462	resistivity of iron and implications for planetary cores. Geophys. Res. Lett. 40, 3337.
463	Denis, C., Rybicki, K. R., Schreider, A. A., TomeckaSucho, S., Varga, P., 2011. Length
464	of the day and evolution of the Earth's core in the geological past. Astronomische
465	Nachrichten 332(1), 24-35.
466	Dumberry, M., Rivoldini, A., 2015. Mercury's inner core size and core-crystallization
467	regime. Icarus 248, 254-268.
468	Dziewonski, A. M., Anderson, D. L., 1981. Preliminary reference Earth model. Phys. Earth
469	Planet. Inter. 25, 297-356.
470	Fortney, J.J., Hubbard, W.B., 2004. Effects of helium phase separation on the evolution of
471	extrasolar giant planets. Astrophys. J. 608, 1039-1049.
472	Funfschilling, D., Brown, E., Nikolaenko, A., Ahlers, G., 2005. Heat transport by turbulent
473	Rayleigh-Benard convection in cylindrical cells with aspect ratio one and larger. J.
474	Fluid Mech. 536, 145-154.
475	Gaidos, E., Conrad, C. P., Manga, M., Hernlund, J., 2010. Thermodynamic constraints on
476	rocky exoplanet dynamos. Astrophys. J. 718, 596-609.
477	Gilet, T., Mulleners, K., Lecomte, J. P., Vandewalle, N., Dorbolo, S., 2007. Critical pa-
478	rameters for the partial coalescence of a droplet. Phys. Rev. E 75, 036303.
479	Gomi, H., Ohta, K., Hirose, K., Labrosse, S., Caracas, R., Verstraete, M. J., Hernlund, J.
480	W., 2013. The high conductivity of iron and thermal evolution of the Earth's core.
481	Phys. Earth Planet. Inter. 224, 88-103.
	23

482	Grossmann, S., Lohse, D., 2002. Prandtl and Rayleigh number dependence of the Reynolds
483	number in turbulent thermal convection. Phys. Rev. E 66, 016305.
484	Grossmann, S., Lohse, D., 2003. On geometry effects in Rayleigh-Benard convection. J.
485	Fluid Mech. 486, 105-114.
486	Hauck, S. A., Aurnou, J. M., Dombard, A. J., 2006. Sulfur impact on core evolution and
487	magnetic field generation on Ganymede. J. Geophys. Res. 111, E09008.
488	Helffrich, G., Kaneshima, S., 2010. Outer-core compositional stratification from observed
489	core wave speed profiles. Nature 468, 807-809.
490	Hirose, K., Labrosse, S., Hernlund, J., 2013. Composition and State of the Core. Ann.
491	Rev. Earth Planet. Sci. 41, 657-691.
492	Huang, SD., Wang, F., Xi, HD., Xia, KQ., 2015. Comparative experimental study
493	of fixed temperature and fixed heat flux boundary conditions in turbulent thermal
494	convection. Phys. Rev. Lett. 115, 15452.
495	Ichikawa, H., Labrosse, S. Kurita, K., 2010. Direct numerical simulation of an iron rain in
496	221 the magma ocean. J. Geophys. Res. 115, doi:10.1029/2009JB006427.
497	Johnston, H., Doering, C.R., 2009. Comparison of turbulent thermal convection between
498	conditions of constant temperature and constant flux. Phys. Rev. Lett. 102, 064501.
499	King, E. M., Stellmach, S., Noir, J., Hansen, U., Aurnou, J. M., 2009. Boundary layer
500	control of rotating convection systems. Nature, $457(7227)$ 301-304.
501	Kraus, R. G., Root, S., Lemke, R. W., Stewart, S. T., Jacobsen, S. B., Mattsson, T. R.,
502	2015. Impact vaporization of planetesimal cores in the late stages of planet formation.

 $_{503}$  Nature Geoscience, 8(4), 269-272.

