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# **1 Predictive-reactive strategy for identical parallel machine rescheduling**

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# 5 Abstract

6 Through new technologies development, customers can create or cancel an order in real time, 7 which disrupts the established production schedule. This realty forces many companies to 8 quickly react for dealing with this situation through rescheduling processes. When efficiency 9 usually measures the performance of a scheduling system, in dynamic environments, stability 10 measures the impact of jobs deviation. Differently from previous works, this paper investigates 11 a new approach to measure simultaneously efficiency by total weighted waiting times, and 12 stability by weighted completion time deviation. This mix could be a very helpful and 13 significant criterion in industrial and health care environments. This paper considers a parallel 14 machine rescheduling problem with jobs arriving over time. Based on predictive-reactive 15 strategy, a mixed integer linear programming model is developed, as well as an online iterative 16 methodology to solve this rescheduling problem. Finally, numerical results are performed for studying the impact of efficiency and stability coefficient, as well as the computing time to 17 18 solve the described problem.

Keywords: Rescheduling, Parallel Machine, Waiting time, Stability, Completion time
 deviation, Disruption.

# 21 **1. Introduction**

22

23 Due to the fourth revolution experiencing, today's industry is developing new technologies and solutions for the production process. In addition, the customers' practices are also changed. 24 25 Henceforth, a customer can, at any time, create or cancel an order in real time. Indeed, these 26 changed situations have a direct impact on work organization, especially production scheduling (Ivanov et al. 2016; Uhlmann, and Frazzon 2018; Da Silva et al., 2019). In fact, production 27 28 planning is subject to unexpected events that disrupt the established schedule, such as: new jobs 29 arrival, cancelation of jobs, machine failures, quality problems, shortage of raw materials, etc. 30 (Li et al., 1993; Sabuncuoglu and Karabuk 1999; Katragjini et al., 2013). Hence, the decision 31 makers are forced to quickly react to deal with these disruptions. Therefore, rescheduling is 32 necessary to revise the initial schedule in a cost-effective manner (Vieira et al., 2003).

33 Rescheduling is the process of updating an established schedule in response to disruptions 34 (Vieira et al., 2003). In the rescheduling literature, the classical efficiency criteria are often used 35 to measure the performance of a schedule, including: the Makespan, the total completion time, 36 the maximum lateness, etc. Differently from previous researches, this work considers a new 37 efficiency criterion, which is the Total Weighted Waiting Times (TWWT). On the scheduling 38 literature, the waiting time is the period that the job has waited before its execution in a system 39 (Jurčišin and Šebo 2015). Indeed, the TWWT could be a very helpful and significant criterion 40 in industrial and health care environments. For instance, in production systems, it can represent

the waiting time of a job in front of a workstation, considering the importance of each job as 41 42 the weight. In hospital systems, the waiting time can represent the delay between a patient's 43 arrival and his actual treatment, considering the emergency level as the weight. Guo et al., 44 (2013) is among the first works that considered the waiting time on rescheduling problems. The 45 authors formulated a single machine rescheduling problem to minimize the sum of waiting times of rework jobs and the original loads with release time. They proved that the problem is 46 47 NP-hard and designed a dynamic insert heuristic algorithm of polynomial-time. To fill the void 48 in existing literature, in our study, we considered the TWWT as an efficiency scheduling 49 measure, which has been defined for the first time by Kan (1976), and classified as NP-hard for 50 a single machine. To the best of our knowledge, there is not any rescheduling problem in the 51 literature which discussed this criterion.

52 The efficiency usually measures the performance of a scheduling system, but, in dynamic 53 environments, the impact of jobs deviation is also studied in the literature, known as stability 54 measure (Wu et al., 1993; Pfeiffer et al., 2007; Zhang et al., 2013). This criterion measures the 55 impact of disruptions induced by moving jobs during a rescheduling event (Rangsaritratsamee 56 et al., 2004). In real life systems, when the sequence is changed, this matter may generate 57 additional costs, such as reallocation costs, raw-materials reordering costs, etc (Rahmani and 58 Ramezanian 2016). Ahmadi et al., (2016) studied a multi-objective jobshop rescheduling problem, in which the disruptions were caused by random machine breakdown. The authors 59 60 considered the makespan as the efficiency measure, and calculated the stability with the average 61 difference between the completion times of the predicted schedule and the realized completion 62 time. In fact, when a disruption occurs, initial completion times of jobs may change and are 63 replaced by real completion times obtained after disruption. Two evolutionary algorithms are 64 applied to solve this problem, with the objective simultaneously combines makespan improvement and stability. Indeed, this paper presents a new approach to measure the schedule 65 stability, which consists in calculating the difference between the completion times of the job 66 67 in the initial schedule and in the new one, associating for each job a weight. We denote by the Total Weighted Completion Time Deviation (TWCTD) this stability criterion. In fact, when a 68 69 job has a high weight (i.e. more important), it is difficult to disrupt it. This is the case of an urgent patient in a hospital, for example. 70

According to (Vieira et al., 2003; Herrmann 2006), there are two basic rescheduling 71 72 strategies. The first is the *dynamic scheduling strategy* which consists in dispatching jobs when 73 it is necessary and using the available information at the moment of dispatching. This strategy 74 uses dispatching rules or other heuristics to prioritize jobs waiting to be processed at a 75 workstation (El-Bouri 2012; Nurre and Sharkey 2018; Bektur, and Saraç 2019; Riahi et al., 76 2019). The second is the *Predictive-reactive scheduling strategy* that consists in generating an 77 initial schedule in a first step, and to update the schedule in response to a disruption (Vieira et 78 al., 2003; Duenas and Petrovic 2008). In our approach, we firstly generate an initial schedule 79 with the objective of minimizing the TWWT. After a disruption, we generate a second schedule 80 to minimize a multi-criterion combining simultaneously efficiency and stability, with the 81 stability measured with the Total Weighted Completion Time Deviation.

82 The analysis of scheduling performance often requires more than one aspect (Loukil et al., 2005). Therefore, in the rescheduling literature, several papers deal with multi-objective 83 84 function. For instance, Wang, D et al., 2015 considered a rescheduling problem disrupted by 85 machine breakdown and deterioration effect. The authors aim to minimize a multi objective 86 function, considering initial operational cost assessed by the total completion time and resource 87 consumption, as well as the rescheduling cost assessed by match-up time and additional 88 resource cost. In this paper, we established a relationship between both parts of the objective 89 function, by associating a coefficient for each measure (i.e.  $\alpha$  efficiency + (1- $\alpha$ ) stability). We 90 called  $\alpha$  the *efficiency-stability coefficient*, and studied the influence of this coefficient on the 91 system.

92 According to Alagöz and Azizoğlu (2003), in the flexible manufacturing systems, changes 93 in jobs assignments to machines may generate some additional costs, like setup and tooling 94 costs. Thus, the authors considered the number of jobs processed on different machines after 95 the disruption as the stability measure in parallel machines rescheduling problem. In the 96 operating rooms scheduling case, this matter can also generate additional costs related to the 97 preparation phase before the operation. In our study, we have used the lexicographic 98 optimization to reduce the number of jobs processed on different machines after disruption. 99 This method is investigated in many papers dealing with the multi objective problems. It always provides a Pareto optimal solution (Chang 2015). It consists in obtaining an arbitrarily small 100 101 improvement for the most important criterion through any loss in other less important criteria 102 (Zykina 2004). In our work, we have assumed the bi-objective function considering 103 simultaneously the efficiency and the stability as the priority function. From the optimal value 104 obtained for this objective function, we minimize then the number of jobs processed on different 105 machines, taking as constraint the optimal value of the priority function.

106 This work addresses a rescheduling problem on identical parallel machines, when the 107 disruption is caused by the arrival of new jobs. A mixed integer linear programming model is 108 developed to describe the problem, and an online iterative methodology to solve it. The 109 proposed methodology provides, for each step, the optimal solution. The presented 110 rescheduling problem has not been studied in the research literature before. The main 111 contributions of this work are as follows:

- We implement a mathematical model based on sequence formulation, after we have
   improved it to match the parallel machines problem. Besides, we develop an online
   iterative methodology adapting this model to our rescheduling problem, and we
   discuss its limitation in function of the number of jobs.
- We consider for the first time '*TWWT*' as a criterion in a parallel machine rescheduling
   problem, which is a very significant criterion in several environments.
- We adopt a new approach in parallel machine rescheduling problem by simultaneously
   considering the efficiency defined by the *TWWT*, and the stability as the *Total Weighted Completion Time Deviation*.
- We establish a lexicographic optimization, by minimizing the number of jobs which
   are processed on different machines after disruption.

The rest of the paper is organized as follows: we present in section 2 the literature review. Our research motivation is given in section 3. In section 4 the problem description, as well as the strategy that we propose to tackle it. In section 5, the mathematical model is presented. We then analyze the numerical results in section 6. We conclude and propose some perspectives in section 7.

- 128 **2. Literature review**
- 129

130 In this section, we focus on the different issues studied in the rescheduling. The rescheduling 131 literature is very rich. Vieira et al. (2003), Li and Ierapetritou (2008), Ouelhadj and Petrovic (2009), and recently Uhlmann, and Frazzon (2018) provided interesting reviews of the state-of-132 133 the-art of developing research on rescheduling at those times. In the rescheduling literature, the 134 classical efficiency criteria are often used to measure the performance of a schedule, including 135 the makespan (Yuan and Mu 2007; Zakaria and Petrovic 2012; Tang et al., 2016; Li et al. 2017; Wu et al., 2018), the total completion time (Lu et al., 2003; Yang 2007), the total weighted 136 137 completion time (Hall and Potts 2010; Luo et al., 2018), the average flowtime, the average 138 tardiness and the percentage tardy (Kunnathur et al, 2004), the total weighted tardiness (Mason et al., 2004; Kaplan and Rabadi 2015), the total flow time (Ozlen and Azizoğlu 2011), and the 139 140 maximum lateness (Hall and Potts 2004). As well, the rescheduling literature has taken interest 141 in studying different types of machine environments such as: single machine (Unal et al., 1997; 142 Hall and Potts 2004; Hall et al., 2007), flowshop (Yan-hai et al., 2005; Katragjini et al., 2013), 143 jobshop (Bierwirth and Mattfeld 1999; Mason et al., 2004; Salido et al., 2017; Yan et al., 2018; 144 Larsen and Pranzo 2019), or openshop (Liu and Zhou 2013b). Moreover, there are also several 145 papers dealing with parallel machines rescheduling problems. Yin et al., (2016) studied a 146 rescheduling problem on identical parallel machines, and considered the total completion time 147 as the original scheduling objective and the maximum time deviation or the total virtual 148 tardiness with respect to the original schedule as the deviation cost associated with a disruption 149 caused by machine breakdowns. The complexity of the described problem is studied and a 150 pseudo-polynomial time solution algorithm is proposed. Hamzadayi and Yildiz (2016) treated 151 a dynamic identical parallel machines scheduling problem, in which sequence dependent setup operations are performed by a single server. An event driven rescheduling strategy is proposed 152 153 to control the dynamic system, with the objective of minimizing the makespan. The authors 154 indicated that the simulated annealing based complete rescheduling approach produces the best 155 performance. Alagöz and Azizoğlu (2003) addressed a rescheduling problem in parallel 156 machine environments under machine eligibility constraints. The authors considered the total 157 flow time as efficiency measure, and the number of jobs processed on different machines after 158 disruption as stability measure. Several heuristics are proposed to provide a set of approximate 159 efficient schedules. For other related papers, dealing with parallel machine rescheduling, the reader may refer to Church and Uzsoy (1992); Vieira et al., (2000); Azizoglu and Alagöz 160 161 (2005); Curry and Peters (2005); Duenas and Petrovic (2008); Arnaout (2010); ShangGuan et 162 al., (2012); Liu and Zhou (2013a), and recently Wang et al., (2018); Ferrer et al., (2018); 163 Kovalyov et al., (2019); Cunha et al., (2020).

164 The waiting time is the period during which a job is waiting before its execution in a system (Jurčišin and Šebo 2015). In the scheduling literature, this criterion is used to measure the 165 166 schedule efficiency. Guo et al., (2016) treated a rescheduling problem with the objective of 167 minimizing the maximum waiting time, inspired from quartz manufacturing industry, where 168 waiting times represent the waiting for some materials before the reheating step in oven, where 169 both the rework stream and the regular production stream meet. Thus, the authors studied and 170 analyzed the complexity of a rescheduling problem on a single machine, with the objective of 171 deciding where to insert the rework jobs in an initial sequence of regular jobs to minimize 172 maximum waiting time. Guo and Xie (2017) formulated a two mixed integer programming 173 models for a single machine rescheduling problem with the objective of minimizing the total 174 waiting time. The studied problem came also from quartz glass factory, considering that the 175 waiting time is the waiting for materials before the welding step, and its minimization saves the 176 energy consumption. However, in dynamic environments, stability criteria are also studied. Several papers in the literature deal with this criterion. Akkan (2015) considered a multi 177 178 objective rescheduling problem that simultaneously measures the scheduling efficiency with 179 the maximum tardiness, and the stability with the sum of absolute starting time deviations, 180 which are the sum of absolute difference between starting times of jobs before and after 181 rescheduling. The author demonstrated that his algorithm improves the stability of schedules 182 with no degradation in the maximum tardiness. Gao et al. (2018) studied a rescheduling 183 problem on a flexible jobshop, with newly arrived priority jobs which are inserted in the existing schedule. The authors considered a bi-objective rescheduling criterion. The first is the 184 185 efficiency, and the second is the stability which is defined as the percentage of machineschanged operations of the existing jobs during rescheduling. Pfeiffer et al., (2007) proposed a 186 schedule stability measure calculated with two penalties. The first is the starting time deviation 187 188 penalty, which is the difference between starting times of jobs at the new and previous 189 rescheduling points. The second is the penalty related to the deviation of job starting time from 190 the current time. Moreover, we found other related works dealing with stability measure in 191 rescheduling problems, such as starting time deviation and total deviation penalty 192 (Rangsaritratsamee et al., 2004), starting time deviation (Cui et al., 2018), the amount of 193 operations and starting times operations which have been altered (Li et al., 2015, Peng et al. 194 2018), the absolute positional disruption, the positional disruption and absolute completion time 195 disruption (Hoogeveen et al., 2012), the total sequence disruption (Yuan et al., 2007), the 196 maximum time disruption (delivery times of jobs to customers changes) (Liu and Ro 2014). For 197 considering the both aspects, efficiency combining with stability, the most of the treated mathematical models use a multi objective function, such as (Wu et al., 1993; 198 199 Rangsaritratsamee et al., 2004; Qi et al., 2006; Wang et al., 2017; Peng et al., 2019).

In the rescheduling literature, we found also several papers dealing with operating rooms rescheduling, modeling the problem as a machine scheduling problem. For instance, Stuart and Kozan (2012) addressed a rescheduling problem of a day-to-day running of a day surgery unit, modeling the problem as a single machine scheduling problem, with sequence dependent processing time and due date. They proposed a branch and bound algorithm to solve the problem. Wang, B *et al.*, (2015) discussed a surgery scheduling problem for single surgical suite, where each patient should be treated in same order by three stages. The system is disrupted by the arrival of random emergency surgeries. The authors handled the system as a
no-wait permutation flowshop scheduling problem and developed a predictive reactive
approach to tackle it. For other related papers, the reader may refer to Fei *et al.*, (2010), Farrokhi *et al.*, (2014), M'Hallah and Al-Roomi (2014), Addis *et al.*, (2016), Zhong and Shi (2018).