- Kudo, A., 2013. The generation of turbulence below midlevel cloud bases: The effect of
   cooling due to sublimation of snow. J. Applied Meteor. Climat., 52(4), 819-833.
- Labrosse, S., 2015. Thermal evolution of the core with a high thermal conductivity, Phys. Earth Planet Inter. 247, 36-55..
- Labrosse, S., Hernlund, J. W., Coltice, N., 2007. A crystallizing dense magma ocean at the base of the Earth's mantle. Nature 450, 866-869.
- Landeau, M., Olson, P., Deguen, R., Hirsh, B., 2016. Core merging and stratification
  following giant impact, Nature Geoscience DOI: 10.1038/NGEO2808.
- Nakajima, M., Stevenson, D. J., 2015. Melting and mixing states of the Earth's mantle
  after the Moon-forming impact. Earth Planet. Sci. Lett. 427, 286-295.
- <sup>514</sup> Olson, P., Christensen, U. R., 2006. Dipole Moment Scaling for Convection-Driven Plane-<sup>515</sup> tary Dynamos. Earth Planet. Sci. Lett. 250, 561-571.
- <sup>516</sup> Olson, P., Deguen, R. Rudolph, M.L., Zhong, S., 2015. Core evolution driven by mantle <sup>517</sup> global circulation. Phys. Earth Planet. Inter., 243, 44-55.
- Olson, P., Reynolds, E., Hinnov, L., Goswami, A., 2016. Variation of ocean sediment thick ness with crustal age. Geochem. Geophys. Geosyst. 17, doi:10.1002/2015GC006143.
- Poirier, J.-P., 2000. Introduction to the physics of the Earth's interior, 2nd Edition. Cam bridge University Press.
- <sup>522</sup> O'Rourke, J. G., Stevenson, D.J., 2016. Powering Earth?s dynamo with magnesium pre-<sup>523</sup> cipitation from the core. Nature 529(7586), 387-389.

524	Rückriemen, T., Breuer, D., Spohn, T., 2014. The Fe snow regime in Ganymede's core:
525	A deep-seated dynamo below a stable snow zone. J. Geophys. Res. Planets. $120(6)$ ,
526	1095-1118.
527	Rudge, J. F., Kleine, T., Bourdon, B., 2010. Broad bounds on Earth's accretion and core
528	formation constrained by geochemical models. Nature Geoscience $3(6)$ , $439-443$ .
529	Sato, M., Sumita, I., 2007. Experiments on gravitational phase separation of binary im-
530	miscible fluids. J. Fluid Mech. 591, 289-319.
531	Siebert, J., Corgne, A., Ryerson, F. J., 2011. Systematics of metal-silicate partitioning for
532	many siderophile elements applied to Earth's core formation. Geochim. Cosmochim.
533	Acta 75, 1451-1489.
534	Stanley, S., 2010. A dynamo model for axisymmetrizing Saturn's magnetic field. Geophys.
535	Res. Lett. 37, L05201.
536	Stellmach, S., Lischper, M., Julien, K., Vasil, G., Cheng, J. S., Ribeiro, A., Aurnou, J. M.,
537	2014. Approaching the asymptotic regime of rapidly rotating convection: Boundary
538	layers versus interior dynamics. Physical review letters $113(25)$ , $254501$ .
539	Stevenson, D.J., 1980. Saturns luminosity and magnetism. Science 208, 746-748.
540	Takafuji, N., Hirose, K., Mitome, M. Bando, Y., 2005. Solubilities of O and Si in liquid
541	iron in equilibrium with (Mg,Fe)SiO3 perovskite and the light elements in the core.
542	Geophys. Res. Lett. 32, L06313.
543	Tarduno, J. A., Cottrell, R. D., Davis, W, J., Nimmo, F., Bono, R.K., 2015. A Hadean
544	to Paleoarchean geodynamo recorded by single zircon crystals. Science $349(6247)$ ,
545	521-524.

546	Tonks, W. B., H.J. Melosh, 1993. Magma ocean formation due to giant impacts. J.
547	Geophys. Res. Planets 98(E3), 5319-5333.
548	Verzicco, R., Sreenivasan, K.R., 2008. Comparison of turbulent thermal convectin between
549	conditions of constant temperature and constant flux. J. Fluid Mech. 595, 203-219.
550	Vilim, R., Stanley, S., Hauck II, S. A., 2010. Iron snow zones as a mechanism for generating
551	Mercury's weak observed magnetic field. J. Geophys. Res. 115, E11003.
552	Vocaldo, L., Alfe, D., Gillan, M. J., Price, G. D., 2003. The properties of iron under core
553	conditions from frst principles calculations. Phys. Earth Planet. Inter. 140, 101-125.
554	Ward, W. R., Colombo, G., Franklin, F. A., 1976. Secular resonance, solar spin down, and
555	the orbit of Mercury. Icarus, $28(4)$ , $441-452$ .
556	Williams, G. E., 2000. Geological constraints on the Precambrian history of Earth's rotation
557	and the Moon's orbit. Rev. Geophys. 38, 37-59.