211 The Predictive-reactive scheduling strategy consists in generating an initial schedule in a 212 first step, and to update it in response to a disruption (Vieira et al., 2003). In the literature, several researchers have adopted predictive-reactive approach. For example, Yang and Geunes 213 214 (2008) considered a predictive-reactive scheduling on a single machine with uncertain future 215 jobs. The authors determined the amount of planned idle time for uncertain jobs and their positions in the predictive schedule. Then, the schedule reacts when a disruption occurs, through 216 217 including the new jobs in the idle times. Gürel et al. (2010) developed an anticipative 218 scheduling approach based on a predictive reactive strategy, on parallel non-identical machines 219 with controllable processing times. Firstly, an initial schedule is designed to minimize the total 220 manufacturing cost of the jobs. When a machine breakdown occurs, a reactive schedule is 221 generated and the remaining schedule is repaired.

# **3. Motivation**

223

Our research motivation is inspired from real cases which can be encountered, either in hospital environment or in industrial environment. In what follows, we present an illustration of our problem in the context of hospital systems and in the context of industrial systems.

227 Among the hospital departments, the Operating Theater (OT) represents the largest hospital cost category by 33% (Macario et al., 1995). Hence, operating rooms scheduling has been 228 229 identified as an interesting potential area by hospital decision makers. Moreover, among the 230 heard complaints in the health care services, the long waiting lists are the most received 231 (Cardoen et al., 2010). Therefore, it is relevant to react on the minimization of the patient 232 waiting time, to reduce hospital costs and improve patient's satisfaction. In practice, there are 233 two types of operations, the elective operations that are known in advance, and the emergency 234 operations caused by the arrival of an urgent patient. These ones are unknown in advance, and represent a disruption for the already established schedule. To cope with this uncertainty, 235 236 Wullink et al. (2007) proved that the approach consisting to share OT between elective and 237 emergency operations is better than the approach of dedicating one or several OTs for 238 emergency operations. That justifies our approach of modelling the system as a parallel machine 239 rescheduling problem. In addition, according to surgery priorities, the patients can be divided 240 to five majors' groups (Abedini et al., 2016). Thus, we have considered for each job a weight 241 representing its emergency level. The aim of our study is to model this practical example as a 242 parallel machine rescheduling problem, consisting in the predictive (elective) step to minimize 243 the patient weighted waiting times, and in the reactive step (i.e. when the emergency operations 244 occur), the same criterion combined with the stability, in order not to deviate too much from 245 the initial schedule.

This described system can also be an illustration of industrial cases, as described by Guo et *al.* (2016), where the waiting time is the waiting period for some materials before the reheating

step in oven, with disruptions caused by the arrival of new orders. The weight can also be considered, representing the customer priority.

### **4. Problem description**

We study a parallel machine rescheduling problem, under disruptions caused by the arrival of new jobs. For each job *j*, we associate a processing time  $p_j$ , a release date  $r_j$  and a weight  $w_j$ . When a job *j* starts at time  $S_j$ , it is processed to completion time  $C_j$  without interruption (i.e.  $C_j$  $S_j + p_j$ ). The waiting time  $W_j$  of job *j* is the period during which the job has waited, from its entry into the system  $r_j$ , until its execution at the starting time. Then, it is defined as  $W_j = S_j - r_j - r_j - p_j$  (see Fig.1).

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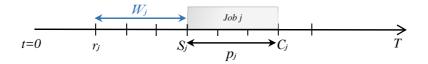


Fig. 1 The waiting time of job *j* 

#### 258



In the studied system, we supposed that we have a set of *n* jobs,  $N = \{1, 2, ..., n\}$ , already available to be scheduled in the set of parallel machines  $M = \{1, 2, ..., nm\}$ , all the jobs information  $(p_j, r_j, w_j)$  is available at the beginning. An initial schedule should be determined with the objective of minimizing the *TWWT*, i.e.  $\sum_{j \in N} w_j W_j$ . Indeed, a mathematical model is

developed to solve the initial problem, that can be represented in standard notation by 264  $P|r_i|\sum w_i W_i$ . During execution of the jobs, the initial schedule can be disrupted by the 265 266 arrival of new jobs. Consequently, a new set of jobs is generated,  $N' = \{1, 2, ..., n'\}$ , which 267 contains the unexecuted jobs (i.e. the jobs that haven't started) as well as new arrival jobs. The methodology is to omit the already executed jobs, and to combine the unexecuted jobs with 268 269 new arrival ones to create an updated schedule. Therefore, a new reactive schedule is generated 270 to update the existing one, simultaneously considering efficiency measured by original objective  $\sum_{j \in N'} w_j W_j$  and stability measured by the deviation from the original schedule, as 271

272 described hereafter.

Stability measure: If no disruption occurs, the job *j* will finish processing at completion time of original schedule  $Co_j$ . Else, if a disruption occurs and a new job is inserted inside the old schedule, some jobs will change their positions. Hence, a new schedule will be established. Consequently, the job *j* will really finish in the real completion time  $C_j$ . Then, the difference between  $Co_j$  and  $C_j$  can be used to assess the deviation cost. In addition, we used the weight  $w_j$ for each job, which makes it difficult to deviate important jobs. Hence, the stability objective is defined as  $\sum_{j \in N} w_j (C_j - Co_j)$ . We called it the *Total Weighted Completion Times Deviation* 

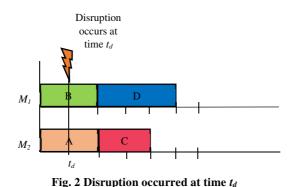
280 (*TWCTD*). In this approach, we only calculate the stability criterion for the jobs existing in the 281 previous schedule ( $j \in N$ ). However, once the new jobs are scheduled in their first sequence, they will be concerned by the stability criterion in the ulterior schedules. When  $w_{j}(C_{j} - Co_{j}) > 0$ , a deviation has occurred and an instability penalty is generated.

Along with that, we established a relationship between the both parts of objective functions, by integrating  $\alpha$  as an efficiency-stability coefficient. Thus,  $\alpha$  is associated to efficiency part and  $(1 - \alpha)$  to stability, where  $\alpha$  is a real number between zero and one. Finally, we defined the new objective function that simultaneously measures efficiency and stability as  $\alpha \sum_{j \in N'} w_j W_j + (1 - \alpha) \sum_{j \in N} w_j (C_j - Co_j)$ . Then, the dynamic rescheduling problem can be

289 represented in standard notation by:  $P | r_j | \alpha \sum w_j W_j + (1-\alpha) \sum w_i (C_j - Co_j)$ .

In the rescheduling process, the disruptions occur while the machine executes jobs. Therefore, we noted by  $t_d$  the current time when a disruption occurs (see Fig.2).

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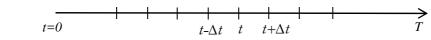
Indeed, all executed jobs before  $t_d$  must keep the same position. Thus, these jobs are omitted, and the new set N' will be scheduled, then a new sequence will be established, it begins, for each machine, from the completion time of the last executed job.

#### 297 Online iterative methodology

Firstly, we have discretized the finite time horizon [0, *T*], into periods  $\Delta t$  (see Fig.3). Indeed,  $\Delta t$  is the time period length which represents the time step. The occurrence of disruptions may be possible only at these times. In fact, when a job occurs at time *t*, this date will be its release date. In order to simplify the calculations, we assumed that  $\Delta t = 1$  unit of time, the same time unit that we used for the jobs data  $p_j$ ,  $r_j$ , and  $w_j$ .

303

304



305

We then defined  $\theta(t)$  a binary variable, equals to 1 if a job (or several jobs) occurs at time *t*, and 0 otherwise. The generation of its values is explained in the numerical results section. The algorithm below describes the online iterative methodology.

Fig. 3 Time discretization

- 309 Solve the initial problem
- 310 LIST =  $\{J_1, ..., J_n\}$
- 311 Memorize solution
- 312 For (tin 1 to T)
- 313 If  $(\theta(t)=1)$
- 314 Add new job(s) to LIST.
- 315 O mit the already executed jobs from LIST (comparing their memorized
- 316 starting time with t)
- 317 Reschedule the new problem with jobs in LIST
- 318 Memorize solution
- 319 End If
- 320 End For
- 321 The following flowchart describes the predictive-reactive strategy that we used to tackle the
- 322 problem (see Fig.4).

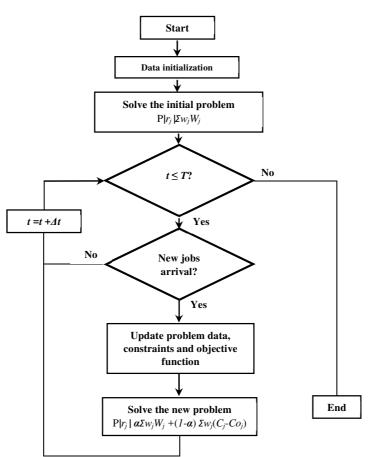


Fig. 4 The flowchart of predictive-reactive strategy

# **5. Mathematical model**

A mixed integer linear programming model is implemented in this section, it is based on predictive-reactive strategy, Thus, in the first subsection, we present the mathematical model before disruption. In the second subsection, we present the mathematical model after disruption.

#### **5.1 Mathematical model before disruption**

The proposed model is based on sequence position formulation (assigning a job to a position). In the scheduling literature, several papers used this formulation. For instance, Eren (2009), Baker and Keller (2010), Kooli and Serairi (2014) and Guo and Xie (2017) in single machine scheduling problems. As well, other authors, like Abdel-Jabbar et al. (2014) and Beezão et al. (2017), used this formulation for parallel machine scheduling problems. However, most of this works consider the Makespan as a criterion. Indeed, our problem consists in minimizing the TWWT. Hence, supplementary data and variables are considered, such as (weights, release dates, waiting time). In fact, we were inspired by Beezão et al. (2017) model and have adapted it to our variables and constraints. The parameters, variables and constraints of the model are given below:

339 Parameters:

- *N*: set of jobs {1, 2, ..., *n*}
- *K*: set of positions  $\{1, 2, ..., n\}$
- *M*: set of machines {1, 2, ..., *nm*}
- *j*: index of job, j = 1, 2, ..., n
- *k*: index of position, k = 1, 2, ..., n
- *m*: index of machine, *m* =1, 2, ..., *nm*
- $w_j$ : weight of job j
- $r_j$ : release date of job j
- $p_j$ : processing time of job j

349 *bigM*: big value, 
$$bigM = \sum_{i=1}^{n} p_i + \max r_i$$

350 Decision variables:

 $x_{jkm} = \begin{cases} 1 & \text{if the job } j \text{ is assigned to machine } m \text{ in } k^{\text{th}} \text{ position} \\ 0 & \text{Otherwise} \end{cases}$ 

- $CP_{km}$ : Completion time of job in  $k^{th}$  position in machine *m*.
- $SP_{km}$ : Starting time of job in  $k^{th}$  position in machine *m*.
- $C_j$ : Completion time of job *j*.
- $W_j$ : Waiting time of job j.

356 Objective function: 
$$Min \sum_{j \in N} w_j W_j$$

*s.t*:

$$\sum_{m=1}^{nm} \sum_{k=1}^{n} x_{jkm} = 1 \quad \forall j \in \mathbb{N}$$

$$\tag{1}$$

$$360 \qquad \sum_{j=1}^{n} x_{jkm} \le 1 \ \forall k \in K, \forall m \in M$$
(2)

361 
$$\sum_{j=1}^{n} x_{j(k+1)m} \leq \sum_{j=1}^{n} x_{jkm} \quad \forall k = 1..n-1, \forall m \in M$$
 (3)

362 
$$SP_{km} \ge \sum_{j=1}^{n} r_j x_{jkm} \quad \forall k \in K, \forall m \in M$$
 (4)

363 
$$SP_{(k+1)m} \ge SP_{km} + \sum_{j=1}^{n} p_j x_{jkm} \quad \forall k = 1...n-1, \forall m \in M$$
 (5)

364 
$$CP_{km} = SP_{km} + \sum_{j=1}^{n} p_j x_{jkm} \quad \forall k \in K, \forall m \in M$$
 (6)

$$365 \qquad C_{j} \geq CP_{km} - bigM \ (1 - x_{jkm}) \ \forall j \in N \ , \forall k \in K \ , \forall m \in M$$
(7)

$$366 \qquad C_{j} \leq CP_{km} + bigM (1 - x_{jkm}) \quad \forall j \in N , \forall k \in K, \forall m \in M$$
(8)

$$367 W_j = C_j - r_j - p_j \quad \forall j \in N$$
(9)

368 
$$CP_{km}, SP_{km}, C_j, W_j \ge 0 \quad \forall j \in N, \forall k \in K, \forall m \in M$$
 (10)

$$369 \qquad x_{jkm} \in \{0,1\} \quad \forall j \in N, \forall k \in K, \forall m \in M$$

$$(11)$$

370 Constraint (1) specifies that each job is affected to one position in a machine. Constraint (2) 371 consists in having only one or no job per position in a machine. Constraint (3) specifies that, if the position k is not occupied, the position k+1 is not occupied too. Constraint (4) consists in 372 making, for all machines, the starting time of  $k^{th}$  position greater than or equal to assigned 373 374 release date. Constraint (5) consists in making, for all machines, the starting time of  $(k+1)^{\text{th}}$ position greater than or equal to the previous position completion time. Constraint (6) specifies 375 that, for all machines, the completion time of  $k^{th}$  position is equal to starting time of  $k^{th}$  position 376 plus the assigned processing time. Constraint (7) defines, for all machines, the completion time 377 378 of job *j*, which is greater than or equal to completion time of assigned position, where *bigM* 379 must be sufficiently large. For that reason, we defined for our model a value of *bigM* according to the total completion times and maximum value of release dates to take into account jobs 380 availability. Thus,  $bigM = \sum_{j=1}^{n} p_j + \max r_j$ . Constraint (8) is a cut that allows reducing the 381 computing time. Constraint (9) defines the waiting time of job *j*, according to its completion 382 time, release date, and processing time, Constraint (10) consists in making all variables greater 383 384 than or equal to zero. Constraint (11) consists in having a binary decision variable.