Property	Notation	Units	Experiment Type 1	Experiment Type 2
upper fluid density	$ ho_U$	${ m kg}~{ m m}^{-3}$	$0.82 \times 10^3$	$0.82 \times 10^3$
lower fluid density	$\rho_L$	$kg m^{-3}$	$1.0 \times 10^3$	$1.0 \times 10^3$
rain-lower fluid density difference	$\Delta \rho$	$kg m^{-3}$	0.3-25	-10
rain viscosity	$ u_r$	$m^2 s^{-1}$	$1 \times 10^{-6}$	$1.6  imes 10^{-6}$
upper fluid viscosity	$ u_U$	$\mathrm{m}^2~\mathrm{s}^{-1}$	$1.2 \times 10^{-6}$	$1.2 \times 10^{-6}$
lower fluid viscosity	$ u_L$	$\mathrm{m}^2~\mathrm{s}^{-1}$	$1 \times 10^{-6}$	$1 \times 10^{-6}$
upper fluid depth	$d_U$	m	0.192	0.192
lower fluid depth, initial	$d_L$	m	0.178	0.178
rain interfacial tension	$\sigma_r$	${\rm N~m~s^{-1}}$	$2.2 - 2.4 \times 10^{-2}$	$2.6 \times 10^{-2}$
rain rate	R	${\rm m~s^{-1}}$	$3.4 - 4.6  imes 10^{-4}$	$4.5  imes 10^{-4}$
rain buoyancy flux	F	$\mathrm{m}^2~\mathrm{s}^{-3}$	$1.35 - 110 \times 10^{-6}$	$-4.5 \times 10^{-5}$
rain drop radius	$r_r$	m	$\sim 10^{-3}$	$\sim 10^{-3}$
plume velocity	w	${\rm m~s^{-1}}$	$3.4 - 14.3 \times 10^{-3}$	$< 4 \times 10^{-4}$
Dimensionless Parameter	Definition	Experiment	Experiment	Early Core
		Type 1	Type 2	(Estimated)
Bond Number, B	$g\Delta\rho r_r^2/\sigma$	0.012-0.018	0.015	$\sim 0.1$
Ohnesorge Number, $Oh$	$\rho_r \nu_r / \sqrt{\sigma r_r}$	$\sim 0.15$	$\sim 0.17$	$\sim 0.1$
Density Ratio, $\epsilon$	$\Delta  ho /  ho_L$	$0.3 \text{-} 25 \times 10^{-3}$	-0.01	$\sim 4.6$
Rayleigh Number, $Ra_F$	$F d_L^4 / \nu_L^3$	$1.35 \text{-} 112 \times 10^9$	$-4.5 \times 10^{10}$	$\sim 10^{29}$
Plume Reynolds Number, $Re$	$wd_L^{-}/\nu_L^{-}$	$6.05 \text{-} 25.5 \times 10^2$	$< 2  imes 10^1$	$\sim 2 \times 10^7$
Magnetic Reynolds Number, $Rm$	$ud_L/\eta$	na	na	$\sim 2 \times 10^3$

 Table 1: Rain-Driven Convection Experiment Properties

Notation	Definition, Units	Early Earth	Mercury	Ganymede
$r_c$	convection radius, km	$3480^{a}$	$500^{b}$	$650^{j}$
Ω	rotation rate, $10^{-5}$ rad s <sup>-1</sup>	$5^c$	$0.124^{d}$	1.02
$\eta$	magnetic diffusivity, $m^2 s^{-1}$	$0.8^{\ e}$	$\sim 1$	$0.7^{-k}$
ho	average density, $10^3 \text{ kg m}^{-3}$	$11^{\ a}$	$7.7$ $^{b}$	j
$q_s$	adiabatic heat flux, mW $m^{-2}$	$100^{f}$	$10^{b}$	$4^j$
q	CMB heat flux, mW $m^{-2}$	50-100 <sup>f</sup>	$3 - 10^{b}$	$2-4^{l}$
$H_c$	temperature scale height, km	$6500^{g}$	$1400^{b}$	$1100^{b}$
$g\Delta ho/ ho$	precipitation buoyancy, m $s^{-2}$	$4.6^{h}$	$0.4^{e}$	$0.4^e$
R	precipitation rate, km $Gyr^{-1}$	2.5	50	10
F	pricipitation buoyancy flux, $10^{-13}$ m <sup>2</sup> s <sup>-3</sup>	6	4	1.3
ν	kinematic viscosity, $10^{-6} \text{ m}^2 \text{ s}^{-1}$	1	1	$1^{i}$
k	thermal conductivity, W $m^{-1}k^{-1}$	$130^{f}$	$120^{k}$	$30^{j}$