#### **5.2 Mathematical model after disruption**

This second model is used after a disruption caused by the arrival of new jobs. We denoted by *nt* the number of the unexecuted jobs at time *t*, and *nj* the number of new arrived jobs. Thus, the new jobs have the same entry parameters as the first ones. For each job, we have  $w_j$ ,  $p_j$ , and *r<sub>i</sub>* which correspond to the time when the job occurs. So, the new parameters are as follows:

390 <u>New parameters:</u>

391 n' = nt + nj

- 392 N': set of jobs  $\{1, 2, ..., n'\}$
- 393 *K*': set of positions {1, 2, ..., *n*'}
- 394 *j*: index of job, j = 1, 2, ..., n'
- 395 *k*: index of position, *k* =1, 2, ..., *n*'
- 396 *Co<sub>j</sub>*: original completion time of job *j* (obtained by the resolution of the initial problem).
- 397  $\alpha$ : efficiency-stability coefficient.
- 398 *xo<sub>jkm</sub>*: variable assigning jobs to positions in the initial problem

We notice that the parameters  $xo_{jkm}$ , and  $Co_j$  are not decision variables. They are memorized when the initial model is solved. we recall that we only calculate the stability criterion for the jobs existing in the previous schedule ( $j \in N$ ). The decision variables  $x_{jkm}$ ,  $CP_{km}$ ,  $SP_{km}$ ,  $C_j$ ,  $W_j$  are the same for this new model. However, the new objective function is as follows:

403 
$$Min \alpha \sum_{j \in N'} w_j W_j + (1 - \alpha) \sum_{j \in N} w_j (C_j - Co_j)$$

404 The constraints (1), (2), (3), (4), (5), (6), (7), (8), (9), (10) and (11) are also used for this new 405 model.

In addition, when new jobs are added, the completion time of a job will be greater than its original completion time, because the original completion time have been obtained through minimization of the principal criterion "*TWWT*" only, since it is not concerned by the stability. Indeed, the job is placed in its ideal position, and it will not be moved forward after the rescheduling. Thus, in all rescheduling steps, we assumed that:

 $411 C_{i} \ge Co_{i} \quad \forall j \in N (12)$ 

#### 412 **6. Numerical results**

The proposed mixed integer linear programming model has been designed on FICO Xpress IVE and has been performed on a Core i5 2.40GHz laptop. The programed model is composed of two parts. The first contains the predictive approach, and consists in solving the initial problem normally, with the objective of minimizing the *TWWT*. The second contains the reactive approach, and consists in rescheduling at each time the jobs occur, accordingly to the online iterative methodology previously described. The system omits the already executed jobs, and combines the still unexecuted jobs with the new ones to create an updated schedule. The
model implementation has been developed accordingly to the chart presented on Fig.4. This
proposed methodology has been tested on the instances described hereafter, and it allowed
giving, at each step, the optimal solution.

In this section, we present the numerical results obtained through the model application, ontwo parallel machines. The data used in this section are as follows:

425

Table 1	parameter	values
---------	-----------	--------

Parameters	Values
$W_j$	~ <i>U</i> (1,5)
$p_j$	$\sim N(2.5, 0.5)(ut)$
Т	24 ( <i>ut</i> )

426

427 The data that we have chosen can be adapted for real cases, either in a hospital or in an 428 industrial environment. The simulation will be over a 6-hours' time horizon. The weight values 429 can represent the 5-emergency levels or 5 priority levels of customers. We assumed also that  $\Delta t$ 430 =1 unit of time (*ut*), and 1 *ut* is equivalent to 15 minutes. The processing times can represent 431 the durations of operations or a product manufacturing time, and follow a normal distribution 432 with mean 2.5 and standard deviation 0.5, obtaining operations of 1 ut (15 minutes) to 4 ut (60 433 minutes), with more probability to have a processing time of 2 ut or 3 ut. The values of the 434 variable  $\theta(t)$  are randomly generated with the Bernoulli distribution which gives, at each time 435 t, the value 1 with probability  $p_{\theta}$ , and 0 with probability  $1-p_{\theta}$ . At first, we considered  $p_{\theta} = 0.8$ 436 (high appearance probability), then we tested also for  $p_{\theta} = 0.5$  (medium appearance probability) 437 and  $p_{\theta} = 0.2$  (small appearance probability).

438 We established three main studies. Firstly, we examined the influence of efficiency-stability 439 coefficient  $\alpha$  on the optimal schedules. Secondly, we used the lexicographic method to 440 minimize the number of altered jobs. Finally, we tested the computing time of the model 441 resolution with different instances, to show its limitations according to the problems' size.

# 442 **6.1 Influence of efficiency-stability coefficient on the optimal schedules**

443 In this study, we vary the value of  $\alpha$  from 0.5 to 1 to discuss its impact on the optimal 444 schedule. We have assumed that the efficiency criterion is the principal one, while the stability 445 criterion is the secondary. Thus, it is not necessary to test the values of  $\alpha$  inferior to 0.5.

We first calculate the initial objective obtained by solving the offline problem. After each disruption, we update the problem, then we calculate the new objective function. The number of altered jobs is also calculated in this study, which represents the number of jobs which changed of machine after rescheduling. For that, we included the supplementary parameters:  $^{i}A_{jm}$  to assign jobs to machines in iteration *i*, and *Dif<sub>j</sub>* that represents the deviation of a job from its machine.

452  
453
$${}^{i}A_{jm} = \begin{cases} 1 \text{ if } \sum_{k=1}^{n} x_{jkm} = 1 \\ 0 \text{ Otherwise} \end{cases} \quad \forall j, \forall m, \forall i$$
(13)

454

$$Dif_{j} = \begin{cases} 1 & \text{if } \sum_{m=1}^{nm} \left| {}^{i}A_{jm} - {}^{i-1}A_{jm} \right| \neq 0 \\ 0 & \text{Otherwise} \end{cases} \quad \forall j$$

13

456

457 Therefore, the number of altered jobs is given by:  $\sum_{j \in N} Dif_j$ . We note that  $A_{jm}$  and  $Dif_j$  are

(14)

not considered as decision variables in this study, but they will be considered as such in thelexicographic optimization sub section.

The study was conducted and analyzed for 25 different instances, generated accordingly to the parameters presented in Table 1. We present, in the following example, the data and the results obtained on a particular instance with two parallel identical machines.

#### 463 Example

464 In this example, the processing times  $p_j$ , release dates  $r_j$  and the weights  $w_j$  for 5 jobs are 465 given in the Table 2.

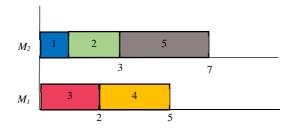
466

	1	•	2		-
job	1	2	3	4	5
$r_j$	0	1	0	1	2
$p_j$	1	2	2	3	4
$W_j$	5	1	4	2	1

Table 2. Initial problem data

467

468 The problem is solved with the objective to minimize the total weighted waiting times. So, 469 the obtained optimal value is  $\sum_{j=1}^{5} w_j W_j = 3$ . The optimal solution is given in Fig.5, we noted 470 it "the first schedule".



471

472

Fig. 5 The optimal solution for the initial problem

In the reactive approach, we assumed that the disruptions occur by the arrival of new jobs.
In this example, a total of 20 jobs are treated online. The obtained results are given in the Table
3.

In the Table 3, we assumed that a disruption occurs at each step with appearance probability  $p_{\theta} = 0.8$  (20 disruptions appeared in the total). At each disruption, we reschedule the problem, and we extract four information: the value of the efficiency criterion "*TWWT*", the value of the stability criterion "*TWCTD*", the number of jobs which are executed on a different machine after the disruption "*N*° of altered jobs", as well as the value of the objective function that combines *TWWT* and *TWCTD* thanks to  $\alpha$ . We have also numbered the schedules with their

#### 482 step number. Different values of $\alpha$ are tested, to discuss the impact of this parameter on the 483 obtained solutions.

484

#### Table 3. Influence of $\alpha$ on the optimal schedules

- *TWWT*: Total Weighted Waiting Times Σ<sub>J∈N</sub>, w<sub>j</sub>W<sub>j</sub>
   *TWCTD*: Total Weighted Completion Time Deviation Σ<sub>j∈N</sub> w<sub>j</sub>(C<sub>j</sub> Co<sub>j</sub>)
- (3) N° of altered jobs
  (4) Objective function
- 485 486 487 488 489

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$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		0.5	30	-			33	-	•		39	-			43	•	•	
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0.8       49       16       2       42,4       50       17       0       43,4       52       19       0       45,4       53       20       2       46,         0.7       49       16       2       39,1       50       17       0       40,1       52       19       0       42,1       53       20       2       46,         0.6       58       9       0       38,4       60       10       2       40       63       13       2       43       65       15       2       45		-																57
0.7       49       16       2       39,1       50       17       0       40,1       52       19       0       42,1       53       20       2       43,         0.6       58       9       0       38,4       60       10       2       40       63       13       2       43       65       15       2       45						-			2	-			2	-				49,7
0.6 58 9 0 38,4 60 10 2 40 63 13 2 43 65 15 2 45		0.8		16	2	42,4			0	43,4		19	0	45,4	53	20		46,4
										40,1								43,1
0.5 58 9 1 33,5 60 10 2 35 63 13 1 38 66 14 0 40					0								2				2	45
	_	0.5	58	9	1	33,5	60	10	2	35	63	13	1	38	66	14	0	40

490

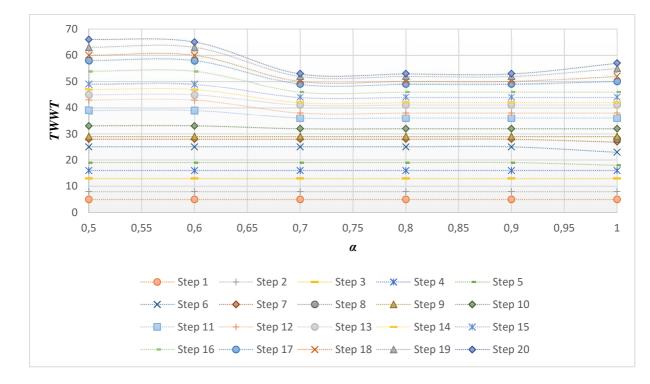
491	For $\alpha = 1$ , the objective function only considers the first criterion, <i>TWWT</i> . We noted that,
492	when the new jobs arrive, they have been scheduled according to their weights and their
493	processing times. Generally, when $\alpha = 1$ , and if all jobs are available, the <i>wSPT-rule</i> is optimal
494	for this problem.

Otherwise, for  $\alpha$  values between 0.9 and 0.7, the stability is also considered. In this case, we 495 496 have noted two observations:

• Short term: The optimal schedule has the same value of *TWWT* as when  $\alpha = 1$ , but the value of the second criterion *TWCTD* is smaller. Indeed, the schedule is more stable. In this case, during the model execution, if there are two solutions which give the same value of *TWWT*, the system chooses the one that minimizes the stability.

• Long term: The model gives a better value of both criteria (*TWWT* and *TWCTD*) 502 compared to  $\alpha = 1$ . This is a result of the proactive effect induced by the stability 503 criterion. Indeed, when we have two similar solutions in terms of efficiency, the 504 system prioritizes the one that minimizes  $\sum_{j \in N} w_j (c_j - c_{o_j})$ . This decision impacts the 505 efficiency criterion in the next steps.

506 For  $\alpha = 0.6$  and 0.5, the *TWWT* increases, because we give more importance to the stability 507 criterion. Figure 6 shows, for each step, the variation of *TWWT* according to  $\alpha$ .



508

509

Fig. 6 *TWWT* in function of  $\alpha$  with  $p_{\theta}$ =0.8

510 In the short term, the value of *TWWT* is stable in most of cases. In the long term, the value 511 of *TWWT* is smaller when  $\alpha = 0.7$ , 0.8 and 0.9 compared to others values as result of proactive 512 effect induced by the stability criterion. To clearly illustrate this phenomenon, we present the 513 Gantt diagram (Table 5) of the optimal sequences given by model resolution for  $\alpha = 0.8$ , 514 compared to those obtained with  $\alpha = 1$ , on the eleven first modified schedules (first eleven 515 steps) for the instance below (Table 4).

- 516
- 517 518
- 519 520

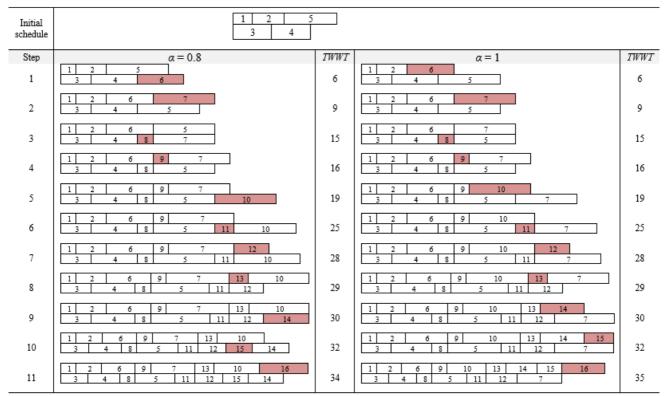
Job j rj pj wj	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
rj	0	1	0	1	2	2	3	4	6	7	9	10	11	12	13	14
рj	1	2	2	3	4	3	4	1	1	4	1	2	1	3	2	4
wj	5	1	3	2	1	1	1	5	3	1	5	3	4	1	1	1

Table 4. Problem data



#### 523

Table 5. Gantt diagram of the optimal sequences



524

From the first step until step 10, in both cases, the model provides the same value of the principal criterion *TWWT*. However, when  $\alpha = 0.8$ , the model provides more a stable schedule compared to  $\alpha = 1$ . This difference has impacted the schedule in step 11. For instance, in the step 9, with  $\alpha = 1$ , the system places the job 14 before the job 7. Whereas, if we consider the stability criterion (*TWCTD*), the system proposes the opposite to have a stable schedule. Consequently, this choice impacts the value of *TWWT* in the step 11. Thus, the difference of one unit of time between the schedule when  $\alpha = 1$  and  $\alpha = 0.8$ .

532 To confirm this behavior, we present in Figure 7, the average of *TWWT* in function of *alpha*,

533 on the 25 instances generated.

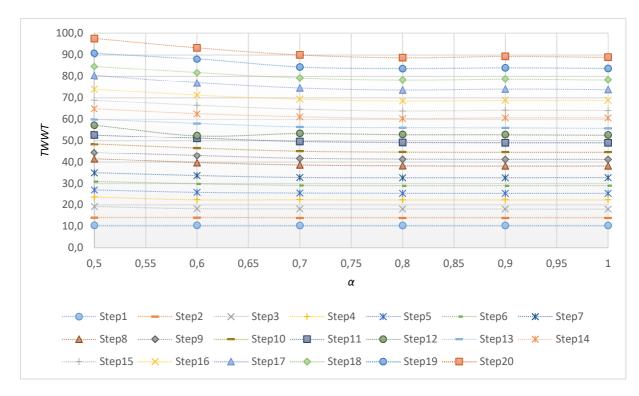






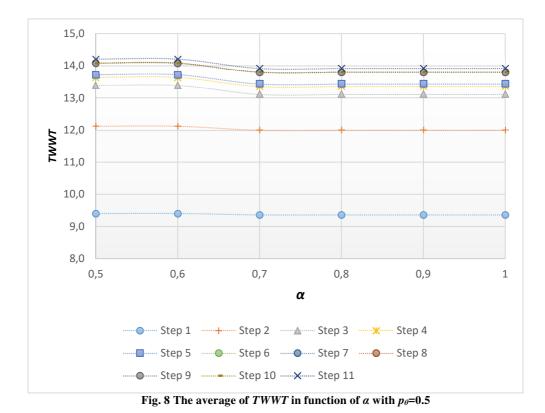
Fig. 7 The average of *TWWT* in function of  $\alpha$  with  $p_{\theta}=0.8$ 

536 Among the 25 instances that we have tested, for 8 of them, the proactive effect appears. In 537 Fig 7, we observe that the average of *TWWT* is stable in the short term. However, in the long 538 term, it is increasing when  $\alpha$  goes down to 0.7.