Table 2: Core Precipitation Properties (Nominal Values)

 $\overline{}^{a}$  PREM Dziewonski and Anderson (1981);  $^{b}$  Dumberry and Rivoldini (2015);  $^{c}$  Williams (2000);  $^{d}$  Ward et al. (1976);  $^{e}$  Hirose et al. (2013);  $^{f}$  Labrosse (2015);  $^{g}$  Vocadlo et al. (2003);  $^{h}$  PREM CMB buoyancy contrast;  $^{i}$  Perrialt et al. (2010);  $^{j}$  Christensen (2015)  $^{k}$  Deng et al. (2013)  $^{l}$  Hauk et al. (2006)  $^{m}$  Chen et al. (2008)



Figure 1: **Precipitation-Driven Convection.** Schematics of precipitation-driven convection in cooling planetary cores and laboratory analog. (a) Iron-snow; (b) Magnesium precipitation; (c) Laboratory apparatus, with the dashed box indicating the region imaged in Figure 2. M,P,C denote the mantle, the precipitation-dominated region, and the convection-dominated region, respectively.  $r_c$  denotes convective region radius. Small arrows indicate precipitation directions; large arrows denote convection.



Figure 2: Rain-Driven Convection Experiments. In each case, raindrops (an aqueous solution) released at a constant and spatially uniform rate, fall through the upper liquid (silicone oil) into the lower liquid (another aqueous solution). In images (a) and (b) the blue-dyed rain is initially 1% denser than the lower liquid (Type 1 experiments). This close-up sequence, corresponding to the dashed box in Figure 1 with time given in seconds after convective onset, shows the development of 34 two-phase emulsion layer, phase separation producing compositional plumes and turbulent convection, resulting in homogenization of the lower liquid. In images (c) and (d) the rain is initially 1% less dense than the lower liquid (Type 2 experiments). In this case the rain products accumulate in the interfacial region and stratify the lower liquid. Experimental parameters are given in Table 1.



Figure 3: **Development of a Rain-Driven Convection Region.** This sequence shows the development of rain-driven convection in a Type 1 experiment with 0.1% excess rain density. (a): Onset of small scale compositional plumes; (b): Growth and turbulent merging of compositional plumes; (c): Large-scale convection in the lower layer; (d) mixing and homogenization. Time is given in seconds after rain injection begins.



Figure 4: **Density Effects in Rain-Driven Convection.** Comparison of rain-driven turbulent convection in Type 1 experiments with large and small density contrasts. (a): Convection with initial rain excess density of 0.03%; (b): Convection with initial rain excess density of 2.5%. Time is given in seconds after convective onset.



Figure 5: Rayleigh Number-Reynolds Number Relation in Rain-Driven Convection Reynolds number Re based on plume descent speed versus flux Rayleigh number  $Ra_F$ from five Type 1 (dense rain) experiments, in which the Rayleigh number increases with increasing excess density of the rainfall. Symbol size is representative of 1 s.d. uncertainties in Re and  $Ra_F$ . Power law fit exponent and coefficient are given in the plot. Dashed line is a fit by Grossmann and Lohse (2002) to plume velocities in Rayleigh-Benard experiments.



Figure 6: Dynamo Regimes from Magnesium Precipitation in Earth's Core Dipole magnetic moment and local Rossby number for dynamo action in the totally fluid core (prior to inner core nucleation) driven by magnesium precipitation. Axes are core heat flux and precipitation rate. An adiabatic heat flux of 100 mW m<sup>-2</sup> is assumed. Additional parameters are given in Table 2.



Figure 7: Dynamo Regimes from Iron-snow Precipitation in Mercury Magnetic Reynolds number Rm and local Rossby number  $Ro_{\ell}$  for dynamo action in the assumed totally fluid iron alloy core of Mercury, driven by iron-snow precipitation. Axes are iron-snow precipitation rate and convective radius. Total and adiabatic heat fluxes of 5 and 50 mW m<sup>-2</sup> are assumed. Additional parameters are given in Table 2.



Figure 8: Dynamo Regimes from Iron-snow Precipitation in Ganymede Dynamo regimes in the assumed totally fluid iron alloy core of Gamymede, driven by iron-snow precipitation. Axes are heat flux at the top of the convecting region and precipitation rate. An adiabatic heat flux of 5 mW m<sup>-2</sup> is assumed. No-dynamo region (a) has subcritical magnetic Reynolds number; region (b) has subcritical heat flux. Additional parameters are given in Table 2. 36