539 In the case of  $p_{\theta} = 0.8$  (high appearance probability), and when alpha equals 1, the system 540 does not consider the stability. So, if we have various solutions that gives the same value of 541 TWWT, the system chooses arbitrarily one of them, as observed in the step 5 on Table 5, 542 between the jobs 7 and 10. Consequently, this arbitrary choice impacts the next schedules. In 543 the example of Table 5, the difference is shown in the step 11. Therefore, as result of this 544 behaviour, we have concluded that the stability criterion can generate a proactive effect, when 545  $\alpha$  is between 0.7 and 0.9, providing better results compared to a mono-criterion considering only efficiency. This behaviour, that we called "proactive effect" appears when we have a 546 547 various choice in some steps, i.e. when the set of jobs that have to be executed is bigger.

548 To confirm this conclusion, we have tested other sets of instances, with  $p_{\theta} = 0.5$  (medium 549 appearance probability) and  $p_{\theta} = 0.2$  (small appearance probability) on the same time horizon 550  $T = 24 \ ut$ . The average of *TWWT* in function of  $\alpha$  is respectively presented in figures 8 and 9.

- 551
- 552
- 553
- 554





In figure 8, the average of *TWWT* increases when  $\alpha$  becomes inferior to 0.7. Moreover, we have observed the proactive effect in only one out of the 25 instances we have tested. In fact, when  $p_{\theta} = 0.5$ , the jobs appear with a medium frequency. Then, the set of jobs that have to be executed at each step is small compared to  $p_{\theta} = 0.8$ . Hence, the system does not have various choices at each step. Thus, the proactive effect does not appear as often as for  $p_{\theta} = 0.8$ .

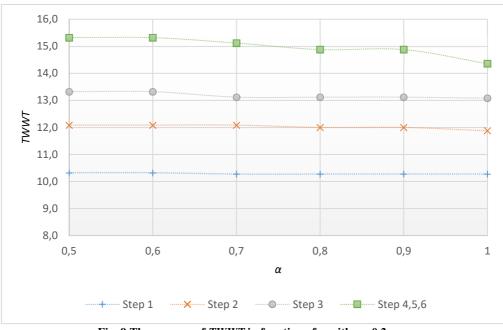
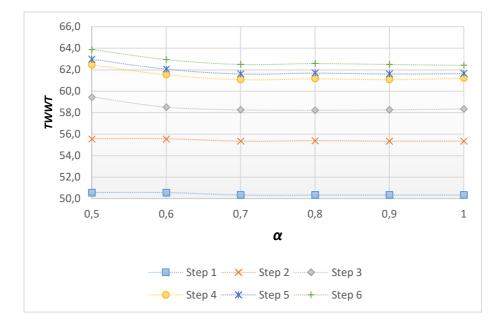


Fig. 9 The average of *TWWT* in function of  $\alpha$  with  $p_{\theta}=0.2$ 

562 In figure 9, the average of *TWWT* decreases with  $\alpha$ . Indeed, when  $p_{\theta} = 0.2$ , the jobs appear 563 with a small frequency. Then, the number of disruptions is very small, and we have not observed 564 the proactive effect. However, in the last steps (4,5,6), the average of *TWWT* is identical, 565 because the disruptions occur after the execution of existing jobs. Thus, the jobs do not wait,

and TWWT does not increase. Therefore, we have also tested this case by increasing the number 566

567 of initial jobs to seven jobs. The results are shown in Figure 10.



568

Fig. 10 The average of *TWWT* in function of  $\alpha$  for 7 initial jobs and  $p_{\theta}=0.2$ 

570 With 7 initial jobs, we observed the proactive effect in 2 instances out of the 25 tested. The 571 increase of the number of initial jobs allows to increase the set of jobs that have to be executed at each time, and the probability to observe a proactive effect. This is what we have observed. 572

#### 573 6.2 Lexicographic optimization for minimizing the number of altered jobs

574 The lexicographic optimization consists in optimizing the first objective function (of higher priority). Then, among the possible alternative optima, we optimize the second objective and 575 so on (Mavrotas 2009). In this part, we performed as follows: we first optimize the multi 576 objective function that simultaneously measures efficiency and stability criteria, 577  $f_1 = \alpha \sum_{j \in N} w_j W_j + (1 - \alpha) \sum_{j \in N} w_j (C_j - Co_j)$ , obtaining the min  $f_i = f_i^*$ . Then, we secondly 578

optimize the number of altered jobs  $f_2 = \sum_{i \in N} Dif_j$  by adding the constraint  $f_1 \le f_1^*$ , in order to 579

580 keep the optimal solution of the first optimization. To do this, we put the constraints  $A_{jm}$  and 581 *Dif<sub>i</sub>* into a linear form:

582

583 
$$A_{jm} = \sum_{k=1}^{n'} x_{jkm} \quad \forall j \; \forall m$$
(15)  
584 
$$Dif_{i} \geq {}^{1}A_{im} - {}^{0}A_{im} \; \forall j \; \forall m$$
(16)

584 
$$Dif_{j} \geq {}^{1}A_{jm} - {}^{0}A_{jm} \quad \forall j \; \forall m$$

Constraint (15) specifies that each job is affected to machine m. Constraint (16) consists in 585 586 having the binary variables *Dif<sub>j</sub>* positive when the job changes of machine during an iteration, 587 and equal to zero otherwise.

588 In the solution presented in Table 3, the number of altered jobs is not minimized. Therefore, at each iteration, the model gives a different value of the number of altered jobs. In the following 589 590 table, we present the lexicographic optimization of the same example. The aim is to minimize 591  $f_2$  with  $f_1 \le f_1^*$  as a constraint. However, if the model cannot reduce the number of altered jobs 592 to zero, we relaxed the constraint in order to obtain a better solution for  $f_2$ . Therefore, the 593 constraint becomes  $f_1 \le f_1^*(1+\varepsilon)$ , with  $\varepsilon$  a relaxation coefficient. In this study, we vary the value 594 of this coefficient until we reduce  $f_2$  to zero. For that purpose, we fixed the value of  $\alpha$  at 0.8, the 595 value for which we observed the most the proactive effect in the last sub section. The results 596 we have obtained are given in the Table 6.

597

#### Table 6. Optimal solution of number of altered jobs, with $f_1 \leq f_1^*(1+\varepsilon)$ .

- 598 (1) TWWT: Total Weighted Waiting Times  $\sum_{i \in N} w_i W_i$
- 599 (2) *TWCTD*: Total Weighted Completion Time Deviation  $\sum_{j \in N} w_j (C_j - Co_j)$

600 (3)  $f_1^{*}(1+\varepsilon)$ (4)  $f_2: \sum_{j \in \mathbb{N}} Dif_j$ 

601 602

-	(1)	( <b>0</b> )	( <b>2</b> )	(4)	(1)	$\langle 0 \rangle$	( <b>2</b> )	(4)	(1)	( <b>0</b> )	( <b>2</b> )	(4)	(1)	( <b>0</b> )	(2)	$(\mathbf{A})$
З	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)
		$2^{nd}$ Sc	hedule			$3^{rd}$ Sc	hedule			$4^{th}$ Sc	hedule		5 <sup>th</sup> Schedule			
0	5	2	4,4	0	8	2	6,8	0	13	3	11	0	16	3	13,4	0
		6 <sup>th</sup> Scl	hedule			7 <sup>th</sup> Sc	hedule			$8^{th}$ Sc	hedule			9 <sup>th</sup> Sc	hedule	
0	19	3	15,8	0	25	4	20,8	0	28	4	23,2	0	29	5	24,2	0
		10 <sup>th</sup> Sc	hedule			11 <sup>th</sup> Sc	chedule			12 <sup>th</sup> Sc	chedule			13 <sup>th</sup> So	chedule	
0	30	5	25	0	32	7	27	0	36	8	30,4	1	42	7	35	0
0.01	-	-	-	-	-	-	-	-	36	8	30.7	1	-	-	-	-
0.02	-	-	-	-	-	-	-	-	36	8	31.0	1	-	-	-	-
0.03	-	-	-	-	-	-	-	-	36	8	31.3	1	-	-	-	-
0.04	-	-	-	-	-	-	-	-	36	8	31.6	1	-	-	-	-
0.05	-	-	-	-	-	-	-	-	38	7	31.9	0	-	-	-	-
		14 <sup>th</sup> Sc	chedule			15 <sup>th</sup> Sc	chedule			16 <sup>th</sup> Sc	chedule			17 <sup>th</sup> So	chedule	
0	44	7	0	0	46	9	38.6	0	48	9	40.2	0	53	11	44.6	0
		18 <sup>th</sup> Sc	chedule			19 <sup>th</sup> Sc	chedule			20 <sup>th</sup> Sc	chedule			21 <sup>th</sup> Sc	chedule	
0	57	11	47.8	0	59	12	49.4	0	62	15	52.6	1	64	17	54.6	0
0.01	-	-	-	-	-	-	-	-	62	15	53.1	1	-	-	-	-
0.02	-	-	-	-	-	-	-	-	63	16	53.6	0	-	-	-	-

As can be seen in Table 6, from the  $2^{nd}$  schedule until the  $11^{th}$ , the model reduced the value 603 of  $f_2$  to zero, with  $\varepsilon = 0$ . For the  $12^{th}$  schedule, we have increased the value of  $\varepsilon$  up to 0.05 to 604 obtain  $f_2 = 0$ , and  $f_1^*$  becomes  $f_1^*(1 + \varepsilon)$ . For the 13<sup>th</sup> schedule, we proceed in the same way, 605 considering the last solution obtained in the previous schedule. 606

607 Among the 20 schedules, we varied  $\varepsilon$  in only two of them. It means that, in the majority of 608 cases, we can minimize  $f_2$  without impacting  $f_1^*$ . However, when we reduce  $f_2$  to zero by varying  $\varepsilon$ , the value of  $f_1 * (1 + \varepsilon)$  increases as well as the values of *TWWT* and *TWCTD*. This causes an 609 increase in  $f_1^*$  in the following iterations, as in the 13<sup>th</sup> schedule for example, in which  $f_1^* = 35$ 610 611 compared to its value in Table 3, where  $f_1 * = 32.4$ .

#### 612 **6.3** Computing time study

613 In this study, we tested on 10 different instances the Maximum Duration of Iteration (MDI) 614 and the Computing Time (CT) for the execution of all iterations. The sets of tested instances 615 contain respectively 5 and 7 initial jobs. They are disrupted by the arrival of new jobs over a horizon of T = 24 ut and  $\alpha = 0.8$ . We varied the appearance probability  $p_{\theta}$  with different values 616 617 (0.2; 0.5; 0.8; 1) to analyze its impact on the MDI and CT. Then, we calculated the minimum,

- 618 maximum, average and standard deviation of *MDI* and *CT*. The obtained results are respectively
- 619 presented in Table 7 and Table 8.

Initial jobs	$p_{ heta}$	$\operatorname{Min} MDI(s)$	Max MDI (s)	Avg MDI (s)	Std dev MDI (s)
5	0.2	0.12	0.26	0.17	0.05
	0.5	0.13	0.38	0.21	0.07
	0.8	0.21	1.14	0.44	0.31
	1	0.24	112	19.25	38.4
7	0.2	1.37	2.88	1.97	0.51
	0.5	1.58	3.66	2.03	0.69
	0.8	4.37	542	64.1	167
	1	403	6324	3606	2069

# Table 7 Maximum Duration of Iteration

621

622 When  $p_{\theta}$  increases, the set of jobs that have to be executed at each iteration increases too 623 much, as well as the average of *MDI*. As well, the average *MDI* increases also when the set of 624 initial jobs is bigger.

In the rescheduling system, we have to establish a planning after each disruption. This one should be made as soon as possible, and at latest before the appearance of another disruption. In our study, according to the time discretization, the disruption can be possible at each  $\Delta t$ . Thus, if the *MDI* exceeds  $\Delta t$ , it is unacceptable. In our case, based on the assumption that  $\Delta t$  is equivalent to 15 minutes, and according to Table 7, the proposed model is effective in solving the problems of 7 initial jobs subject to disruptions which appear at each period by a probability with up to 0.8. It is equivalent to 27 jobs in the total on average.

632

Initial jobs	$p_{ heta}$	$\operatorname{Min}CT(s)$	$\operatorname{Max} CT(s)$	Avg $CT(s)$	Std dev $CT(s)$
	0.2	0.27	0.51	0.35	0.07
5	0.5	0.42	0.69	0.51	0.07
3	0.8	1.01	2.31	1.57	0.4
	1	2.39	460	65	142
	0.2	3.98	6.12	4.96	0.68
7	0.5	5.71	9.86	6.52	1.2
7	0.8	16.48	8012	829	2523
	1	1231	20945	10622	6933

Table 8. Computing time

633

634 We can remark that the computing time depends on the set of initial jobs and the appearance 635 frequency of jobs. If these ones are bigger, the average and the standard deviation of *CT* 636 increase, which makes difficult to estimate the computing time for solving the proposed model.

637 As mentioned previously, the set of jobs that have to be rescheduled at each step contains 638 the unexecuted jobs combined with the new ones. Thus, when a job with a long processing time 639 occupies the machine, if disruptions still appears during this period, the set of jobs that have to 640 be rescheduled increases, because it will contain a lot of unexecuted jobs that are waiting since 641 the machine is busy. This matter appears when the disruptions coincide with a long processing 642 time's job. This explains the big values of the average and standard deviation of *CT* when  $p_{\theta} =$ 643 0.8 and  $p_{\theta} = 1$ , observed in Table 8.

# 644 **7. Conclusion and perspectives**

645 In this paper, we have proposed a new multi criterion objective function for a parallel 646 machine rescheduling problem. The proposed measure combines simultaneously efficiency 647 represented by total weighted waiting times, and stability as the weighted completion time 648 deviation. This multi criterion has never been studied in the literature before, and it can be a 649 very helpful and significant criterion in industrial and hospital environments. We also measured 650 the number of jobs processed on different machines after disruption. To tackle this problem, we 651 adopted a predictive-reactive strategy which consists in updating at each time the schedules, in 652 response to a disruption caused by the arrival of new jobs. Consequently, we developed a mixed 653 integer linear programming model, as well as an iterative methodology to solve the rescheduling 654 problem. The resolution of the problem provides, for each step, an optimal solution. The 655 numerical results we have presented in this paper allow us to observe that:

- 656 The stability criterion can generate a proactive effect, when  $\alpha$  is between 0.7 and 0.9, 657 providing better results compared to a mono-criterion considering only efficiency.
- 658 Using the lexicographic optimization, in the majority of cases, we can minimize the
   659 number of jobs which are processed on different machines after disruption without
   660 impacting the principal objective function.
- 661 The computing time and maximum duration of iteration depend on the set of initial
  662 jobs and on the appearance frequency of the new arrival jobs. When these ones are
  663 bigger, *CT* and *MDI* increase.

These research works can help decision makers to provide, at each step, an optimal schedule in response to a disruption caused by the arrival of new jobs in a parallel machines scheduling problem. Although the proposed model provides optimal solutions, it is limited in terms of number of jobs. Therefore, in our future works, we intend to propose heuristics that allow to browse more jobs in a short time. We also intend to take interest in flowshop rescheduling problem.

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671 **References** 

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